
Mesons and Tetraquarks

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Mesons and the quark model

From mesons spectroscopy you end up quite quickly into talking about constituent quarks

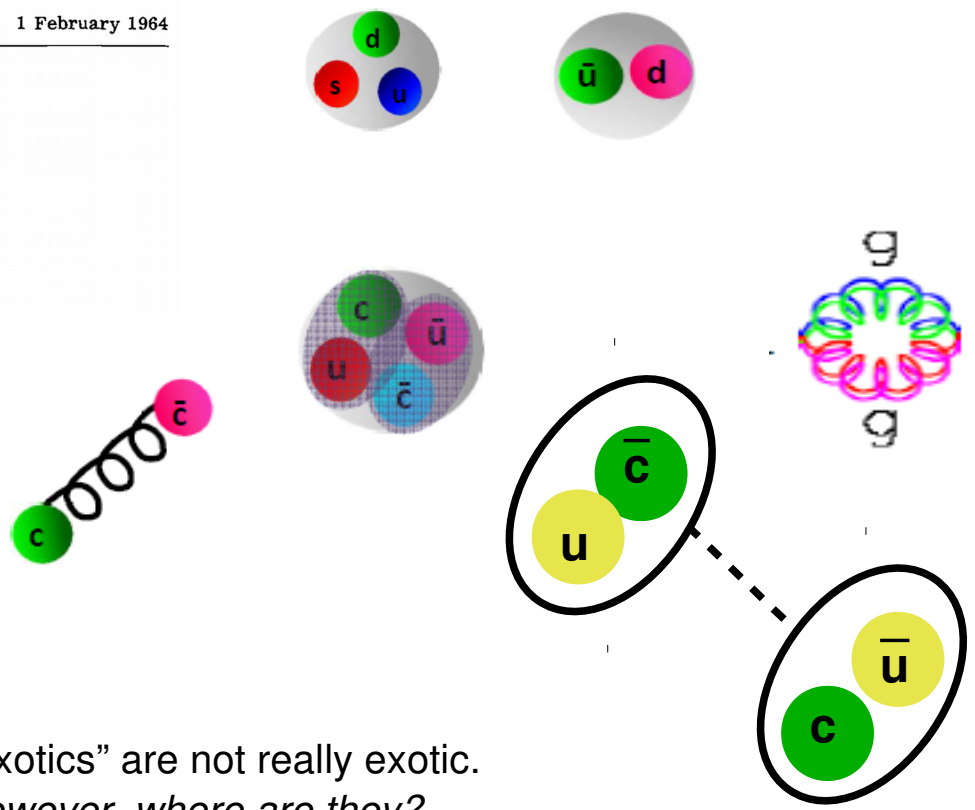
A SCHEMATIC MODEL OF BARYONS AND MESONS *

M. GELL-MANN

California Institute of Technology, Pasadena, California

Received 4 January 1964

A simpler and more elegant scheme can be constructed if we allow non-integral values for the charges. We can dispense entirely with the basic baryon Λ if we assign to the triplet t the following properties: spin $\frac{1}{2}$, $z = -\frac{1}{3}$, and baryon number $\frac{1}{3}$. We then refer to the members $u^{\frac{2}{3}}$, $d^{-\frac{1}{3}}$, and $s^{-\frac{1}{3}}$ of the triplet as "quarks" q and the members of the anti-triplet as anti-quarks \bar{q} . Baryons can now be constructed from quarks by using the combinations (qqq) , $(qqq\bar{q})$, etc., while mesons are made out of $(q\bar{q})$, $(qq\bar{q}\bar{q})$, etc. It is assumed that the lowest baryon configuration (qqq) gives just the representations **1**, **8**, and **10** that have been observed, while the lowest meson configuration $(q\bar{q})$ similarly gives just **1** and **8**.

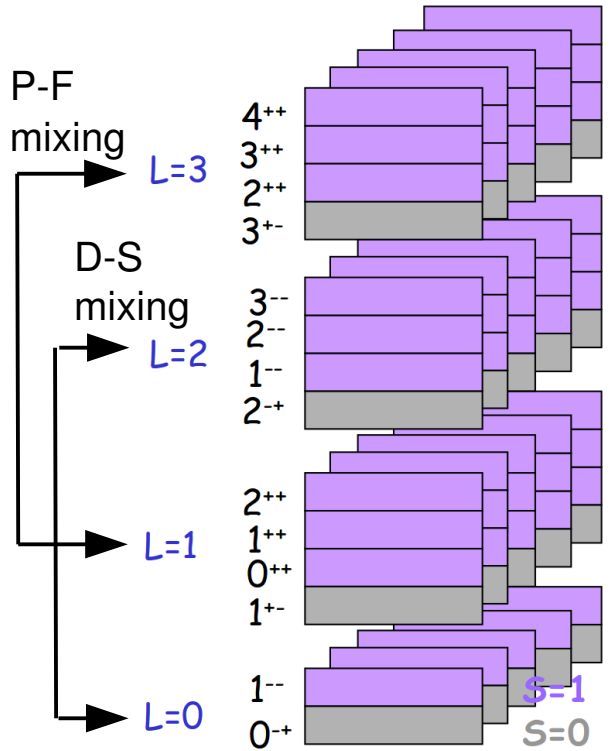
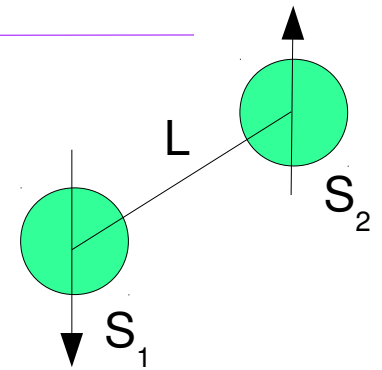


"Exotics" are not really exotic.
However, where are they?

Low mass

- $\Lambda_{\text{QCD}}/m_q \gg 1$
- $v/c \sim 1$
- **L is not a good quantum number**

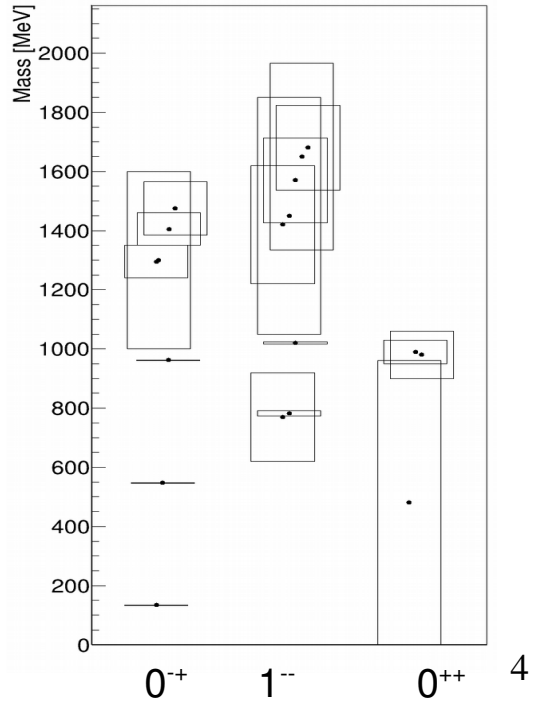
Broad resonances
 $\Gamma \sim \Delta M \sim M$



- ρ, K^*, ω, ϕ
- π, K, η, η'
- a, K, f, f'
- b, K, h, h'
- ρ, K^*, ω, ϕ
- π, K, η, η'

Mesons come in nonets of the same J^{PC} Quantum Numbers

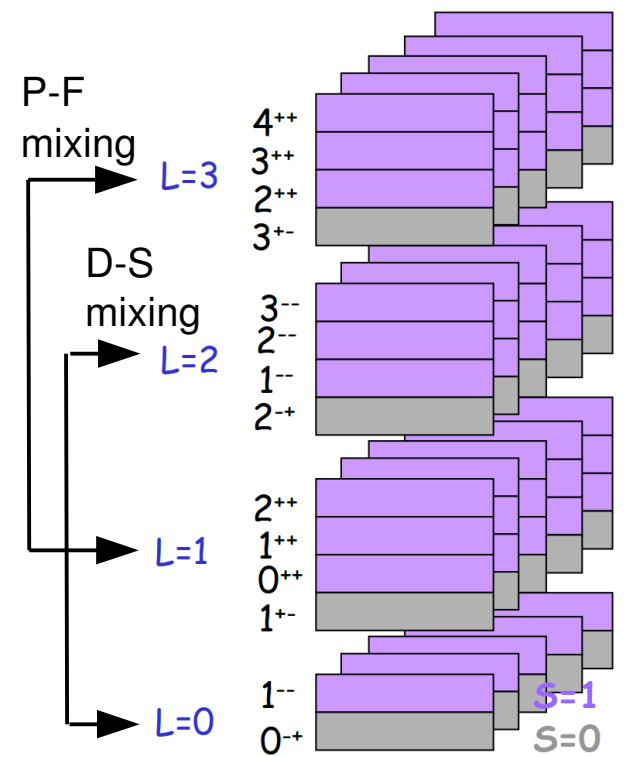
SU(3) is broken last two members mix



Low mass: experimental tools

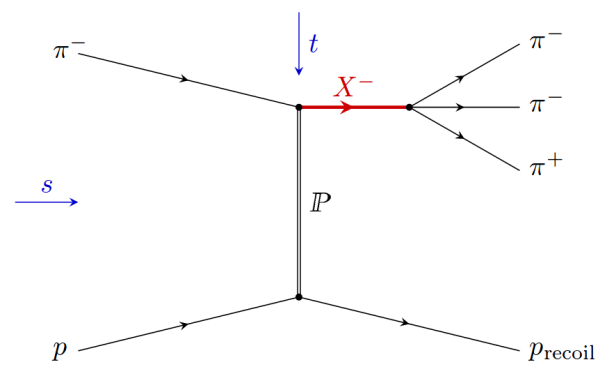
- $\Lambda_{\text{QCD}}/m_q \gg 1$
- $v/c \sim 1$
- **L is not a good quantum number**

Exotic quantum numbers: $J^{PC} = 0^{++}, 1^{+-}, 2^{+-}, 3^{+-} \dots$

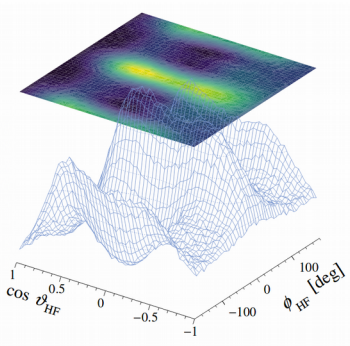
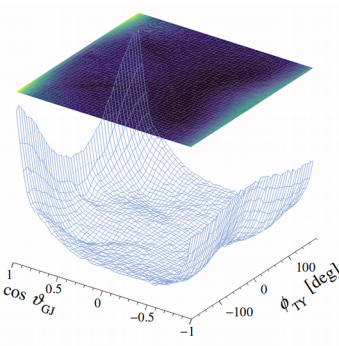
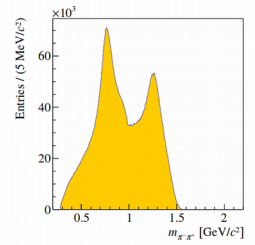
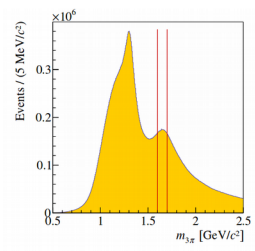


- ρ, K^*, ω, ϕ
- π, K, η, η'
- a, K, f, f'
- b, K, h, h'
- ρ, K^*, ω, ϕ
- π, K, η, η'

Experimental tools: Partial Wave analysis

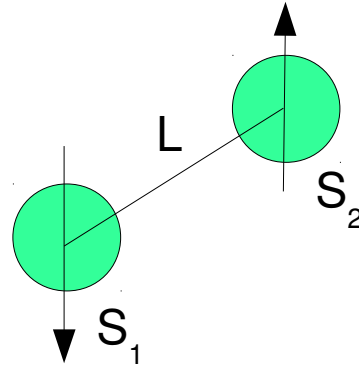


Compass @ CERN
 CLAS @ JLAB
 ...



High mass

- $\Lambda_{\text{QCD}}/m_q < 1$
- $v/c \ll 1$
- **L is a good quantum number**



Narrow resonances
 $\Gamma < \Delta M \ll M$

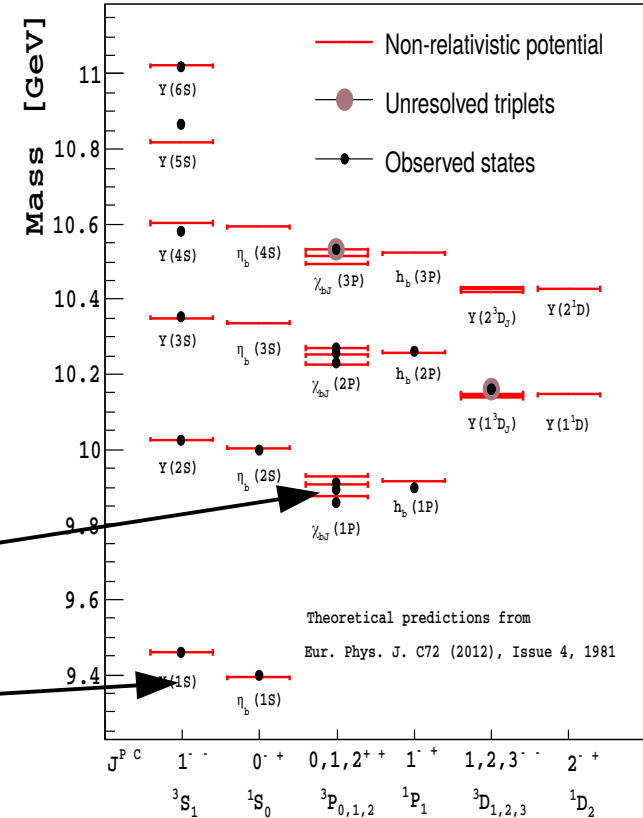
Quarkonium as a prototype of a simple QCD-based bound state

$$V(r) \sim \frac{-4}{3} \frac{\alpha_s}{r} \quad \text{for } r \ll \frac{1}{\Lambda}$$

$$V_{spin}(r) = \left(\frac{1}{2m_1^2} \vec{L} \cdot \vec{S}_1 + \frac{1}{2m_2^2} \vec{L} \cdot \vec{S}_2 \right) \frac{1}{r} \frac{d}{dr} (V(r) + 2V_1(r))$$

$$+ \frac{1}{m_1 m_2} \vec{L} \cdot (\vec{S}_1 + \vec{S}_2) \frac{1}{r} \frac{dV_2(r)}{dr}$$

$$+ \frac{1}{m_1 m_2} (\hat{r} \cdot \vec{S}_1 \hat{r} \cdot \vec{S}_2 - \frac{1}{3} \vec{S}_1 \cdot \vec{S}_2) V_3(r) + \frac{1}{3m_1 m_2} \vec{S}_1 \cdot \vec{S}_2 V_4(r)$$



Fine splitting

Hyperfine splitting

High mass: experimental tools

- $\Lambda_{\text{QCD}}/m_q < 1$
- $v/c \ll 1$
- **L is a good quantum number**

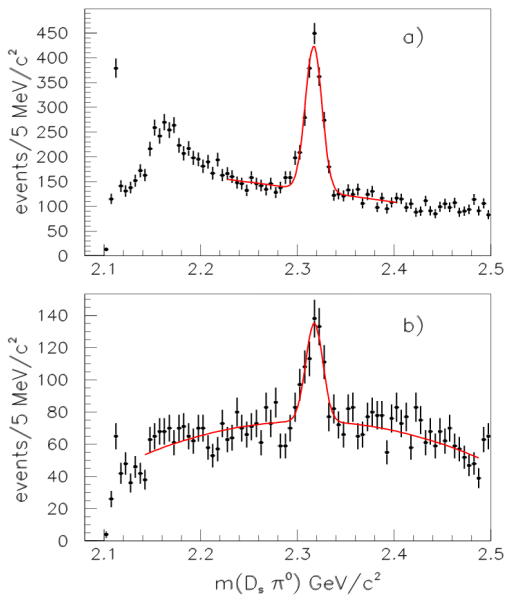
Search for narrow peaks not fitting the expected spectra

Unique signatures:

- Narrow states $\Gamma < \Delta M \ll M$
- Flavored (open or hidden) final states
- Spin effects decouple
- Net charge in bottomonium- like implies at least 4 quarks involved!

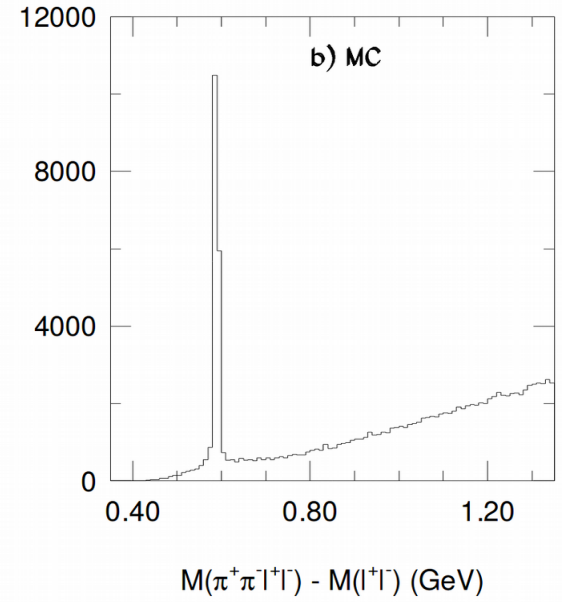
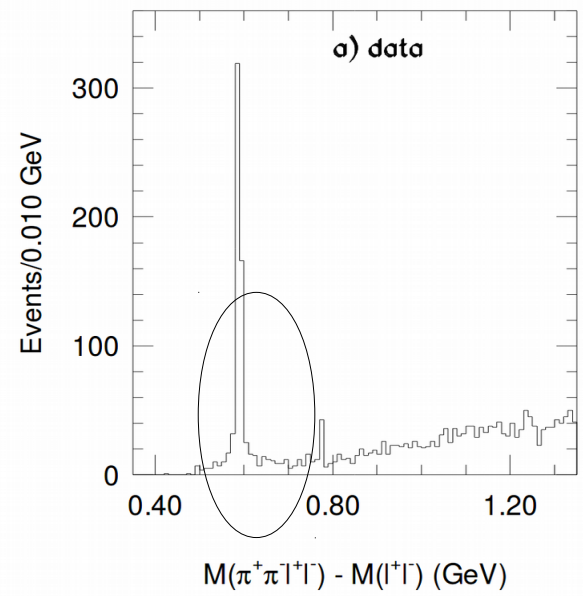
BaBar: $D_{sJ}(2317)$

Phys.Rev.Lett. 90 (2003) 242001



Belle: $X(3872)$

Phys.Rev.Lett. 91 (2003) 262001



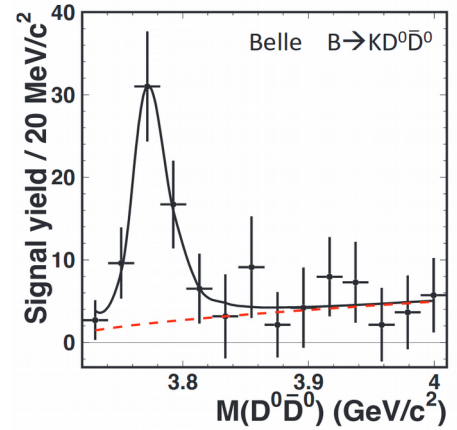
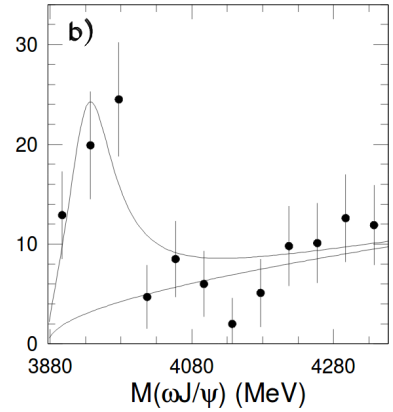
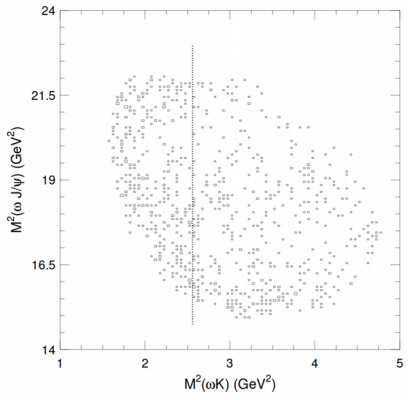
The uniqueness of quarkonia: the X(3915) saga

Seen by Belle in $B \rightarrow \omega J/\psi K$

Phys.Rev.Lett. 94 (2005) 182002

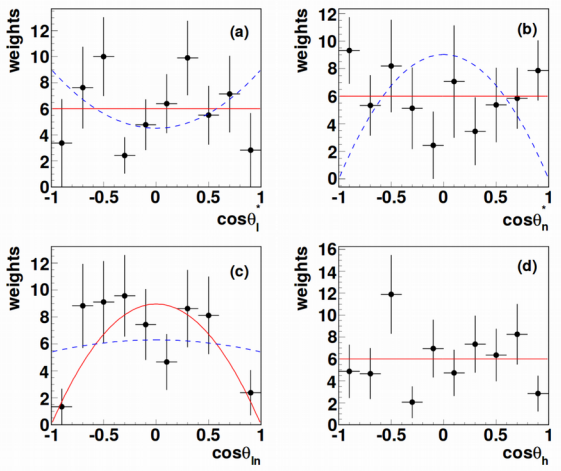
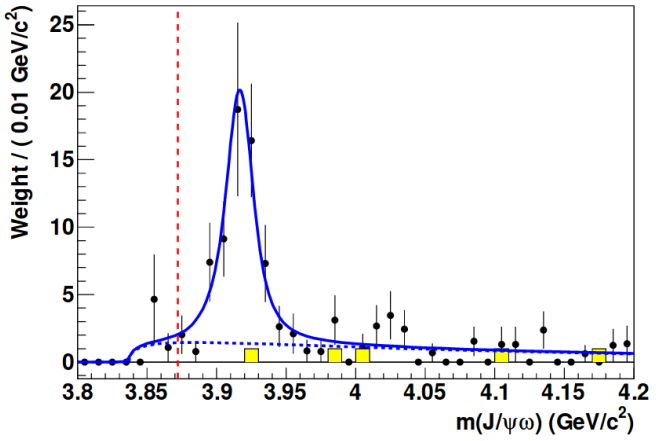
NOT seen $B \rightarrow KDD$

Phys.Rev.Lett. 94 (2005) 182002



Confirmed by BaBar in $\gamma\gamma \rightarrow \omega J/\psi$

Phys.Rev. D86 (2012) 072002



Angular analysis favours 0^{++} over 2^{++} (if helicity 2 is dominating)

The X(3915) is the conventional state $\chi_{cJ0}(2P)$ (?)

The uniqueness of quarkonia: the X(3915) saga

Phys.Rev. D91 (2015) no.5, 057501

Is the X(3915) the $\chi_{c0}(2P)$?

Stephen Lars Olsen¹

¹Center for Underground Physics, Institute for Basic Science, Daejeon 305-811, Korea
(Dated: October 27, 2014)

The Particle Data Group has assigned the X(3915) meson, an $\omega J/\psi$ mass peak seen in $B \rightarrow K\omega J/\psi$ decays and $\gamma\gamma \rightarrow \omega J/\psi$ two-photon fusion reactions, as the $\chi_{c0}(2P)$, the 2^3P_0 charmonium state. Here it is shown that if the X(3915) is the $\chi_{c0}(2P)$, the measured strength of the $\gamma\gamma \rightarrow X(3915)$ signal implies an *upper* limit on the branching fraction $\mathcal{B}(\chi_{c0}(2P) \rightarrow \omega J/\psi) < 7.8\%$ that conflicts with a $> 14.3\%$ *lower* limit derived for the same quantity from the $B \rightarrow KX(3915)$ decay rate. Also, the absence any signal for $X(3915) \rightarrow D^0\bar{D}^0$ in $B^+ \rightarrow K^+D^0\bar{D}^0$ decays is used to establish the limit $\mathcal{B}(X(3915) \rightarrow D^0\bar{D}^0) < 1.2 \times \mathcal{B}(X(3915) \rightarrow \omega J/\psi)$. This contradicts expectations that $\chi_{c0}(2P)$ decays to $D^0\bar{D}^0$ would be a dominant process, while decays to $\omega J/\psi$, which are Okubo-Zweig-Iizuka suppressed, would be relatively rare. These, plus reasons given earlier by Guo and Meissner, raise serious doubts about the $X(3915) = \chi_{c0}(2P)$ assignment.

$\chi_{cJ0}(2P)$ should have:

X(3915)

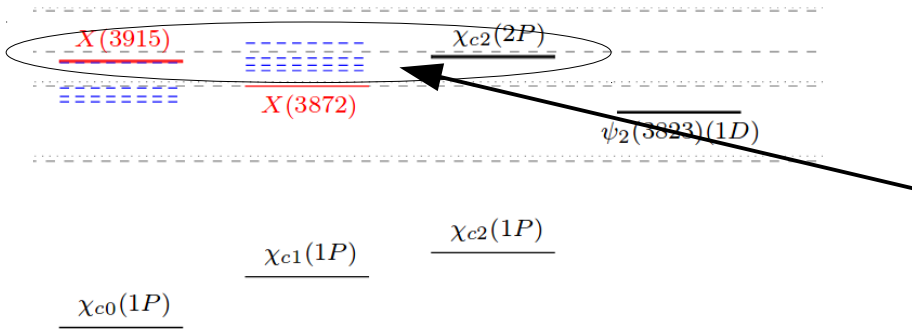
1) Dominant decay to $D^0\bar{D}^0$



2) Be 80-120 MeV below $\chi_{cJ2}(2P)$



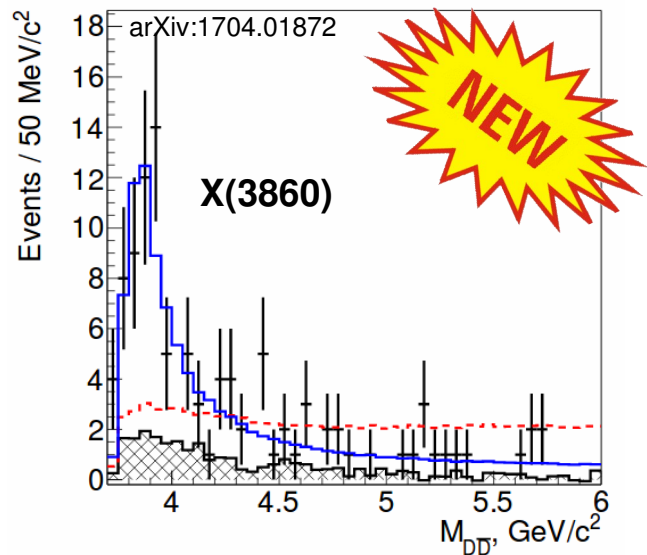
3) $\mathcal{B}(\chi'_{c0} \rightarrow \omega J/\psi) < 7.8\%$.



$$\Delta M(2P) = 8.8 \pm 3.2 \text{ MeV}$$

The uniqueness of quarkonia: the X(3915) saga

Belle 2017: New analysis of $e^+e^- \rightarrow J/\psi D^0\bar{D}^0$: **X(3860)**



$\chi_{cJ0}(2P)$ should have:

1) Dominant decay to $D^0\bar{D}^0$

2) Be 80-120 MeV below $\chi_{cJ2}(2P)$

3) $\mathcal{B}(\chi'_{c0} \rightarrow \omega J/\psi) < 7.8\%$.

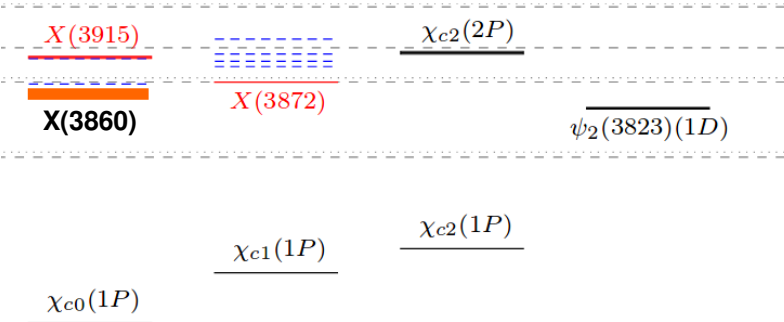
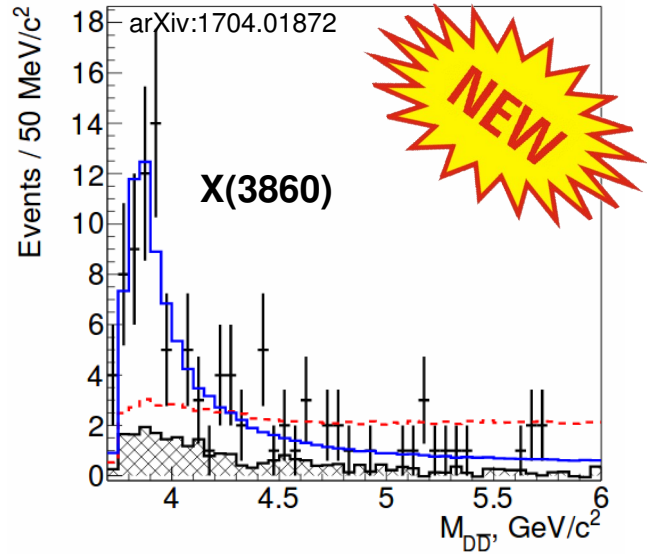
X(3915)

X(3860)



The uniqueness of quarkonia: the X(3915) saga

Belle 2017: New analysis of $e^+e^- \rightarrow J/\psi D^0\bar{D}^0$: **X(3860)**



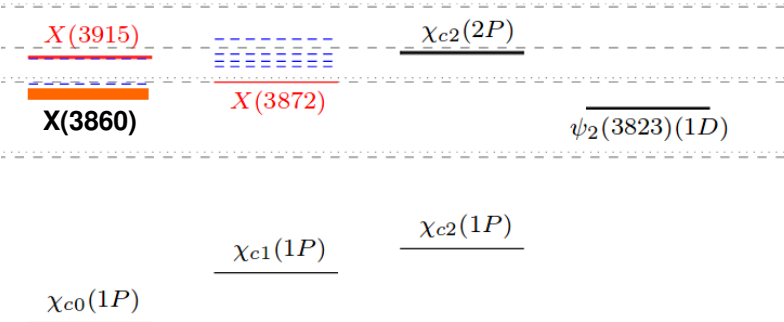
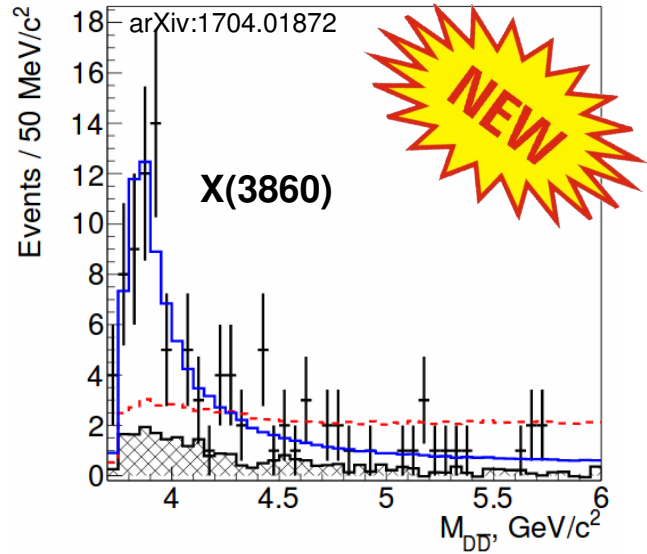
$\chi_{cJ0}(2P)$ should have:

- 1) Dominant decay to $D^0\bar{D}^0$
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- 3) $\mathcal{B}(\chi'_{c0} \rightarrow \omega J/\psi) < 7.8\%$.

	X(3915)	X(3860)
1) Dominant decay to $D^0\bar{D}^0$	✗	✓
2) Be 80-120 MeV below $\chi_{cJ2}(2P)$	✗	✓
3) $\mathcal{B}(\chi'_{c0} \rightarrow \omega J/\psi) < 7.8\%$	✗	

The uniqueness of quarkonia: the X(3915) saga

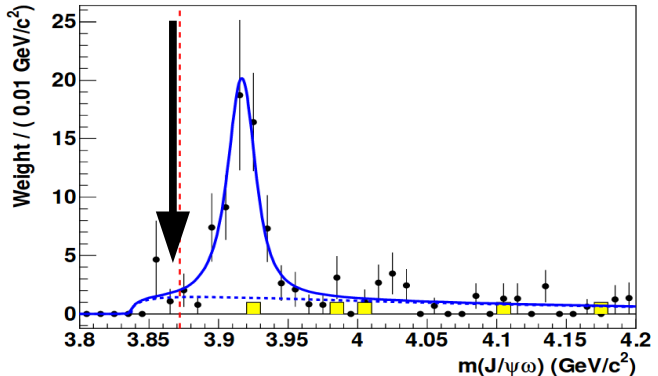
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$\chi_{cJ0}(2P)$ should have:

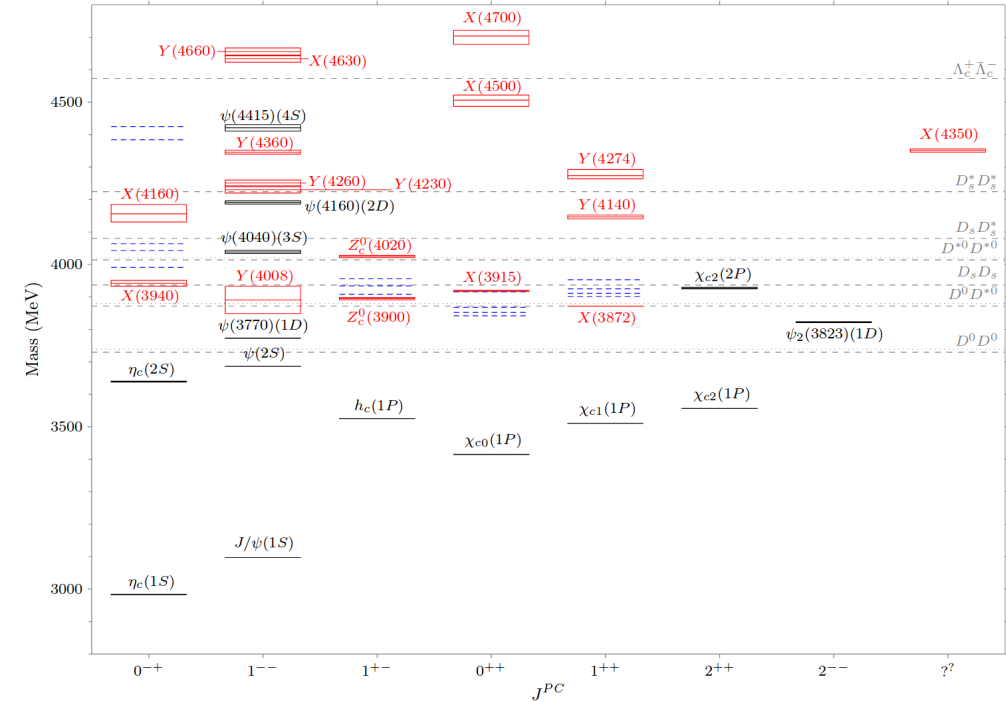
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Part I: tetraquarks and exotica

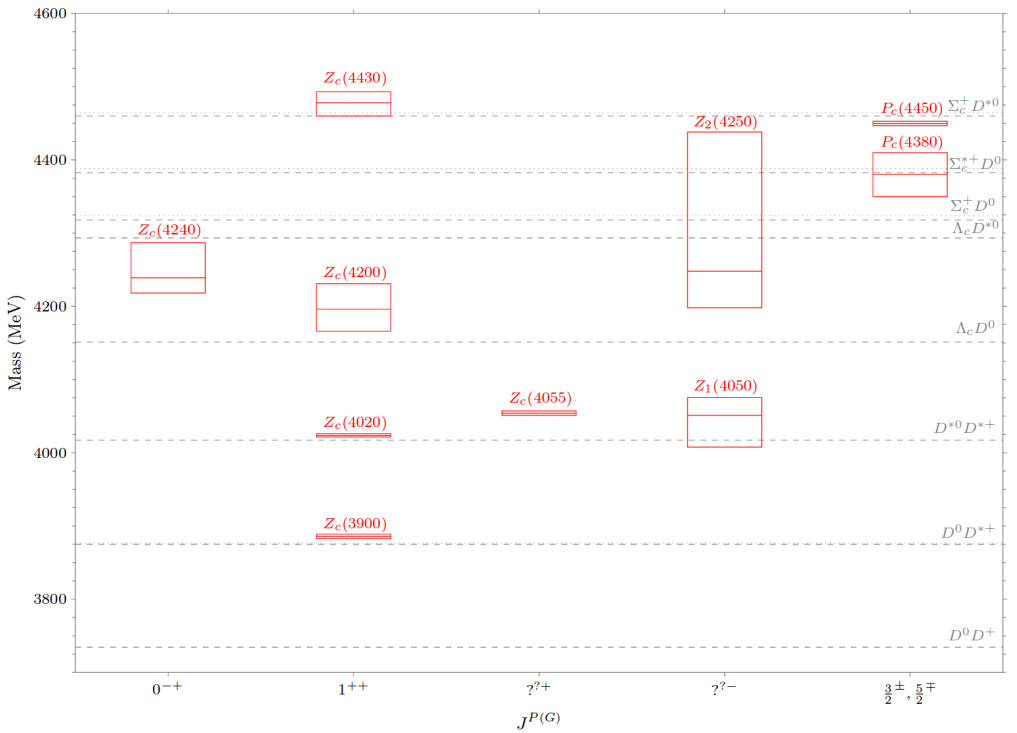
Exotica in charmonia



Intriguing patterns:

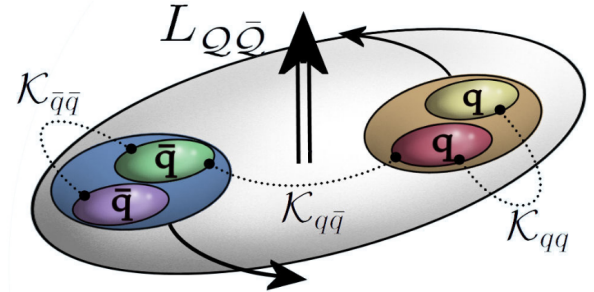
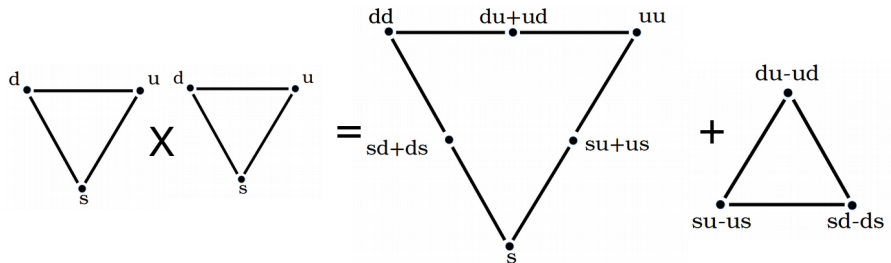
$$M_{Z(4430)} - M_{Z(3900)} \sim M_{\psi} - M_{J/\psi}$$

Charged charmonia.
Minimal quark content is $c\bar{c}q\bar{q}$

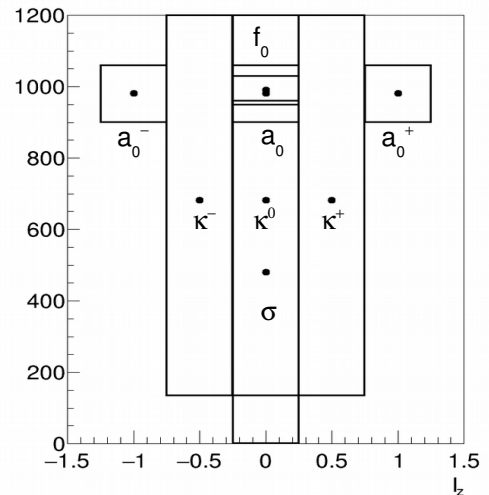
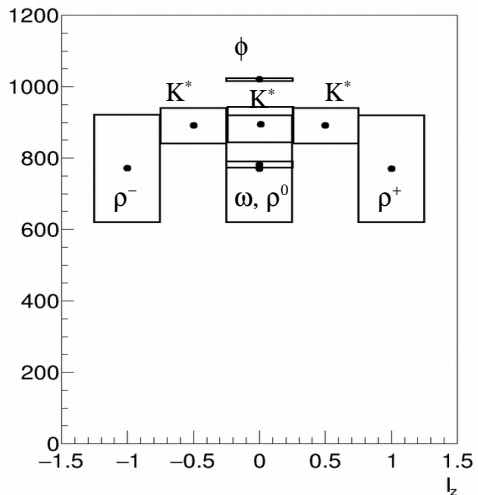
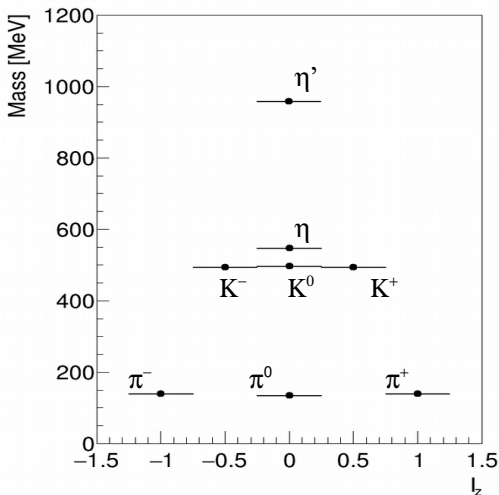


Understanding exotica: the tetraquark model

Based on the idea of di-quark



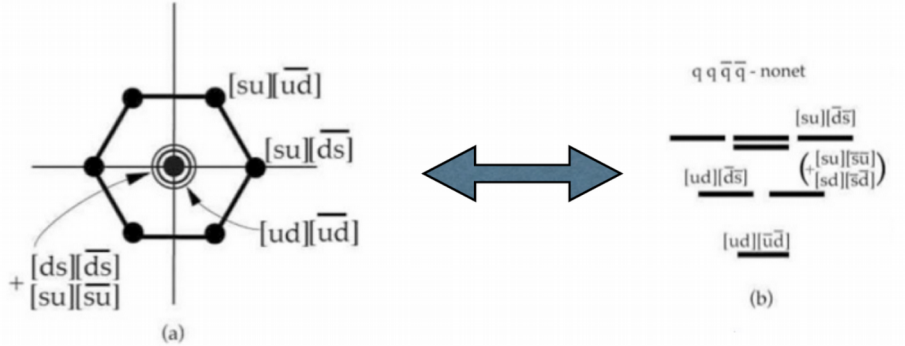
Originally motivated by the scalar mesons puzzle (Maiani et al, 2004)



Understanding exotica: the tetraquark model

Maiani et al, Phys.Rev.Lett. 93 (2004) 212002

t'Hooft et al, Phys.Lett. B662 (2008) 424-430



$$\sigma^{[0]} = [ud][\bar{u}\bar{d}]$$

$$\kappa = [su][\bar{u}\bar{d}]; [sd][\bar{u}\bar{d}] \text{ (+ conjugate doublet)}$$

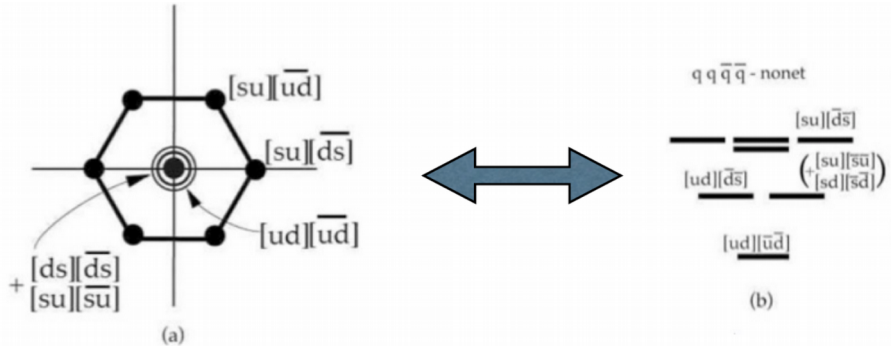
$$f_0^{[0]} = \frac{[su][\bar{s}\bar{u}] + [sd][\bar{s}\bar{d}]}{\sqrt{2}}$$

$$a_0 = [su][\bar{s}\bar{d}]; \frac{[su][\bar{s}\bar{u}] - [sd][\bar{s}\bar{d}]}{\sqrt{2}}; [sd][\bar{s}\bar{u}]$$

Understanding exotica: the tetraquark model

Maiani et al, Phys.Rev.Lett. 93 (2004) 212002

t'Hooft et al, Phys.Lett. B662 (2008) 424-430



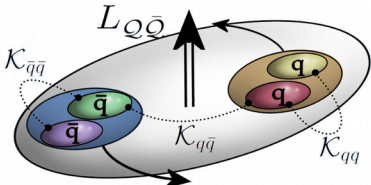
$$\sigma^{[0]} = [ud][\bar{u}\bar{d}]$$

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$$a_0 = [su][\bar{s}\bar{d}]; \frac{[su][\bar{s}\bar{u}] - [sd][\bar{s}\bar{d}]}{\sqrt{2}}; [sd][\bar{s}\bar{u}]$$

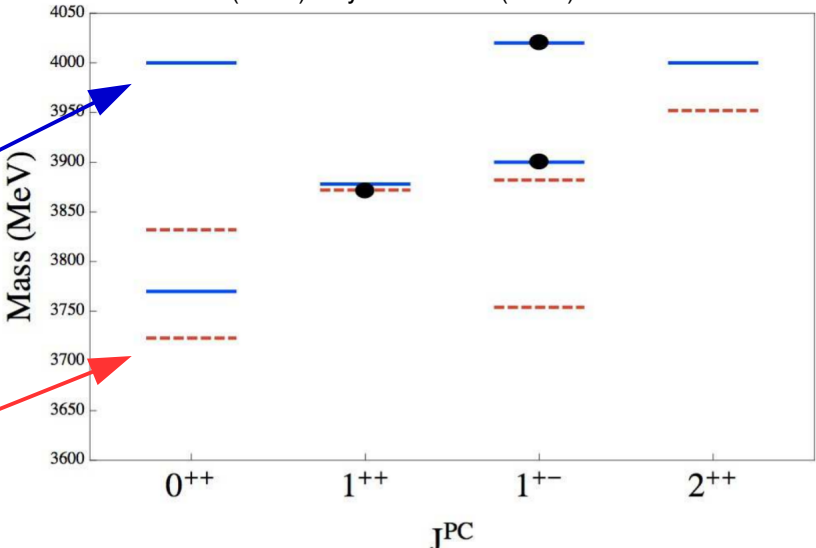
Tetraquark in the heavy sector



Interaction within di-quark dominates
 $H \sim 2\kappa_{qc}(s_q \cdot s_c + s_{\bar{q}} \cdot s_{\bar{c}})$

Interaction across di-quarks dominates
 $H \sim 2\kappa_{q\bar{q}}s_{q\bar{q}}(s_{q\bar{q}} + 1)$

Maiani et al (2014) Phys.Rev. D89 (2014) 114010

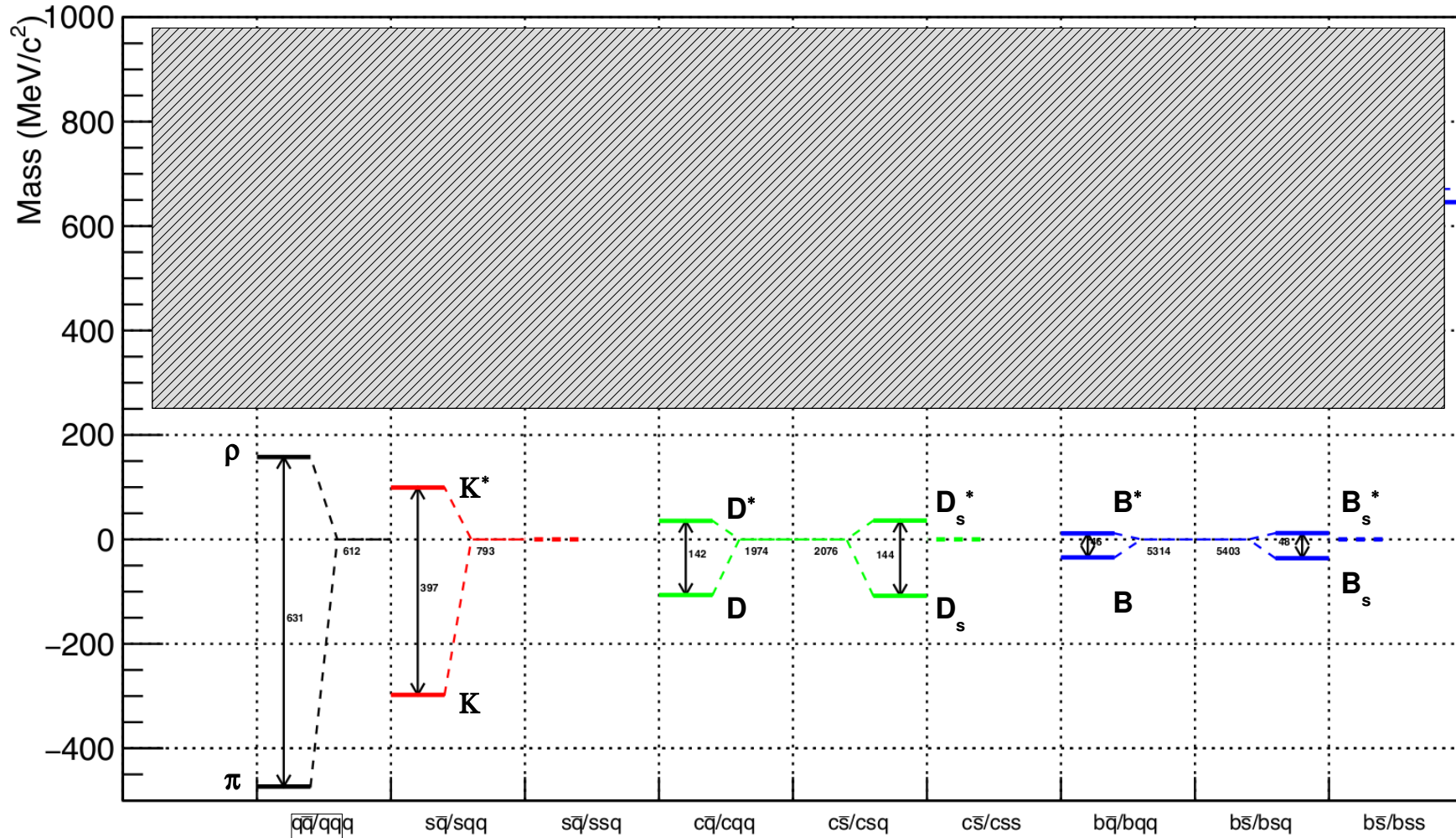


κ_{qc} fixed by mass difference between Z(3900) and Z(4430)

κ_{qq} fixed by mass difference baryons

Di-quarks: something more?

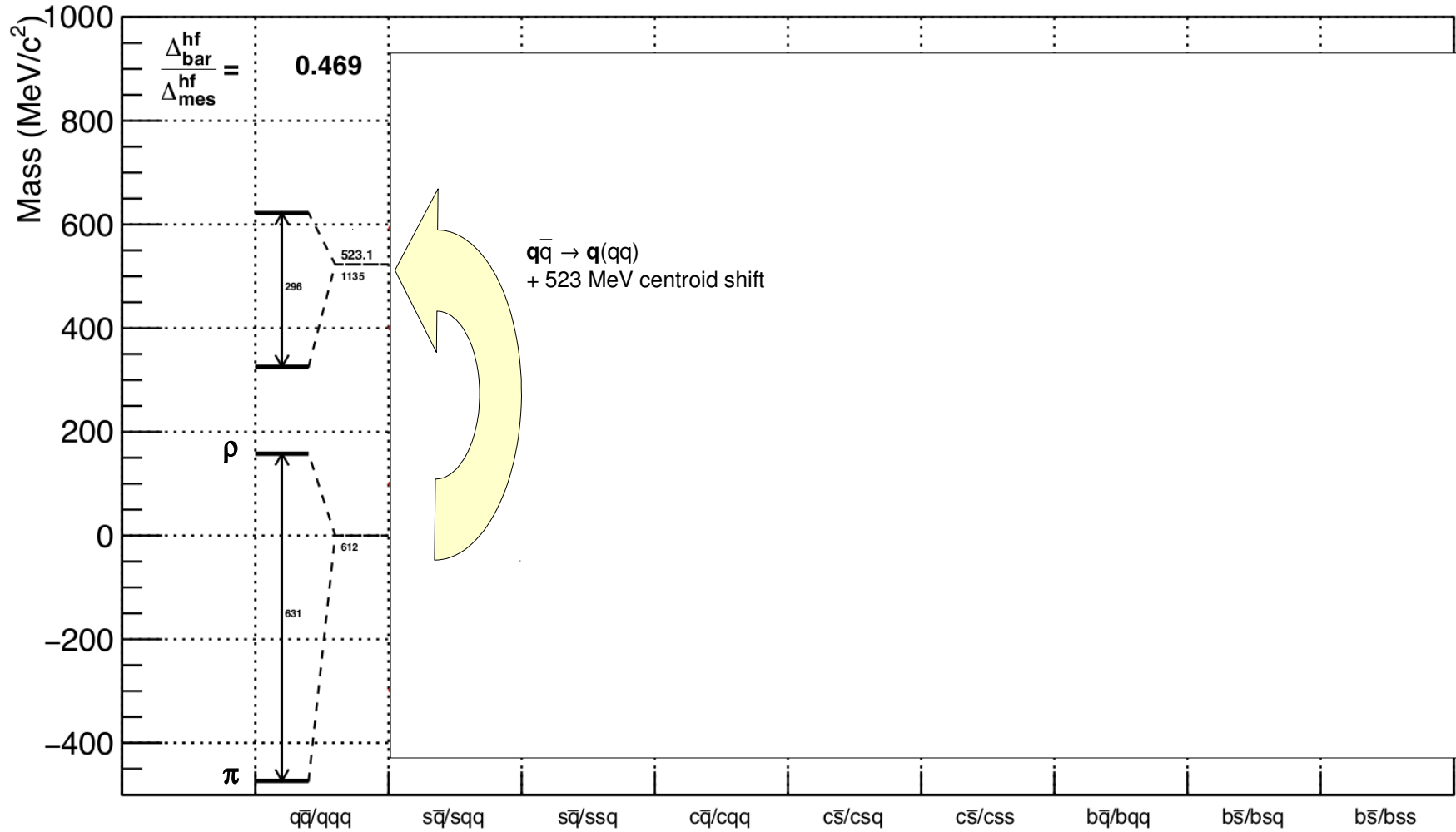
Frascati Phys.Ser. 60 (2015) 1-302



Nice scaling of the hyperfine splitting. Potential model not so bad even at low mass?

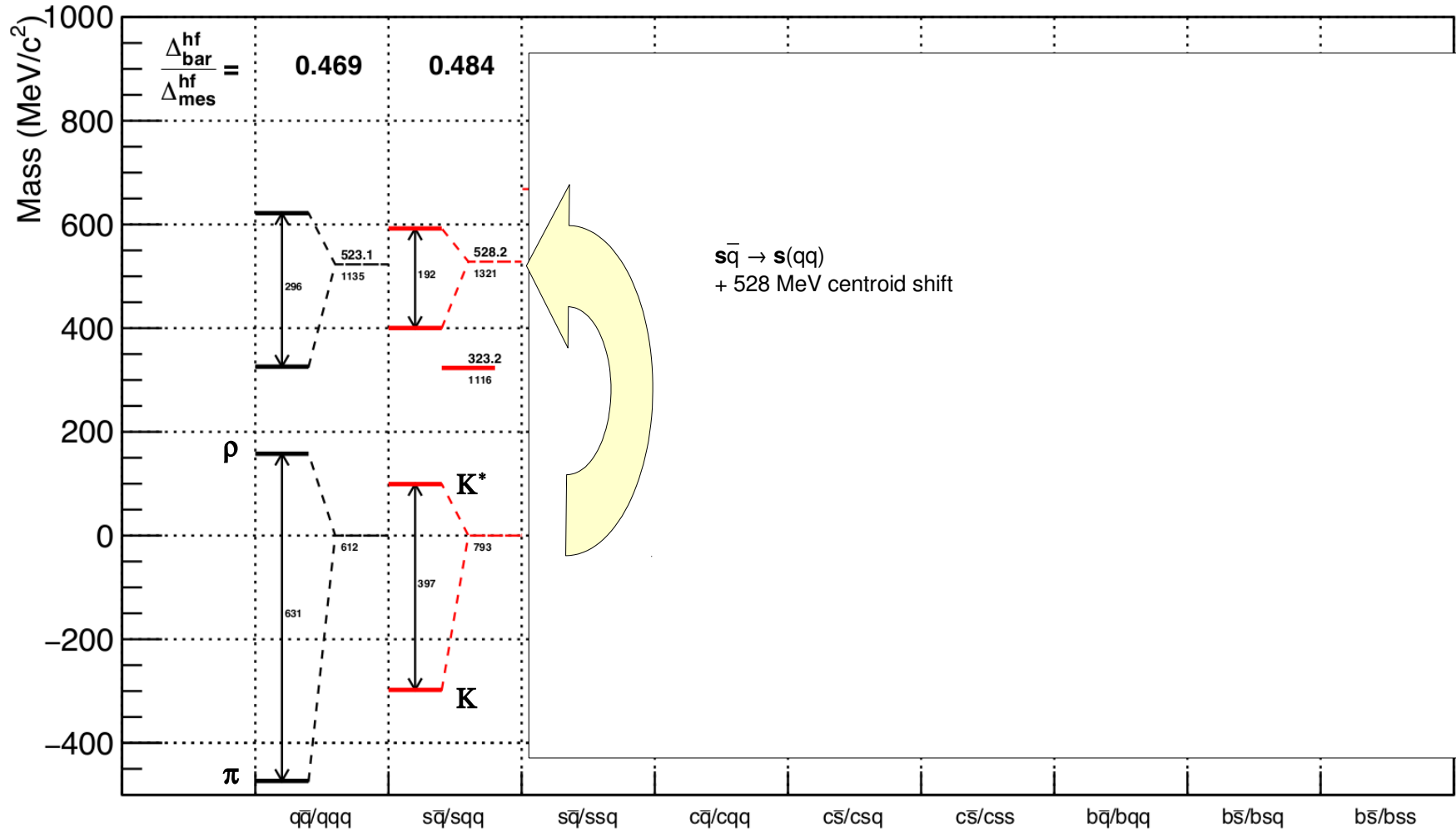
Di-quarks: something more?

Frascati Phys.Ser. 60 (2015) 1-302



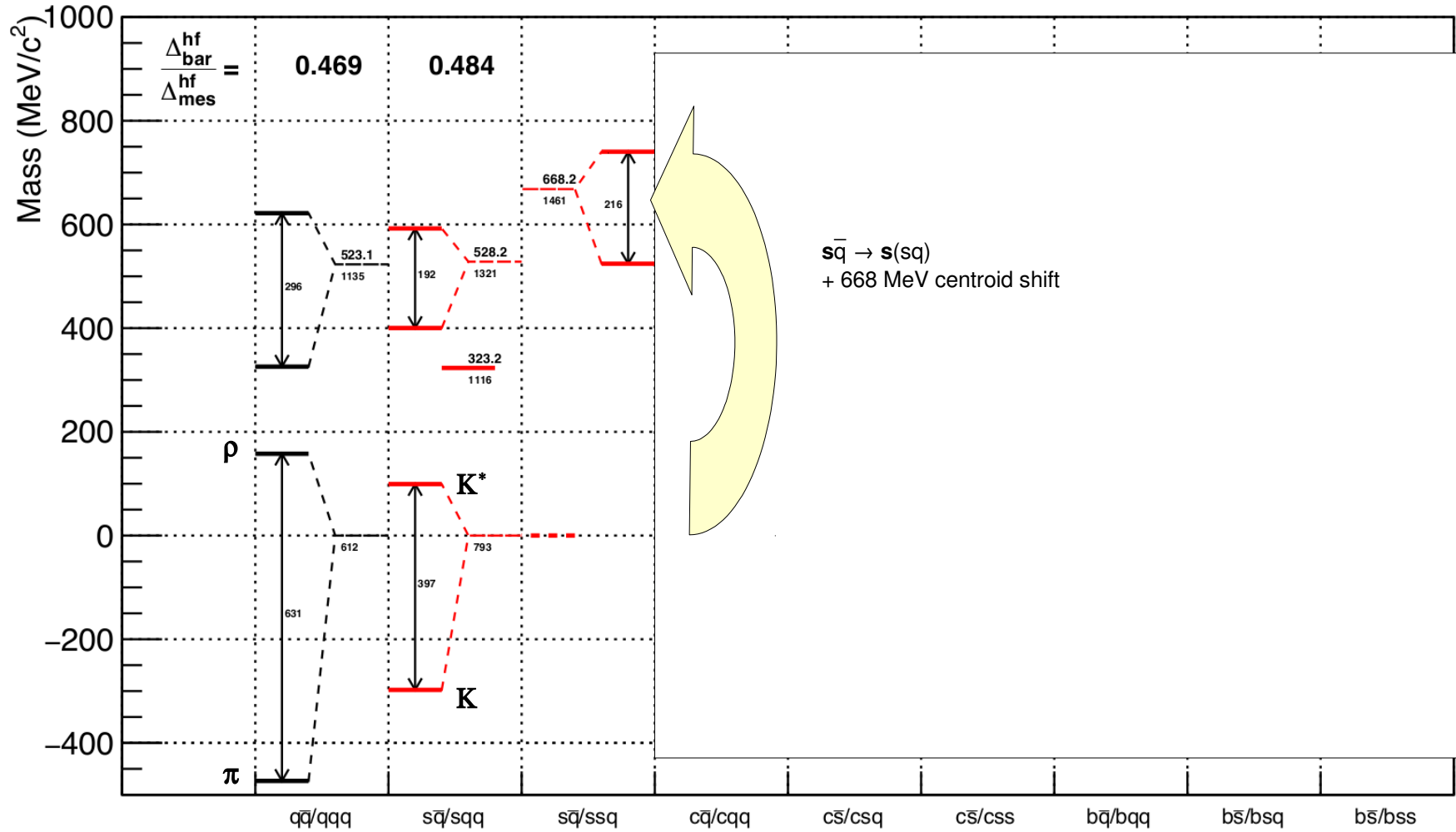
Di-quarks: something more?

Frascati Phys.Ser. 60 (2015) 1-302



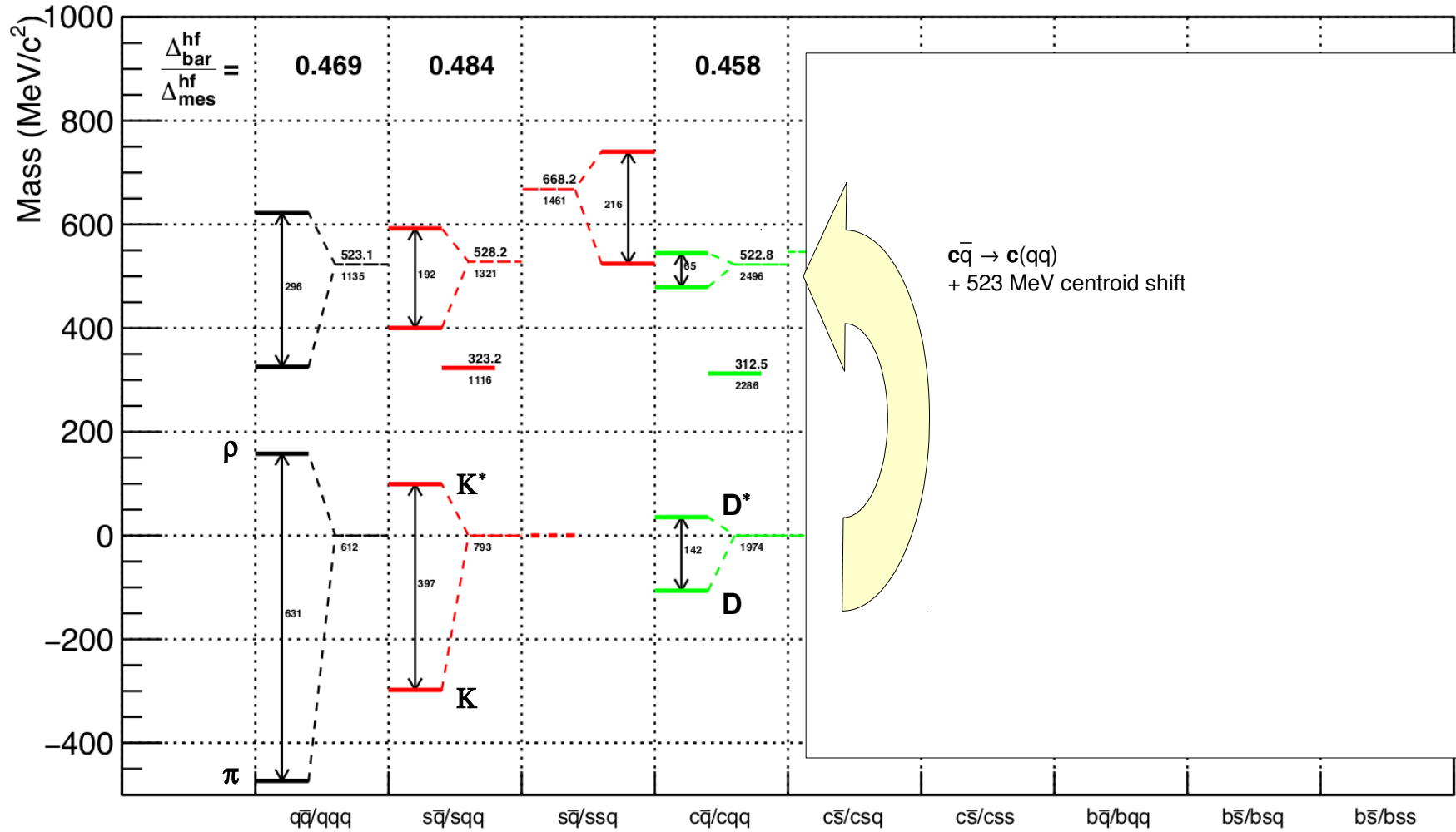
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Frascati Phys.Ser. 60 (2015) 1-302



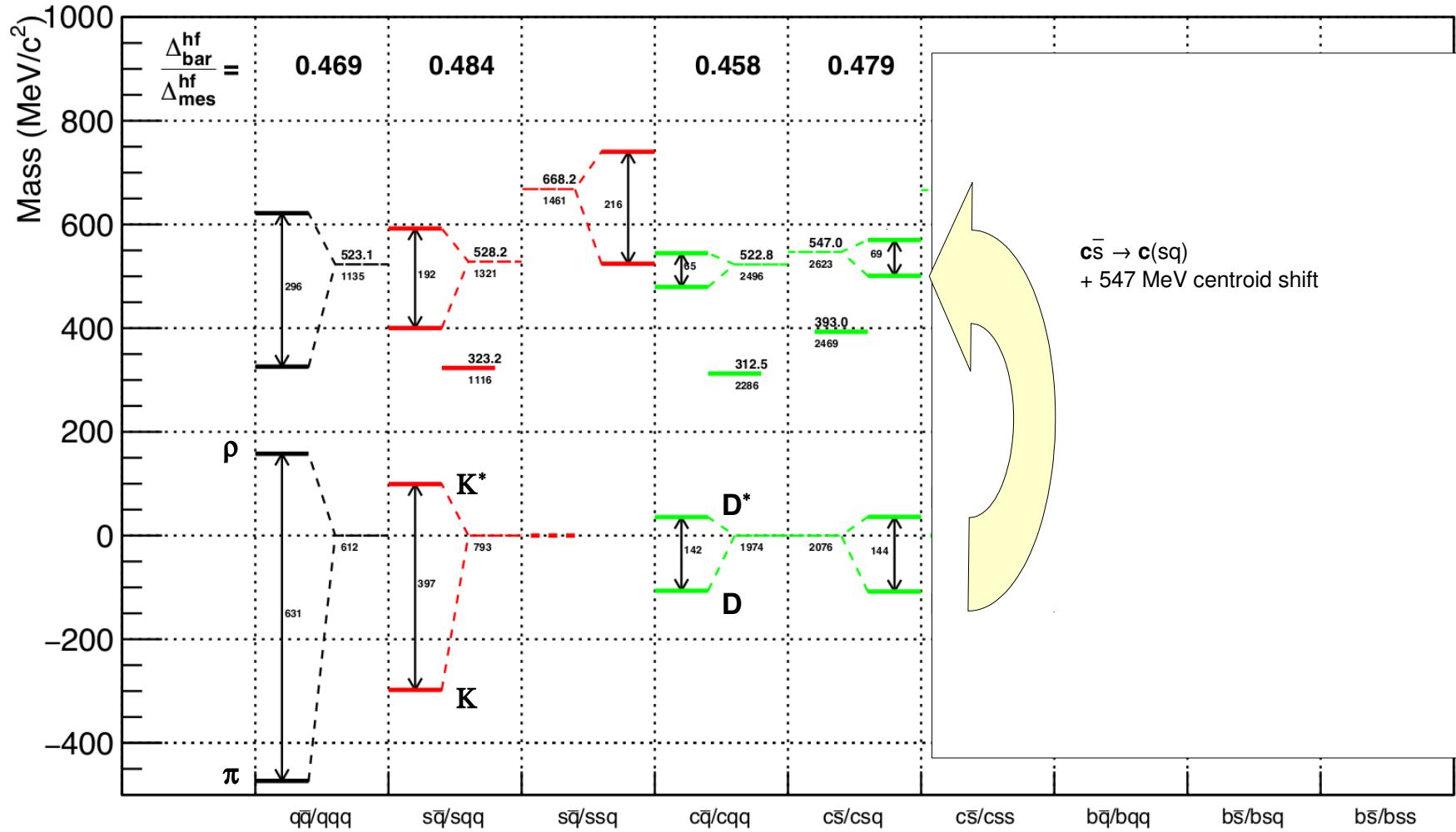
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Di-quarks: something more?

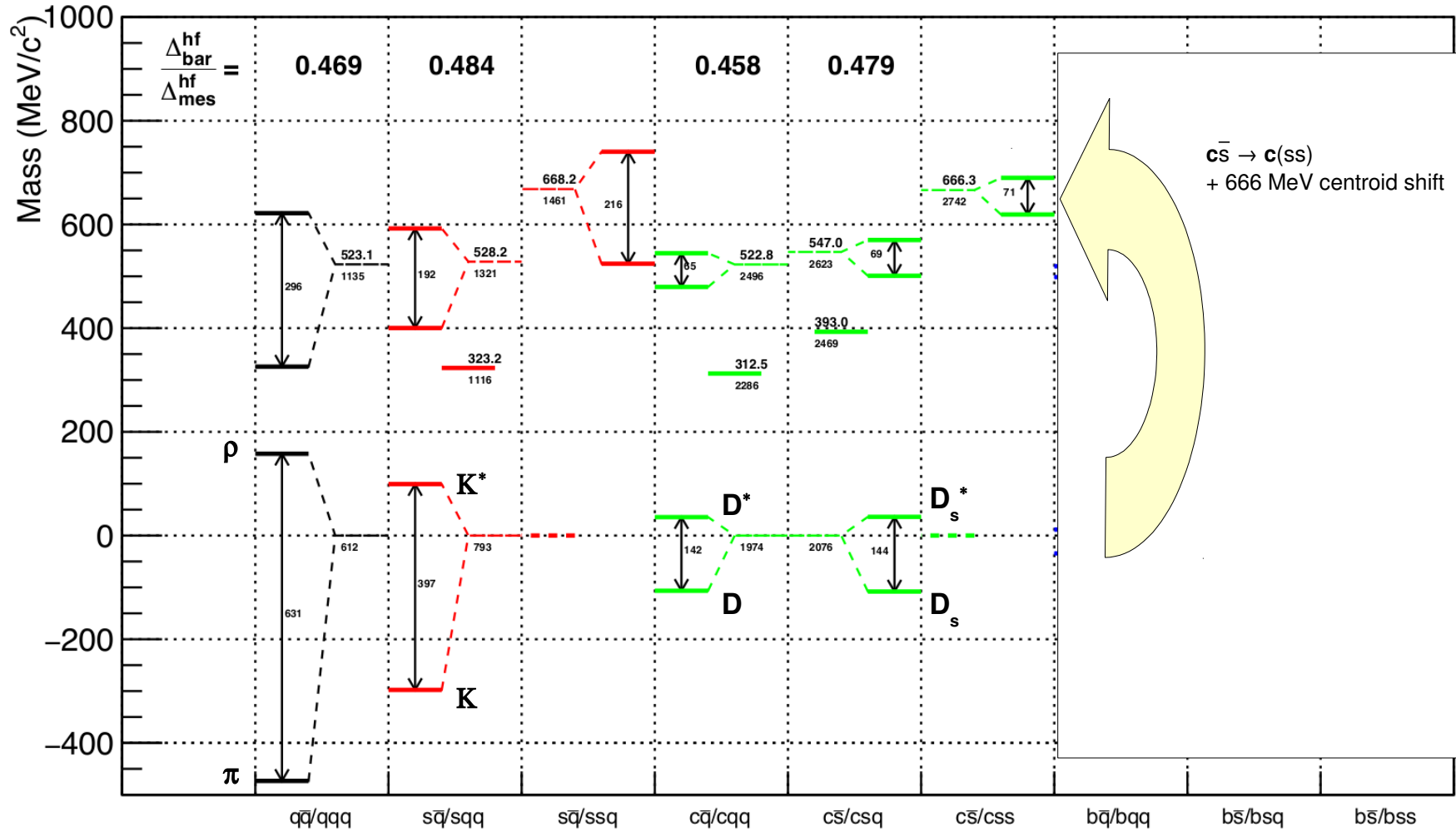
Frascati Phys.Ser. 60 (2015) 1-302



- $q\bar{q} \rightarrow q(qq)$
+ 523 MeV centroid shift
- $s\bar{q} \rightarrow s(qq)$
+ 528 MeV centroid shift
- $c\bar{q} \rightarrow c(qq)$
+ 523 MeV centroid shift
- $c\bar{s} \rightarrow c(sq)$
+ 547 MeV centroid shift
- $s\bar{q} \rightarrow s(sq)$
+ 668 MeV centroid shift

Di-quarks: something more?

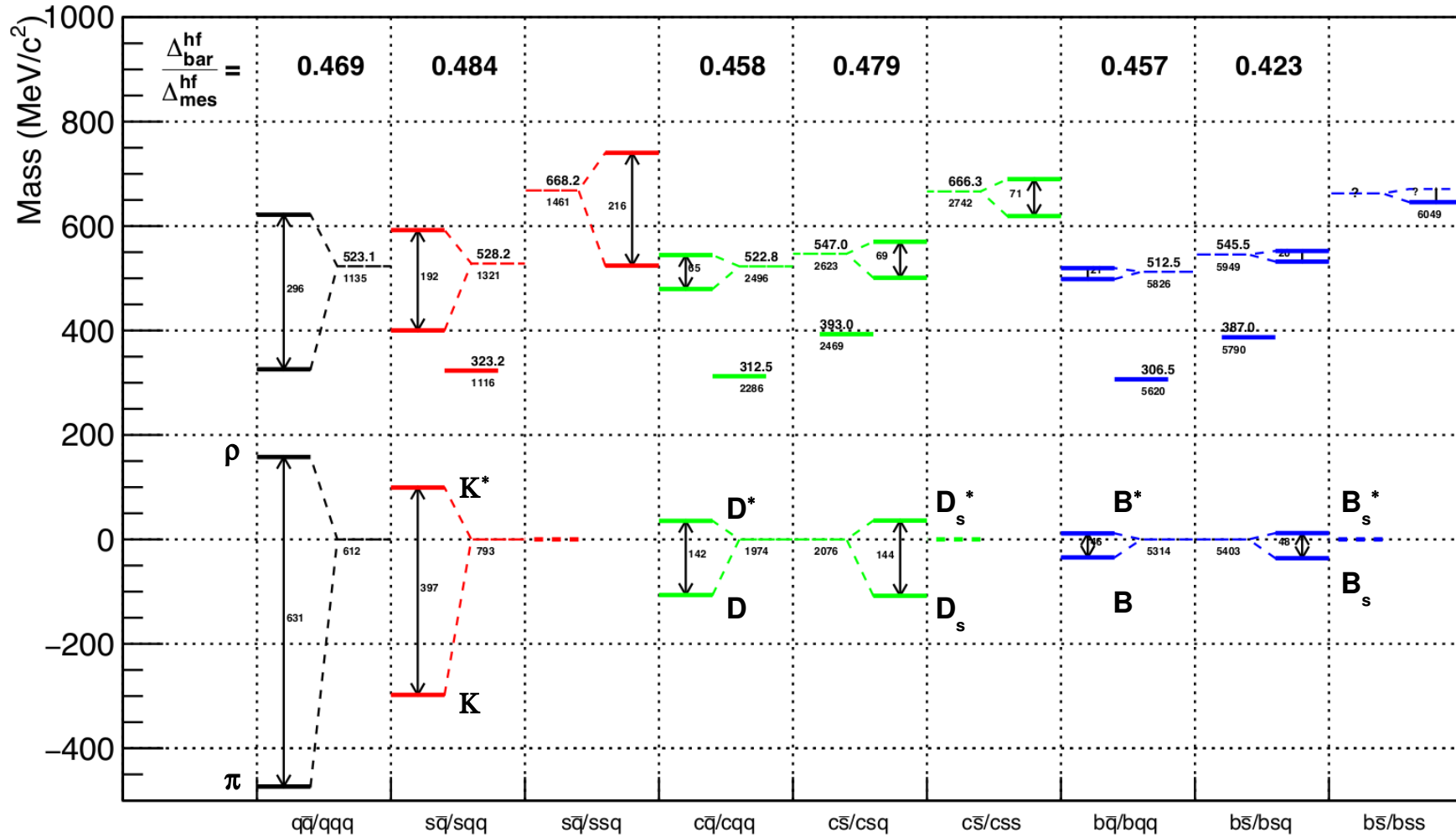
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- $c\bar{s} \rightarrow c(sq)$
+ 547 MeV centroid shift
- $s\bar{q} \rightarrow s(sq)$
+ 668 MeV centroid shift

Di-quarks: something more?

Frascati Phys.Ser. 60 (2015) 1-302



S=0 → S=0

- $q\bar{q} \rightarrow q(qq)$
+ 523 MeV centroid shift
- $s\bar{q} \rightarrow s(sq)$
+ 528 MeV centroid shift
- $c\bar{q} \rightarrow c(qq)$
+ 523 MeV centroid shift
- $b\bar{q} \rightarrow b(qq)$
+ 512 MeV centroid shift

S=1 → S=1

- $c\bar{s} \rightarrow c(sq)$
+ 547 MeV centroid shift
- $b\bar{s} \rightarrow b(sq)$
+ 547 MeV centroid shift

S=1 → S=2

- $s\bar{q} \rightarrow s(sq)$
+ 668 MeV centroid shift
- $c\bar{s} \rightarrow c(ss)$
+ 666 MeV centroid shift

Tetraquark candidates: matching the data

$Q\bar{Q}q\bar{q}$ ($q = u, d$)

A.Ali, talk @ B2TiP workshop 2015

Label	J^{PC}	charmonium-like		bottomonium-like	
		State	Mass [MeV]	State	Mass [MeV]
X_0	0^{++}	—	3756	—	10562.2
X'_0	0^{++}	—	4024	—	10652.2
X_1	1^{++}	$X(3872)$	3890	—	10607.2
Z	1^{+-}	$Z_c^+(3900)$	3890	$Z_b^{+,0}(10610)$	10607.2
Z'	1^{+-}	$Z_c^+(4020)$	4024	$Z_b^+(10650)$	10652.2
X_2	2^{++}	—	4024	—	10652.2
Y_1	1^{--}	$Y(4008)$	4024	$Y_b(10891)$	10891.1
Y_2	1^{--}	$Y(4260)$	4263	$Y_b(10987)$	10987.5
Y_3	1^{--}	$Y(4290)$ (or $Y(4220)$)	4292	—	10981.1
Y_4	1^{--}	$Y(4630)$	4607	—	11135.3
Y_5	1^{--}	—	6472	—	13036.8

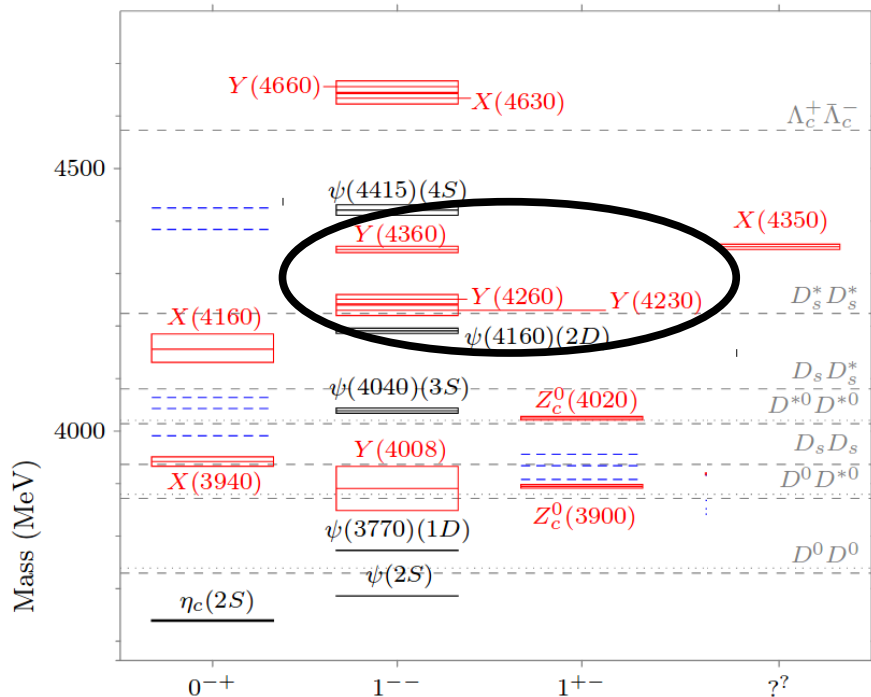
More states than observed ones....

$Q\bar{Q}s\bar{s}$

Phys.Rev. D93 (2016) no.9, 094024

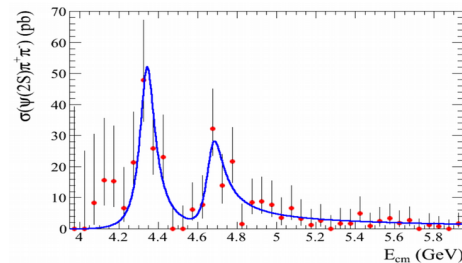
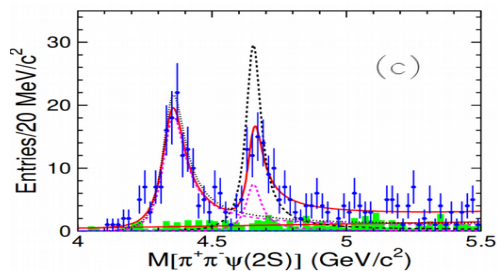
State	Pred. Mass	Observed
X_0 $ 0^{++}\rangle_1$	3920	$\chi_{c0}(3915)^*$
X'_0 $ 0^{++}\rangle_2$	4360	$X(4350)?$
X_1 $ 1^{++}\rangle$	4140	$Y(4140)^*$
Z $ 1^{+-}\rangle_1$	4140	
Z' $ 1^{+-}\rangle_2$	4360	
X_2 $ 2^{++}\rangle$	4360	$X(4350)?$
$ 0^{--}\rangle$	4320	$Y(4274)?$
$ 0^{-+}\rangle_1$	4320	$Y(4274)?$
$ 0^{-+}\rangle_2$	4540	
Y_1 $ 1^{--}\rangle_2$	3920	$Y(4008)$
Y_2 $ 1^{--}\rangle_1$	4230	$Y(4230)^*$
$ 1^{-+}\rangle_1$	4230	
$ 1^{-+}\rangle_2$	4450	
Y_3 $ 1^{--}\rangle_3$	4360	$Y(4360)^*$
Y_4 $ 1^{--}\rangle_4$	4630	$Y(4660)$
$ 2^{-+}\rangle_1$	4050	
$ 2^{-+}\rangle_2$	4270	$Y(4274)?$
$ 2^{--}\rangle_1$	4050	
$ 2^{--}\rangle_2$	4450	
$ 3^{--}\rangle$	4180	

The case of vector charmonia

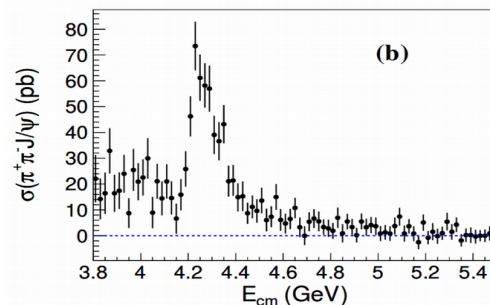
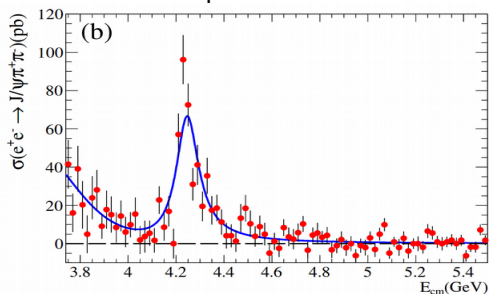


- Several states piled up
- Little (or none) overlap of decay modes
- **Y(4360) only in $\pi\pi \psi(2S)$**
- **Y(4260) only in $\pi\pi J/\psi$**

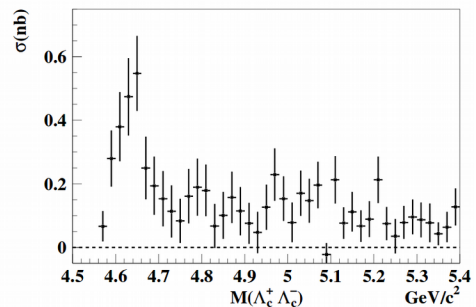
$$e^+e^- \rightarrow \pi\pi \psi(2S)$$



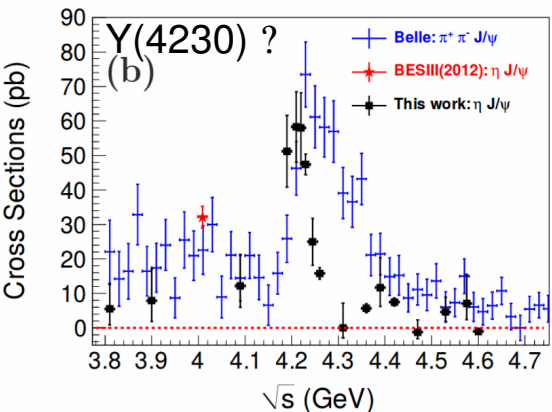
$$e^+e^- \rightarrow \pi\pi J/\psi$$



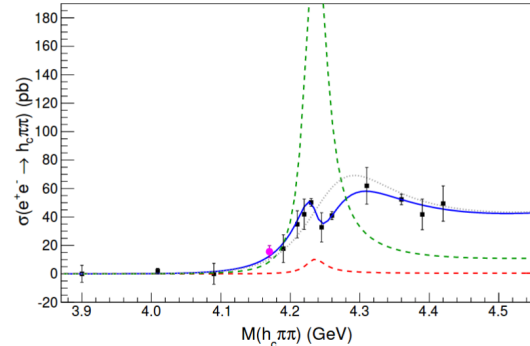
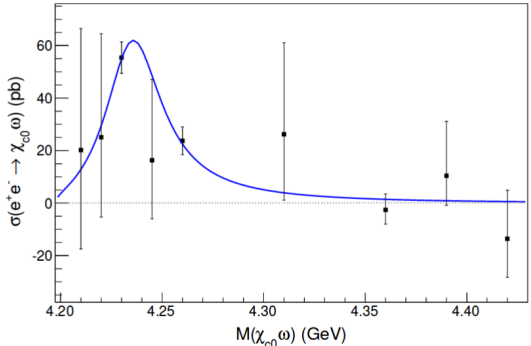
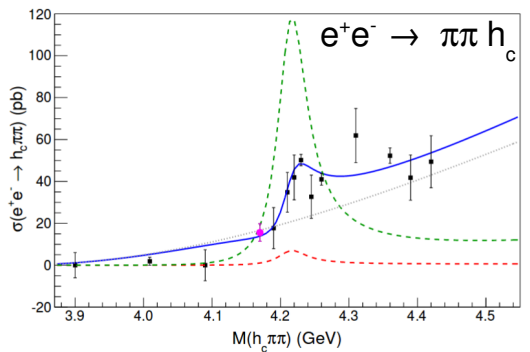
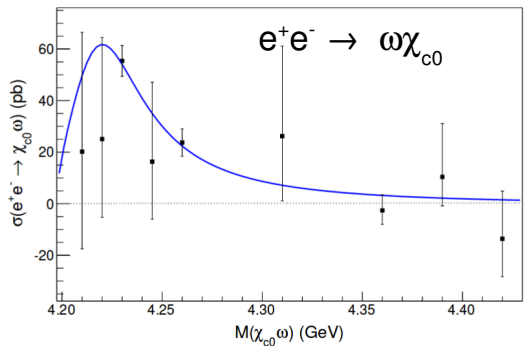
$$e^+e^- \rightarrow \Lambda_c^+ \bar{\Lambda}_c^-$$



Y(4260): how many states?



Phys.Rev. D91 (2015) no.11, 117501

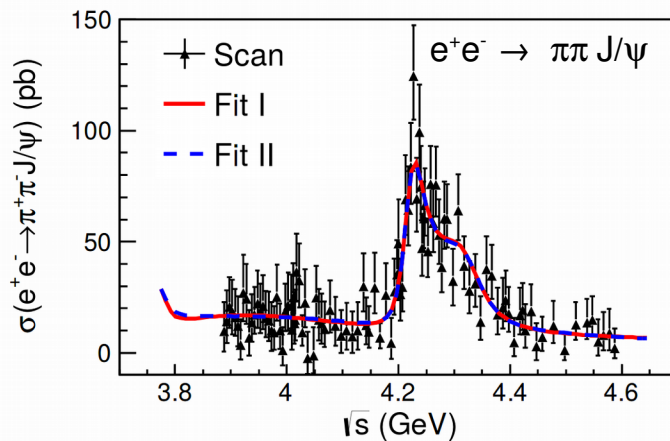
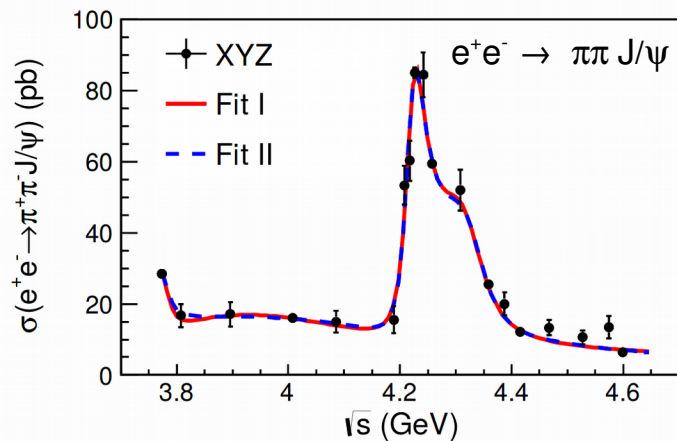


- Y(4360) only in $\pi\pi \psi(2S)$
- Y(4260) only in $\pi\pi J/\psi$
- Y(4230) $\eta J/\psi$
- also in $\pi\pi h_c, \omega\chi_c$
- better fit with Y(4230) + Y(4260)

m_1	$(4234.4 \pm 5.7) \text{ MeV}$
Γ_1	$(34 \pm 16) \text{ MeV}$
m_2	$(4255 \pm 18) \text{ MeV}$
Γ_2	$(158 \pm 52) \text{ MeV}$

Y(4260): yet other states!

BESIII scan: Phys. Rev. Lett. 118, 092001 (2017)



$M = 4222 \text{ MeV}, \Gamma = 44 \text{ MeV}$
 $M = 4320 \text{ MeV}, \Gamma = 101 \text{ MeV}$

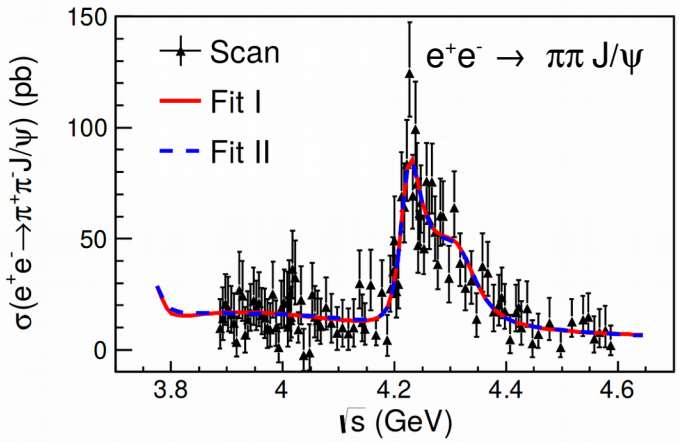
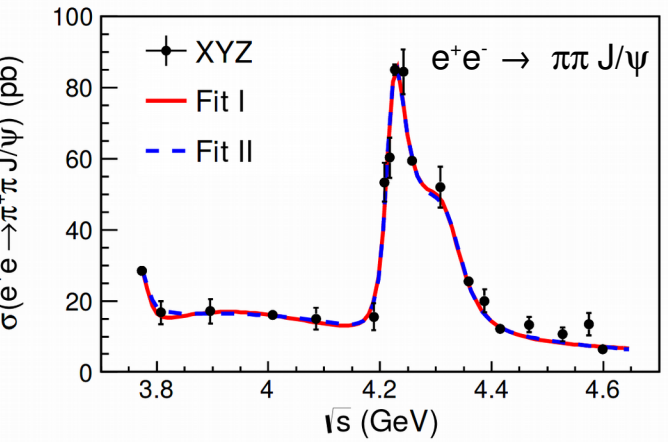
The Y(4260) simply does not exist!

Parameters	Fit result
$M(R_1)$	$3812.6^{+61.9}_{-36.6} (\dots)$
$\Gamma_{\text{tot}}(R_1)$	$476.9^{+78.4}_{-64.8} (\dots)$
$M(R_2)$	$4222.0 \pm 3.1 (4220.9 \pm 2.9)$
$\Gamma_{\text{tot}}(R_2)$	$44.1 \pm 4.3 (44.1 \pm 3.8)$
$M(R_3)$	$4320.0 \pm 10.4 (4326.8 \pm 10.0)$
$\Gamma_{\text{tot}}(R_3)$	$101.4^{+25.3}_{-19.7} (98.2^{+25.4}_{-19.6})$

Background PDF

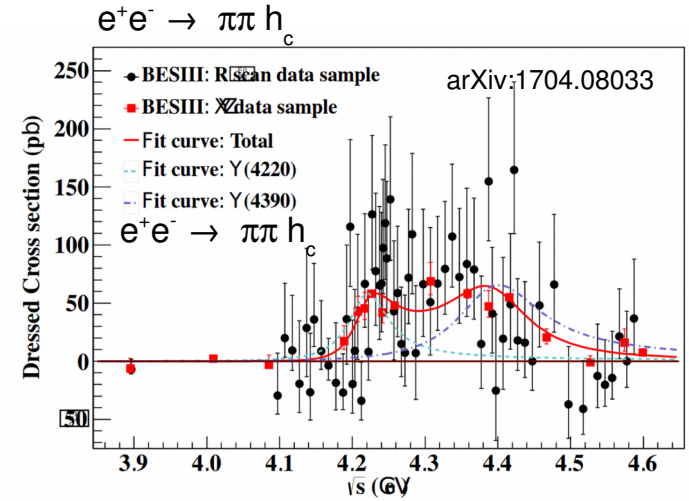
Y(4260): yet other states!

BESIII scan: Phys. Rev. Lett. 118, 092001 (2017)



$M = 4222 \text{ MeV}, \Gamma = 44 \text{ MeV}$
 $M = 4320 \text{ MeV}, \Gamma = 101 \text{ MeV}$

The Y(4260) simply does not exist!



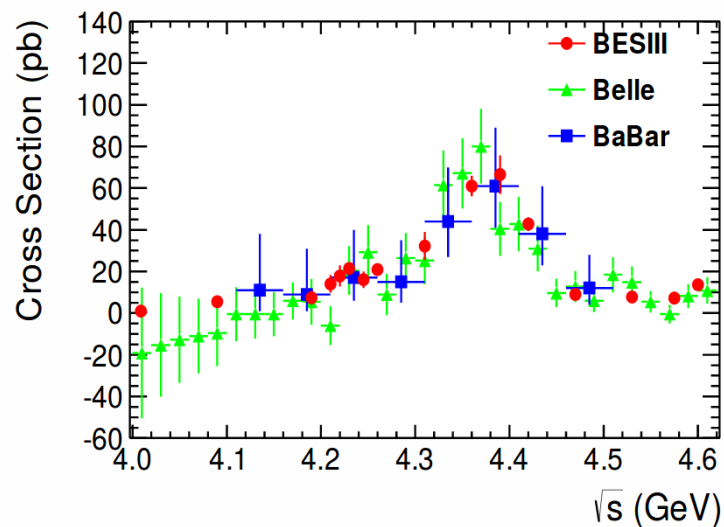
$M = 4218 \text{ MeV}, \Gamma = 66 \text{ MeV}$
 $M = 4391 \text{ MeV}, \Gamma = 140 \text{ MeV}$

In summary, Y(4260) region hosts in total 4 $J^{PC} = 1^-$ states:

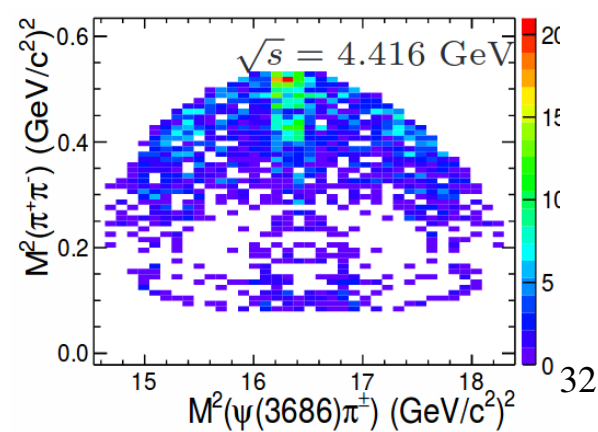
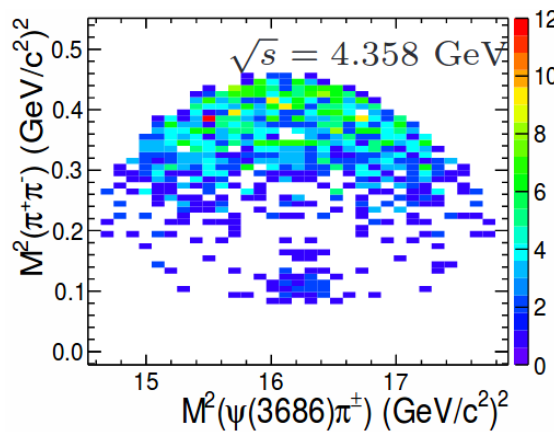
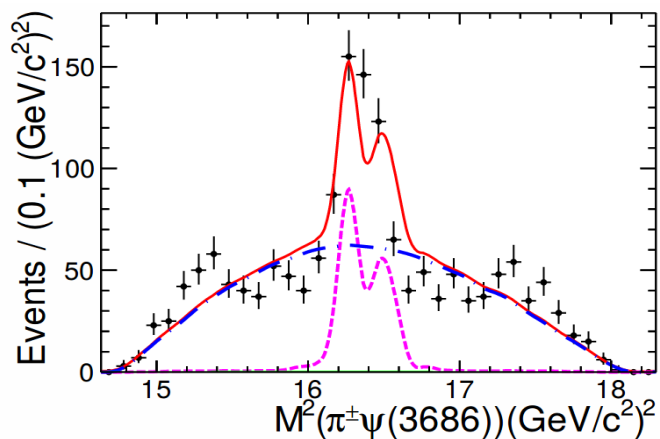
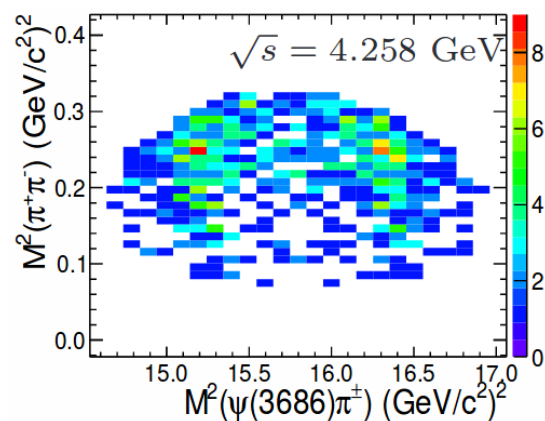
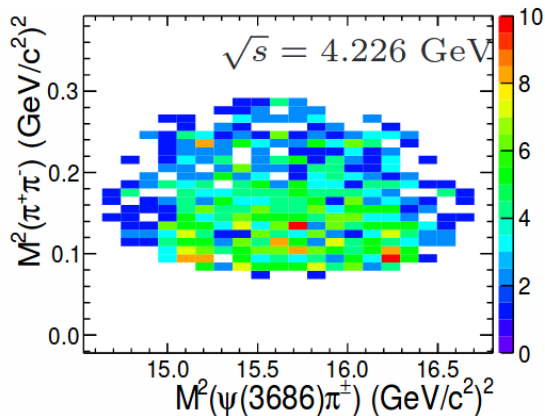
- Y(4230) [$\Gamma \sim 50 \text{ MeV}$] in all the decay modes, including $\omega\chi_c$ and $\eta J/\psi$
- Y(4320) [$\Gamma \sim 100 \text{ MeV}$] only in $\pi\pi J/\psi$
- Y(4360) [$\Gamma \sim 50 \text{ MeV}$] only in $\pi\pi \psi'$
- Y(4390) [$\Gamma \sim 140 \text{ MeV}$] only in $\pi\pi h_c$

Breaking news!

arXiv:1703.08787 [hep-ex], $e^+e^- \rightarrow \pi\pi\psi'$



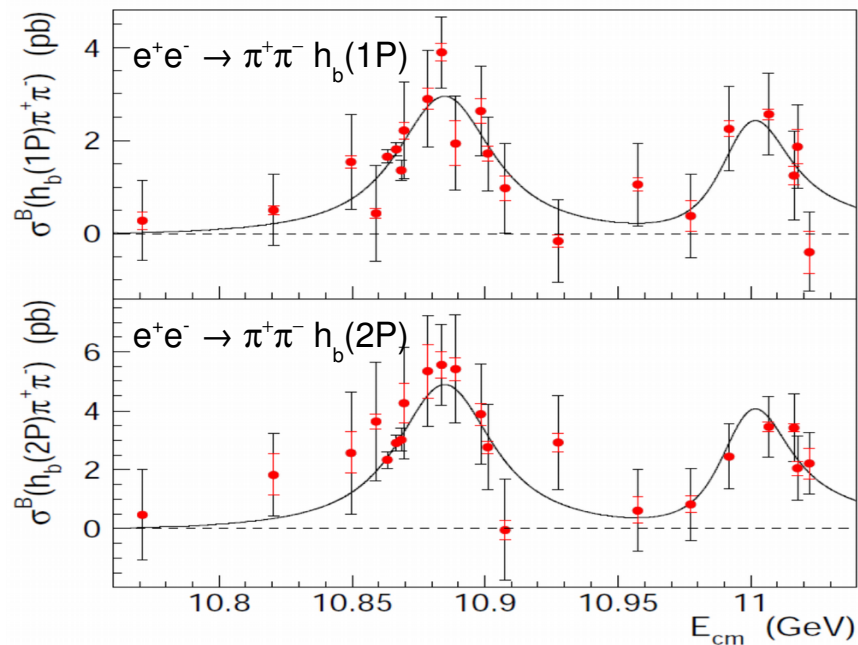
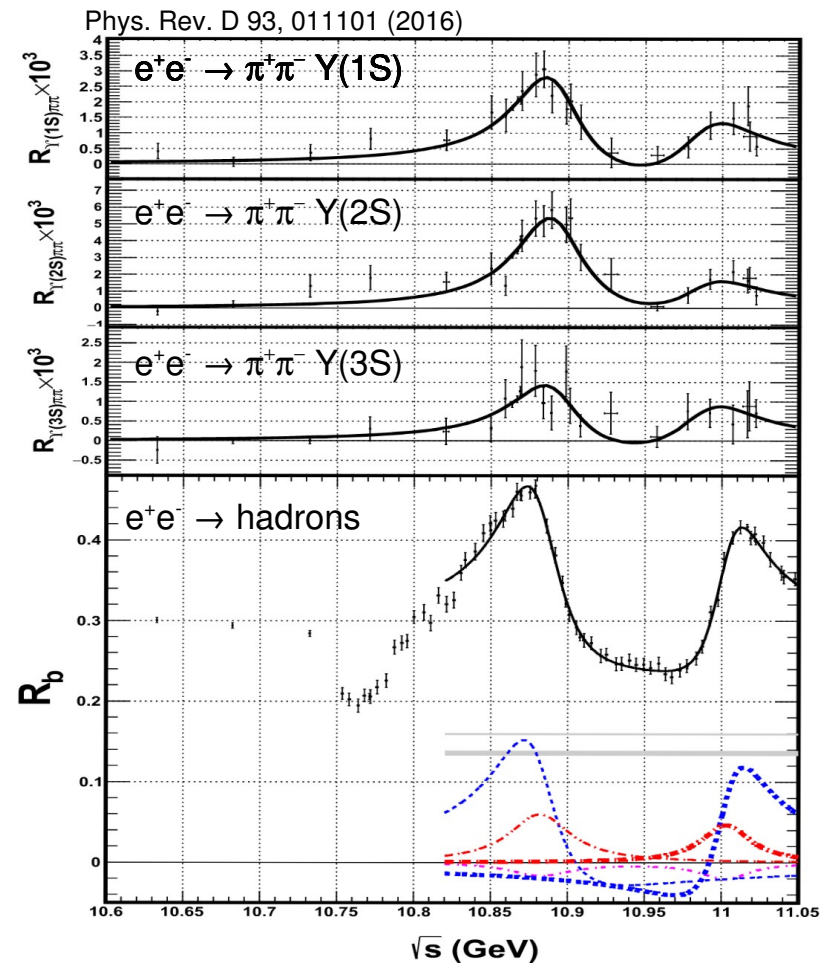
Some structures are there, but a good fit has not been found yet



A look at Bottomonium

Comparing the spectra it is reasonable (at first) to relate $Y(4260)$ and $Y(5S)$

Yet, the situation is rather different!

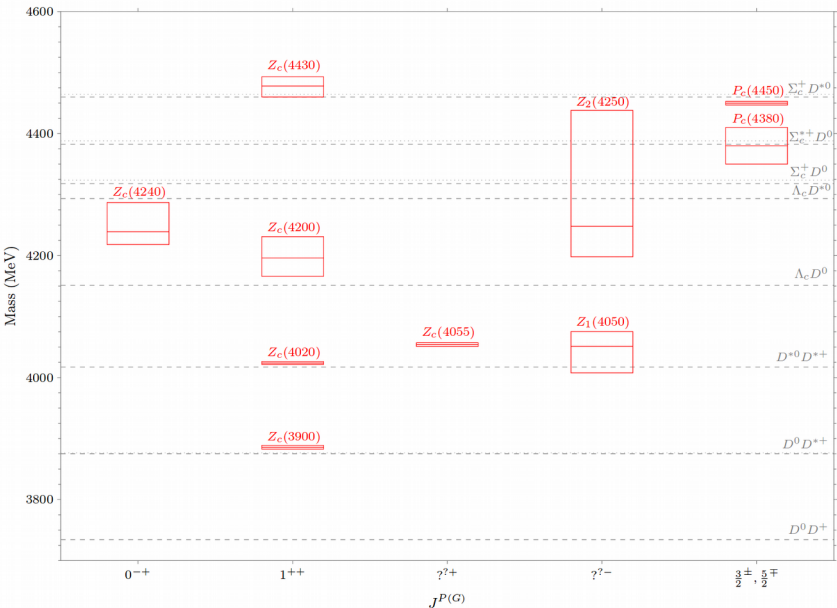


Part II: what's next

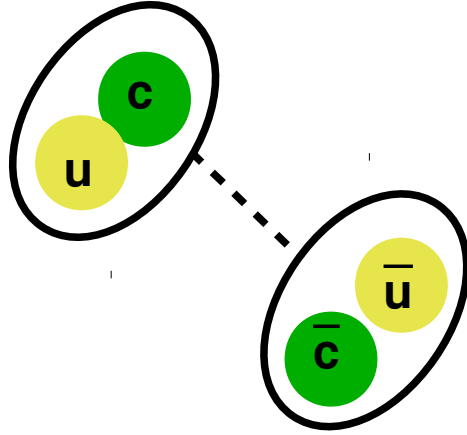
- Probing the exotic's nature
- New approaches to the light sector?
- Heavy meson annihilations as probes for collective effects

Exotica: alternative models

Compact tetraquarks are not the only model on the market



Several exotica are on a meson-meson threshold.
 → Hadronic molecules?



Loosely bound states of color singlets

Powerful model: describes effects in light mesons and baryon sector as well
 (**very recent review: arXiv:1705.00141**)

Matches well with data in some cases

Zb, Zc
 X(3872)

Phys. Rev. Lett. 116, 212001

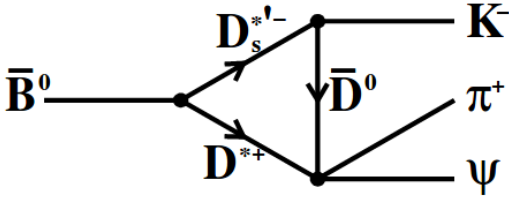
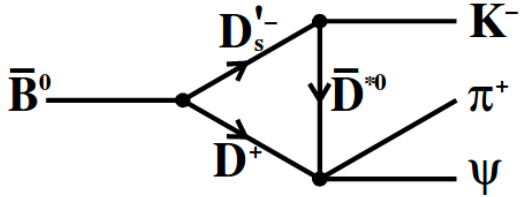
Channel	Fraction, %	
	$Z_b(10610)$	$Z_b(10650)$
$\Upsilon(1S)\pi^+$	$0.54^{+0.16+0.11}_{-0.13-0.08}$	$0.17^{+0.07+0.03}_{-0.06-0.02}$
$\Upsilon(2S)\pi^+$	$3.62^{+0.76+0.79}_{-0.59-0.53}$	$1.39^{+0.48+0.34}_{-0.38-0.23}$
$\Upsilon(3S)\pi^+$	$2.15^{+0.55+0.60}_{-0.42-0.43}$	$1.63^{+0.53+0.39}_{-0.42-0.28}$
$h_b(1P)\pi^+$	$3.45^{+0.87+0.86}_{-0.71-0.63}$	$8.41^{+2.43+1.49}_{-2.12-1.06}$
$h_b(2P)\pi^+$	$4.67^{+1.24+1.18}_{-1.00-0.89}$	$14.7^{+3.2+2.8}_{-2.8-2.3}$
$B^+\bar{B}^{*0} + \bar{B}^0B^{*+}$	$85.6^{+1.5+1.5}_{-2.0-2.1}$...
$B^{*+}\bar{B}^{*0}$...	$73.7^{+3.4+2.7}_{-4.4-3.5}$

Decay of a molecule into its components

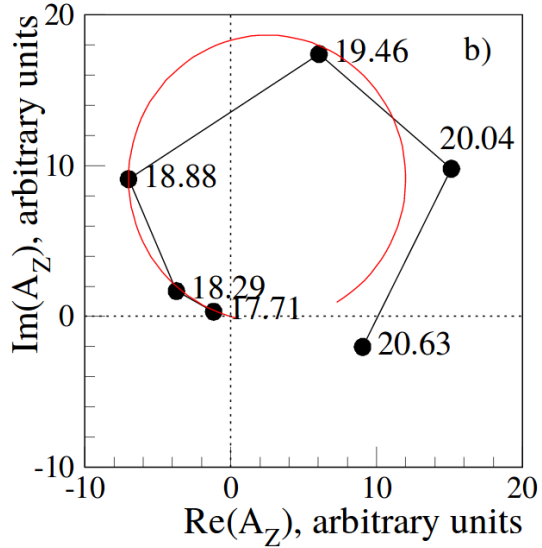
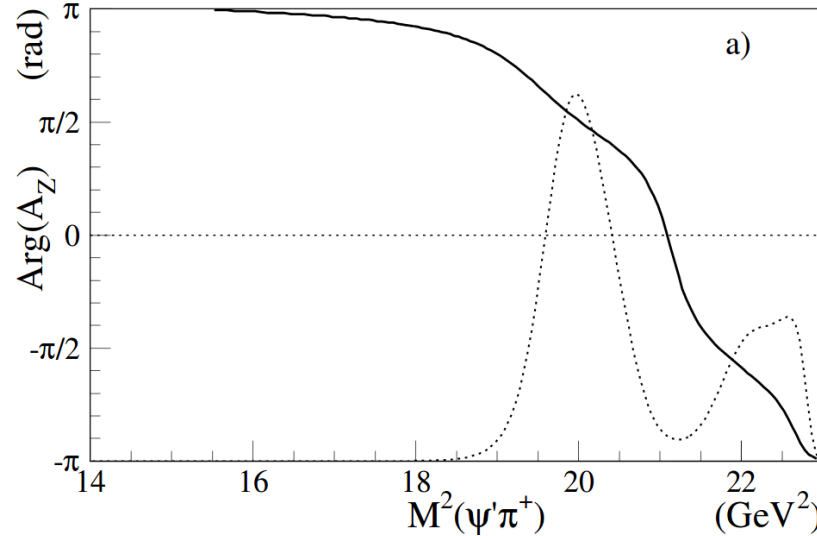
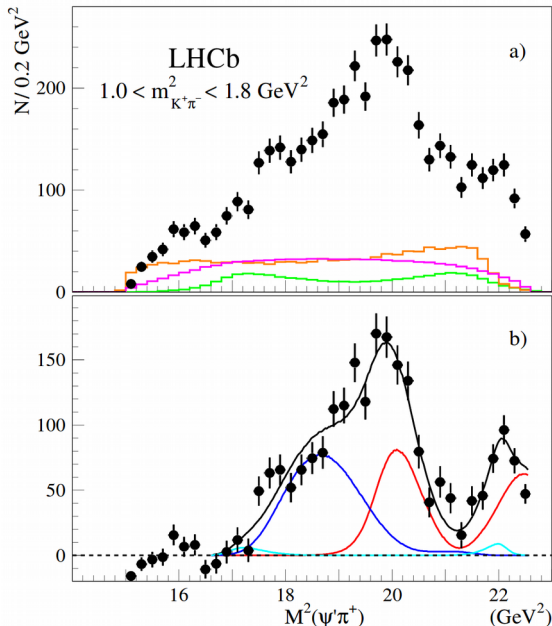
Exotica: alternative models

Several exotica are on a meson-meson threshold.
 → Dynamic effects?

Phys.Lett. B748 (2015) 183-186



Can describe the $Z(4430)$ even in the phase structure



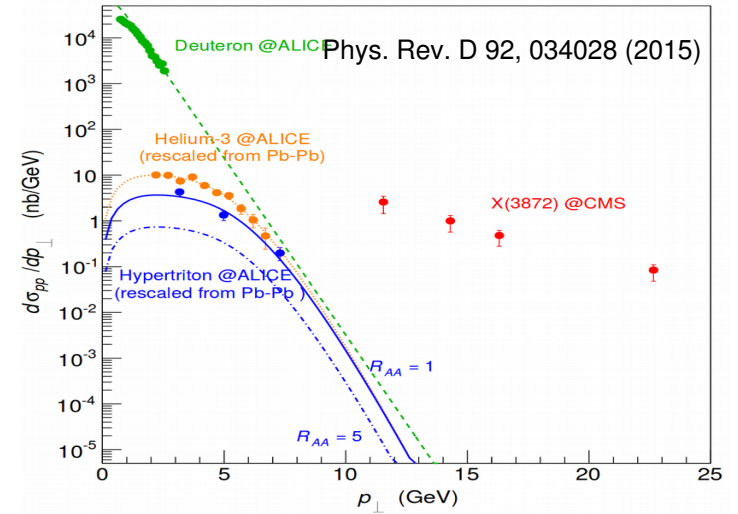
X(3872) in hadronic events

Esposito et Al, Phys. Rev. D 92, 034028 (2015)

If the X(3872) is a loosely bound molecule like deuteron, it's not likely to be produced at high p_T in hadron collisions, while

If the X(3872) is a compact tetraquark, it can.

Inclusive production as probe of the exotic's nature



Inclusive production as probe

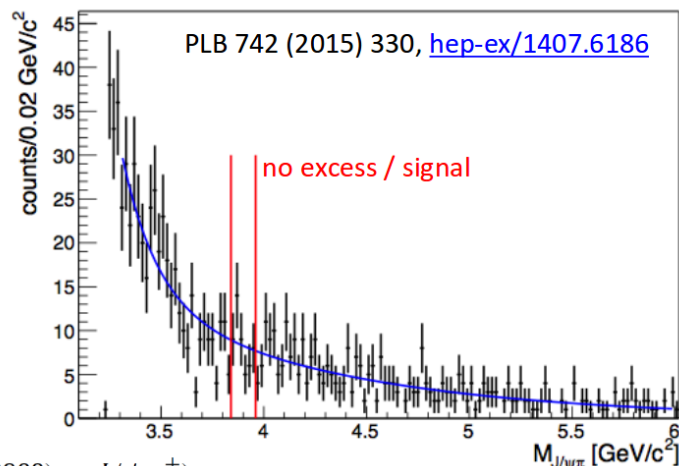
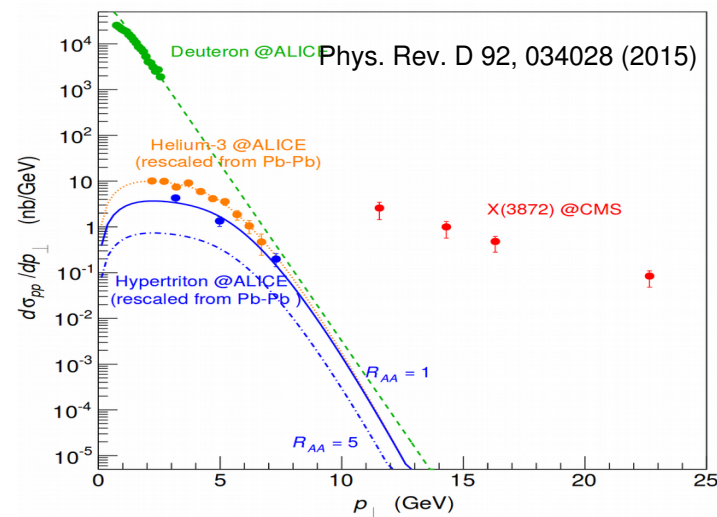
Esposito et Al, Phys. Rev. D 92, 034028 (2015)

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Inclusive production as probe of the exotic's nature

Compass 2015: no $Z_c(3900)$!



$$\frac{BR(Z_c^{\pm}(3900) \rightarrow J/\psi\pi^{\pm}) \times \sigma_{\gamma N \rightarrow Z_c^{\pm}(3900)N}}{\sigma_{\gamma N \rightarrow J/\psi N}} < 3.7 \cdot 10^{-3}$$

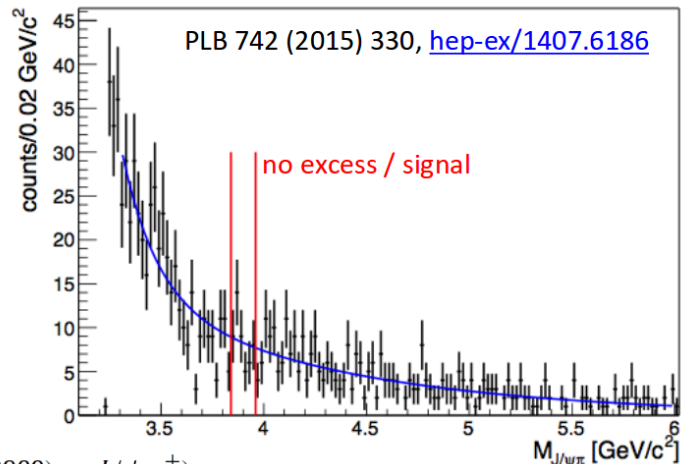
Inclusive production as probe

Esposito et Al, Phys. Rev. D 92, 034028 (2015)

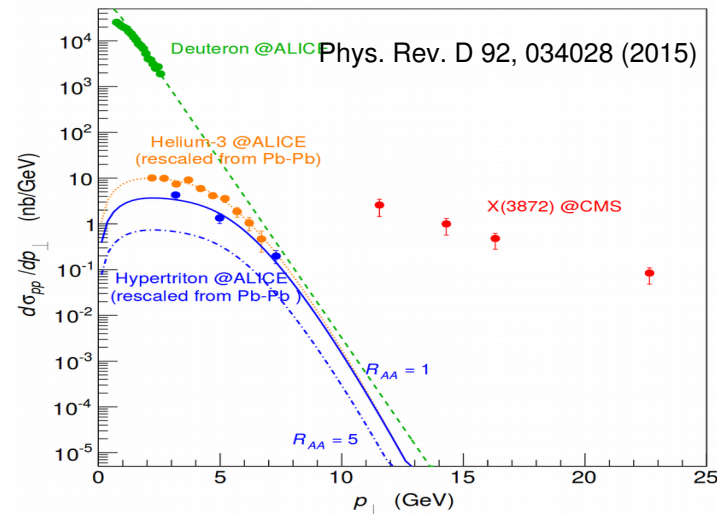
If the X(3872) is a loosely bound molecule like deuteron, it's not likely to be produced at high p_T in hadron collisions, while
 If the X(3872) is a compact tetraquark, it can.

Inclusive production as probe of the exotic's nature

Compass 2015: no $Z_c(3900)$!



$$\frac{BR(Z_c^\pm(3900) \rightarrow J/\psi \pi^\pm) \times \sigma_{\gamma N \rightarrow Z_c^\pm(3900)N}}{\sigma_{\gamma N \rightarrow J/\psi N}} < 3.7 \cdot 10^{-3}$$



Results on other exotica from low-energy hadronic events?

Inclusive production as probe in $Y(1S)$ decays

Esposito et Al, Phys. Rev. D 92, 034028 (2015)

If the $X(3872)$ is a loosely bound molecule like deuteron, it's not likely to be produced at high p_T in hadron collisions, while

If the $X(3872)$ is a compact tetraquark, it can.

Inclusive production as probe of the exotic's nature

$Y(nS)$ annihilations provide hadronic events

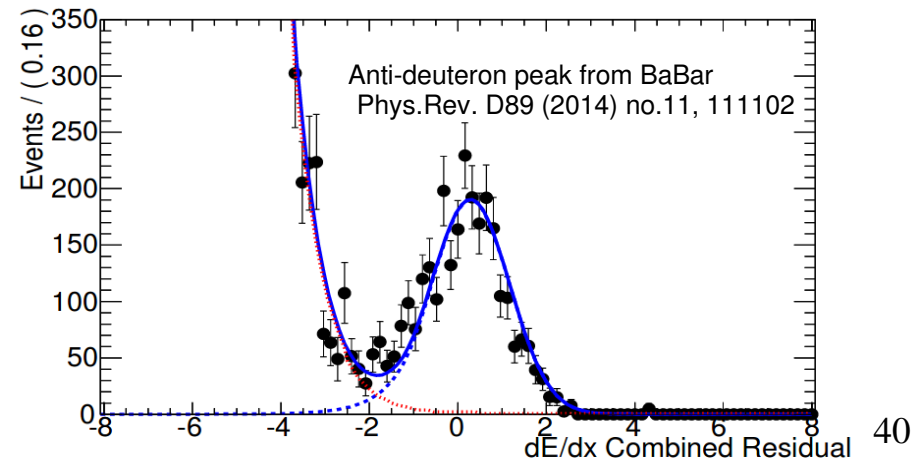
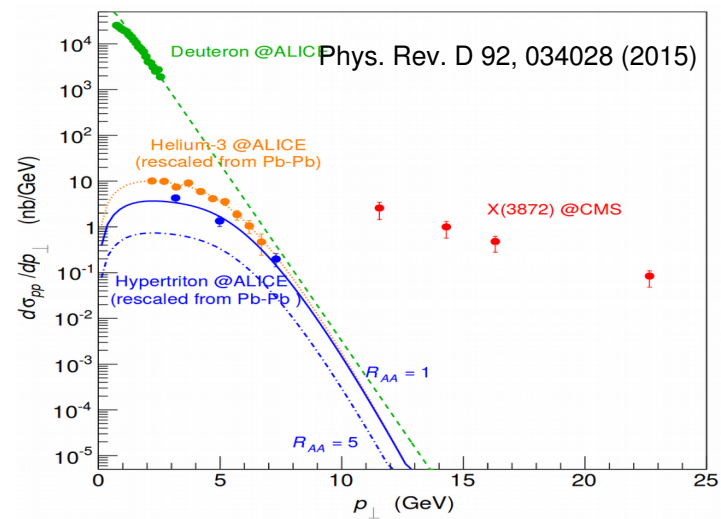
Small phase space, but very high partonic density

10 GeV in $r \sim 0.1$ fm

Known production of deuteron

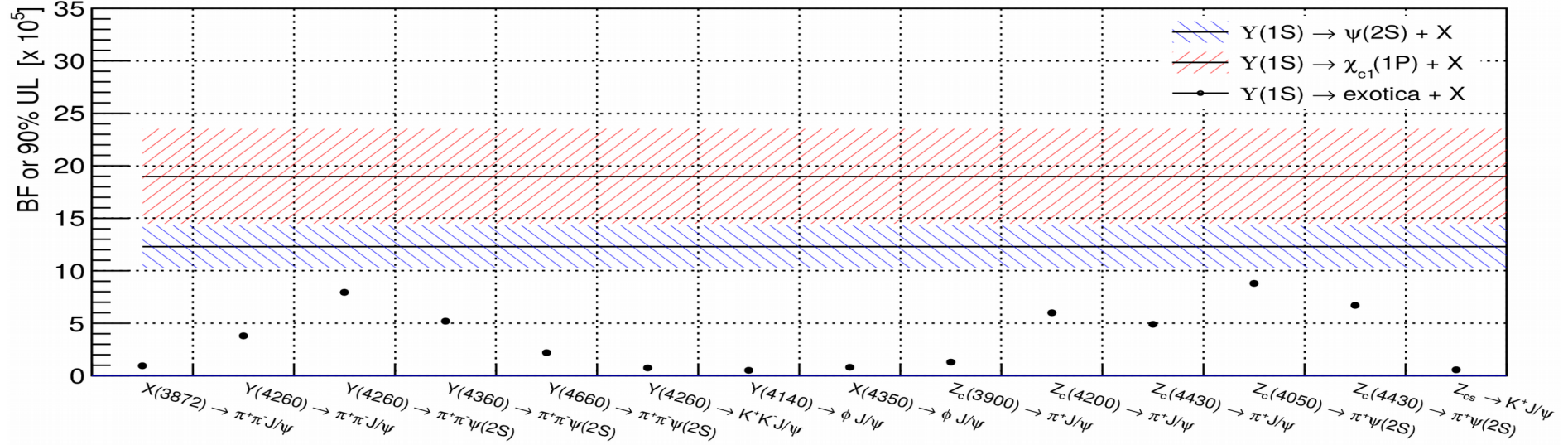
Phys.Rev. D89 (2014) no.11, 111102

Process	Rate
$\mathcal{B}(\Upsilon(3S) \rightarrow \bar{d}X)$	$(2.33 \pm 0.15^{+0.31}_{-0.28}) \times 10^{-5}$
$\mathcal{B}(\Upsilon(2S) \rightarrow \bar{d}X)$	$(2.64 \pm 0.11^{+0.26}_{-0.21}) \times 10^{-5}$
$\mathcal{B}(\Upsilon(1S) \rightarrow \bar{d}X)$	$(2.81 \pm 0.49^{+0.20}_{-0.24}) \times 10^{-5}$
$\sigma(e^+e^- \rightarrow \bar{d}X) [\sqrt{s} \approx 10.58 \text{ GeV}]$	$(9.63 \pm 0.41^{+1.17}_{-1.01}) \text{ fb}$
$\frac{\sigma(e^+e^- \rightarrow \bar{d}X)}{\sigma(e^+e^- \rightarrow \text{Hadrons})}$	$(3.01 \pm 0.13^{+0.37}_{-0.31}) \times 10^{-6}$



Exotic $c\bar{c}$ in $Y(1S)$

Belle, Phys. Rev. D 93, 112013

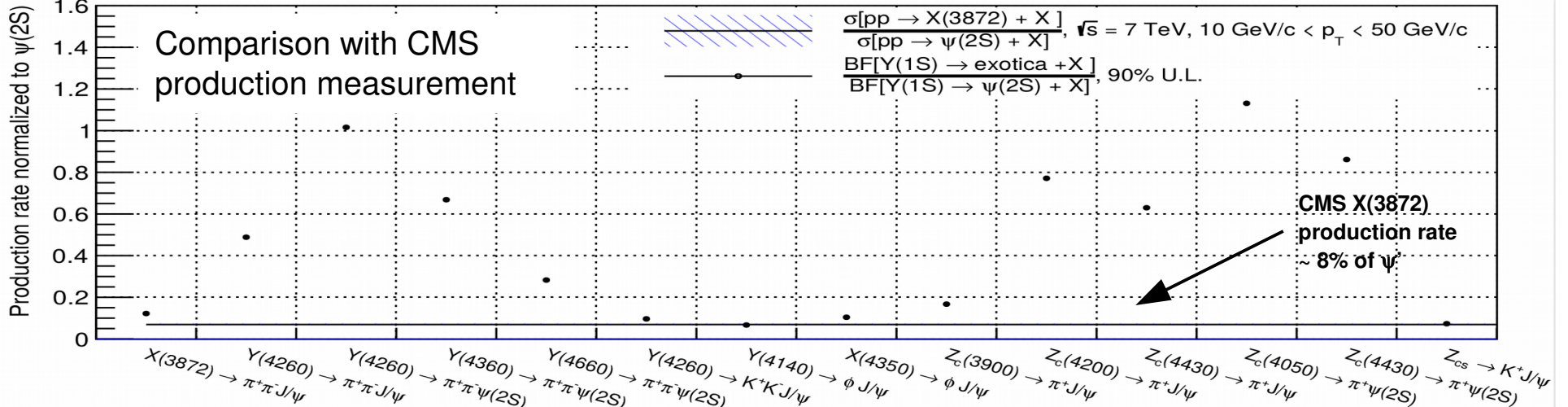
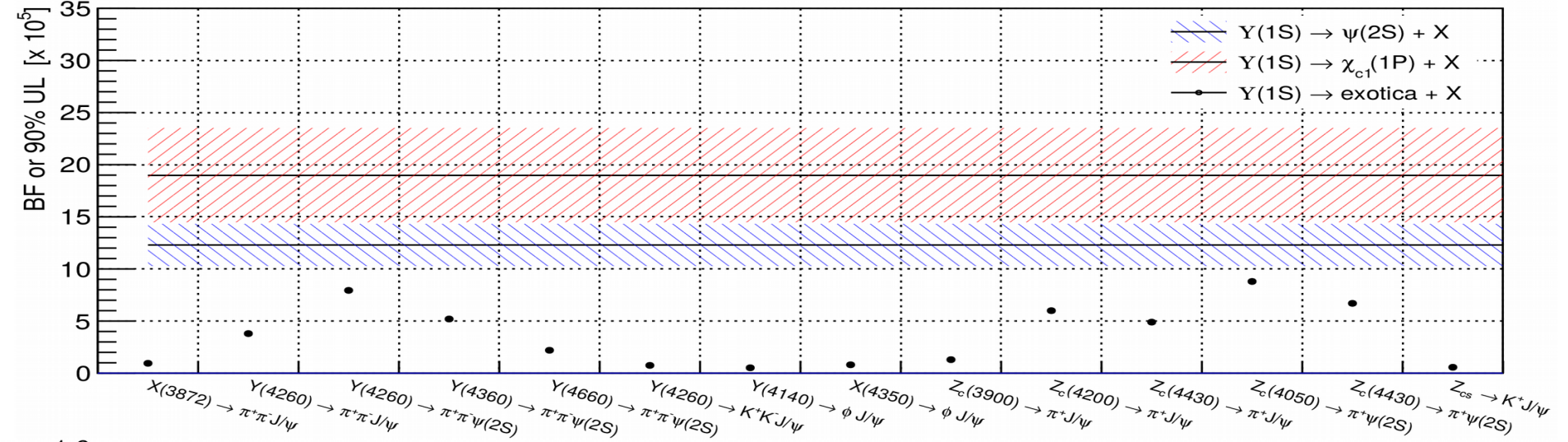


Belle 2017: Inclusive production of exotic and conventional charmonia in $Y(1S)$ annihilations

- No exotica
- What can we compare with?
 - CMS measurement of $X(3872)$ production

Exotic $c\bar{c}$ in $Y(1S)$

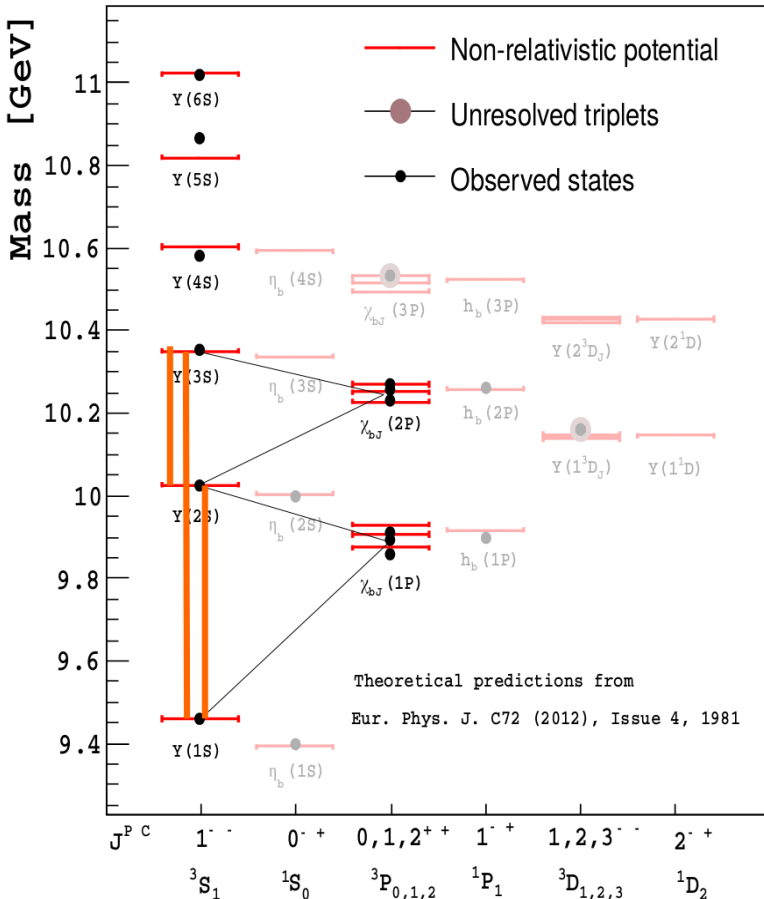
Belle, Phys. Rev. D 93, 112013



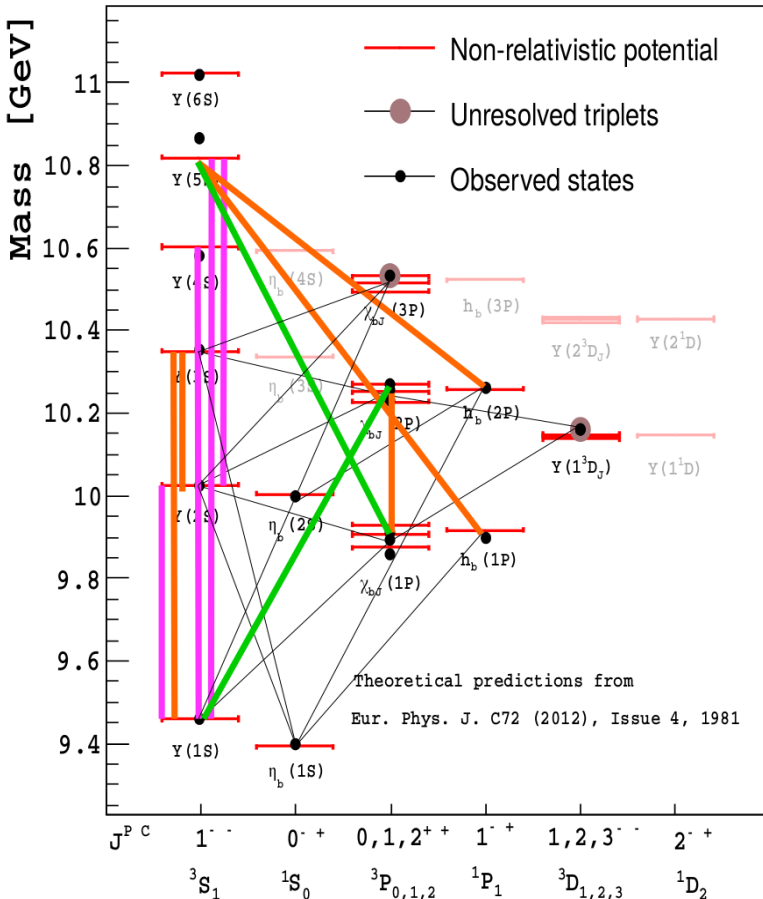
Transitions as a new probe

... and outstanding progresses in the study of transitions with the discovery of several selection rule violations.

Transitions pattern circa year 2000



Transitions pattern year 2015



Transitions as a new probe for light exotica

Di-pion transitions among quarkonia can be modeled as the emission of a gluon pair in the **QCD Multipole Expansion** formalism

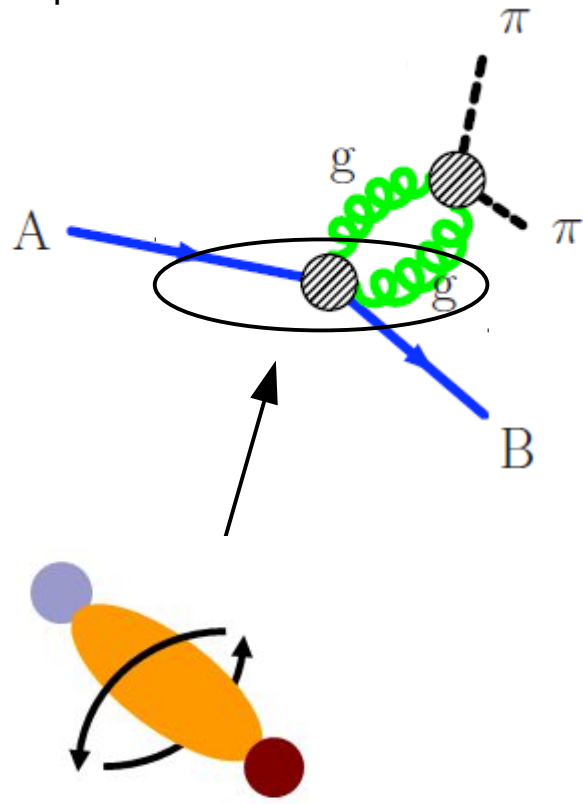
Intermediate $q\bar{q}g$ states can be factorized

$$\mathcal{M}(\Phi_i \rightarrow \Phi_f + h) = \frac{1}{24} \sum_{KL} \frac{\langle f | d_{m}^{ia} | KL \rangle \langle KL | d_{na}^j | i \rangle}{E_i - E_{KL}} \langle h | \mathbf{E}^{ai} \mathbf{E}_a^j | 0 \rangle$$

Phys.Rev. D76 (2007) 074035

The transition of higher excited states of quarkonia into lower ones (including the ground state) without flavor change but emitting photon or light mesons is believed to offer rich information on the hadron structure and governing dynamics, especially for the heavy quarkonia physics, for example, Brambilla *et al.* [23] studied the quarkonium radiative decays which are realized via electromagnetic interactions.

Our studies indicate that the transitions of $\psi(ns)(\Upsilon(ns)) \rightarrow \psi(ms)(\Upsilon(ms)) + \pi\pi$ may provide valuable information about the hybrid structures which have so far not been identified in experiments yet.



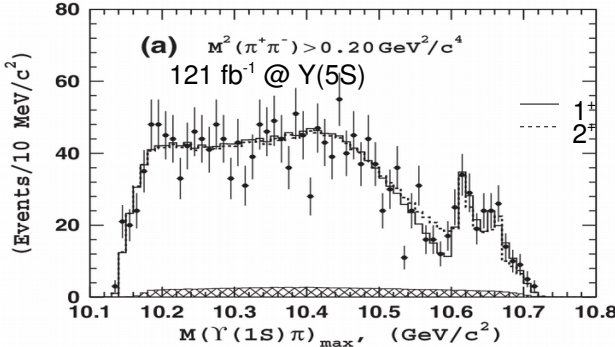
Scalar mesons in di-pion transitions

Phys.Rev. D91 (2015) no.7, 072003

$$Y(5S) \rightarrow \pi\pi Y(1S)$$

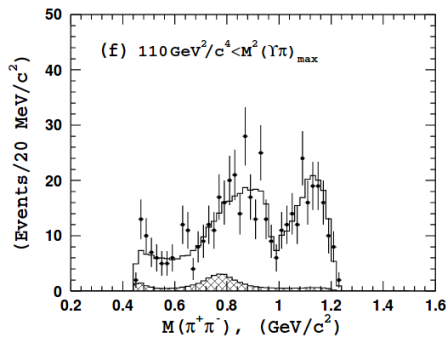
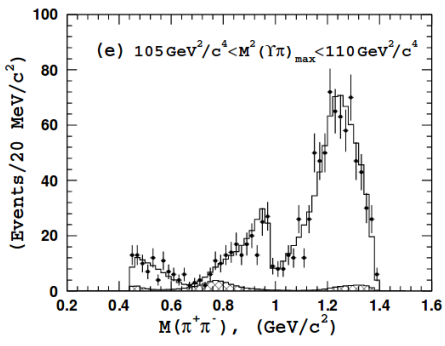
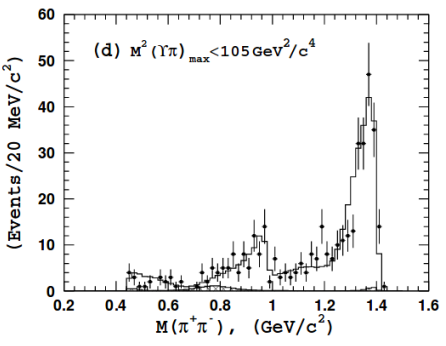
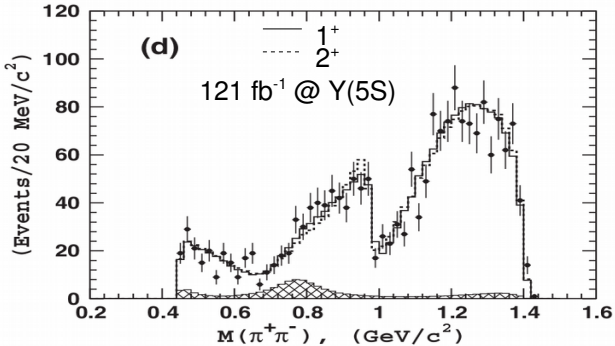
$$\mathcal{M}_{Y\pi\pi} = \mathcal{A}_{Z_1\pi} + \mathcal{A}_{Z_2\pi} + \mathcal{A}_{Y\sigma} + \mathcal{A}_{Yf_0} + \mathcal{A}_{Yf_2} + \mathcal{A}_{NR}$$

Y(1S)π⁺π⁻



- Dalitz structure contains several 0⁺⁺ contributions
- Statistics is too limited to fit them now

→ Possibility for BelleII to contribute to solve the scalar meson puzzle?



Pion scattering length from di-pion transitions

At low energy the $\pi\pi$ interaction is described by two scattering lengths who vanish in the chiral limit:

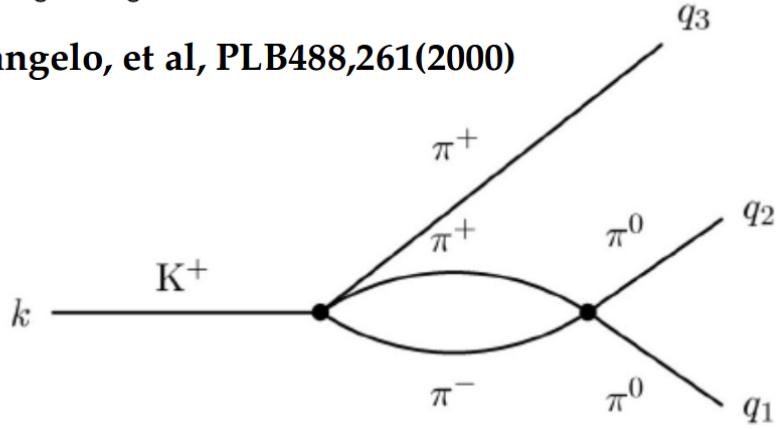
$$a_0^0 = \frac{7M_\pi^2}{32\pi F_\pi^2} + \mathcal{O}(m_q^2) \quad a_0^2 = -\frac{M_\pi^2}{16\pi F_\pi^2} + \mathcal{O}(m_q^2)$$

Weinberg, PRL17,616(1966)

Using ChPT, theory predicts:

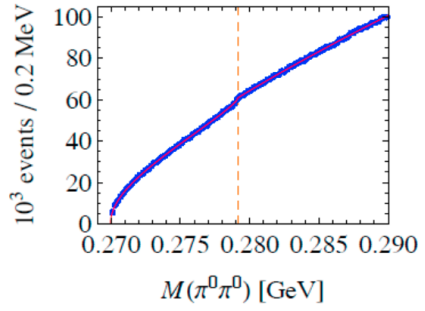
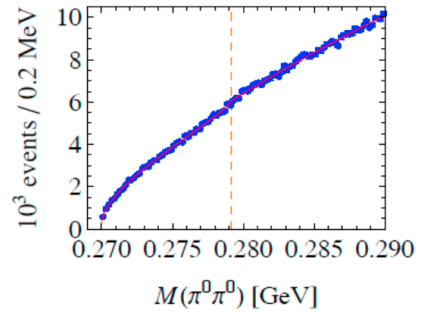
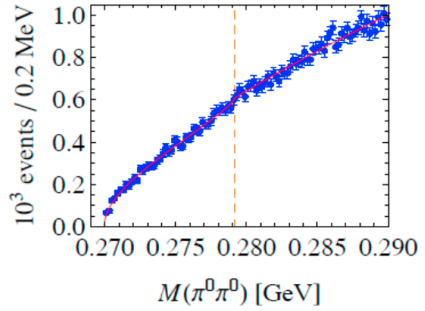
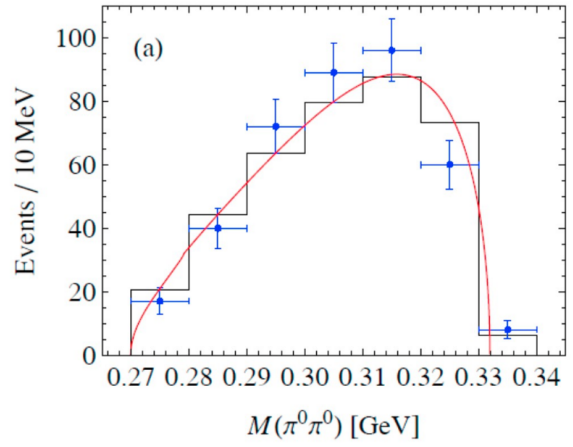
$$a_0^0 - a_0^2 = 0.265 \pm 0.004$$

Colangelo, et al, PLB488,261(2000)



Q-value for $Y(3S) \rightarrow \pi\pi$ $Y(2S)$ is only 50 MeV

Liu et al, EPJC73, 2284 (2013)



Conclusions

The phenomenology of exotica is broad and not confined to the discovery of new resonances

What we need now is:

- *Systematic, high statistics measurement of the hadronic transitions*
 - *New way to access the hybrids?*

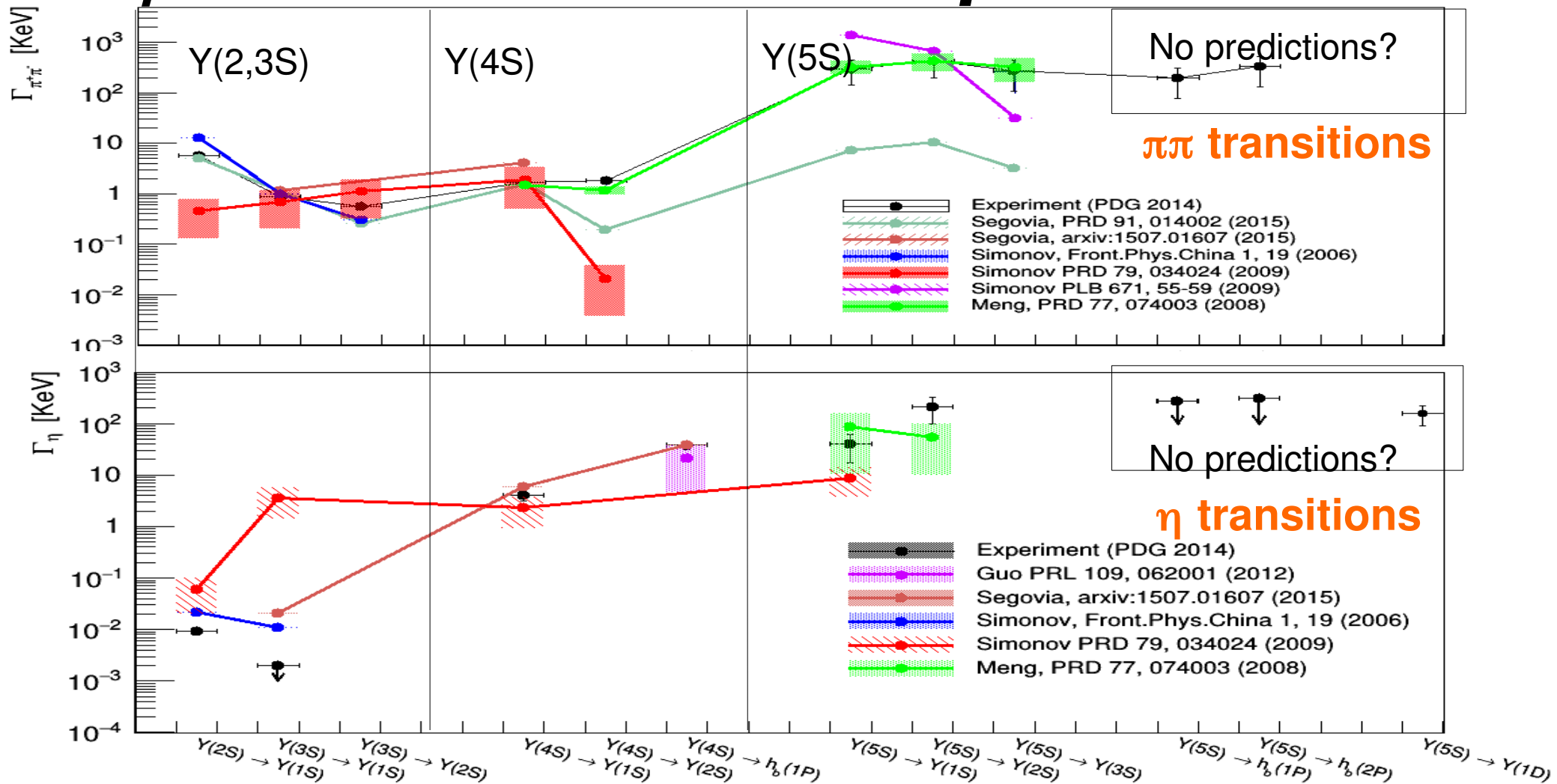
- *Theoretical breakthroughs*
 - *Prominent role of di-quark correlations?*
 - *Meson – Baryon – Tetraquark symmetries ?*
 - *Common models?*

- *Measurement of inclusive production in hadronic events*

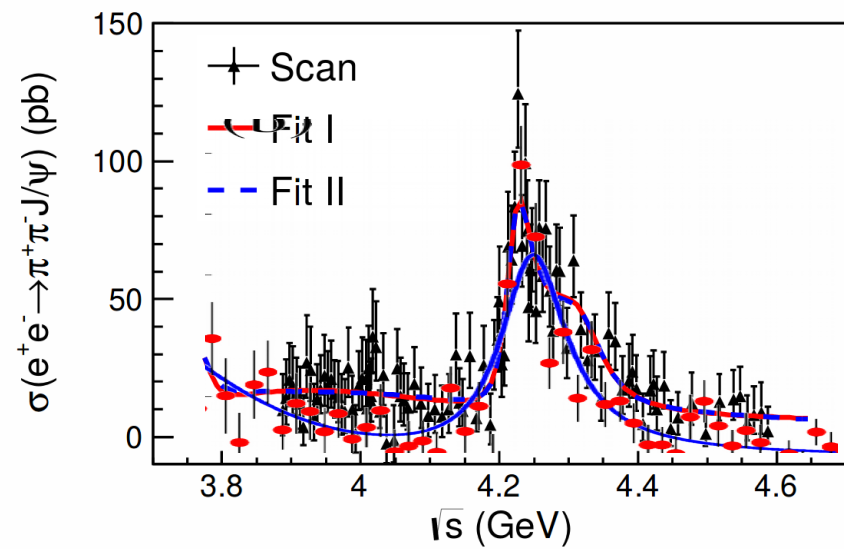
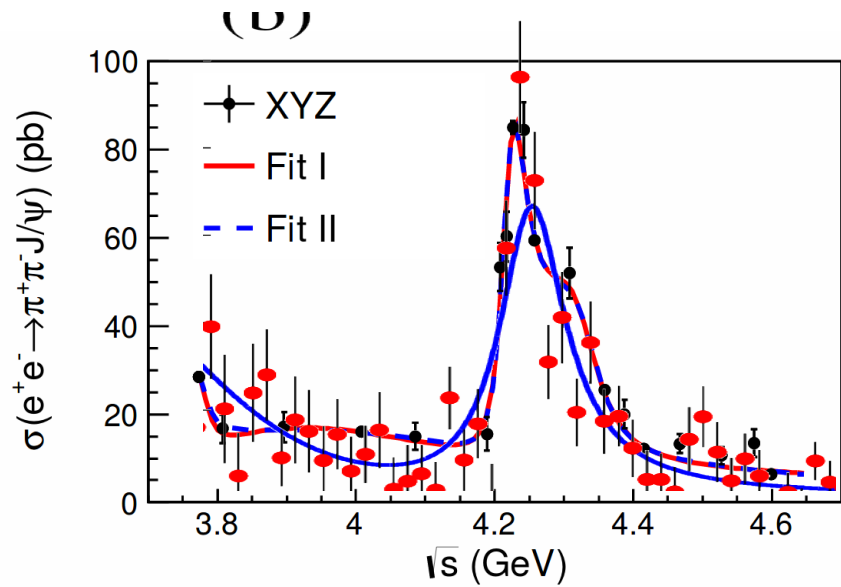
- *Waiting for more results from JLAB and COMPASS!*

Backup

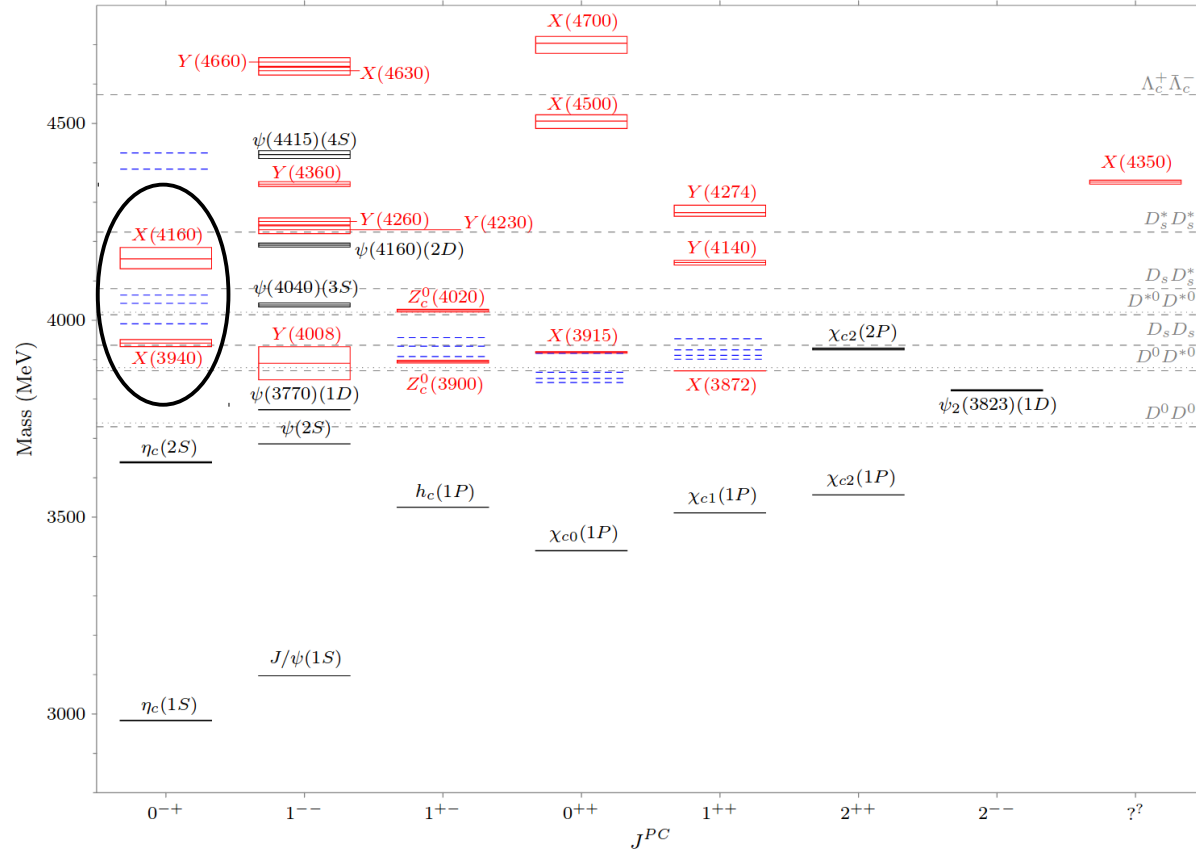
$\pi\pi/\eta$ transitions: Th. VS Exp



$\Upsilon(4260)$



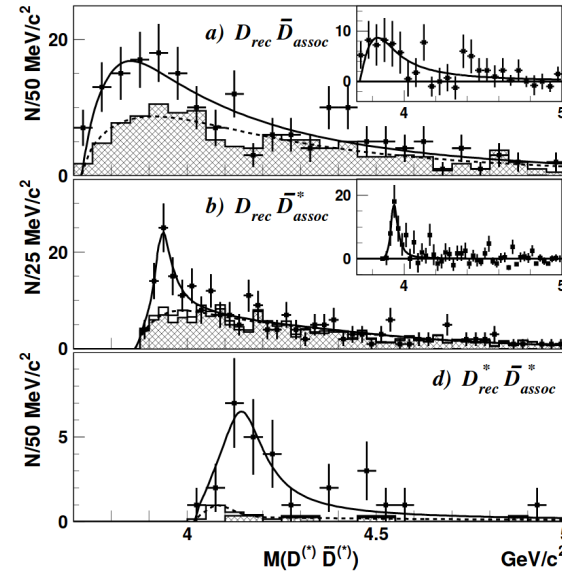
Charmonium exotica



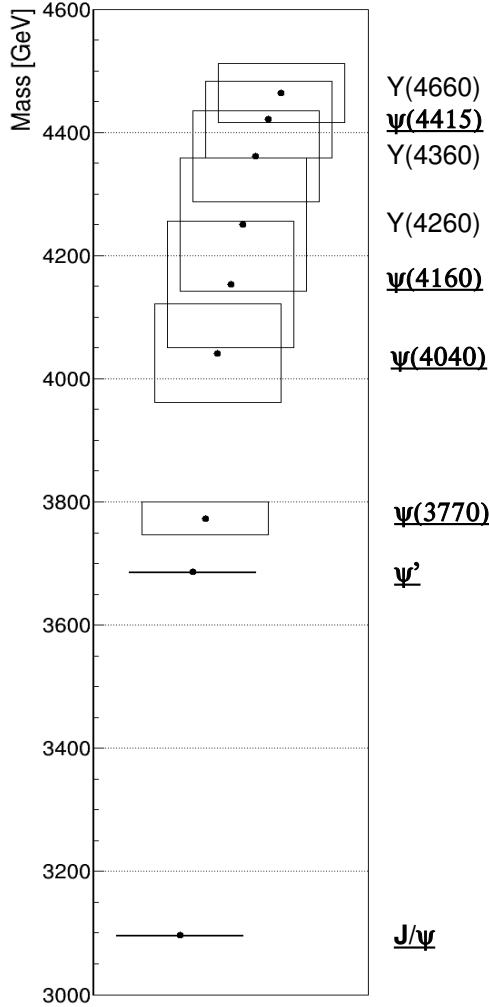
Pseudo-scalar: X(3940), X(4160)

Seen in

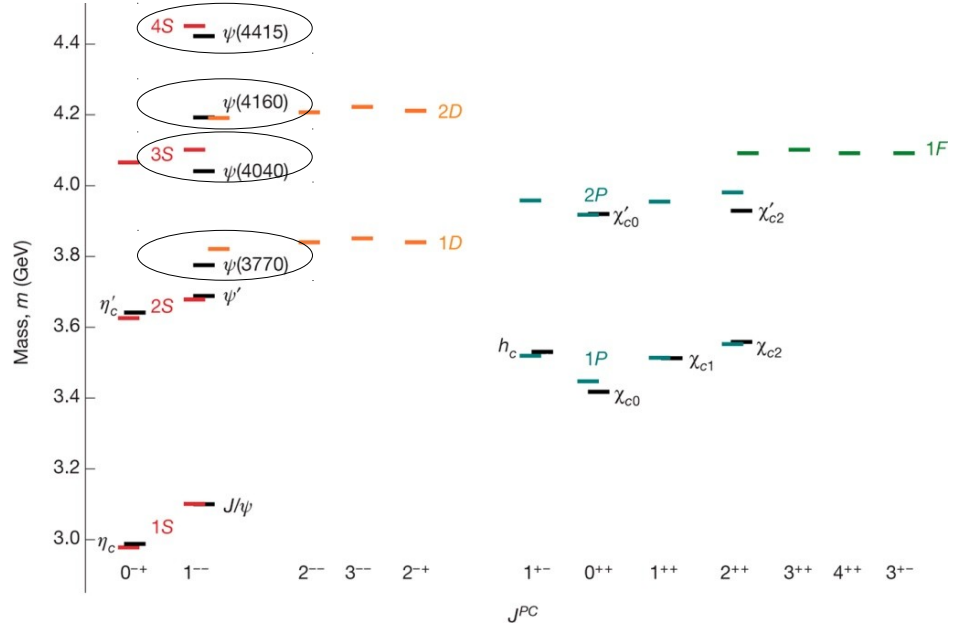
$e^+e^- \rightarrow J/\psi + D^*D^*$



Vector Charmonia



Nature **534**, 487–493 (2016)

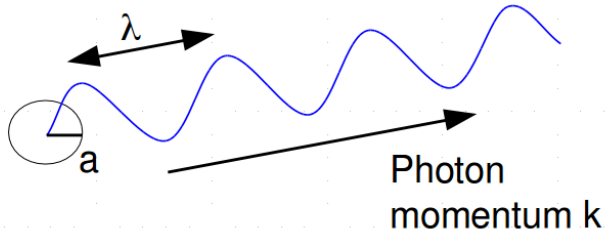


Some are (roughly) matching the expected cc resonances in S and D wave

Vector Charmonia

Kuang, Front.Phys.China 1, 19 (2006)

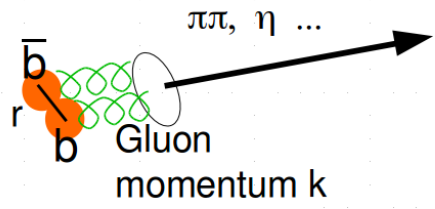
QED multipole expansion term:
 $a/\lambda \sim ak < 1$



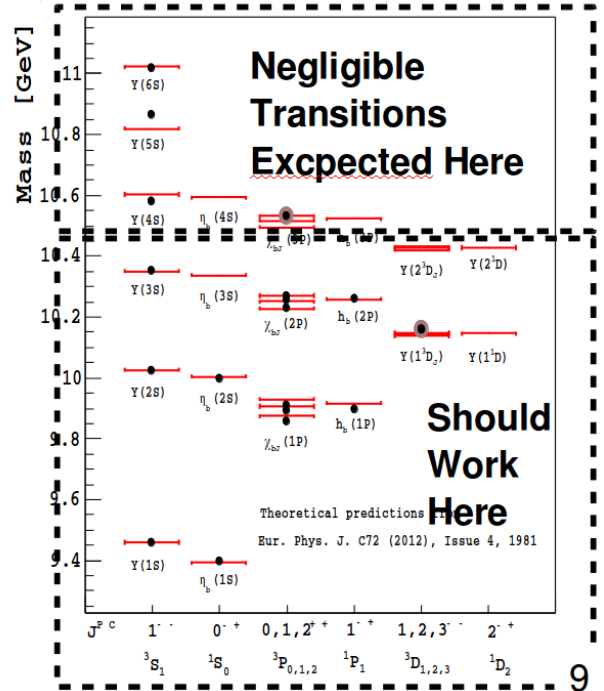
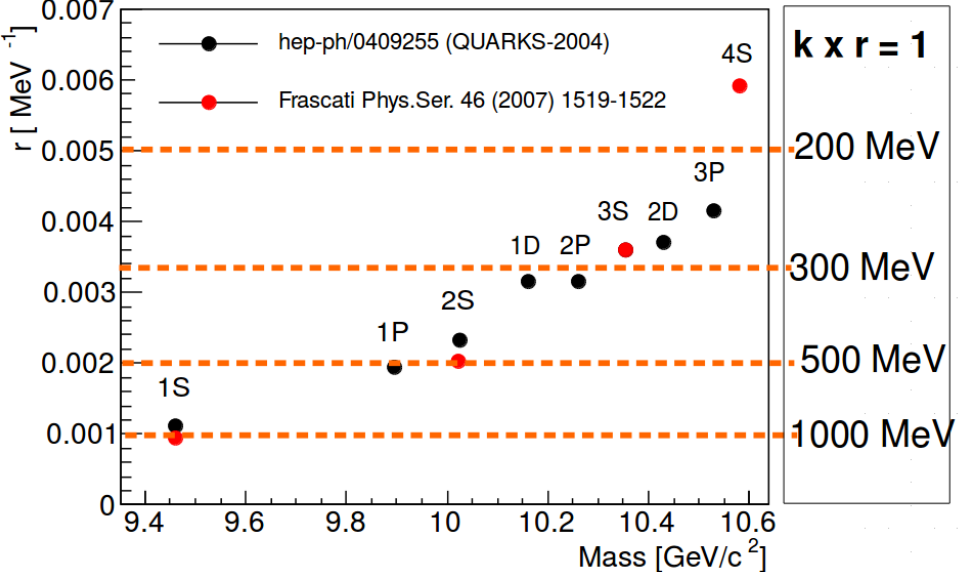
In quarkonia:

$r \sim 0.1 \text{ fm}$
 $k \sim 100 \text{ MeV}$

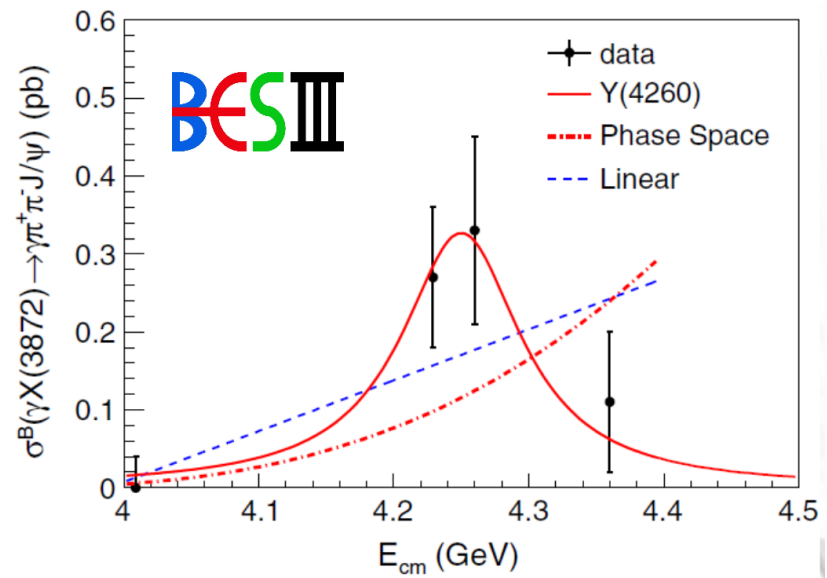
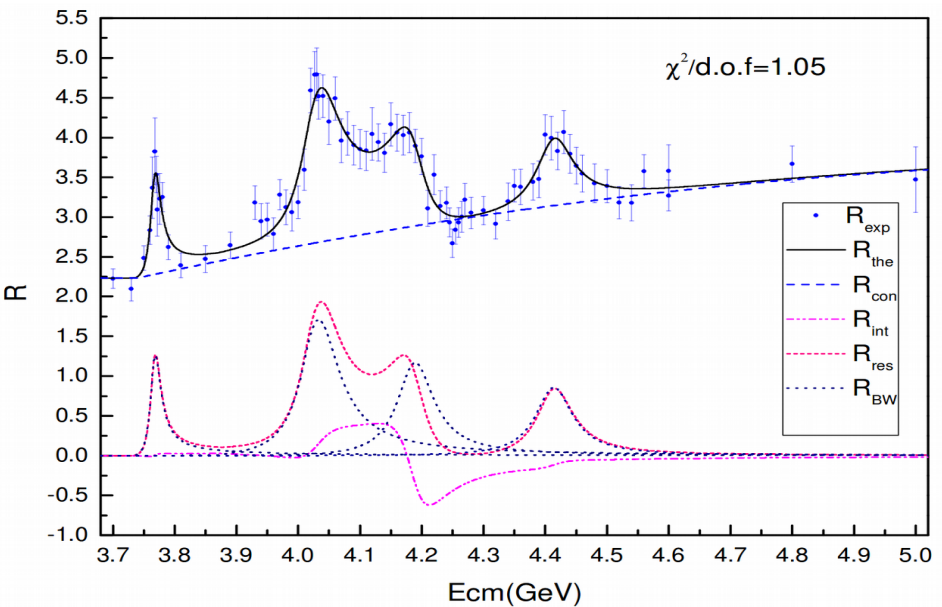
$rk < 1$



Radius (potential model)

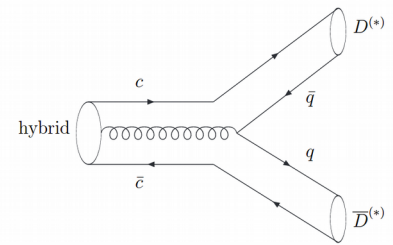


Y(4260): different models

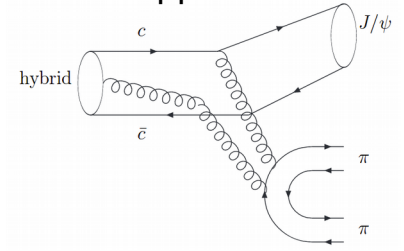


Hybrid interpretation?

Suppressed by $\sim 1/m_c^2$



Not suppressed



$$\frac{B(Y(4260) \rightarrow \gamma X(3872))}{B(Y(4260) \rightarrow \pi^+ \pi^- J/\psi)} \sim 0.1$$

- No signal of Y(4360)
- OK with tetraquark model