

M. Marongiu, A. Giribono, A. Mostacci, L. Palumbo (Sapienza University)

E. Chiadroni, G. Di Pirro, G. Franzini, V. Shpakov, A. Stella, C. Vaccarezza, A. Variola (LNF-INFN)

A. Cianchi (Tor Vergata University)

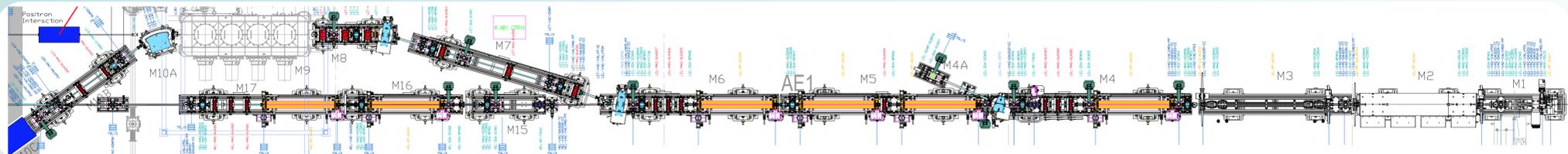
## Abstract

Advanced linear accelerator design may use **Optical Transition Radiation (OTR)** screens to measure **beam spot size**; for instance, such screens are foreseen in **plasma based accelerators (EuPRAXIA@SPARC\_LAB)** or **Compton machines (Gamma Beam Source@ELI-NP)**. OTR angular distribution strongly depends on **beam energy**. Since OTR screens are typically placed in several positions along the LINAC to monitor **beam envelope**, one may perform a **distributed energy measurement** along the machine. Furthermore, a **single shot energy measurement** can be useful in **plasma accelerators** to measure **shot to shot energy variations after the plasma interaction**. Preliminary measurements of OTR angular distribution of about 100 MeV electrons have been already performed at the **SPARC\_LAB facility**. In this paper, we discuss the **sensitivity** of this measurement to **beam divergence** and others parameters, as well as the **resolution** required and the needed **upgrades** of conventional OTR diagnostics, using as an example the data collected at SPARC\_LAB.

## 1. Linac layout

The Gamma Beam Source (GBS) machine is an advanced source of up to **20 MeV Gamma Rays** based on **Compton back-scattering**, i.e. collision of an **intense high power laser beam** and a **high brightness electron beam** with maximum kinetic energy of about **720 MeV**.

The Linac will provide trains of bunches in each RF pulse, spaced by the same time interval needed to recirculate the laser pulse in a properly conceived and designed laser recirculator, in such a way that **the same laser pulse will collide with all the electron bunches in the RF pulse**, before being dumped. The final optimization foresees trains of **32 electron bunches** separated by **16 ns**, distributed along a **0.5 μs RF pulse**, with a repetition rate of **100 Hz**.



## 2. Optical Transition Radiation

The radiation is emitted when a **charged particle beam** crosses the **boundary between two media** with **different optical properties** [1] (here **vacuum** and a thin reflecting **silicon screen**).

**Advantages** of OTR are the **instantaneous emission process** enabling fast **single shot measurements**, and the **good linearity** (neglecting coherent effects).

**Disadvantages** are that the process of radiation generation is **invasive**, i.e. a screen has to be inserted in the beam path, and that the radiation **intensity** is much **lower** in comparison to scintillation screens.

The **beam energy** can be measured by means of observation of **OTR angular distribution**.

$$\frac{dI^2}{d\omega d\Omega} \propto \frac{\sin^2 \theta}{\left(\frac{1}{\gamma^2} + \sin^2 \theta\right)^2} \quad (1)$$

Due to the **beam divergence**, the angular distribution of the whole beam will be **different from 0 at the center**; the **ratio** between the **minimum** and the **maximum intensity** is related to the beam divergence. A parameter called **visibility** defines the **reliability** of the beam divergence measurement ( $V > 0.1$ ) in analogy with the contrast function. Since the **visibility increase** with the **beam energy**, one can also estimate the **minimum measurable divergence for a given energy** [2].

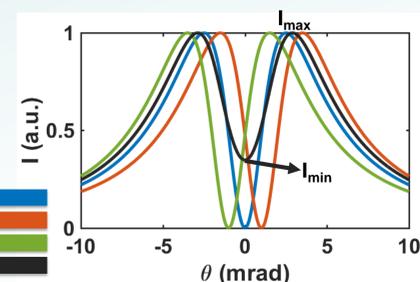
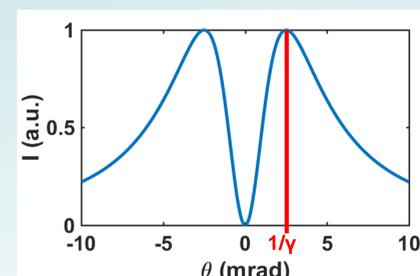
$$V = \frac{I_{max} - I_{min}}{I_{max} + I_{min}} \quad (2)$$

$$I \propto \int_{-\infty}^{\infty} \frac{(\theta - \xi)^2}{[1/\gamma^2 + (\theta - \xi)^2]^2} \exp\left[-\frac{\xi^2}{2\sigma'^2}\right] d\xi = \frac{\sqrt{\pi}\mu}{\nu} \Re[\Phi(z) \left(\frac{1}{2} + \mu\nu z\right)] - \mu^2 \quad (3)$$

$$\mu = \frac{1}{\sqrt{2}\sigma'} \quad \Phi(z) = \frac{1 - \text{erf}(z)}{\exp[-z^2]}$$

$$z = \mu(\nu + i\theta) \quad \nu = \frac{1}{\gamma} \quad [2]$$

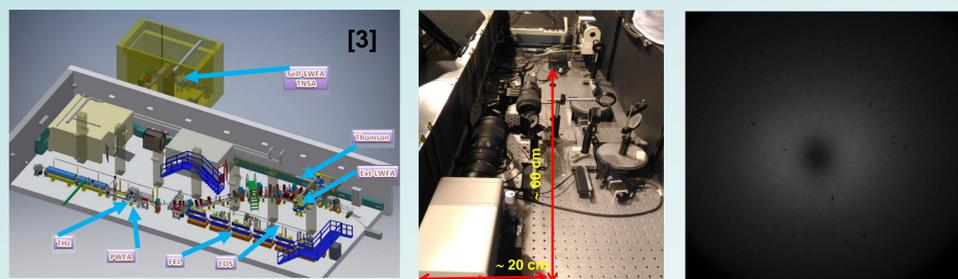
Assuming a **Gaussian distribution** of the divergences, the **beam angular distribution** can be written as the **convolution** between Eq. (1) and the Gaussian distribution as in Eq. (3).



## 3. SPARC\_LAB Data

**Conventional Techniques** (spectrometer and quadrupole scan)

	$E$ (MeV)	$Q$ (pC)	$\sigma'_x$ (mrad)	$\sigma'_y$ (mrad)
Data set 1	110.82 (0.07)	108 (3)	0.52 (0.03)	0.66 (0.02)
Data set 2	123.1 (0.04)	120 (4)	1.1 (0.09)	1.04 (0.09)



Focal length equal to 400mm. Pixel size equal to 6.5μm. Therefore each pixel is 16.25μrad

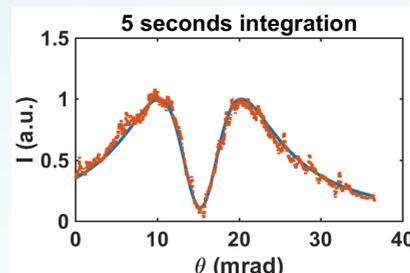
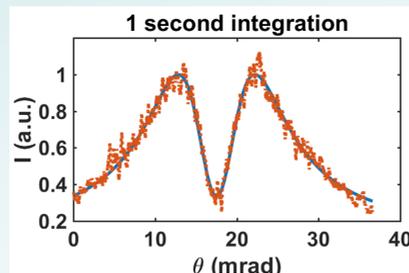
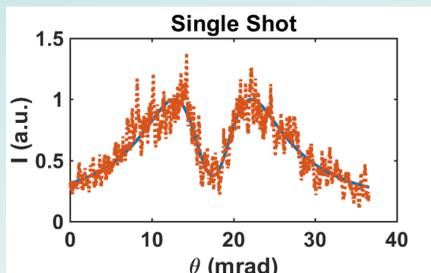
**Fit Results**

	Data set 1	Data Set 2	Data set 1	Data Set 2	Data set 1
$E$ (MeV)	105.35 (2.04)	122.13 (2.04)	$E$ (MeV)	108.33 (1.53)	123.66 (1.02)
$\sigma'_x$ (mrad)	0.72 (0.21)	1.4 (0.1)	$\sigma'_x$ (mrad)	0.75 (0.09)	1.3 (0.05)
$\sigma'_y$ (mrad)	0.74 (0.17)	1.3 (0.1)	$\sigma'_y$ (mrad)	0.77 (0.08)	1.2 (0.04)
			$E$ (MeV)	109.87 (0.55)	
			$\sigma'_x$ (mrad)	0.72 (0.04)	
			$\sigma'_y$ (mrad)	0.78 (0.06)	

The **energy** is well predicted by the fit; especially for the higher energy data set.

Due to the **lack of visibility**, see Eq. (2), the **divergences** are **overestimated**: at higher energy (i.e. **180 MeV**) these parameters could be **better estimated** [2].

The **accuracy** is higher with conventional techniques (i.e. **spectrometer and quadrupole scan**); the OTR angular distribution, at this energies, is a **complementary technique** useful for a **distributed measurement**.



## 4. Conclusions

The OTR could be a very **useful diagnostic tool** in order to measure the **beam energy**.

Due to the fact that the **OTR screen** are placed **all along the machine**, a **distributed energy measurement** can be performed; the **energy jitter shot to shot** could also be evaluated during the **commissioning stage** of the machine or **after plasma interaction** if the **signal to noise ratio (SNR)** is high enough (i.e. high energy, high charge). Indeed the data analysis shows a **strong dependence** of the **uncertainty to the SNR**.

New **distributed measurements** are foreseen especially to evaluate the **performances of the accelerating structures** at the ELI-GBS facility during the **commissioning stage**. Using a **gated camera** (Hamamatsu Orca4), it's foreseen the measurement also of a **single bunch** of the pulse train.

## References

- [1] V. Ginzburg, et al., "Radiation of a uniformly moving electron due to its transition from one medium into another", Zhurnal eksperimentalnoi i teoreticheskoi fiziki, 1946
- [2] A. Cianchi, et al., "Transverse emittance diagnostics for high brightness electron beams", NIM A, 2016
- [3] M. Ferrario, et al., "SPARC\_LAB present and future", NIM A, 2013