

# QFT-HEP

nodes:

Bari  
Catania  
**LNF: Maria Paola Lombardo** → large scale lattice QCD computations  
Lecce  
Napoli

Pietro Colangelo  
INFN – Bari  
on behalf of the IS QFT-HEP



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in-medium effects on heavy hadron masses and widths  
QCD thermodynamics with  $N_f=2+1+1$  Wilson fermions  
topology in hot QCD  
connection between the QGP and QCD conformal window

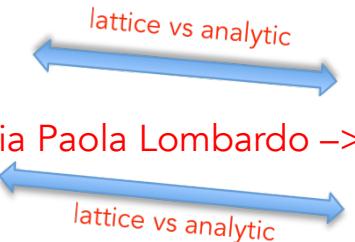
Pietro Colangelo  
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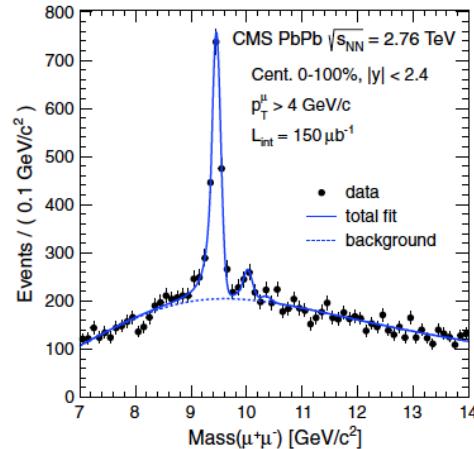
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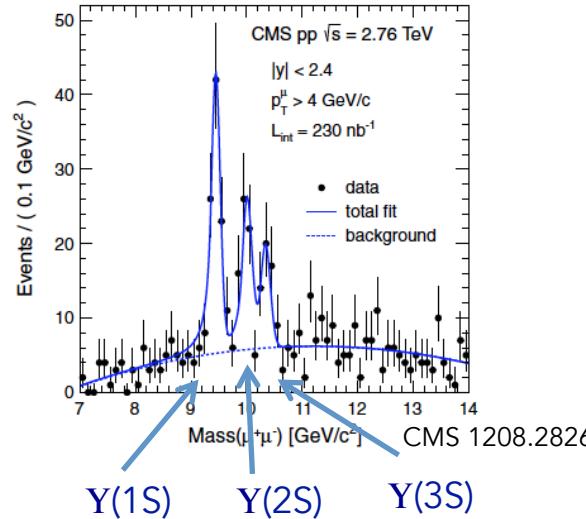
# Transport and response properties of strongly interacting systems

## heavy quarkonium in a thermalized medium

PbPb

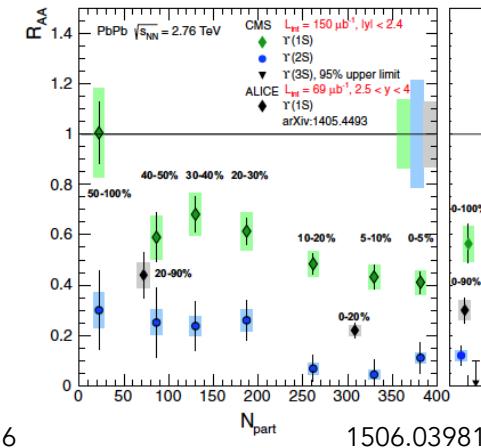


pp



$$\frac{Y(2S)/Y(1S)|_{PbPb}}{Y(2S)/Y(1S)|_{pp}} = 0.21 \pm 0.07(\text{stat}) \pm 0.02(\text{syst}),$$

$$\frac{Y(3S)/Y(1S)|_{PbPb}}{Y(3S)/Y(1S)|_{pp}} = 0.06 \pm 0.06(\text{stat}) \pm 0.06(\text{syst}) \\ < 0.17(95\% \text{CL}).$$



lattice calculation of spectral functions: issue of systematic errors  
interplay with analytic methods (AdS/QCD)

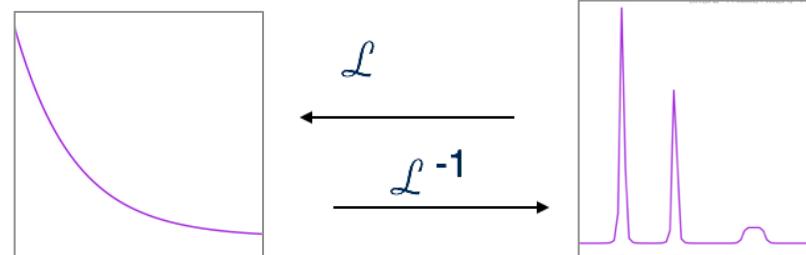
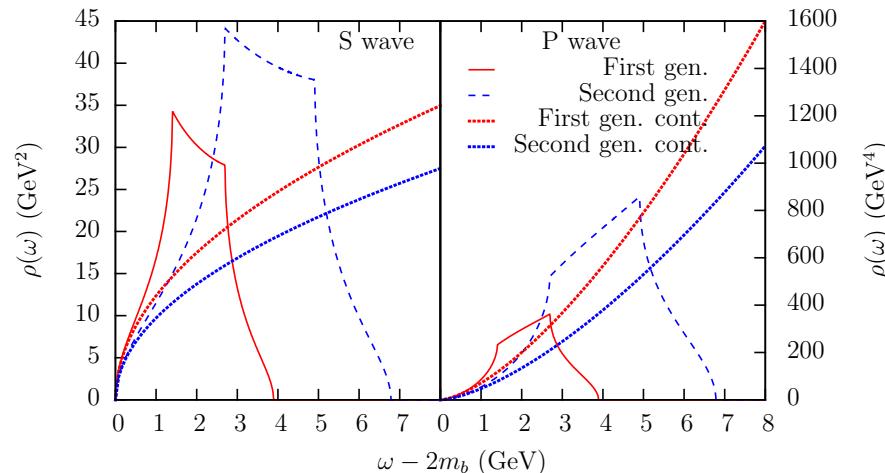
## ISSUES

$$G(\tau) = \int_0^\infty \frac{d\omega}{2\pi} K(\tau, \omega) \rho(\omega), \quad 0 \leq \tau < \frac{1}{T},$$

finite lattice produces structures in spectral functions

transform acts as a smoothing operator

inverse problem ill posed



## relativistic vs nonrelativistic kernels

$$\text{QCD: } K(\tau, \omega) = \frac{(e^{-\omega\tau} + e^{-\omega(1/T-\tau)})}{1 - e^{-\omega/T}}.$$

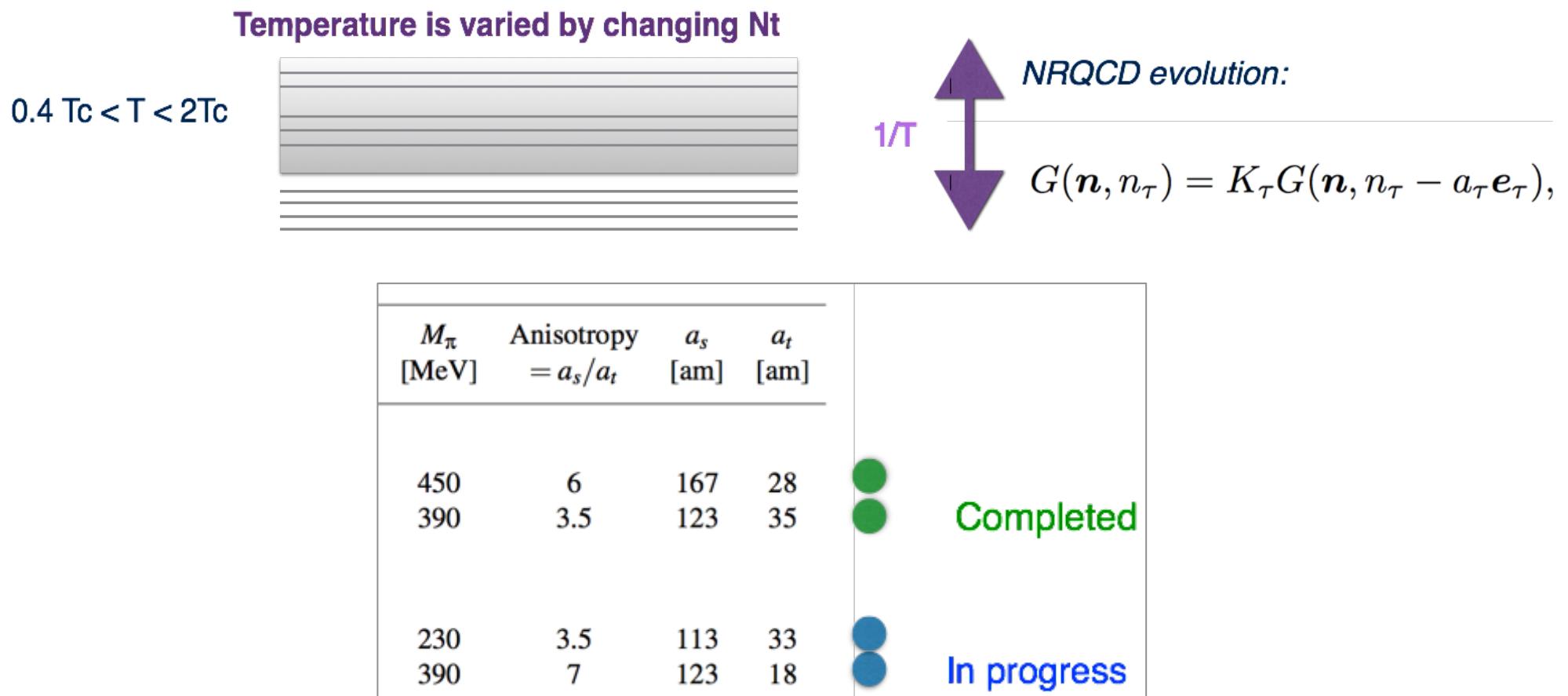
$$\text{NRQCD: } K(\tau, \omega) \simeq (e^{-\omega\tau} + e^{-\omega(1/T-\tau)}):$$

in NRQCD all the T dependence in the spectral function

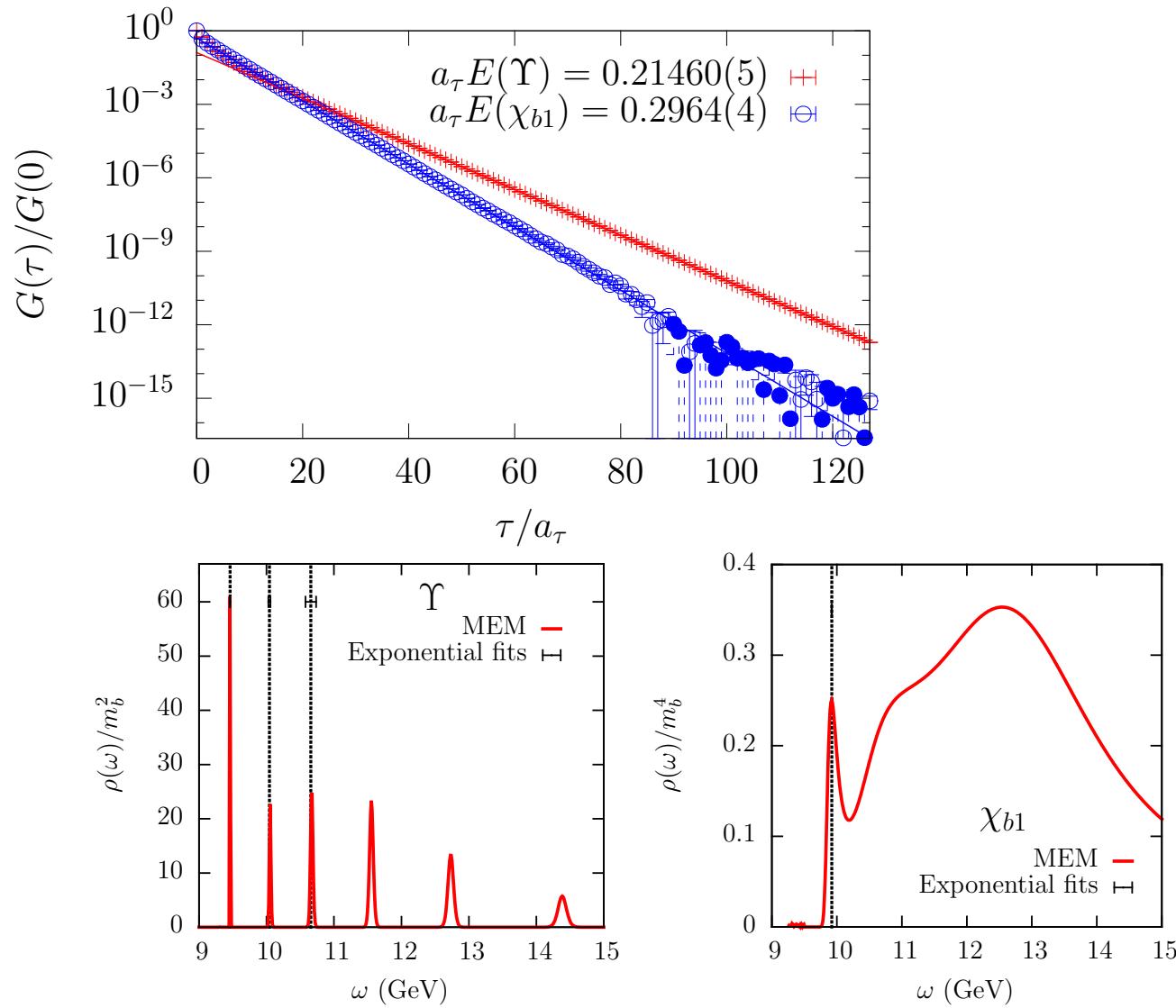
## FASTSUM Coll.

lattice setup: anisotropic lattice

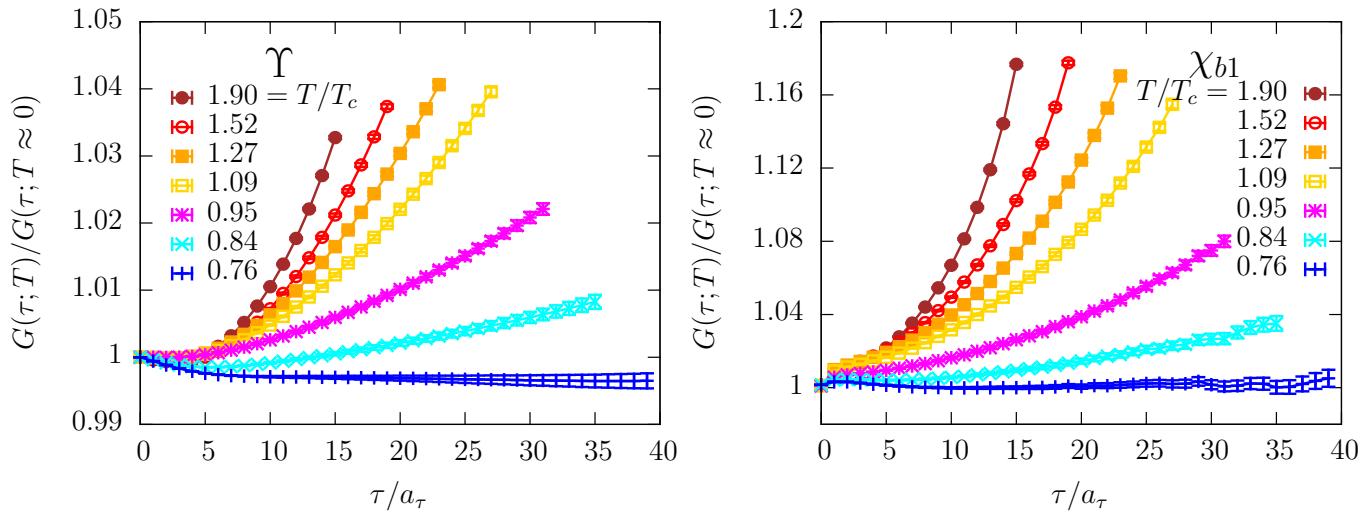
Wilson clover fermions for the sea quarks, NRQCD for bottom quarks



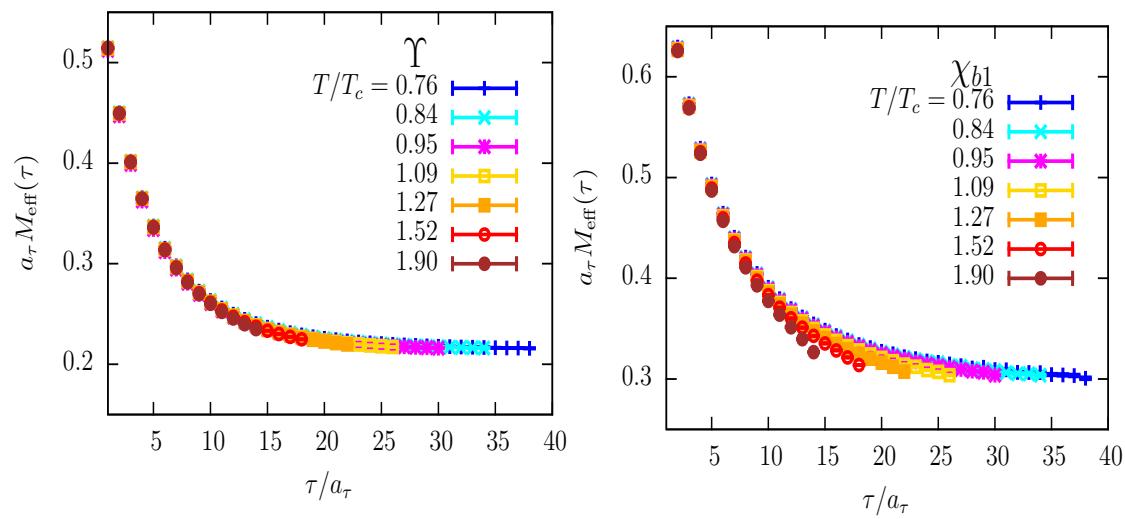
T=0



high T  
Y(1S) correlators

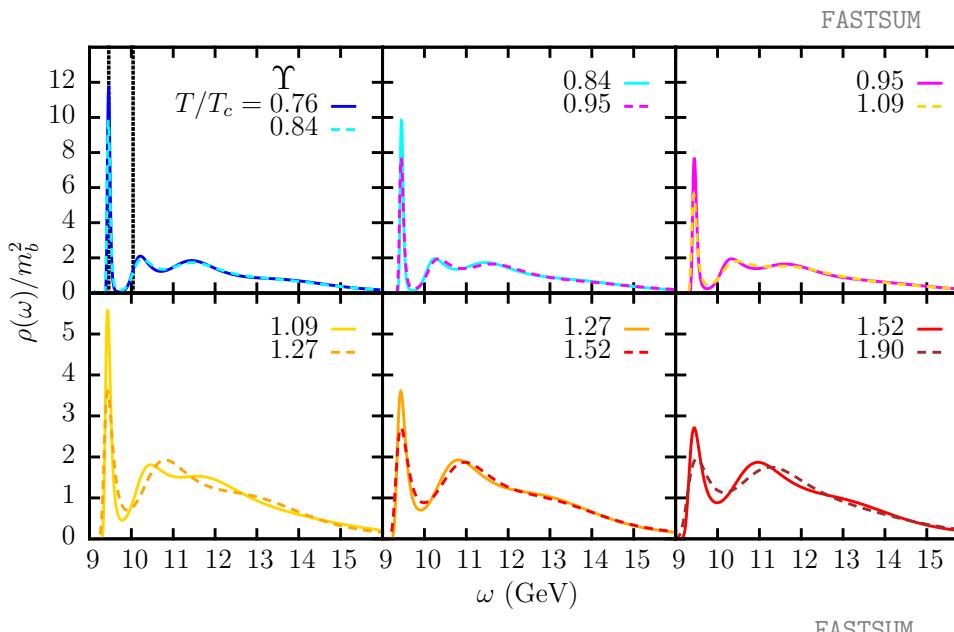


effective  
masses



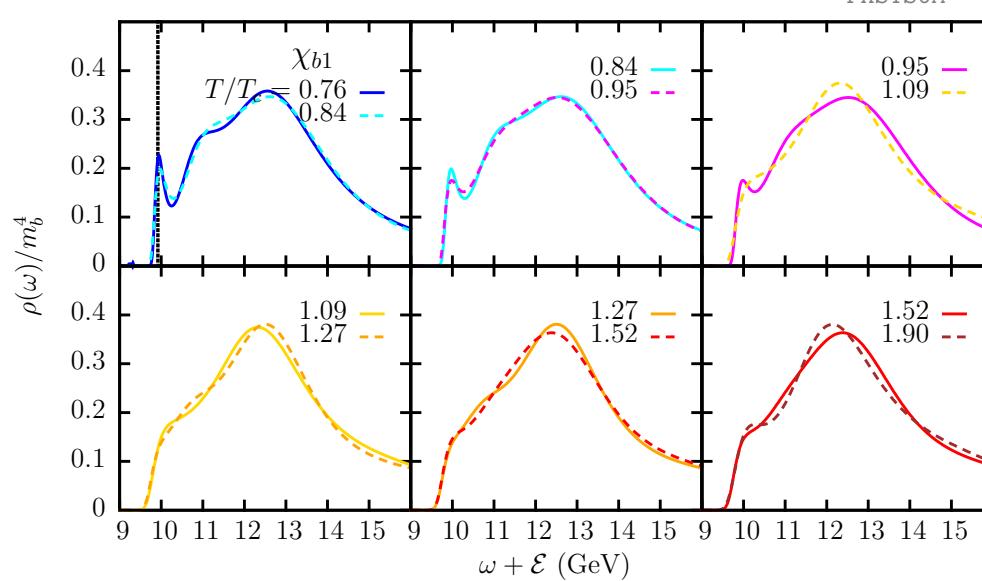
## Y spectral function

$Y(1S)$  survives up to  $\sim 1.9T_c$



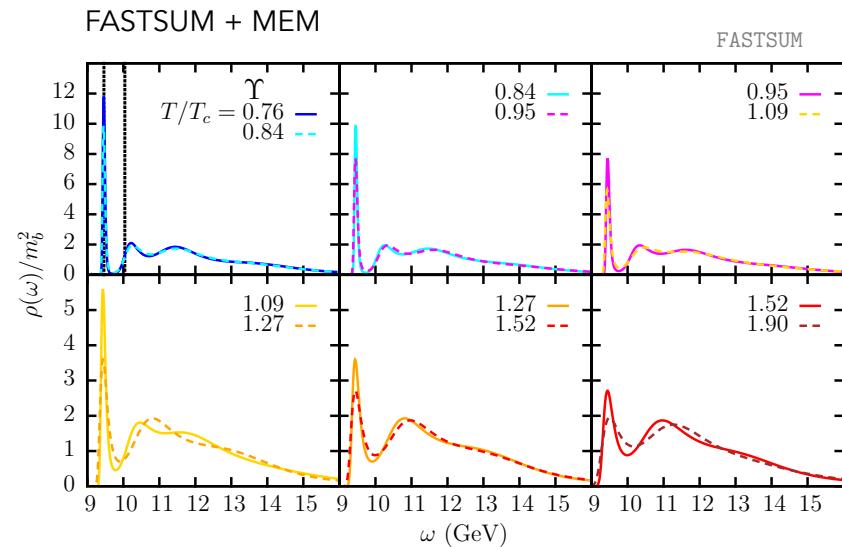
## X<sub>b1</sub> spectral function

$X_{b1}$  melts at  $\sim T_c$

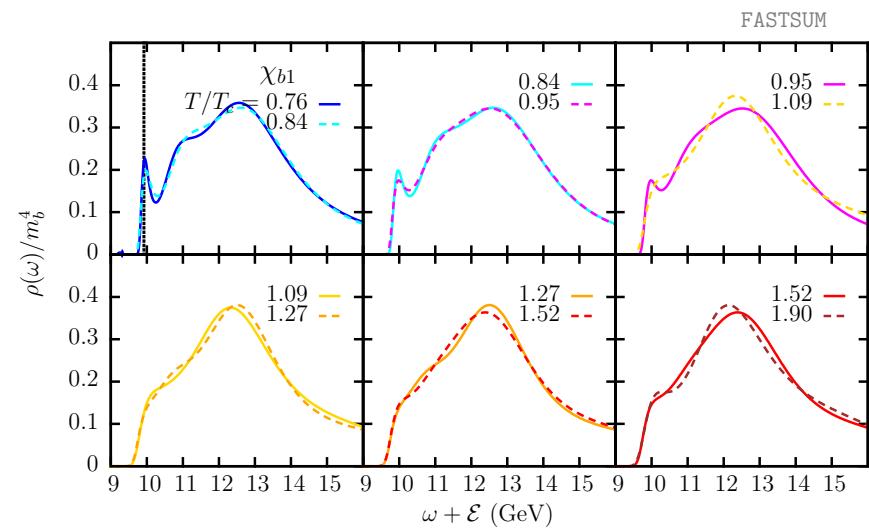


# ISSUE OF THE RECONSTRUCTION METHOD

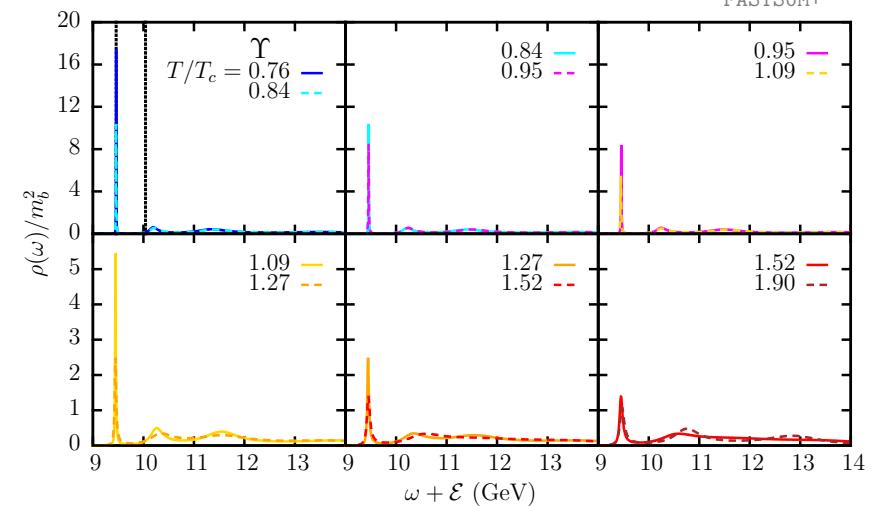
**Y**



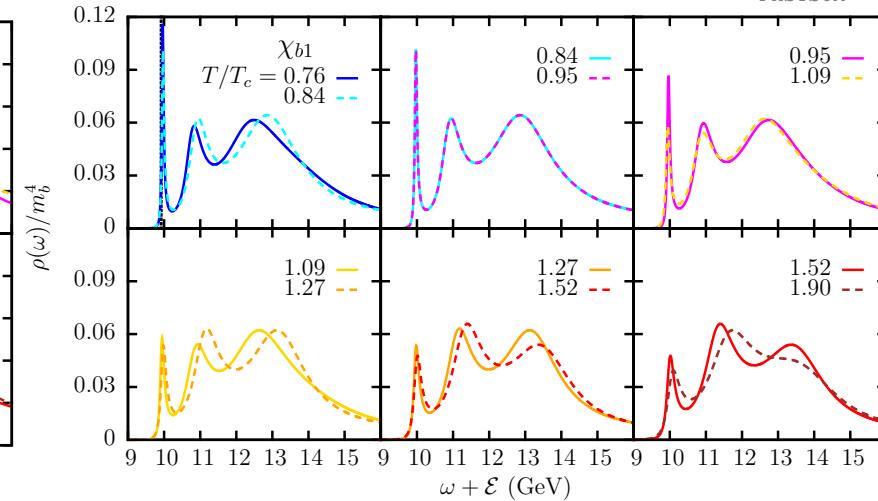
**X<sub>b1</sub>**



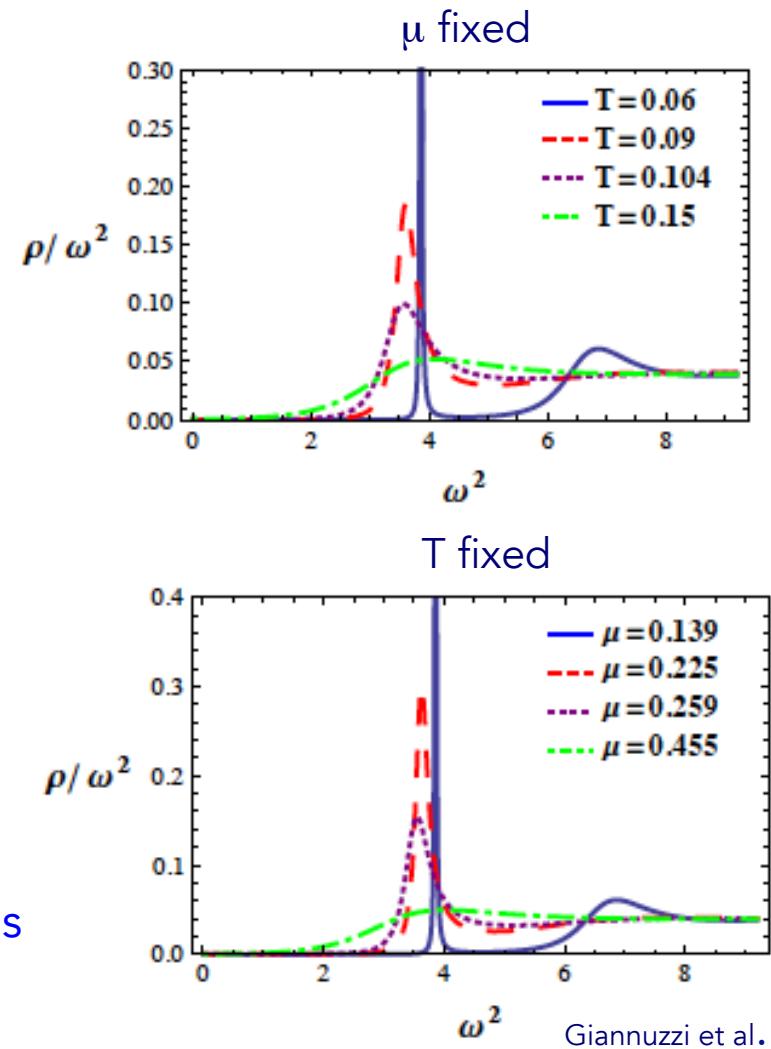
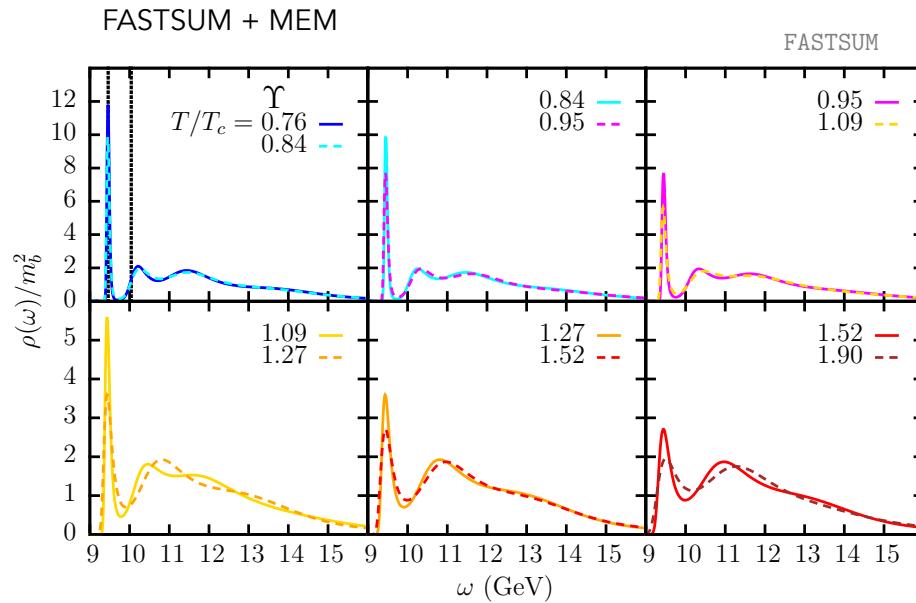
FASTSUM + Burnier & Rothkopf 2015



FASTSUM+



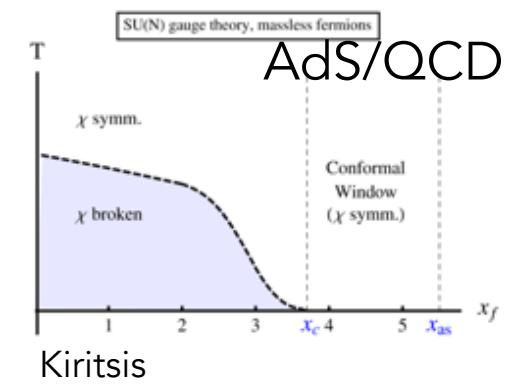
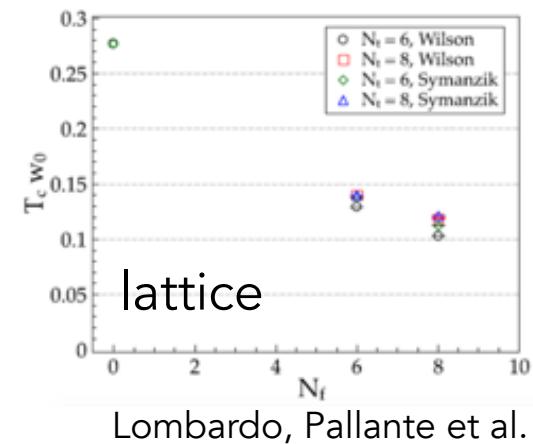
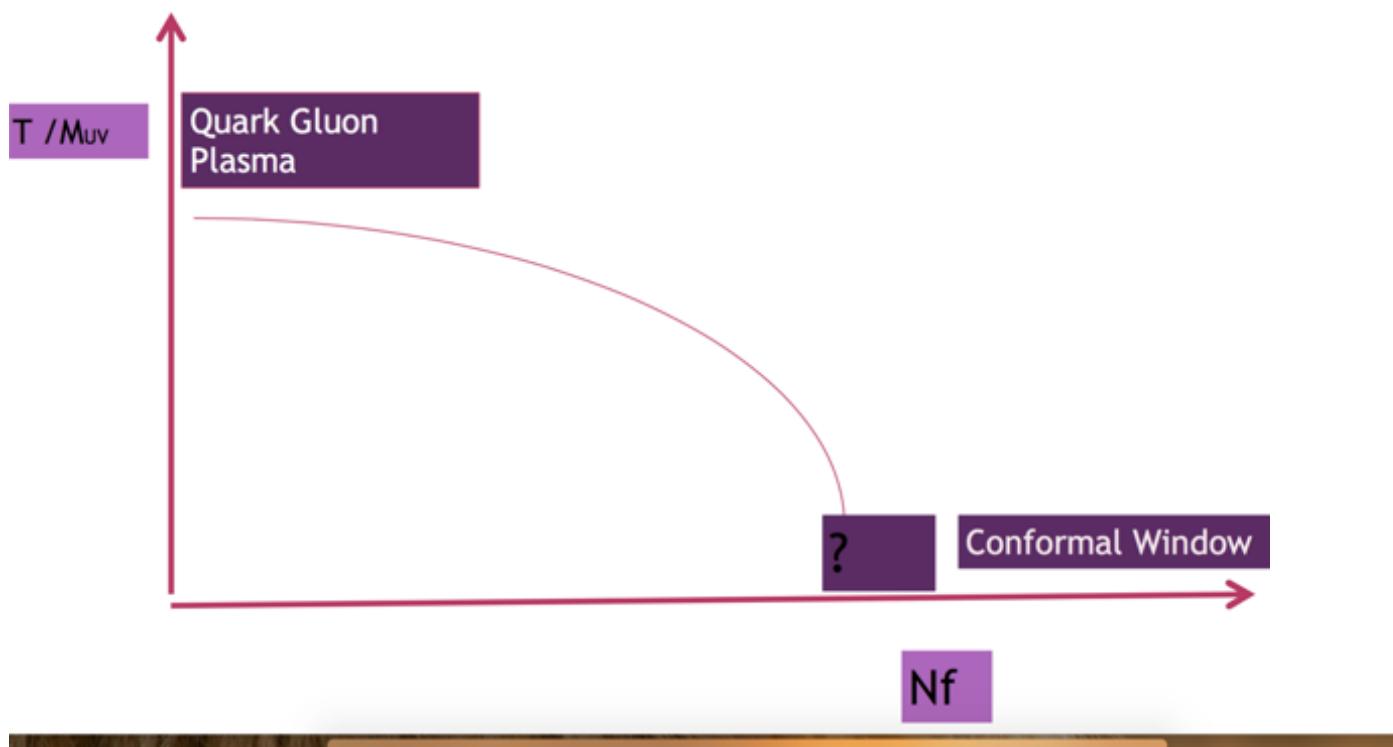
# ISSUE OF THE RECONSTRUCTION METHOD: use info from AdS/QCD



- different priors
- dependence on the input data set features

# QGP continuously connected to conformal QCD

$$G_H(t) = \tilde{c}_H \frac{\exp(-\tilde{m}_H t)}{t^{\alpha_H}}$$



## from free correlators to quasi-conformal behaviour

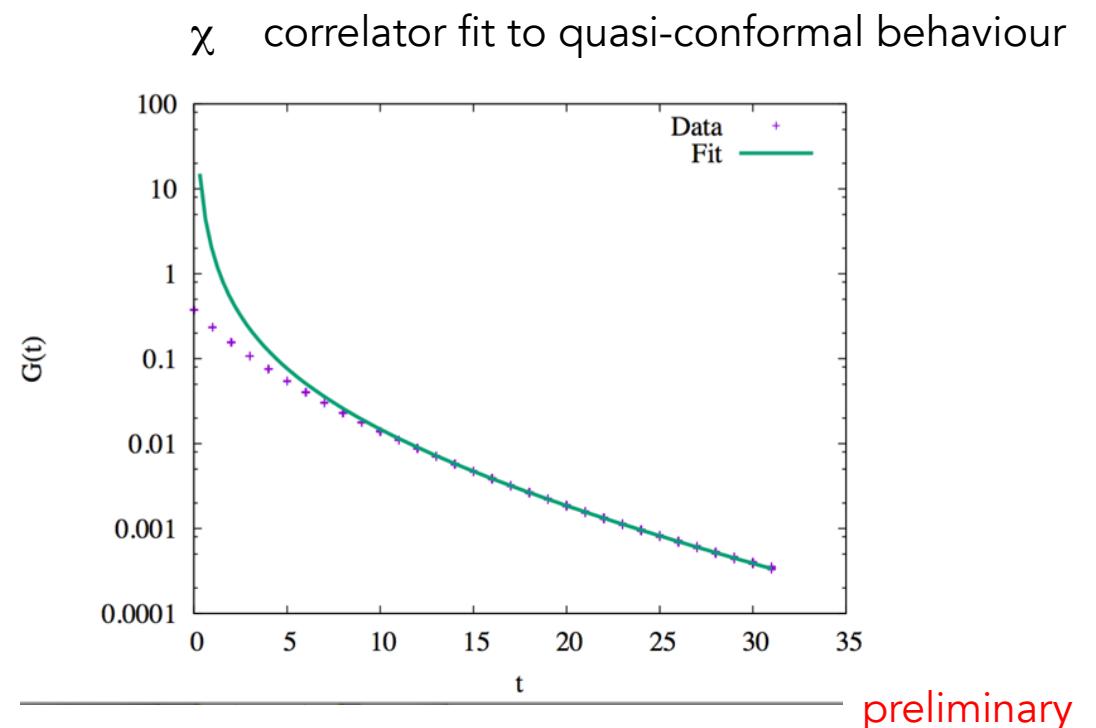
fits: include a T dependence in the coefficients

$$G(\tau) \rightarrow \frac{e^{-\omega_0(T)\tau}}{\tau^{\alpha(T)+1}}$$

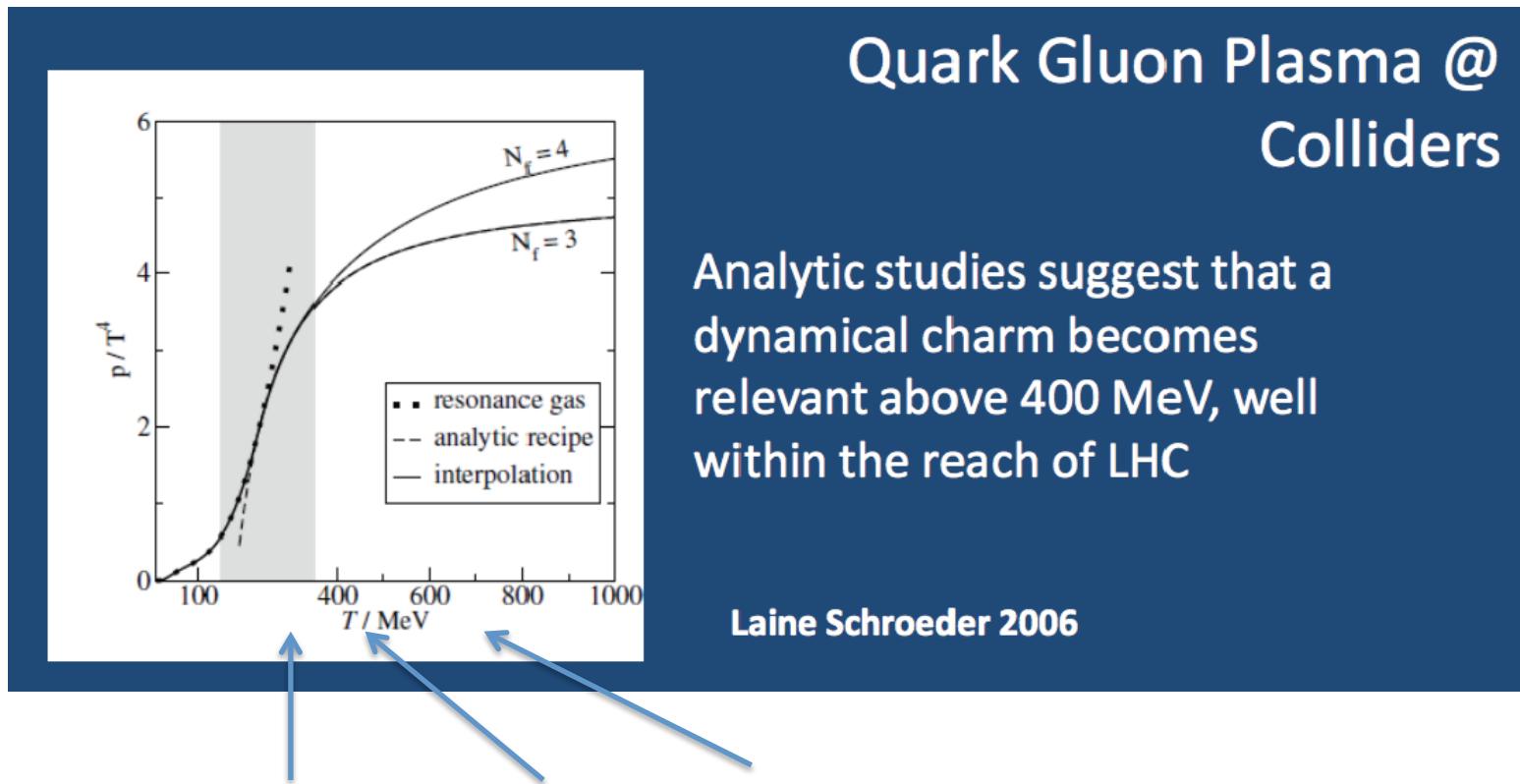
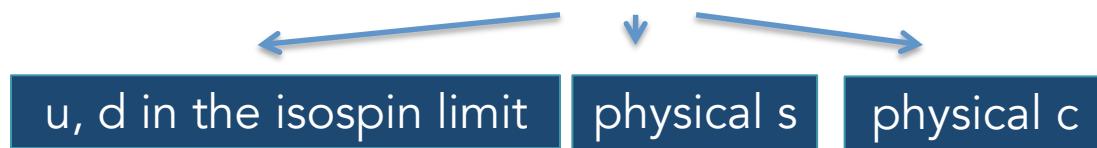
in a quasi-conformal theory

$$G(\tau) \rightarrow \frac{e^{-\omega_0(T)\tau}}{\tau^{\alpha_H(T)}}$$

$\alpha_H = 3 - 2\gamma$  Iwasaki 2013



## HOT QCD and $N_f=2+1+1$ twisted mass Wilson fermions



## Setup Nf=2+1+1

Number of flavours	$m_{\pi^\pm}$
	210
$N_f = 2 + 1 + 1$	260
	370
	470
$N_f = 2$	360
	430

$T = 0$ (ETMC) nomenclature	$\beta$	$a$ [fm] [6]	$N_\sigma^3$	$N_\tau$	$T$ [MeV]	# confs.
A60.24	1.90	0.0936(38)	$24^3$	5	422(17)	585
				6	351(14)	1370
				7	301(12)	341
				8	263(11)	970
				9	234(10)	577
				10	211(9)	525
				11	192(8)	227
			$32^3$	12	176(7)	1052
				13	162(7)	294
				14	151(6)	1988
				5	479(22)	595
				6	400(18)	345
				7	342(15)	327
				8	300(13)	233
				9	266(12)	453
B55.32	1.95	0.0823(37)	$32^3$	10	240(11)	295
				11	218(10)	667
				12	200(9)	1102
				13	184(8)	308
				14	171(8)	1304
				15	160(7)	456
				16	150(7)	823
				6	509(20)	403
				7	436(18)	412
				8	382(15)	416
			$32^3$	10	305(12)	420
				12	255(10)	380
				14	218(9)	793
				16	191(8)	626
				18	170(7)	599
				20	153(6)	582
				40 <sup>3</sup>		
				48 <sup>3</sup>		

fermionic action

$$S_f^{\text{light}}[U, \chi_l, \bar{\chi}_l] = \sum_{x,y} \bar{\chi}_l(x) [\delta_{x,y} - \kappa D_W(x,y)[U] + 2i\kappa a \mu_l \gamma_5 \delta_{x,y} \tau^3] \chi_l(y), \quad (1)$$

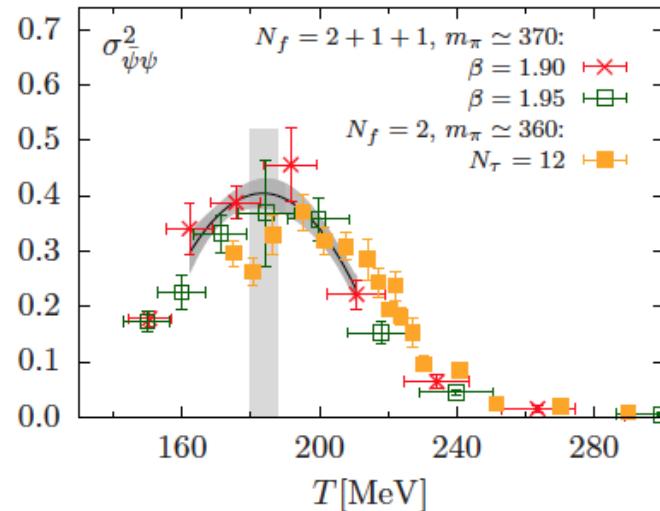
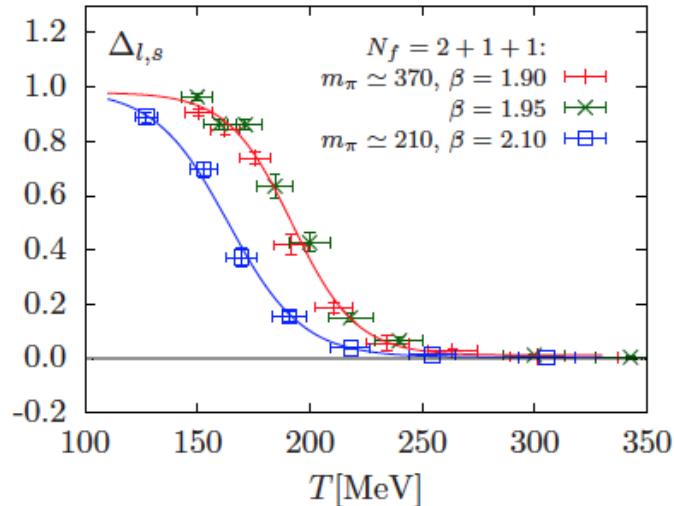
$$S_f^{\text{heavy}}[U, \chi_h, \bar{\chi}_h] = \sum_{x,y} \bar{\chi}_h(x) [\delta_{x,y} - \kappa D_W(x,y)[U] + 2i\kappa a \mu_\sigma \gamma_5 \delta_{x,y} \tau^1 + 2\kappa a \mu_\delta \delta_{x,y} \tau^3] \chi_h(y),$$

renormalized subtracted chiral condensate

$$\Delta_{l,s} = \frac{\langle \bar{\psi}\psi \rangle_l - \frac{\mu_l}{\mu_s} \langle \bar{\psi}\psi \rangle_s}{\langle \bar{\psi}\psi \rangle_l^{T=0} - \frac{\mu_l}{\mu_s} \langle \bar{\psi}\psi \rangle_s^{T=0}},$$

disconnected chiral susceptibility

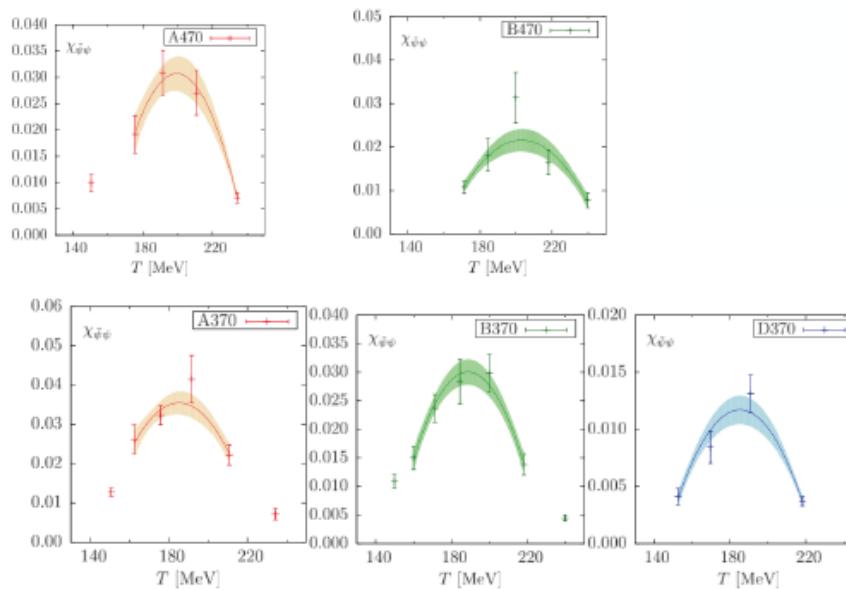
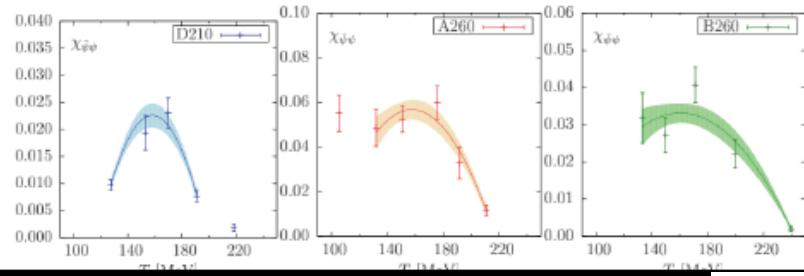
$$\sigma_{\bar{\psi}\psi}^2 = \frac{V}{T} (\langle (\bar{\psi}\psi)^2 \rangle_l - \langle \bar{\psi}\psi \rangle_l^2), \quad V = a^4 N_\sigma^3 N_\tau.$$



Mass

Chiral  
susceptibility

Scaling  
with the pion  
mass



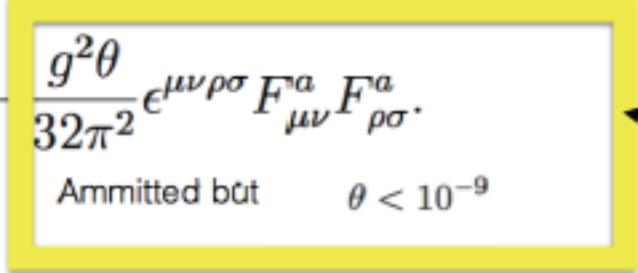
pseudocritical temperature

Ensemble	$a$ [fm]	$m_\pi$ [MeV]	$T_\chi$ [MeV]	$T_\Delta$ [MeV]	$T_{\text{deconf}}$ [MeV]
D210	0.065	213	158(1)(4)	165(3)(1)	176(8)(8)
A260	0.094	261	157(8)(14)	172(2)(1)	188(6)(1)
B260	0.082	256	161(13)(2)	177(2)(1)	192(9)(2)
A370	0.094	364	185(5)(3)	191(2)(0)	202(3)(0)
B370	0.082	372	189(2)(1)	194(2)(0)	201(6)(0)
D370	0.065	369	185(1)(3)	180(5)(1)	193(13)(2)
A470	0.094	466	200(4)(6)	193(5)(2)	205(4)(2)
B470	0.082	465	203(2)(2)	202(7)(1)	212(6)(1)

## Topology ( $N_f = 2+1+1$ )

$$\mathcal{L}_{QCD}(\theta) = \mathcal{L}_{QCD} + \frac{g^2 \theta}{32\pi^2} \epsilon^{\mu\nu\rho\sigma} F_{\mu\nu}^a F_{\rho\sigma}^a.$$

Admitted but  $\theta < 10^{-9}$



$$Q = \int d^4x \frac{g^2}{32\pi^2} \text{tr} F \tilde{F}$$

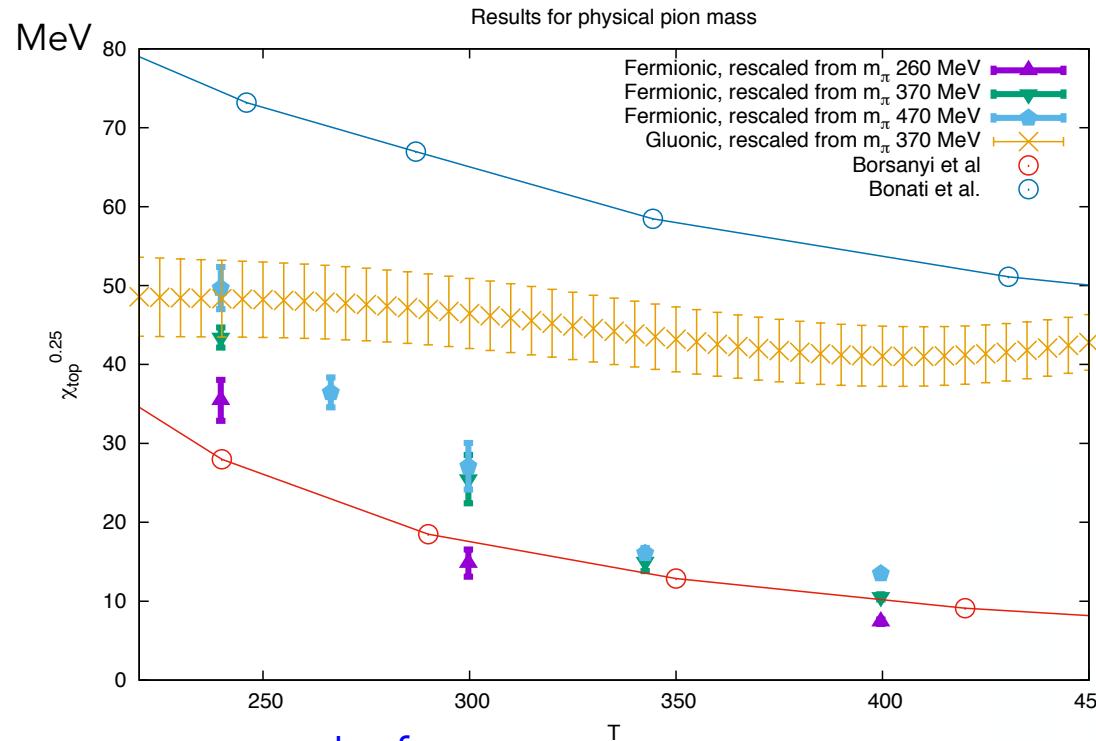
$$Z_{QCD}(\theta, T) = \int [dA][d\psi][d\bar{\psi}] \exp \left( -T \sum_t d^3x \mathcal{L}_{QCD}(\theta) \right) = \exp[-V F(\theta, T)]$$

$$\left. \frac{\partial^2 F(\theta, T)}{\partial \theta^2} \right|_{\theta=0} \equiv \chi(T) = (\langle Q^2 \rangle - \langle Q \rangle^2)/V$$

$$\chi_{top} = \langle Q_{top}^2 \rangle / V = m_l^2 \chi_{5, disc}$$

Topology ( $N_f = 2+1+1$ )

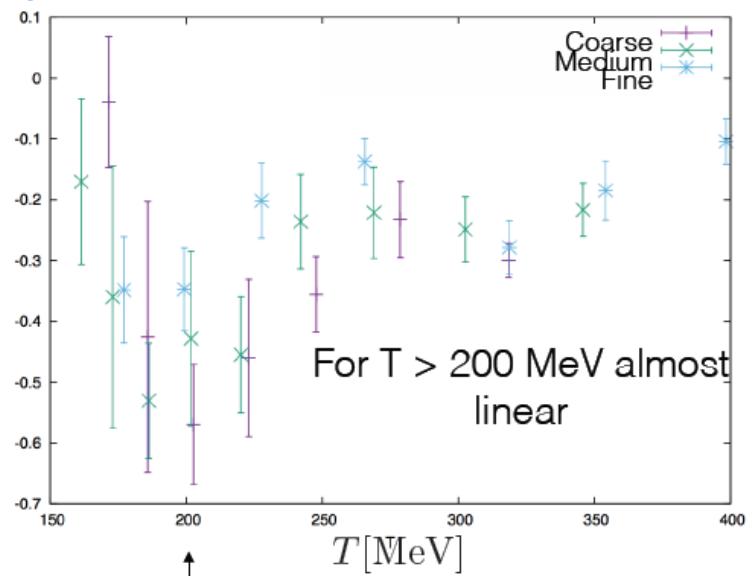
gluonic operator  $m_\pi = 370$  MeV  
 fermionic operator  $m_\pi = 210-470$  MeV



new results from  
 fermionic method

$$\frac{d\chi^{1/4}}{dT}$$

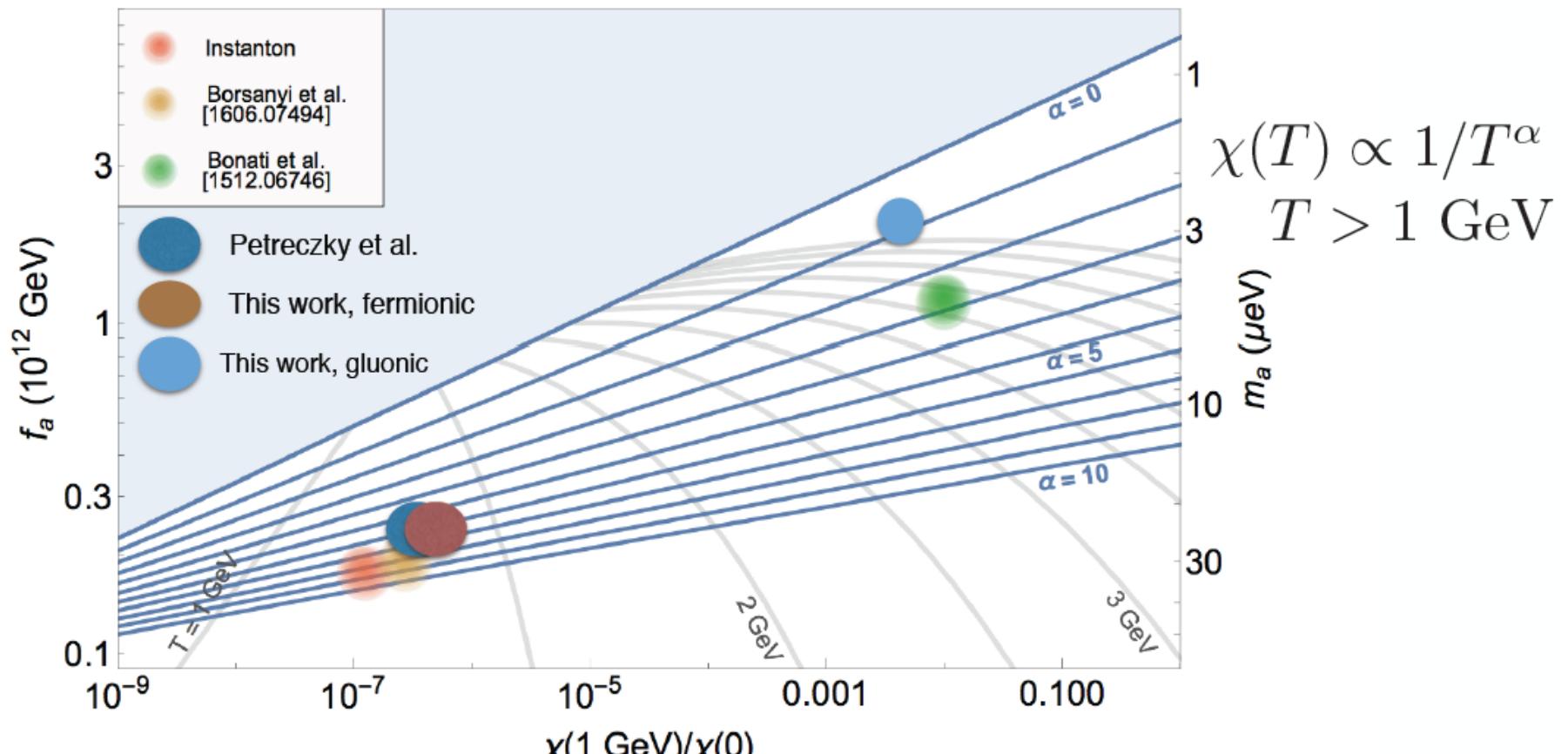
puzzling features  
 of gluonic method



Inflection point around 200 MeV

Needed assumption on  
fraction of DM made of axions

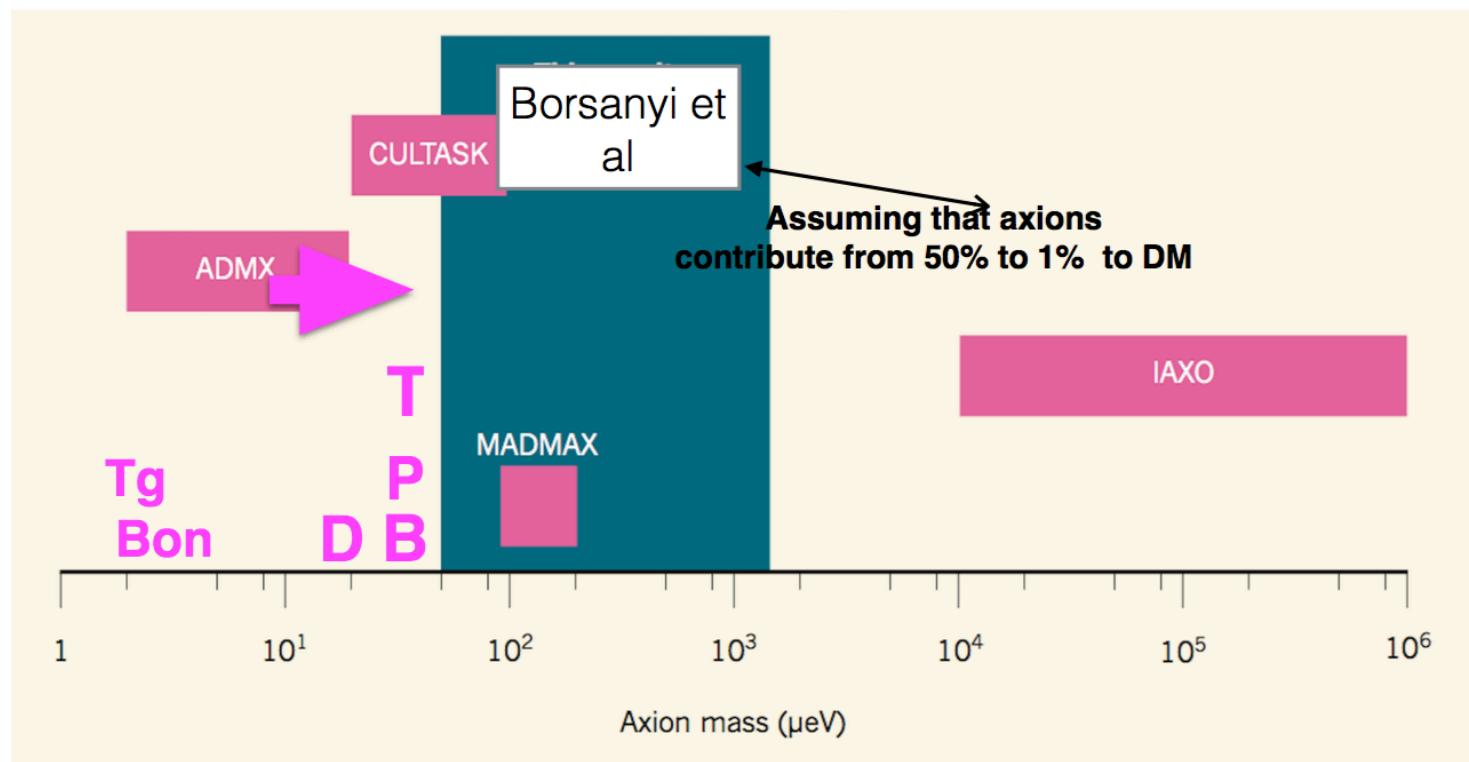
*Assume:* Axions make all of Dark Matter



$$m_a^2(T)f_a^2 = \left. \frac{\partial^2 F(\theta, T)}{\partial \theta^2} \right|_{\theta=0} \equiv \chi(T), \quad \text{PhD Thesis, G. Grilli di Cortona, Sissa 2016}$$

## Lower limits on the axion mass assuming that axions make 100% of DM:

Tg: This work, gluonic; Bon: Bonati et al.; D: DIGA, B: Borsanyi et al.,  
P: Petreczky et al., T: this work, fermionic



Updated from Nature N&V

## computing needs

at present:

FASTSUM (spectral functions) -> DIRAC UK (400 Mio core hours up to 2018)  
hot QCD with Wilson fermions -> Dubna+Berlin facilities

needs (next 3 years)

10 Mio core hours -> participation in computational activity  
(not only design and analysis)

(hopefully) 100 Mio core hours -> simulations not included in already funded  
projects (e.g. finite volume effects  
for topology at high T)