

16-12-2016



Status of GINGERino

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GINGER meeting @ DEI, 16-12-2016 Padova

Outline



- **Introduction**

Sagnac interferometry & Ring Lasers Gyroscopes

- **Earth rotation (ER) measurements**

ER in Geodesy

- **State of the art of Ring Laser Gyroscopes**

ER in Relativity (GINGER idea)

- **Ongoing research at LNGS**

Deep Underground rotations:

GINGERino (underground seismology)

- **Conclusion**

Sagnac interferometry

Sagnac delay line

$$\Delta t_{Sagnac} = \frac{4A}{c^2} \vec{\Omega} \cdot \vec{n}$$

Resonant cavity

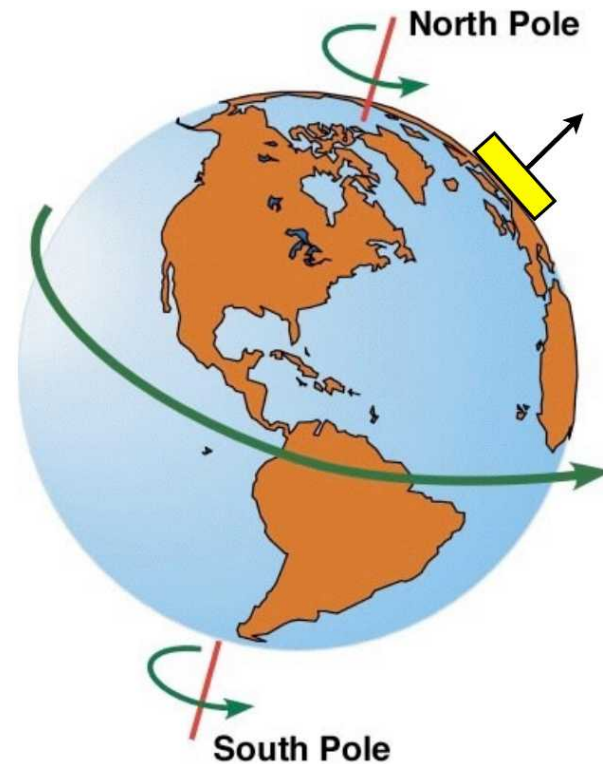
$$\Delta f_{Sagnac} = \frac{4A}{P\lambda} \vec{\Omega} \cdot \vec{n}$$

$$\text{Scale factor } K_s = \frac{4A}{P\lambda}$$

Ring laser

Internal generation,
Simple detection:
 optical beat CW-CCW

- No moving masses
- No signal for a linearly accelerating reference-frame (and gravity)
- $L > 1 \text{ m} \rightarrow$ Earth rotation is the bias!



Ring Laser Gyroscopes

Pure frequency measurement
 No need external space reference frame

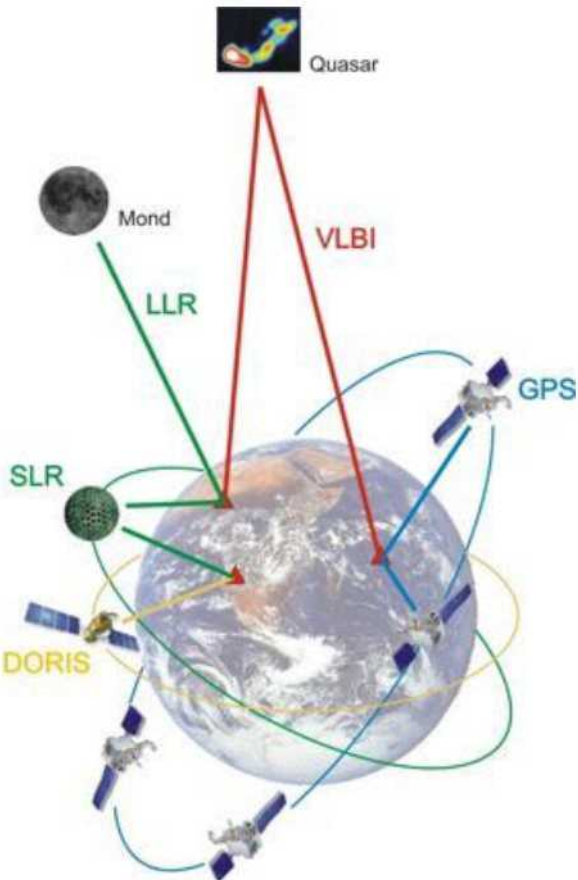
Earth rotation in Geodesy

Precise measurements of Earth rotation vector

- Link between **ICRF** (International Celestial Reference Frame) and **ITRF** (International Earth Reference Frame),
→ determination of the **EOP** (Earth Orientation Parameters)
- Earth's interior and atmospheric phenomena



Anglo-Australian Observatory



Typical Observations are based on “stellar methods”

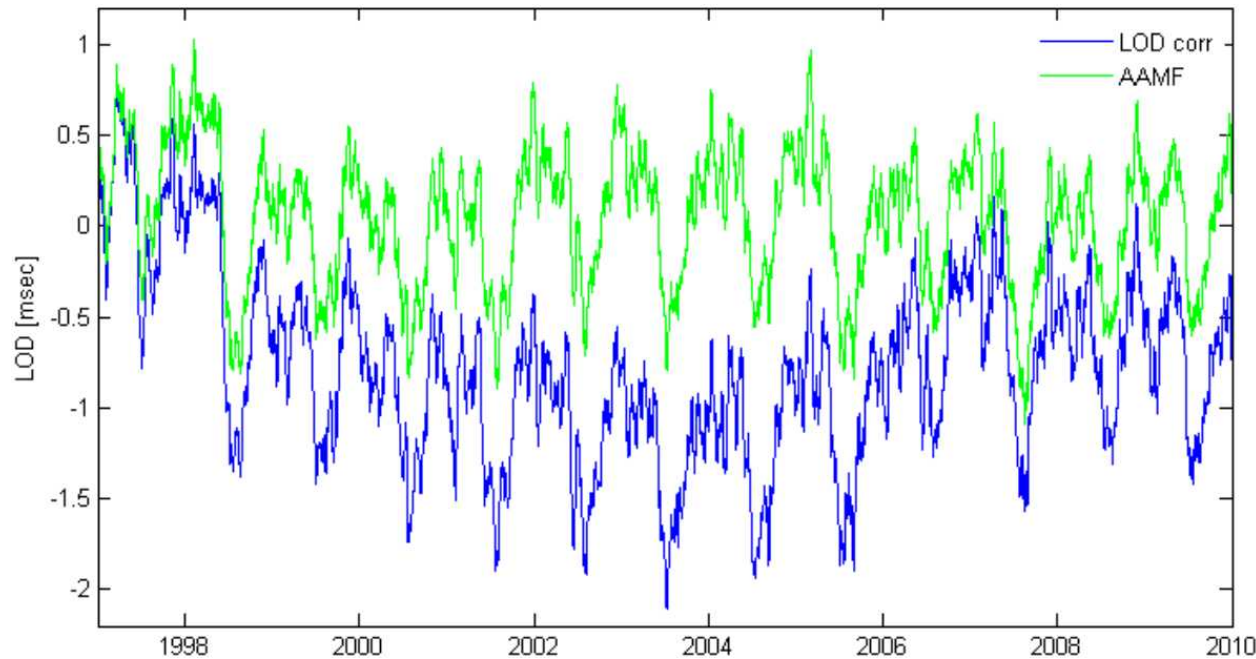
Navigation (GNSS), Satellite Laser Ranging (SLR), Lunar Laser Ranging (LLR), and Very Long Baseline Interferometry (VLBI), Doppler Orbitography and Radio-positioning Integrated by Satellite (DORIS)...

The measurement objects are defined in a **celestial frame of reference**, while the sensors are located on the Earth.

Earth rotation in Geodesy

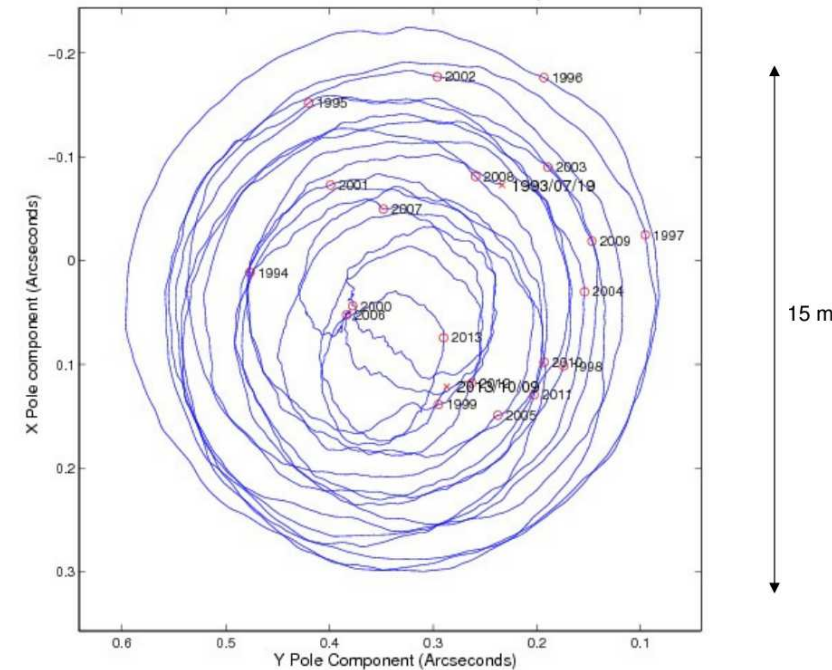


Modulus variations (Length Of Day)



Measured LOD and Atmospheric Angular Momentum from Weather Model

Direction variations



Polar Motion, moon and sun torque, free oscillation, geodynamics

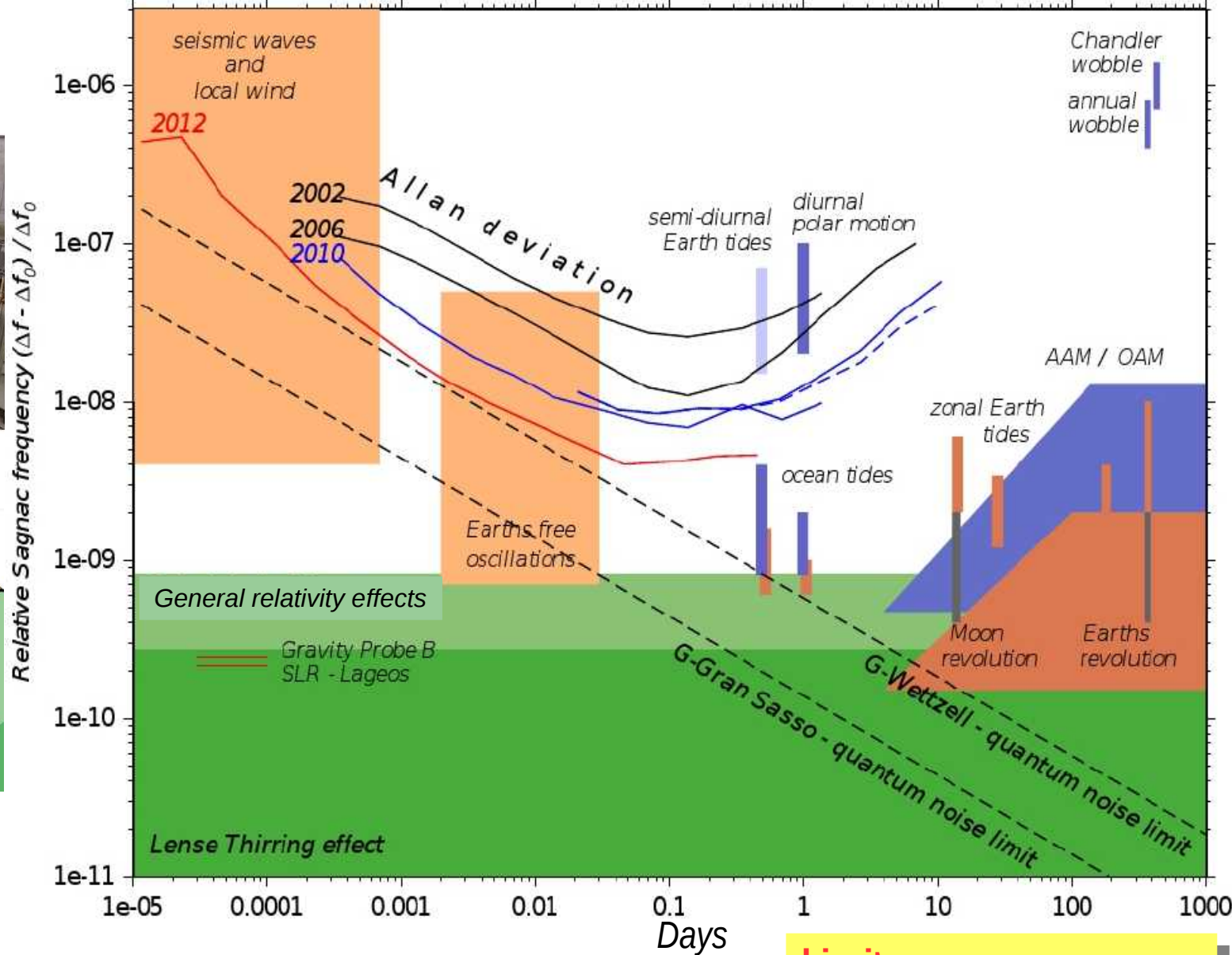
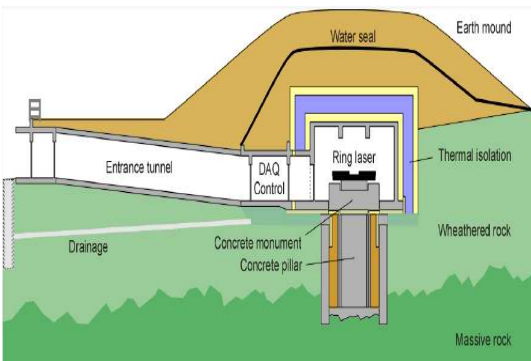
Sub daily time scale?

- "Stellar" methods have typically lower time resolution
- Need to link: Earth based reference frame <--> Celestial reference frame

Ring Laser Gyroscopes can play this role [target resolution $10^{-9} \Omega_E$]

State of the art: "G" ring laser at Wettzell (Germany)

Monolithic (L=4m)
+ perimeter stab. (comb)



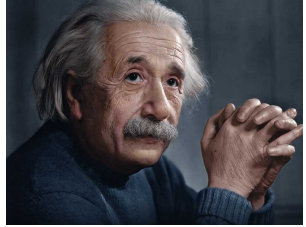
GEODESY

- Diurnal (Oppolzer) *K.U.Schreiber, et al., J. Geophys. Res., 109, (2004)*
- Annual (circular)+Chandler (elliptical) Wobble T=432 s.d. *K.U.Schreiber, et al., PRL, 107, 173904 (2011)*

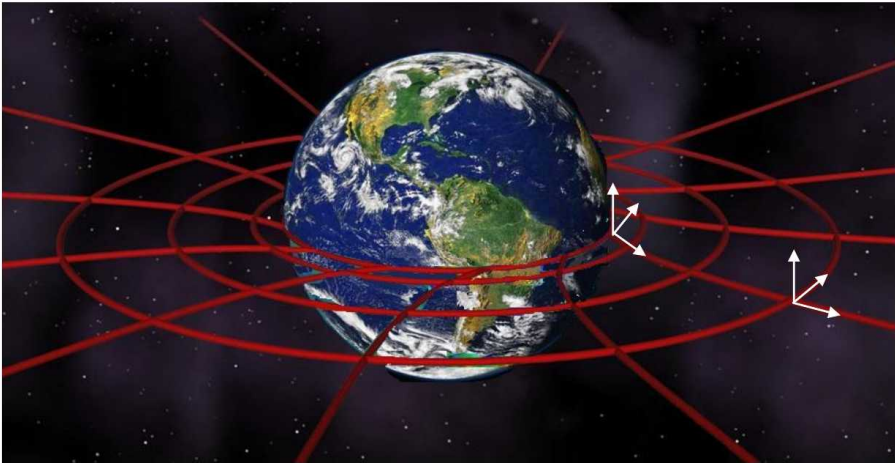
Limits

- Surface noise
- Ring Laser Dynamics

Earth rotation and General Relativity



"The axis of a **gyroscope** will precess following the curvature of the **local space-time** due to: **Earth's Mass** (*Geodetic precession*) and **Earth's Rotation** (*Lense-Thirring or Frame Dragging*)"

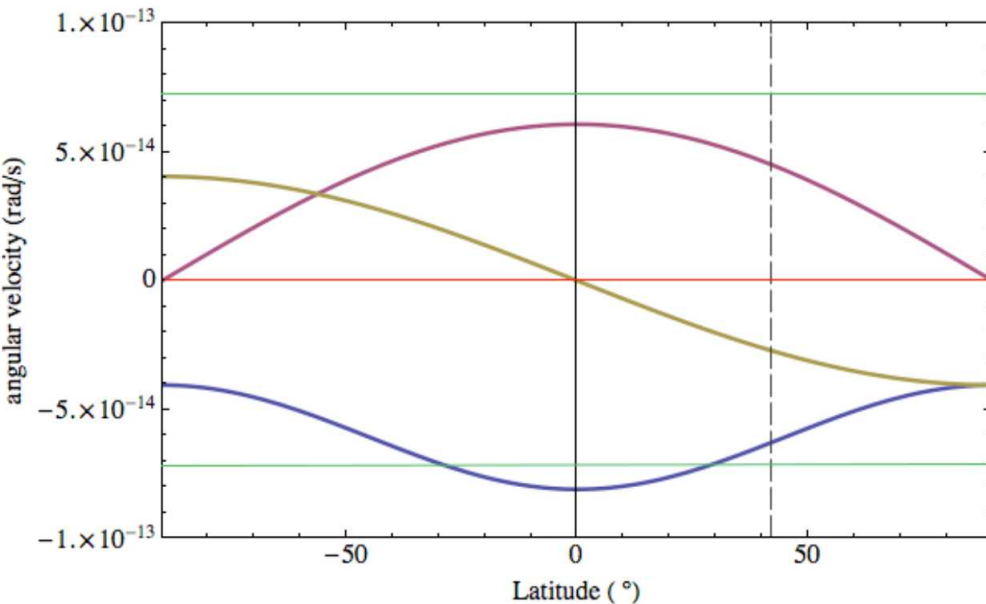


Results in Space : Lageos+GRACE & Lares, Gravity Probe B

..on ground with a laser Gyroscope

$$\delta \vec{\Omega} \simeq \frac{GM}{c^2 R} \Omega_E \sin \theta \hat{e}_\theta + \frac{G}{c^2 R^3} J_E \Omega_E [\hat{j}_E - 3(\hat{j}_E \cdot \hat{u}_r) \hat{e}_r]$$

$$6.98 \cdot 10^{-10} \Omega_E \quad 2.31 \cdot 10^{-10} \Omega_E$$



Relativistic corrections are on the **meridian plane** and depend on the **latitude of the laboratory**

- $\delta \vec{\Omega} \cdot \vec{u}_r$ (radial)
- $\delta \vec{\Omega} \cdot \vec{u}_E$ (Earth axis)
- $\delta \vec{\Omega} \cdot \vec{u}_{NS}$ (north-south)

GINGER motivation

F. Bosi et al., Phys. Rev. D 84, (2011)

Satellites are in geodetic motion (free fall),
while in ground laboratory the observer is in a non inertial motion

Metric is tested on different length scales (planetary \rightarrow meter-scale)

The apparatus is more accessible in a terrestrial laboratory
(the experiment can be repeated)

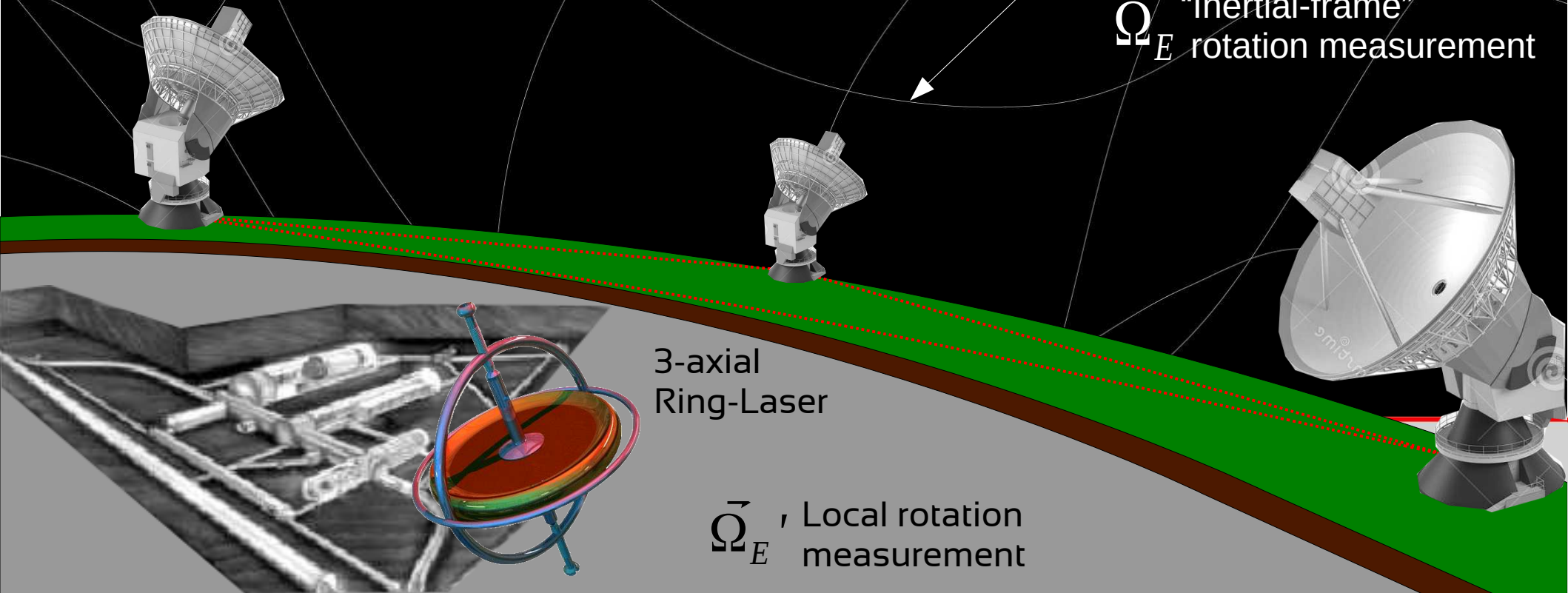
Different interpretation, no need of gravitational field models

Quasars

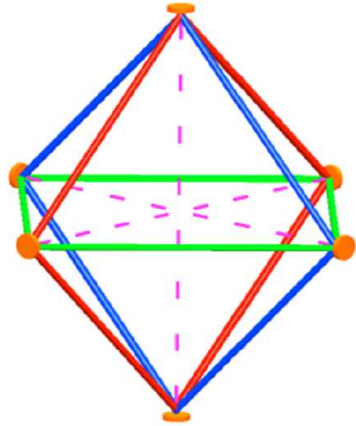
Ω_E "Inertial-frame"
rotation measurement

3-axial
Ring-Laser

$\vec{\Omega}_E$, Local rotation
measurement



GINGER key-points

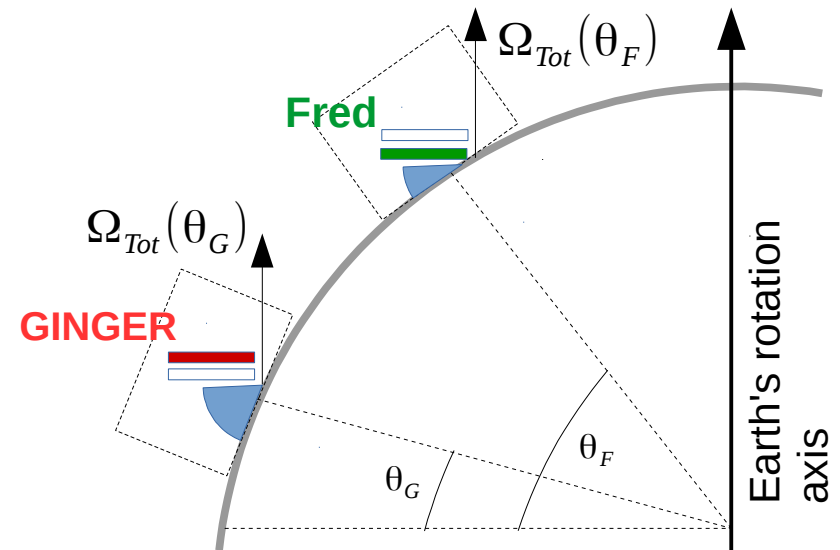


Multi axial approach

- Measure vector modulus + direct comparison with IERS
- Use one shared-mirrors octahedral array
- Minimize laser dynamics non-reciprocal effects ($L > 6\text{m}$) + modeling

Multi site approach

- Exploit the dependence of GR terms on the **latitude (differential measurement)**
- Use **2 TWIN RINGS** oriented at the maximum signal at different latitudes
- **Calibrate the 2 TWIN RINGS** when located at the same latitude (only mirrors defects)



Requirements

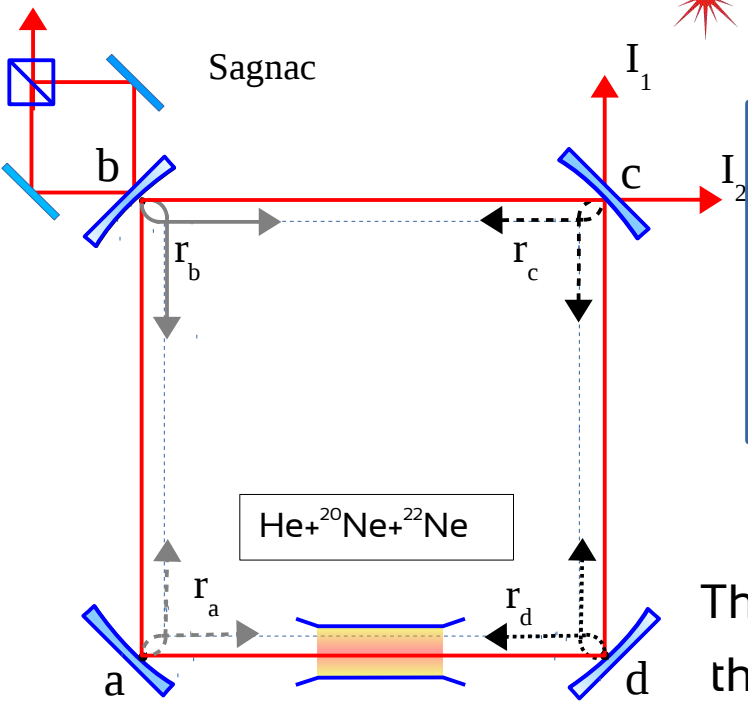
$$f_{Si} = \frac{4 A_i}{P_i \lambda_i} \vec{\Omega} \cdot \hat{n}_i + syst. \quad \frac{|\delta f_{Si}|}{|f_i|} < 10^{-10}$$

Systematics are diluted if $L > 6\text{ m}$

Strong requirements on GEOMETRY

Underground laboratory → low rotational noise

Ring Laser dynamics



Opposite beams coupled dynamics

$$\begin{aligned} \dot{I}_1 &= \alpha_1 I_1 - \beta I_1^2 - \theta_2 I_2 I_1 + r_2 \sqrt{I_1 I_2} \cos(\psi - \epsilon_1), \\ \dot{I}_2 &= \alpha_2 I_2 - \beta I_2^2 - \theta_1 I_2 I_1 + r_1 \sqrt{I_1 I_2} \cos(\psi + \epsilon_2), \\ \dot{\psi} &= \omega_s + \tau_1 I_1 - \tau_2 I_2 - r_2 \sqrt{\frac{I_2}{I_1}} \sin(\psi - \epsilon_2) - r_1 \sqrt{\frac{I_1}{I_2}} \sin(\psi + \epsilon_1) \end{aligned}$$

Non reciprocal dispersion

Backscattering

The backscattering parameters $r_1, r_2, \epsilon_1, \epsilon_2$ depend on the **interference of back scattered waves** (amplitude and phases)

Critical!

1) position and shape of the **laser finger-print on the mirror**



2) **interdistances** between the scattering centers



BUT

● In small rings, backscattering can be estimated (and subtracted)!



● In large rings ($L > 4\text{m}$ and excellent mirrors) cavities (linewidth $< f_s$) backscattering is out of resonance



Beam path geometry is the ultimate limit to stability

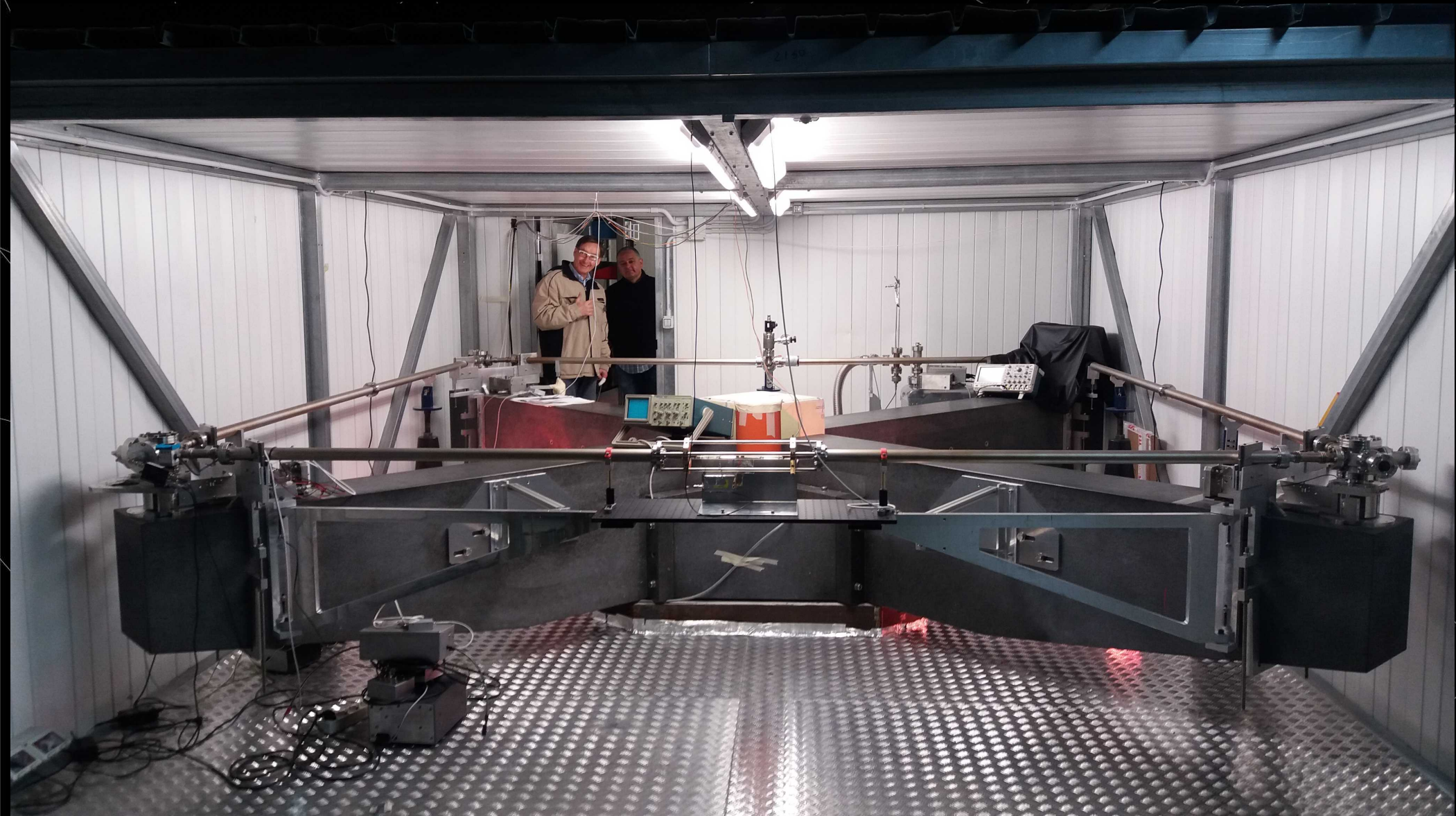
GINGERino: deep underground ring laser



He-Ne laser at 633 nm

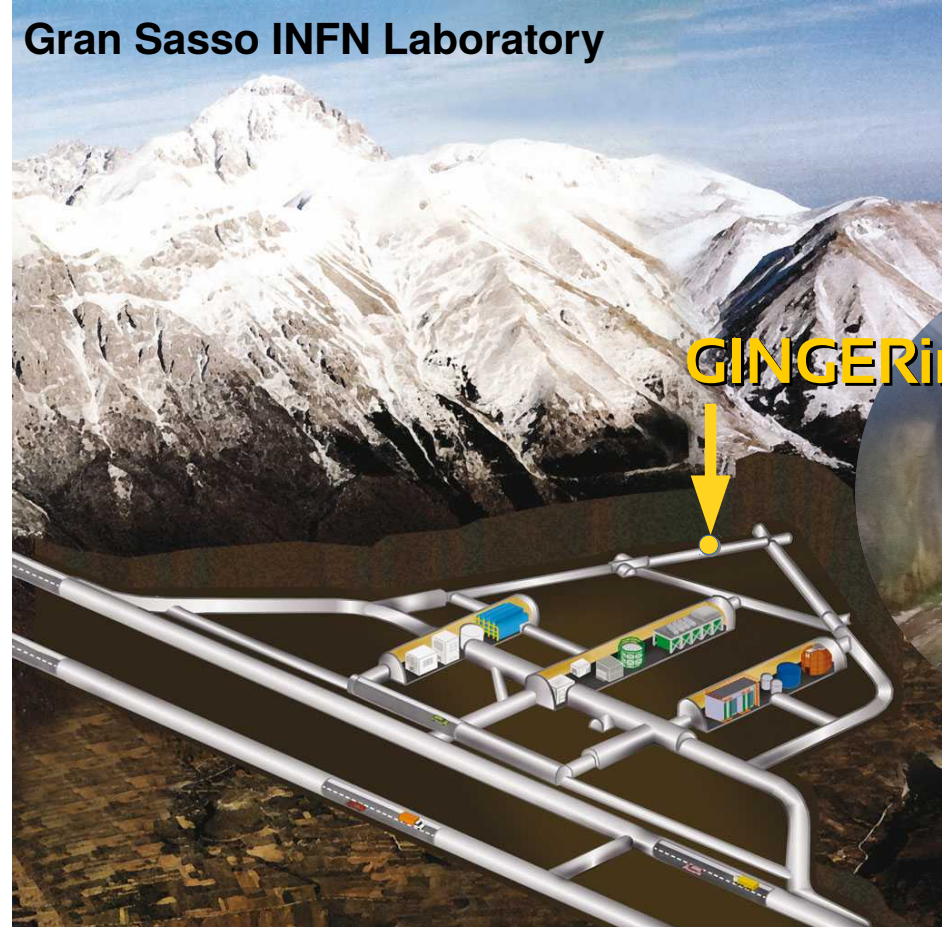
Square cavity, $L=3.6$ m, Mirrors r.o.c= 4 m

Earth rotation Sagnac bias: $f_s=280.4$ Hz



Installation site

Gran Sasso INFN Laboratory

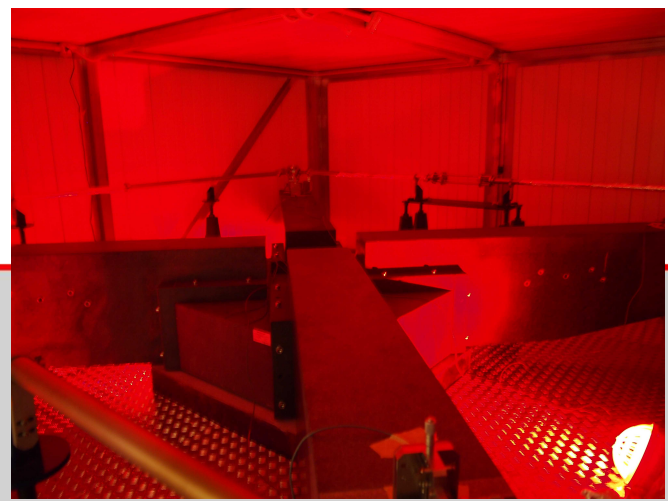
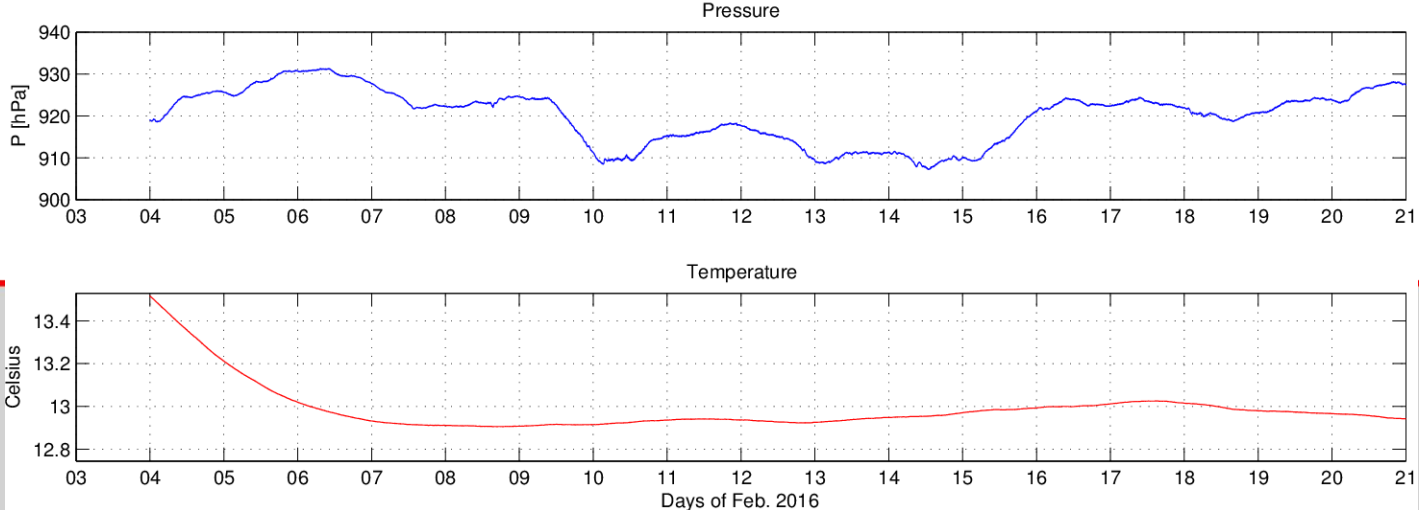


- The laboratory is located beneath 1 km of rock, Isolated from the other experiments

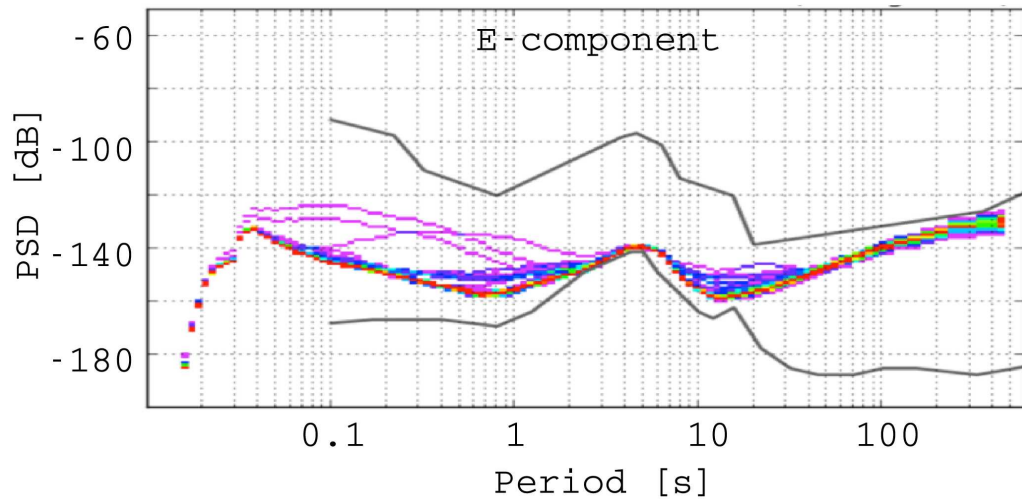
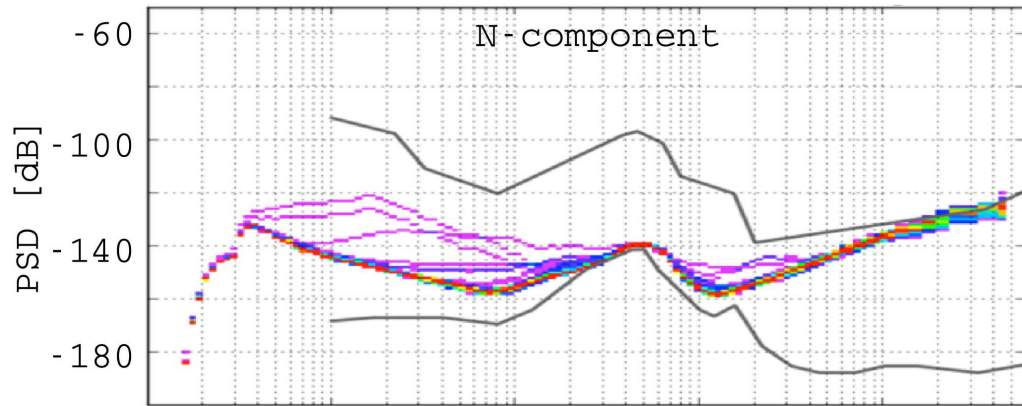
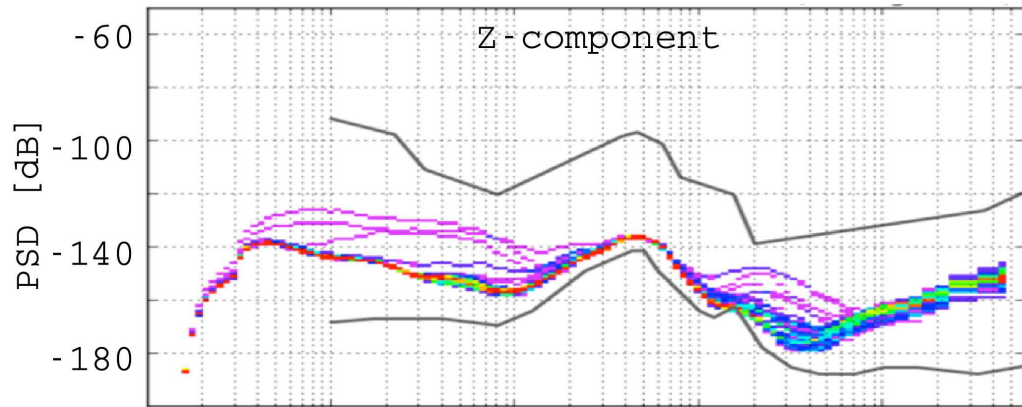


- Natural conditions:
T=8 °C, Relative humidity>90%

- **TEMPERATURE** increased by IR-lamps
Tint:--> 13°C, relative humidity--> 60%

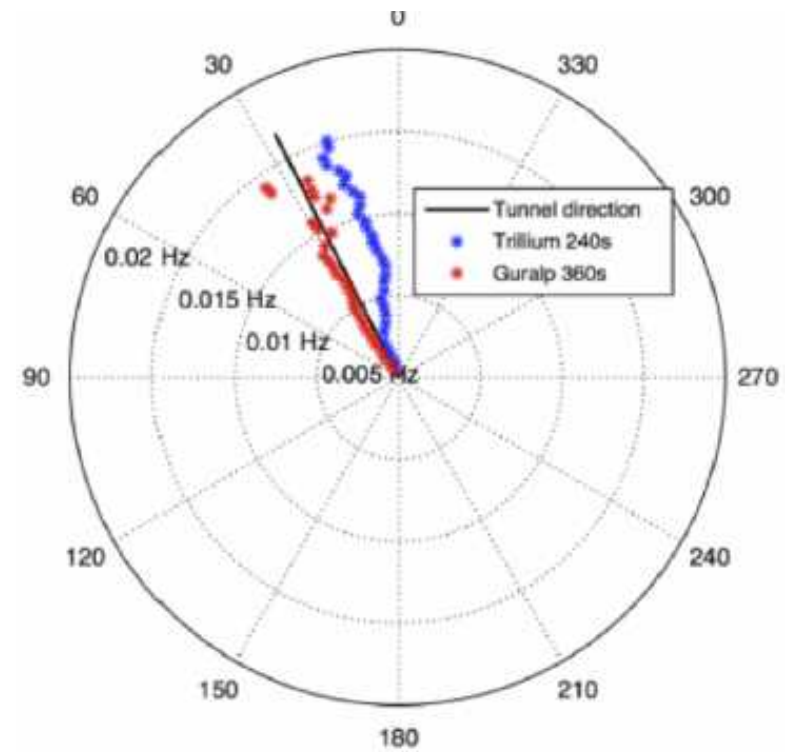
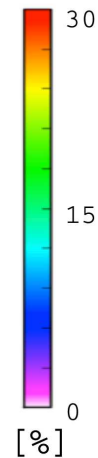


Seismic noise



Flicker noise at long periods
(east and north):

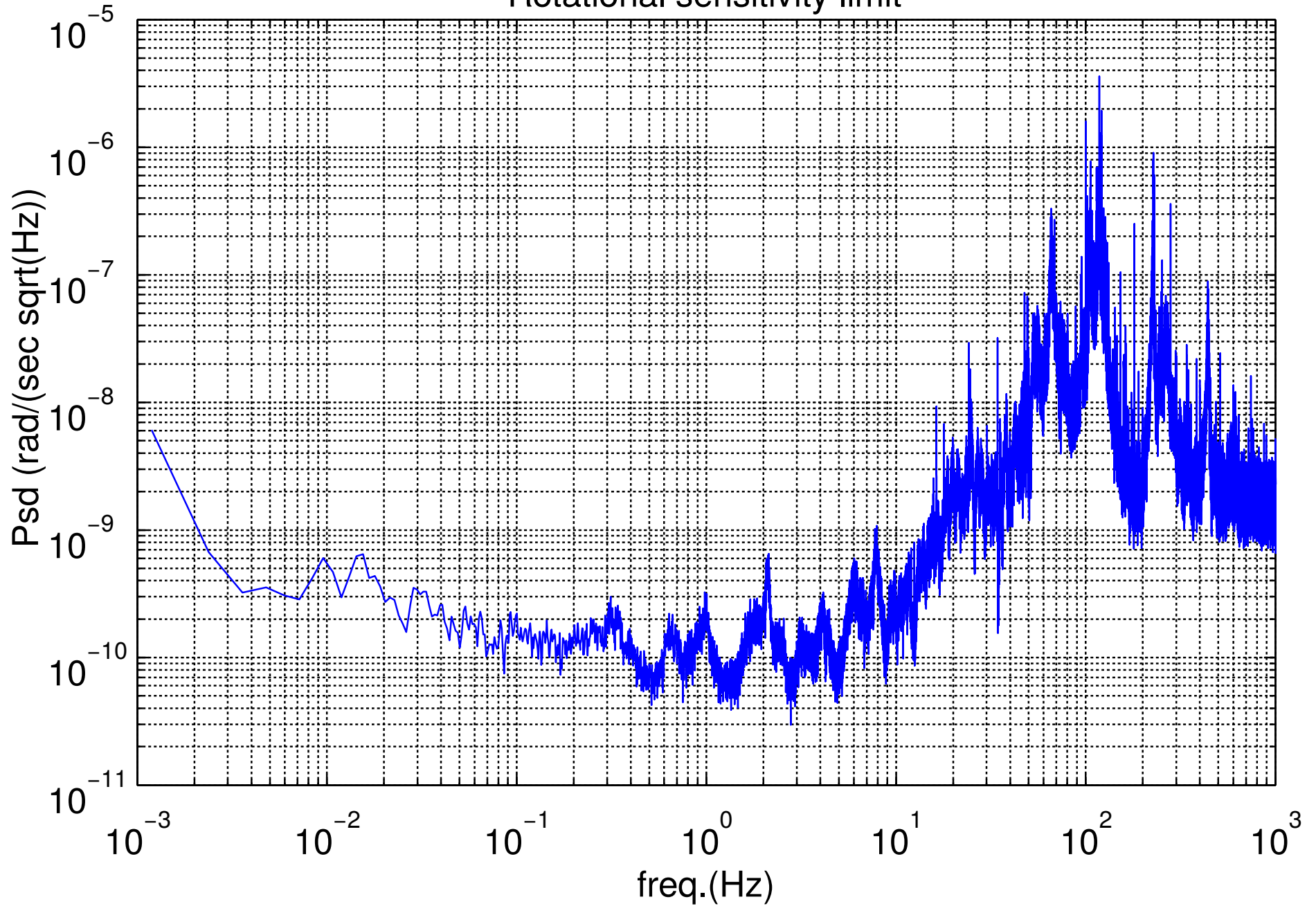
- Propagates along the tunnel direction
- Possibly related to strong pressure variations.
- Better isolation from the experimental halls will help. Pressure tight doors.



Rotational noise (raw data)



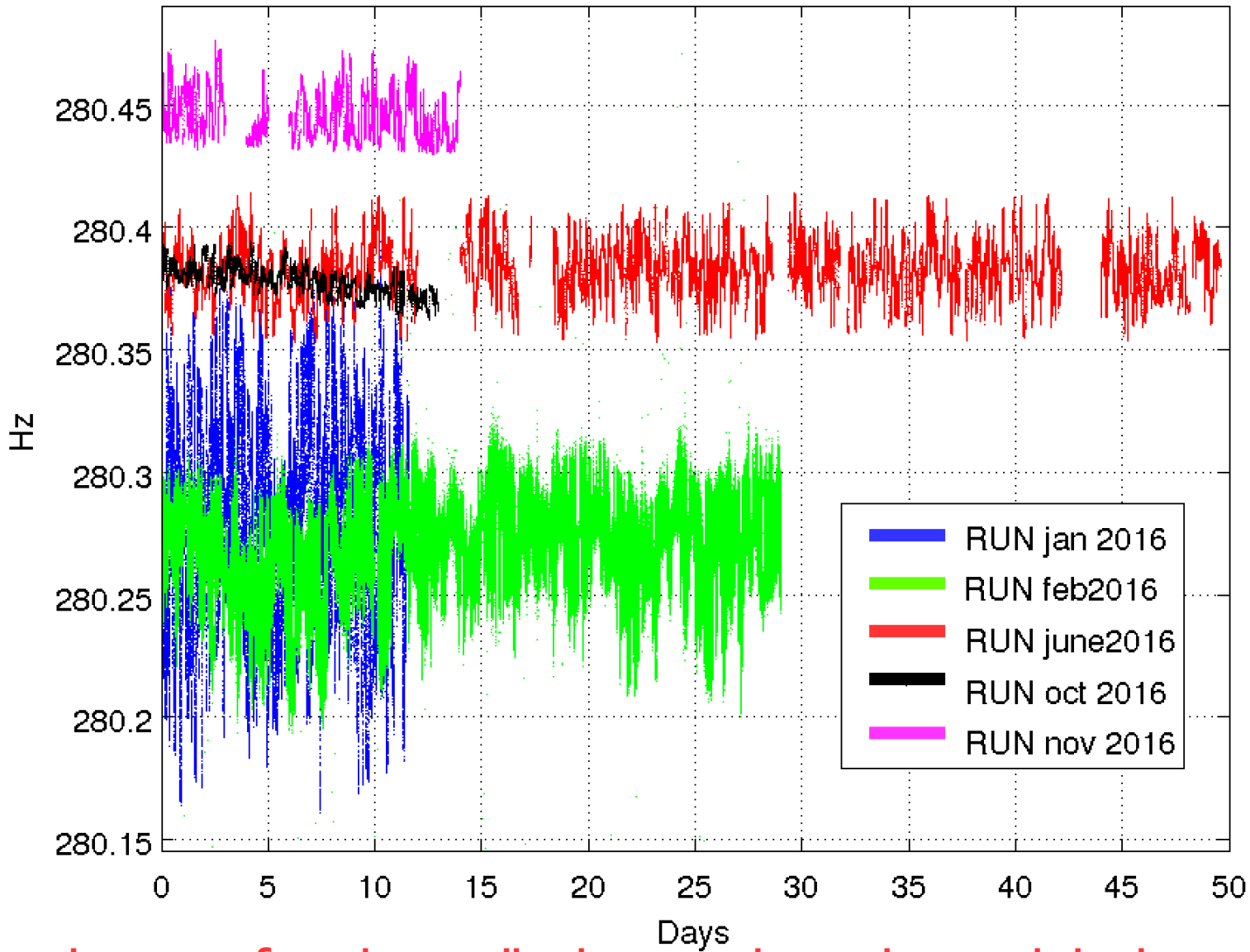
Rotational sensitivity limit



GINGERino raw data



GINGERino RAW Sagnac freq.



Excess noise comes from the coupling between the two beams via backscattering/losses

Present Shot-noise limit: $\Omega_{SN} = 4 \cdot 10^{-10} \text{ rad}/(s \sqrt{\text{Hz}})$

[Expected: tenfold improvement with best quality supermirrors]

Data processing

Acquired optical signals (5 kS/s)

$S(n)$ = Sagnac
 $I_1(n)$ = CCW monobeam
 $I_2(n)$ = CW monobeam
 $G(n)$ = Excitation level

Power Control

Analog PI circuit stabilizes the I_2 ($t > 1$ s)

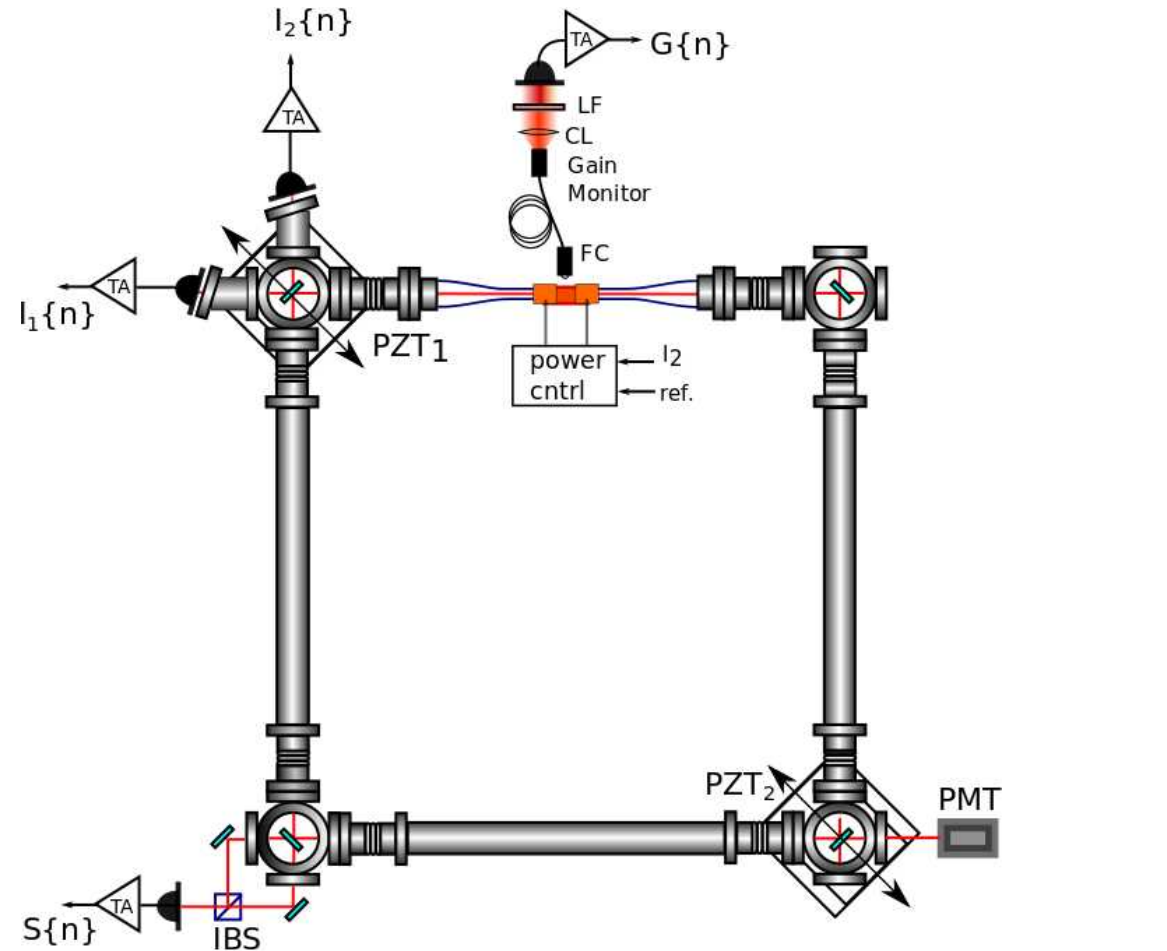
Backscattering correction

Identified parameters

$$\hat{r}_1 = \frac{i_2 \omega}{2(c/L) \sqrt{I_1 I_2}}$$

$$\hat{r}_2 = \frac{i_1 \omega}{2(c/L) \sqrt{I_1 I_2}}$$

$$\hat{\varepsilon} = \frac{\phi_1 - \phi_2}{2}$$



$$I_1(t) \simeq \frac{\alpha_1}{\beta} + 2r_2 \sqrt{\alpha_1 \alpha_2} \frac{\alpha_1 \cos(\varepsilon + \omega_s t) + (\frac{\omega_s}{c/L}) \sin(\varepsilon + \omega_s t)}{\beta (\alpha_1^2 + (\frac{\omega_s}{c/L})^2)} - 2 \frac{r_1 r_2 (c/L)}{\beta \omega_s} \sin(2\varepsilon)$$

$$I_2(t) \simeq \frac{\alpha_2}{\beta} + 2r_1 \sqrt{\alpha_1 \alpha_2} \frac{\alpha_2 \cos(\varepsilon - \omega_s t) - (\frac{\omega_s}{c/L}) \sin(\varepsilon - \omega_s t)}{\beta (\alpha_1^2 + (\frac{\omega_s}{c/L})^2)} + 2 \frac{r_1 r_2 (c/L)}{\beta \omega_s} \sin(2\varepsilon)$$

$$\Psi(t) \simeq (\omega_s - \frac{2r_1 r_2 (c/L)^2 \cos(2\varepsilon)}{\omega_s}) t + (c/L) \frac{r_1 \sqrt{\frac{\alpha_1}{\alpha_2}} \cos(\varepsilon - \omega_s t) + r_2 \sqrt{\frac{\alpha_2}{\alpha_1}} \cos(\varepsilon + \omega_s t)}{\omega_s}$$

A. Beghi et al. Applied Optics 51, 31 (2012)

D. Cuccato et al. Metrologia 51, 97, (2014)

Example: 24 h backscattering correction

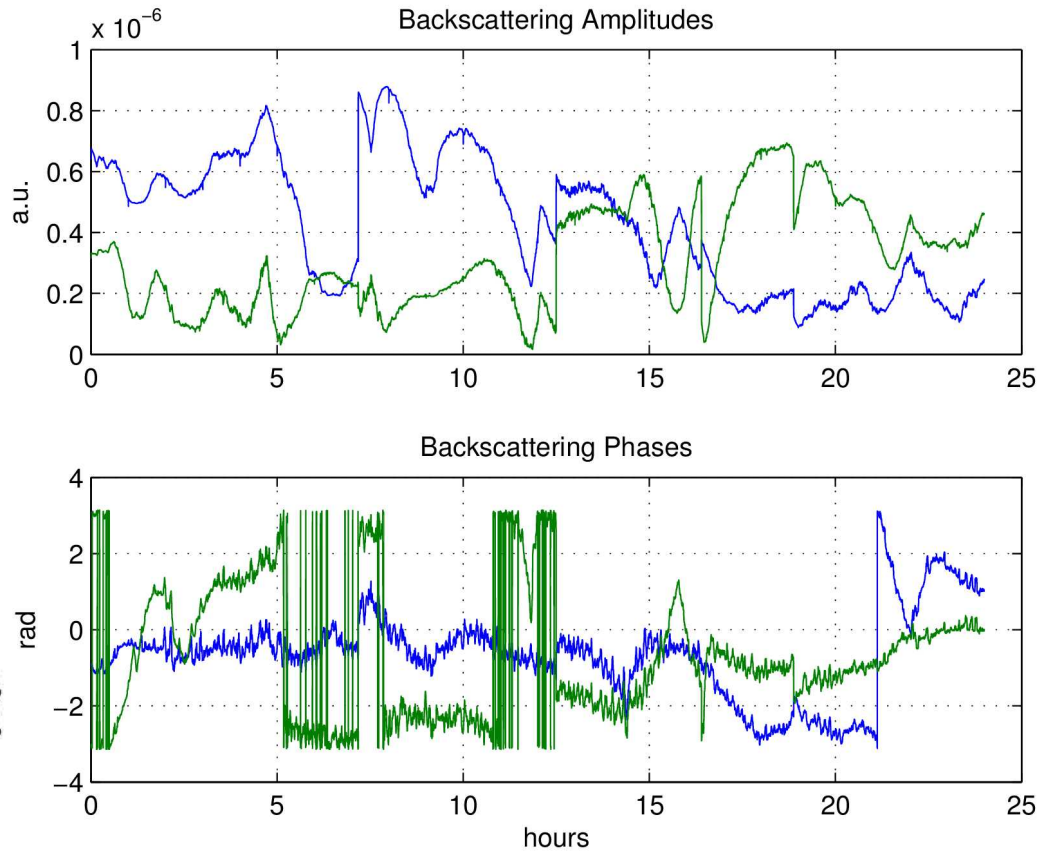
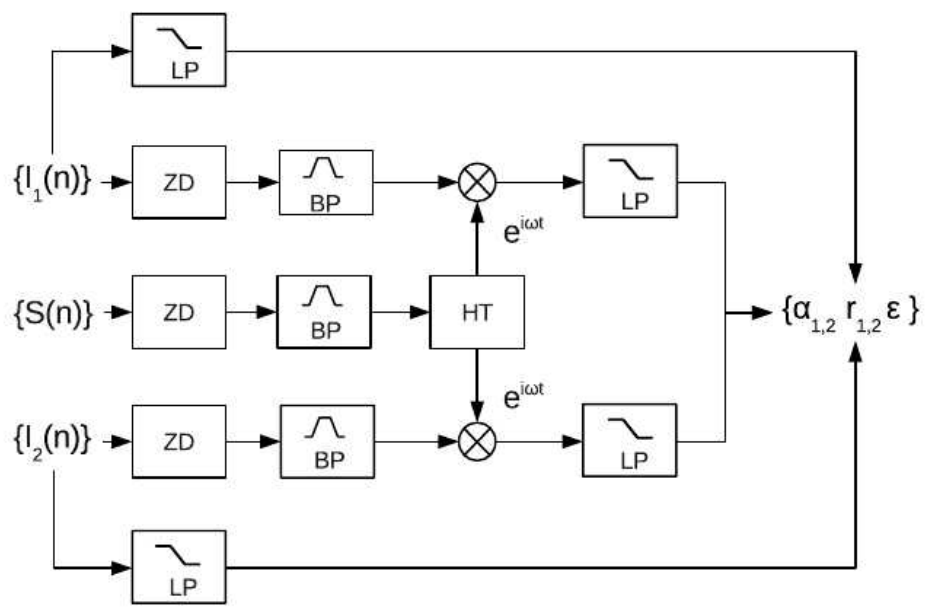
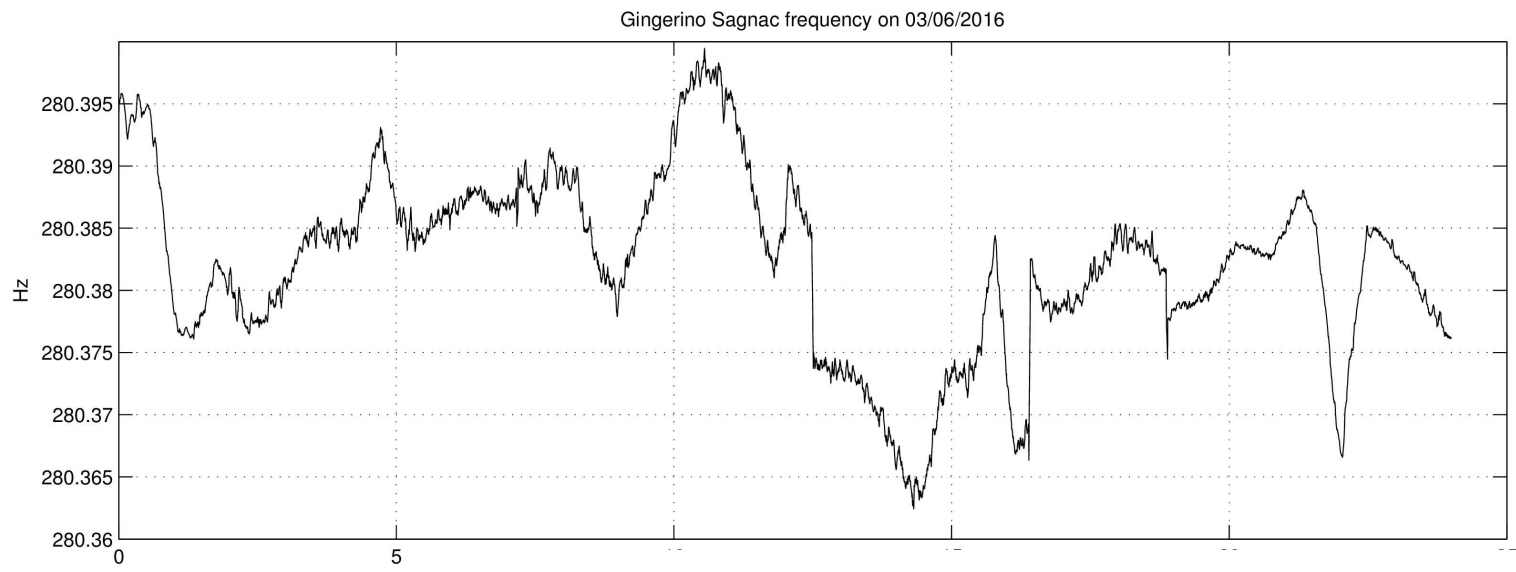
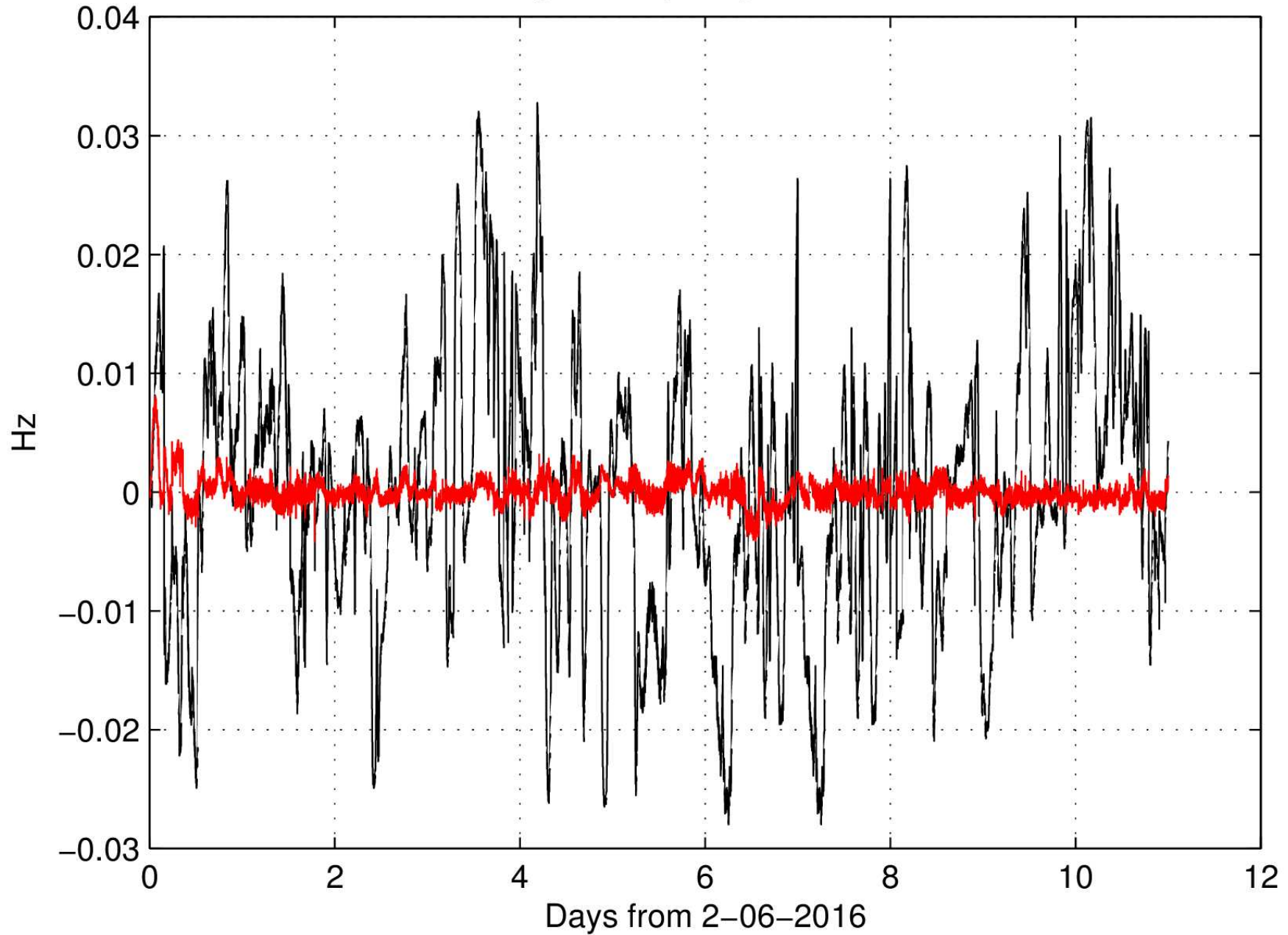


Fig. 3. Schematic of the parameter estimation procedure. LP, lowpass Butterworth filter; BP, bandpass Butterworth filter; ZD, zoom and decimation routine; HT, Hilbert transform (see text).

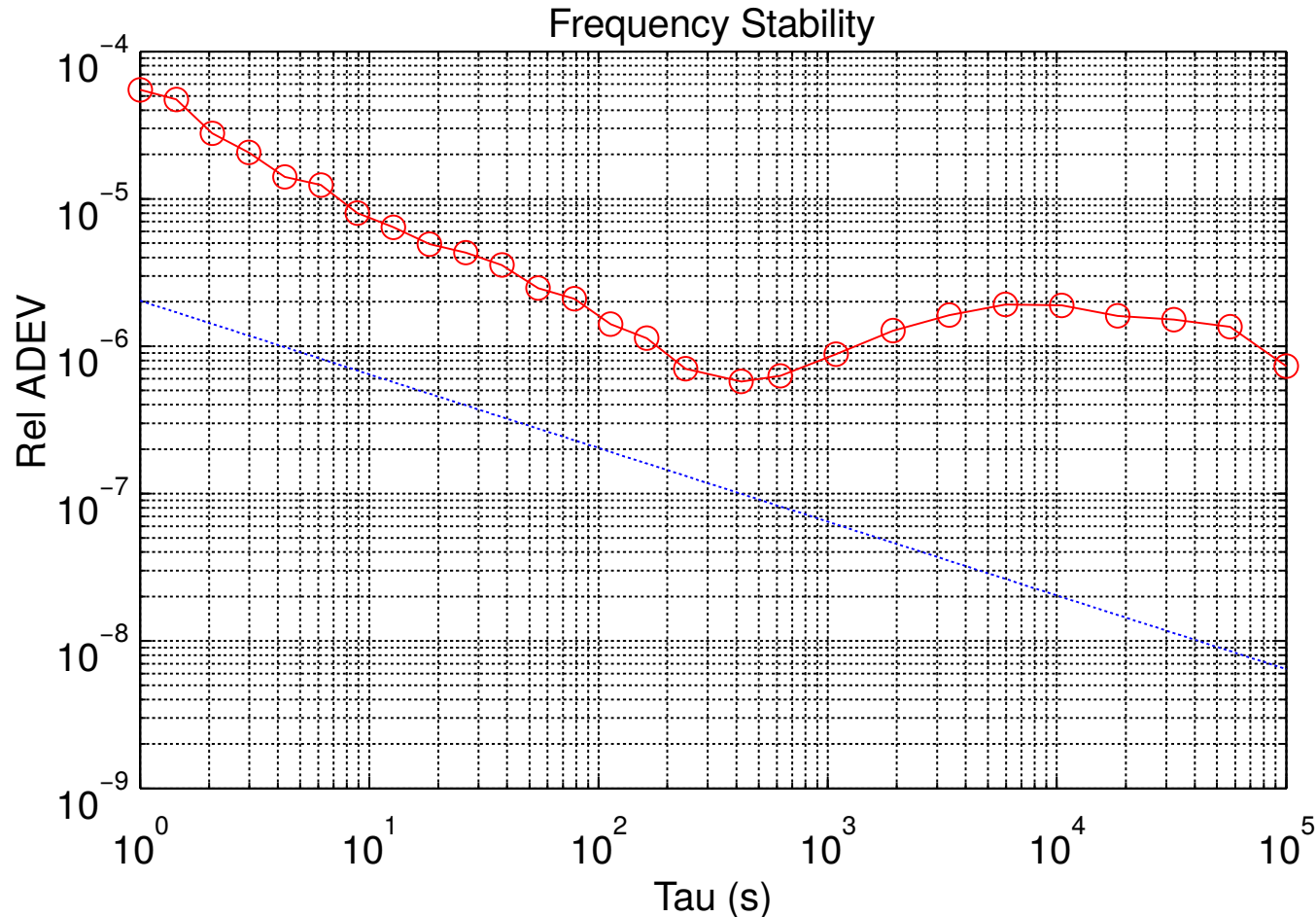
Long period observations 2-13 june 2016



Sagnac frequency fluctuation



Long period observations 2-13 june 2016

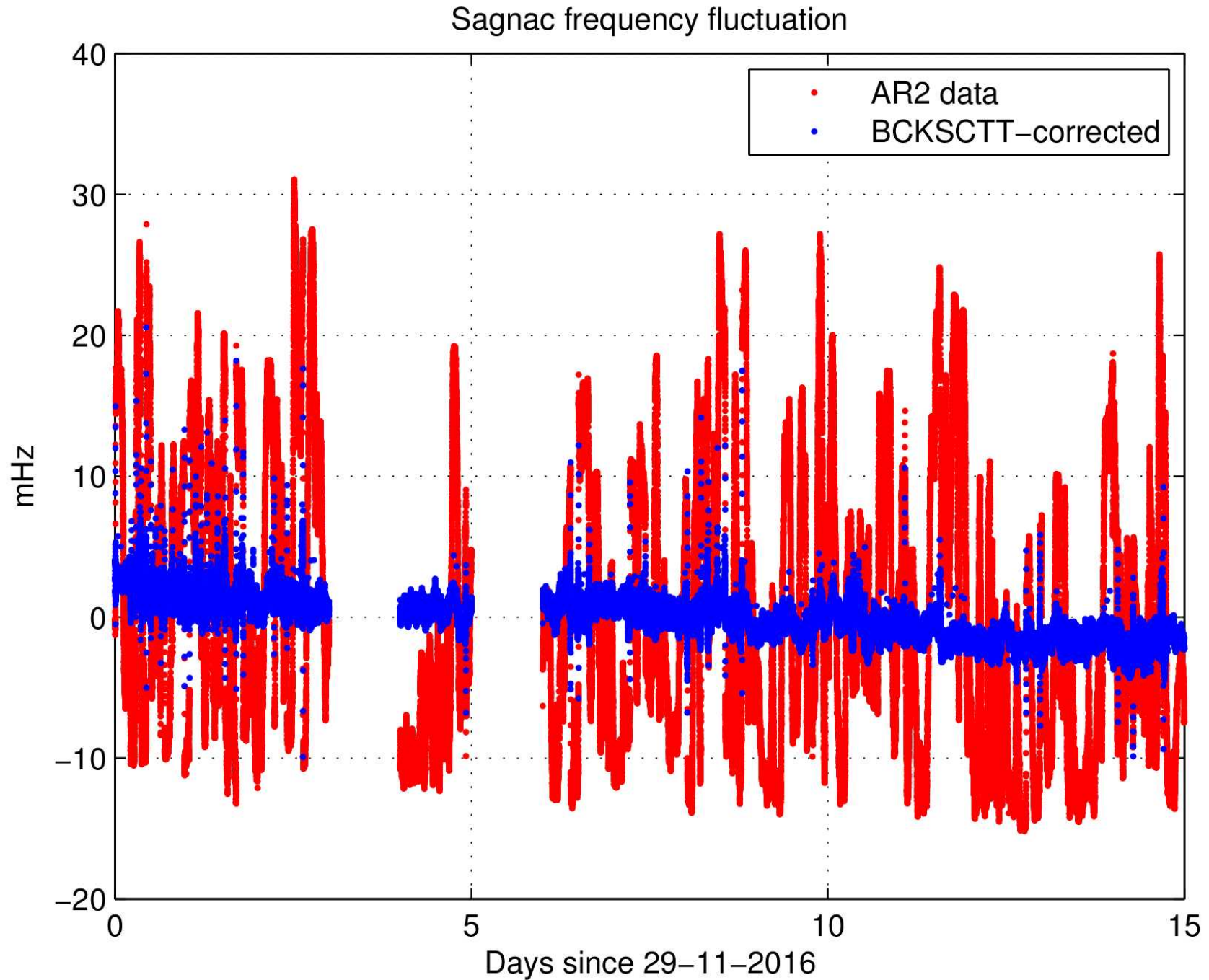


Maximum resolution: 0.6 ppm at 500 s of integration time
→ **30 p rad/s**

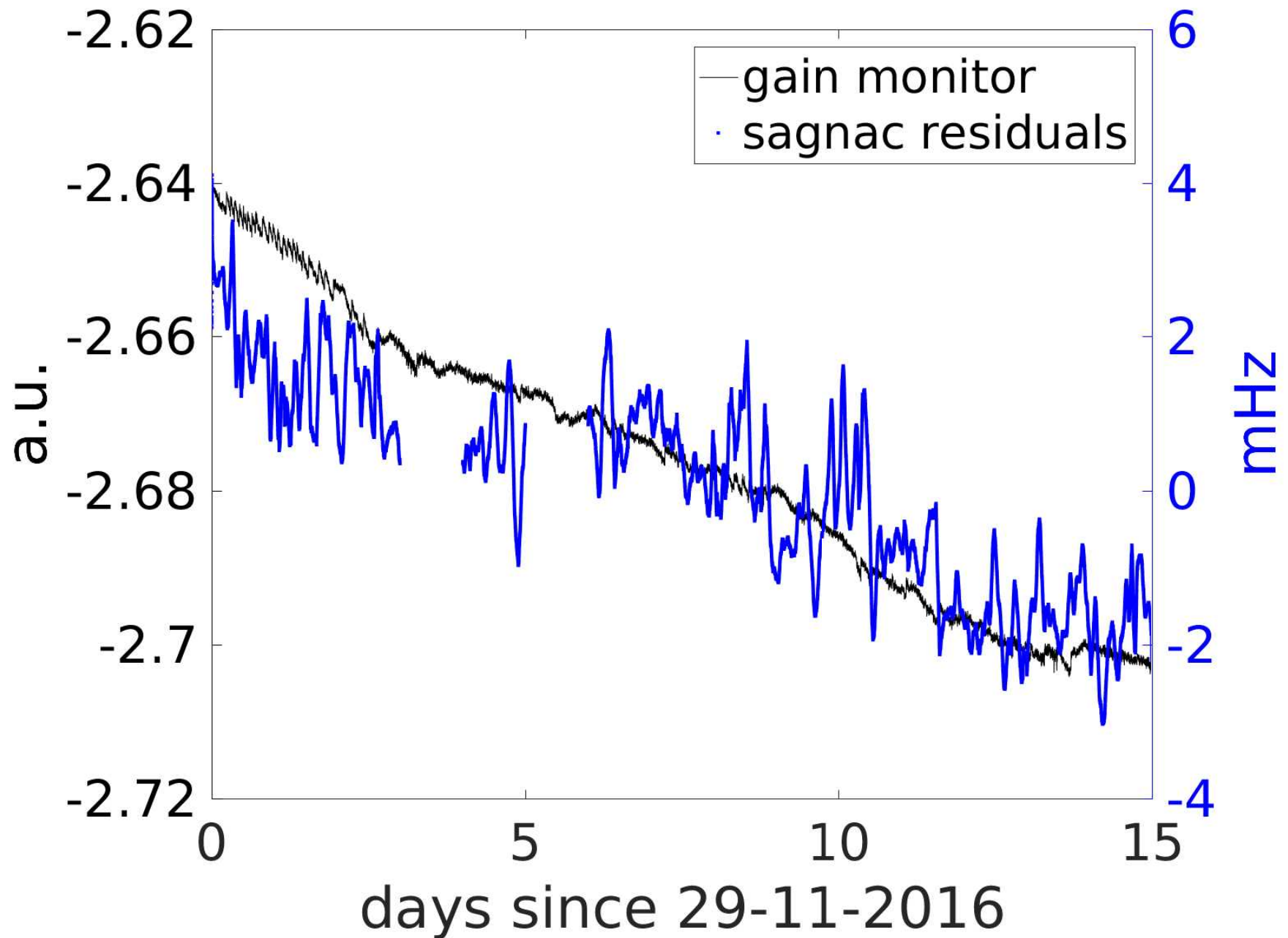
Noise limits:

- Laser optical frequency fluctuations
- Residual fluctuation in the ambient temperature and pressure
- Local Tilts (to be investigated)

Preliminary analysis of the November 2016 RUN



Losses monitor and Sagnac residuals





Present stability determination is in progress...



Conclusion



RING laser gyros are approaching the resolution of $10^{-9} \Omega_E$ (impact on GEODESY)

Ground based Tests of GR are under study
(Multi axial / Multi-site approach are considered)

