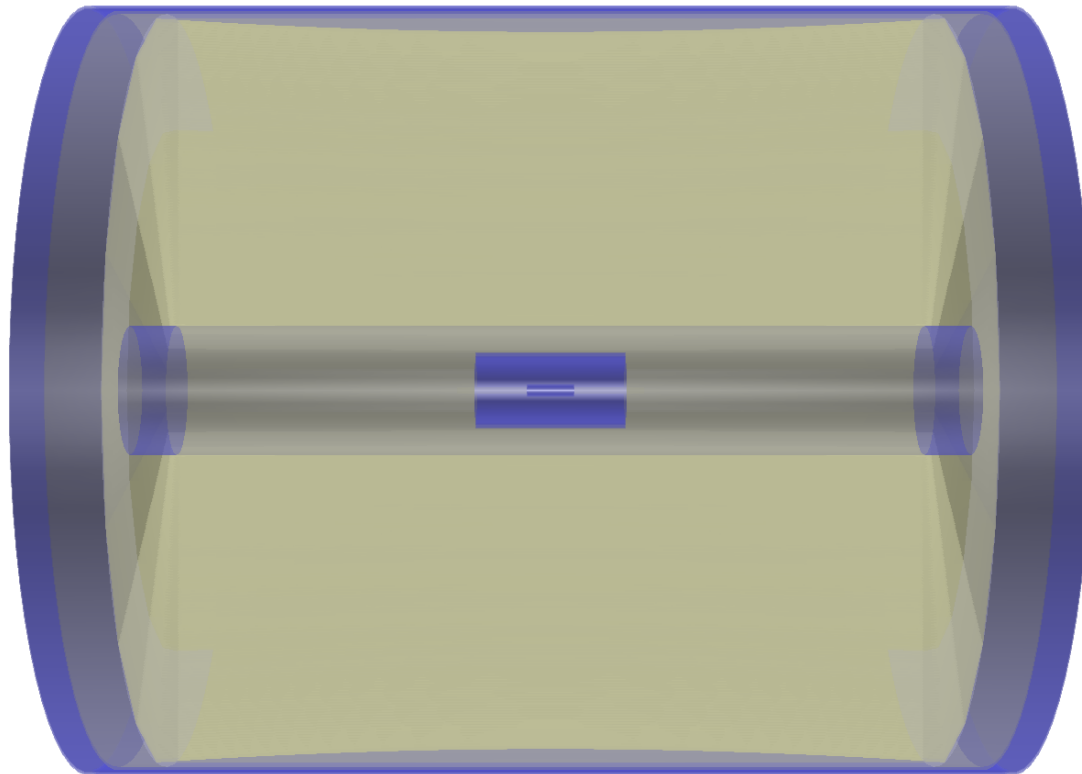


# IDEA Tracking (CDCH+VTX+PSHW) Simulation Status



**Tassielli G.F.**  
*INFN Lecce & Università del Salento*



# IDEA tracking system geant simulation

Currently we implemented a standalone geant4 simulation as a starting point:

- **Geant4 10.01 p03**
- Physics List: QGSP\_BERT 4.0
- 2T Constant Magnetic Field, G4ClassicalRK4 particle motion integrator engine
- particles generator used: General Particle Source

The code is organized in a **modular** way, the geometry description is “**quite**” **plug and play**, it is possible to import in a framework with minor changes.

We use the **ROME** (developed for MEG experiment) framework to manage the output data and run the track fitting and reconstruction:

<https://midas.psi.ch/rome/>

The **GenFit2** is interfaced to perform this preliminary study on the expected tracking system performances on track fitting.

We started to perform Pattern Recognition studies



# IDEA tracking system geant simulation

Simulation status:

- The Drift Chamber (**DCH**) geometry is described at a great level of details
- A simplified Hit creation module is used for this preliminary studies:
  - no XT relation used (is easy to switch it on), only pure geometrical information are used
  - eventual tracks hits pile-up is not well taken into account
  - Single Cell resolution is assumed constant and gaussian at a level of 100  $\mu\text{m}$
- The Silicon Vertex (**SVX**) is simplified, just a layer of equivalent material arranged in ladders
- A simplified Hit creation module is used for this preliminary studies:
  - no sensor dead time is taken into account
  - eventual tracks hits pile-up is not well taken into account
- The Pre-Shower Tracker (**PSHW**) is a copy of the SVX just with different dimensions

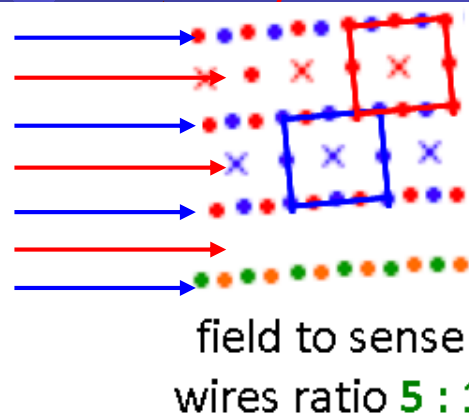
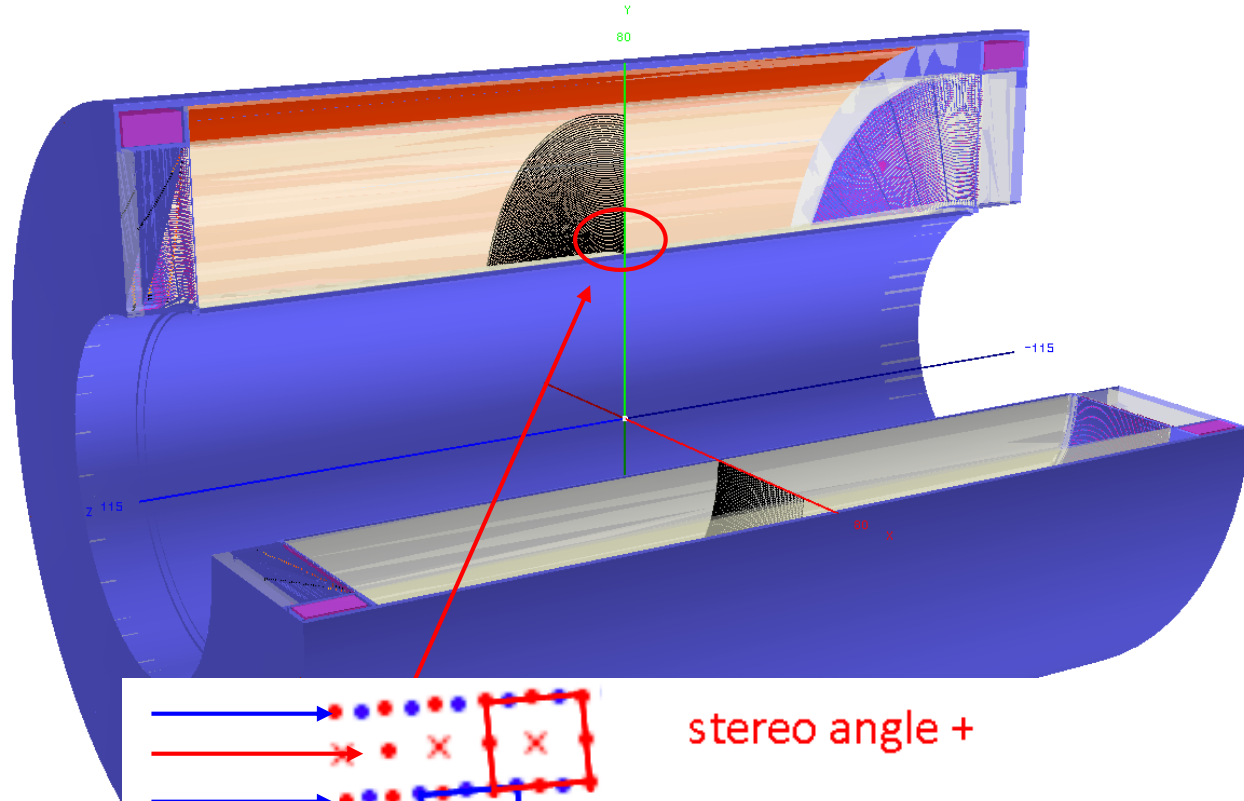
The geometry description is parametric, it is easy to try different configurations.



# IDEA DCH geometry simulation

It is simulated with a high level of details (~99%) and is **fully parametric**.

The geometry description was optimized for geant4 navigation (run time). The gas volume is divided in a set of hyperboloid shells (Blue and Red arrows) and the right voxelization factor is chosen for each layer. Blue ones to contain only the field wires. Red ones to contain the central layers wires.



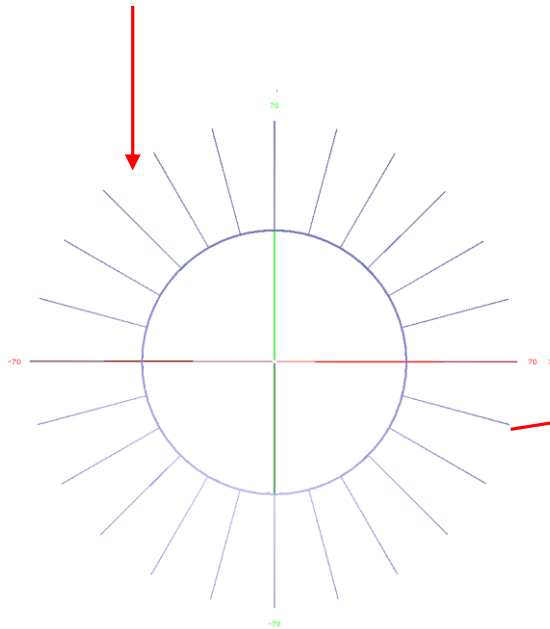
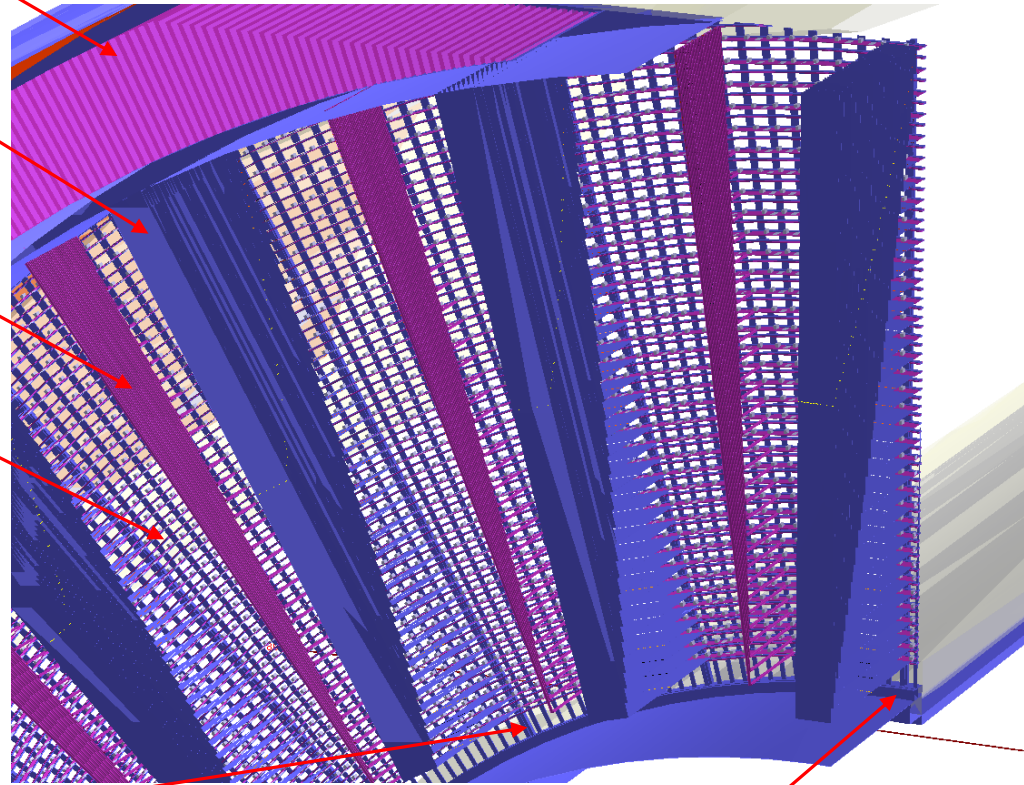
stereo angle +

stereo angle -

guard layer

# IDEA DCH geometry simulation

- (Optional) Electronics boards: 12 cm x 6 cm x 3mm G10 (FR4);
- signal cables (only downstream): 2.032 cm x 25  $\mu\text{m}$  Kapton + 40  $\mu\text{m}$  16 pairs of Copper wires;
- HV cables (only downstream): 500  $\mu\text{m}$  Copper wire + 500  $\mu\text{m}$  Teflon insulation;
- Wire anchoring (see next slide);
- Carbon fiber wire support.

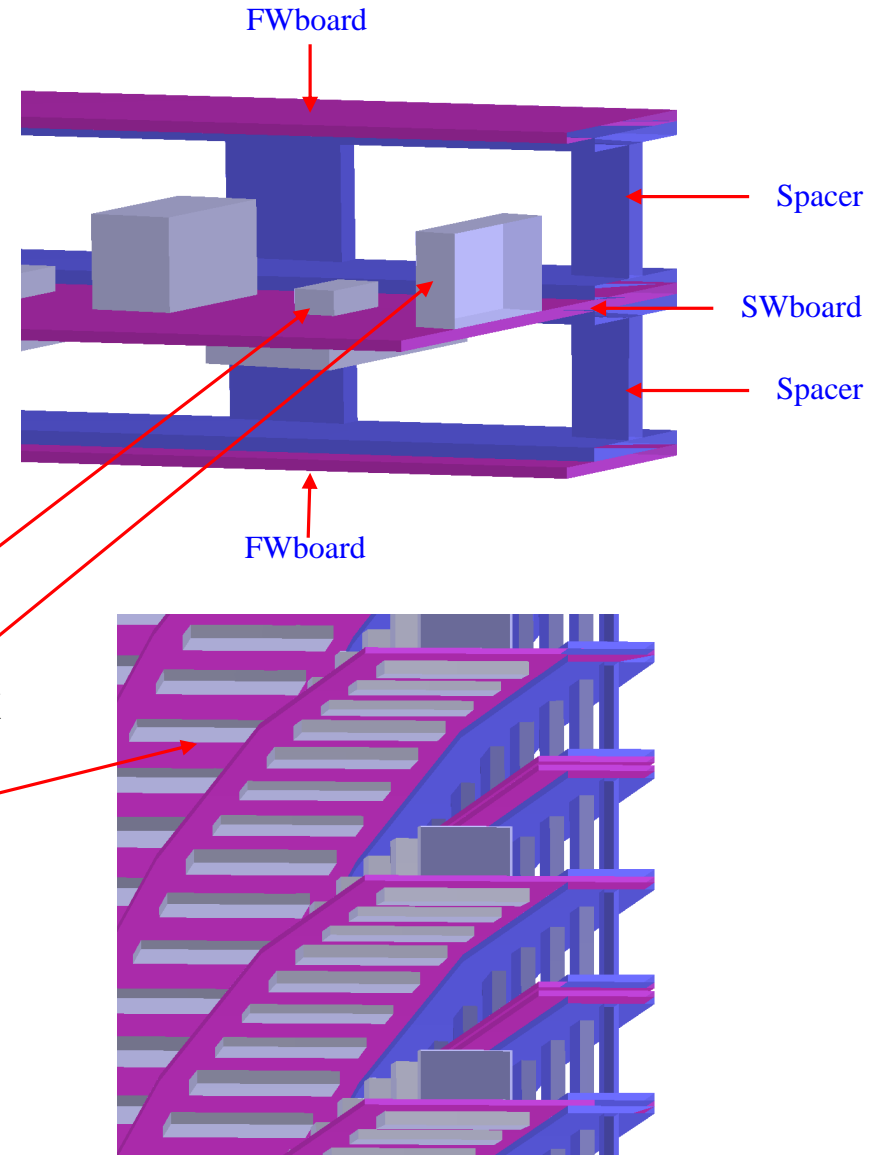


Connecting ring is described as a circular layer:  
0.5 cm x 1.5 cm Carbon fiber

# IDEA DCH geometry simulation

The wire anchoring system:

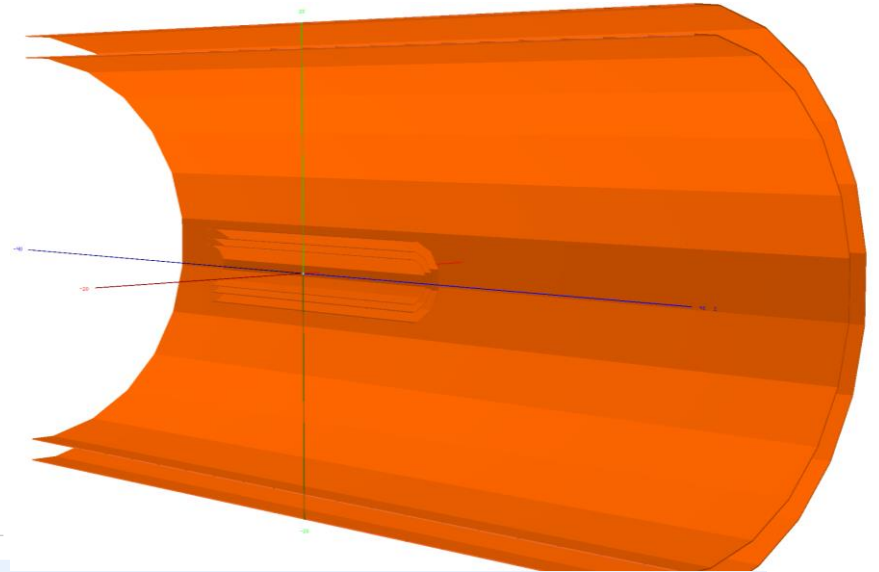
- Field wire board: 4 mm x 200  $\mu\text{m}$  G10(FR4);
- Spacer: (see F. Grancagnolo talk for details) made of polycarbonate, instead of holes it is drawn with spokes but with the same area ratio.
- Sense wire board: 1 cm x 200  $\mu\text{m}$  G10(FR4) plus components:
  - 1) termination resistance: 1.6 mm x 800  $\mu\text{m}$  x 450  $\mu\text{m}$  Aluminum;
  - 2) HV Capacitance: 3.17 mm x 1.57 mm x 1.7 mm Aluminum;
  - 3) HV resistance (only downstream): 5 mm x 2.5 mm x 550  $\mu\text{m}$  Aluminum.





# IDEA SVX geometry simulation

- Currently the layers are just made of Si with thickness equivalent to the expected layer  $X_0$  (it is possible to describe a layer as a stack of different shells of different materials);
- The dimensions of the ladders are just evaluated to cover the space with reasonable dimensions;
- The ladders are disposed close to each other (not in a realistic way), there can be some dead space (at a level of few  $\mu\text{m}$ );



Example of the SVX configuration file

```
6 string svx.motherVolMat = "G4_AIR";
7
8 string svx.extFile      = "";
9 double svx.z0          = 0;
10
11 int svx.geomType       = 00; //decimal digit:magior version, unit digit:minor version
12 // 00:dummy geometry, the ladder has cylindrical shape instead of plan
13
14 //double svx.voxelization = 0; //Choose voxelization method for the gas volumes that contain wires, i
15
16 bool svx.doDetailedSurfCheck = false;
17 bool svx.debugLayer         = false;
18
19 // Cell parameter needed only for the square cell case
20
21 int svx.nLayers           = 7;
22 vector<double> svx.LayersInRad = { 17.0, 23.0, 31.0, 180.0, 200.0, 330.0, 340.0};
23 vector<int> svx.nPhiSectors   = {12, 12, 12, 24, 24, 36, 36};
24 vector<int> svx.nLaddersPerSector = {10, 10, 10, 20, 20, 30, 30};
25 vector<double> svx.LaddersHalfLength = {12.5, 12.5, 12.5, 20, 20, 25, 25}; // Per Layer (The ladder are suppl
26 vector<double> svx.LaddersThickness = {0.28, 0.28, 0.28, 0.94, 0.94, 0.94, 0.94}; // Per Layer
27 vector<int> svx.R0Types           = {1, 1, 1, 1, 1, 1, 1}; //1: Pixel; 2: Strip // Per Layer
28 vector<double> svx.R0firstSideDim = {0.02, 0.02, 0.02, 0.02, 0.02, 0.02, 0.02}; // Per Layer
29 vector<double> svx.R0firstSideInsul = {0.0005, 0.0005, 0.0005, 0.0005, 0.0005, 0.0005, 0.0005}; // Per Layer
30 vector<double> svx.R0secondSideDim = {0.02, 0.02, 0.02, 0.02, 0.02, 0.02, 0.02}; // Per Layer
31 vector<double> svx.R0secondSideInsul = {0.0005, 0.0005, 0.0005, 0.0005, 0.0005, 0.0005, 0.0005}; // Per Layer
32 vector<double> svx.R0angle         = {0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0}; // Per Layer
33
34
35 // First Layer Ladder description
36 int svx.l1.ld.nShells = 1;
37 vector<string> svx.l1.ld.ShellsMaterial = { "G4_Si" };
38 vector<double> svx.l1.ld.ShellsThickness = { 0.28 }; //summed with R0 thickenss must be consisten with the tot
39 int svx.l1.ro.nShells = 1;
40 vector<string> svx.l1.ro.ShellsMaterial = { "G4_Si" };
41 vector<double> svx.l1.ro.ShellsThickness = { 0.28 }; //summed with ladder thickness must be consisten with the
```

# IDEA single track fitting

We simulated single tracks at fixed theta (65 deg) and we fitted all tracks hits with Kalman filter (genfit2).

Only a quality cut on  $\text{Chi}^2/\text{nDof} < 25$  was applied.

To be compared with Mogens fast MC results:

$$\sigma_p(1\text{GeV}) \sim 0.07 \%$$

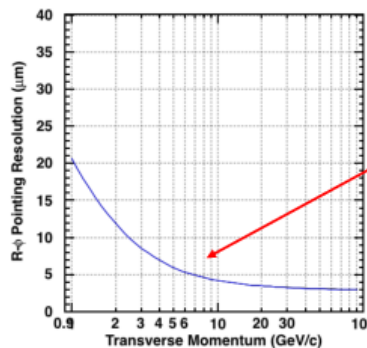
$$\sigma_p(100\text{GeV}) \sim 0.4 \%$$

$$\sigma_d(1\text{GeV}) \sim 20 \mu\text{m}$$

$$\sigma_d(100\text{GeV}) \sim 3 \mu\text{m}$$

## IDEA Tracking System Performance – First Results

- Beam pipe:  $r = 1.56 \text{ cm}$ ;  $0.48\%$  of  $X_0$
- Five VTX layers ( $5 \mu\text{m}$  resolution)
  - $r = 1.7, 2.3, 3.1 \text{ cm}$ ;  $0.3\%$  of  $X_0$  per layer
  - $r = 15, 25 \text{ cm}$ ;  $1\%$  of  $X_0$  per layer
- Drift chamber ( $112$  layers of  $100$  ( $75$ )  $\mu\text{m}$  resolution)
  - $r = 35\text{-}200 \text{ cm}$
- One precise Si strip measurement ( $10 \mu\text{m}$  resolution)
  - $r = 201 \text{ cm}$
- Very light: Total of  $\sim 5\%$  of  $X_0$  before pre-shower

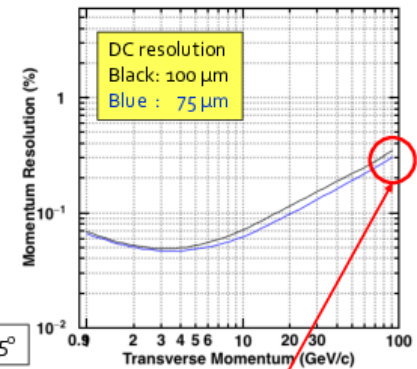


Performance at  $\theta = 65^\circ$

$$\sigma_{d_0} = a \oplus \frac{b}{p \sin^{3/2} \theta}$$

$a \simeq 3 \mu\text{m}$     $b \simeq 18 \mu\text{m GeV}$

Results by ALICE tracking system optimization tool kindly provided by R. Shahoyan



Reaching 0.3% at 100 GeV

Very fresh results.  
Optimization to be done!





# IDEA (baseline) geometry simulation

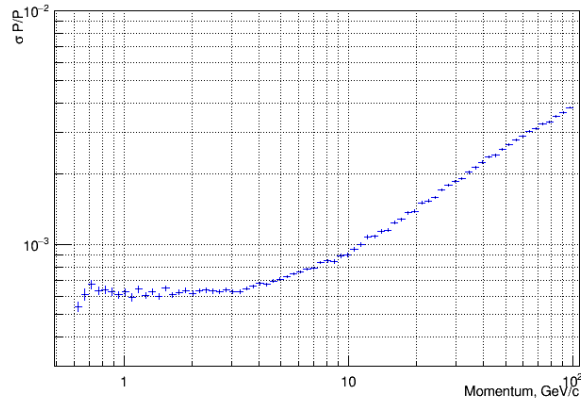
Following dimensions reported by Mogens talks at FCC-Berlin

- **Pipe:** equivalent to 0.48%  $X_0$  at radius of 15.6 mm (170  $\mu\text{m}$  of Ti, *to avoid overlaps*)
- **SVX:** (for this study) 7 layers of Si:
  - radii: 17.0, 23.0, 31.0, 180.0, 200.0, 330.0, 340.0 mm;
  - lengths: 250, 250, 250, 800, 800, 1500, 1500 mm (coverage not checked);
  - thickness 0.28, 0.28, 0.28, 0.94, 0.94, 0.94, 0.94 mm
  - pixel 20  $\mu\text{m}$ ;
- **DCH:** (gas He 90% i-C<sub>4</sub>H<sub>10</sub> 10%)
  - radii: 345, 2000 mm;
  - length: 4000 mm;
  - Cell: 56448;
  - Layers: 112;
  - Cell size: 11.85 – 14.7 mm;
  - Stereo angle: 48 - 250 mrad.
- **PSHW:** 2 active layers (+ 2 Lead radiator layers):
  - radii: 2012, 2027 mm (2004, 2014);
  - Lengths: 4800, 4800 mm (4800, 4800);
  - thickness 0.94, 0.94 mm (6, 11)
  - pixel 70  $\mu\text{m}$ ;

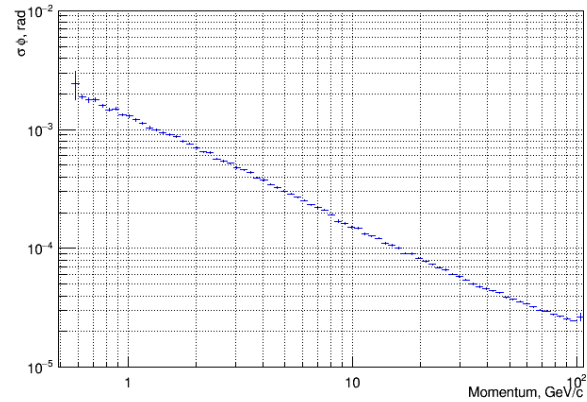


# Resolutions ( $\mu^-$ at fixed $\theta=65\text{deg}$ )

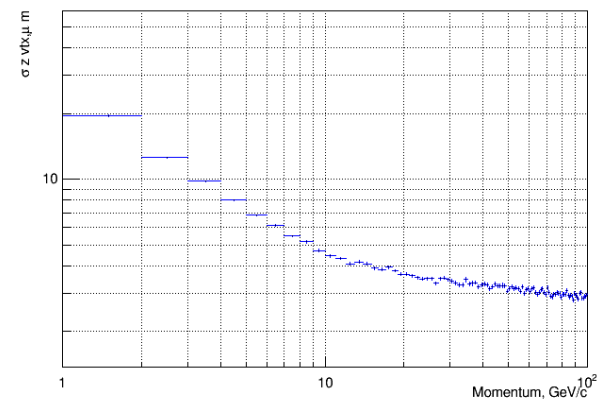
Momentum Resolution



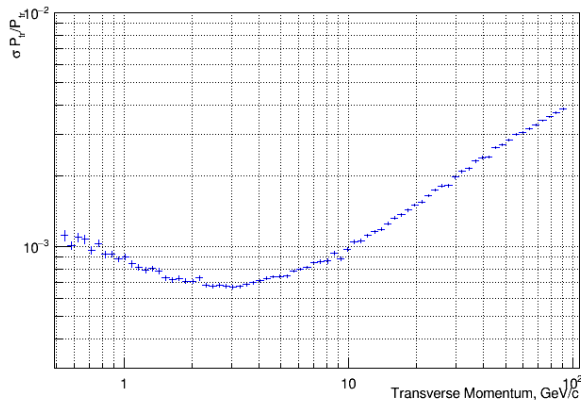
Phi Resolution



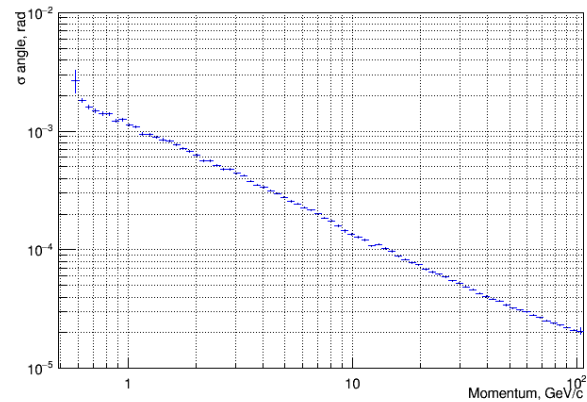
Z vtx Resolution



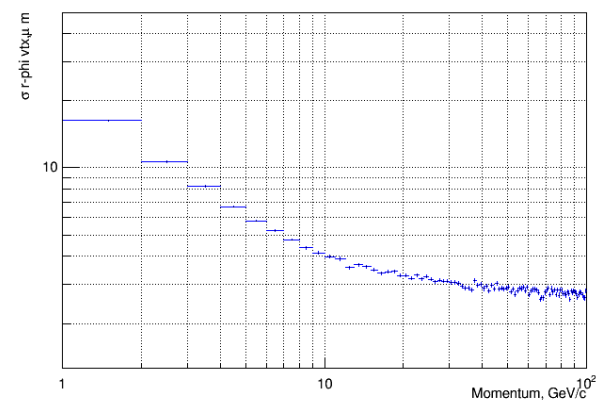
Transverse Momentum Resolution



Theta resolution



R-phi vtx Resolution



# IDEA single track fitting (additional tests)

We perform a comparison of the following configuration:

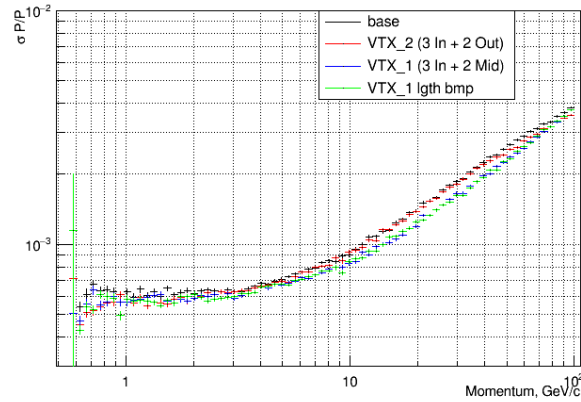
- Using a VTX made of the 3 inner layers and the 2 outer ones (VTX\_2).
- Using a VTX made of the 3 inner layers and the 2 central ones (VTX\_1).
- With VTX\_1 use a thinner Beam Pipe (made of 1mm of Beryllium).

Moreover we performed a scan of the resolutions as a function of the theta angle for tracks of fixed momenta (1, 5, 10, 30, 100 GeV).

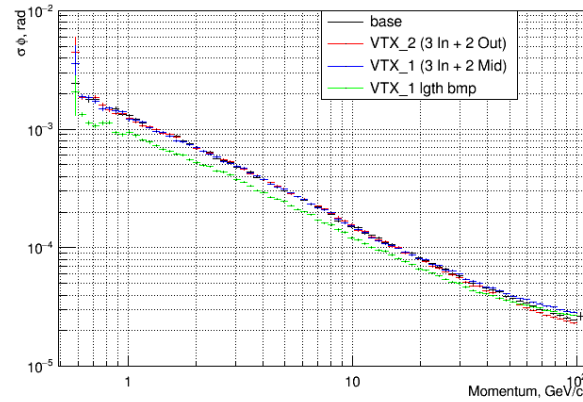


# Resolutions ( $\mu^-$ at fixed $\theta=65\text{deg}$ )

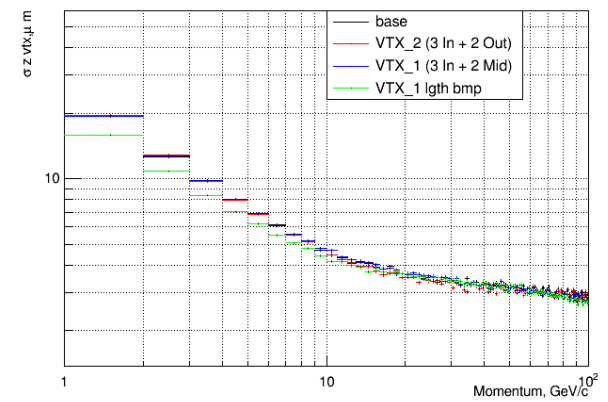
Momentum Resolution



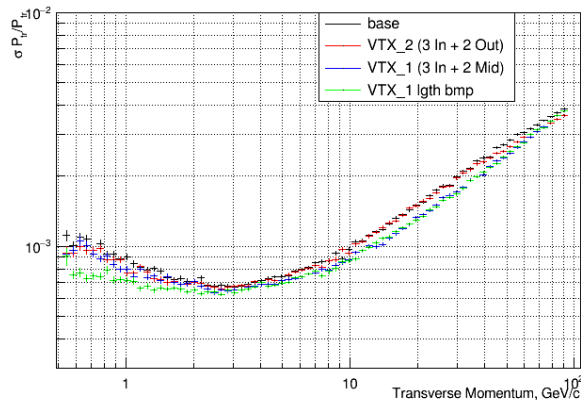
Phi Resolution



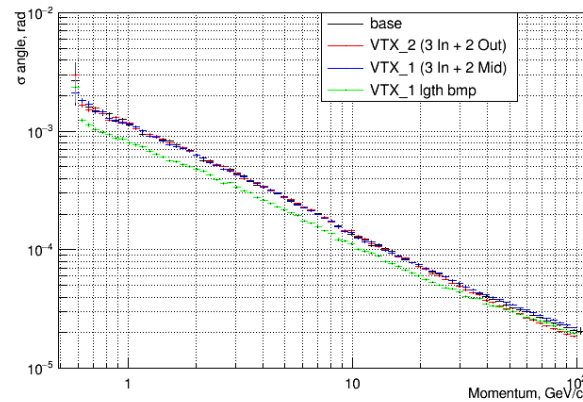
Z vtx Resolution



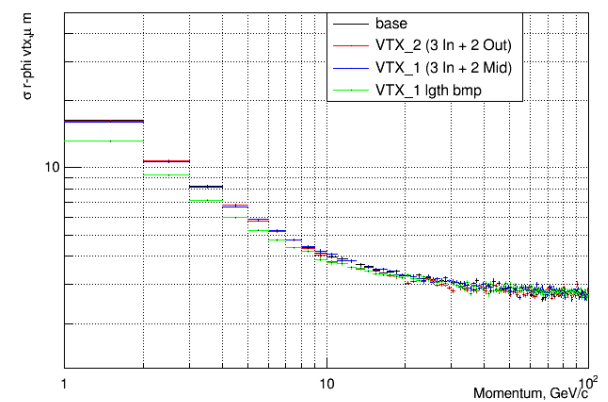
Transverse Momentum Resolution



Theta resolution

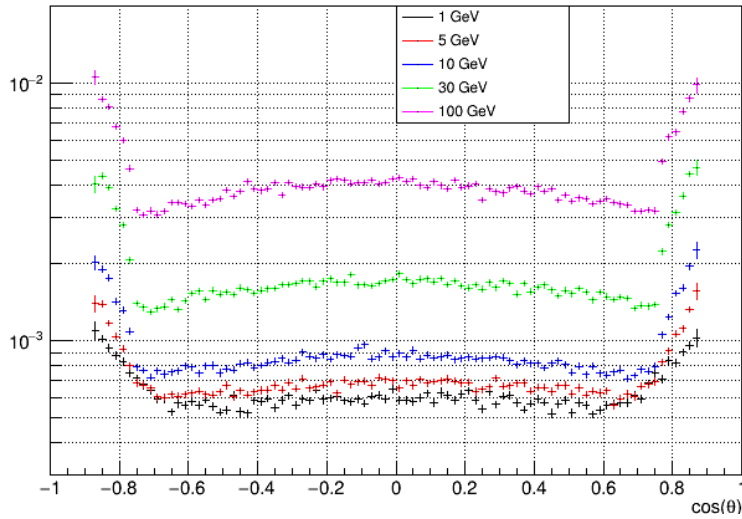


R-phi vtx Resolution

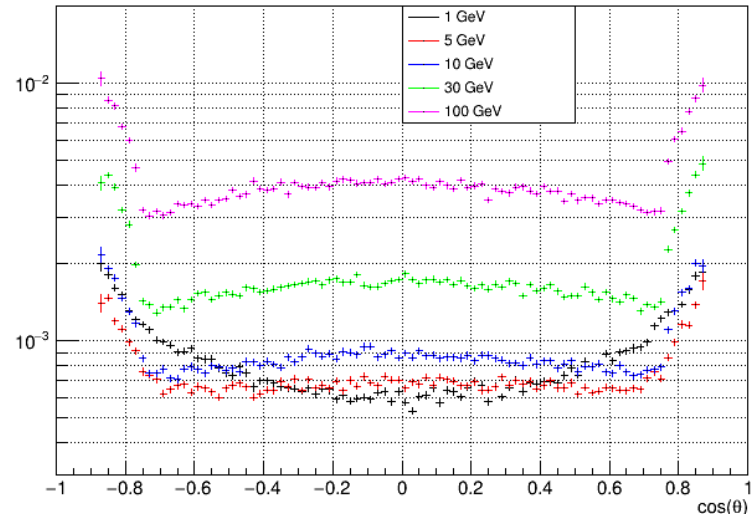


# Resolutions ( $\mu^-$ as function of $\theta$ )

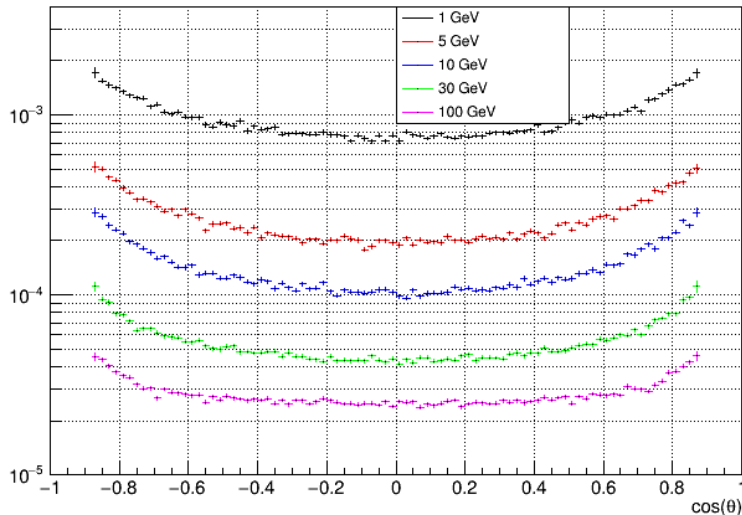
Momentum resolution vs Theta



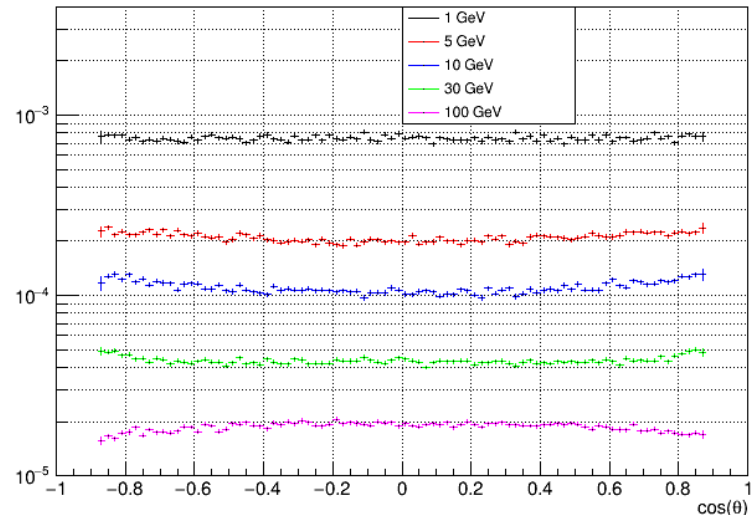
Pt resolution vs Theta



Phi resolution vs Theta

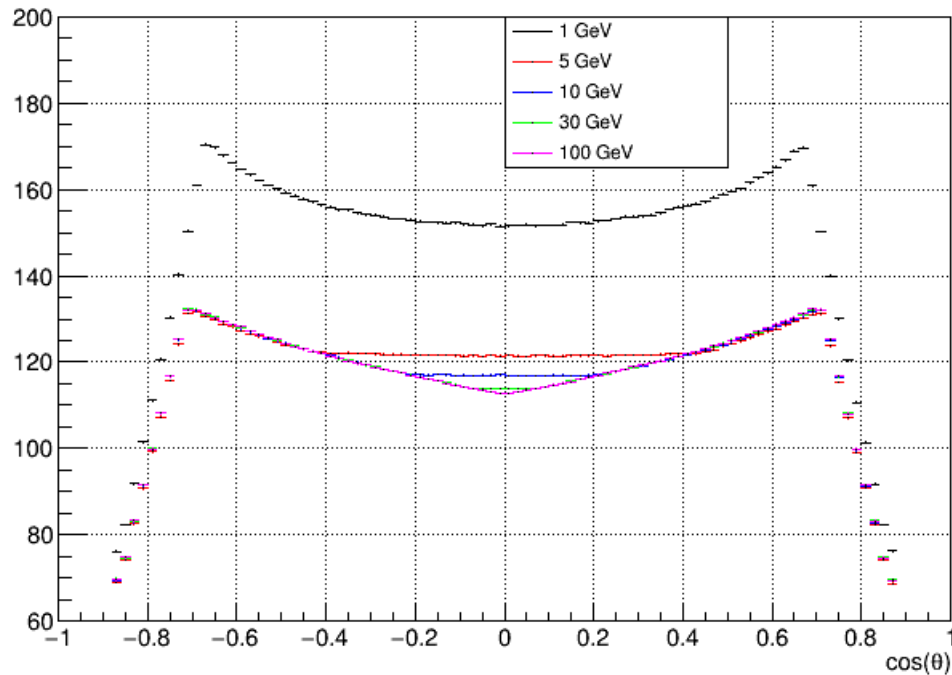


Theta resolution vs Theta

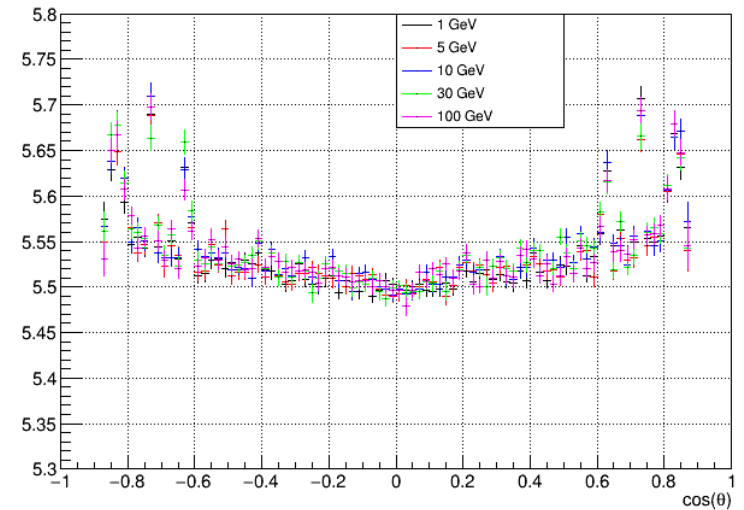


# Resolutions ( $\mu^-$ as function of $\theta$ )

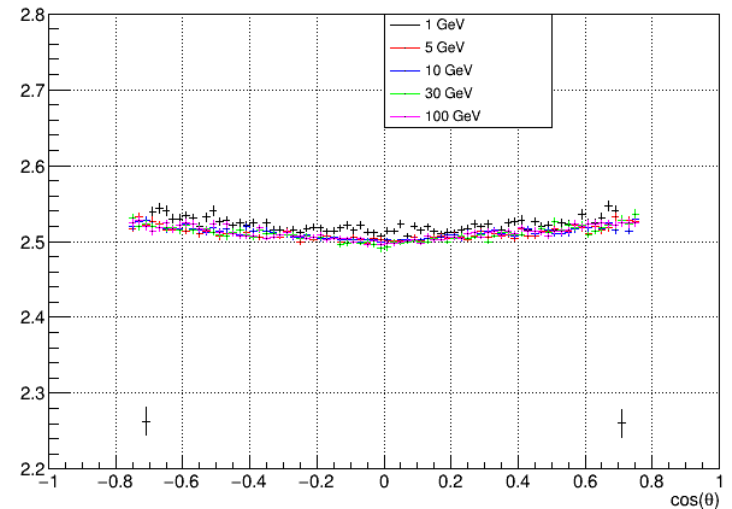
N. good Hits DCH resolution vs Theta



N. good Hits SVX resolution vs Theta



N. good Hits PSHW resolution vs Theta





# track finding strategies

track finding strategies possible alternatives: **global** vs **local**

- **global methods:**
  - treat hits in all detector layers simultaneously
  - find all tracks simultaneously
  - result independent of starting point or order of hits
  - examples: template matching, hough transforms, neural nets, cellular automation, ....
- **local methods ('track following'):** (currently used)
  - start with construction of track seeds
  - add hits by following each seed through detector layers
  - eventually improve seed after each hits (e.g. with Kalman filter technique)



# Pattern Recognition code borrowed from MEG2

Part of the code has been initially developed by Alice Off-line Project (AliRoot),

then it was adapted to specific cases:

- 2005: as MEG1 initial framework (as MEGRoot),
- 2007: ILC 4th concept design performance studies (as ILCRoot),
- 2010: Mu2e I-tracker proposal,
- 2013: MEG2 DCH tracking.

*Wire measurement,  
stereo layers*

Code not yet completely cleaned up



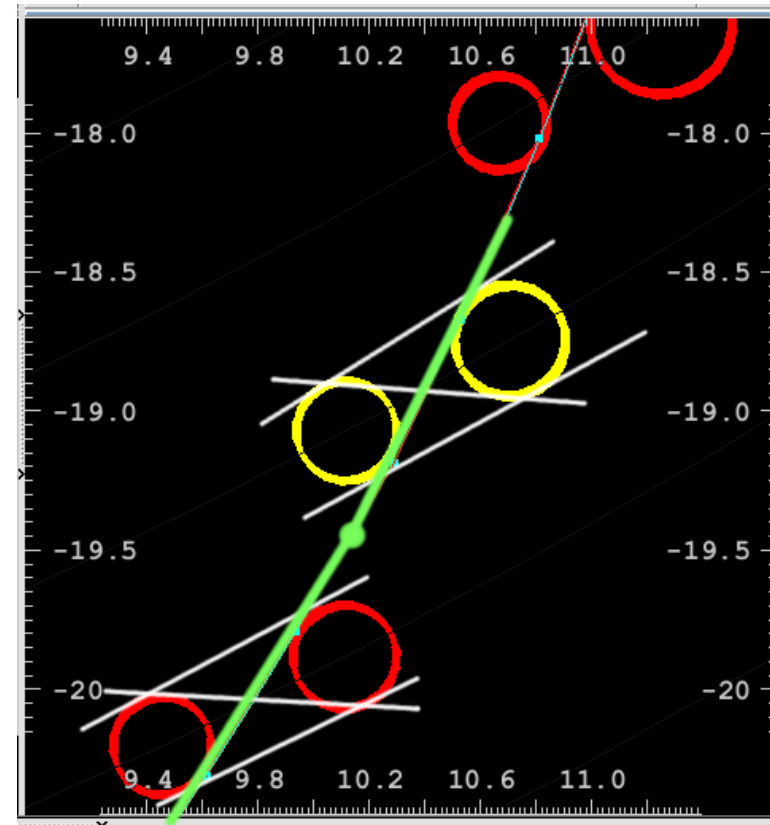
## 2 pairs seed construction (DCH only)

### Seeding from 2 pairs of hits (each pair on same layer) pointing at the origin

- 2 consecutive hits in same layer  
→ 4=2x2(Left-Right) pairs with direction
- 2 pairs from nearest layers compatible:  
 $|\Delta\cos(\varphi(\text{direction})-\varphi(\text{position}))|<0.2$ ,  
crossing Z inside DCH
- 1 pair with origin → Pt estimate  
(averaged over 2 pairs)
- Cross Point of 2 opposite stereo pairs give  
Z-coordinate (with  $\Delta\varphi$  correction  
from Pt)
- $P_z = 0$  at beginning

Z measurement give additional compatibility  
check between 2 hits and between 2 pairs

**Combinatory low:** 2 local compatibilities + 1 from opposite  
stereo view, but with direction angle check

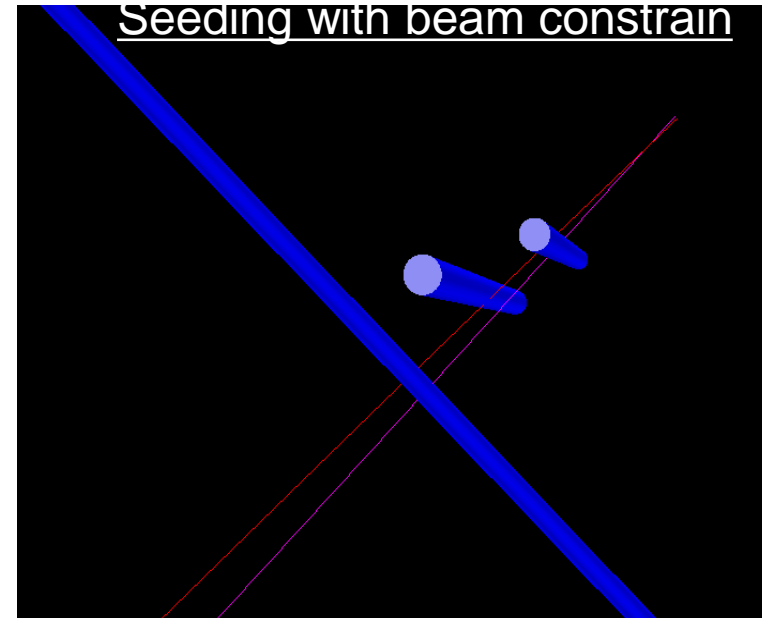


**Red hits** projection at  $z=0$  plane  
**Yellow** rotated according to  $\varphi$

# additional seed construction (DCH only)

## Seeding from 3 hits in different layers with origin constraint

- Take any 2 free hits from different stereo layers with a gap (4 or 6 layers)
- Cross Point of 2 wires give Z-coordinate (must be inside DCH volume)
- Select nearest free hits at middle (+-1) layer
- 2 hits from same stereo layer give initial angle in Rphi
- origin added with sigma Rphi~ 4cm Z ~ 100 cm (Mu2e case)
- Seeds constructed for all  $2 \times 2 \times 2 = 8$  combination of Left-Right possibilities
- Checked that at -4 (+-1) layer are available free hits with  $\chi^2 < 16$
- Extrapolate and assign any compatible hits (by  $\chi^2$ ) from last to first hits
- Refit segment to reduce beam constraint
- Check quality of track segment:
  - $\chi^2/\text{NDF} < 4$
  - number of hits found ( $\geq 7$ )
  - number of shared hits ( $< 0.4N_{\text{found}}$ )



**Combinatory high:**  
local compatibility over  
different layers,  
+ 1 from different stereo view

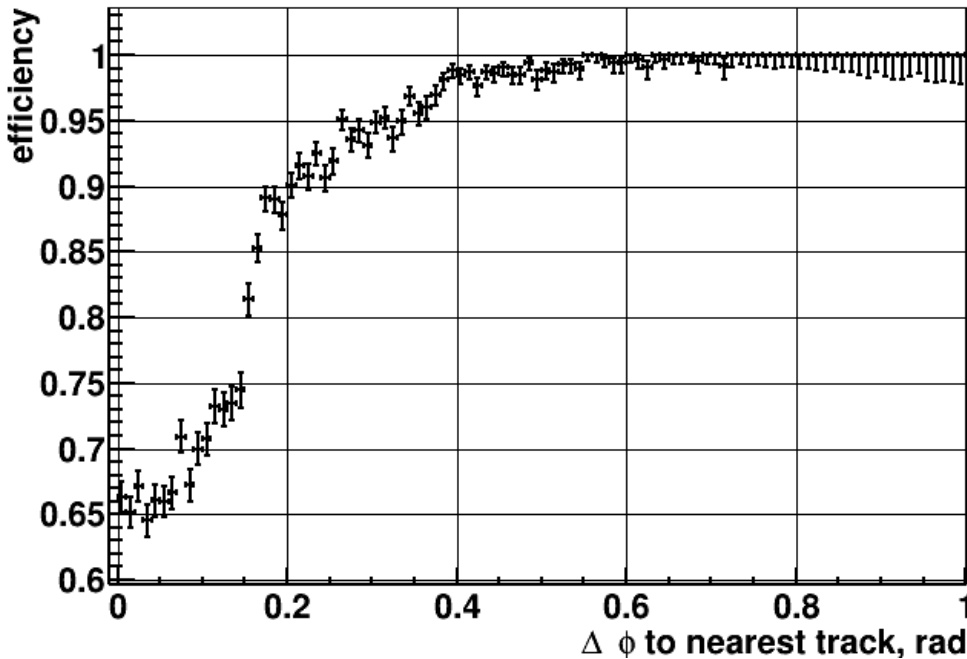
# Track finding preliminary results

- We studied the double track separation by simulating 10 tracks events.
- We checked the performance for the case of a PR based on DCH only and with the help of external tracker (SVX)
- We checked the main limiting factor for the DCH only in the actual configuration.

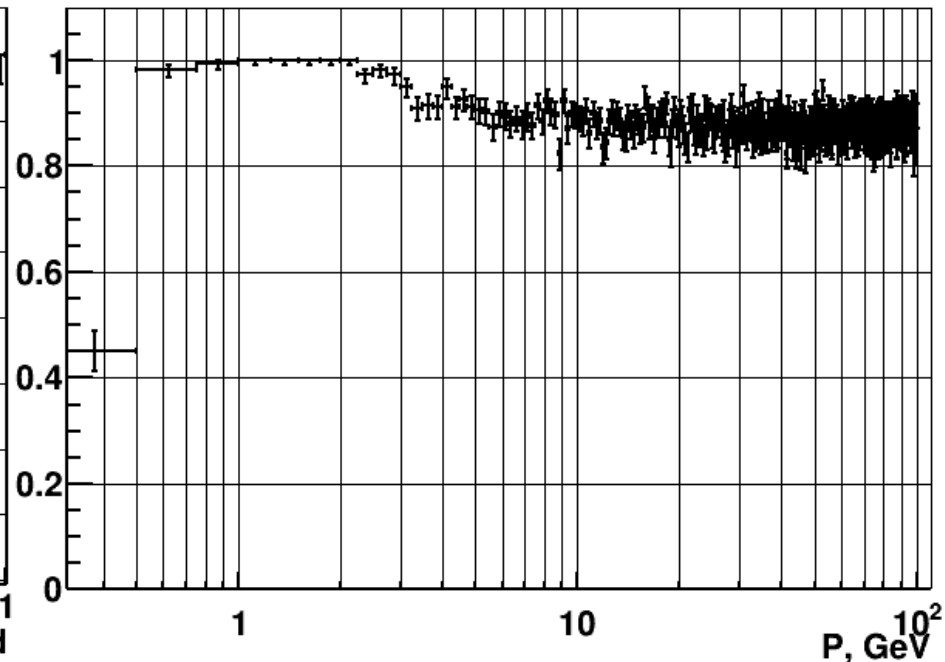


# 10 $\mu$ 's (0-100 GeV), DCH only (no longitudinal info used)

efficiency to find track in proximity of another ( $|\cos \theta| < 0.8$ )



efficiency to find something at 1 turn ( $|\cos \theta| < 0.8$ )



Efficiency defined as fake ratio  $< 0.3$

Efficiency for 10 muons  $\sim 0.85$

Ineffective up to 0.15-0.5 rad presence of another track

Mostly random stereo view matching (eff  $\sim 50\%$ ) for  $< 0.15$  rad

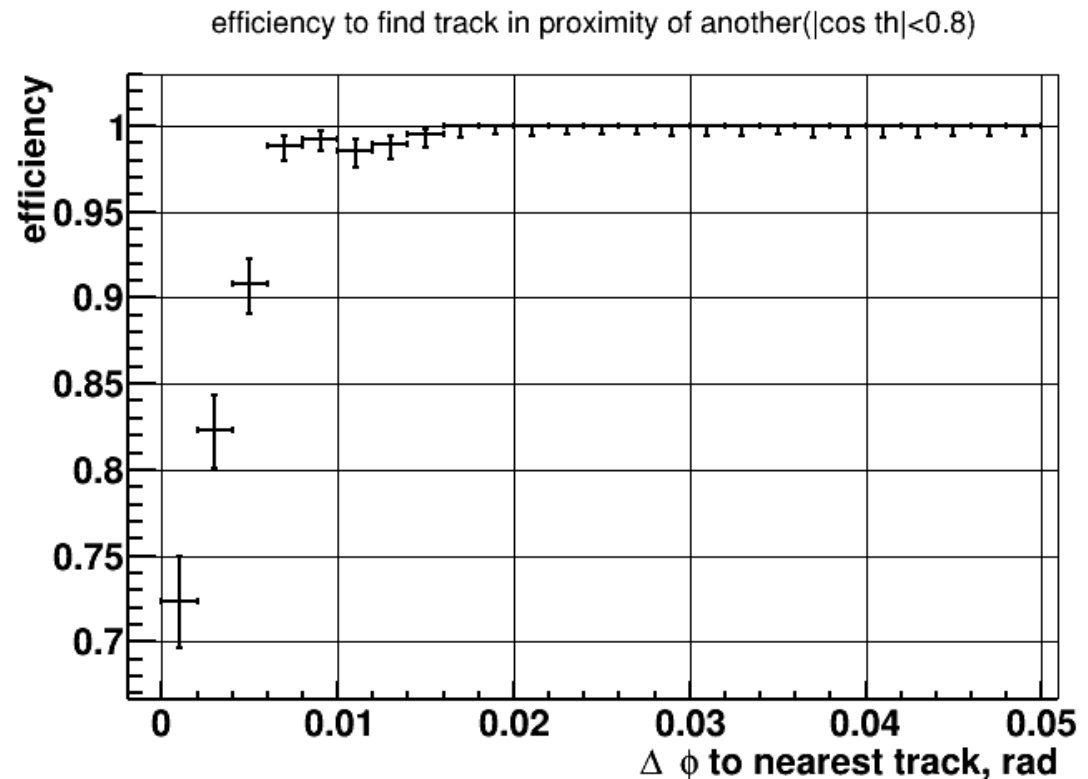


# 10 $\mu$ 's (0-100 GeV), **DCH only** (no longitudinal info used) with Z vtx preselection of seeds

short initial 7 hit track segment must match in Z with SVX seeds  
with distance <1 cm

Min  $\Delta\phi_0 \sim 0.005$  rad

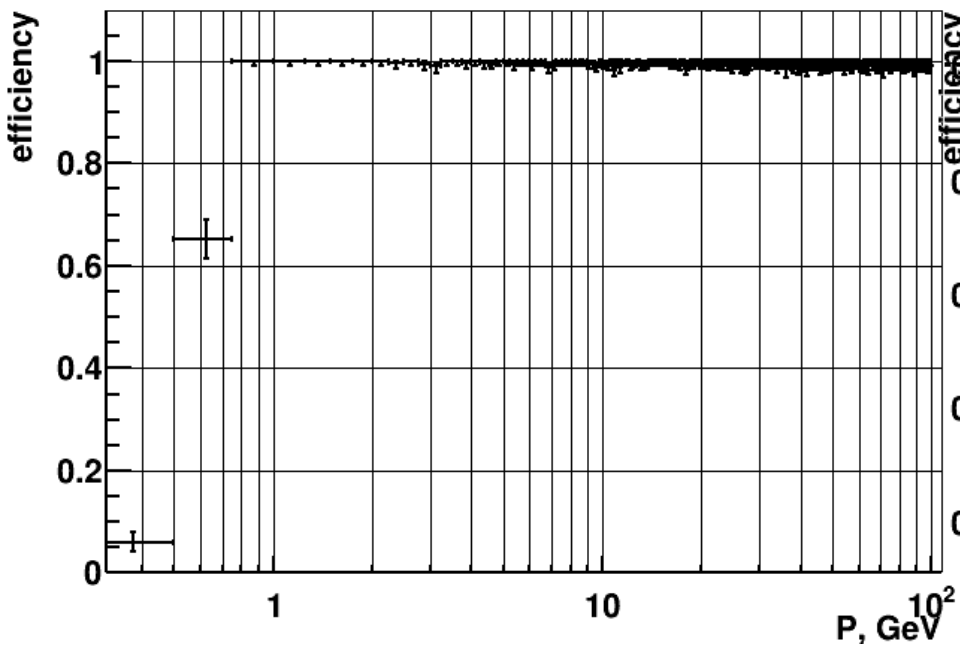
But will not help for  
decaying tracks after the  
SVX



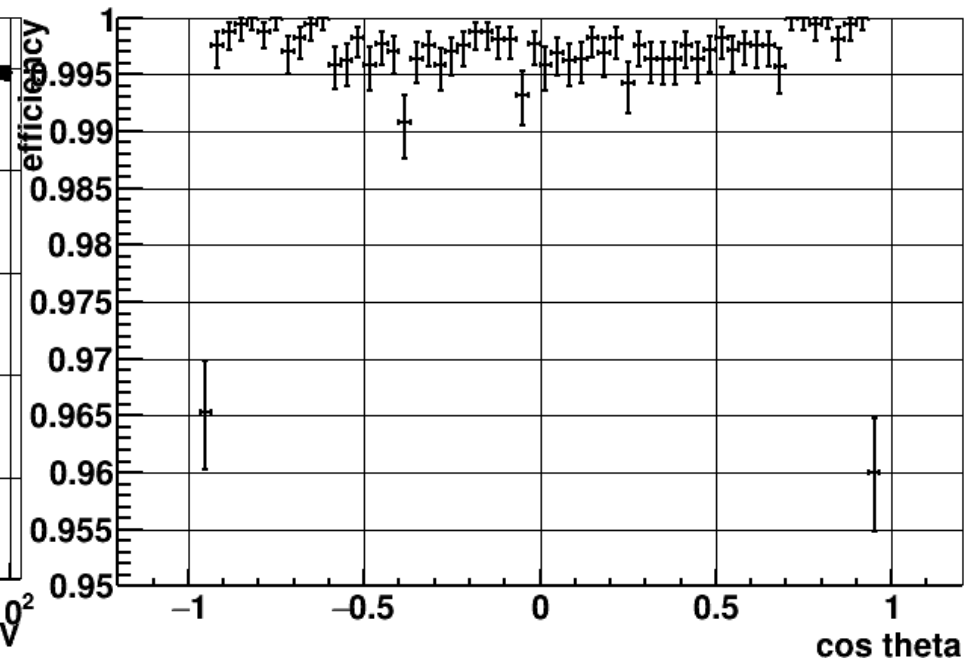
# 10 $\mu$ 's (0-100 GeV), **DCH only** (no longitudinal info used) with Z vtx preselection of seeds

$$\Delta\phi_0 \sim 0.005 \text{ rad}$$
$$\text{eff} \sim 99.5\%$$

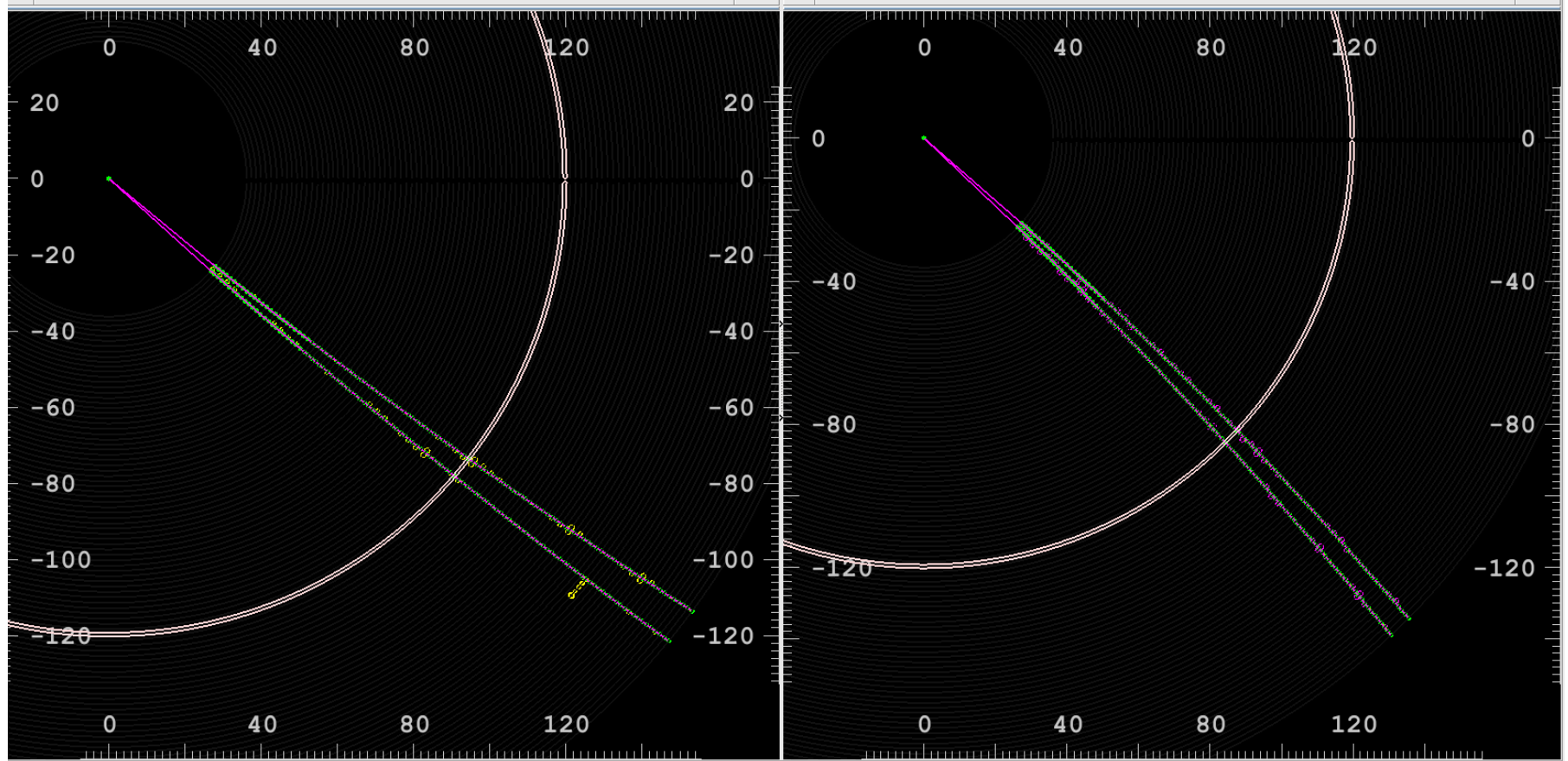
efficiency to find 0.6nhits at 1 turn ( $|\cos \theta| < 0.8$  over all tracks)



efficiency to find 0.6nhits at 1 turn ( $P > 1$  GeV) over all tracks



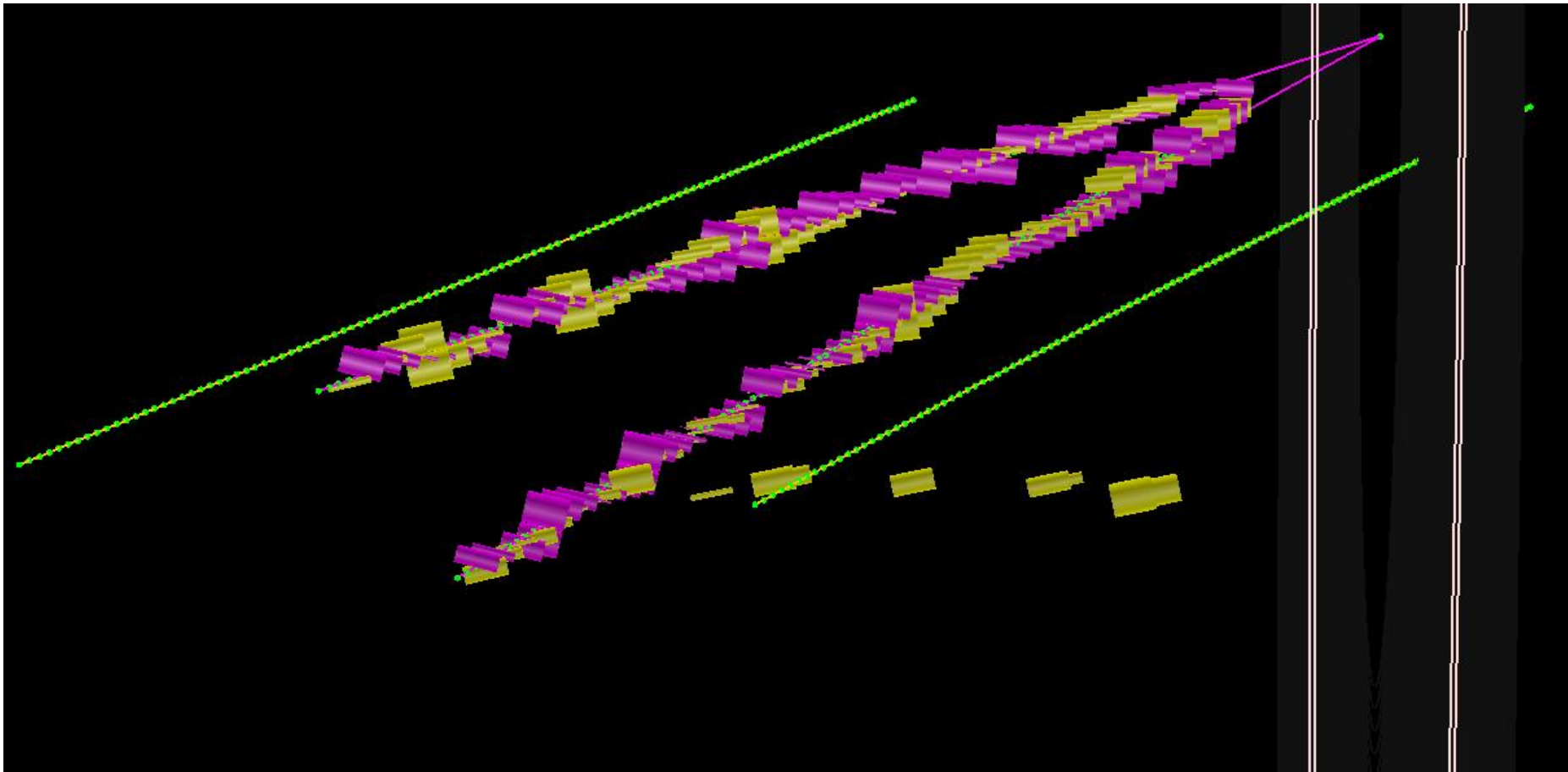
# DCH limiting factor, Stereo view mismatching



One full segment is connected with wrong from another stereo view  
Chi2 - perfect



# DCH limiting factor, Stereo view mismatching



One full segment is connected with wrong from another stereo view

Chi2 - perfect



# DCH limiting factor, Stereo projection mismatching

The limiting factor comes from the linear increasing of the stereo angle with the radius and the track topology, possible solution to solve the issue are:

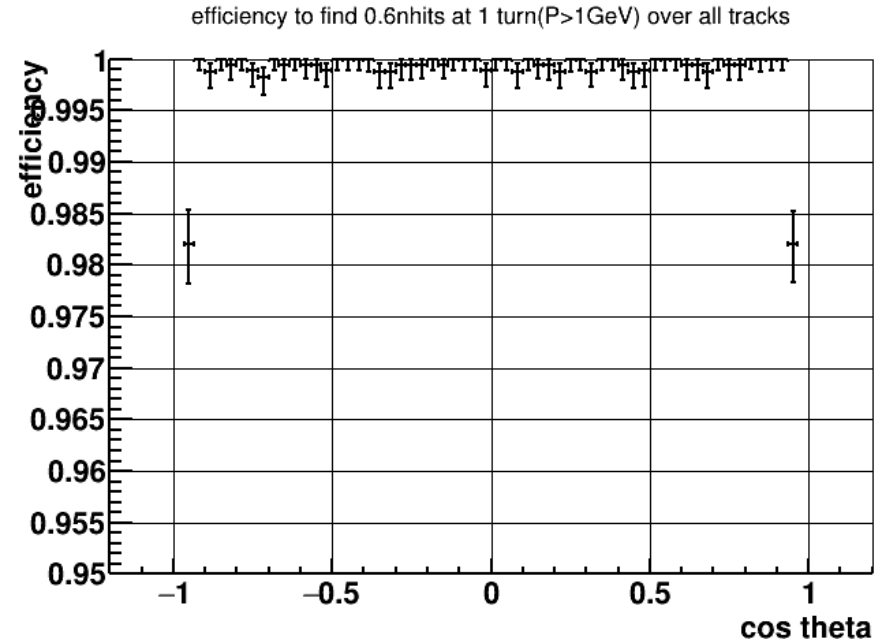
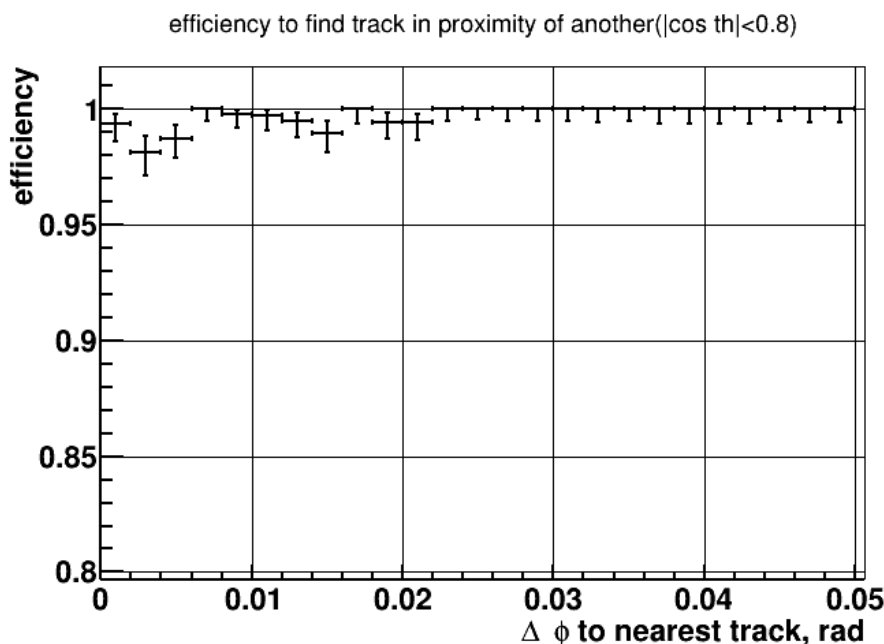
- use an external system to solve mismatching
- **change finding approach:**
  - If good track was found, hits are removed from next iteration seeding
  - Mismatched track at first iteration may not be a good track after cleaning
- or start seeding from PSHW layers
- or seeding with Z vertex constraint
- or step back from 3D finding to 2D track finding per stereo view and then global stereo segment matching

**Possible gain:** can be much faster track finding - seeding only from nearest wires (if no Z coordinate information)



# 10 $\mu$ 's (0-100 GeV), DCH only (using longitudinal info)

Assuming a  $\sigma_z$  3 cm per hit  $\rightarrow \sigma_z \sim 0.3$  cm for tracks  
helps to resolve mismatching at this level for  $\Delta z$ ,  
and in addition over  $\Delta \tan \lambda$



Cell size factor changes from 0.03 to 0.0077 from inner to outer layer

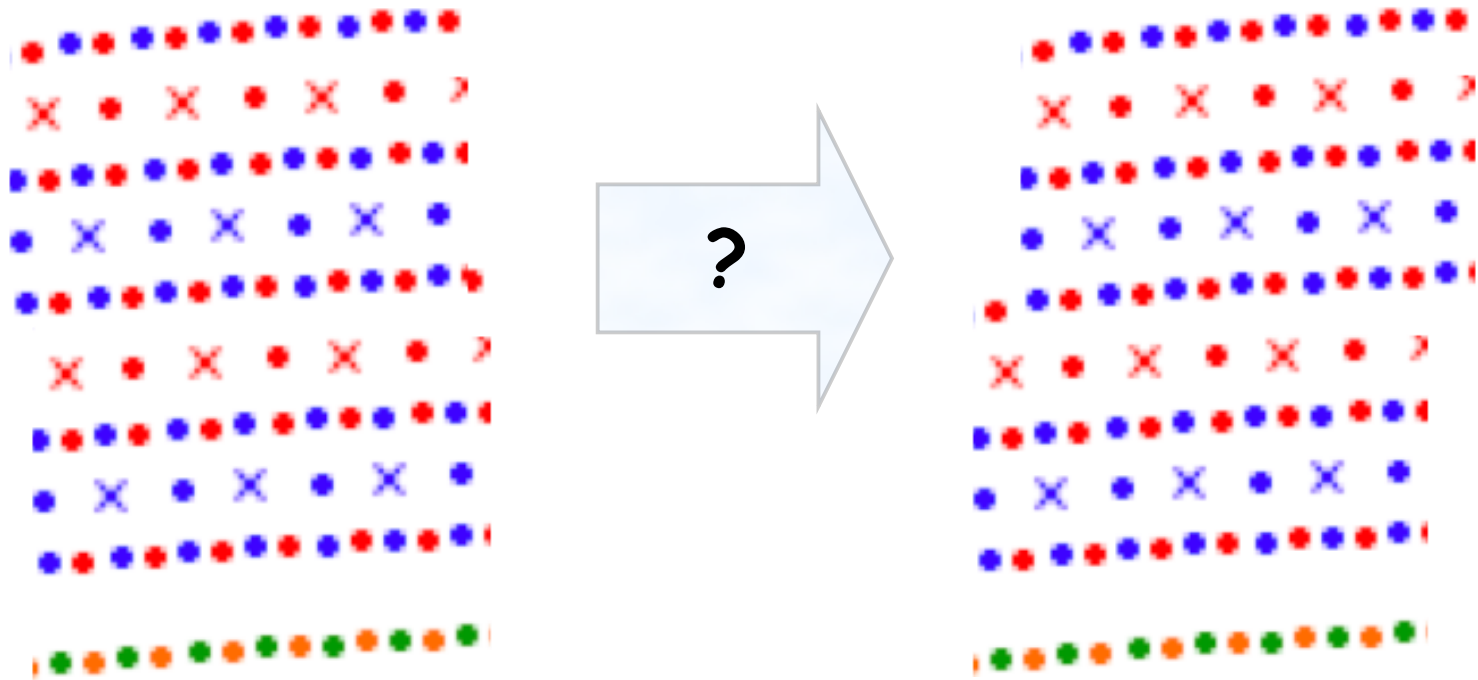
Will depend over overlapped hits reconstruction,  
assuming hits separated if  $|\Delta t| > 50$  nsec

Maybe should be special dial in tracking of close tracks (rearrange hits,...)





# A possible simple change in DCH layout could help



Now in geometry cells from same stereo view are on same phi position;  
Probably it is better to make shift over half cell  
to reduce initial local combinatory

# Summary

- We have a working full simulation of the IDEA tracking systems;
- The track fitting preliminary results look reasonable, in agreement with the Fast MC and show the effect of the PSHW on gain in resolution for high momentum tracks;
- We started to approach the PR problem.
  
- To do:
  - continue to work on the PR to improve the results for the DCH alone case;
  - try to make an optimization of the current IDEA geometry configuration (SVX: n. layers and radii; DCH dimensions and cell layout);
  - improve the hit makers to handle correctly the tracks pile up;
  - Simulate the  $dN/dx$  and the PID;
  - Simulate and test the possible longitudinal resolution;
  - simulate some background effects?
  - porting the DCH geometry etc. into the FCC framework;
  - Interface the PR with the new framework;
  - ... etc ...



backup



# Starting point: Hit simulation approaches

- Common steps:
  - reject the ionization acts releasing less than 10 eV in the gas or that has a G4Step length less than  $5\mu\text{m}$ ;
  - assign the G4Step to the corresponding drift cell (resolve some geometric equations);
  - evaluate the Distance of Closest Approach for each track crossing a cell;
  - convert the DCA in time, smear it with the resolution (converted in time) and sum it to the signal propagation time along the wire and to the particle flight time;
  - all the obtained hit times for a cell are time ordered;
- Simple model for the hit creation:
  - Constant drift velocity (ex.  $2\text{ cm}/\mu\text{s}$ ), B field effects neglected;
  - spatial resolution, gaussian and constant with respect to the impact parameter, ( $\sim 100\mu\text{m}$ );
  - the hits with a time difference shorter than the maximum drift time (for the cell) are grouped together;
  - (eventually evaluate the expected Number of Clusters);
  - Create the hit needed by the reconstruction;
- *Detailed model (not yet implemented):*
  - *Use a realistic XT relation;*
  - *Simulate in detail the Cluster generation and the Signal Waveforms;*
  - *Analyze the waveform and extract the reconstructed Impact parameter and  $dN/dX$  and  $dE/dx$ .*



# Starting point: Kalman Filter Tracking

## Currently performed with GenFit2

- Seeds are constructed at specific layer (begins from outer radii)
- Back interpolate to inner radii
- Tracking done in usual way:
  - Find the extrapolation to the next layer for each track segment
  - Track parameters and Covariance matrix updated at each layer (MS included)
  - Select and assign compatible hits to track
  - hit are accepted if  $\chi^2 < 16$  (hit can be already used by another track)
  - Update track parameters according to accepted hits
- If a good enough track is found:
  - $X^2/NDF < \text{min}X^2\text{cut}$  ,  $N_{\text{hits}} > \text{min}N_{\text{cut}}$ , density of hits  $>$  min density cut
- then attached hits to this track are signed as used (and they can't be used in seeding)
- Seeding repeats again from next layer and re-iterate
- At the end, all found tracks are refitted from inside to outside (with possible assignment of acceptable hits) and vice-versa
- Shared and double tracks are removed by selecting according to quality factors (based on  $\chi^2$ , number of hits, hit density) and hits from track are signed as used



# Global method - histogramming

## Simplest global method: Histogramming

(conformal mapping, hough transform, etc..)

Measurement transformed to surface(line) in track parameter space  
 Maximum in histogram gives track candidate

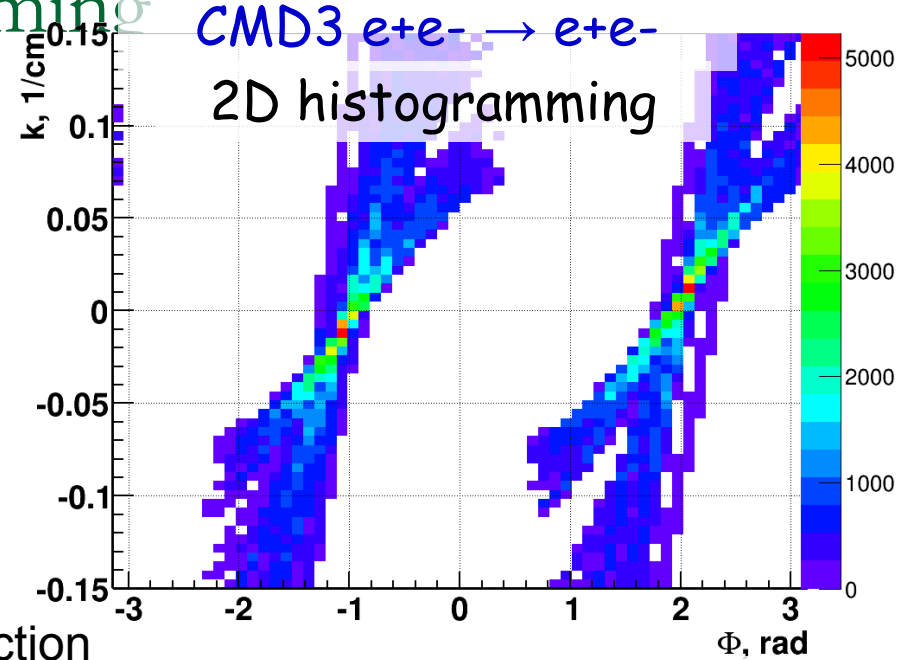
Can be done if it is additional constrains  
 or track parameters well splitted:  
 5D track with beam constrain  $\rightarrow$   
 Independently 2D in R-Phi and 2D in Z- $\theta$  projection

## COMET straw chamber

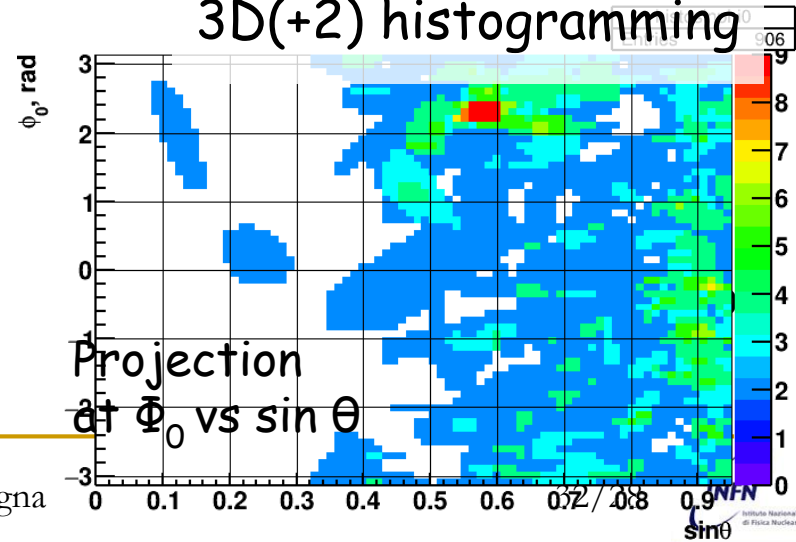
Only 5 stations with large spacing  
 - low connections between layers  
 - impossible to do track following

2 pairs:  
 $\sin \theta, \phi_0, 1/P$   
 $+x_0 (y_0)$

All combinations filled  
 (points in parameters space)

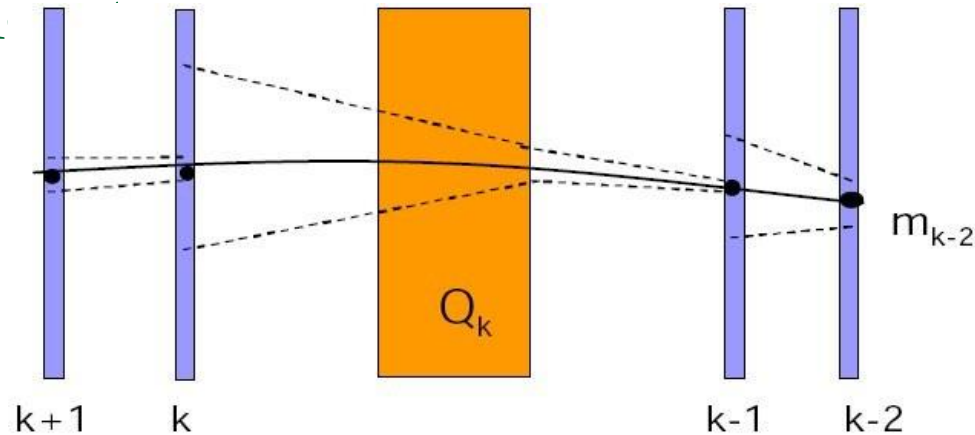


## 105 MeV $e^-$ with noise 3D(+2) histogramming





# Local Method: Track Foll



Follow track candidate iteratively through detection layers

start from an initial track segment (“seed”)

requires dedicated algorithm

extrapolate: estimate the expected track position in the next detection layer

search: look for hits within a window around the estimated track position

update: if a hit is found inside this search window, add it to the track candidate and update the track parameters

iterate: extrapolate the updated track candidate to the next detection layer

**should be broad seeding**: track reconstruction efficiency can depend on it, compromise between efficiency and CPU performance

**allow for detector inefficiencies**: if no hit is found in one layer, continue with the next layer; abandon the candidate if no hits are found in several consecutive layers

**allow for combinatorics**: if more than one hit is found inside the search window, create a separate “branch” for each candidate; follow all branches concurrently

# Variations of Kalman Filter

It can be some variations in implementation (most of them just matter of terminology for specific cases) or with extensions

## SRKF – Square Root Kalman Filter:

Covariance matrix decompose in square root form  
– can give numerical stability

## Information Kalman Filter:

rewritten in form of inverse covariance matrix  
- useful when some parameters can have infinite sigma

## GSF – Gaussian-Sum Filter:

to deal with not gaussian fluctuations - instead of single Gaussian, pdfs modeled by mixture of Gaussians (implemented as a number of Kalman Filters run in parallel)

## CKF - The Combinatorial Kalman Filter

Integrate track fitting and pattern recognition  
– track splitted in case of few compatible hits

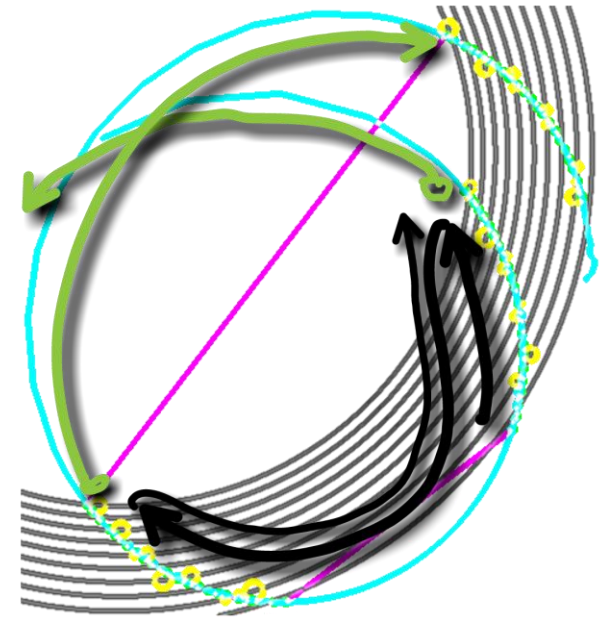
## DAF – Deterministic Annealing Filter

On a same surface, several hits may compete for track with different weights  
– good for outliers removal



# Kalman Filter Tracking (track following method)

- 1) Seeds constructed from outer layers (iteratively layer by layer from not used hits)
- 2) track prolonged by Kalman Filter (over single turn)
- 3) shared and double track removal by quality factor (based on  $\chi^2$ , N of hits, hits density)



as output from PR  
Track turns  
(or sometimes separated  
track segment)

Now matching over 2 segment in same turn  
**are not working**

# Stereo projection

Trajectory:

$$\varphi = \varphi_0 + \arcsin(r/2R) \sim \varphi_0 + r/2R + O(1/6 * (r/2R)^3)$$

(<100  $\mu\text{m}$  for >10 GeV)

Stereo configuration:  $t = a * r_0$ , ( $a = \pm |a|$ )

Stereo projection:  $\varphi_{\text{tr}\pm} \sim \varphi_0 + r/2R - t(r) * z/r \sim \varphi_0 + r * (1/2R - a * \tan\lambda)$

Shift of trajectory with  $\Delta z$  :  $\Delta\varphi_0 = a * \Delta z$

Shift with  $\Delta \tan\lambda$  :  $\Delta 1/2R = a \Delta \tan\lambda$

+ - stereo has different sign of shift

Enough to match any 2 tracks (arbitrary pair of  $P$ ,  $\varphi_0$ ,  $\tan\lambda$ ,  $z$ )

$$a = 1.3 * 10^{-3} \text{ 1/cm}, \quad 1/R \text{ (1/cm)} = 1/Pt \text{ (1/GeV)} * 2\pi * 3 * 10^{-3} \text{ (GeV/cm/}\pi\text{)}$$

$\Delta 0.1 \text{ рад (between 2 tracks)} \rightarrow \Delta z = 40 \text{ cm}$

$$\Delta 1/Pt = 0.43 \Delta \tan\lambda \quad : \quad 1/50 \text{ GeV} \rightarrow 0.05 \text{ rad}$$

