

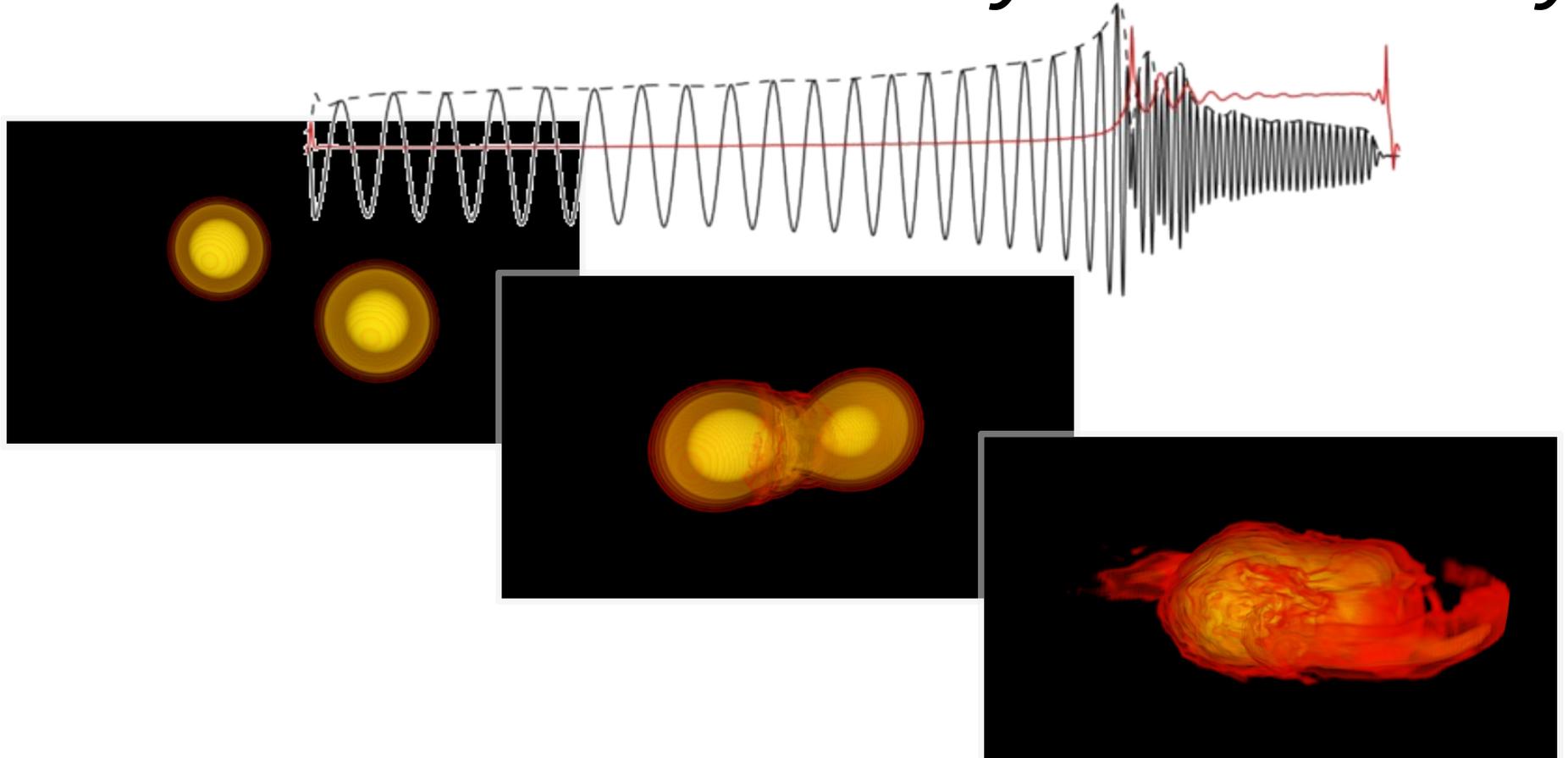


UNIVERSITÀ
DI PARMA



S. Bernuzzi Roma June, 20th 2017

Modeling GWs waves from NS mergers with numerical and analytical relativity



*** Outline ***

- Motivations
- Analytical/numerical techniques for waveform modeling in GR
- Parametrizing “the EOS”
- TEOBResum: a resummed tidal EOB model
- Fast and efficient representation of waveforms
- Closed-form tidal approximant from NR
- Parameter space studies
- Simulating NS with generic spin consistently
- Merger remnant: (an alternative) peak frequency characterization and emission energetics and timescale

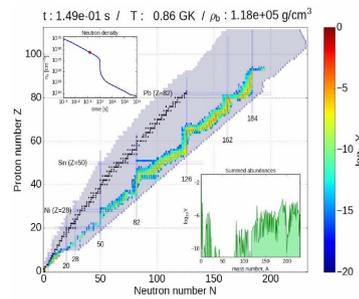
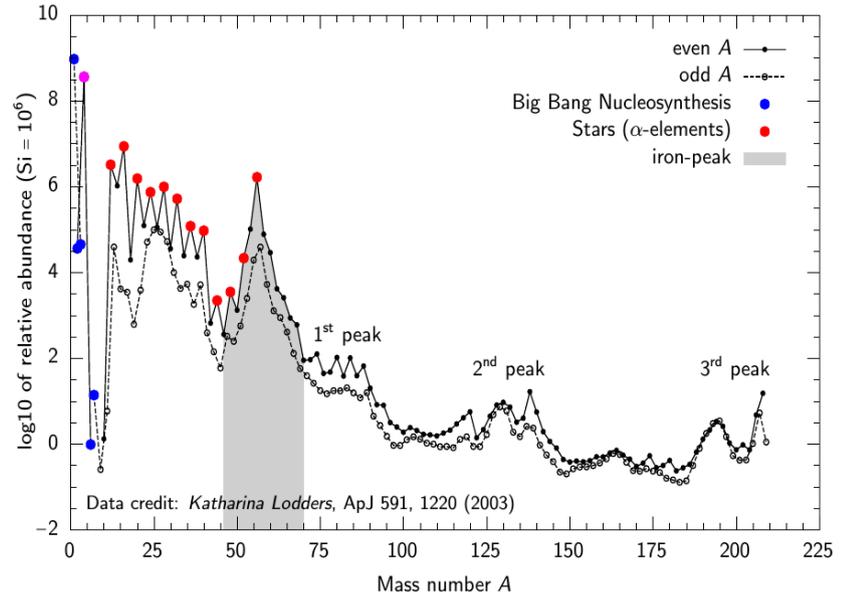
What can we learn from neutron star mergers?

FUNDAMENTAL PHYSICS

Strong-field tests GR (dynamics)

Structure of bulk matter at supranuclear densities

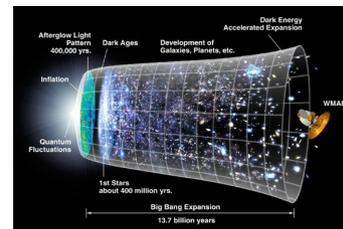
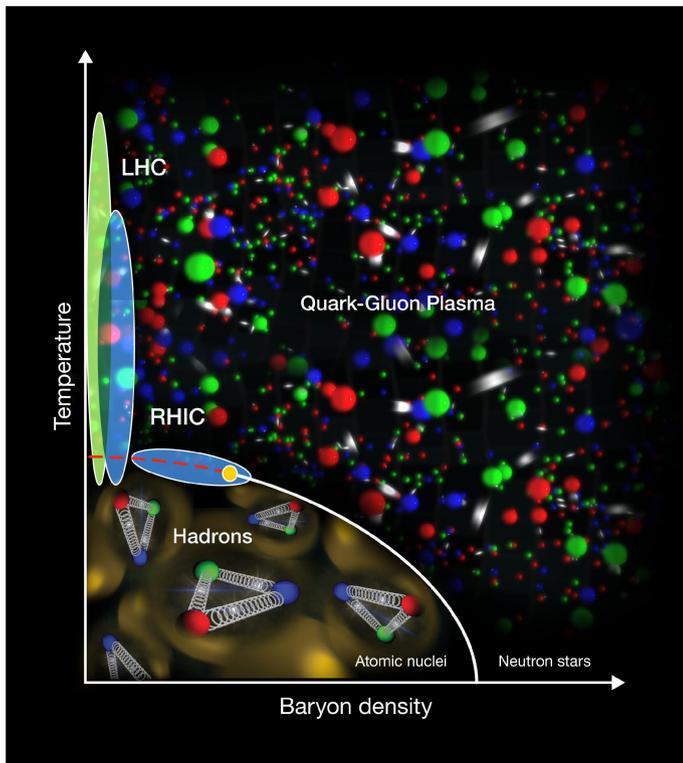
Heavy elements nucleosynthesis



ASTROPHYSICS (Multi-messenger)

Origin of gamma-ray burst

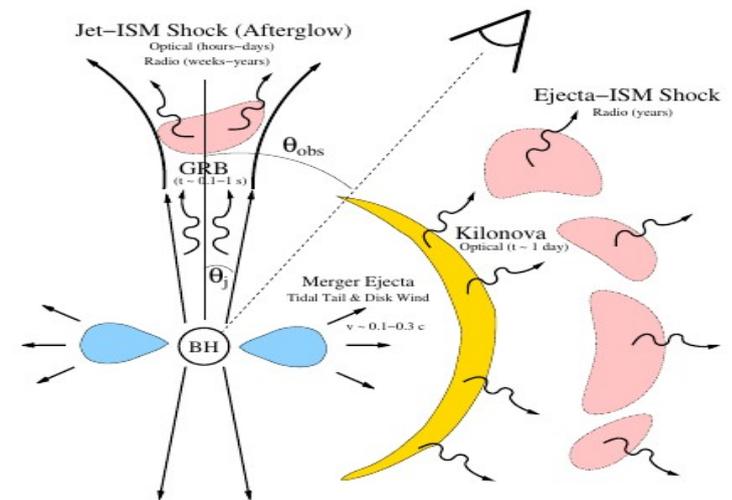
Origin of kilonovae, site for r-processes



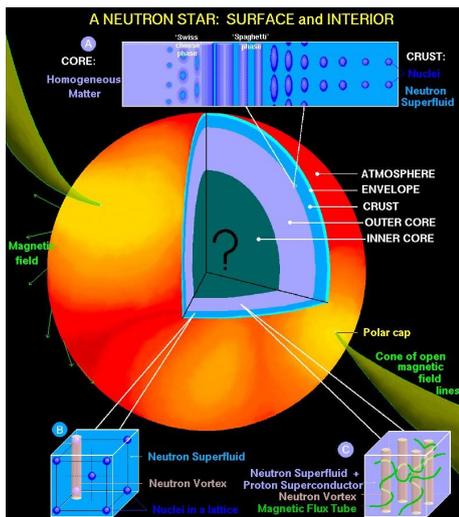
COSMOGRAPHY

Measure Hubble constant

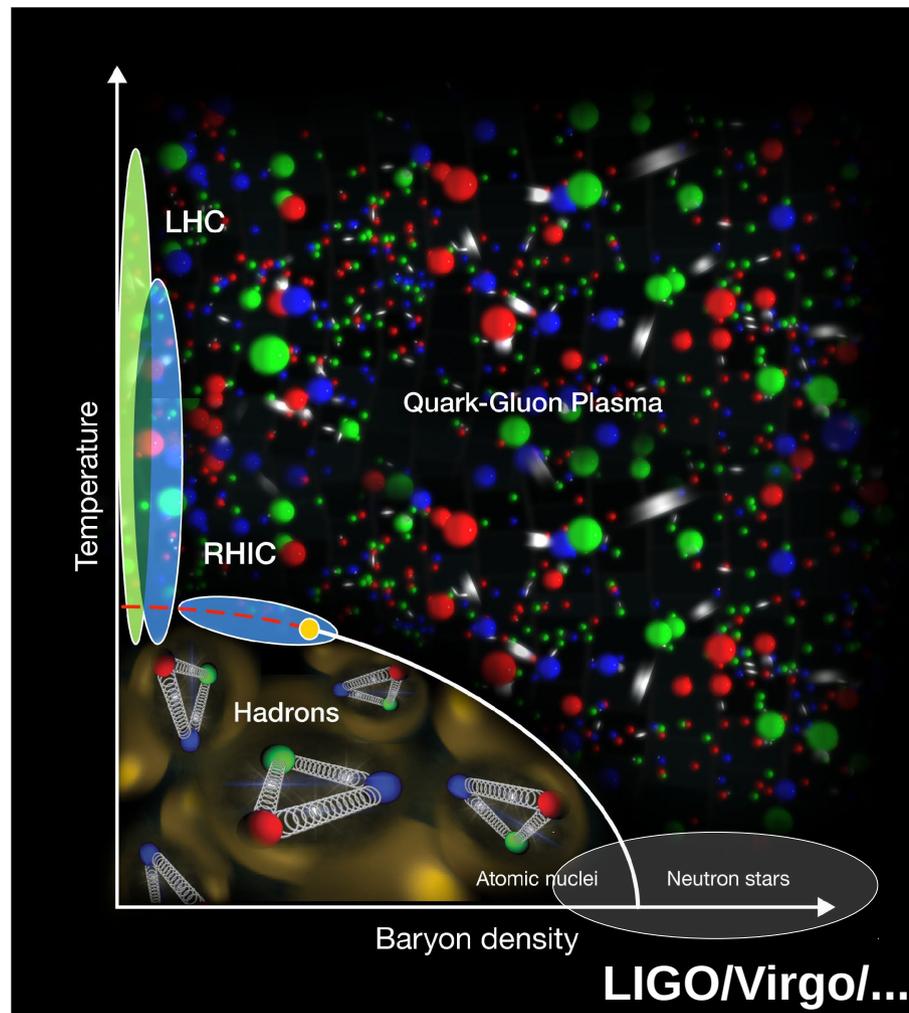
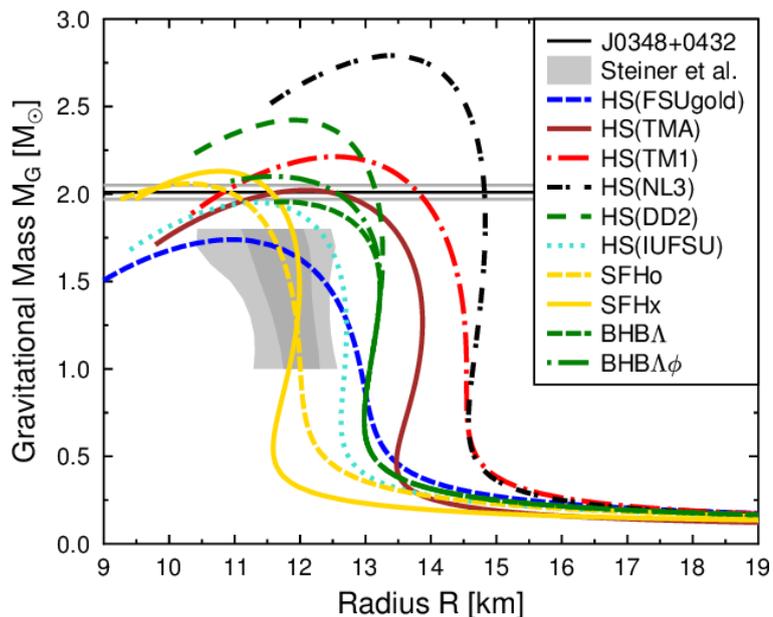
Standard sirens, Calibrate cosmic distance ladder



Constraining the NS Equation of State

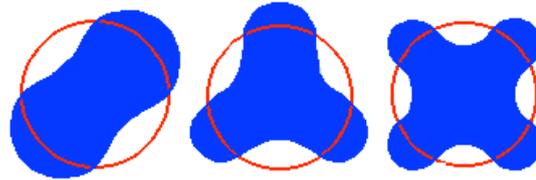
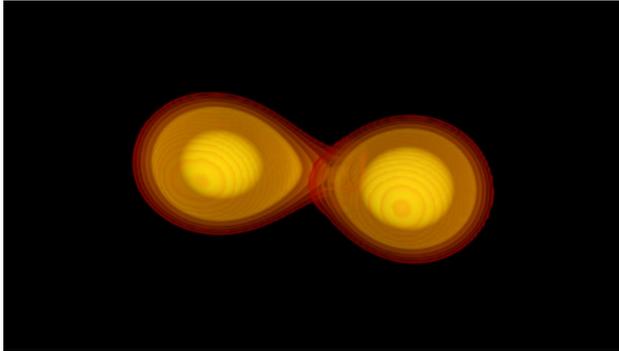


Different EOS → different star's structure



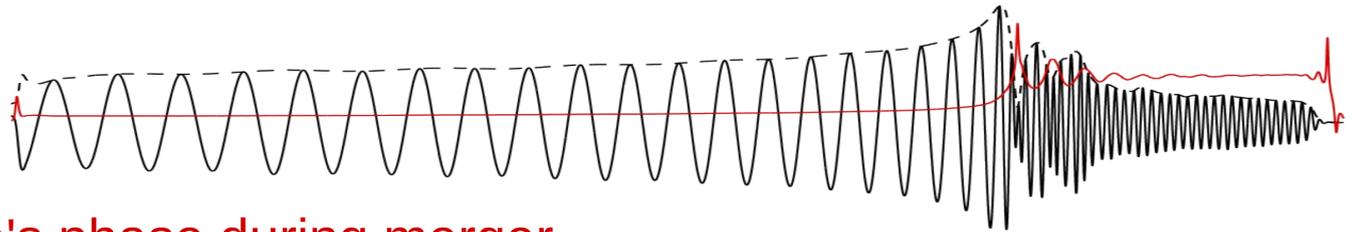
Binary neutron star mergers

How to?



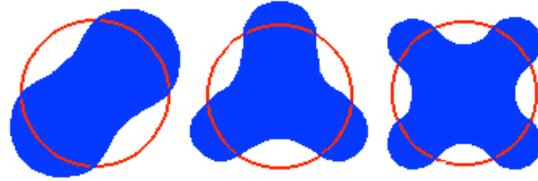
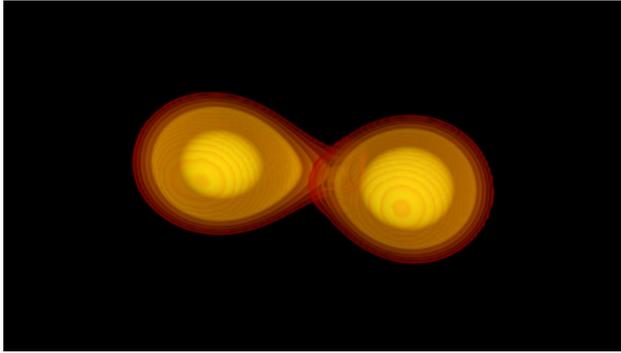
$$\lambda_2 \propto \frac{Q_{ij}}{\partial_{ij} \Phi_{ext}}$$

Tides depend critically on EOS



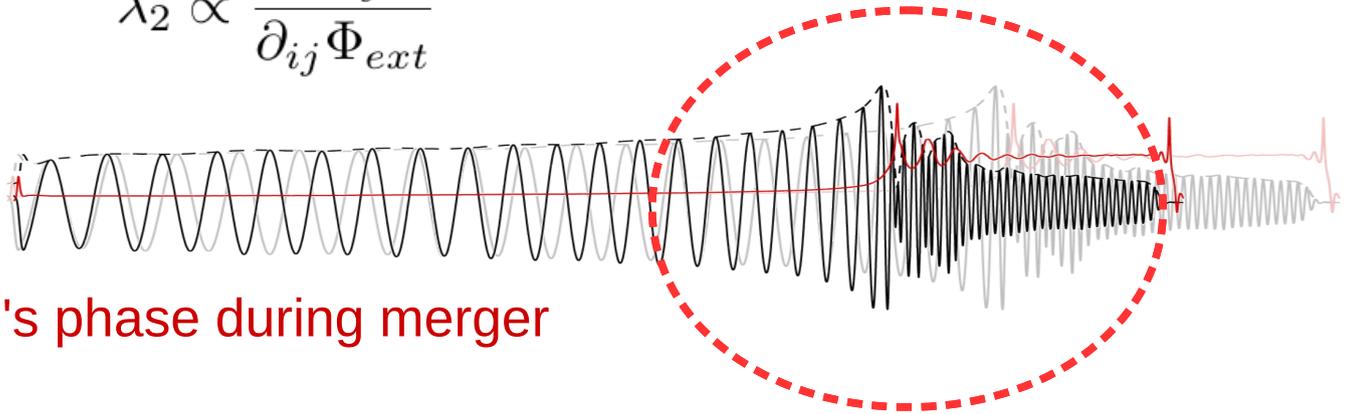
Tides determine the wave's phase during merger

How to?



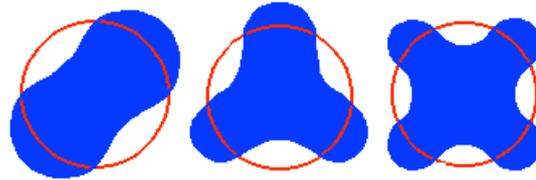
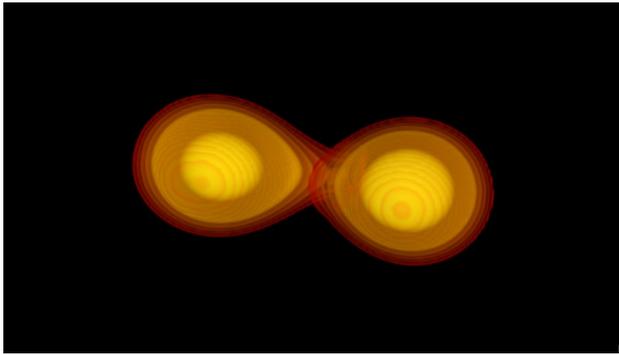
$$\lambda_2 \propto \frac{Q_{ij}}{\partial_{ij} \Phi_{ext}}$$

Tides depend crucially on EOS



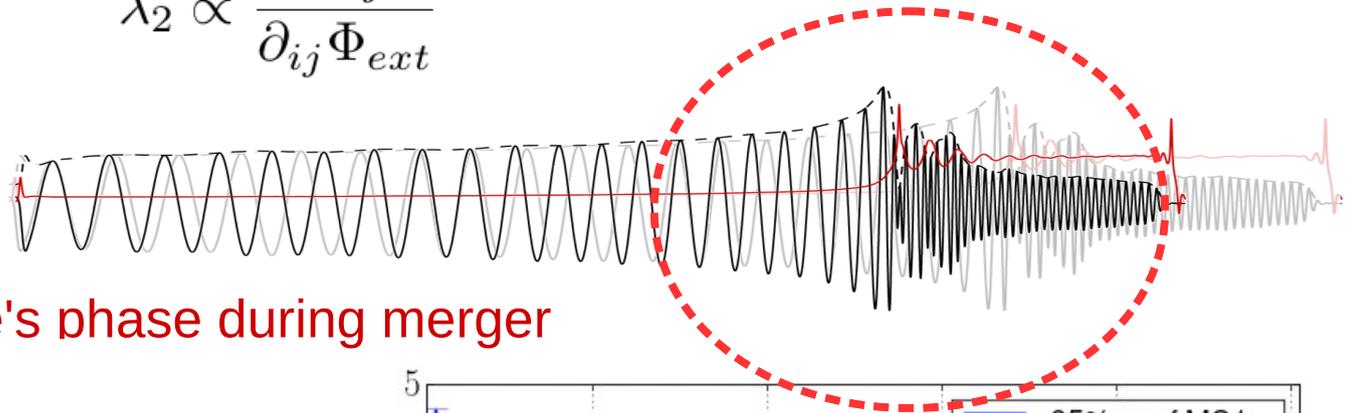
Tides determine the wave's phase during merger

How to?

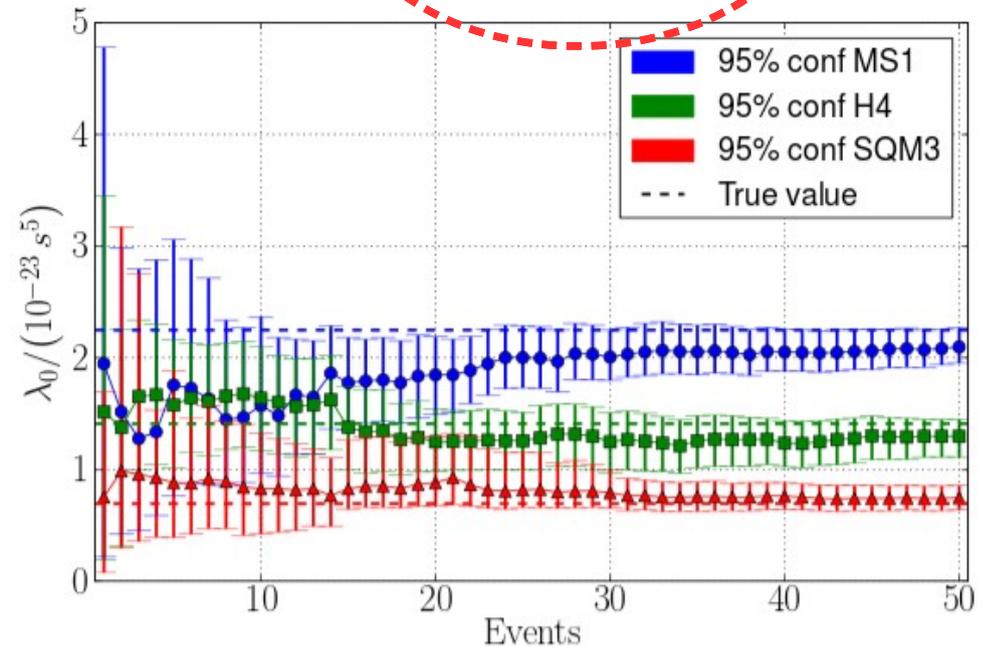
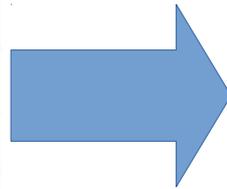
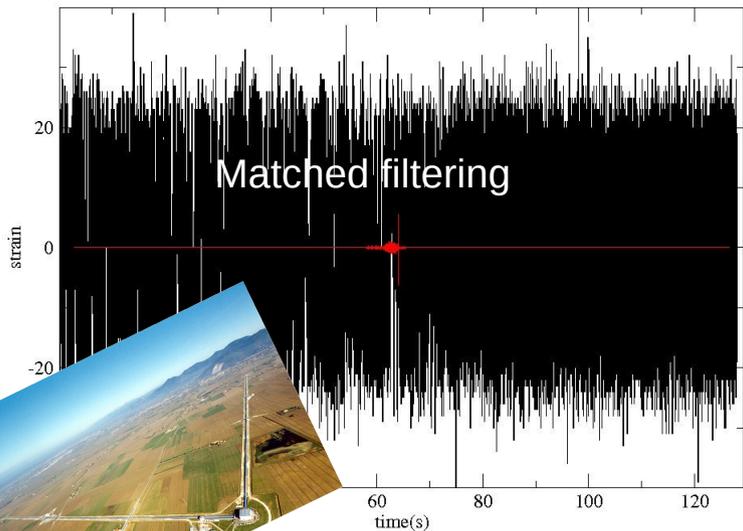


$$\lambda_2 \propto \frac{Q_{ij}}{\partial_{ij} \Phi_{ext}}$$

Tides depend crucially on EOS

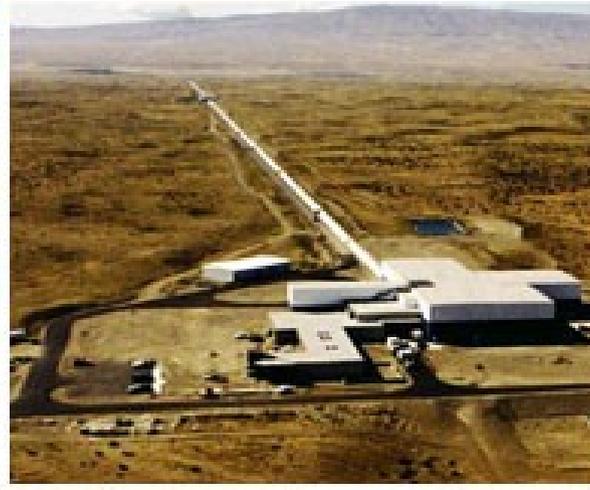


Tides determine the wave's phase during merger

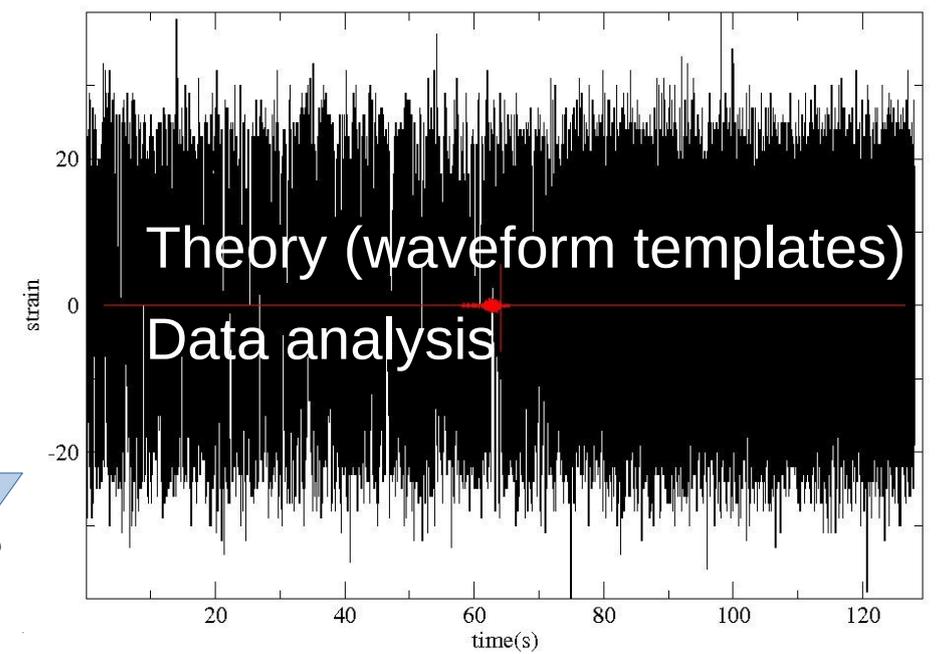
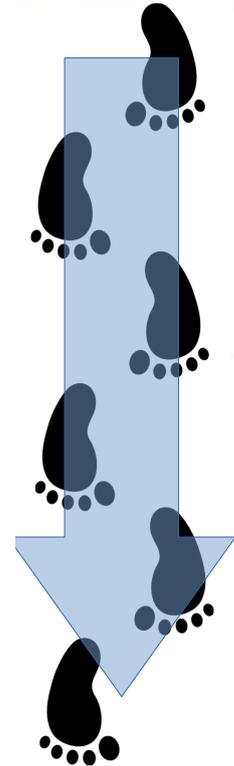
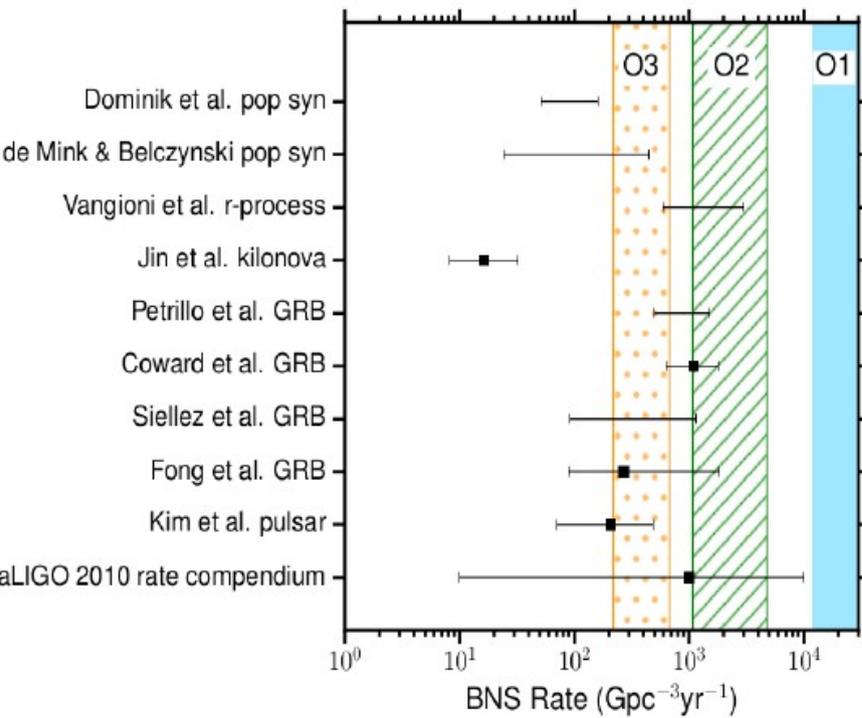


[Del Pozzo+ PRL 111 (2013)]

GW observations require detailed signal models

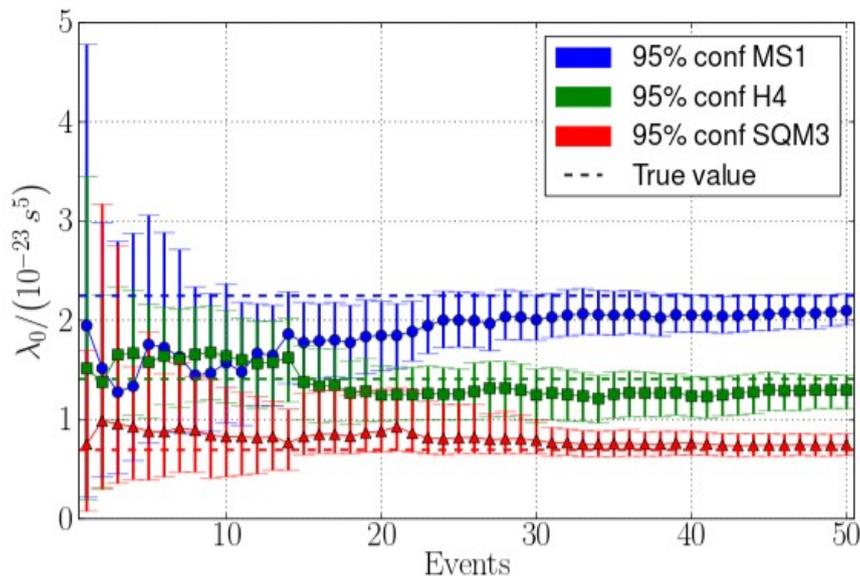


LIGO Lab/Virgo



Source parameters, interpretation (“science”)

Data-analysis status



[Del Pozzo+ arXiv:1307.8338]

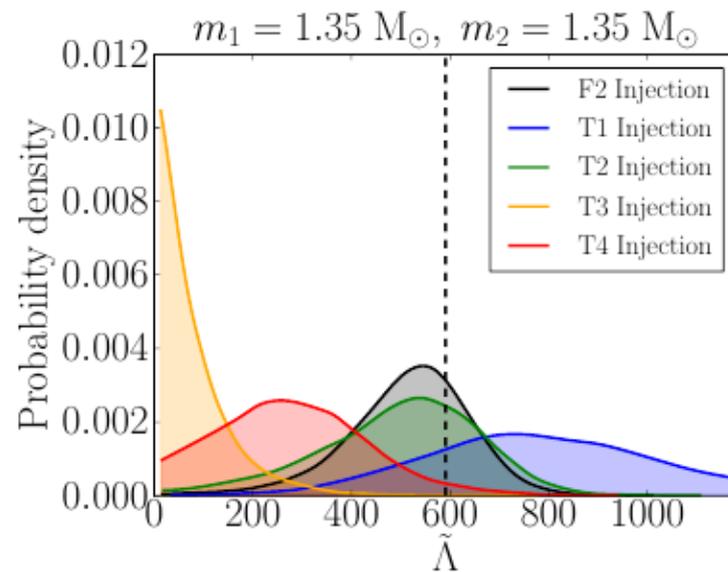
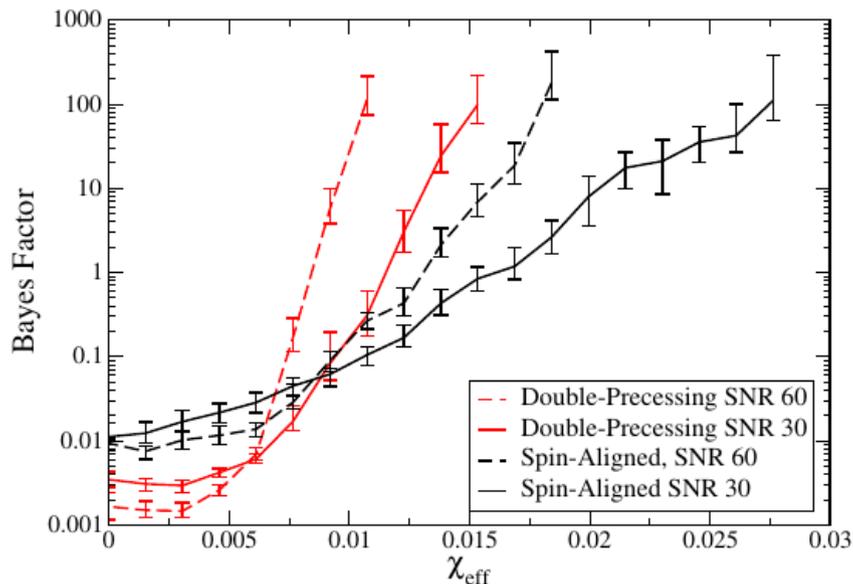
Tidal parameters can be constrained by LIGO/Virgo using multiple observations

[Agathos+ arXiv:1503.05405]

Mass-prior effect is crucial
(confirm biases due to waveform systematics)

[Wade+ arXiv:1402.5156, Lackey+ arXiv:1410.8866]

Uncertainties in the waveform models lead to systematic errors in EOS ~ statistical errors

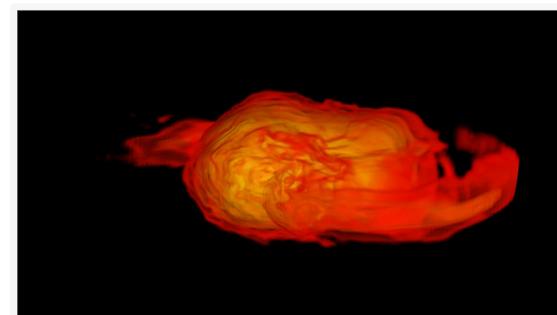
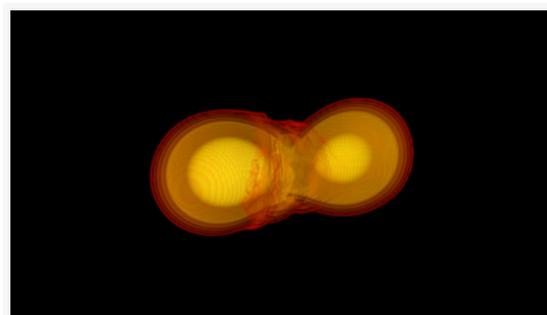
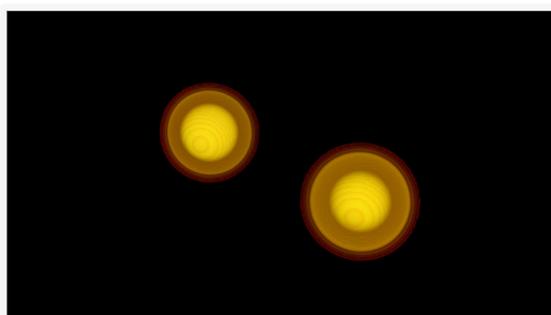
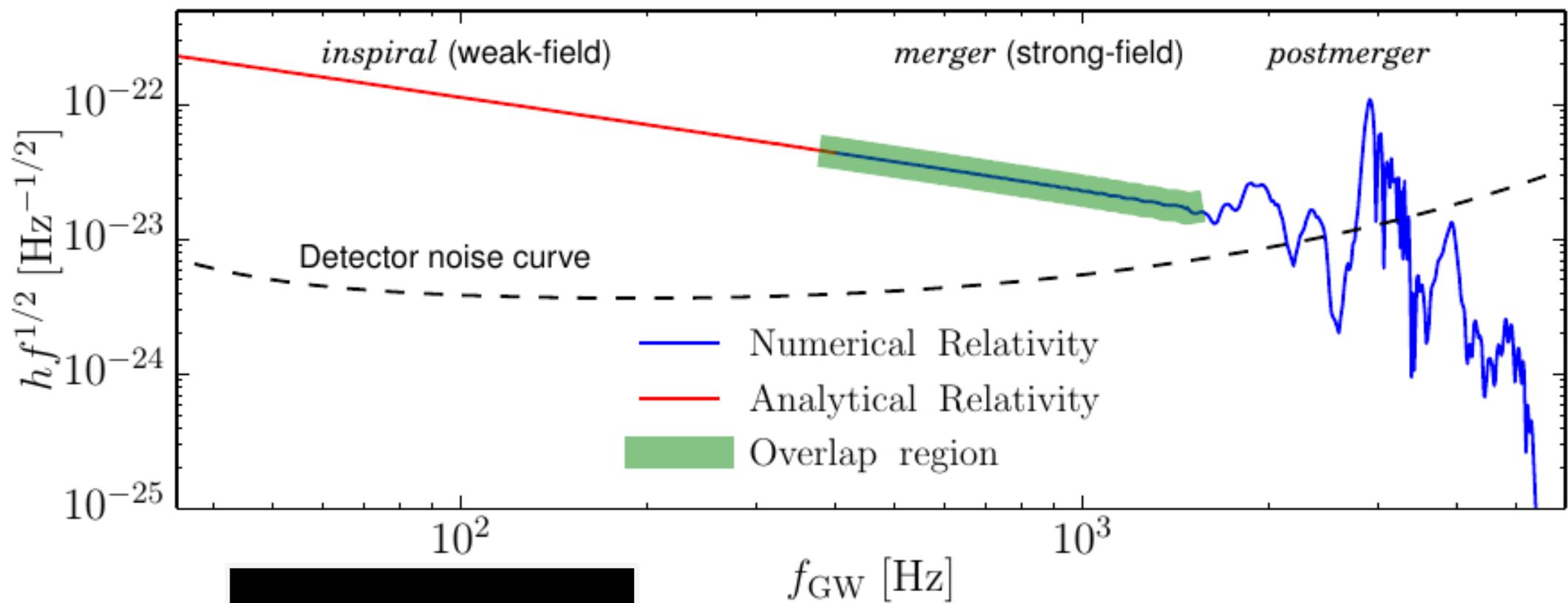


[Chatziioannou+ arXiv:1404.3108]

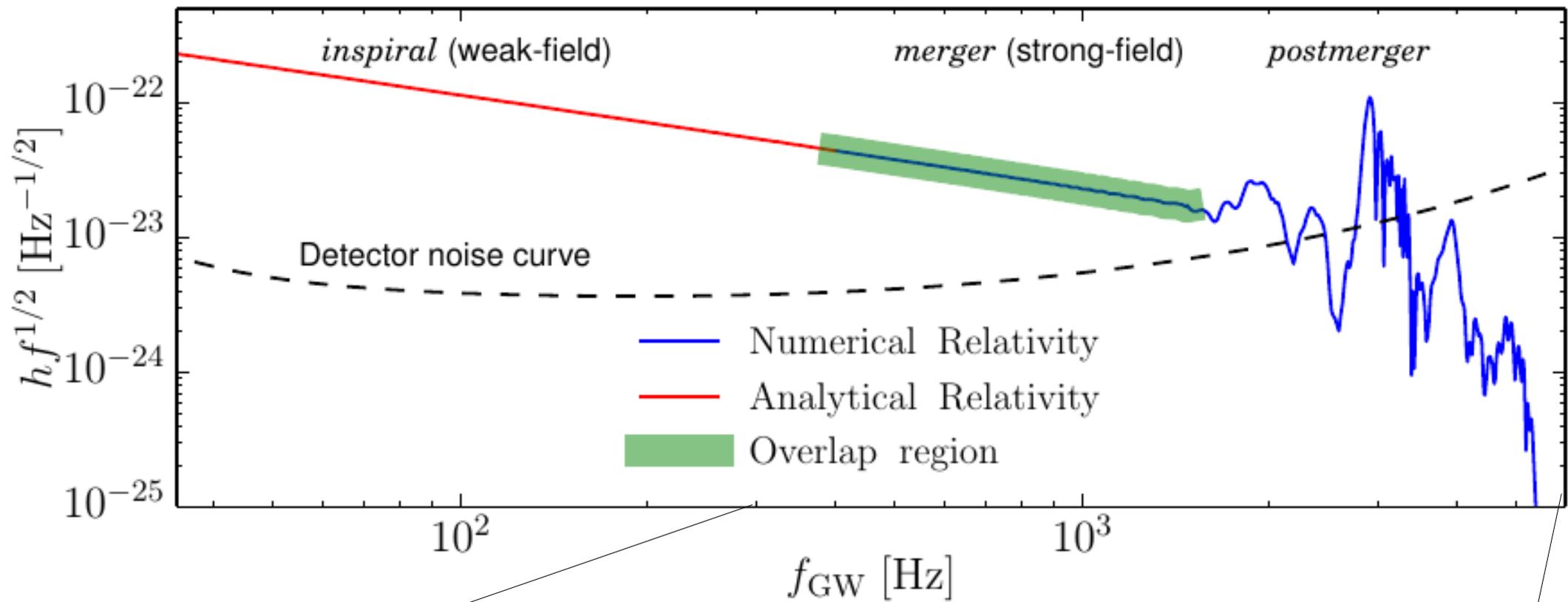
SNR > ~30, large biases on masses and spins if precessing spin effects not modeled (small spins < 0.2)

See also [Read+ arXiv:0901.3258, Hinderer+ arXiv:0911.3535, Damour+ arXiv:1203.4352]

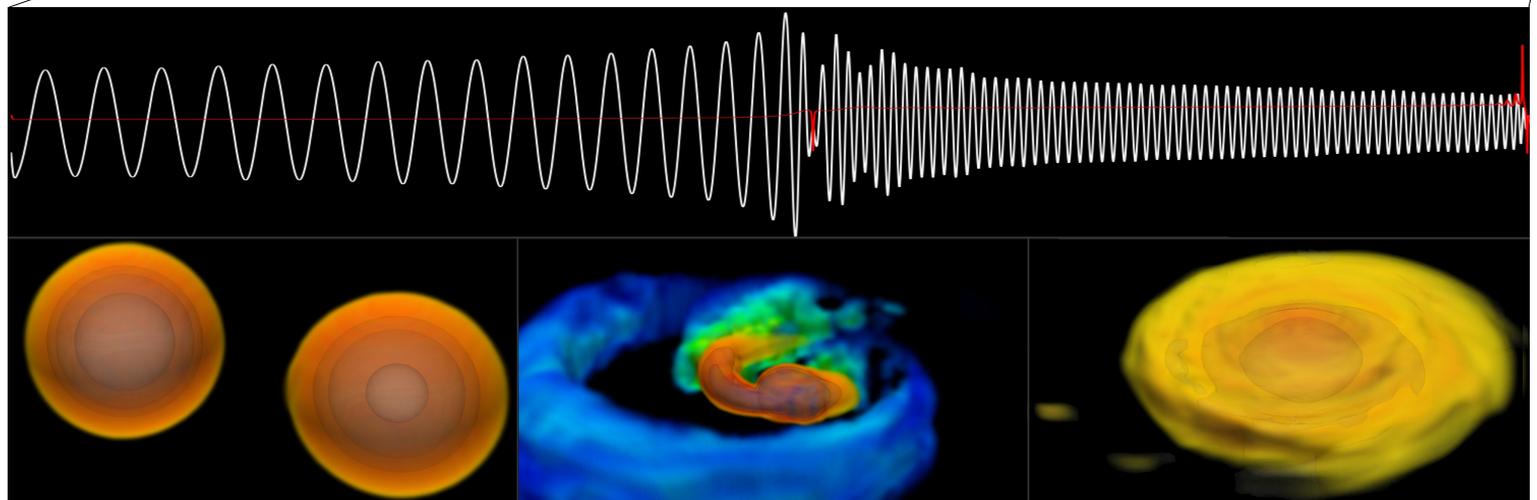
The GW spectrum



The GW spectrum



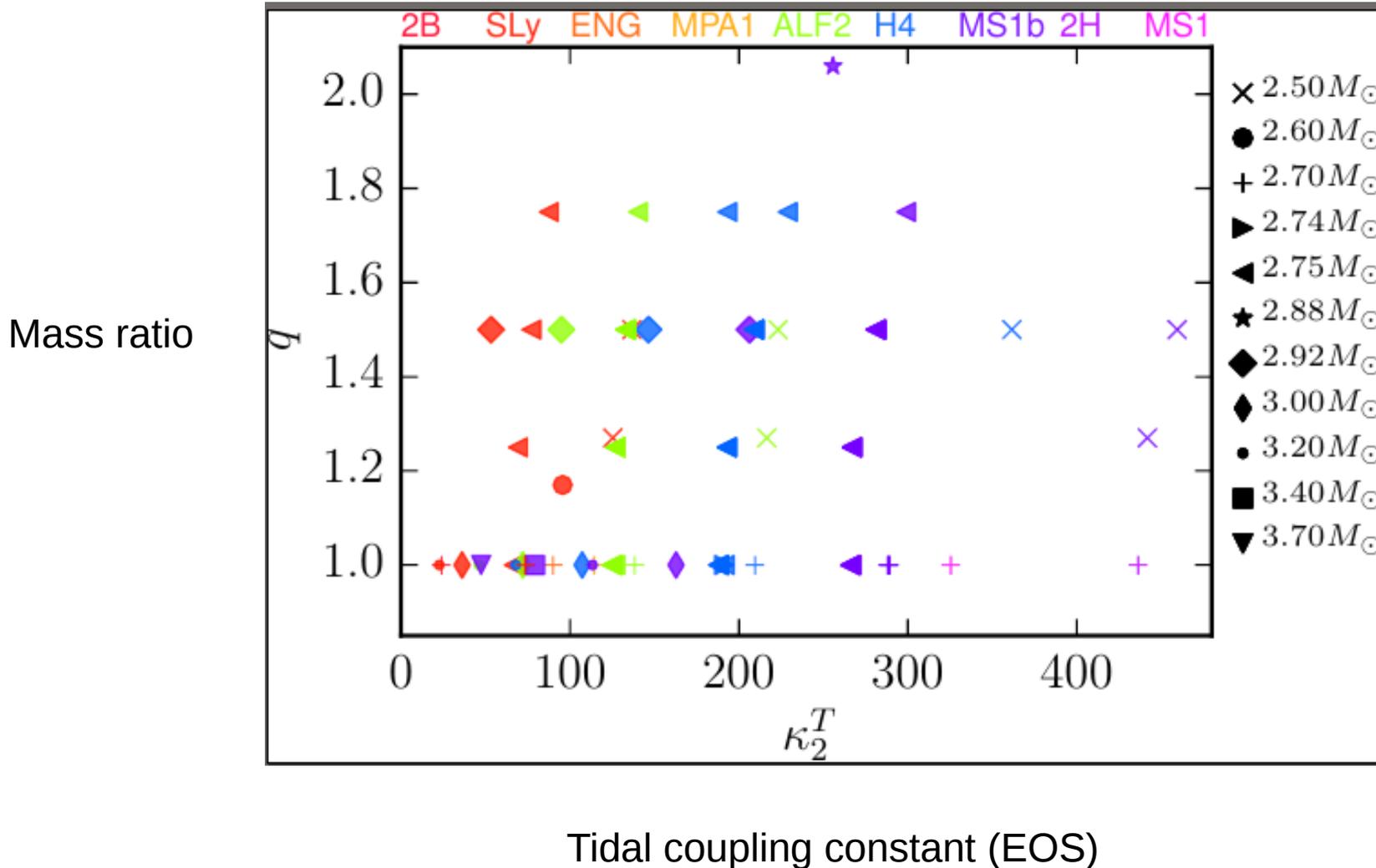
NR simulation
ONLY!



Exploring the BNS parameter space

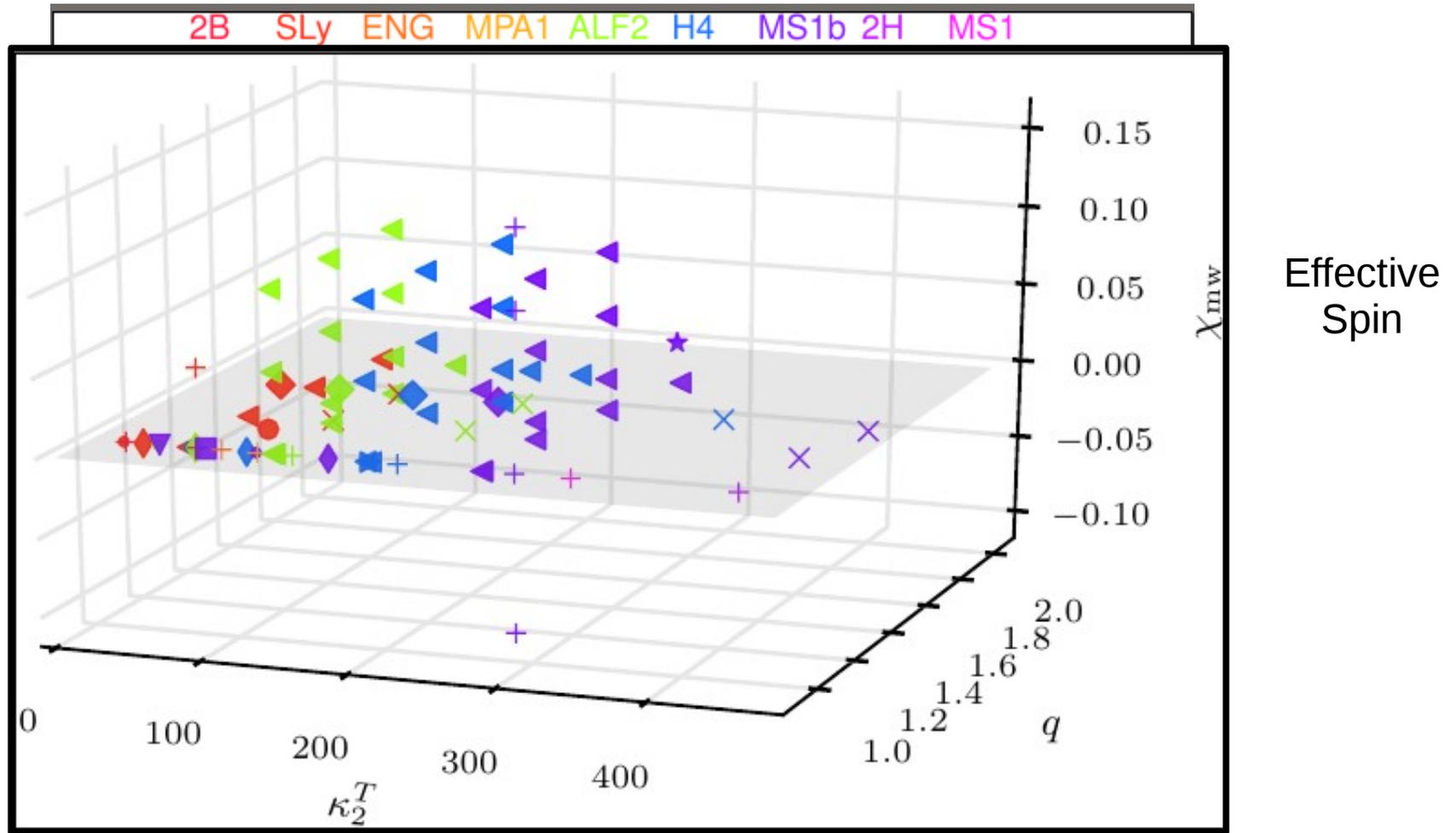
[Dietrich, Ujevic, SB, Tichy, Bruegmann PRD95 024029 (2017)]

[Dietrich, SB, Ujevic, Tichy PRD95 044045 (2017)]



Exploring the BNS parameter space

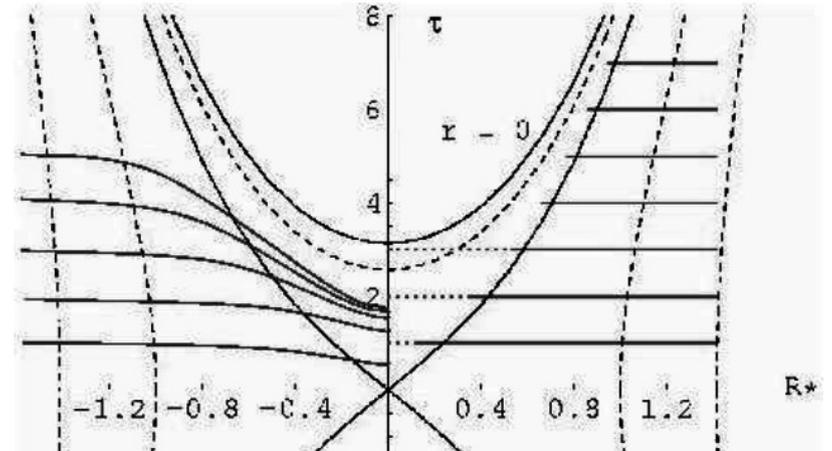
Largest exploration of parameter space in strong-field regime available to date



Tidal coupling constat (EOS)

Mass ratio

$$\begin{aligned}
\partial_t \bar{\Gamma}^i &= -2 \bar{A}^{ij} \partial_j \alpha + 2 \alpha \left[\bar{\Gamma}^i_{jk} \bar{A}^{jk} - \frac{3}{2} \bar{A}^{ij} \partial_j \ln(\chi) \right. \\
&\quad \left. - \frac{1}{3} \bar{\gamma}^{ij} \partial_j (2 \hat{K} + \Theta) - 8 \pi \bar{\gamma}^{ij} S_j \right] + \bar{\gamma}^{jk} \partial_j \partial_k \beta \\
&\quad + \frac{1}{3} \bar{\gamma}^{ij} \partial_j \partial_k \beta^k + \beta^j \partial_j \bar{\Gamma}^i - (\bar{\Gamma}_d)^j \partial_j \beta^i \\
&\quad + \frac{2}{3} (\bar{\Gamma}_d)^i \partial_j \beta^j - 2 \alpha \kappa_1 [\bar{\Gamma}^i - (\bar{\Gamma}_d)^i], \\
\partial_t \Theta &= \frac{1}{2} \alpha [R - \bar{A}_{ij} \bar{A}^{ij} + \frac{2}{3} (\hat{K} + 2\Theta)^2] \\
&\quad - \alpha [8 \pi \rho + \kappa_1 (2 + \kappa_2) \Theta] + \beta^i \partial_i \Theta,
\end{aligned}$$



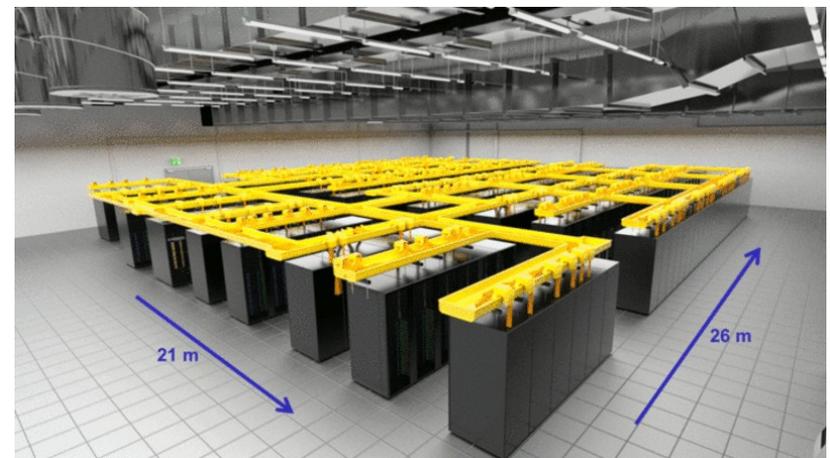
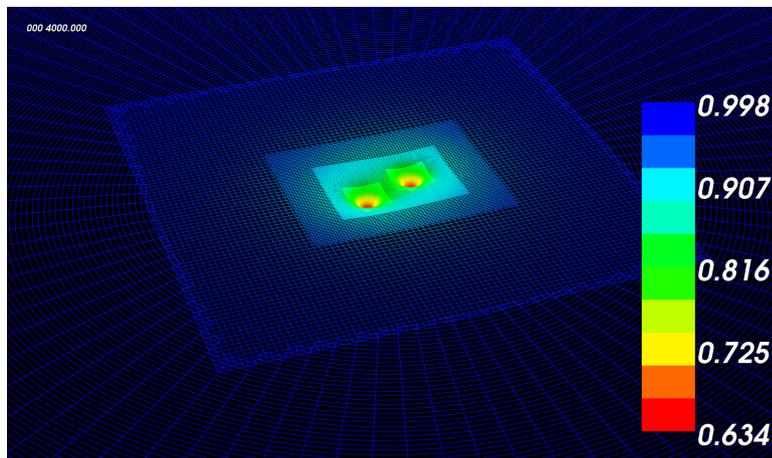
*GR Formulation and Cauchy problem
+ GR hydrodynamics*

Coordinates and Singularities

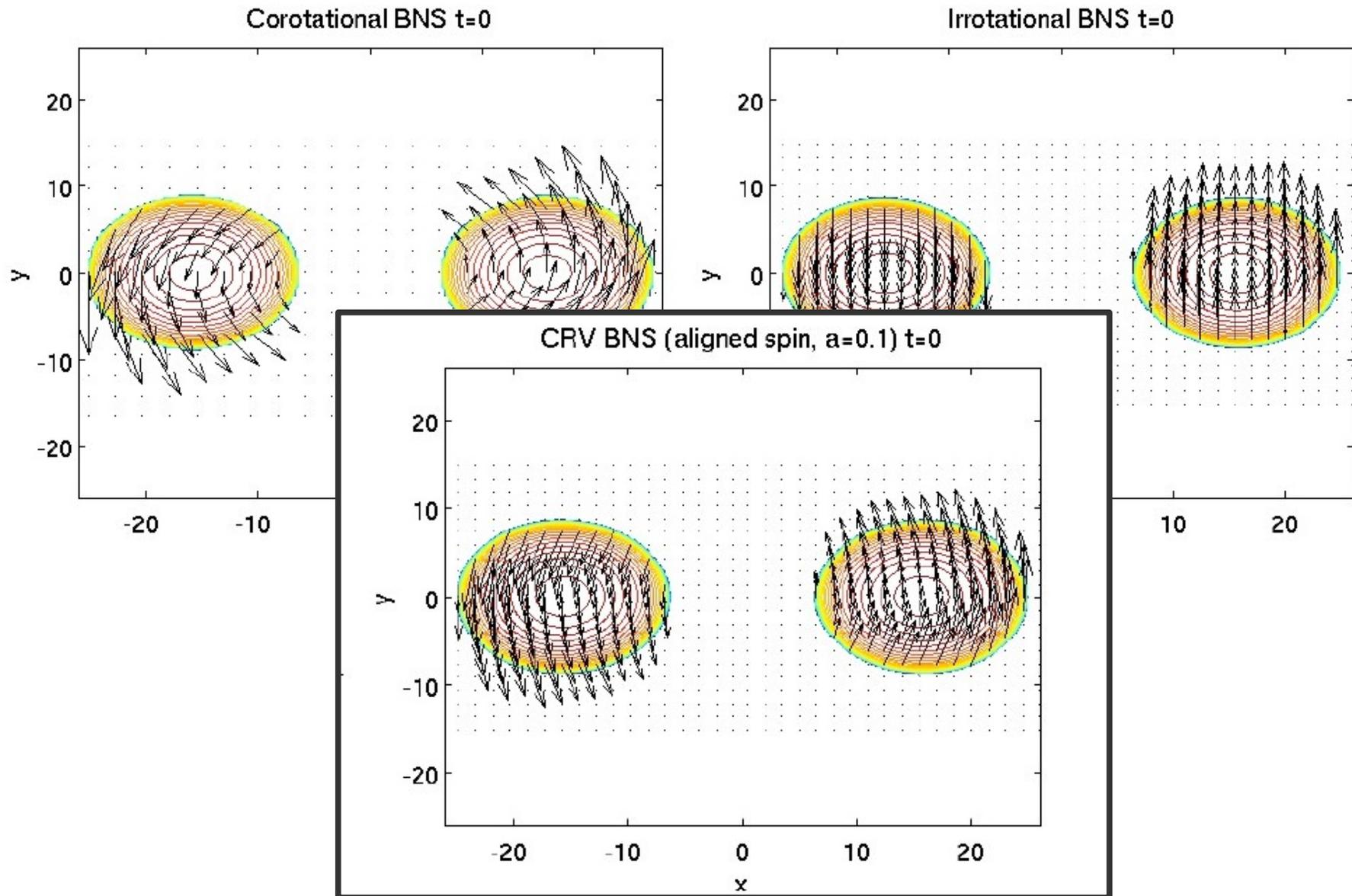
Numerical relativity in a nutshell

Numerical methods for PDEs on adaptive grids

High-performance-computing (HPC)



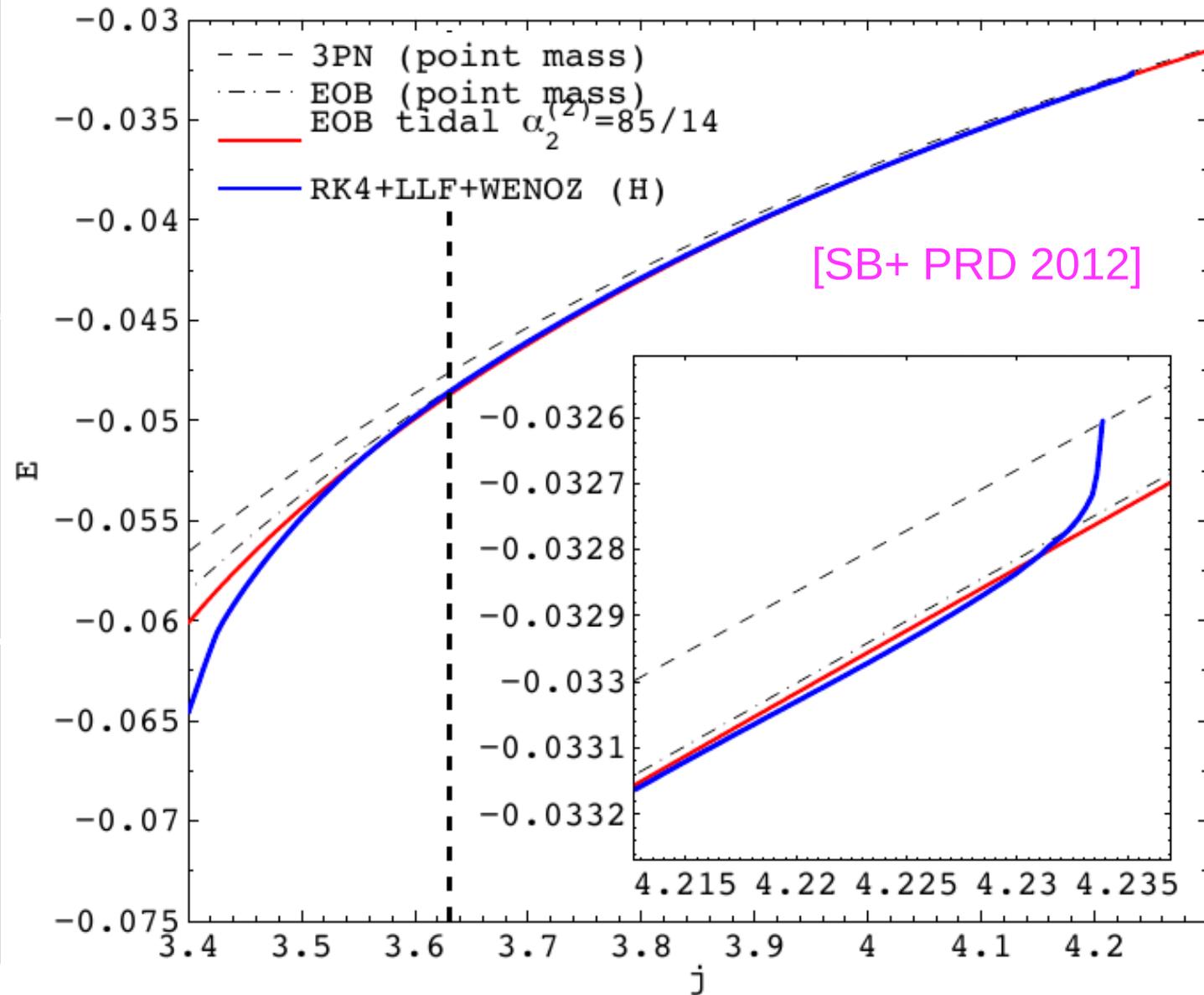
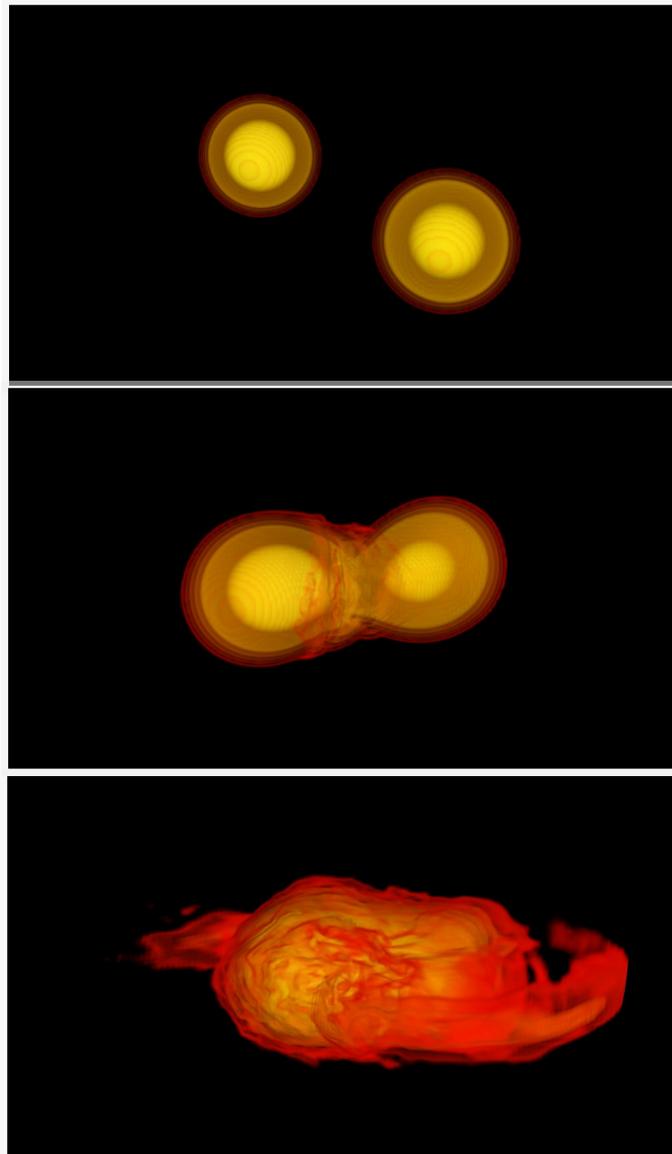
Quasiequilibrium circular initial data



Constant Rotational Velocity approach

[Tichy arXiv:1209.5336, arXiv:1107.1440]

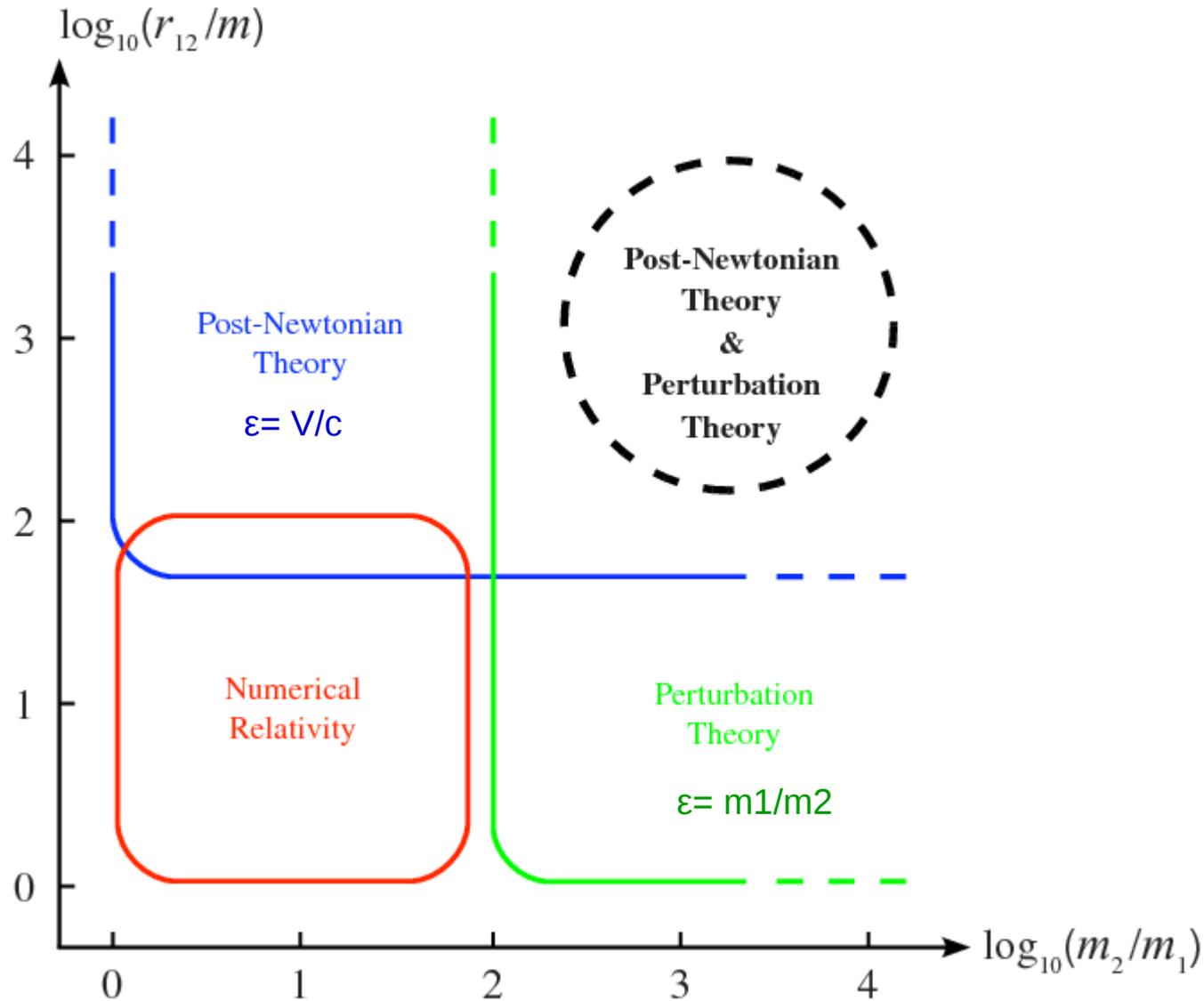
How to extract meaningful info from simulations?



[Damour+ PRL 2012] → Probe conservative dynamics

Methods for the GR 2-body problem

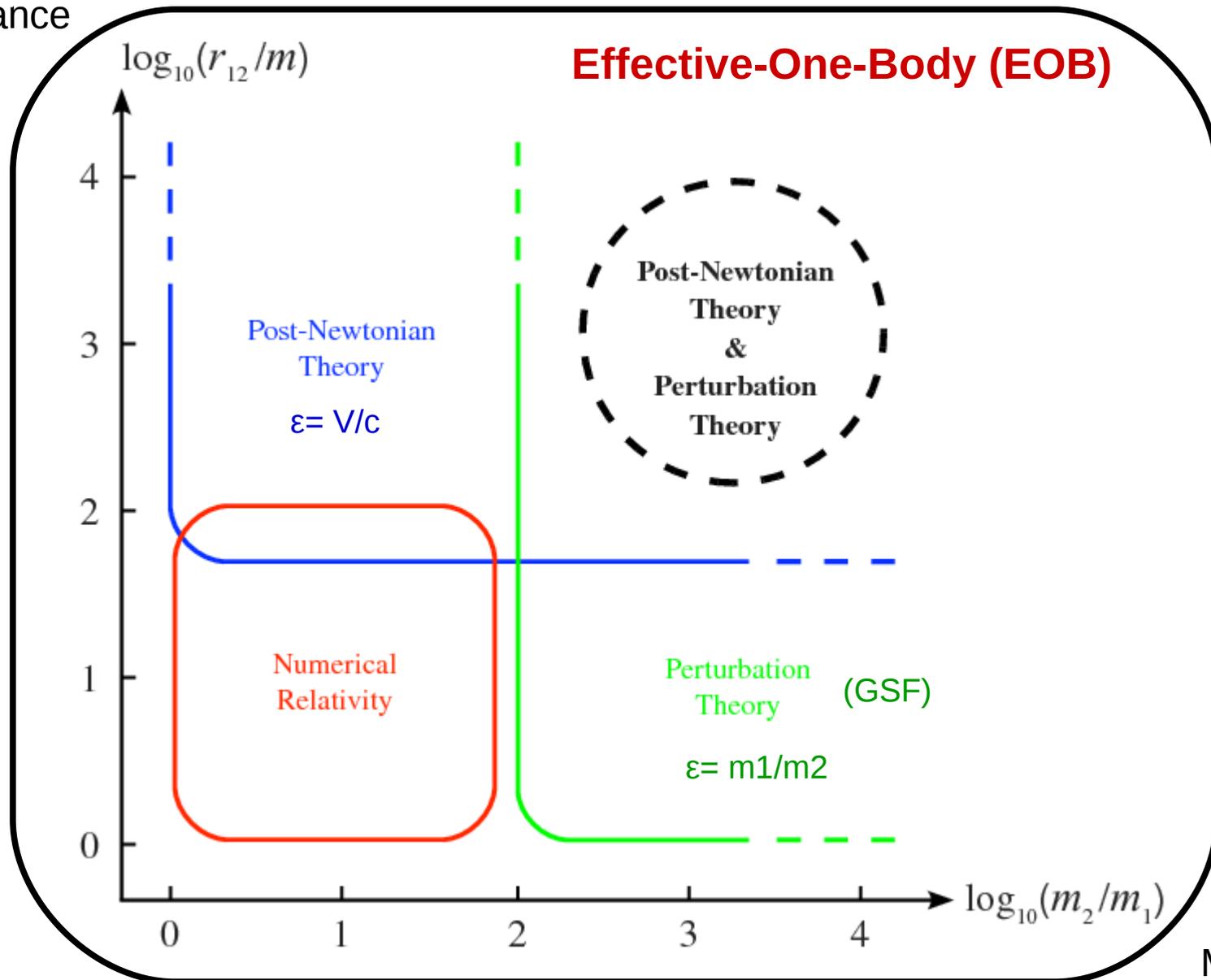
Separation distance



Mass-ratio

Effective-One-Body framework

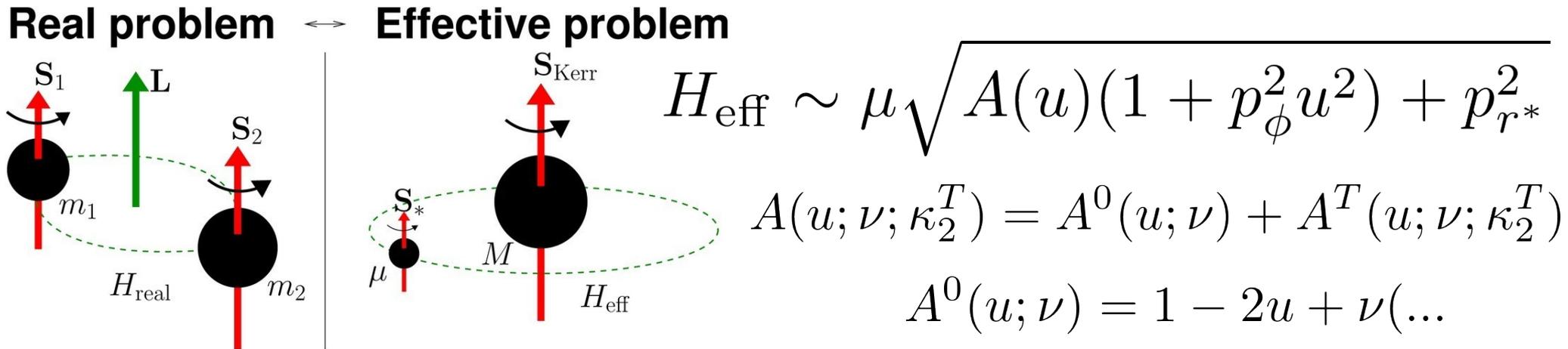
Separation distance



Mass-ratio

Effective-One-Body

[Buonanno&Damour PRD 1999,2000]

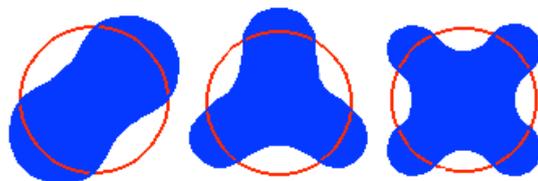
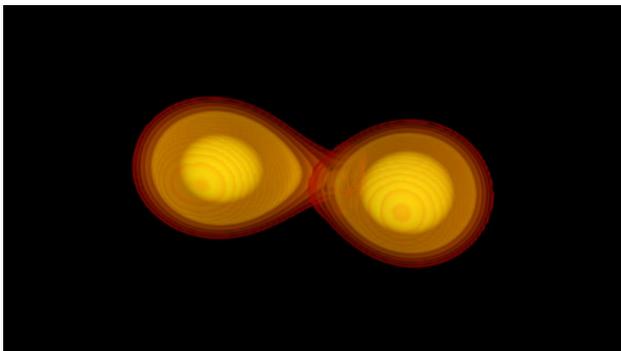


Credit: A.Taracchini/AEI

- Includes test-mass limit (i.e. particle on Schwarzschild)
- Includes post-Newtonian and self-force results
- Uses resummation techniques → predictive strong-field regime
- **Includes tidal interactions** (→ BNS) [Damour&Nagar PRD 2010]
- Flexible framework, can include NR results (“NR-informed”)
- Most accurate framework to describe compact binary waveforms

See e.g. [Taracchini+ PRD 2014][SB+ PRL 2015][Nagar+ PRD 2015][Hinderer+ 2016]

Relativistic Tides



[Hinderer arXiv:0711.2420,
Damour&Nagar arXiv:0906.0096,
Binnington&Poisson arXiv:0906.1366]

$$\lambda_2 \propto \frac{Q_{ij}}{\partial_{ij} \Phi_{ext}}$$

$$\kappa_2^T = 2 \left[\frac{X_A}{X_B} \left(\frac{X_A}{C_A} \right)^5 k_2^A + \frac{X_B}{X_A} \left(\frac{X_B}{C_B} \right)^5 k_2^B \right]$$

[Damour&Nagar arXiv:0911.5041]

Tidal contribution to (post-) Newtonian dynamics and waveform:

Hamiltonian
(Newtonian limit):

$$H_{\text{EOB}} \approx Mc^2 + \frac{\mu}{2} (\mathbf{p}^2 + A(r) - 1)$$

$$A(r) = 1 - 2/r - \kappa_2^T (\lambda_2) / r^6$$

*Tides are attractive and
"act" at small separations*

Tidal coupling
constant

Waveform:

$$h \sim Af^{-7/6} e^{-i\Psi(f)} \approx Af^{-7/6} e^{-i\Psi_{PP}(f) + i39/4 \kappa_2^T x(f)^{5/2}}$$

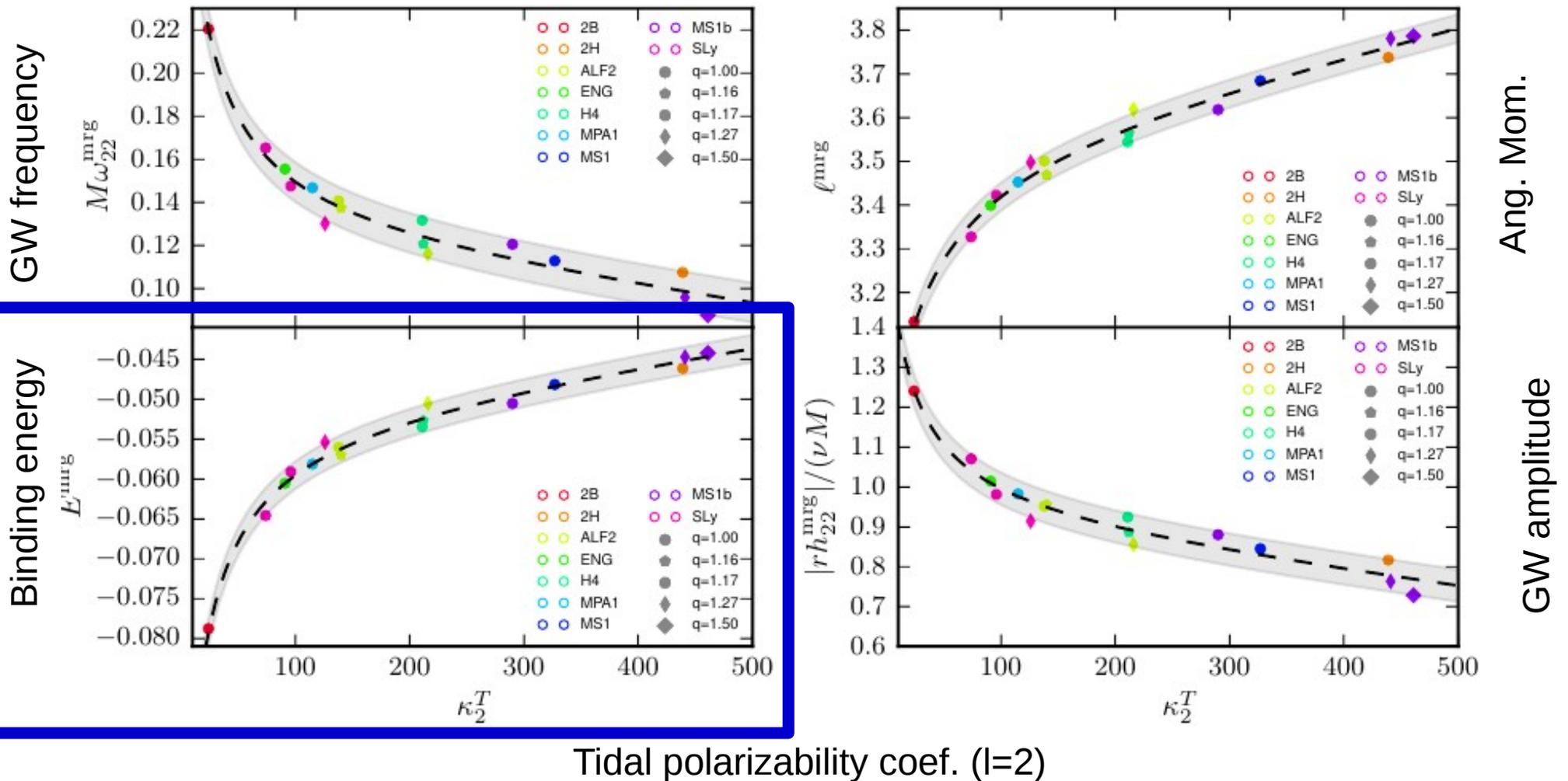
Key point: No other binary parameter (mass, radii, etc) enter separately the formalism

One parameter to characterize merger dynamics

[SB,Nagar,Balmelli,Dietrich,Ujevic PRL 112 (2014)]

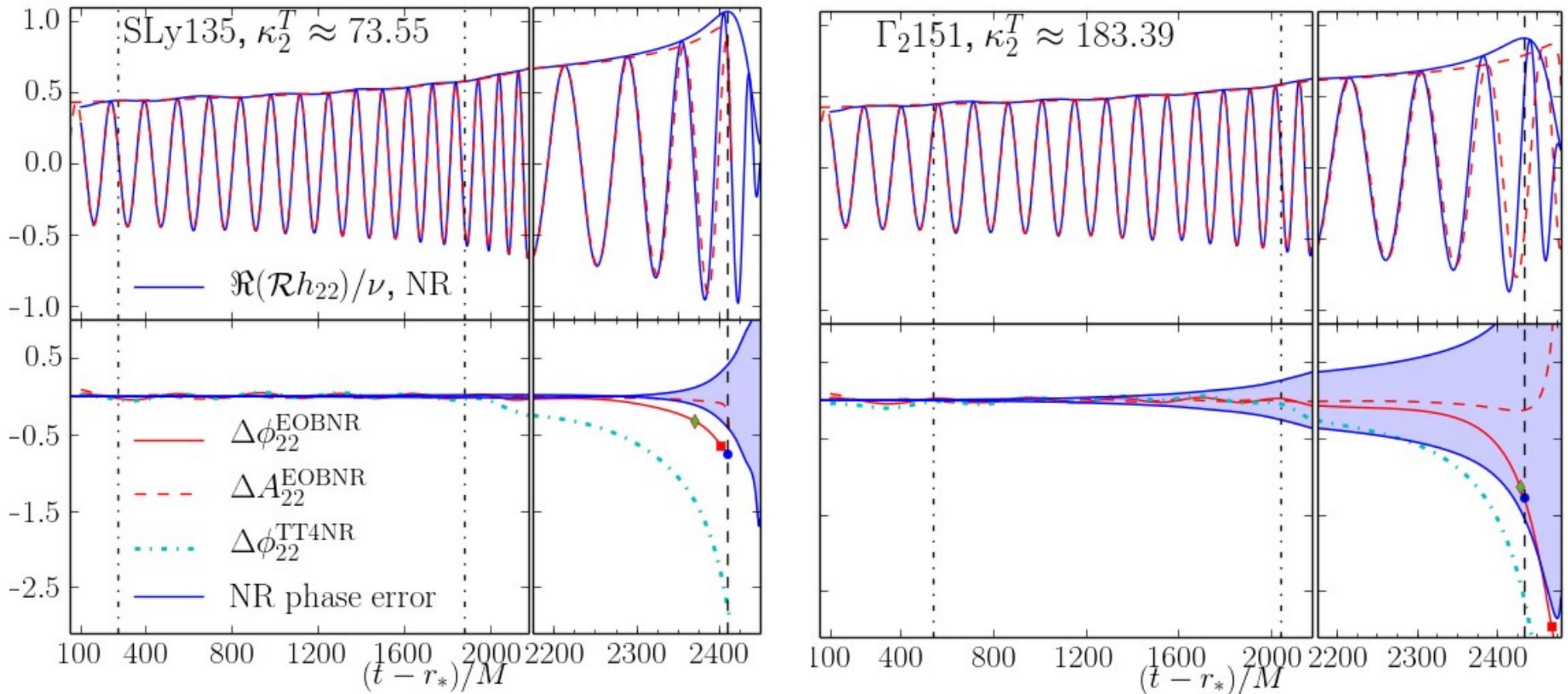
Predict energy emitted in GW for all binaries, range 1-2% M
(all possible EOS, masses, mas-ratios)

Predict energy emitted for given binary by specifying solely the kappa value



First waveform model for **inspiral** → **merger**

[SB,Nagar,Dietrich,Damour PRL 114 (2015)]



- Effective-one-body model with tides, GSF Resummed approach [Bini+ 2014]
- Valid from low frequencies to merger, PREDICT the merger waveform
- Accuracy: uncertainties of the numerical data (improve simulations!)

See [Hinderer+ PRL 116 (2016)] for an alternative approach

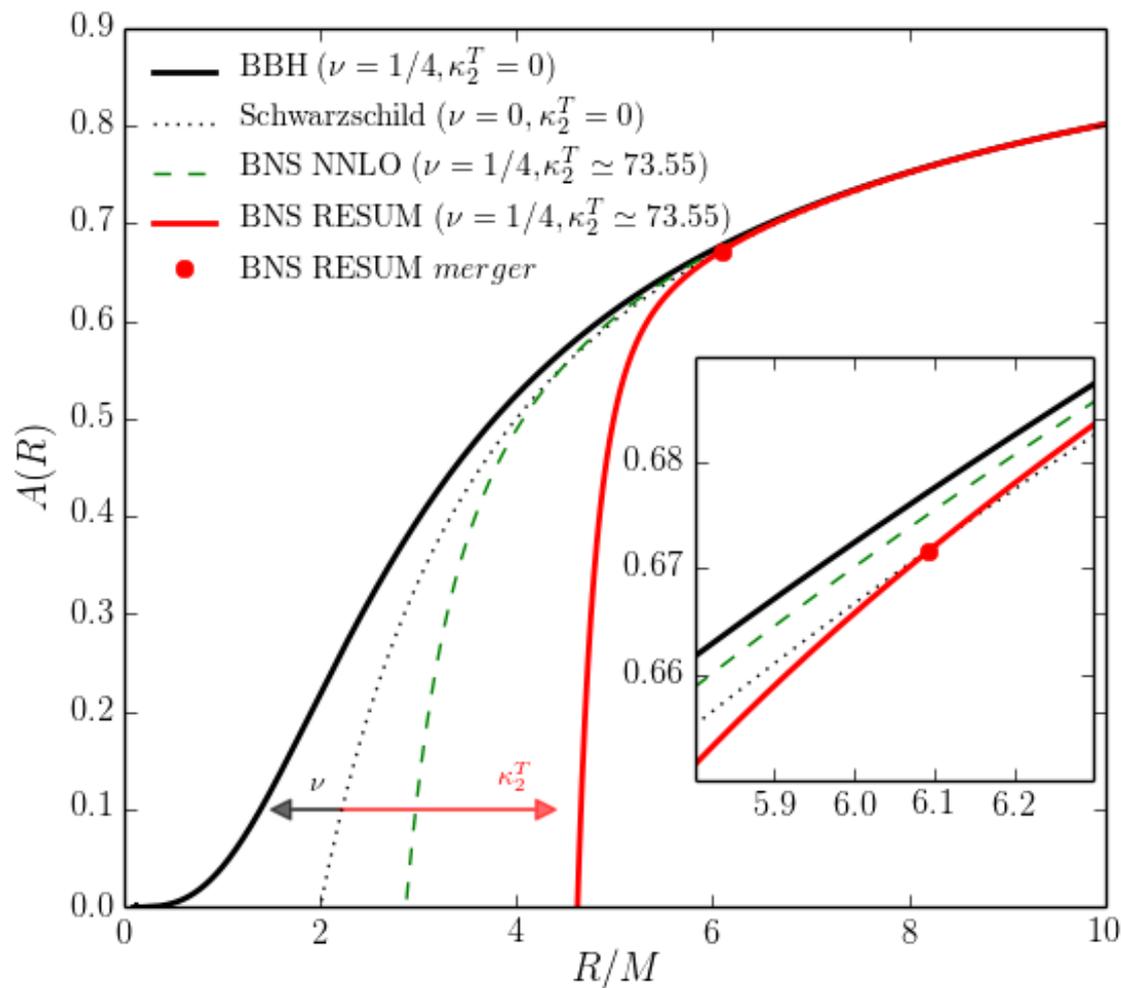
A GSF-based A(R) potential

$$H_{\text{EOB}} \approx Mc^2 + \frac{\mu}{2} (\mathbf{p}^2 + A(r) - 1)$$

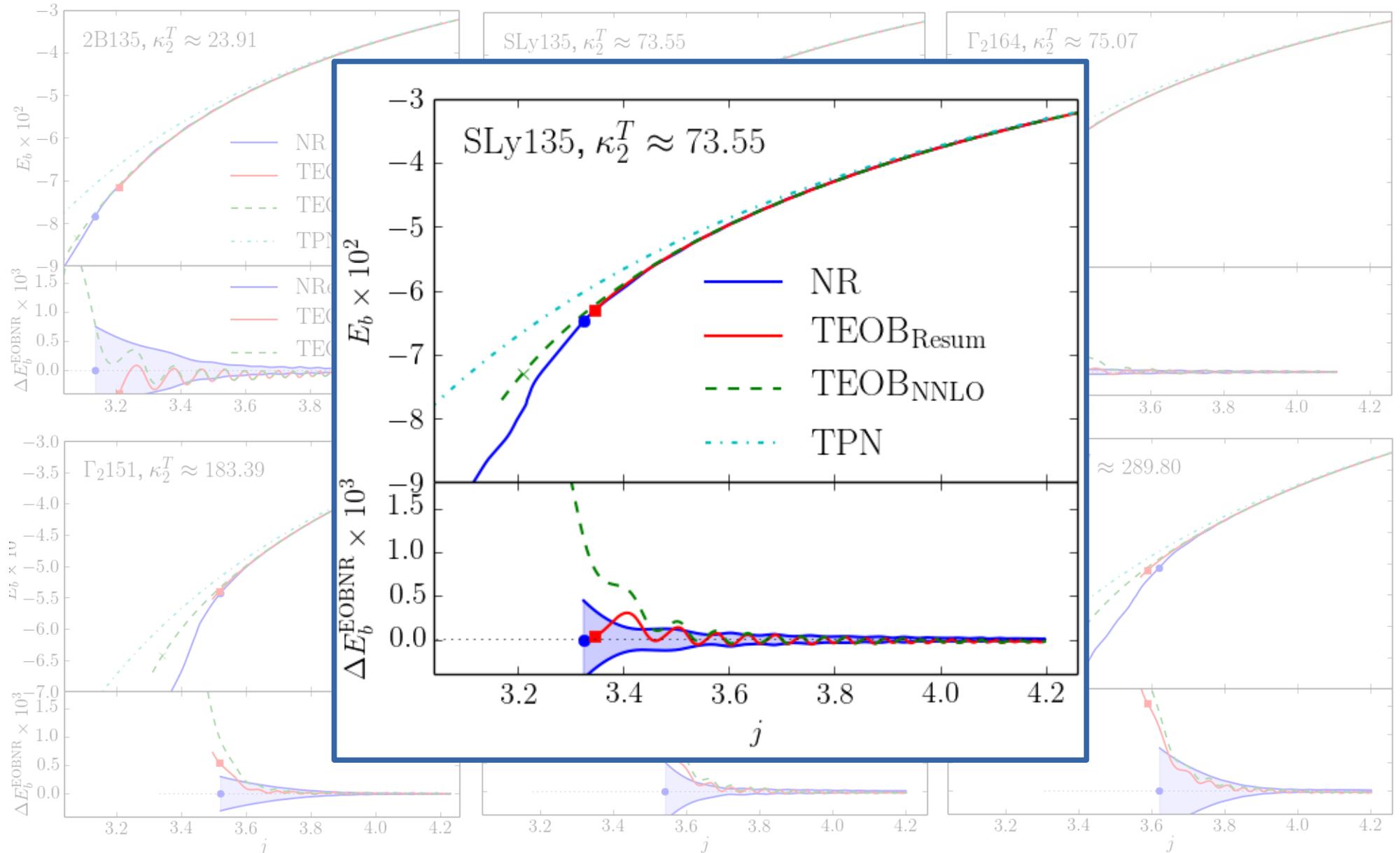
$$A(r) = 1 - 2/r - \kappa_2^T(\lambda_2)/r^6$$

[Bini&Damour PRD 2015]

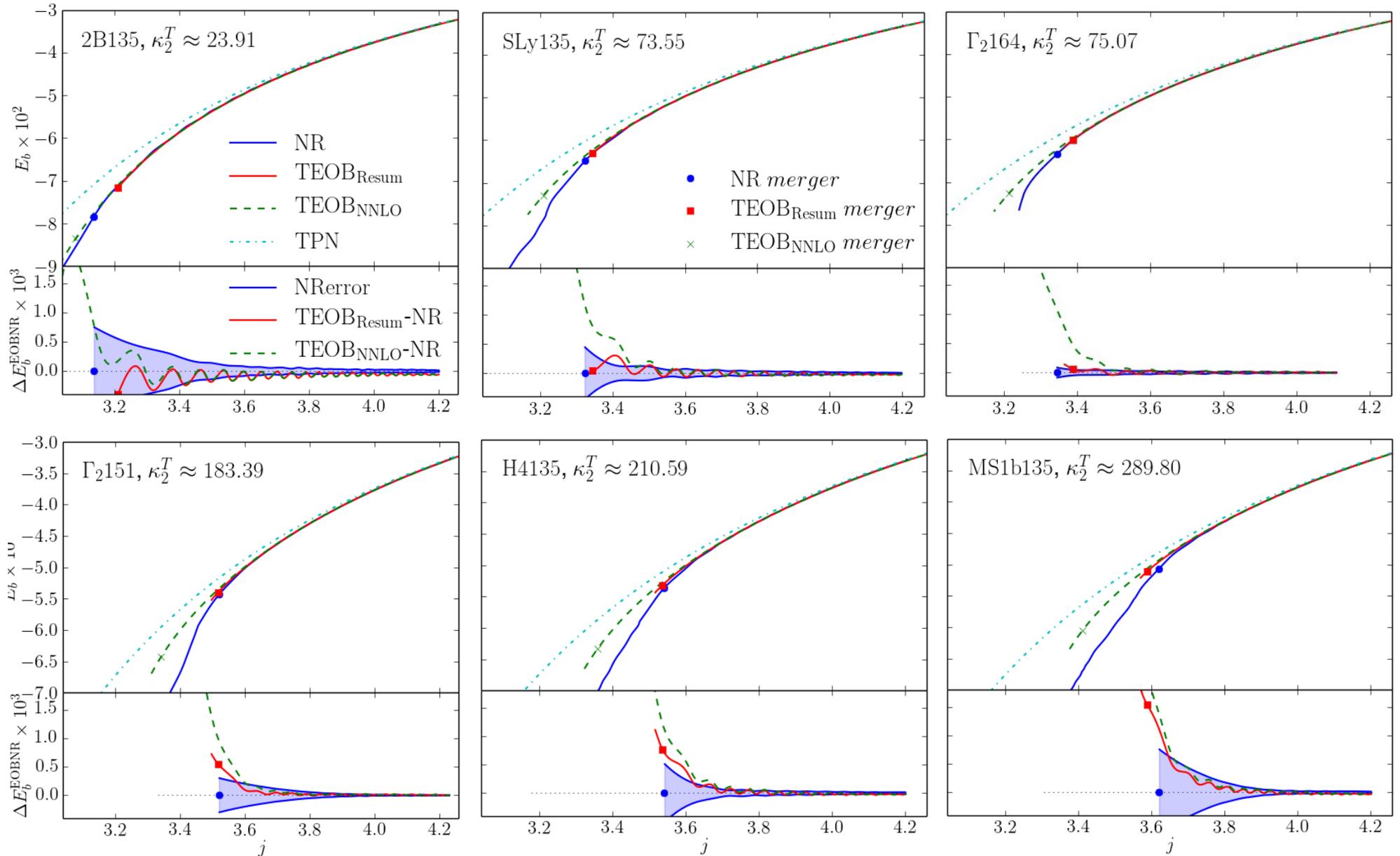
[SB,Nagar,Dietrich,Damour PRL 2015a]



Performance of the resummed tidal potential

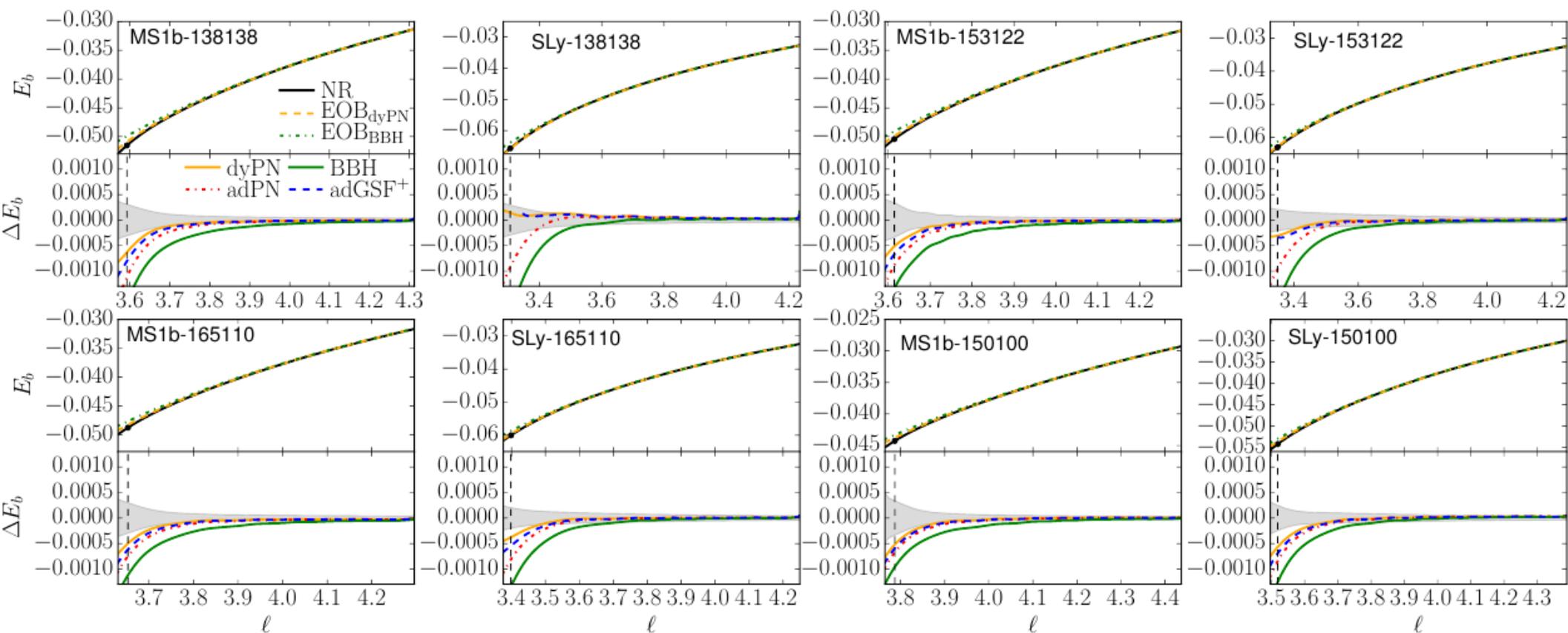


Performance of the resummed tidal potential



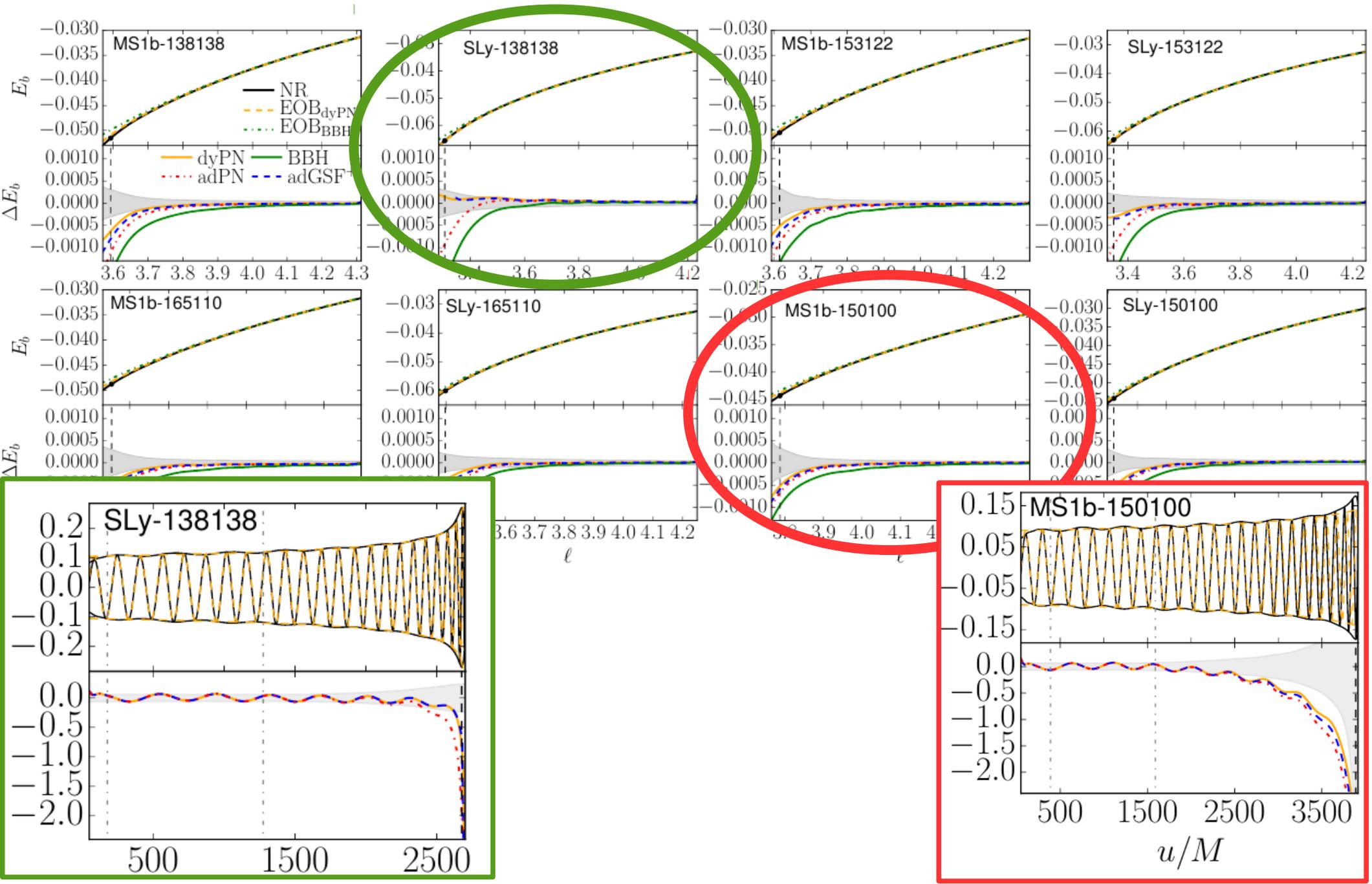
Comparison of EOB tidal models

[Dietrich&Hinderer arXiv:1702.02053]



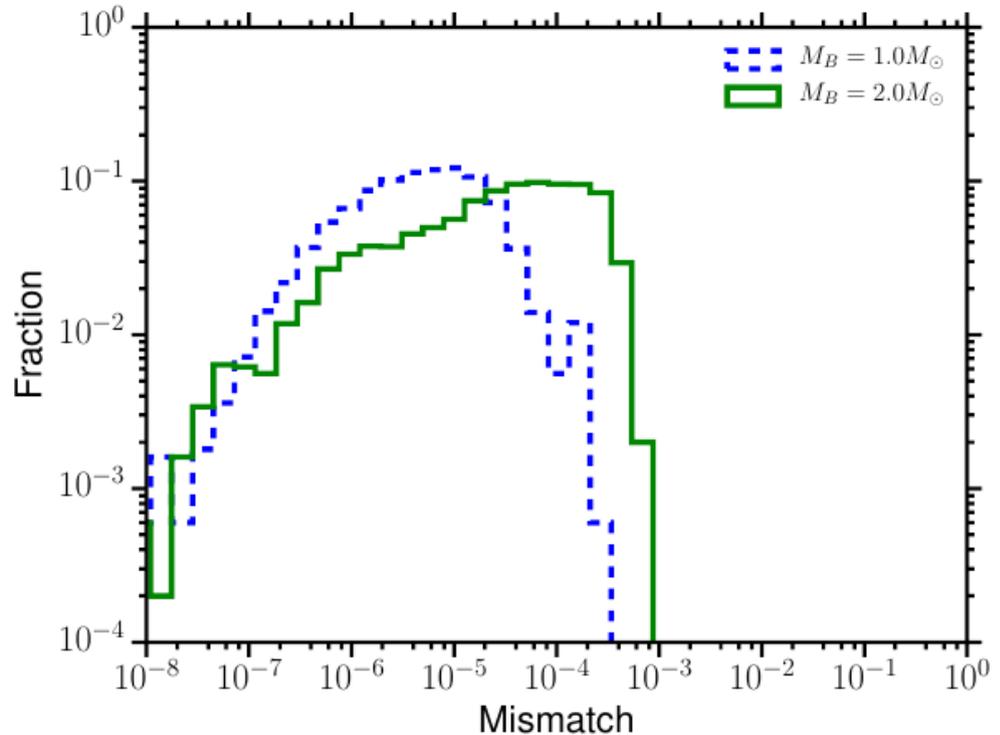
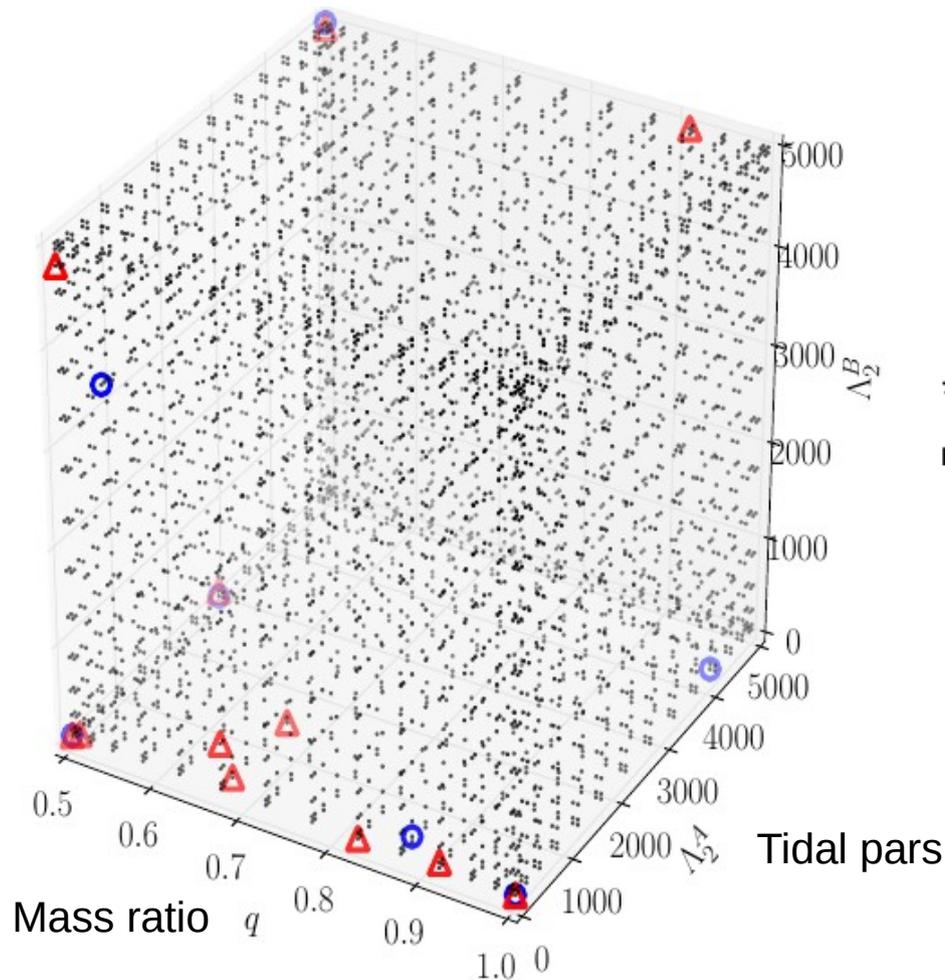
Comparison of EOB tidal models

[Dietrich&Hinderer arXiv:1702.02053]



Fast templates for GW data-analysis of BNS

[Lackey, SB, Galley, Meidam, Van Den Broeck PRD (2017) – In Press]

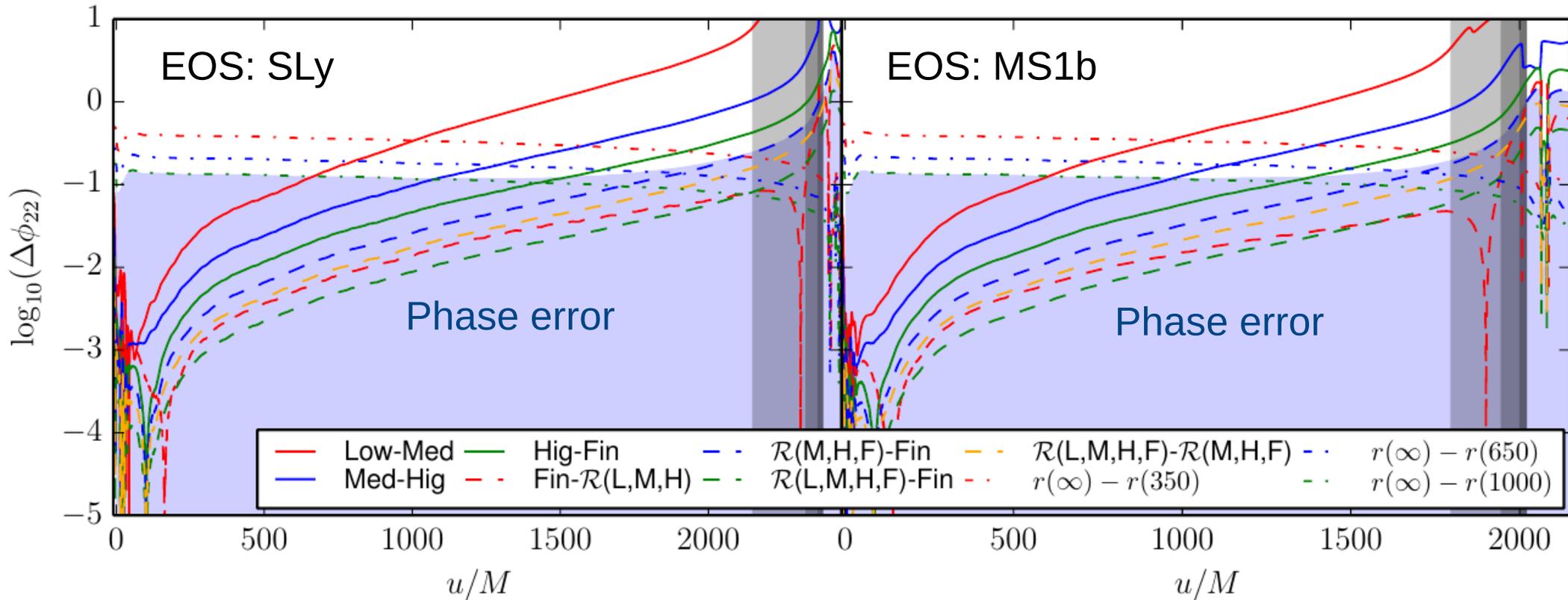


First model accurate to merger available in LIGO/Virgo library

- **SURROGATE** technique
- Training set in 3D par space: Chebyshev-Gauss-Lobatto 16^3 nodes.
- Basis #: 12 amplitude, 7 phase + Empirical interpolation
- Speed = ~ 0.07 s (30 Hz to mrg); ~ 0.8 s (10 Hz to mrg) \rightarrow enable 10^7 - 10^8 evaluations (PE)

Improved NR GW with high-order WENO schemes

[SB,Dietrich PRD94 064062 (2016)]

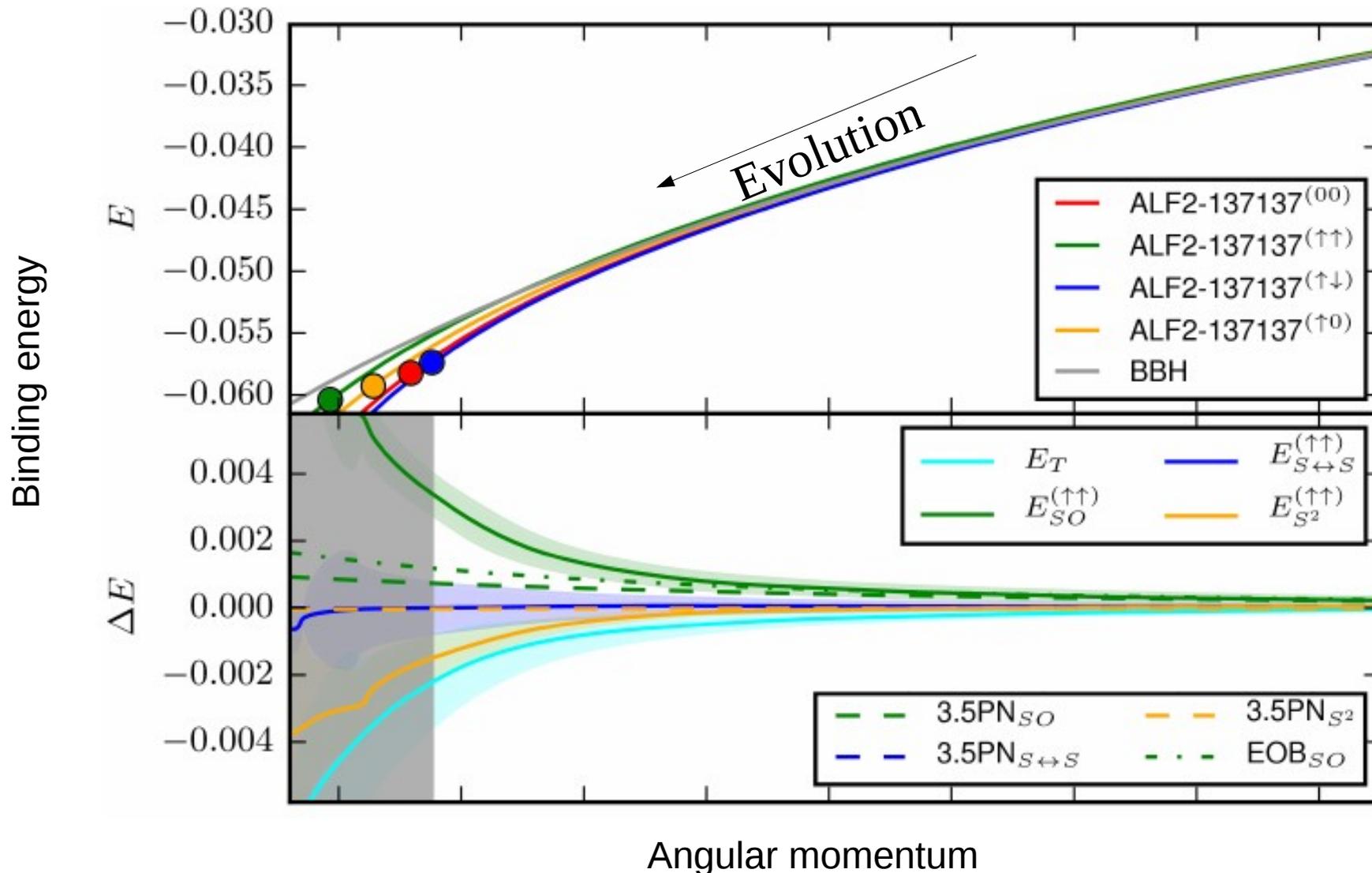


- Robust convergence assessment (although not 5th order)
- Large resolution span (64^3 - 192^3), no alignment
- Error budget: significant improvement wrt FV schemes

See also [SB+ arXiv:1205.3403] [Radice+ arxiv:1306.6052]

Spins & tides during merger: energetics

[Dietrich, SB, Ujevic, Tichy PRD 95 (2017)]

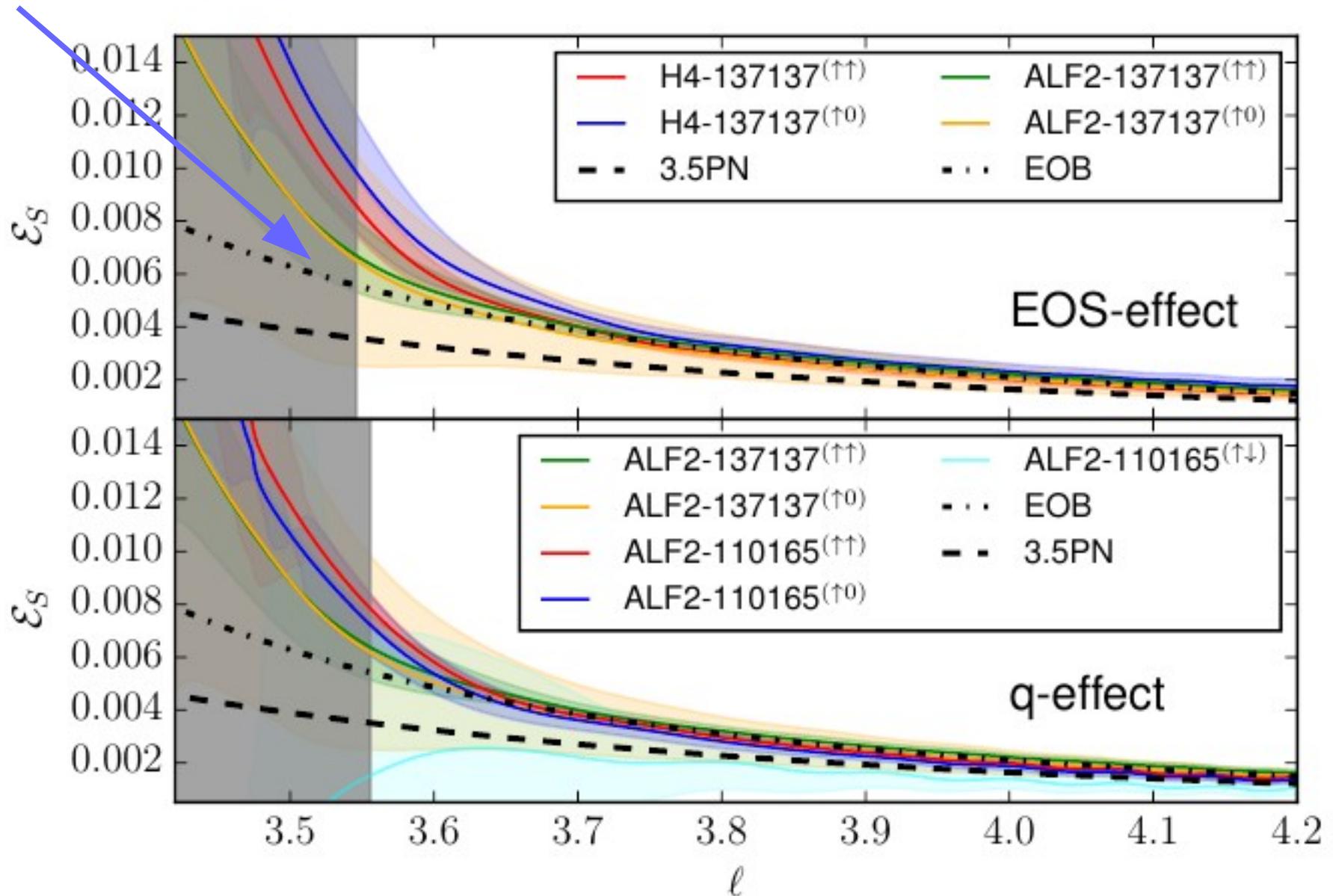


See also [SB, Dietrich, Tichy, Bruegmann arXiv:1311.4443]

Spins & tides during merger: energetics

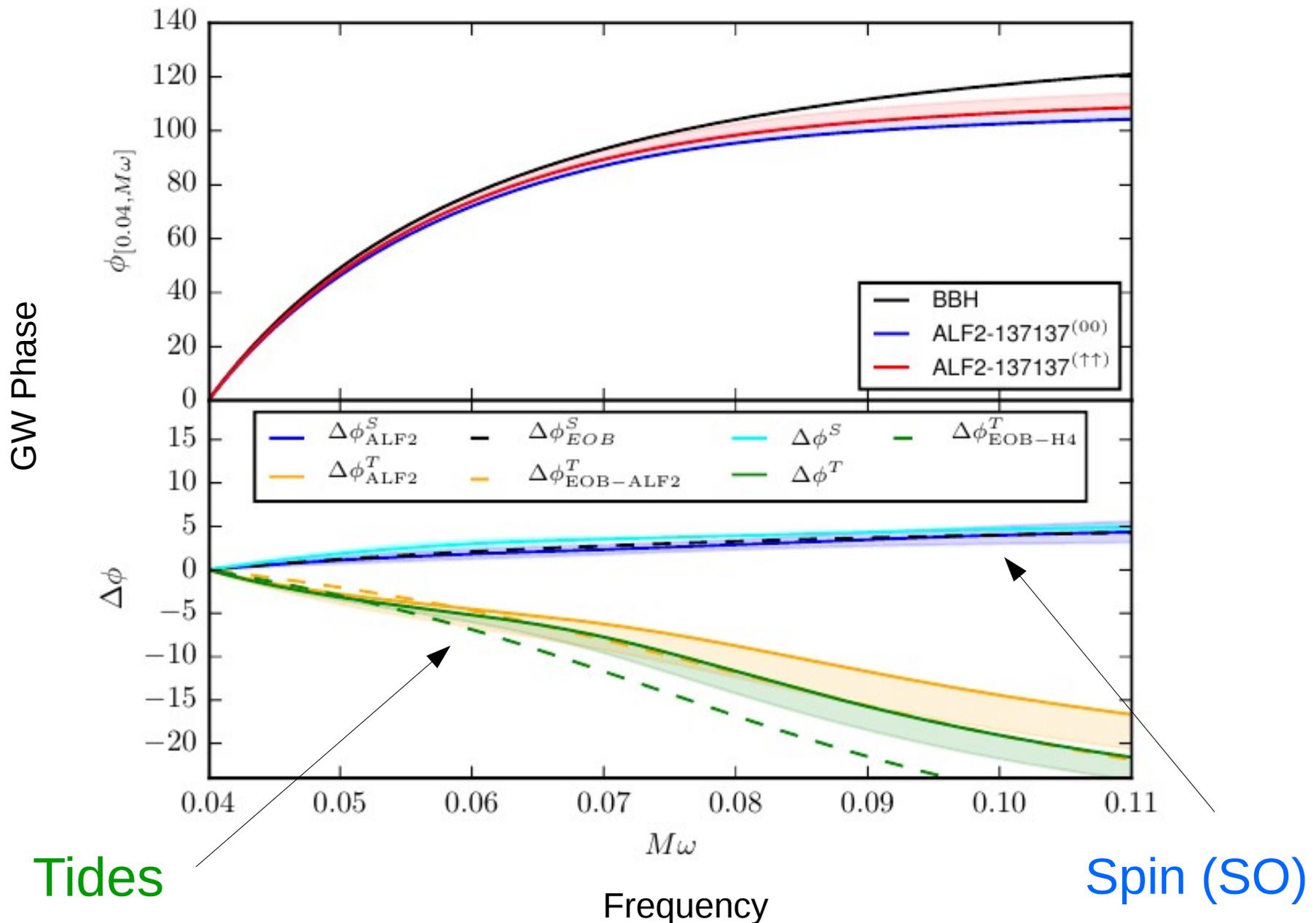
[Dietrich, SB, Ujevic, Tichy PRD 95 (2017)]

Spin-orbit and spin²



Spins & tides during merger: phasing

[Dietrich, SB, Ujevic, Tichy PRD 95 (2017)]



Closed-form tidal approximants from NR

[Dietrich, SB, Tichy arXiv:1706.02969]



$$\phi(\hat{\omega}) \approx \phi_0(\hat{\omega}) + \phi_{SO}(\hat{\omega}) + \phi_T(\hat{\omega})$$

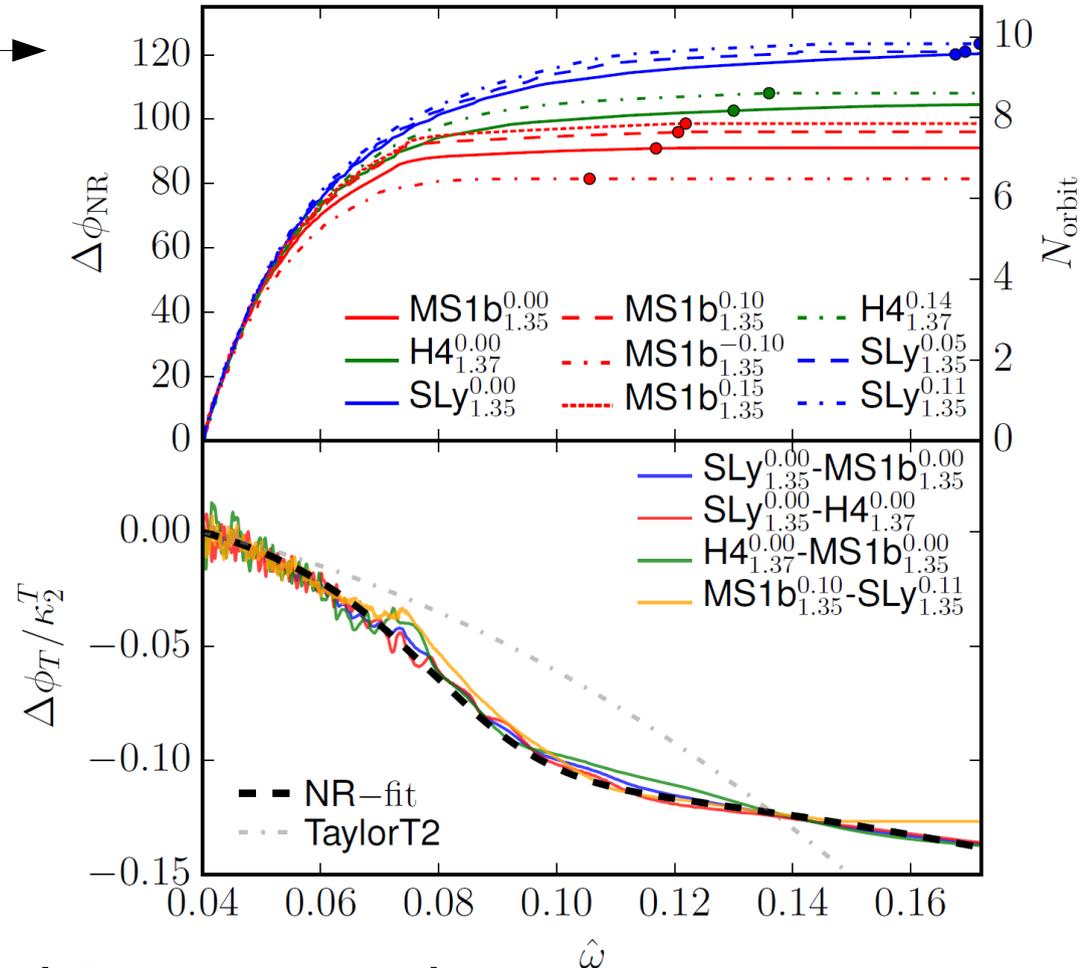
$$\phi_T = -\kappa_2^T \frac{C_{\text{Newt}}}{X_A X_B} x^{5/2} \times \frac{1 + n_1 x + n_{3/2} x^{3/2} + n_2 x^2 + n_{5/2} x^{5/2} + n_3 x^3}{1 + d_1 x + d_{3/2} x^{3/2}}$$

1. Extract tidal phase

2. Fix coefs in effective resummed PN-expression

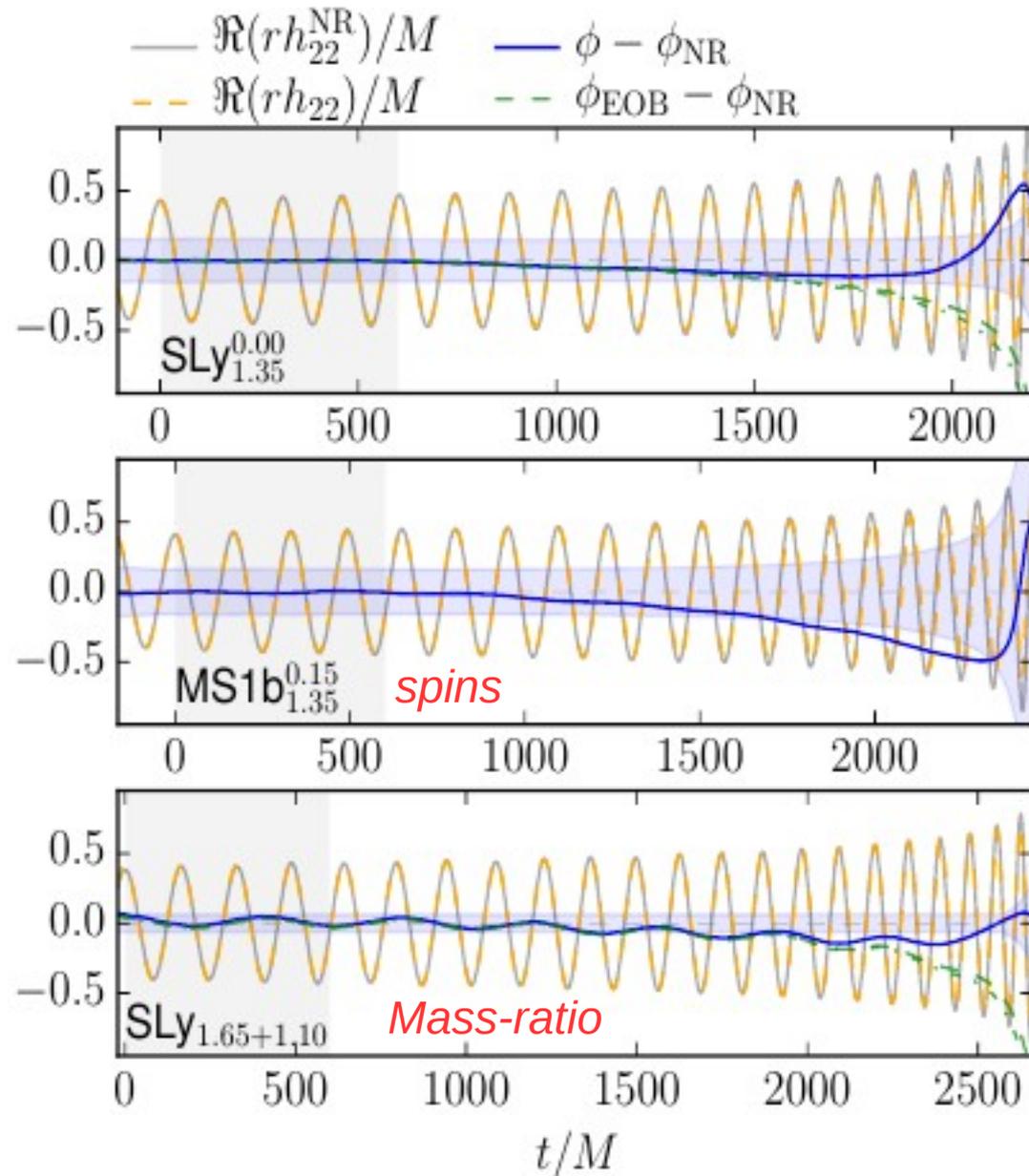
3. Use SPA and freq-domain expression

4. **CAN BE USED WITH ANY BBH BASELINE!**



Time-domain approximant

[Dietrich, SB, Tichy arXiv:1706.02969]



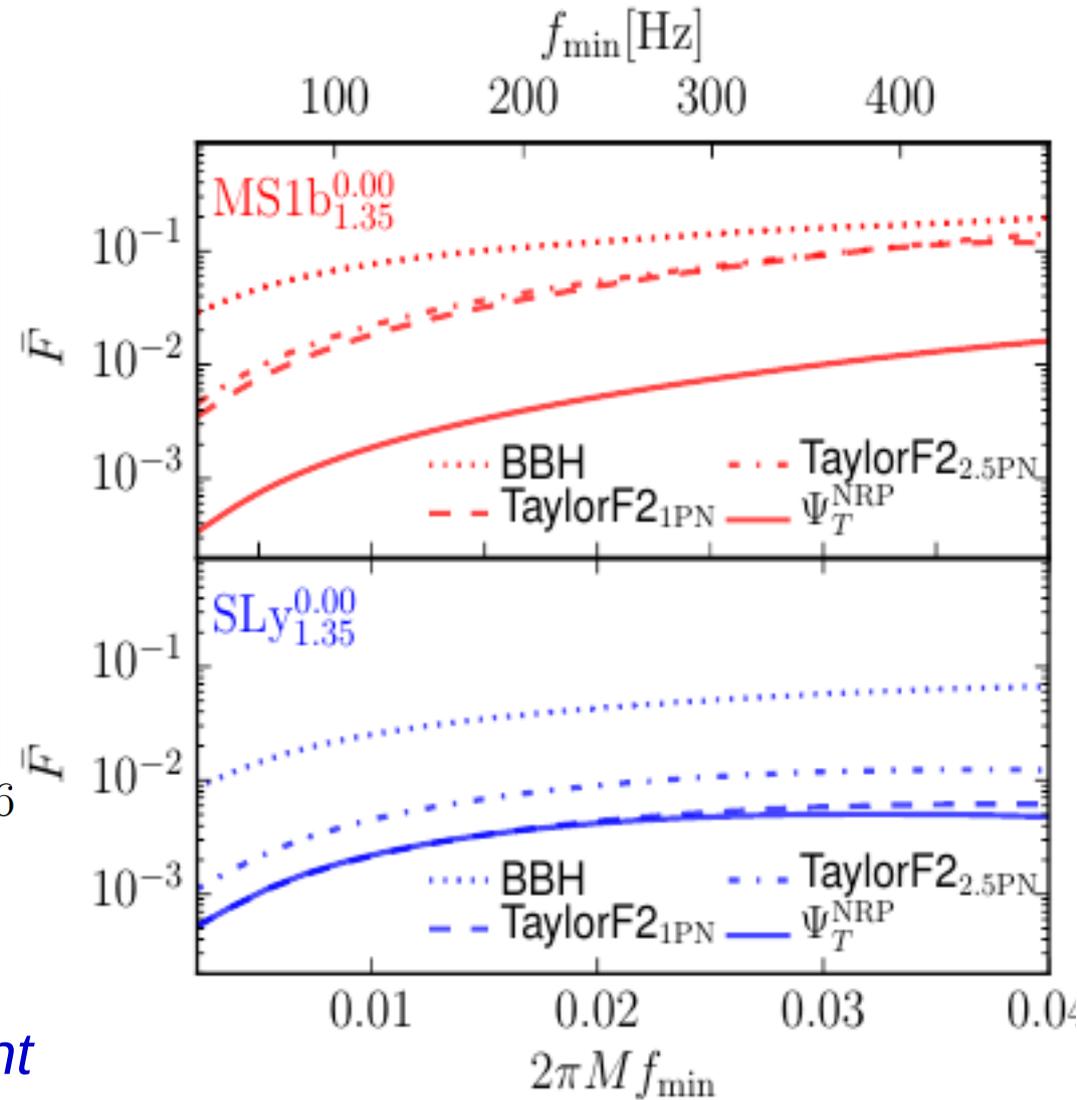
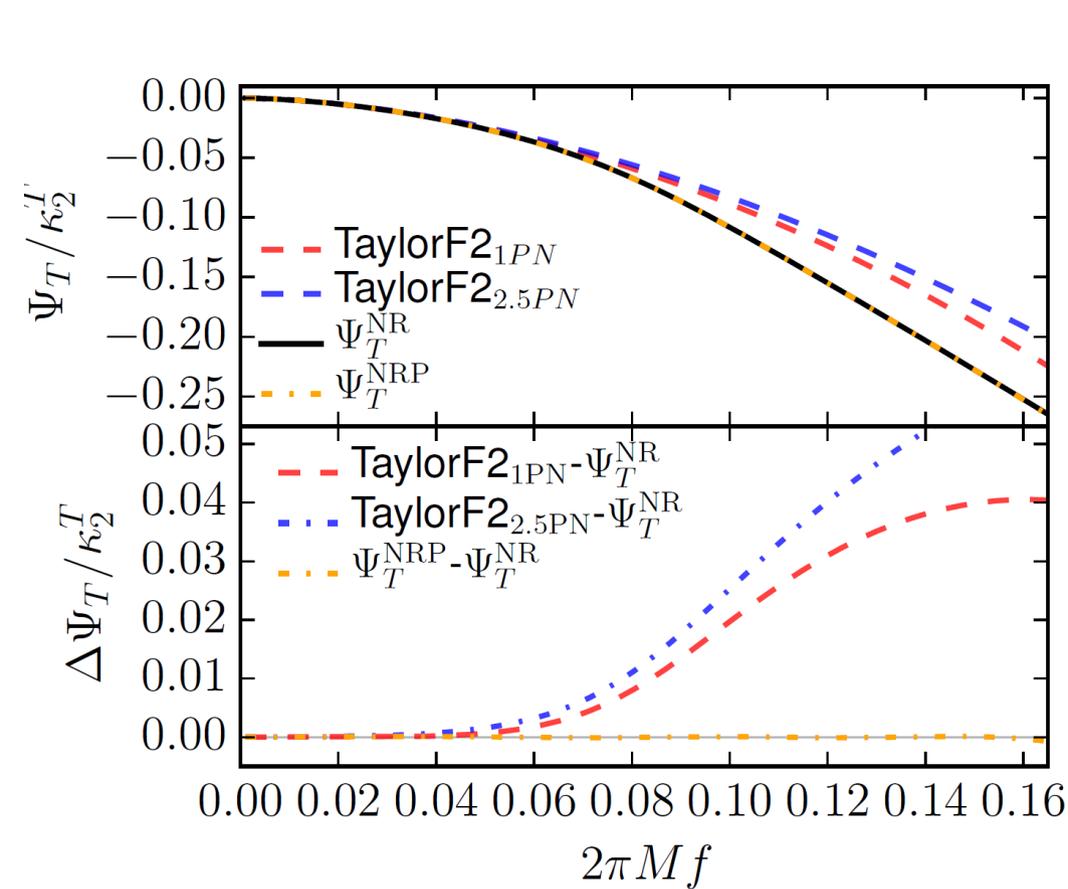
- Compatible with NR (10 orbits)
- Compatible with NR-hybrids (300 orbits)
- Use with any BBH baseline

*New error-controlled (4-5 resolutions)
Eccentricity-reduced ($e \sim 1e-3$)
NR simulations*

*Same performances as
Tidal EOB*

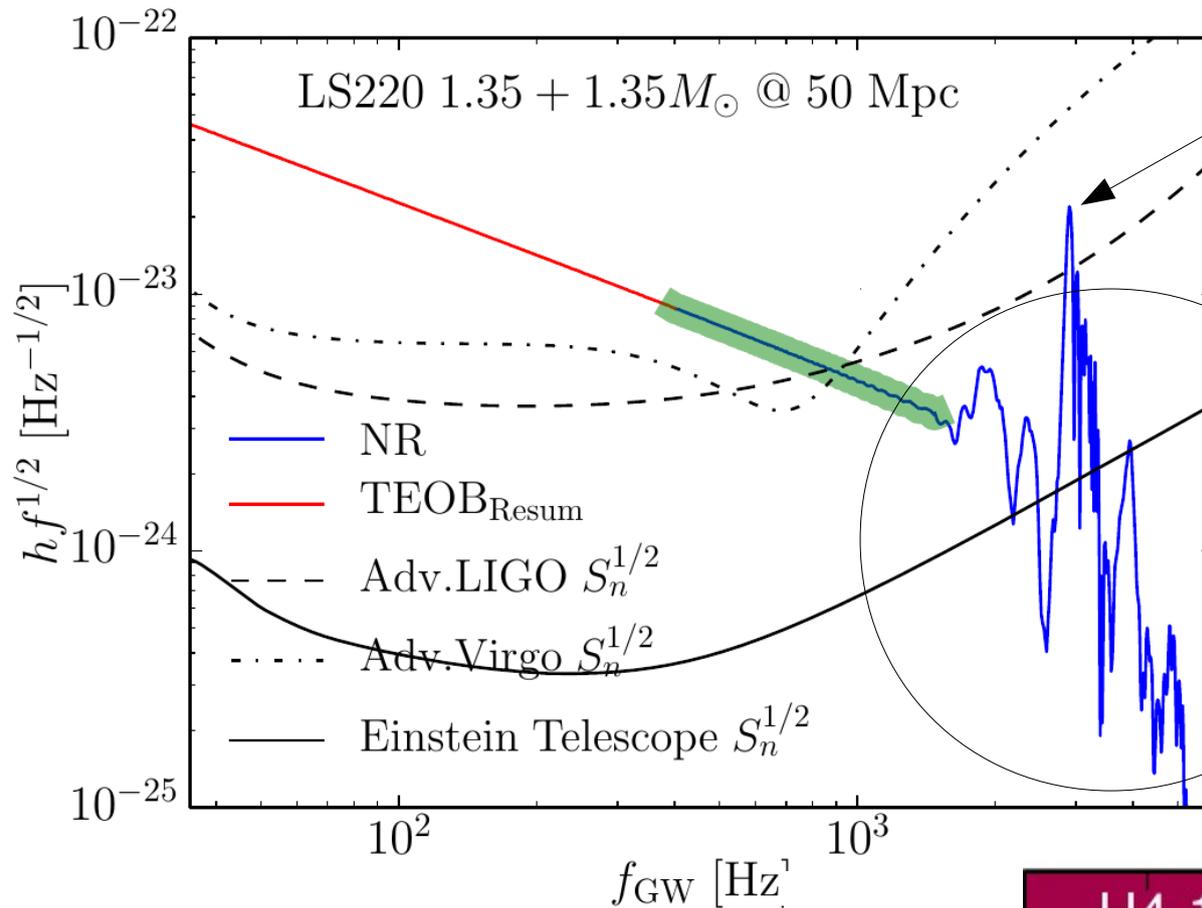
Frequency-domain approximant

[Dietrich, SB, Tichy arXiv:1706.02969]



First NR-based tidal approximant
Fast, flexible, accurate

Postmerger spectrum



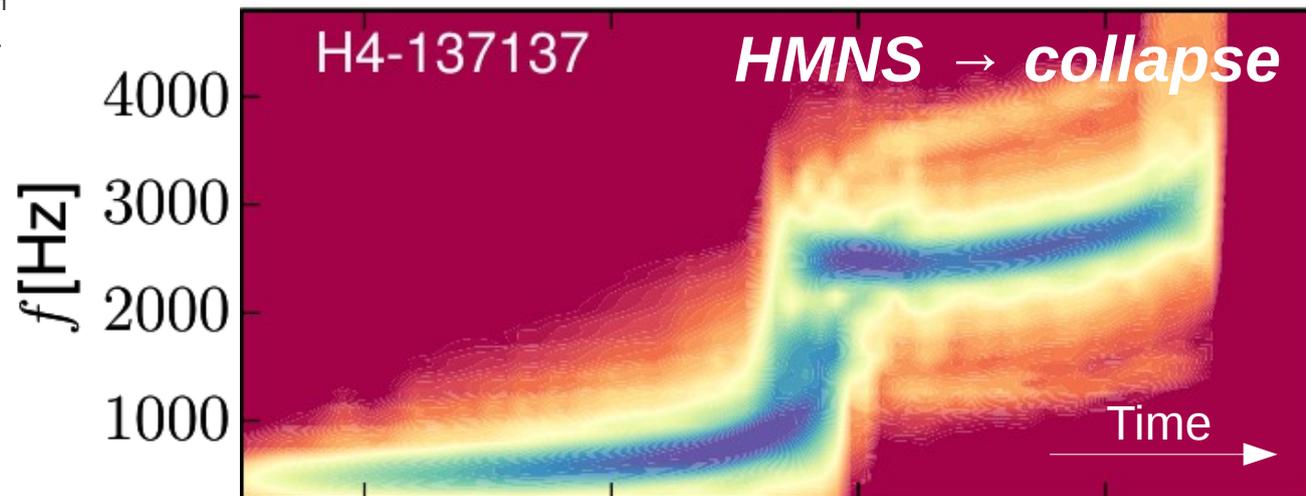
Rich frequency content

Main peak f_2 ($m=2$)

HMNS rot. freq at \sim peak luminosity

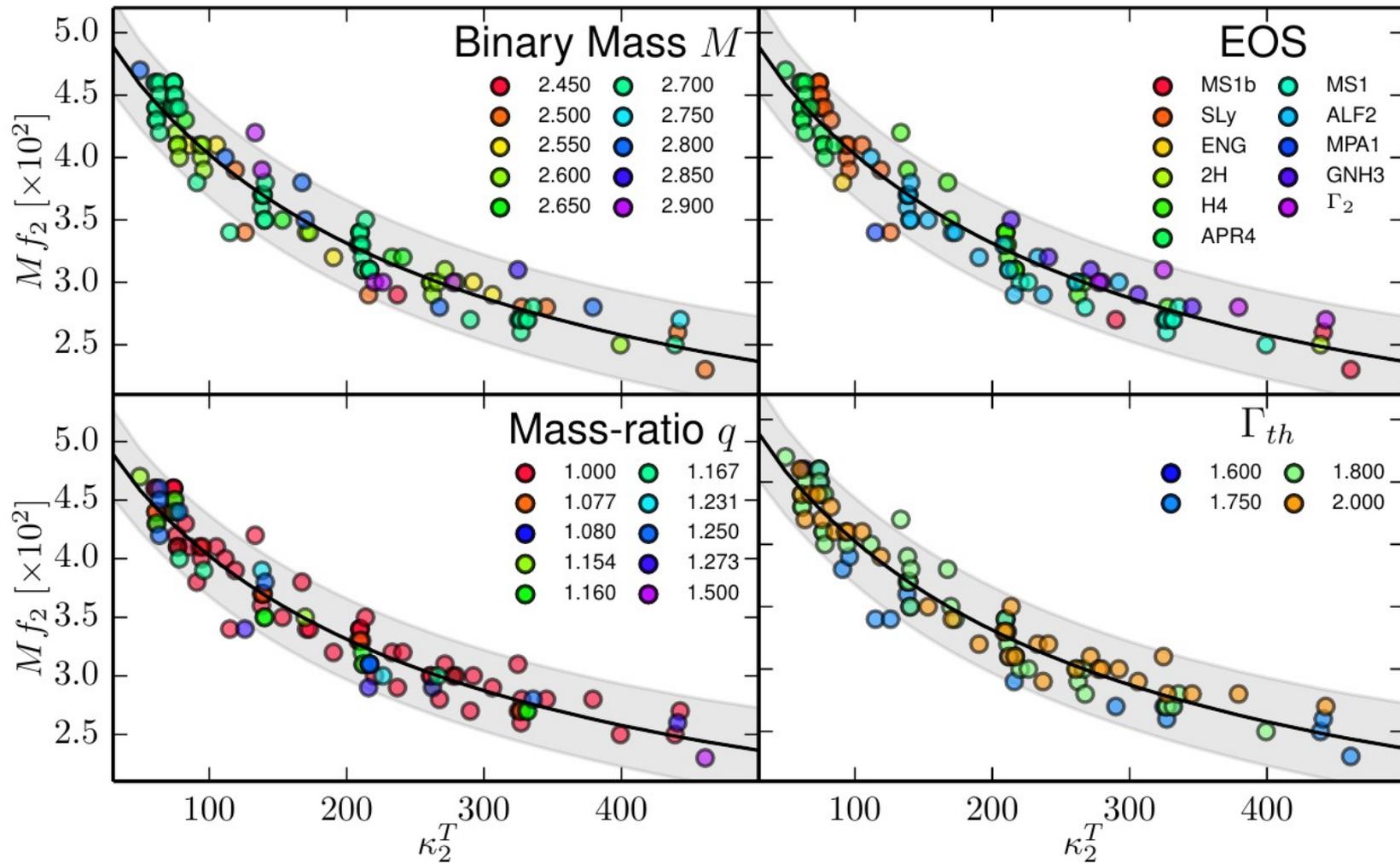
- Various models associate f_2 to isolated equil. star properties
- Possibility to extract “EOS-related info” ($R_x, M_{\text{max}}, \dots$)
- Conceptually independent on inspiral-merger models

[Bauswein+ arXiv:1106.1616,
Hotokezaka+ arXiv:1307.5888,
Takami+ arXiv:1403.5672,
Clark+ arXiv:1509.08522, ...]



Peak frequency correlates to tidal parameter

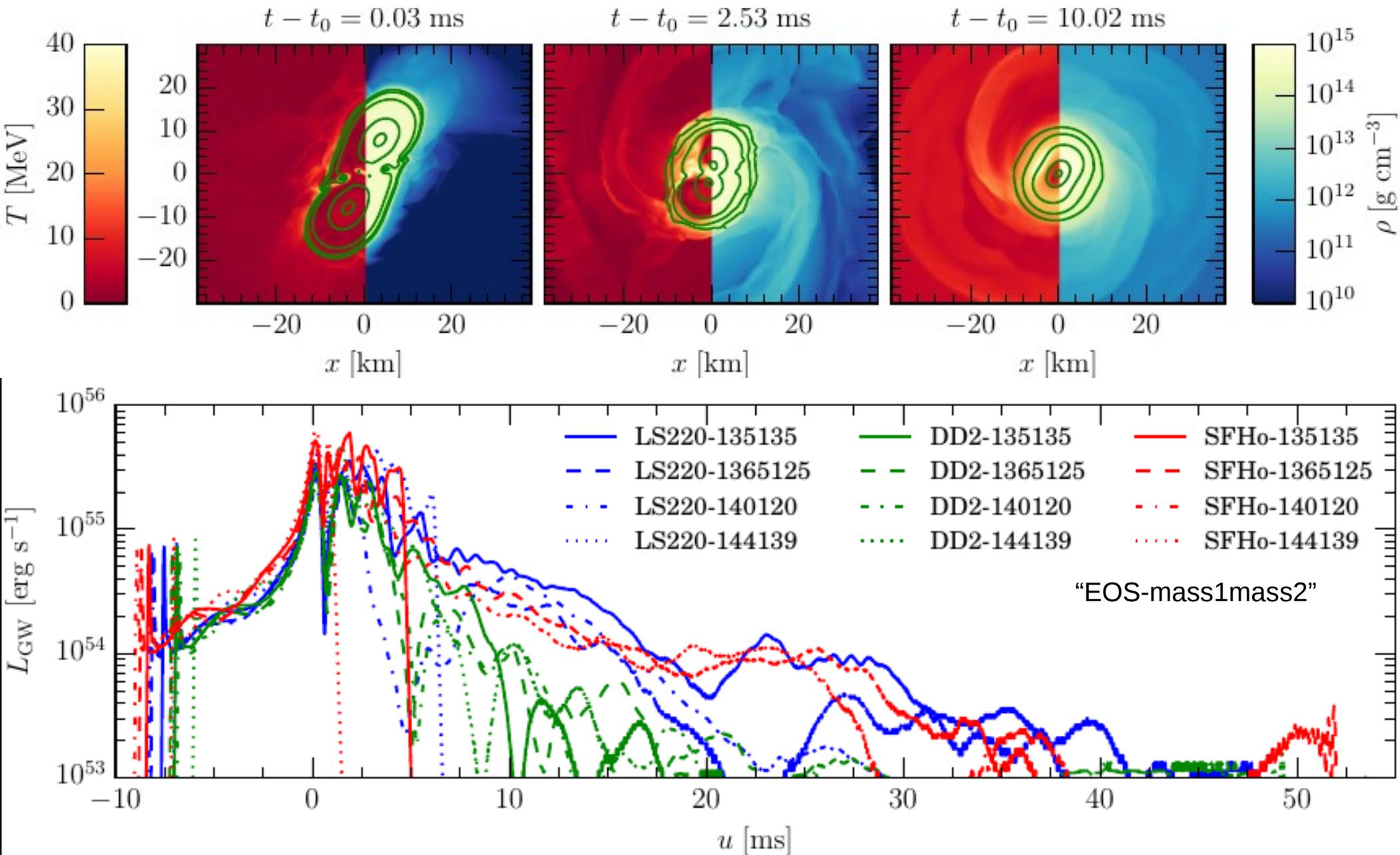
[SB, Dietrich, Nagar PRL 115 (2015)]



- Large NR dataset (~ 100 , 3 codes) [+ Hotokezaka+ arXiv:1307.5888, Takami+ arXiv:1403.5672]
- Postmerger frequencies essentially determined by *merger* physics
- Conceptually “compatible” with inspiral-merger \rightarrow Unified model !

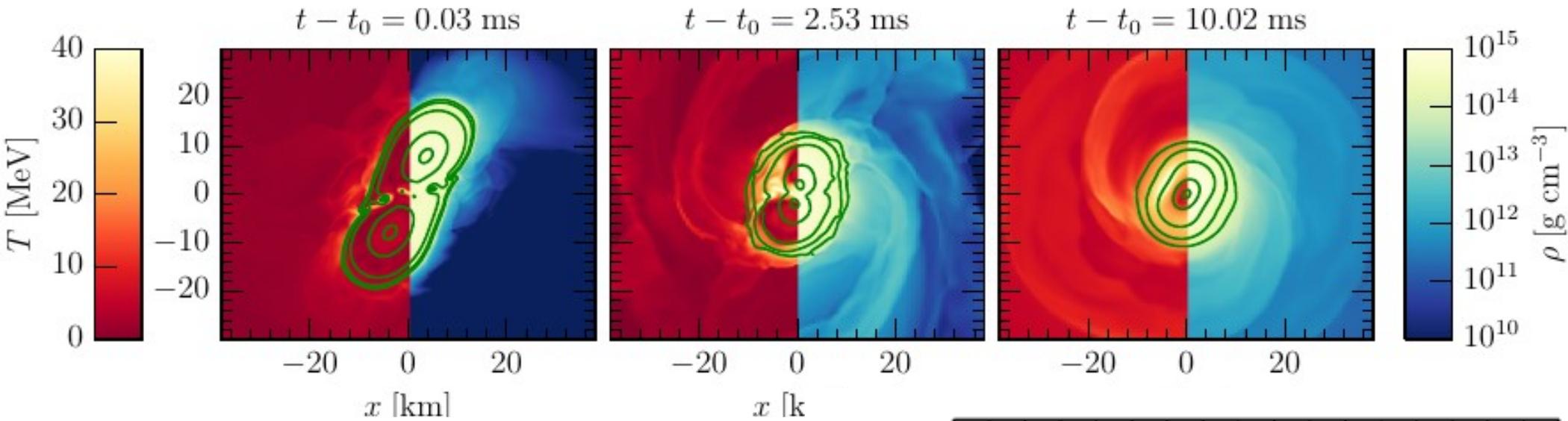
Remnant HMNS is the loudest GW phase

[SB, Radice, Ott, Roberts, Moesta, Galeazzi PRD94 024023 (2016)]



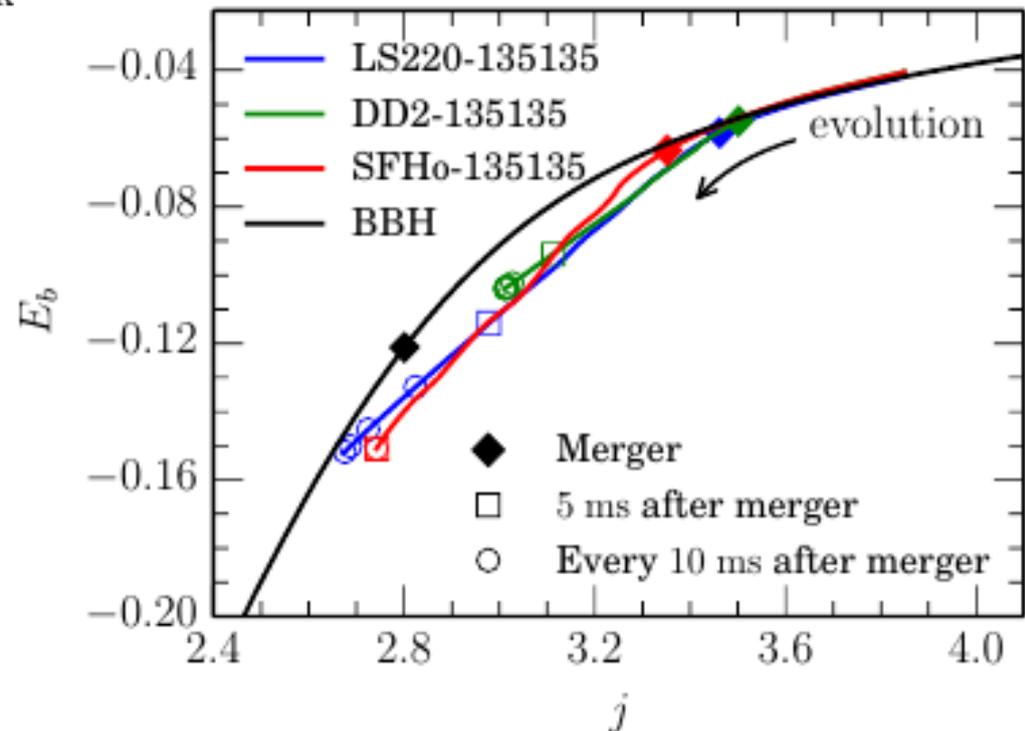
Remnant HMNS is the loudest GW phase

[SB, Radice, Ott, Roberts, Moesta, Galeazzi PRD94 024023 (2016)]



- Emission is FAST: $\tau_{\text{GW}} \sim 20$ ms
- Emission is LOUD: $E(\text{HMNS}) \sim 2x E(\text{merger})$
- Note: explain the $f_2(\kappa_2)$ correlation

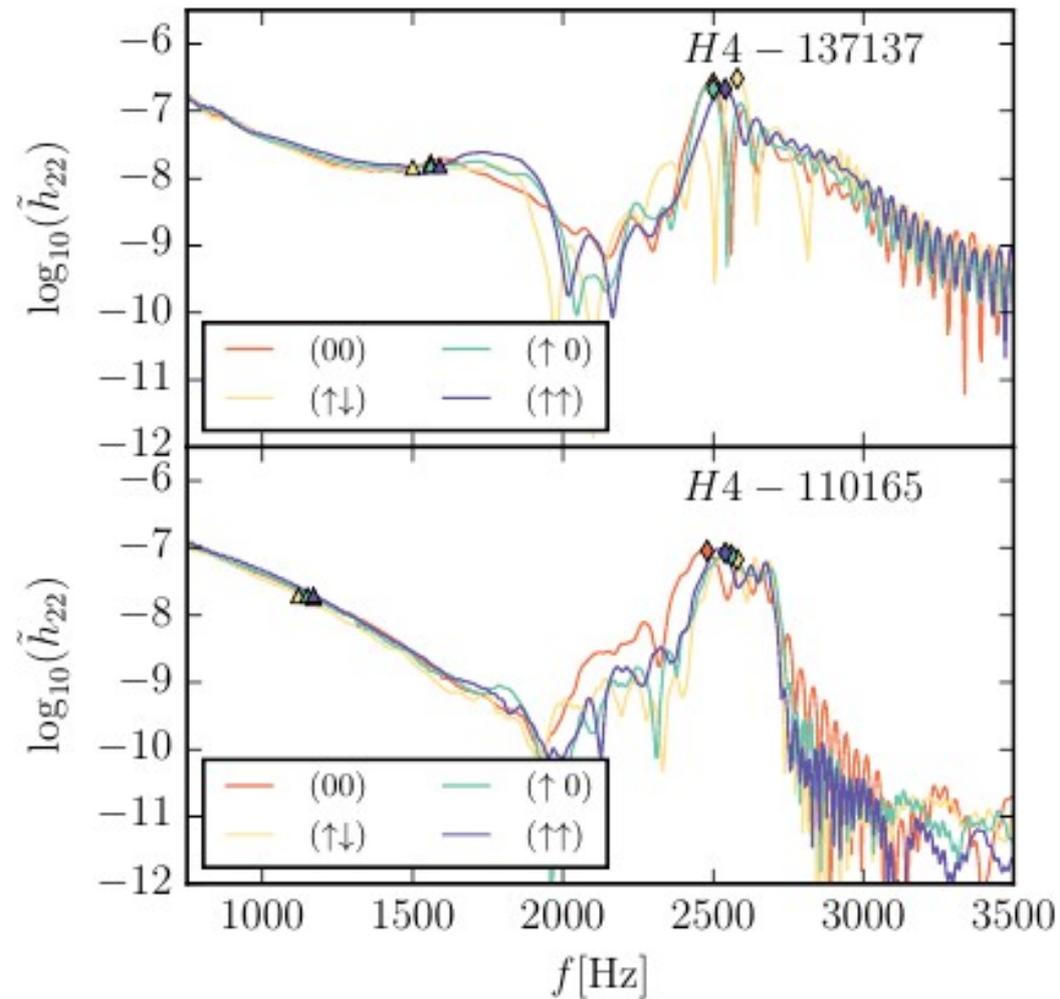
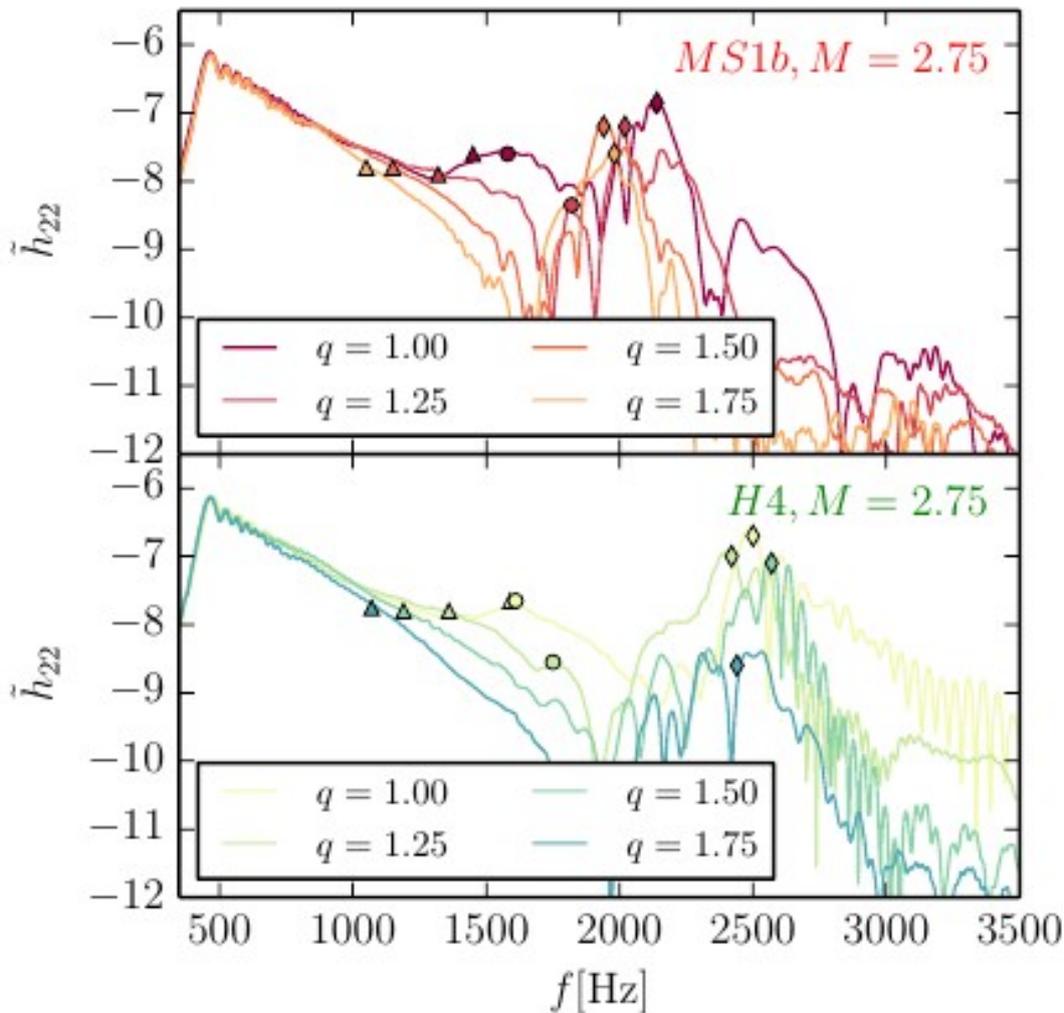
*Simulations w/ microphysics & neutrinos
largest-to-date campaign*



Postmerger spectrum

Mass-ratio effects

Spin effects

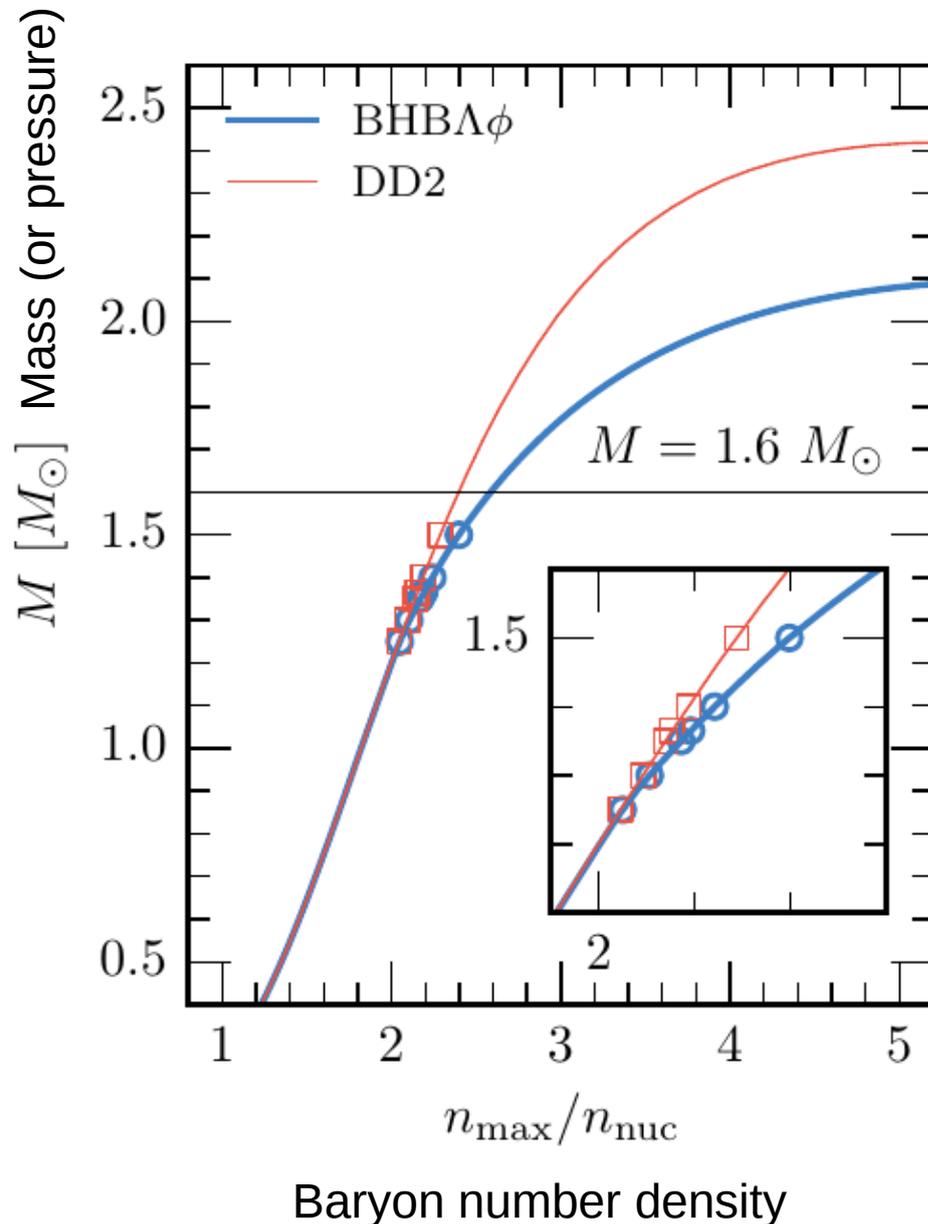


[Dietrich, Ujevic, SB, Tichy, Bruegmann arXiv:1607.06636]

[Dietrich, SB, Ujevic, Tichy arXiv:1611.07367]

Merger remnant reaches extreme densities

Can GW observations inform us about EOS changes at those densities?

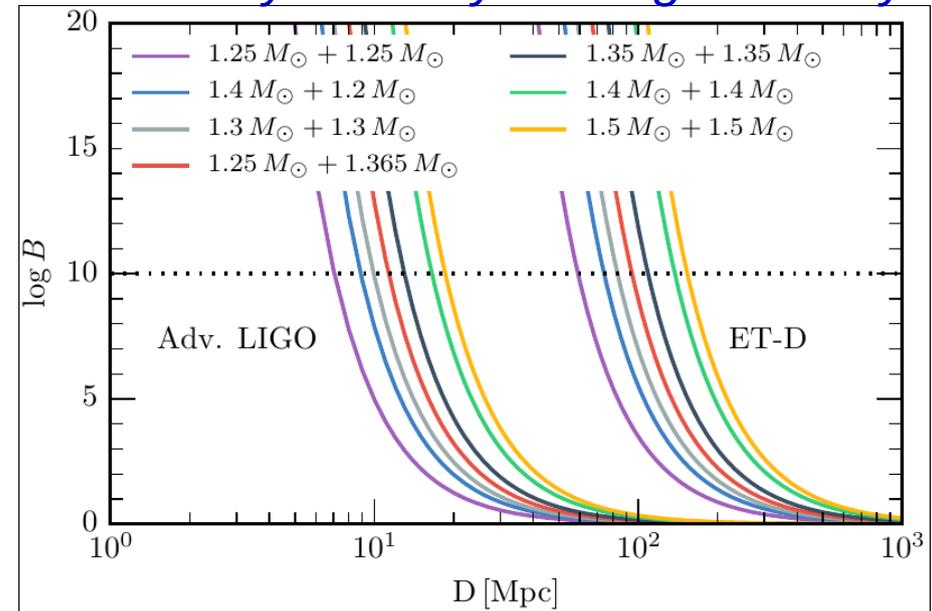
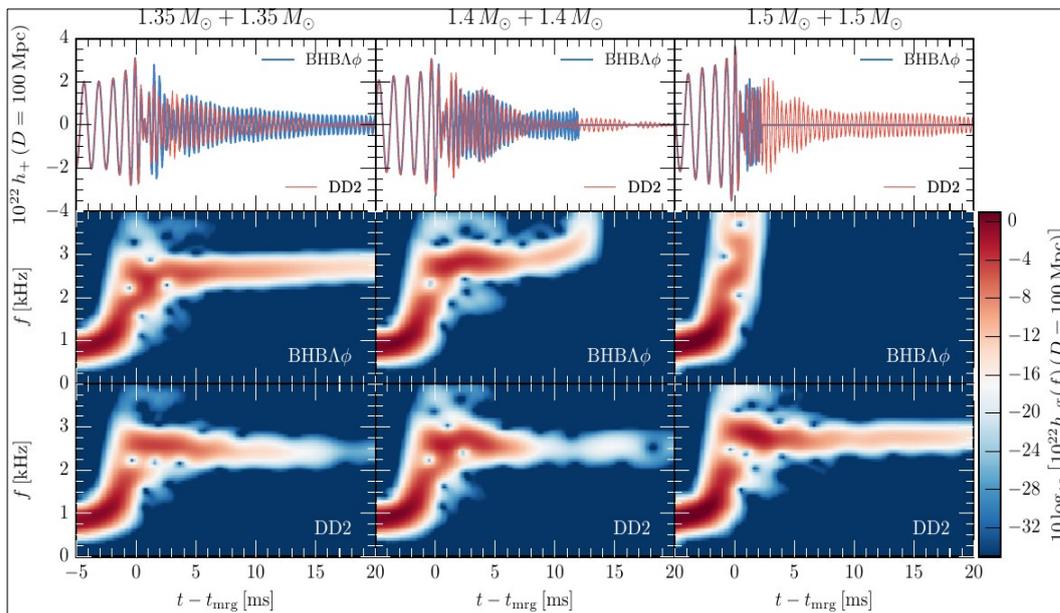


- Baryon number density $n \sim 3\text{-}5 n_{\text{nuc}}$
- Extra DOF/phase transitions?
- Specific model: Λ -hyperons
[Banik+ arxiv:1404.6173]
Microphysical EOS compatible with astro and nuclear phys constraints
- In general: “softness” effects

GWs could probe such “softness effects”

[Radice, SB, Del Pozzo, Ott, Roberts (2017) arXiv:1612.06429]

Data-analysis study: distinguishability



log(Bayes factor) vs. Source distance

- Postmerger GW morphology contains unique info
- Detailed and generic models are necessary for DA studies
- High-freq. GW challenging to detect (→ Einstein telescope)

*** Summary ***

- The (leading order) tidal polarizability coupling constant parametrizes strong-field dynamics and EOS effects [[SB+ arXiv:1402.6244](#)]
- TEOBResum first tidal EOB model “up to merger” [[SB+ arXiv:1412.4553](#)]
- High-order methods help Improving NR simulations [[SB+ arXiv:1205.3403](#), [Radice+ arxiv:1306.6052](#), [SB&Dietrich 1604.07999](#)]
- Fast and efficient representation of waveforms [[Lackey+ arXiv:1610.04742](#)]
- Parameter space: masses, mass ratio, EOS, spins, microphysics [[SB+ arXiv:1311.4443](#), [Dietrich+ arXiv:1611.07367](#), [Dietrich+ arXiv:1607.06636](#), [SB+ arXiv:1512.06397](#), [Radice+ arXiv:1612.06429](#)]
- Energetics and waveforms with spins, first precessing simulation [[SB+ arXiv:1311.4443](#), [Dietrich+ arXiv:1507.07100](#), [Dietrich+ arXiv:1611.07367](#)]
- Postmerger peak frequency correlates with tidal coupling constant [[SB+ arXiv:1504.01764](#)]
- Postmerger emission is “fast and loud” [[SB+ arXiv:1512.06397](#)]