

Impedance Theory & Modeling

Eliás Métral

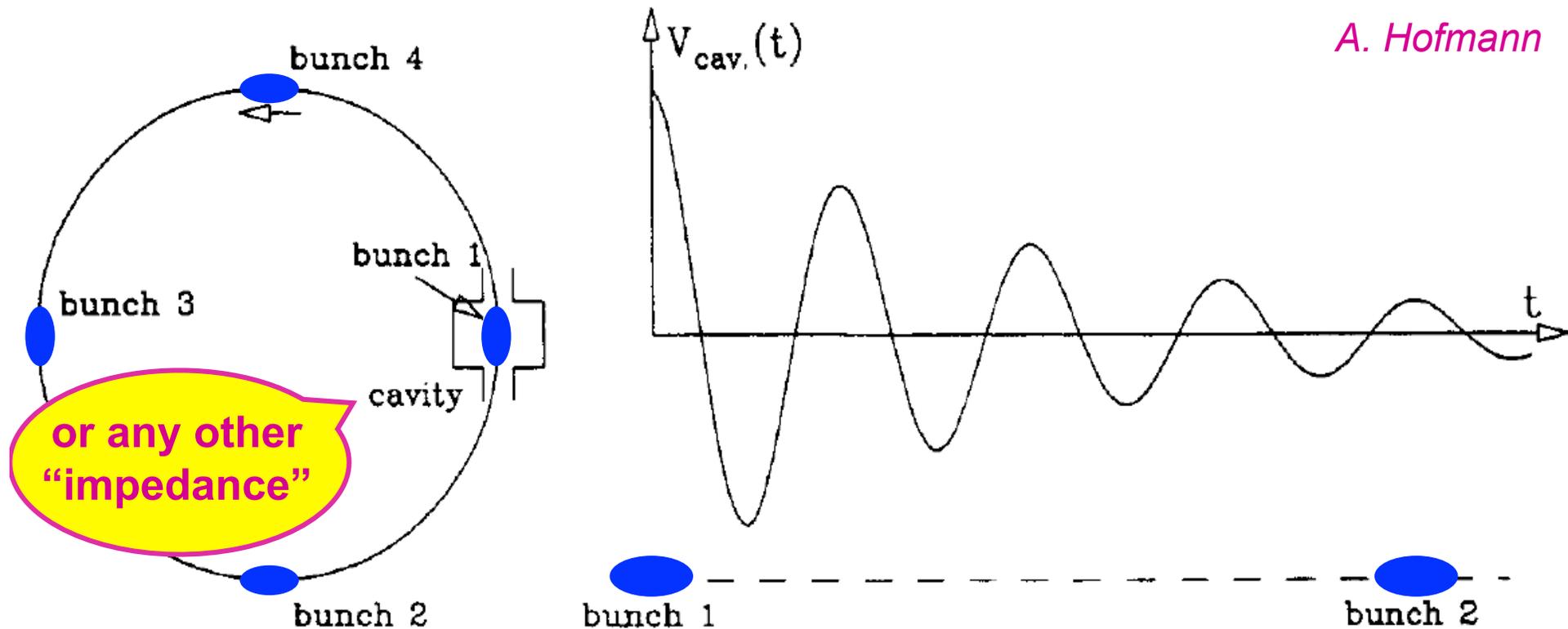
BE/ABP-HSC (Collective/Coherent Effects)

<https://espace.cern.ch/be-dep-workspace/abp/HSC/SitePages/Home.aspx>

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<http://emetral.web.cern.ch/emetral/>



- ◆ **“Impedances” limit performance of ALL machines**
 - Beam instabilities => Increased beam size, beam losses
 - Excessive heating => Deformed / melted components, beam dumps
- ◆ **Each equipment of each accelerator has an “impedance” => To be characterized and minimized!**



ETTORE MAJORANA FOUNDATION AND CENTRE FOR SCIENTIFIC CULTURE







23-28 April 2014
Europe/Zurich timezone

Search...

ICFA mini-Workshop on "Electromagnetic wake fields and impedances in particle accelerators"

Overview

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- Scientific programme and timeline
- International Advisory Committee (IAC)
- List of items to be discussed
- Contacts
- List of participants
- Timetable
- Erice - Get there
- Excursions
- Application form
- Flyer
- Picture of the workshop

Support

- ✉ Delphine.rivoiron...
- ☎ 004122 767 25 23

ICFA mini-Workshop on "Electromagnetic wake fields and impedances in particle accelerators" to be held in Erice, Sicily, in 2014 from April 24th to April 28th. The Workshop will be hosted by "ETTORE MAJORANA FOUNDATION AND CENTRE FOR SCIENTIFIC CULTURE".



THE ROOTS OF WESTERN CIVILIZATION

The quadrilingual gravestone in Ziza Museum in Palermo, Sicily. The languages are Latin, Greek, Arabic and Hebrew. The dates appearing in the four languages, each computed in its own calendar, correspond to 1148 a.d. .

🕒 **Starts** 23 Apr 2014 21:00
Ends 28 Apr 2014 18:00
Europe/Zurich

👤 **Elias Metral**
Vittorio Giorgio Vaccaro

Scientific programme and timeline

Wednesday 23/04/2014: Arrival

21:00 - 23:00: Get-Together-Party

Thursday 24/04/2014:

Session 1: Impedance theory and related effects

Session 2: Impedance numerical simulations

Session 3: Impedance bench and beam-based measurements

Friday 25/04/2014:

Session 4: Extensions of the impedance concept

Session 5: Impedance challenges for new projects

Session 6: Building the impedance model of a machine

Banquet in the evening

Saturday 26/04/2014:

Session 7: Space charge and resistive-wall impedances

Session 8: Geometrical impedance

Session 9: Impedance of diagnostics structures

Poster session at the end of the afternoon

Sunday 27/04/2014: Full-day excursion

Monday 28/04/2014:

Session 10: Impedance of collimators and kickers

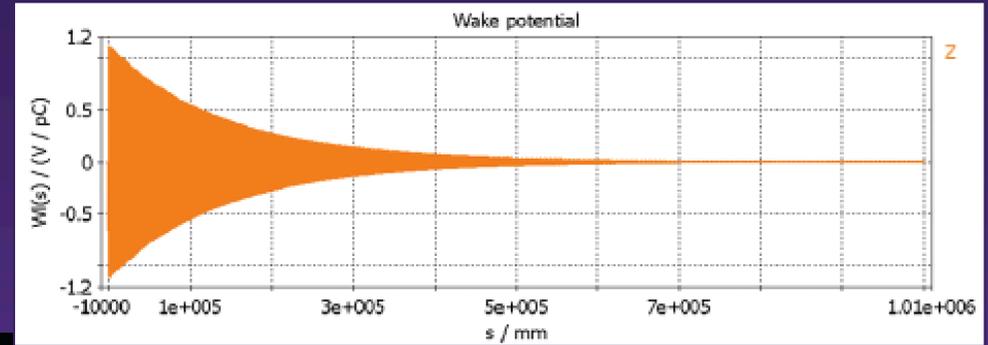
Session 11: Summaries

Tuesday 29/04/2014: Departure

$$E_z = - \frac{Z I}{2\pi R}$$

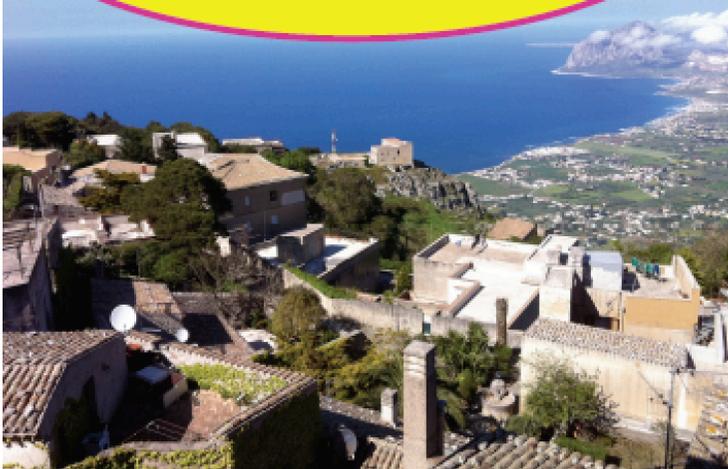
A. Sessler and V. Vaccaro

February 6, 1967



The very 1st paper on impedance was written in November, 1966

Many thanks again for all Vittorio!
(and let's celebrate the 1/2 century in 2016-2017)



- ◆ “Known” 1st introduction of the beam coupling impedance concept for particle accelerators => A. Sessler and V. Vaccaro (1967)

$$U = Z I$$

Ohm's law in electricity

~ Integrated force

=>

$$Z = - \frac{E_z 2 \pi R}{I}$$

Longitudinal impedance
(frequency domain)

In Memoriam: Andrew Sessler, Former Laboratory Director, Acclaimed Physicist and Humanitarian



BERKELEY LAB

Bringing Science Solutions to the World



Andy Sessler (1928-2014)



◆ ...There was another paper in 1966...which could not be known...

Distribution: (closed) AR and ISR Scientific Staff.



ISR-RF/66-35
November 18, 1966

LONGITUDINAL INSTABILITY OF A COASTING BEAM ABOVE TRANSITION, DUE TO
THE ACTION OF LUMPED DISCONTINUITIES.

by V.G. Vaccaro

1. Generalities

We assume that the electrical action on an ion beam, of a discontinuity in a tank is that of an impedance. We still consider the

where a is the beam radius. The passage of an ion beam induces a field in the discontinuity, which is given by:

$$E_d = -Z I/d, \quad (4)$$

where d is the magnitude of the discontinuity, and Z is the impedance of the discontinuity.

REFERENCES

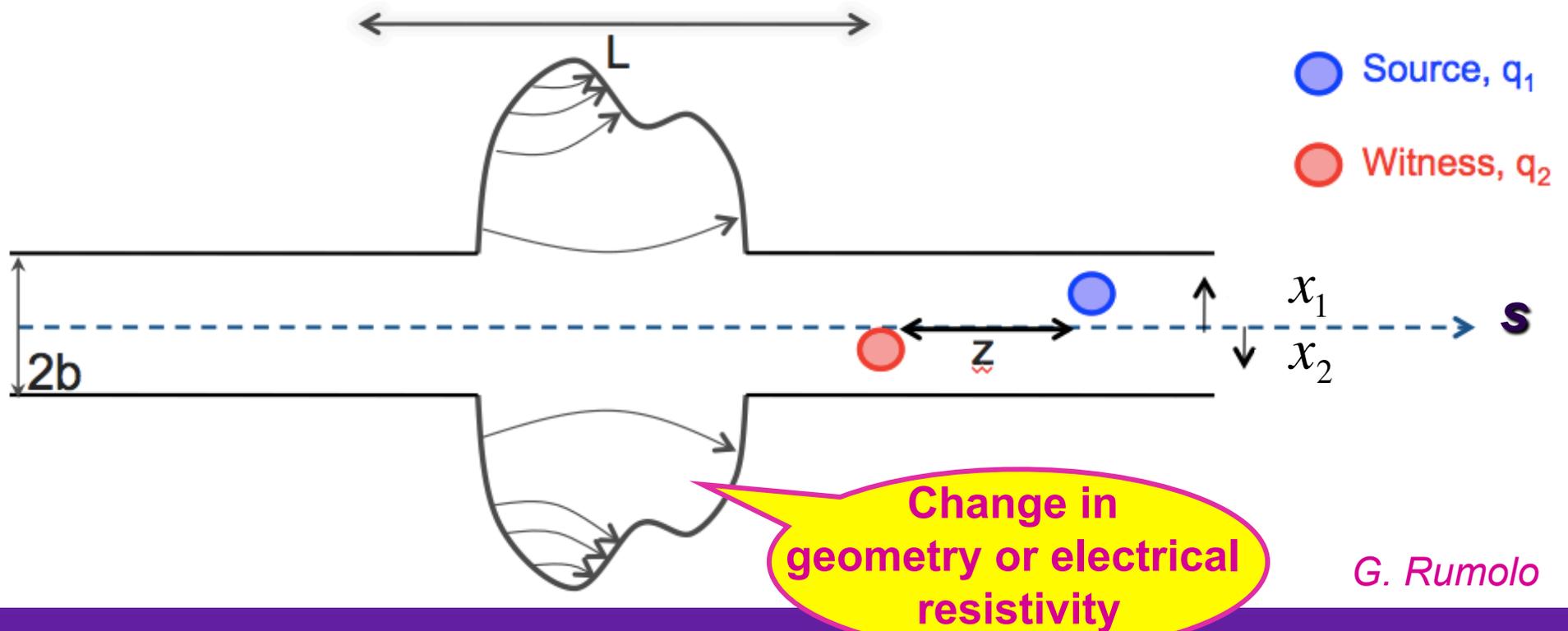
- 1) V.K. Neil and A.M. Sessler
Longitudinal Resistive Instabilities of Intense Coasting Beams in Particle Accelerator
Rev. Sci. Instr. 36, 429 (1965)
- 1) A.M. Sessler and V.G. Vaccaro
Longitudinal Instabilities of Azimuthally Uniform Beams in Circular Vacuum Chambers of Arbitrary Electrical Properties (in preparation).

◆ **Wake field (wake function)** = concept in space / time domain (came few years later => 1969)

=> The 2 are linked by Fourier transforms

LNF - 69/80
23 Dicembre 1969

A. G. Ruggiero and V. G. Vaccaro : THE WAKE FIELD OF AN OSCILLATING PARTICLE IN THE PRESENCE OF CONDUCTIVE PLATES WITH RESISTIVE TERMINATIONS AT BOTH ENDS. -



◆ 2 fundamental approximations behind the “conventional impedances / wakes”

- Rigid-beam approximation =>

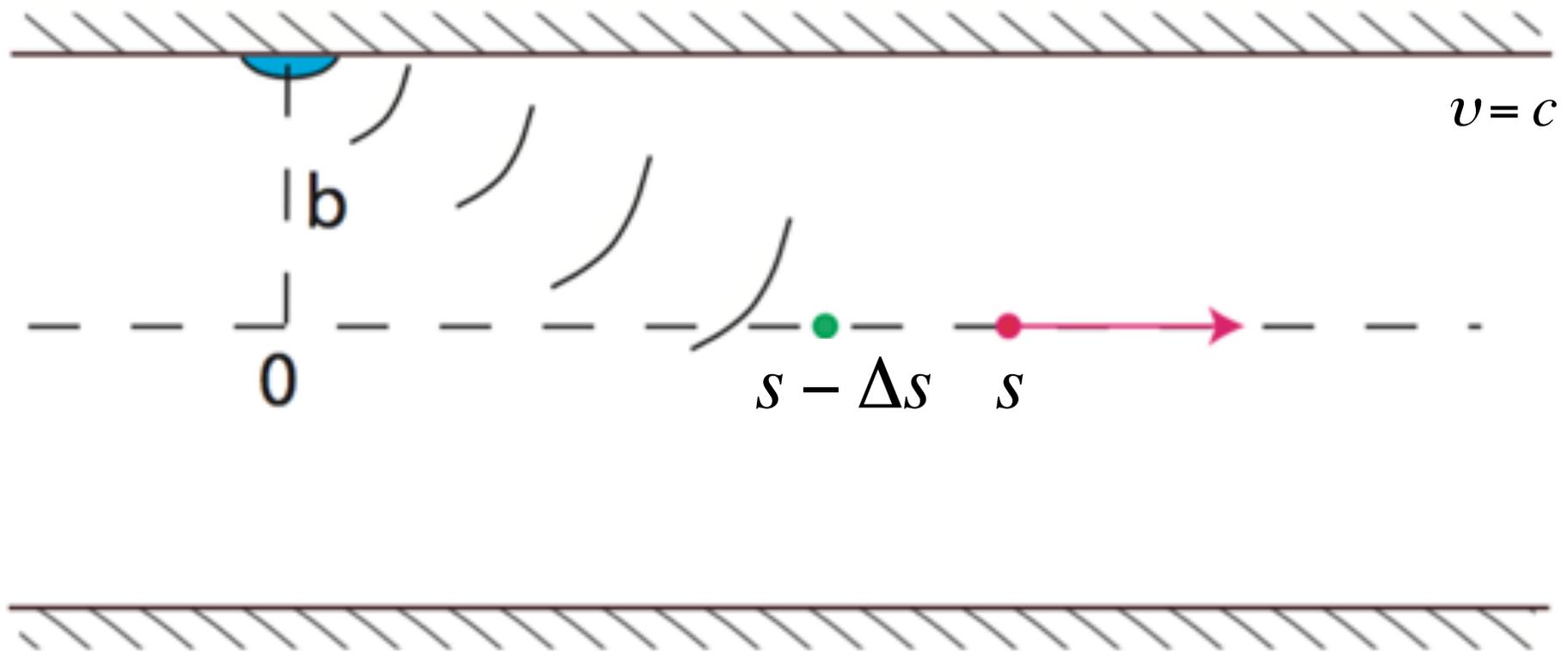
$$z = S_{witness} - S_{source} = \text{Constant}$$

- Impulse approximation =>

$$v \Delta p = \int_0^L F ds$$

Wake potential

◆ “Catch-up” distance



K. Bane and G. Stupakov

$$s^2 = (ct)^2 = (s - \Delta s)^2 + b^2$$

$$\text{If } \Delta s \ll b \Rightarrow s \approx \frac{b^2}{2 \Delta s}$$

- ◆ **Maxwell equations** \Rightarrow Panofsky-Wenzel theorem

$$\vec{\nabla} \times \Delta \vec{p} = 0$$

For $\beta = \text{constant}$

$$\beta = \frac{v}{c}$$

- ◆ **If** $\beta = 1$ \Rightarrow $\vec{\nabla}_{\perp} \cdot \Delta \vec{p}_{\perp} = 0$

◆ **Considering the case of a** cylindrically symmetric chamber

$$v \Delta p_s (r, \theta, z) = \int_0^L F_s ds = -q_1 q_2 x_1^m r^m \cos m\theta W'_m(z)$$

Longitudinal wake
function ($m = 0$)

Transverse wake
function ($m = 1$)

$$v \Delta p_r (r, \theta, z) = \int_0^L F_r ds = -q_1 q_2 x_1^m m r^{m-1} \cos m\theta W_m(z)$$

$$v \Delta p_\theta (r, \theta, z) = \int_0^L F_\theta ds = q_1 q_2 x_1^m m r^{m-1} \sin m\theta W_m(z)$$

- ◆ **Impedances are related to wake functions by Fourier transforms**

$$Z_m^{//}(\omega) = - \int_{-\infty}^{+\infty} W_m'(z) e^{jkz} \frac{dz}{v}$$

$$Z_m^{\perp}(\omega) = j \int_{-\infty}^{+\infty} W_m(z) e^{jkz} \frac{dz}{v}$$

- ◆ **As the conductivity, permittivity and permeability of a material depend in general on frequency, it is usually better (or easier) to treat the problem in the frequency domain, i.e. compute the impedance instead of the wake function**
- ◆ **It is also easier to treat the case $\beta \neq 1$**

◆ **2 important properties of impedances**

- As wake functions are real, it can be shown that

$$\left[Z_m^{\parallel}(\omega) \right]^* = Z_m^{\parallel}(-\omega)$$

$$-\left[Z_m^{\perp}(\omega) \right]^* = Z_m^{\perp}(-\omega)$$

- As consequence of Panofsky-Wenzel theorem

$$Z_m^{\parallel}(\omega) = k Z_m^{\perp}(\omega)$$

- ◆ **Another interesting property of impedances is the directional symmetry (Lorentz reciprocity theorem): same impedance is obtained from both sides if entrance and exit are the same**

- ◆ **Situation is more involved in the case of non axi-symmetric structures (or $\beta \neq 1$). Taking into account only linear terms**

or dipolar

or quadrupolar

$$q_1 = q_2 = q$$

$$\int_0^L F_x ds = -q^2 \left[x_1 W_x^{\text{driving}}(z) - x_2 W^{\text{detuning}}(z) \right]$$

$$\int_0^L F_y ds = -q^2 \left[y_1 W_y^{\text{driving}}(z) + y_2 W^{\text{detuning}}(z) \right]$$

$$Z_x [\Omega] = x_1 Z_x^{\text{driving}} - x_2 Z^{\text{detuning}}$$

$$Z_y [\Omega] = y_1 Z_y^{\text{driving}} + y_2 Z^{\text{detuning}}$$

- ◆ **Analytical computations are possible only if structures are fairly simple**
- ◆ **In practice this is often not the case and one has to rely on numerical techniques**
- ◆ **First numerical wake field computations were performed in time domain (Balakin1978 and Weiland1980)**
- ◆ **For highly relativistic bunches, due to causality, wake fields can catch up with trailing particles only after traveling the catch-up distance => Compute wakes in linacs by using a mesh that moves together with the bunch (moving mesh technique introduced by Bane-Weiland1983)**

- ◆ **Nowadays many methods are available for beam coupling impedance computation**
 - Time Domain (TD) method
 - Frequency Domain (FD) method
 - Eigenmode methods
 - Methods based on beam excitation in FD

- ◆ **Main ElectroMagnetic (EM) codes currently used**
 - ABCI
 - Ansys HFSS
 - CST Studio (MAFIA)
 - GdfidL
 - ECHO2D
 - ACE3P
 - Etc.

◆ Time Domain (TD)

- Finite Differences Time Domain (FDTD) and Finite Integration Technique (FIT) with leapfrog algorithm for time stepping
- More specialized techniques
 - Boundary element method (TD-BEM)
 - Finite volume method (FVTD)
 - Discontinuous Galerkin Finite Element (DG-FEM)
 - Implicit methods
- Bunch length and wake length are the 2 important parameters for TD impedance computation
- The criterion for the time step is also referred to as the Courant-Friedrichs-Lewy (CFL) criterion
- Suitable at **medium and high frequencies**, and particularly in **perfectly conducting structures**

◆ **Frequency Domain (FD): Eigenmode methods**

- When high quality factor structures are under investigation and high accuracy is required

Shunt impedances

$$Z_m^{||}(\omega) = \frac{R_s}{1 + jQ \left(\frac{\omega}{\omega_r} - \frac{\omega_r}{\omega} \right)}$$

$$Z_m^{\perp}(\omega) = \frac{\omega_r}{\omega} \frac{R_{\perp}}{1 + jQ \left(\frac{\omega}{\omega_r} - \frac{\omega_r}{\omega} \right)}$$

Quality factor

(Angular) resonance frequency

$$W_m^{||}(t) = \frac{\omega_r R_s}{Q} e^{-\alpha t} \left[\cos(\bar{\omega}_r t) - \frac{\alpha}{\bar{\omega}_r} \sin(\bar{\omega}_r t) \right]$$

$$W_m^{\perp}(t) = \frac{\omega_r^2 R_{\perp}}{Q \bar{\omega}_r} e^{-\alpha t} \sin(\bar{\omega}_r t)$$

$$\bar{\omega}_r = \omega_r \sqrt{1 - \frac{1}{4Q^2}}$$

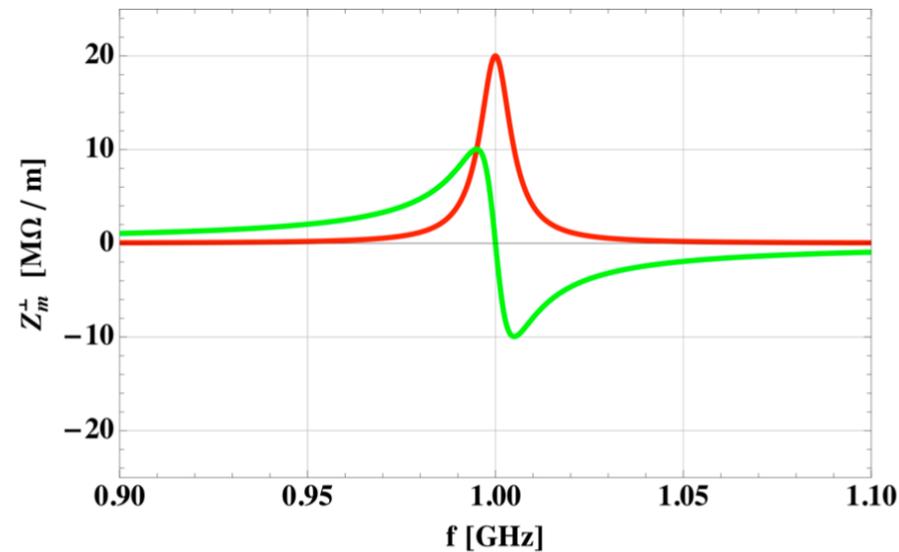
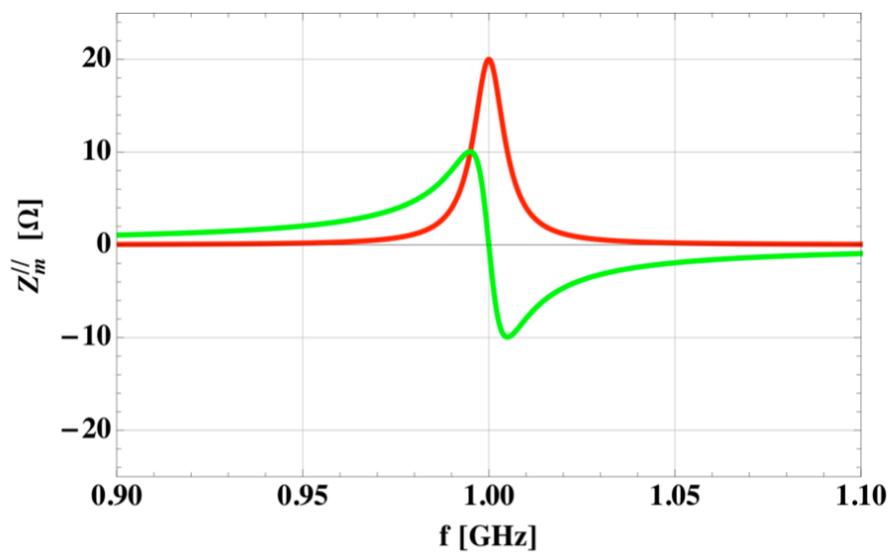
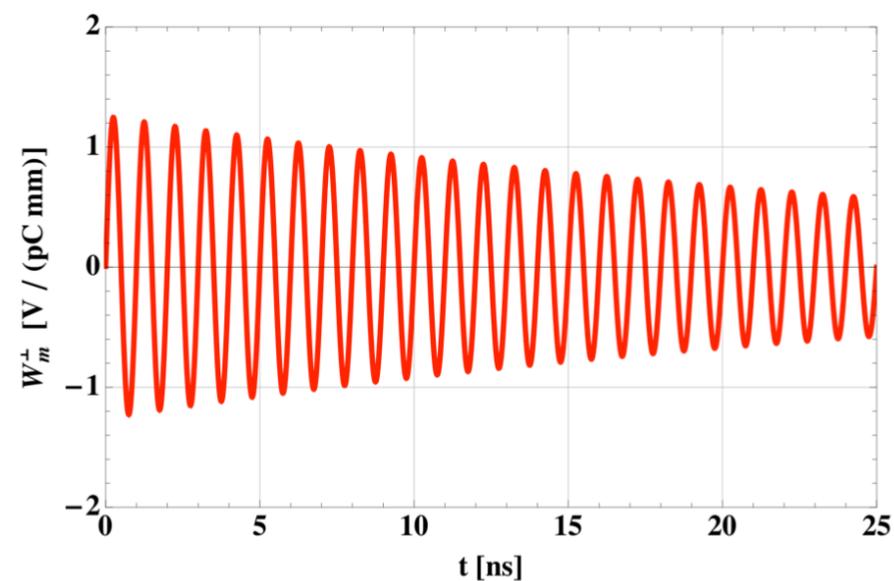
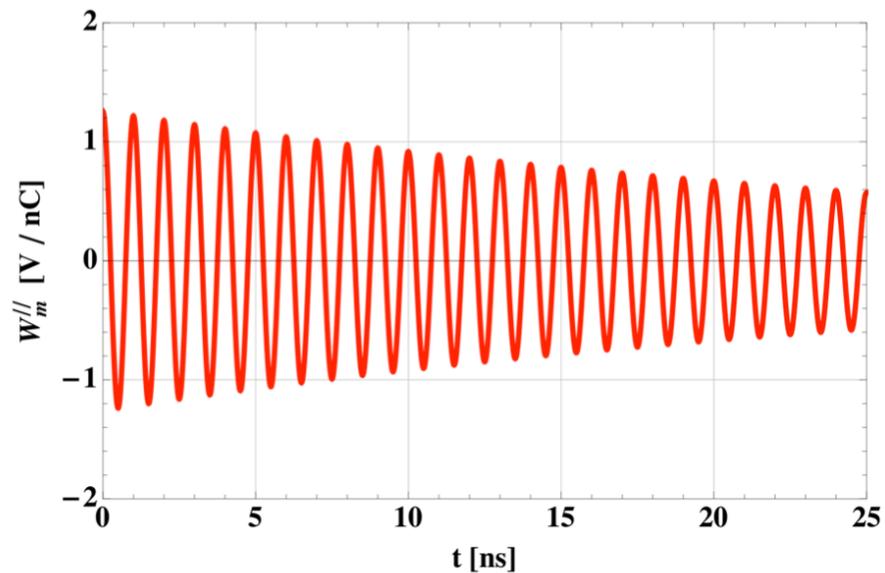
$$\alpha = \frac{\omega_r}{2Q}$$

$$R_s = 20 \Omega$$

$$R_{\perp} = 20 \text{ M}\Omega/\text{m}$$

$$f_r = 1 \text{ GHz}$$

$$Q = 100$$



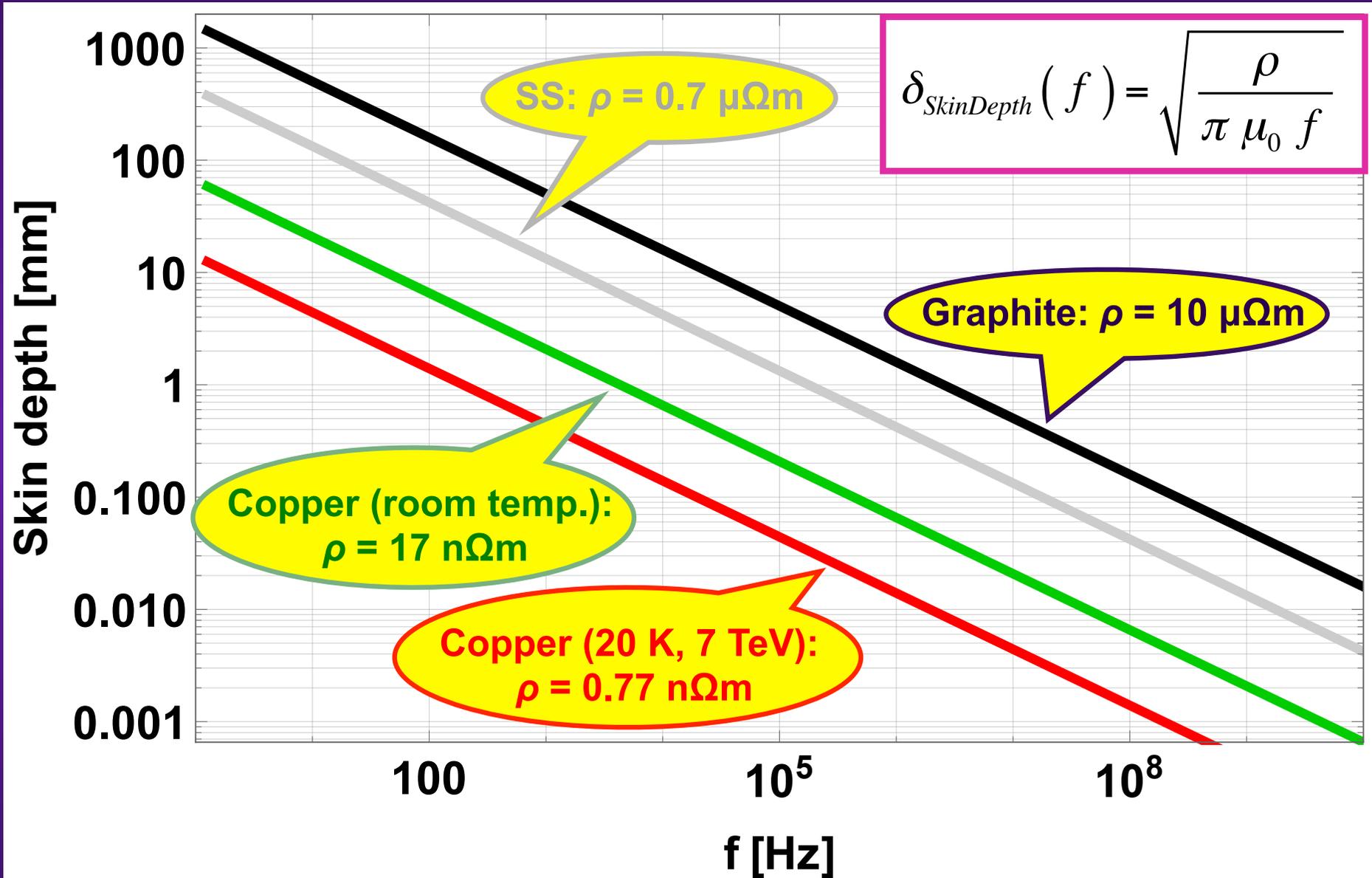
◆ **Frequency Domain (FD):** Methods based on beam excitation in FD

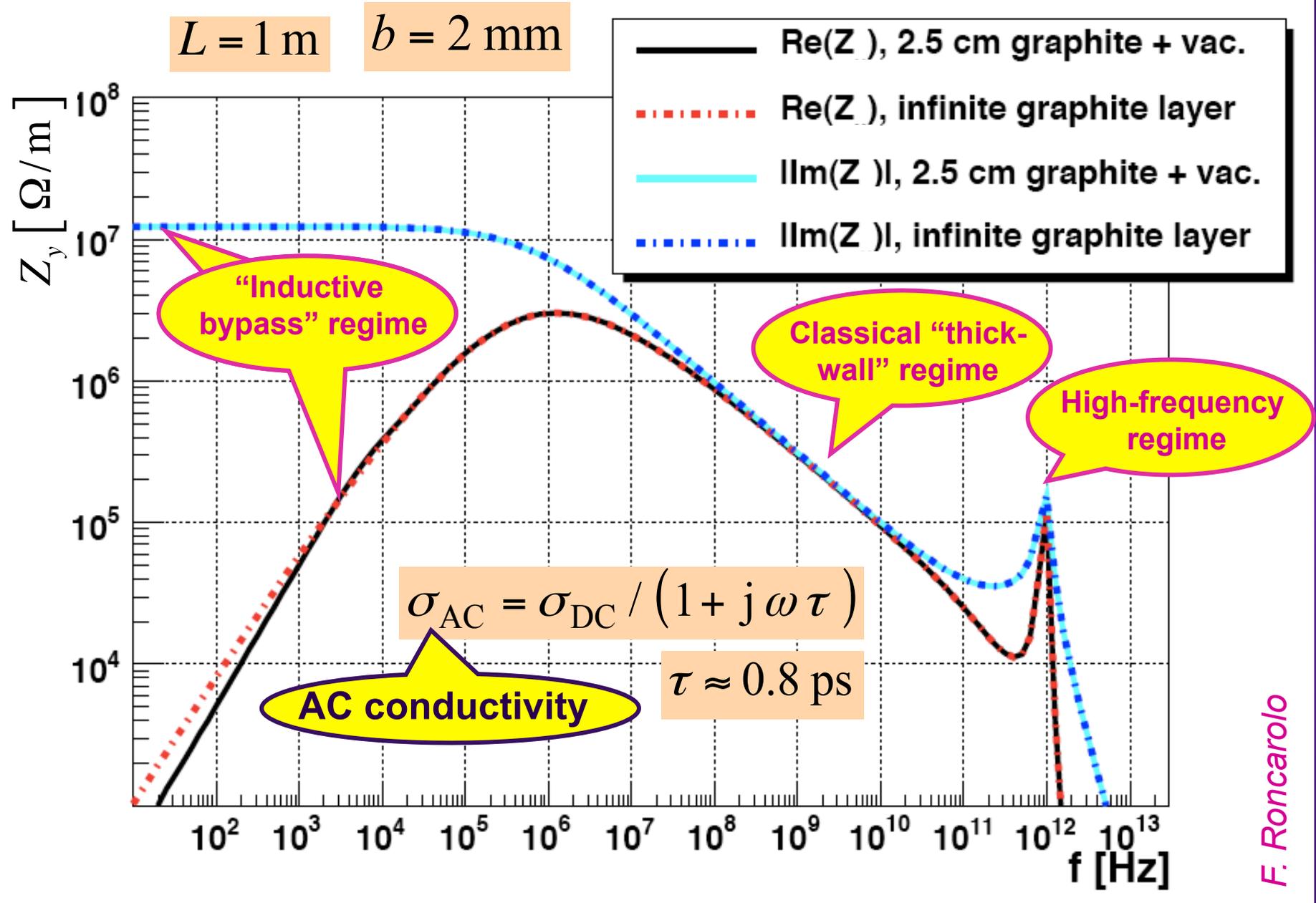
- At low frequencies, the CFL criterion poses a strong requirement on the time step
- Due to uncertainty principle, lower frequencies require computing longer wakes. As the time step is fixed by structure properties via the CFL criterion, this leads to the necessity to compute many time steps
- FD methods prevail for
 - Low frequency
 - Low velocity of the beam
 - Dispersively lossy materials

- ◆ **Particularly difficult components are** those which combine elements of geometric wake fields and resistive elements **(like tapered collimators or dielectric structures)**
- ◆ **Impedances of surface roughness and of small random pumping slots (e.g. LHC beam screen) are difficult to model**
- ◆ EM properties of some materials **(vs. frequency) are not well known and should be measured with precision**

◆ Analytical computations

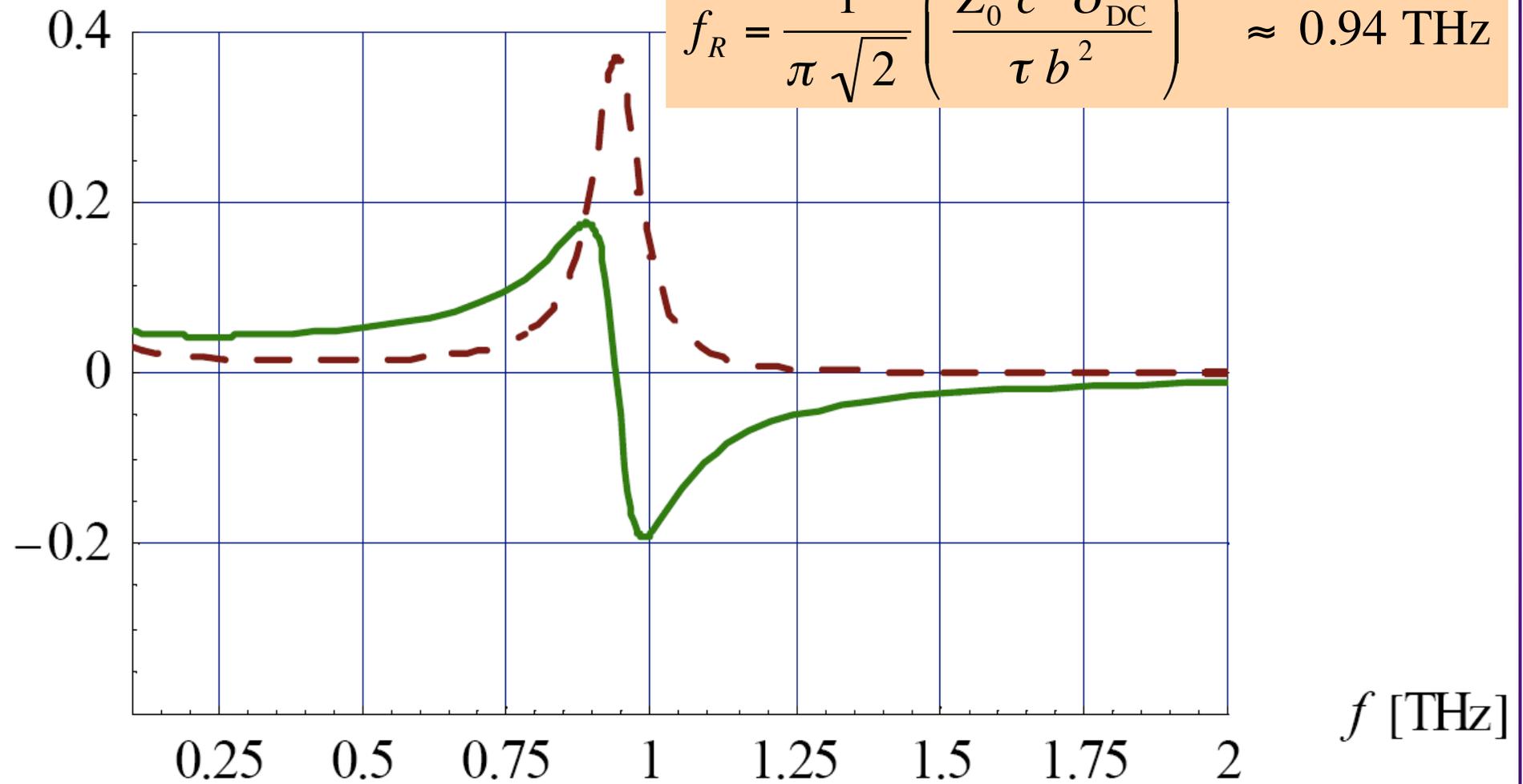
- **FIELD MATCHING:** Continuity of EM field components on separating surfaces
 - Many studies performed
 - IW2D code for round or // plates (N. Mounet)
- **MODE MATCHING:** Decomposition of the fields in summation of modes and matching of each mode coefficient by proper field projection on the correspondent mode
 - Effect of finite length (N. Biancacci)
 - IW2D valid if $L \gg b$



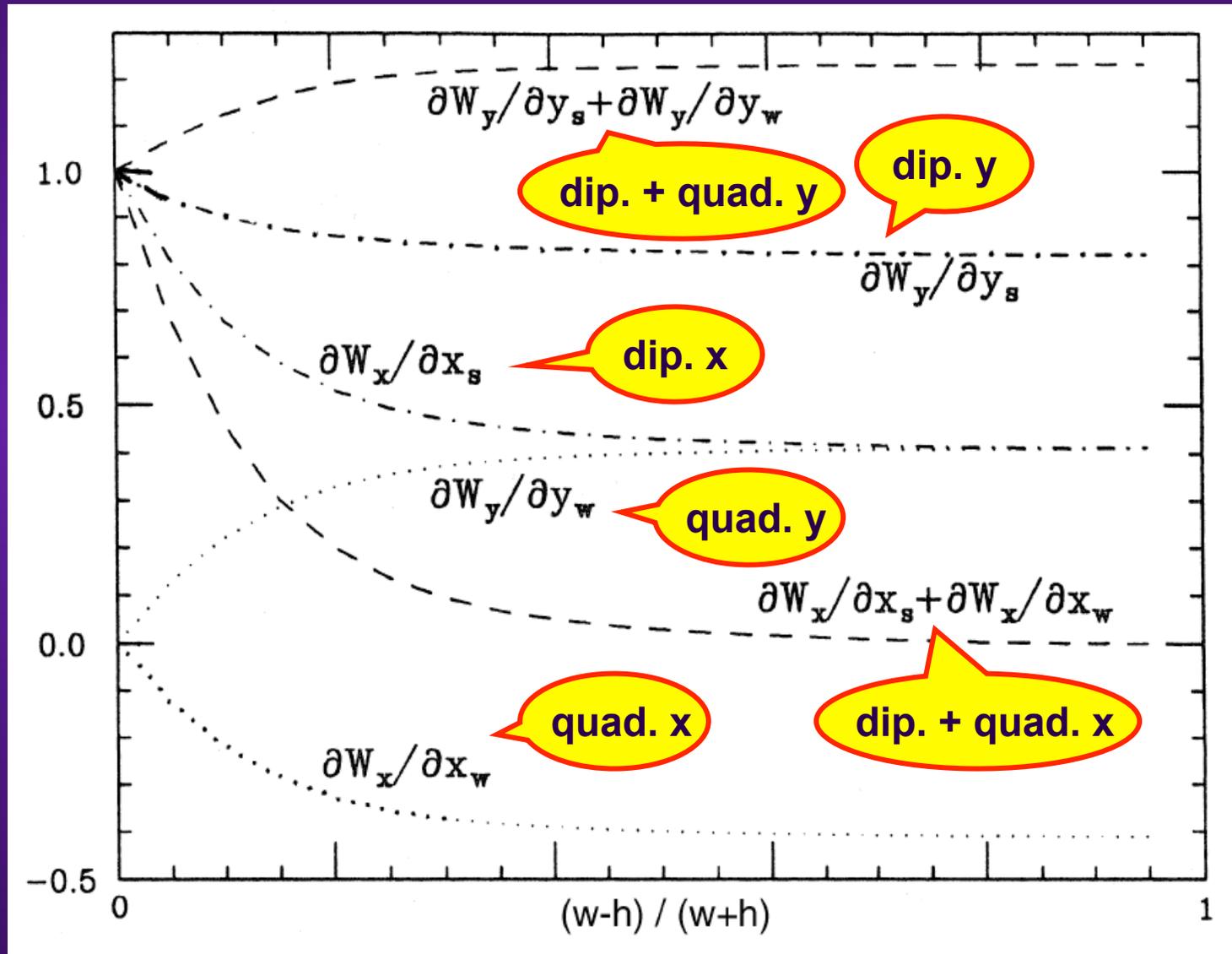


F. Roncarolo

Z_y [M Ω /m]



Yokoya form factors for dipolar and quadrupolar impedances in resistive elliptical pipes (compared to circular)



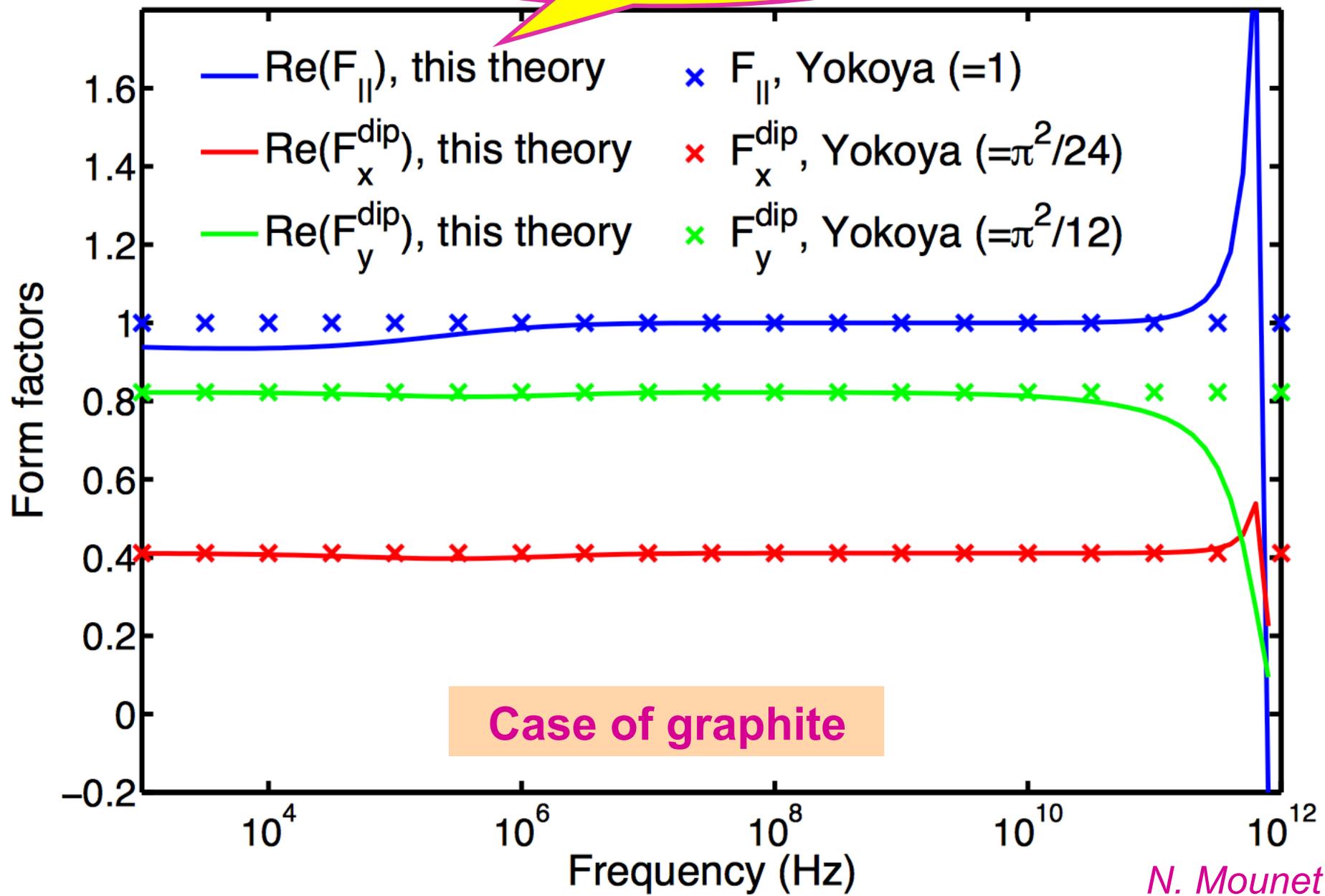
$$\frac{\pi^2}{8}$$

$$\frac{\pi^2}{12}$$

$$\frac{\pi^2}{24}$$

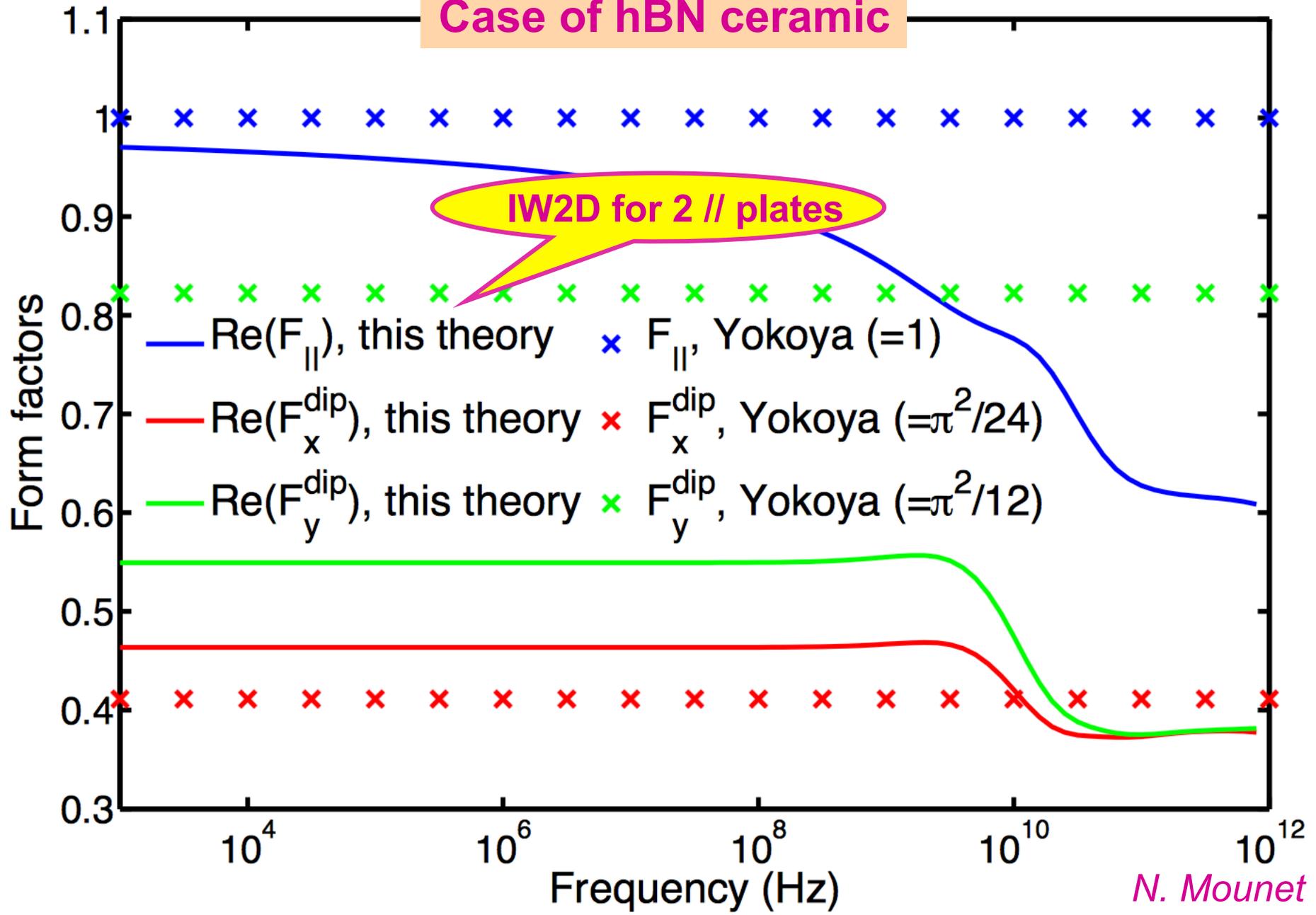
$$-\frac{\pi^2}{24}$$

IW2D for 2 // plates



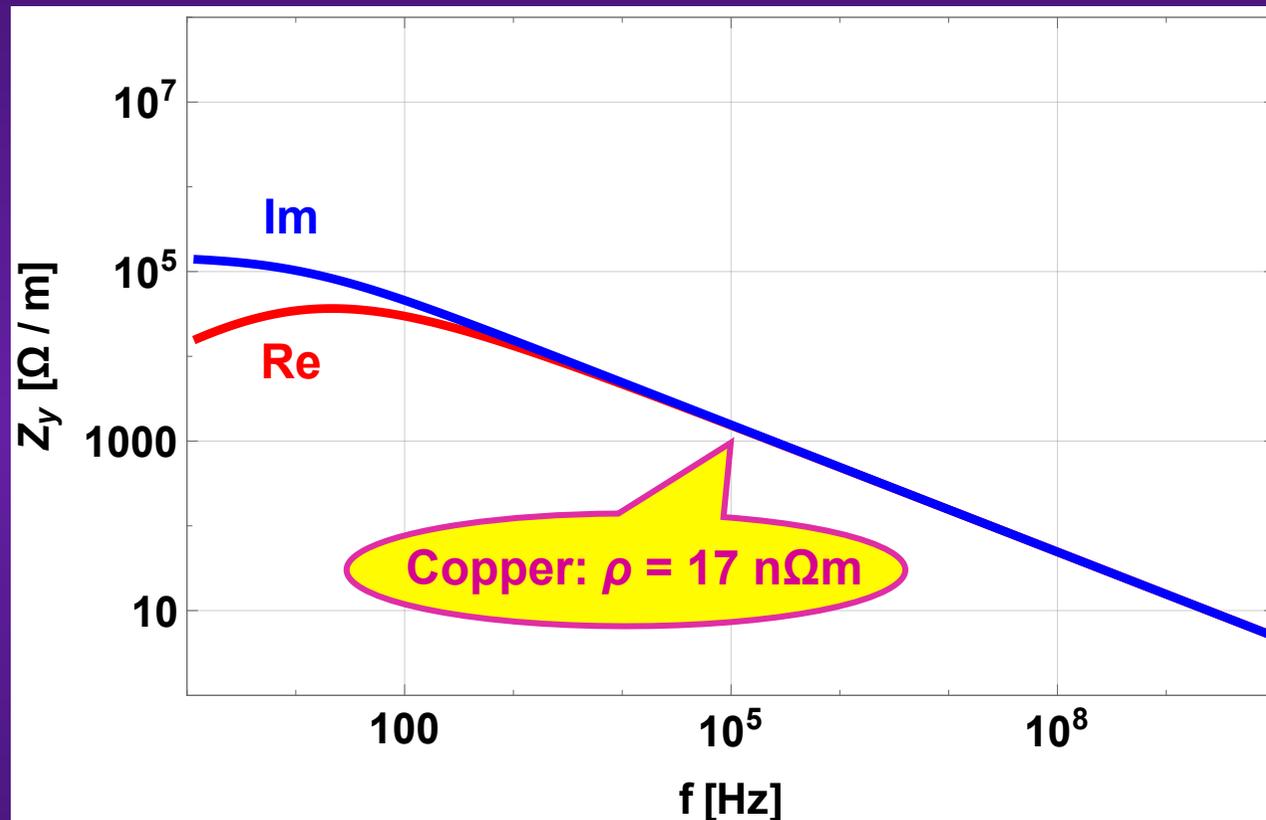
N. Mounet

Case of hBN ceramic

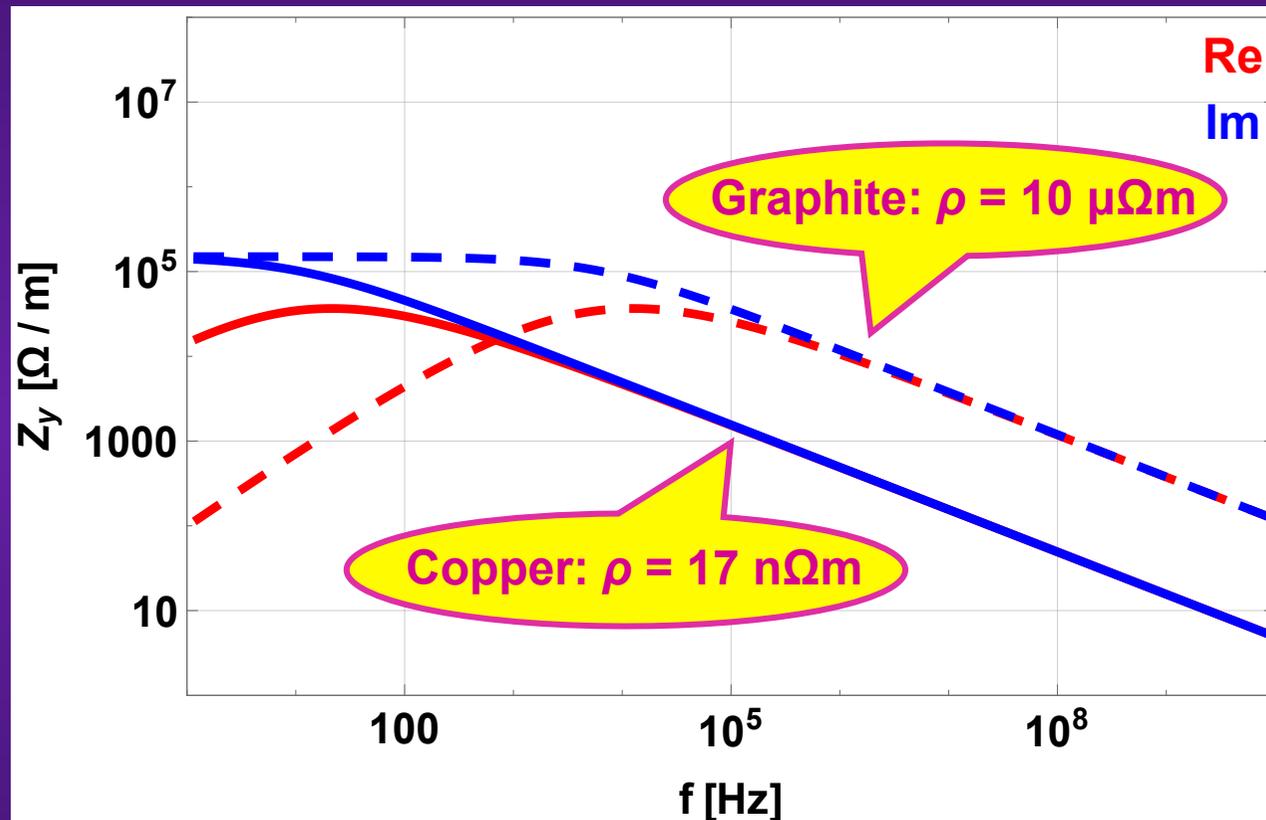


N. Mounet

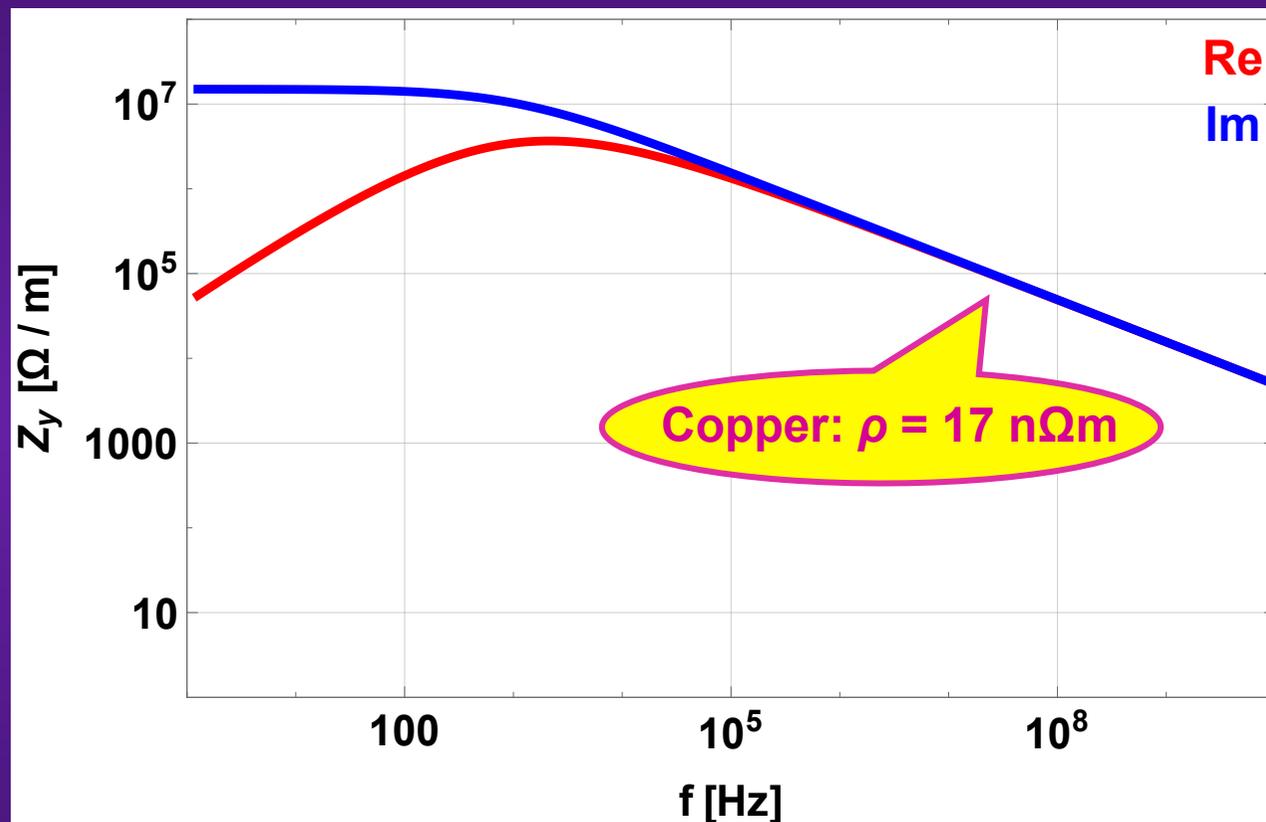
LHC beam pipe: round, 20 mm radius, 1 m long



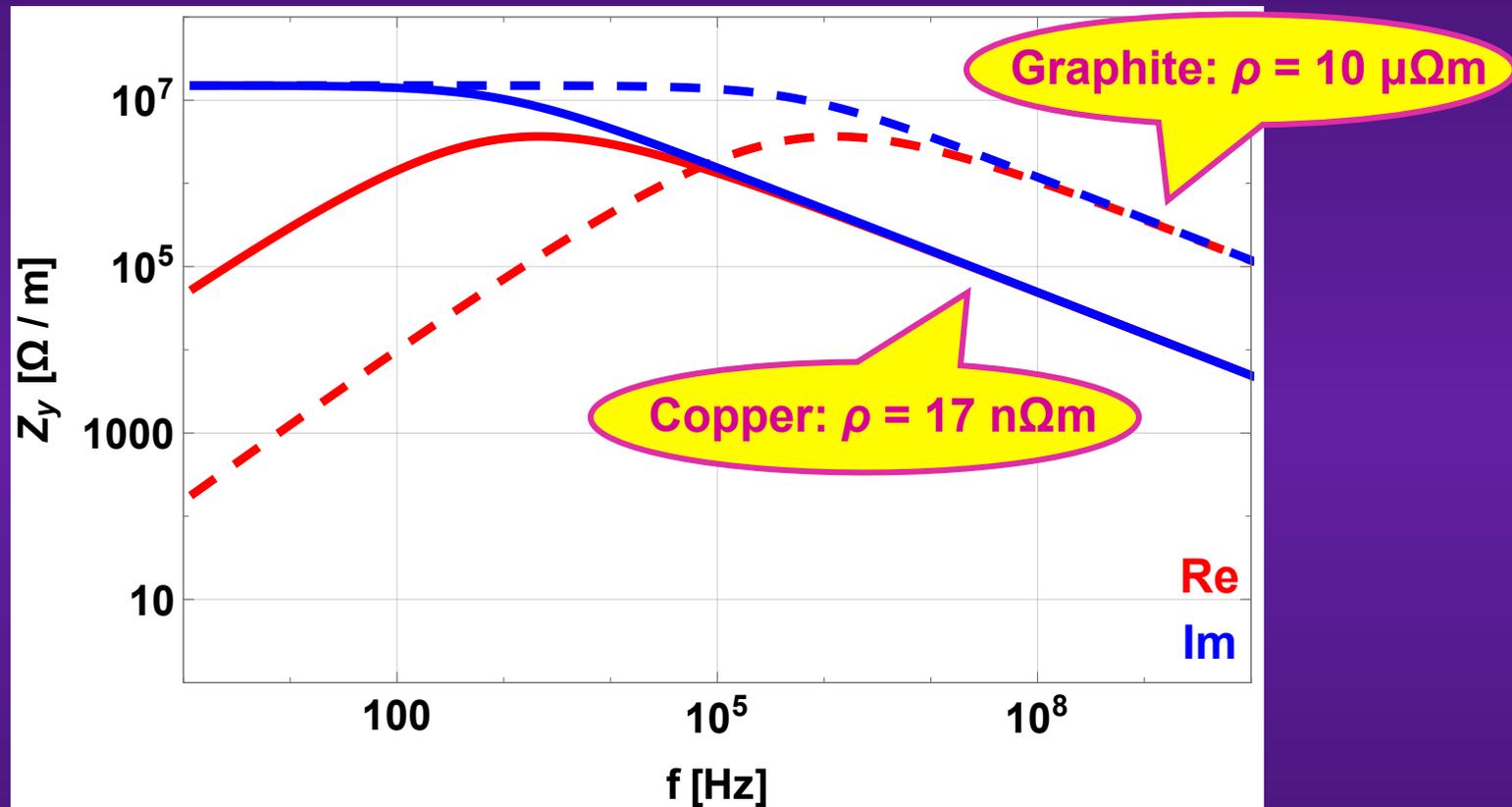
LHC beam pipe: round, 20 mm radius, 1 m long



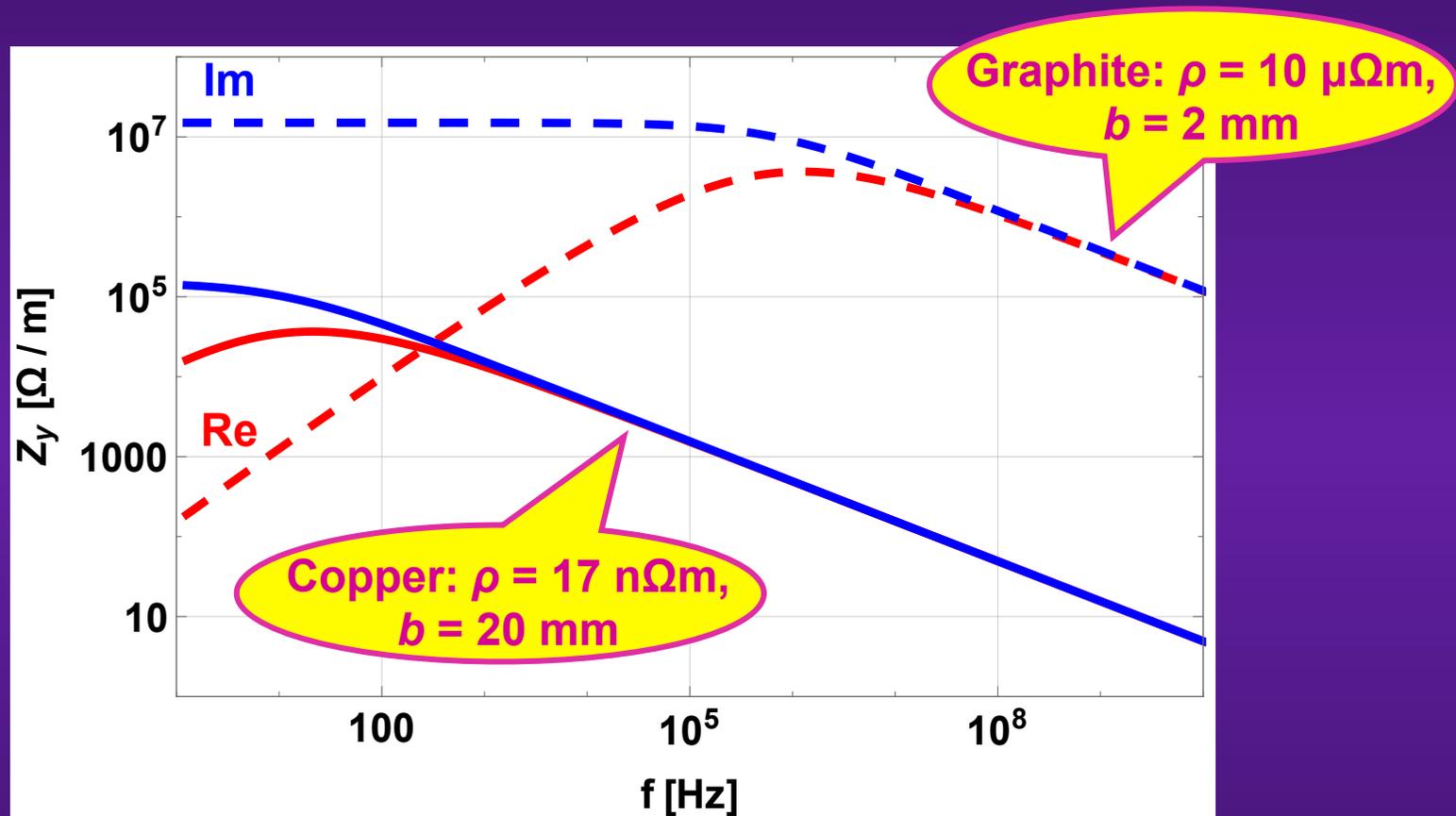
LHC beam pipe: round, 2 mm radius, 1 m long



LHC beam pipe: round, 2 mm radius, 1 m long

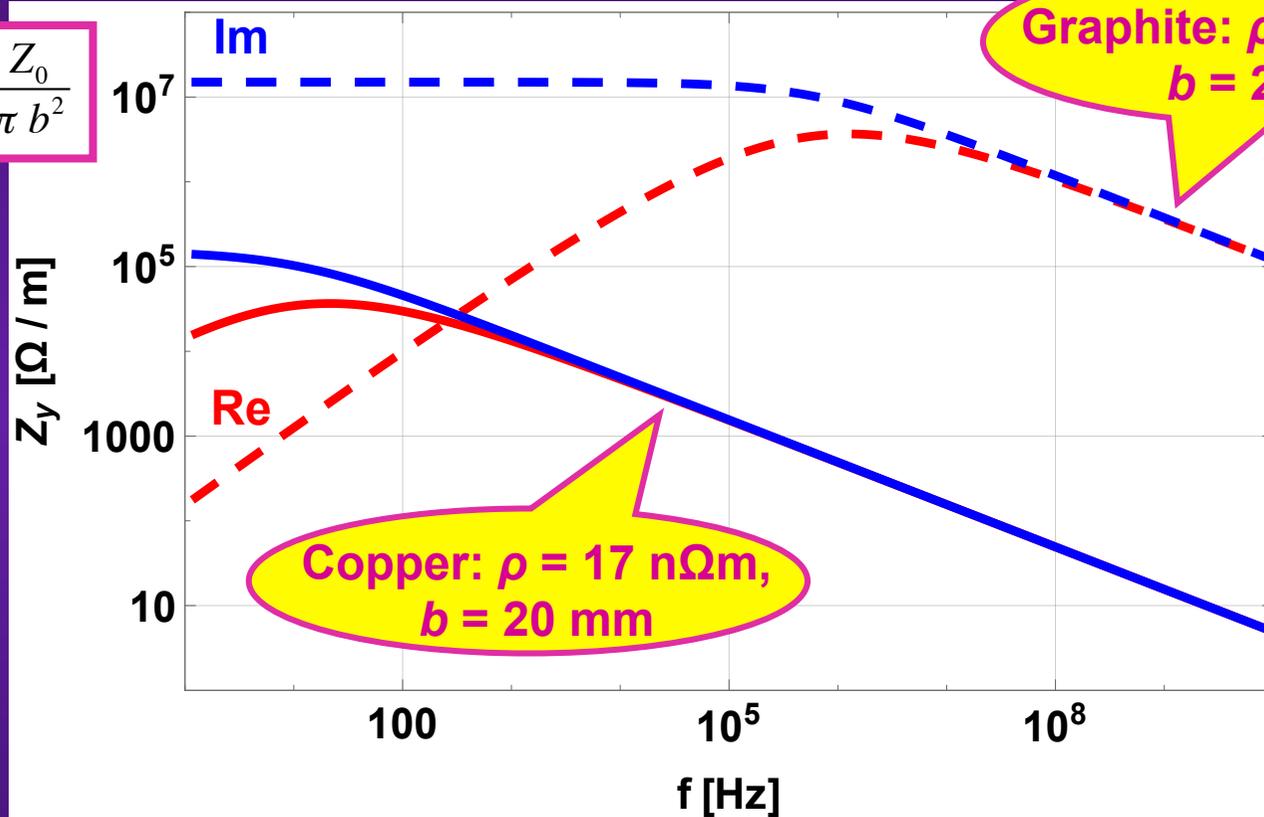


LHC beam pipe: round, 1 m long



LHC beam pipe: round, 1 m long

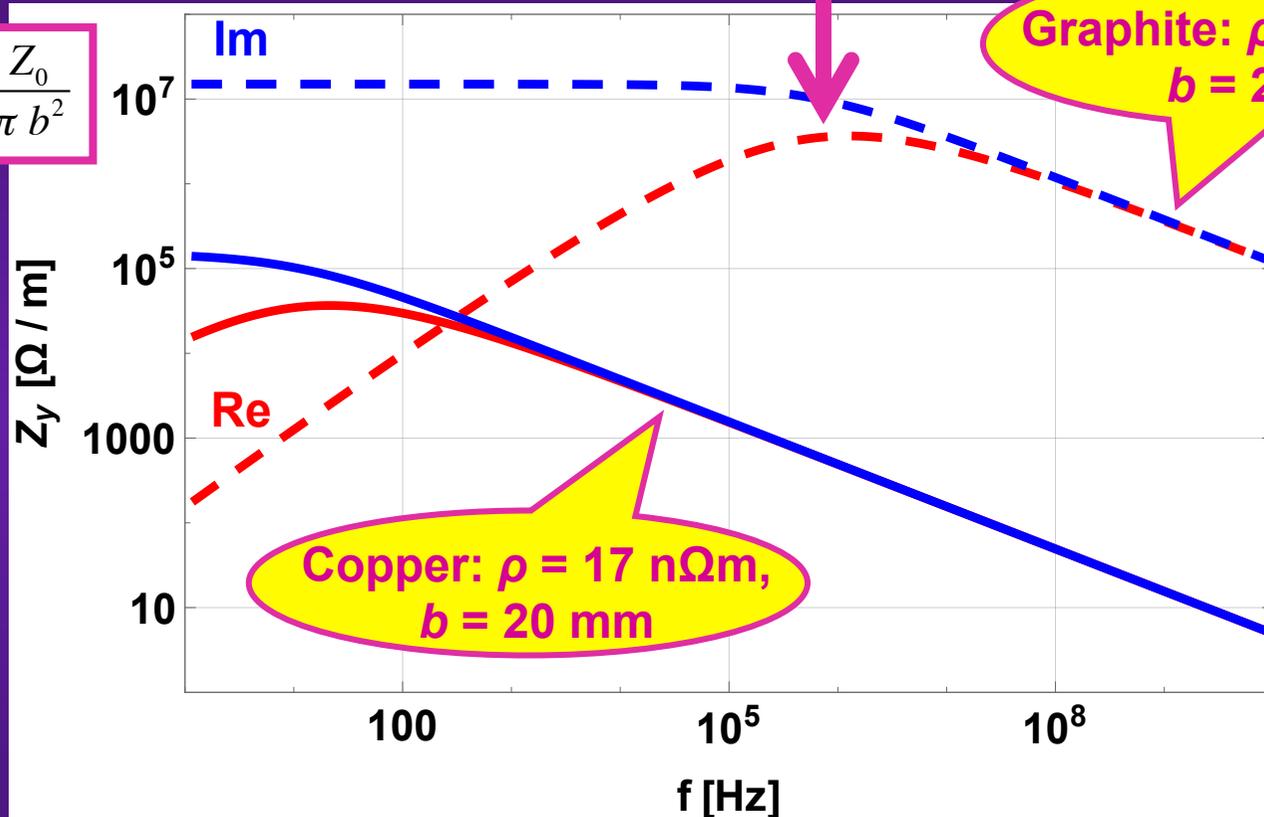
$$Z_y(f \rightarrow 0) = \frac{j Z_0}{2\pi b^2}$$



LHC beam pipe: round, 1 m long

$$f_{\max, \text{Re}} \approx \frac{\rho}{b^2} \times \frac{1}{\pi \mu_0}$$

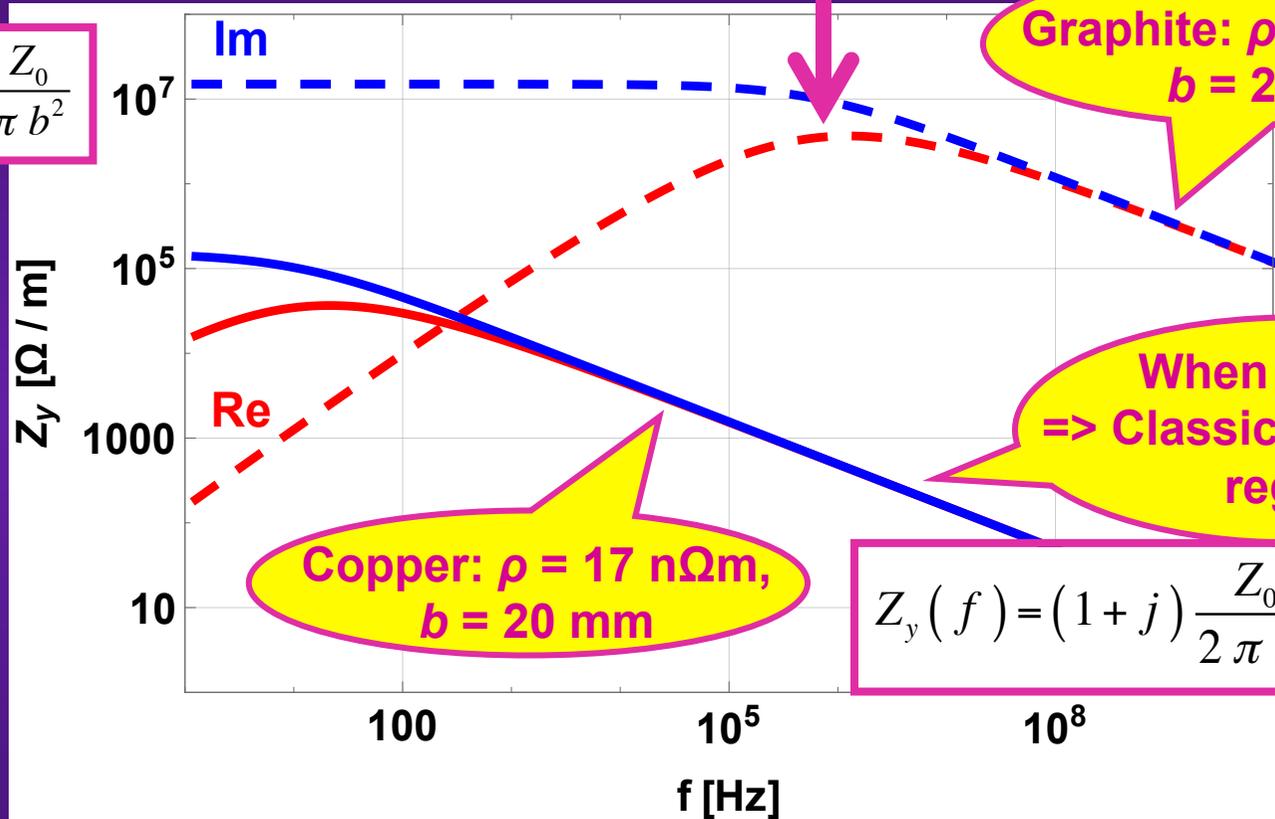
$$Z_y(f \rightarrow 0) = \frac{j Z_0}{2 \pi b^2}$$



LHC beam pipe: round, 1 m long

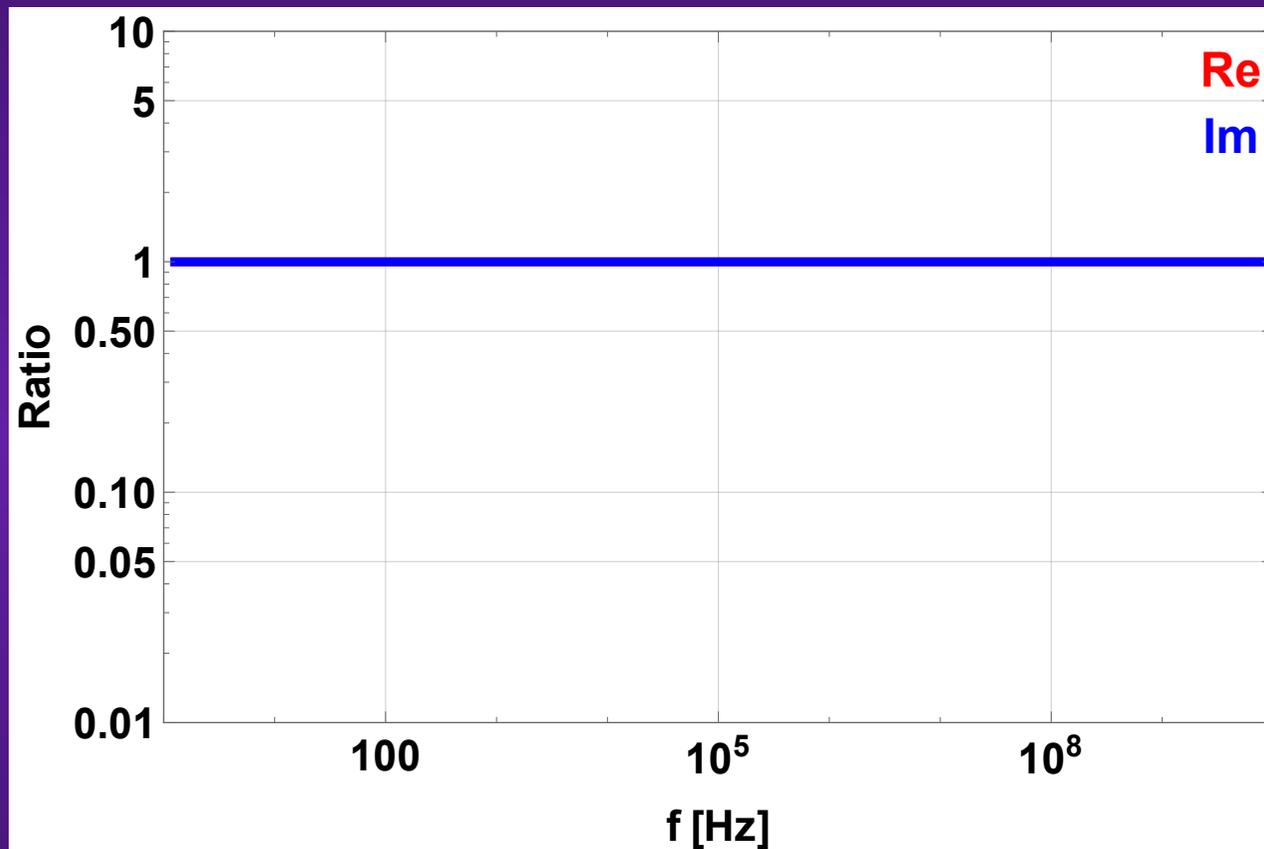
$$f_{\max, \text{Re}} \approx \frac{\rho}{b^2} \times \frac{1}{\pi \mu_0}$$

$$Z_y(f \rightarrow 0) = \frac{j Z_0}{2 \pi b^2}$$



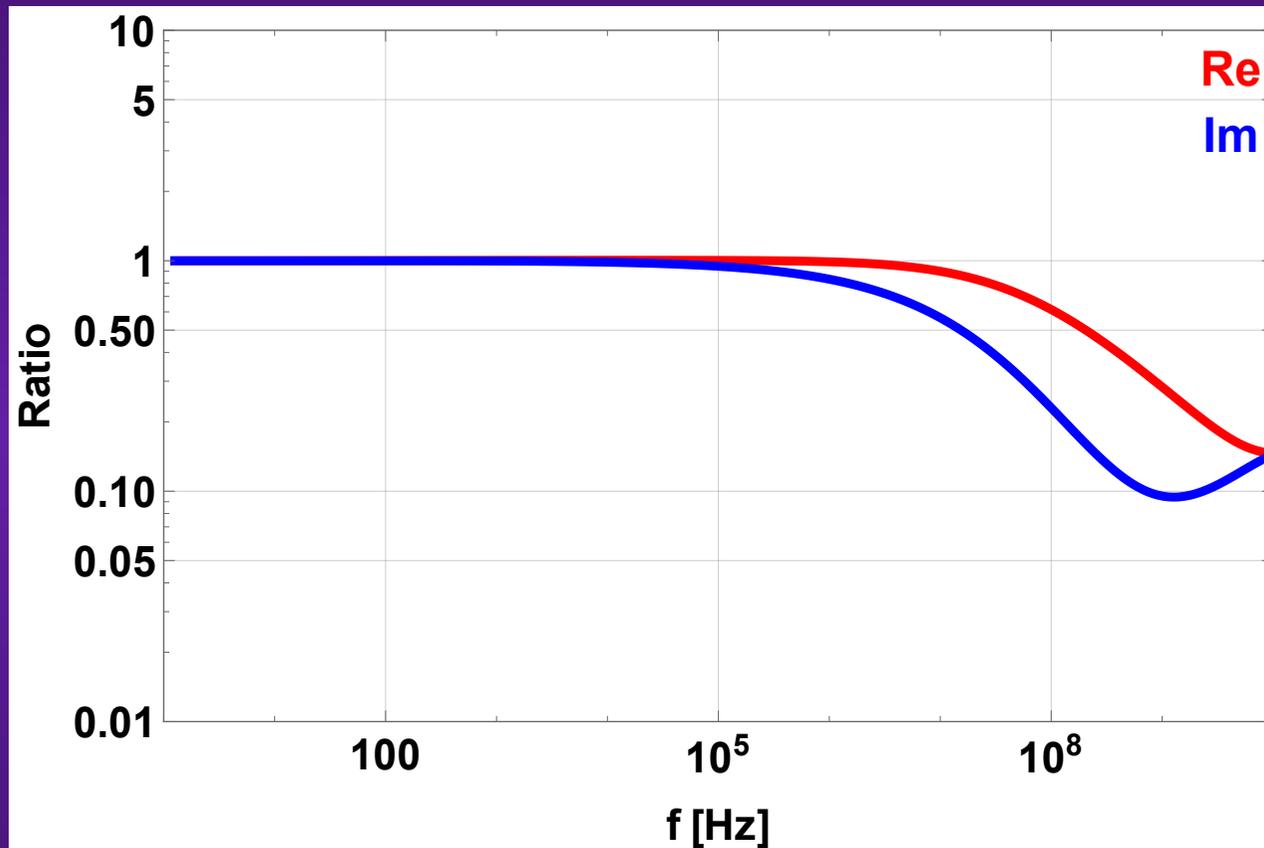
$$Z_y(f) = (1 + j) \frac{Z_0}{2 \pi b^3} \delta_{\text{SkinDepth}}(f)$$

SS beam pipe with 20 mm radius and 0 μm copper coating (room temp.)



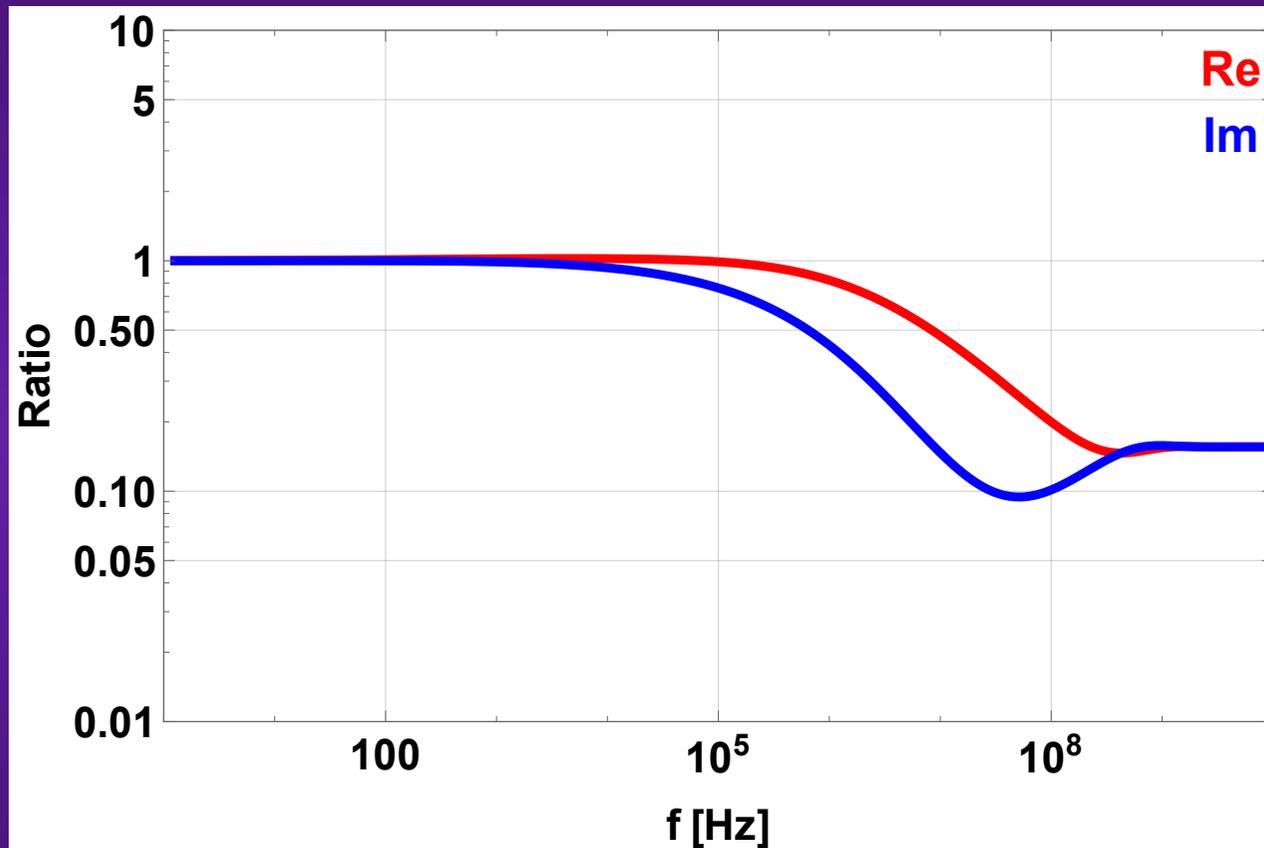
$$\text{Ratio} = \frac{Z_y(\text{ with coating })}{Z_y(\text{ without coating })}$$

SS beam pipe with 20 mm radius and 1 μm copper coating (room temp.)



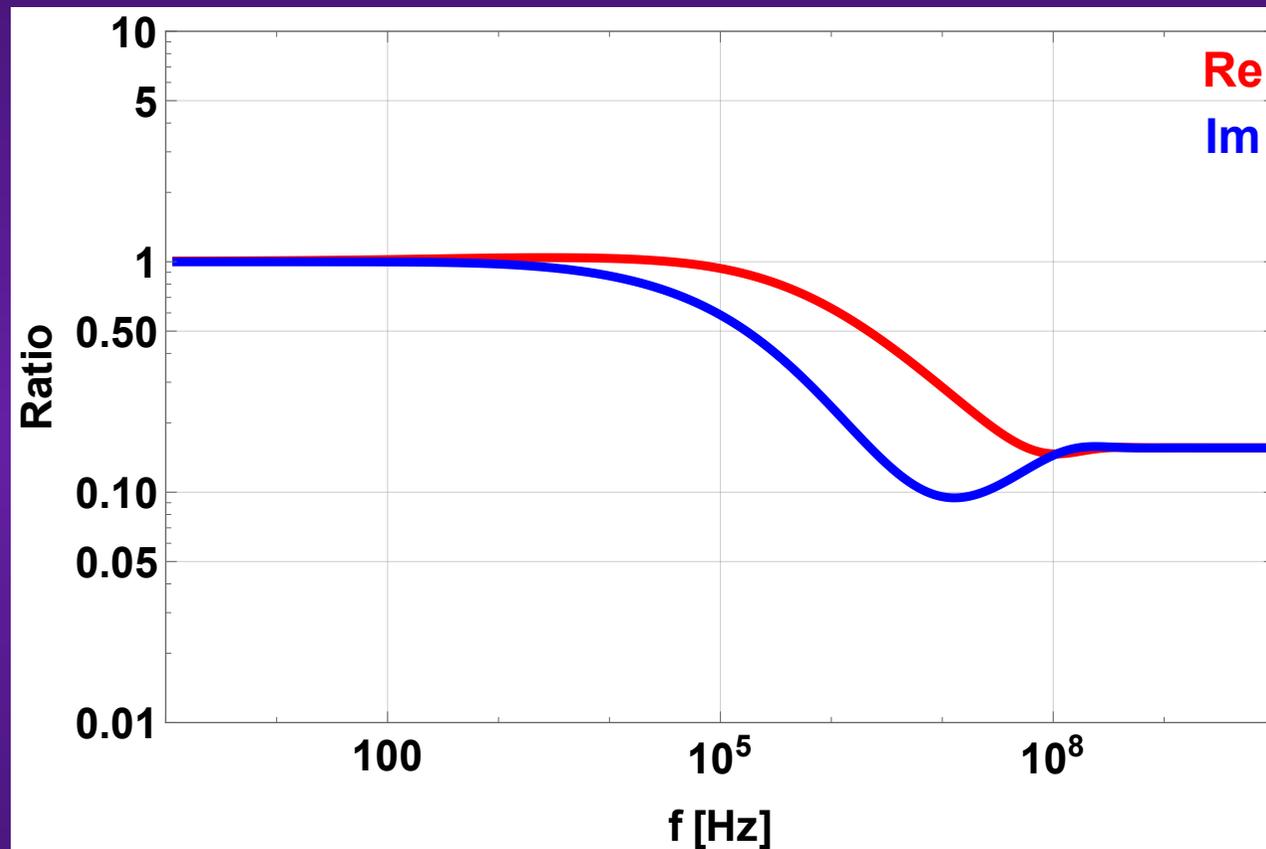
$$\text{Ratio} = \frac{Z_y (\text{ with coating })}{Z_y (\text{ without coating })}$$

SS beam pipe with 20 mm radius and 5 μm copper coating (room temp.)



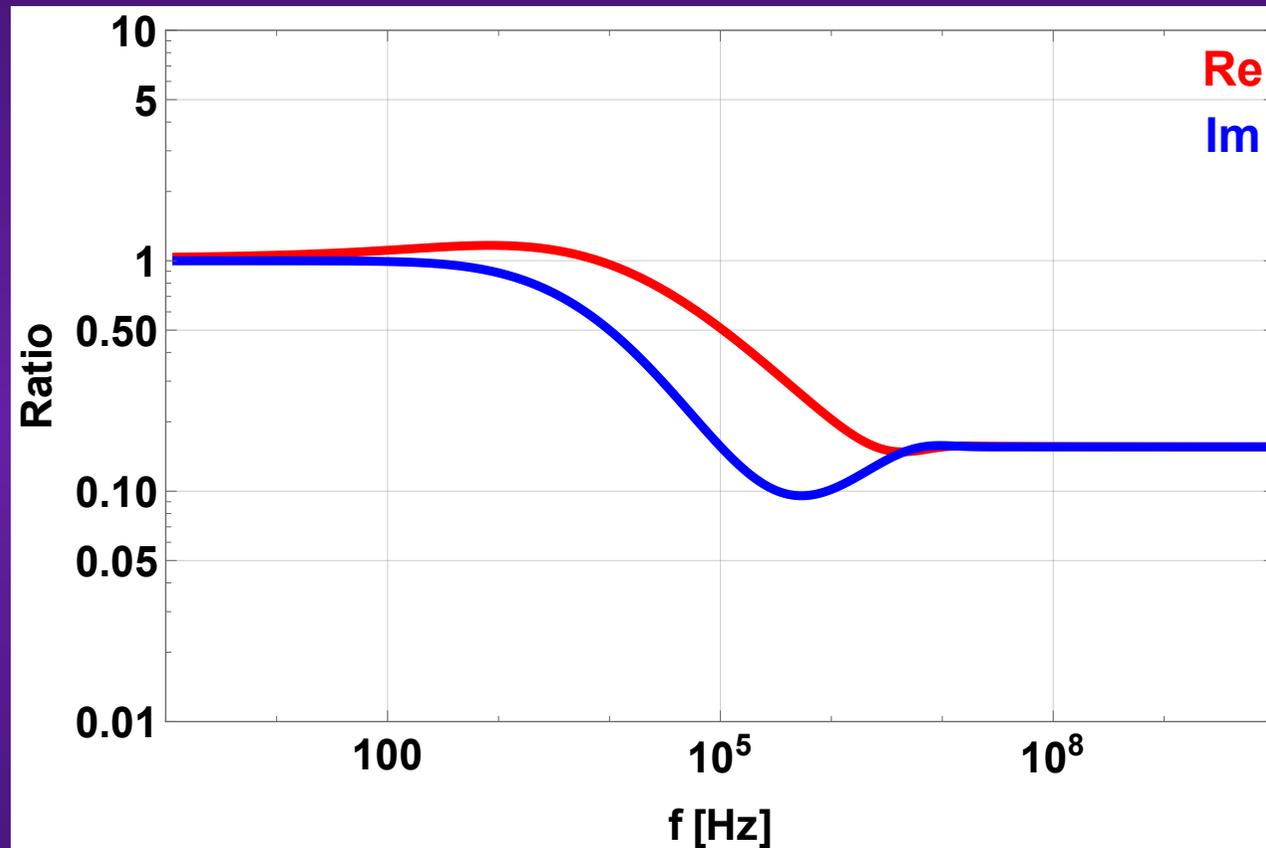
$$\text{Ratio} = \frac{Z_y(\text{ with coating })}{Z_y(\text{ without coating })}$$

SS beam pipe with 20 mm radius and 10 μm copper coating (room temp.)



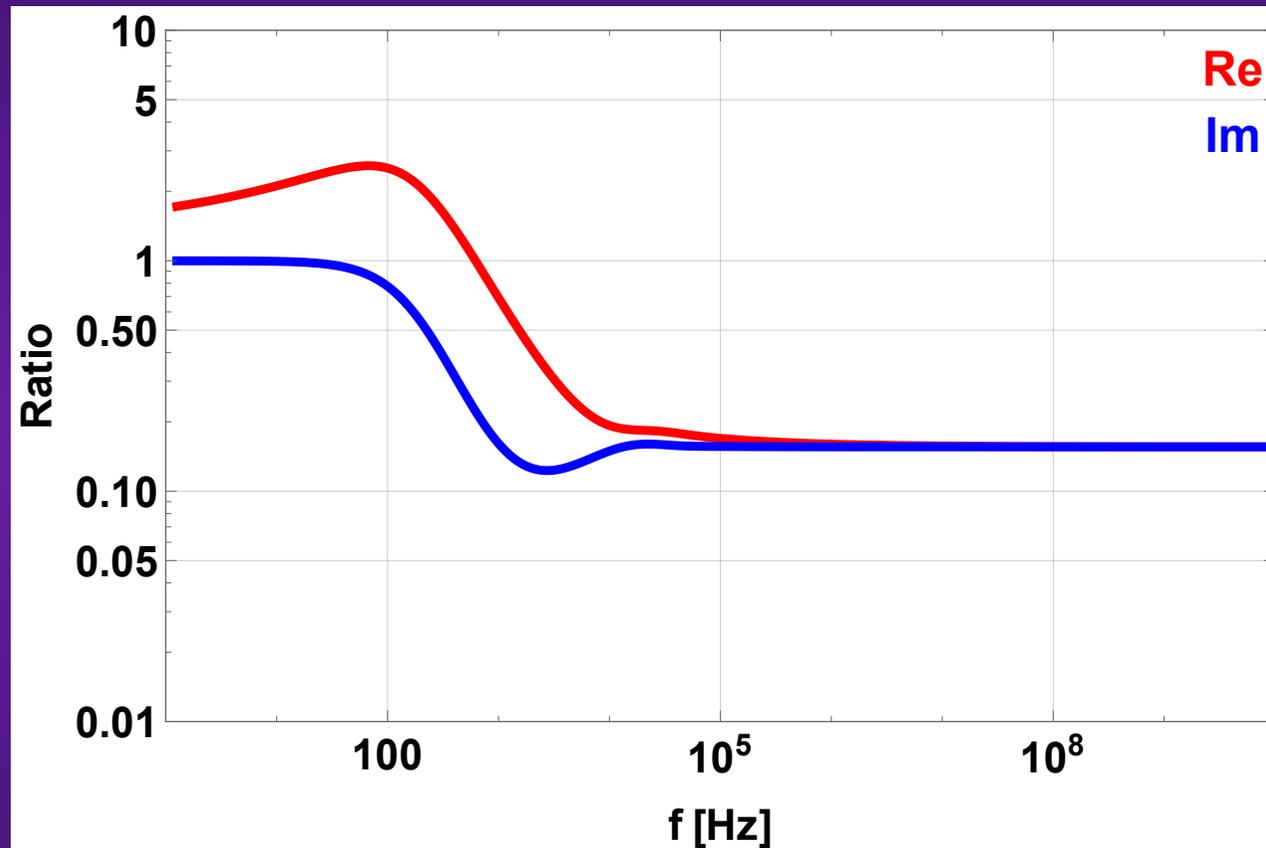
$$\text{Ratio} = \frac{Z_y(\text{ with coating })}{Z_y(\text{ without coating })}$$

SS beam pipe with 20 mm radius and 50 μm copper coating (room temp.)



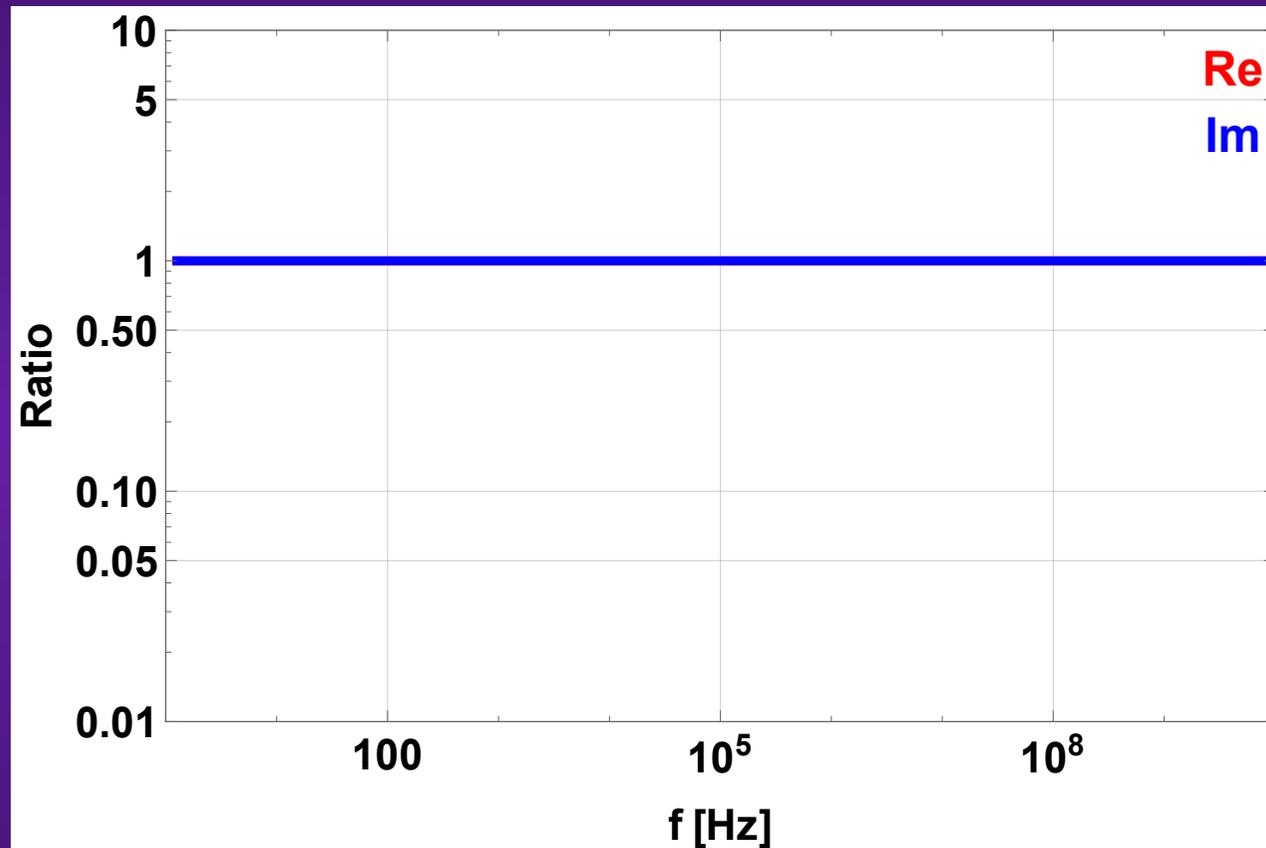
$$\text{Ratio} = \frac{Z_y(\text{ with coating })}{Z_y(\text{ without coating })}$$

SS beam pipe with 20 mm radius and **1000 μm = 1 mm** copper coating (room temp.)



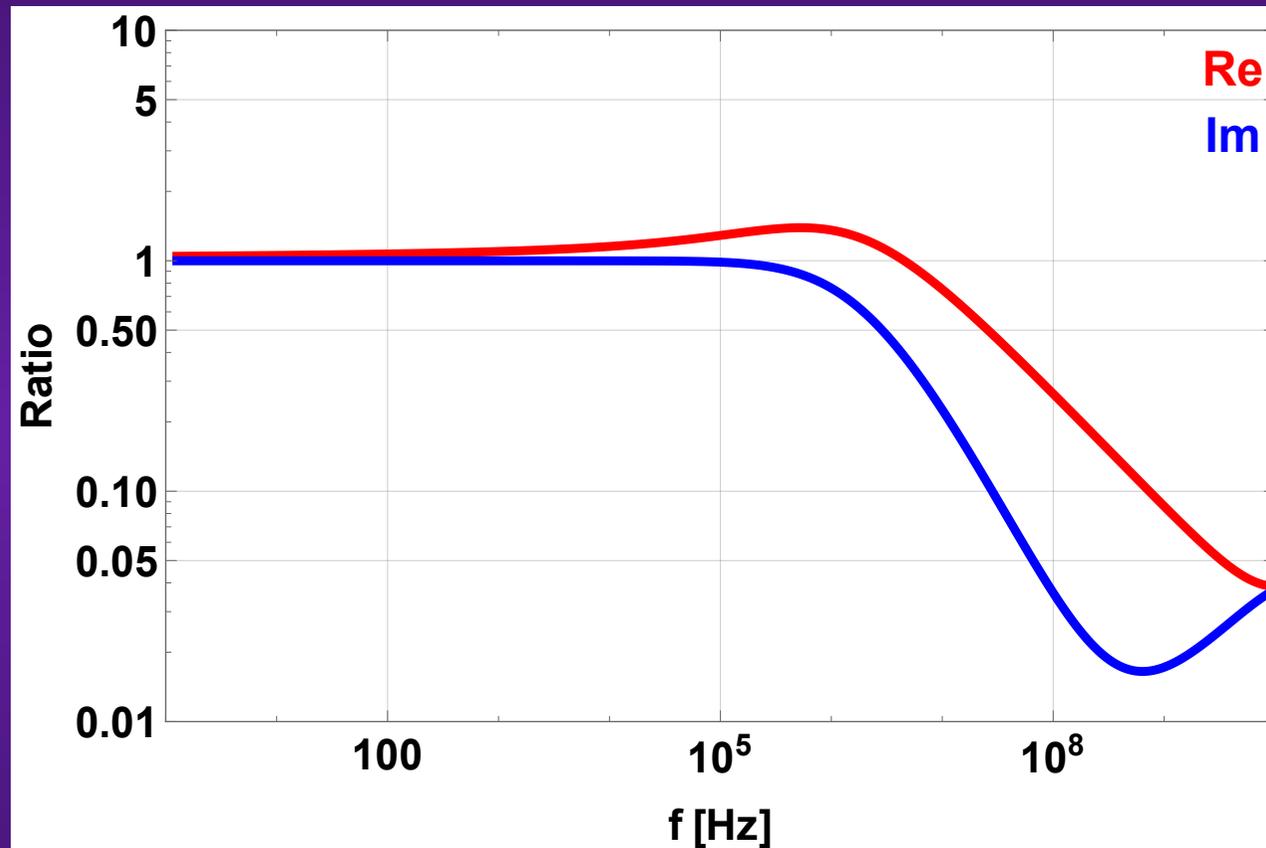
$$\text{Ratio} = \frac{Z_y(\text{ with coating })}{Z_y(\text{ without coating })}$$

Graphite beam pipe with 2 mm radius and 0 μm copper coating (room temp.)



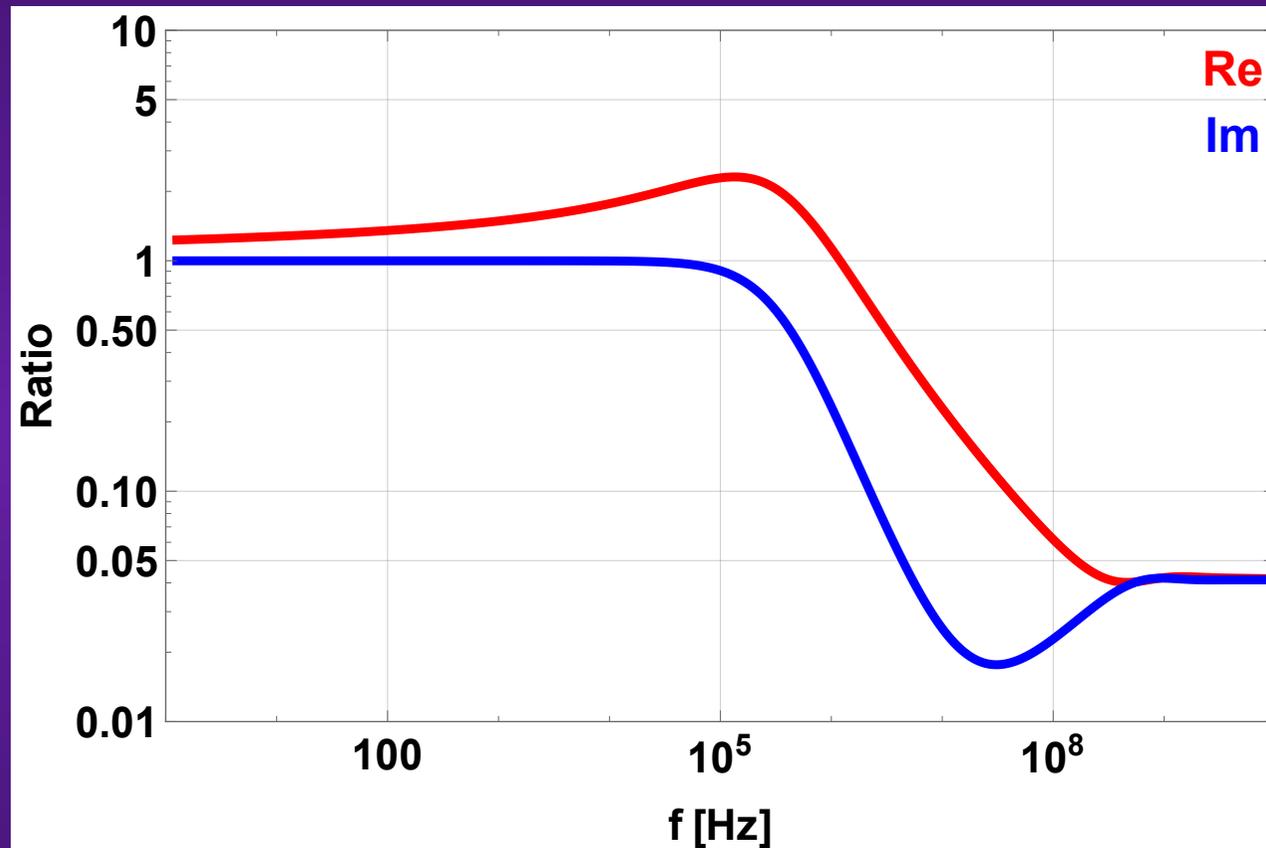
$$\text{Ratio} = \frac{Z_y(\text{ with coating })}{Z_y(\text{ without coating })}$$

Graphite beam pipe with 2 mm radius and 1 μm copper coating (room temp.)



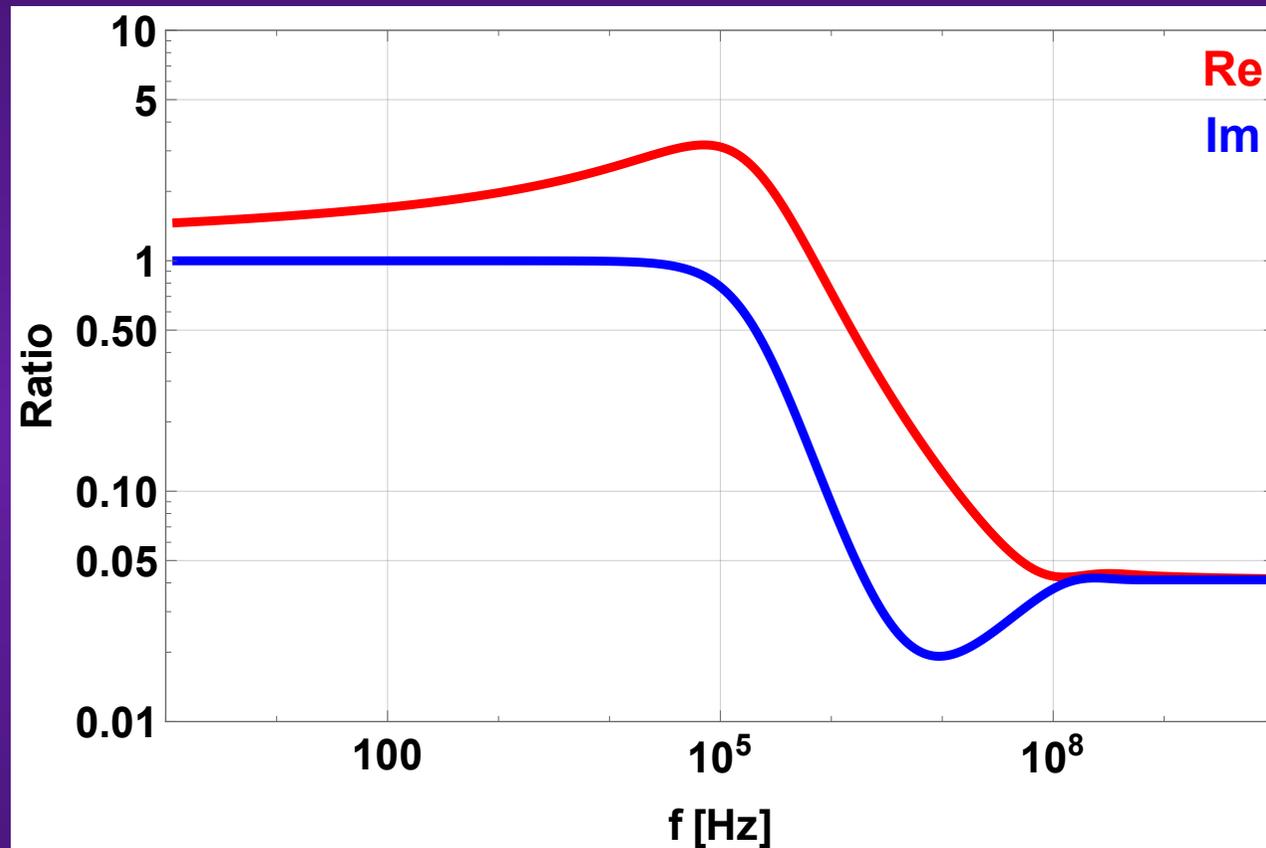
$$\text{Ratio} = \frac{Z_y(\text{ with coating })}{Z_y(\text{ without coating })}$$

Graphite beam pipe with 2 mm radius and 5 μm copper coating (room temp.)



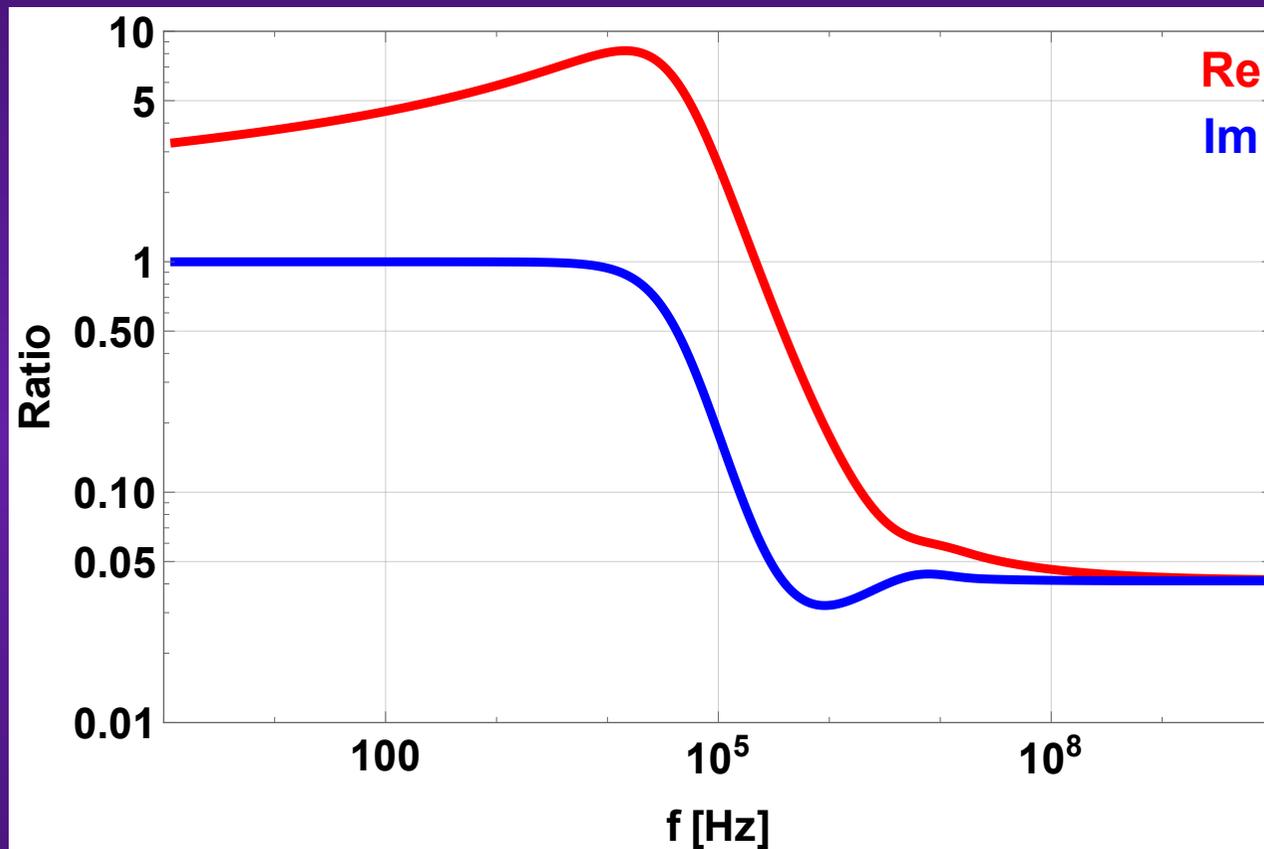
$$\text{Ratio} = \frac{Z_y (\text{ with coating })}{Z_y (\text{ without coating })}$$

Graphite beam pipe with 2 mm radius and 10 μm copper coating (room temp.)



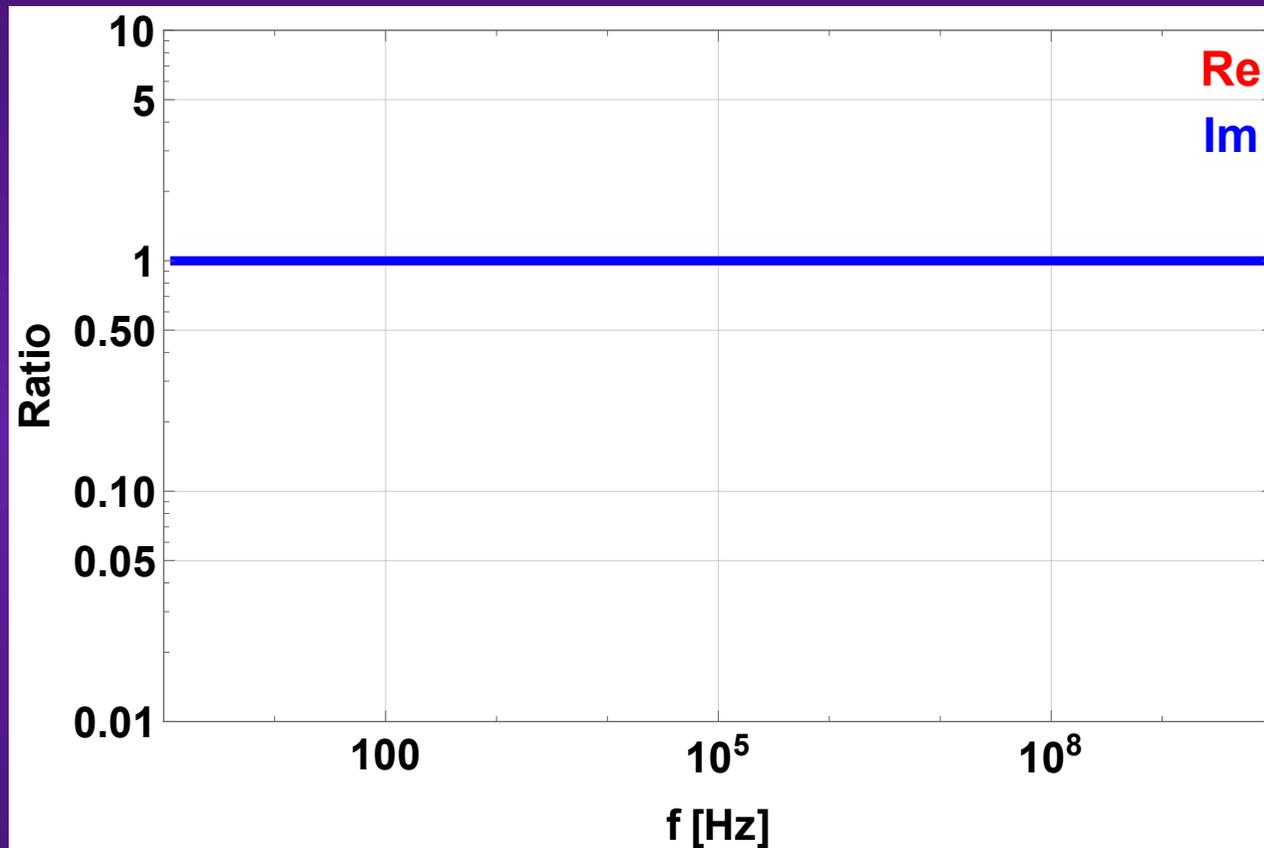
$$\text{Ratio} = \frac{Z_y(\text{ with coating })}{Z_y(\text{ without coating })}$$

Graphite beam pipe with 2 mm radius and 50 μm copper coating (room temp.)



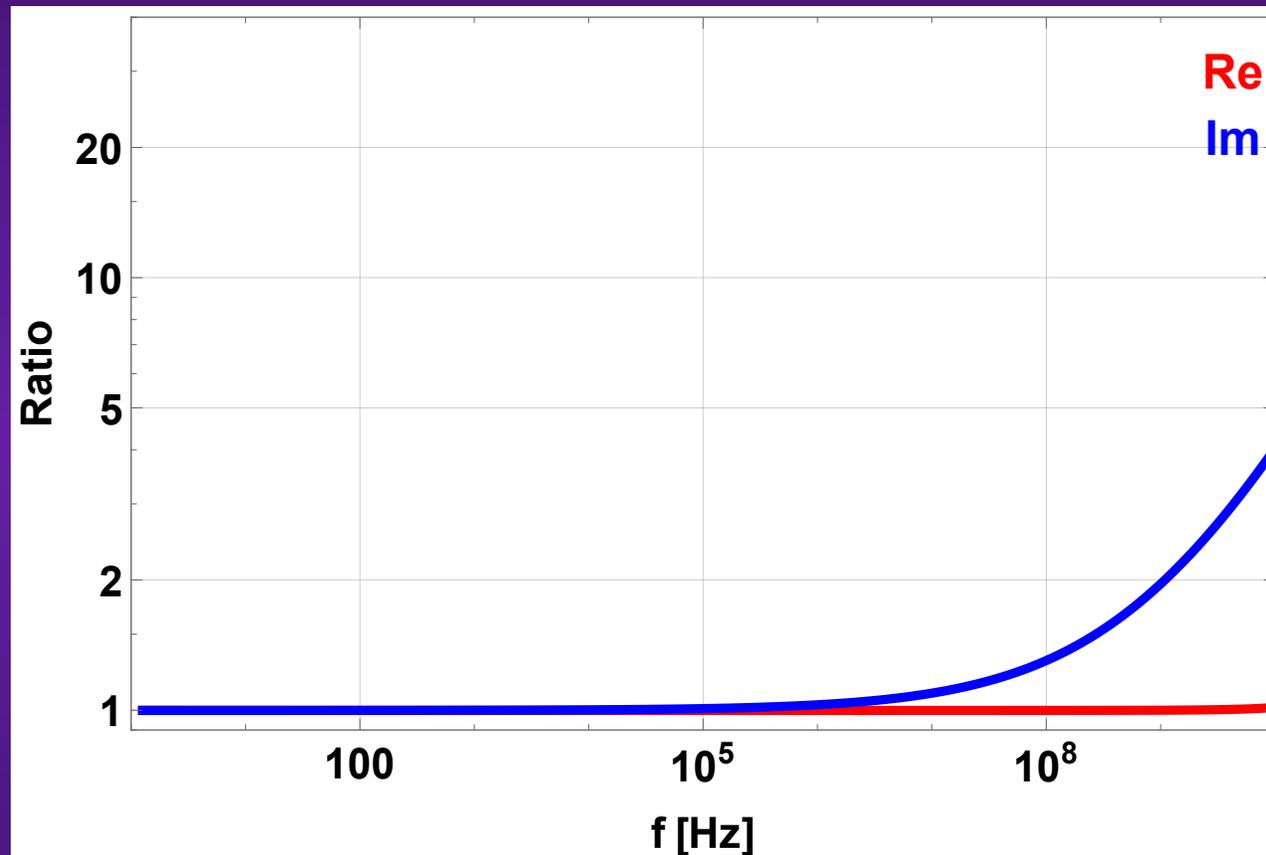
$$\text{Ratio} = \frac{Z_y(\text{ with coating })}{Z_y(\text{ without coating })}$$

Copper (room temp.) beam pipe with 20 mm radius and 0 μm graphite coating



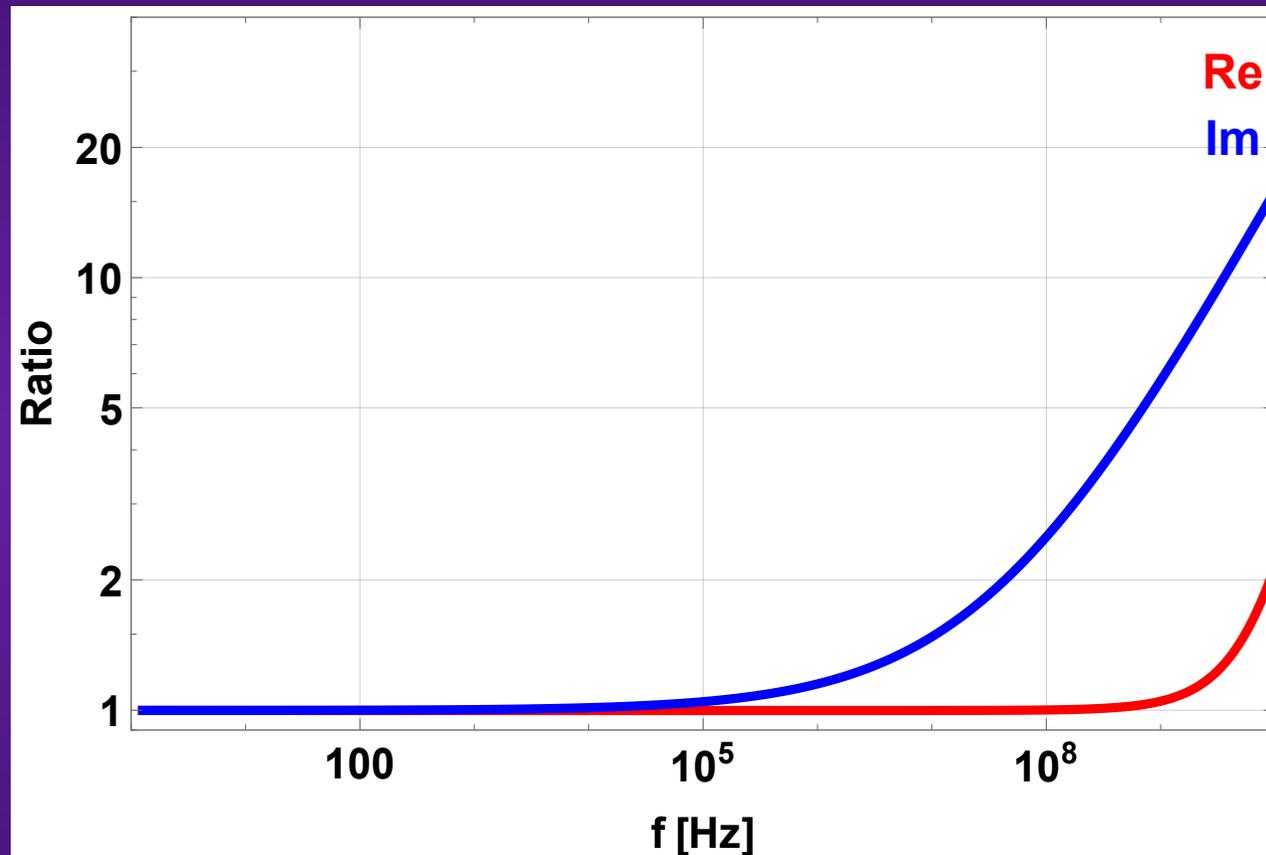
$$\text{Ratio} = \frac{Z_y(\text{ with coating })}{Z_y(\text{ without coating })}$$

Copper (room temp.) beam pipe with 20 mm radius and 1 μm graphite coating



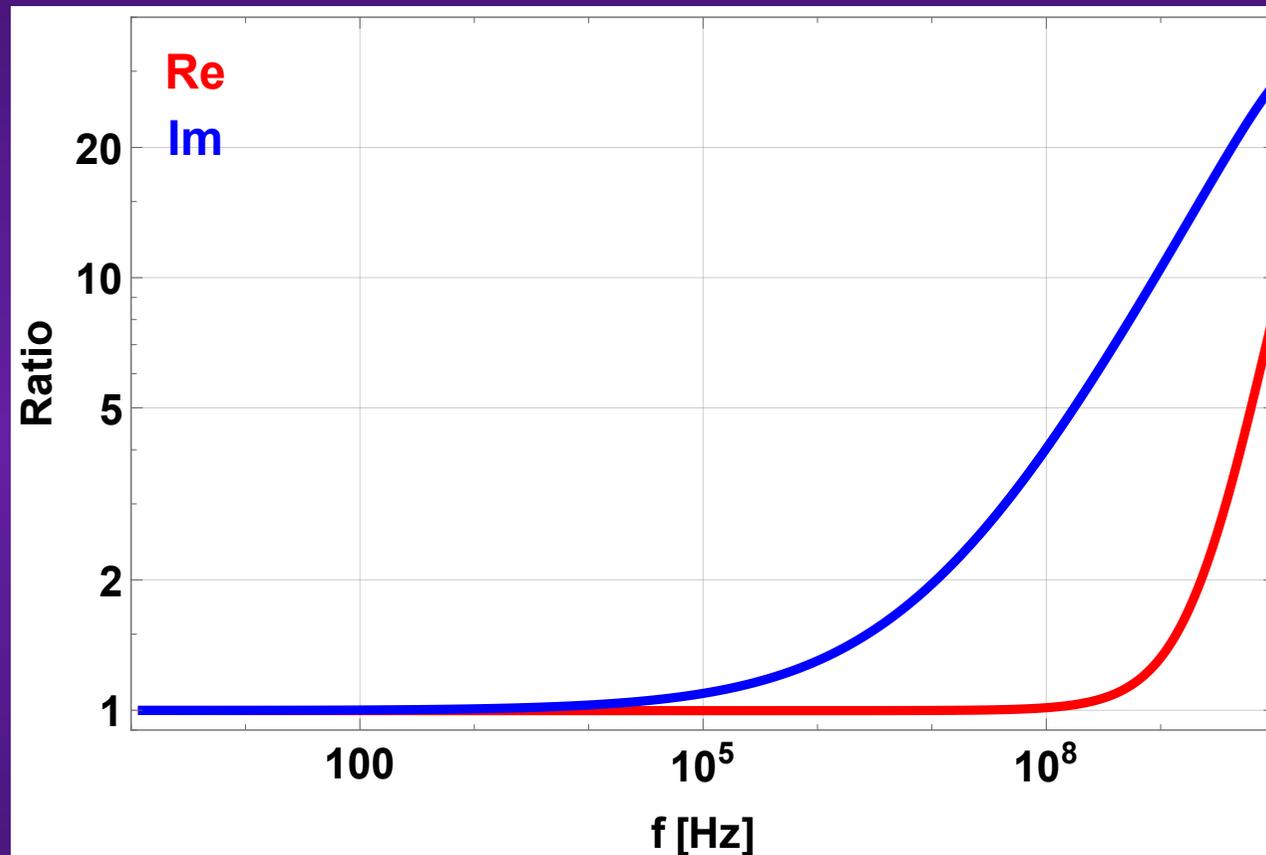
$$\text{Ratio} = \frac{Z_y(\text{ with coating })}{Z_y(\text{ without coating })}$$

Copper (room temp.) beam pipe with 20 mm radius and 5 μm graphite coating



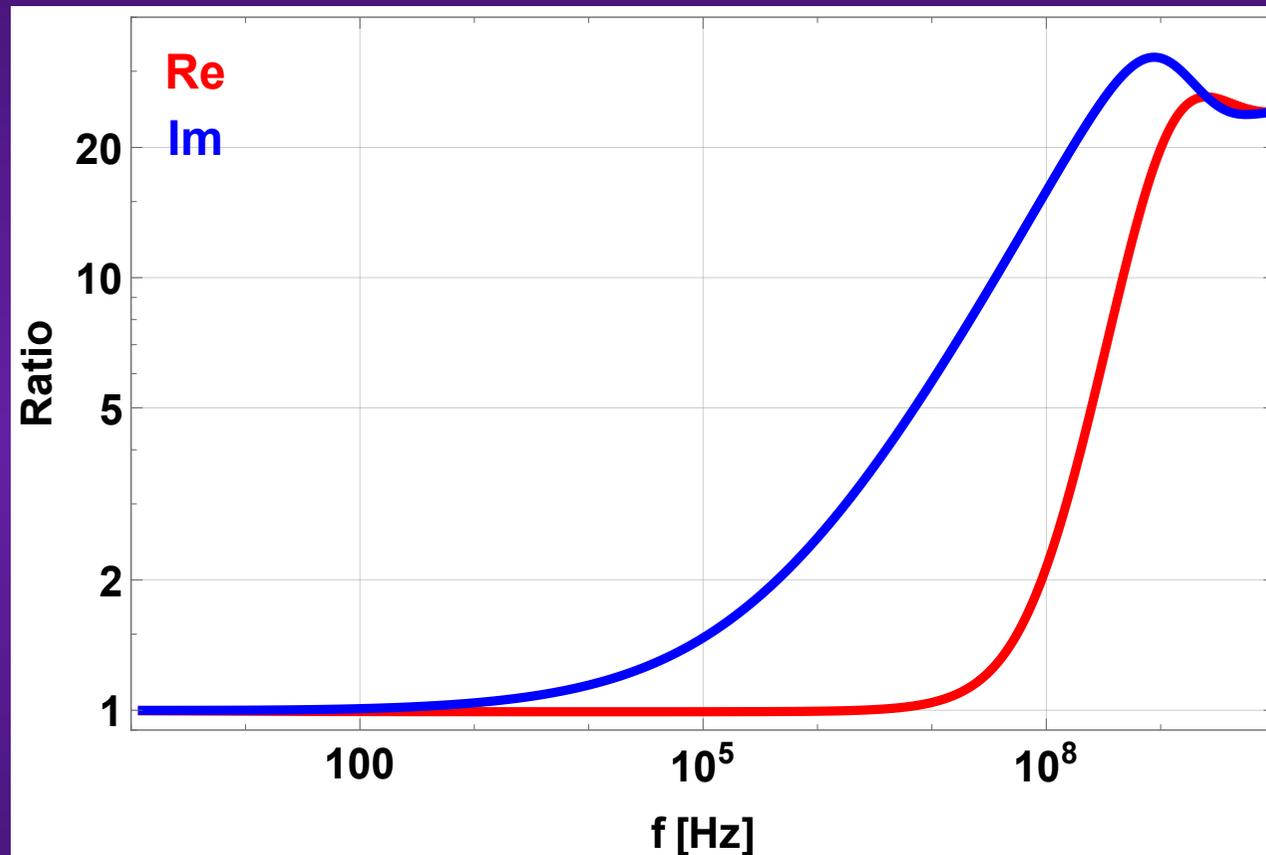
$$\text{Ratio} = \frac{Z_y (\text{ with coating })}{Z_y (\text{ without coating })}$$

Copper (room temp.) beam pipe with 20 mm radius and 10 μm graphite coating



$$\text{Ratio} = \frac{Z_y(\text{ with coating })}{Z_y(\text{ without coating })}$$

Copper (room temp.) beam pipe with 20 mm radius and 50 μm graphite coating



$$\text{Ratio} = \frac{Z_y(\text{ with coating })}{Z_y(\text{ without coating })}$$

CONCLUSION

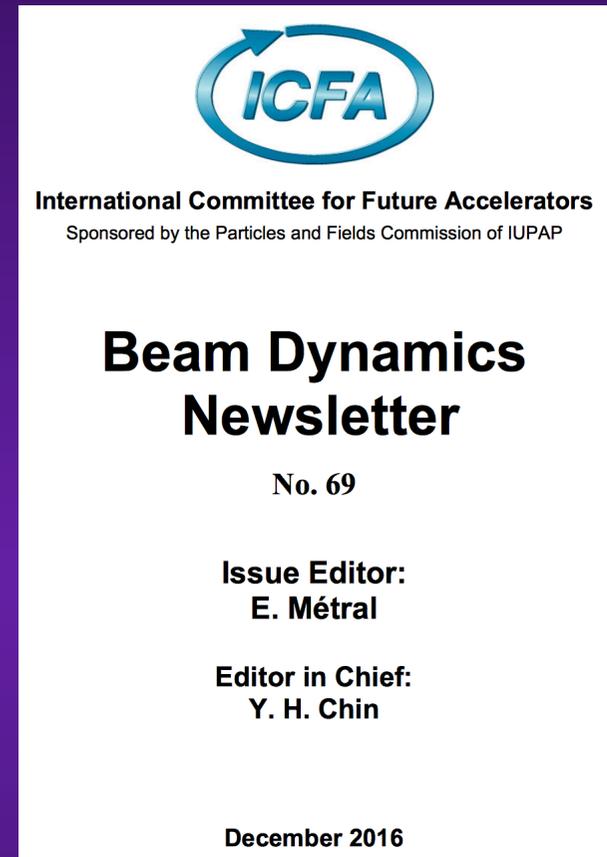
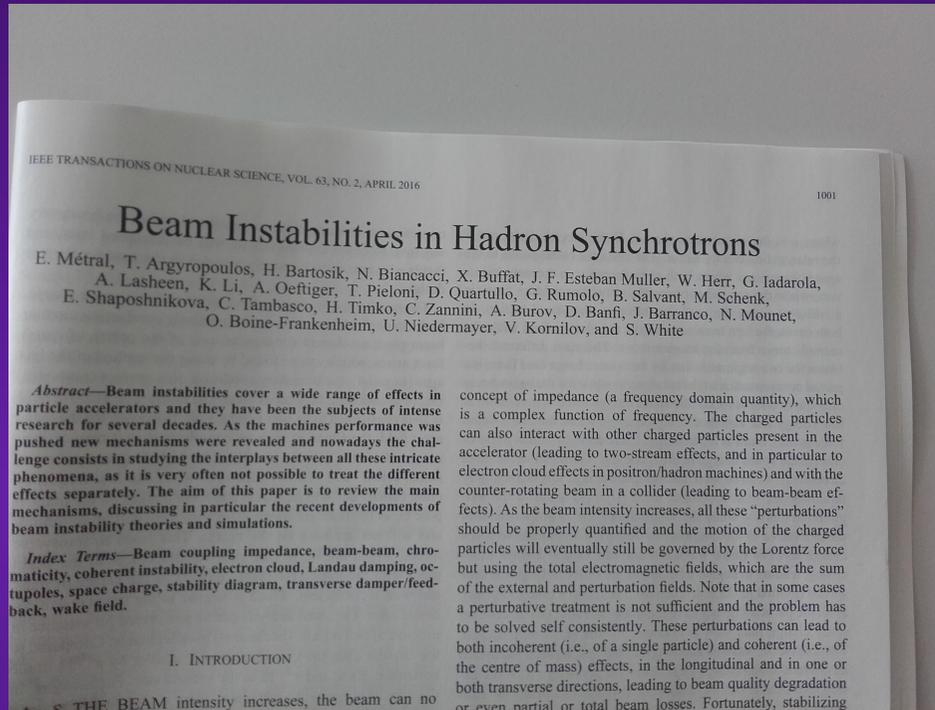
- ◆ 50 years of studies: happy birthday!
- ◆ Several extensions of impedance concept: space charge, e-cloud, CSR
- ◆ Still challenges for the future...(e.g. due to surface treatments to fight e-cloud)



The impedance is 50!



2 recent reviews with many references therein



Article for special edition of IEEE TNS for 50th anniversary of PAC conference, originally launched by IEEE in 1965 (50 pages)

Theme: Collective Effects in Particle Accelerators => 26 articles (310 pages)

- First one by F. Zimmermann on Introduction to Collective Effects
- Last one by F. Antoniou et al. on Mitigation of Collective Effects by Optics Optimization