

# Predictions for single-diffractive Drell-Yan production at the LHC at 13 TeV

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\*We acknowledge Dipartimento di Fisica e Geologia,  
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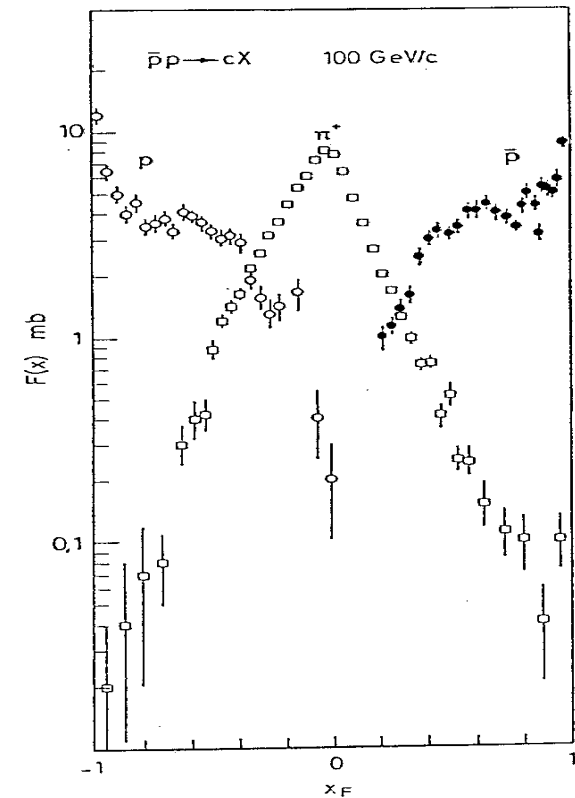
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## Outline

- Forward particle production in  $pp$  and  $ep$  collisions
- Hard diffraction in DIS : factorisation and evolution
- Factorisation tests at HERA
- Diffractive PDFs from combined HERA proton-tagged data
- Single-diffractive Drell-Yan pair production : a case study at hadron colliders
- Factorisation breaking effects vs  $Q^2$ ,  $\sqrt{s}$ ...

## The leading particle effect in hadronic collisions

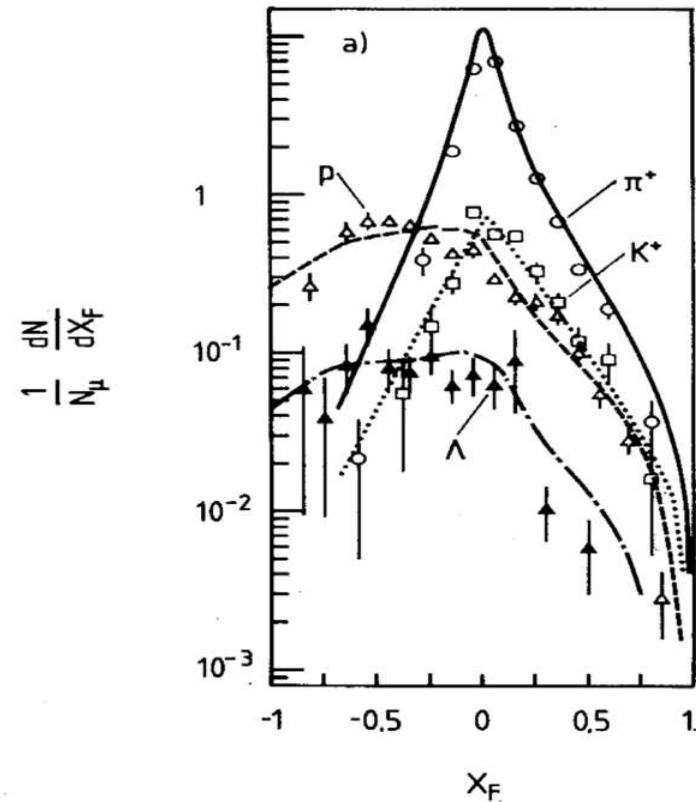
- particle production in hadronic collisions:  
 $\bar{p}p \rightarrow c + X$
- $x_F = 2p_{||}/\sqrt{s}$  in hadronic centre of mass
- **Leading particle effect** : privileged quark-flavour quantum number flow from the initial state particle to the final state one
- the more the quark-flavour content is conserved from initial to final state hadron  $c$ , the more the latter carries a substantial fraction of the energy available in the reaction:  $d\sigma \sim (1 - x_F)^n$
- Mesons don't show LPE
- **However, no large momentum transfer  $\rightarrow$  pQCD not applicable**



Basile & al. '81

## The leading particle effect in DIS

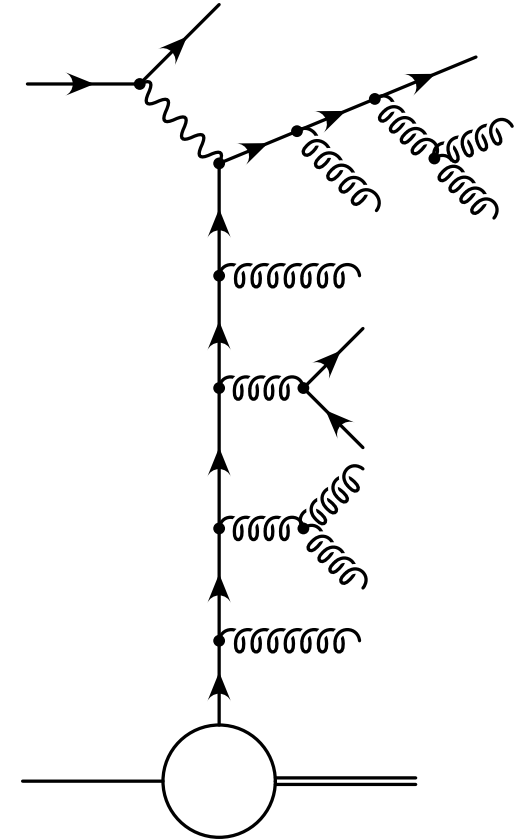
- Same effect observed in DIS
- $\mu p \rightarrow \mu + h + X$ , DIS@280 GeV
- Same pattern as in hadronic collisions
- LPE for backward proton (uud) and  $\Lambda$  (uds)
- No LPE for  $\bar{\Lambda}$  ( $\bar{u}\bar{d}\bar{s}$ ),  $\bar{p}$  ( $\bar{u}\bar{u}\bar{d}$ ) and mesons
- But here an hard scale is present,  
 $Q^2 \gg \Lambda_{QCD}^2$ , pQCD analysis is possible:
  - $\Lambda$  production : F.A.C. *EPJ* **C73** (2013) 2435
  - $n$  production : F.A.C. *EPJ* **C74** (2014) 3029



EMC Coll. '81

## Fragmentation in SIDIS

- Deep Inelastic Scattering event in which a virtual photon interacts with a parton cascade in the nucleon
- Define  $t = (P - p_h)^2$
- $t \sim Q^2$  current fragmentation :  $d\sigma \propto f \otimes D$
- $0 \ll t \ll Q^2$  central region: higher order corrections, current/target separation depends on factorisation scale
- $t \sim 0$  target fragmentation :  $d\sigma \propto M$ , fracture functions (Trentadue, Venaziano '94)



## Hard diffraction in DIS

- **Experiment**

- (hard) diffraction rebirth at HERA
- $e(k) + p(P) \rightarrow e(k') + p(P') + X$

- **kinematics**

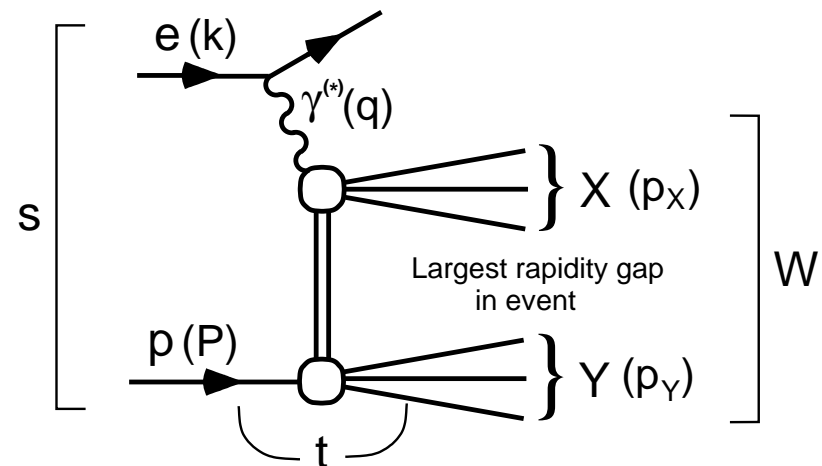
- proton fragmentation region
- $|t| \leq 1 \text{ GeV}^2$
- $x_{\mathbb{P}} \simeq 1 - E_{P'}/E_P < 0.1$

- **diffractive selection:**

- large rapidity gap
- $M_X$ -method
- proton tagging

- **Key features**

- Leading twist:  $\mathcal{O}(Q^{-4})$  (as iDIS)
- scaling violations of diffractive structure functions  $\rightarrow$  parton dynamics



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## Theory setup in DDIS

- Hard-scattering factorisation:

$$F_k^{D(3)}(\beta, Q^2, x_{\mathcal{P}}) = \sum_i \int_{\beta}^1 \frac{d\xi}{\xi} f_i^D(\beta, \mu_F^2; x_{\mathcal{P}}) C_{ki}\left(\frac{\beta}{\xi}, \frac{Q^2}{\mu_F^2}, \alpha_s(\mu_R^2)\right) + \mathcal{O}\left(\frac{1}{Q^2}\right)$$

Grazzini, Trentadue, Veneziano'98, Collins '98

- $C_{ki}$  ( $k = 2, L$ ) calculable as a power expansion  $\alpha_s$ , same as in iDIS
- Diffractive parton distributions:  $f_i^D(\beta, \mu_F^2, x_{\mathcal{P}})$
- Partonic structure of the colourless exchange
- DPDFs obey DGLAP evolution equations (for  $t$  integrated up to  $t_{max} \ll Q^2$ )

$$Q^2 \frac{\partial f_i^D(\beta, Q^2, x_{\mathcal{P}})}{\partial Q^2} = \frac{\alpha_s(Q^2)}{2\pi} \int_{\beta}^1 \frac{du}{u} P_{ji}(u) f_j^D\left(\frac{\beta}{u}, Q^2, x_{\mathcal{P}}\right)$$

- Phenomenological analyses of DPDFs via pQCD fits of DDIS data

## Factorisation in hard diffraction: overview

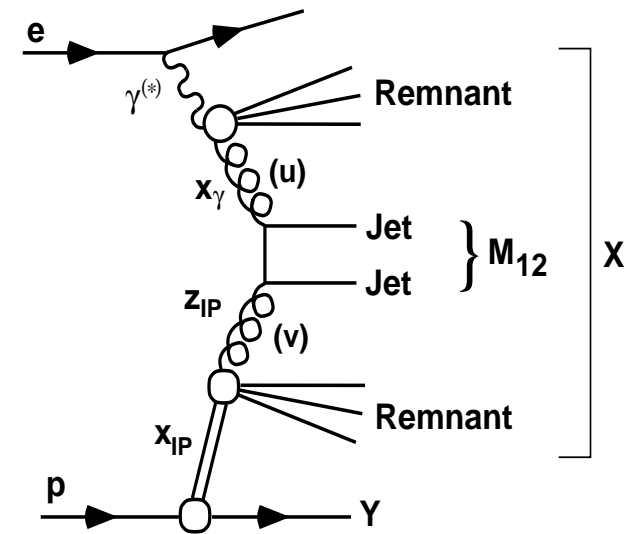
- Diffractive PDFs have been used to test hard-scattering factorisation in

- dijet in DIS at HERA
- dijet in PHP at HERA ( $Q^2 \simeq 0$ ,  $E_T \sim 5, 6$  GeV)
- dijet and electroweak boson production in  $p\bar{p}$  collisions at Tevatron

- Results:

- dijet in DIS:  $\text{data/NLO} \simeq 1$
- dijet in PHP: **debated**  
H1 reports violation:  $\text{data/NLO} \simeq 0.5$   
ZEUS consistent with no violation:  $\text{data/NLO} \simeq 1$
- $p\bar{p}$  : **Striking** breakdown observed at Tevatron:  $\text{data/NLO} \simeq 0.1$

- NB: Factorisation **predicted to fail** in Resolved PHP and hadronic collisions





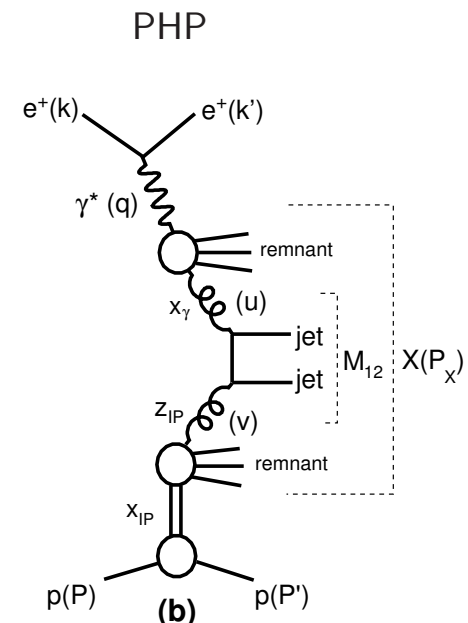
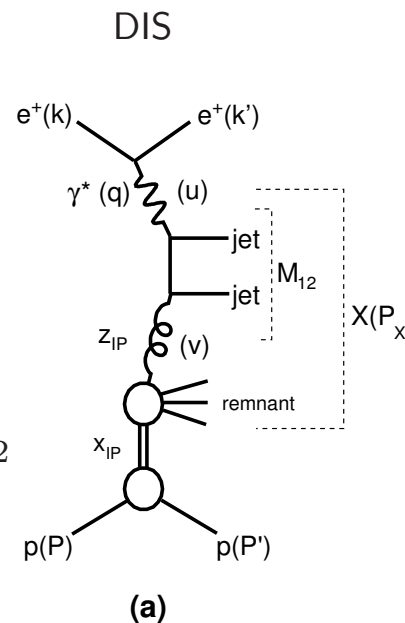
## Most recent factorisation tests at HERA

- Focus on the latest H1 results : **JHEP 1505 (2015) 056**

1. Event phase space:  
 PHP :  $Q^2 < 2 \text{ GeV}^2$   
 DIS :  $4 \text{ GeV}^2 < Q^2 < 80 \text{ GeV}^2$
2. diffractive phase space:  
 $0.010 < x_{\mathbb{P}} < 0.024$
3. jet phase space:  
 $E_T^{*\text{jet}1(2)} > 5.5(4.0) \text{ GeV}$

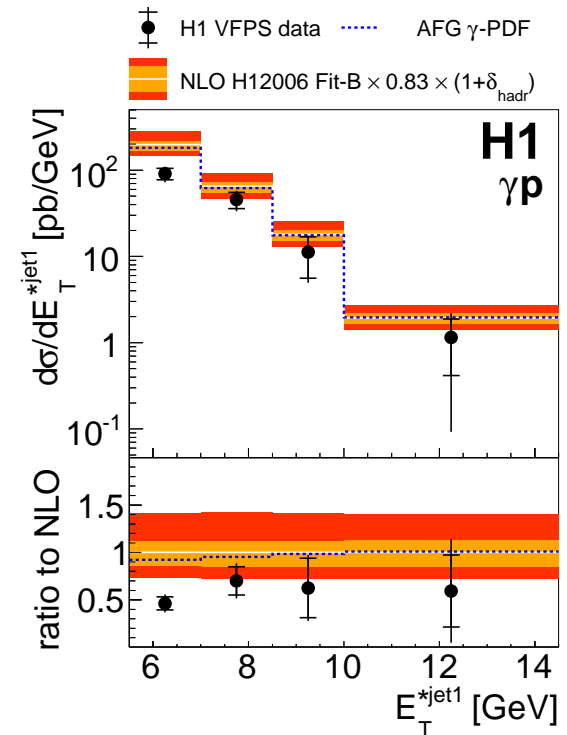
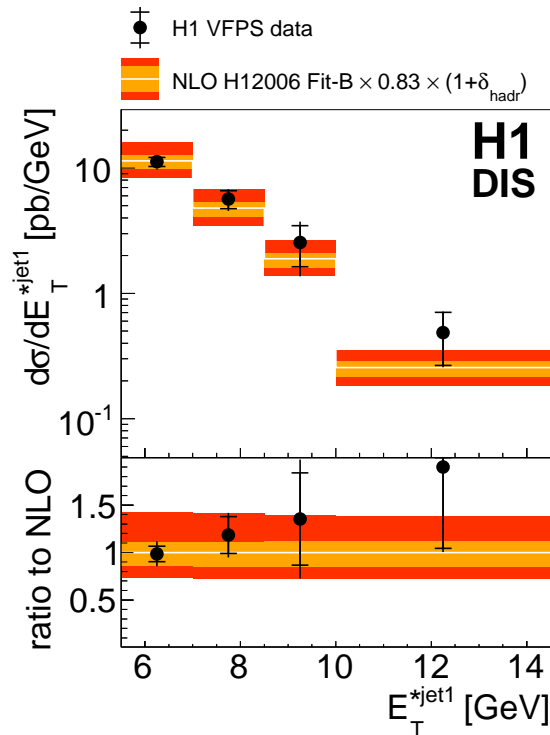
- **Theory**

1. NLO accuracy
2. scale set to  $\mu_R^2 = \mu_F^2 = \langle E_T^{*\text{jet}} \rangle^2 + Q^2$
3. Theo uncertainty:  $\mu \rightarrow 0.5\mu, 2.0\mu$
4. DPDFs from previous H1 '06 analysis



## Results: $E_T^{*jet1}$ distribution

- $E_T^{*jet1}$ :  
leading jet  
transverse energy
- distribution controlled  
by ME :  $E_T^{-4}$
- large NLO corrections
- $E_T$ -dependence  
of the suppression  
not confirmed
- Desiderata:
  - Diffractive PHP at higher  $E_T$  with good statistics



## Results: double ratios

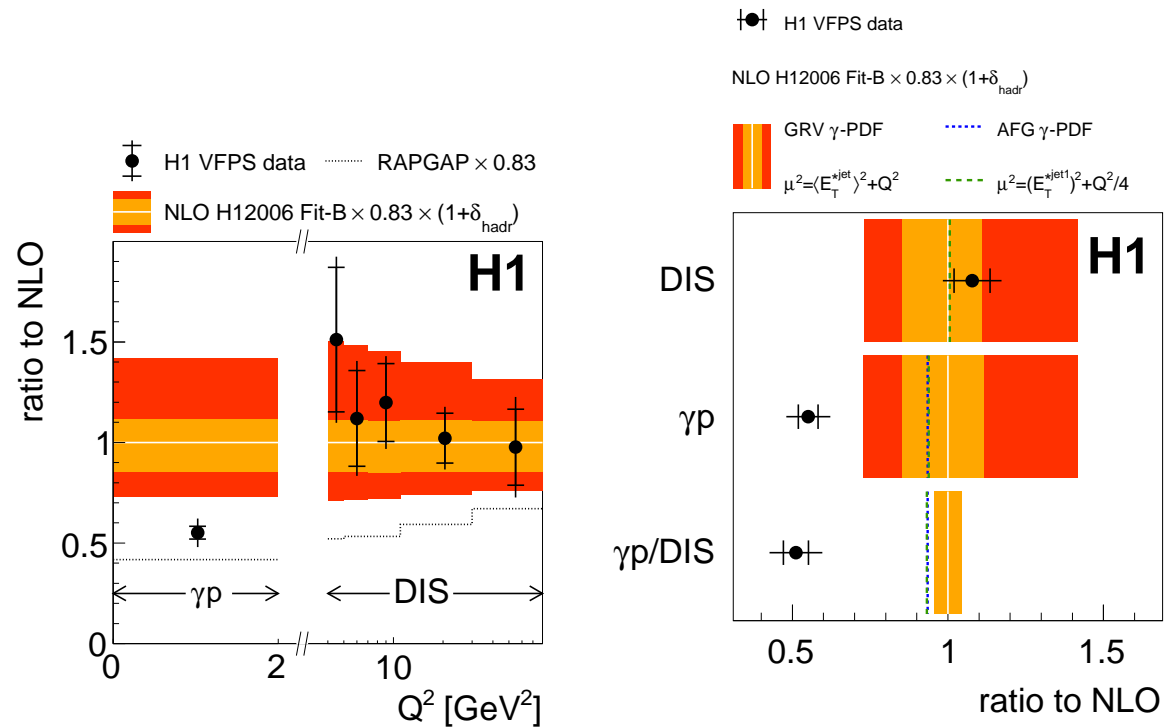
- large NLO corrections:  
jets produced nearly  
at threshold (soft  
gluon resum?)

↳ Consider ratios

- H1 confirms an  
overall suppression  
factor  $\sim 0.5$
- Critical variable:  $Q^2$   
not  $E_T$

Emerging picture:

- ⇒ factorisation **broken** for (spatially extended) hadrons
- ⇒ factorisation **OK** for pointlike probes as the virtual photon



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## diffractive PDFs pQCD fits : status

- Knowledge on DPDFs can be further refined
  - Global fit? LRG+FPS+jets+charm diffractive data from both HERA collaboration
  - Latest fits:
    - \* H1 2006 (iDIS)
    - \* H1 2007 (iDIS+jets)
    - \* ZEUS 2010 (iDIS+jets)
  - gluon DPDF poorly constrained in DDIS: include in the fit diffractive dijet data
- In this talk:
  - QCD analysis of combined H1 and ZEUS proton tagged DDIS data (EPJ '12)
  - cross-calibration: improved precision of the cross section measurements
  - $2.5 < Q^2 < 200 \text{ GeV}^2$
  - $0.00035 < x_P < 0.09$
  - $0.09 < |t| < 0.55 \text{ GeV}^2$  (restricted  $t$ -range to avoid extrapolations)
  - $10^{-3} < \beta < 1$

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## Fitting strategy

### Remarks:

- hard-scattering factorisation holds at fixed values of  $x_{\mathcal{P}}$  and  $t$
- dependence on  $x_{\mathcal{P}}$  and  $t$  fully contained in DPDFs
- these conditional parton distributions are uniquely fixed by the kinematics of the outgoing proton: **DPDFs are, in principle, different for different values of  $x_{\mathcal{P}}$  and  $t$ .**
- Approach exploited in F.A.C and L.Favart arXiv:1205.6356

### H1ZEUS12 data:

- 192 points for  $\sigma_r^{D(3)}(\beta, Q^2, x_{\mathcal{P}}) = F_2^{D(3)}(\beta, Q^2, x_{\mathcal{P}}) - \frac{y^2}{1+(1-y)^2} F_L^{D(3)}(\beta, Q^2, x_{\mathcal{P}})$
- 10  $x_{\mathcal{P}}$  bins, on average 20 points in each  $x_{\mathcal{P}}$  bin  
⇒ too low sensibility to use this approach ⇒ simpler approach

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## Initial condition and pQCD details

Fully factorised ansatz, momentum distributions at  $Q_0^2$ :

$$\begin{aligned}\mathcal{F}(x_{\mathbb{P}}) &= x_{\mathbb{P}}^{f_0} (1 + f_1 x_{\mathbb{P}}^{f_2}), \\ \beta \Sigma(\beta, Q_0^2, x_{\mathbb{P}}) &= \mathcal{F}(x_{\mathbb{P}}) A_q \beta^{B_q} (1 - \beta)^{C_q} (1 + D_q \beta^{E_q}), \\ \beta g(\beta, Q_0^2, x_{\mathbb{P}}) &= \mathcal{F}(x_{\mathbb{P}}) A_g \beta^{B_g} (1 - \beta)^{C_g}.\end{aligned}$$

- $M_\Sigma$ : flavour symmetric singlet distribution
- minimisation performed with MINUIT, stat  $\oplus$  syst errors

pQCD settings @LO

- Evolution and convolution with QCDNUM17 Botje '11
- ZM VFNS scheme
- $m_c = 1.4$  GeV,  $m_b = 4.5$  GeV,  $\alpha_s(M_Z^2) = 0.130$ ,  $Q_0^2 = 1.5$  GeV<sup>2</sup> (tuned)
- $\mu_F^2 = \mu_R^2 = Q^2$
- No  $Q^2$  or  $y$  cuts imposed

## Best-fit results and $\chi^2$ breakdown

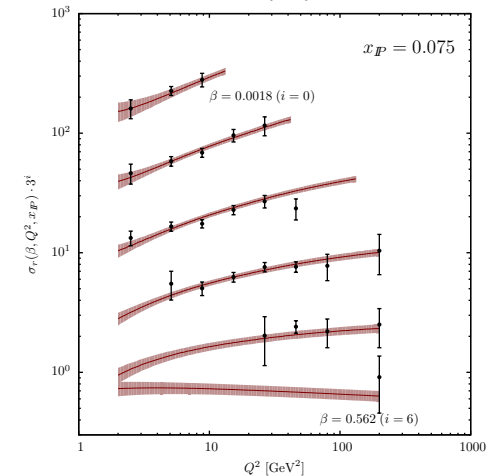
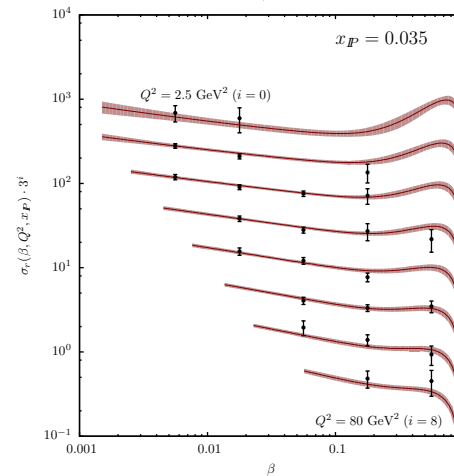
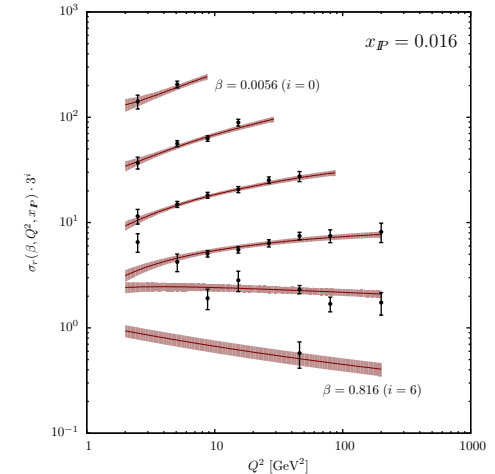
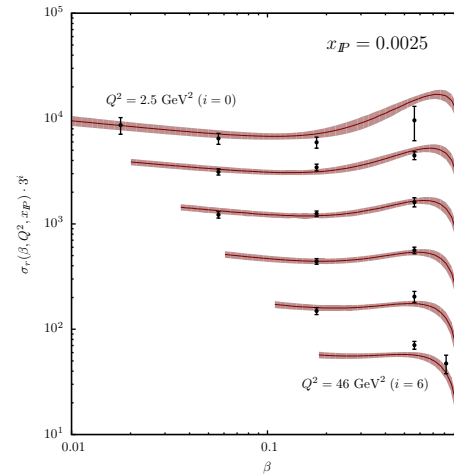
- $C_q$  and  $C_g$  difficult to constrain :  $C_q = C_g = 0.5$ , large  $\beta$  controlled by  $D_q$  and  $E_q$
- mild dependence of  $\chi^2$  on  $Q_0^2$  (tuned)
- $\chi^2/d.o.f = 167/(192 - 9) = 0.91$
- parameters well constrained, no misrepresentation in any  $x_P$  bin

Parameter	$p_i \pm \delta p_i$
$f_0$	$-1.208 \pm 0.022$
$f_1$	$48.2 \pm 11.9$
$f_2$	$1.42 \pm 0.13$
$A_q$	$0.0039 \pm 0.0007$
$B_q$	$-0.237 \pm 0.026$
$C_q$	0.5
$D_q$	$22.6 \pm 2.8$
$E_q$	$2.28 \pm 0.20$
$A_g$	$0.057 \pm 0.011$
$B_g$	$0.41 \pm 0.13$
$C_g$	0.5

$x_P$	$\chi^2$	Fitted points
0.00035	4.44	4
0.0009	6.78	10
0.0025	21.36	16
0.0085	20.34	24
0.0160	20.70	26
0.0250	27.24	25
0.0350	13.85	24
0.0500	28.69	27
0.0750	13.10	26
0.0900	10.51	10
Total	167.0	192

## Best-fit vs combined H1ZEUS12 data

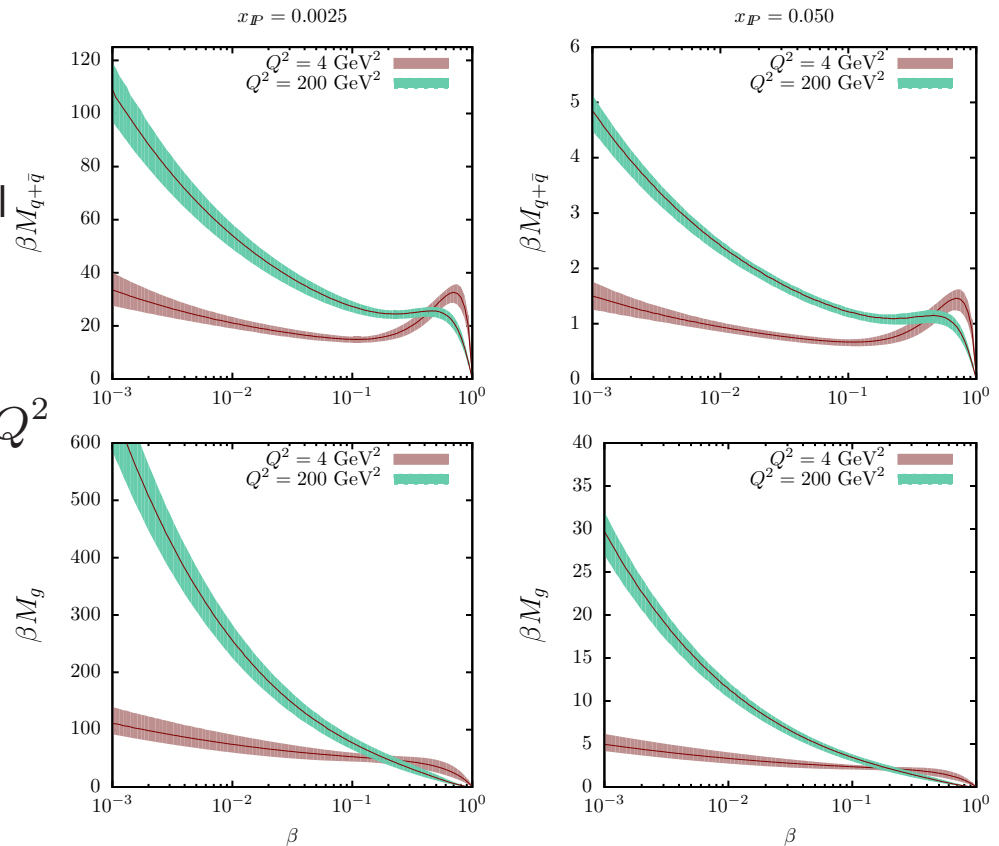
- $\sigma_r$  vs  $\beta$  and  $Q^2$
- the initial condition assumes same  $\beta$ -shape in all  $x_{IP}$ -bins
- this theo bias induces unnatural small error with the standard  $\Delta_\chi^2 = 1$  criterion.
- Allow for more flexibility:  
one  $\chi^2$ -unit for  $x_{IP}$  bin  
 $\rightarrow \Delta_\chi^2 = 10$





## DPDFs evolution

- Singlet and gluon momentum distributions for two different  $x_P$  at different  $Q^2$
- band: propagation of experimental uncertainties with  $\Delta\chi^2 = 10$  (eigenvector method)
- **Singlet (top)**: valence-like at low  $Q^2$
- **Gluon (bottom)**: fast rise with raising  $Q^2$  at low  $\beta$
- Error shrinkage at high  $Q^2$ : effect of pQCD evolution
- Evolution washes away the large- $\beta$  bump



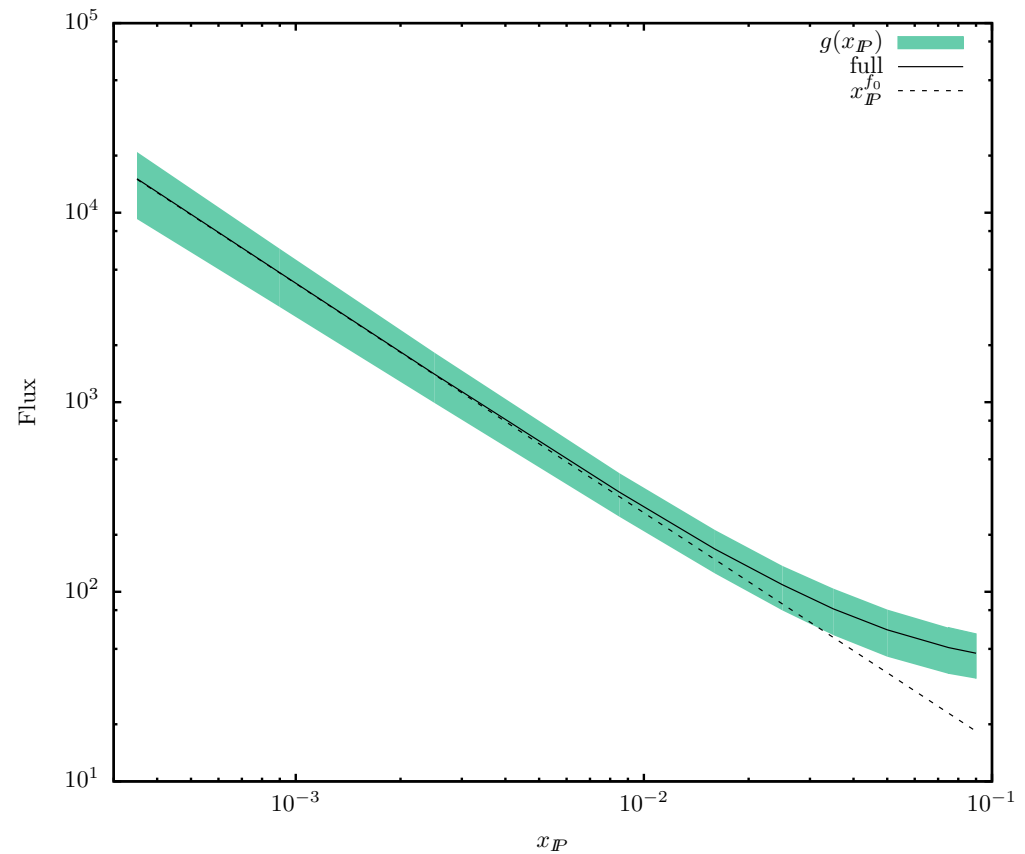
## Flux factor

- flux factor with (solid) and without (dashed)

the **extra power term**:

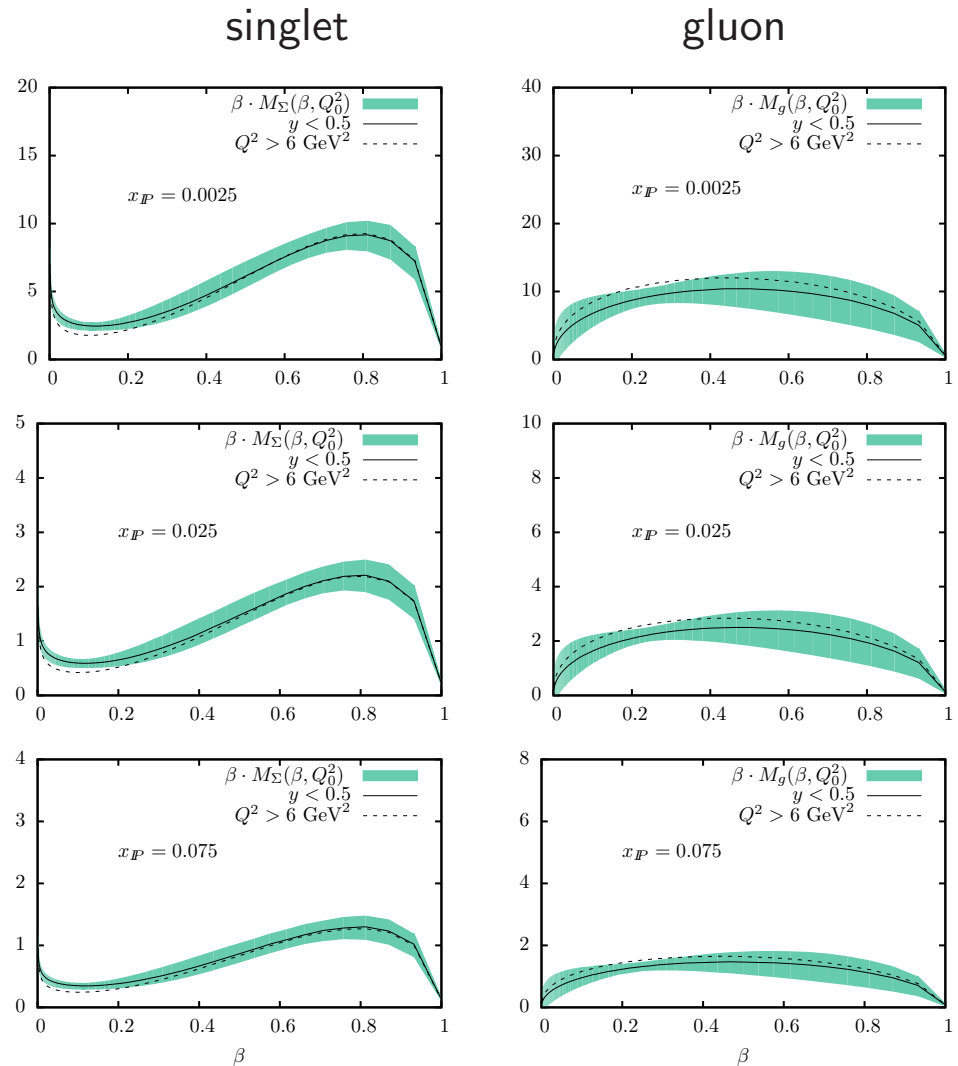
$$\mathcal{F}(x_P) = x_P^{f_0} (1 + f_1 x_P^{f_2})$$

- band = best fit +  $\Delta\chi^2 = 10$



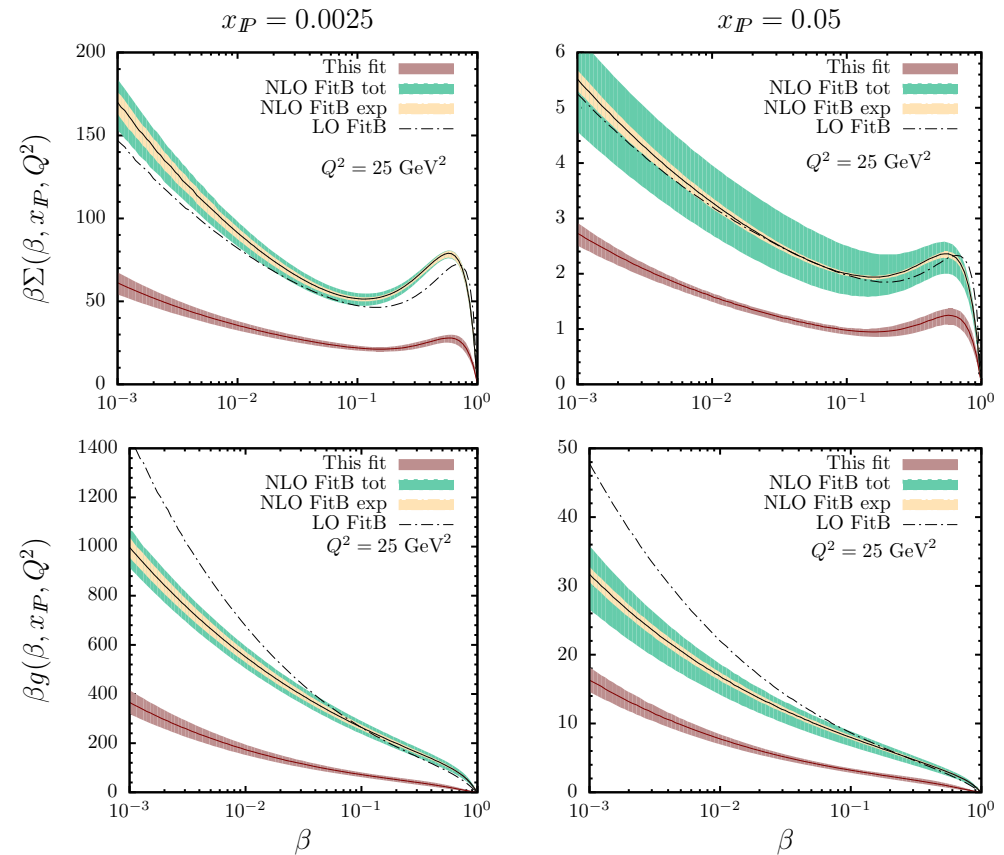
## Fit results and stability

- $Q^2 = 1.5 \text{ GeV}^2$
- Band = best fit  $\oplus \Delta\chi^2 = 10$
- stability of the fit checked against variation of the cuts:
  - best-fit (band) vs fit with  $y < 0.5$  (solid)
  - fit with  $Q^2 > 6 \text{ GeV}^2$  (dashed)
- **insensitive** to variation of phase space boundary



## Best-fit vs H1 parametrisations

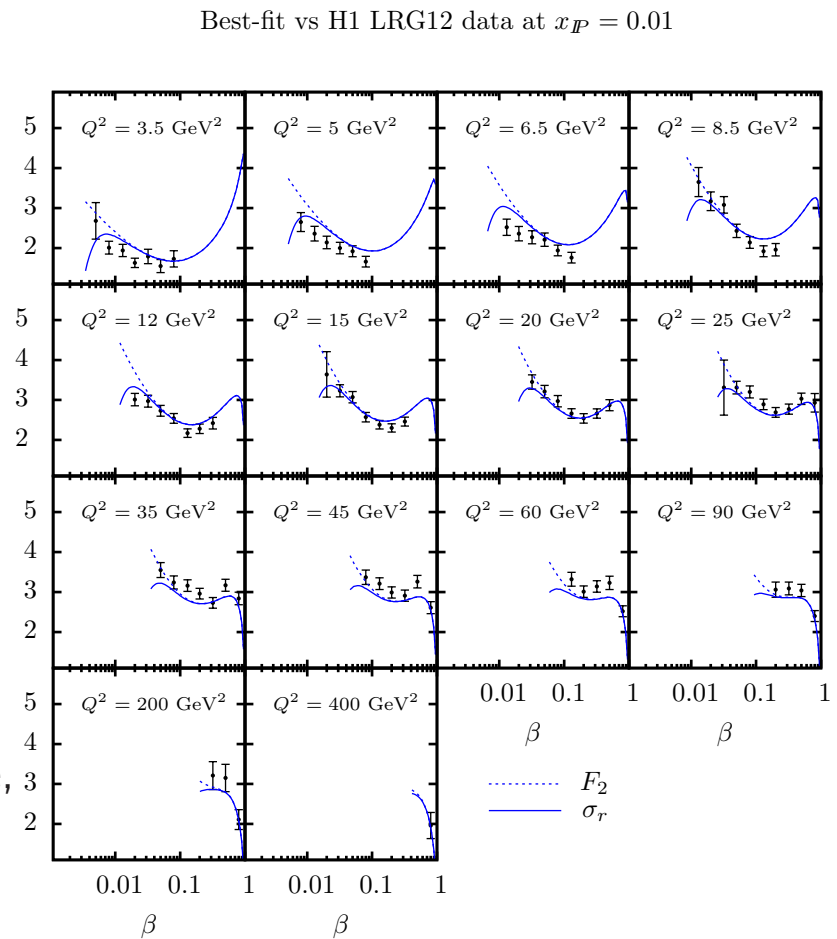
- Singlet (top) and gluon (bottom) momentum distribution at  $Q^2 = 25 \text{ GeV}^2$
- Comparison with FitB (based on LRG06 DIS data):
- similar hard valence at large  $\beta$ .
- no gluon structure at large  $\beta$
- Reduced errors at large  $x_{\mathcal{P}}$ , where FitB is dominated by systematic errors (for LRG06 :  $x_{\mathcal{P}}^{max} < 0.03$ )



- Normalisations shift due to different  $t$  range and proton dissociation background

## Preliminary NLO Best-fit vs H1 LRG 2012 data

- **preliminar** NLO fit ready  
(no error estimates yet)
- comparison with H1 LRG 2012 inclusive DDIS data  
(H1 Coll. EPJ C72 (2012) 2014)
- $x_P = 0.01$  : overlap region of two data sets
- Best fit scaled up by a factor 2.3:
  - Extrapolation to  $0 < |t| < 1 \text{ GeV}^2$
  - proton dissociative background
- Acceptable description of H1 data in shape, BUT  $Q^2$ -dependent normalisation offset
- attempt combination?



## Hadronic collisions : on hard-scattering factorisation

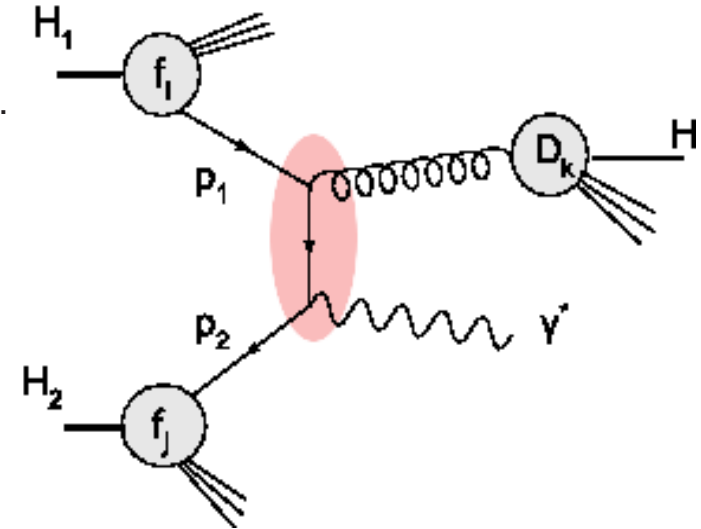
- Hard-scattering factorisation is at the basis of discovery and precision physics at hadron colliders.
- Factorisation proven only for inclusive Drell-Yan (soft exchanges are power suppressed when one sums over final states).

- Generalise:  $H_1 + H_2 \rightarrow H + \gamma^* + X$

- Assume hard scattering factorisation:

$$d\sigma \propto f_{H_1} \otimes f_{H_2} \otimes D_H \otimes d\hat{\sigma}$$

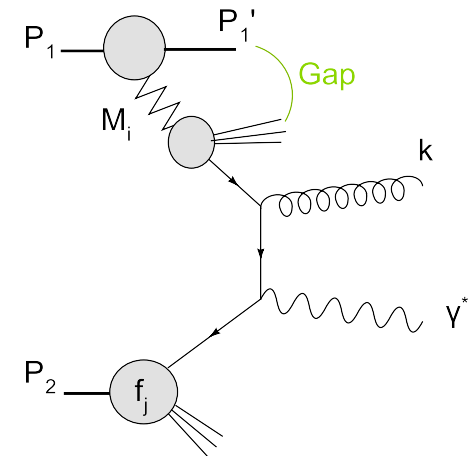
- $H = \pi^\pm$  at high  $p_t$  : factorisation should be ok
- $H = \pi^\pm$  at low  $p_t$  : underlying event (beyond factorisation)
- $H =$  forward  $p$  at low  $p_t$  : single-diffractive DY, factorisation breaking



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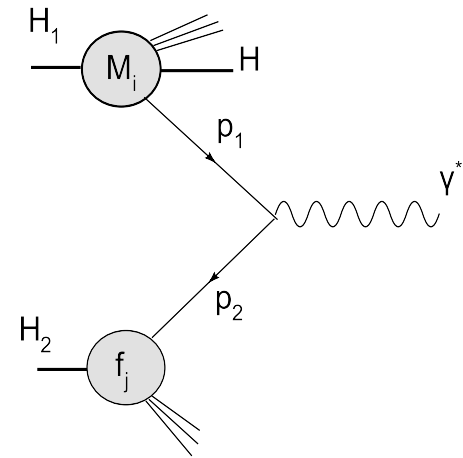
## Hard Diffraction at LHC

- Numerous analyses on soft and hard diffraction are ongoing at LHC by all Collaborations.
- Method :
  - LRG with main detectors
  - forward proton tagger
- ▶ Strategy: Assume hard scattering factorization : use HERA DPDFs to predict (single) diffractive cross sections for
  - $W^\pm, Z$  (clean, rare)
  - dijet (abundant, busy)
  - $\gamma$ -jet
  - ...
- Drell-Yan pairs provide easily tunable  $Q^2$  (relevant scale)



## Single Diffractive DRell-Yan: details

- SD-DY cross section written in terms of final state lepton rapidities  $y_3, y_4$  and transverse momentum  $p_t$
- $Y = \frac{1}{2}(y_3 + y_4)$ ,  $\bar{y} = \frac{1}{2}(y_3 - y_4)$
- $\beta = \frac{x_1}{x_{\mathbb{P}}} = \frac{p_t}{x_{\mathbb{P}}\sqrt{s}}(e^{y_3} + e^{y_4}) \equiv \frac{M_{\mu\mu}}{x_{\mathbb{P}}\sqrt{s}}e^Y$
- $x_2 = \frac{p_t}{\sqrt{s}}(e^{-y_3} + e^{-y_4}) \equiv \frac{M_{\mu\mu}}{\sqrt{s}}e^{-Y}$



- Assume factorisation:

$$\frac{d\sigma^D}{dy_3 dy_4 dp_t dx_{\mathbb{P}}} = \sum_q e_q^2 \frac{f_q^D(\beta, x_{\mathbb{P}}, \mu_F^2)}{x_{\mathbb{P}}} f_{\bar{q}}(x_2, \mu_F^2) \frac{2p_t \hat{s}}{3s} \frac{2\pi\alpha_{em}^2}{\hat{s}^2} \frac{\hat{t}^2 + \hat{u}^2}{\hat{s}^2}$$

- factorisation scale :  $\mu_F = M_{\mu\mu}$
- $f_q^D$  from the fit,  $f_q$  CTEQ6@LO



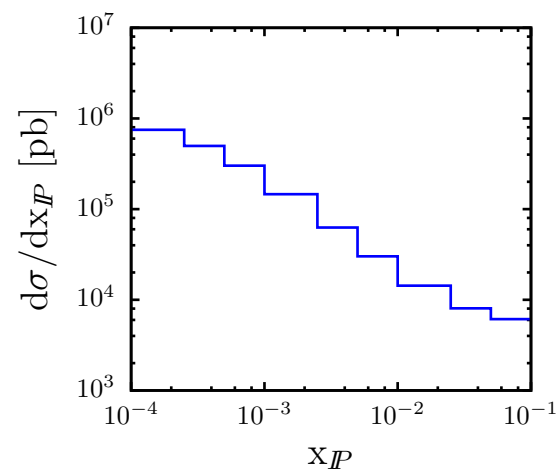
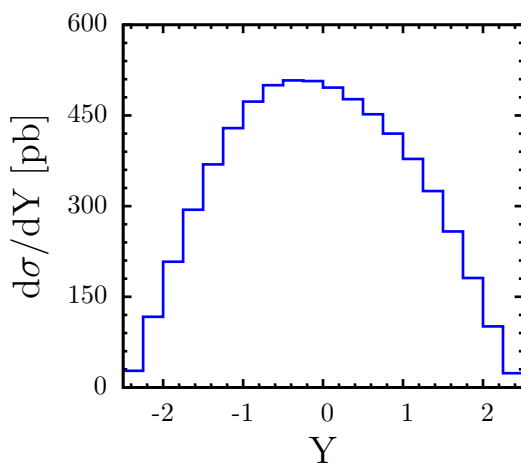
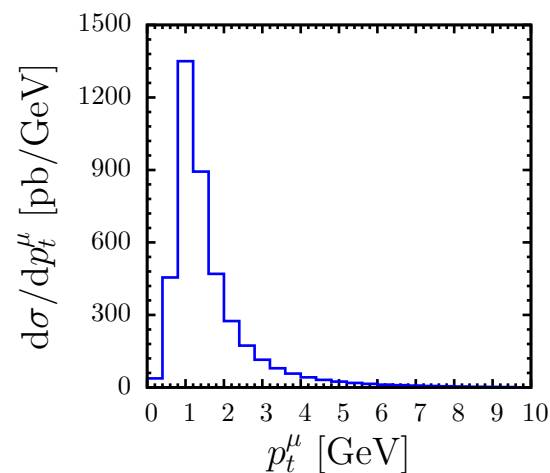
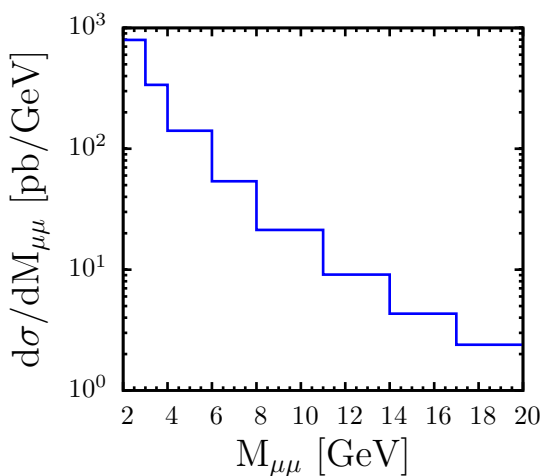
## SD-DY fiducial cross sections

$pp$	$\sqrt{s}=13$ TeV
Muon pair kinematics	$ y^\mu  < 2.45$ $2 < M_{\mu\mu} < 20$ GeV No cuts on muon $p_t$ or $\mathbf{p}$
Proton kinematics	$0.09 <  t  < 0.55$ GeV <sup>2</sup> $10^{-4} < x_P < 10^{-1}$
$\sigma^{SD,DY}$	$1635 \pm 60$ (exp) $^{+650}_{-460}$ (scale) pb

- single-side result (x2 double side)
- the result **does not include SGR**
- integrated over the  $t$ -range of the out of which dPDFs are extracted.
- dominated by **theo errors** associated with **higher order corrections**
- if  $\mathcal{L}^{-1} = 0.4\text{pb}^{-1}$ ,  $N = 1635\text{pb} \cdot 2 \cdot 0.1 \cdot 0.4\text{pb}^{-1} = 130$  events

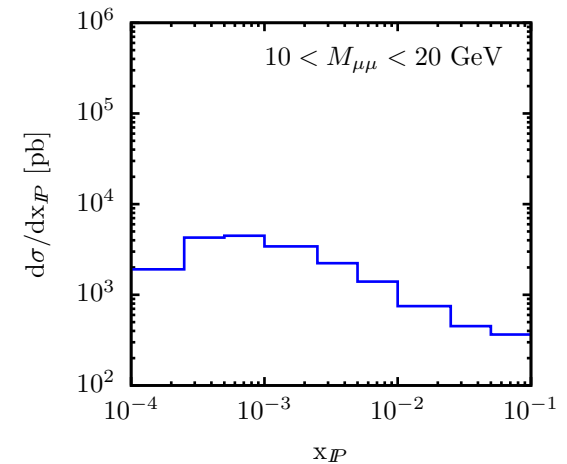
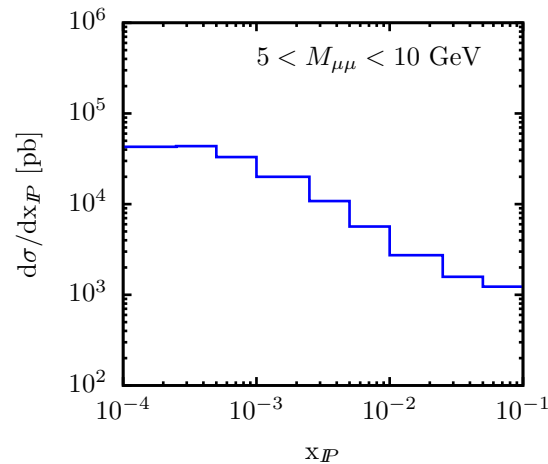
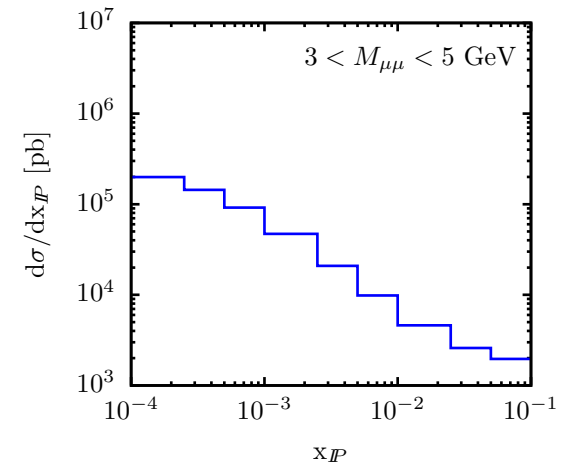
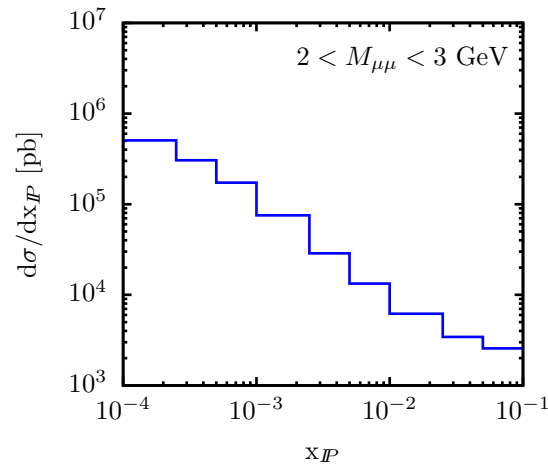
## SD-DY cross sections, first glance

- $p_t$  distribution as a maximum at  $M_{\mu\mu}^{min}$
- jacobian peak
- Scattered proton at positive  $Y \sim 9$
- DY pair has a rather symmetric  $Y$  distribution



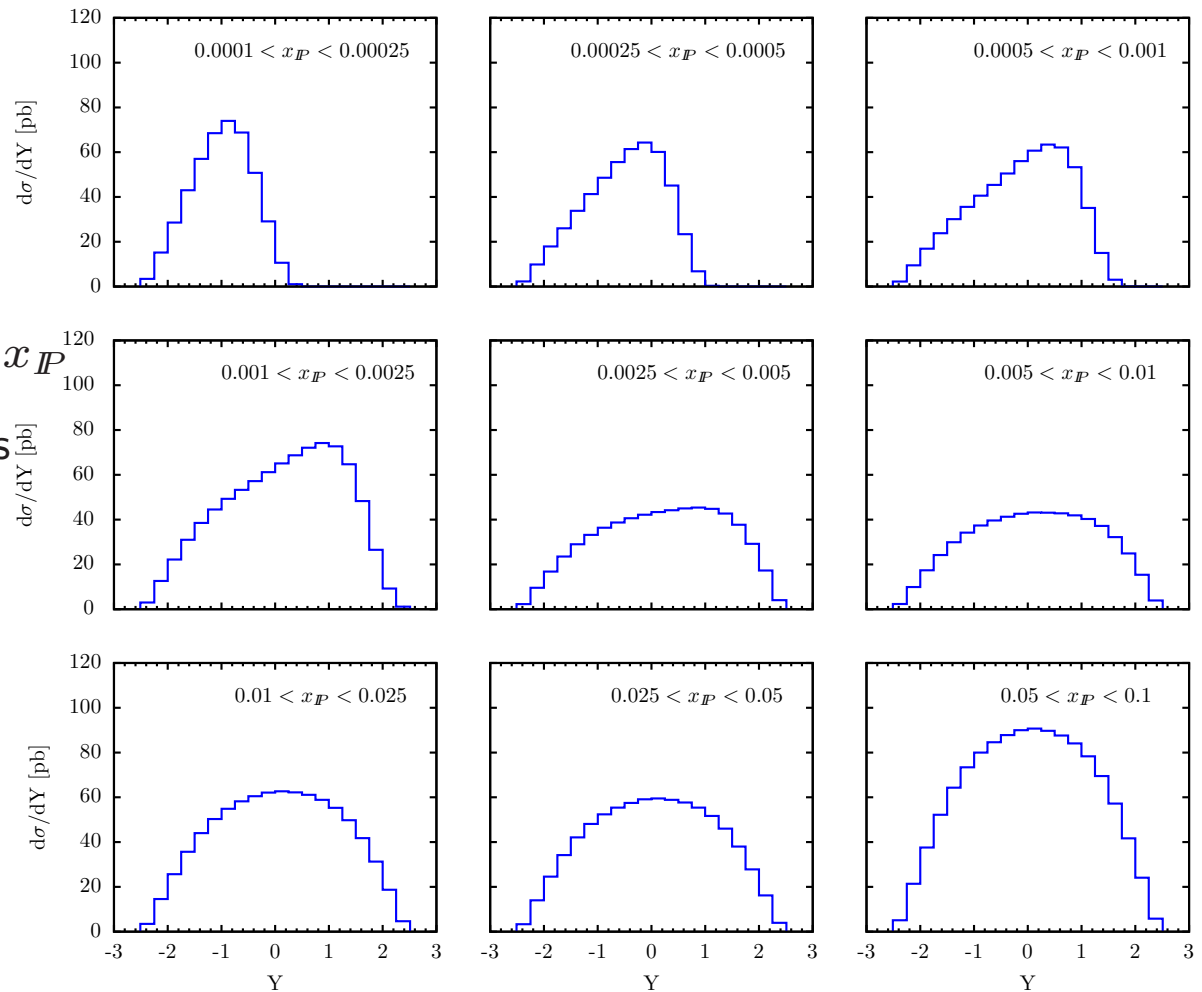
## $x_{\mathcal{P}}$ -dependence

- at low  $M_{\mu\mu}$  behaves as inverse power of  $x_{\mathcal{P}}$
- at higher masses, the pomeron has not enough energy to produce the pair:  
 $\Rightarrow x_{\mathcal{P}}$  distributions flattens at low  $x_{\mathcal{P}}$



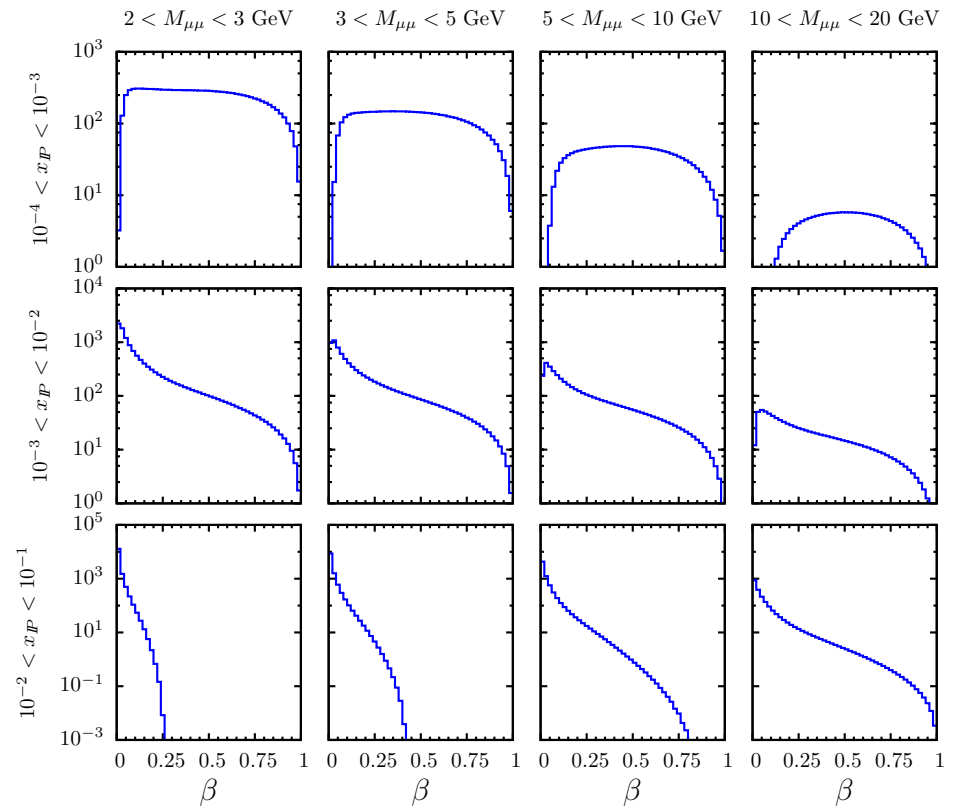
## $x_P$ - $Y$ correlations

- cross section integrated over masses  
 $2 < M_{\mu\mu} < 20$  GeV
- rapidity of the pair  $Y$  strongly correlated with  $x_P$
- at large  $x_P$  distributions get rather symmetric
- $Y < 0$  dissociated proton direction



## Universality and diffractive PDFs

- Sensitivity of the measurement to diffractive PDFs
- $\beta$  is fractional momentum with respect to the pomeron
- recall :  $M_{\mu\mu}^2 = \beta x_P x_1 s$
- Up to normalisation effects, **is dPDFs  $\beta$ -dependence in hadronic collisions** compatible with the one observed at HERA? (pomeron universality)



## SD-DY: asymmetries and ratio

Control theoretical error  $\Rightarrow$  consider ratios

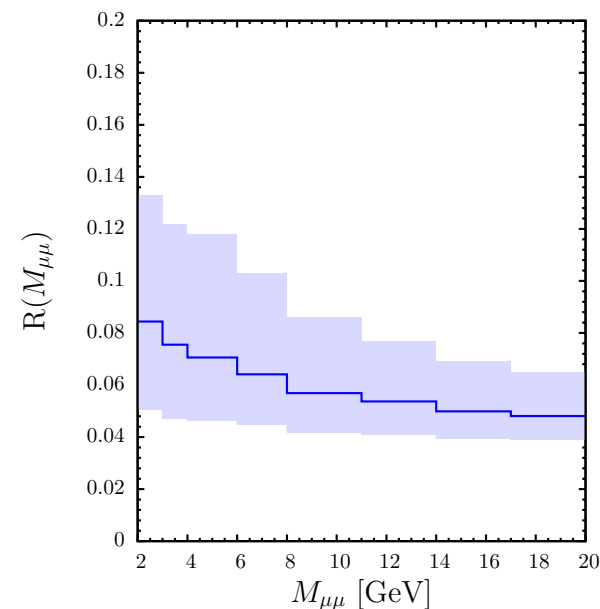
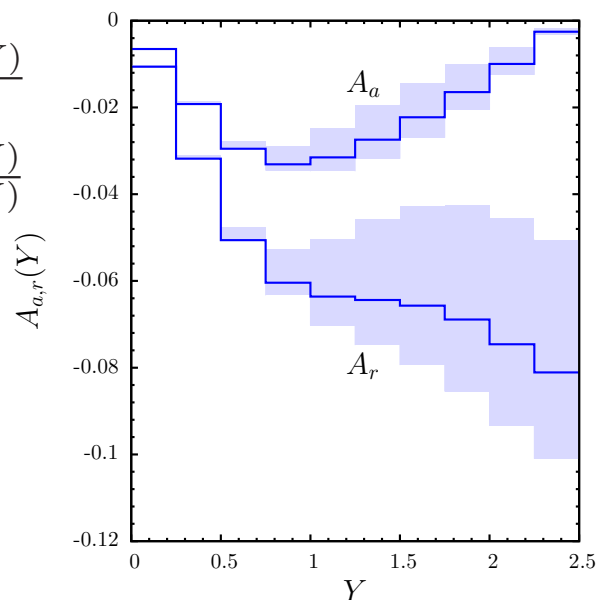
- $A_a(Y) = \frac{d\sigma(Y) - d\sigma(-Y)}{\sigma^{SD, DY}}$

- $A_r(Y) = \frac{d\sigma(Y) - d\sigma(-Y)}{d\sigma(Y) + d\sigma(-Y)}$

- NB: inclusive DY does not show such an asymmetry

- $R = \frac{\sigma(pp \rightarrow pXY)}{\sigma(pp \rightarrow XY)}$

- peculiar  $M_{\mu\mu}$  dependence of the ratio
- slowly decreasing from 9% to 5% (no SGR included)



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## Some phenomenological speculation

	DIS	PHP	hadronic collisions
MPI	no	?	yes
factorisation in diffraction	yes	?	no

- DIS :  $|b| \sim 1/Q$  (c.f.r. dipole model, Nikolaev and Zakharov '91)
- hadronic collision :  $|b| \sim 1/\Lambda_{QCD}$

⇒ Critical is then the **transverse profile**  $T(\mathbf{b})$  of the probe:

$\mathbf{b}$  relative distance of interacting partons (from double parton scattering)

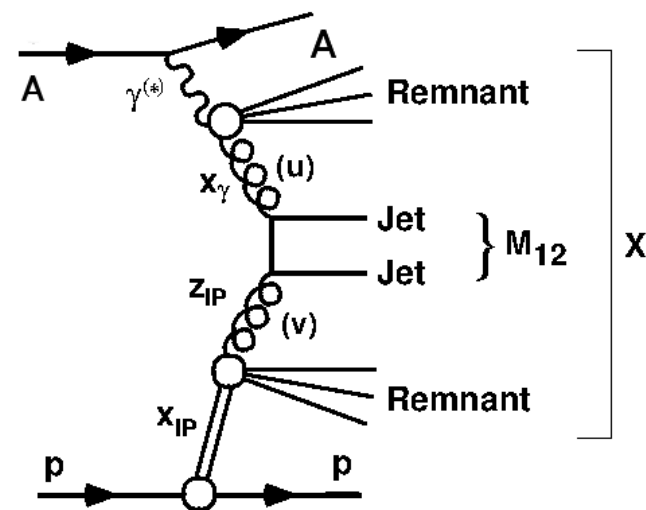
rethink diffraction:

$$\sigma^{SD} \propto \int d^2\mathbf{b} T_{a=\gamma^*,\gamma,p}(\mathbf{b}) T_{b=p}(\mathbf{b})$$

## LHC as a $\gamma p$ machine

PHP regime crucial for studying factorisation breaking and the transition from large to small  $b$  (interparton transverse distance) of the probe:

Can we use  $pA$  collisions at LHC to exploit the large quasi-real photon flux from  $A$  to measure diffractive dijets in  $\gamma p$ ?



- Hard scale in the final state :  
like in PHP in  $ep$  they guarantee the applicability of pQCD techniques.
- Factorisation breaking related to jets  $E_T$  or to size  $b \sim 1/Q$  of the quasi-real photon?



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## Conclusions and Perspectives

- **Impressive knowledge** on hard diffraction accumulated by HERA and Tevatron
- This knowledge is **quantitative** and **predictive** (dPDFs etc.)
- **Hard diffraction** program at hadron collider:
  - Prediction: with  $0.4\text{pb}^{-1} \sim 130$  SD-DY events
  - SD-DY is ideal place to study details of factorisation breaking vs  $Q^2, \sqrt{s}$
  - Explore the feasibility to use LHC  $pA$  runs in  $\gamma p$  mode to settle the diffractive PHP factorisation issue raised at HERA
- Plans (**in stand-by**):
  - NLO fit  $\rightarrow$  can be used to predict cross section in other SD channel: dijet, prompt photon,  $W$
  - Impact of higher order corrections : SD-DY @ NLO