

# ***Optically controlled laser-plasma electron accelerators for compact $\gamma$ - ray sources***

Serge Kalmykov

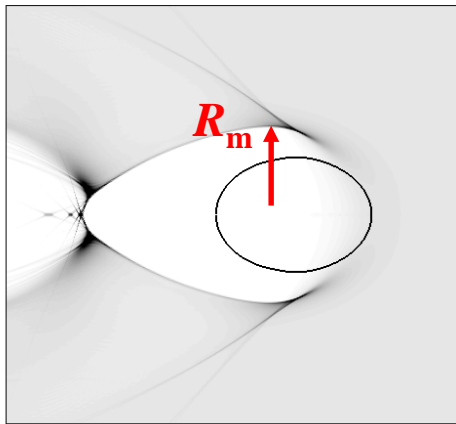
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# Laser-plasma acceleration – transverse matching provides partial control



## Controlling transverse effects:

Match the pulse spot size to

$$R_m = 2^{3/2} k_p^{-1} (P/P_{cr})^{1/6} \gg k_p^{-1}$$

⇒ **Stable self-guiding & Full electron cavitation**

## Longitudinal effects

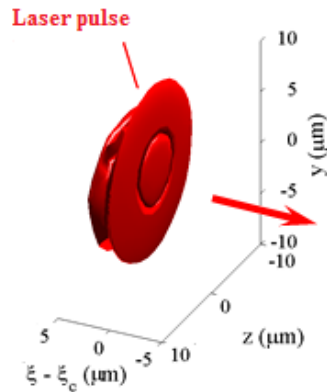
– red-shift of the pulse leading edge & self-compression due to negative GVD of radiation in plasma –

**remain uncontrolled**

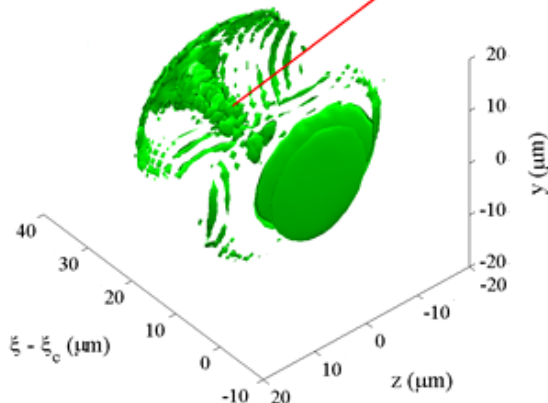
⇒ Reduced phase velocity of the bubble

⇒ Early electron dephasing, limited energy gain

⇒ **Massive continuous self-injection**



Dark current -  
continuously injected  
electrons



# Matching strategy leads to unfavorable energy scaling

Match pulse length and spot size to make electrons dephase as the pulse depletes:

$$\tau_L = 2R_m / (3c)$$

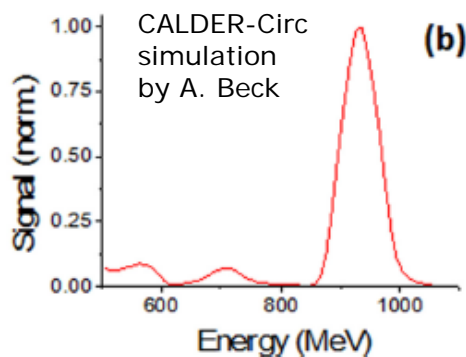
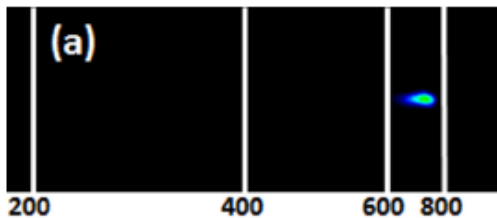
Energy gain at dephasing/depletion:  $\Delta E \text{ [GeV]} = 0.125 (P[\text{PW}])^{1/3} (n_{20} \lambda_{\mu\text{m}}^2)^{-2/3}$

Robust self-guiding & self-injection:  $P/P_{\text{cr}} > 10 \Rightarrow n_{20} \lambda_{\mu\text{m}}^2 > 1.8 \times 10^{-3} (P[\text{PW}])^{-1}$

056703-7 Banerjee *et al.* Phys. Plasmas 19, 056703 (2012)

Stringent scaling of the energy gain:

$$\Delta E \text{ (GeV)} < 8.6 P[\text{PW}]$$



$$\Delta E \approx 1 \text{ GeV}$$

$\Rightarrow$

$$P \approx 120 \text{ TW}$$

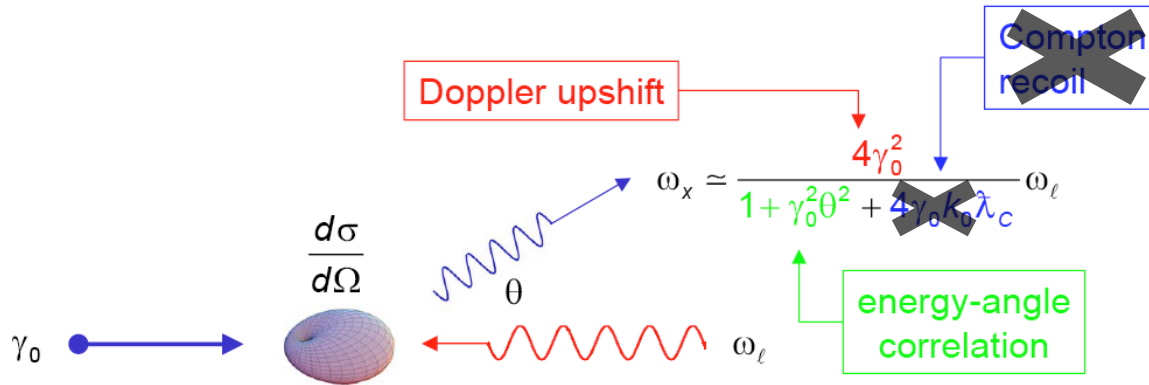
$$\tau_L \approx 32 \text{ fs}$$

$$L_{\text{dephasing}} \approx 0.7 \text{ cm}$$

Regime is accessible, but

**the repetition rate is  $\lll 10 \text{ Hz}$**

# Inverse Compton (Thomson) scattering and its requirements for e-beams



From: C. P. J. Barty,  
LLNL Proposal for the ELI-NP  $\gamma$ -Source,  
ELI-NP Gamma Source Meeting,  
04/18/2011

- Photon flux  $> 10^6$ /shot/full bandwidth  
E-beam 5-D brightness  $> 10^{16}$  A/m<sup>2</sup> [A. Cianchi *et al.*, *NIM A* **829**, 343 (2016)]  
Sub-% energy spread in the e-beam
- Photon energy 10-20 MeV – **challenge**  
GeV e-beams needed – scaling suggests using PW-/kJ-scale pulses
- Repetition rate in kHz to raise the dosage – **major challenge**  
MW-class average-power laser amplifiers are not going to be available soon

# Raising the repetition rate: GeV LPA with sub-Joule (10-TW-scale) pulses

Moderate average power:

1. Enables *high repetition rate* needed by applications that require high dosage (medicine, nuclear fluorescence studies *etc.*)  
  
1J @1 kHz = 1 kW — a hard, yet manageable laser engineering problem.
2. Helps *reduce the size and cost of facilities.*
3. *Lifts the barriers for first-principle modeling.*
4. Enables *real-time control* of the laser pulse phase (using genetic algorithms) for optimization of the acceleration process  
[Z.-H. He *et al.*, Coherent control of plasma dynamics, *Nat. Comm.* **6**, 7156 (2015)]

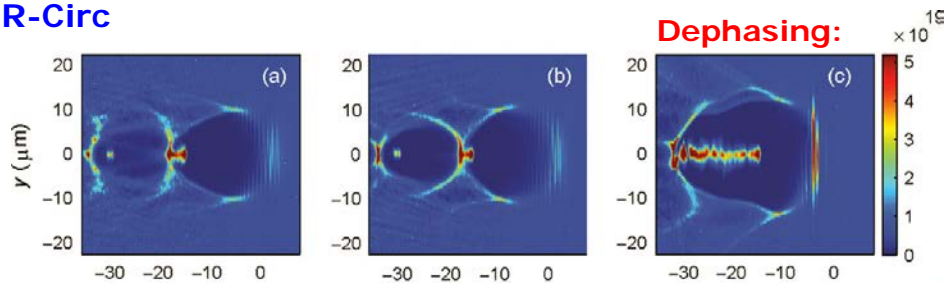
# Transform-limited, 10-TW-class pulse rapidly destroys itself and e-beam ☹

1. Self-guiding needs a dense, highly dispersive plasma ( $\sim 10^{19} \text{ cm}^{-3}$ )
2. Self-compression of the pulse

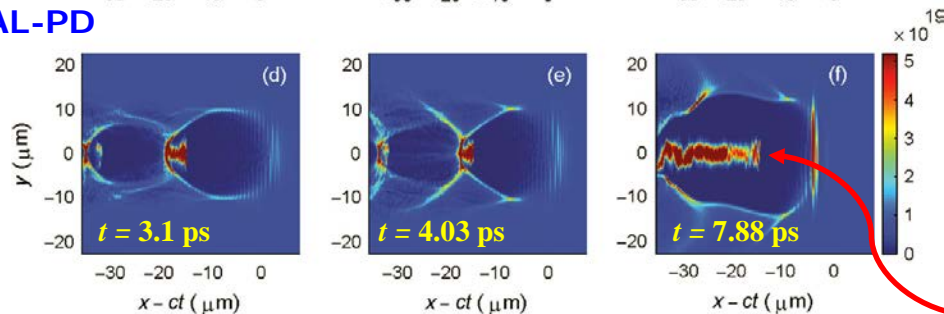
(a) keeps the energy gain below half-GeV

(b) forces expansion of the bubble, hence massive dark current

**CALDER-Circ**  
code:



**VORPAL-PD**  
code:



Power / energy / length	70 TW / 2.1 J / 30 fs
Plasma density, $n_0$	$6.5 \times 10^{18} \text{ cm}^{-3}$
$P/P_{\text{cr}} \approx 16$	

B. M. Cowan *et al.*, *J. Plasma Phys.* **78**, 469 (2012)

$E \approx 420 \text{ MeV} + \text{huge tail}$

# Large bandwidth ( $\Delta\lambda \sim \lambda_0$ ) and negative chirp solve the problem 😊

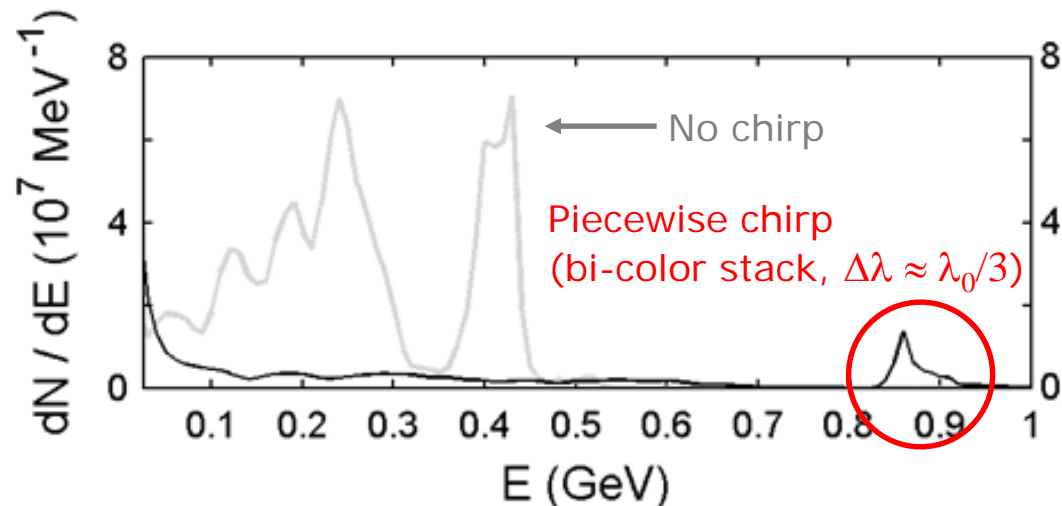
These features:

- mitigate the frequency red-shift
- slow down pulse self-compression in dense plasmas ( $\sim 10^{19} \text{ cm}^{-3}$ )
- extend the dephasing length, boosting the energy gain to GeV level
- strongly reduce the energy tail.

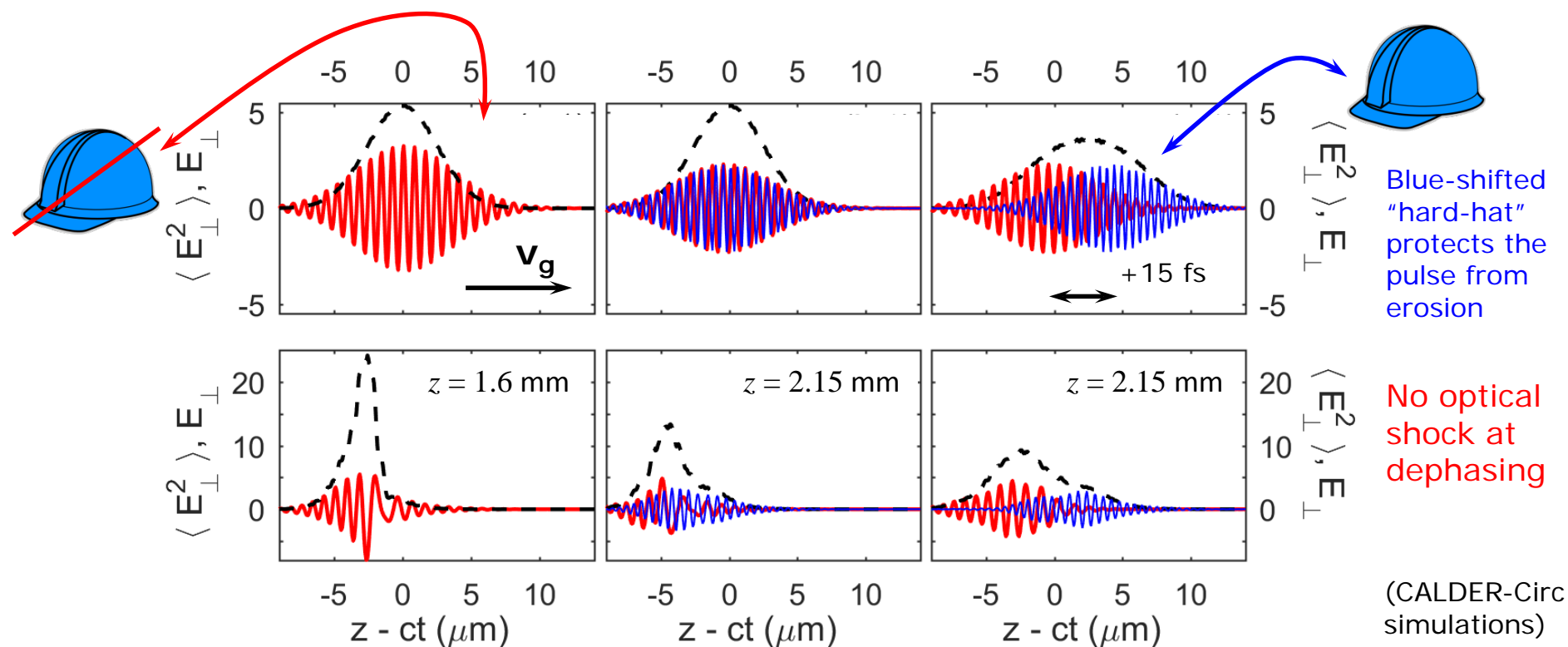
**HIGH EXPECTATIONS:** Background-"free" near-GeV acceleration with 1.4J laser energy

20–30 fs pulse

$n_0 = 6.5 \times 10^{18} \text{ cm}^{-3}$



# Temporally advanced blue-shifted "head" protects the optical driver from nonlinear erosion

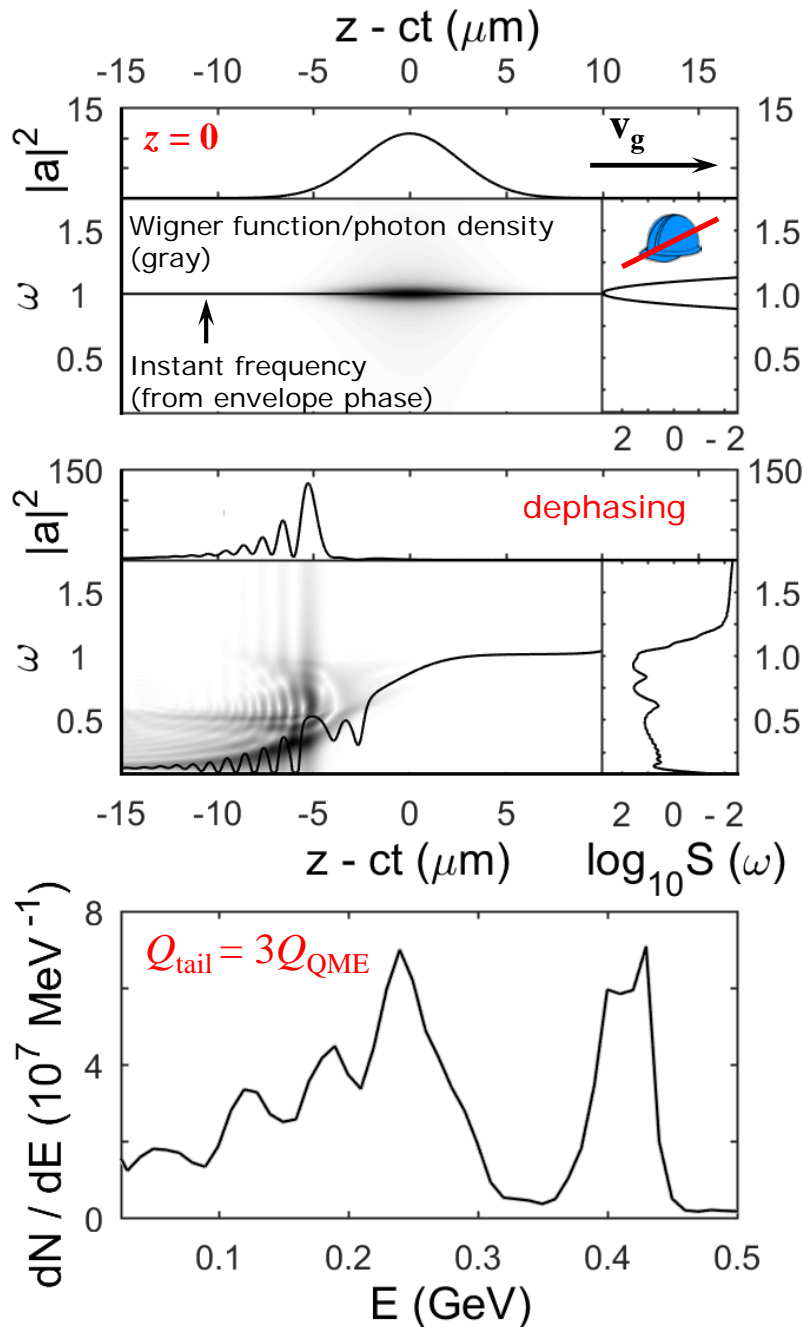


Head: 20 fs, 0.7 J,  $\lambda_{\text{tail}} = 0.8 \mu\text{m}$   
 Tail: 20 fs, 0.7 J,  $\lambda_{\text{head}} \approx 0.53 \mu\text{m}$  } orthogonally polarized (**incoherent mixing**)

- Frequency shift in Raman cells with subsequent conventional CPA  
 [F. B. Grigsby *et al.*, *JOSA B* **25**, 346 (2008)]
- Energy-efficient methods of 2<sup>nd</sup> harmonic pulse generation.



# Acceleration with a single TLP: Electron beam ruined



Pulse at dephasing:

Compressed to a single cycle and 60%-depleted

"Photon phase-space rotation": mid-IR photons slide into the bubble

QME bunch:

$\langle E \rangle$	427 MeV
$\sigma_E / \langle E \rangle$	6%
$\varepsilon_{\text{norm}, \perp}$	0.7 mm mrad
Charge	0.495 nC
RMS current	90 kA
RMS divergence	2.9 mrad

5-D brightness:

$$2\langle I \rangle (\pi \varepsilon_{\text{norm}, \perp})^{-2} = 3.8 \times 10^{16} \text{ A/m}^2 \quad 9$$

# Bi-color stack: Doubling electron energy

QME e-beam at dephasing ( $L_{\text{dephasing}} \times 1.8$ ):

$\langle E \rangle$  882 MeV ( $\times 2$  of reference)

$\sigma_E / \langle E \rangle$  3.2%

$\varepsilon_{\text{norm}, \perp}$  0.4 mm mrad  
( $\times 1/2$  of reference)

Charge 73 nC

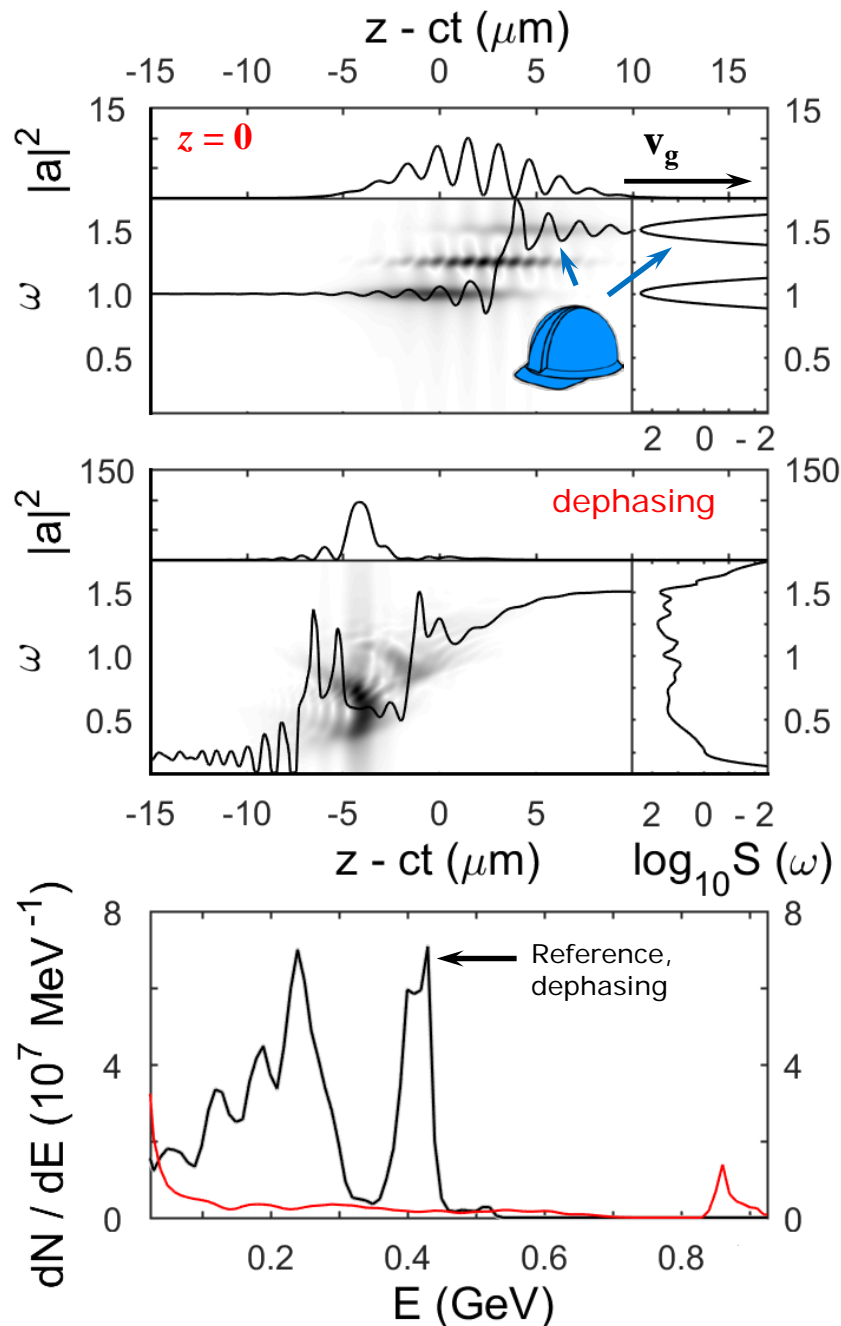
RMS current 88 kA (same as reference)

RMS divergence 1.35 mrad

5-D brightness  $1.1 \times 10^{17} \text{ A/m}^2$   
( $\times 3$  of reference)

Tail at dephasing:

Reduction by a factor 6 in charge, by a factor 20 in average flux

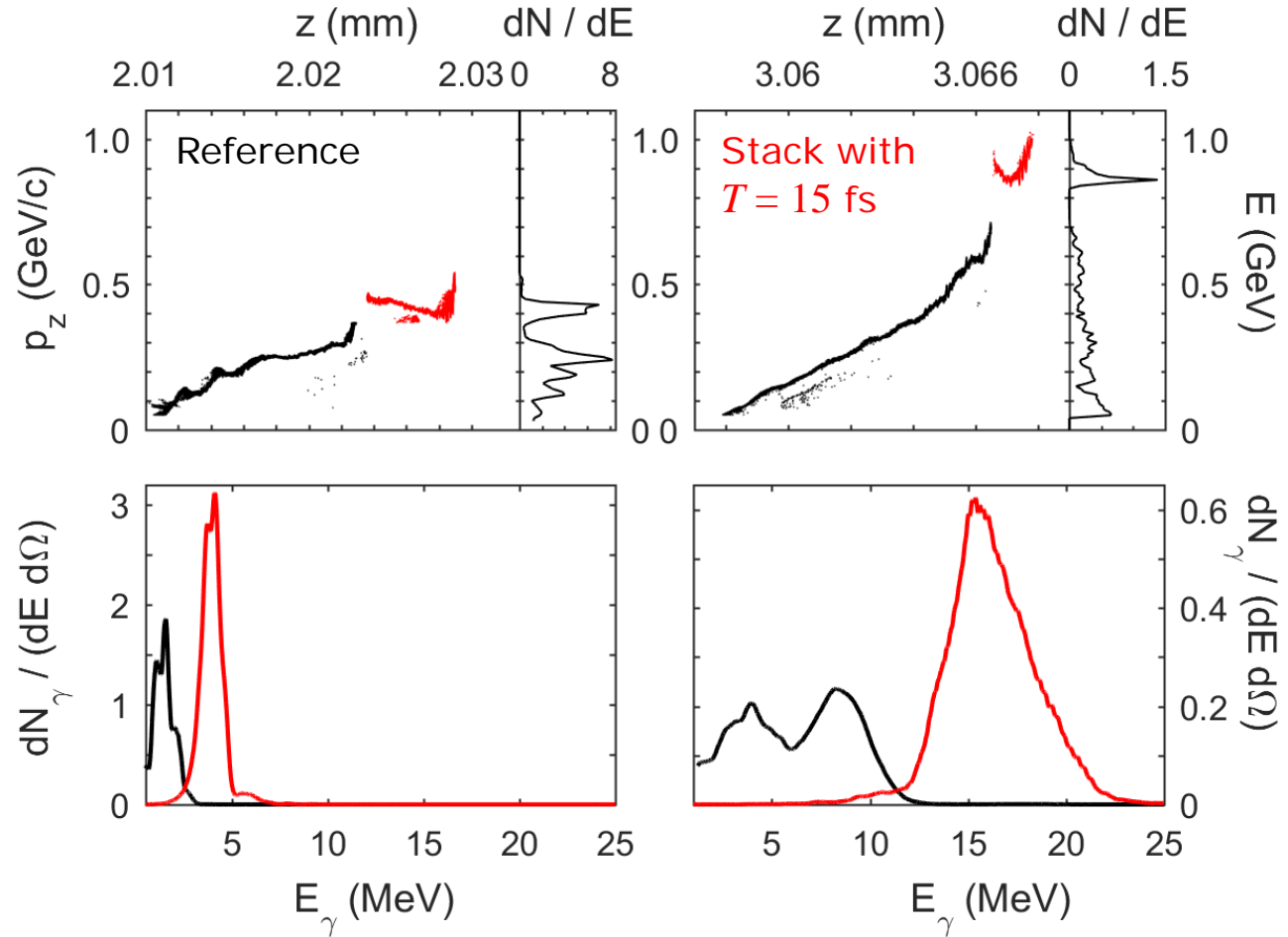


# Improvement in Thomson scattering signal

E-beam phase space and flux (in  $10^7 \text{ MeV}^{-1}$ ) at dephasing

Photon flux  
(in  $10^{12} \text{ MeV}^{-1} \text{ sr}^{-1}$ )  
in the e-beam  
propagation direction

- head-on collision
- on-axis observation



- Photon energy boost by a factor 4.2 (to 16 MeV)
- Increase in the signal to background ratio, from 2:1 to 4:1

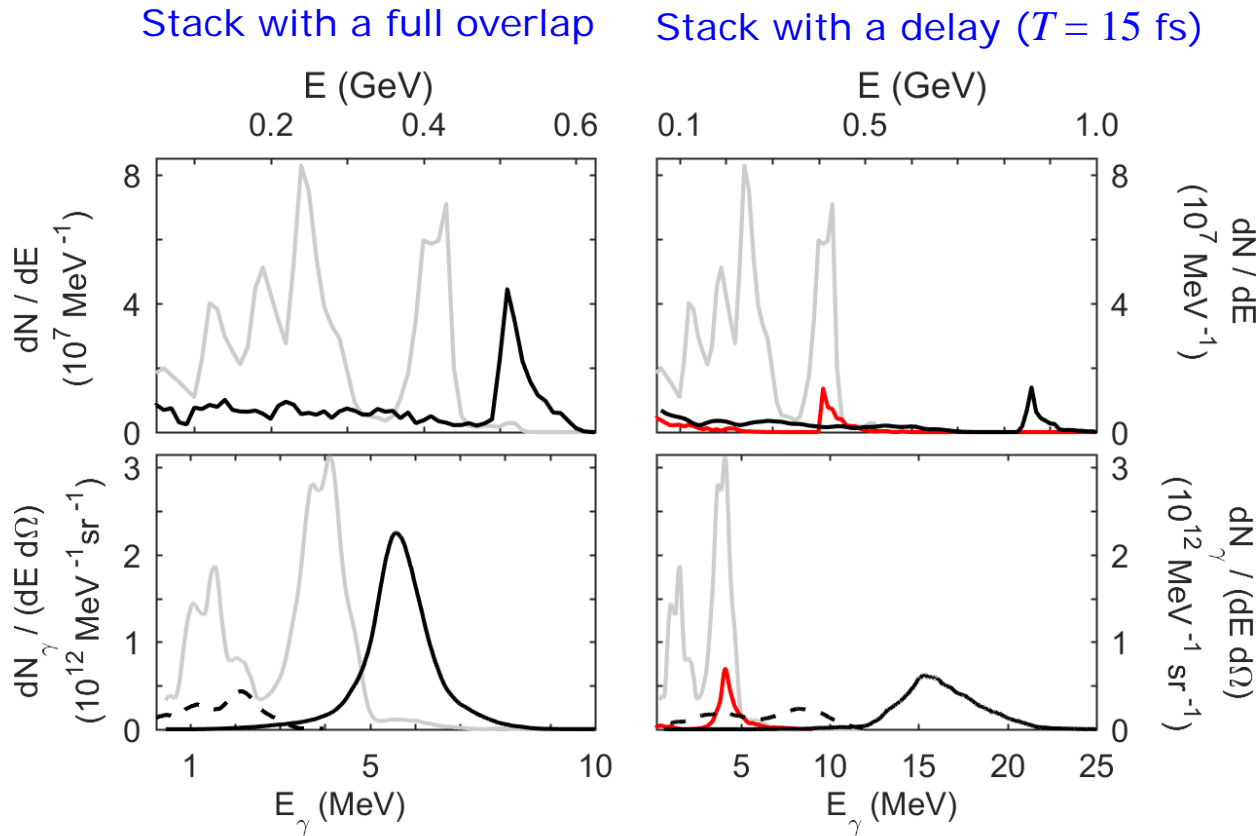
**Thomson back-scattering (almost linear regime, quasi-planar-wave interaction):**

Interaction laser pulse: Linearly polarized,  $r_0 = 16.8 \text{ } \mu\text{m}$ ;  $a_0 = 0.1$ ;  $\lambda = 0.8 \text{ } \mu\text{m}$ ; FWHM 250 fs

# Time delay in the stack controls $\gamma$ -photon flux and energy

Electron energy spectra  
at dephasing

$\gamma$ -ray flux  
in the direction  
of e-beam propagation

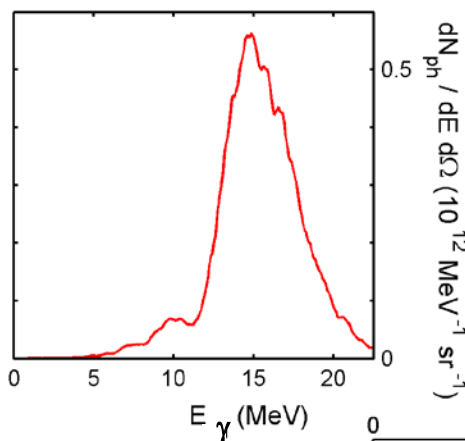
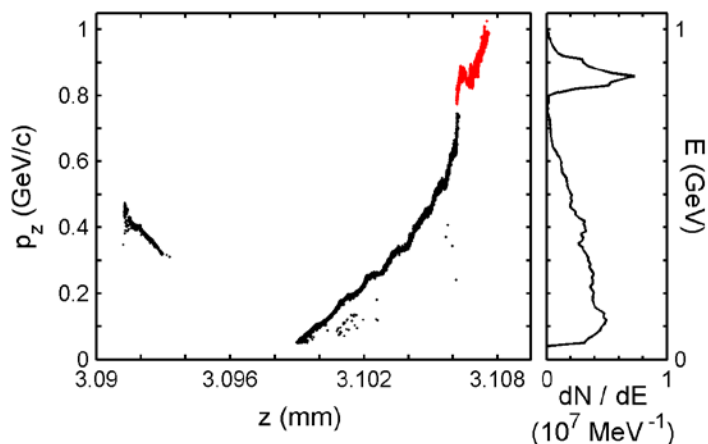


QME $\gamma$ -ray signals	Reference	Stack wit full overlap ( $T = 0$ )	Stack with $T = 15$ fs	
			$z = 1.47$ mm	Dephasing (3.07 mm)
$\langle E_\gamma \rangle$ (MeV)	3.85	5.67	4.35	16
$\sigma_E / \langle E_\gamma \rangle$ , %	18.7	17.1	21.3	15.5
$N_\gamma$ per $\Omega_d$	$8.95 \times 10^6$	$5.08 \times 10^6$	$1.52 \times 10^6$	$1.58 \times 10^6$
Energy ( $\mu$ J)/power in $\Omega_d$	5.5 (1 GW)	4.6 (1.2 GW)	1.1 (1.3 GW)	4 (4.7 GW)

# Few-% energy spread of e-beam imparts 15–20% bandwidth into the Thomson signal

Full phase space  
of e-beam:

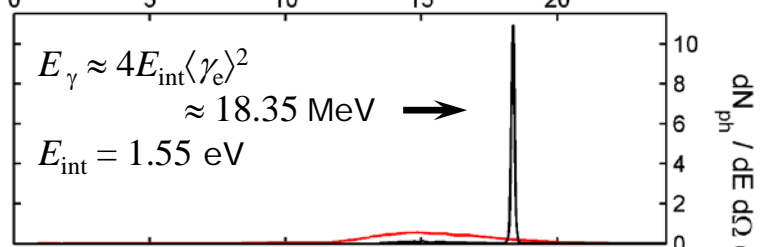
$$\begin{aligned} \langle p_z \rangle &= 1726 \, m_e c, & \sigma_{pz} &= 56 \, m_e c & (3.25\% \text{ energy spread}) \\ \langle p_r \rangle &= 0, & \sigma_{pr} &= 2.3 \, m_e c & (1.35 \text{ mrad divergence}) \end{aligned}$$



$$\begin{aligned} \langle E_\gamma \rangle &= 16 \text{ MeV} \\ \sigma_E &= 2.5 \text{ MeV} \\ &(15.5\% \text{ spread}) \end{aligned}$$

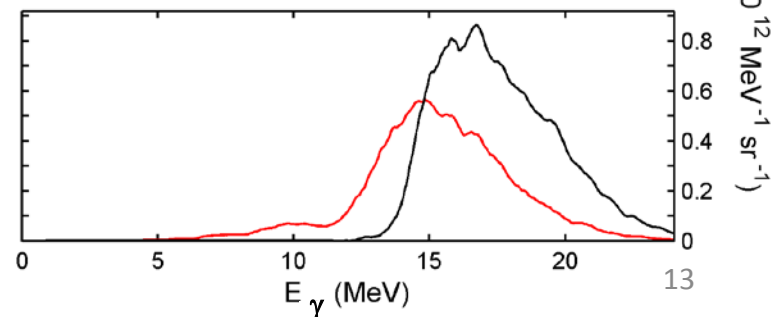
Reduced phase space I:

$$\begin{aligned} \langle p_z \rangle &= 1726 \, m_e c, & \sigma_{pz} &= 0 & (\approx 0\% \text{ energy spread}) \\ \langle p_r \rangle &= 0, & \sigma_{pr} &= 2.3 \, m_e c & (1.35 \text{ mrad divergence}) \end{aligned}$$



Reduced phase space II:

$$\begin{aligned} \langle p_z \rangle &= 1726 \, m_e c, & \sigma_{pz} &= 56 \, m_e c & (3.25\% \text{ energy spread}) \\ \langle p_r \rangle &= 0, & \sigma_{pr} &= 0 & (\text{zero divergence}) \end{aligned}$$

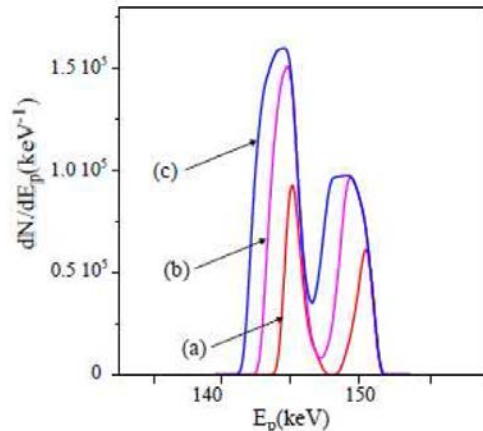


# Electrons from stack-driven LPA for quasi-monochromatic Thomson sources

- High-power (1–5 GW), fs-length  $\gamma$ -ray pulses contain  $> 10^6$  photons in the sub- $\mu$ sr observation solid angle
- This flux corresponds to the full bandwidth (1–2.5 MeV) imparted by a few-% energy spread in the e-beam
- Mean photon energy is tunable between 4 and 16 MeV without losing photons in the  $\mu$ sr observation solid angle  $\Omega_d = (\pi/2)\langle\gamma_e\rangle^{-2}$
- Signal to background ratio is better than 4:1
- Changing time delay in the stack permits accurate tuning  $e/\gamma$  energy and flux, with the same laser energy and frequency ratio in the stack
- Sub-Joule energy in stack components affords kHz repetition rate at the affordable average power
- Expectation of  $10^{10}$  ph/s flux (good for NRF applications).

# Trains of multi-color X/ $\gamma$ -ray pulses: What are they good for?

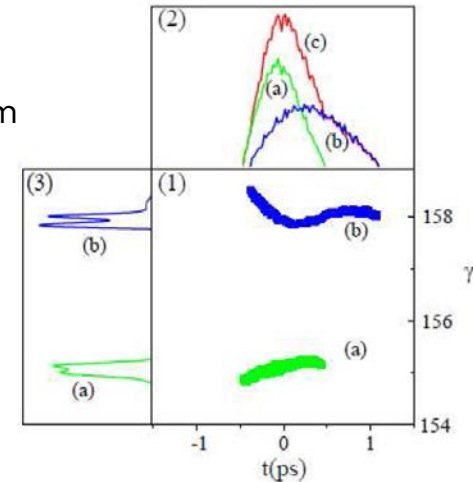
Comb-like X/ $\gamma$  - ray beam: Train of wave packets with an adjustable frequencies and time delays



A bi-color X-ray beam @ SPARC-LAB

Source: a comb-like e-beam – a train of bunches with adjustable energies and time delays

Bi-color e-beam from SPARC-LAB:



Images:

V. Petrillo *et al.*, Dual-color X-rays from Thomson or Compton sources, *Proc. SPIE* **9512**, 95121E (2015)

Generation mechanism: bi-color FEL or **inverse Compton (Thomson) scattering**

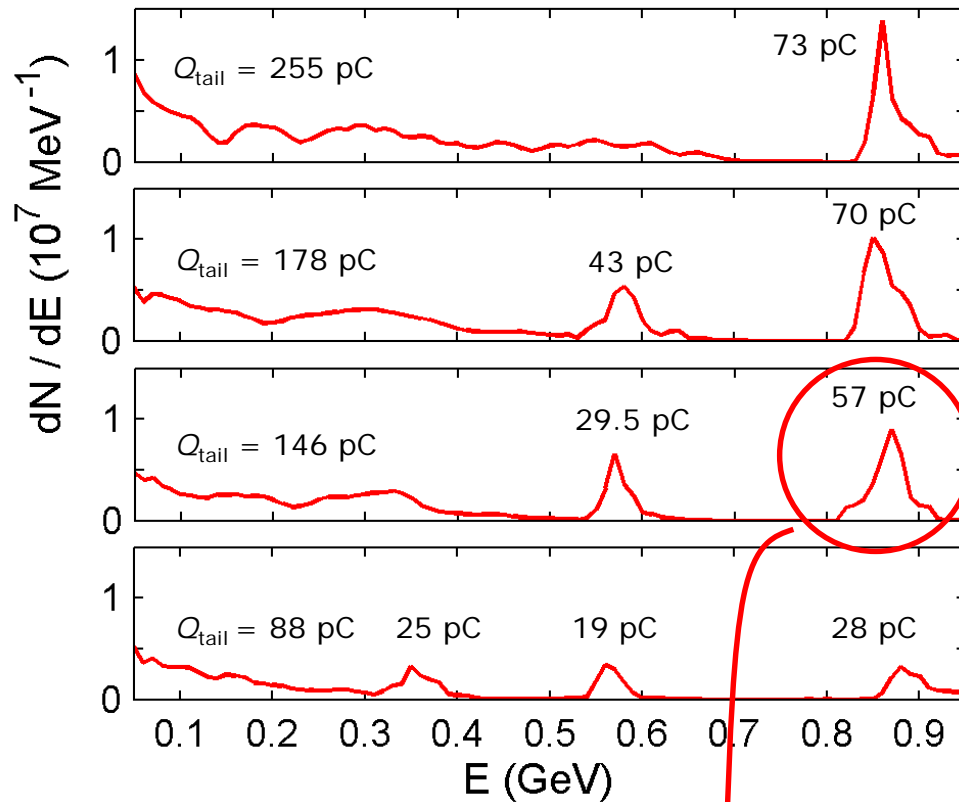
Applications:

- **Ultrafast** (on a fs- to ps-scale) **pump-probe experiments** in AMO or HEDP
- Time-domain spectroscopy [J. F. Cahoon *et al.*, *Science* **319**, 1820 (2008)]
- Screening/diagnostic mammography: Color components help discriminate chemical composition of absorbing tissues [I. Willekens *et al.*, *Eur. Soc. Radiography*, 2011]
- **Nuclear photonics** [S. Chen *et al.*, *Phys. Rev. Lett.* **110**, 155003 (2013)]

# Generating comb-like e-beams in stack-driven LPA

Stack (with  $T = 15$  fs) permits focusing head and tail differently.

Weak focusing of the tail ( $R_{\text{tail}} \geq R_{\text{head}}$ ) destabilizes the bubble.  
Periodic injection generates a polychromatic train of bunches.



$$R_{\text{tail}} = R_{\text{head}} = 13.6 \mu\text{m}$$

$$R_{\text{tail}} = (3/2)^{1/2} R_{\text{head}}$$

$$R_{\text{tail}} = 2^{1/2} R_{\text{head}}$$

$$R_{\text{tail}} = 3^{1/2} R_{\text{head}}$$

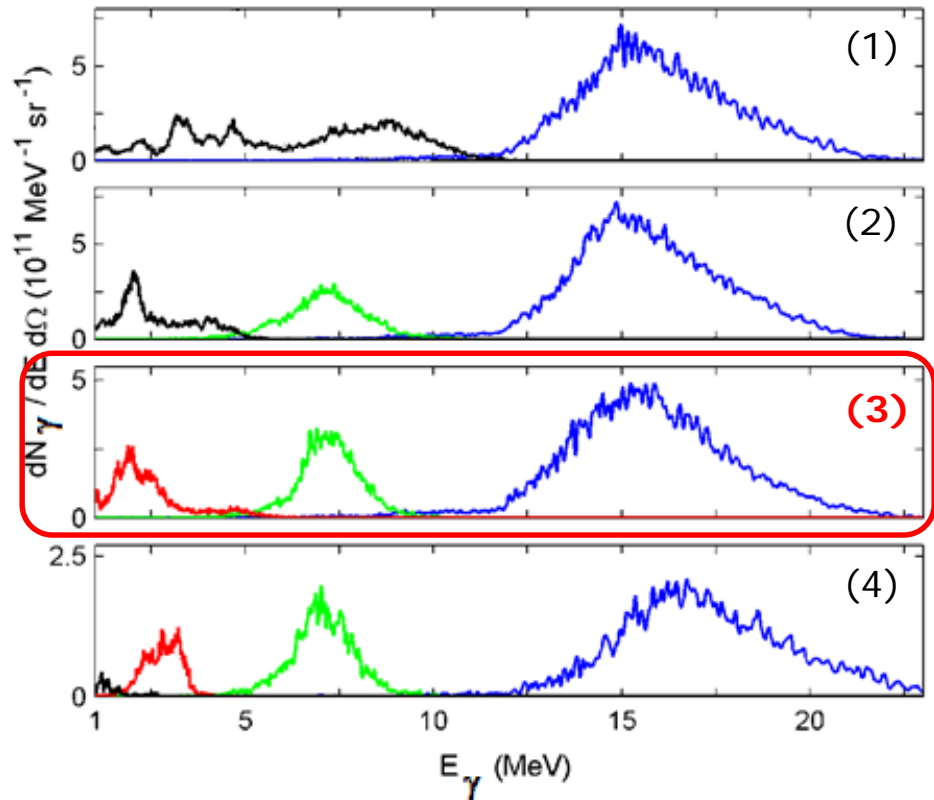
— too weak focusing makes injection ineffective

Brightness ( $10^{17} \text{ A/m}^2$ ): (1) 0.44 (2) 0.96

$\sigma_E / \langle E \rangle$ : (1) 3.2% (2) 2.4%



# Generating X/ $\gamma$ -ray pulse trains using comb-like e-beams from stack-driven LPA



A weak continuous tail transforms into a set of distinct bands

Characteristics of  $\gamma$ -ray energy bands (QME pulses):

$$\sigma_E / \langle E_\gamma \rangle: \quad 14.7 \text{ to } 19.5\%$$

$$N_\gamma \text{ per } \Omega_d: \quad 0.4 \text{ to } 1.6 \times 10^6$$

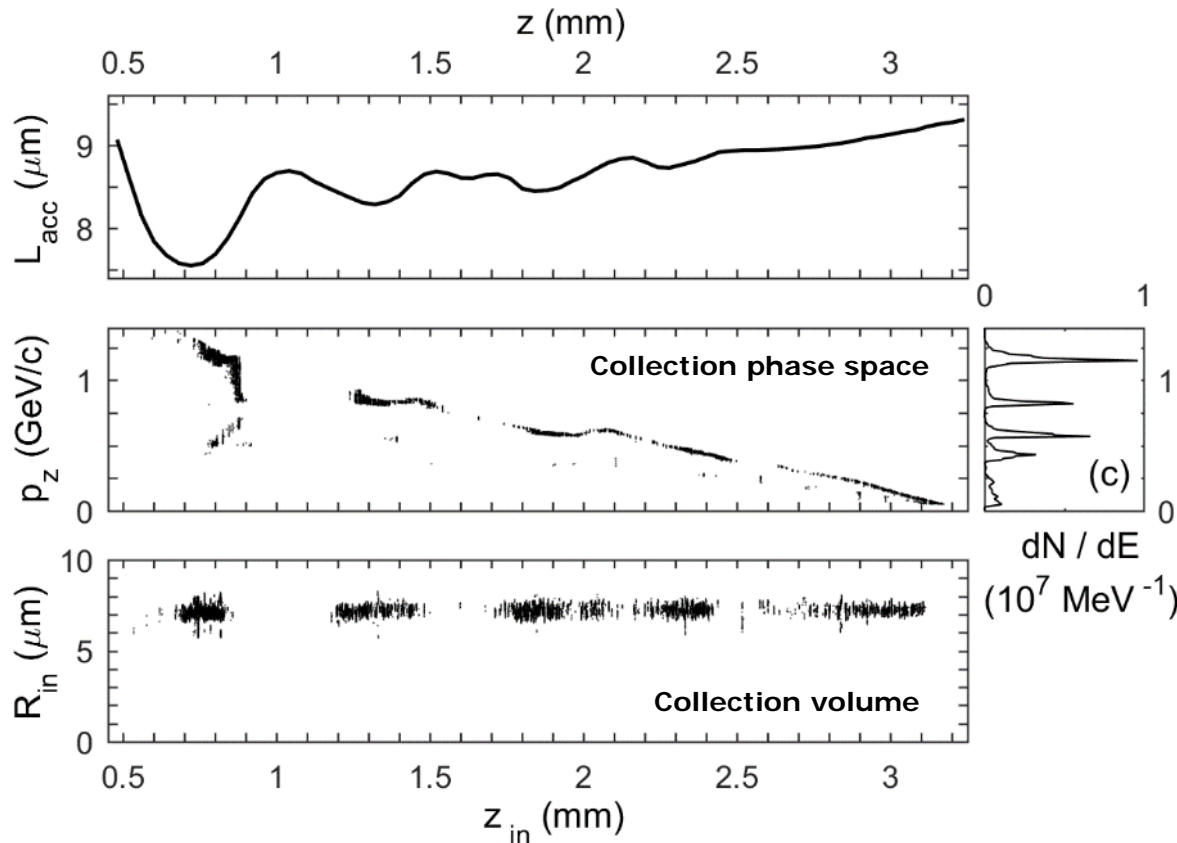
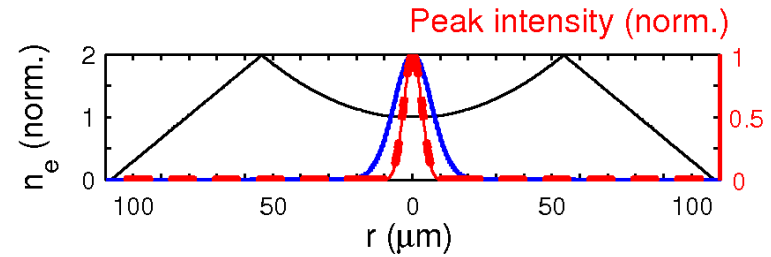
Total energy per band,  
in detector solid angle,

$$\Omega_d = (\pi/2) \langle \gamma_e \rangle^{-2}: \quad 0.17 \text{ to } 4 \mu\text{J}$$

Case 3	1	2	3
$\langle E_\gamma \rangle$ (MeV)	2.8	7.25	15.8
$\sigma_E / \langle E_\gamma \rangle, \%$	19.4	14.7	15.7
$N_\gamma$ per $\Omega_d$	$0.91 \times 10^6$	$0.62 \times 10^6$	$1.25 \times 10^6$
Energy/power per $\Omega_d$ ( $\mu\text{J}$ )	0.4 (0.17 GW)	0.72 (0.75 GW)	3.16 (4.27 GW)

# Propagating the stack in a channel (a) adds more control, (b) further boosts electron energy

Same stack as before, with a  $T = 15$  fs delay.  
Stack head and tail have the same spot sizes, matched to the single-mode channel.

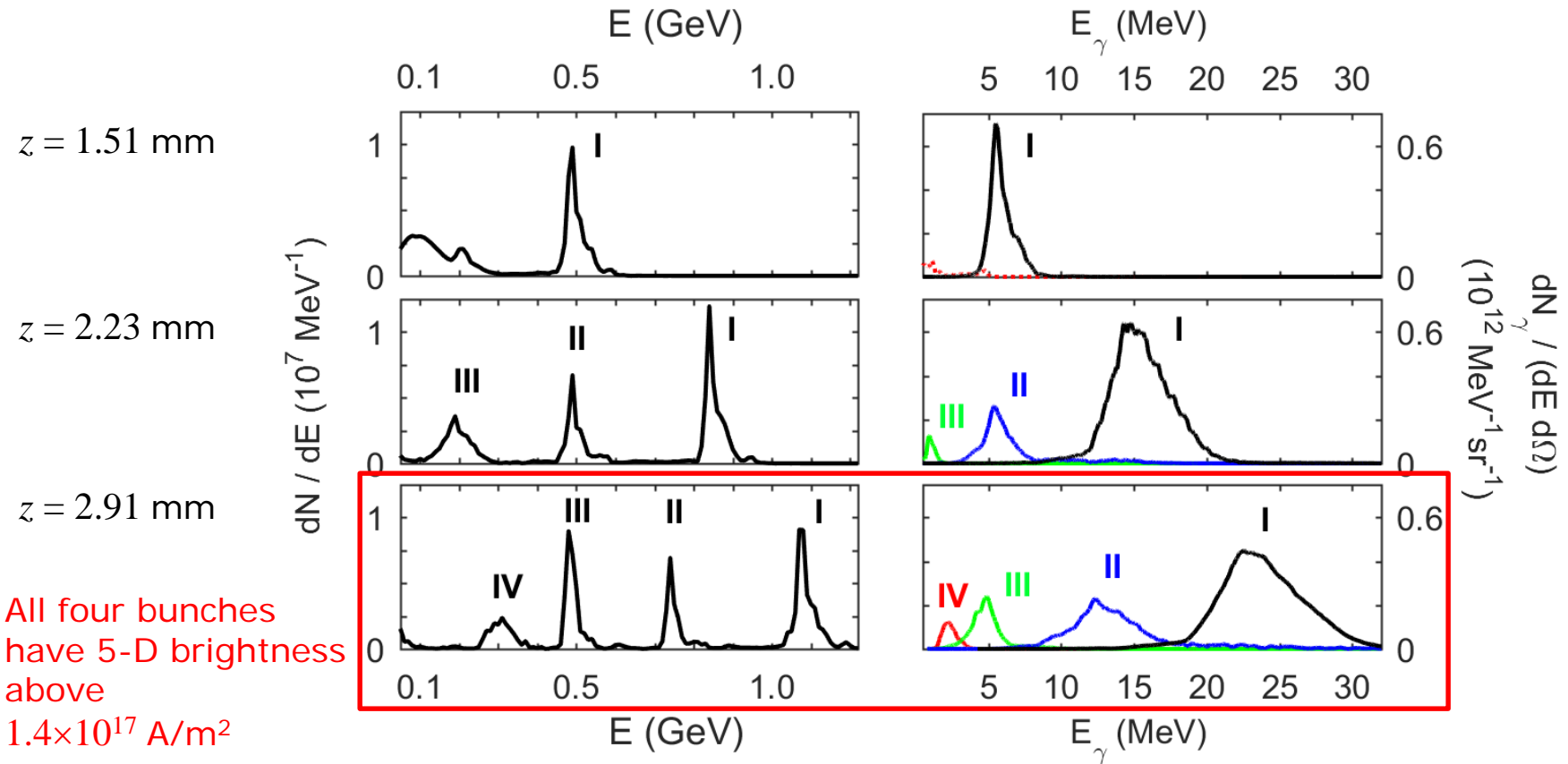


$$n_e(r) = \begin{cases} n_0 \left( 1 + \frac{r^2}{r_{ch}^2} \right) & , \text{ for } r \leq r_{ch} \\ 2n_0 \left( 2 - \frac{r}{r_{ch}} \right) & , \text{ for } r_{ch} < r \leq 2r_{ch} \\ 0 & \text{ for } r > 2r_{ch} \end{cases}$$

The e-comb absorbs 10% of laser energy

The peak energy 1.2 GeV (vs ~ 430 MeV of the reference case)

# Progress of comb-like e-beam through dephasing and generation of multi-color $\gamma$ -ray beams



4-color $\gamma$ -ray signal	1	2	3	4
$\langle E_\gamma \rangle$ (MeV)	24.1	12.6	4.67	2.27
$\sigma_E / \langle E_\gamma \rangle$ , %	15	18.4	20	22.6
$N_\gamma$ per $\Omega_d$	$1.64 \times 10^6$	$0.66 \times 10^6$	$0.585 \times 10^6$	$0.595 \times 10^6$
Energy/power per $\Omega_d$ ( $\mu\text{J}$ )	6.5 (10.3 GW)	1.34 (1.8 GW)	0.46 (0.39 GW)	0.22 (0.34 GW)

# Summary

Designing the LPA drive pulse as an incoherent stack of independent sub-Joule, transform-limited pulses with a large difference frequency ( $\Delta\omega \sim \omega_0$ ) permits an *unprecedented freedom in e-beam phase space control*, suppressing the background and increasing 5-D brightness of individual bunches above  $\sim 10^{17}$  A/m<sup>2</sup>.

Stack-driven LPAs promise generation of fs-length, ultra-bright, near-GeV electron bunches at a kHz repetition rate, with affordable average power.

These bunches (or trains of bunches) promise to drive quasi-monochromatic (or comb-like) Thomson-scattering  $\gamma$ -ray sources, tunable into 10's of MeVs, while keeping the  $\gamma$ -ray pulse length extremely short (100's of as) and the number of photons high ( $> 10^6$ ).

## ACKNOWLEDGEMENTS

Inverse Thomson scattering simulations were completed by S.Y.K. utilizing the Holland Computing Center of the University of Nebraska.

SYK cordially thanks Natasha Pavlovikj of HCC for assistance.

# Addenda

Simulation tools:      fully relativistic PIC codes & particle tracker for radiation calculation

- Exploring optical pulse evolution in the plasma and beam loading effects: **WAKE** (extended-paraxial, ponderomotive guiding center, quasi-static)  
[P. Mora and T. M. Antonsen, Jr., *Phys. Plasmas* **4**, 217 (1997)]
  - Accurate simulation of self-injection and acceleration: **CALDER-Circ** (quasi-cylindrical, fully explicit; poloidal mode decomposition of fields and currents)  
[A. F. Lifschitz *et al.*, *J. Comp. Phys.* **228**, 1803 (2009)]
- Also: numerical Cherenkov-free EM solver; 2<sup>nd</sup> or 3<sup>rd</sup> order macro-particles  
[R. Lehe, A. F. Lifschitz *et al.*, *PR-STAB Beams* **16**, 021301 (2013)]

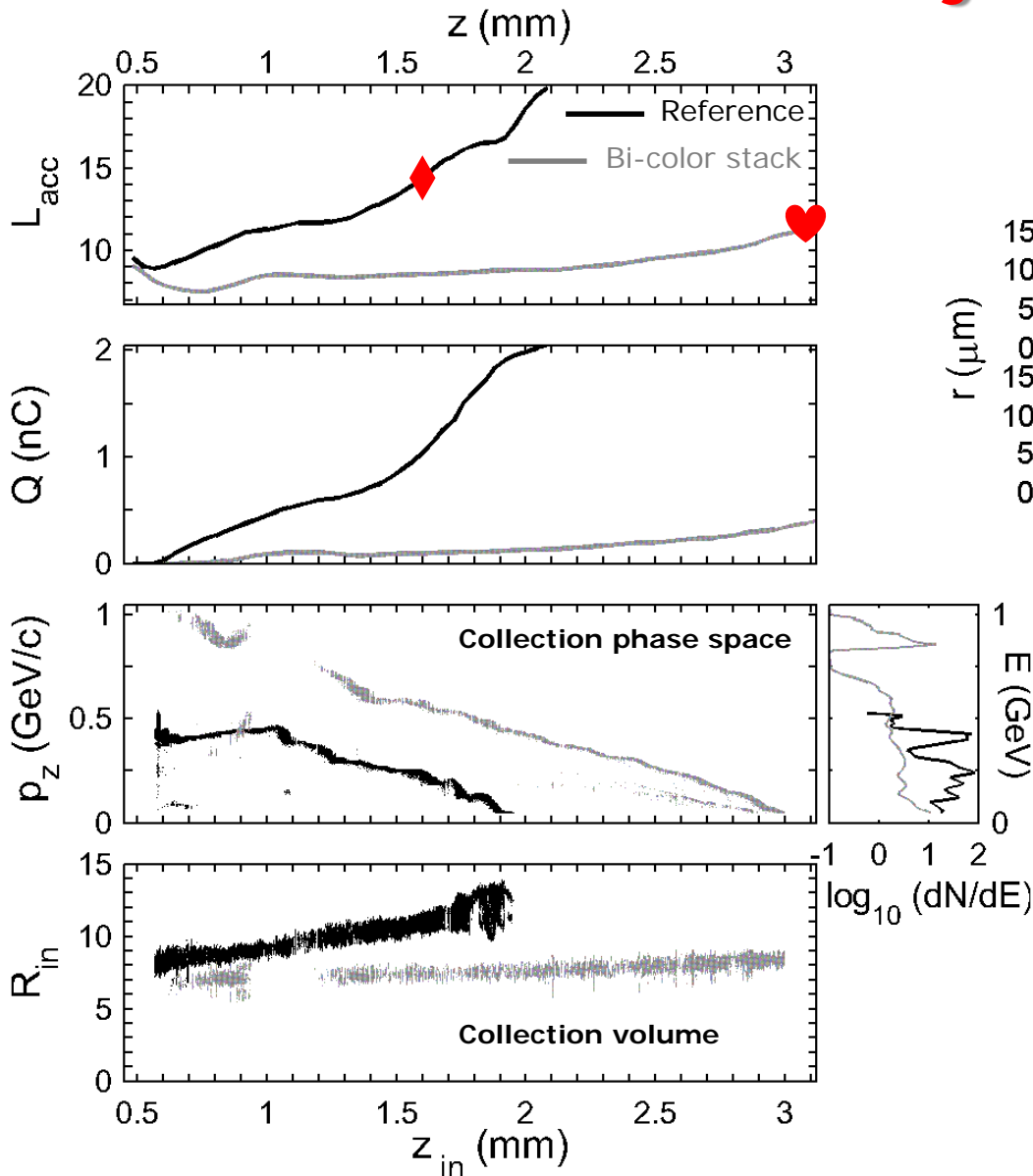
➤ **Inverse Thomson scattering code**

[I. Ghebregziabher *et al.*, *Phys. Rev. Accel. Beams* **16**, 030705 (2013)]

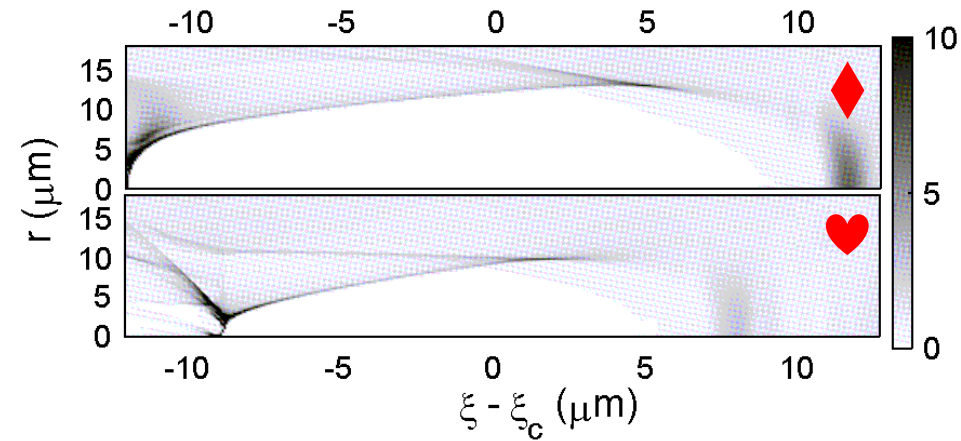
fully relativistic particle tracker; laser beam is paraxial; radiation calculation using classical formula

$$\frac{d^2 I}{d\omega d\Omega} = 2|\mathbf{A}(\omega)|^2, \quad \mathbf{A}(\omega) = \left(\frac{e^2}{8\pi^2 c}\right)^{1/2} \int_{-\infty}^{\infty} e^{i\omega t} \left[ \frac{\mathbf{n} \times [(\mathbf{n} - \boldsymbol{\beta}) \times \dot{\boldsymbol{\beta}}]}{(1 - \boldsymbol{\beta} \cdot \mathbf{n})^3} \right] dt, \quad \frac{d^2 I_e}{d\omega d\Omega} = \frac{1}{N_s} \sum_{i=1}^{N_s} \frac{d^2 I_i}{d\omega d\Omega}.$$

# Stack vs. reference: Suppressing continuous injection



Quasi-static bubble (WAKE simulations):



Due to much slower self-compression of the stack

- bubble expands slowly
- *continuous injection insignificant (hence the weak energy tail)*