

# Signature of the $\gamma$ -softness in nuclei at the Se-Ge region

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# In this study;

- Focus on the  $\gamma$ -band of some nuclei in the Se-Ge region.
- These nuclei;
  - $^{74}\text{Se}$ ,  $^{76}\text{Se}$ ,  $^{78}\text{Se}$  isotopes and
  - $^{66}\text{Ge}$ ,  $^{68}\text{Ge}$  isotopes
- Their gamma bands show a typical band structure of the  $\gamma$ -softness.
- The experimental levels in  $\gamma$ -band have
  - the odd–even couplings
  - like (2+), (3+, 4+), (5+, 6+), (7+, 8+), ....

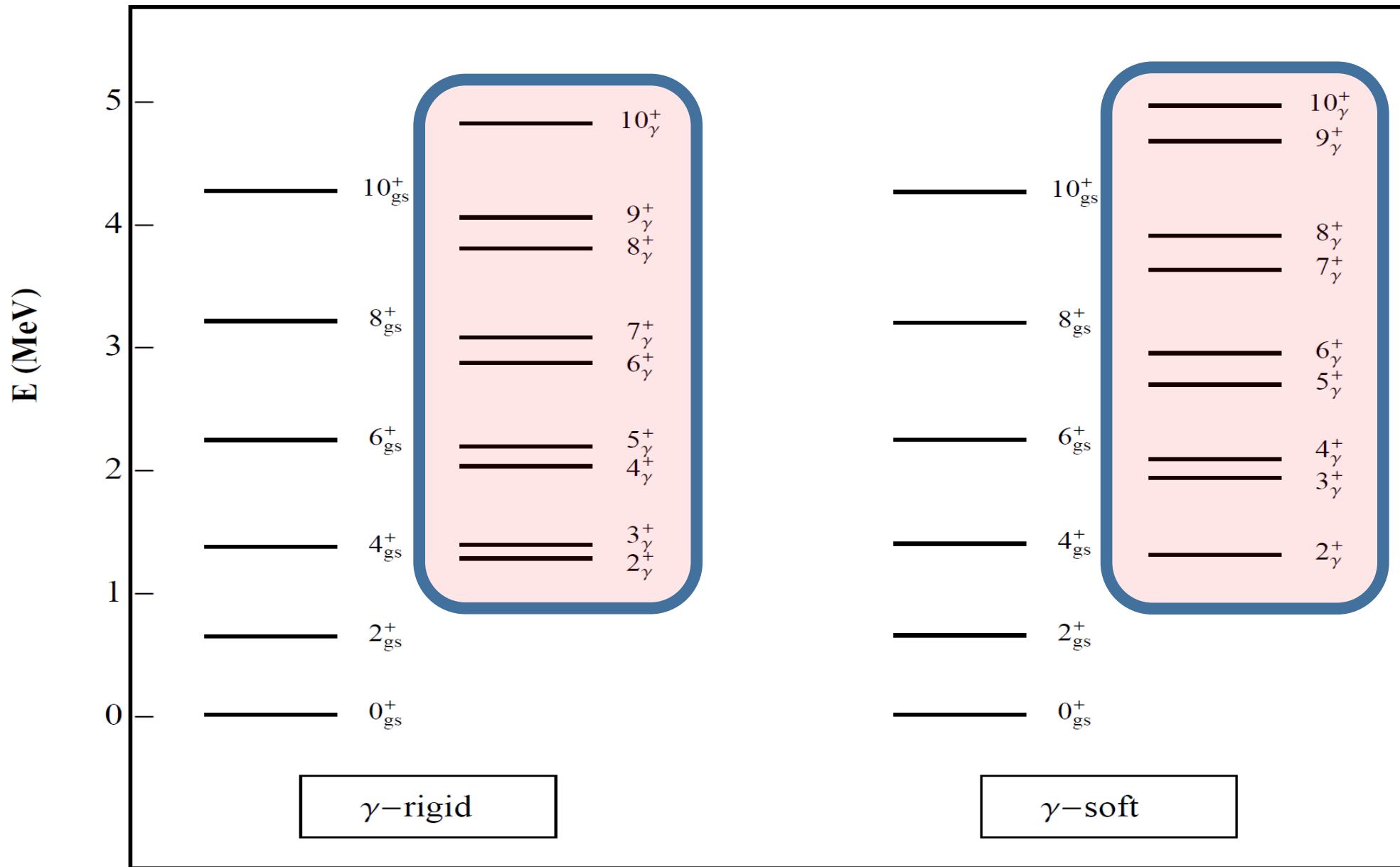
# In this study;

- Detail analyzing of  $\gamma$ -band levels for given isotopes.  
... with interacting boson model-1 (ibm-1);  
energy levels were calculated and compared experimental data
- The signature splitting  $S(J)$  observed in the  $\gamma$ -band.

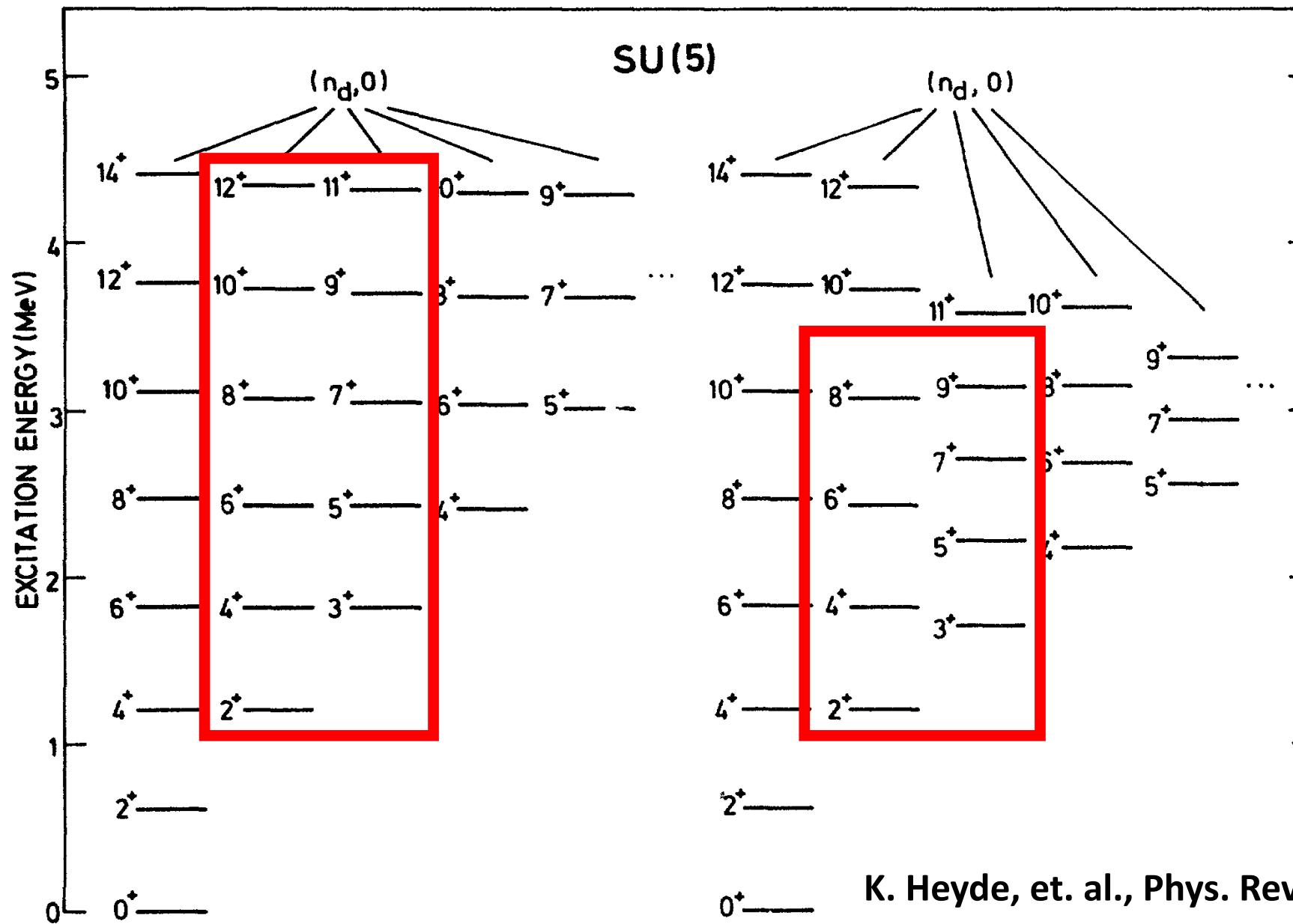
$$S(J) = \frac{E(J) - E(J-1)}{E(J) - E(J-2)} \cdot \frac{J(J+1) - (J-1)(J-2)}{J(J+1) - J(J-1)} - 1$$

N. V. Zamfir, R. F. Casten, Phy. Lett. B 260 (1991) 265.  
I. Stefanescu, A. Gelbergb, J. Jolie, P. Van Isacker, P. Von Brentano, et. Al., Nucl. Phys. A 789 (2007) 125.  
B. Sorgunlu, P. Van Isacker, Nucl. Phy. A 808 (2008) 27.

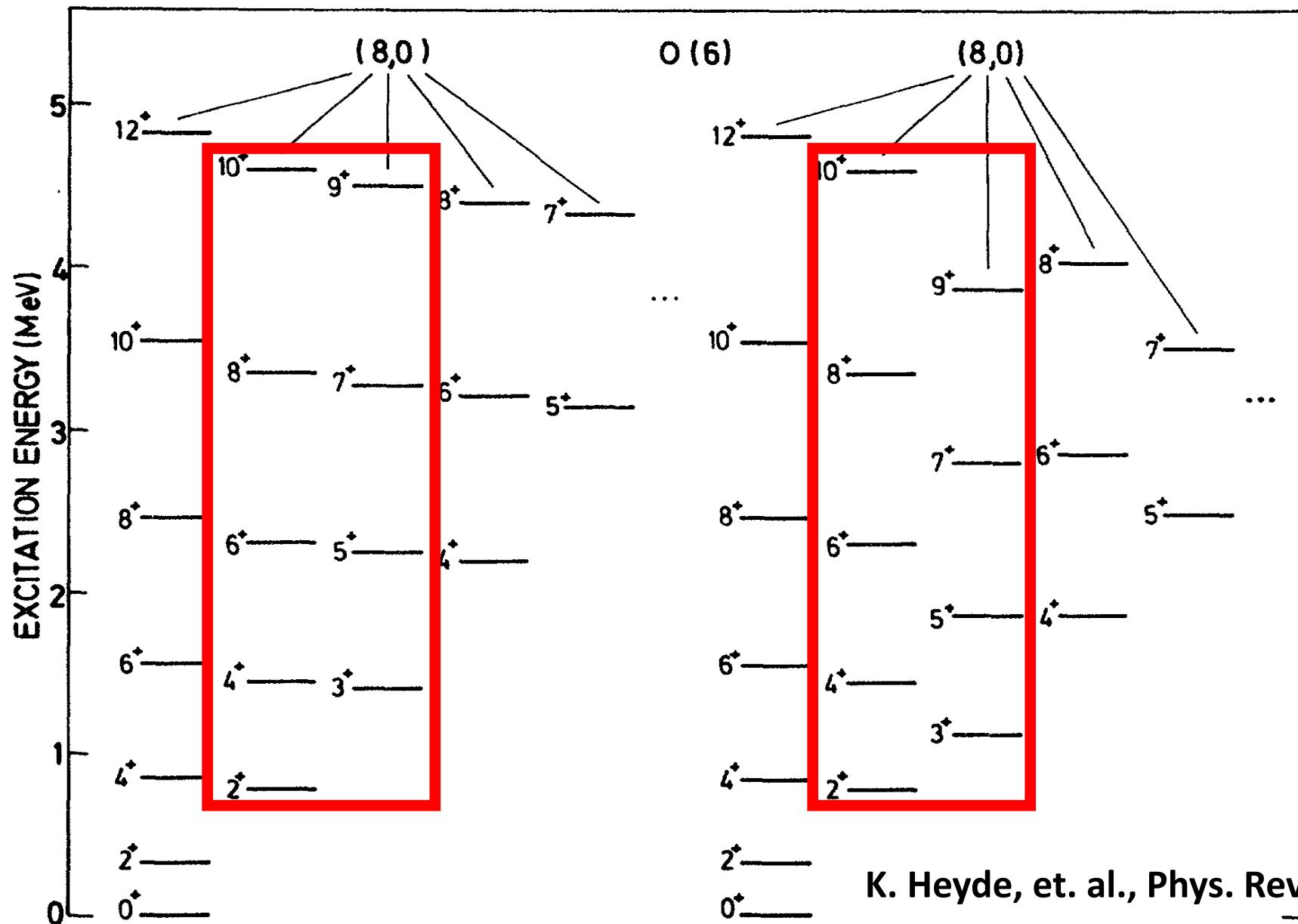
# $\gamma$ -rigid & $\gamma$ -soft



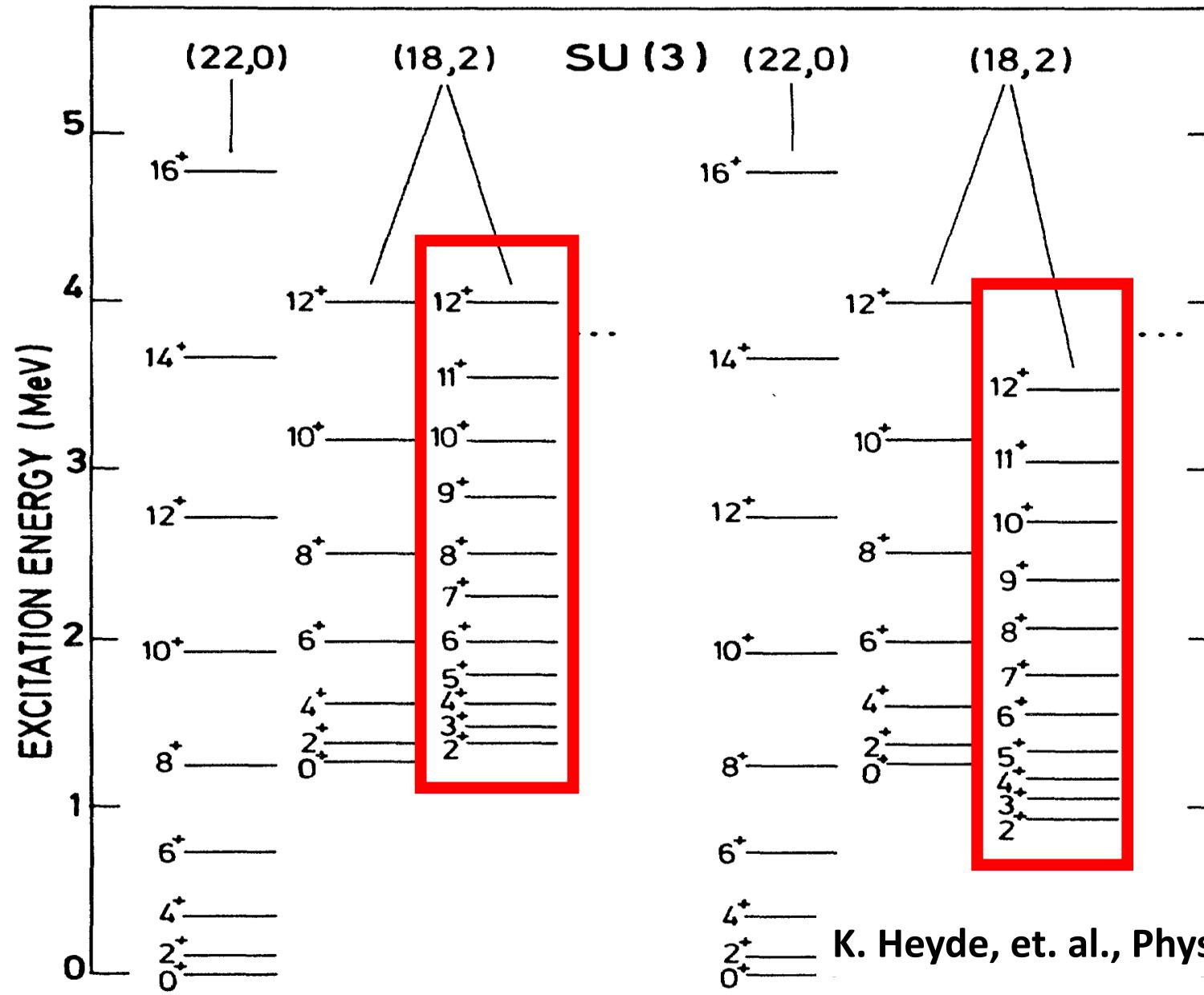
# The effect of triaxial term in IBM-1 for $U(5)$



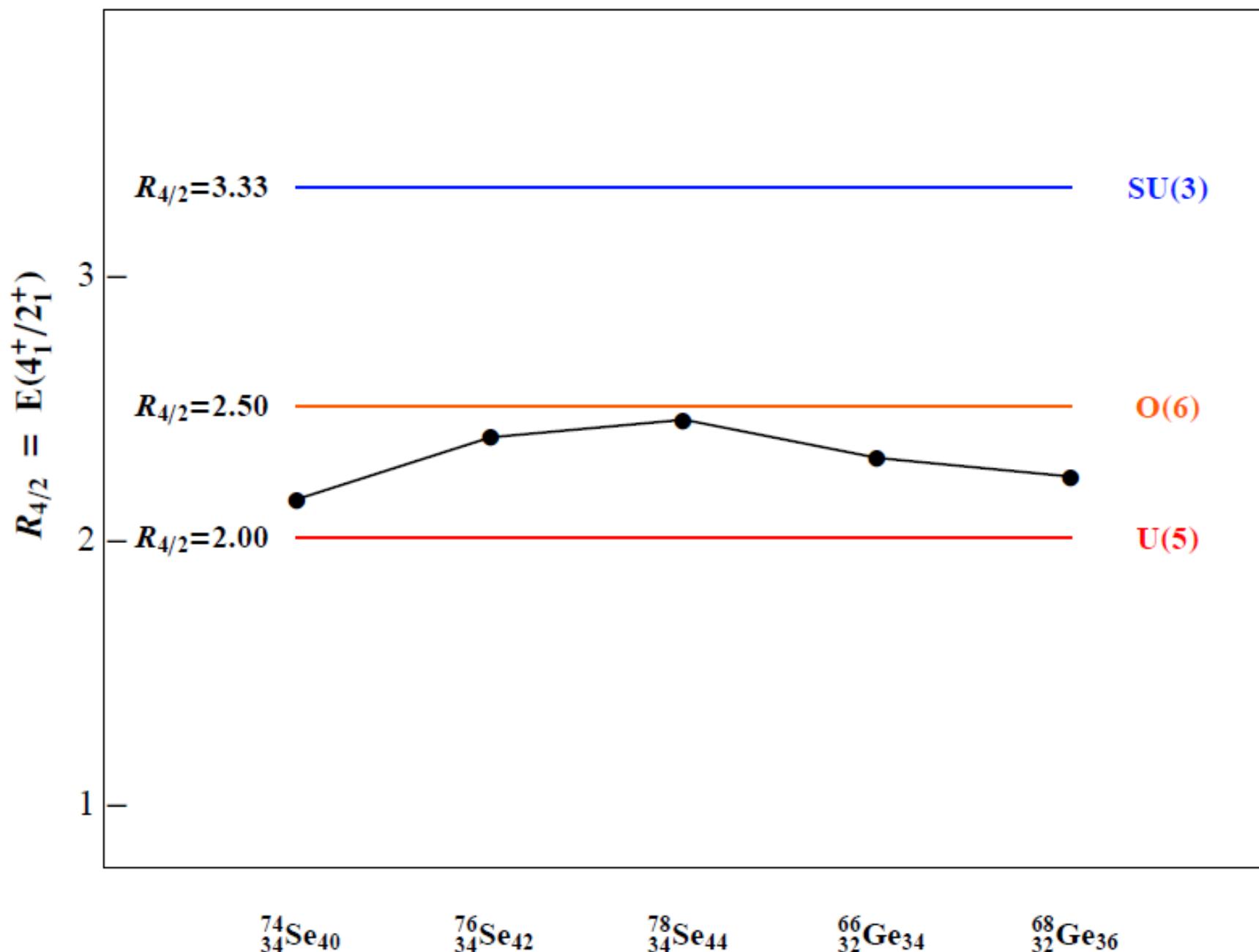
# The effect of triaxial term in IBM-1 for O(6)



# The effect of triaxial term in IBM-1 for $SU(3)$



K. Heyde, et. al., Phys. Rev. C 29 (1984) 1420.



## Hamiltonian

$$\hat{H} = \epsilon \hat{n}_d + a_1 \hat{L} \cdot \hat{L} + a_2 \hat{Q} \cdot \hat{Q}$$

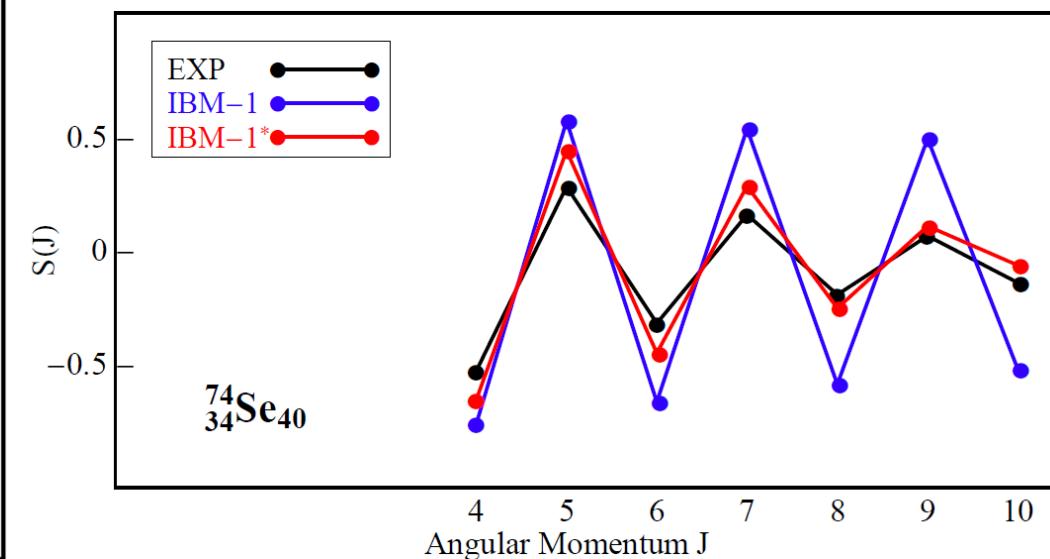
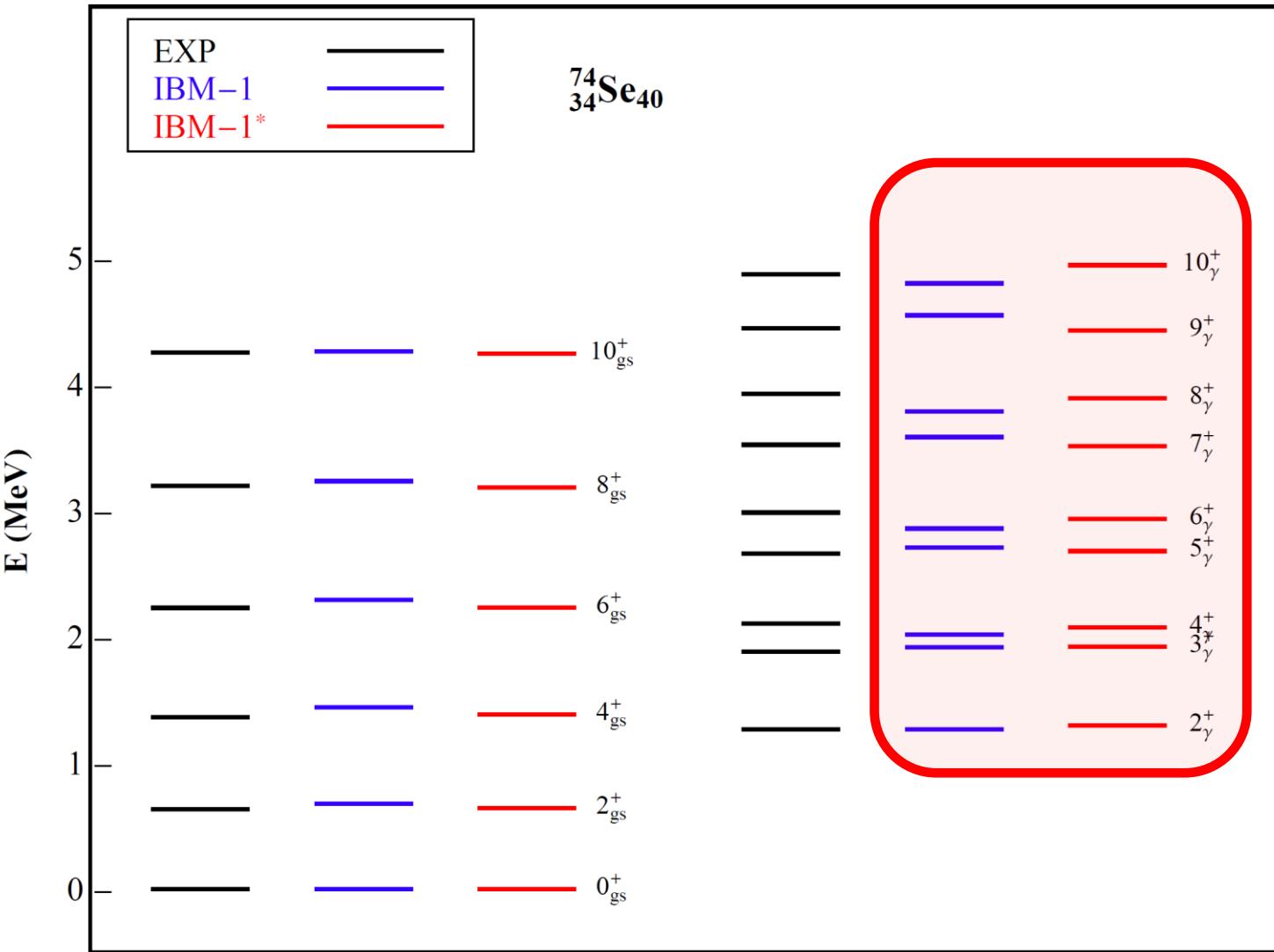
$$\hat{H} = \epsilon \hat{n}_d + a_0 \hat{P}_+ \cdot \hat{P}_- + a_1 \hat{L} \cdot \hat{L} + a_2 \hat{Q} \cdot \hat{Q} + \sum_L \nu_L [d^+ d^+ d^+]^{(L)} \cdot [\tilde{d} \tilde{d} \tilde{d}]^{(L)}$$

$$\Delta(E) = \sqrt{\frac{1}{N_E} \sum_i (E_{\text{ex}}^i - E_{\text{th}}^i)^2}$$

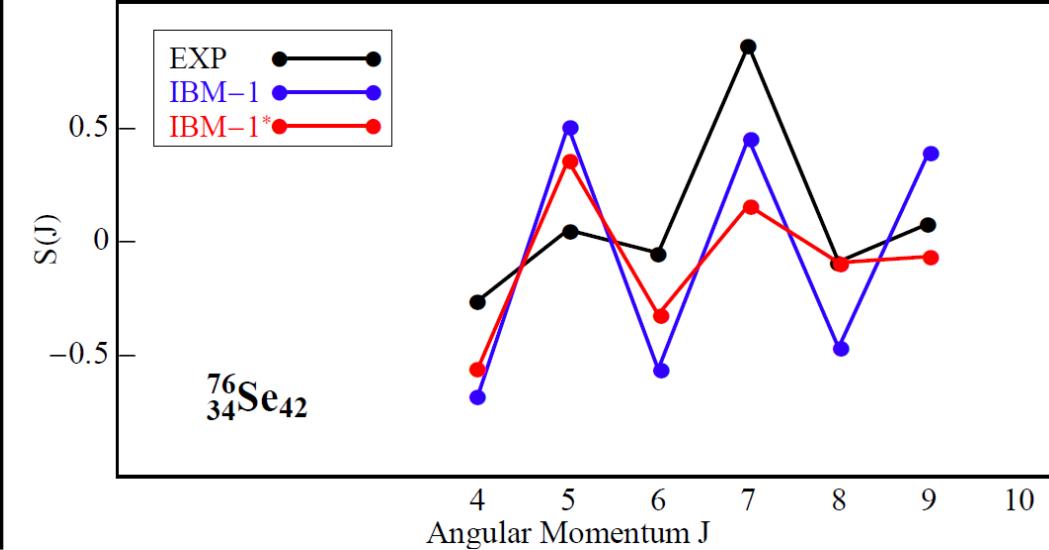
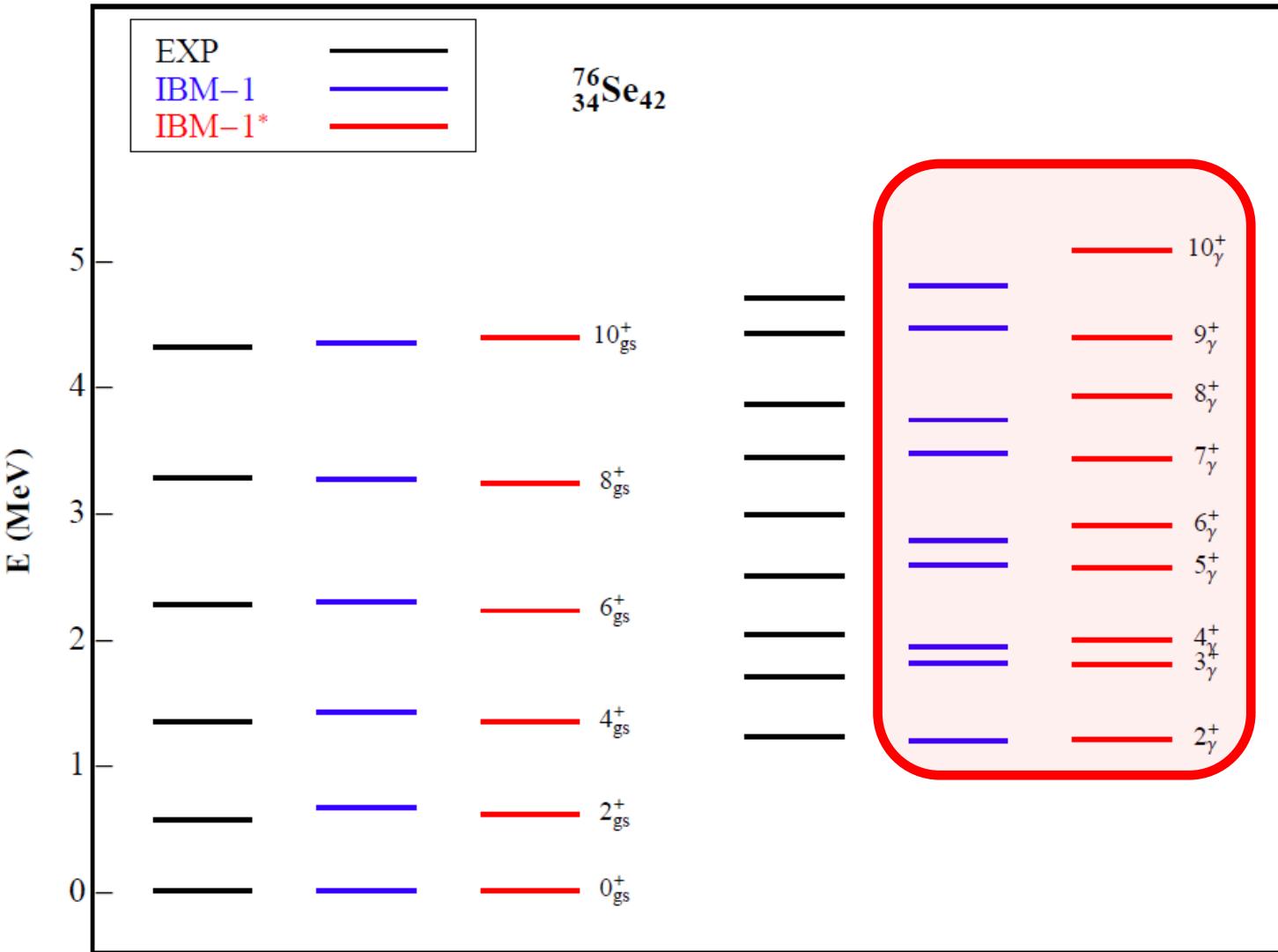
To understand the effect of this **cubic term** & to test the  $\gamma$ -softness behavior  
 Useful way is to look the signature splitting of  $\gamma$ -band within given formula as  $S(J)$

$$S(J) = \frac{E(J) - E(J-1)}{E(J) - E(J-2)} \cdot \frac{J(J+1) - (J-1)(J-2)}{J(J+1) - J(J-1)} - 1$$

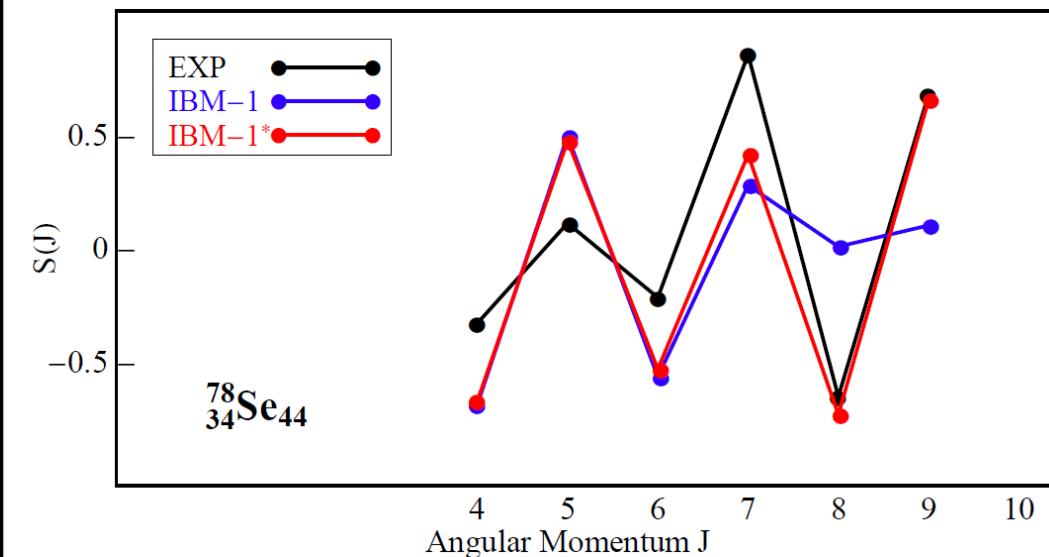
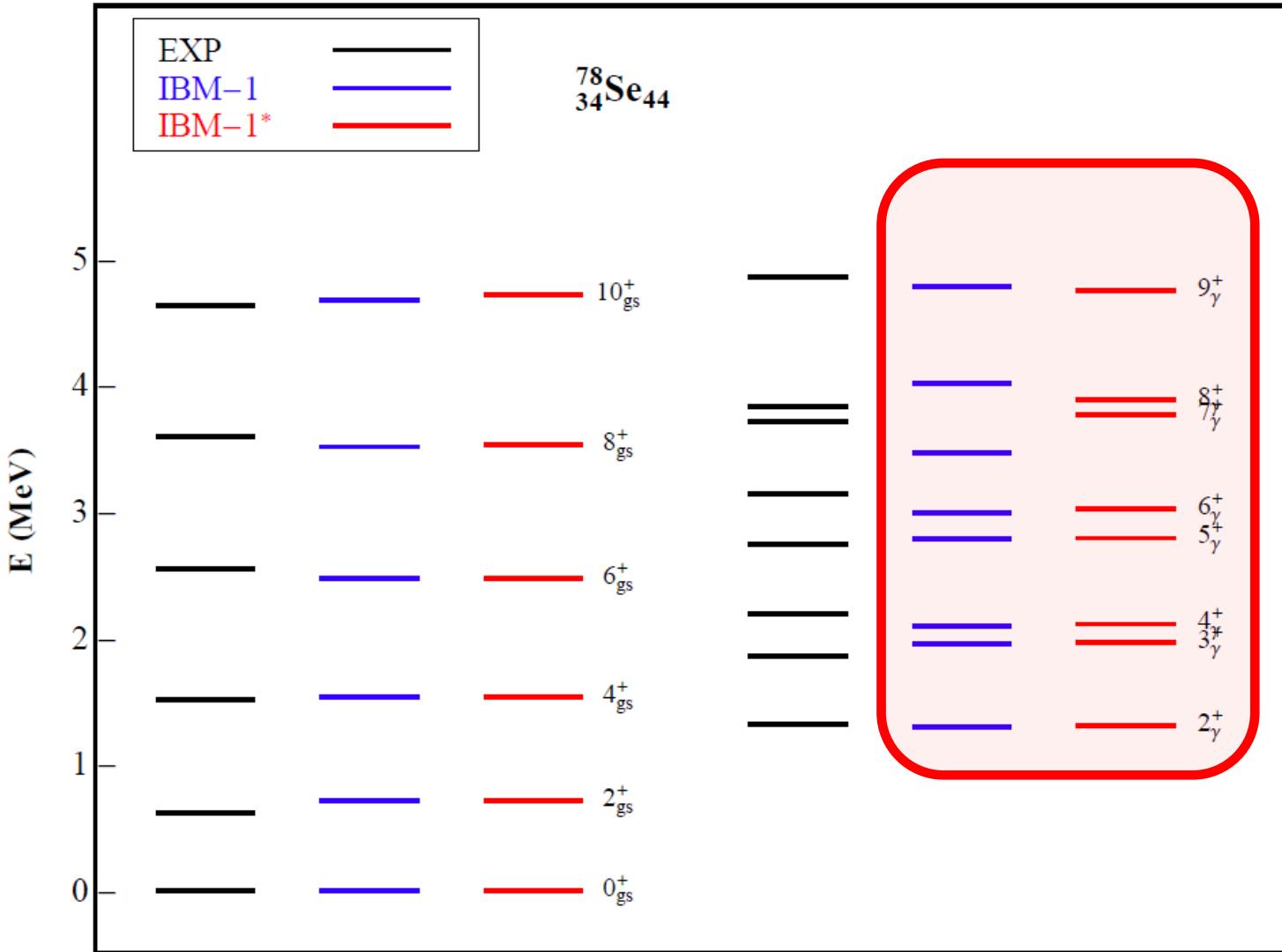
	$\epsilon$	$a_0$	$a_1$	$a_2$	$v_3$	$\chi$	$\sigma$
$^{74}\text{Se}$	0.5667	-	0.0124	0.0034	-	-0.950	0.076
	0.8762	0.1223	0.0105	0.0140	-0.0501	-0.950	0.032



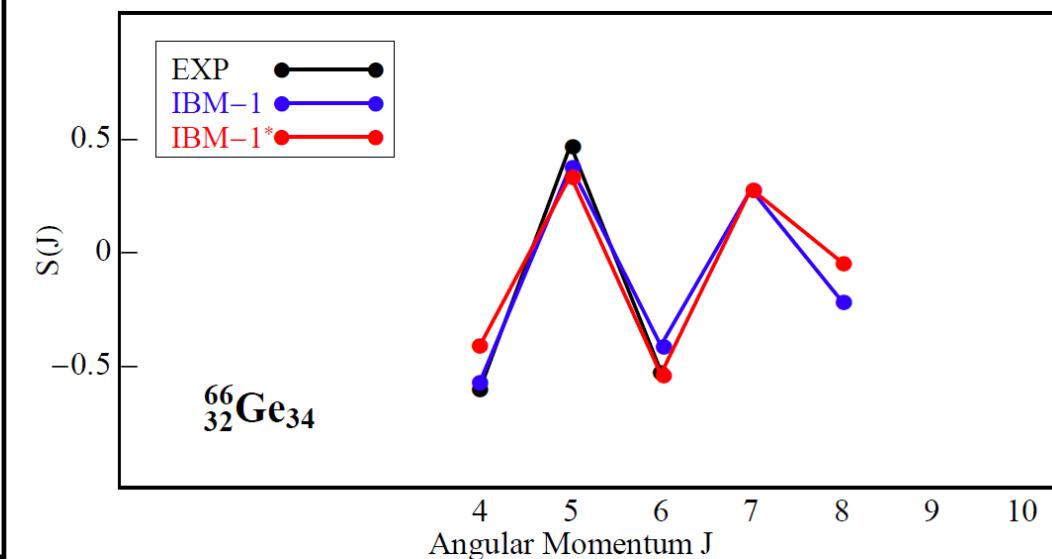
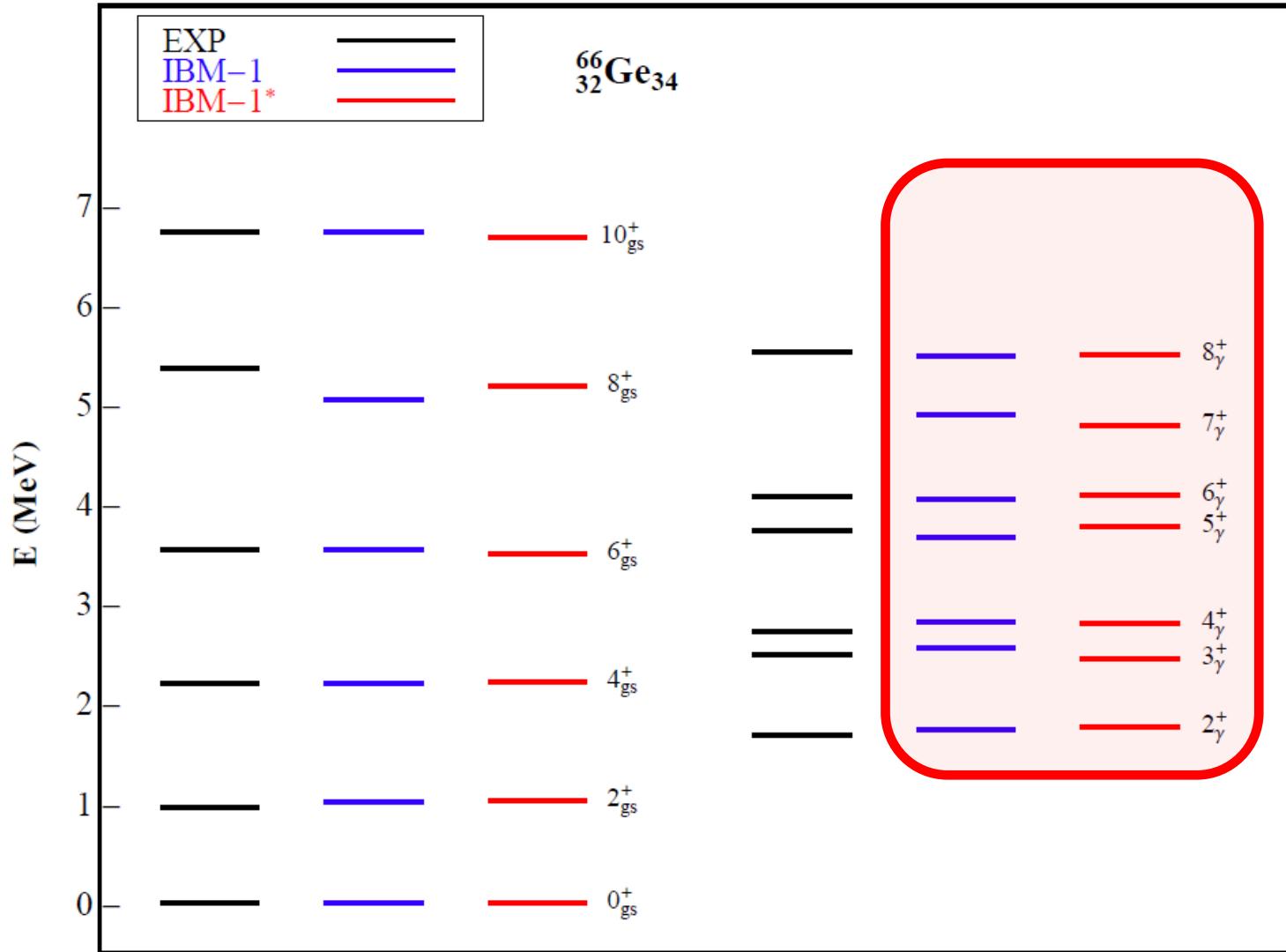
	$\epsilon$	$a_0$	$a_1$	$a_2$	$v_3$	$\chi$	$\sigma$
$^{76}\text{Se}$	0.5022	-	0.0161	0.0064	-	-0.950	0.092
	0.8530	0.1455	0.0122	0.0112	-0.0776	-0.950	0.056



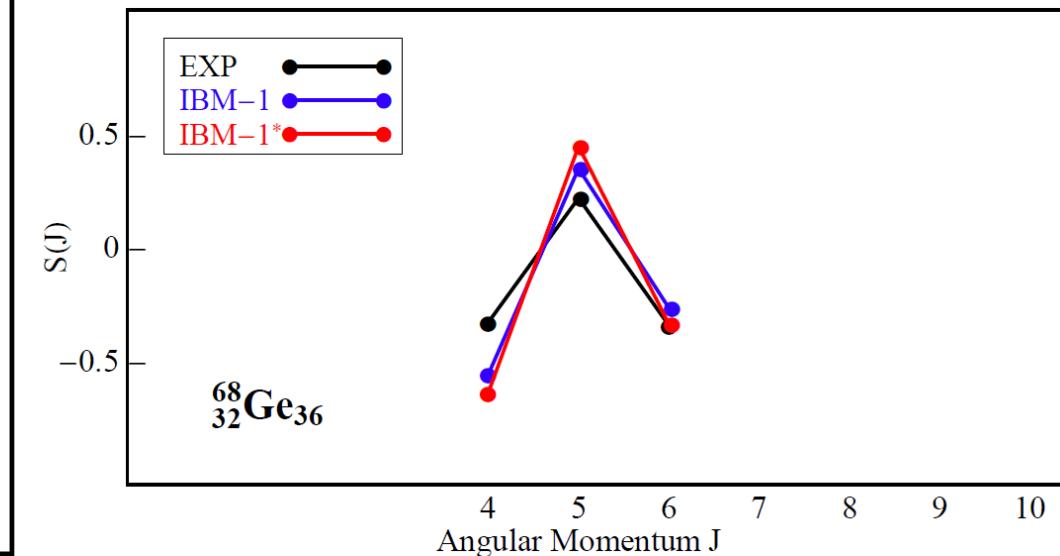
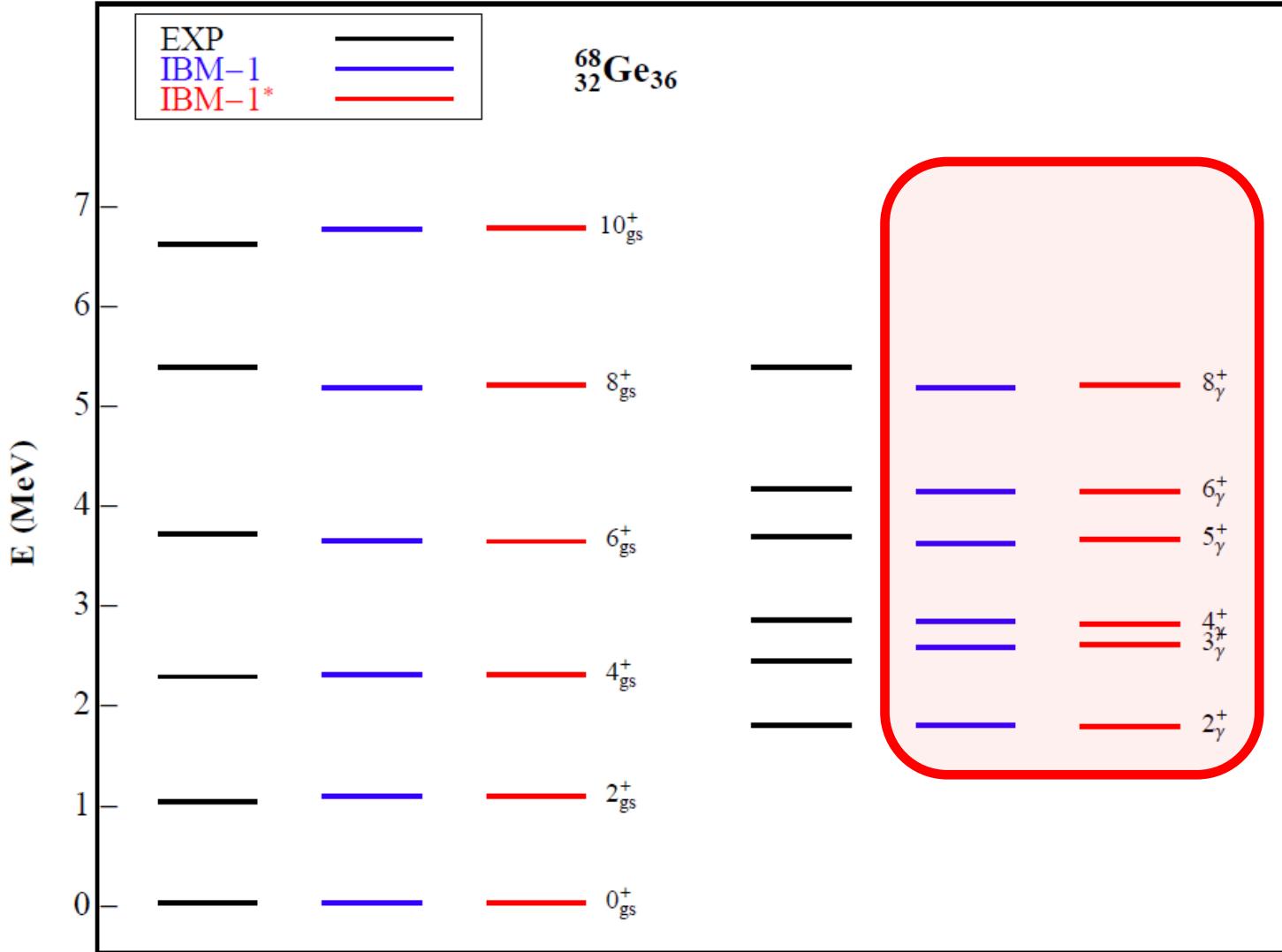
	$\epsilon$	$a_0$	$a_1$	$a_2$	$v_3$	$\chi$	$\sigma$
$^{78}\text{Se}$	0.5537	-	0.0173	0.0082	-	-0.950	0.092
	0.3955	-0.1046	0.0166	-0.0059	-0.0222	-0.950	0.078



	$\epsilon$	$a_0$	$a_1$	$a_2$	$v_3$	$\chi$	$\sigma$
$^{66}\text{Ge}$	0.6913	-	0.0335	0.0302	-	-0.500	0.130
	0.5270	-0.1166	0.0318	0.0264	-0.0390	-0.500	0.099



	$\epsilon$	$a_0$	$a_1$	$a_2$	$v_3$	$\chi$	$\sigma$
$^{68}\text{Ge}$	0.5788	-	0.0379	0.0566	-	-0.500	0.098
	0.5652	0.0022	0.0390	0.0596	0.0217	-0.500	0.096



$$\hat{H} = \hat{n}_d + a_1 \hat{L} \cdot \hat{L} + a_2 \hat{Q} \cdot \hat{Q} + \dots$$

$$\Delta(E) = \sqrt{\frac{1}{N_E} \sum_i (E_{\text{ex}}^i - E_{\text{th}}^i)^2}$$

$$\hat{H} = \hat{n}_d + a_0 \hat{P}_+ \cdot \hat{P}_- + a_1 \hat{L} \cdot \hat{L} + a_2 \hat{Q} \cdot \hat{Q} + \sum_L v_L [d^+ d^+ d^+]^{(L)} \cdot [\overbrace{d} \overbrace{d} \overbrace{d}]^{(L)}$$

The table lists experimental values for various isotopes of Selenium and Germanium, along with calculated parameters  $a_0$ ,  $a_1$ ,  $a_2$ ,  $v_3$ ,  $\chi$ , and  $\sigma$ .

	$\epsilon$	$a_0$	$a_1$	$a_2$	$v_3$	$\chi$	$\sigma$
$^{74}\text{Se}$	0.5667	-	0.0124	0.0034	-	-0.950	0.076
	0.8762	0.1223	0.0105	0.0140	-0.0501	-0.950	0.032
$^{76}\text{Se}$	0.5022	-	0.0161	0.0064	-	-0.950	0.092
	0.8530	0.1455	0.0122	0.0112	-0.0776	-0.950	0.056
$^{78}\text{Se}$	0.5537	-	0.0173	0.0082	-	-0.950	0.092
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# THANK YOU VERY MUCH

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Measured and calculated B(E2) values in units of  $10^{-2} e^2 b^2$  for  $^{76}\text{Se}$ .

$J_i^\pi \rightarrow J_f^\pi$	EXP	IBM-1	IBM-1*
$2_{gs}^+ \rightarrow 0_{gs}^+$	8.41 (0.28)	5.82	7.82
$4_{gs}^+ \rightarrow 2_{gs}^+$	13.58 (0.55)	9.97	13.41
$6_{gs}^+ \rightarrow 4_{gs}^+$	13.00 (2.21)	12.43	16.65
$8_{gs}^+ \rightarrow 6_{gs}^+$	15.68 (4.69)	13.17	17.57
$10_{gs}^+ \rightarrow 8_{gs}^+$	9.94 (3.03)	12.21	16.26
$2_\gamma^+ \rightarrow 0_{gs}^+$	0.23 (0.03)	0.005	0.02
$3_\gamma^+ \rightarrow 2_{gs}^+$	0.36 (0.22)	0.008	0.03
$4_\gamma^+ \rightarrow 4_{gs}^+$	4.21 (1.93)	6.49	6.33
$4_\gamma^+ \rightarrow 2_\gamma^+$	5.55 (1.93)	6.75	8.09
$5_\gamma^+ \rightarrow 3_\gamma^+$	12.81 (6.34)	7.36	8.58
$5_\gamma^+ \rightarrow 4_{gs}^+$	0.90 (0.47)	0.008	0.02
$6_\gamma^+ \rightarrow 4_\gamma^+$	5.55 (4.96)	9.34	11.31
$7_\gamma^+ \rightarrow 5_\gamma^+$	7.65 (5.79)	8.99	10.6
$0_\beta^+ \rightarrow 2_{gs}^+$	8.99 (6.07)	10.48	12.51

