## Exotic quarks from composite models

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## Outline

- Introduction
- Composite models
- Production of excited composite quarks at LHC
- Signal and background study
- Bounds from recasting an experimental analysis


## The Standard Model, its shortcomings and extensions

The Standard Model


Shortcomings of SM
It can not accomodate

- neutrino masses
- gravitational interaction
- dark matter
- matter-antimatter asymmetry
- The fermions are the foundamental blocks of the matter
- The bosons mediate the interactions
- The standard model had great success in describing the experimental observations
- However it has some shortcomings


## Extensions of SM

- GUT
- String theory
- Supersymmetry
- Extra-dimensions
- Composite models


## Composite model for quarks and leptons

- Compositness of leptons and quarks is one possible scenario beyond the Standard Model
- In a composite scenario fermions are assumed to have an internal substructure.
- In a composite scenario we expect to observe excited leptons and quarks
- In general the following parameters are introduced:
- $m_{*}$ : mass of the excited states
- $\wedge$ : Energy scale at which the internal substructure becomes manifest In our study we will use the parameterization $m_{*}=\Lambda$


## Extended weak isospin model

- It describes the excited states trough the weak isospin symmetry
- It doesn't refer to the internal dynamics
- Analogy with strong isospin $\rightarrow$ prediction of hadronic states before the discovery of quarks and gluons
- $\operatorname{SM} q, \ell \in I_{W}=0,1 / 2$ e $W^{ \pm}, Z, \gamma \in I_{W}=0,1$
$\Rightarrow$ excited fermions $\in I_{W} \leq 3 / 2$

| $I_{W}$ | Multiplet | $Q$ | $Y$ |
| :---: | :---: | :---: | :---: |
| 0 | $L^{-}$ | -1 | -2 |
| $\frac{1}{2}$ | $\mathbf{L}=\binom{L^{0}}{L^{-}}$ | 0 | -1 |
|  | -1 |  |  |
| $\mathbf{1}$ | $\mathbf{L}=\left(\begin{array}{c}L^{0} \\ L^{-} \\ L^{--}\end{array}\right.$ | 0 <br> -1 <br> -1 | -2 |
| -2 | $\mathbf{L}=\left(\begin{array}{c}L^{+} \\ L^{0} \\ L^{-} \\ L^{--}\end{array}\right)$ | 1 <br> 0 <br> -1 <br> -2 | -1 |


| IW | Multiplet | Q | Y |
| :---: | :---: | :---: | :---: |
| 0 | U | 2/3 | 4/3 |
| 0 | D | -1/3 | -2/3 |
| $\frac{1}{2}$ | $\Psi=\binom{U}{D}$ | $\begin{gathered} \hline 2 / 3 \\ -1 / 3 \\ \hline \end{gathered}$ | 1/3 |
| 1 | $U=\left(\begin{array}{c}U^{+} \\ U \\ D\end{array}\right)$ | $\begin{gathered} 5 / 3 \\ 2 / 3 \\ -1 / 3 \\ \hline \end{gathered}$ | 4/3 |
| 1 | $D=\left(\begin{array}{c}U \\ D \\ D^{-}\end{array}\right)$ | $\begin{gathered} \hline 2 / 3 \\ 1 / 3 \\ -4 / 3 \\ \hline \end{gathered}$ | -2/3 |
| $\frac{3}{2}$ | $\Psi=\left(\begin{array}{c}U^{+} \\ U \\ D \\ D^{-}\end{array}\right)$ | $\begin{gathered} 5 / 3 \\ 2 / 3 \\ -1 / 3 \\ -4 / 3 \\ \hline \end{gathered}$ | 1/3 |

## The higher isospin multiplets in the quark sector

- The isospin multiplets with $I_{W}=1$ and $I_{W}=3 / 2$ contain ordinary charged excited quarks ( $U, D$ ) and exoticly charged excited quarks ( $U^{+}, D^{-}$)
- The higher isospin multiplets contribute solely to the iso-vector current and do not contribute to the hypercharge current
- The exoticly charged excited quarks interact with the standard model fermions only via $W^{+}$and $W^{-}$gauge bosons
- Because all gauge fields carry no hypercharge $Y$, a given multiplet couples truogh the gauge field to light multiplet with the same $Y$
- In order to conserve the $S U(2)$ currents, the couplings between excited and ordinary fermions are magnetic moment type transition couplings.
- The lagrangians are:
$\mathcal{L}^{(l W=3 / 2)}=\frac{f_{3} / 2}{\Lambda} \sum_{M, m, m^{\prime}} C\left(\frac{3}{2}, M \mid 1, m ; \frac{1}{2}, m^{\prime}\right) \times\left(\bar{\Psi}_{M} \sigma_{\mu \nu} q_{L m^{\prime}}\right) \partial^{\nu}\left(W^{m}\right)^{\mu}+$ h.c.
$\mathcal{L}^{(l / w=1)}=\frac{g f_{1}}{\Lambda} \sum_{m=-1,0,1}\left[\left(\bar{U}_{m} \sigma_{\mu \nu} u_{R}\right)+\left(\bar{D}_{m} \sigma_{\mu \nu} d_{R}\right)\right] \partial^{\nu}\left(W^{m}\right)^{\mu}+$ h.c.
( $g$ is the $S U(2)$ coupling, $f_{1}, f_{3 / 2}=1, C$ are the Clebsch-Gordan coefficients, we assume $\Lambda=m_{*}$ ).


## Production process for $\mathrm{U}^{+}$

- For the $u u \rightarrow U^{+} d$ sub-process we have $t$ and $u$-channel
- For the $u \bar{d} \rightarrow U^{+} \bar{u}$ sub-process we have $s$ and $t$-channel

b)


For the production of $D^{-}$we have a similar situation

## Partonic sub-processes cross sections $\left(I_{W}=1\right)$

The case $I_{W}=1$ is characterized by the absence of the interference between the kinematic channels

$$
\begin{aligned}
\left(\frac{d \hat{\sigma}}{d \hat{t}}\right)_{u u \rightarrow U^{+} d}^{I W=1}= & \frac{1}{4 \hat{s}^{2} m_{*}^{2}} \frac{g^{4} f_{1}^{2}}{16 \pi} \frac{\hat{t}}{\left(\hat{t}-M_{W}^{2}\right)^{2}}\left[m_{*}^{2}\left(\hat{t}-m_{*}^{2}\right)+2 \hat{s} \hat{u}+m_{*}^{2}(\hat{s}-\hat{u})\right] \\
& +\frac{1}{4 \hat{s}^{2} m_{*}^{2}} \frac{g^{4} f_{1}^{2}}{16 \pi} \frac{u}{\left(\hat{u}-M_{W}^{2}\right)^{2}}\left[m_{*}^{2}\left(\hat{s}-m_{*}^{2}\right)+2 \hat{t} \hat{u}+m_{*}^{2}(\hat{t}-\hat{u})\right] \\
\left(\frac{d \hat{\sigma}}{d \hat{t}}\right)_{u \bar{d} \rightarrow U^{+} \bar{u}}^{I W=1}= & \frac{1}{4 \hat{s}^{2} m_{*}^{2}} \frac{g^{4} f_{1}^{2}}{16 \pi} \frac{\hat{s}}{\left(\hat{s}-M_{W}^{2}\right)^{2}}\left[m_{*}^{2}\left(\hat{s}-m_{*}^{2}\right)+2 \hat{t} \hat{u}+m_{*}^{2}(\hat{t}-\hat{u})\right] \\
& +\frac{1}{4 \hat{s}^{2} m_{*}^{2}} \frac{g^{4} f_{1}^{2}}{16 \pi} \frac{\hat{t}}{\left(\hat{t}-M_{W}^{2}\right)^{2}}\left[m_{*}^{2}\left(\hat{t}-m_{*}^{2}\right)+2 \hat{s} \hat{u}+m_{*}^{2}(\hat{s}-\hat{u})\right]
\end{aligned}
$$

## Partonic sub-processes cross sections ( $I_{W}=3 / 2$ )

The case $I_{w}=3 / 2$ is characterized by nonzero interference between the kinematic channels

$$
\begin{aligned}
\left(\frac{d \hat{\sigma}}{d \hat{t}}\right)_{u u \rightarrow U^{+} d}^{I W=3 / 2}= & \frac{1}{4 \hat{s}^{2} m_{*}^{2}} \frac{g^{4} f_{3 / 2}^{2}}{16 \pi} \frac{\hat{t}}{\left(\hat{t}-M_{W}^{2}\right)^{2}}\left[m_{*}^{2}\left(\hat{t}-m_{*}^{2}\right)+2 \hat{s} \hat{u}-m_{*}^{2}(\hat{s}-\hat{u})\right] \\
& +\frac{1}{4 \hat{s}^{2} m_{*}^{2}} \frac{g^{4} f_{3 / 2}^{2}}{16 \pi} \frac{\hat{u}}{\left(\hat{u}-M_{W}^{2}\right)^{2}}\left[m_{*}^{2}\left(\hat{u}-m_{*}^{2}\right)+2 \hat{s} \hat{t}-m_{*}^{2}(\hat{s}-\hat{t})\right] \\
& +\frac{1}{4 \hat{s}^{2} m_{*}^{2}} \frac{g^{4} f_{3 / 2}^{2}}{16 \pi} \frac{1}{\left(\hat{u}-M_{W}^{2}\right)} \frac{1}{\left(\hat{t}-M_{W}^{2}\right)}\left(\hat{s} \hat{t} \hat{u}+\frac{3}{8} \hat{u} \hat{t} m_{*}^{2}\right) \\
\left(\frac{d \hat{\sigma}}{d \hat{t}}\right)_{u \bar{d} \rightarrow U^{+} \bar{u}}^{I_{W}=3 / 2}= & \frac{1}{4 \hat{s}^{2} m_{*}^{2}} \frac{g^{4} f_{3 / 2}^{2}}{16 \pi} \frac{\hat{s}}{\left(\hat{s}-M_{W}^{2}\right)^{2}}\left[m_{*}^{2}\left(\hat{s}-m_{*}^{2}\right)+2 \hat{t} \hat{u}-m_{*}^{2}(\hat{t}-\hat{u})\right] \\
& +\frac{1}{4 \hat{s}^{2} m_{*}^{2}} \frac{g^{4} f_{3 / 2}^{2}}{16 \pi} \frac{\hat{t}}{\left(\hat{t}-M_{W}^{2}\right)^{2}}\left[m_{*}^{2}\left(\hat{t}-m_{*}^{2}\right)+2 \hat{s} \hat{u}-m_{*}^{2}(\hat{s}-\hat{u})\right] \\
& +\frac{1}{4 \hat{s}^{2} m_{*}^{2}} \frac{g^{4} f_{3 / 2}^{2}}{16 \pi} \frac{1}{\left(\hat{s}-M_{W}^{2}\right)} \frac{1}{\left(\hat{t}-M_{W}^{2}\right)}\left(\hat{s} \hat{t} \hat{u}+\frac{3}{8} \hat{s} \hat{t} m_{*}^{2}\right)
\end{aligned}
$$

## Production cross section

$\sigma=\sum_{a, b} \int_{\frac{m^{* 2}}{s}}^{1} d \tau \int_{\tau}^{1} \frac{d x}{x} f_{a}(x, \hat{Q}) f_{b}\left(\frac{\tau}{x}, \hat{Q}\right) \hat{\sigma}\left(\tau s, m_{*}\right)$
$\left(\hat{\sigma}\right.$ : partonic cross section calculated in the center of mass frame, $f_{a}$ : partonic distribution function, $x$ : longitudinal partonic momentum fraction, $\hat{Q}$ : factorization scale.)





The bands correspond to the varition of the factorization scale from $\hat{Q}=M_{W}$ to $\hat{Q}=m_{*}$

The production of $U^{+}$has a larger cross section because this process involves sub-processes with $u$ quarks in the initial state, that is the most available quark in the proton.

## Excited quarks decay and final signature

$U^{+} \rightarrow W^{+} u$
$\Gamma=\alpha \frac{f^{2}}{\sin ^{2} \theta_{w}} \frac{m_{*}}{8}\left(2+\frac{M_{w}^{2}}{m_{*}^{2}}\right)\left(1-\frac{M_{w}^{2}}{m_{*}^{2}}\right)^{2}$


We consider the decay chain $Q \rightarrow W^{+} q \rightarrow \ell^{+} \nu q$
$\Rightarrow$ The final signature is $\ell^{+} \not \phi_{T} j j$
This signature can be given by the processes:
$p p \rightarrow U^{+} j \rightarrow W^{+} j j \rightarrow \ell^{+} \not{ }_{T}{ }^{\top} j j$
$p p \rightarrow \bar{D}^{-} j \rightarrow W^{+} j j \rightarrow \ell^{+} \not \phi_{T} j j$
$p p \rightarrow U j \rightarrow W^{+} j j \rightarrow \ell^{+} \not{ }_{T} j j$
$p p \rightarrow \bar{D} j \rightarrow W^{+} j j \rightarrow \ell^{+} ధ_{T} j j$
All these contributions are included in the simulations

## Contributions to the final signature

The $U^{+}$and $\bar{D}^{-}$interact with the SM Gauge boson $W$, the $U$ and $\bar{D}$ interact with the SM gauge bosons $W, Z, \gamma$ :

- The $U^{+}$and $\bar{D}^{-}$contribute to $W q q$ channel with branching ratio $\mathcal{B}\left(Q \rightarrow W^{+} q\right)=1$, while the $U$ and $\bar{D}$ with $\mathcal{B}\left(Q \rightarrow W^{+} q\right) \approx 0.22$
- The $U$ and $\bar{D}$ production happen with diagrams involving all the SM gauge bosons, this enhances these contributions

$$
I_{W}=1
$$

$$
I_{W}=3 / 2
$$

| $m_{*}$ <br> $(\mathrm{GeV})$ | $U^{+}$ <br> $(\mathrm{fb})$ | $U$ <br> $(\mathrm{fb})$ | $\bar{D}$ <br> $(\mathrm{fb})$ | $\bar{D}^{-}$ <br> $(\mathrm{fb})$ | $\sigma_{\mathrm{tot}}\left(e^{+} p_{T j j}\right)$ <br> $(\mathrm{fb})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 500 | 7782.0 | 6303.0 | 2594.0 | 2679.0 | 19358.0 |
| 1000 | 1277 | 978 | 329.4 | 357.3 | 2941.7 |
| 1500 | 344.6 | 250.30 | 73.390 | 90.400 | 758.69 |
| 2000 | 107.7 | 74.580 | 23.370 | 28.330 | 233.98 |
| 2500 | 39.05 | 24.740 | 8.689 | 9.1740 | 81.653 |
| 3000 | 13.5 | 9.5770 | 4.043 | 2.459 | 29.579 |
| 3500 | 4.281 | 3.612 | 1.119 | 0.7004 | 9.7124 |
| 4000 | 1.424 | 1.3470 | 0.2401 | 0.2161 | 3.2272 |
| 4500 | 0.4957 | 0.4958 | 0.06098 | 0.06365 | 1.11613 |
| 5000 | 0.1799 | 0.18530 | 0.01819 | 0.0211 | 0.4045 |


| $m_{*}$ <br> $(\mathrm{GeV})$ | $U^{+}$ <br> $(\mathrm{fb})$ | $U$ <br> $(\mathrm{fb})$ | $\bar{D}$ <br> $(\mathrm{fb})$ | $\bar{D}^{-}$ <br> $(\mathrm{fb})$ | $\sigma_{\text {tot }}\left(e^{+} \not p_{T} j j\right)$ <br> $(\mathrm{fb})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 500 | 11080 | 3446.0 | 1506.0 | 477.60 | 16509.6 |
| 1000 | 2240 | 623.70 | 151.30 | 47.46 | 3062.46 |
| 1500 | 806.3 | 203.20 | 28.750 | 8.8000 | 1047.05 |
| 2000 | 343.2 | 82.890 | 6.3130 | 1.954 | 434.357 |
| 2500 | 159.9 | 40.760 | 1.7260 | 0.5253 | 202.911 |
| 3000 | 60.25 | 24.130 | 0.44890 | 0.15880 | 84.9877 |
| 3500 | 23.55 | 8.5430 | 0.12390 | 0.053250 | 32.2702 |
| 4000 | 9.347 | 2.0480 | 0.03894 | 0.018810 | 11.4527 |
| 4500 | 3.191 | 0.6354 | 0.01335 | 0.006457 | 3.84621 |
| 5000 | 1.043 | 0.2034 | 0.004864 | 0.002433 | 1.2537 |

## Analysis structure

- Partonic processes simulation (CalcHEP)
- $m^{*} \in[500,5000] \mathrm{GeV}$ with steps of 250 GeV
- 100000 events per sample
- Study of the kinematic variables $\rightarrow$ kinematic cuts
- Simulation of detector effects (DELPHES): efficiency, resolution, geometrical acceptance etc.
- Study of the statistical significance


## Kinematical cuts

- The main background is the process $p p \rightarrow W_{j j} \rightarrow \ell^{+} p_{T} j j$
- We want to find kinematical cuts that can separate the signal and the backround




- We can separate signal and background with the cuts $p_{T}(j 1) \geq 180 \mathrm{GeV} \quad p_{T}(j 2) \geq 100 \mathrm{GeV}$


## Transverse mass

- One of the decay product of the excited quark is a neutrino
- For neutrinos it is not possible to reconstruct the longitudinal momentum
- therefore it is not possible to exactly reconstruct the excited quark mass
- we can reconstruct the transverse mass

The transverse mass is defined in terms of the reconstructed trensverse momentum of the $W$ gauge boson ( $p_{T W}=p_{T \ell}+p_{T \nu}$ ) and the transverse momentum of the leading jet: $M_{T}^{2}=\left(\sqrt{p_{T W}^{2}+M_{W}^{2}}+p_{T j 1}\right)^{2}-\left(p_{T W}+p_{T j 1}\right)^{2}$


The transverse mass distribution shows a peak with a relatively sharp end-point at $M_{T} \approx m_{*}$

## Excited quark reconstructed mass (with approximation)

We can still reconstruct the invariant mass of the exotic quark to some degree of accuracy

- We start from the conservation of four-momento: $M_{W}^{2}=\left(p_{\ell}+p_{\nu}\right)^{2}$
- From it we obtain a second-order equation for $p_{L}^{\nu}$
- Among the two solutions we select the one that gives the more central (smaller pseudorapidity) $W$
- Now we can reconstruct the invariant mass $M_{\ell \nu_{\ell} j_{1}}$


The $M_{\ell \nu_{\ell j_{1}}}$ distribution has a clear peak in correspondence of the excited quark mass

## Reconstruction and selection efficiencies

## Selection:

2 jets and 1 lepton with
$p_{T}(j 1) \geq 180 \mathrm{GeV}$,
$p_{T}(j 2) \geq 100 \mathrm{GeV}$

| Background |  |  |  |
| :---: | :---: | :---: | :---: |
|  | $\sigma_{b}$ before cut (fb) | $\sigma_{b}$ after cut (fb) | $\left(\epsilon_{6}\right)$ |
|  | 8200000 | 14678 | 0.00179 |
| Signal ( $\left.I_{W}=1\right)$ |  |  |  |
| m. (GeV) | $\sigma_{x}$ before cut (fb) | $\sigma_{x}$ after cut (fb) | $\left(\epsilon_{x}\right)$ |
| 500 | 19358 | 12213.1 | 0.630906 |
| 1000 | 2941.7 | 2367.87 | 0.804931 |
| 1500 | 758.69 | 643.786 | 0.848549 |
| 2000 | 233.98 | 203.191 | 0.868412 |
| 2500 | 81.653 | 71.5896 | 0.876754 |
| 3000 | 29.579 | 26.1131 | 0.882824 |
| 3500 | 9.7124 | 8.6383 | 0.88941 |
| 4000 | 3.2272 | 2.87522 | 0.890934 |
| 4500 | 1.11613 | 0.994357 | 0.890897 |
| 5000 | 0.4045 | 0.362569 | 0.896339 |
| Signal ( $I_{W}=3 / 2$ ) |  |  |  |
| $m_{\text {, }}$ (GeV) | $\sigma_{x}$ before cut (fb) | $\sigma_{x}$ after cut (fb) | $\left(\epsilon_{n}\right)$ |
| 500 | 16509.6 | 8888.19 | 0.538365 |
| 1000 | 3062.46 | 2257.67 | 0.737208 |
| 1500 | 1047.05 | 841.233 | 0.803432 |
| 2000 | 434.357 | 358.925 | 0.826336 |
| 2500 | 202.911 | 169.963 | 0.837622 |
| 3000 | 84.9877 | 73.1053 | 0.860187 |
| 3500 | 32.2702 | 27.4566 | 0.850835 |
| 4000 | 11.4527 | 9.31689 | 0.813507 |
| 4500 | 3.84621 | 3.13297 | 0.814562 |
| 5000 | 1.2537 | 1.01801 | 0.812003 |

## Statistical significance study

Statistical Significance: $S=\frac{N_{s}}{\sqrt{N_{s}+N_{b}}}$, with $N_{s}=L \sigma_{s} \epsilon_{s}, N_{b}=L \sigma_{b} \epsilon_{b}$ Luminosity needed to have a given $S: L=\frac{S^{2}}{\sigma_{s} \epsilon_{s}}\left[1+\frac{\sigma_{b} \epsilon_{b}}{\sigma_{s} \epsilon_{s}}\right]$


|  | $3-\sigma$ | $5-\sigma$ |
| :---: | :---: | :---: |
| $\mathrm{L}\left(\mathrm{fb}^{-1}\right)$ | $m \cdot(\mathrm{GeV})$ | $m \cdot(\mathrm{GeV})$ |
| 30 | $2570+50-30$ | $2330+40-30$ |
| 300 | $3130+50-40$ | $2890+60-40$ |
| 3000 | $3630+50-40$ | $3420+60-50$ |



|  | $3-\sigma$ | $5-\sigma$ |
| :---: | :---: | :---: |
| $\mathrm{L}\left(\mathrm{fb}^{-1}\right)$ | $m_{\boldsymbol{*}}(\mathrm{GeV})$ | $m_{*}(\mathrm{GeV})$ |
| 30 | $3140+70-50$ | $2820+50-40$ |
| 300 | $3730+40-50$ | $3450+50-50$ |
| 3000 | $4260+30-50$ | $4035+30-30$ |

## Recast of an experimental analysis

We give bounds on the excited quarks in $I_{W}=1,3 / 2$ multiplets by recasting results from CMS-PAS-B2G-12-016

## CMS-PAS-B2G-12-016

- Search for exotic light flavour quark partners
- $\sqrt{s}=8 \mathrm{TeV}$
- $19.6 \mathrm{fb}^{-1}$
- We compare the observed limit on $\sigma(p p \rightarrow D q) \times \mathcal{B}(D \rightarrow Z q)$ of the experimental analysis with the prediction of our model
- In our model this signature is produced by the states $D, \bar{D}, U, \bar{U}$


$$
\begin{gathered}
I_{W}=1 \rightarrow m_{*}>1150 \mathrm{GeV} \\
I_{W}=3 / 2 \rightarrow m_{*}>1710 \mathrm{GeV}
\end{gathered}
$$

## Conclusions

This is the first study of the production at the LHC of the excited quarks which appear in composite models with weak isospin multiplets $I_{W}=1$ and $I_{W}=3 / 2$

- Cross section for excited quarks
- Implementation of the magnetic type Gauge interactions in the CalcHEP generator
- Fast simulation of the detector reconstruction for signal and relevant background based on DELPHES
- Luminosity curves as function of $m_{*}$ for $S=3$ and $S=5$
- Bound on the excited quark mass by recasting an experimental analysis

Future improvement of the study:

- The two dimensional parameter space ( $\Lambda, m_{*}$ ) could be fully explored
- The effect of expected contact interaction should be taken into account

