



# **Stato studi acceleratore Muon Collider**

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for the team**

# Outline

- $e^+$  ring with target
- Multi-turn simulations
- Conclusion and Perspectives

# Preliminary scheme for low emittance $\mu$ beam production

## Goal:

$$@T \approx 10^{11} \mu/s$$

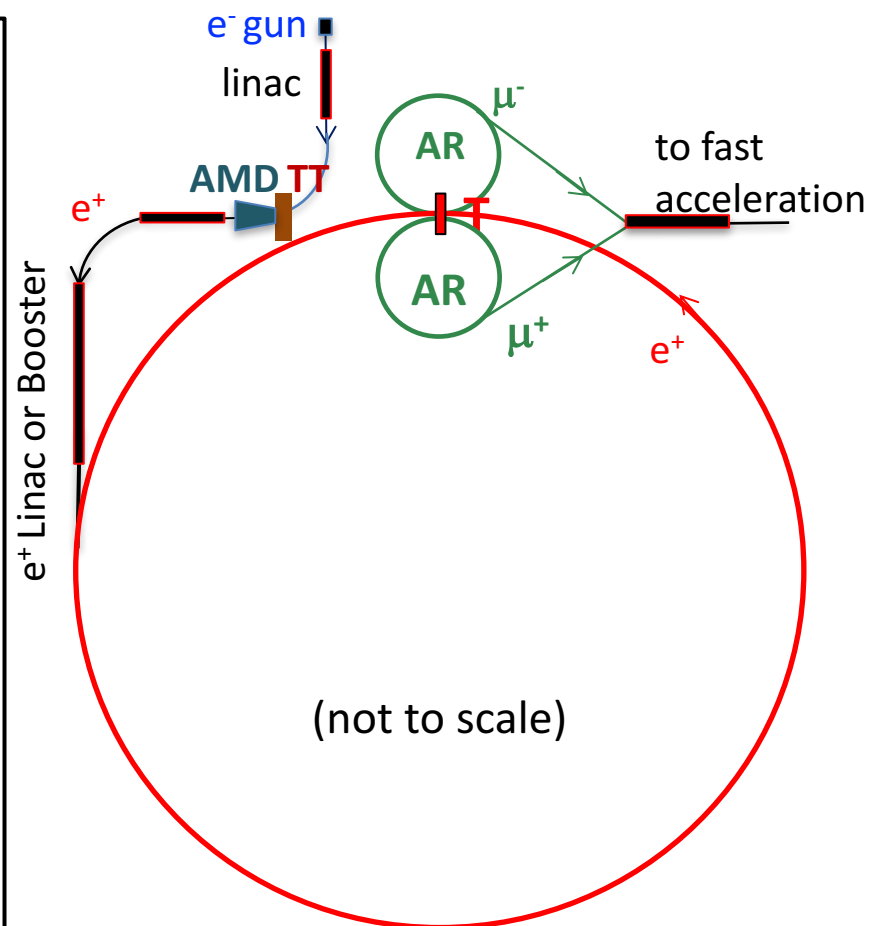
Efficiency  $\approx 10^{-7}$  (with Be 3mm)  $\rightarrow$

$10^{18} e^+/s$  needed @T  $\rightarrow$

$e^+$  stored beam with T

need the largest possible lifetime to minimize positron source rate

LHeC like  $e^+$  source required rate with lifetime( $e^+$ )  $\approx 250$  turns [i.e. 25% momentum aperture]  $\rightarrow$   
 $n(\mu)/n(e^+ \text{ source}) \approx 10^{-5}$



# Preliminary scheme for low emittance $\mu$ beam production

## from $e^+$ SOURCE to RING:

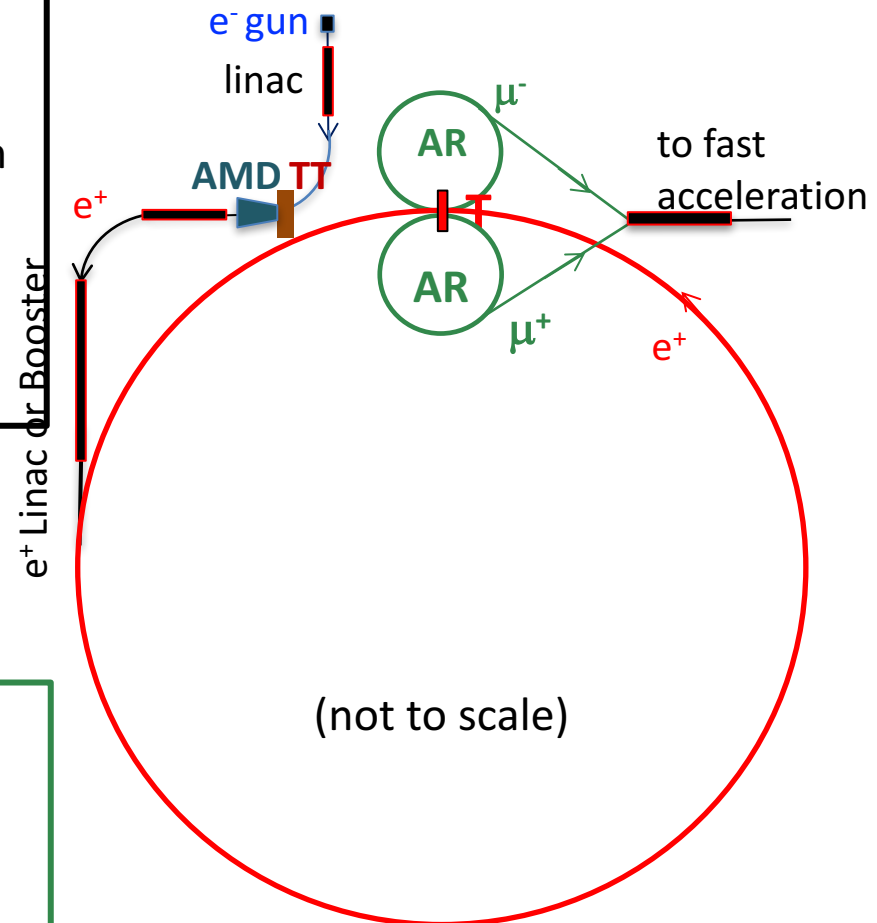
- $e^-$  on conventional Heavy Thick Target (TT) for  $e^+e^-$  pairs production.
- possibly with  $\gamma$  produced by  $e^+$  stored beam on T  $\rightarrow$
- Adiabatic Matching Device (AMD) for  $e^+$  collection  $\rightarrow$
- acceleration (linac / booster), injection  $\rightarrow$

## $e^+$ RING:

- 6.3 km 45 GeV storage ring with target T for muon production

## from $\mu^+ \mu^-$ production to collider

- produced by the  $e^+$  beam on target T with  $E(\mu) \approx 22 \text{ GeV}$ ,  $\gamma(\mu) \approx 200 \rightarrow \tau_{\text{lab}}(\mu) \approx 500 \mu\text{s}$
- AR: 60 m isochronous and high mom. acceptance rings will recombine  $\mu$  bunches for  $\sim 1 \tau_{\mu}^{\text{lab}} \approx 2500$  turns
- fast acceleration
- muon collider



# Preliminary scheme for low emittance $\mu$ beam production

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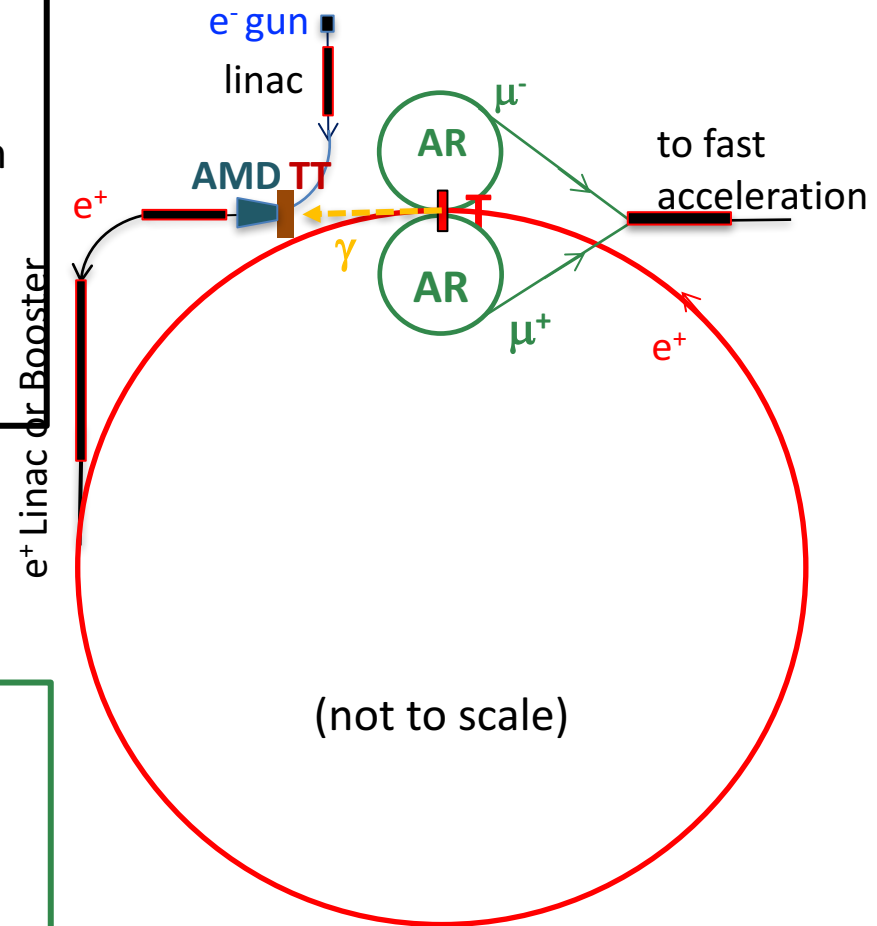
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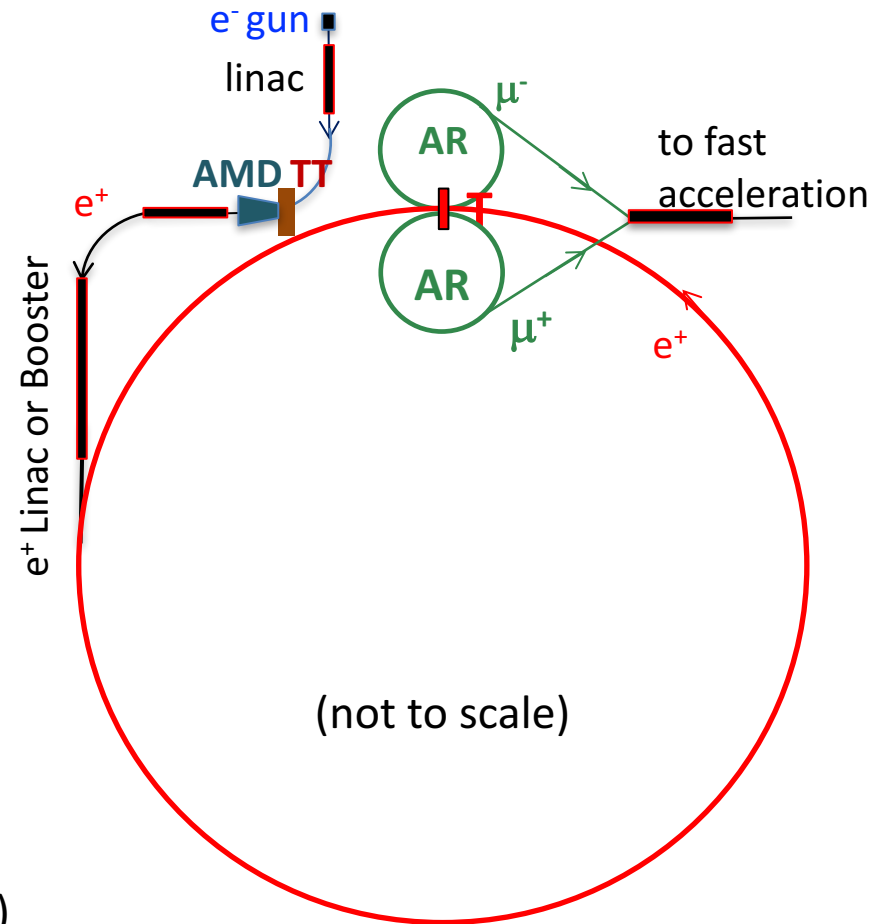
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- muon collider



# Preliminary scheme for low emittance $\mu$ beam production

e <sup>+</sup> ring parameter	unit	
Circumference	km	6.3
Energy	GeV	45
bunches	#	100
e <sup>+</sup> bunch spacing = T <sub>rev</sub> (AR)	ns	200
Beam current	mA	240
N(e <sup>+</sup> )/bunch	#	3 · 10 <sup>11</sup>
U <sub>0</sub>	GeV	0.51
SR power	MW	120



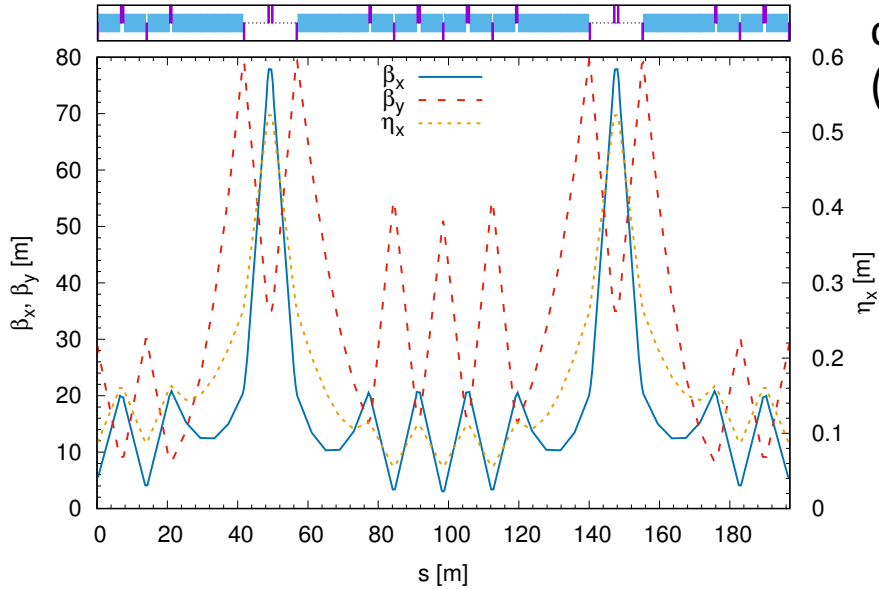
(also 28 km foreseen to be studied as an option)

# Key topics for this scheme

- **Low emittance and high momentum acceptance 45 GeV  $e^+$  ring**
- **O(100 kW) class target in the  $e^+$  ring for  $\mu^+ \mu^-$  production**
- **High rate positron source**
- **High momentum acceptance muon accumulator rings**

# Low emittance 45 GeV positron ring

cell

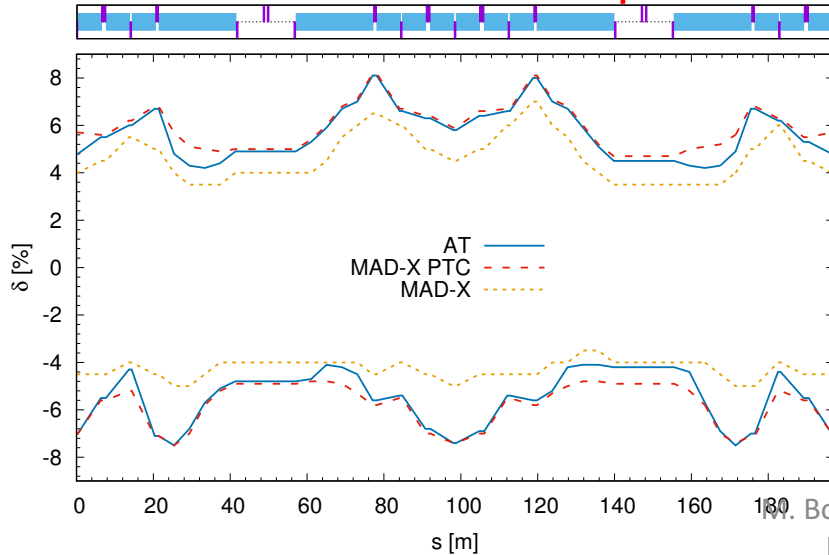


circumference 6.3 km: 197 m x 32 cells  
(no injection section yet)

## Table e+ ring parameters

Parameter	Units	
Energy	GeV	45
Circumference	m	6300
Coupling(full current)	%	1
Emittance x	m	$5.73 \times 10^{-9}$
Emittance y	m	$5.73 \times 10^{-11}$
Bunch length	mm	3
Beam current	mA	240
RF frequency	MHz	500
RF voltage	GV	1.15
Harmonic number	#	10508
Number of bunches	#	100
N. particles/bunch	#	$3.15 \times 10^{11}$
Synchrotron tune		0.068
Transverse damping time	turns	175
Longitudinal damping time	turns	87.5
Energy loss/turn	GeV	0.511
Momentum compaction		$1.1 \times 10^{-4}$
RF acceptance	%	$\pm 7.2$
Energy spread	dE/E	$1 \times 10^{-3}$
SR power	MW	120

## momentum acceptance



Physical aperture=5 cm constant

no errors

Good agreement between **MADX PTC** / **Accelerator Toolbox**,  
both used for particle tracking in our studies

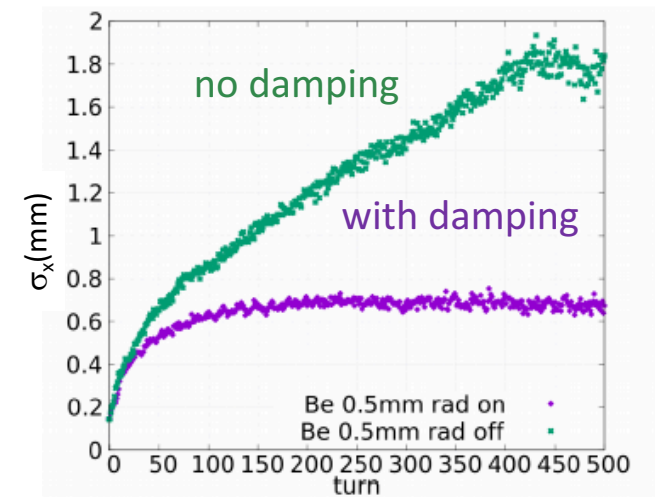


# Multi-turn simulations

1. Initial 6D distribution from the equilibrium emittances
2. 6D  $e^+$  distribution tracking up to the target (AT and MAD-X PTC)
3. tracking through the target (with Geant4beamline and FLUKA and GEANT4)
4. back to tracking code

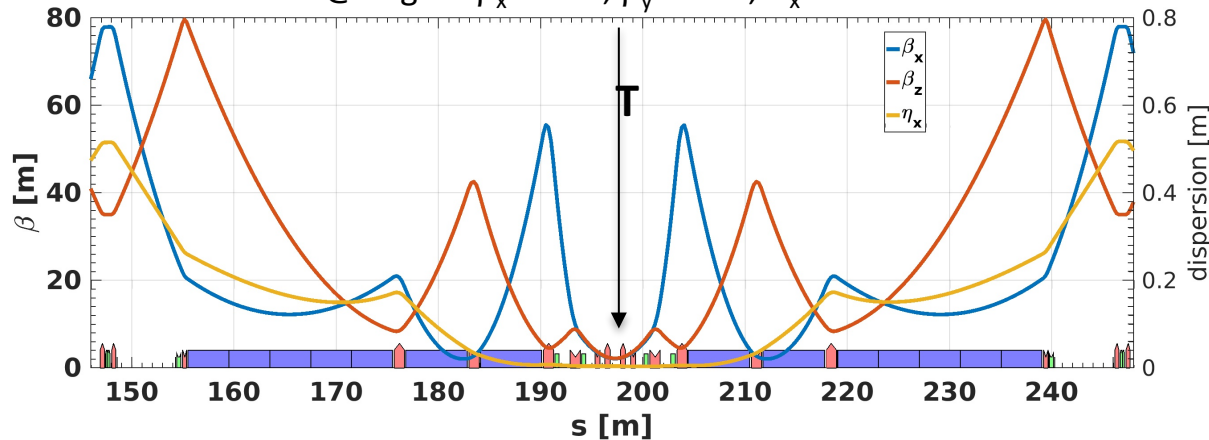
At each pass through the muon target the  $e^+$  beam

- gets an angular kick due to the **multiple Coulomb scattering**, so at each pass changes  $e^+$  beam divergence and size, resulting in an emittance increase.
- undergoes **bremsstrahlung energy loss**: to minimize the beam degradation due to this effect,  $D_x=0$  at target
- in addition there is natural radiation **damping** (it prevents an indefinite beam growth)



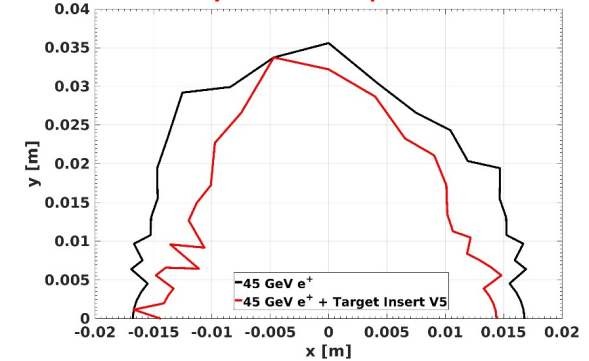
# Preliminary low- $\beta$ IR for muon target insertion

@target:  $\beta_x=1.6\text{m}$ ;  $\beta_y=1.7\text{m}$ ;  $D_x=5.4\text{mm}$

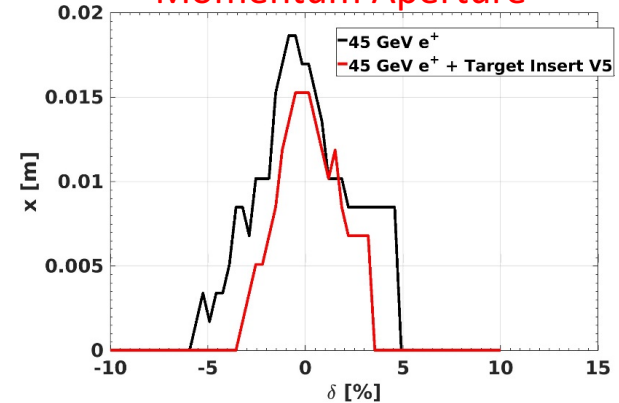


- @target location:
  - $D_x \approx 0$
  - low- $\beta$
- Further optimizations are underway:
  - match the transverse minimum beam size with constraints of target thermo-mechanical stress
  - match with other contributions to muon emittance (production, accumulation)
  - dynamic and momentum aperture can be optimized

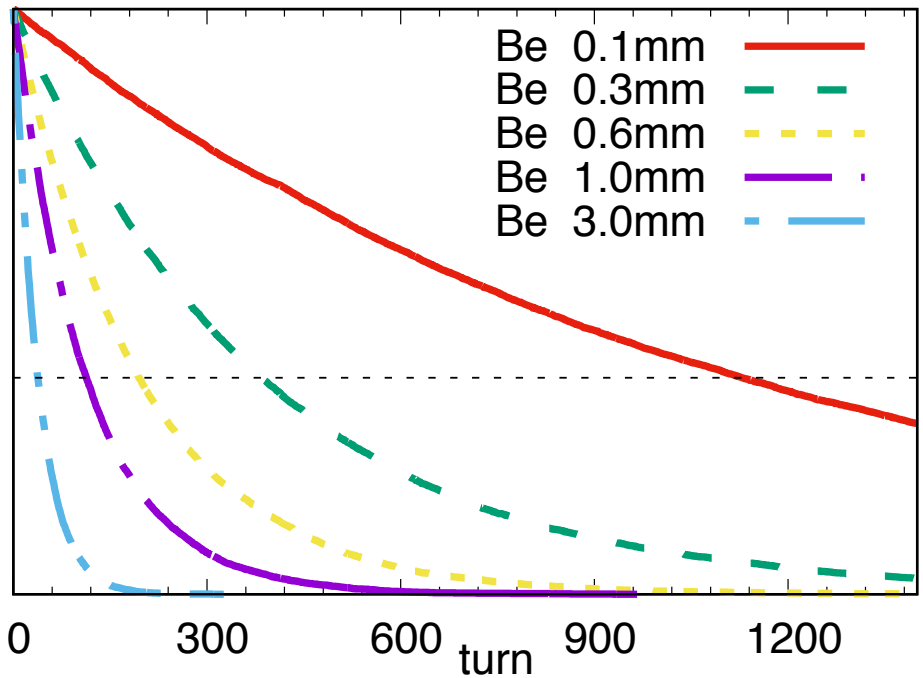
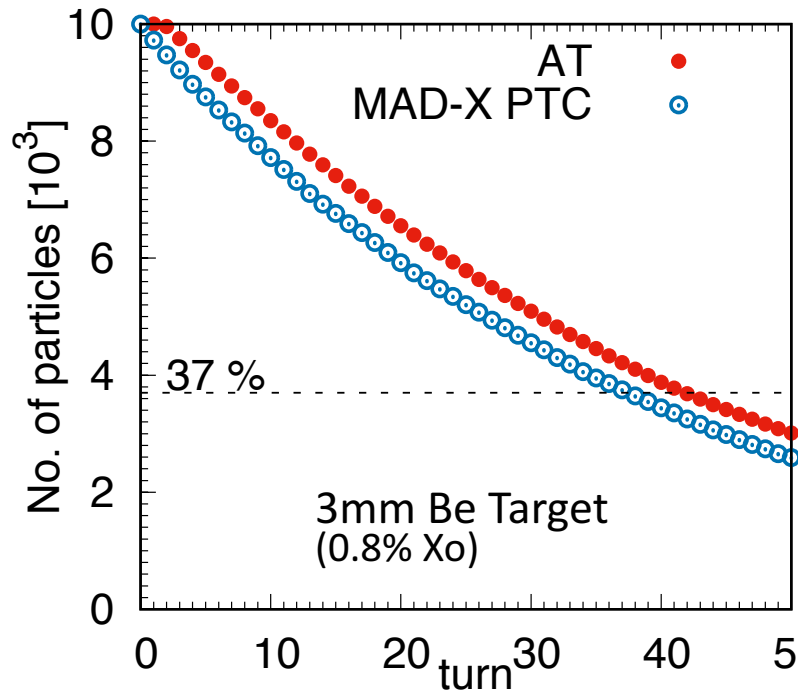
## Dynamic Aperture



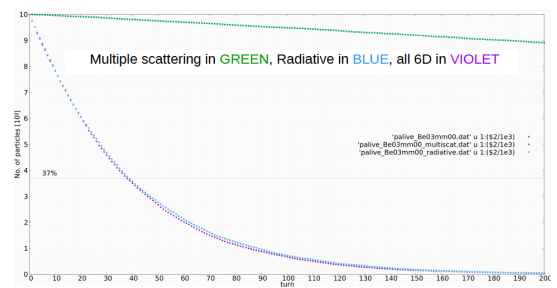
## Momentum Aperture



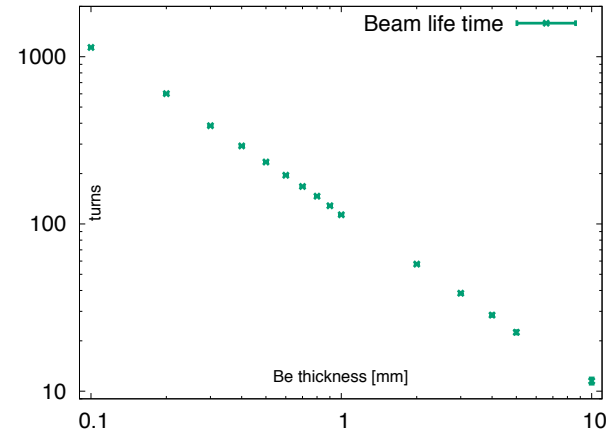
# e+ lifetime with Be target



determined by **bremstrahlung** and **momentum acceptance**  
 Lifetime with  $\sim 40$  turns agreement within 10%



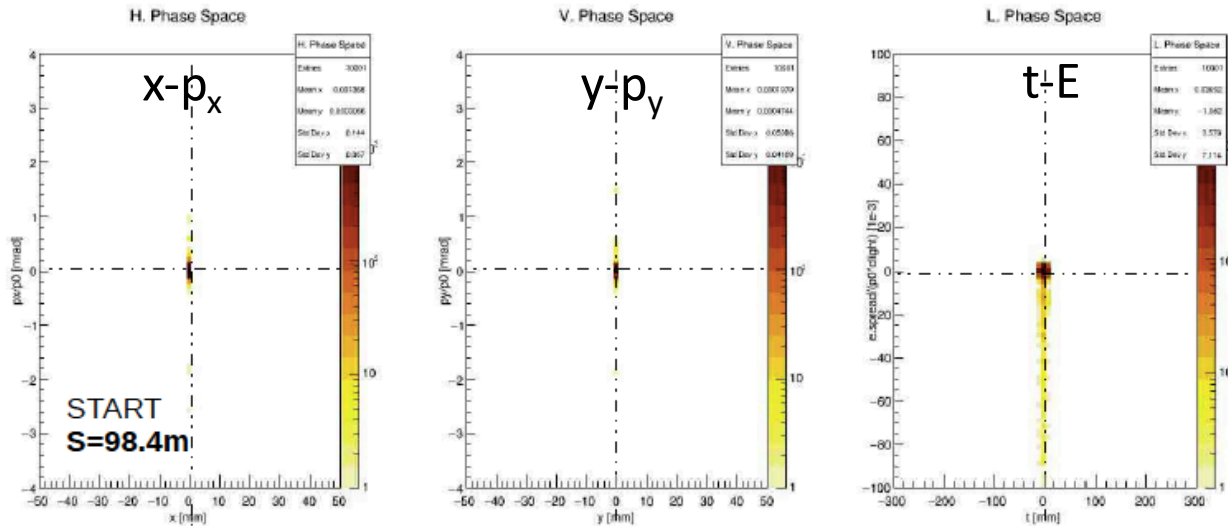
Lifetime  $\propto 1/\text{thickness}$  as expected



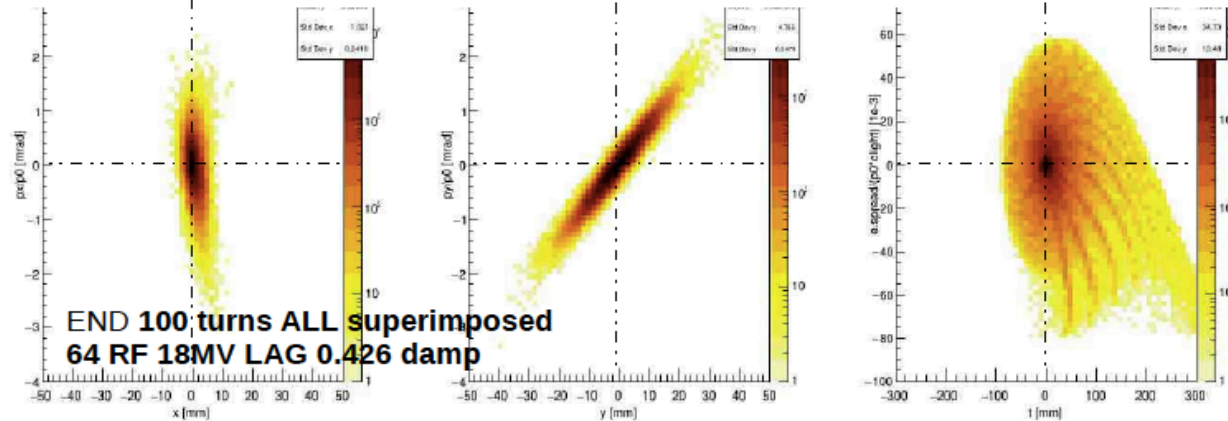
2-3% e+ losses happen in the first turn

# e+ ring with target: beam evolution in the 6D phase space

before target,  
starting point



after 40 turns

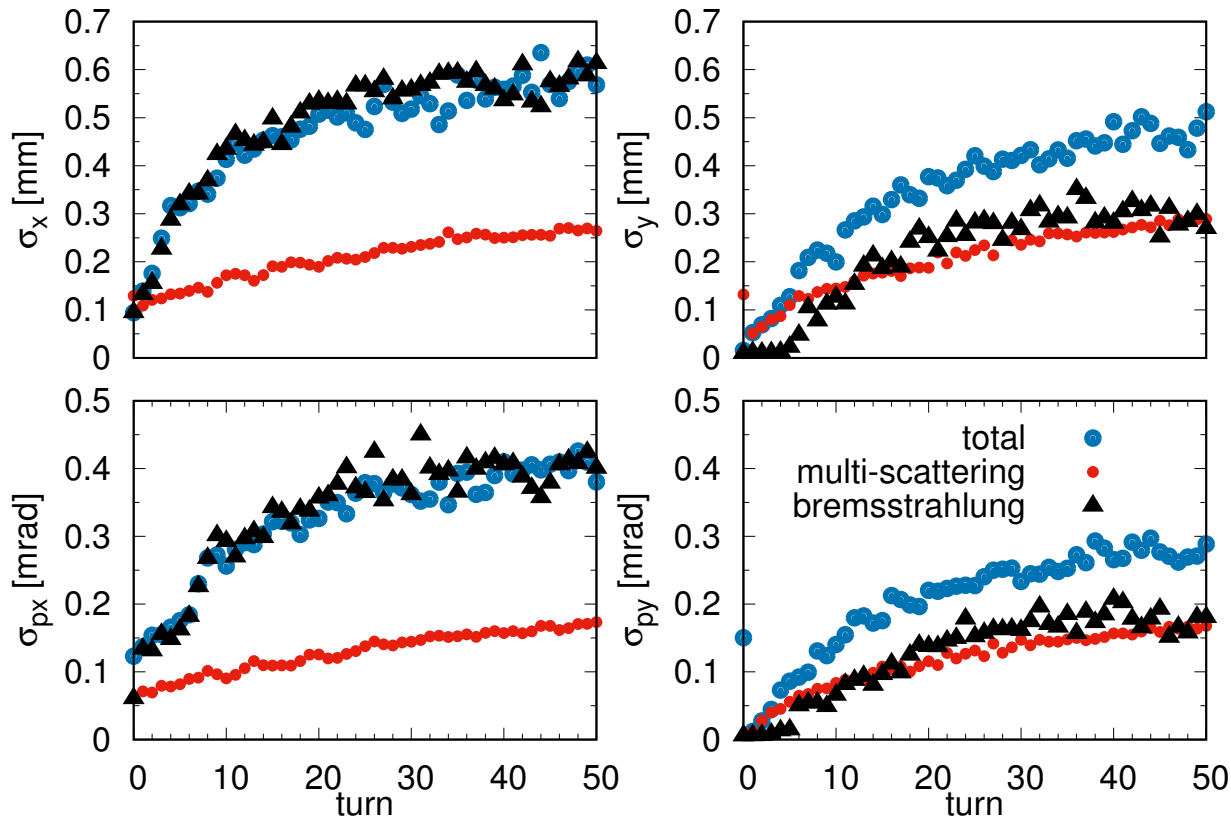


MAD-X PTC & GEANT4 6-D tracking simulation of

e+ beam with 3 mm Be target along the ring (not at IR center in this example)

# Evolution of e+ beam size and divergence

3mm Be Target (0.8% Xo) at center of IR



bremsstrahlung and multiple scattering artificially separated by considering alternatively effects in longitudinal (dominated by **bremsstrahlung**) and transverse (dominated by **multiple scattering**) phase space due to target; in **blue** the combination of both effects (realistic target)

Some bremsstrahlung contribution due to residual dispersion at target  
 multiple scattering contribution in line with expectation:  $\sigma_{MS} = \frac{1}{2} \sqrt{n_D} \sigma'_{MS} \beta$   
 one pass contribution due to the target:  $\sigma'_{MS} = 25 \mu\text{rad}$

# Muon emittance

$$\varepsilon(\mu) = \varepsilon(e^+) \oplus \varepsilon(\text{MS}) \oplus \varepsilon(\text{rad}) \oplus \varepsilon(\text{prod}) \oplus \varepsilon(\text{AR})$$

would like all contributions of same size  
knobs:

$\varepsilon(e^+)$  =  $e^+$  emittance

$\varepsilon(\text{MS})$  = multiple scattering contribution

$\varepsilon(\text{rad})$  = energy loss (brem.) contribution

$\varepsilon(\text{prod})$  = muon production contribution

$\varepsilon(\text{AR})$  = accumulator ring contribution

$\beta_x \beta_y$  @target & target material

$\beta_x \beta_y D_x$  @target & target material

$E(e^+)$  & target thickness

AR optics & target

with constraints from target survival

now:  $\varepsilon(\mu)$  dominated by  $\varepsilon(\text{MS}) \oplus \varepsilon(\text{rad})$  -> lower dispersion & lower  $\beta$ -functions at target  
with beam spot at the limit of the target survival

also test different material

- crystals in channeling better:  $\varepsilon(\text{MS})$ ,  $\varepsilon(\text{rad})$ ,  $\varepsilon(\text{prod})$  (also gain in lifetime)
- light liquid jet target better:  $\varepsilon(\text{MS})$ ,  $\varepsilon(\text{rad})$   
(also gain in lifetime & target thermo-mechanical characteristics)

# Preliminary consideration on e<sup>+</sup> production

[L.Rinolfi *et al.* NIM B **309** (2013)50-55]

The target represented on the figure is a conventional one.

It would be also possible to have an *hybrid positron source* using a crystal providing channeling radiation and an amorphous converter for photon conversion into e<sup>+</sup>e<sup>-</sup> pairs

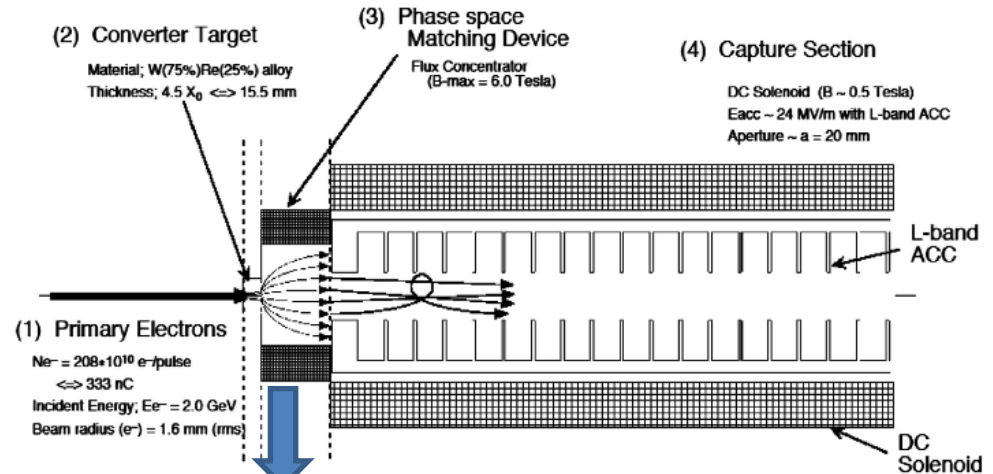
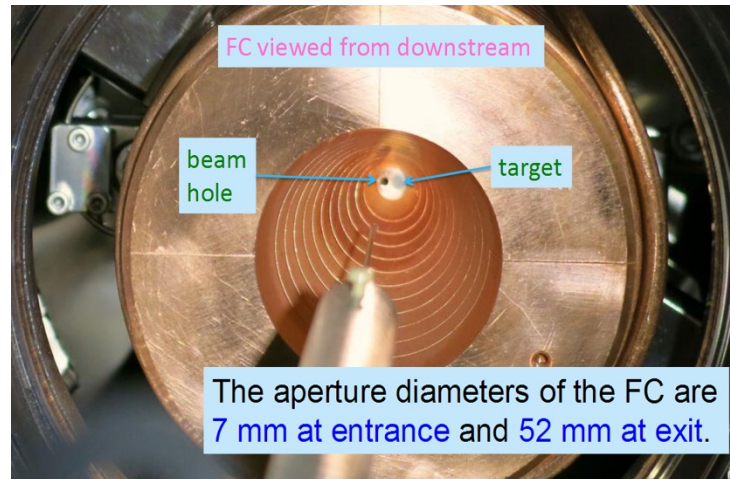


Fig. 2. Layout of the CLIC e<sup>+</sup> source with a single target.



Flux concentrated used for the Adiabatic Matching Device  
(from T.Kamitani, LCWS-2014, Belgrade)

# FOCUSING SYSTEMS FOR POSITRON SOURCES

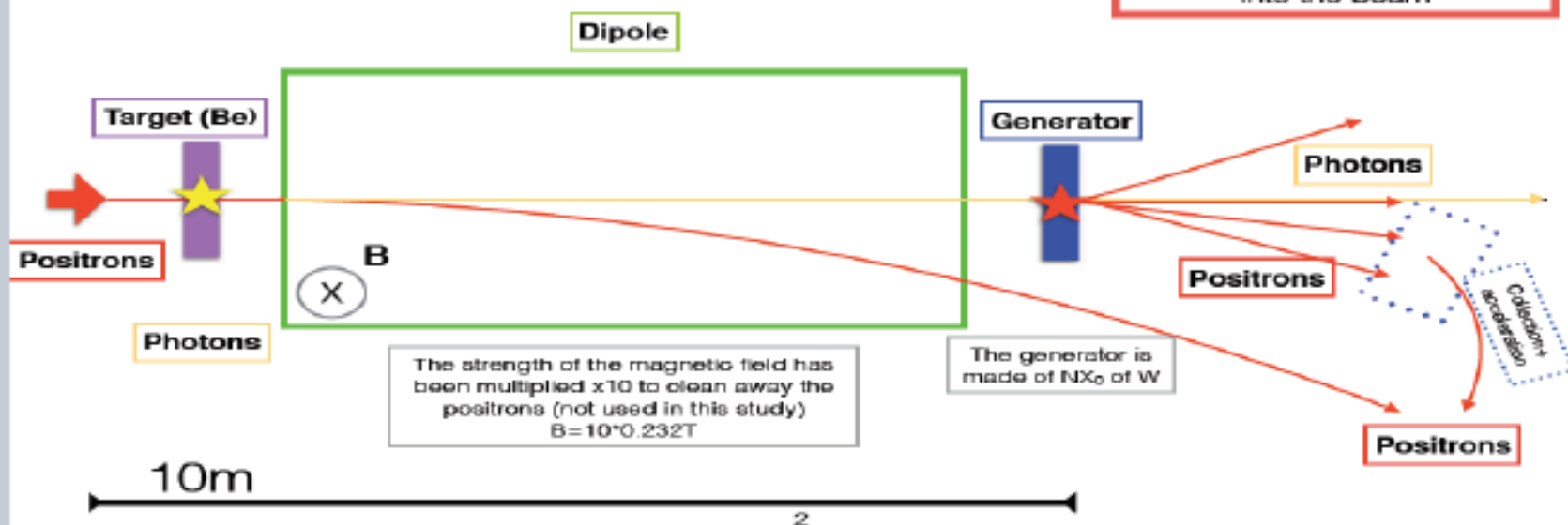
2

## setup

Positrons in the target create photons at very small angles wrt to the beam  
(via radiative bhabha:  
 $e^+ e^- \rightarrow e^+ e^- \gamma$ )

Photons in the Generator create positrons  
(via pair production)

These positrons could be accelerated and re-injected into the beam

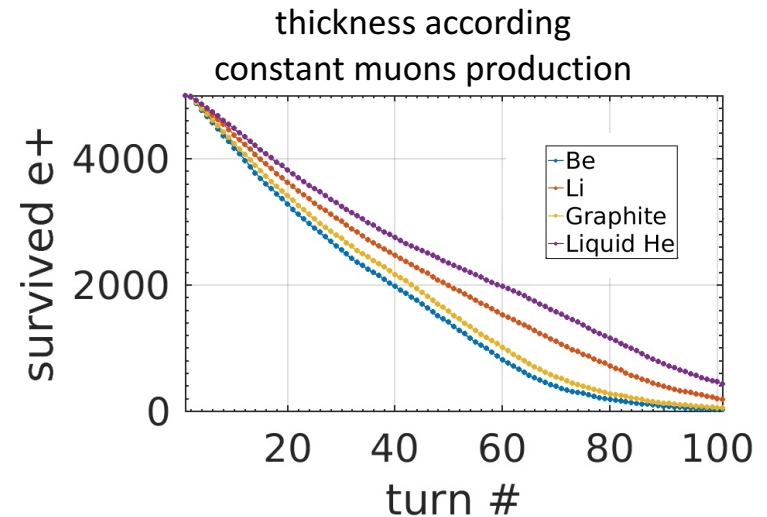
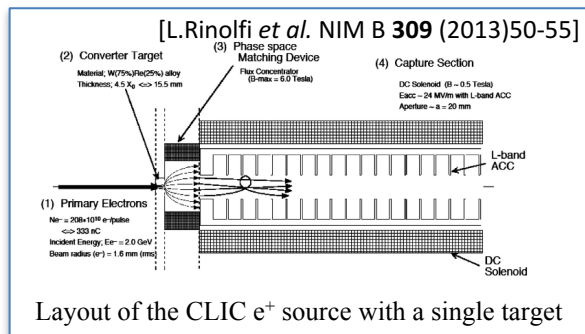






# Conclusion and Perspectives

- First design of low emittance  $e^+$  ring with preliminary studies of beam dynamics
- Optimization requires other issues to be preliminary addressed:
  - target material & characteristics
  - $e^+$  accelerator complex



- muon accumulator rings design

Preliminary studies for a low emittance muon source are promising

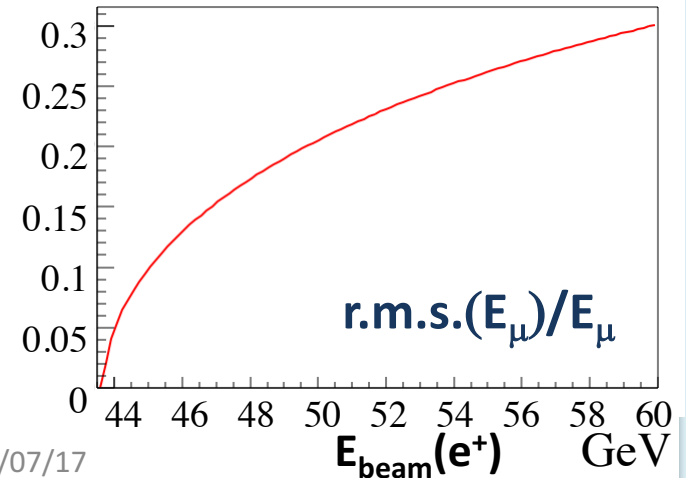
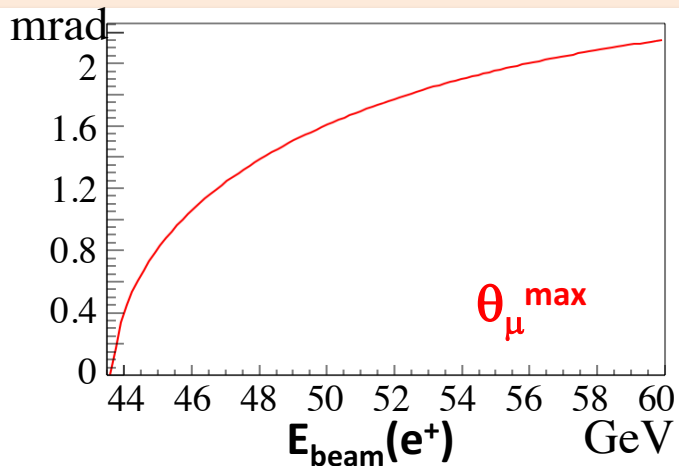
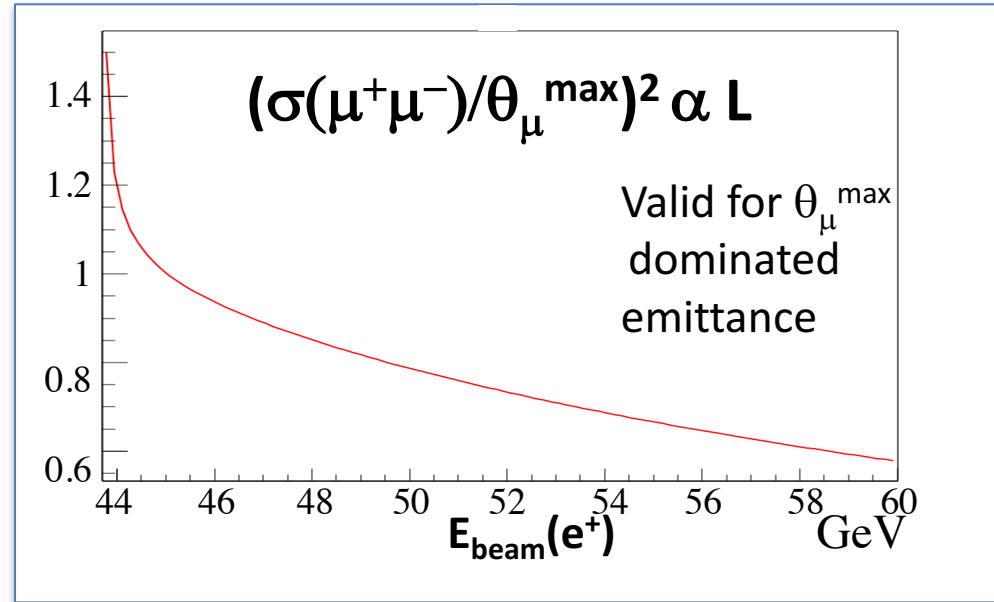
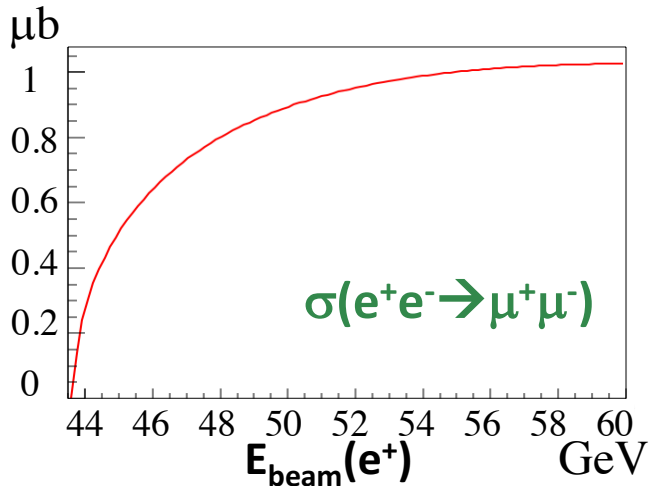
We will continue to optimize all the parameters, lattices, targets, etc. in order to assess the ultimate performances of a muon collider based on this concept

# Back-up

# Luminosity of $\mu^+\mu^-$ Collider vs $e^+$ beam energy

Parametric behaviours

Is there an optimal value for the positron beam energy?



**Key R&D**

MW proton driver  
MW class target  
NCRF in magnetic field

Ionization cooling  
High field solenoids (30T)  
High Temp Superconductor

Cost eff. low RF SC  
Fast pulsed magnet (1kHz)

Detector/  
machine interface

**Key Challenges**

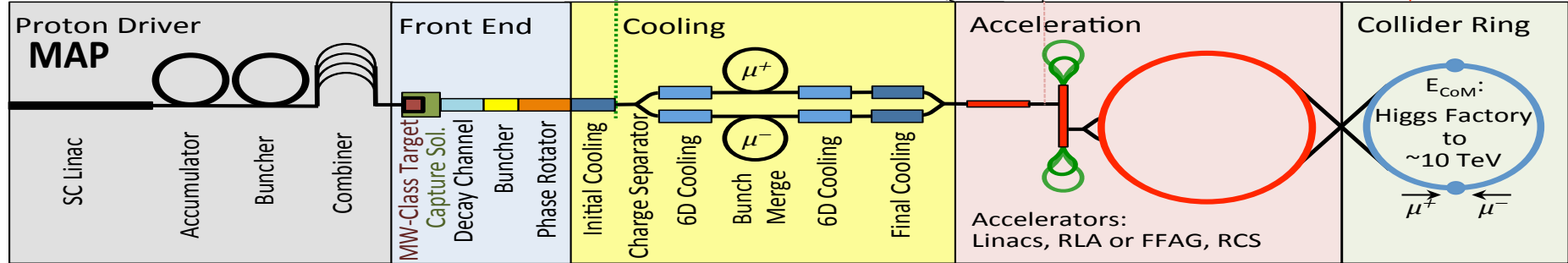
$\sim 10^{13}-10^{14} \mu / \text{sec}$   
Tertiary particle  $p \rightarrow \pi \rightarrow \mu$ :

Fast cooling  
( $\tau=2\mu\text{s}$ ) by  $10^6$  (6D)

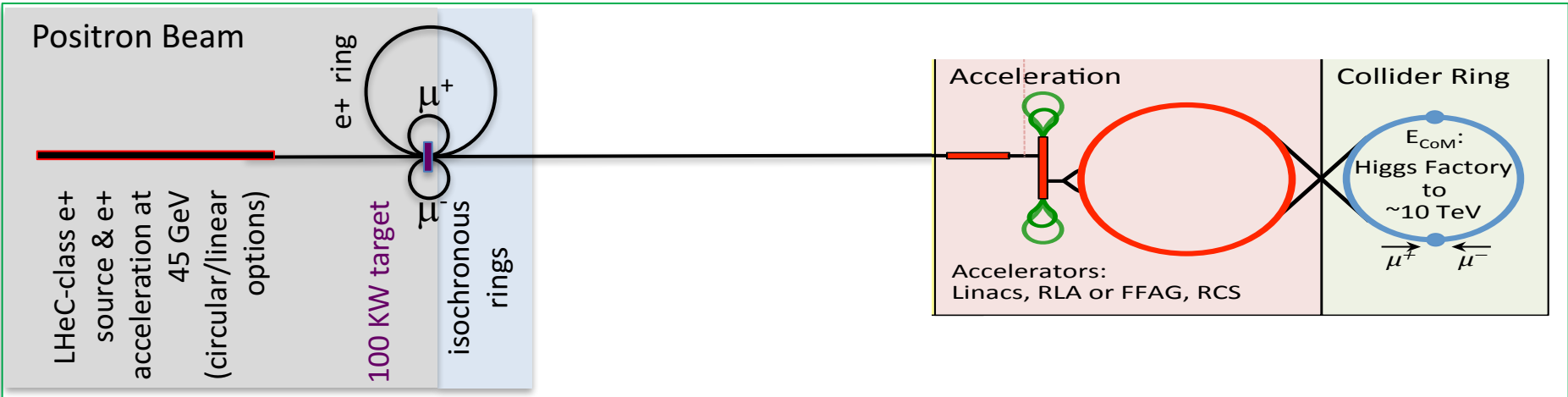
Fast acceleration  
mitigating  $\mu$  decay

Background  
by  $\mu$  decay

**Muon Collider**



share the same complex



**Key Challenges**

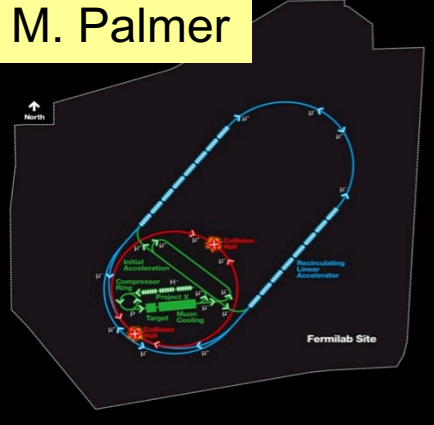
$\sim 10^{11} \mu / \text{sec}$  from  $e^+e^- \rightarrow \mu^+\mu^-$

**Key R&D**

$10^{15} e^+/\text{sec}$ , 100 kW class target, NON destructive process in  $e^+$  ring

**EASIER AND CHEAPER DESIGN, IF FEASIBLE**

# Muon Collider Parameters



**Muon Collider Parameters**

Parameter	Units	Higgs	Multi-TeV		
		Production Operation			Accounts for Site Radiation Mitigation
CoM Energy	TeV	0.126	1.5	3.0	6.0
Avg. Luminosity	$10^{34} \text{cm}^{-2} \text{s}^{-1}$	0.008	1.25	4.4	12
Beam Energy Spread	%	0.004	0.1	0.1	0.1
Higgs Production/ $10^7$ sec		13,500	37,500	200,000	820,000
Circumference	km	0.3	2.5	4.5	6
No. of IPs		1	2	2	2
Repetition Rate	Hz	15	15	12	6
$\beta^*$	cm	1.7	1 (0.5-2)	0.5 (0.3-3)	0.25
No. muons/bunch	$10^{12}$	4	2	2	2
Norm. Trans. Emittance, $\epsilon_{TN}$	$\pi$ mm-rad	0.2	0.025	0.025	0.025
Norm. Long. Emittance, $\epsilon_{LN}$	$\pi$ mm-rad	1.5	70	70	70
Bunch Length, $\sigma_s$	cm	6.3	1	0.5	0.2
Proton Driver Power	MW	4	4	4	1.6
Wall Plug Power	MW	200	216	230	270

Exquisite Energy Resolution Allows Direct Measurement of Higgs Width

Success of advanced cooling concepts  $\Rightarrow$  several  $\ll 10^{32}$  [Rubbia proposal:  $5 \ll 10^{32}$ ]