

Universal Relations in Neutron Stars: Implications in Gravitational-wave Astronomy

Kent Yagi

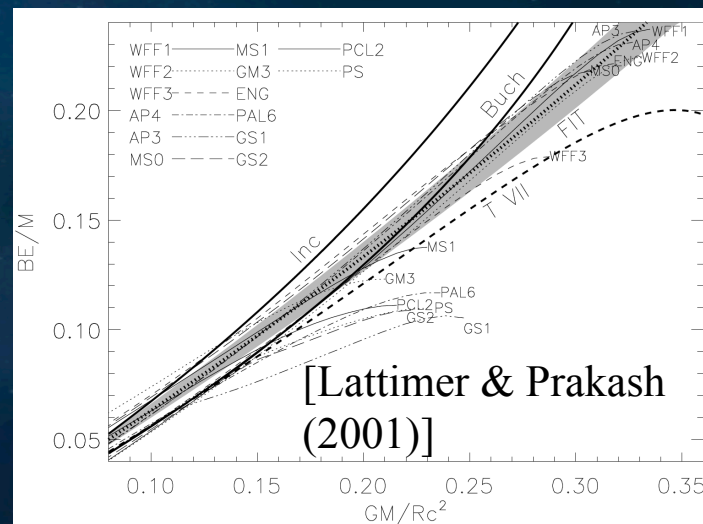
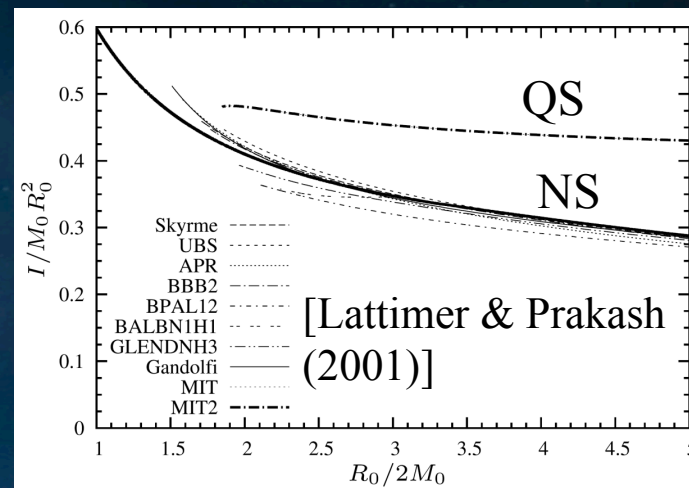
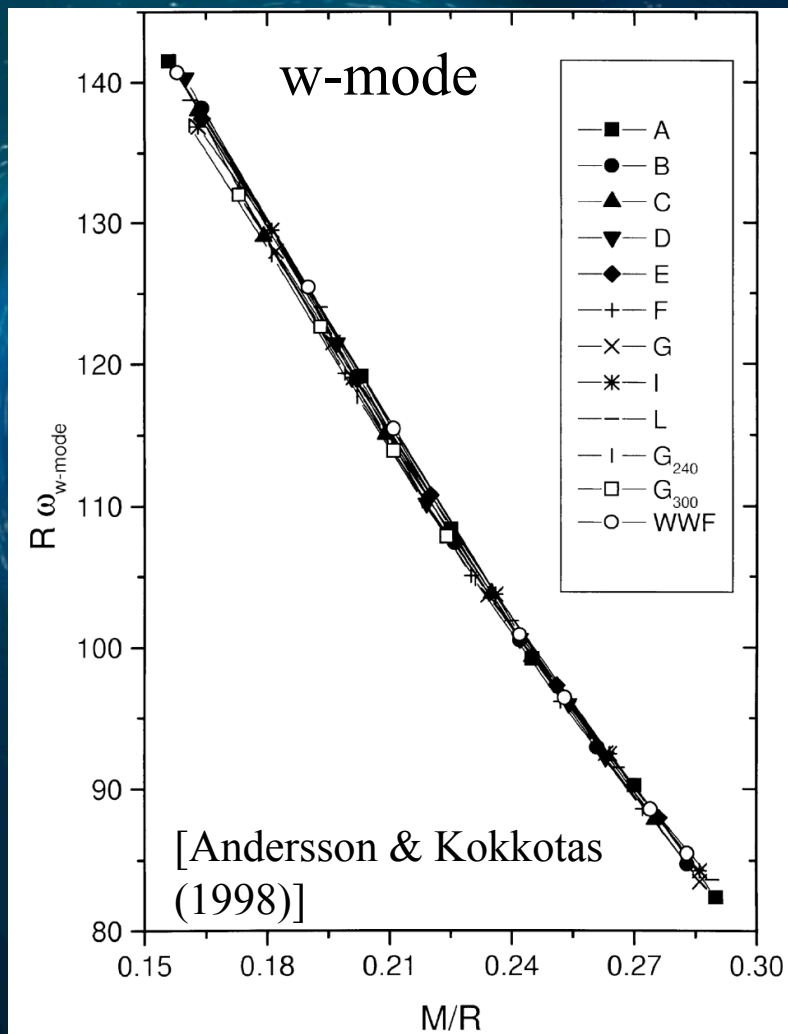
Princeton University

Sapienza University, Rome

June 20th 2017

Universal Relations: Isolated NSs

relations among NS observables that do not depend strongly on the equation of state

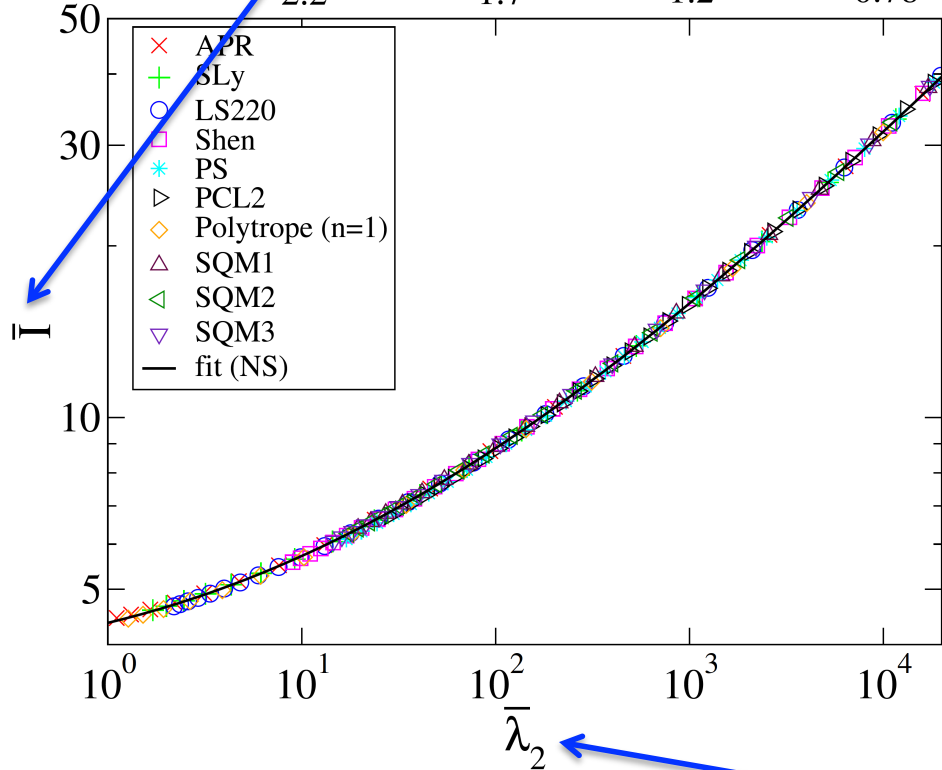


I-Love-Q Relations

[KY & Yunes, Science 341 365 (2013)]

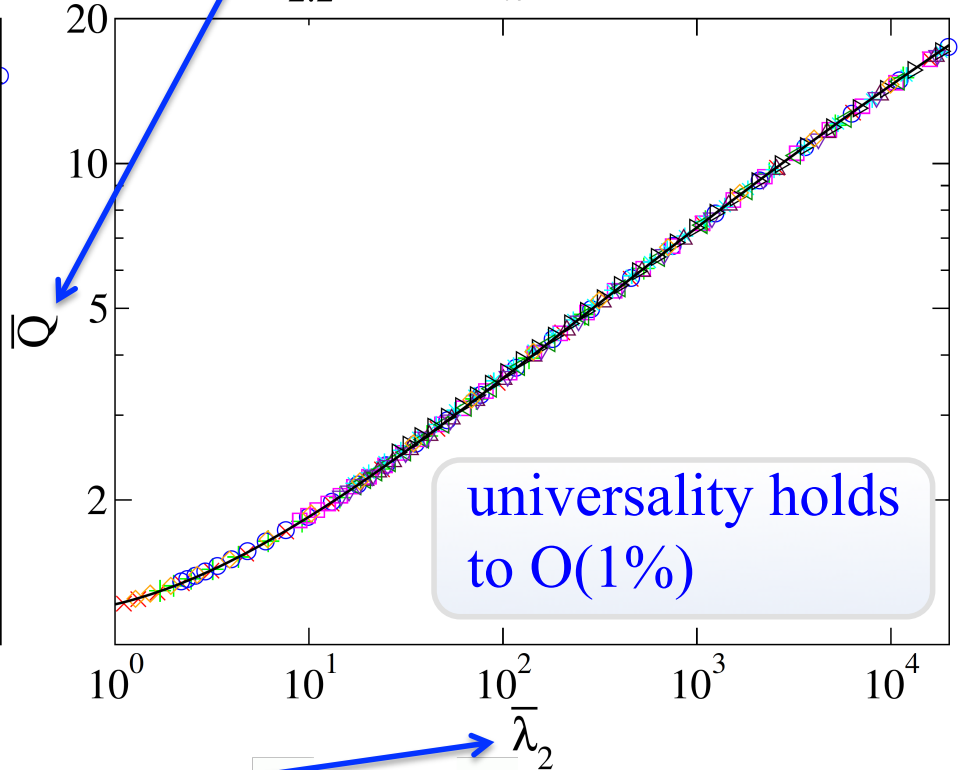
moment of inertia

$M \text{ (APR)} [M_{\odot}]$

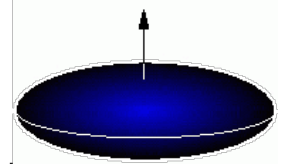


(spin-induced)
quadrupole moment

$M \text{ (APR)} [M_{\odot}]$



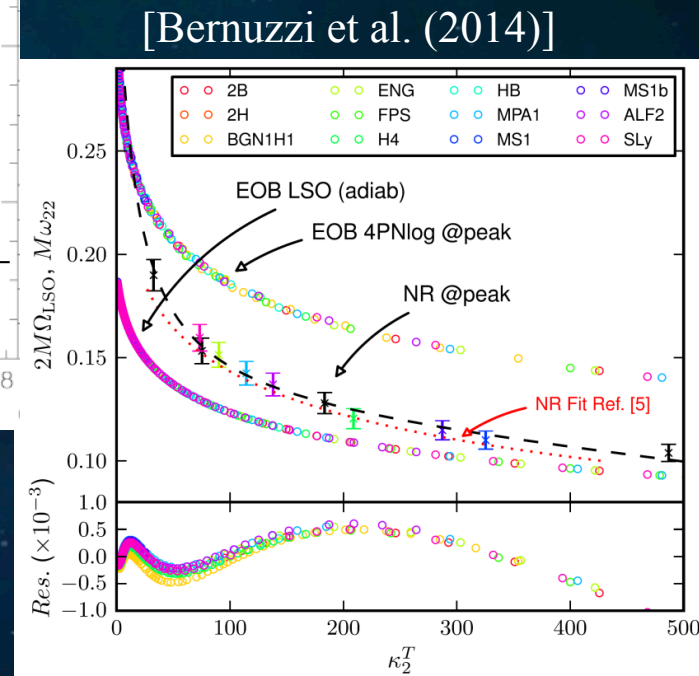
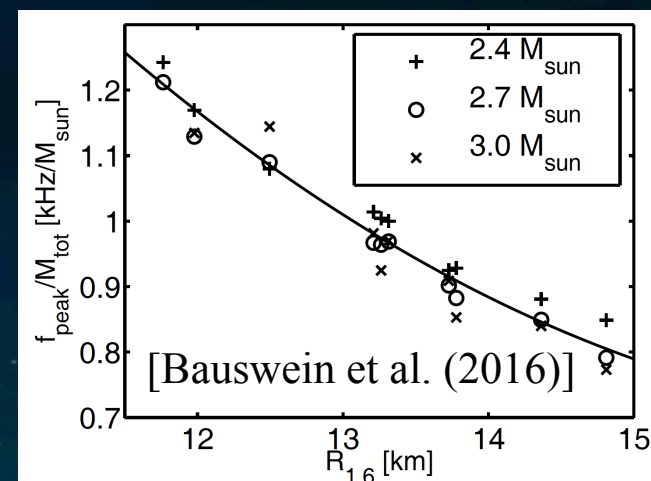
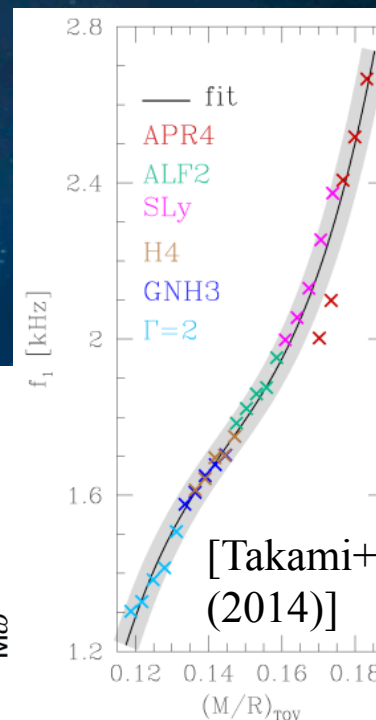
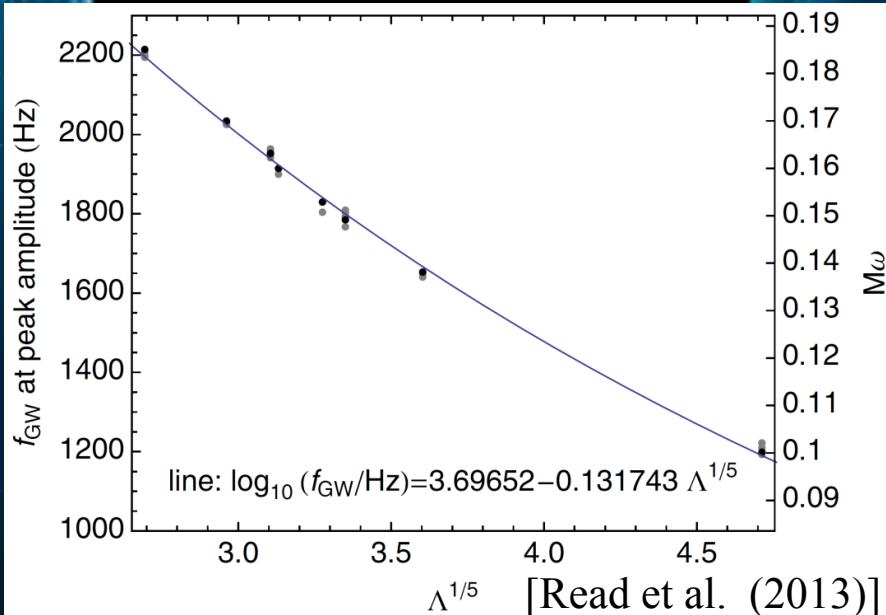
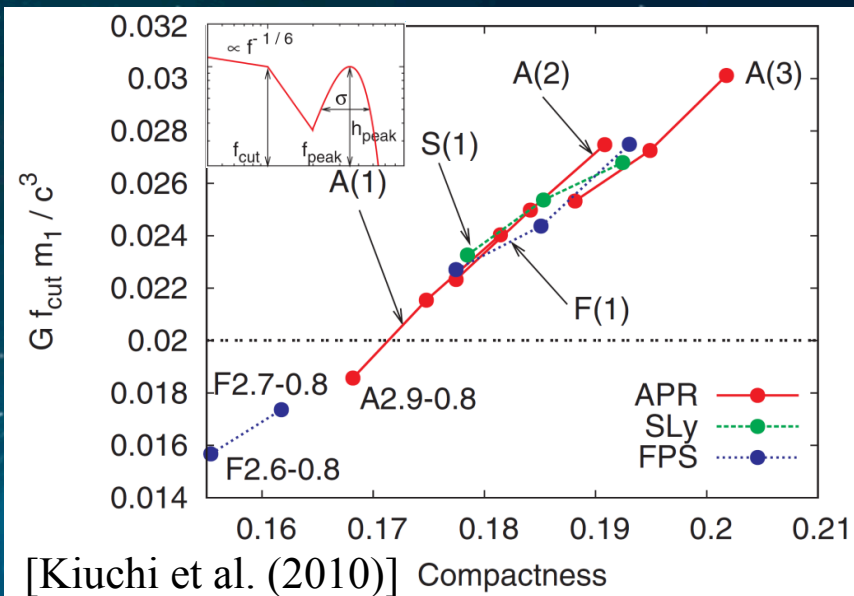
Olate



tidal Love number
(tidal deformability)



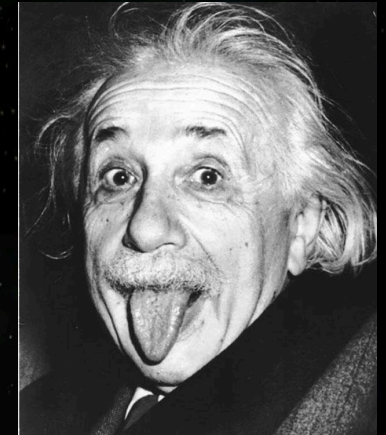
Universal Relations: Binary NS Mergers



Outline

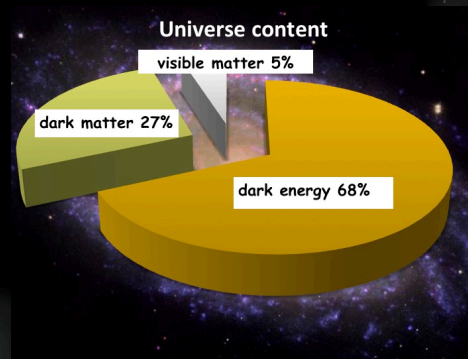
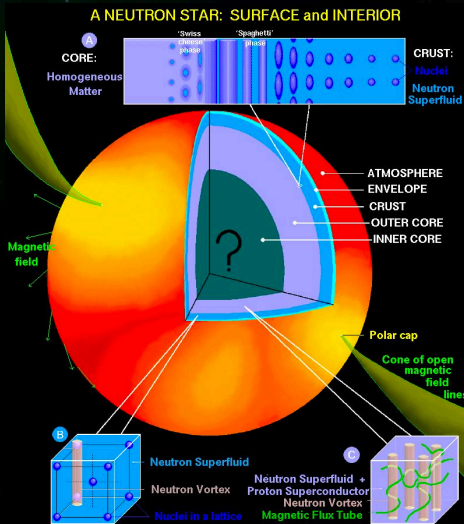
Astrophysics

Gravitational
Physics



Universal Relations

review article [KY & Yunes, Phys. Rept. (2017)]



Nuclear Physics

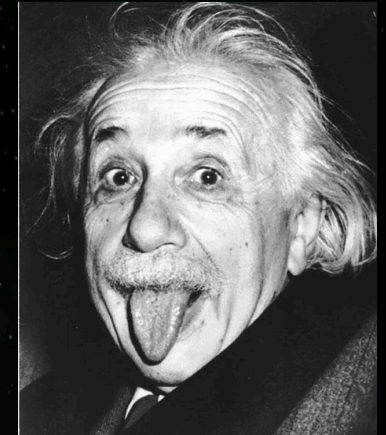
Cosmology

Outline

Astrophysics

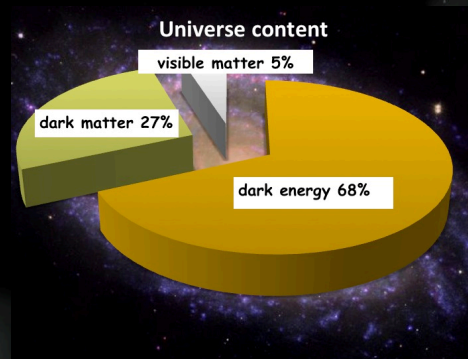
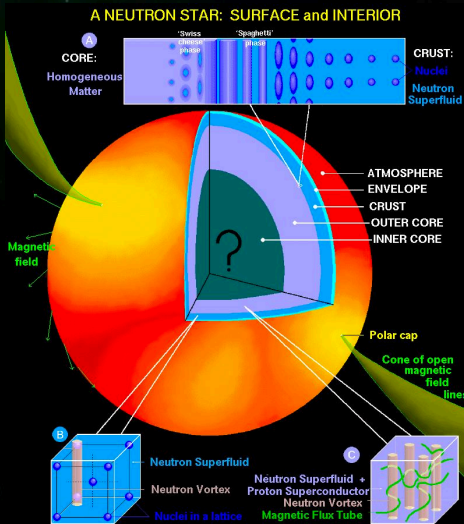


Gravitational
Physics



Universal Relations

review article [KY & Yunes, Phys. Rept. (2017)]



Nuclear Physics

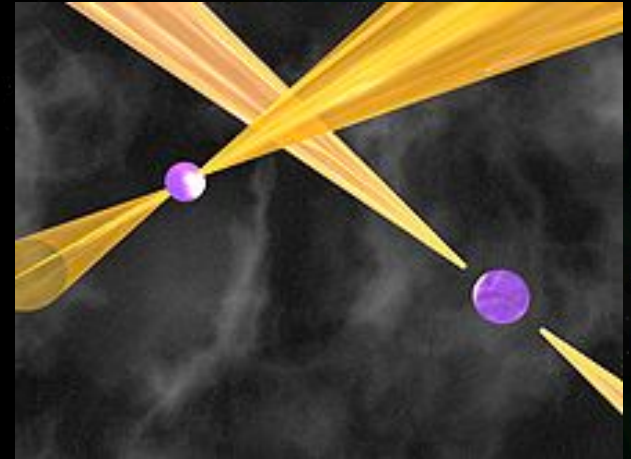
Cosmology

Supernova Scenario

[Newton, Steiner & KY (2016)]

double binary pulsar J0737-3039

- ✓ low eccentricity
- ✓ primary pulsar spin & orbital angular momentum nearly aligned
- ✓ small system velocity



J0737-3039B

- ✓ small kick velocity
- ✓ **symmetric** explosion
- ✓ short time scale

electron-capture supernova

- ✓ **unique core mass** for instability onset
[1.366, 1.377] M_{\odot} [Miyaji et al. (1980),
Nomoto (1984,87)]

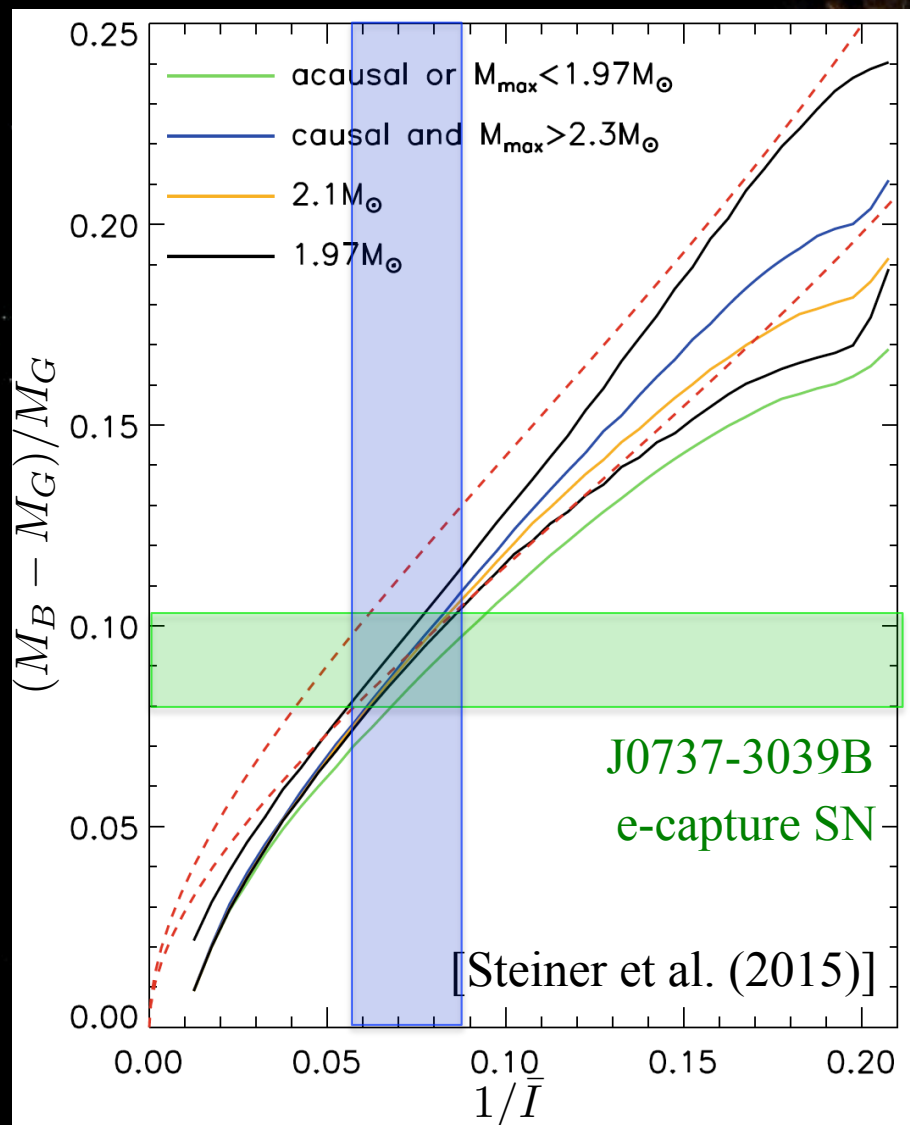
- ✓ **small mass loss** $\lesssim 0.01 M_{\odot}$

$M_G = 1.25 M_{\odot}$  [Podsiadlowski et al. (2005),
Kitaura et al. (2006)]

baryon mass: $M_B \approx [1.366, 1.377] M_{\odot}$

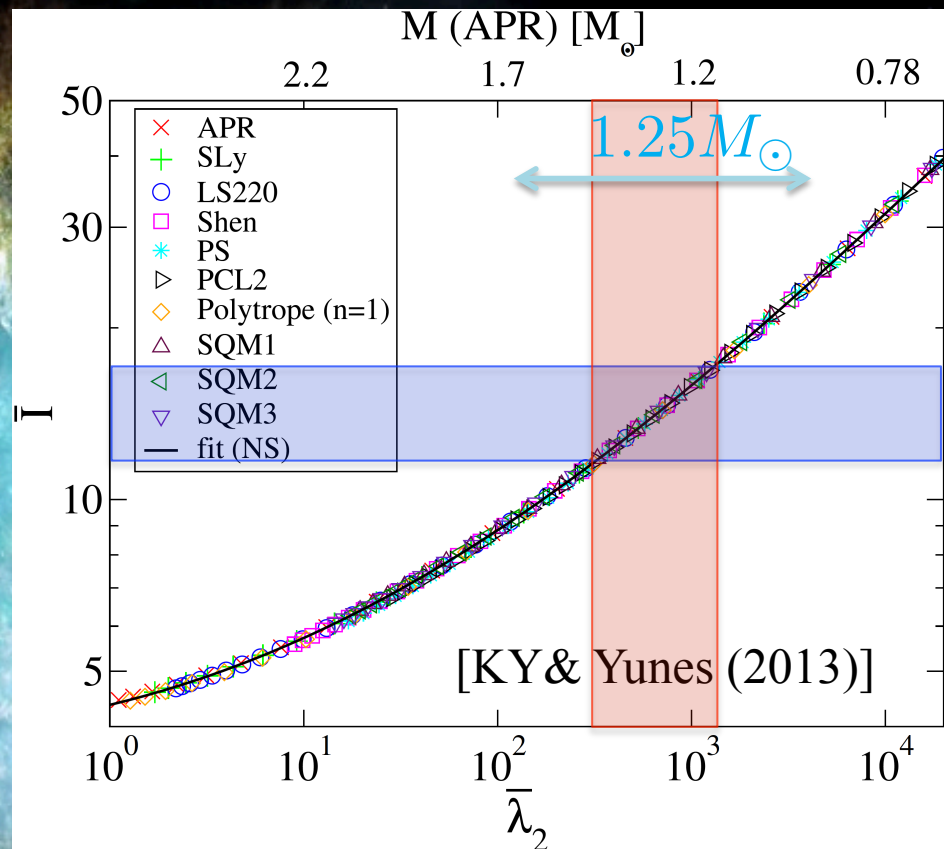
Supernova Scenario

binding energy vs moment of inertia



[Newton, Steiner & KY (2016)]

moment of inertia vs tidal deformability

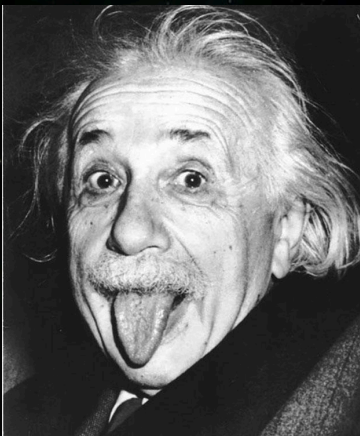


GW **tidal** measurement
can probe **formation**
scenario of NSs!

Outline

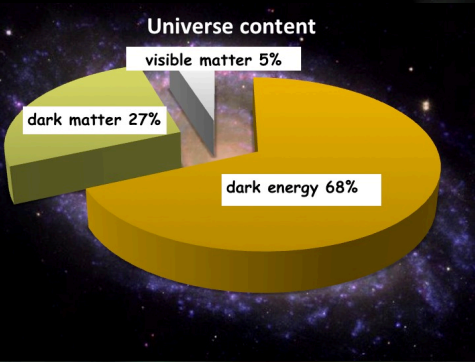
Astrophysics

Gravitational
Physics



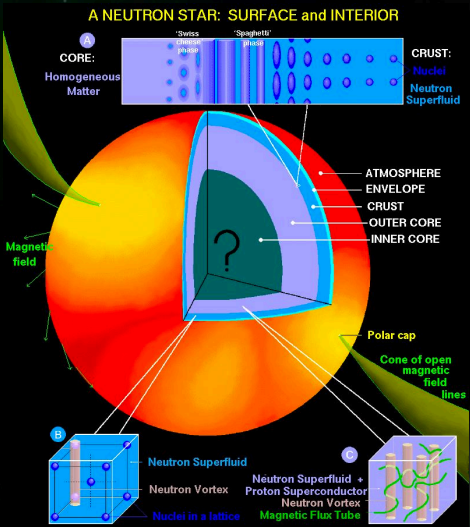
Universal Relations

review article [KY & Yunes, Phys. Rept. (2017)]



Cosmology

Nuclear Physics

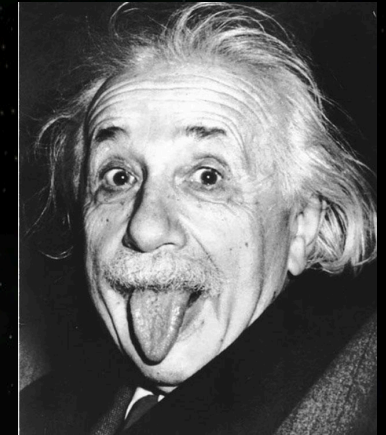


Outline

Astrophysics



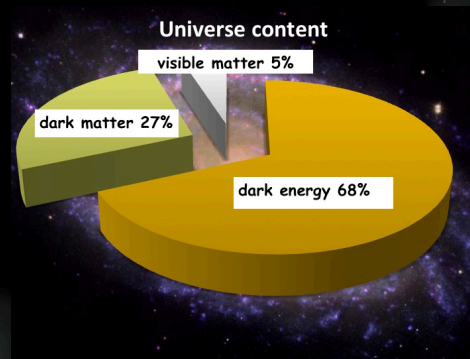
Gravitational
Physics



Universal Relations

review article [KY & Yunes, Phys. Rept. (2017)]

- ✓ Binary NS inspiral
- ✓ Binary NS post-merger



Nuclear Physics

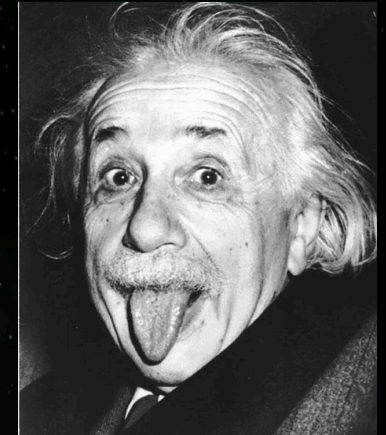
Cosmology

Outline

Astrophysics



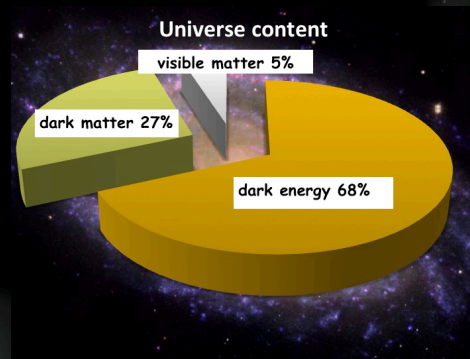
Gravitational
Physics



Universal Relations

review article [KY & Yunes, Phys. Rept. (2017)]

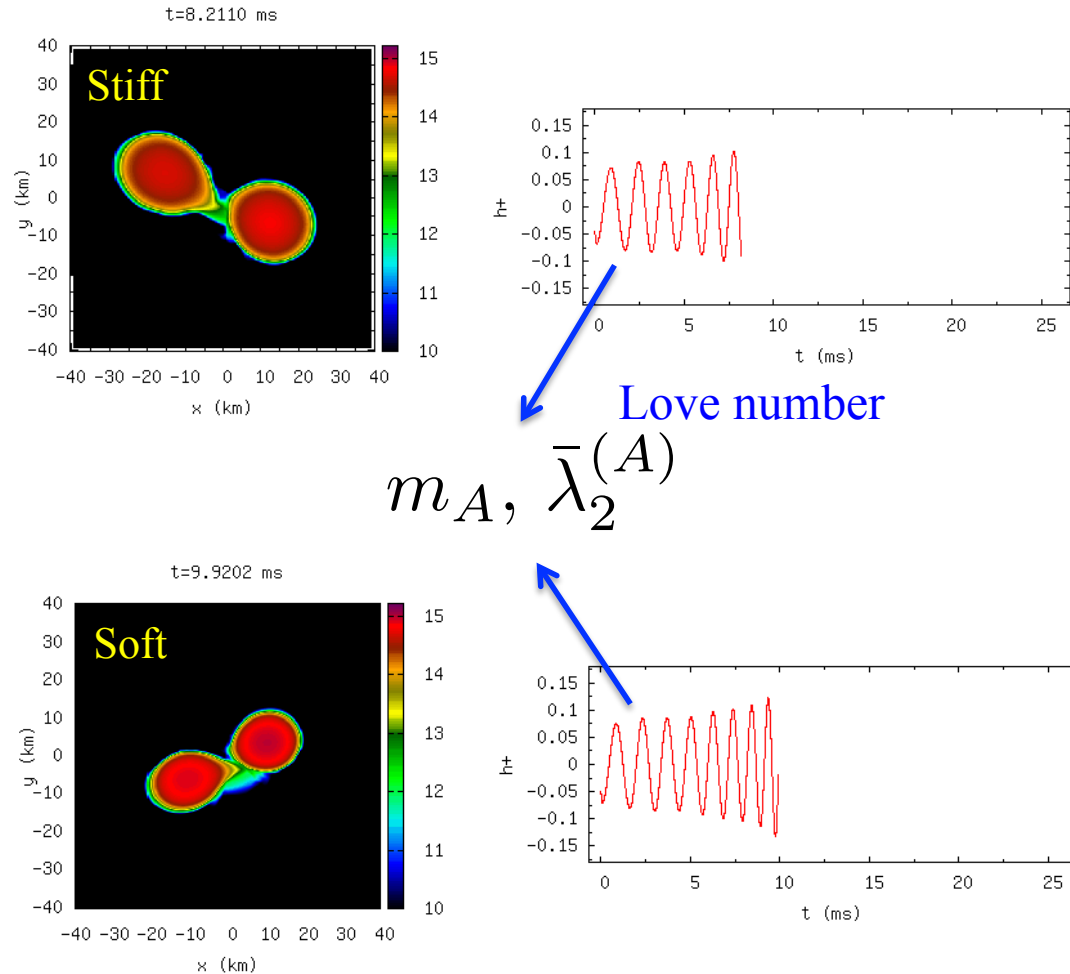
- ✓ Binary NS inspiral
- ✓ Binary NS post-merger



Nuclear Physics

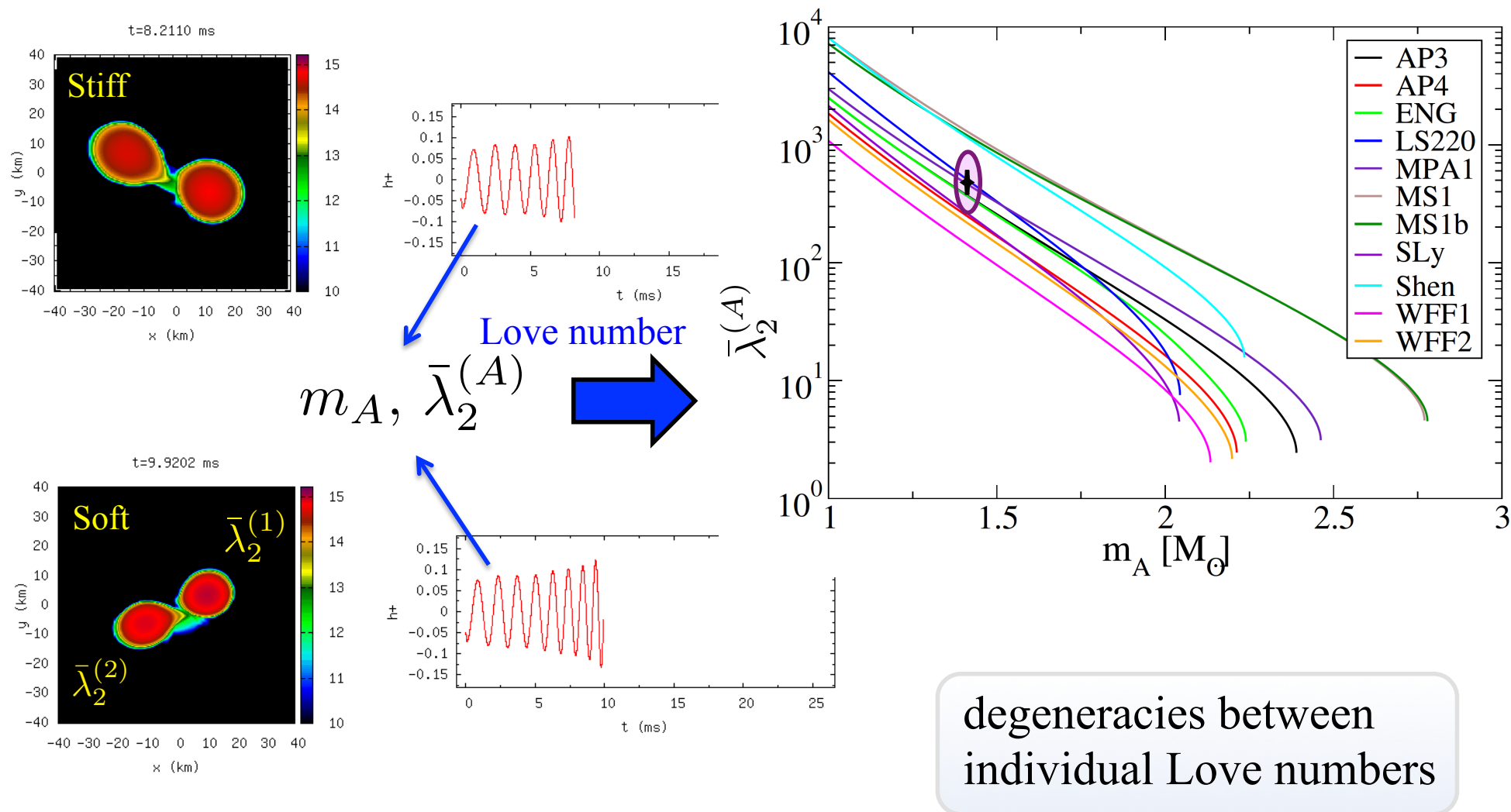
Cosmology

GW Nuclear Astrophysics



Simulations by Kenta Hotokezaka

GW Nuclear Astrophysics



Simulations by Kenta Hotokezaka

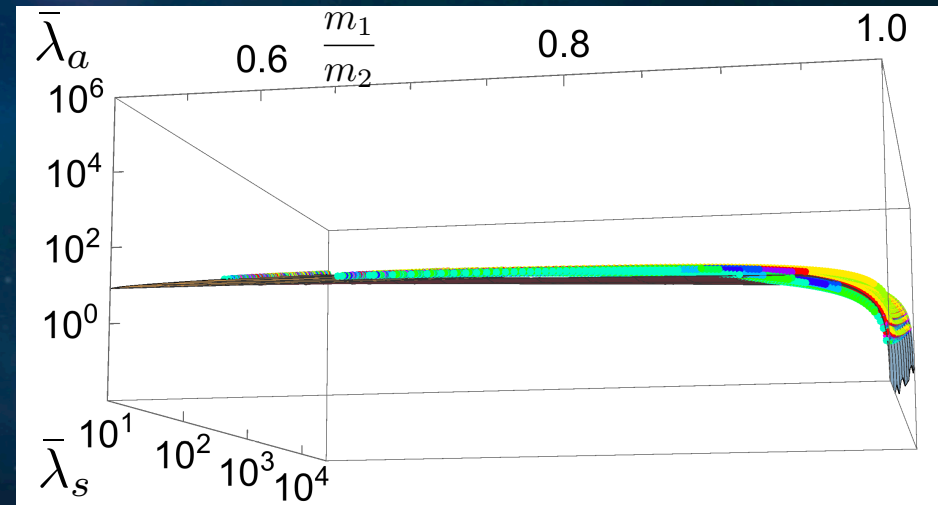
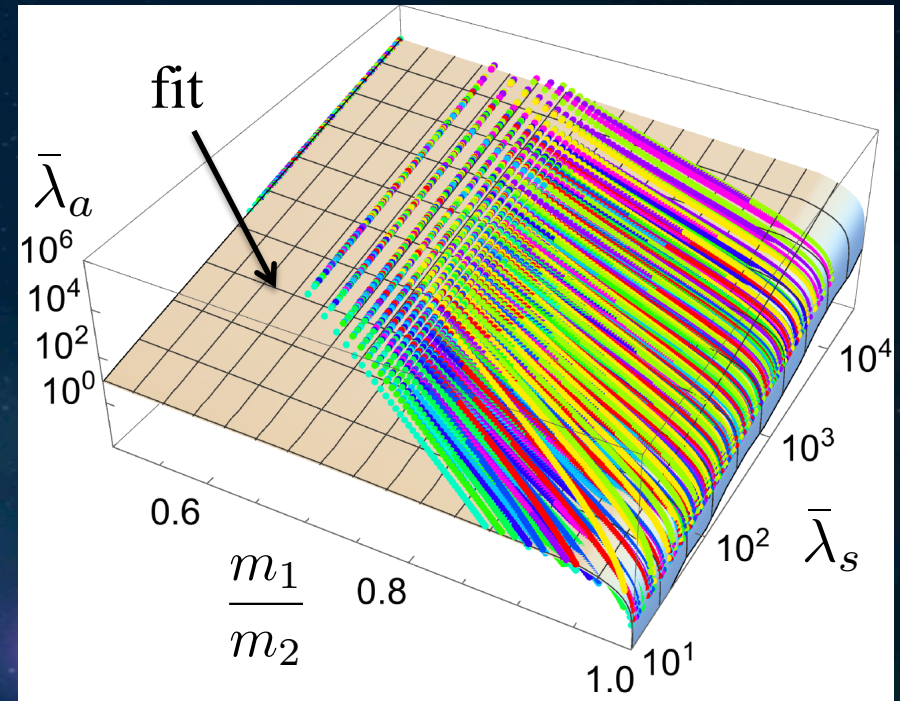
Binary Love Relations

symmetric/anti-symmetric

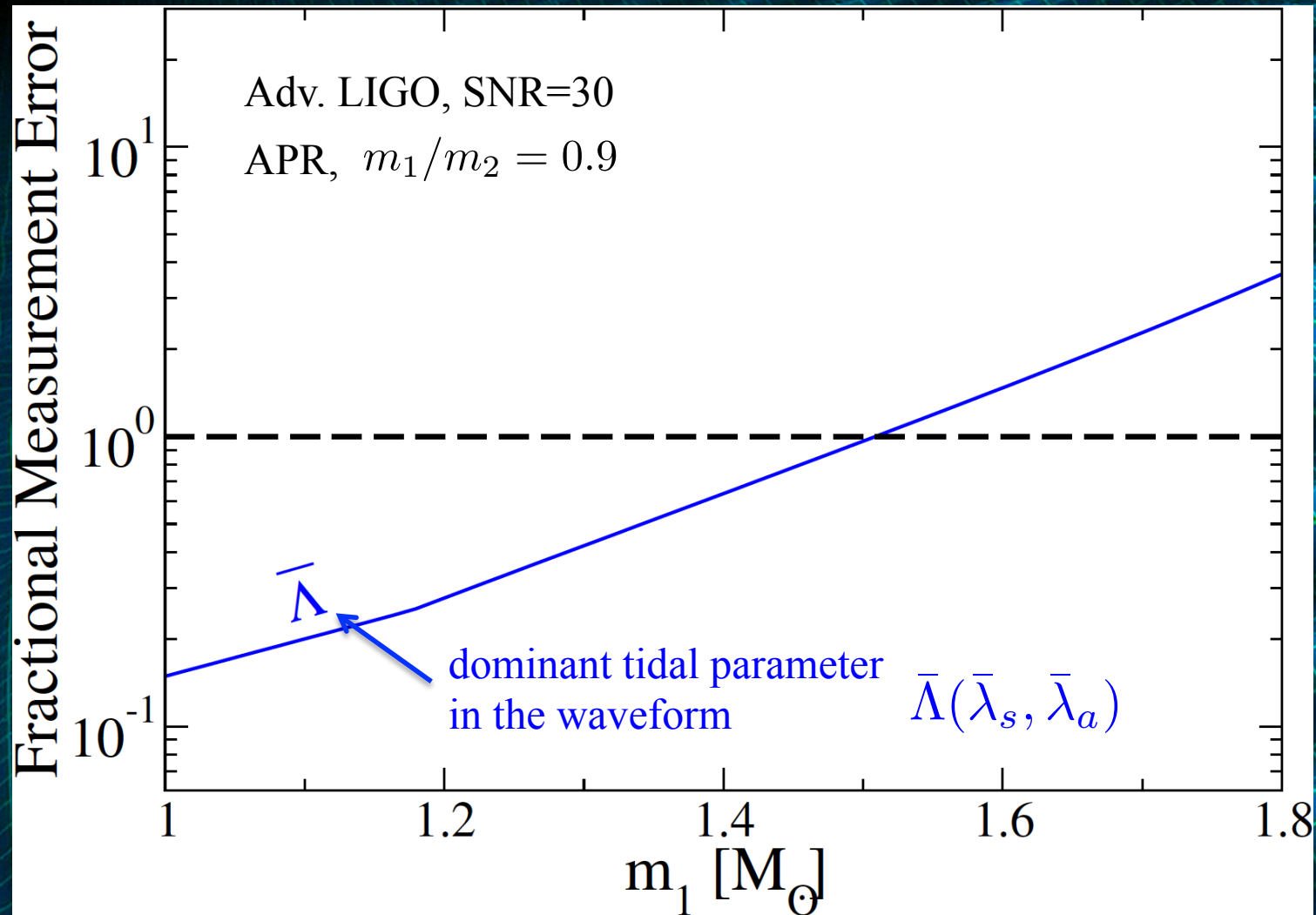
$$\bar{\lambda}_s = \frac{\bar{\lambda}_2^{(1)} + \bar{\lambda}_2^{(2)}}{2}, \quad \bar{\lambda}_a = \frac{\bar{\lambda}_2^{(1)} - \bar{\lambda}_2^{(2)}}{2}$$



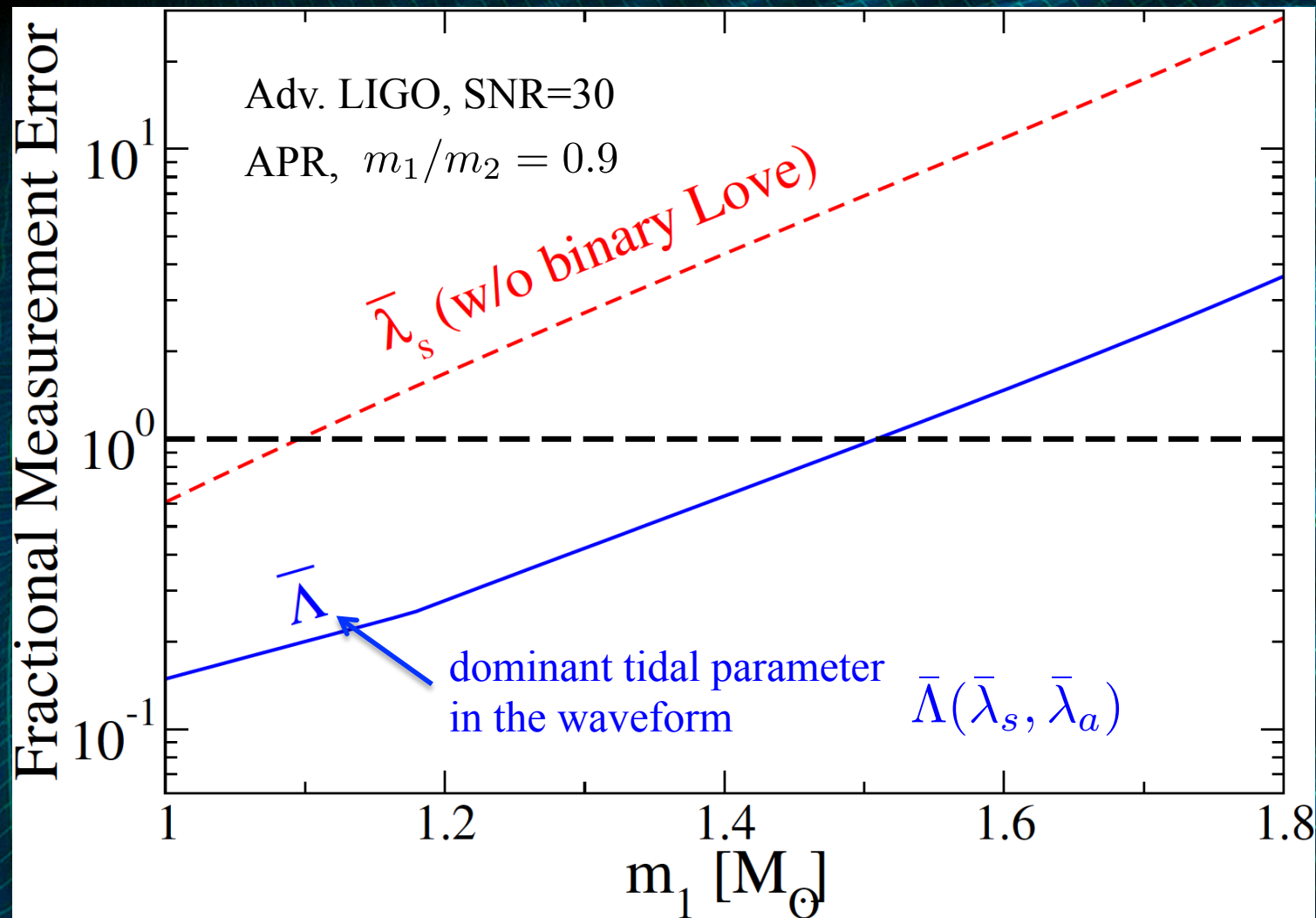
Universal to $\mathcal{O}(10\%)$



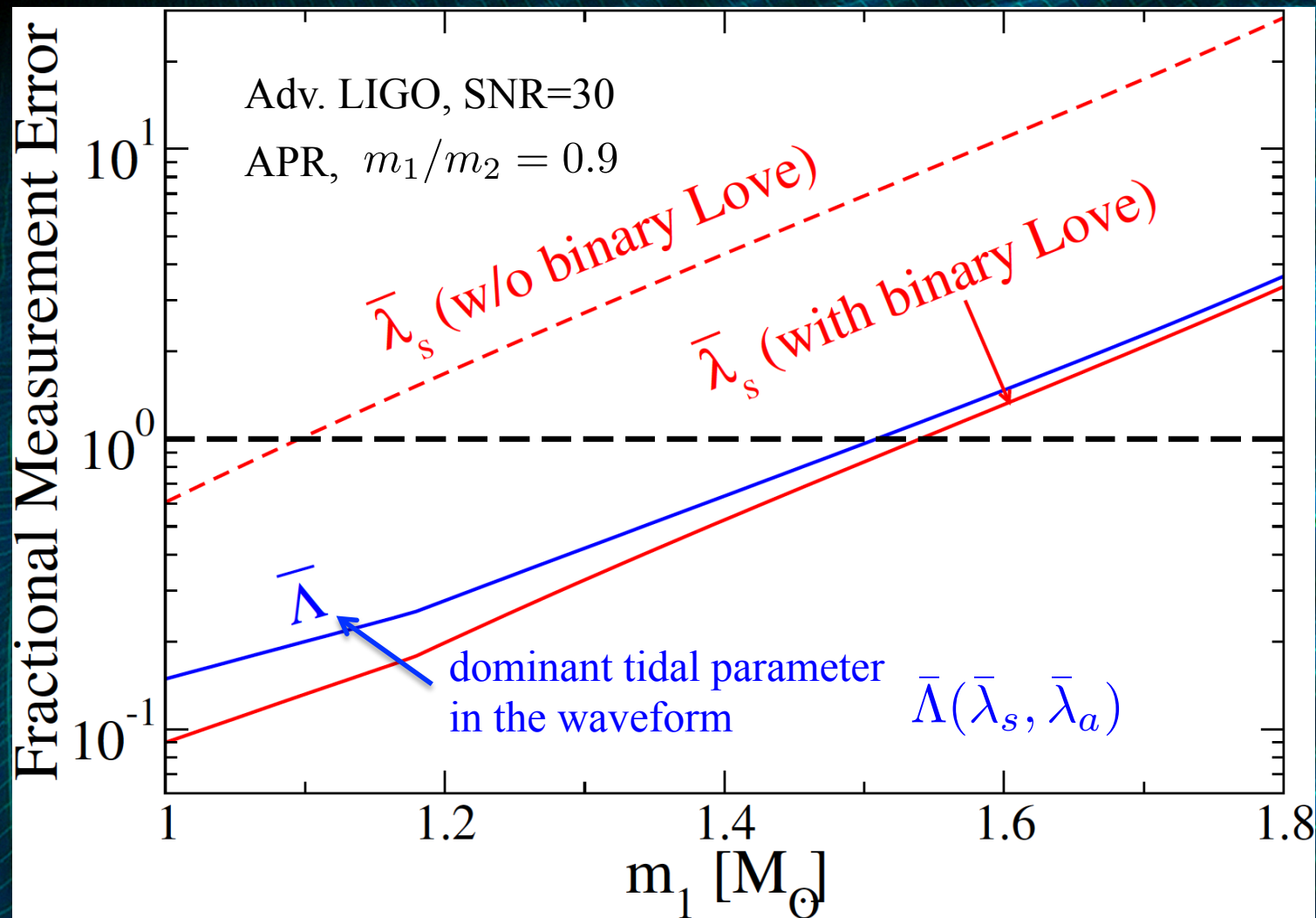
Impact of Binary Love Relations



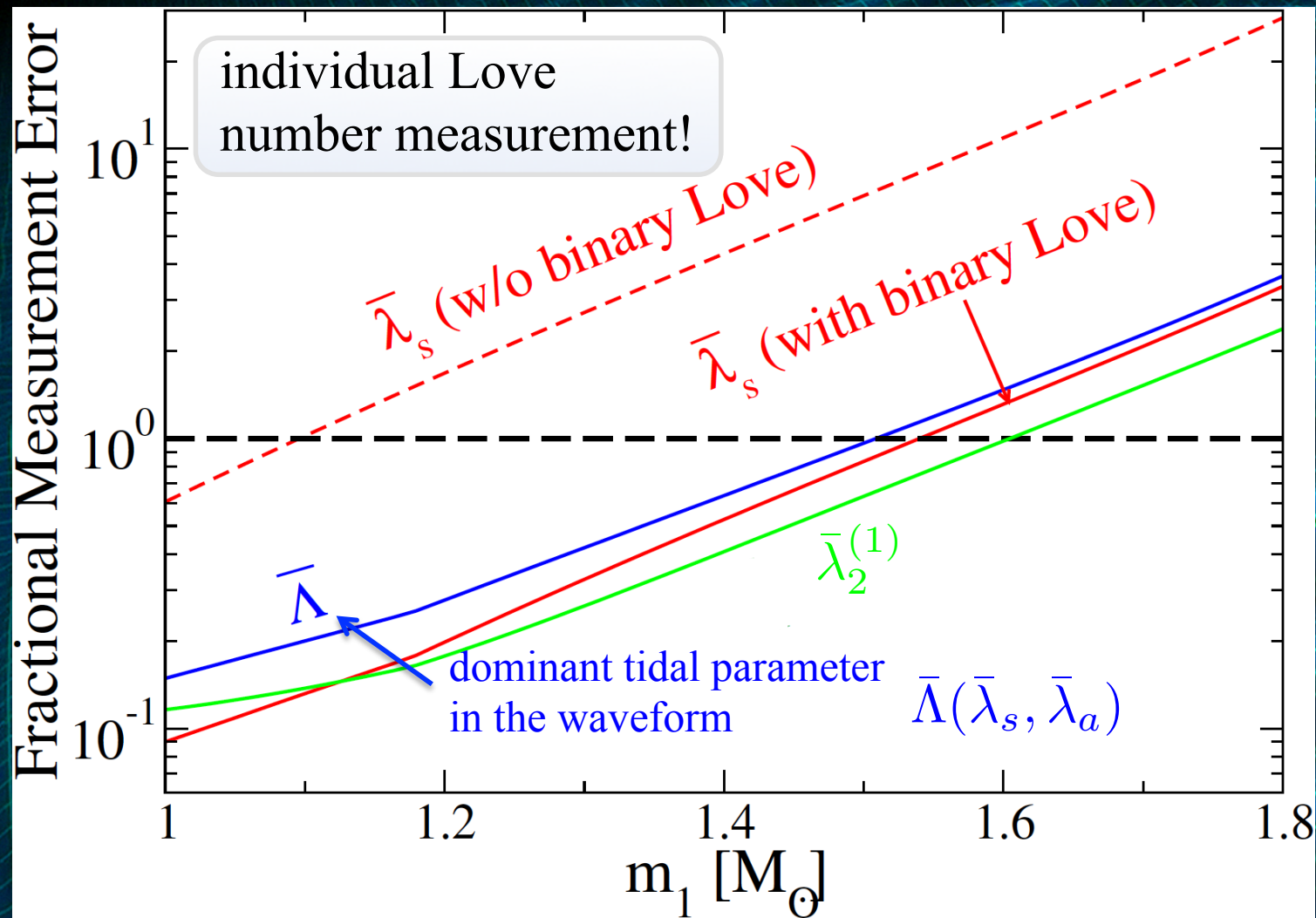
Impact of Binary Love Relations



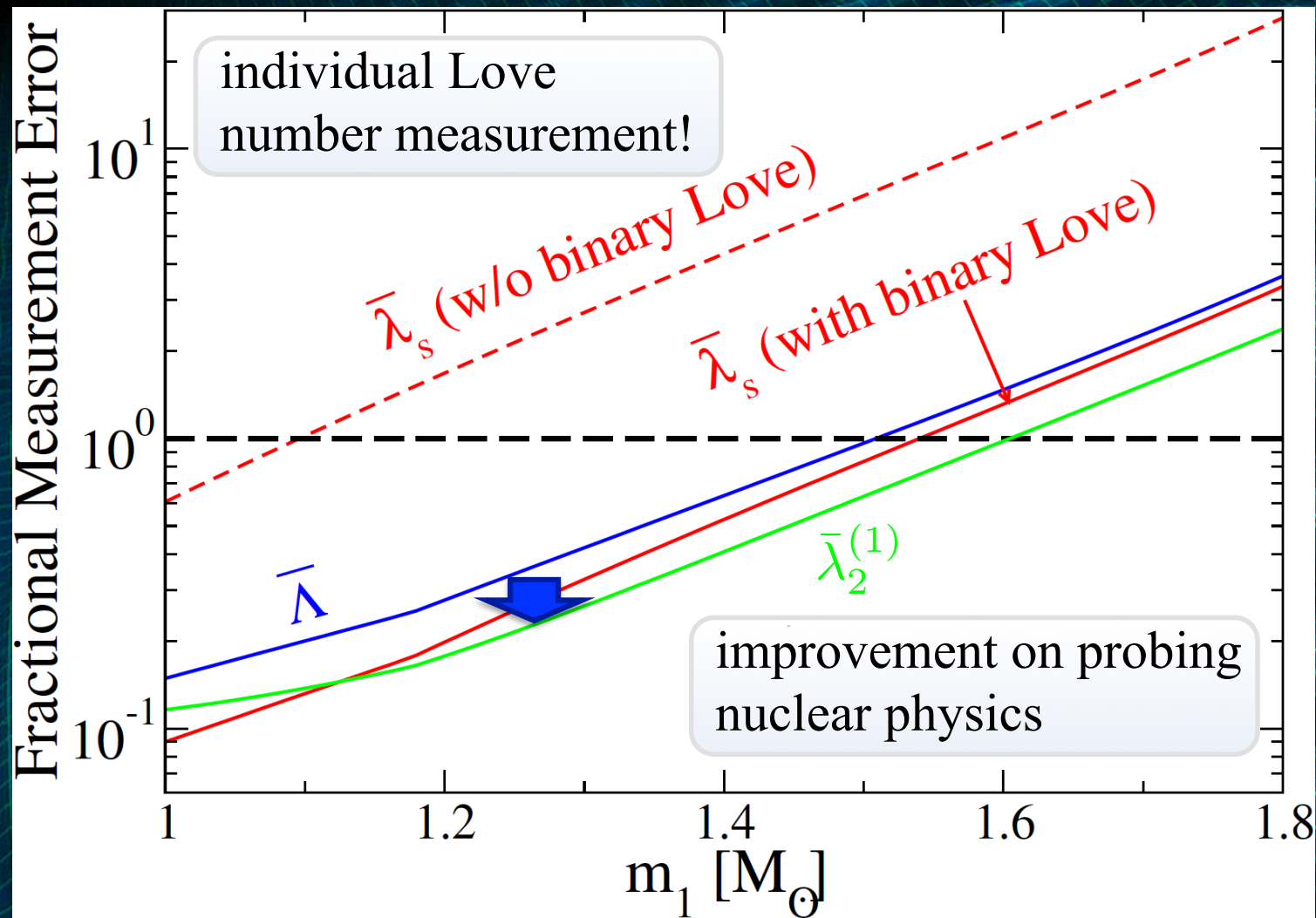
Impact of Binary Love Relations



Impact of Binary Love Relations



Impact of Binary Love Relations

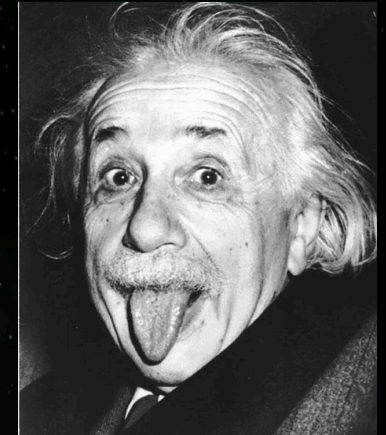


Outline

Astrophysics



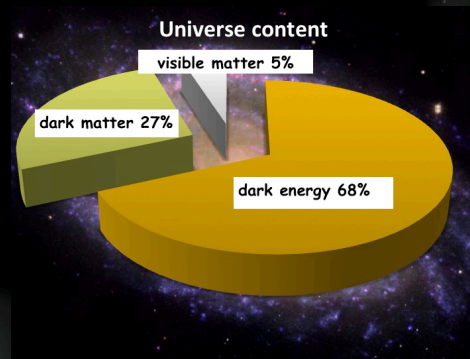
Gravitational
Physics



Universal Relations

review article [KY & Yunes, Phys. Rept. (2017)]

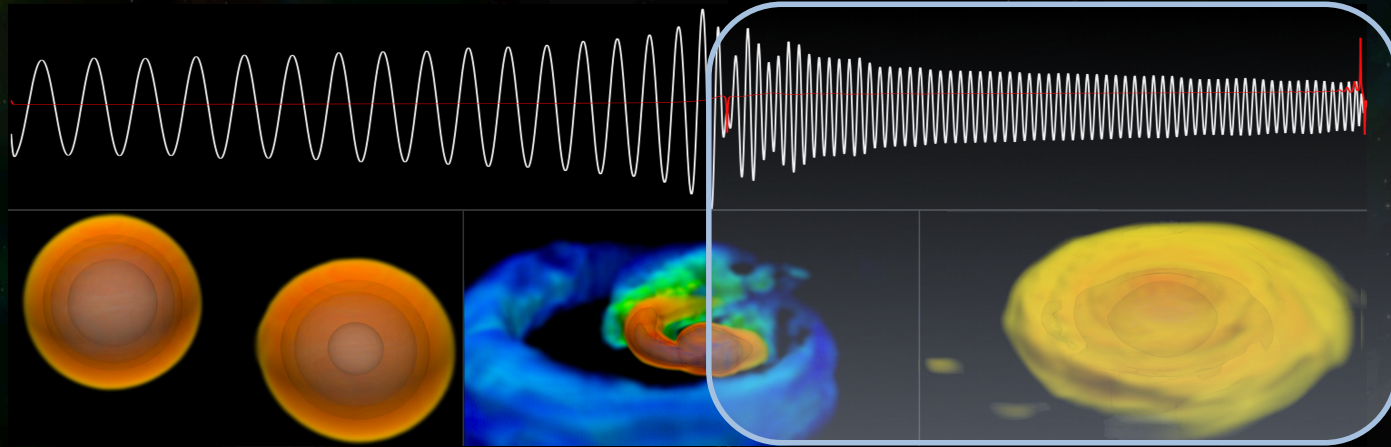
- ✓ Binary NS inspiral
- ✓ Binary NS post-merger



Nuclear Physics

Cosmology

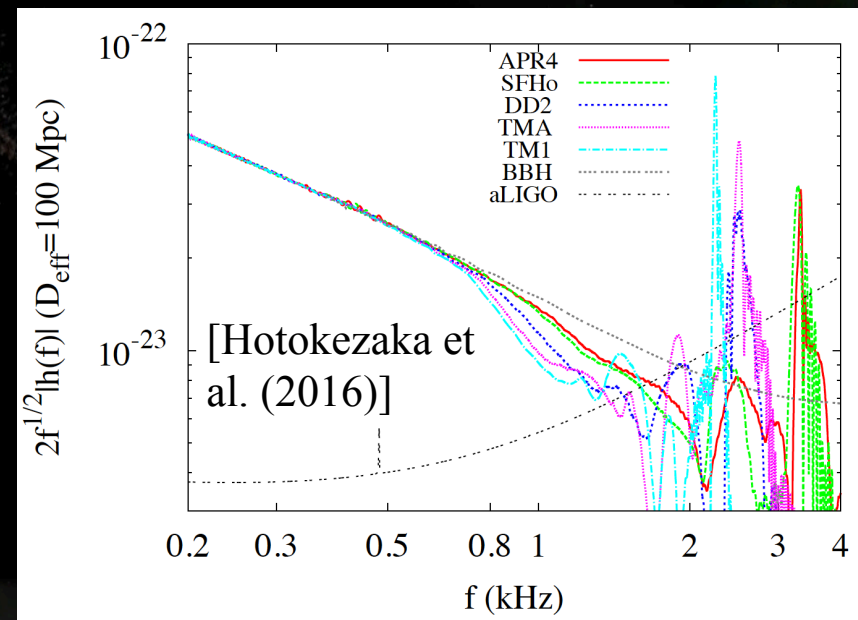
Probing Nuclear Physics with Post-merger GWs



- Contains rich information on **nuclear physics**
- Detection is challenging
- **Coherently stack multiple events!**

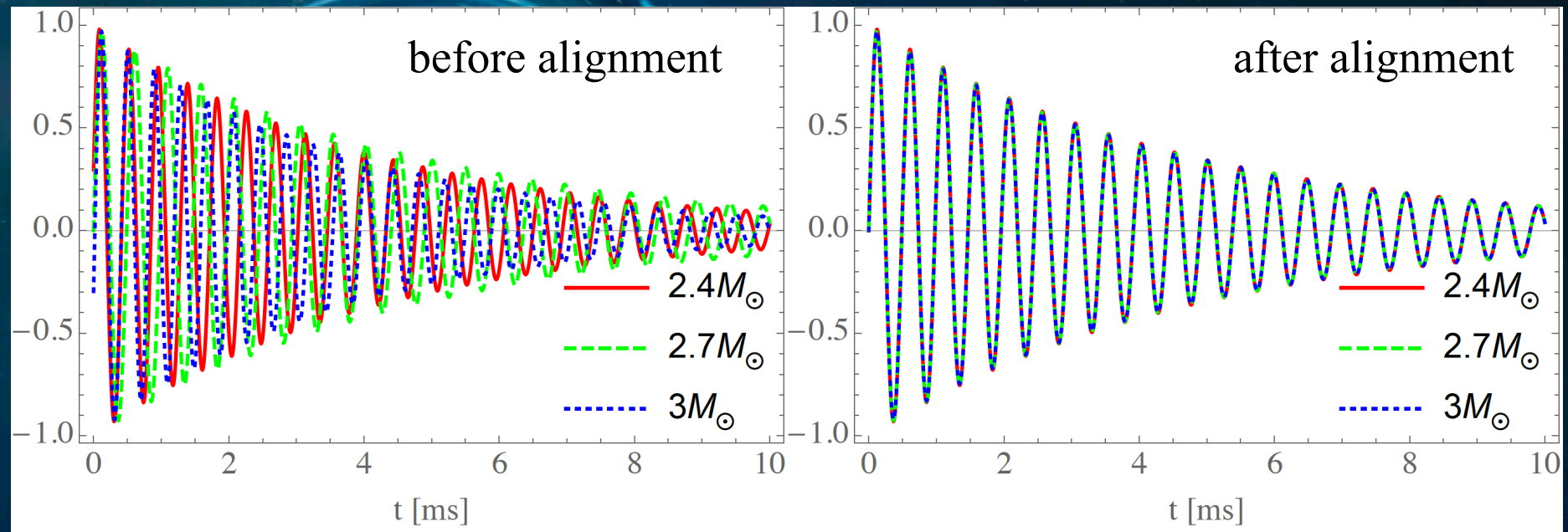
[Bose et al. (2017)]

[Yang, Paschalidis, KY et al. (in prep.)]



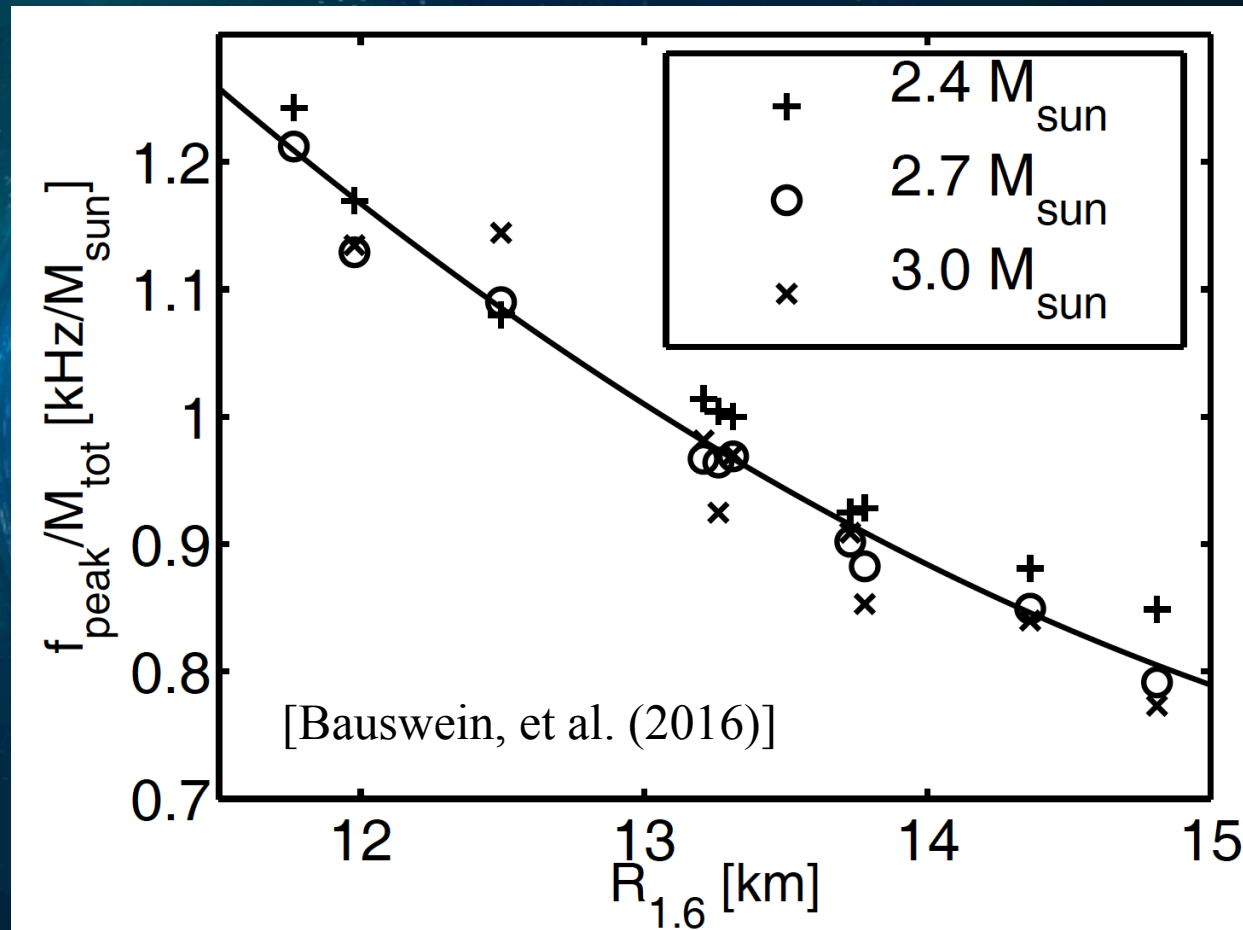
Coherent Mode Stacking [Yang, Paschalidis, KY et al. (in prep.)]

Phase alignment is crucial!



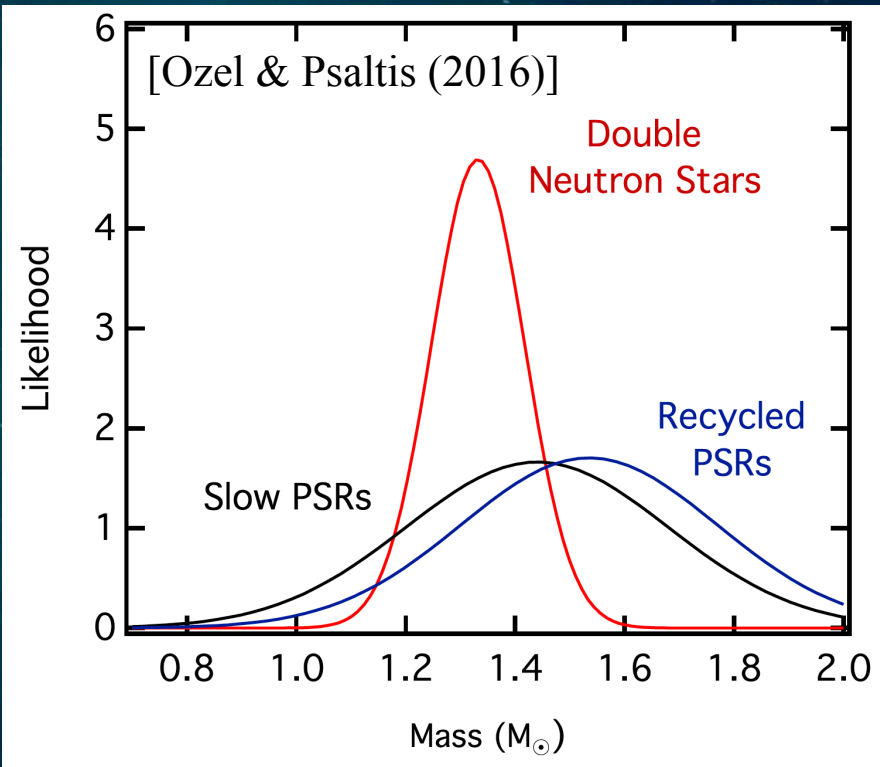
Coherent Mode Stacking [Yang, Paschalidis, KY et al. (in prep.)]

Align frequency with **universal relation!**

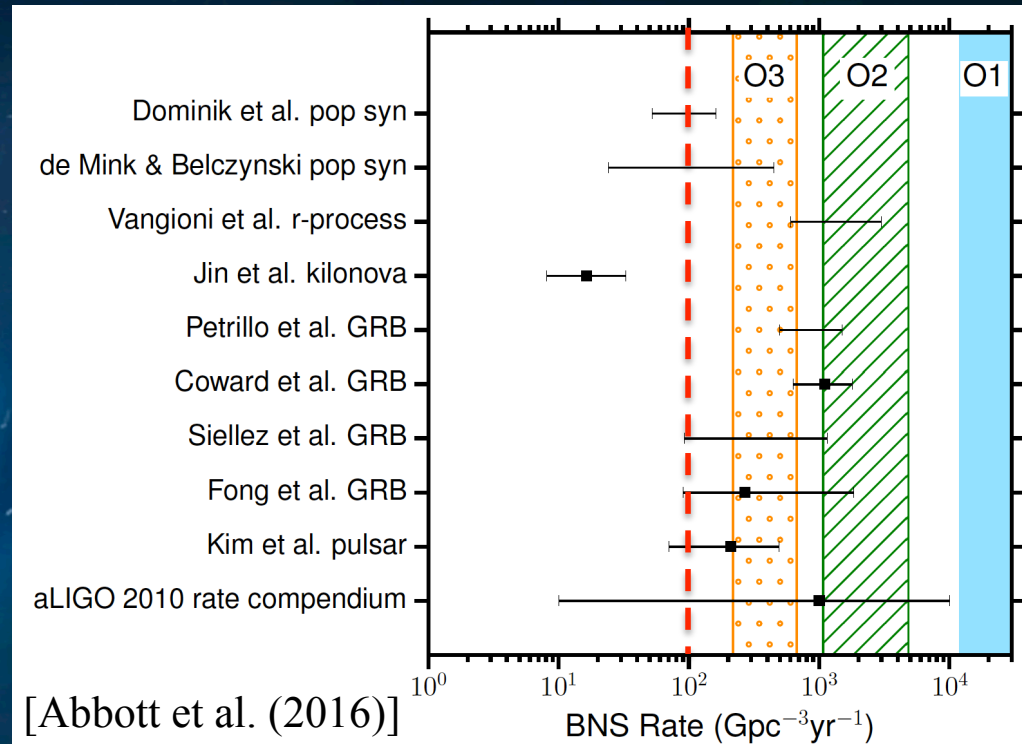


Monte Carlo Simulations [Yang, Paschalidis, KY et al. (in prep.)]

mass distribution



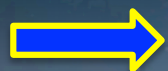
merger rate



SNR reduction due to phase misalignment caused by measurement uncertainties in the constant phase offset

$$\delta\phi \sim \frac{1}{\text{SNR}}$$

difficult to detect post-merger GWs with aLIGO even after stacking

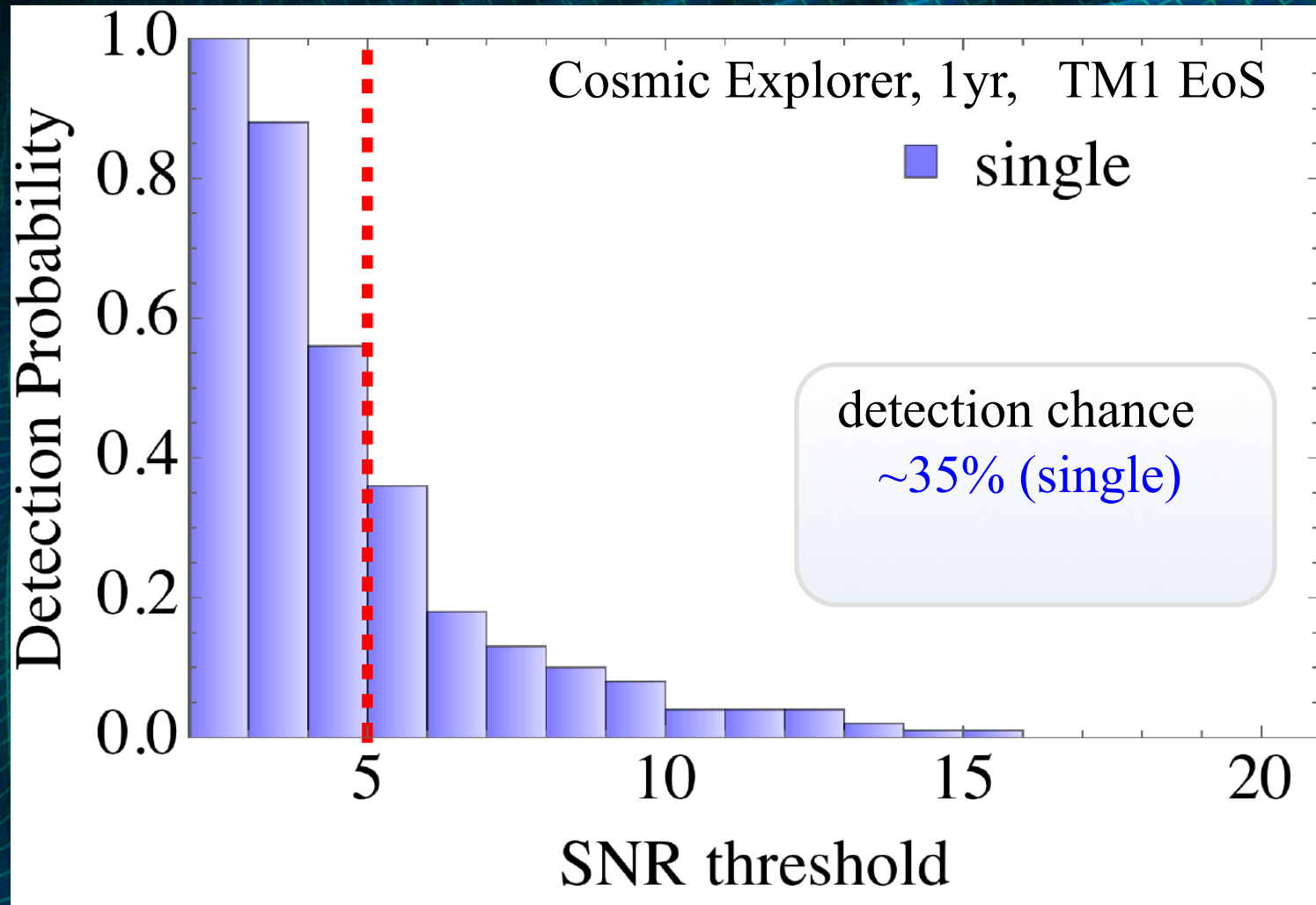


need 3rd generation detectors like Cosmic Explorer

Single vs Stacking

[Yang, Paschalidis, KY et al. (in prep.)]

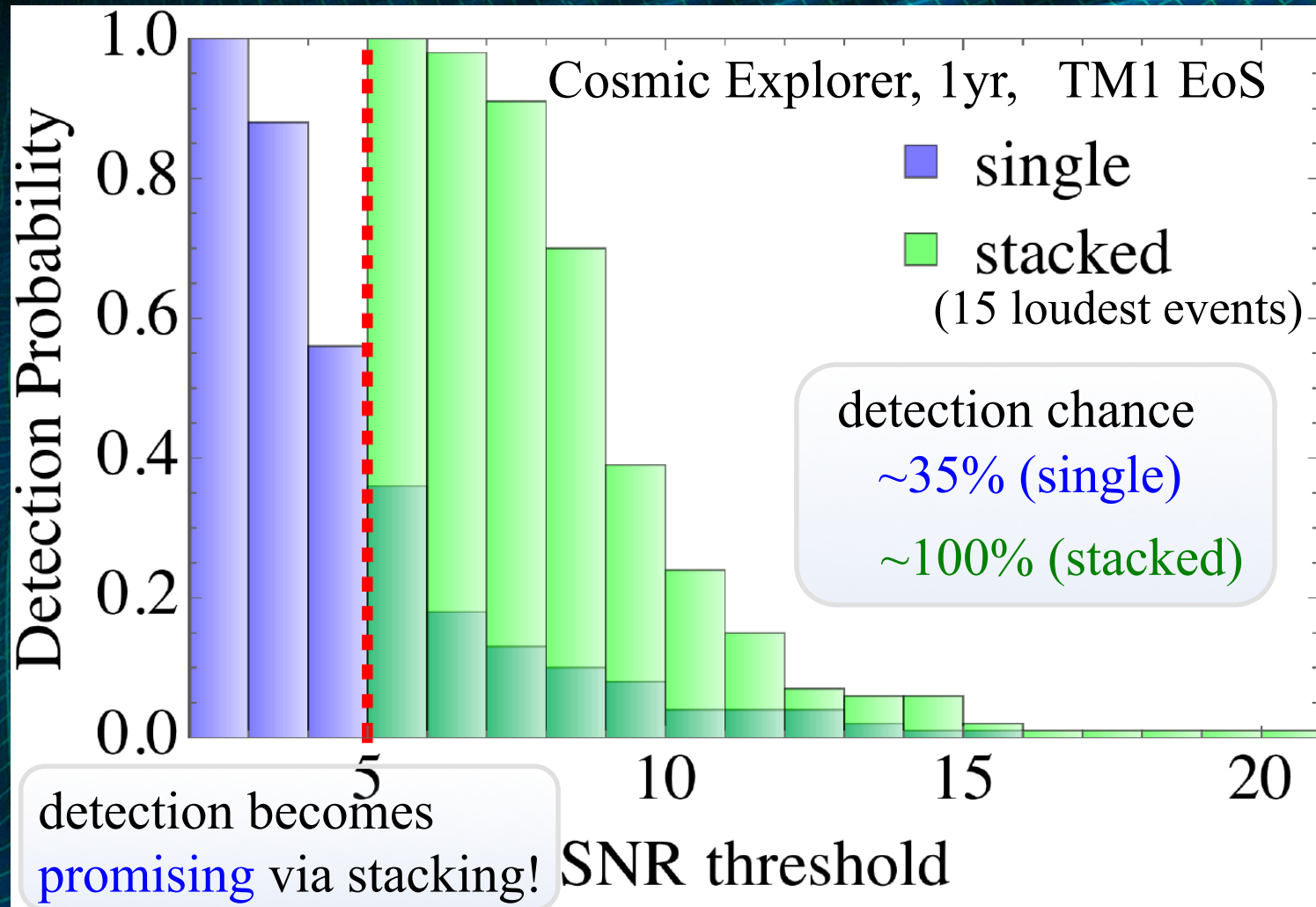
detection probability of post-merger GWs



Single vs Stacking

[Yang, Paschalidis, KY et al. (in prep.)]

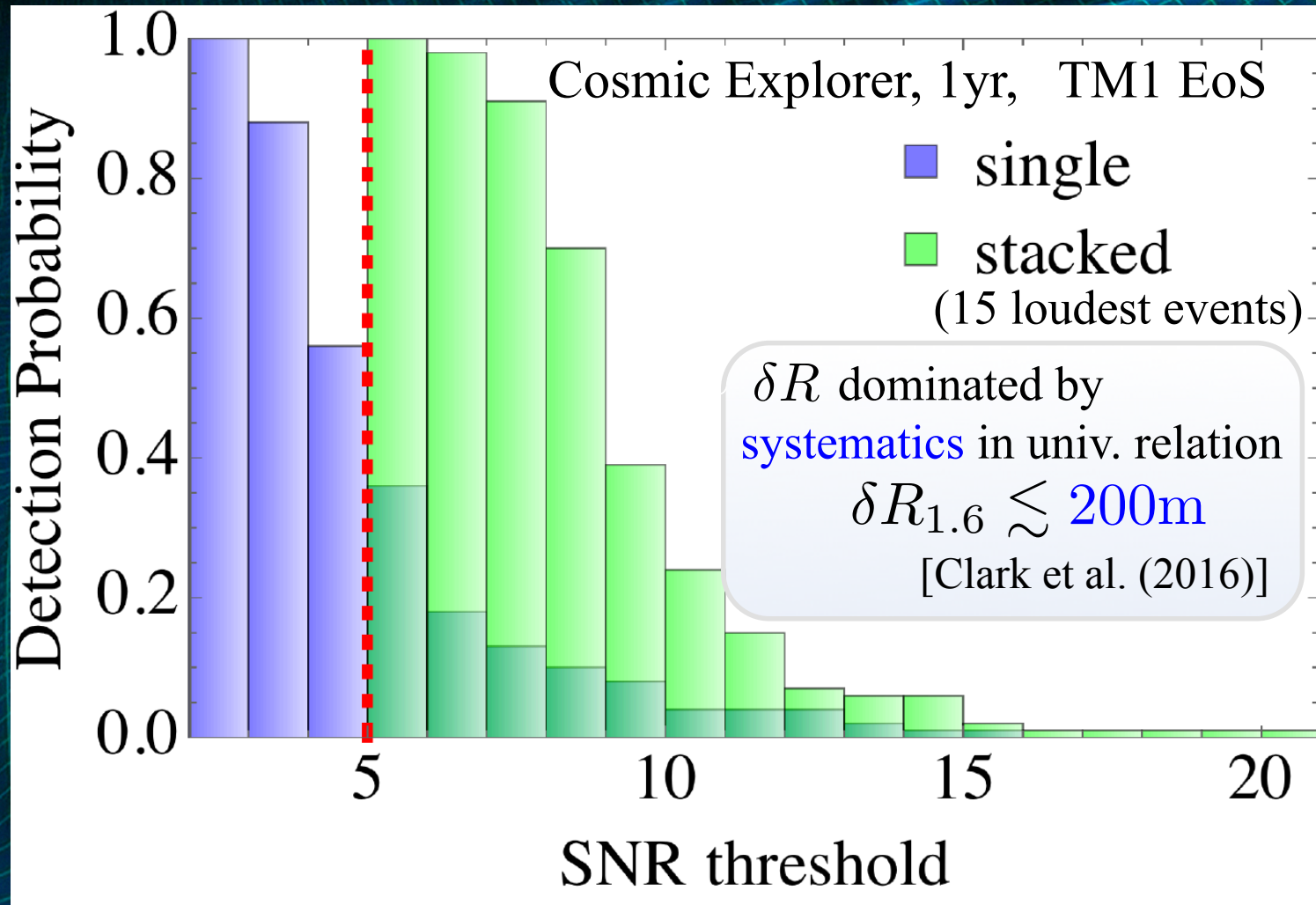
detection probability of post-merger GWs



Single vs Stacking

[Yang, Paschalidis, KY et al. (in prep.)]

detection probability of post-merger GWs

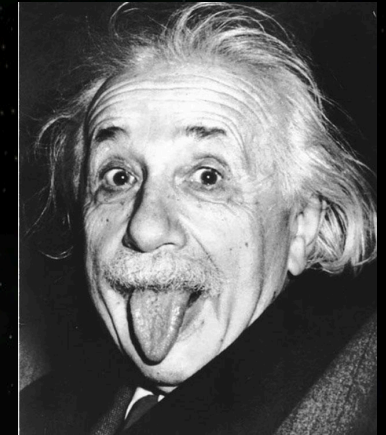


Outline

Astrophysics

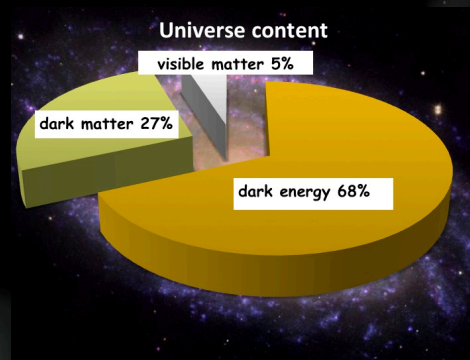
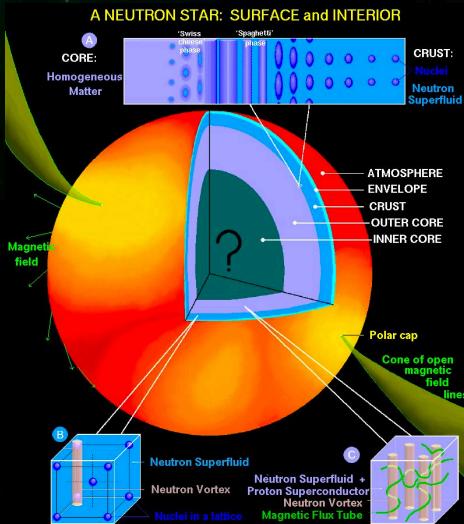


Gravitational
Physics



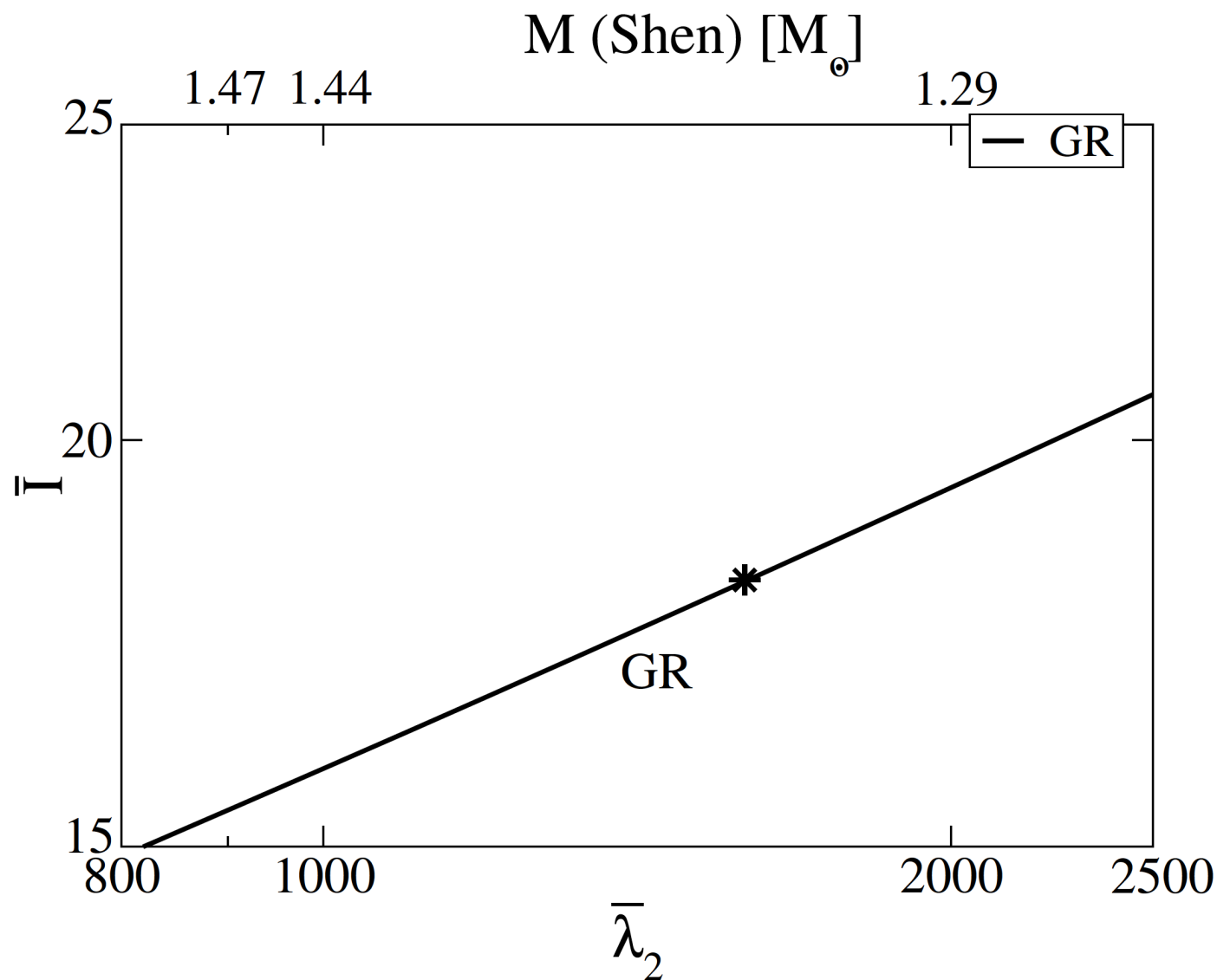
Universal Relations

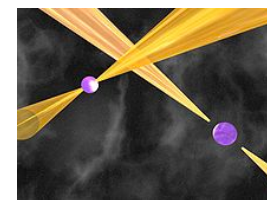
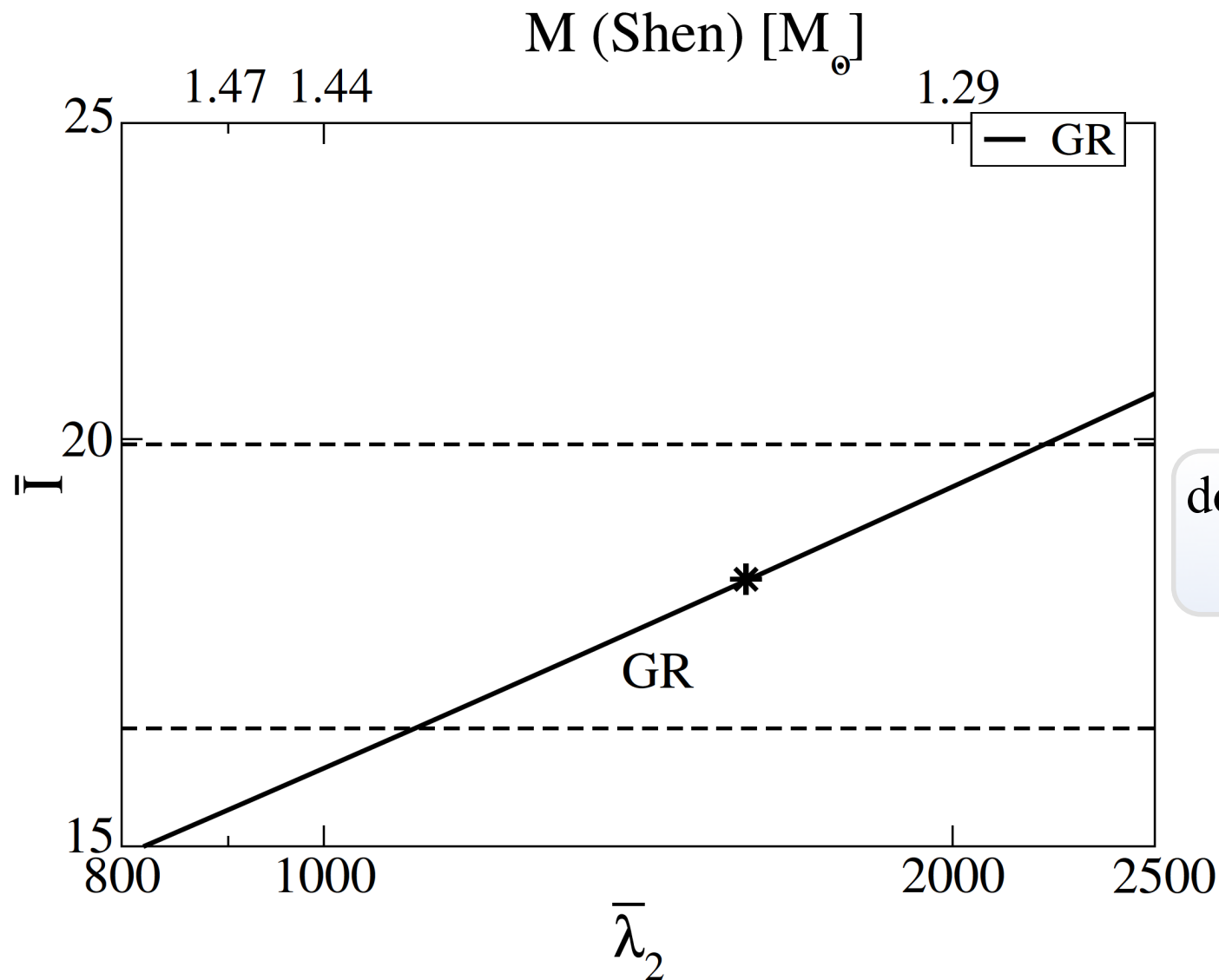
review article [KY & Yunes, Phys. Rept. (2017)]



Nuclear Physics

Cosmology

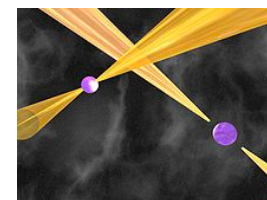
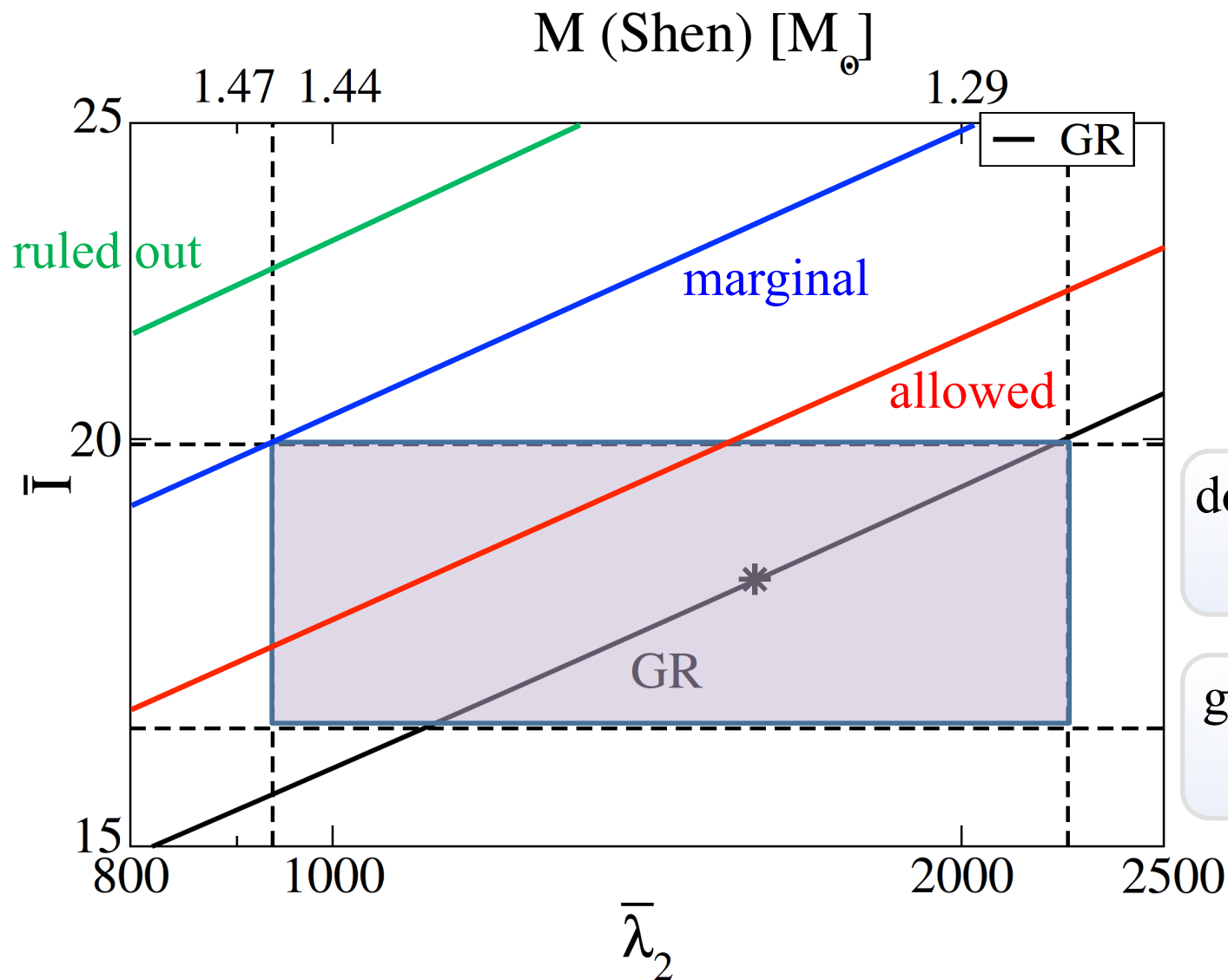




double binary pulsar
 $\Delta \bar{I} / \bar{I} = 10\%$

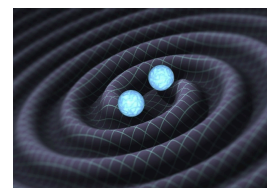
Strong Gravity Tests

[KY & Yunes, Science 341 365 (2013)]



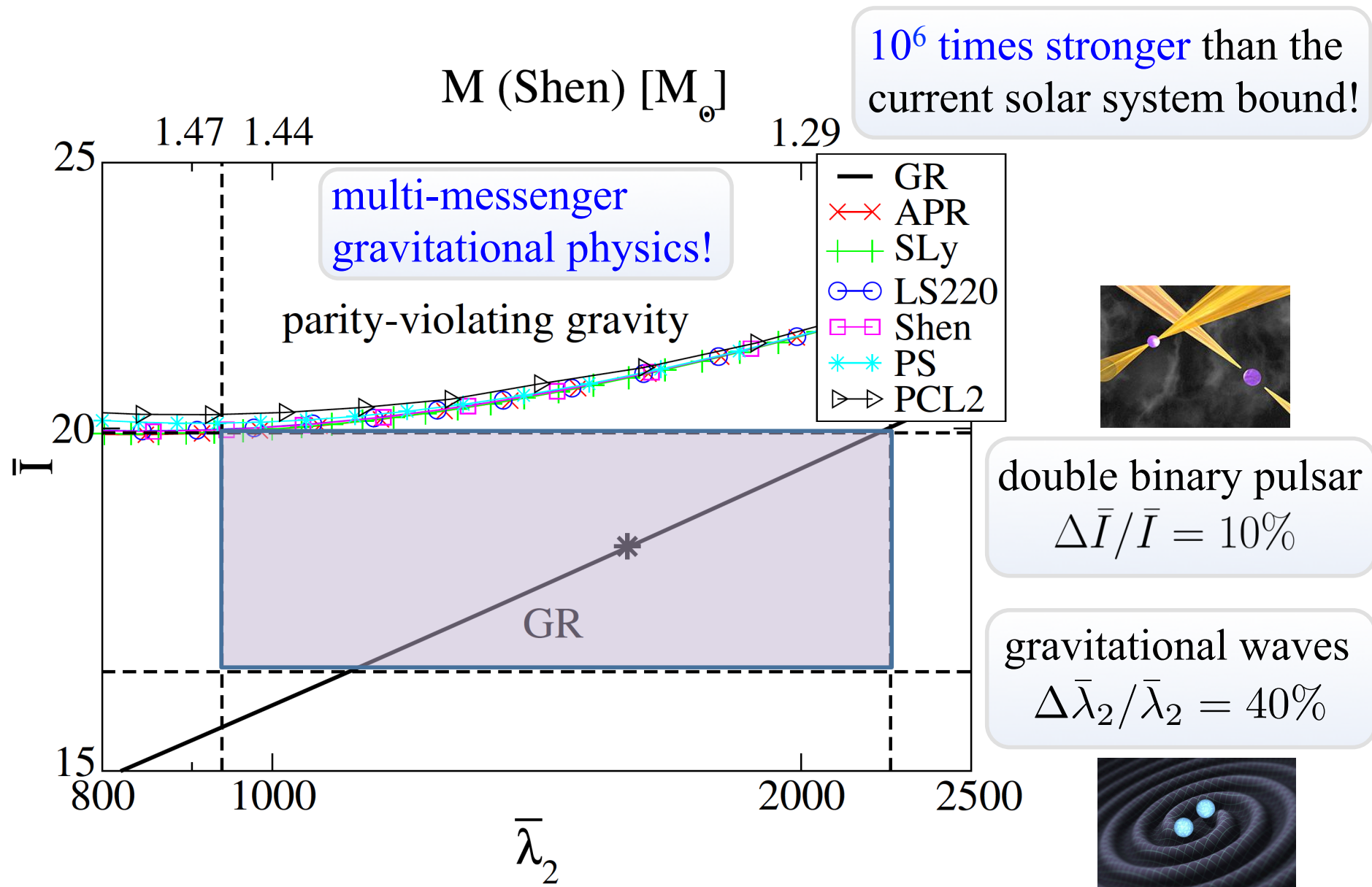
double binary pulsar
 $\Delta \bar{I} / \bar{I} = 10\%$

gravitational waves
 $\Delta \bar{\lambda}_2 / \bar{\lambda}_2 = 40\%$



Strong Gravity Tests

[KY & Yunes, Science 341 365 (2013)]



I-Love-Q in Modified Theories of Gravity

Modified Theories of Gravity

- ✓ (massless) scalar-tensor
[Pani & Berti (2014)]
- ✓ (massive) scalar-tensor
[Doneva & Yazadjiev (2016)]
- ✓ $f(R)$
[Doneva et al. (2015)]
- ✓ Einstein-dilaton Gauss-Bonnet
[Kleihaus et al. (2014, 2016)]
- ✓ dynamical Chern-Simons
[Yagi & Yunes (2013)]
- ✓ Eddington-inspired Born-Infeld
[Sham et al. (2014)]

Exotic Compact Objects

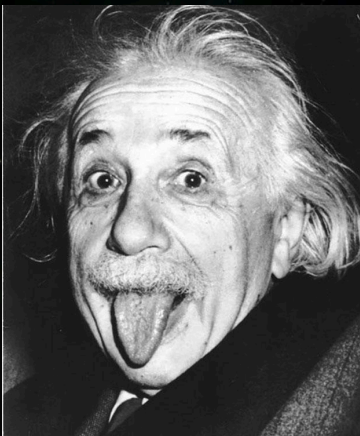
- ✓ boson star / dark star
[Maselli et al. (2017)]
- ✓ gravastar
[Pani (2015),
Uchikata et al. (2016)]



Outline

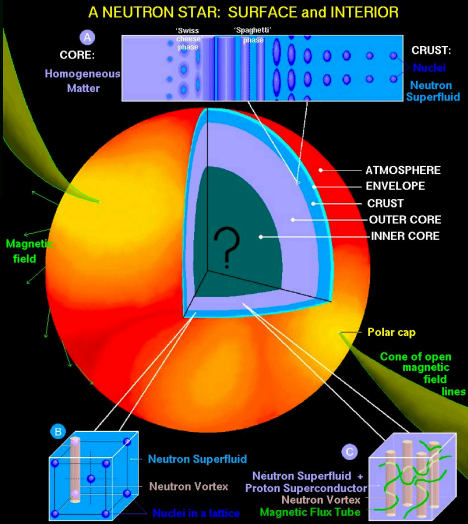
Astrophysics

Gravitational
Physics

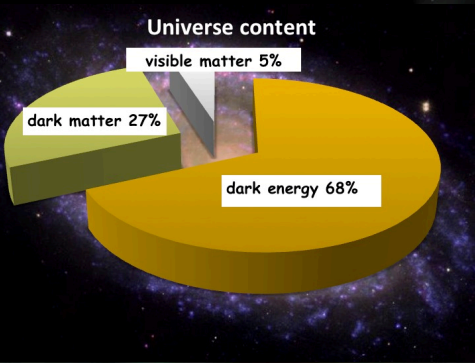


Universal Relations

review article [KY & Yunes, Phys. Rept. (2017)]



Nuclear Physics



Cosmology

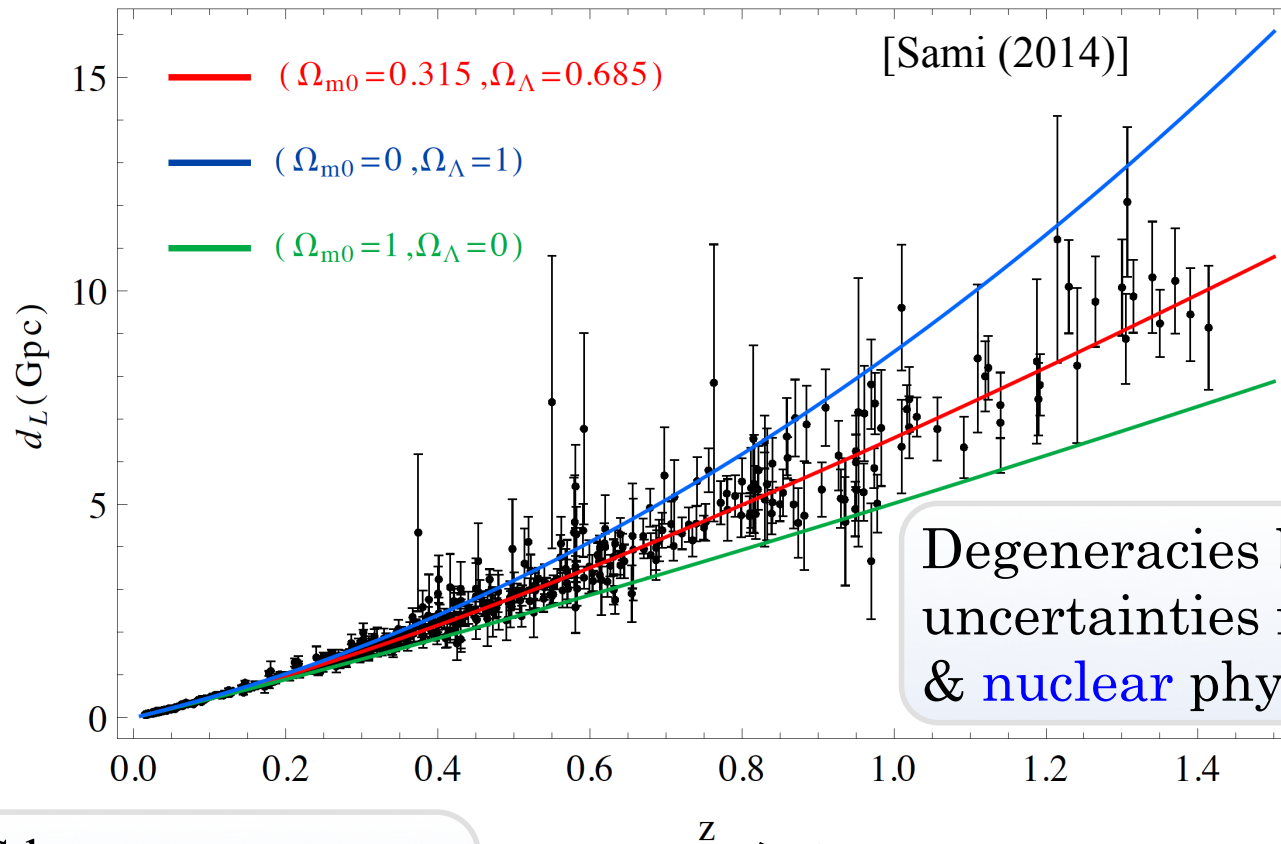
GW Cosmology

[Messenger & Read (2012)]

type Ia SNe → standard candles

NS/NSs → standard sirens

GW
amplitude



Degeneracies between
uncertainties in **cosmology**
& **nuclear** physics

Correct EoS known

→ Break the degeneracy
between mass and z

→ $m(1+z)$
 $\bar{\lambda}_2(m, \text{EoS})$

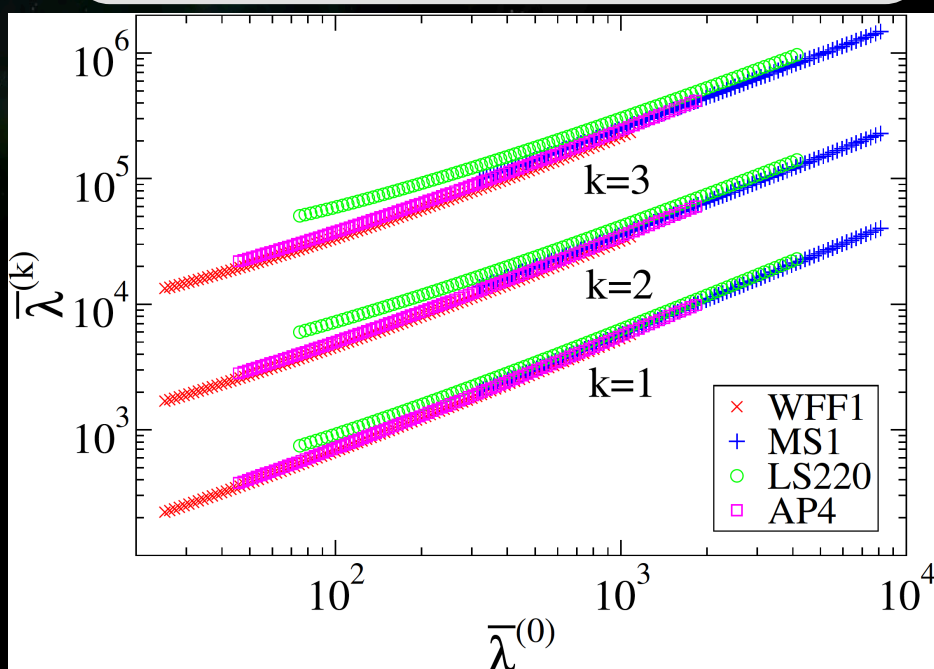
Perfect knowledge of EoS...?

Taylor expanded tidal deformability

[Messenger & Read (2012)]

fiducial mass

$$\bar{\lambda}_2(m) = \sum_{k=0} \frac{\bar{\lambda}^{(k)}}{k!} \left(1 - \frac{m}{m_0}\right)^k$$

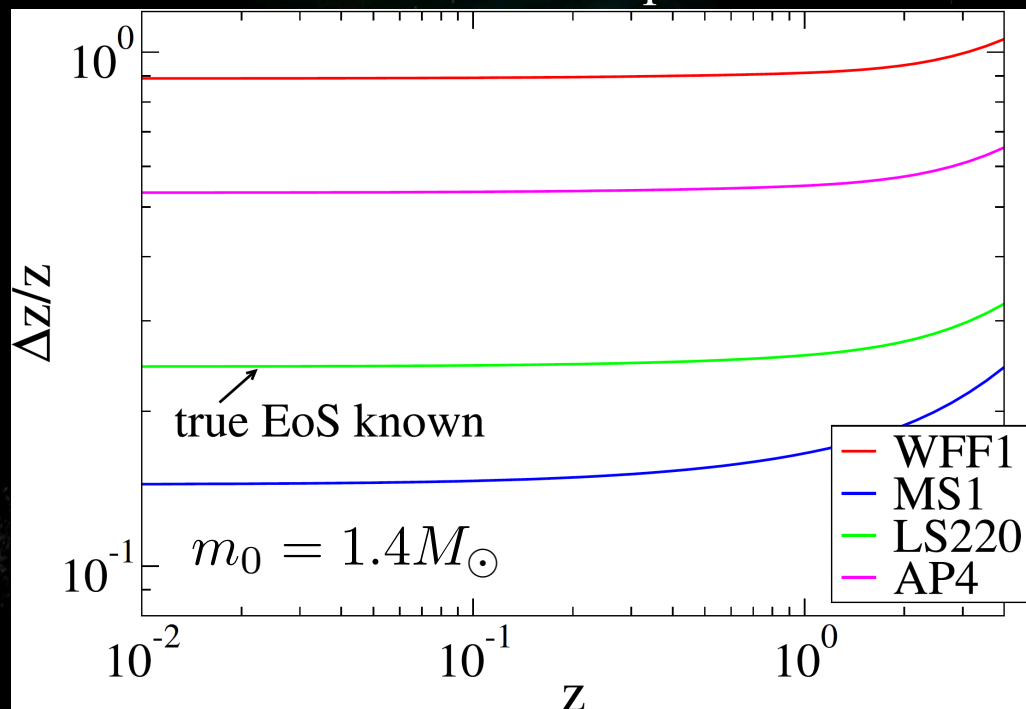


Universal to $\mathcal{O}(10\%)$

Redshift measurement

$$(m_1, m_2) = (1.4, 1.4)M_\odot$$

Einstein Telescope



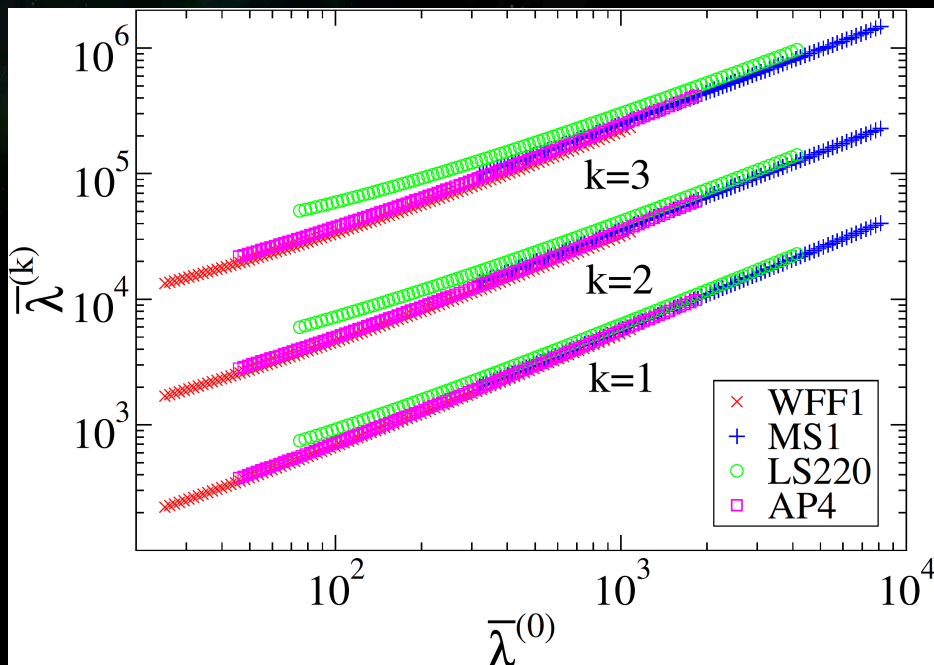
Perfect knowledge of EoS...?

Taylor expanded tidal deformability

[Messenger & Read (2012)]

fiducial mass

$$\bar{\lambda}_2(m) = \sum_{k=0} \frac{\bar{\lambda}^{(k)}}{k!} \left(1 - \frac{m}{m_0}\right)^k$$

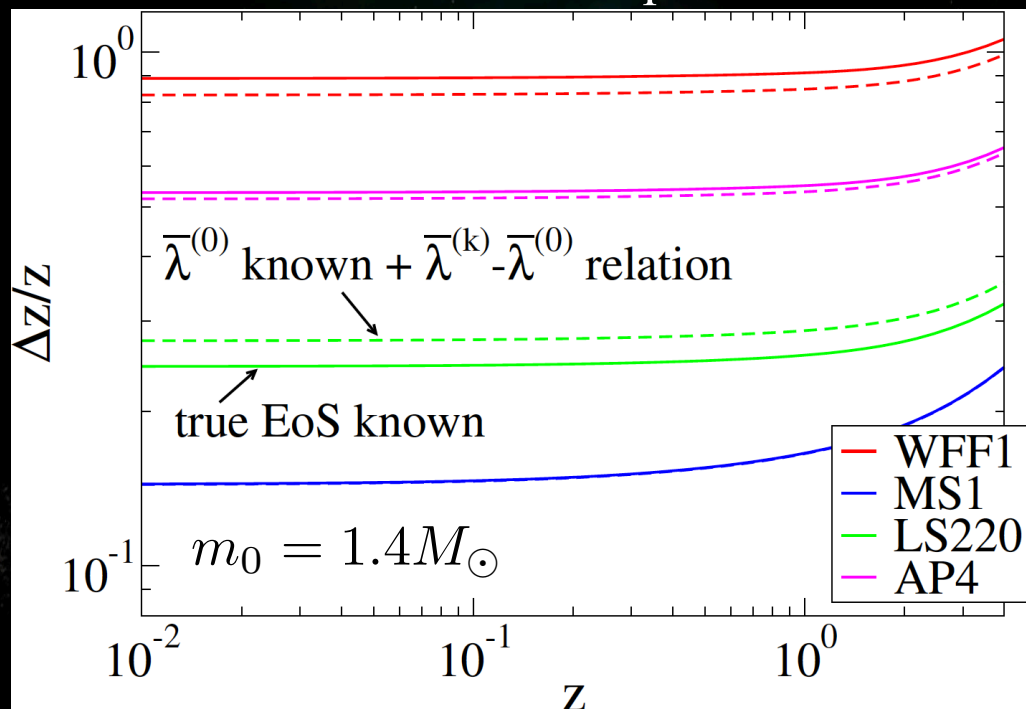


Universal to $\mathcal{O}(10\%)$

Redshift measurement

$$(m_1, m_2) = (1.4, 1.4)M_\odot$$

Einstein Telescope



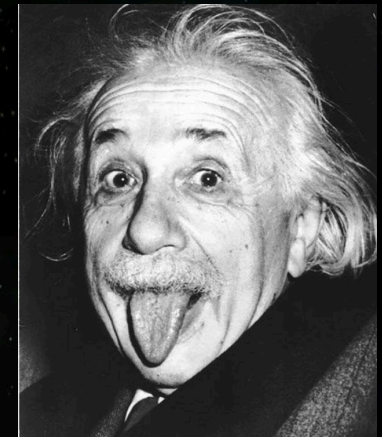
- ✓ difference $\sim 10\%$ at most
- ✓ possible to perform GW cosmology even if only $\bar{\lambda}^{(0)}$ is known

Conclusions

Takeaway

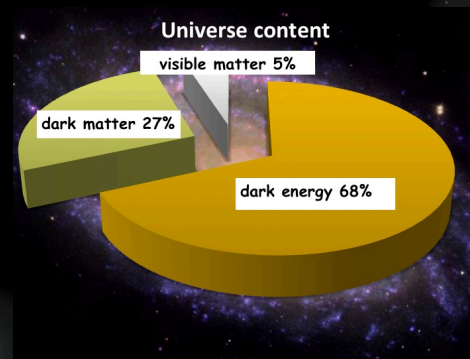
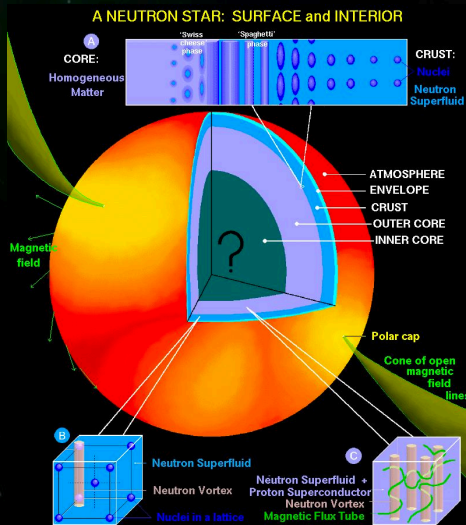
Astrophysics

Gravitational
Physics



Universal Relations

review article [KY & Yunes arXiv:1608.02582]



Nuclear Physics

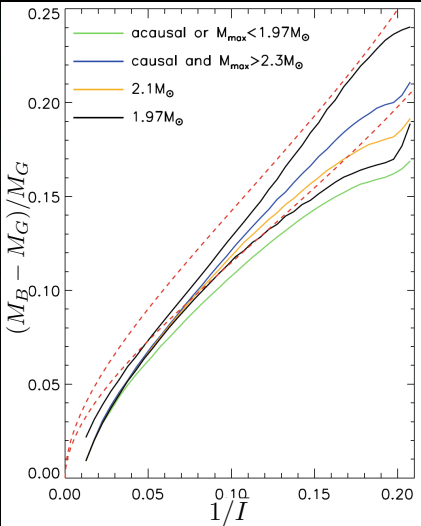
Cosmology

Outline

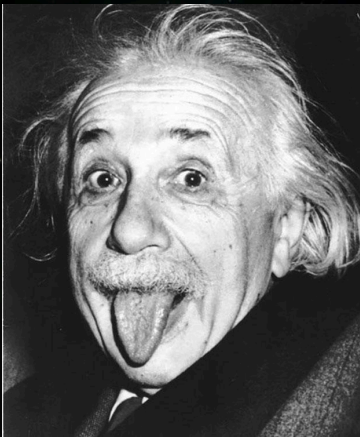
Kent Yagi

Takeaway

Astrophysics

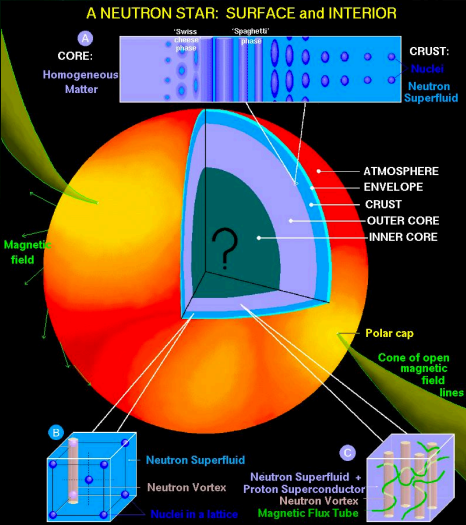
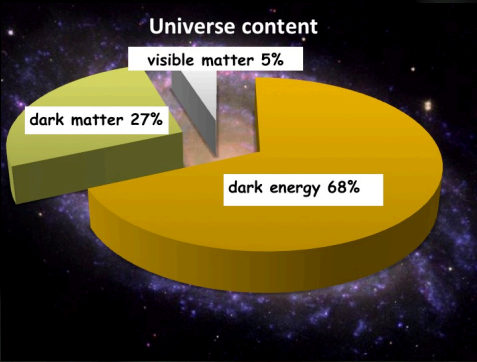


Gravitational Physics



Universal Relations

review article [KY & Yunes arXiv:1608.02582]

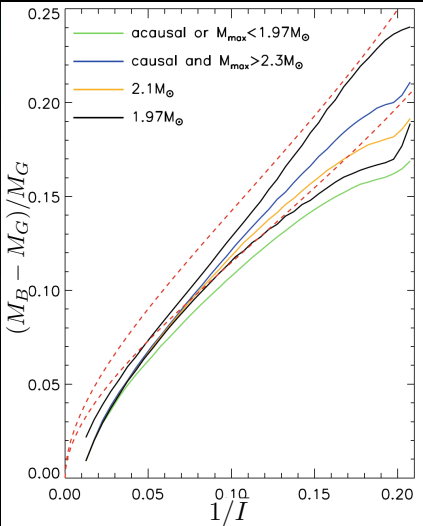


Nuclear Physics

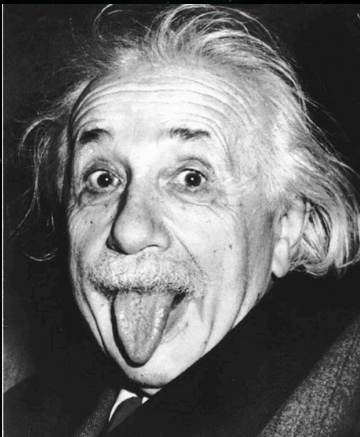
Cosmology

Takeaway

Astrophysics

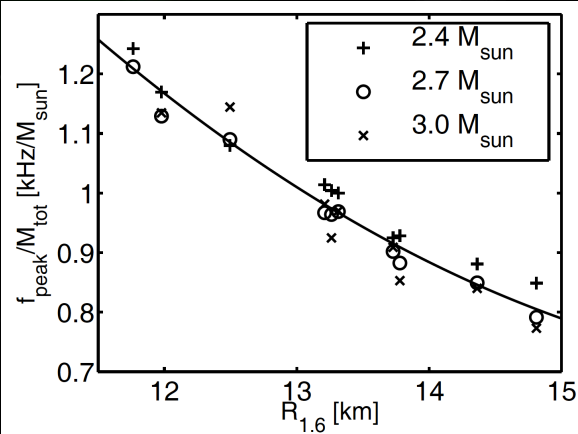


Gravitational Physics

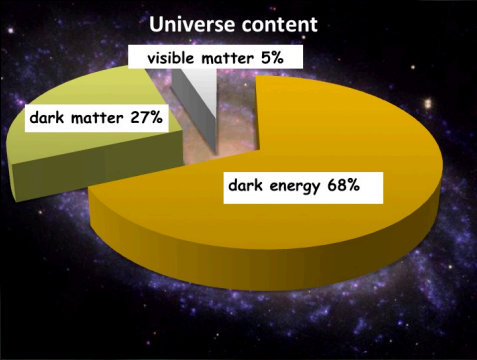


Universal Relations

review article [KY & Yunes arXiv:1608.02582]



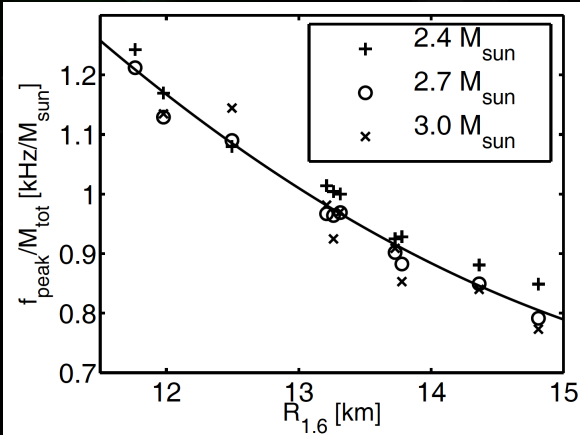
Nuclear Physics



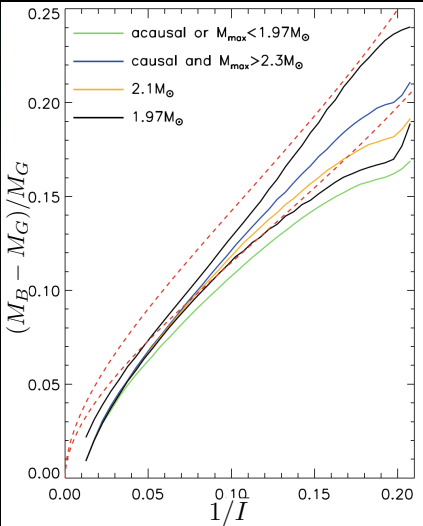
Cosmology

Takeaway

Astrophysics

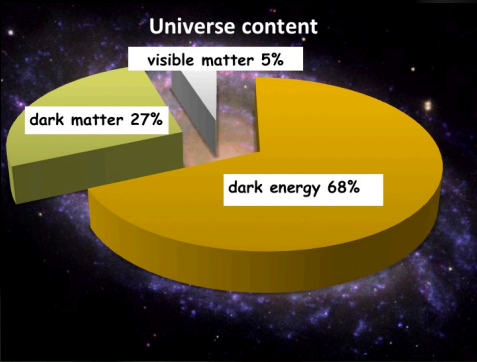


Nuclear Physics

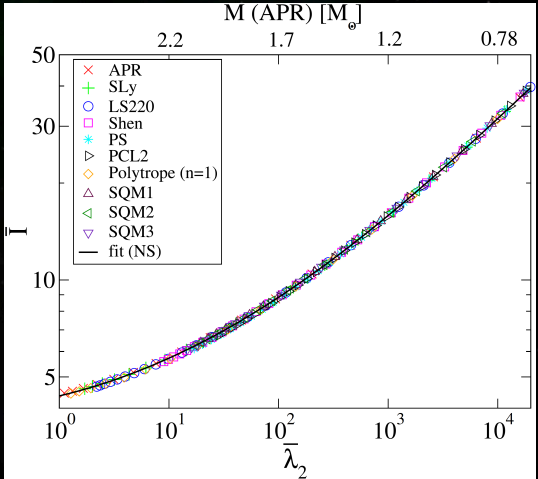


Universal Relations

review article [KY & Yunes arXiv:1608.02582]



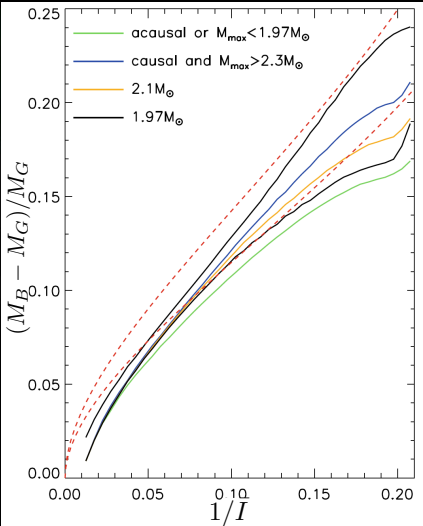
Gravitational Physics



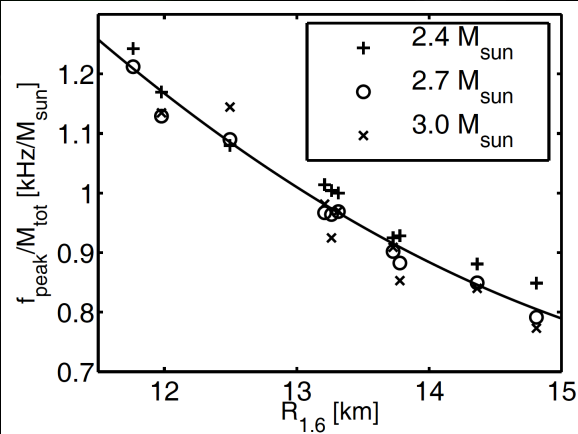
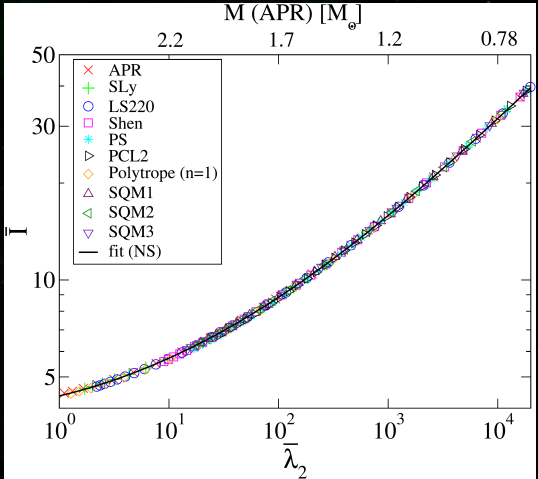
Cosmology

Takeaway

Astrophysics

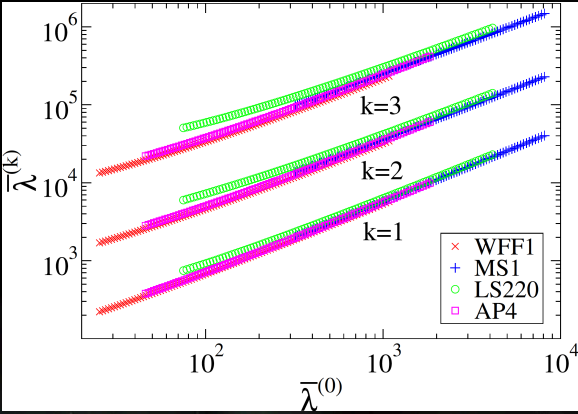


Gravitational Physics



Universal Relations

review article [KY & Yunes arXiv:1608.02582]

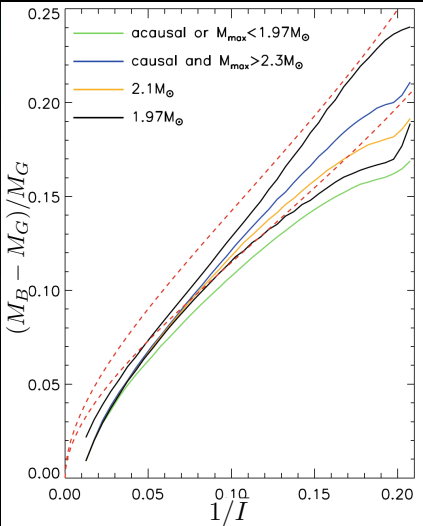


Nuclear Physics

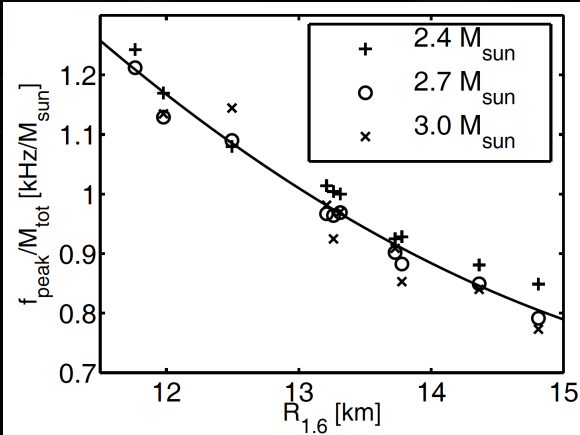
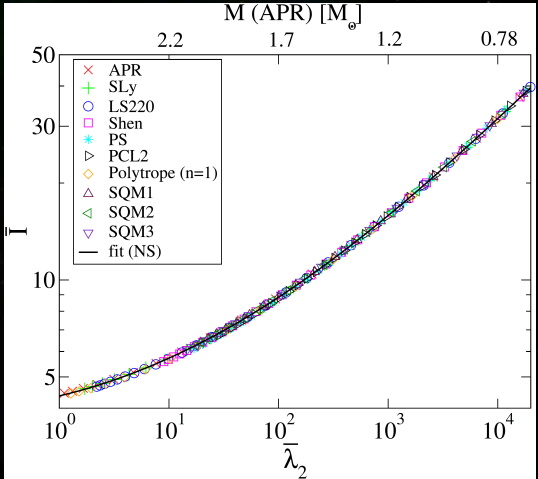
Cosmology

Takeaway

Astrophysics

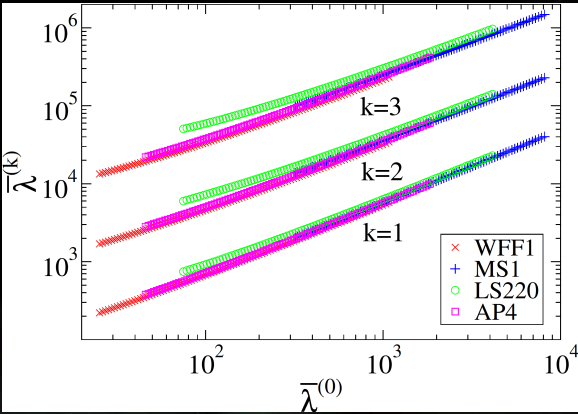


Gravitational Physics



Universal Relations

review article [KY & Yunes arXiv:1608.02582]



Nuclear Physics

Cosmology

Thank You