

# **Novel proposal for a low emittance muon collider**

**M. Antonelli (LNF)**

# Outline

- Muons case
- Muon accelerators challenges:
  - **muon production**
    - ✓ LEMMA
  - high-gradient acceleration and collider rings
  - Performances
- Conclusions

The strength of a  $\mu$ -beam facility lies in its richness:

- Muon rare processes
- Neutrino physics
- Higgs factory
- Multi-TeV frontier



$\mu$ -colliders can essentially do the HE program of  $e^+e^-$  colliders with added bonus (and some limitations)

# Muon based colliders great potential



As with an  $e^+e^-$  collider, a  $\mu^+\mu^-$  collider offers a precision probe of fundamental interactions without energy limitations

- By **synchrotron radiation** (limit of  $e^+e^-$  **circular** colliders)
- By **beam-strahlung** (limit of  $e^+e^-$  **linear** colliders)

Muon Collider is the ideal technology to extend lepton high energy frontier in the **multi-TeV** range with **reasonable dimension, cost and power consumption**

Muon based **Higgs factory** takes advantage of a strong coupling to Higgs mechanism by  $s$  resonance

**IF THE MUON BEAM NOVEL TECHNOLOGY  
CAN BE DEMONSTRATED TO BE FEASIBLE**

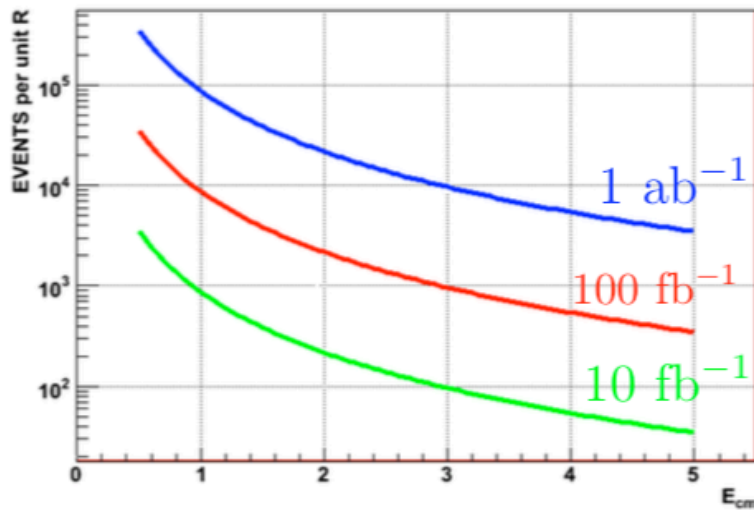
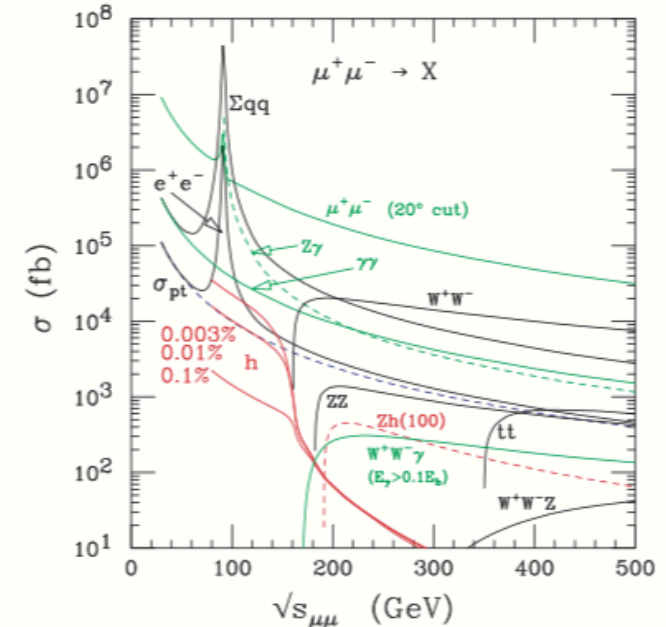


# MultiTeV Lepton Collider Basics

- For  $\sqrt{s} < 500 \text{ GeV}$ 
  - SM threshold region: top pairs;  $W^+W^-$ ;  $Z^0Z^0$ ;  $Z^0h$ ; ...
- For  $\sqrt{s} > 500 \text{ GeV}$ 
  - For SM pair production ( $|\theta| > 10^\circ$ )  
 $R = \sigma / \sigma_{\text{QED}}(\mu^+\mu^- \rightarrow e^+e^-) \sim \text{flat}$   

$$\sigma_{\text{QED}}(\mu^+\mu^- \rightarrow e^+e^-) = \frac{4\pi\alpha^2}{3s} = \frac{86.8 \text{ fb}}{s(\text{TeV}^2)}$$
  - High luminosity required

Standard Model Cross Sections



$$\sqrt{s} = 3.0 \text{ TeV} \quad \mathcal{L} = 10^{34} \text{ cm}^{-2} \text{sec}^{-1} \\ \rightarrow 100 \text{ fb}^{-1} \text{year}^{-1}$$

$\Rightarrow 965 \text{ events/unit of } R$

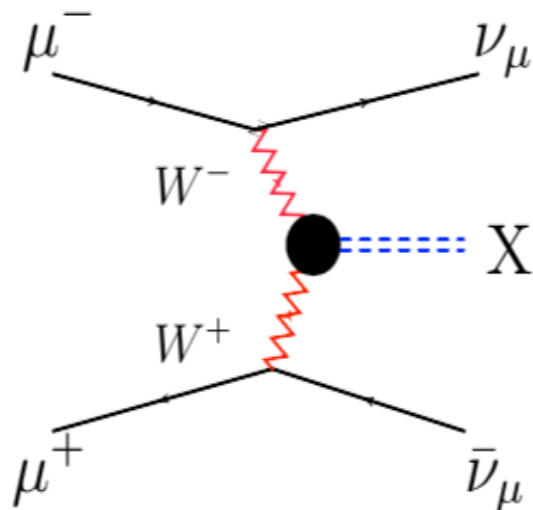
Processes with  $R \geq 0.1$  can be studied

Total - 540 K SM events per year

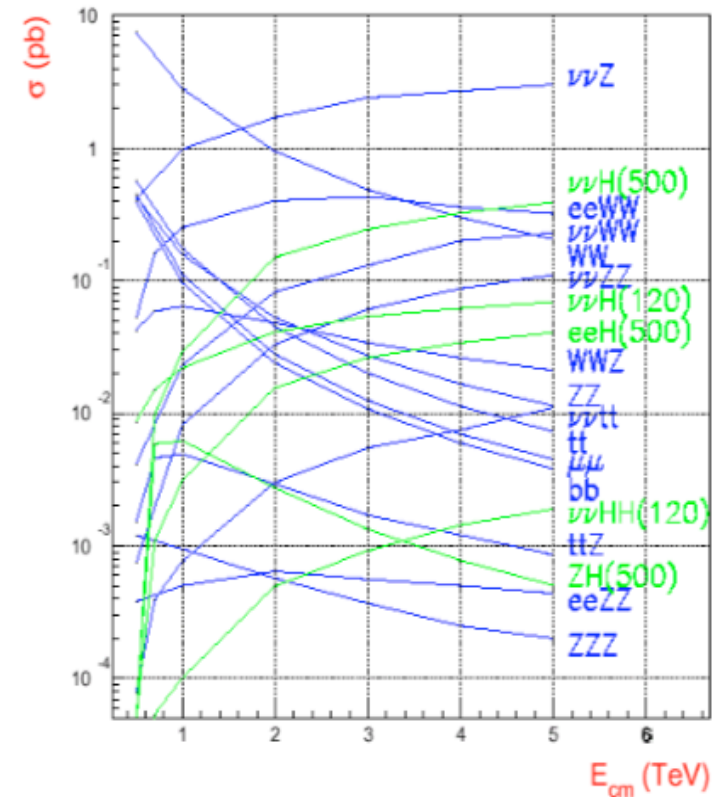
$$== 10^{36} \text{ cm}^{-2} \text{ s}^{-1} @ \sqrt{s} 30 \text{ TeV}$$

# Vector boson fusion

- For  $\sqrt{s} > 1$  TeV - Fusion Processes
  - Large cross sections
  - Increase with  $s$ .
  - Important at multi-Tev energies
  - $M_X^2 < s$
- Backgrounds for SUSY processes
- t-channel processes sensitive to angular cuts



CLIC (or MC  $e \leftrightarrow \mu$ )



$$\sigma(s) = C \ln\left(\frac{s}{M_X^2}\right) + \dots$$

# SM Higgs

(after ~10 years of running)

- Resonant Higgs production:

- Unique measurements  $mh$  and  $\Gamma h$

( $mh \sim 0.1$  MeV,  $\Gamma h \sim 0.2$  MeV)

- Best test of 2nd generation Higgs couplings ( $h \rightarrow \mu+\mu-$ )

- HZ production:

- Similar to  $e^+e^-$  measurements but lower statistics factor 10 (ILC/CEPC) 100 FCC-ee

- VBF at multiTeV

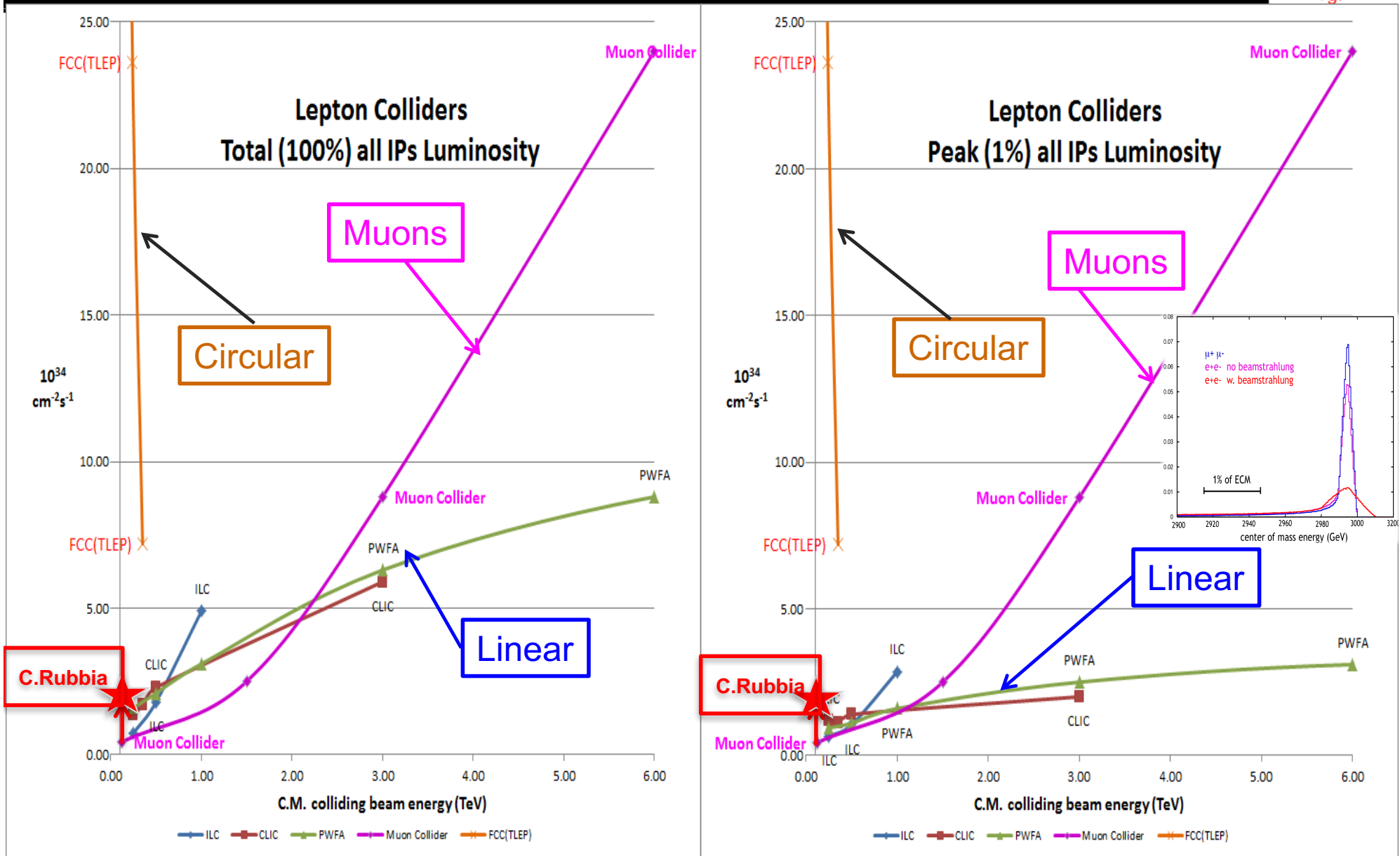
- High  $x_s(O(1\text{Pb})@6\text{TeV})$  & high lumi better statistics than FCC-ee ?
  - Competitive (probably best) measurement of HH production

Error on	$\mu\mu$ resonance	ILC	FCC-ee
$m_H$ (MeV)	0.06	30	8
$\Gamma_H$ (MeV)	0.17	0.16	0.04
$g_{Hbb}$	2.3%	1.5%	0.4%
$g_{HWW}$	2.2%	0.8%	0.2%
$g_{H\tau\tau}$	5%	1.9%	0.5%
$g_{H\gamma\gamma}$	10%	7.8%	1.5%
$g_{H\mu\mu}$	2.1%	20%	6.2%
$g_{HZZ}$	–	0.6%	0.15%
$g_{Hcc}$	–	2.7%	0.7%
$g_{Hgg}$	–	2.3%	0.8%
$BR_{invis}$	–	<0.5%	<0.1%

of

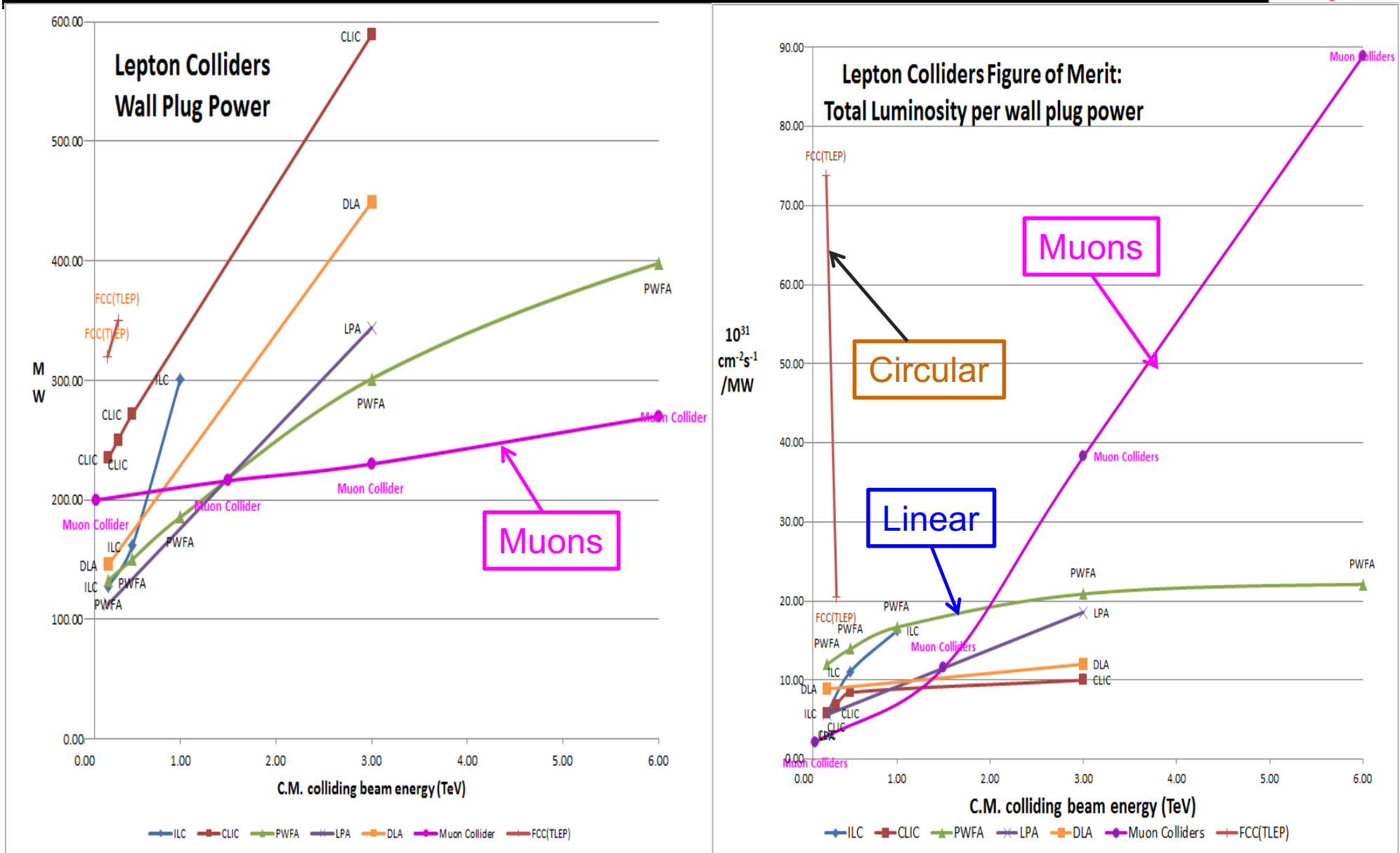
P. Janot

# Muon Colliders potential of extending leptons high energy frontier with high performance





# Muon Colliders extending leptons high energy frontier with potential of considerable power savings



# Muon Source

## Goals

- **Neutrino Factories:**  $O(10^{21})$   $\mu/\text{yr}$  within the acceptance of a  $\mu$  ring
- **Muon Collider:** luminosities  $>10^{34}/\text{cm}^{-2}\text{s}^{-1}$  at TeV-scale ( $\sim N_{\mu}^2 / \epsilon_{\mu}$ )

## Options

Conventional: Tertiary production through **proton on target** (and then cool), baseline for Fermilab design study

$$\text{Rate} > 10^{13} \mu/\text{sec} \quad N_{\mu} = 2 \cdot 10^{12} / \text{bunch}$$

Unconventional:

- **$e^+e^-$  annihilation: positron beam on target** (very low emittance and no cooling needed), baseline for our proposal here

$$\text{Rate} \sim 10^{11} \mu/\text{sec} \quad N_{\mu} \sim 5 \times 10^7 / \text{bunch}$$

- **by Gammas: GeV-scale Compton  $\gamma$**  not discussed here

$$\text{Rate} \sim 5 \cdot 10^{10} \mu/\text{sec} \quad N_{\mu} \sim 10^6 \quad (\text{Pulsed Linac}) \quad [\text{V. Yakimenko (SLAC)}]$$

$$\text{Rate} > 10^{13} \mu/\text{sec} \quad N_{\mu} \sim \text{few} \cdot 10^4 \quad (\text{High Current ERL})$$

see also: W. Barletta and A. M. Sessler NIM A 350 (1994) 36-44

# Exploring the potential for a Low Emittance Muon Collider

## References:

- M. Antonelli, “*Very Low Emittance Muon Beam using Positron Beam on Target*”, **ICHEP (2016)**
- M. Antonelli, E. Bagli, M. Biagini, M. Boscolo, G. Cavoto, P. Raimondi and A. Variola, “*Very Low Emittance Muon Beam using Positron Beam on Target*”, **IPAC (2016)**
- M. Antonelli, “*Performance estimate of a FCC-ee-based muon collider*”, **FCC-WEEK 2016**
- M. Antonelli, “*Low-emittance muon collider from positrons on target*”, **FCC-WEEK 2016**
- M. Antonelli, M. Boscolo, R. Di Nardo, P. Raimondi, “*Novel proposal for a low emittance muon beam using positron beam on target*”, **NIM A 807 101-107 (2016)**
- P. Raimondi, “*Exploring the potential for a Low Emittance Muon Collider*”, in **Discussion of the scientific potential of muon beams workshop**, CERN, Nov. 18<sup>th</sup> 2015
- M. Antonelli, **Presentation Snowmass 2013**, Minneapolis (USA) July 2013, [M. Antonelli and P. Raimondi, Snowmass Report (2013) also INFN-13-22/LNF Note

Also investigated SLAC team:

L. Keller, J. P. Delahaye, T. Markiewicz, U. Wienands:

- “*Luminosity Estimate in a Multi-TeV Muon Collider using  $e^+e^- \rightarrow \mu^+\mu^-$  as the Muon Source*”, MAP 2014 Spring workshop, Fermilab (USA) May '14
- Advanced Accelerator Concepts Workshop, San Jose (USA), July '14

# Idea for low emittance $\mu$ beam

Conventional production: from **proton on target**

$\pi$ , K decays from proton on target have typical  $P_\mu \sim 100 \text{ MeV}/c$   
( $\pi$ , K rest frame)

whatever is the boost  $P_T$  will stay in Lab frame  $\rightarrow$

**very high emittance** at production point  $\rightarrow$  **cooling needed!**

Direct  $\mu$  pair production:

Muons produced from  $e^+e^- \rightarrow \mu^+\mu^-$  at  $\sqrt{s}$  around the  $\mu^+\mu^-$  threshold ( $\sqrt{s} \sim 0.212 \text{ GeV}$ ) in asymmetric collisions (to collect  $\mu^+$  and  $\mu^-$ )

NIM A Reviewer: *“A major advantage of this proposal is the lack of cooling of the muons.... the idea presented in this paper may truly revolutionise the design of muon colliders ... ”*

## Advantages:

1. **Low emittance possible:**  $P_\mu$  is tunable with  $\sqrt{s}$  in  $e^+e^- \rightarrow \mu^+\mu^-$   $P_\mu$  can be **very small** close to the  $\mu^+\mu^-$  threshold
2. **Low background:** Luminosity at low emittance will allow low background and low  $\nu$  radiation (easier experimental conditions, can go up in energy)
3. **Reduced losses from decay:** muons can be produced with a relatively high boost in asymmetric collisions
4. **Energy spread:** Muon Energy spread **also small at threshold**, it gets larger as  $\sqrt{s}$  increases, one can use correlation with emission angle (eventually it can be reduced with short bunches)

## Disadvantages:

- **Rate:** much smaller cross section wrt protons

$$\sigma(e^+e^- \rightarrow \mu^+\mu^-) \sim 1 \mu\text{b at most}$$

*i.e.* Luminosity( $e^+e^-$ ) =  $10^{40} \text{ cm}^{-2} \text{ s}^{-1} \rightarrow$  gives  $\mu$  rates  $10^{10} \text{ Hz}$

# Possible Schemes

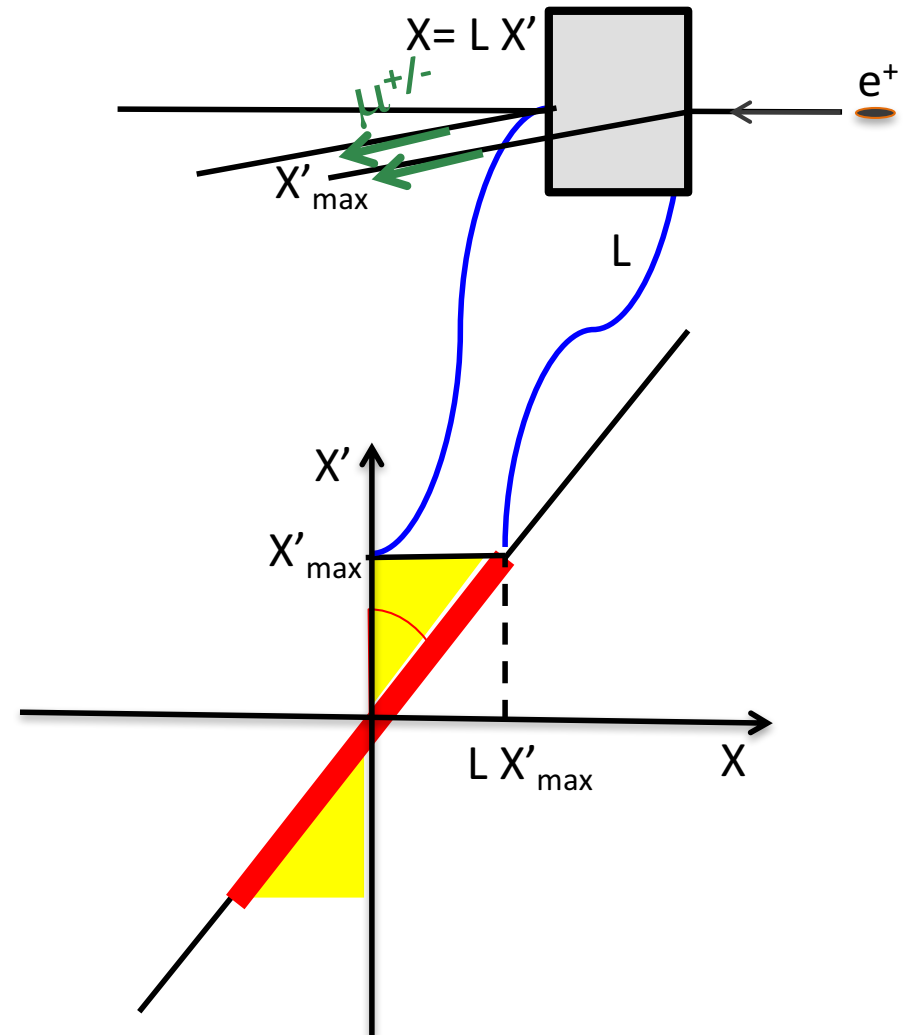
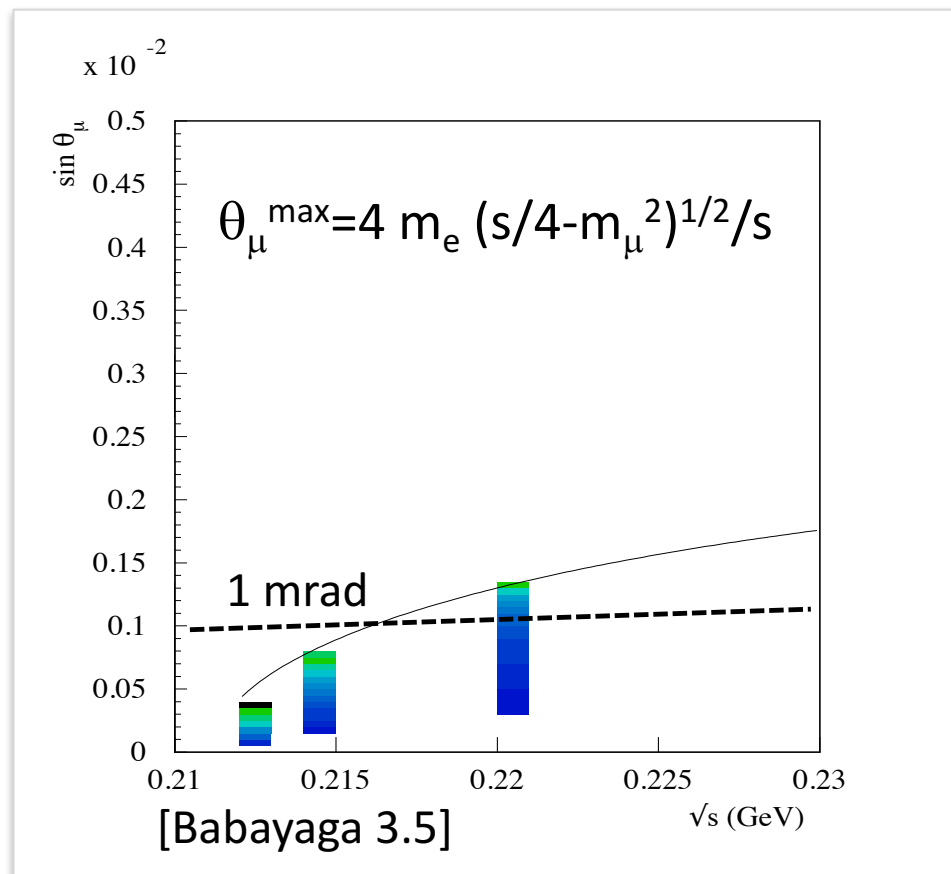
- **Low energy collider with e<sup>+</sup>/e<sup>-</sup> beam (e<sup>+</sup> in the GeV range):**
  1. Conventional asymmetric collisions (but required luminosity is beyond current knowledge)
  2. Positron beam interacting with continuous beam from electron cooling (too low electron density,  $10^{20}$  electrons/cm<sup>-3</sup> needed to obtain an reasonable conversion efficiency to muons)
- **Electrons at rest (seems more feasible):**
  3. e<sup>+</sup> on Plasma target
  4. e<sup>+</sup> on standard target (eventually crystals in channeling)
    - Need Positrons of ~45 GeV
    - $\gamma(\mu) \sim 200$  and  $\mu$  laboratory lifetime of about 500  $\mu$ s



Ideally muons will *copy* the positron beam

# Muons angle contribution to $\mu$ beam emittance

The target thickness and c.o.m. energy completely determine the emittance contributions due to muon production angle



$$\epsilon_{\mu} = X X'_{\max} / 12 = L (\theta_{\mu}^{\max})^2 / 12$$

# Criteria for target design

- **Number of  $\mu^+\mu^-$  pairs produced per interaction:**

$$n(\mu^+\mu^-) = n^+ \rho^- L \sigma(\mu^+\mu^-)$$

$n^+$  = number of  $e^+$

$\rho^-$  = target electron density

$L$  = target length

- **$\rho^- L$  constraints**

- Ideal target ( $e^-$  dominated)

$$(\rho^- L)_{\max} = 1/\sigma(\text{radiative bhabha}) \approx 10^{25} \text{ cm}^{-2}$$

(beam lifetime determined by radiative Bhabha)

- With  $(\rho^- L)_{\max}$  one has a maximal  $\mu^+\mu^-$  production efficiency  $\sim 10^{-5}$
- Muon beam emittance increases with  $L$  (in absence of intrinsic focusing effects)  $\rightarrow$  increase  $\rho^-$
- Conventional target  $(\rho^- L)_{\max}$  depends on material (see next slides)



# Criteria for target design

Bremsstrahlung on nuclei and multiple scattering (MS) are the dominant effects in real life...  $X_0$  and electron density will matter:

- **Heavy materials**

- minimize emittance (enters linearly) → Copper has about same contributions to emittance from MS and  $\mu^+\mu^-$  production
- high  $e^+$  loss (Bremsstrahlung is dominant)

- **Very light materials**

- maximize production efficiency(enters quad) →  $H_2$
- even for liquid need  $O(1m)$  target → emittance increase

- **Not too heavy materials(Be, C )**

- Allow low emittance with small  $e^+$  loss

**optimal: not too heavy and thin**

# Application for Multi-TeV Muon Collider as an example

- Use thin target with high efficiency and small  $e^+$  loss
- Positrons in storage ring with high momentum acceptance
- No need of extreme beam energy spread

# Possible target: 3 mm Be

45 GeV  $e^+$  impinging beam

- Emittance at  $E_\mu = 22$  GeV:

$$\varepsilon_x = 0.19 \cdot 10^{-9} \text{ m-rad}$$

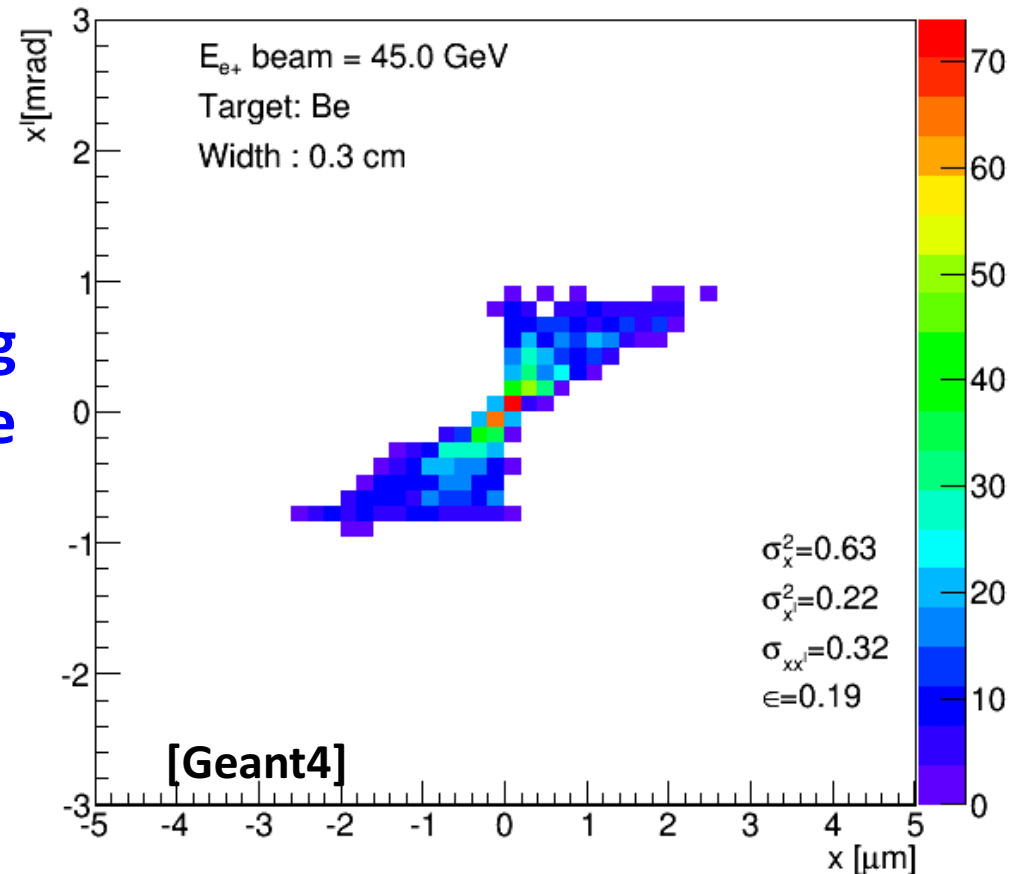
**Multiple Scattering  
contribution is negligible**

->  $\mu$  after production is not affected by nuclei in target

->  $e^+$  beam emittance is preserved, not being affected by nuclei in target (see also next slide)

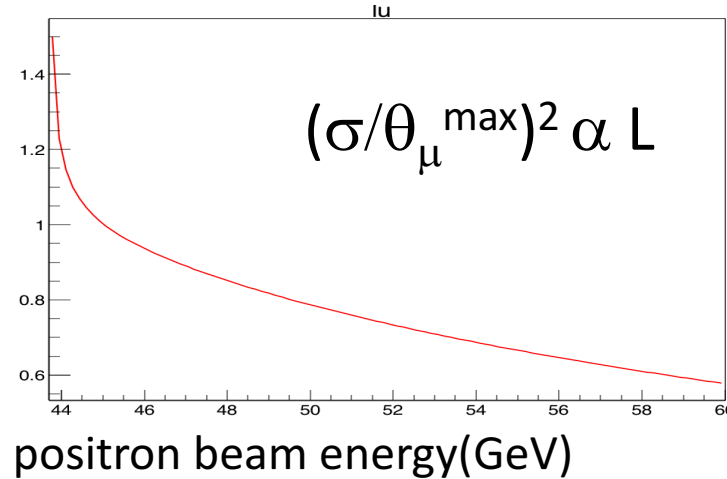
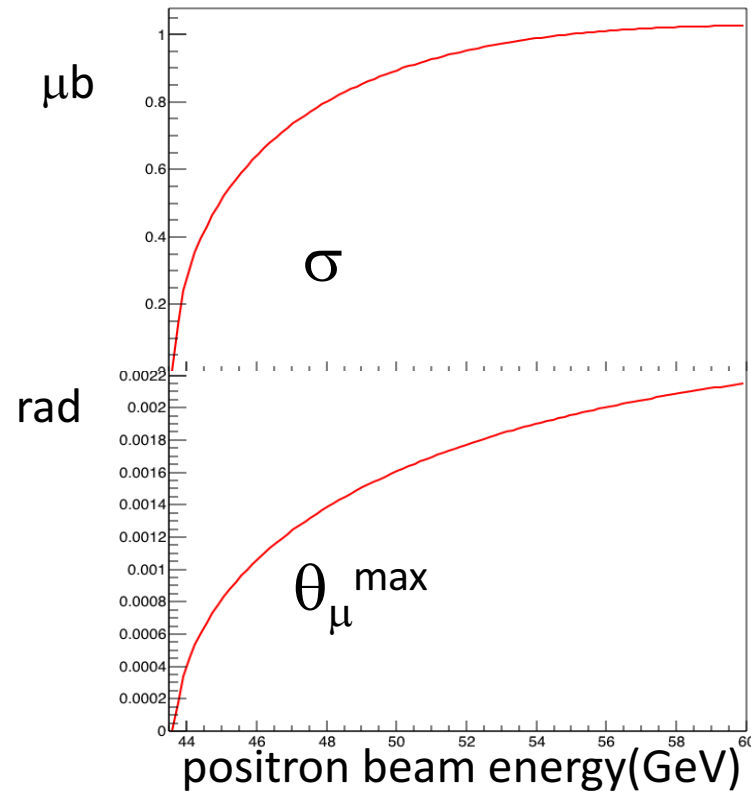
- Conversion efficiency:  $10^{-7}$
- Muons beam energy spread: 9%

## Muons at the target exit surface

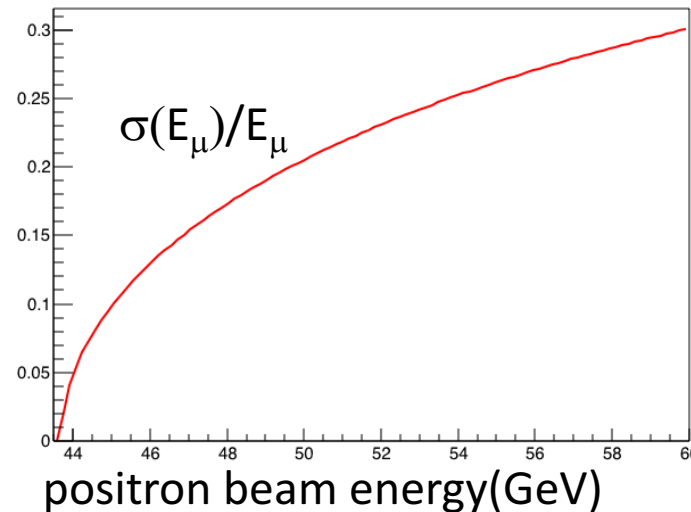


# Luminosity vs $e^+$ beam energy

Is there an optimal value for the positron beam energy?

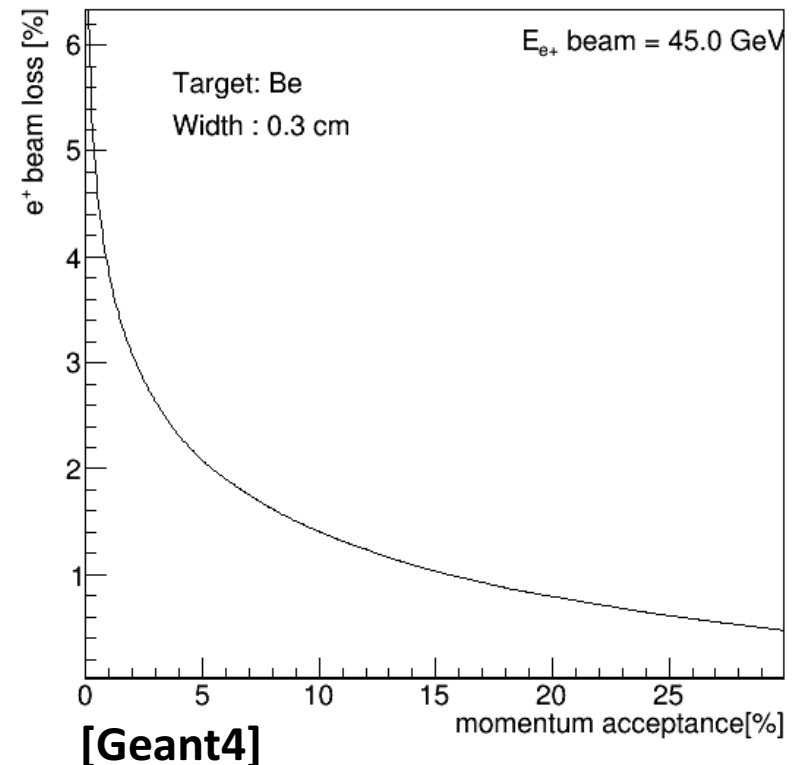
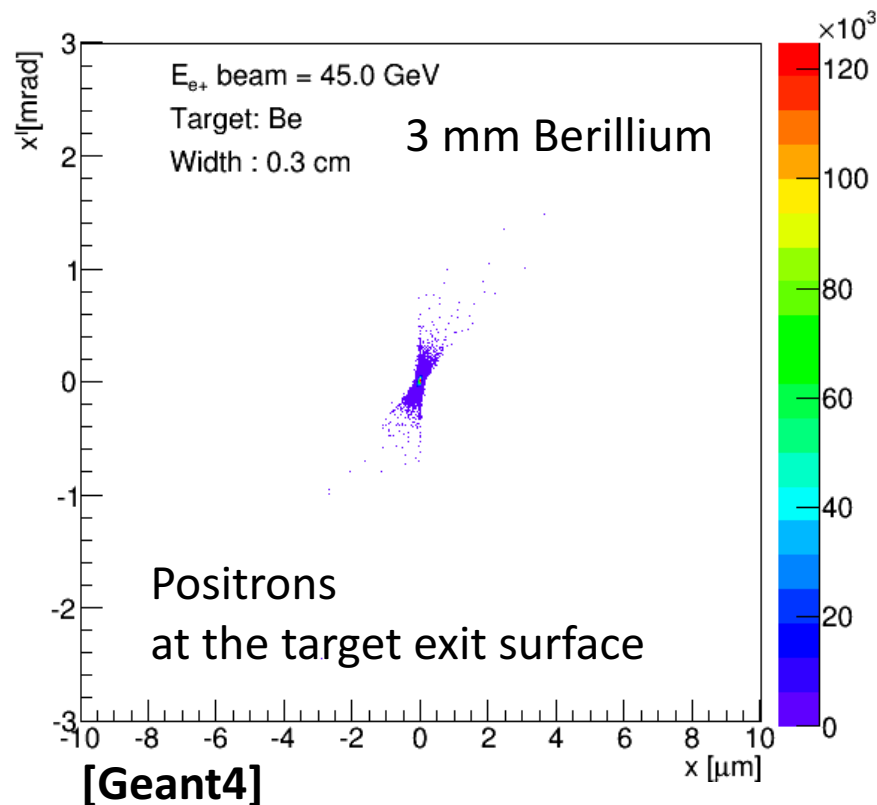


Valid for  $\theta_{\mu}^{\text{max}}$   
dominated  
emittance



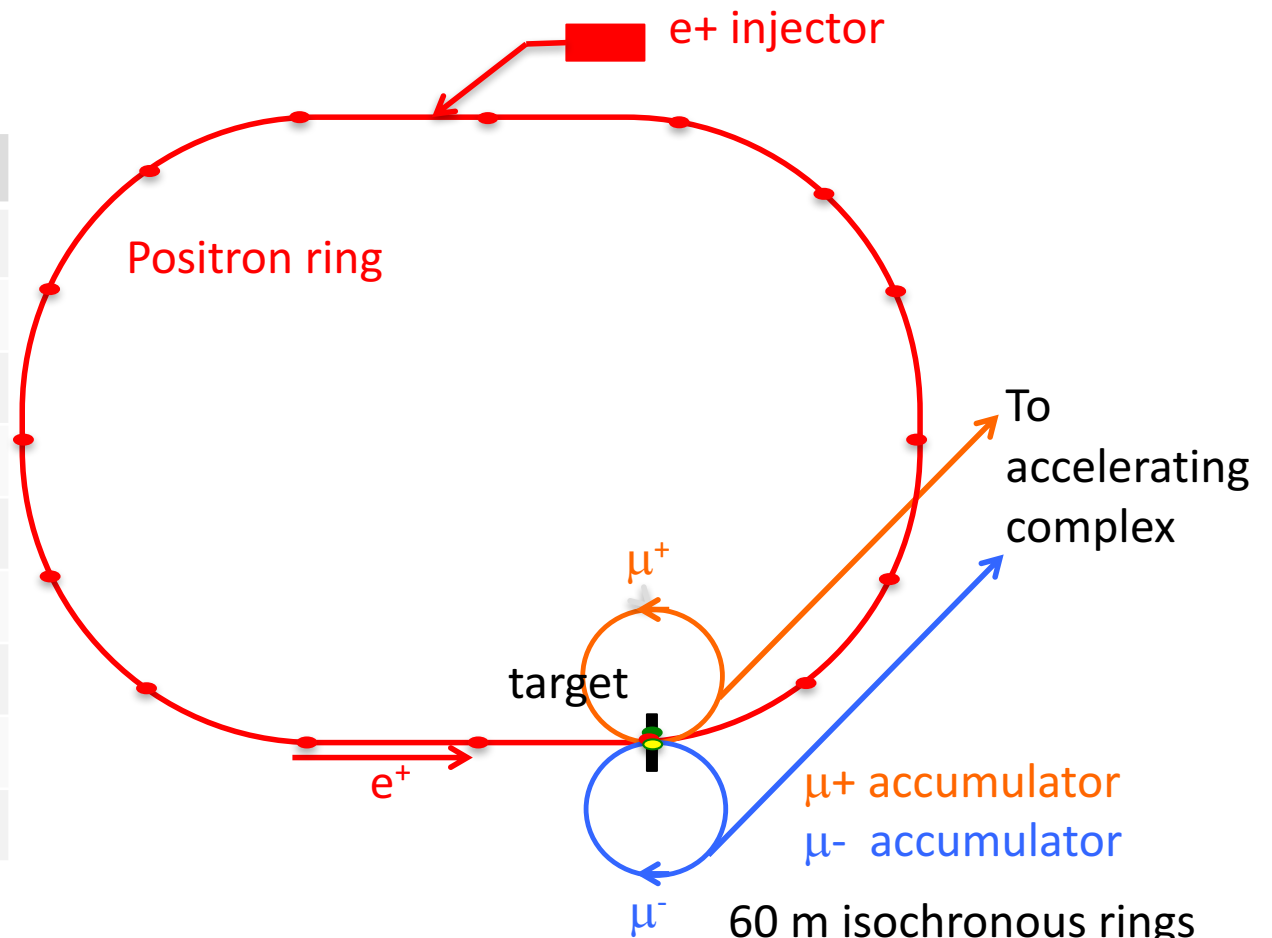
# Positrons Storage Ring Requirements

- Transverse phase space almost not affected by target
- Most of positrons experience a small energy deviation:  
A large fraction of  $e^+$  can be stored (depending on the momentum acceptance)
  - 10% momentum acceptance will increase the effective muon conversion efficiency (produced muon pairs/produced positrons) by factor 100



# Schematic Layout for muon source from e+

Circumference	6 km
$\rho$	0.6 km
number e+ bunches	100
e+ bunch spacing	200 ns
Beam current	240 mA
e+ Particles/bunch	$3 \cdot 10^{11}$
Rate e+ on target	$1.5 \cdot 10^{18}$ e+/s
$U_0$	0.58 GeV
$P_{\text{tot}}$	139 MW
B	0.245 T



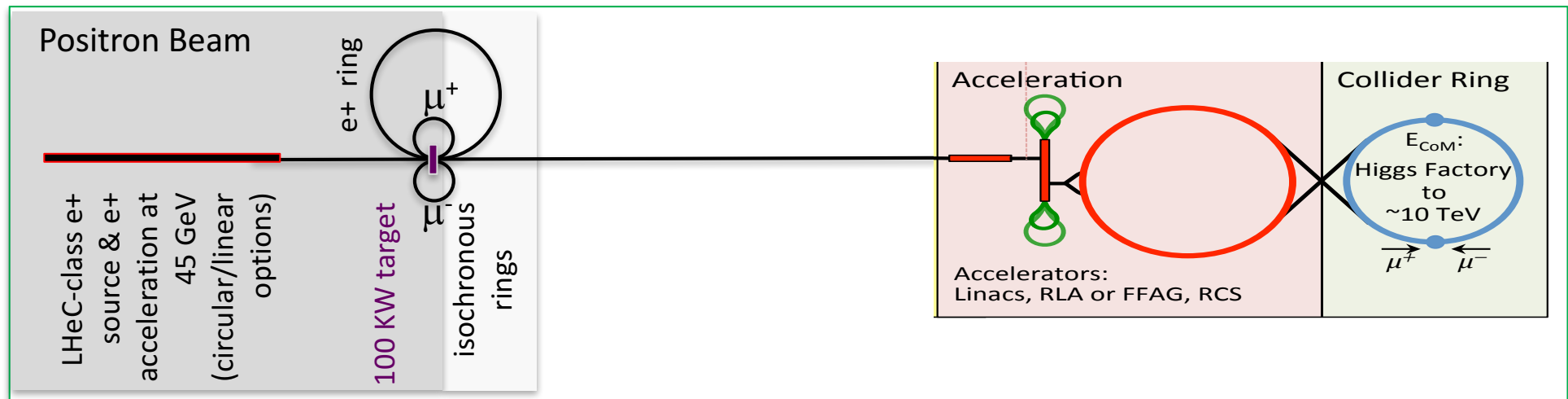
## Key point:

**Positron source requirements strictly related to the e+ ring momentum acceptance**

60 m isochronous rings recombine bunches for  $\sim 1 \tau_{\mu}^{\text{lab}} \sim 2500$  turns

$$n_b = \sum_{i=1}^{N_T} e^{-\Delta t(N_T-i)/\tau_{\mu}^{\text{lab}}}$$

# Muon Collider: Schematic Layout for positron based muon source

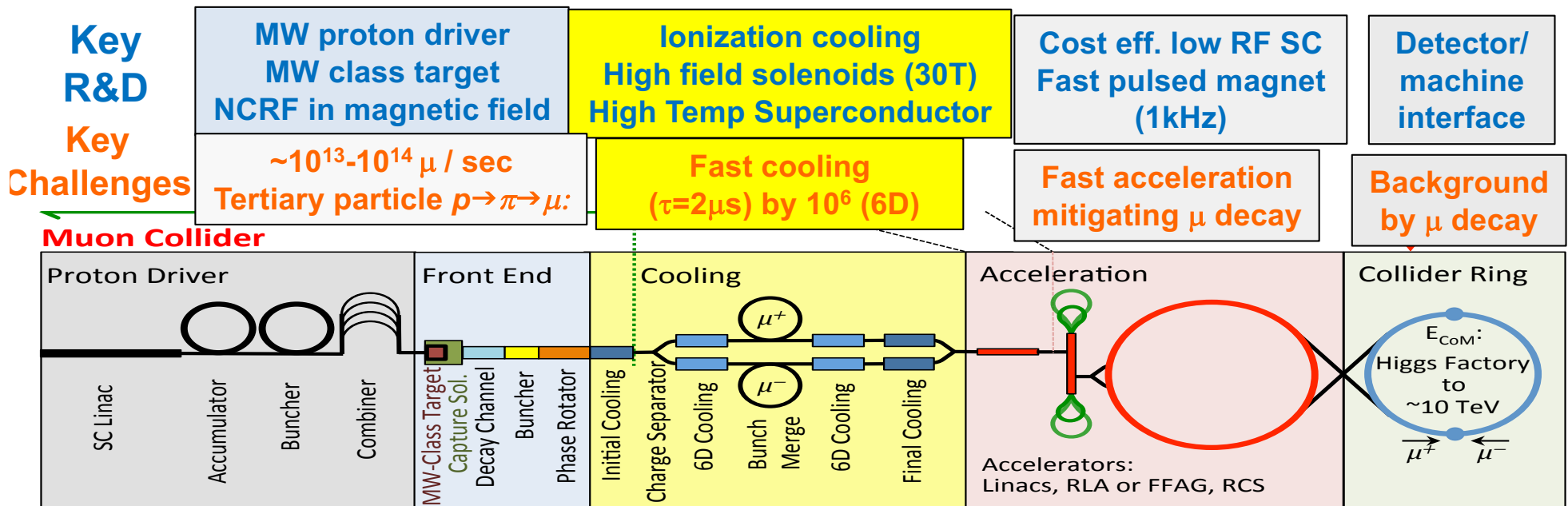


**Key Challenges**

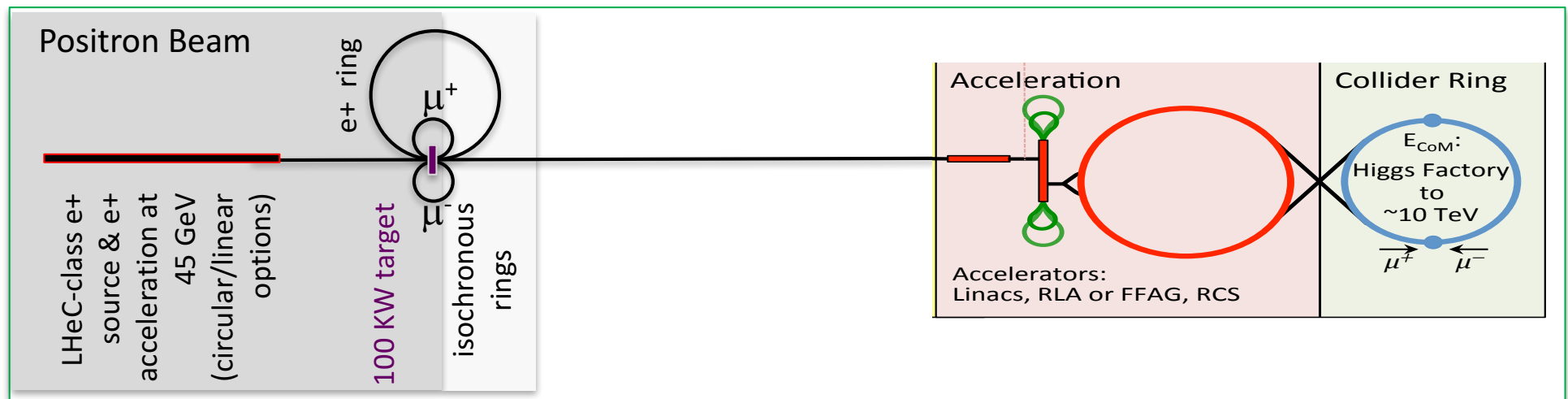
$\sim 10^{11} \mu / \text{sec}$  from  $e^+e^- \rightarrow \mu^+\mu^-$

**Key R&D**

$10^{15} e^+/\text{sec}$ , 100 kW class target, NON destructive process in  $e^+$  ring



share the same complex



**Key Challenges**

$\sim 10^{11} \mu / \text{sec}$  from  $e^+e^- \rightarrow \mu^+\mu^-$

**Key R&D**

$10^{15} e^+/\text{sec}$ , 100 kW class target, NON destructive process in  $e^+$  ring

**EASIER AND CHEAPER DESIGN, IF FEASIBLE**



# Muon beam parameters

Assuming

- a positron ring with a total 25% momentum acceptance (10% easily achieved) and
- $\sim 3 \times$  LHeC positron source rate

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	positron source	proton source
$\mu$ rate[Hz]	$9 \cdot 10^{10}$	$2 \cdot 10^{13}$
$\mu$ /bunch	$4.5 \cdot 10^7$	$2 \cdot 10^{12}$
normalised $\epsilon$ [ $\mu\text{m-mrad}$ ]	40	25000

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**Very small emittance, high muon rates** but relatively small bunch population:

- The actual number of  $\mu$ /bunch in the muon collider can be larger by a factor  $\sim \tau_{\mu}^{\text{lab}}(\text{HE})/500 \mu\text{s}$  ( $\sim 100$  @6 TeV) by topping up.

# Low EMittance Muon Accelerator Draft Parameters

comparable luminosity with  
lower  $N\mu$ /bunch  
(lower background)  
thanks to very small  
emittance (and lower beta\*)

Of course, a design  
study is needed to  
validate this table

		LEMC-6TeV
<b>Parameter</b>	<b>Units</b>	
LUMINOSITY/IP	$\text{cm}^{-2} \text{s}^{-1}$	5.09E+34
Beam Energy	GeV	3000
Hourglass reduction factor		1.000
Muon mass	GeV	0.10566
Lifetime @ prod	sec	2.20E-06
Lifetime	sec	0.06
c*tau @ prod	m	658.00
c*tau	m	1.87E+07
1/tau	Hz	1.60E+01
Circumference	m	6000
Bending Field	T	15
Bending radius	m	667
Magnetic rigidity	T m	10000
Gamma Lorentz factor		28392.96
N turns before decay		3113.76
$\beta_x$ @ IP	m	0.0002
$\beta_y$ @ IP	m	0.0002
Beta ratio		1.0
Coupling (full current)	%	100
Normalised Emittance x	m	4.00E-08
Emittance x	m	1.41E-12
Emittance y	m	1.41E-12
Emittance ratio		1.0
Bunch length (zero current)	mm	0.1
Bunch length (full current)	mm	0.1
Beam current	mA	0.048
Revolution frequency	Hz	5.00E+04
Revolution period	s	2.00E-05
Number of bunches	#	1
N. Particle/bunch	#	6.00E+09
Number of IP	#	1.00
$\sigma_x$ @ IP	micron	1.68E-02
$\sigma_y$ @ IP	micron	1.68E-02
$\sigma_{x'}$ @ IP	rad	8.39E-05
$\sigma_{y'}$ @ IP	rad	8.39E-05

# Radiological hazard due to neutrinos from a muon collider

Colin Johnson, Gigi Rolandi and Marco Silari

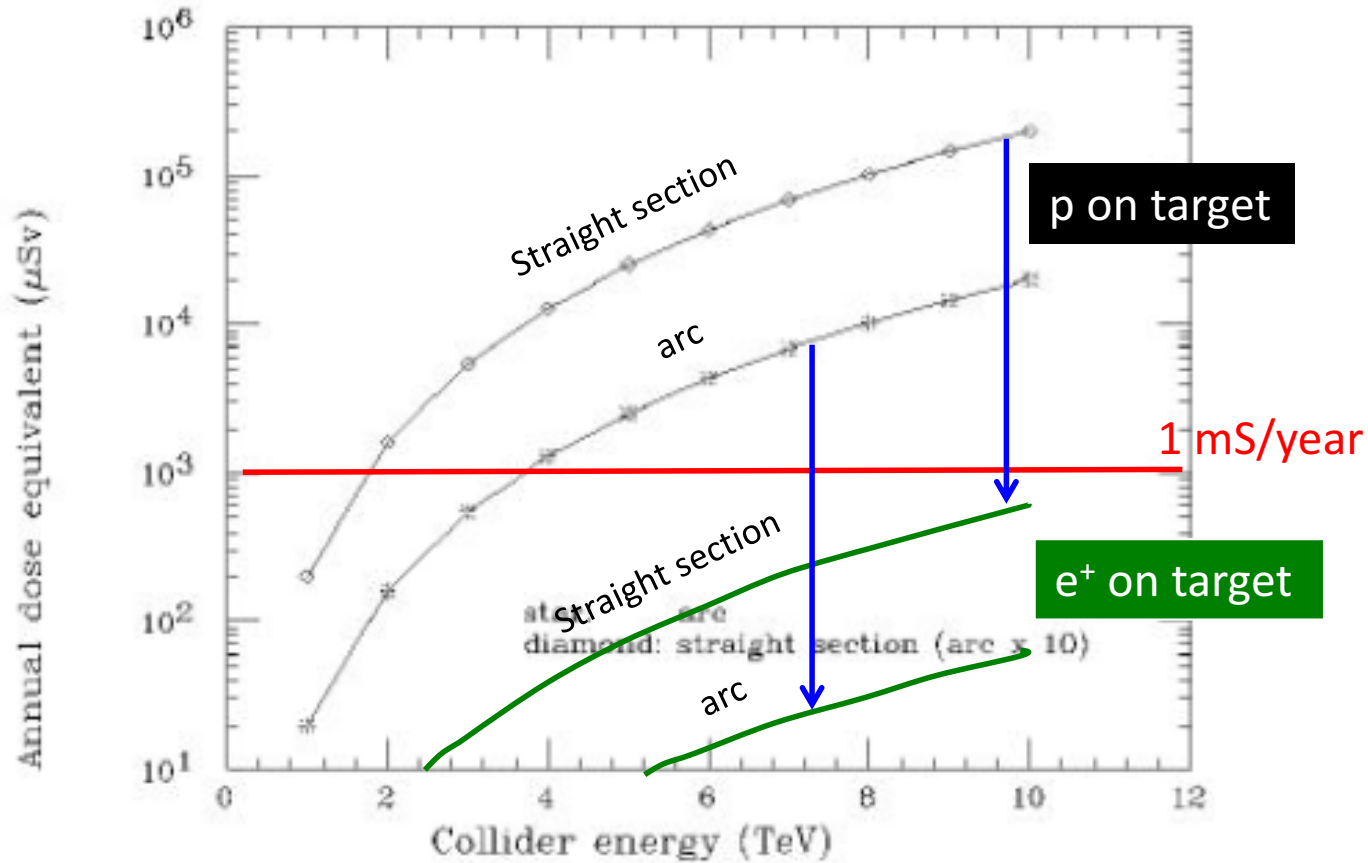


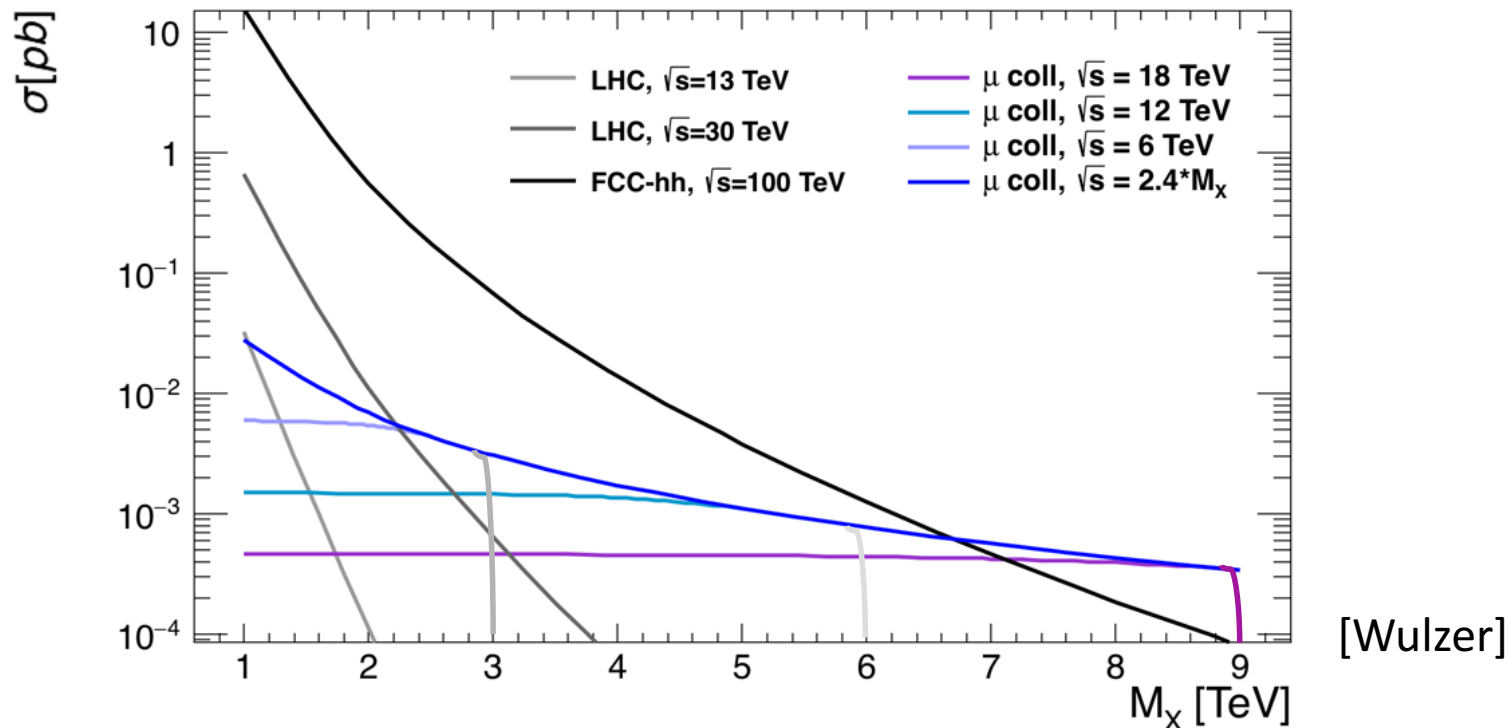
Fig. 1. Dose equivalent due to neutrino radiation at 36 km distance (collider at 100 m depth)

muon rate: p on target option  $3 \times 10^{13} \mu/\text{s}$

e<sup>+</sup> on target option  $9 \times 10^{10} \mu/\text{s}$

# Muon collider reach: an example

- Study the same benchmark used for White Paper:
  - New heavy particles, both colored and EW charged ( $\sim$ vector like quarks)  $\rightarrow$  xsec can be predicted
  - FCC reach stops at  $M_x = 7$  TeV
- Hadron machine pays the price of the exponentially falling PDF  $\rightarrow$  multi-TeV muon machine can be competitive!



# Key Feasibility Issues

Positron Source

Muon Target

Positron Ring

**HIGH rate**

**Non destructive**

**Mom. acceptance**

Targets survival

NEED

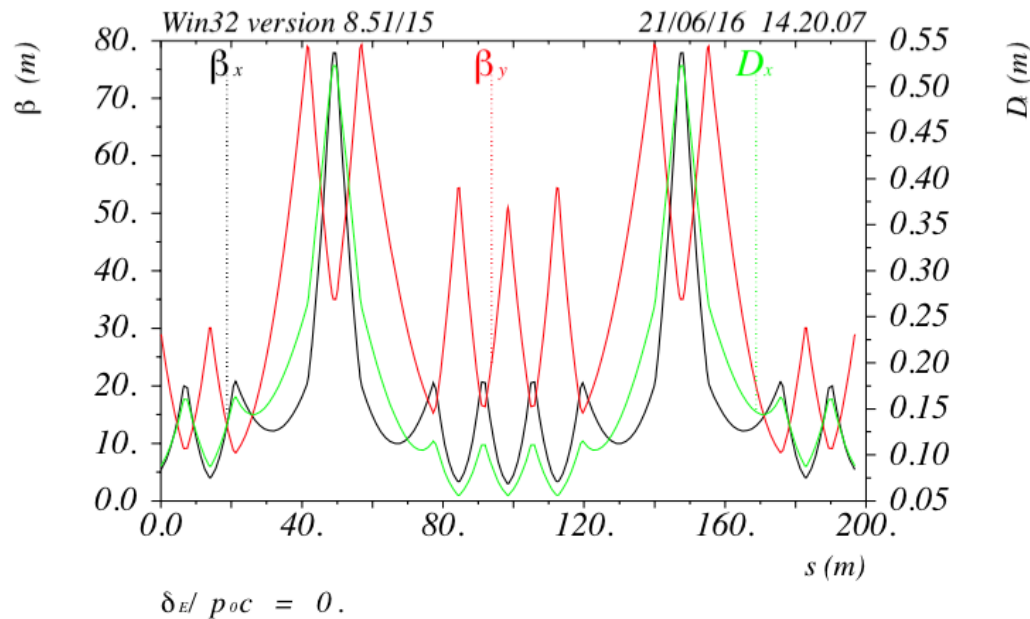
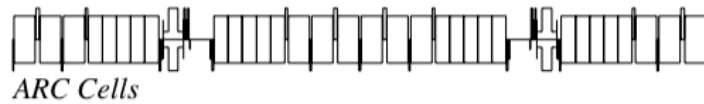
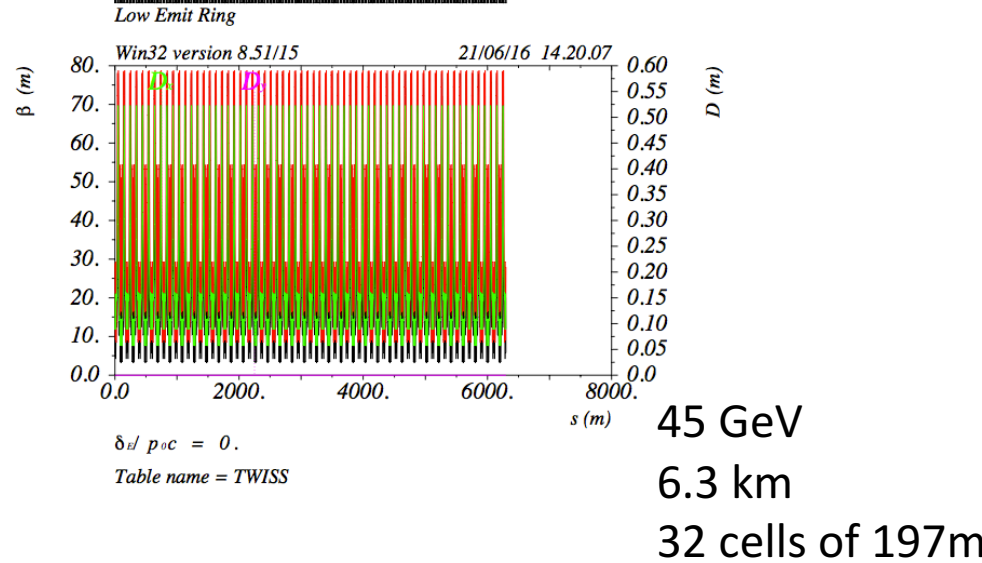
deep investigation  
(design study)

- $\mu$  Acceleration
- Collider Ring
- Collider MDI
- Collider Detector

(mostly) independent on muon source  
Benefit from MAP studies

LEMMA at the starting line

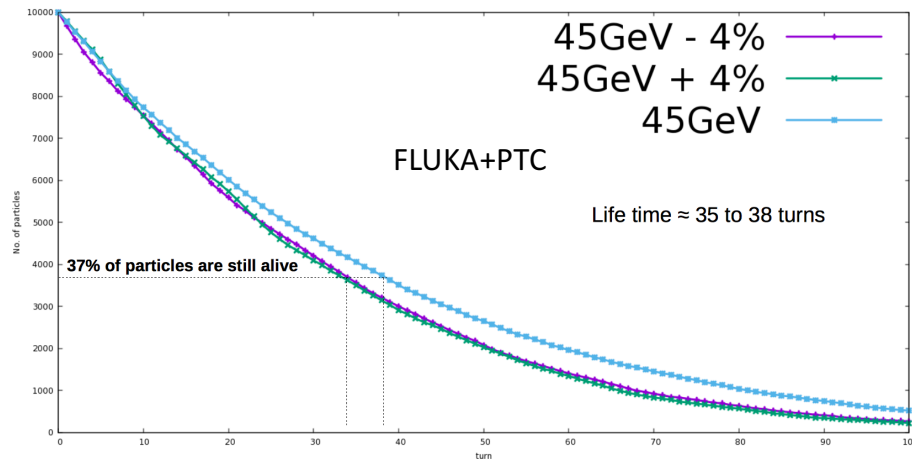
# First Optics for e<sup>+</sup> ring



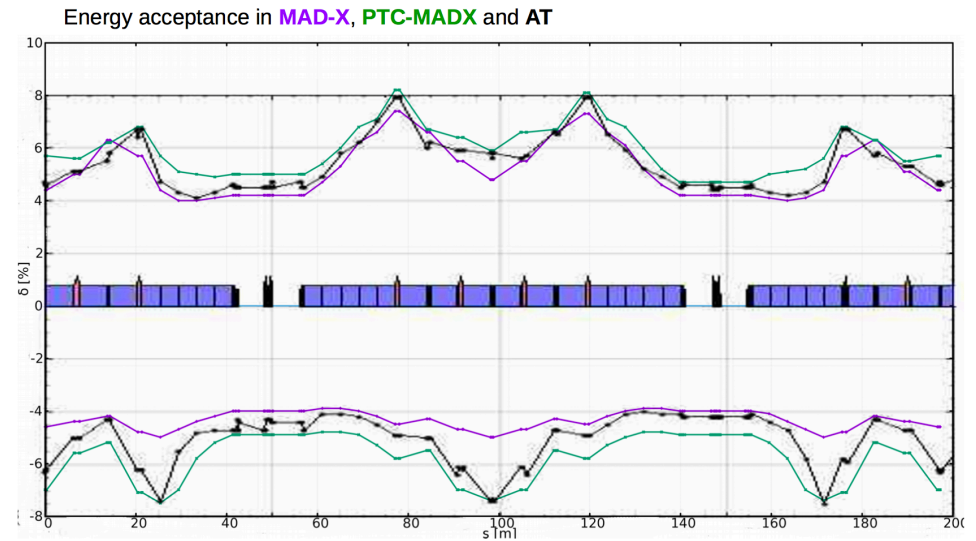
Parameter	Units	pos_Ring
Energy	GeV	45
Circumference	m	6300
Bending radius	m	709.6
Magnetic rigidity	T m	150
Lorentz factor		88062.62
Coupling (full current)	%	1
Emittance x (from model)	m	5.73E-09
Emittance y	m	5.73E-11
Bunch length (zero current)	mm	3.6
Beam current	mA	240
RF frequency	Hz	5.00E+08
RF voltage	GV	0.768
Revolution frequency	Hz	4.76E+04
Harmonic number	#	10508
Revolution period	s	2.10E-05
Number of bunches	#	100
N. Particle/bunch	#	3.15E+11
Synchronous phase	#	0.73
Synchrotron frequency	Hz	2415.31
Synchrotron tune	#	5.08E-02
synchrotron period	turns	19.70
Overvoltage		1.50
Transverse damping time	turns	175.00
Transverse damping time	s	0.0037
Longitudinal damping time	turns	87.50
Longitudinal damping time	s	1.84E-03
Energy Loss/turn	GeV	0.511
Momentum compaction		1.21E-04
B field	T	0.211
Rf energy acceptance	%	3.98
Energy spread (SR)	dE/E	1.00E-03
SR power loss	GW	0.12
SR power/Circumference	kW/m	19.48

# First multi turn simulations (still very preliminary)

Use different methods: AT/PTC/MADX (optics)+ GEANT/FLUKA (target)



Results from other combinations within 10%



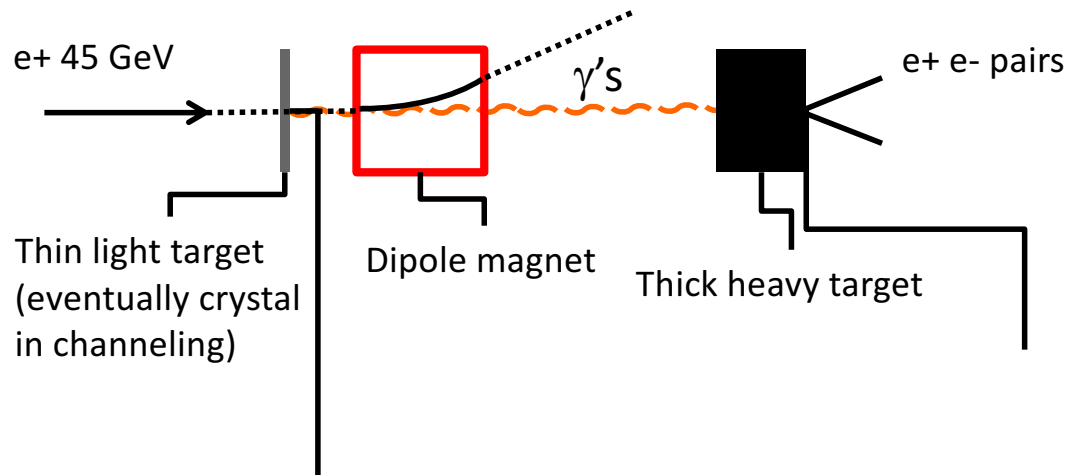
- Dedicated “interaction” region under study to decrease losses and beam size increase
- Emittance contribution from various sources have to be matched
- Optimize momentum aperture
- Design muon accumulator rings



# Embedded positron source?

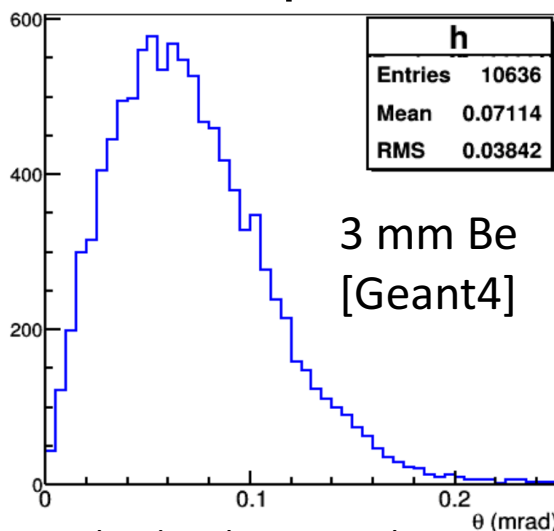
Positron source extending the target complex?  
Possibility to use the  $\gamma$ 's from the  $\mu$  production target to produce  $e^+$

Positron collection based on Adiabatic Matching Device under study

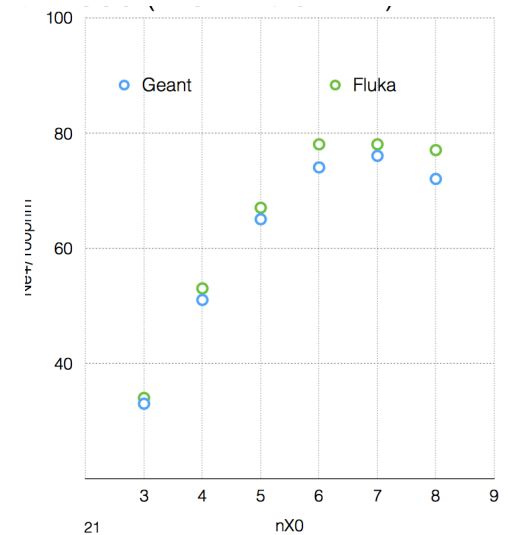
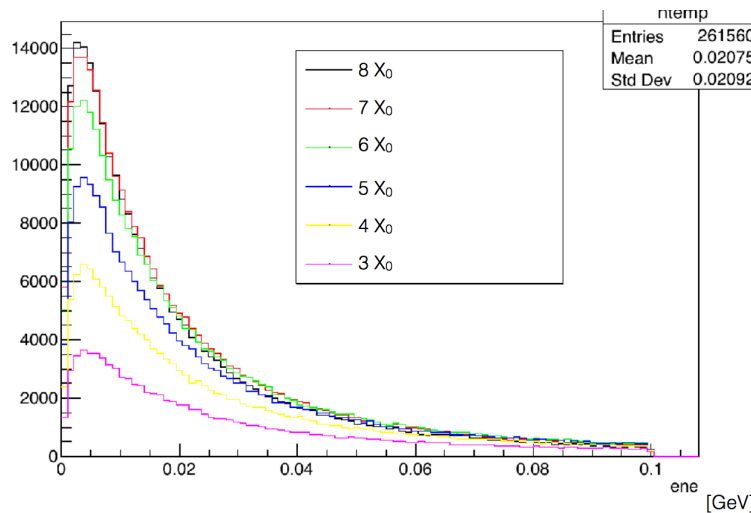


Proposed for example for CLIC

Produce a fraction of  $e^+$  of the incoming positron beam

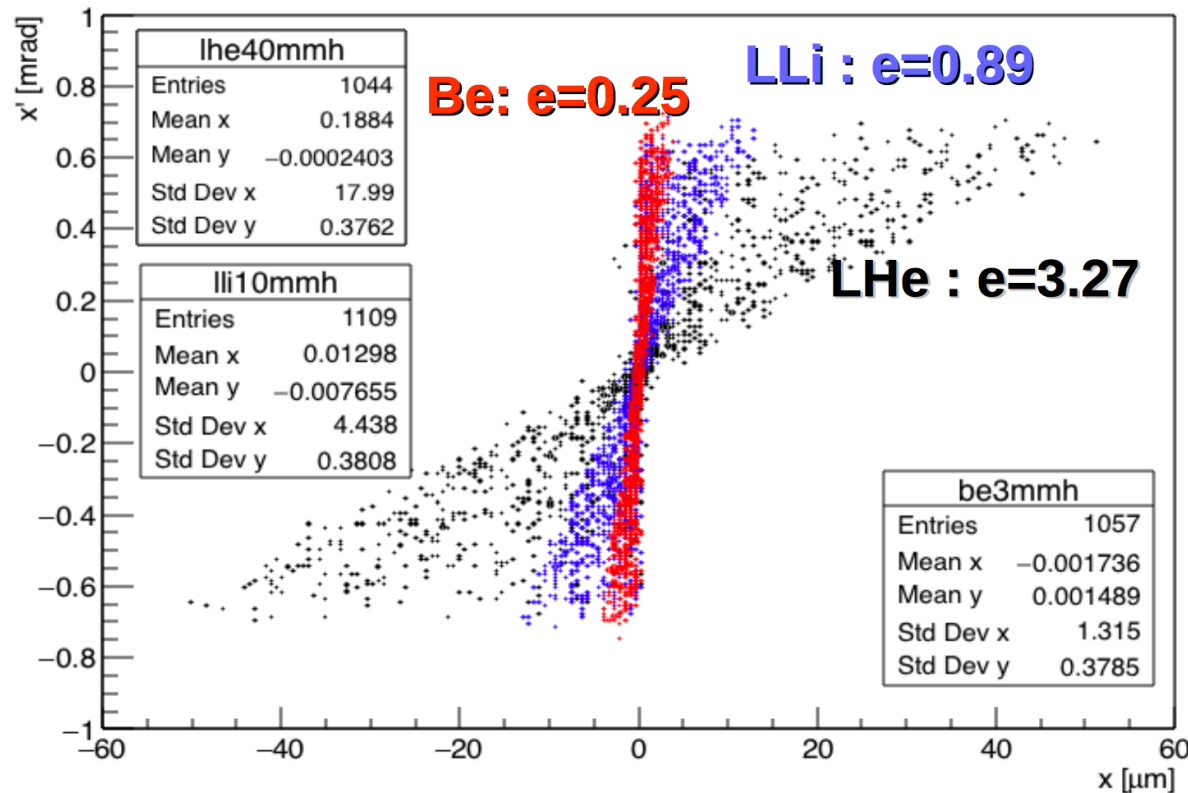


$\gamma$ 's angular distribution at the target exit

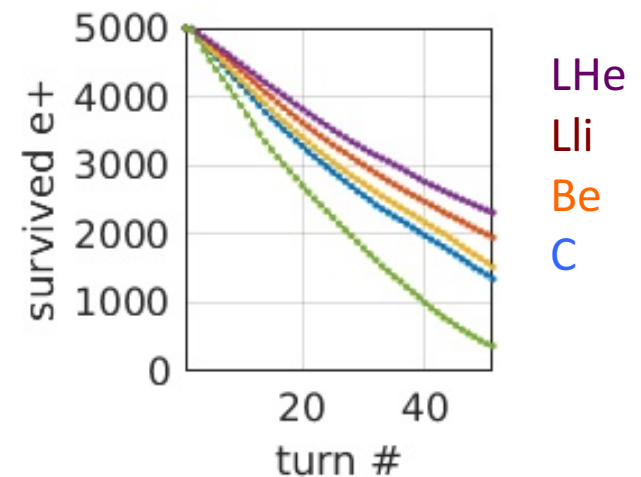


# Going to lighter targets for $\mu$ production

Look to light liquid targets to reduce problems of thermo-mechanical stresses



LLi might be a good option



Proposed/tested for targets for  $n$  production

High Boiling point 1615 K  
Mass evaporation?  
Safety?

# Crystals as a target ?

## Positrons

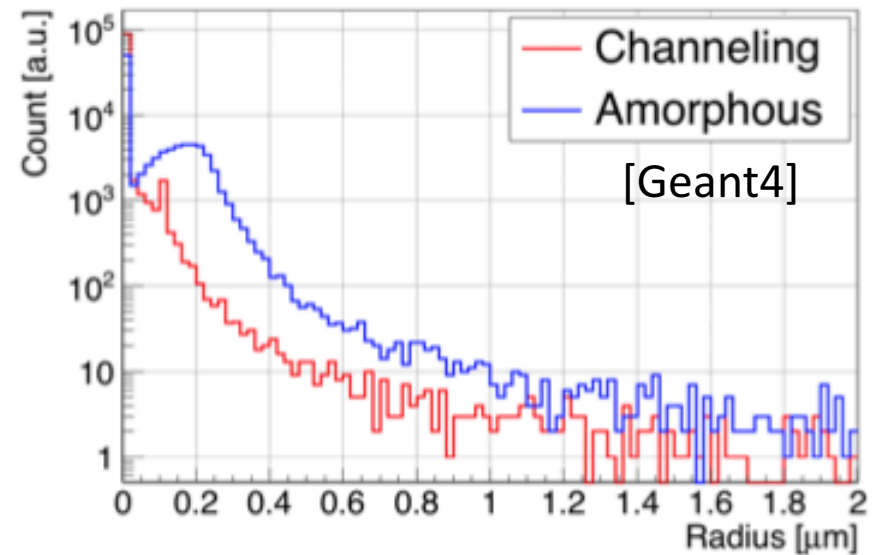
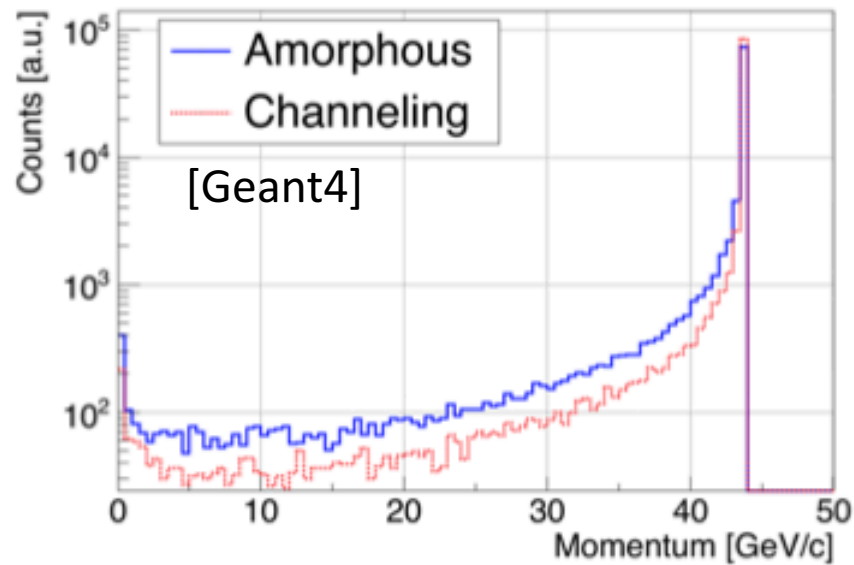
43.8 GeV  $e^+$

4.1 mm Si Target

Channeling plane: (110)

Momentum

Position



# Tests with e<sup>+</sup> beam

Use tertiary 45 GeV e<sup>+</sup> beam in CERN North area (H4)  
(ask for 2 weeks of beam time for next year)

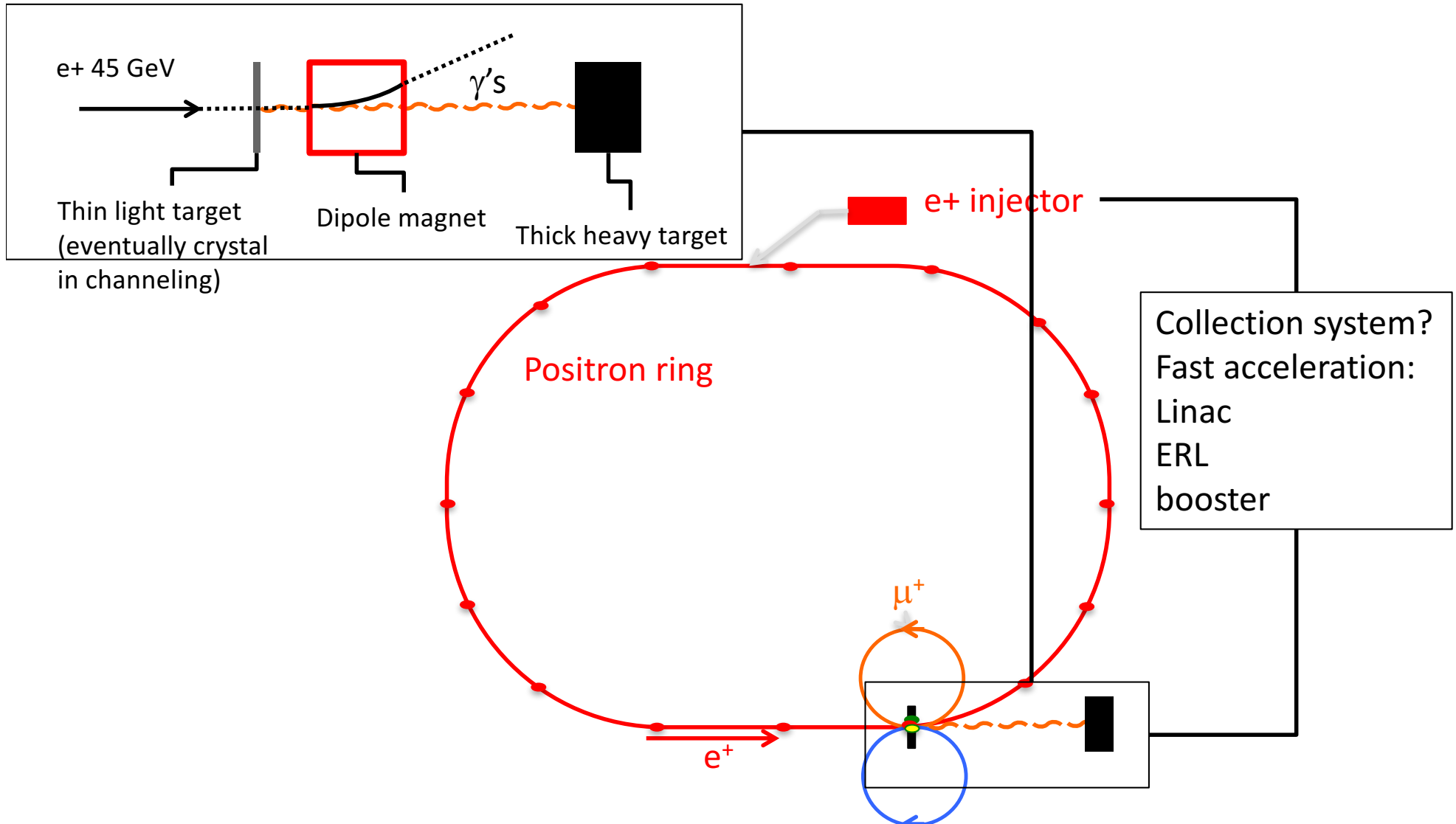
- Low intensity (one by one e<sup>+</sup> tracking) with crystals and amorphous targets:
  - measure beam degradation (emittance energy spectrum)
  - measure produced photons flux and spectrum
- High intensity (up to  $5 \times 10^6$  /spill) with amorphous targets:
  - measure muon production rate and muons kinematic properties

# Conclusion

- Very low emittance muon beams can be obtained by means of positron beam on target
- Low emittance would allow to extend the center of mass energy
- interesting muon rates require:
  - Challenging positron source (synergy with LHeC/FCC-eh, ILC,...)
  - Positron ring with high momentum acceptance (synergy with next generation SL sources and FCC-ee)
  - Thin targets surviving to  $\sim 100$  KW
- We are working on all these issues
- fast muon acceleration concepts and collider rings design studied by MAP

# Backup Slides

# Embedded positron source?

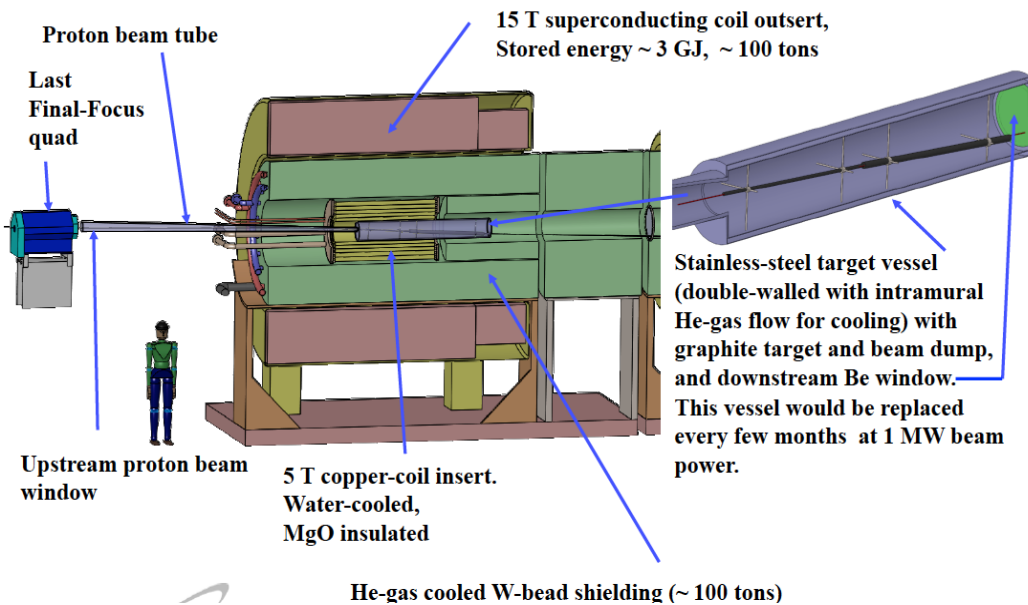


# MAP muon generation by Proton driver

H.Kirk (BNL)

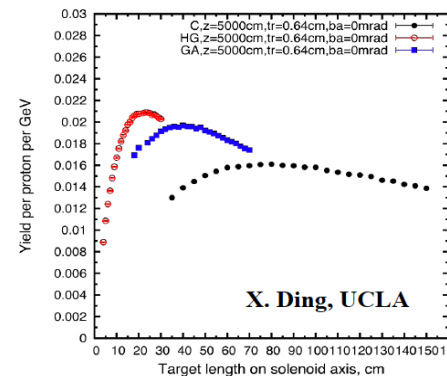


## A Graphite Target Core



- MW-Class proton driver at ~5-10 GeV
- Capture solenoid system ( $\mu^+$  &  $\mu^-$ )
  - 15 T outsert, 5 T insert
  - ~3GJ stored energy

## Choice of Target Materials II

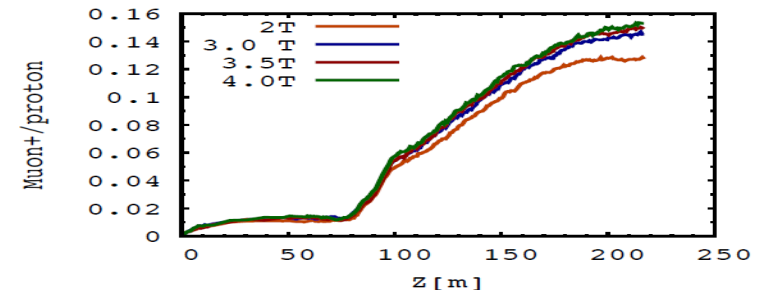
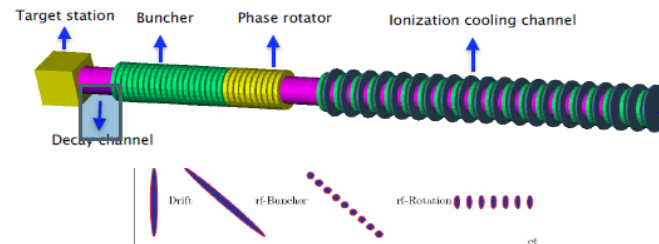


- High Z (e.g. Hg)
- Mid Z (e.g. Ga)
- Low Z (e.g. Carbon)

A **25%** advantage of using high-Z Hg compared to low-Z Carbon  
 Low-z Carbon is attractive due to its simplicity and robustness

- Initial operation with 1MW carbon target
- Upgrade to multi-MW with Liquid Metal Jet Technology (demonstrated in MERIT Experim.)

Proton Beam: KE = 6.75 GeV  
 Normalization: For Hg  $\Sigma(\mu^+ + \mu^-)/\text{proton} \approx 1$



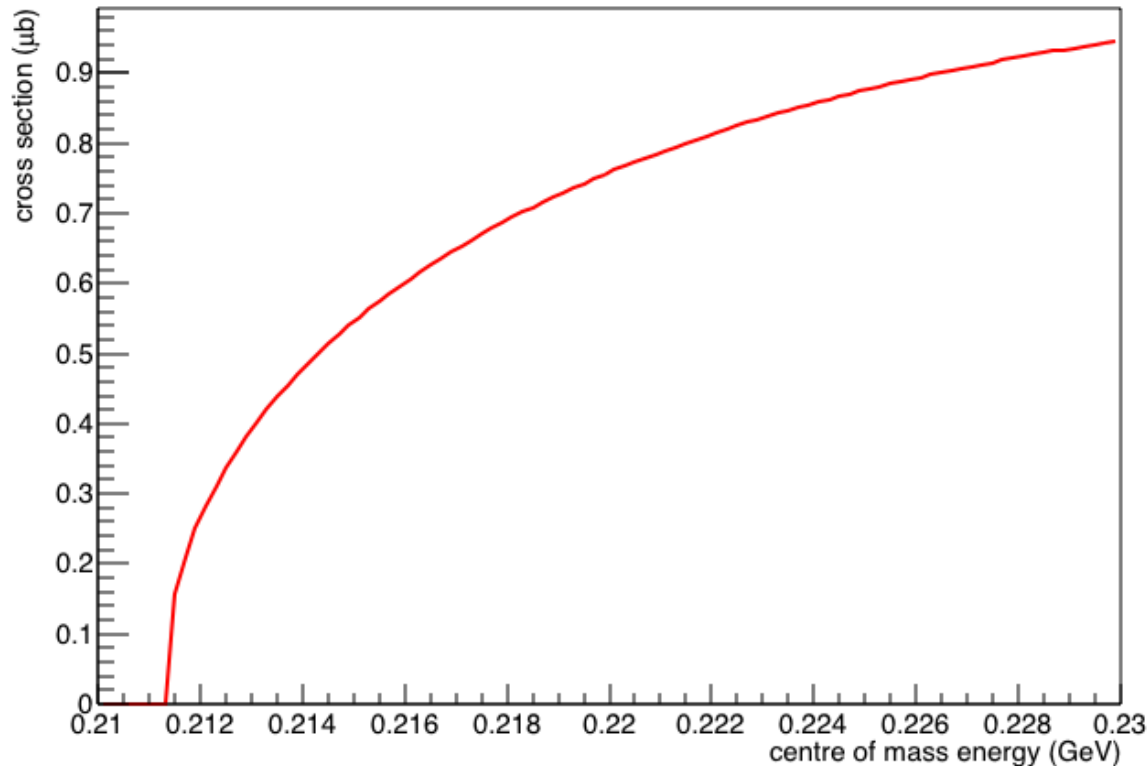
H.K.Sayed (BNL)

Muon per proton production at Front End exit



# Processes at $\sqrt{s}$ around 0.212 GeV

- Bhabha scattering,  $\mu^+\mu^-$  production  $\gamma\gamma$  (not relevant)
- $e^+e^- \rightarrow \mu^+\mu^-$  cross section:



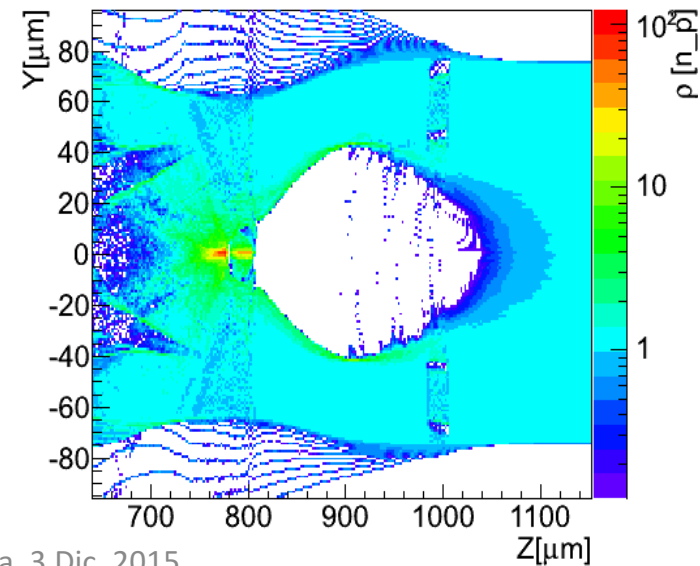
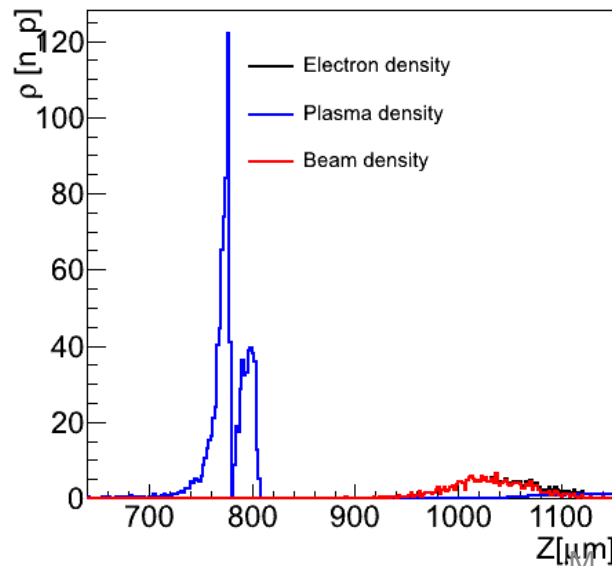
Muonium production also investigated:

huge cross section (mb range)  
 $10^{-4}$  eV width

Not viable.... Deeper studies?

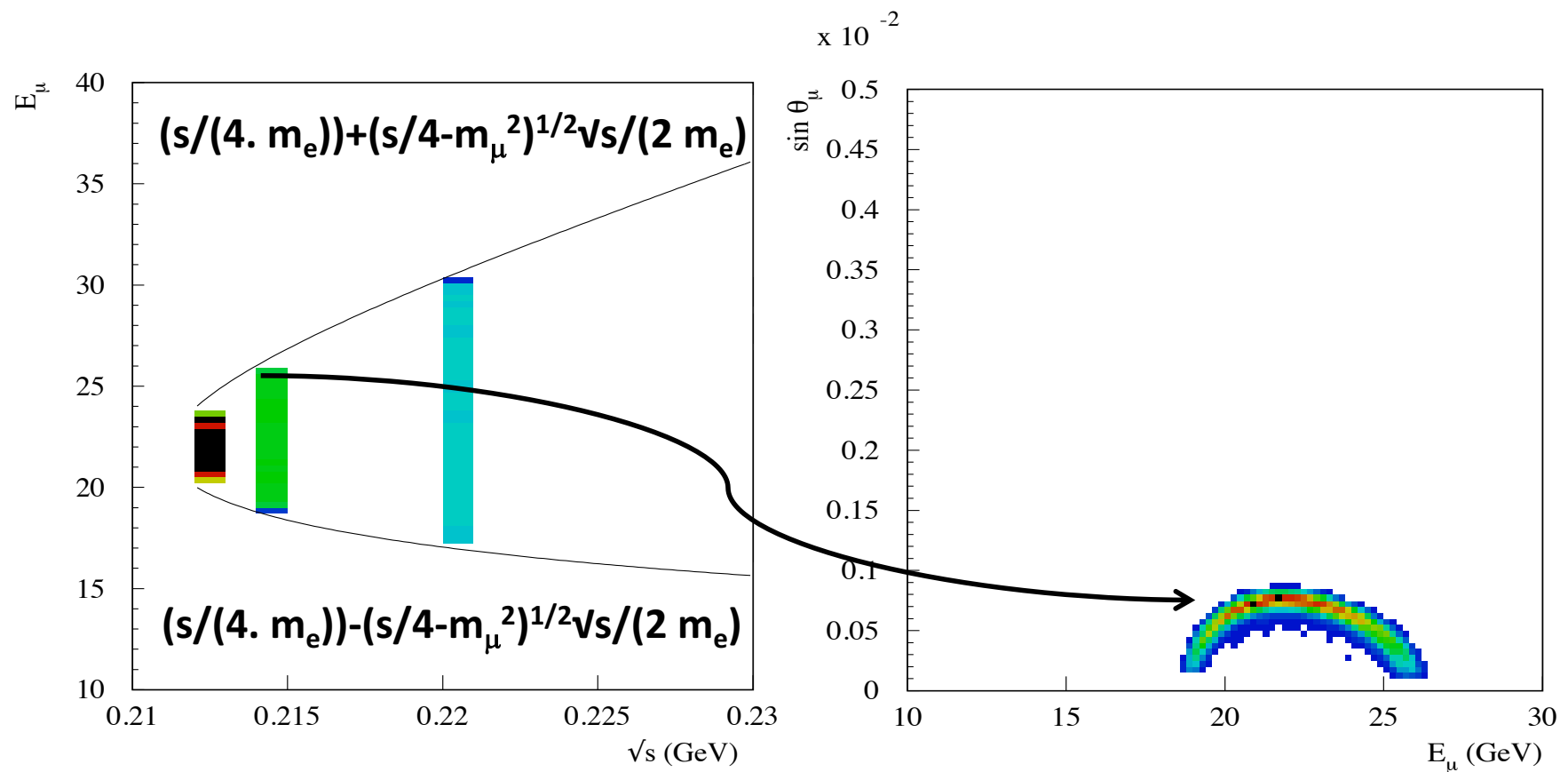
# Few statements on the plasma option

- Plasma would be a good approximation of an ideal electron target ++ autofocussing by Pinch effect
- enhanced electron density can be obtained at the border of the blow-out region (up x100)
- Simulations for  $n_p = 10^{16}$  electrons/cm<sup>3</sup> (C. Gatti, P. Londrillo)
- Region size decreases with  $1/\sqrt{n_p}$  even don't know if blowout occurs at  $n_p \sim 10^{20}$  electrons/cm<sup>3</sup>



# Processes at $\sqrt{s} \sim 0.212$ GeV $e^+$ on target

$e^+e^- \rightarrow \mu^+\mu^-$  muons energy spread:



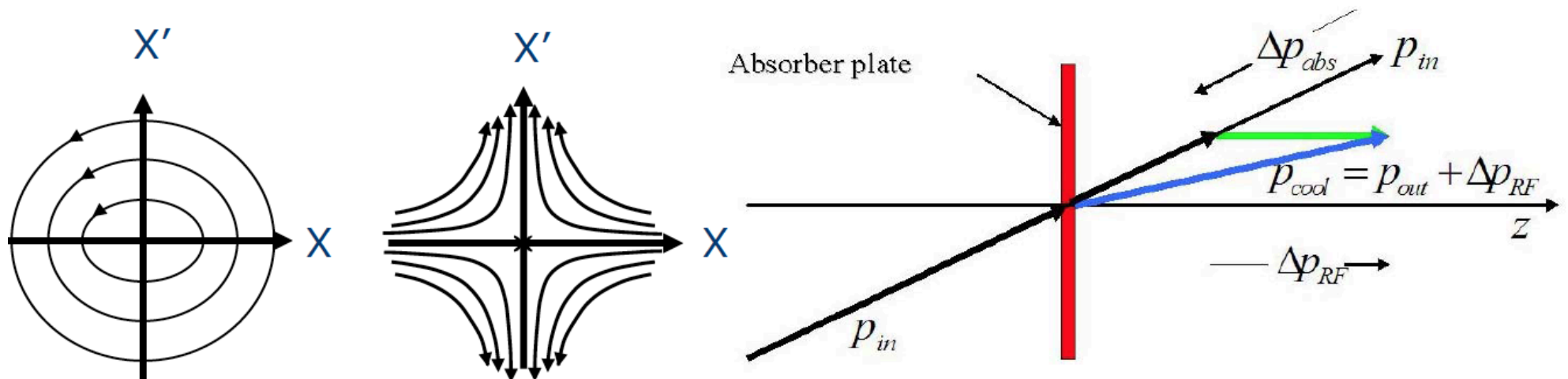
# Parametric-resonance Ionization Cooling

see Derbenev, Johnson, Beard

Excite  $\frac{1}{2}$  integer parametric resonance (in Linac or ring)

- Like vertical rigid pendulum or  $\frac{1}{2}$ -integer extraction
- Elliptical phase space motion becomes hyperbolic
- Use  $xx' = \text{const}$  to reduce  $x$ , increase  $x'$
- Use IC to reduce  $x'$

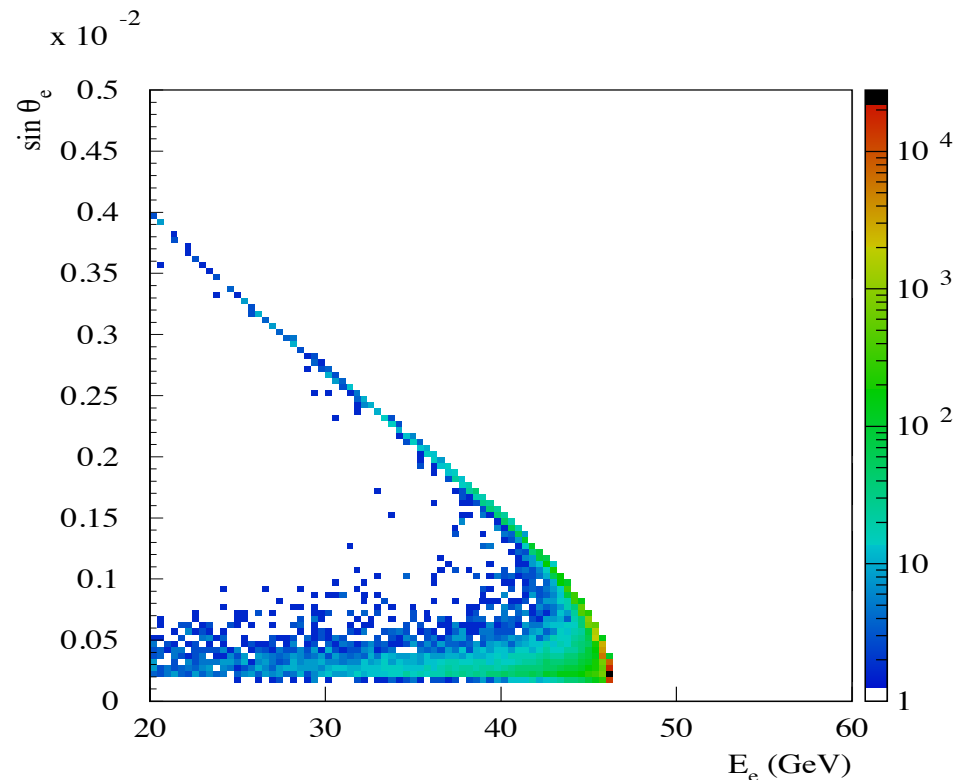
Detuning issues being addressed (chromatic and spherical aberrations, space-charge tune spread). Simulations underway. New progress by Derbenev.



# Processes at $\sqrt{s} \sim 0.212$ GeV $e^+$ on target

$e^+e^- \rightarrow e^+e^- (\gamma\text{'s})$  is the dominant process

- Babayaga for “large” angles and
- BBBrems for collinear (dominant  $\sigma \sim 150$  mb,  $\delta E/E < 2\%$ )



# Positron sources: studies on the market

- Summary of  $e^+$  sources projects (all very aggressive):

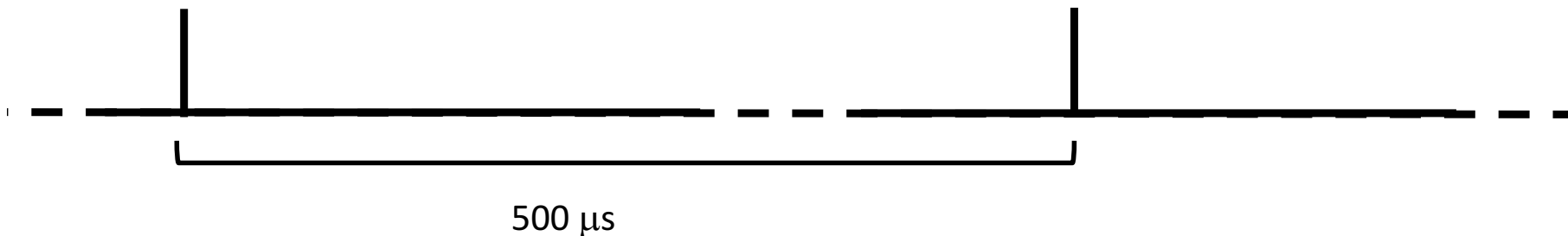
In [F. Zimmermann, et al., 'POSITRON OPTIONS FOR THE LINAC-RING LHeC', WEPPR076 Proceedings of IPAC2012, New Orleans, Louisiana, USA]

	SLC	CLIC	ILC	LHeC pulsed	LHeC ERL
$E$ [GeV]	1.19	2.86	4	140	60
$\gamma\epsilon_x$ [ $\mu\text{m}$ ]	30	0.66	10	100	50
$\gamma\epsilon_y$ [ $\mu\text{m}$ ]	2	0.02	0.04	100	50
$e^+$ [ $10^{14}\text{s}^{-1}$ ]	0.06	1.1	3.9	18	440

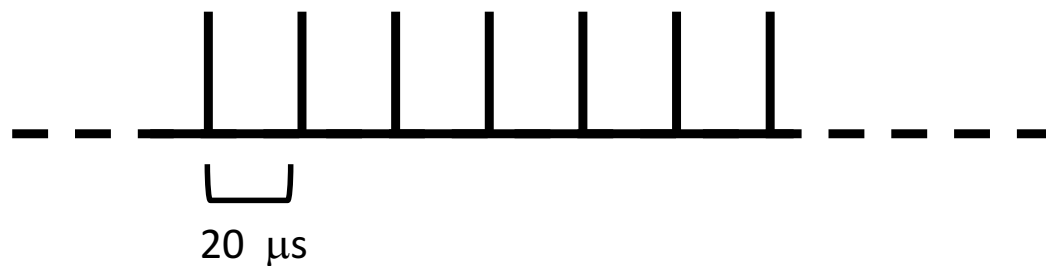
➤ This is the most critical issue

# rebunching at 6 TeV

bunch structure from production



bunch structure at collider



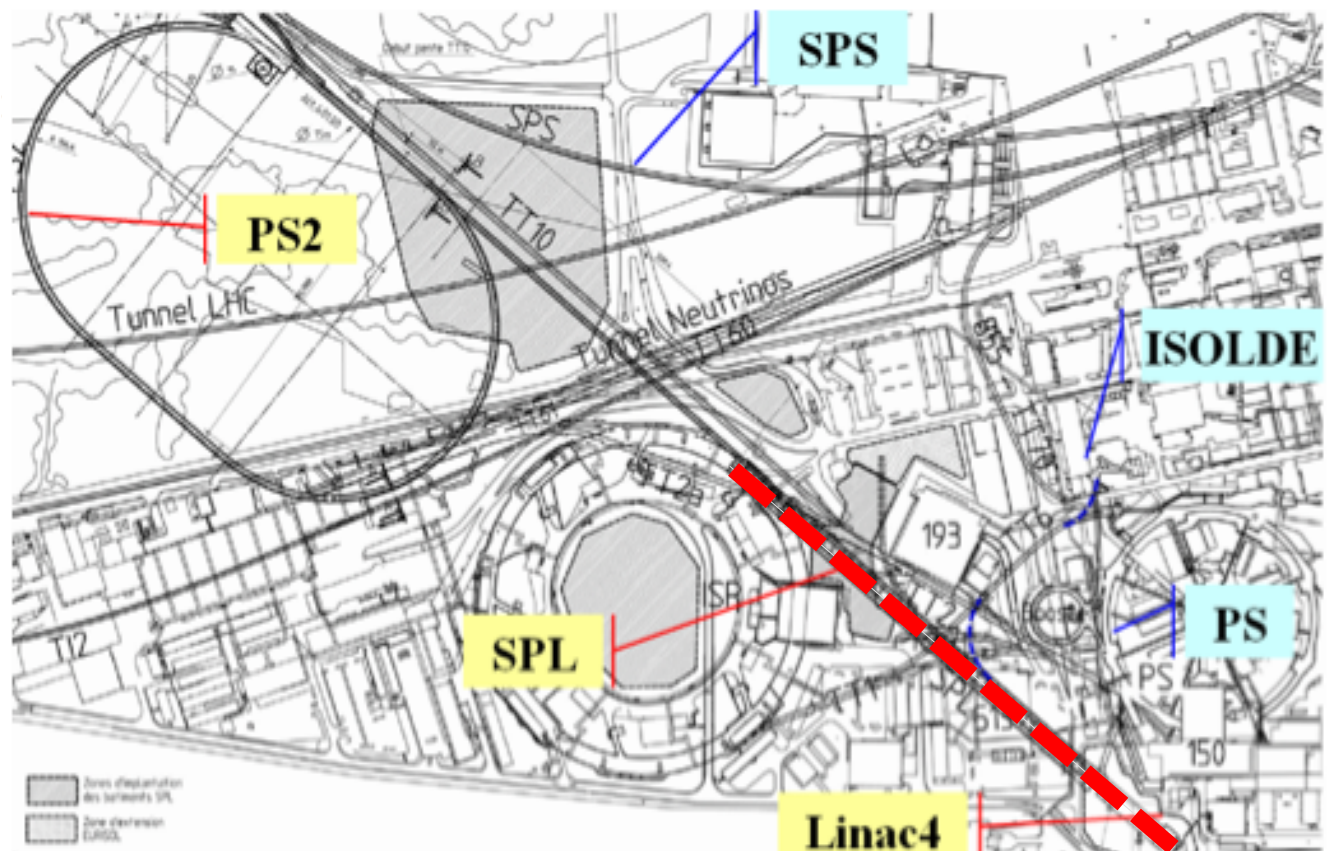
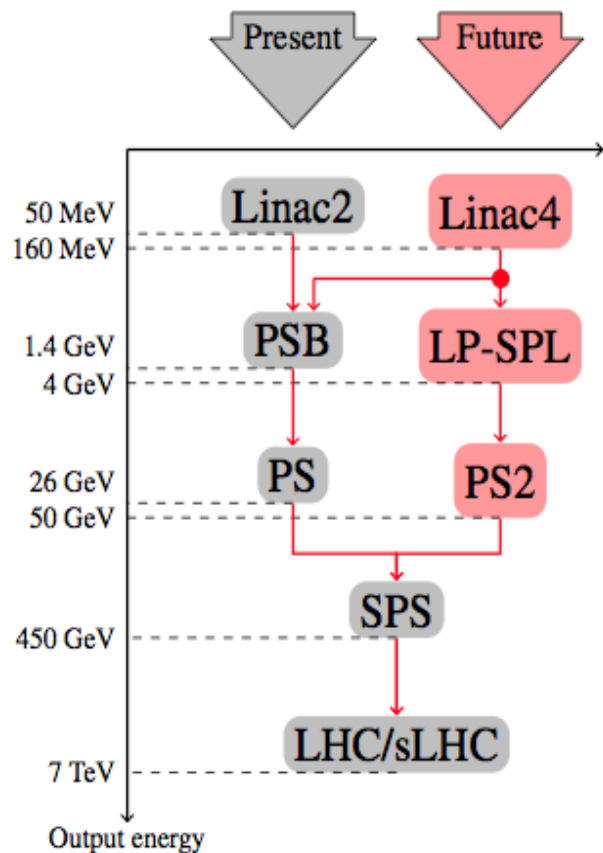
perform continuous injection every 500 μs

rebunch effective for  $\sim 1$  muon lifetime 66 ms (factor 66/0.5)

no damping -> fill transverse phase space maintaining lumi increase

# Future accelerators programs at CERN

- A new LHC injector complex to increase the collider luminosity 10x with the High Luminosity LHC (HL-LHC).
- Two accelerators (the LP-SPL and a new 50 GeV synchrotron, PS2) would replace the three existing ones (Linac2, the PSB, and the PS), with the injection of the SPS at 50 GeV,

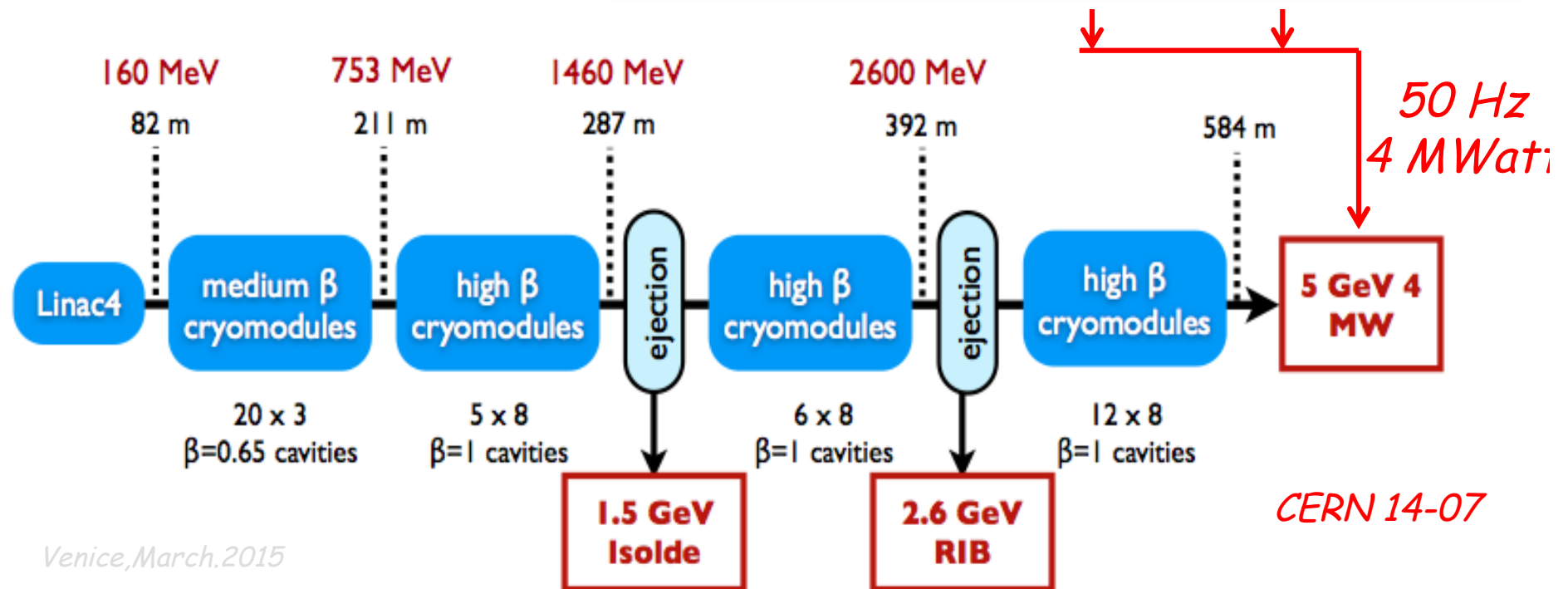




# CERN-SPL parameters

- Layout of superconducting SPL with intermediate extractions.
- SPL design is very flexible and it can be adapted to the needs of many high-power proton beam applications.

Parameter	Units	HP-SPL		LP-SPL
		Low-current	High-current	
Energy	GeV	5	5	4
Beam power	MW	4	4	0.144
Repetition rate	Hz	50	50	2
Average pulse current	mA	20	40	20
Peak pulse current	mA	32	64	32
Source current	mA	40	80	40
Chopping ratio	%	62	62	62
Beam pulse length	ms	0.8	0.4	0.9
Protons per pulse	$10^{14}$	1.0	1.0	1.13



# A muon based Higgs factory at CERN

- A muon cooled Higgs factory can be easily housed within CERN
- The new 5 GeV Linac will provide at 50 c/s a multi MWatt H- beam with enough pions/muons to supply the muon factory.
- The basic additional accelerator structure will be the following:
  - Two additional small storage rings with  $R \approx 50$  m will strip H- to a tight p bunch and compress the LP-SPL beam to a few ns.
  - Muons of both signs are focused in a axially symmetric  $B = 20$  T field, reducing progressively pt with a horn and  $B = 2$  T
  - A buncher and a rotator compresses muons to  $\approx 250$  MeV/c
  - Muon Cooling in 3D compresses emittances by a factor 106.
  - Bunches of about  $2 \times 10^{12}$   $m^\pm$  are accelerated to 62.5 GeV
  - Muons are colliding in a SC storage ring of  $R \approx 60$  m (about one half of the CERN-PS ,1/100 of LHC) where about 104 Higgs events/y are recorded for each of the experiments.

# Staged Neutrino Factory and Muon Colliders

## Increasing complexity parameters challenges



### Neutrino Factory at intensity frontier

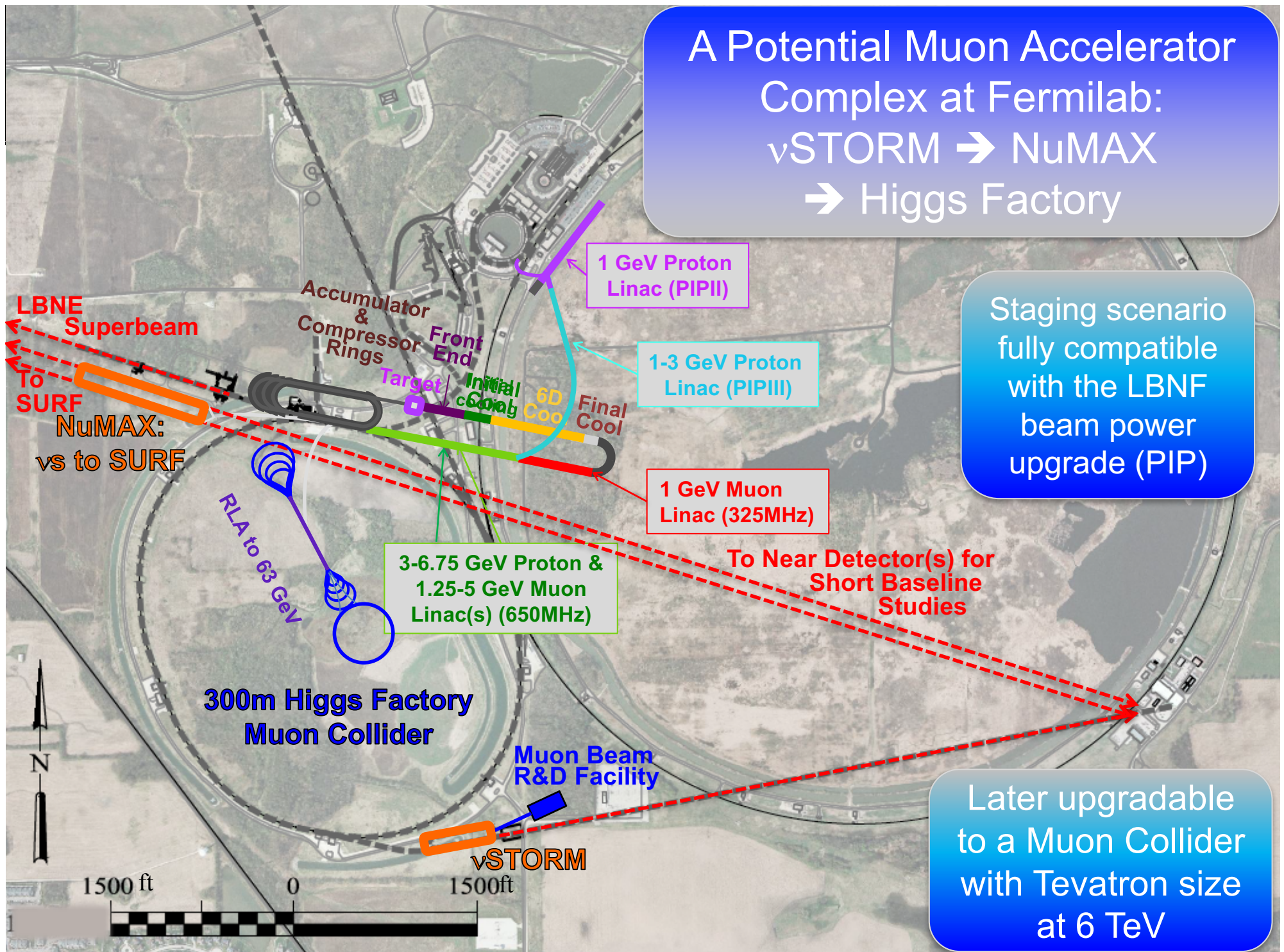
System	Parameters	Unit	nuSTORM	NuMAX Commissioning	NuMAX	NuMAX+
Performance	$\nu_e$ or $\nu_\mu$ to detectors/year	-	$3 \times 10^{17}$	$4.9 \times 10^{19}$	$1.8 \times 10^{20}$	$5.0 \times 10^{20}$
	Stored $\mu^+$ or $\mu^-$ /year	-	$8 \times 10^{17}$	$1.25 \times 10^{20}$	$4.65 \times 10^{20}$	$1.3 \times 10^{21}$
Detector	<b>Far Detector:</b>	Type	SuperBIND	MIND / Mag LAr	MIND / Mag LAr	MIND / Mag LAr
	Distance from Ring	km	1.9	1300	1300	1300
	Mass	kT	1.3	100 / 30	100 / 30	100 / 30
	Magnetic Field	T	2	0.5-2	0.5-2	0.5-2
	<b>Near Detector:</b>	Type	SuperBIND	Suite	Suite	Suite
	Distance from Ring	m	50	100	100	100
	Mass	kT	0.1	1	1	2.7
Neutrino Ring	Magnetic Field	T	Yes	Yes	Yes	Yes
	Ring Momentum	GeV/c	3.8	5	5	5
	Circumference (C)	m	480	737	737	737
	Straight section	m	184	281	281	281
	Number of bunches	-	-	60	60	60
Acceleration	Charge per bunch	$1 \times 10^9$	-	6.9	26	35
	Initial Momentum	GeV/c	-	0.25	0.25	0.25
	Single-pass Linacs	GeV/c	-	1.0, 3.75	1.0, 3.75	1.0, 3.75
		MHz	-	325, 650	325, 650	325, 650
Repetition	Hz	-	30	30	60	
Cooling			No	No	Initial	Initial
	Proton Beam Power	MW	0.2	1	1	2.75
Proton Driver	Proton Beam	GeV	120	6.75	6.75	6.75
	Protons/year	$1 \times 10^{21}$	0.1	9.2	9.2	25.4
	Repetition	Hz	0.75	15	15	15

### Muon Collider at the energy frontier

Parameter	Units	Higgs Factory		Top Threshold Options		Multi-TeV Baselines		Accounts for Site Radiation Mitigation
		Startup Operation	Production Operation	High Resolution	High Luminosity			
CoM Energy	TeV	0.126	0.126	0.35	0.35	1.5	3.0	6.0
Avg. Luminosity	$10^{34} \text{ cm}^{-2} \text{ s}^{-1}$	0.0017	0.008	0.07	0.6	1.25	4.4	12
Beam Energy Spread	%	0.003	0.004	0.01	0.1	0.1	0.1	0.1
Higgs* or Top* Production/ $10^7$ sec		3,500*	13,500*	7,000*	60,000*	37,500*	200,000*	820,000*
Circumference	km	0.3	0.3	0.7	0.7	2.5	4.5	6
No. of IPs		1	1	1	1	2	2	2
Repetition Rate	Hz	30	15	15	15	15	12	6
$\beta^*$	cm	3.3	1.7	1.5	0.5	1 (0.5-2)	0.5 (0.3-3)	0.25
No. muons/bunch	$10^{12}$	2	4	4	3	2	2	2
No. bunches/beam		1	1	1	1	1	1	1
Norm. Trans. Emittance, $\epsilon_{TN}$	$\pi$ mm-rad	0.4	0.2	0.2	0.05	0.025	0.025	0.025
Norm. Long. Emittance, $\epsilon_{LN}$	$\pi$ mm-rad	1	1.5	1.5	10	70	70	70
Bunch Length, $\sigma_z$	cm	5.6	6.3	0.9	0.5	1	0.5	0.2
Proton Driver Power	MW	4	4	4	4	4	4	1.6
<b>Cooling</b>		<b>6D no final</b>			<b>Full 6D</b>			

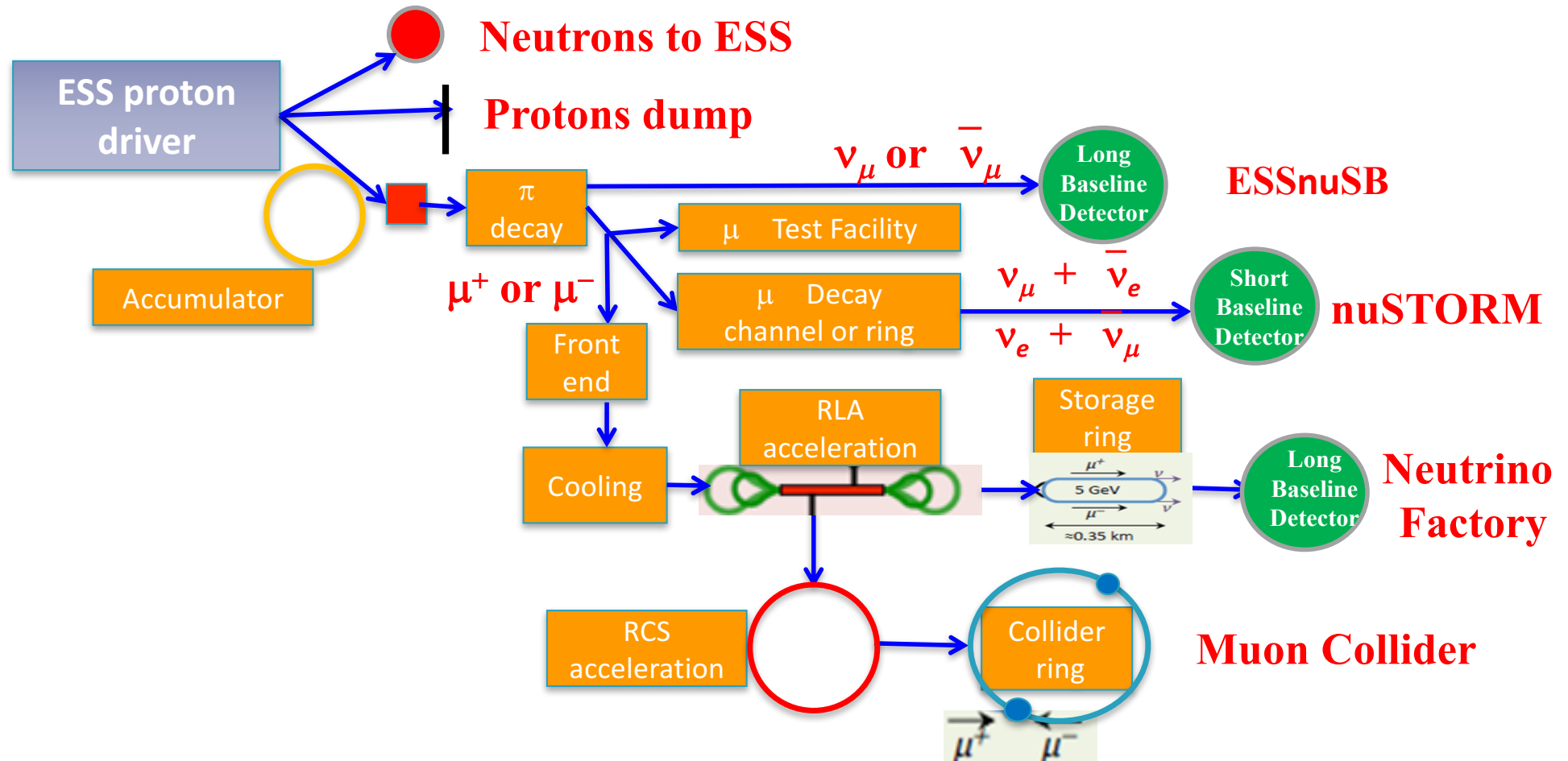
# A Potential Muon Accelerator Complex at Fermilab: $\nu$ STORM $\rightarrow$ NuMAX $\rightarrow$ Higgs Factory

Staging scenario fully compatible with the LBNF beam power upgrade (PIP)



Later upgradable to a Muon Collider with Tevatron size at 6 TeV

# ESS neutrino and muons facility



J.P.Delahaye

ESS\_NuSTORM



# Beam characteristics

Main ESS facility parameters concerning the proton beam.

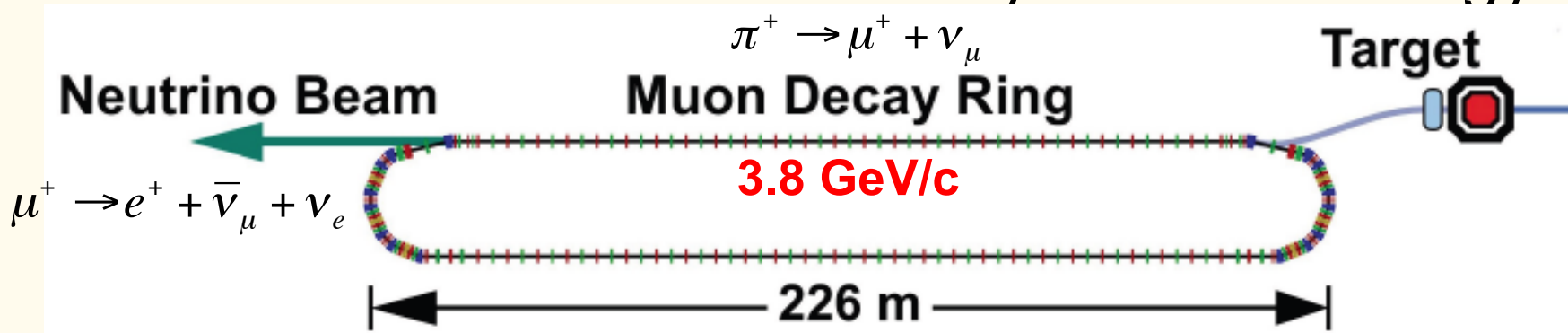
Parameter	Value
Average beam power	5 MW
Proton kinetic energy	2.0 GeV
Average macro-pulse current	62.5 mA
Macro-pulse length	2.86 ms
Pulse repetition rate	14 Hz
Maximum accelerating cavity surface field	45 MV/m
Maximum linac length (excluding contingency and upgrade space)	352.5 m
Annual operating period	5000 h
Reliability	95%

Number of neutrinos per  $\text{m}^2$  crossing a surface placed on-axis at a distance of 100 km from the target station during 200 days for 2.0 GeV protons and positive and negative horn current polarities.

	Positive		Negative	
	$N_\nu (\times 10^{10})/\text{m}^2$	%	$N_\nu (\times 10^{10})/\text{m}^2$	%
$\nu_\mu$	396	97.9	11	1.6
$\bar{\nu}_\mu$	6.6	1.6	206	94.5
$\nu_e$	1.9	0.5	0.04	0.01
$\bar{\nu}_e$	0.02	0.005	1.1	0.5

# nuSTORM: Neutrinos from STORed Muons

- nuSTORM: storage ring for 3.8 GeV/c muons that can be realised **now** without any new technology

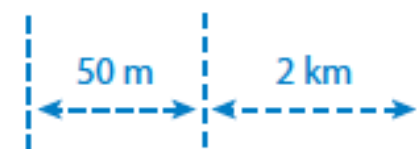
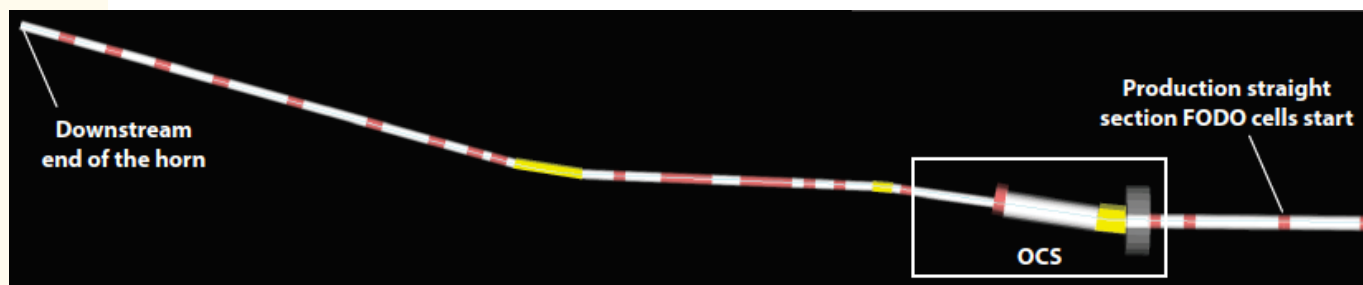
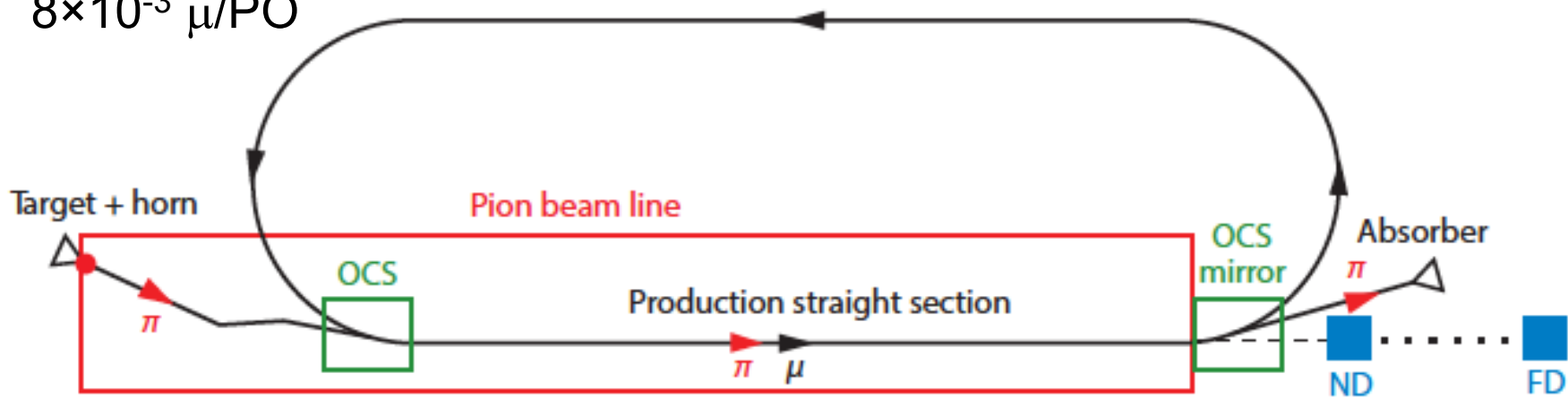


- Pions of 5 GeV/c captured and injected into ring.
- 52% of pions decay to muons before first turn:  $\pi^+ \rightarrow \mu^+ + \nu_\mu$
- This creates a first flash of neutrinos from pion decays
- Ring designed to store muons with  $p = 3.8 \text{ GeV} \pm 10\%$
- Muons decay producing neutrinos:  $\mu^+ \rightarrow e^+ + \bar{\nu}_\mu + \nu_e$
- Creates hybrid beam of neutrinos from pion & muon decay

# nuSTORM Facility

## □ nuSTORM facility:

- 120 GeV protons on carbon or inconel target (100 kW)
- NuMI-style horn for pion collection
- Injection pions ( $5 \text{ GeV}/c \pm 10\%$ ) into storage ring:  $0.09 \pi/\text{POT}$
- Storage ring: large aperture FODO lattice ( $3.8 \text{ GeV}/c \pm 10\%$ ) muons:  $8 \times 10^{-3} \mu/\text{PO}$





# nuSTORM at Fermilab

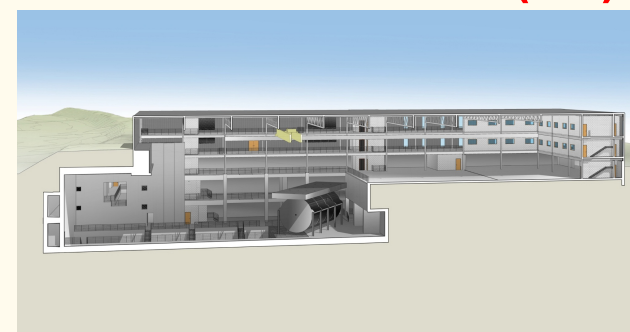
- nuSTORM could be sited at Fermilab  
**Proposal to FNAL PAC: arXiv: 1308.6822**



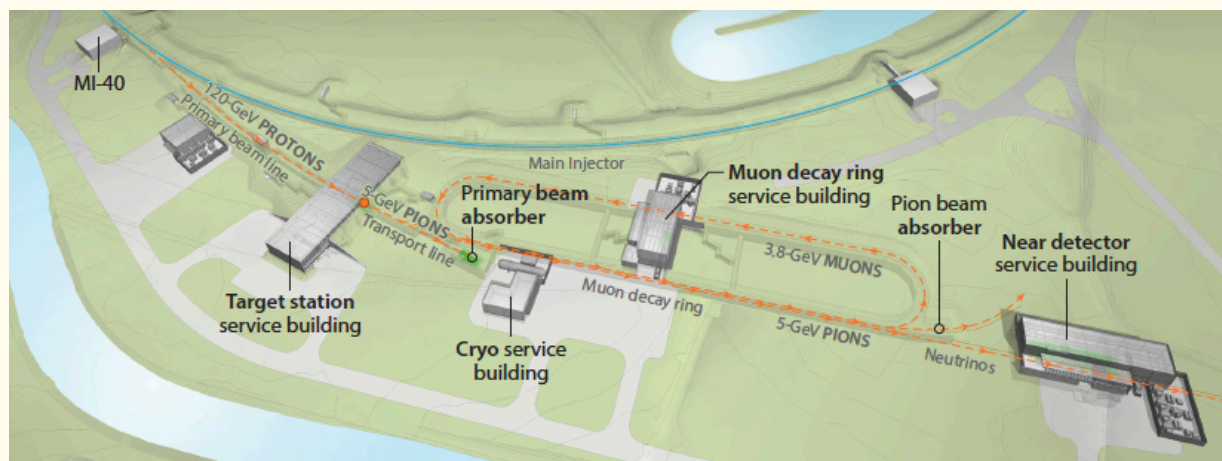
## Near Detector Hall



## Far Detector Hall (D0)



**Target building**



# nuSTORM at CERN

- ❑ nuSTORM could be sited at CERN
  - ❑ Target station in North Area
- EoI to CERN: [arXiv:1305.1419](https://arxiv.org/abs/1305.1419)**

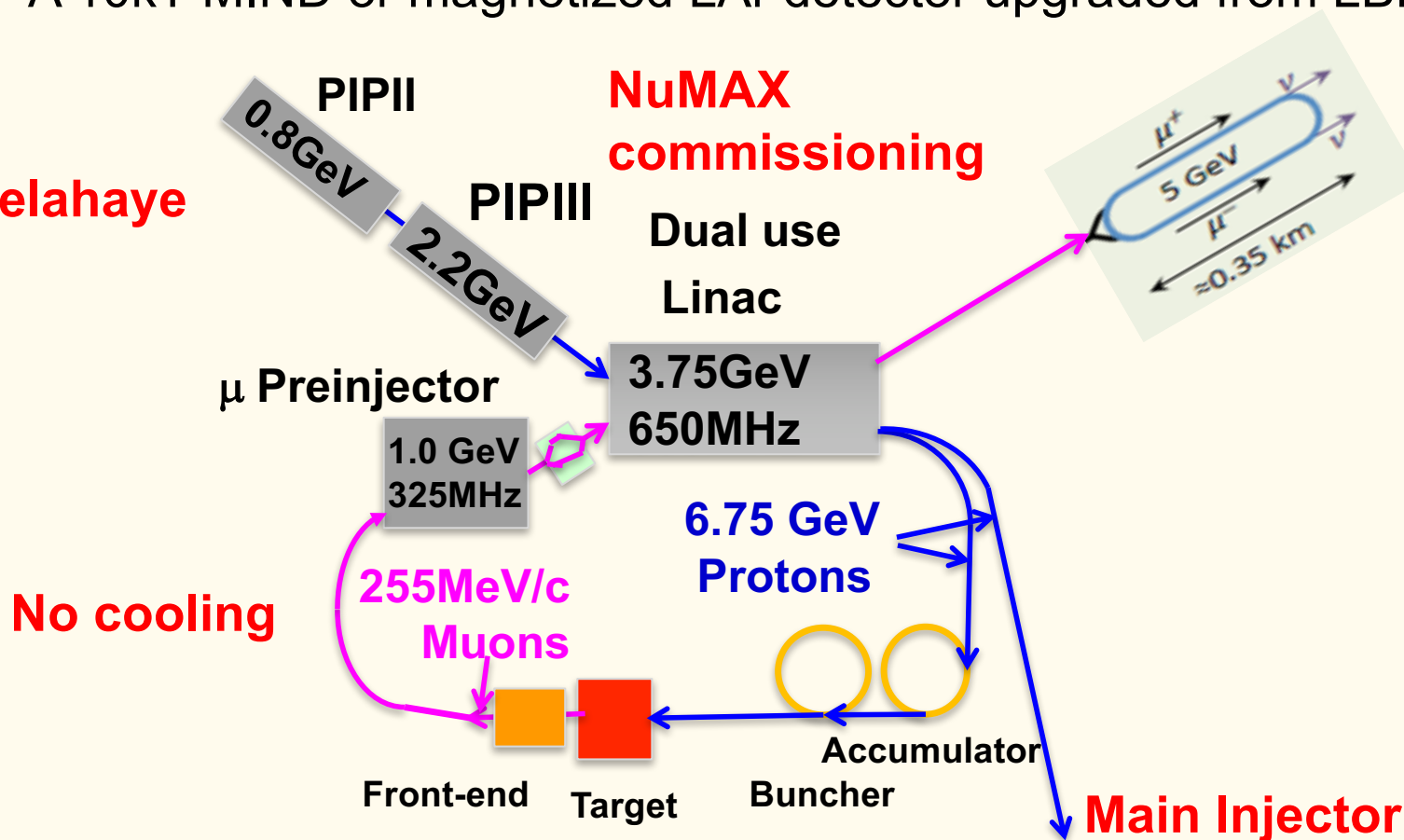


- ❑ For two detector oscillation search: near detector in North Area and far detector in Point 1.8

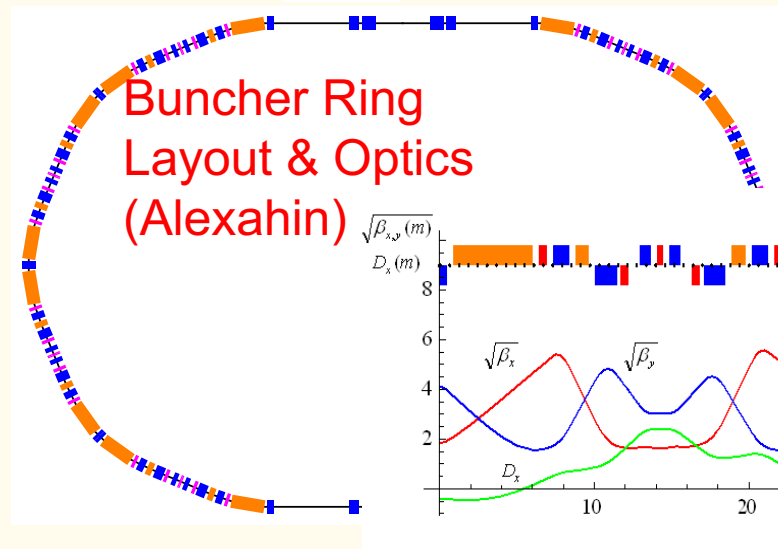
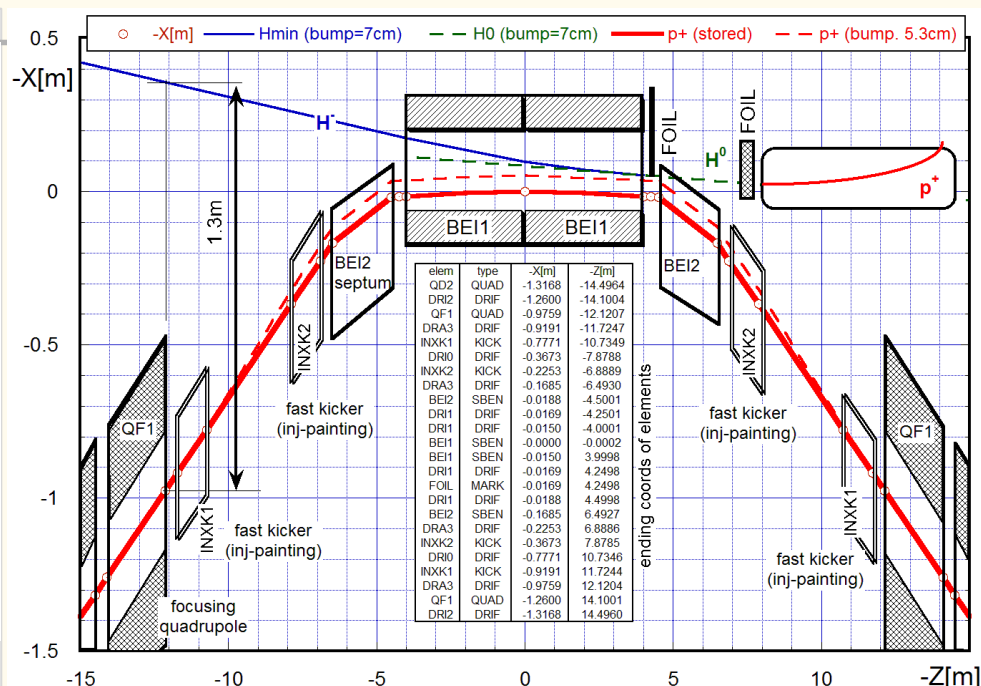
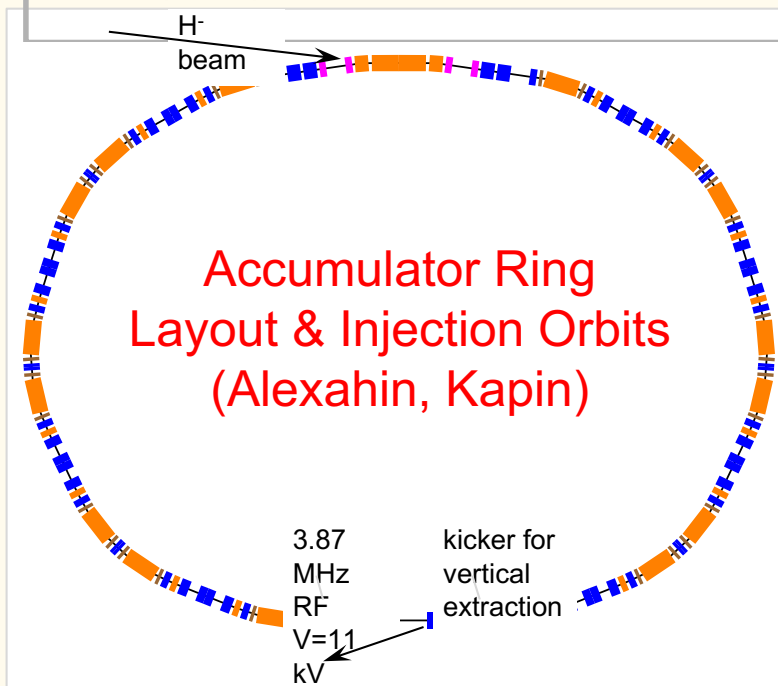
# NuMAX: Neutrino Factory FNAL/Sanford

- ❑ Neutrinos from a Muon Accelerator Complex (NuMAX)
  - Neutrino Factory with  $10^{20}$  straight muons decays/year @ 5 GeV
  - Muon ring at 5 GeV pointing neutrino beam towards Sanford
  - A 10kT MIND or magnetized LAr detector upgraded from LBNE

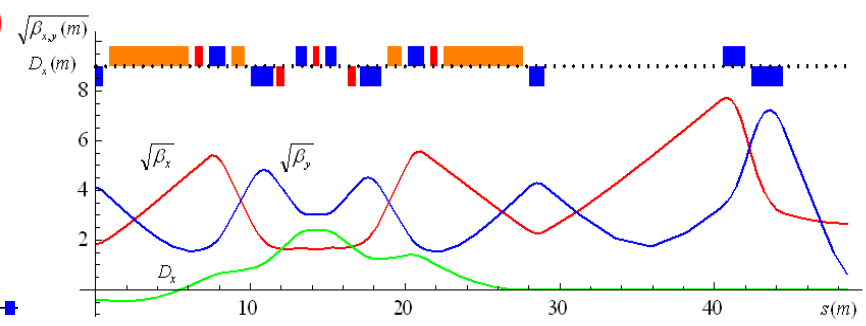
J.P. Delahaye



# Proton Driver



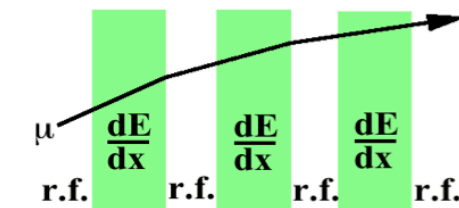
Optics:  
 $\frac{1}{2}$  staight +  
 1 arc cell



- ✓ Based on 6-8 GeV Linac Source
- ✓ Accumulator & Buncher Ring Designs in hand
- ✓ H- stripping requirements same as those established for Fermilab's Project X

# Muon Ionization Cooling

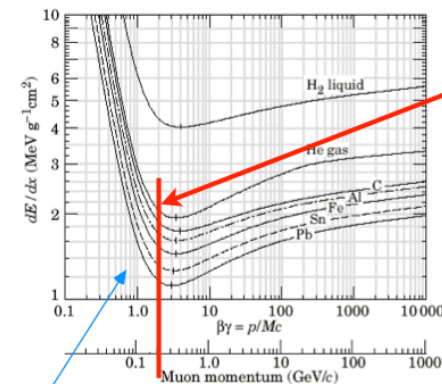
- Muons cool via  $dE/dx$  in low-Z medium



– Absorbers: 
$$\begin{cases} E \rightarrow E - \left\langle \frac{dE}{dx} \right\rangle \Delta s \\ \theta \rightarrow \theta + \theta_{space}^{rms} \end{cases}$$

- RF cavities between absorbers replace  $\Delta E$
- Net effect: reduction in  $p_{\perp}$  at constant  $p_{\parallel}$ , i.e., transverse cooling

$$\frac{d\epsilon_N}{ds} \approx -\frac{1}{\beta^2} \left\langle \frac{dE_{\mu}}{ds} \right\rangle \frac{\epsilon_N}{E_{\mu}} + \frac{\beta_{\perp} (0.014 \text{ GeV})^2}{2\beta^3 E_{\mu} m_{\mu} X_0} \quad (\text{emittance change per unit length})$$



- ionization minimum is  $\approx$  optimal working point:
  - ▶ longitudinal +ive feedback at lower  $p$
  - ▶ straggling & expense of reacceleration at higher  $p$

- 2 competing effects  $\Rightarrow$   $\exists$  equilibrium emittance

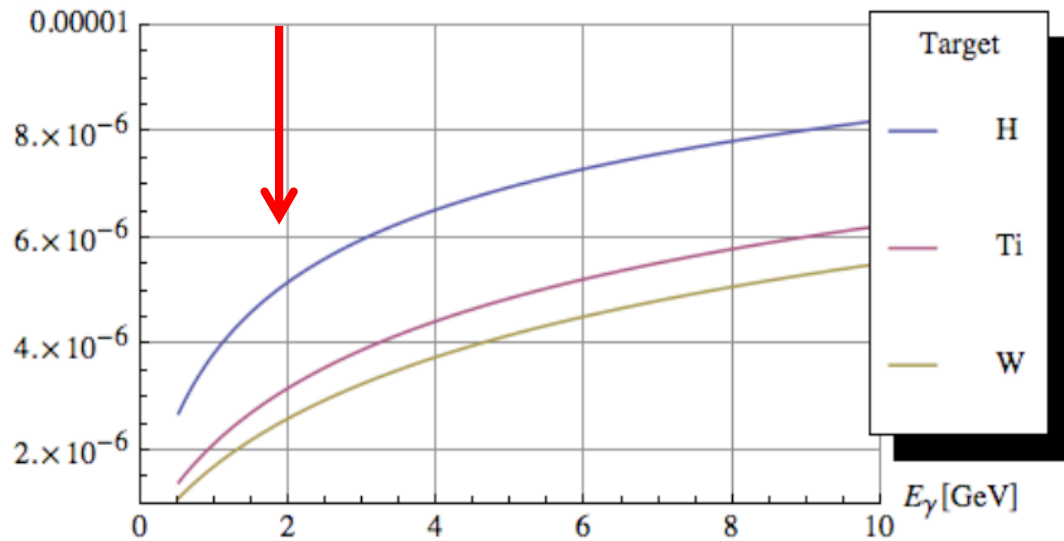
Kaplan

# Muon generation by GeV-scale Compton $\gamma$ s

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(SLAC)

Probability of creating  $\mu^+\mu^-$  pairs as a function of the incident photon energy

$$\frac{\sigma_{tot\mu}}{\sigma_{tot e}} \approx \frac{1}{4} \frac{m_e^2}{m_\mu^2} \text{ or } 0.5 \cdot 10^{-5}$$



26GeV $\gamma$ beam	Pulsed Linac	ERL
e-beam energy [GeV]	36	11
Laser wavelength [ $\mu\text{m}$ ]	10	1
Bunch charge [nC]	10	1.5
Rep. rate [kHz]	0.2	20 / 200
Bunches per beam	250	
Average current [mA]	2	30 / 300
e-beam power [MW]	18	330 / 3300
e-to- $\gamma$ convers. efficiency	3	0.33
$\gamma$ -beam power [MW]	3	20 / 200
Total AC-to- $\gamma$ efficiency	10%	20% / 75%
Peak $\mu^+\mu^-$ [per bunch]	$10^6$	$3 \cdot 10^4$
Average $\mu^+\mu^-$ [per second]	$5 \cdot 10^{10}$	$3 \cdot 10^{11} / 3 \cdot 10^{12}$

- Brightness  $10^3$  larger than with proton driver
- $10^3$  too low with pulsed linac
- $10^2$  flux increase with high current ERL
- Approaching intensities desired for NF (but train structure not favorable for collider luminosity,  $N^2$  issue)