Nucleon 3D imaging

Alessandro Bacchetta

Funded by











see, e.g., C. Lorcé, B. Pasquini, M. Vanderhaeghen, JHEP 1105 (11)

 $\cdots \rightarrow \vec{k}_{\perp}$ dependence

 \vec{b}_{\perp} dependence





Proton 1[









3D "imaging" in momentum space



Unpolarized TMD: cylindrically symmetric

3D "imaging" in momentum space



Unpolarized TMD: cylindrically symmetric

3D "imaging" in momentum space



Unpolarized TMD: cylindrically symmetric







3D "imaging" in impact parameter space



down valence



Diehl, Kroll, arXiv:1302.4604, and talk by M. Diehl at DIS 2013



















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- To benefit society?

Example: impact on high-energy physics

W-boson charge		W^+		W^-		Combined	
Kinematic distribution	p_{T}^ℓ	m_{T}	p_{T}^ℓ	m_{T}	p_{T}^ℓ	m_{T}	
$\delta m_W [\text{MeV}]$							
Fixed-order PDF uncertainty	13.1	14.9	12.0	14.2	8.0	8.7	
AZ tune	3.0	3.4	3.0	3.4	3.0	3.4	
Charm-quark mass	1.2	1.5	1.2	1.5	1.2	1.5	
Parton shower $\mu_{\rm F}$ with heavy-flavour decorrelation	5.0	6.9	5.0	6.9	5.0	6.9	
Parton shower PDF uncertainty	3.6	4.0	2.6	2.4	1.0	1.6	
Angular coefficients	5.8	5.3	5.8	5.3	5.8	5.3	
Total	15.9	18.1	14.8	17.2	11.6	12.9	

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In other words, LHC needs us...

ATLAS Collab. <u>arXiv:1701.07240</u>

$$\mathcal{L}_{\text{QCD}} = \sum_{q} \overline{\psi}_{q} (i \partial \!\!\!/ - g A \!\!\!/ + m) \psi_{q} - \frac{1}{4} G^{a}_{\mu\nu} G^{\mu\nu}_{a}$$

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QCD is the most complex part of the Standard Model and at the same time the most useful, after QED

Either we build the EIC, or we give up understanding QCD


TMD Science Matrix

	Deliverables Observables		What we learn		
BY Charges its that	Sivers &	SIDIS with	Quantum interference & spin-orbital correlations		
	unpolarized	transverse	3D Imaging of quark's motion: valence $+$ sea		
	TMD quarks	polarization;	3D Imaging of gluon's motion		
	and gluon	di-hadron (di-jet)	QCD dynamics in an unprecedented Q^2 (P_{hT}) range		
THE REPORT OF A LOCAL DIST	Chiral-odd	SIDIS with	3rd basic quark PDF: valence + sea, tensor charge		
	functions:	transverse	Novel spin-dependent hadronization effect		
	transversity;	polarization	QCD dynamics in a chiral-odd sector		
	Boer-Mulders		with a wide $Q^2(P_{hT})$ coverage		









Drell-Yan@ **‡** Fermilab



Z production@ Tevatron



Drell-Yan@ **‡** Fermilab



Z production@ Tevatron





Z production@ Tevatron





Z production@LHC Z production@Tevatron



Quark unpol. TMD: extractions

	Framework	HERMES	COMPASS	DY	Z production	N of points
KN 2006 <u>hep-ph/0506225</u>	NLL/NLO	*	×	>	~	98
Pavia 2013 <u>arXiv:1309.3507</u>	No evo	~	×	×	×	1538
Torino 2014 <u>arXiv:1312.6261</u>	No evo	(separately)	(separately)	*	×	576 (H) 6284 (C)
DEMS 2014 <u>arXiv:1407.3311</u>	NNLL/NLO	*	×		•	223
EIKV 2014 <u>arXiv:1401.5078</u>	NLL/LO	1 (x,Q²) bin	1 (x,Q²) bin		•	500 (?)
Pavia 2016 <u>arXiv:1703.10157</u>	NLL/LO		~		~	8059
SV 2017 arXiv:1706.01473	NNLL/ NNLO	×	×	~	~	309

SIDIS



SIDIS 10r Norm. multiplicity $\langle Q^2 \rangle$ =4.8 GeV² $\langle Q^2 \rangle$ =3. GeV² <u>40</u>2⟩=4.3 GeV² (x)=0.022 ⟨x⟩=0.033 ⟨x⟩=0.055 2 10 ⟨Q²⟩=3. GeV² ⟨x⟩=0.022 $\langle Q^2 \rangle$ =3. GeV² $\langle Q^2 \rangle$ =4.8 GeV² ⟨x⟩=0.033 ⟨x⟩=0.055 8 Norm. multiplicity 6 2 10 ⟨Q²⟩=2. GeV² ⟨x⟩=0.022 $\langle Q^2 \rangle$ =2. GeV² $\langle Q^2 \rangle$ =2. GeV² ⟨x⟩=0.033 ⟨x⟩=0.055 8 Norm. multiplicity 6 2 0.3 0.6 0.9 0.3 0.6 0.9 0.3 0.6 0.9 P_{hT}[GeV] P_{hT}[GeV] P_{hT}[GeV]



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Number of data points: 8059 Global χ^2 /dof = 1.52



Bacchetta, Delcarro, Pisano, Radici, Signori, arXiv:1703.10157 see talk by C. Pisano

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It's the dawn of TMD global fits era

Transverse size in momentum space



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Transverse size in momentum space

Bacchetta, Delcarro, Pisano, Radici, Signori, arXiv:1703.10157



Improvement in perturbative accuracy





see talk by A. Vladimirov

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from EIC white paper EPJA 52 (2016)



Х



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Gluon TMDs





see, e.g., Boer, den Dunnen, Pisano, Schlegel, Vogelsang, PRL108 (12) den Dunnen, Lansberg, Pisano, Schlegel, PRL 112 (14) see talks by C. Pisano, F. Murgia, J.H. Lee

Higgs transverse momentum



G. Ferrera, talk at REF 2014, Antwerp, <u>https://indico.cern.ch/event/330428/</u>

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talk by F. Hautmann



Sivers function





Sivers function



Anselmino, Boglione, D'Alesio, Murgia, Prokudin, <u>arXiv:1612.06413</u>



Sivers function



Anselmino, Boglione, D'Alesio, Murgia, Prokudin, <u>arXiv:1612.06413</u>

Most recent extraction, no TMD evolution. It is probably not a big problem for fixed-target DIS, but it will play a major role at EIC

Sivers function SIDIS = - Sivers function Drell-Yan

Collins, PLB 536 (02)





Compass measurement

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talk by B. Parsamyan at DIS 2017



Compass measurement

talk by B. Parsamyan at DIS 2017



Compass measurement

talk by B. Parsamyan at DIS 2017



is due to evolution.

Gluon Sivers TMD

$e \ p \to e \ h \ h \ X$



Gluon Sivers TMD



Estimate of asymmetry related to gluon Sivers TMD. Based also on Monte Carlo input.

Gluon Sivers TMD



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see also talks by F. Murgia for J/ψ production and Lee for EIC





talk by F. Bradamante





Tensor charge is an ideal quantity to compare to lattice QCD



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Tensor charge is needed to constrain beyond-Standard-Model couplings



Tensor charge is an ideal quantity to compare to lattice QCD

Tensor charge is needed beyond-Standard-Model couplings talk by S. Liuti



see also talk by A. Accardi for a way to access tensor charge in inclusive DIS

TRANSVERSITY 2017

5th International Workshop on Transverse Polarization Phenomena in Hard Processes

INFN - Laboratori Nazionali di Frascati, Frascati (Italy) December 11-15, 2017



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GPDs Science Matrix

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	Deliverables	Observables	What we learn
The Charles in All	GPDs of	DVCS and J/ψ , ρ^0 , ϕ	transverse spatial distrib.
	sea quarks	production cross-section	of sea quarks and gluons;
	and gluons	and polarization	total angular momentum
		asymmetries	and spin-orbit correlations
This is a state of the	GPDs of	electro-production of	dependence on
a Nell	valence and	$\pi^+, K \text{ and } \rho^+, K^*$	quark flavor and
and the general second	sea quarks		polarization
Existing and future data



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Example of data and parametrizations

Defurne et al. arXiv:1504.05453



Pisano et al., arXiv:1501.07052



Example of data and parametrizations

Defurne et al. arXiv:1504.05453



Steady progress in data collection and parametrizations. Not all data are well reproduced, yet

Pisano et al., arXiv:1501.07052



Bernauer et al., arXiv:1307.6227



Bernauer et al., arXiv:1307.6227



Form Factors are extracted, fitted, and slope at $Q^2=0$ is determined.

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Bernauer et al., arXiv:1307.6227



Form Factors are extracted, fitted, and slope at $Q^2=0$ is determined.

Friedrich-Walcher Poly. \times dipole 10 par. Poly. \times dipole 9 par. Poly. \times dipole 8 par. Poly. \times dipole 7 par. Poly. + dipole 12 par. Poly. + dipole 11 par. Poly. + dipole 10 par. Poly. + dipole 9 par. Poly. 12 par. Poly. 11 par. Poly. 10 par. Poly. 9 par. Inv. Poly. 9 par. Inv. Poly. 8 par. Inv. Poly. 7 par. Inv. Poly. 6 par. Spline \times dipole 11 par. Spline \times dipole 10 par. Spline \times dipole 9 par. Spline \times dipole 8 par. Spline \times dipole 7 par. Spline 5th order 11 par. Spline 5th order 10 par. Spline 5th order 9 par. Spline 5th order 8 par. Spline 4th order 11 par. Spline 4th order 10 par. Spline 4th order 9 par. Spline 4th order 8 par. Spline 3rd order 11 par. Spline 3rd order 10 par. Spline 3rd order 9 par. Spline 3rd order 8 par.



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Bernauer et al., <u>arXiv:1307.6227</u>



Poly. \times dipole 8 par. Poly. \times dipole 7 par. Poly. + dipole 12 par. Poly. + dipole 11 par. Poly. + dipole 10 par. Poly. + dipole 9 par. Poly. 12 par. Poly. 11 par. Poly. 10 par. Poly. 9 par. Inv. Poly. 9 par. Inv. Poly. 8 par. Inv. Poly. 7 par. Inv. Poly. 6 par. Spline \times dipole 11 par. Spline \times dipole 10 par. Spline \times dipole 9 par. Spline \times dipole 8 par. Spline \times dipole 7 par. Spline 5th order 11 par. Spline 5th order 10 par. Spline 5th order 9 par. Spline 5th order 8 par. Spline 4th order 11 par. Spline 4th order 10 par. Spline 4th order 9 par. Spline 4th order 8 par. Spline 3rd order 11 par. Spline 3rd order 10 par. Spline 3rd order 9 par. Spline 3rd order 8 par.



Form Factors are extracted, fitted, and slope at $Q^2=0$ is determined.

Thanks to the wealth of data, the extraction is mildly sensitive to extrapolation.

The way to 3D imaging



Compton Form Factors are extracted from data

Jefferson Lab

The way to 3D imaging



Compton Form Factors are extracted from data

Jefferson Lab

hermes

The way to 3D imaging



Compton Form Factors are extracted from data

Jefferson Lab



They are fitted with some ansatz and the slope at t=0 for each value of $\boldsymbol{\xi}$ is extracted

 $H_{Im}(\xi,t) = A(\xi)e^{B(\xi)t}$







Dupré, Guidal, Niccolai, Vanderhaeghen, <u>arXiv:1704.07330</u> talk by E. M. Kabuss at DIS2017 and Jörg arXiv:1702.06315

Interference

measurements

Fit of 8 quantities

t-slope of Im ${\cal H}$

Х

Singlet GPD contr.

The errors are large, but slowly we are getting some 3D information. Even if we do not get 3D imaging, GPDs are still gold mines of information about QCD.



Dupré, Guidal, Niccolai, Vanderhaeghen, <u>arXiv:1704.07330</u>



talk by E. M. Kabuss at DIS2017 and Jörg arXiv:1702.06315



The errors are large, but slowly we are getting some 3D information. Even if we do not get 3D imaging, GPDs are still gold mines of information about QCDI (1997).



Dupré, Guidal, Niccolai, Vanderhaeghen, <u>arXiv:1704.07330</u>



talk by E. M. Kabuss at DIS2017 and Jörg arXiv:1702.06315

talks by S. Niccolai and N. D'Hose

Ji's sum rule

$$J^{q} = \frac{1}{2} \int_{0}^{1} dx \, x \left(H^{q}(x,0,0) + E^{q}(x,0,0) \right)$$



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- Requires spanning x at fixed values of ξ (ξ =0 is the most convenient)
- Does not have an interpretation as angular momentum density as a function of x

































Canonical

Kinetic







Canonical





GTMDs



Generalized TMDs and Wigner

Only way to provide^qdirgct_xare $\vec{k} \in \Re T_{\Omega}(\vec{p} \text{ art} q n)$ or $\vec{p} = \sqrt{2}$



based on Pasquini, Lorcé, Xiong, Yuan, PRD 85 (12)

Wigner distributions and GTMDs



Exclusive dijet production

Hatta, Xiao, Yuan, <u>arXiv:1601.01585</u> Hatta, Nakagawa, Xiao, Yuan, Zhao, <u>arXiv:1612.02445</u> Ji, Yuan, Zhao, <u>arXiv:1612.02438</u>



Exclusive double Drell-Yan

Bhattacharya, Metz, Zhou, <u>arXiv:1702.04387</u>



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 Without the EIC, we will have a very limited view of the inner structure of the proton.
- Apart from mainstream activity (golden and silver), a lot of other interesting topics can be addressed (many other polarized objects, higher twist, jets, nuclear corrections, TMD factorization breaking...)

