



University of Bologna & INFN

# Kalman Filter

## 4 FOOT

### first results

**Matteo Franchini**

# Intro

- Use Kalman Filter method to combine hits from different detectors into a precise track reconstruction (momentum!).
- Goal: momentum resolution  $< 4\%$ !
- To be used as a test of the configuration of FOOT (geo + performance).
- Main problem: harmonise multiple sub-detector inputs.

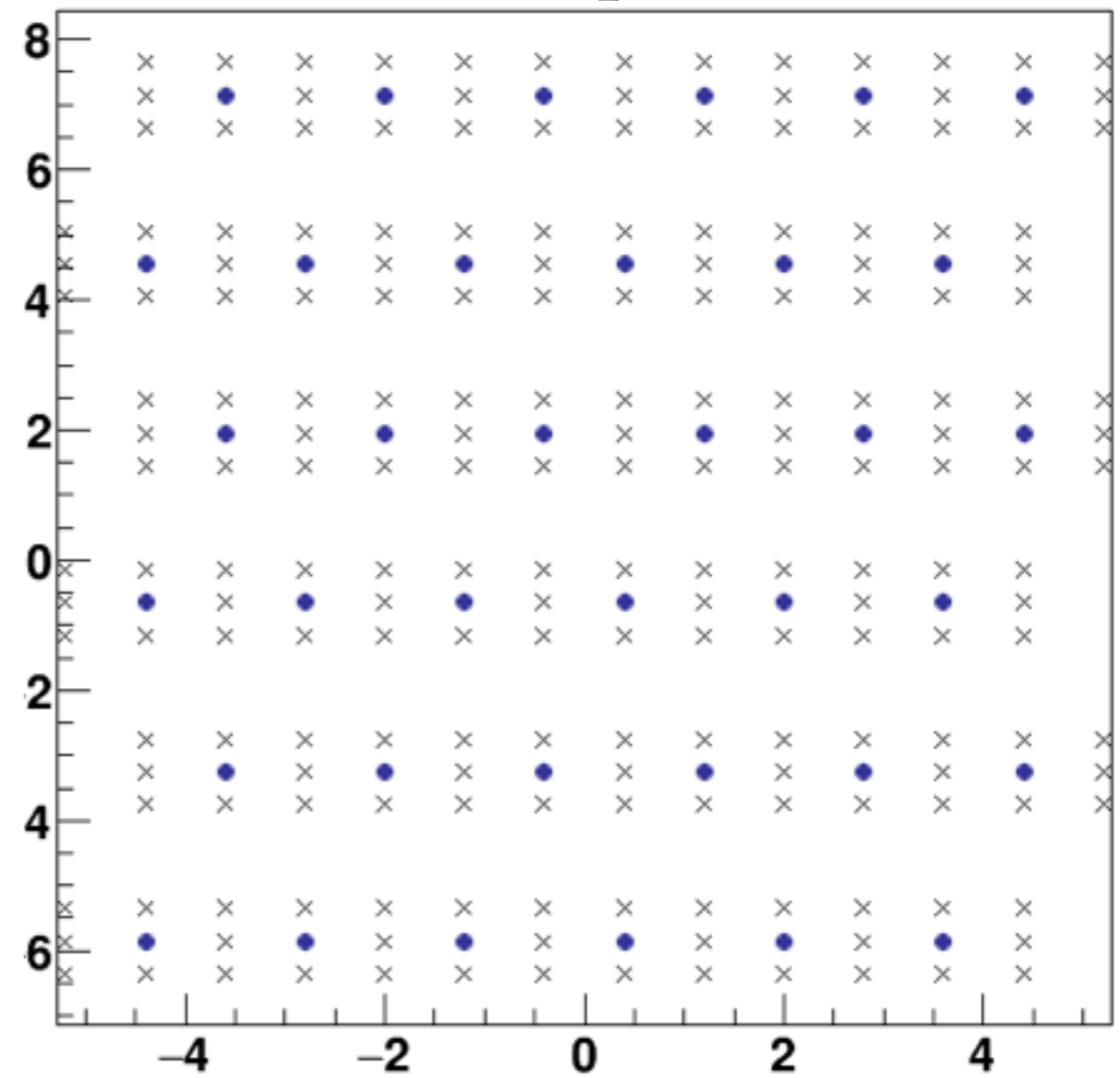
# Technical step until now

- Using the Reconstruction framework, including GenFit (thank Alessio).
- Starting from Drift Chamber package:
  - ✱ geometry implementation from the one in FLUKA's input files.
  - ✱ mirroring Beam Monitor (thanks Yun).
  - ✱ code restyling (FIRST->FOOT, improve in/out, stability, class for wires, ...)
  - ✱ reading event info from ntuple: tests+fixes, add truth matching to hits, fix local/global coordinates transformations(managed by sub detector itself by now).
- C++ class to interface with GenFit and make the Kalman (core code!) + store tracks.
  - ✱ takes hits from different sub-detectors, transmutes in GenFit-like inputs and interpret the fit results.
  - ✱ Use global material and geometry (from each sub-detector) [to be finalised]
- Implementation of the Magnetic Field [last minute!].

# DC view

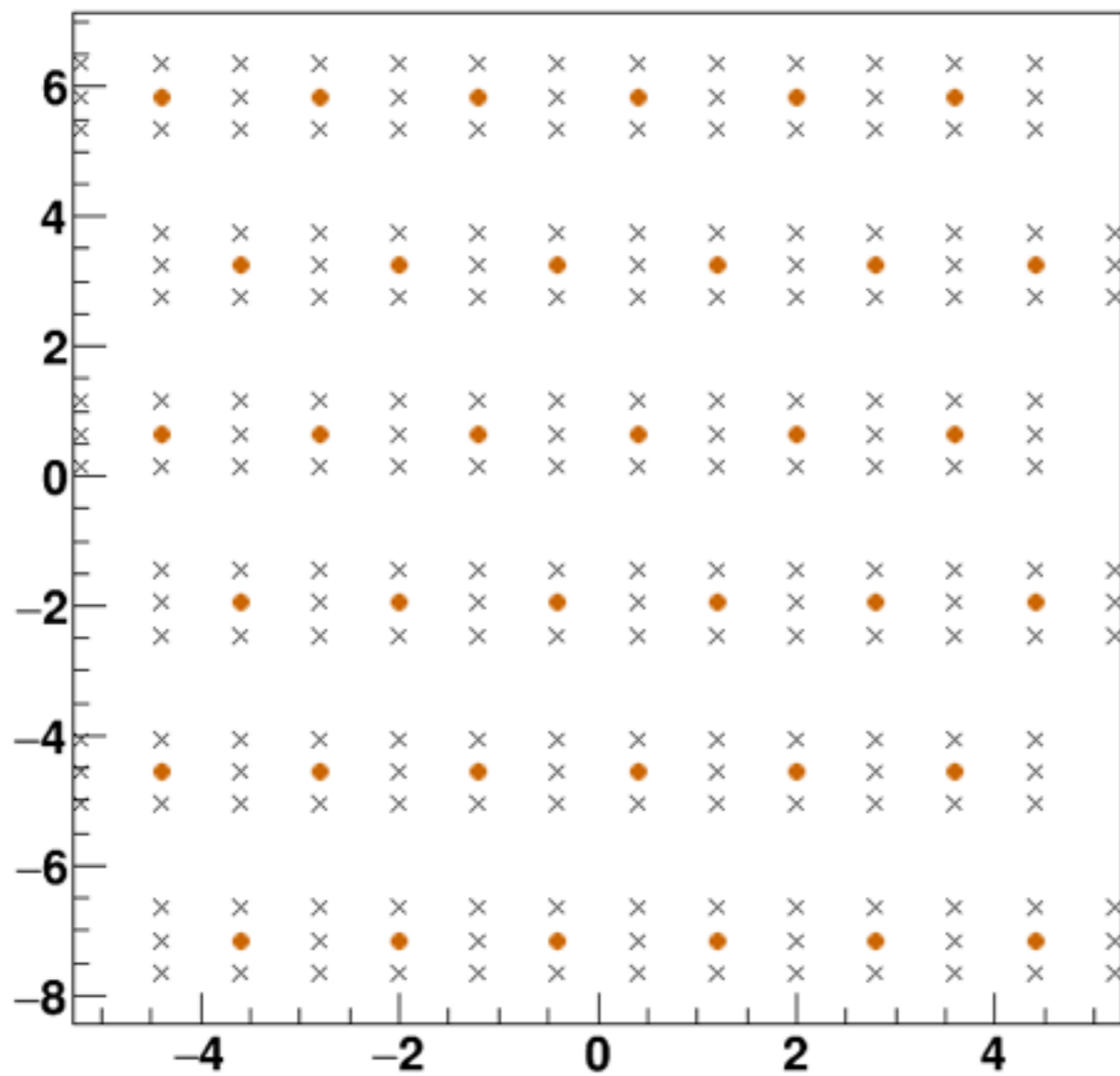
Graph

top



Graph

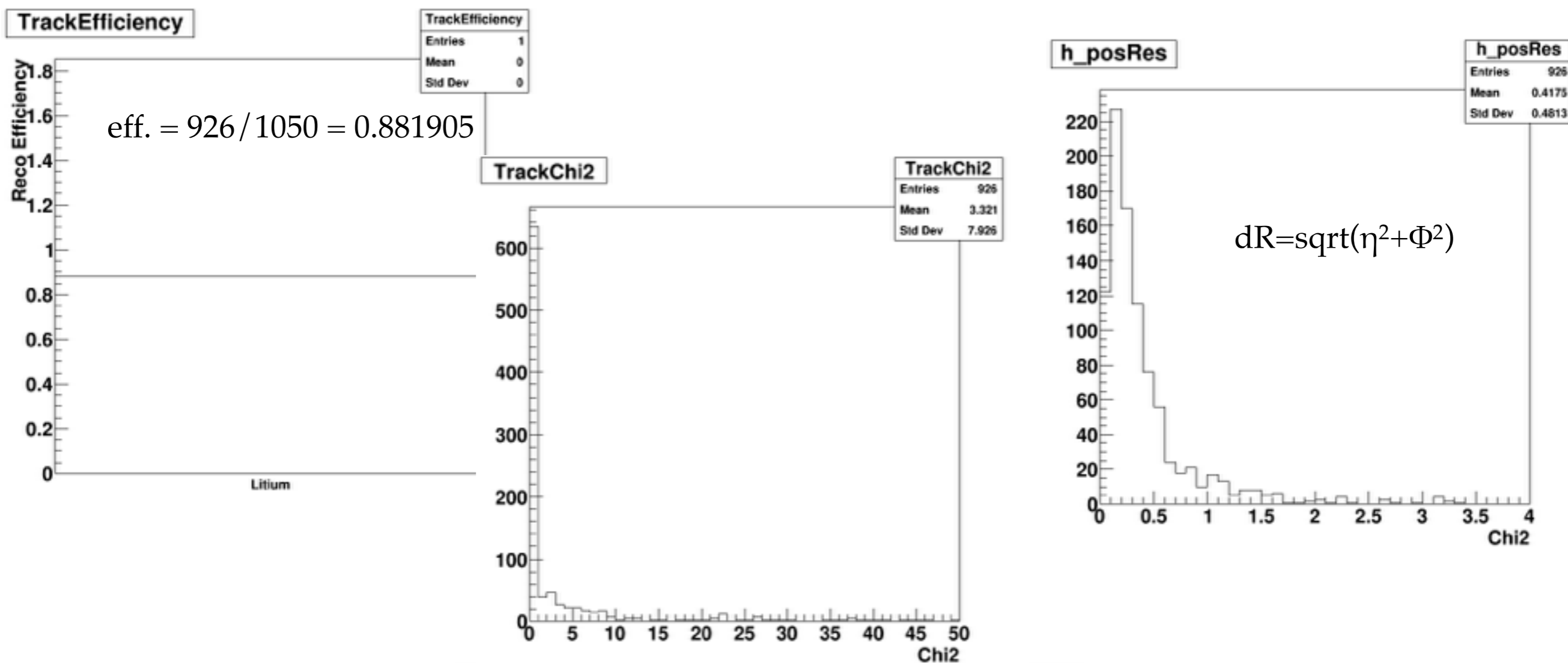
side



# Preliminary results 1

## B field OFF

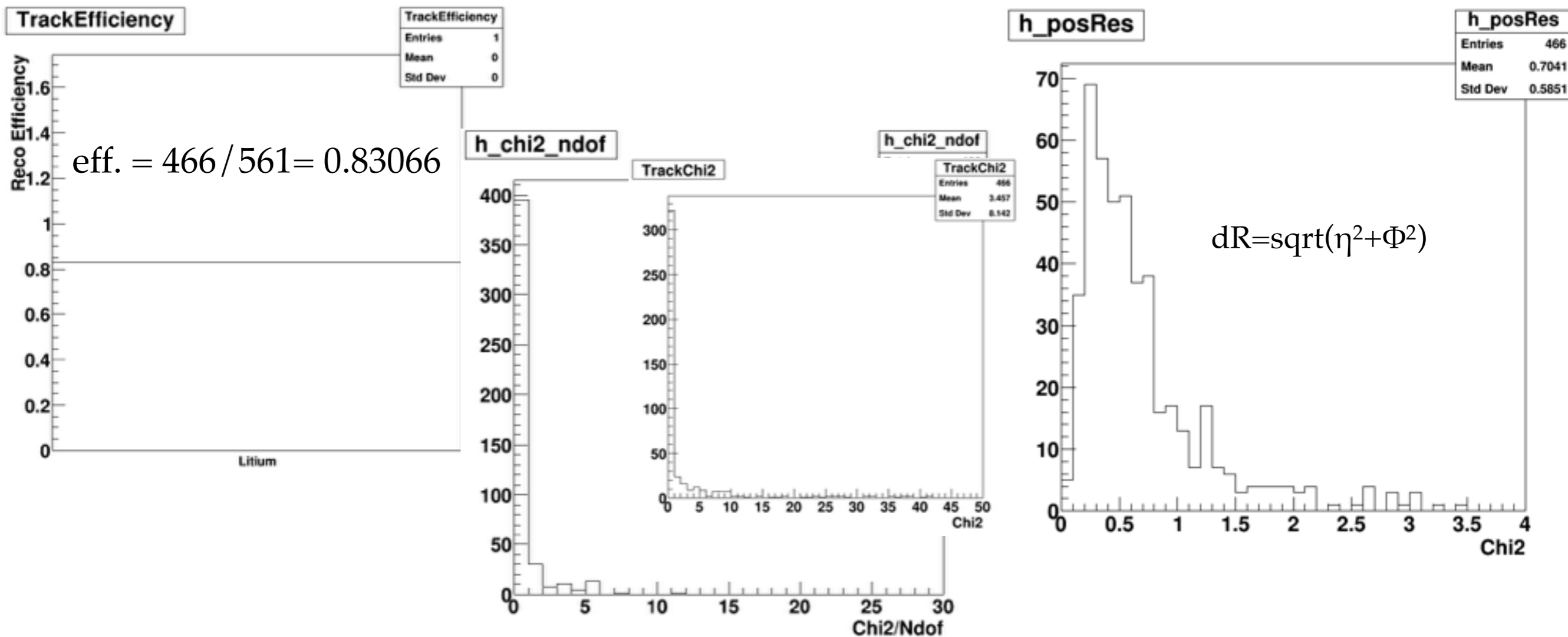
- ◆ **Input file:**  
12C\_C2H4\_noMag\_highThres.root;
- ◆ **Lithium hits ONLY;**
- ◆ **Drift Chamber ONLY;**
- ◆ **no-DC materials still missing (air bubble).**
- ◆ **Seed: (0,0,30)cm, pz=2.4GeV, proton.**
- ◆ **tot nEvents: 17511**



# Preliminary results 2

## B field ON

- ◆ **Input file:**  
12C\_C2H4\_Mag\_highThres.root;
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- ◆ **Drift Chamber ONLY;**
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- ◆ **Seed: (0,0,30)cm, pz=2.4GeV, proton.**
- ◆ **tot nEvents: 9715**



# Next Steps

- **CHECKS!!!** and tuning of the fitter (seed, mass, measurement handling, ...)
- Add pixel detector, Vertex + Internal Tracker. [ongoing]
- Implement all the material, at least between target and DC. [ongoing]
- Hit selection strategy before the KF. [dreamworld stage]
- Testing different Foot configurations:
  - ✱ vacuum “inside” magnets;
  - ✱ no Internal Tracker;

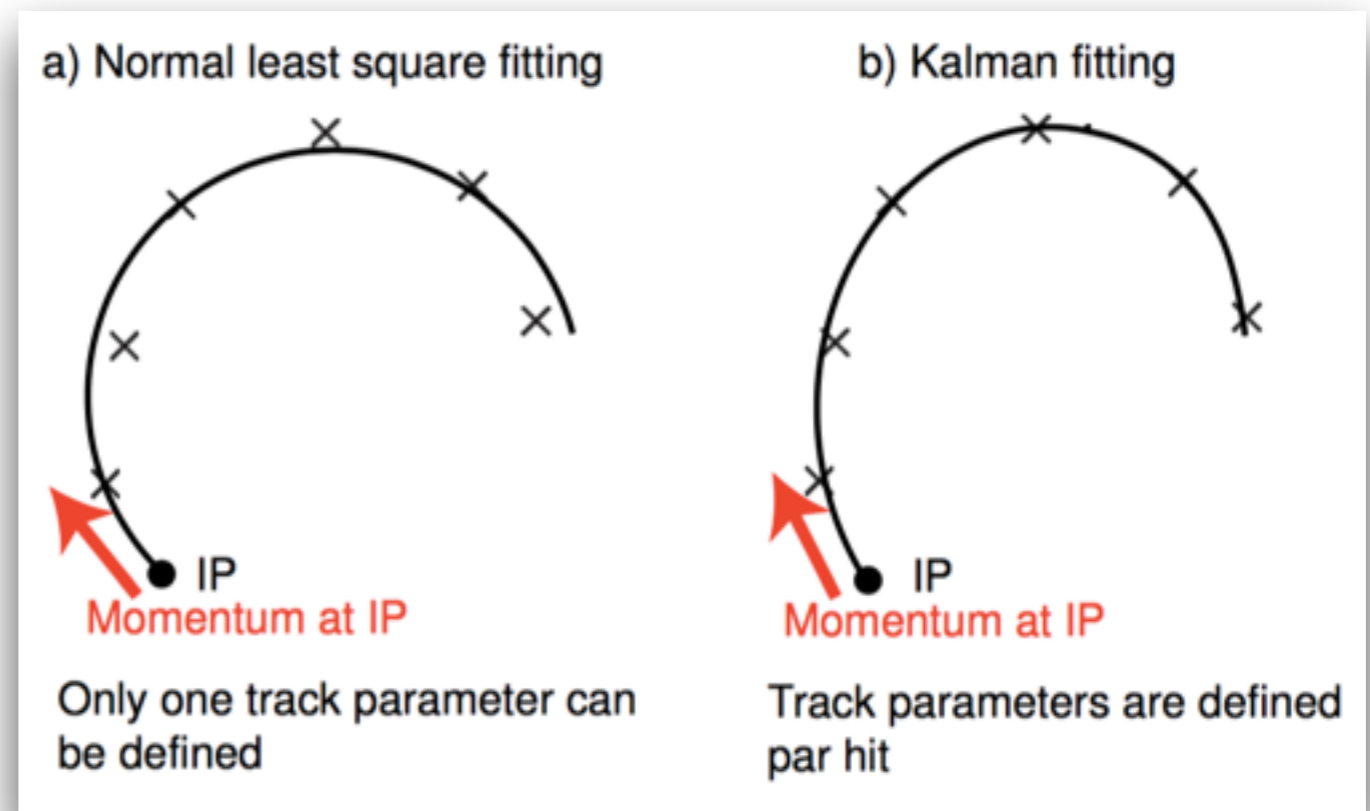
Back-up



# Kalman Filter

- R.E.Kalman proposed an iterative method to estimate the states of a dynamic system starting from a series of measurement points on N surfaces.
- Initially used to calculate the trajectory of ballistic missiles. Later introduced in particle physics (1984).

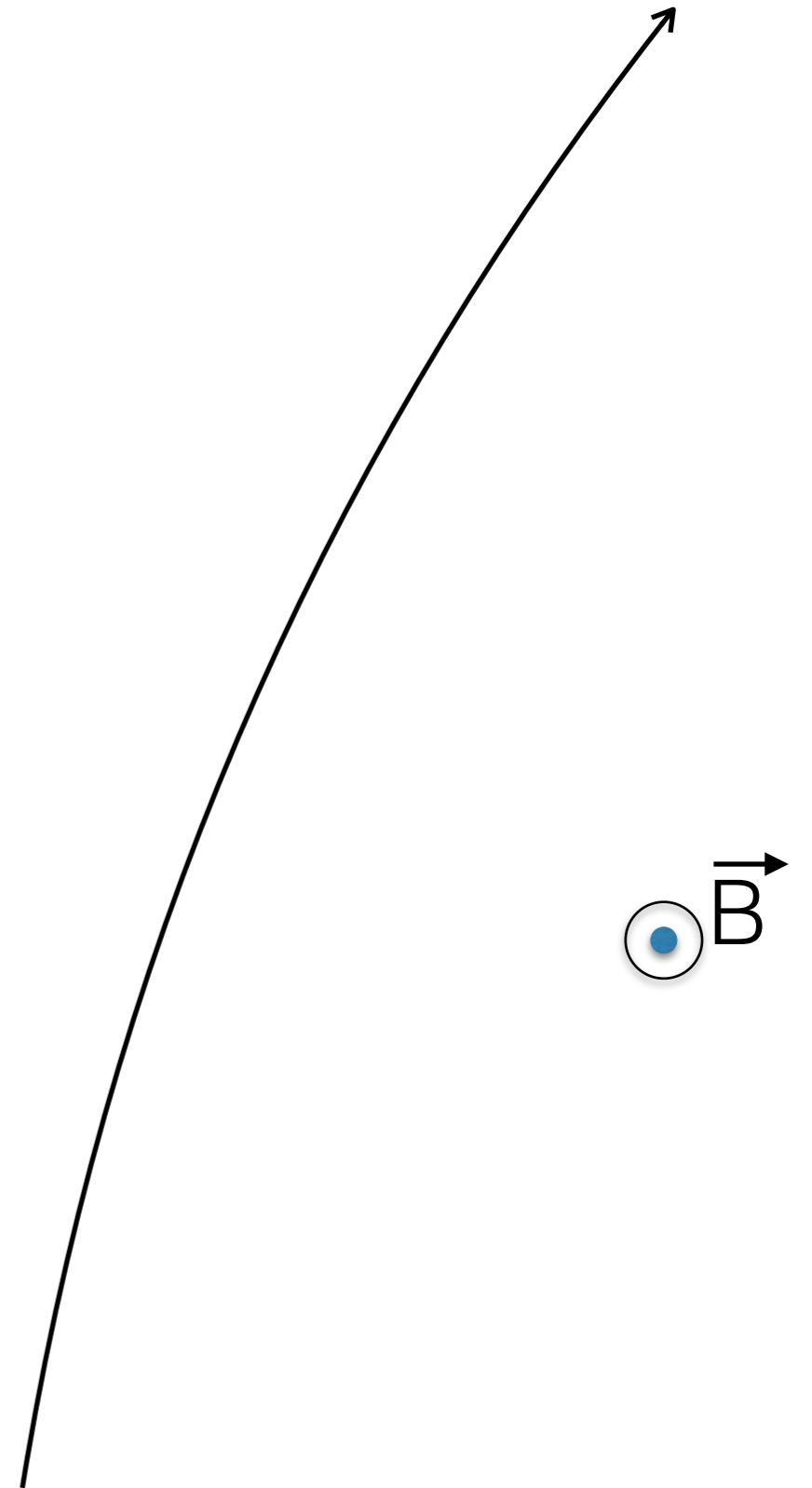
- Precise as a global  $\chi^2$  fitting;
- **Fast**;
- Best **track parameter** found **for each hit!!!**



# Kalman in pills

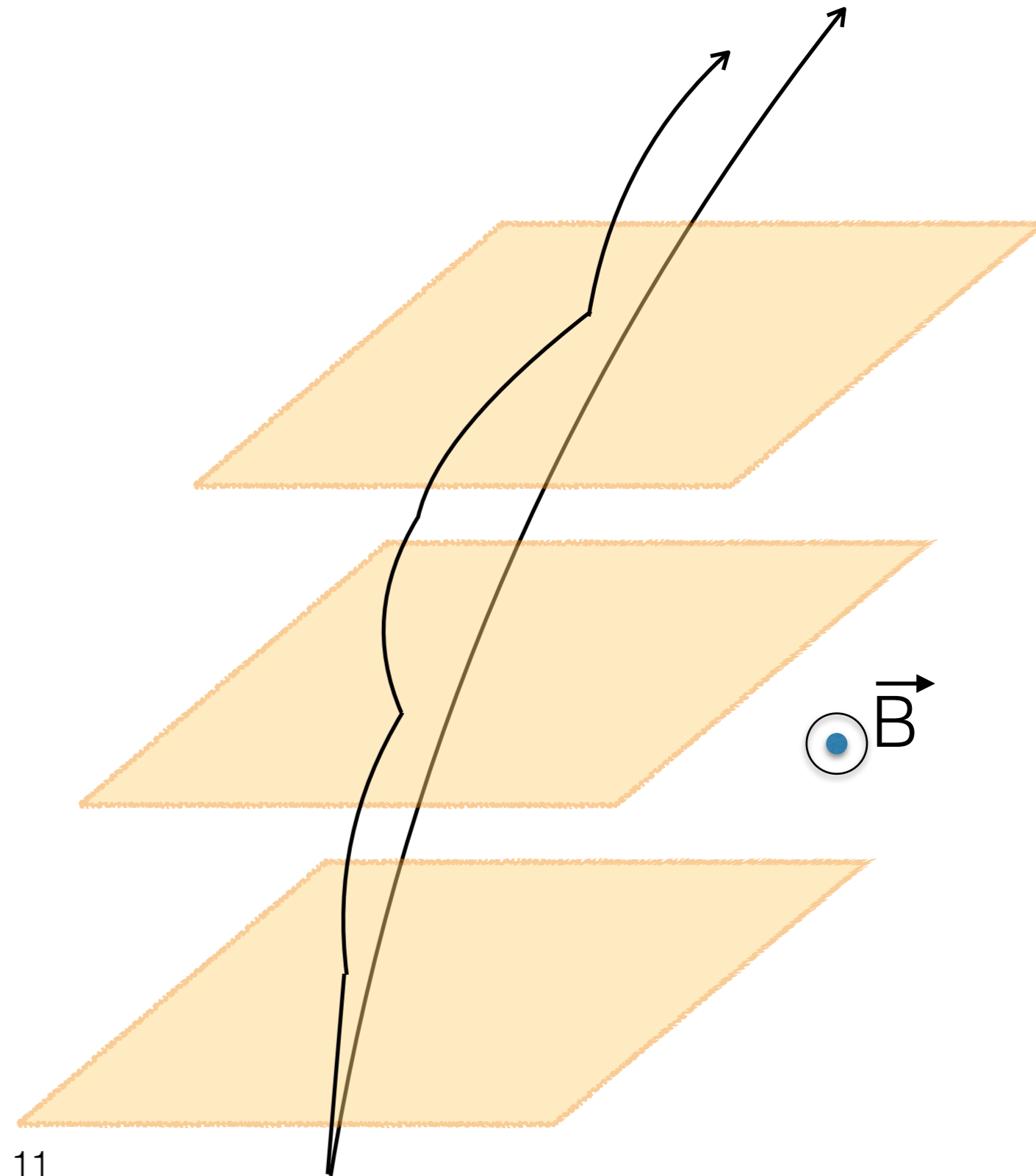
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2. We'll see some measurement hits on the detector layers (considering finite detector uncertainty).
3. Propagate the first hit to the next layer. Propagator Matrix  $F$ .
4. Find the best compromise between the propagated point and the closest hit on the 2<sup>nd</sup> layer. Use a Chi2 and a Projection Matrix  $H$ .
5. Iterate 3 and 4 for the next layers.



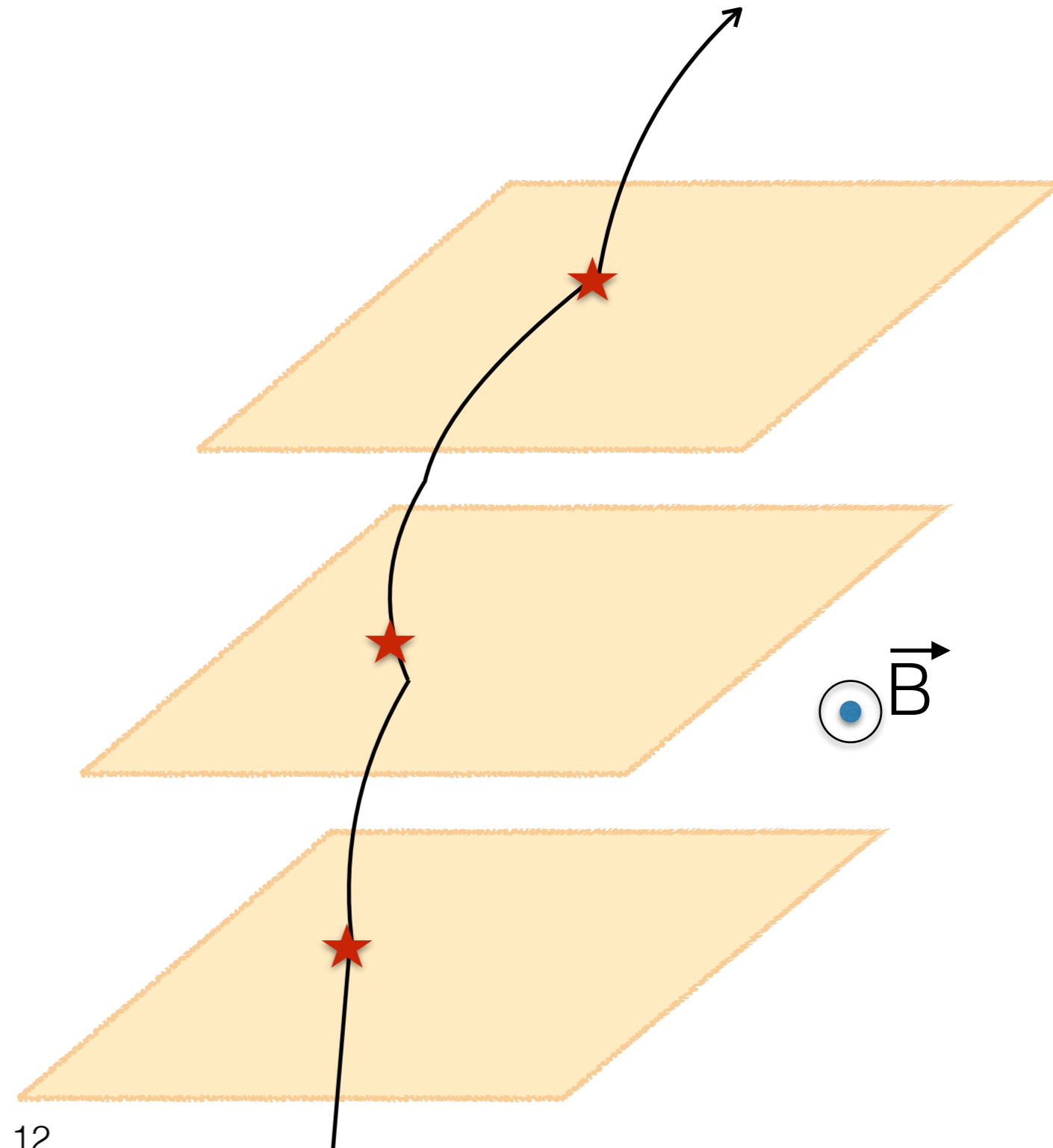
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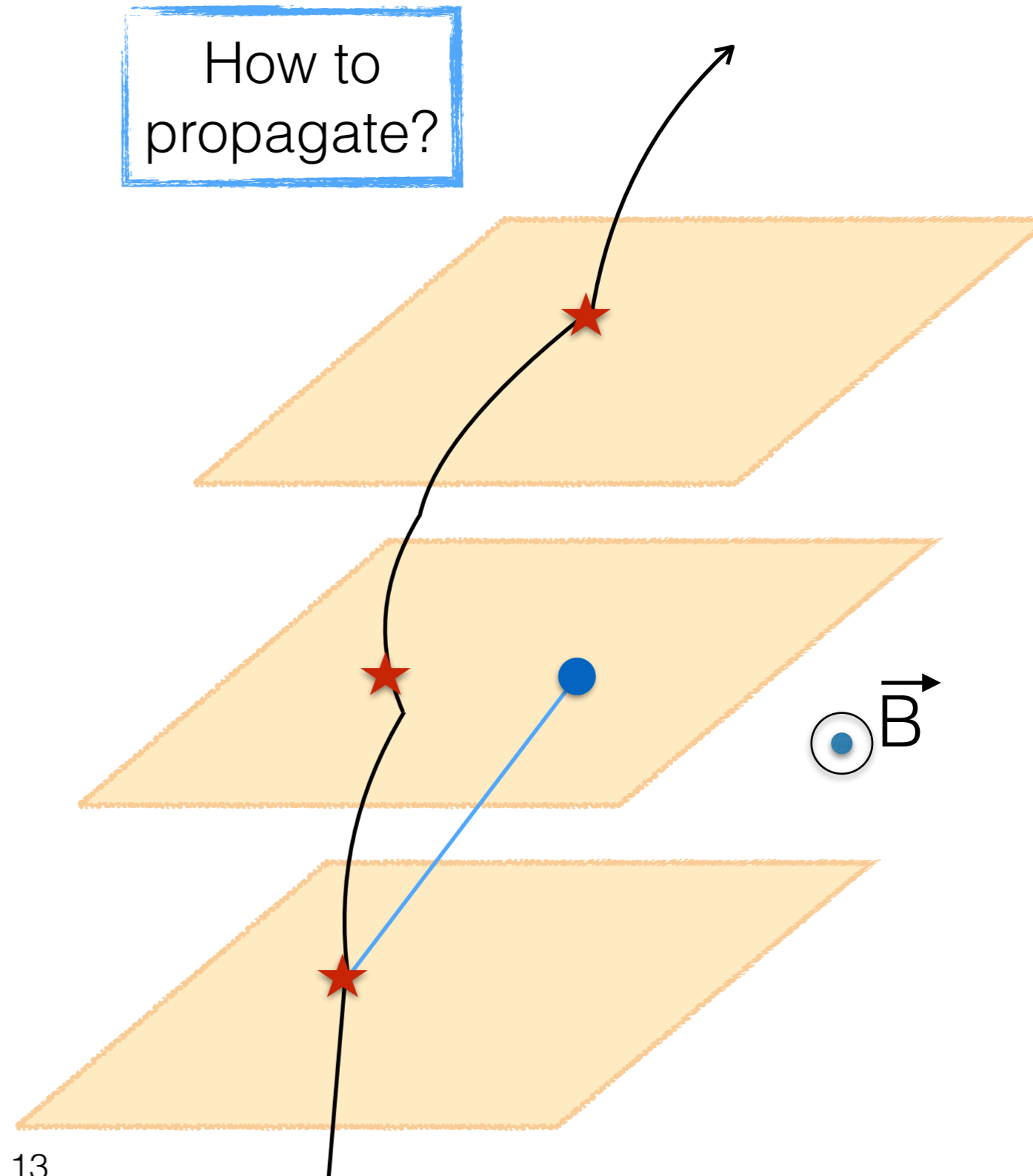
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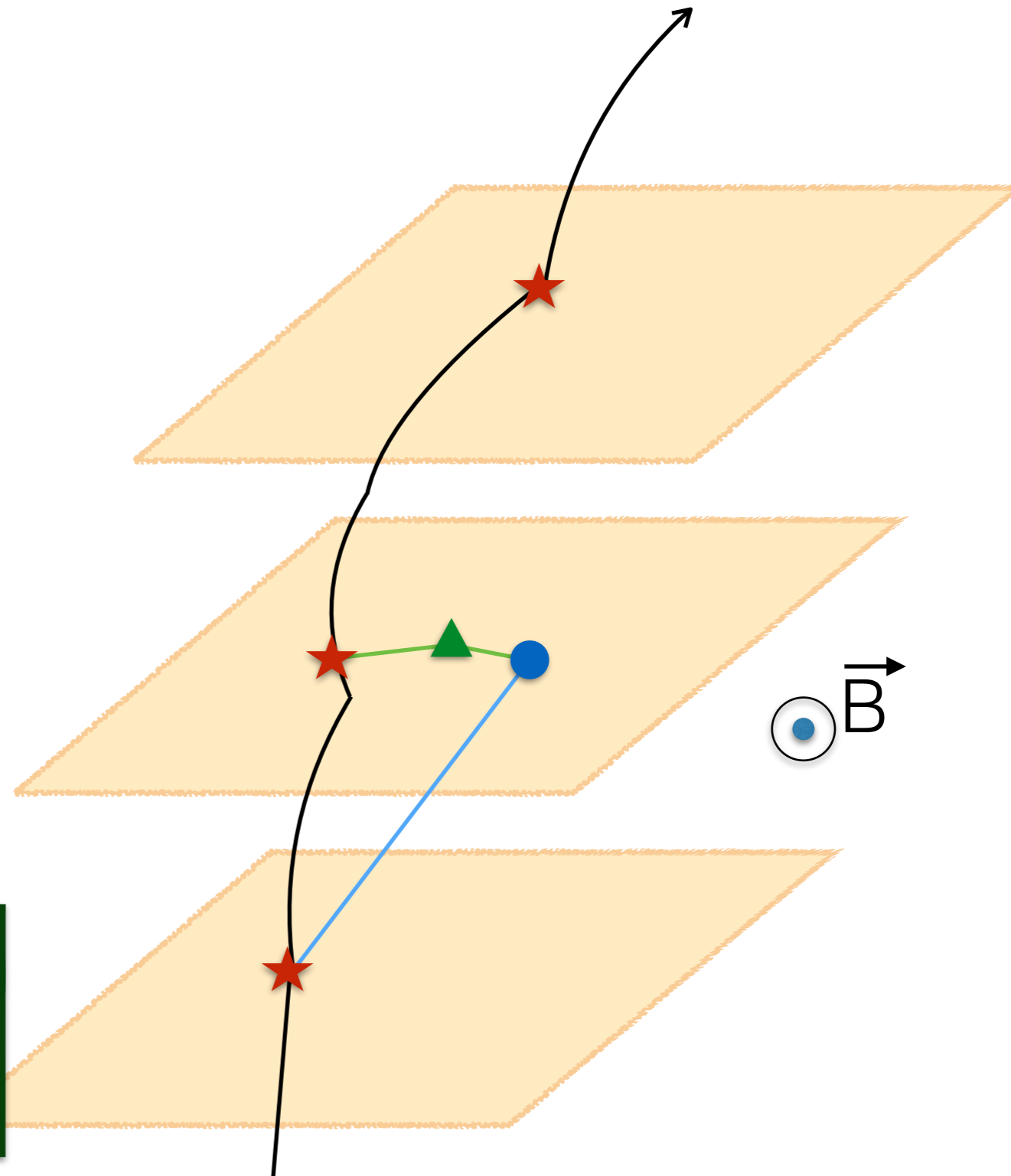
How to propagate?



$$\textcircled{2} = \mathbf{F} \times \text{★}1$$

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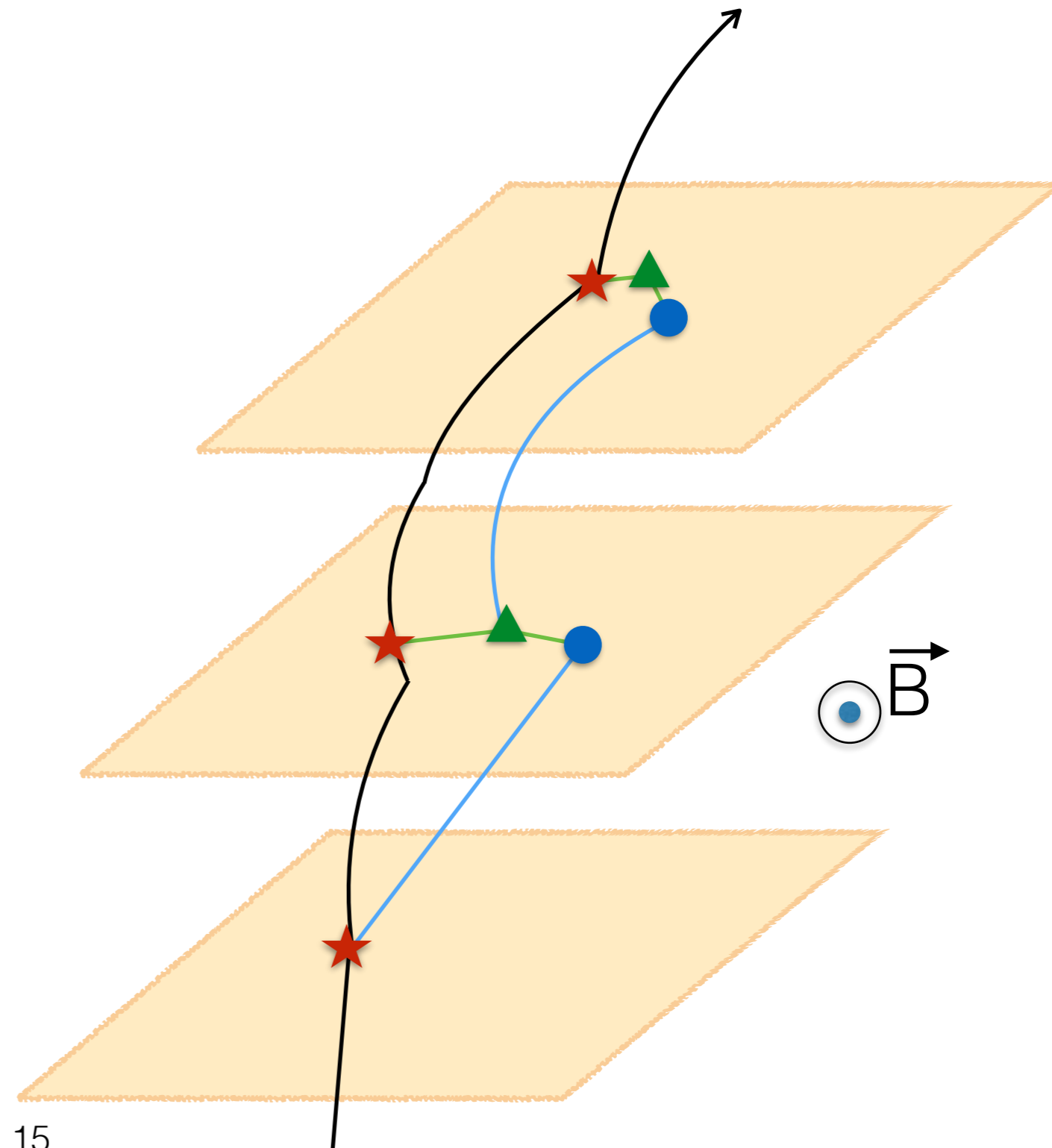
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$$\triangle_2 = \chi^2 (H \times \star_2, H \times \bullet_2)$$

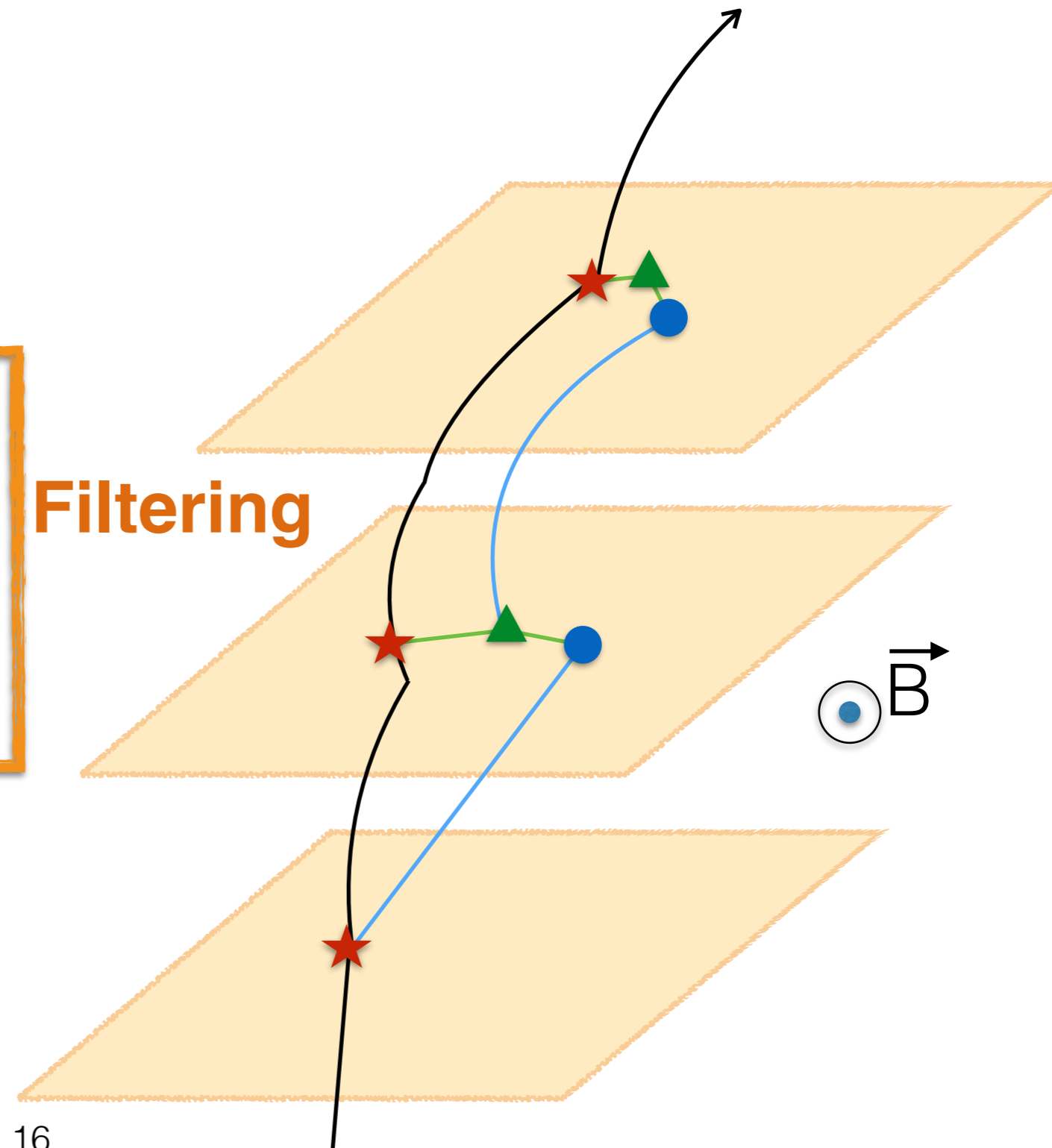
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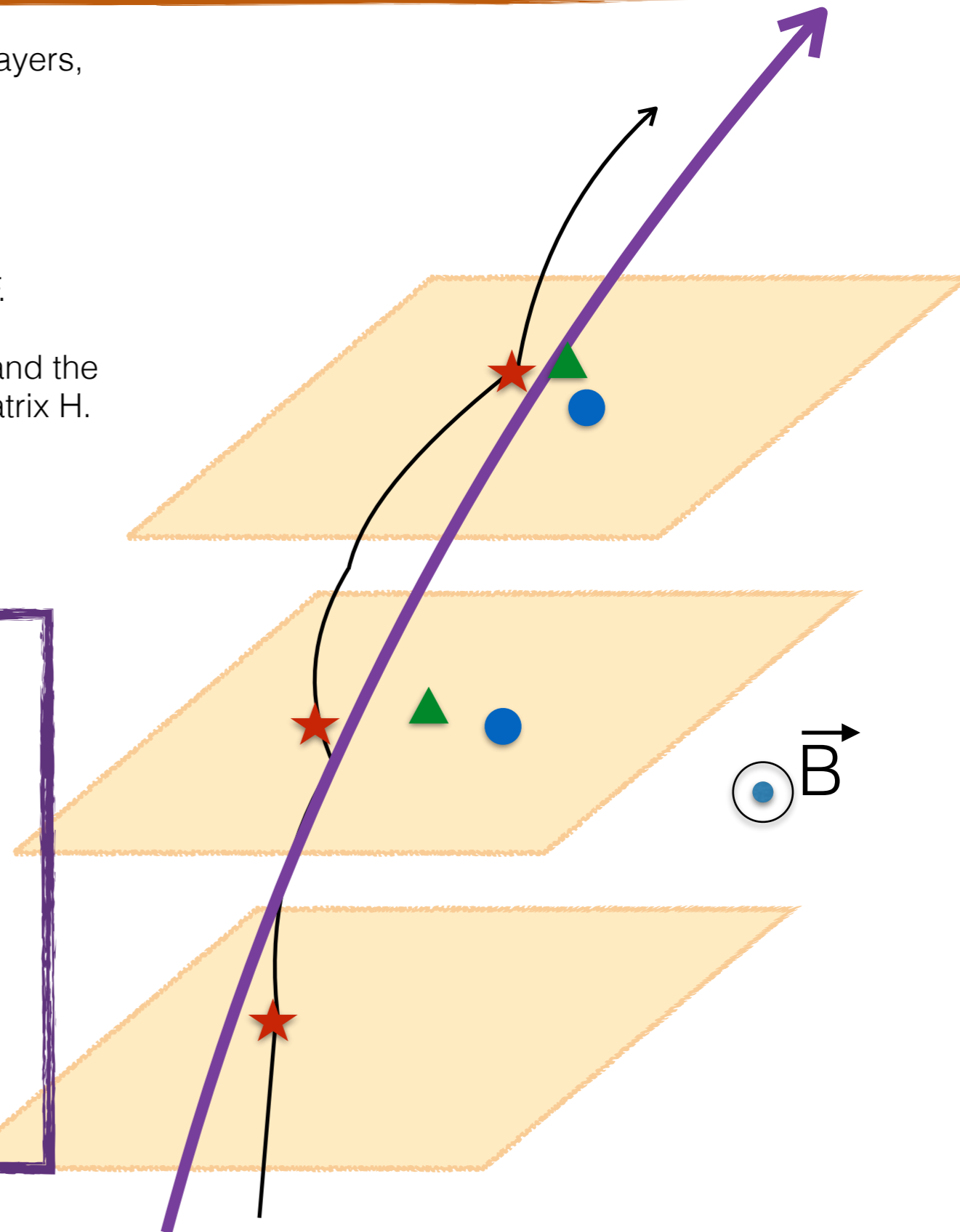


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- At each layer we do not evaluate a point in space, but a **curve (helix)** that best approximate the trajectory at ▲ point;
- The curve found has an associated uncertainty that decrease layer after layer...
- ...so we redo the filtering backward! (Smoothing)



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