



# Laser spectroscopy of neutron-deficient Hg

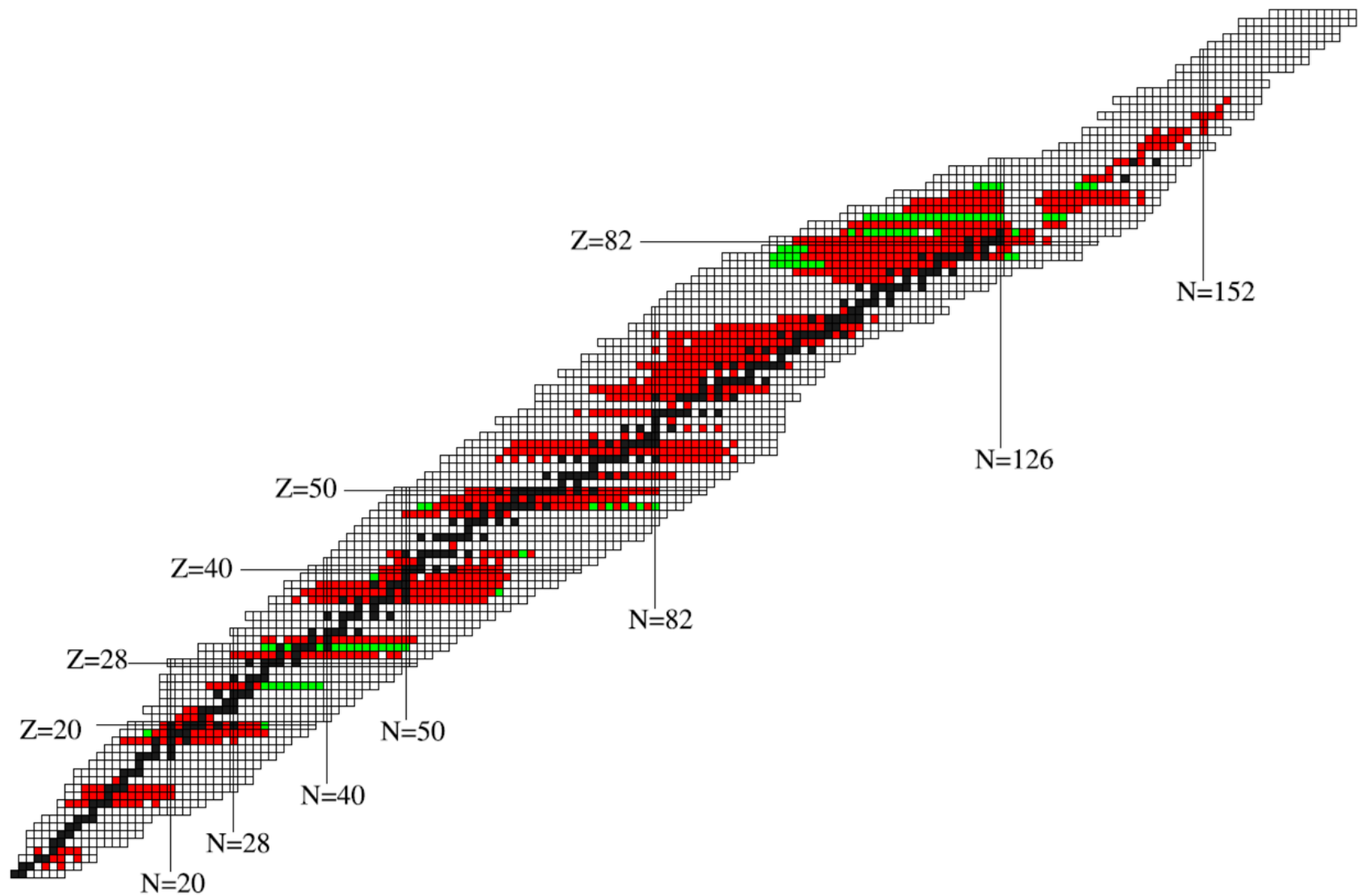
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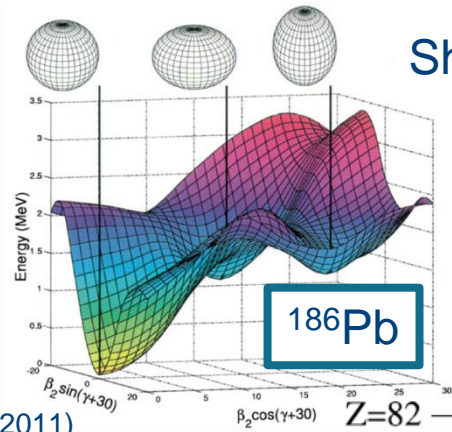


# Outline

- Introduction
- Experiment
- Results
- Comparison to theory
- Conclusions and outlook



# Shape coexistence

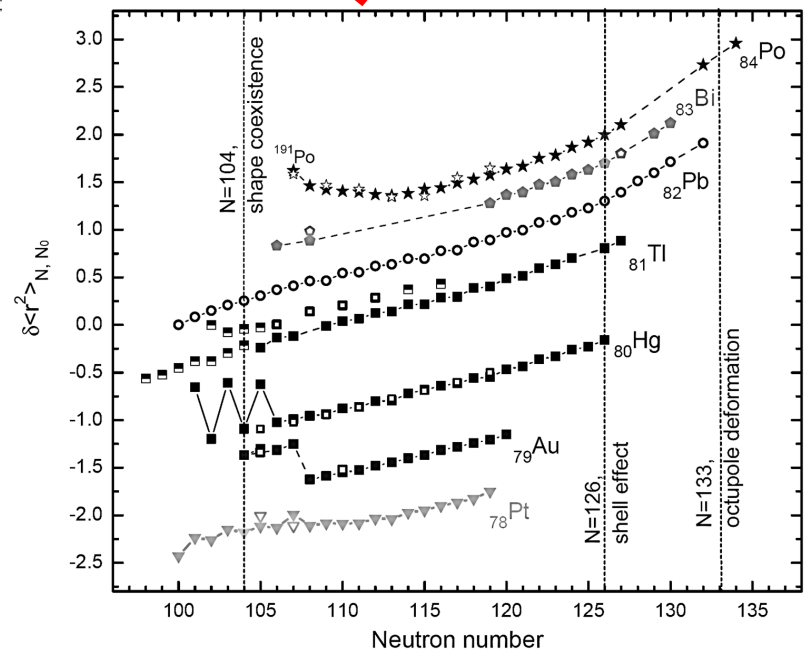
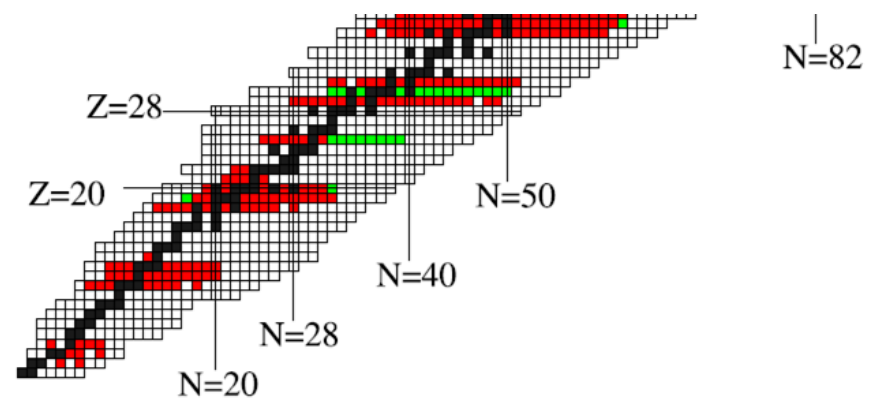
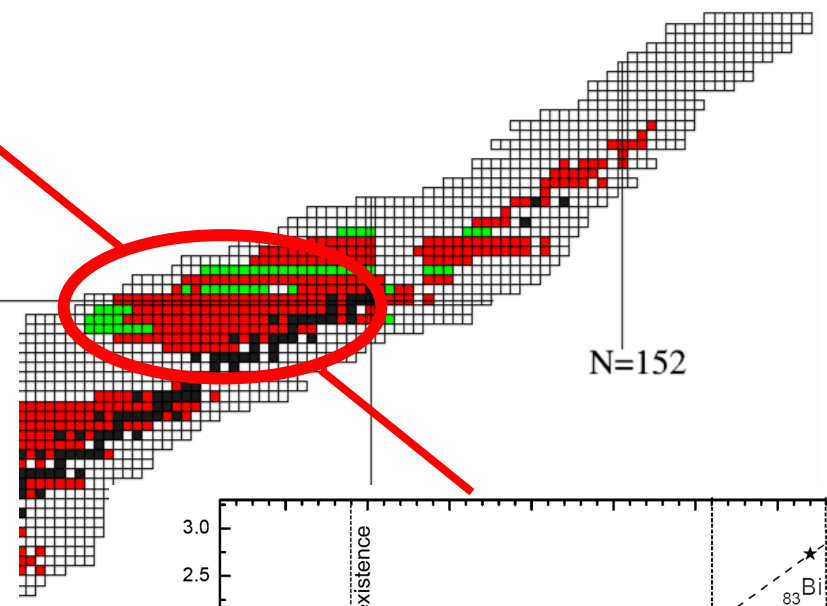


Heyde and Wood, Rev Mod Phys (2011)

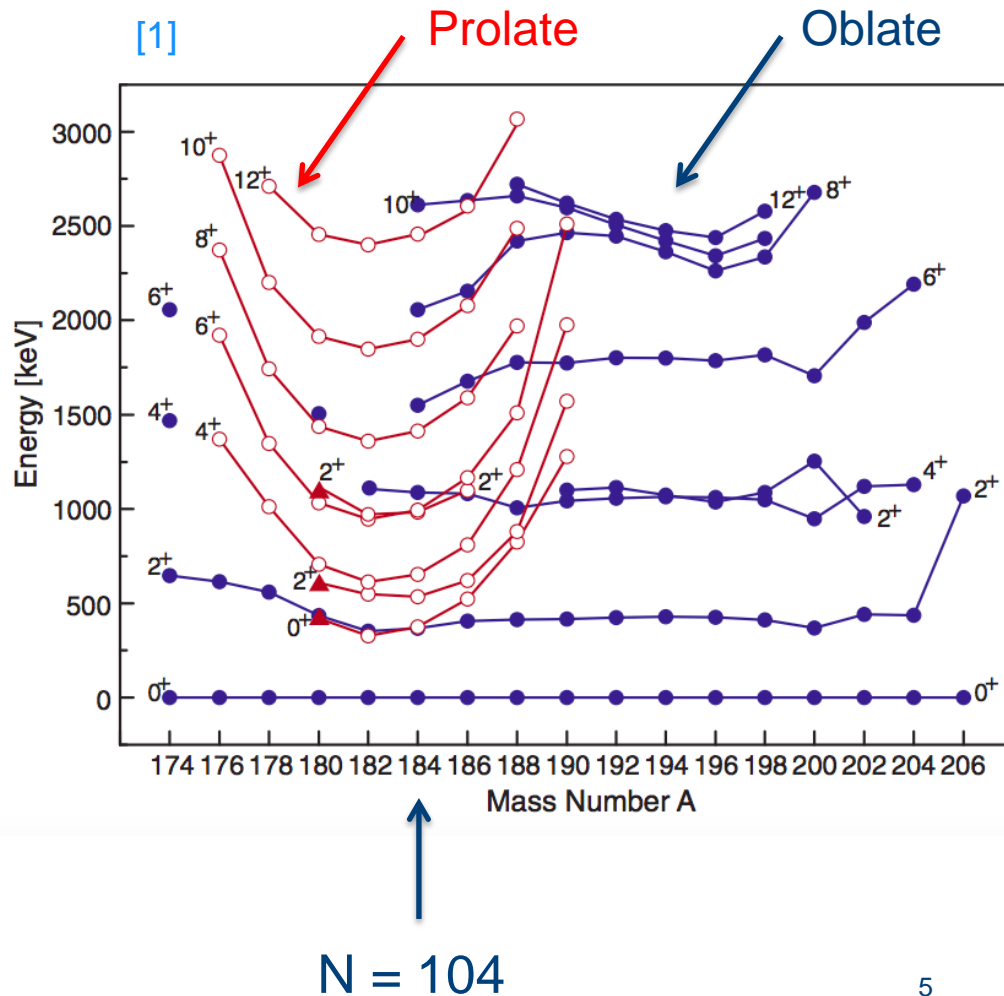
Different types of shape/deformation at low excitation energy

Interplay between:

- Stabilizing effect of closed shells
- Residual proton-neutron interaction



# Level systematics in even-even Hg



Coexistence of different bands in Hg isotopes

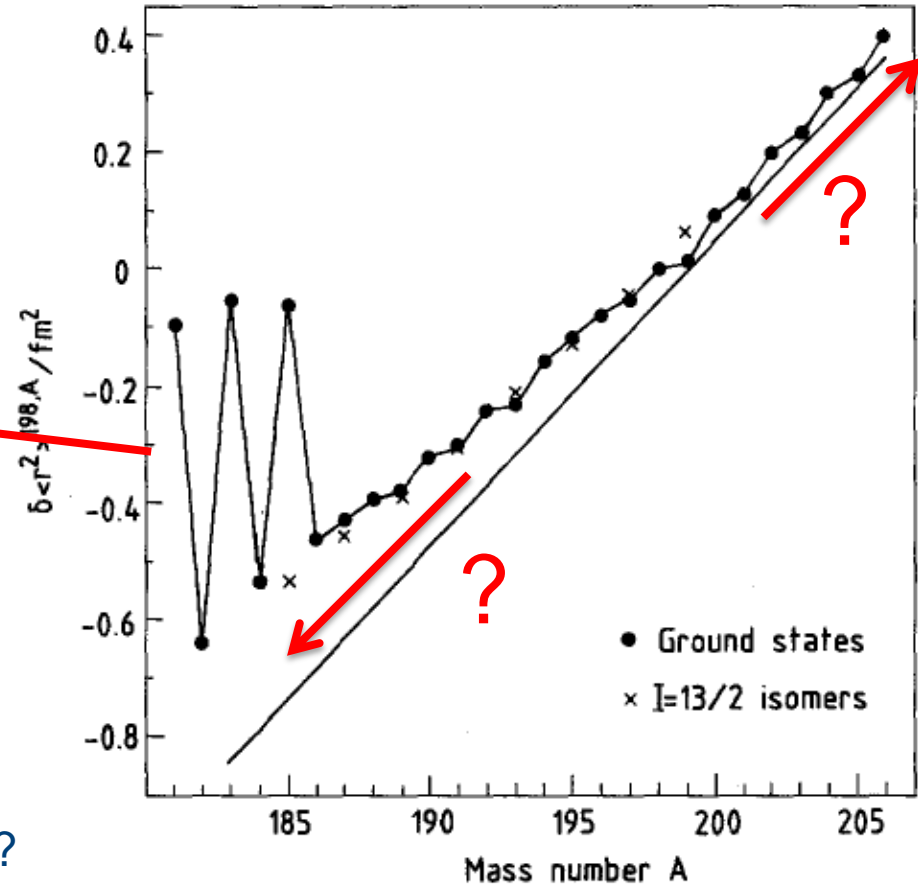
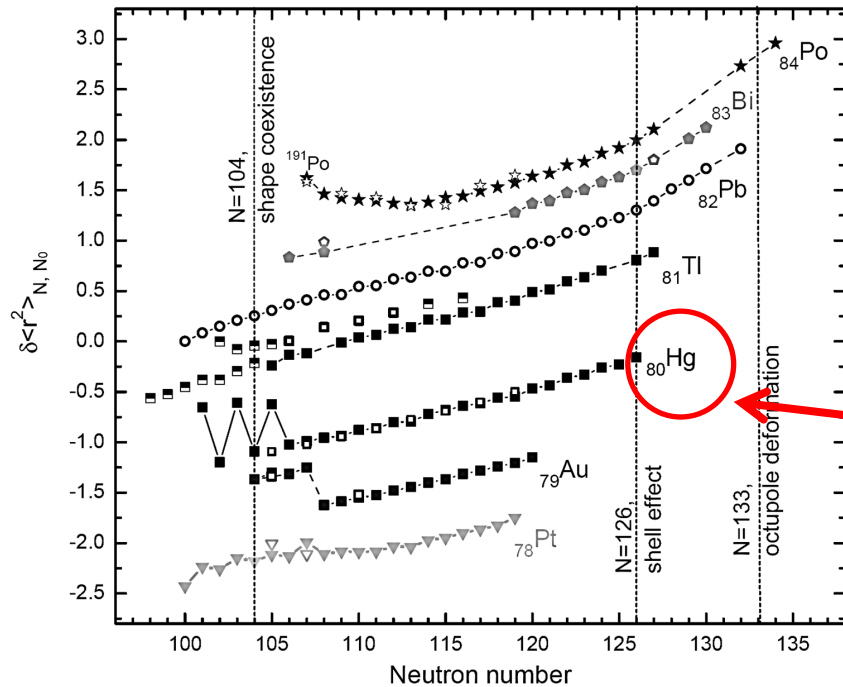
**Prolate intruder** states comes down in energy towards minimum around  $N=104$  midshell region

Studied by multitude of techniques

- Coulex (cfr. Talk K. Wrzosek-Lipska)
- Gamma spec.
- Decay spec.
- ....

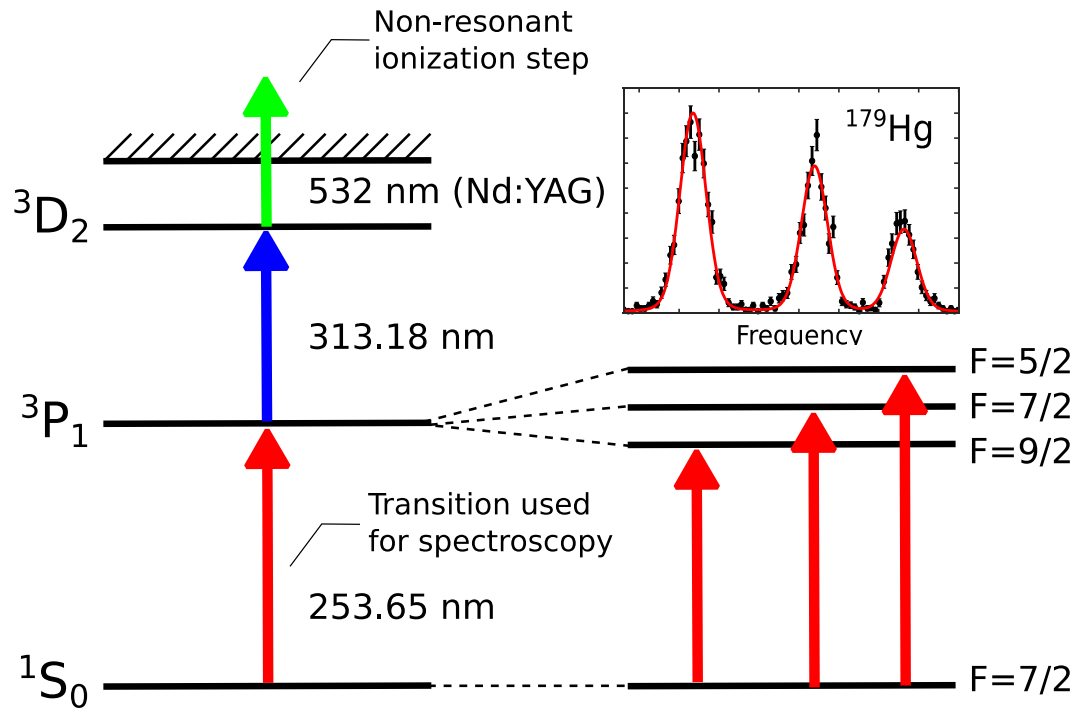
But direct measurement of ground-state charge radii differences and electromagnetic moments missing below  $N=101$

# Charge radii differences



- Where does the shape staggering end?
  - > Excellent tool to test precision of theoretical models
- Kink at  $N=126$  like  $\text{Pb}, \text{Bi}, \text{Po}$  ?

# Laser spectroscopy



Isotope shift,  
hyperfine parameters



$$d\langle r^2 \rangle^{A,A'} \quad I, m, Q,$$

# Laser spectroscopy variables

Measured:

Isotope / Isomer shifts

Hyperfine splitting

Deduced observ.:  
(model indep.)

Sizes

Quadrupole Mom.

Dipole Mom.

Spins

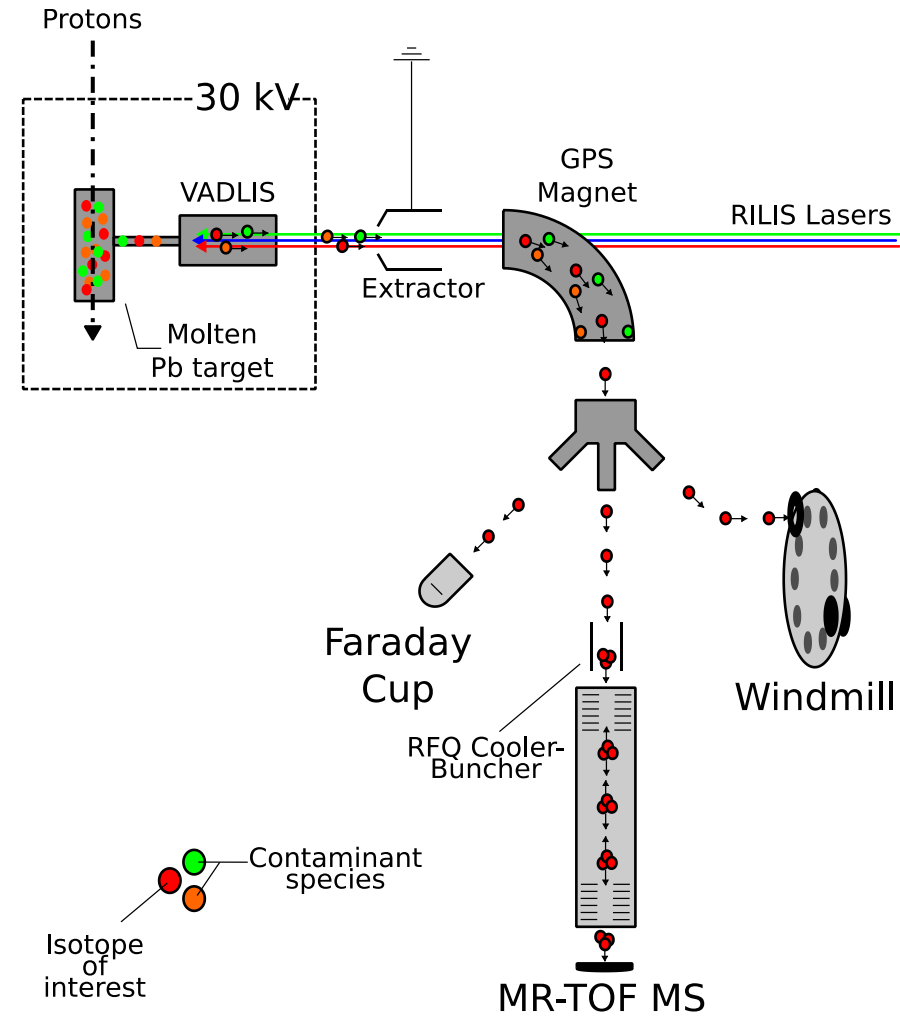
Information:

Shapes/deform. parameters

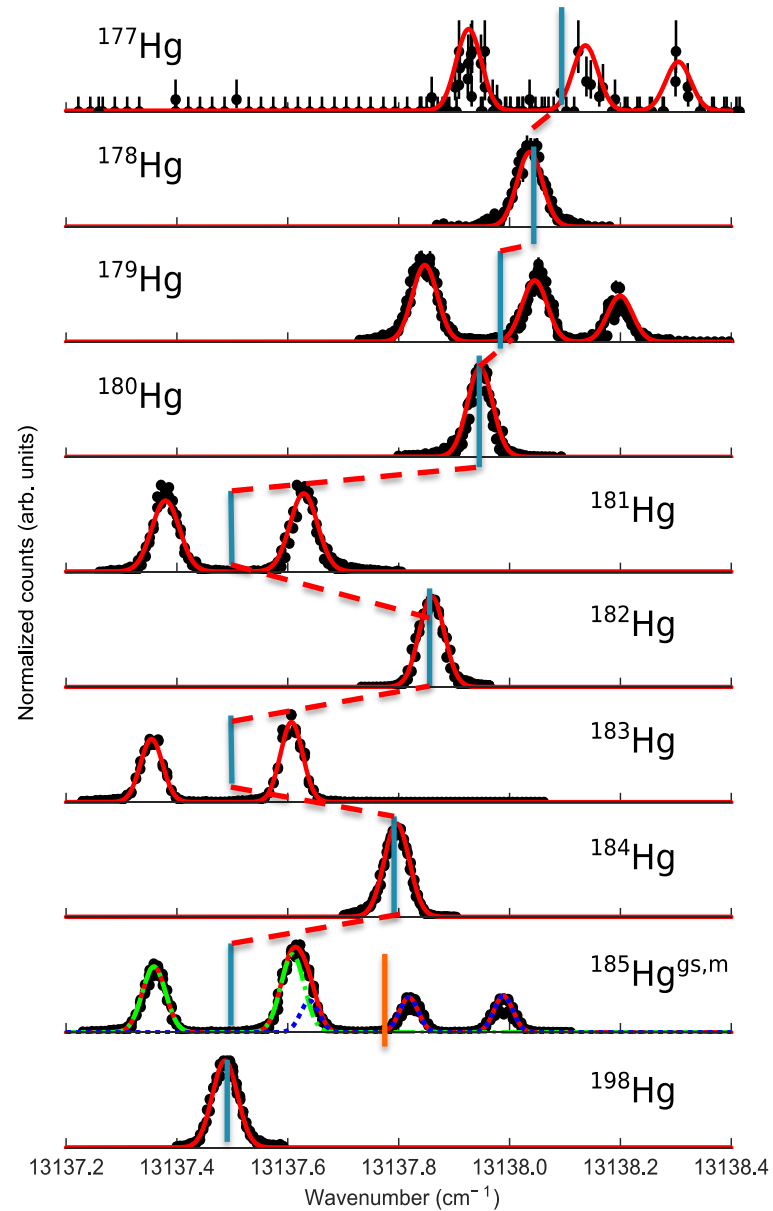
Single particle configurations



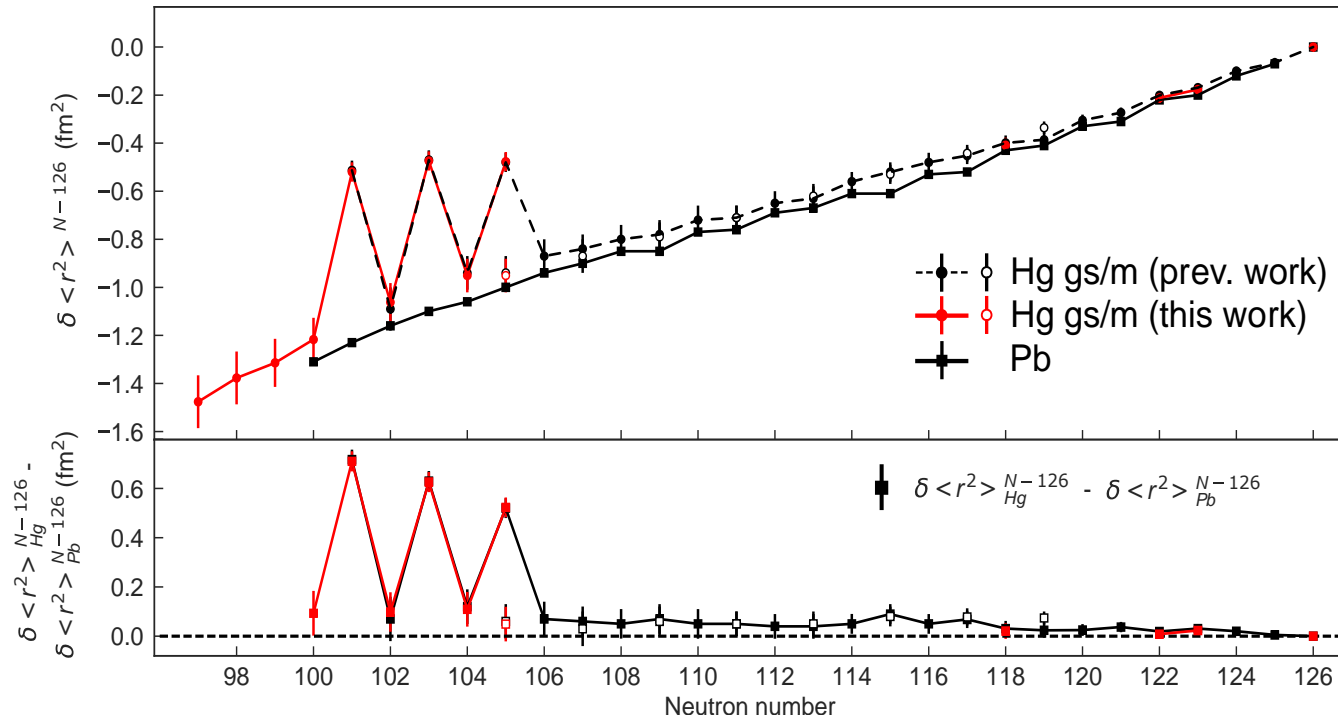
# ISOLDE - CERN



# Hyperfine spectra



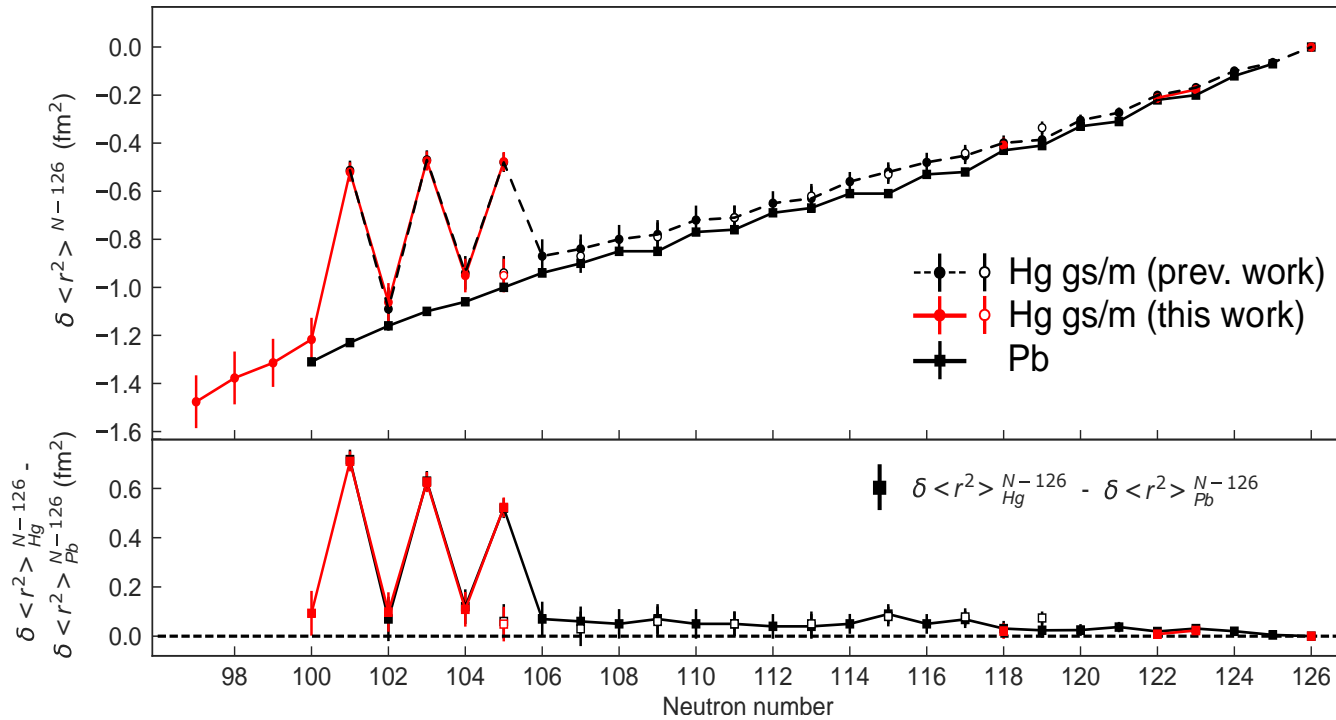
# results



## Charge radii results

- End point of shape staggering observed
- kink at N=126 present as well
- Agreement with previously measured values

# results



Isotope	Spin $I^\pi$	$\mu$ ( $\mu_N$ )	$Q_s$ (b)
$^{177}\text{Hg}$	$(7/2^-)$	-1.025(40)	0.57(83)
	$(9/2^-)$	-1.056(40)	1.21(91)
$^{179}\text{Hg}$	$(7/2^-)$	-0.948(20)	0.76(28)
	$(9/2^-)$	-0.960(20)	1.45(31)
$^{181}\text{Hg}$	$1/2^-$	0.515(4)	-
		0.513(9)	-
$^{183}\text{Hg}$	$1/2^-$	0.521(6)	-
		0.527(1)	-
$^{185}\text{Hg}$	$1/2^-$	0.51(1)	-
		0.513(2)	-
$^{185m}\text{Hg}$	$13/2^+$	-1.01(1) -1.017(9)	-0.15(41) 0.19(32)

moments :

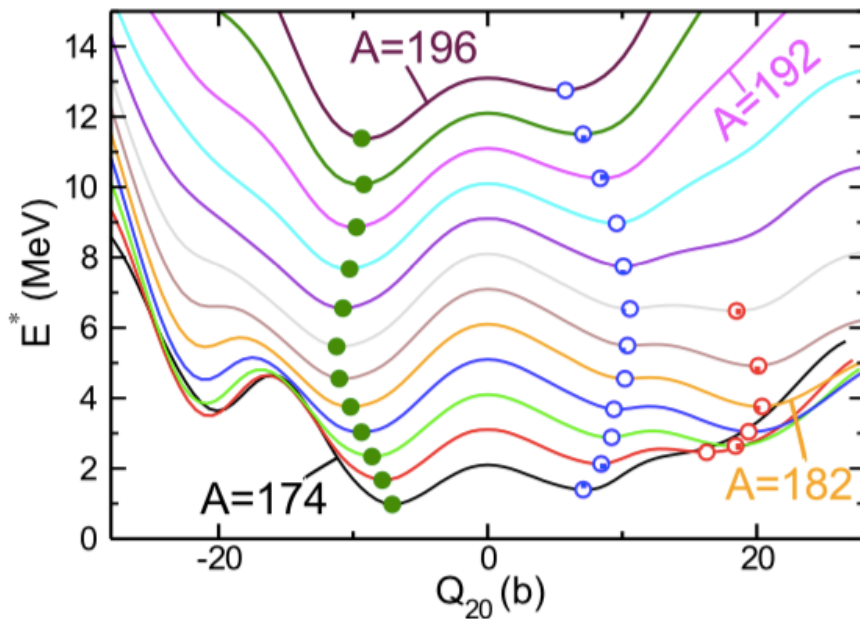
magn  $177\text{-}179\text{-}185\text{m Hg} : \approx -1$

$181\text{-}183\text{-}185 \text{ Hg} : \approx +0.5$

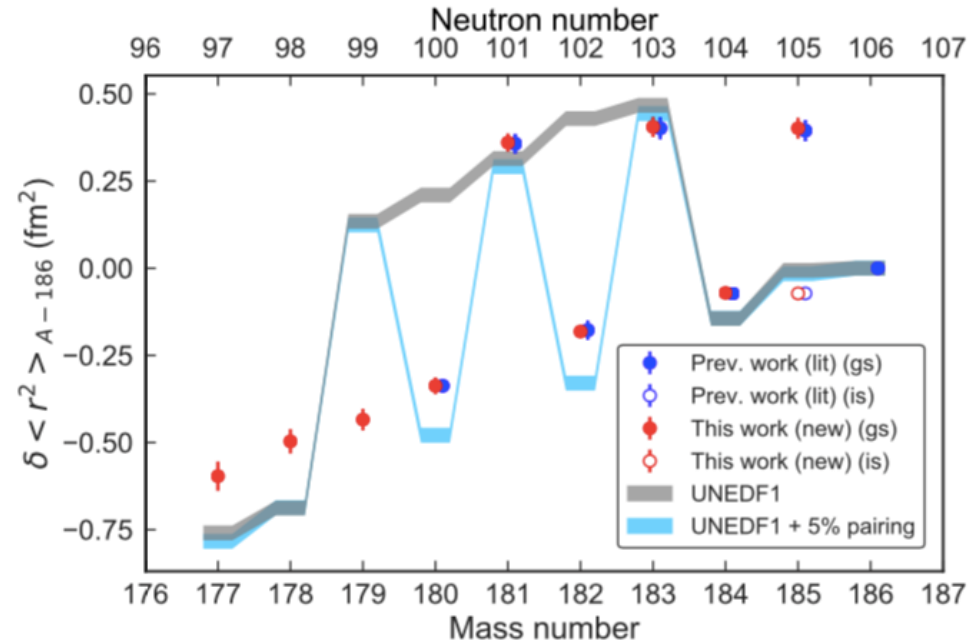
quad  $177\text{-}179\text{-}185\text{m Hg} : \text{small}$

# Shape staggering comparison to DFT

Potential Energy surface



Charge radii



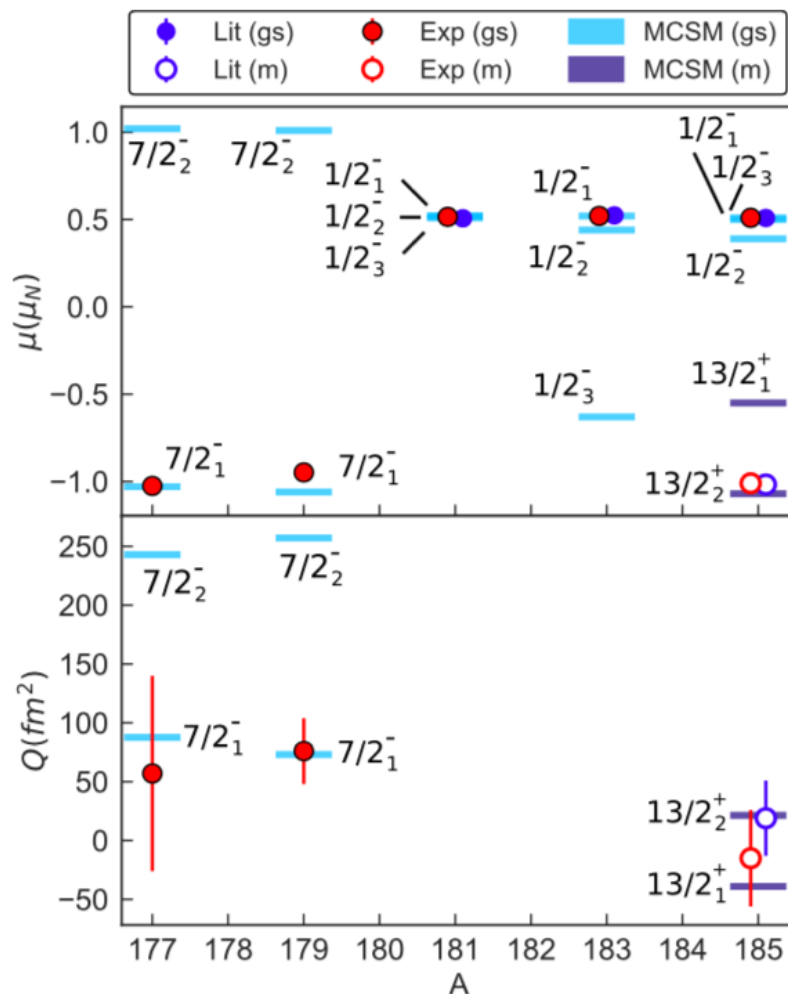
Skyrme functional UNEDF1so [1]

→ Adjusted to global properties of nuclear chart

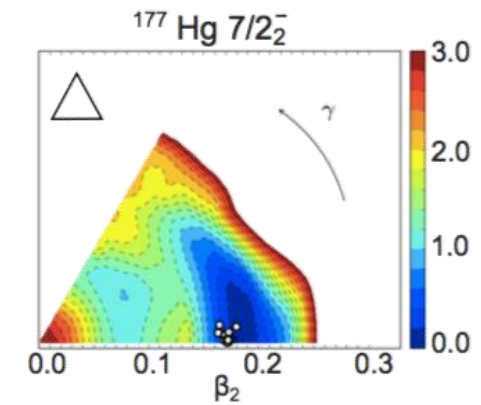
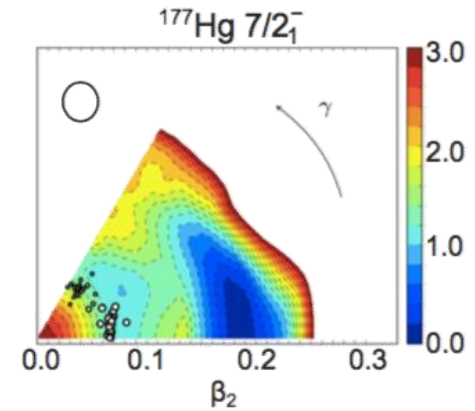
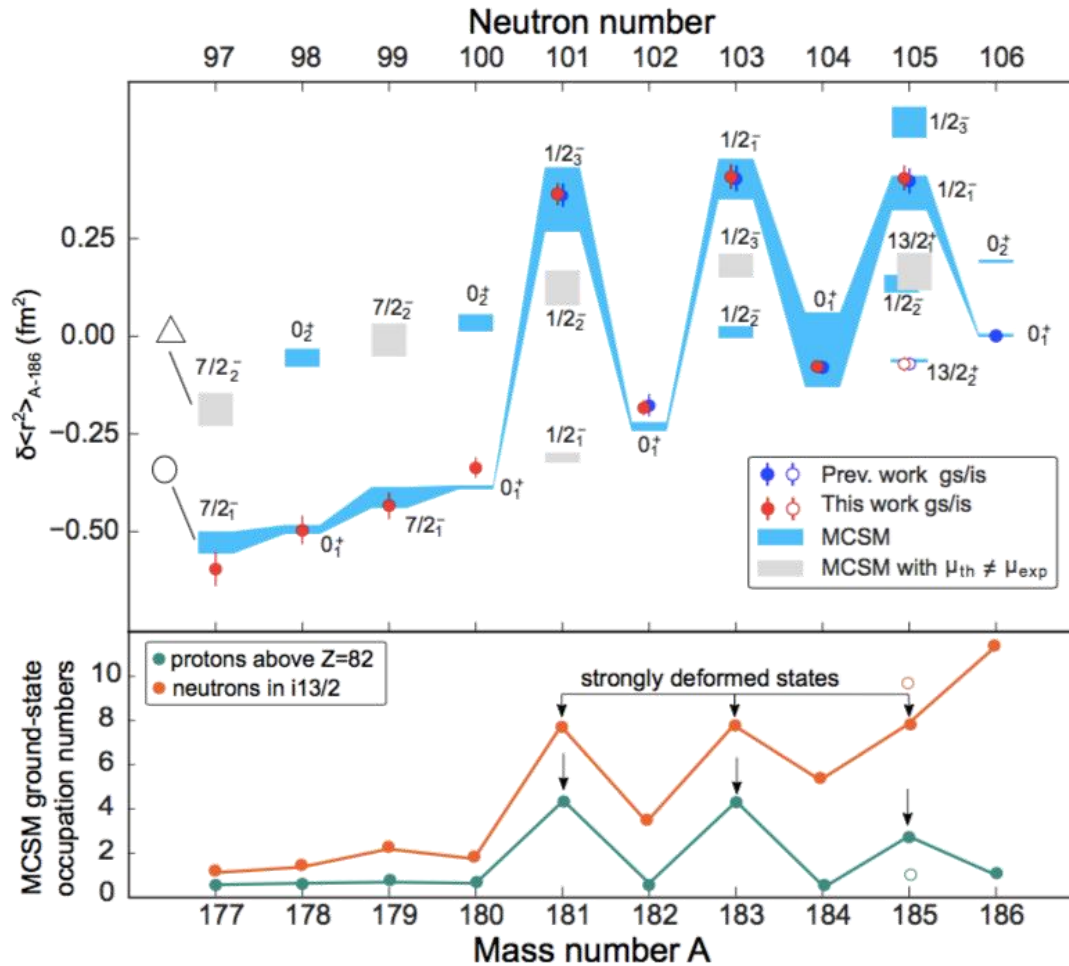
→ Fine tuned SO and pairing to reproduce No spectroscopy

# Electromagnetic moments

## Comparison to MCSM

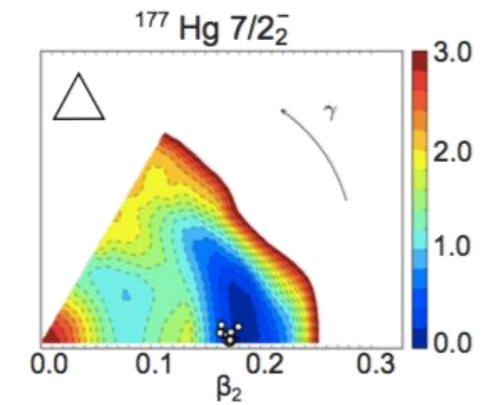
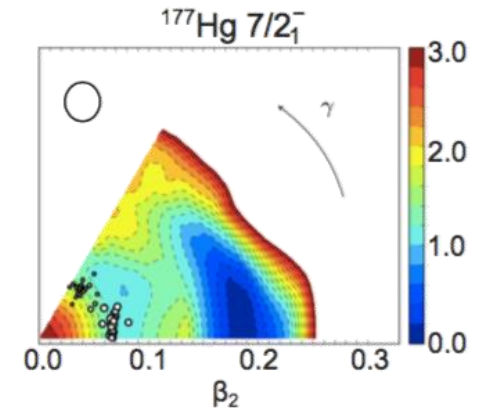
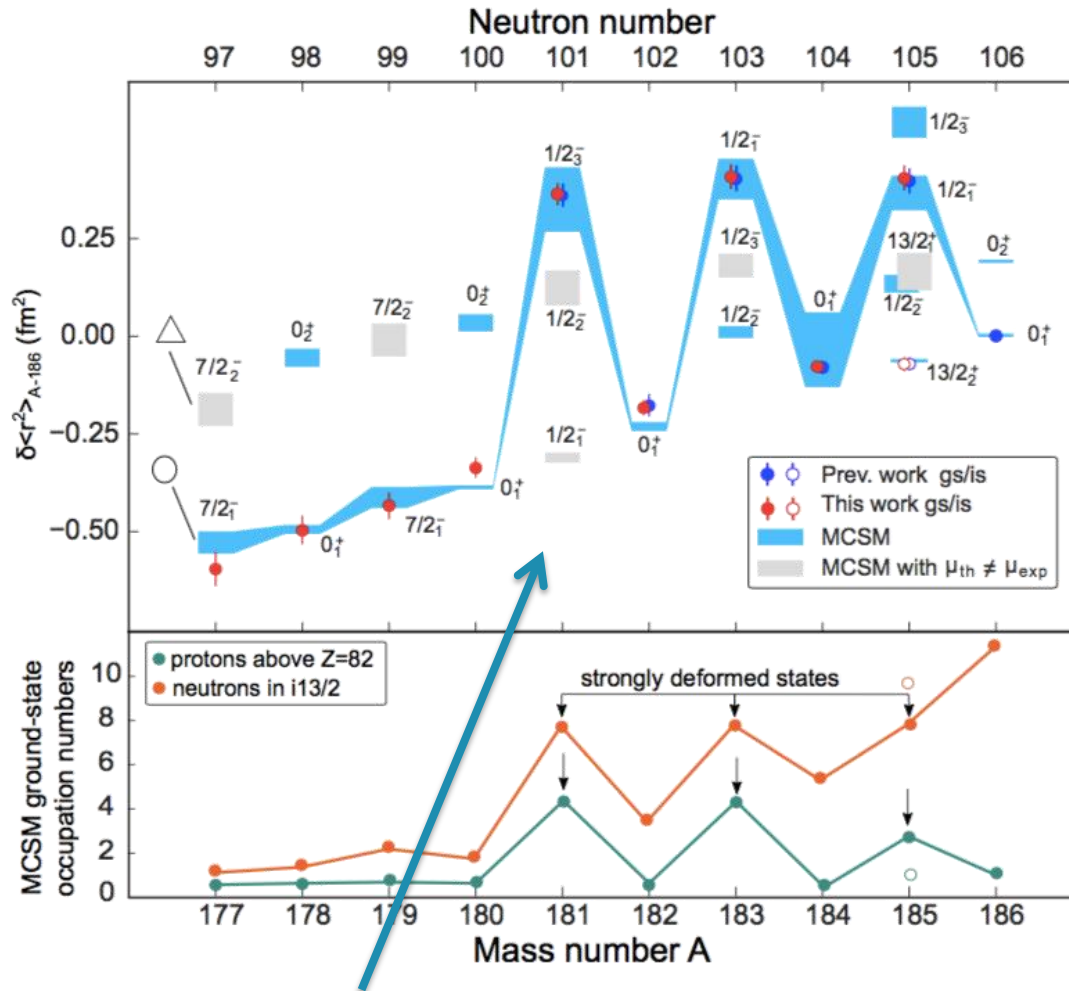


# Shape staggering comparison to MCSM



**$^{132}\text{Sn}$  as fixed core**  
 $\rightarrow$  30 protons and 17-24 neutrons  
 all interacting  $NN, PP$  [1]  $PN$  [2],  
 First for such a heavy system

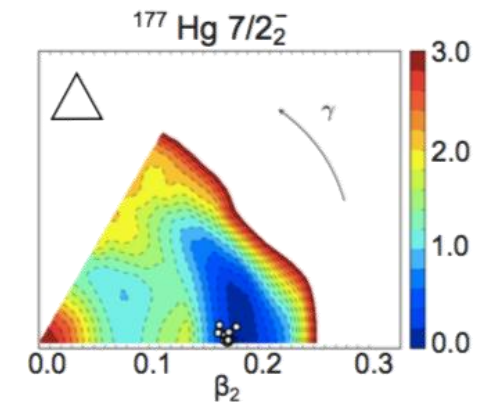
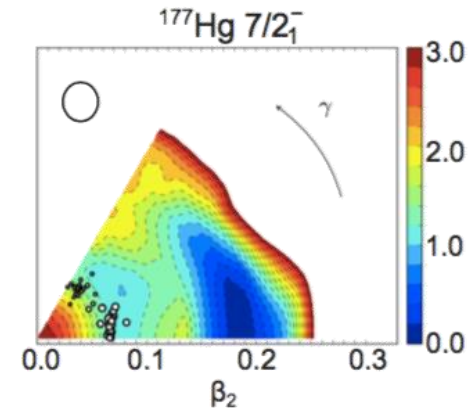
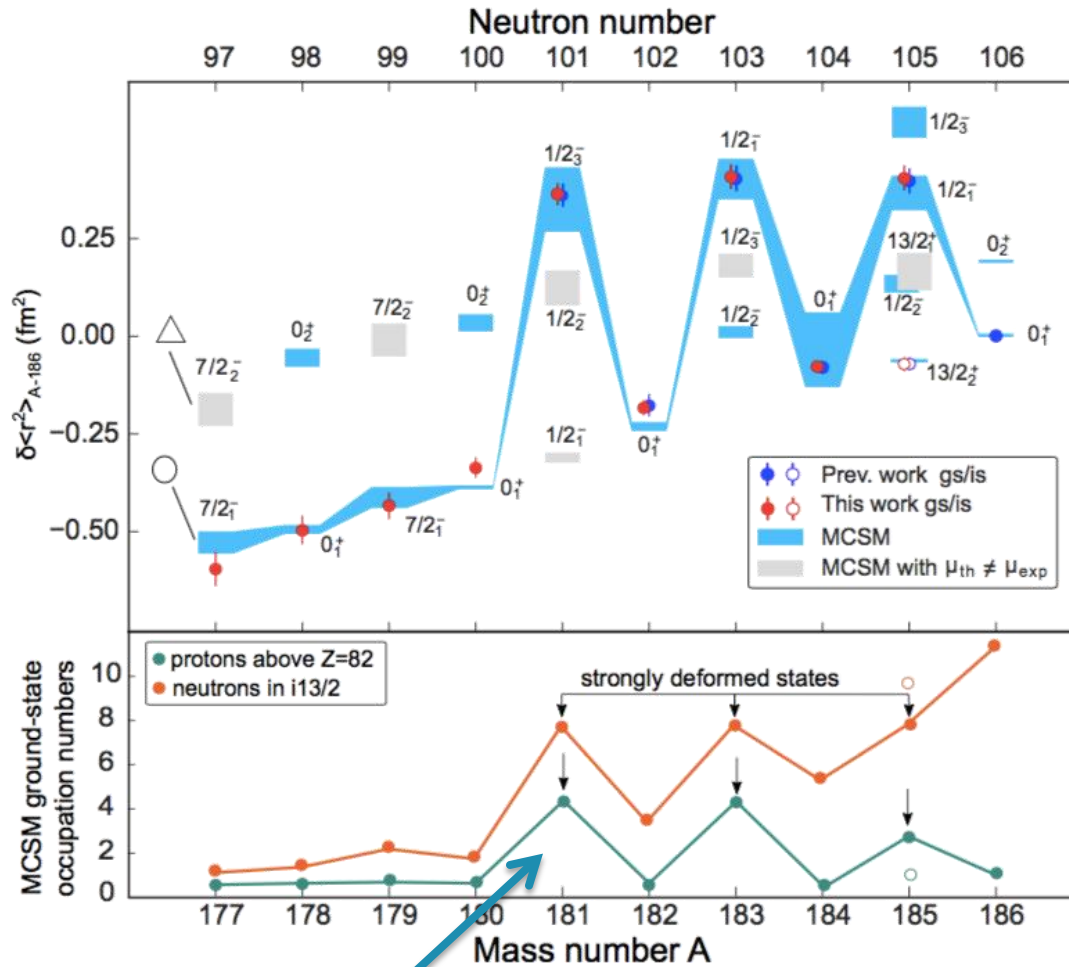
# Shape staggering comparison to theory



Charge radii differences, staggering strength and location well reproduced!  
 In all but  $^{181}\text{Hg}$  and  $^{185m}\text{Hg}$ , state with correct  $d\langle r^2 \rangle = \text{g.s.}$

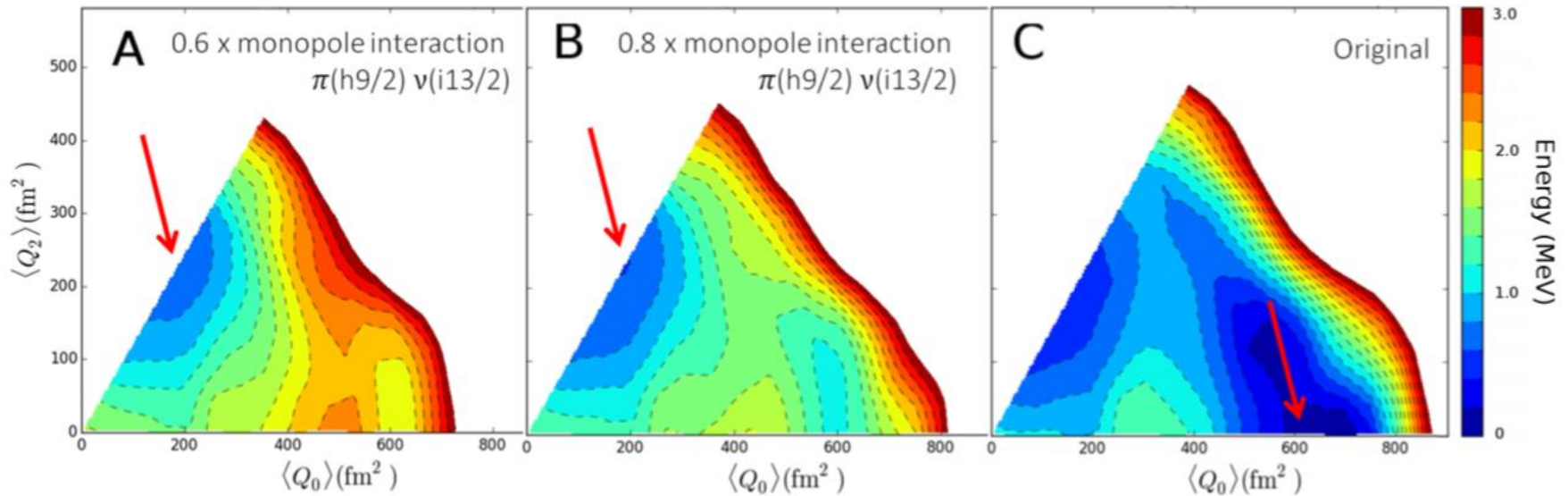


# Shape staggering comparison to theory



Particular occupation numbers of  $n(i_{13/2})$  and  $p(h_{9/2})$  important

# Effect of reducing monopole interaction



# Shape staggering mechanism

Combined action of monopole energy, which stands out compared to others between  $n(i_{13/2})$  and  $p(h_{9/2})$  and due to:

- Large radial overlap of wavefunctions
- Attractive tensor force between  $j_> - j_<'$

$$E_{\text{mon}} = f(j_p, j_n) n_\pi(j_p) n_\nu(j_n)$$

And quadrupole interaction, bringing down the *deformed* state in energy to near-degeneracy with *spherical* state

Cfr. Similar to Type II shell evolution where SPE's are adjusted due to occupation numbers of  $p$  and  $n$  orbitals

Small addition in pairing energy between even/odd-A isotopes dictates the ground state shape

# Conclusion

Experiment: Hg laser spectroscopy at ISOLDE

- \* Determined end-point of shape staggering
- \* Measured electromagnetic moments

Comparison to theory:

- \* DFT – interplay of shape coexistence, pairing and blocking

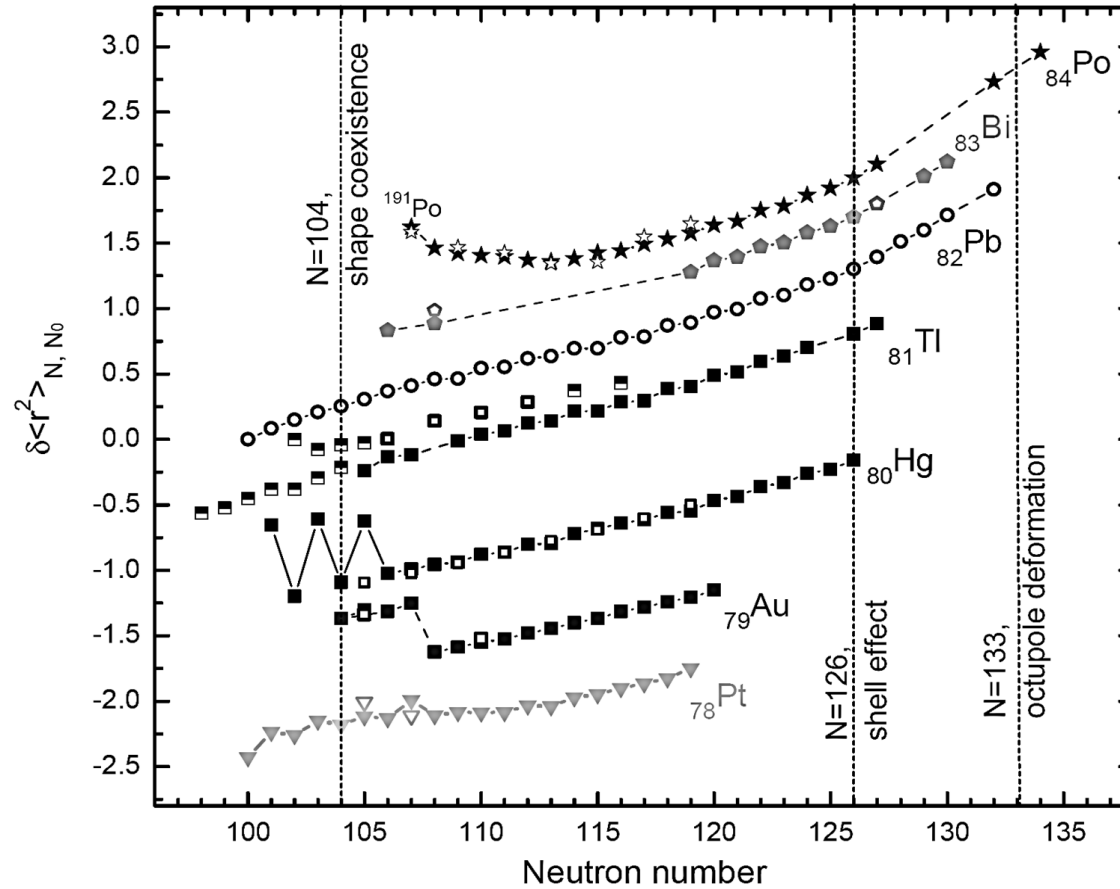
- \* MCSM:

- $n(i_{13/2}) p(h_{9/2})$  interaction responsible
- Related to Type II shell evolution

*Outlook..*

Extending to different measurements and observables

# Outlook



# Thank you for your attention

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