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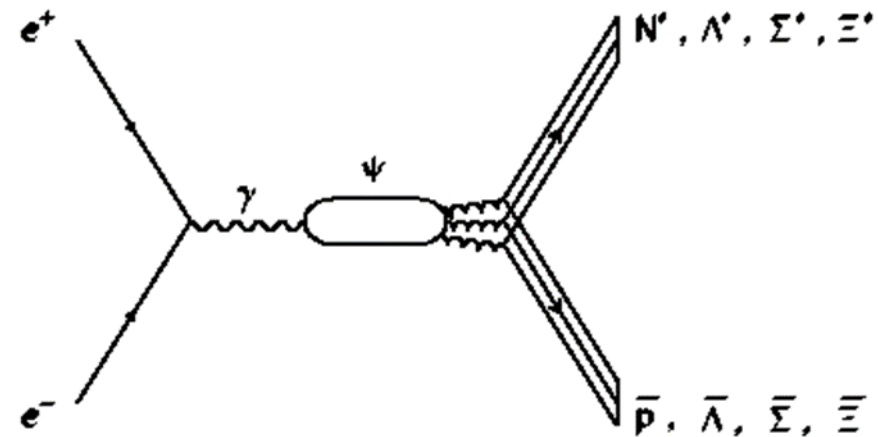
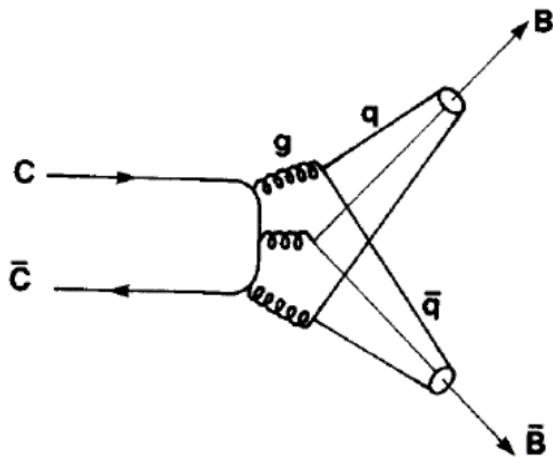
# Revised strategy for determination of hyperon decay parameters

Andrzej Kupsc

Assumption that baryons from  $J/\psi$  and  $\psi(3686)$  decays into baryon-antibaryon are unpolarized has to be revised:

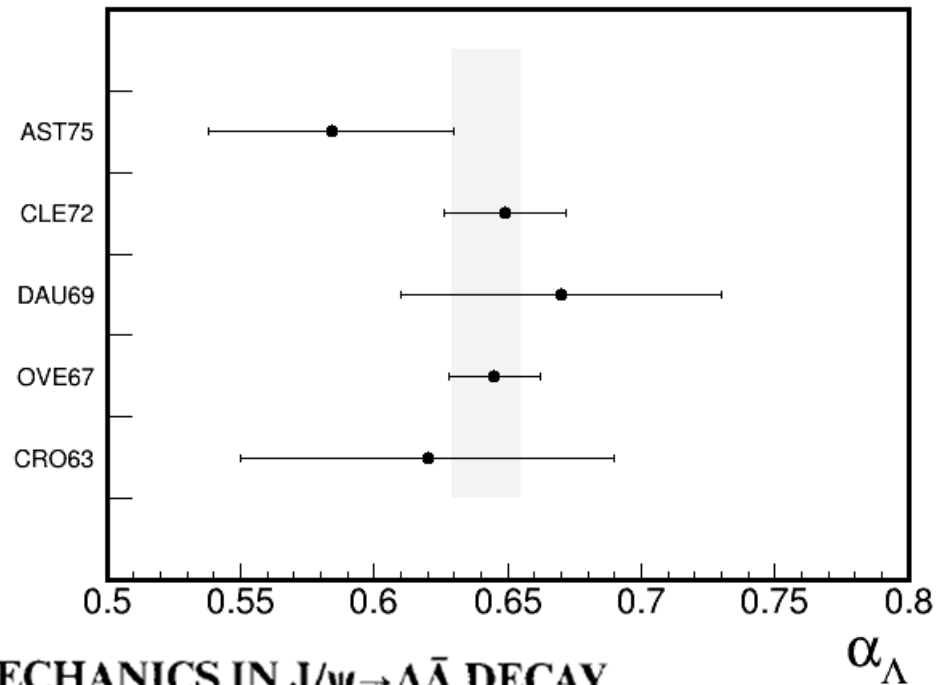
Göran Fäldt, AK arXiv:1702.07288  
Phys.Lett. B772 (2017) 16

Nothing prevents hyperons from decays of  $1^-$  states to be polarized orthogonally to the production plane



# Lambda decay parameters

$$\alpha_\Lambda = 0.642 \pm 0.013$$



LOOKING AT CP INVARIANCE AND QUANTUM MECHANICS IN  $J/\psi \rightarrow \Lambda \bar{\Lambda}$  DECAY

DM2 Coll. (1988) Phys. Lett. B 212, 523

BES, Phys.Rev. D81 (2010) 012003

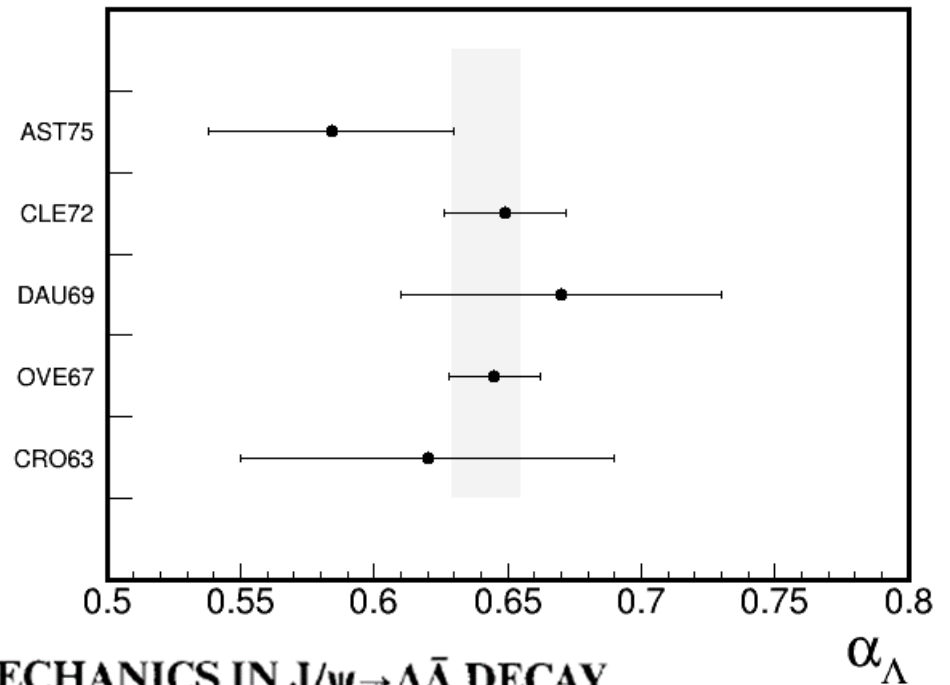
$$A = \frac{\alpha_1 + \alpha_2}{\alpha_1 - \alpha_2} \left[ = \frac{\alpha_\Lambda + \alpha_{\bar{\Lambda}}}{\alpha_\Lambda - \alpha_{\bar{\Lambda}}} \right]$$

	$\alpha_{\bar{\Lambda}}(\bar{\Lambda} \rightarrow \bar{p}\pi^+)$	$A$	
DM2	$-0.63 \pm 0.13$	$0.01 \pm 0.10$	1847 $\Lambda \bar{\Lambda}$
BES	$-0.755 \pm 0.083 \pm 0.063$	$-0.081 \pm 0.055 \pm 0.059$	8997 $\Lambda \bar{\Lambda}$

$$A = 0, \quad \Rightarrow \quad \alpha_\Lambda = -\alpha_{\bar{\Lambda}} = 0.696 \pm 0.038$$

# Lambda decay parameters

$$\alpha_{\Lambda} = 0.642 \pm 0.013$$



## LOOKING AT CP INVARIANCE AND QUANTUM MECHANICS IN $J/\psi \rightarrow \Lambda \bar{\Lambda}$ DECAY

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1847  $\Lambda \bar{\Lambda}$

8997  $\Lambda \bar{\Lambda}$

**BESIII  $0.4 \cdot 10^6$**

$$A = 0, \quad \Rightarrow \quad \alpha_{\Lambda} = -\alpha_{\bar{\Lambda}} = 0.696 \pm 0.038$$

# Formalism for $e^+e^- \rightarrow \gamma^* \rightarrow J/\psi \rightarrow \Lambda\bar{\Lambda}$

Special case of a well established formalism for baryon FFs

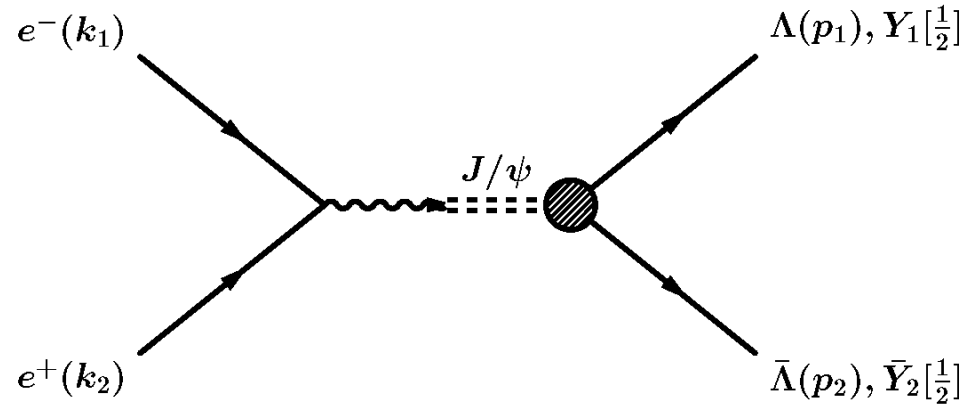
Dubnickova, Dubnicka, Rekaló

Nuovo Cim. A109 (1996) 241

Gakh, Tomasi-Gustafsson Nucl.Phys. A771 (2006) 169

Czyz, Grzelinska, Kuhn PRD75 (2007) 074026

Fäldt EPJ A51 (2015) 74; EPJ A52 (2016)141



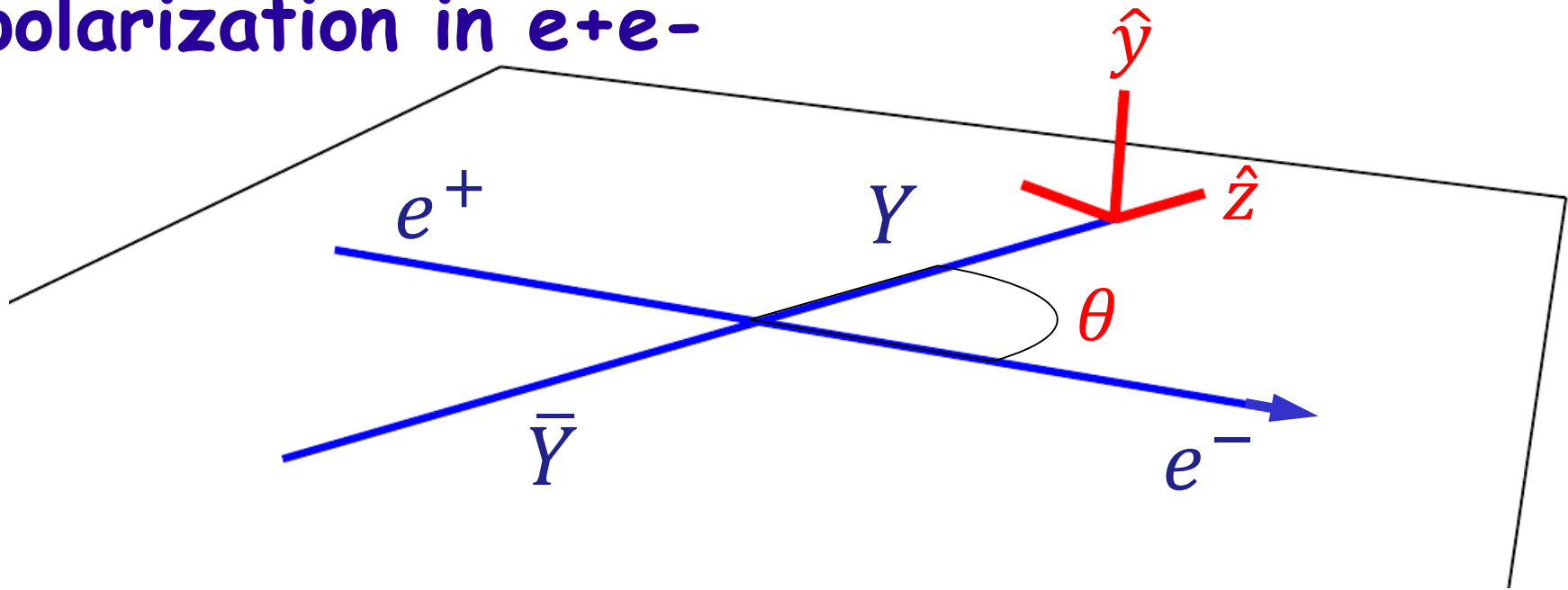
$$\Gamma_{\mu}^{\Lambda}(p_1, p_2) = -ie_g \left[ G_M^{\psi} \gamma_{\mu} - \frac{2M}{Q^2} (G_M^{\psi} - G_E^{\psi}) Q_{\mu} \right]$$

$$Q = p_1 - p_2$$

form factors:  $G_M^{\psi}$  and  $G_E^{\psi}$   $G_E^{\psi} = \frac{\sqrt{s}}{2M_{\Lambda}} \sqrt{\frac{1 - \alpha_{\psi}}{1 + \alpha_{\psi}}} e^{i\Delta\Phi} G_M^{\psi}$

$$\frac{d\Gamma}{d\Omega} \propto 1 + \alpha_{\psi} \cos^2\theta \quad -1 < \alpha_{\psi} < 1$$

# $\Upsilon$ polarization in $e^+e^-$

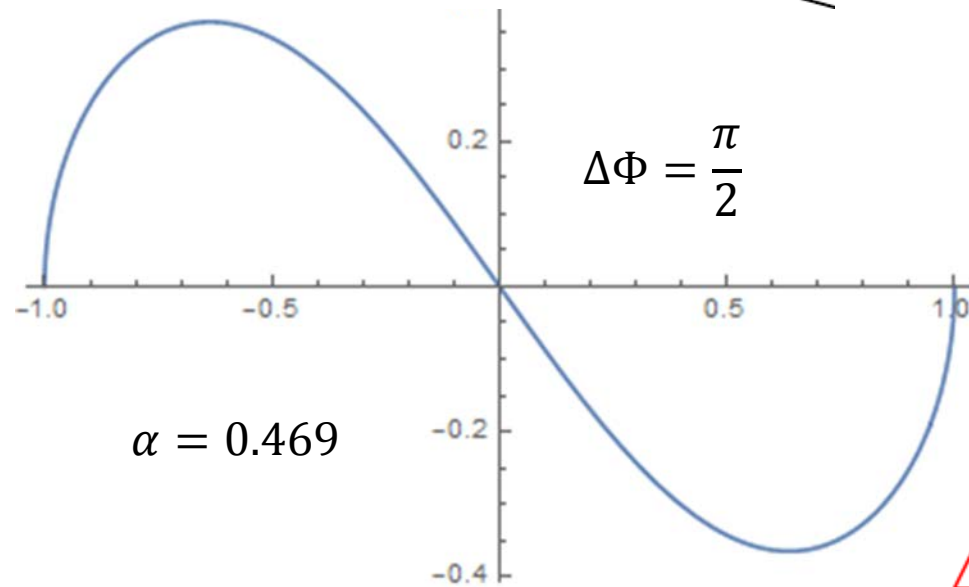


$$\mathbf{P}_Y(\theta) = \frac{\sqrt{1 - \alpha_\psi^2} \cos \theta \sin \theta}{1 + \alpha_\psi \cos^2 \theta} \sin(\Delta\Phi) \hat{y}$$

$$\mathbf{P}_Y(\theta) = -\mathbf{P}_Y(\pi - \theta) = -\mathbf{P}_{\bar{Y}}(\theta)$$

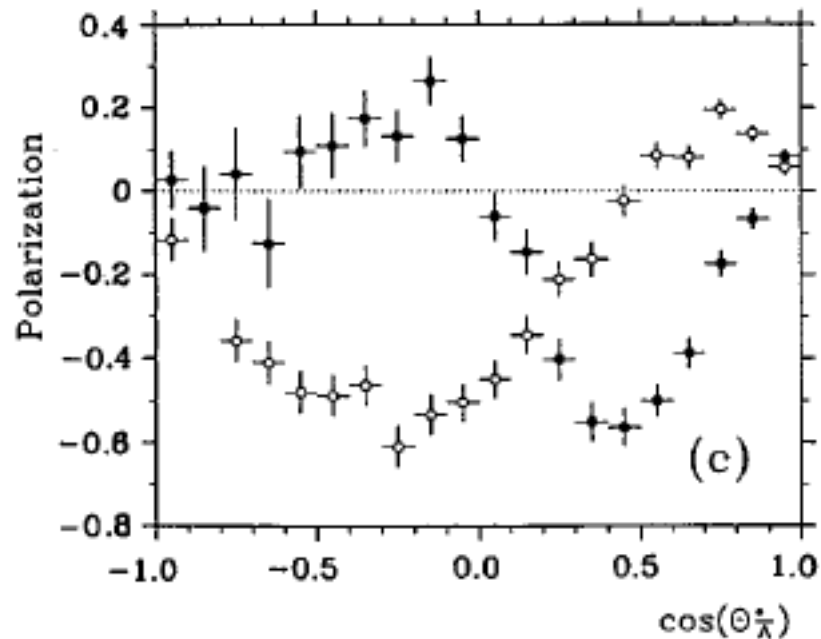
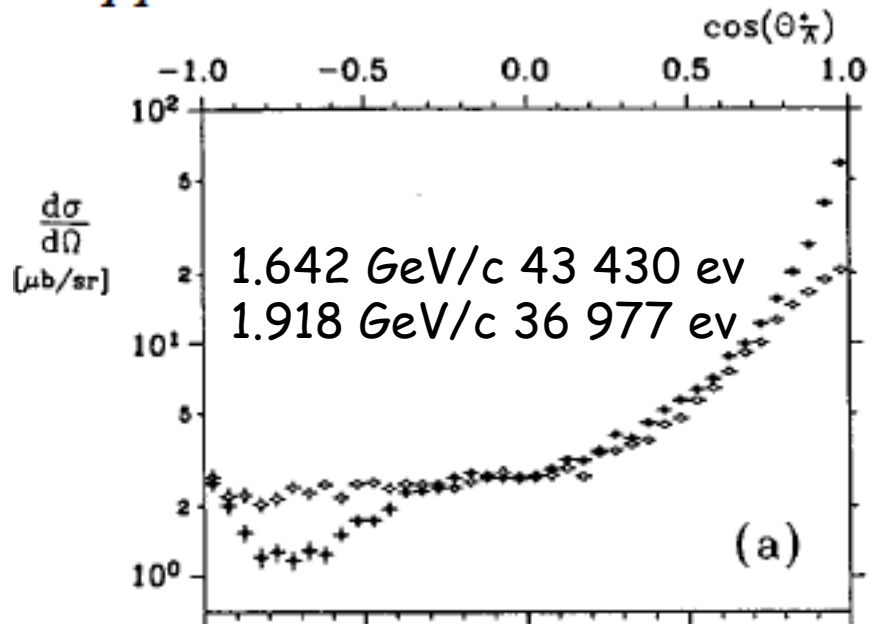
$$\mathbf{P}_Y(0) = \mathbf{P}_Y(\pi/2) = \mathbf{P}_Y(\pi) = \mathbf{0}$$

$$\langle \mathbf{P}_Y(\theta) \rangle = \mathbf{0}$$

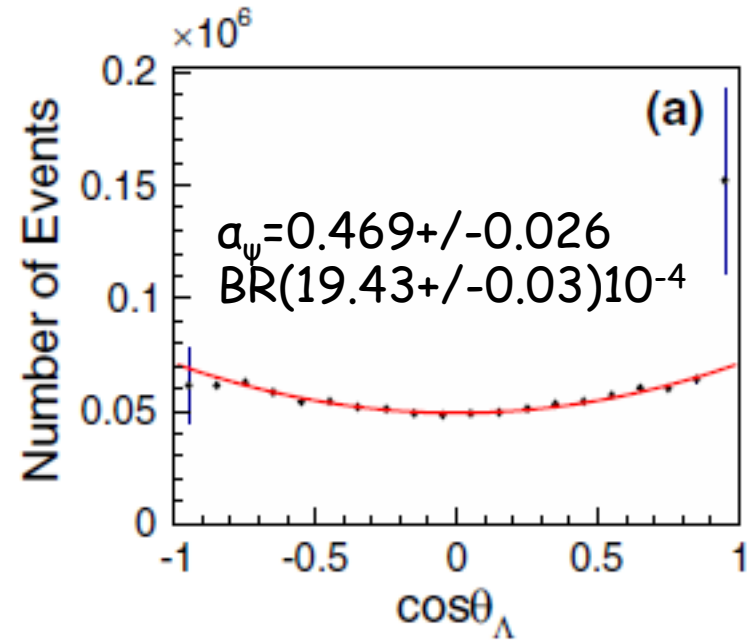


$$\Delta\Phi \neq 0 \Rightarrow \mathbf{P}_Y(\theta) \neq \mathbf{0} !$$

$$\bar{p}p \rightarrow \bar{\Lambda}\Lambda$$



$$e^+e^- \rightarrow \gamma^* \rightarrow J/\psi \rightarrow \Lambda\bar{\Lambda}$$



$$J/\psi \rightarrow \Lambda\bar{\Lambda}$$

$440,675 \pm 670$

BESIII, Phys. Rev. D 95, 052003 (2017)

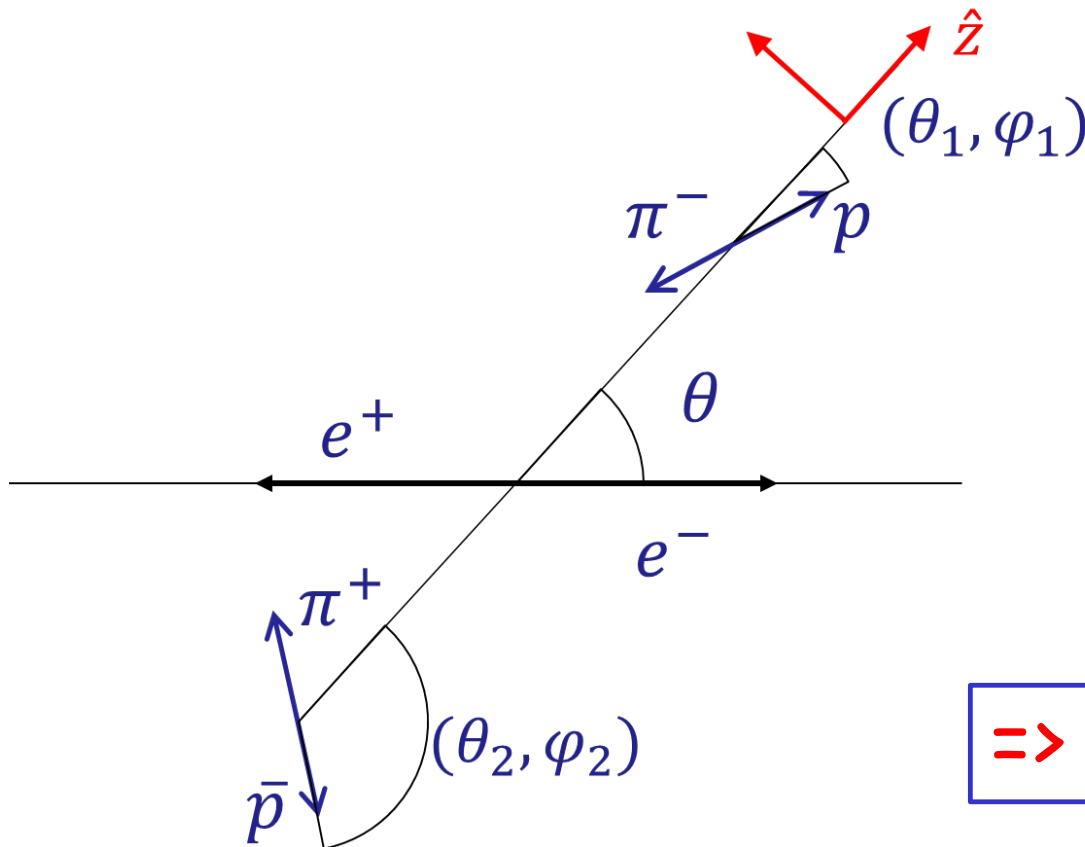
# Single tag decay distributions

$$\frac{d\Gamma}{d\cos\theta d\Omega_1} \propto (1 + \alpha_\psi \cos^2\theta) \{1 + \alpha_1 P_\Lambda(\theta) \sin\theta_1 \sin\phi_1\}$$

$$\Lambda \rightarrow p\pi^-: \Omega_1 = (\cos\theta_1, \phi_1) \quad \alpha_\Lambda = \alpha_1$$

proton direction: spherical coord  
in  $\Lambda$  rest frame

Use max log likelihood  
to fit  $\Gamma(\theta, \theta_1, \phi_1)$



$$\Rightarrow \alpha_\psi \quad \alpha_1 \sin(\Delta\Phi)$$

# Double tag decay distributions

$$e^+ e^- \rightarrow (\Lambda \rightarrow p\pi^-)(\bar{\Lambda} \rightarrow \bar{p}\pi^+)$$

EPJ A52 (2016)141  
arXiv:1702.07288

$$d\sigma \propto \mathcal{W}(\xi) d\cos\theta d\Omega_1 d\Omega_2$$

$$\Lambda \rightarrow p\pi^-: \Omega_1 = (\cos\theta_1, \phi_1)$$

$$\alpha_\Lambda = \alpha_1$$

$$\bar{\Lambda} \rightarrow \bar{p}\pi^+: \Omega_2 = (\cos\theta_2, \phi_2)$$

$$\alpha_{\bar{\Lambda}} = \alpha_2$$

$$\xi : (\cos\theta, \Omega_1, \Omega_2)$$

$$\mathcal{W}(\xi) = 1 + \alpha_\psi \cos^2\theta$$

Spin correlations

$$+ \alpha_1 \alpha_2 \left( \mathcal{T}_1(\xi) + \sqrt{1 - \alpha_\psi^2} \cos(\Delta\Phi) \mathcal{T}_2(\xi) + \alpha_\psi \mathcal{T}_6(\xi) \right)$$

$$+ \sqrt{1 - \alpha_\psi^2} \sin(\Delta\Phi) \sin\theta \cos\theta (\alpha_1 \sin\theta_1 \sin\phi_1 + \alpha_2 \sin\theta_2 \sin\phi_2)$$



# LOOKING AT CP INVARIANCE AND QUANTUM MECHANICS IN $J/\psi \rightarrow \Lambda \bar{\Lambda}$ DECAY

DM2 Coll. (1988) Phys. Lett. B 212, 523

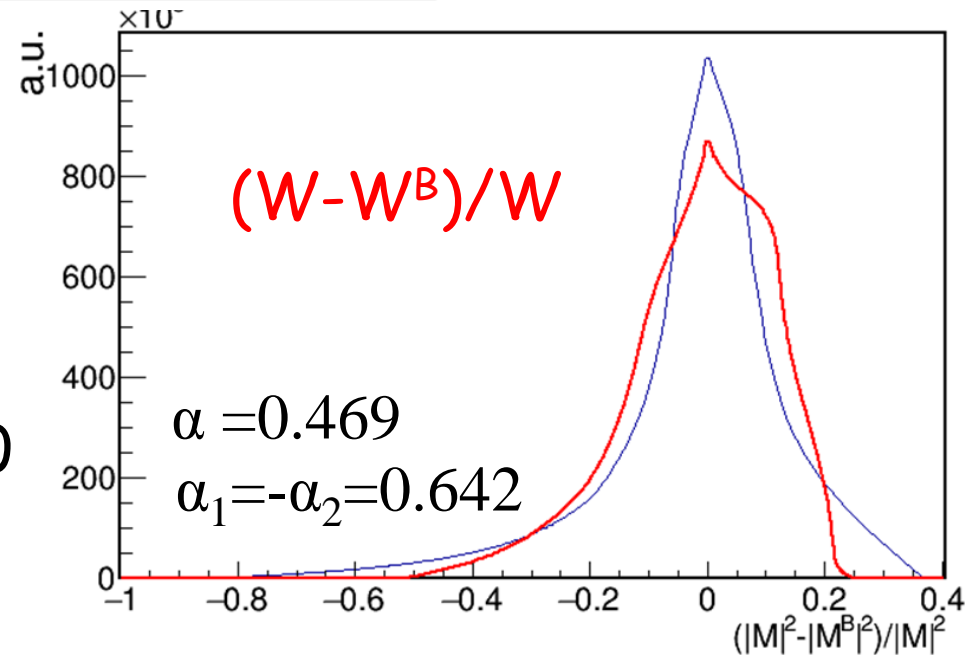
$$W^B(\xi) = 1 + \alpha_\psi \mathcal{G}_1(\xi) + \alpha_1 \alpha_2 \mathcal{G}_2(\xi) + \alpha_\psi \alpha_1 \alpha_2 \mathcal{G}_3(\xi)$$

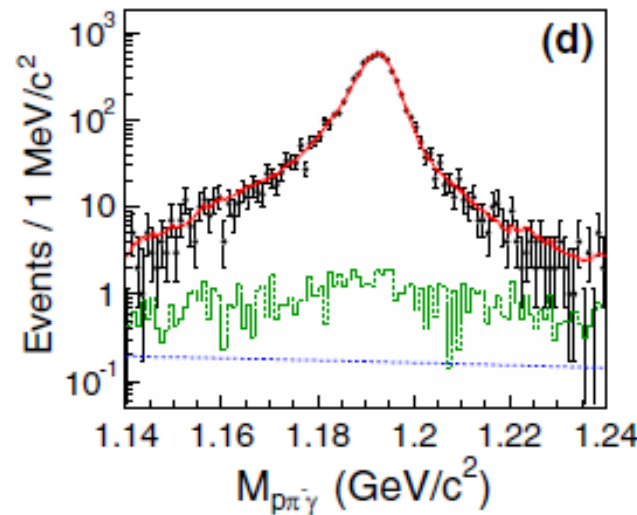
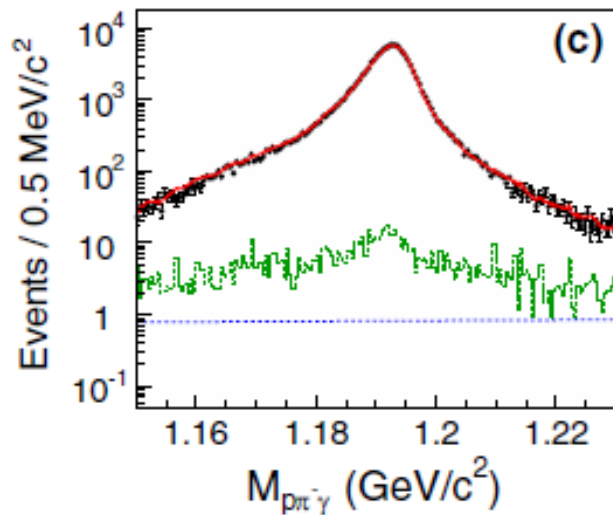
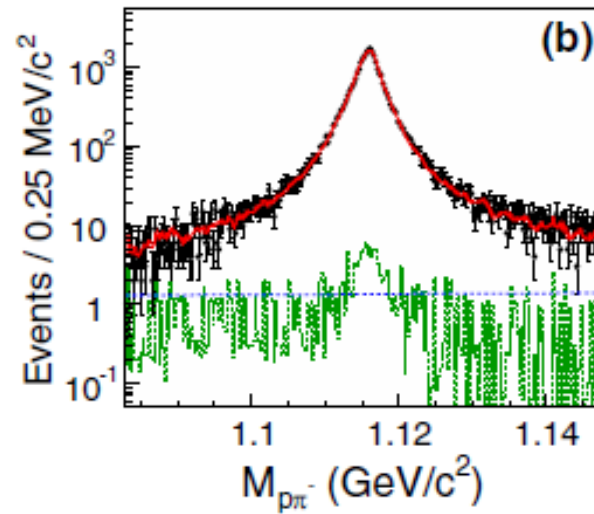
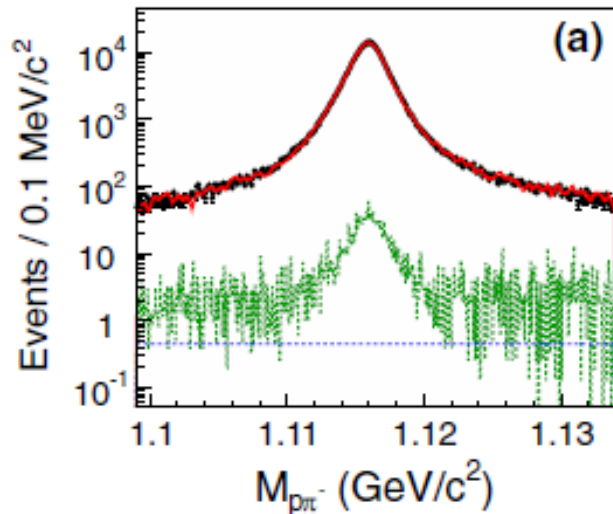
BES, Phys.Rev. D81 (2010) 012003

$$A = \frac{\alpha_1 + \alpha_2}{\alpha_1 - \alpha_2} \left[ = \frac{\alpha_\Lambda + \alpha_{\bar{\Lambda}}}{\alpha_\Lambda - \alpha_{\bar{\Lambda}}} \right]$$

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- Only two parameters:  
 $\alpha_\psi$      $\alpha_1 \cdot \alpha_2$
- $\Lambda$  unpolarized
- $W^B$  and  $W$  differs even for  $\Delta\Phi=0$





Channel	$N_{\text{obs}}$
$J/\psi \rightarrow \Lambda \bar{\Lambda}$	$440,675 \pm 670$
$J/\psi \rightarrow \Sigma^0 \bar{\Sigma}^0$	$111,026 \pm 335$
$\psi(3686) \rightarrow \Lambda \bar{\Lambda}$	$31,119 \pm 187$
$\psi(3686) \rightarrow \Sigma^0 \bar{\Sigma}^0$	$6,612 \pm 82$

Determine  $\Delta\Phi$  for each decay

for  $\Sigma^0$

$\Lambda$  polarized longitudinally

$$P_{\Lambda} = (P_{\Sigma}) \cos\theta_{\Sigma\Lambda}$$

$J/\psi \rightarrow \Sigma^+ \bar{\Sigma}^-$	$\Sigma^+(uus)$	$p\pi^0$ (51.6%)
$\psi(3686) \rightarrow \Sigma^+ \bar{\Sigma}^-$		$n\pi^+$ (48.3%)

Modes

$N_S$

$N_B$

$J/\psi \rightarrow \bar{\Lambda}\Sigma^0 (\Sigma^0 \rightarrow \gamma\Lambda)$

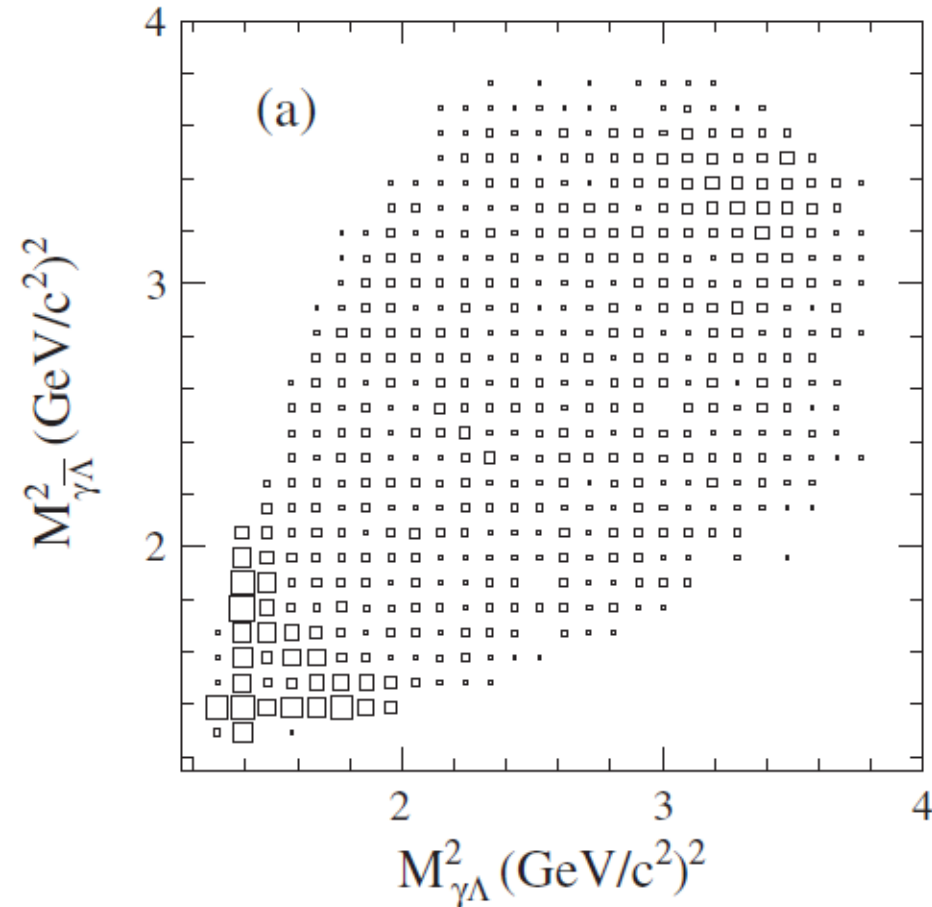
$308 \pm 24$

$105 \pm 10$

$J/\psi \rightarrow \Lambda\bar{\Sigma}^0 (\bar{\Sigma}^0 \rightarrow \gamma\bar{\Lambda})$

$234 \pm 21$

$95 \pm 9$



BESIII, Phys. Rev. D 86, 032008 (2012)  
 $225 \times 10^6$  J/ $\psi$

(now  $1.31 \times 10^6$  J/ $\psi$ )

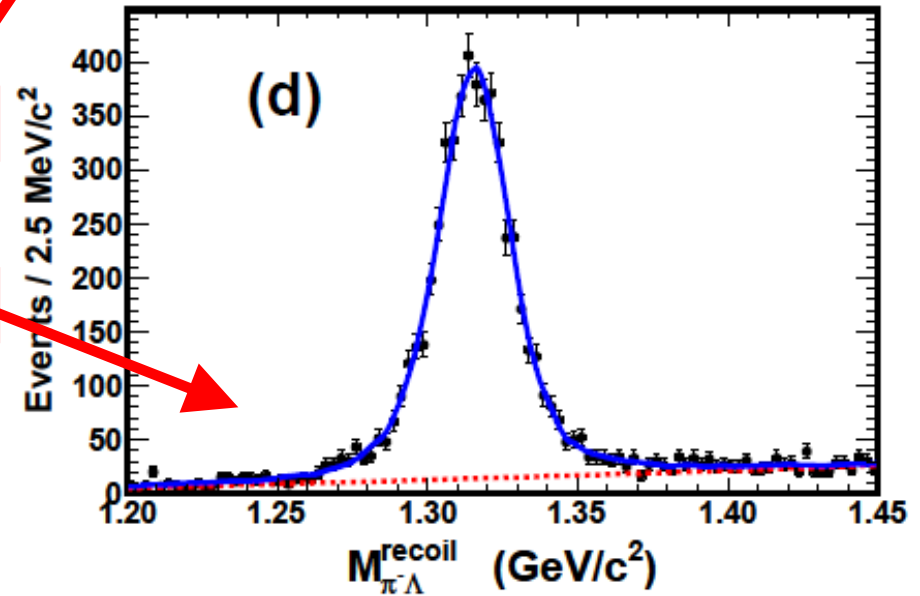
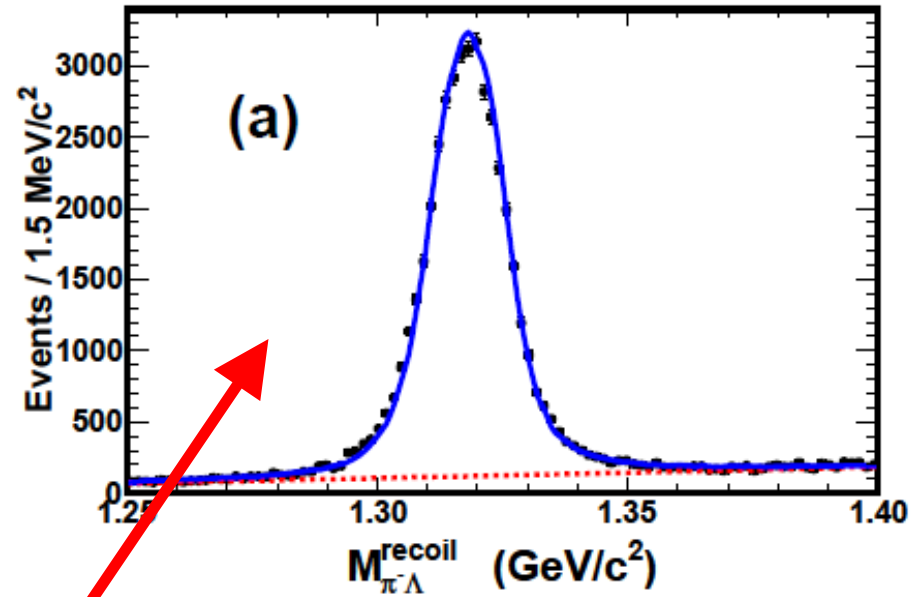
Determine  $\Delta\Phi$  for  $\Lambda\Sigma^0$  transition  
 form factor...

$\Lambda$  polarized longitudinally

$$P_\Lambda = (P_\Sigma) \cos\theta_{\Sigma\Lambda}$$

BESIII  
 Phys. Rev. D 93, 072003 (2016)

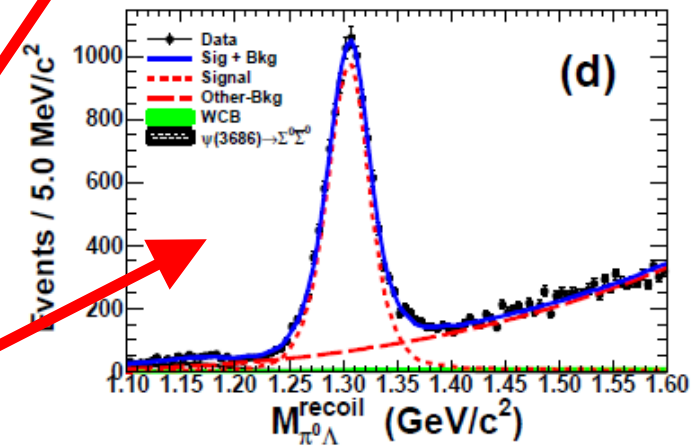
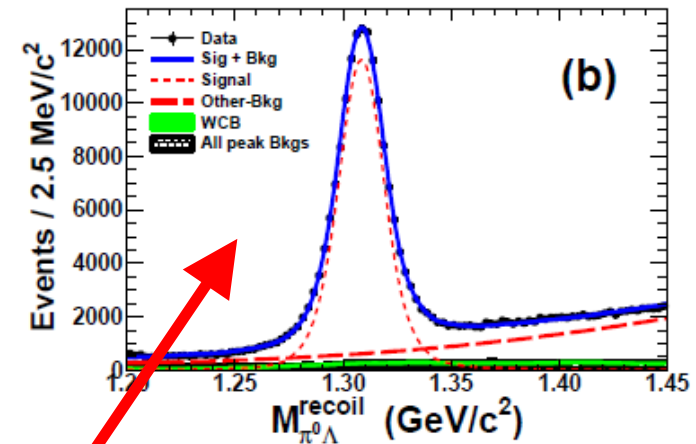
Determine  $\Delta\Phi$  for  $J/\psi$  and  $\psi(3686)$ + all decay parameters?



Channel	$N_{obs}$
$J/\psi \rightarrow \Xi^- \bar{\Xi}^+$	$42810.7 \pm 231.0$
$J/\psi \rightarrow \Sigma(1385)^- \Sigma(1385)^+$	$42594.8 \pm 466.8$
$J/\psi \rightarrow \Sigma(1385)^+ \bar{\Sigma}(1385)^-$	$52522.5 \pm 595.9$
$\psi(3686) \rightarrow \Xi^- \bar{\Xi}^+$	$5336.7 \pm 82.6$
$\psi(3686) \rightarrow \Sigma(1385)^- \Sigma(1385)^+$	$1374.5 \pm 97.8$
$\psi(3686) \rightarrow \Sigma(1385)^+ \bar{\Sigma}(1385)^-$	$1469.9 \pm 94.6$

$\Xi^-(dss) \mid \Lambda\pi^- (99.8\%)$

Determine  $\Delta\Phi$  for  $J/\psi$  and  $\psi(3686)$ + all decay parameters?



Channel	$N_{\text{obs}}$
$J/\psi \rightarrow \Sigma(1385)^0 \bar{\Sigma}(1385)^0$	$102762 \pm 852$
$J/\psi \rightarrow \Xi^0 \bar{\Xi}^0$	$134846 \pm 437$
$\psi(3686) \rightarrow \Sigma(1385)^0 \bar{\Sigma}(1385)^0$	$2536 \pm 185$
$\psi(3686) \rightarrow \Xi^0 \bar{\Xi}^0$	$10839 \pm 123$

# Conclusions/outlook

Well established general formulas for  
 $e^+e^- \rightarrow \gamma^* \rightarrow B_{1/2} \bar{B}_{1/2}$  are applied to  $J/\psi$  and  $\psi(3686)$

Access to decay parameters even using single tag mode  
if corresponding  $\Delta\Phi \neq 0$ .

Charmonia: determine  $\Delta\Phi$  for  $J/\psi$  and  $\psi(3686) \Upsilon\bar{\Upsilon}$  decays  
[including  $\pi \Sigma^0$ ]

Too simplified helicity amplitude formalism for weak decays...