

Structure of Cd isotopes within the beyond-mean-field IBM

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Padua, May 2018

Even-even $^{106-116}\text{Cd}$

^{112}Cd

- Deviation from vibrational picture, due to additional 0+ and 2+ states → intruder?

$$\begin{array}{ccc} 0^+ & \underline{1433} & 4^+ & \underline{1416} & 2^+ & \underline{1468} \\ 0^+ & \underline{1224} & & & 2^+ & \underline{1312} \end{array}$$

- Experimental evidence:

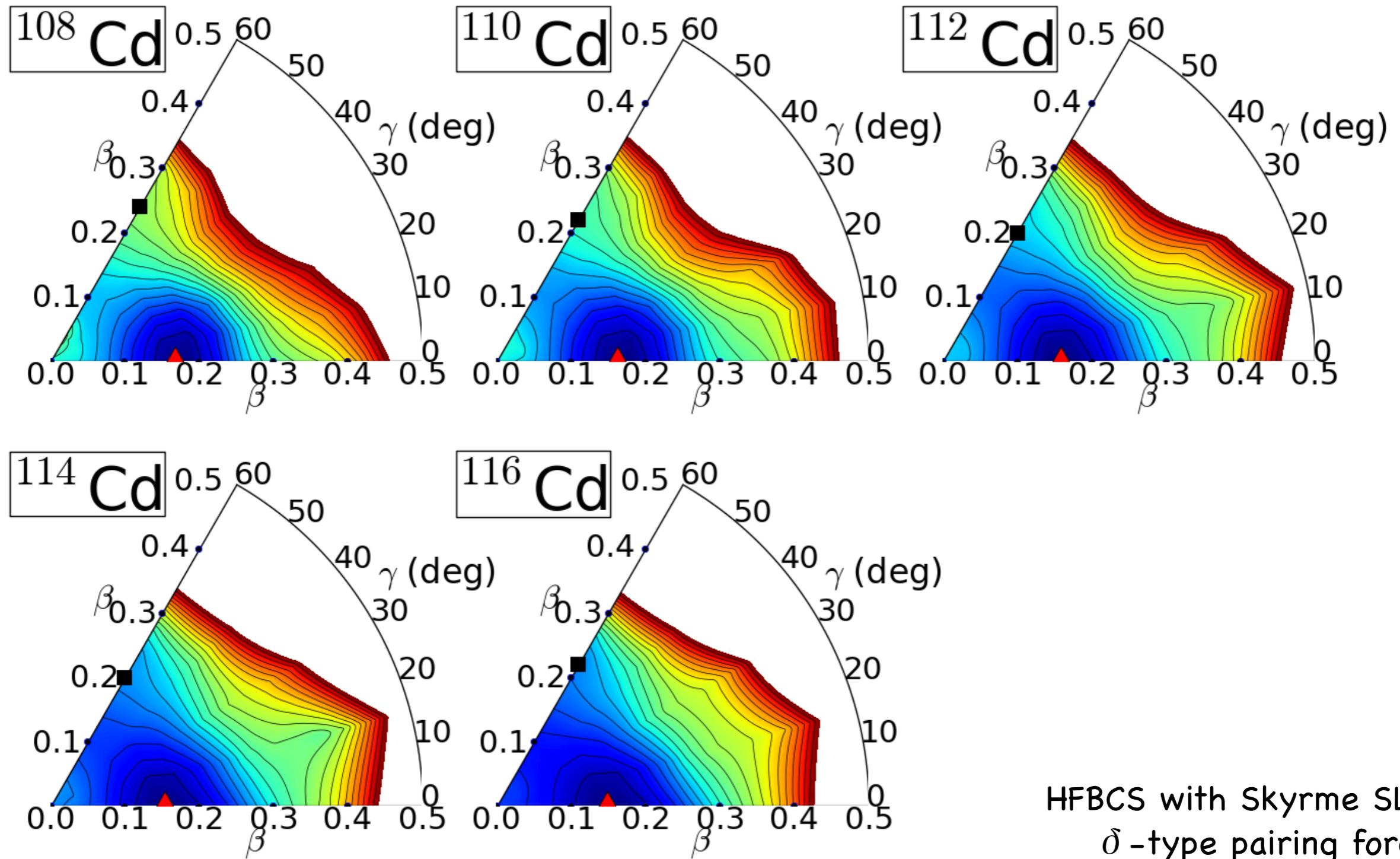
P. E. Garrett (2016), etc. and refs therein

$$2^+ \underline{618}$$

$$0^+ \underline{0}$$

We consider the problem within the DFT framework

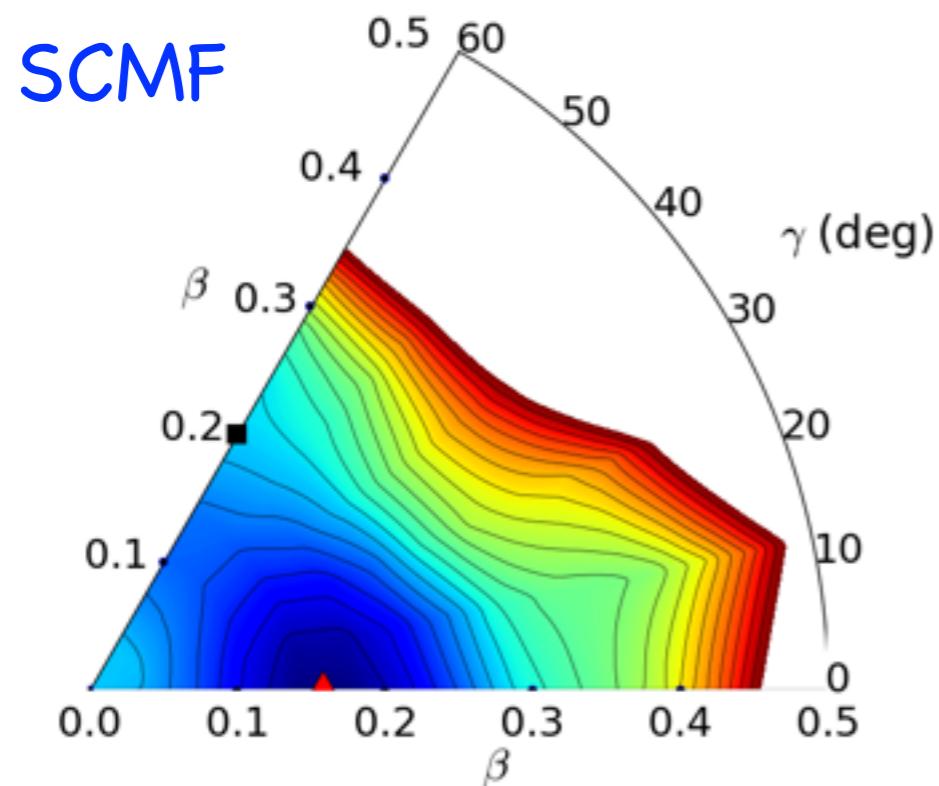
Self-consistent mean-field potential energy surface



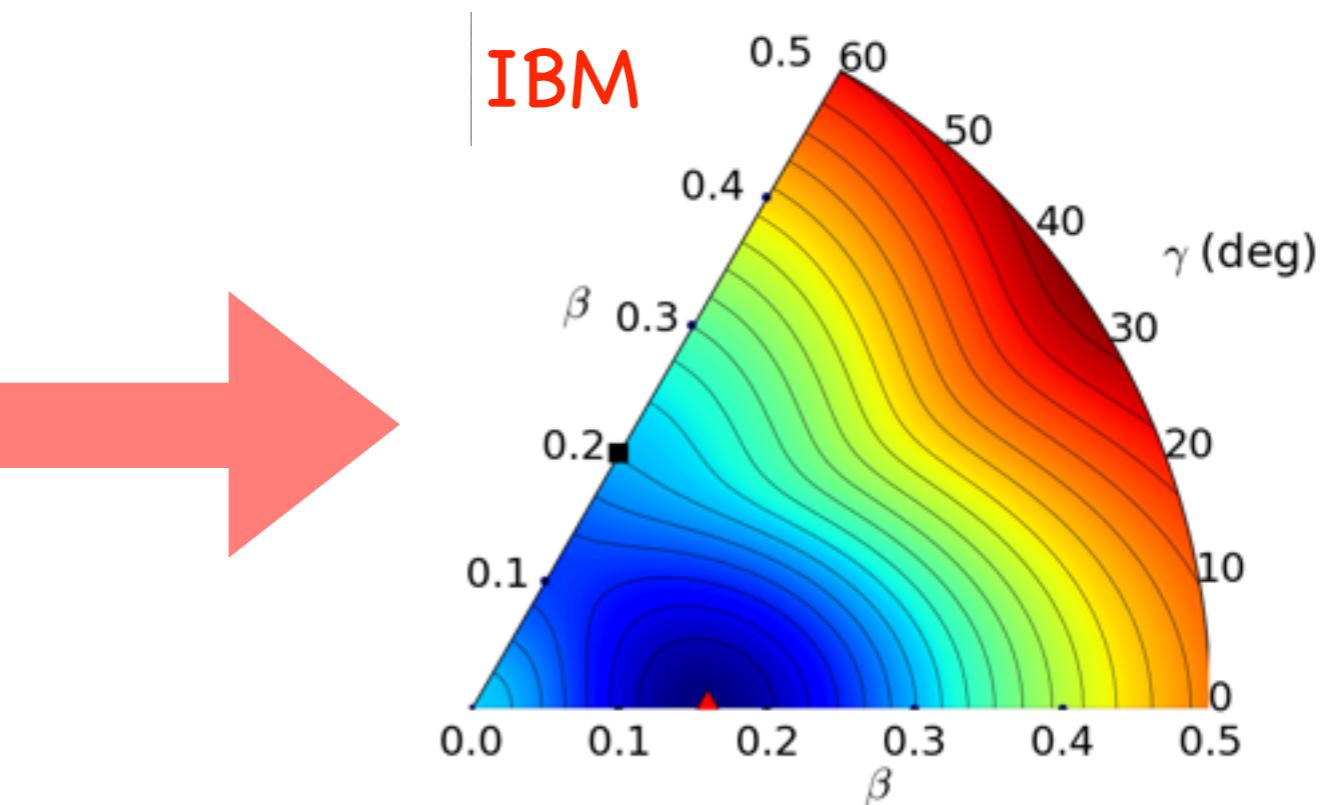
spectroscopic properties → calculated by the IBM Hamiltonian

SCMF-to-IBM mapping

1. SCMF calculation
of energy surface



2. ... mapped to config. mix IBM
surface → strength parameters
of the IBM Hamiltonian



3. energies and electromagnetic transition rates →
diagonalization in lab frame

IBM with configuration mixing

Normal ($\pi(0p-0h)$) config:
prolate global minimum

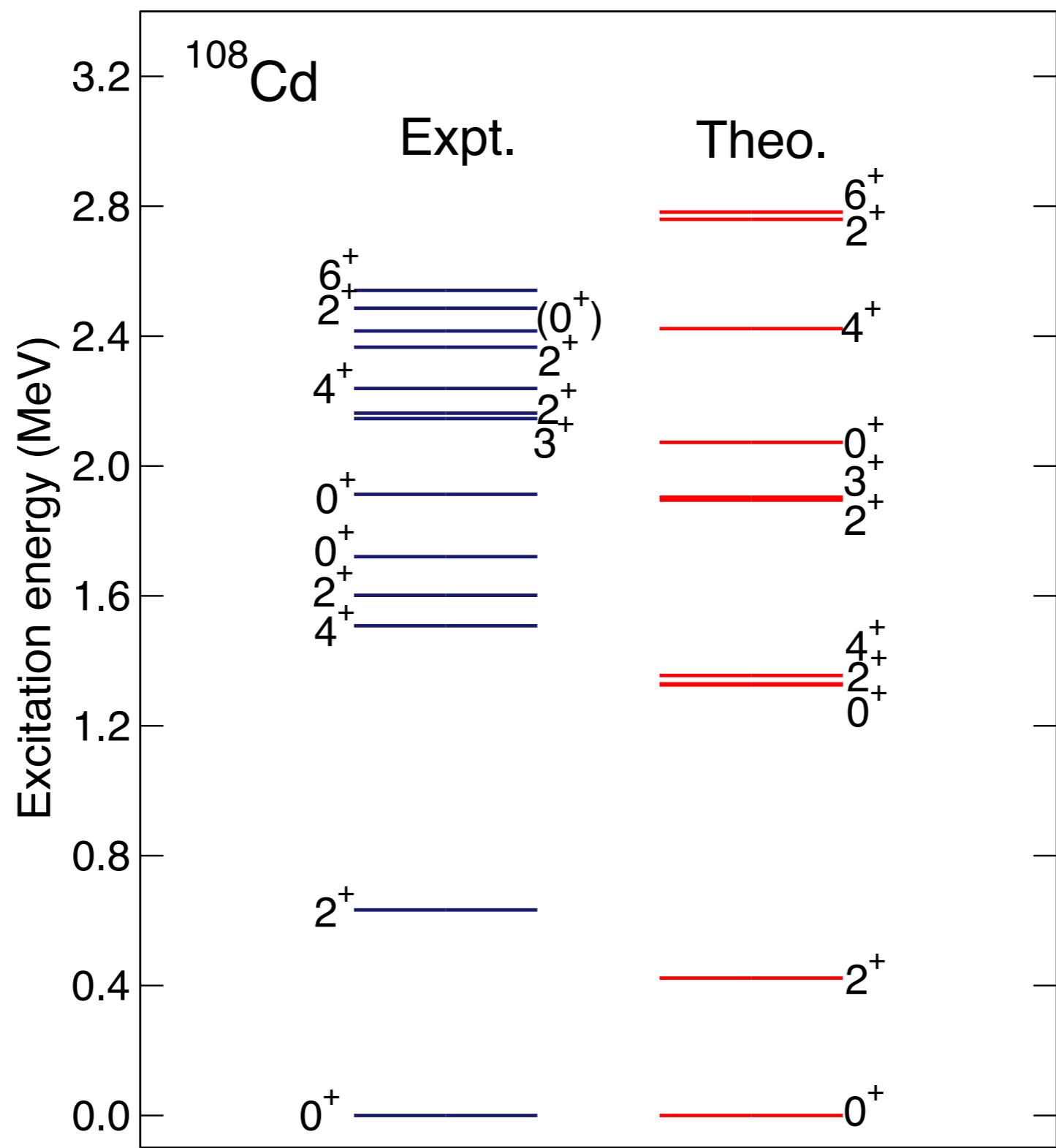
Intruder ($\pi(2p-2h)$) config:
oblate local “minimum”

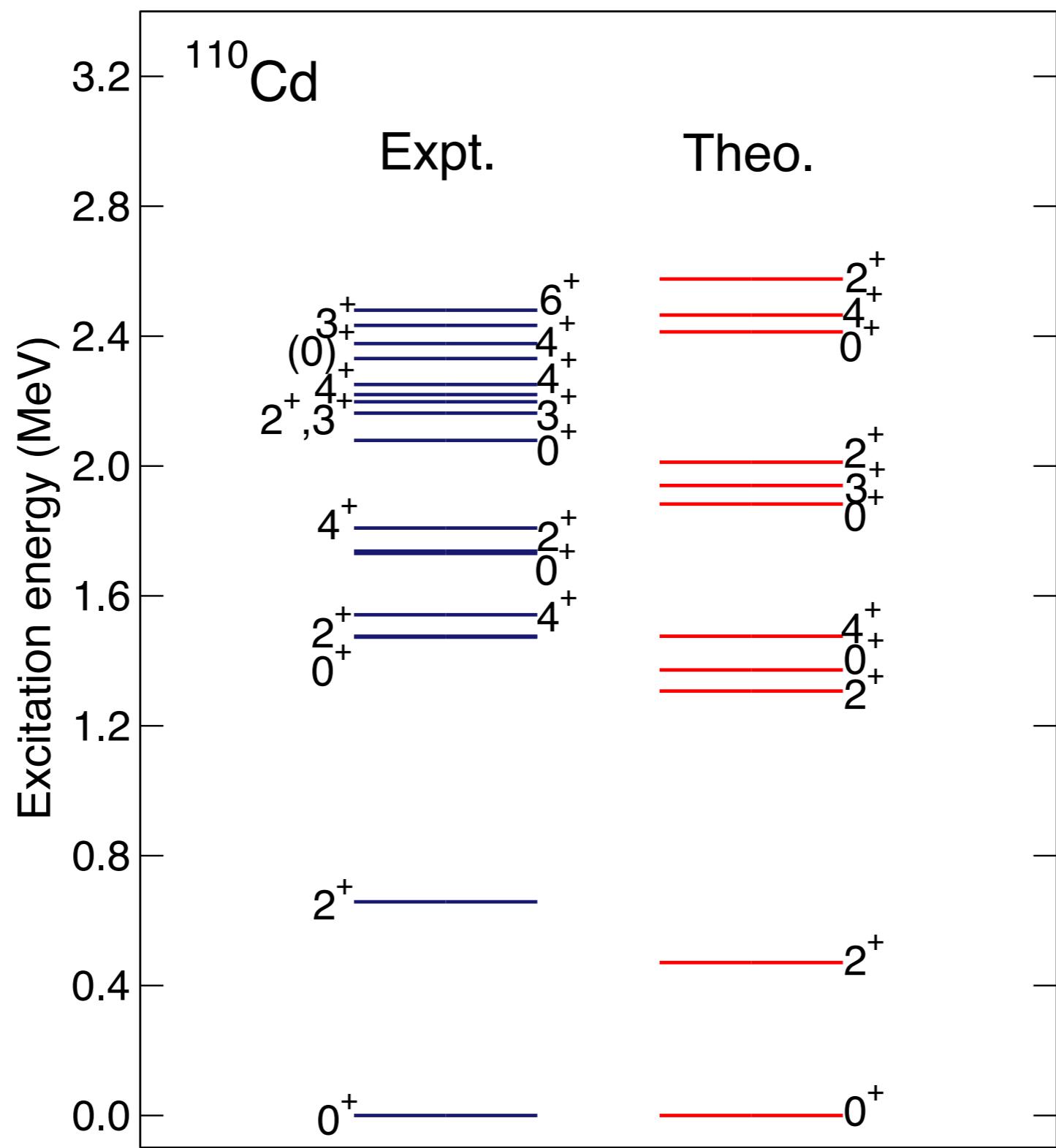
$$\hat{H} = \hat{\mathcal{P}}_1 \hat{H}_1 \hat{\mathcal{P}}_1 + \hat{\mathcal{P}}_3 (\hat{H}_3 + \Delta) \hat{\mathcal{P}}_3 + \hat{H}_{\text{mix}},$$

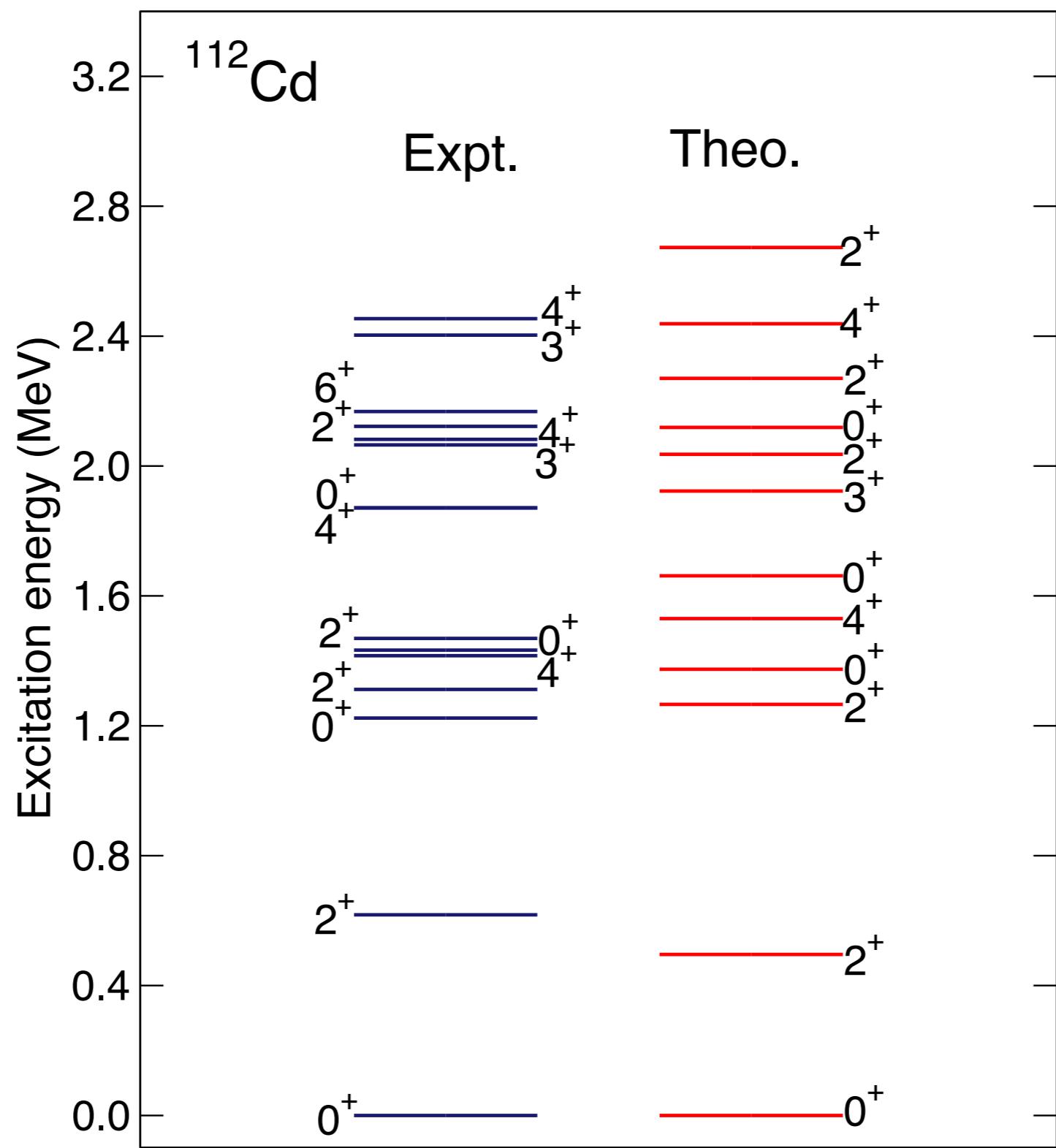
energy needed to promote
protons across $Z=50$

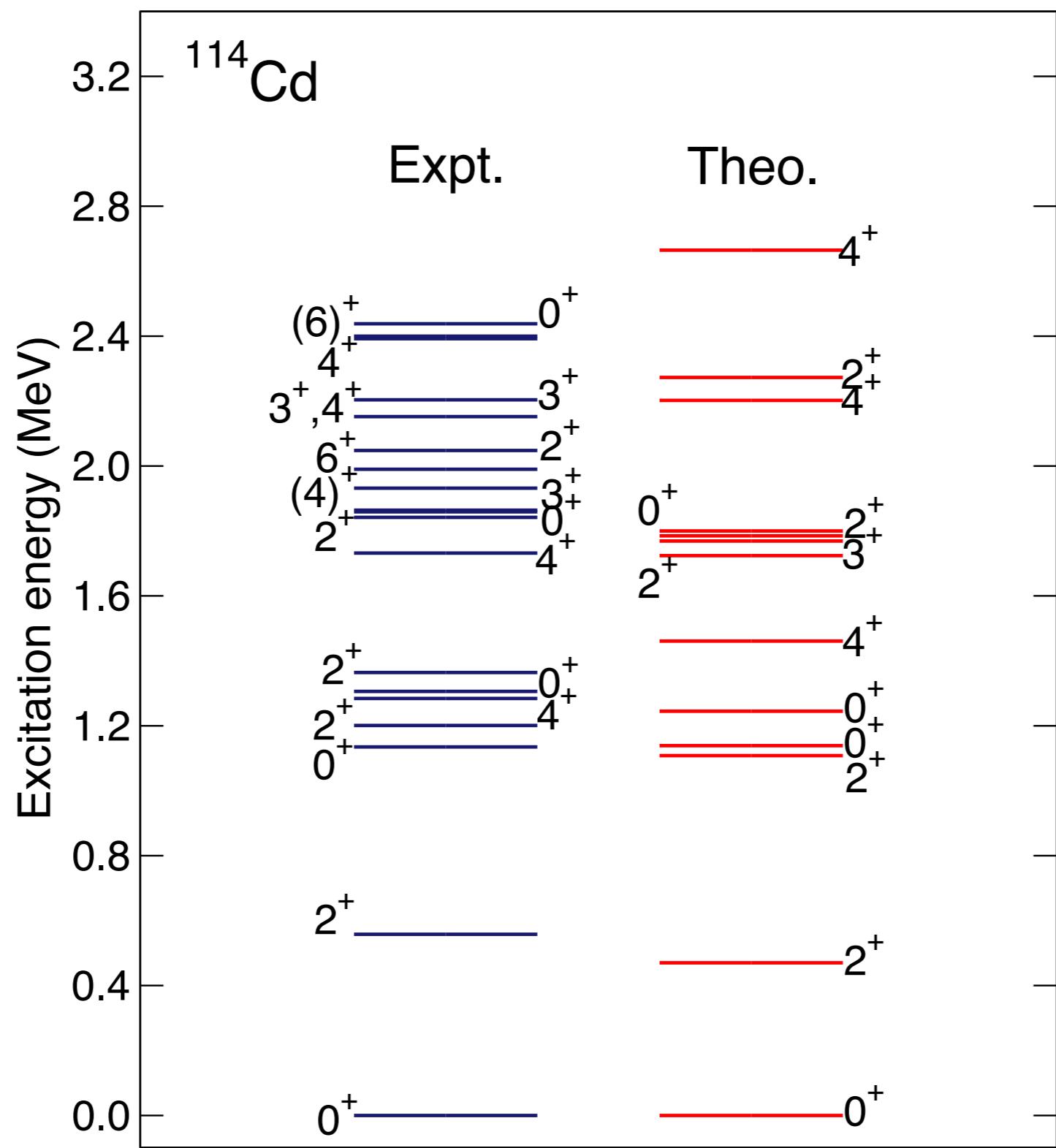
$$\hat{H}_i = \epsilon_d (\hat{n}_{d\nu} + \hat{n}_{d\pi}) + \kappa \hat{Q}_\nu \cdot \hat{Q}_\pi + \kappa' \hat{L} \cdot \hat{L},$$

$$\hat{H}_{\text{mix}} = \omega (s_\pi^\dagger s_\pi^\dagger + d_\pi^\dagger d_\pi^\dagger)^{(0)} + H.c.$$









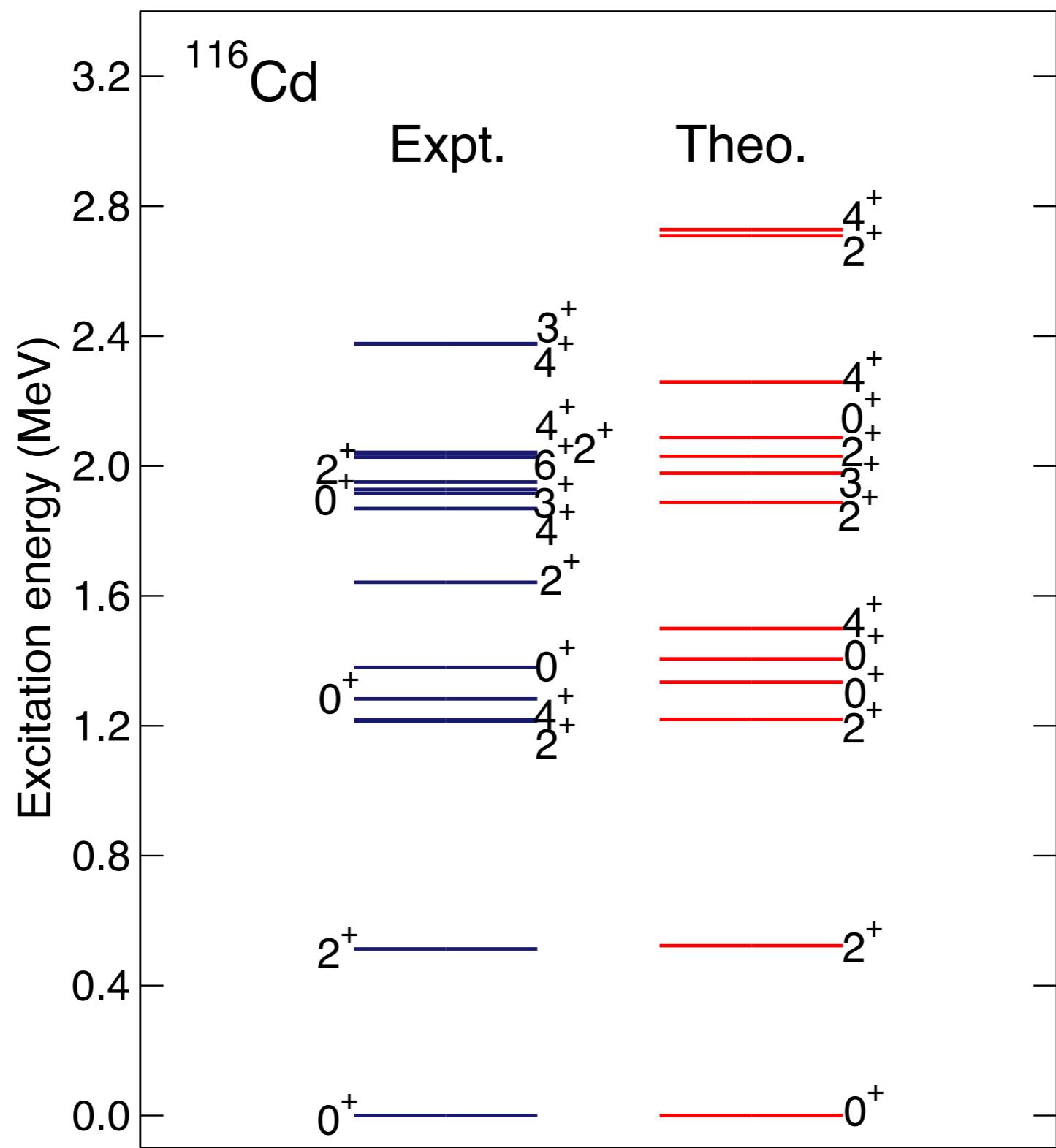


TABLE II: Comparison between experimental and theoretical $B(E2; J_i^+ \rightarrow J_f^+)$ values in Weisskopf units.

J_i^+	J_f^+	^{108}Cd		^{110}Cd		^{112}Cd		^{114}Cd		^{116}Cd	
		Expt	Theo	Expt	Theo	Expt	Theo	Expt	Theo	Expt	Theo
2 ₁	0 ₁	26.6(3)	29	27.0(8)	33	30.3(2)	39	31.1(19)	46	33.5(12)	36
0 ₂	2 ₁	-	1.4	<40	2.8	51(14)	4.5	27.4(17)	2.9	0.79(22)	9.5
2 ₂	0 ₁	1.8(3)	1.1	0.68(14)	1.7	0.65(11)	2.4	0.48(6)	3.2	1.11(18)	1.9
2 ₂	2 ₁	17(5)	6	19(4) or 30(5)	11	39(7)	18	22(6)	21	25(10)	27
2 ₂	0 ₂	-	1.7	1.35(20)	1.2	-	2.6	3.4(7)	11	-	1.7
4 ₁	2 ₁	41(6)	39	42(9)	47	63(8)	55	62(4)	65	56(14)	51
0 ₃	2 ₁	-	0.003	<7.9	0.10	0.0121(17)	0.82	0.0026(4)	4.4	30(6)	1.6
0 ₃	2 ₂	-	13	<1680	29	99(16)	42	127(16)	39	-	96
2 ₃	0 ₁	-	0.02	0.28(4)	0.051	0.88(17)	0.085	0.33(4)	0.072	1.11(18)	0.25
2 ₃	2 ₁	-	0.02	0.7 ⁺³ ₋₄	0.068	0.12(7)	0.14	<0.045	0.17	6.2 ⁺²² ₋₂₆	0.0083
2 ₃	0 ₂	-	16	29(5)	20	120(50)	25	65(9)	32	-	2.8
2 ₃	2 ₂	-	0.17	<8	0.46	-	0.79	-	0.22	-	7.8
2 ₃	0 ₃	-	0.56	-	0.43	-	0.98	-	1.9	86 ⁺²⁴ ₋₃₀	76
3 ₁	2 ₁	-	1.5	0.85(25)	2.5	1.8(5)	3.3	-	4.2	2.6(7)	2.0
3 ₁	2 ₂	-	30	22.7(69)	38	64(18)	47	-	55	61(17)	39
3 ₁	4 ₁	-	3.9	2.4 ⁺⁹ ₋₈	6.8	25(8)	10	-	12	18(10)	11
3 ₁	2 ₃	-	2.3	<5	1.9	-	1.6	-	1.9	-	3.6
4 ₂	2 ₁	-	0.035	0.14(6)	0.083	0.9(3)	0.14	0.50(5)	0.32	3.0(7)	0.22
4 ₂	2 ₂	-	15	22(10)	23	58(17)	31	32(4)	45	230(130)	44
4 ₂	4 ₁	-	4.8	10.7 ⁺⁴⁹ ₋₄₈	8.6	24(8)	13	17(6)	16	150(90)	18
4 ₂	2 ₃	-	1.4	<0.5	0.98	59(20)	0.79	119(12)	5.9	-	31
6 ₁	4 ₁	-	39	62(18)	49	-	59	119(15)	72	110(46)	58
8 ₁	6 ₁	-	34	80(22)	45	-	58	86(28)	73	-	61

Structures of 0+ and 2+ states

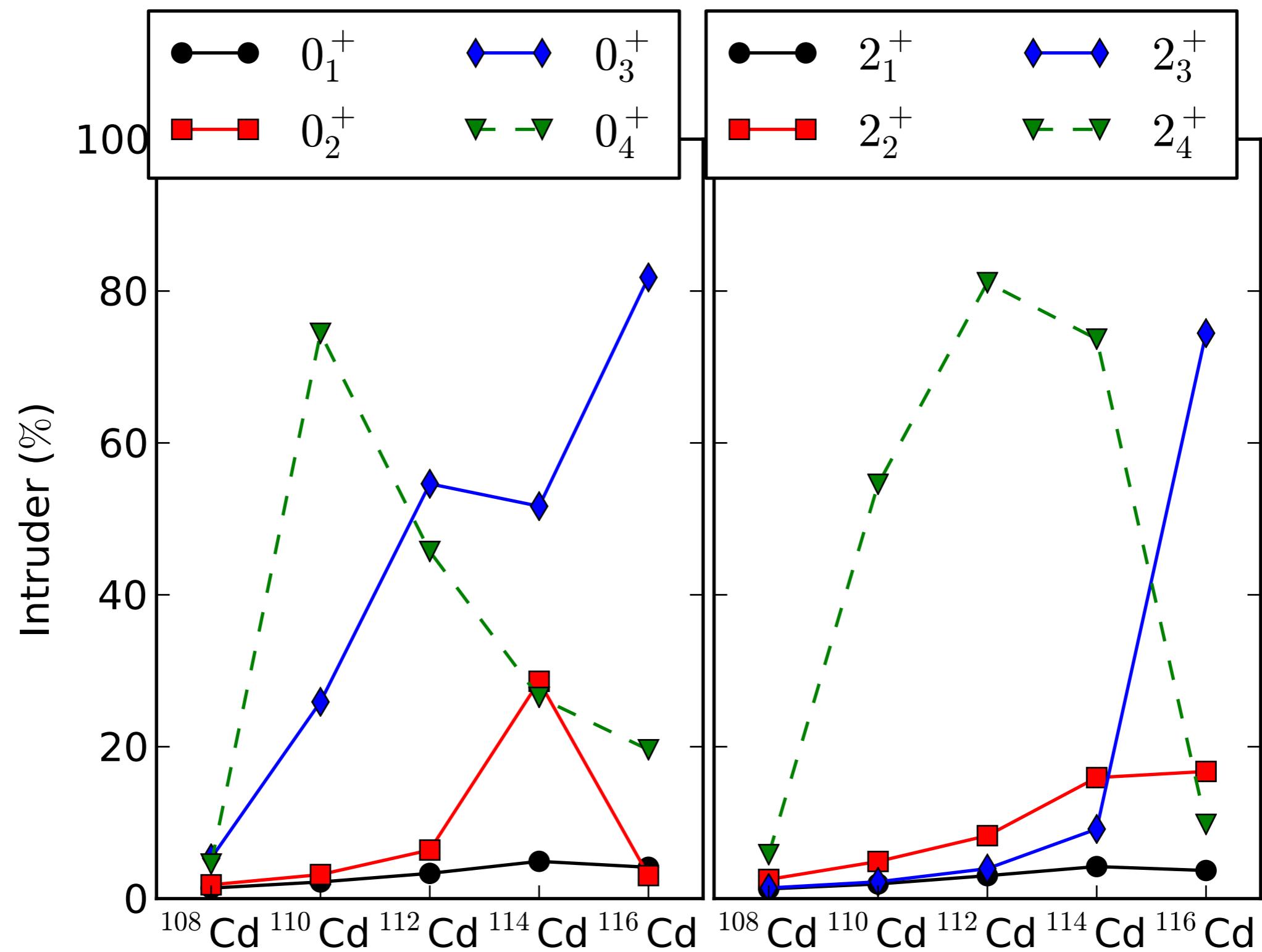


Table IV. Comparison between experimental and theoretical $\rho^2(E0; J_i^+ \rightarrow J_f^+)$ values. The experimental $\rho^2(E0)$ values are not known for ^{108}Cd and ^{116}Cd .

	J_i^+	J_f^+	$\rho^2(E0) \times 10^3$	
			Exp	Theory
^{110}Cd	0 ₂	0 ₁	<31(5) ^a	37
	0 ₃	0 ₁	<11 ^b	1.1
	2 ₂	2 ₁	20(15) ^c	1.1
	2 ₃	2 ₁	9(8) ^a	26
	4 ₃	4 ₁	106 ₋₉₁ ⁺⁹⁸ ^a	0.44
^{112}Cd	0 ₂	0 ₁	34(9) ^d	36
	0 ₃	0 ₁	0.87(5) ^d	8.6
	0 ₃	0 ₂	10.7(6) ^d	12
	2 ₃	2 ₁	31(20) ^c	27
^{114}Cd	0 ₂	0 ₁	19(2) ^d	12
	0 ₃	0 ₁	1.83(13) ^d	44
	0 ₃	0 ₂	0.65(5) ^d	100
	0 ₄	0 ₁	0.9(4) ^d	8.8
	2 ₂	2 ₁	<28 ^c	0.25
	2 ₃	2 ₁	38(5) ^e	22
	2 ₃	2 ₂	22(6) ^e	1.1
	2 ₄	2 ₂	<20 ^e	57
	3 ₂	3 ₁	<130 ^e	35
	4 ₂	4 ₁	67(10) ^e	0.38

Summary

Configuration-mixing IBM based on SCMF

- overall good description of energies and transition rates without empirical fit
- predicts intruder states
- mixing between normal and intruder configs not correctly reproduced
- normal states predicted to be rotational like → too deformed prolate minimum

Thank you

Geometrical Structure

Coherent-state matrix

$$\mathcal{E} = \begin{pmatrix} E_{11}(\beta, \gamma) & E_{13}(\beta, \gamma) \\ E_{31}(\beta, \gamma) & E_{33}(\beta, \gamma) + \Delta \end{pmatrix}$$

$$E_{ii}(\beta, \gamma) = \langle \phi_i | \hat{H}_i | \phi_i \rangle$$

$$E_{ij}(\beta, \gamma) = E_{ji}(\beta, \gamma) = \langle \phi_j | \hat{H}_{\text{mix}} | \phi_i \rangle$$

Boson coherent state

$$|\phi_i\rangle = \Pi_{\rho=\nu,\pi} (s_\rho^\dagger + \beta_\rho \cos \gamma d_{\rho 0}^\dagger + \frac{1}{\sqrt{2}} \sin \gamma (d_{\rho 2}^\dagger + d_{\rho -2}^\dagger)^{N_\rho}) |\text{o}\rangle$$

IBM energy surface → lower eigenvalue of the matrix

Construct config-mix IBM Hamiltonian

1. associate unperturbed $0p-0h$ config (E_{11}) to prolate global minimum and $2p-2h$ config (E_{33}) to oblate local “minimum”
→ parameters for unperturbed IBM Hamiltonians
2. reproduce energy difference between the minima
→ Δ
3. mixing term introduced perturbatively to reproduce “barrier”
→ ω