

Muon collider: opzioni di macchina

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F. Bedeschi (Pi)

Gruppo 1, Catania, 2-3 dicembre 2015

Outline

- Muons case
- Muon accelerators challenges:
 - **muon production**
 - ✓ Conventional: from protons on target
 - ✓ Unconventional: from e^+e^- annihilation
 - emittance reduction via **cooling**
 - high-gradient acceleration
- Conclusions

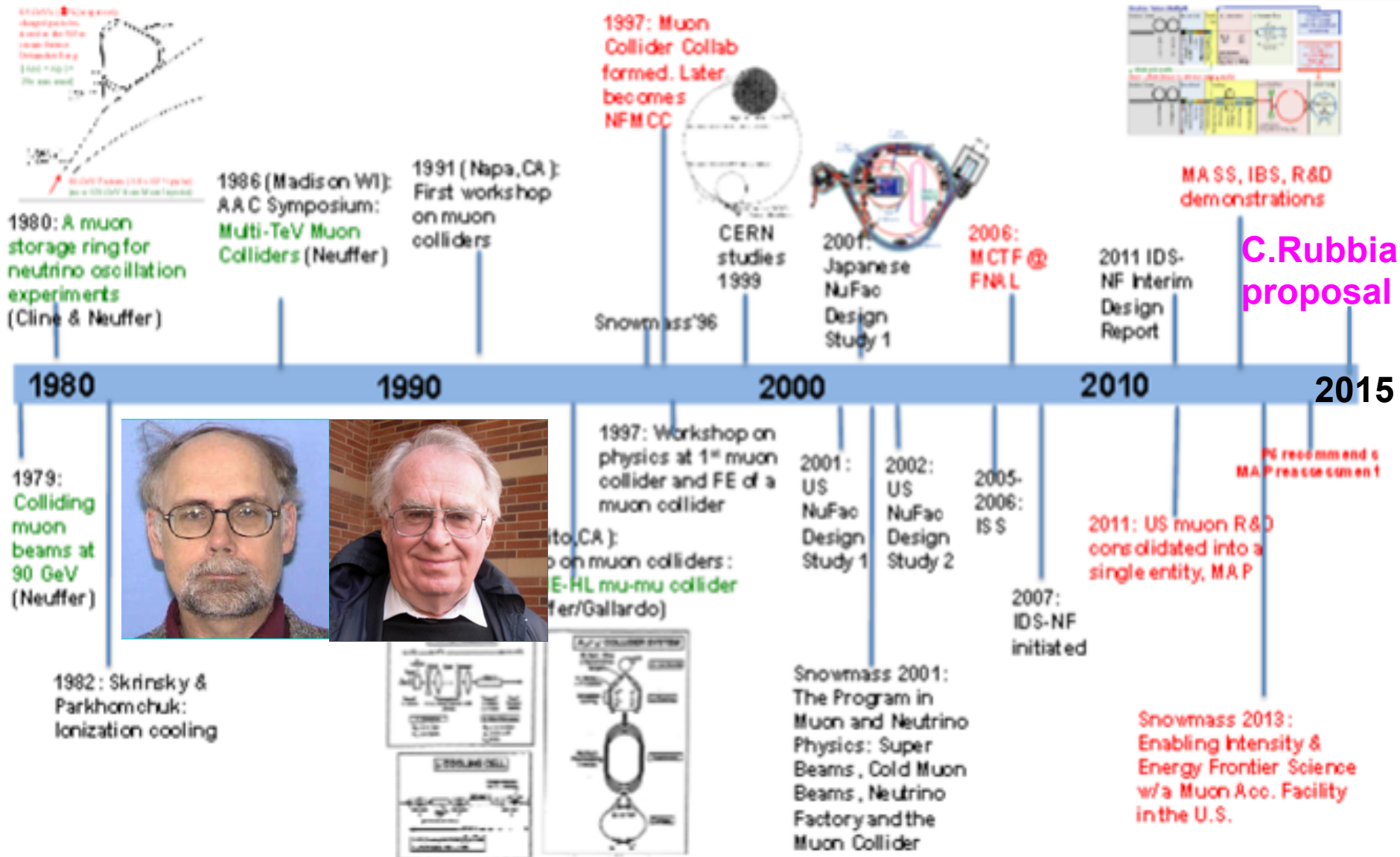
Ancora in fase di R&D o idee, ancora molto lontani rispetto al Linear Collider o Circular collider

I due approcci non sono confrontabili: per il primo c'è uno studio, per il secondo l'idea che, appunto, proponiamo di studiare.

Ref. : “Discussion of the scientific potential of muon beams”, CERN, Nov. 18th 2015
<https://indico.cern.ch/event/450863/>

Muons: a long history of development

Rob Ryne



Muon based colliders great potential



As with an e^+e^- collider, a $\mu^+\mu^-$ collider offers a precision probe of fundamental interactions without energy limitations

- By **synchrotron radiation** (limit of e^+e^- **circular** colliders)
- By **beam-strahlung** (limit of e^+e^- **linear** colliders)

Muon Collider is the ideal technology to extend lepton high energy frontier in the **multi-TeV** range with **reasonable dimension, cost and power consumption**

Muon based **Higgs factory** takes advantage of a strong coupling to Higgs mechanism by s resonance

**IF THE MUON BEAM NOVEL TECHNOLOGY
CAN BE DEMONSTRATED TO BE FEASIBLE**

Muons: Issues & Challenges

- **Limited lifetime: 2.2 μs (at rest)**

- Race against death: generation, acceleration & collision before decay

- Muons decay in accelerator and detector

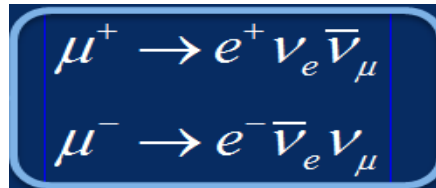
- Shielding of detector and facility irradiation
- Collider and Physics feasibility with large background environment?

Not by beamshtrahlung as with e^+/e^- but by muon decay (e, ν)

Reduced background at high energy due to increased muon lifetime

- Decays in neutrinos:

- Ideal source of well defined electron & muon neutrinos in equal quantities whereas Superbeams by pion decay only provide muon ν :



The neutrino factory
concept

- **Generated as tertiary particles in large emittances**

- powerful MW(s) proton driver and pion decay
- novel (fast) cooling and acceleration methods

$$\pi^+ \rightarrow \mu^+ + \nu_\mu$$

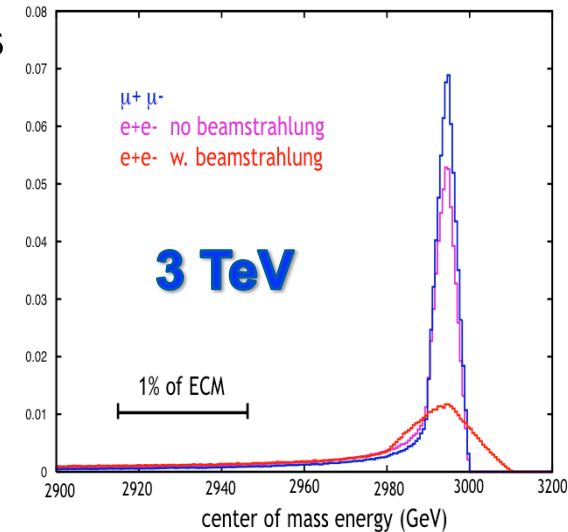
$$\pi^- \rightarrow \mu^- + \bar{\nu}_\mu$$

Development of novel technologies
with key accelerator and detector challenges

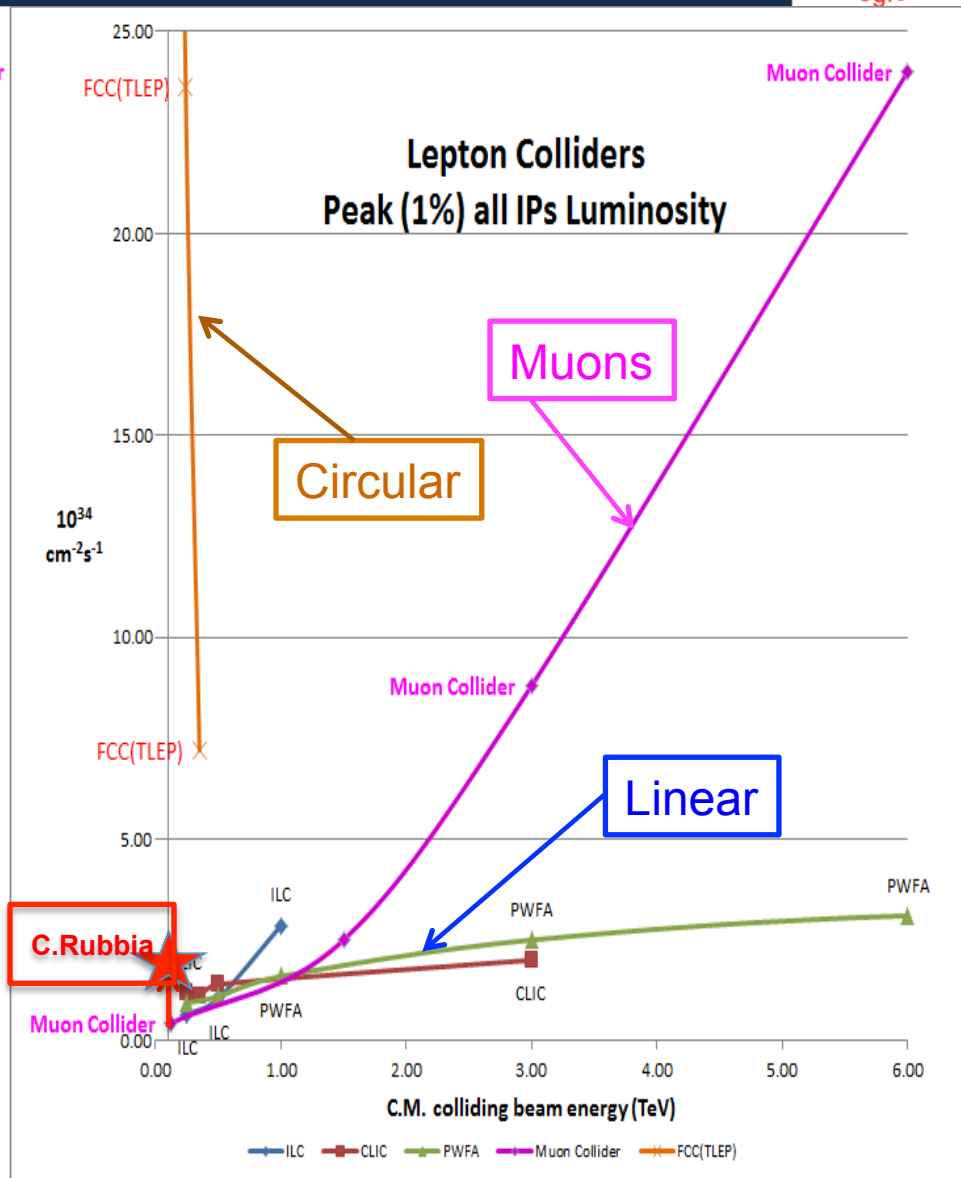
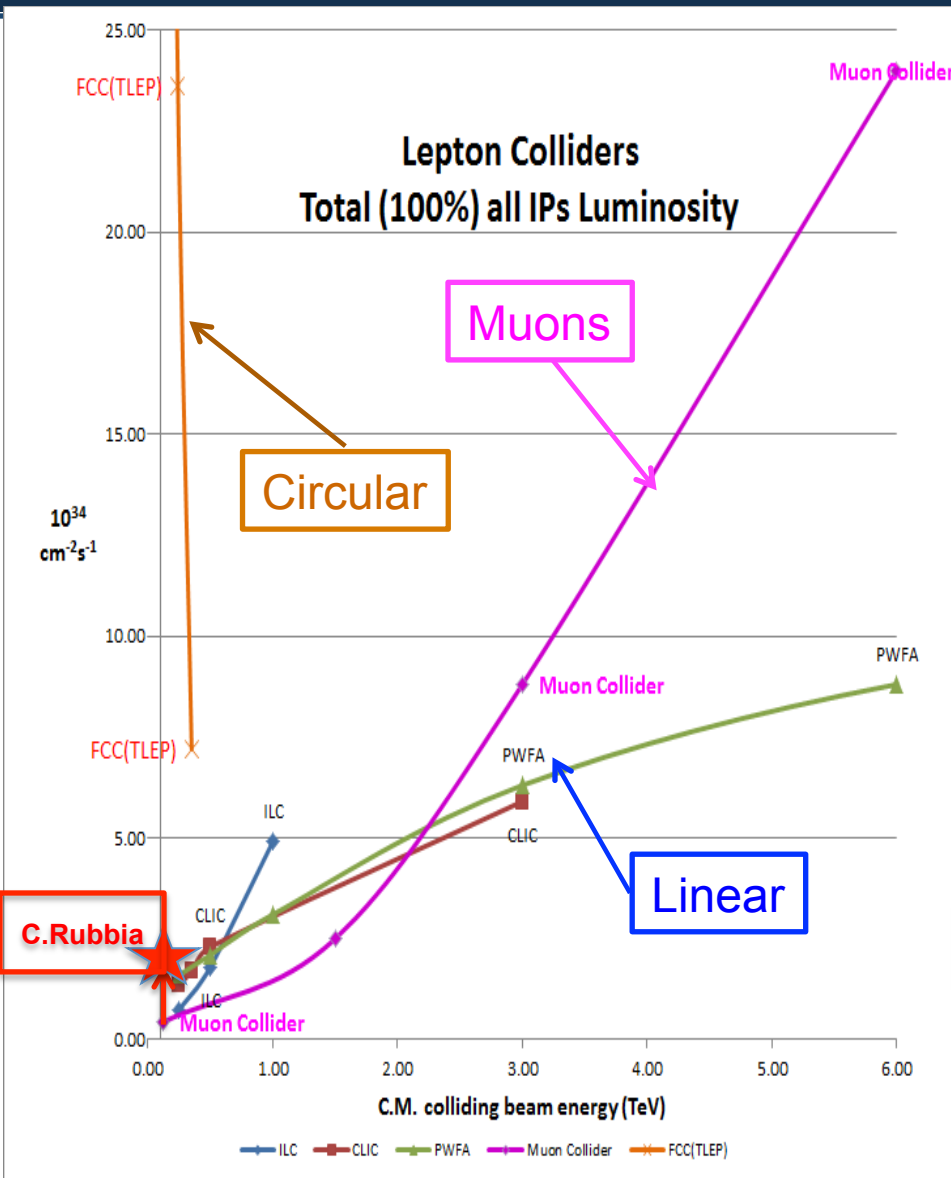
Muon beams specific properties

Muons are leptons like electrons & positrons but with a mass ($105.7 \text{ MeV}/c^2$) 207 times larger

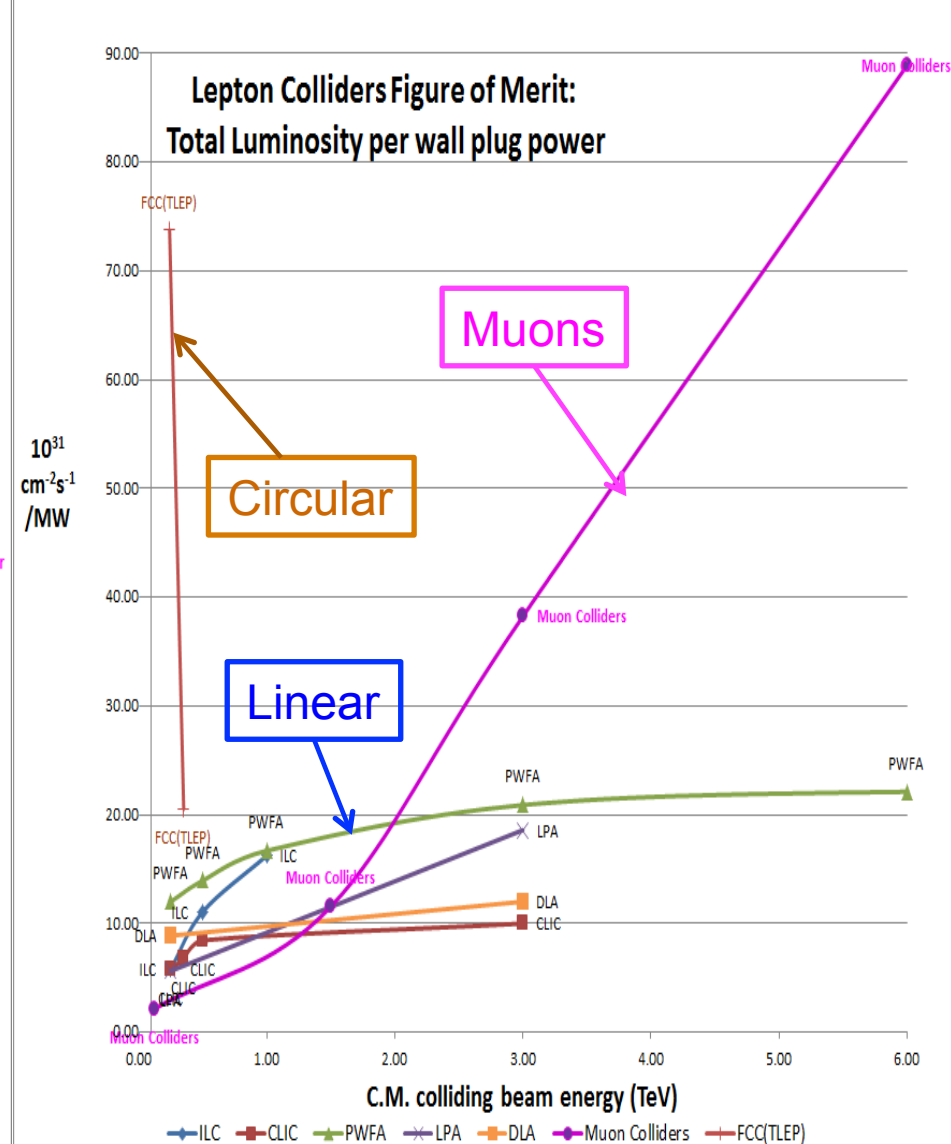
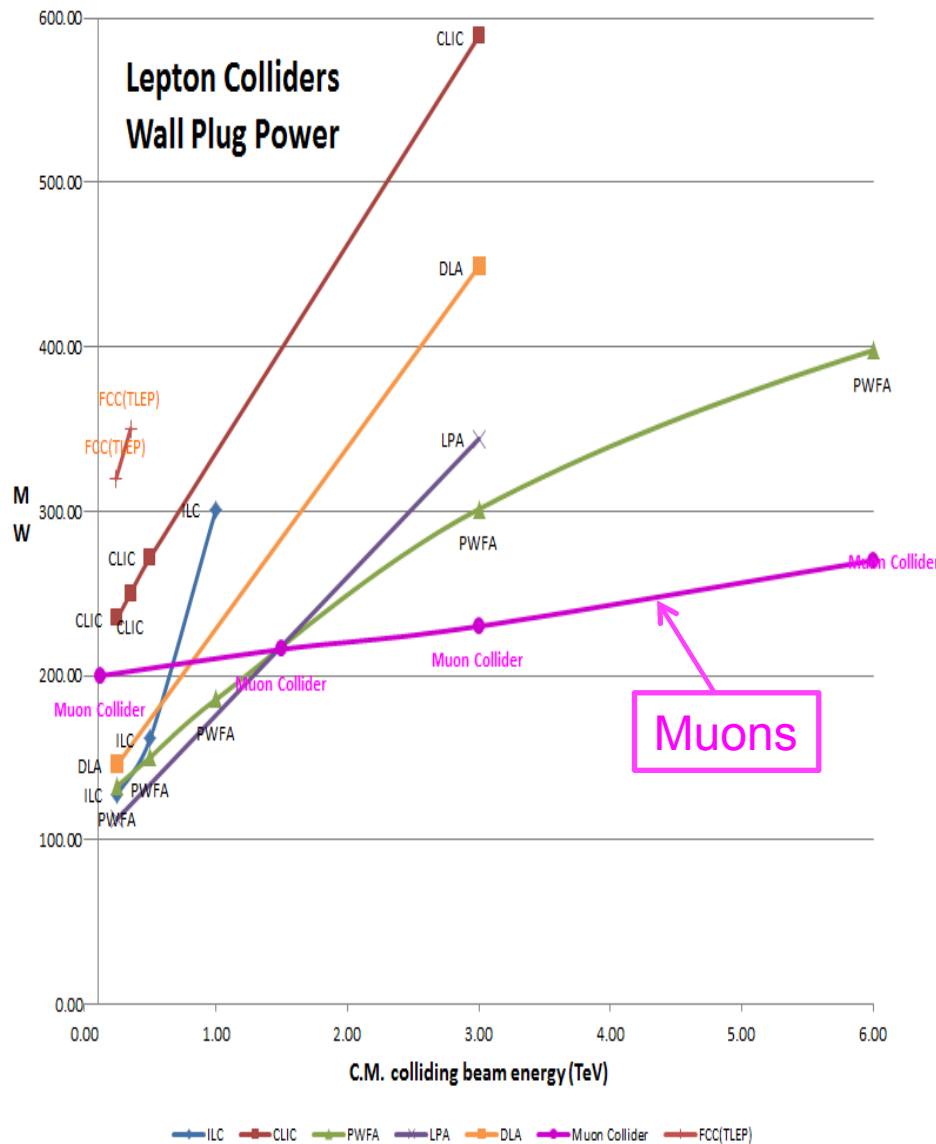
- **Negligible synchrotron radiation emission ($\propto m^{-2}$)**
 - **Multi-pass collisions (1000 turns) in collider ring**
 - High luminosity with reasonable beam power and wall plug power consumption
 - **relaxed beam emittances & sizes, alignment & stability**
 - Multi-detectors supporting broad physics communities
 - Large time ($15 \mu\text{s}$) between bunch crossings
 - **No beam-strahlung at collision:**
 - narrow luminosity spectrum
 - **Multi-pass acceleration in rings or RLA:**
 - Compact acceleration system and collider
 - Cost effective construction & operation
 - **No cooling by synchrotron radiation in standard damping rings**
 - Requires development of novel cooling method



Muon Colliders potential of extending leptons high energy frontier with high performance



Muon Colliders extending leptons high energy frontier with potential of considerable power savings



Muon Source

Goals

- **Neutrino Factories:** $O(10^{21})$ μ/yr within the acceptance of a μ ring
- **Muon Collider:** luminosities $>10^{34}/\text{cm}^{-2}\text{s}^{-1}$ at TeV-scale ($\sim N_{\mu}^2$)

Options

Conventional: Tertiary production through **proton on target** (and then cool), baseline for Fermilab design study

$$\text{Rate} > 10^{13} \mu/\text{sec} \quad N_{\mu} = 2 \times 10^{12} / \text{bunch}$$

Unconventional:

- **e^+e^- annihilation: positron beam on target** (very low emittance and no cooling needed), baseline for our proposal here

$$\text{Rate} \sim 10^{11} \mu/\text{sec} \quad N_{\mu} \sim 5 \times 10^7 / \text{bunch}$$

- **by Gammas: GeV-scale Compton γ s** not discussed here

$$\text{Rate} \sim 5 \times 10^{10} \mu/\text{sec} \quad N_{\mu} \sim 10^6 \quad (\text{Pulsed Linac}) \quad [\text{V. Yakimenko (SLAC)}]$$

$$\text{Rate} > 10^{13} \mu/\text{sec} \quad N_{\mu} \sim \text{few} \times 10^4 \quad (\text{High Current ERL})$$

see also: W. Barletta and A. M. Sessler NIM A 350 (1994) 36-44

Exploring the potential for a Low Emittance Muon Collider

with muon source from e^+ beam on target

References:

- M. Antonelli, M. Boscolo, R. Di Nardo, P. Raimondi, “*Novel proposal for a low emittance muon beam using positron beam on target*”, **NIM A 807 101-107 (2016)**
- P. Raimondi, “*Exploring the potential for a Low Emittance Muon Collider*”, in **Discussion of the scientific potential of muon beams workshop**, CERN, Nov. 18th 2015
- M. Antonelli, **Presentation Snowmass 2013**, Minneapolis (USA) July 2013, [M. Antonelli and P. Raimondi, Snowmass Report (2013) also INFN-13-22/LNF Note

This idea has been investigated with a simulation study by SLAC team:

L. Keller, J. P. Delahaye, T. Markiewicz, U. Wienands:

- “*Luminosity Estimate in a Multi-TeV Muon Collider using $e^+e^- \rightarrow \mu^+\mu^-$ as the Muon Source*”, MAP 2014 Spring workshop, Fermilab (USA) May '14
- Advanced Accelerator Concepts Workshop, San Jose (USA), July '14

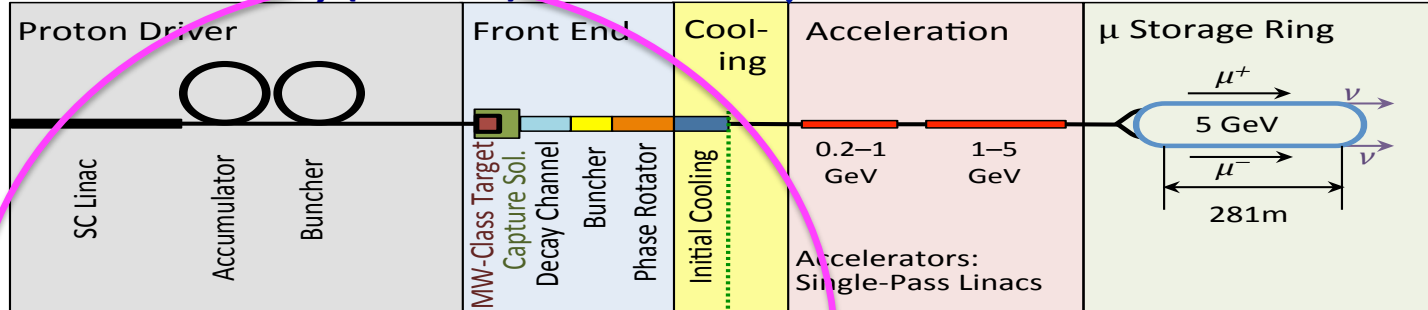
Proton-Based Source

Muon Accelerator Program (MAP)

Muon based facilities and synergies

Mark
Palmer

Neutrino Factory (NuMAX)

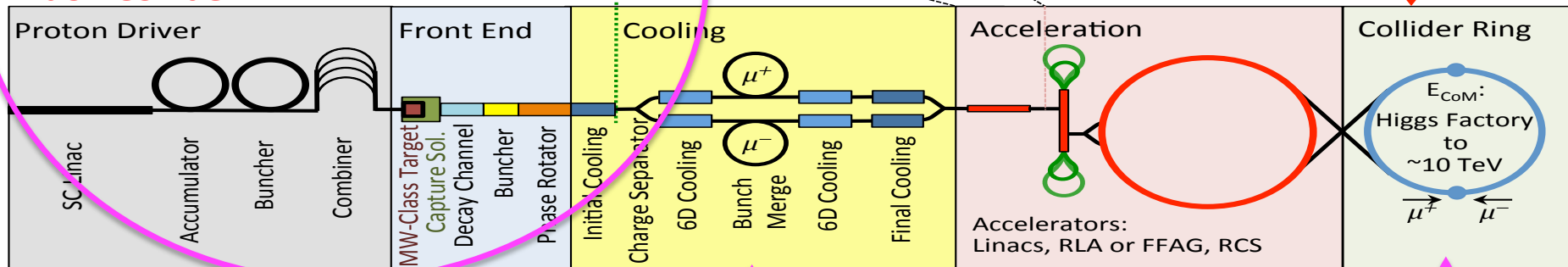


ν Factory Goal:
 10^{21} μ^+ & μ^- per year
within the accelerator
acceptance

μ -Collider Goals:
126 GeV \Rightarrow
 $\sim 14,000$ Higgs/yr
Multi-TeV \Rightarrow
Lumi $> 10^{34} \text{cm}^{-2}\text{s}^{-1}$

Share same complex

Muon Collider



Key
Challenges

$\sim 10^{13}-10^{14}$ μ / sec
Tertiary particle
 $p \rightarrow \pi \rightarrow \mu$:

Fast cooling
($\tau=2\mu\text{s}$)
by 10^6 (6D)

Fast acceleration
mitigating μ decay

Background
by μ decay

Key R&D

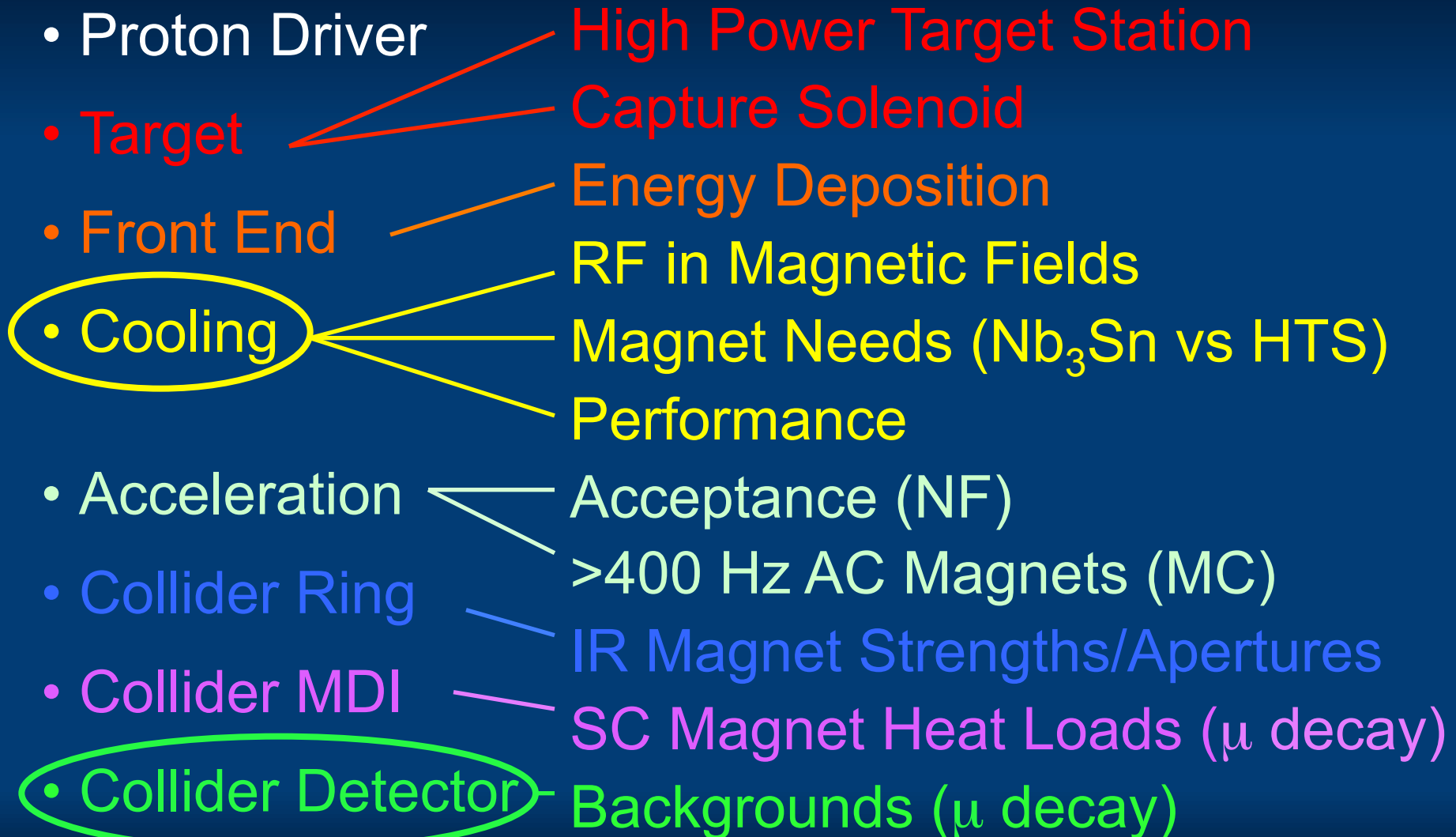
MW proton driver
MW class target
NCRF in magnetic field

Ionization cooling
High field solenoids (30T)
High Temp Superconductor

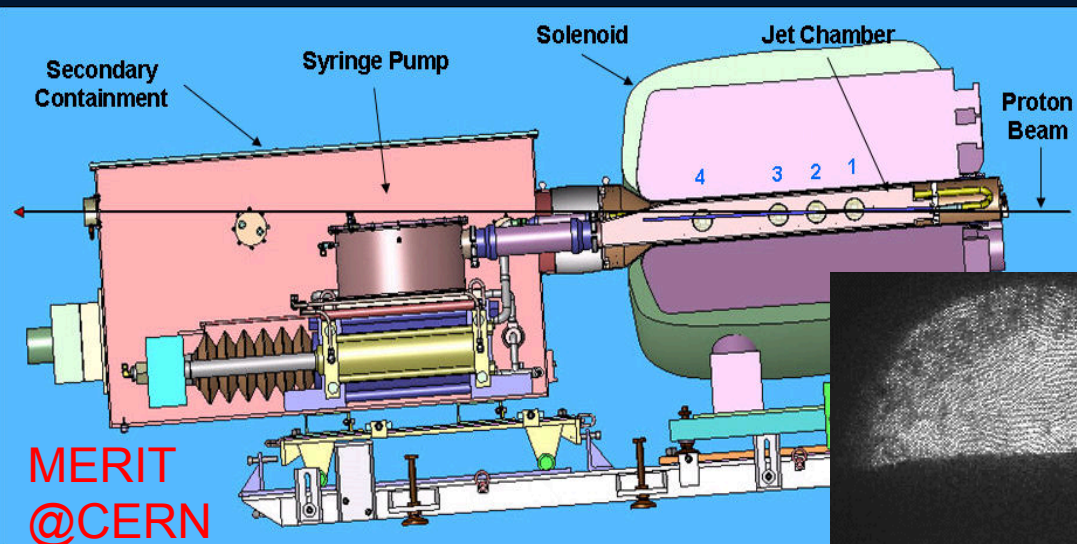
Cost eff. low RF SC
Fast pulsed magnet
(1kHz)

Detector/
machine
interface

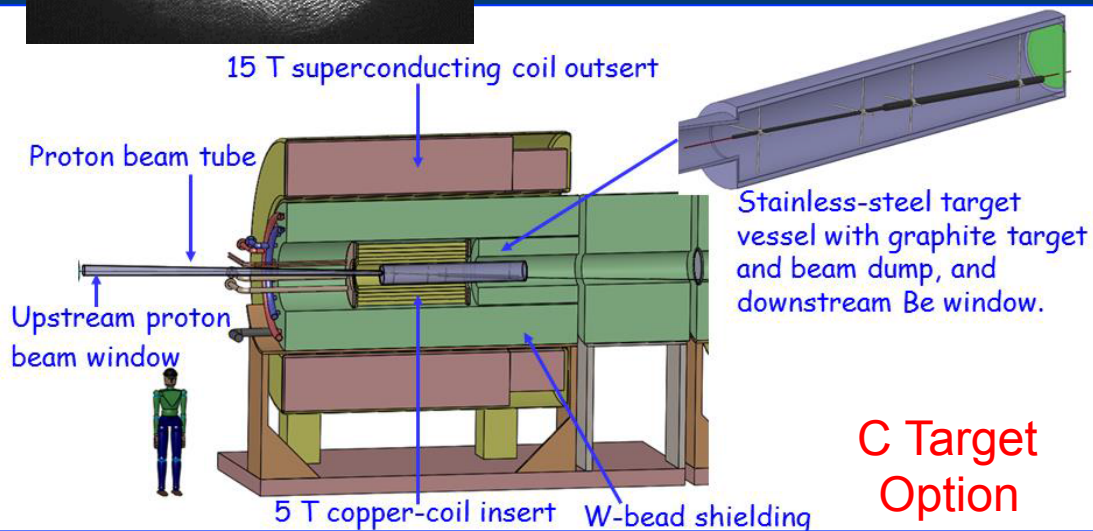
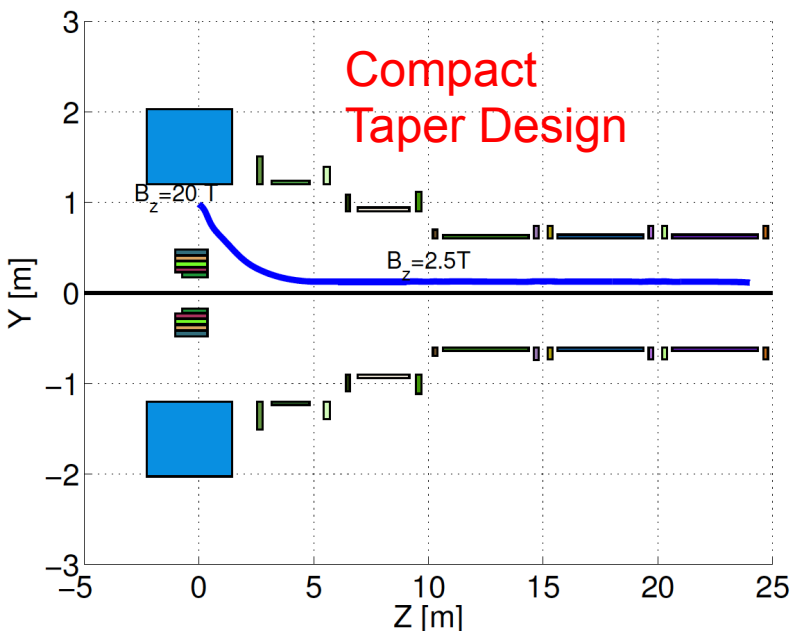
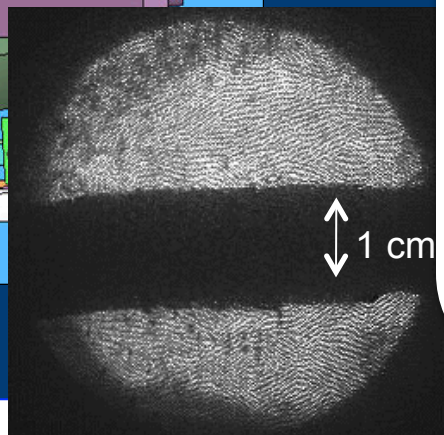
Key Feasibility Issues



High Power Target



- ✓ MERIT Expt:
 - LHg Jet in 15T
 - Capability: 8MW @70Hz
- ✓ MAP Staging aims at 1-2 MW \Rightarrow C Target
- ✓ Improved Compact Taper Design
 - Performance & Cost

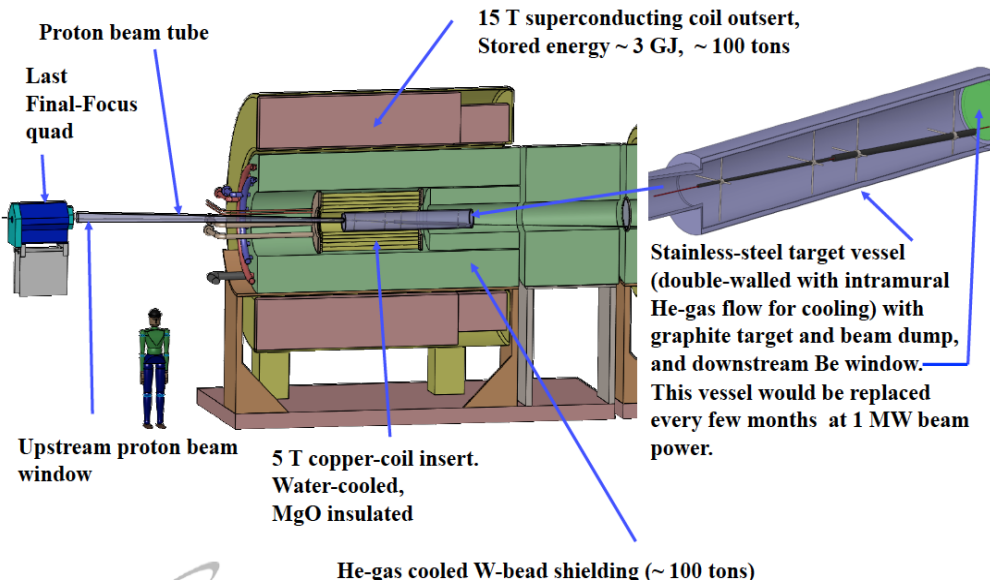


C Target Option

MAP muon generation by Proton driver

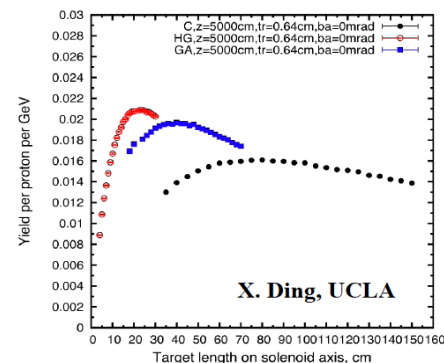
H.Kirk
(BNL)

A Graphite Target Core



- MW-Class proton driver at ~5-10 GeV
- Capture solenoid system (μ^+ & μ^-)
 - 15 T outsert, 5 T insert
 - ~3GJ stored energy

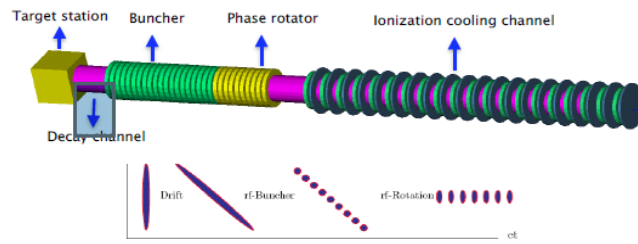
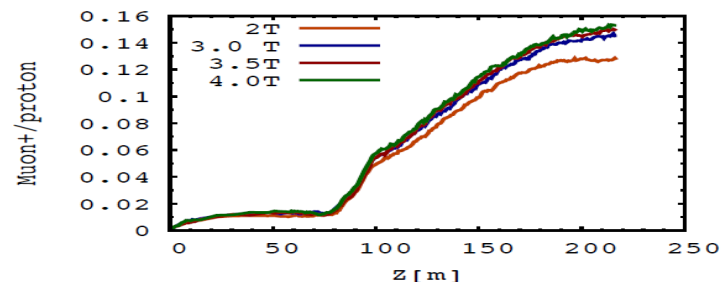
Choice of Target Materials II



- **High Z (e.g. Hg)**
- **Mid Z (e.g. Ga)**
- **Low Z (e.g. Carbon)**

A 25% advantage of using
high-Z Hg compared to
low-Z Carbon
Low-z Carbon is attractive
due to it's simplicity and
robustness

Proton Beam: KE = 6.75 GeV
Normalization: For Hg $\Sigma(\mu^+ + \mu^-)/\text{proton} \approx 1$



H.K.Sayed
(BNL)

Muon per proton production at Front End exit

Ionization Cooling

- No damping from SR -> Ionization 'dE/dx' cooling:
 - Helical 6D Cooling
 - PIC
 - ...



Ionization Cooling Experimental R&D Program

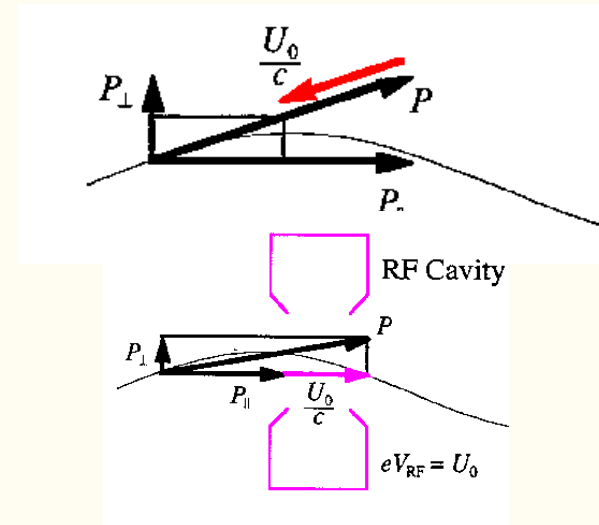
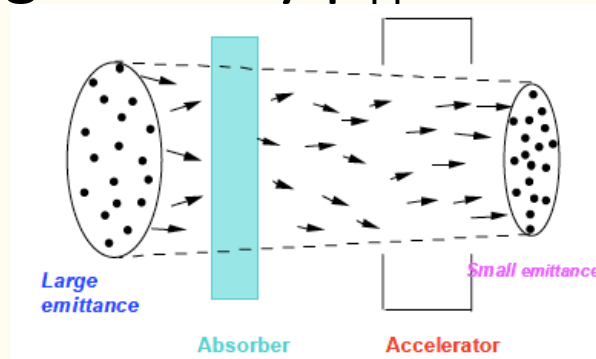
- **MICE** –International Muon Ionization Cooling Experiment
 - μ -beam at RAL ISIS
 - Systems test of complete cooling system
- **MuCOOL** Program
 - Rf, absorber, magnet R&D-supports MICE
 - MuCOOL test area (Fermilab)
 - Muon Collider Task Force
- **MUONS, Inc.** (R. Johnson, et al.)
 - High-pressure rf cavities
 - Helical cooler, Parametric resonance cooler

Ionization Cooling-general principle

This method, called “**dE/dx cooling**” closely resembles to the synchrotron compression of relativistic electrons - with the multiple energy losses in a thin, low Z absorber substituting the synchrotron radiated light.

Transverse Cooling:

- Particle loses momentum in material
- Particle gains only $p_{||}$ in RF



On the other hand,
Multiple scattering in material increases rms emittance



Combining Cooling and Heating:

$$\frac{d\varepsilon_N}{ds} = -\frac{1}{\beta^2 E} \frac{dE}{ds} \varepsilon_N + \frac{\beta_\gamma \beta_\perp}{2} \frac{d\langle \theta_{rms}^2 \rangle}{ds}$$

- **Low-Z** absorbers (H_2 , Li, Be, ...) to reduce multiple scattering
- **High Gradient RF**

- To cool before μ -decay ($2.2\gamma \mu s$)

- To keep beam bunched

- **Strong-Focusing** at absorbers \rightarrow **small beam size and large divergence then damped by absorber + RF**

- To keep multiple scattering

- less than beam divergence ...

\Rightarrow **Quad** focusing ?

\Rightarrow **Li lens** focusing ?

\Rightarrow **Solenoid** focusing?

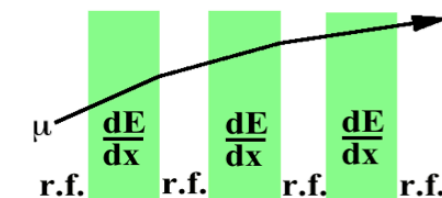
$$\frac{d\langle \theta_{rms}^2 \rangle}{ds} = \frac{z^2 E_s^2}{\beta^2 c^2 p_\mu^2 L_R}$$

Cooling Methods

- The particular challenge of muon cooling is its short lifetime
 - Cooling must take place very quickly
 - More quickly than any of the cooling methods presently in use
- ⇒ Utilize energy loss in materials with RF re-acceleration

Muon Ionization Cooling

• Muons cool via dE/dx in low- Z medium



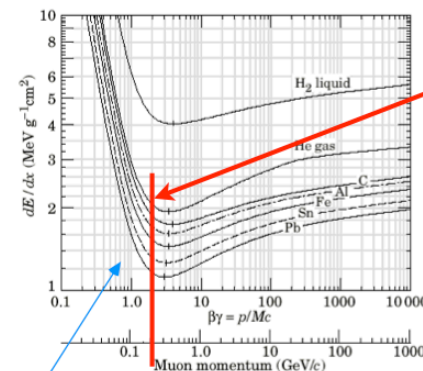
– Absorbers:

$$\begin{cases} E \rightarrow E - \left\langle \frac{dE}{dx} \right\rangle \Delta s \\ \theta \rightarrow \theta + \theta_{space}^{rms} \end{cases}$$

– RF cavities between absorbers replace ΔE

– Net effect: reduction in p_{\perp} at constant p_{\parallel} , i.e., transverse cooling

$$\frac{d\epsilon_N}{ds} \approx -\frac{1}{\beta^2} \left\langle \frac{dE_{\mu}}{ds} \right\rangle \frac{\epsilon_N}{E_{\mu}} + \frac{\beta_{\perp} (0.014 \text{ GeV})^2}{2\beta^3 E_{\mu} m_{\mu} X_0} \quad (\text{emittance change per unit length})$$



- ionization minimum is \approx optimal working point:

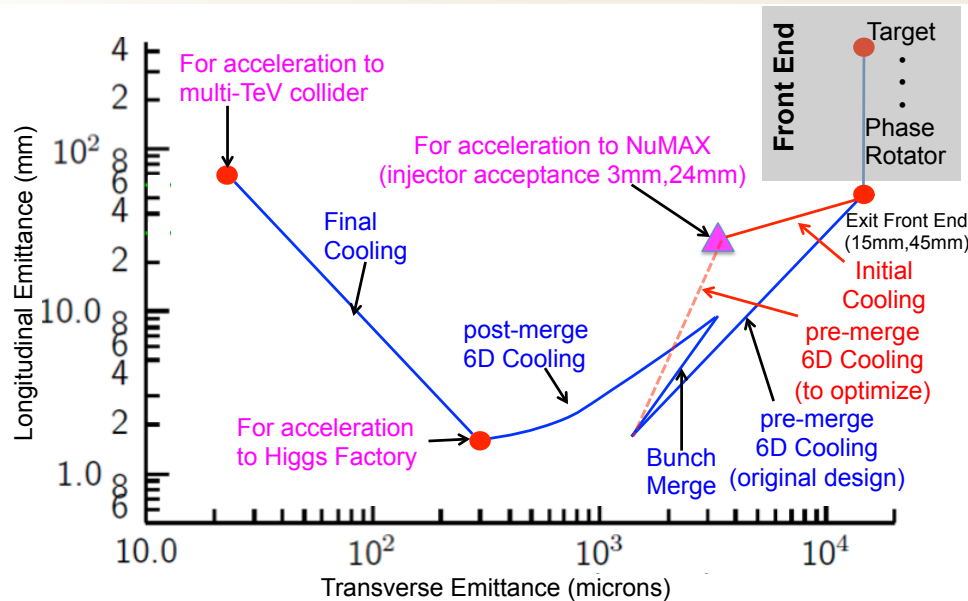
- ▶ longitudinal +ive feedback at lower p
- ▶ straggling & expense of reacceleration at higher p

- 2 competing effects \Rightarrow \exists equilibrium emittance

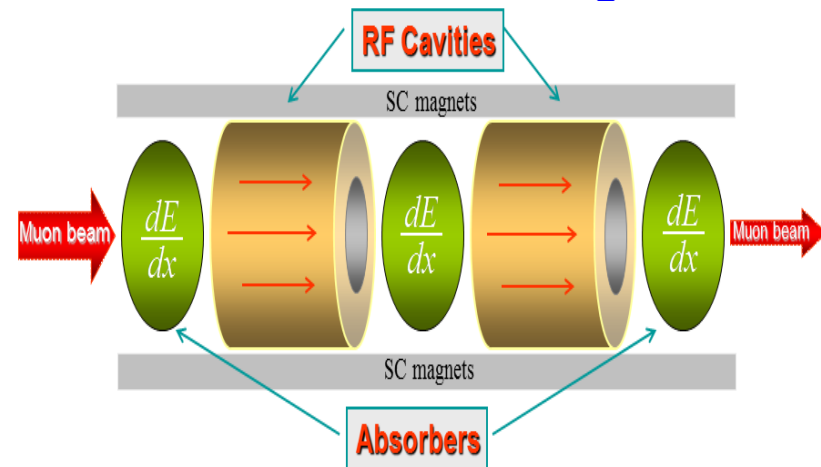
Kaplan

MAP Cooling scheme overview

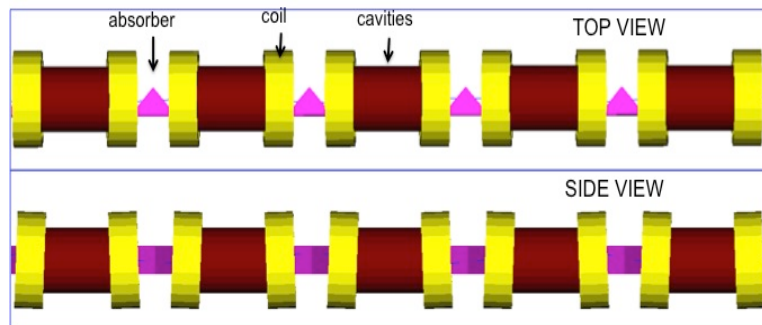
P.Snopok
(IIT)



Ionization cooling



Vacuum Cooling Channel (VCC)

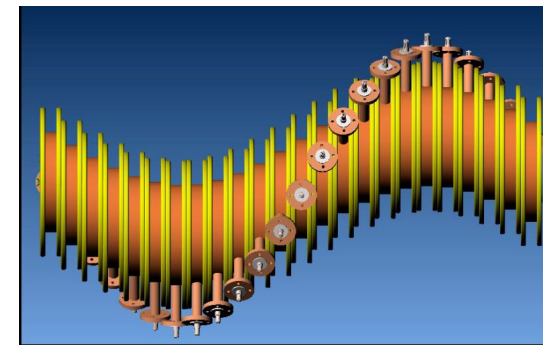


Two
methods

Major
challenges

Accelerating field limitation
by magnetic field (10 T)

Helical Cooling Channel (HCC)

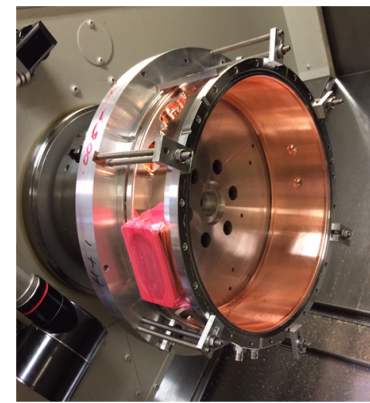
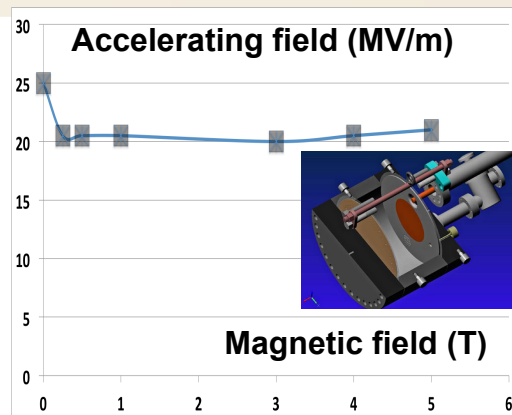
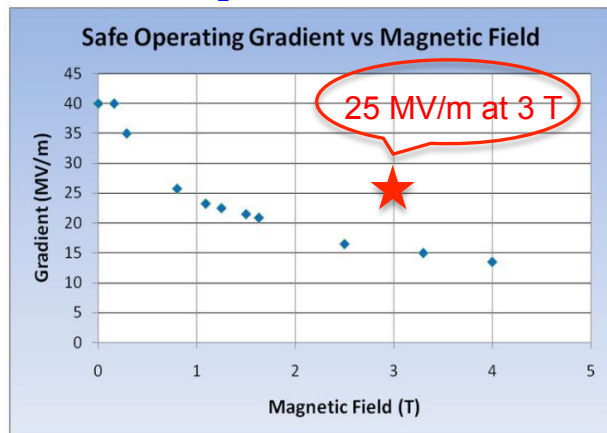


High pressure (160atm)
Gas (GH₂) filled RF cavities

RF cavities in strong magnetic field

D.Li
(LBNL)

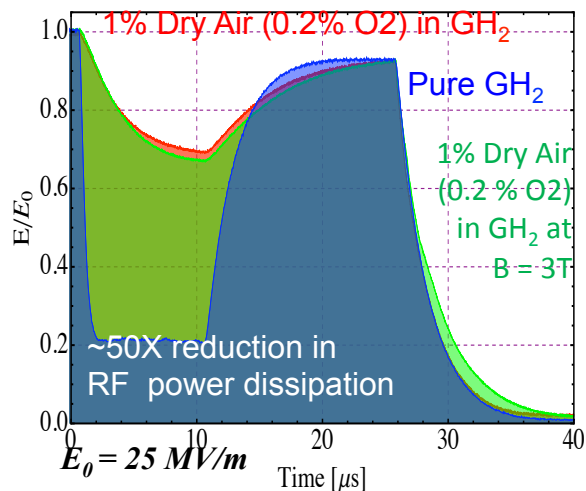
RF cavity in vacuum:



Breakdown by field emission very encouraging !

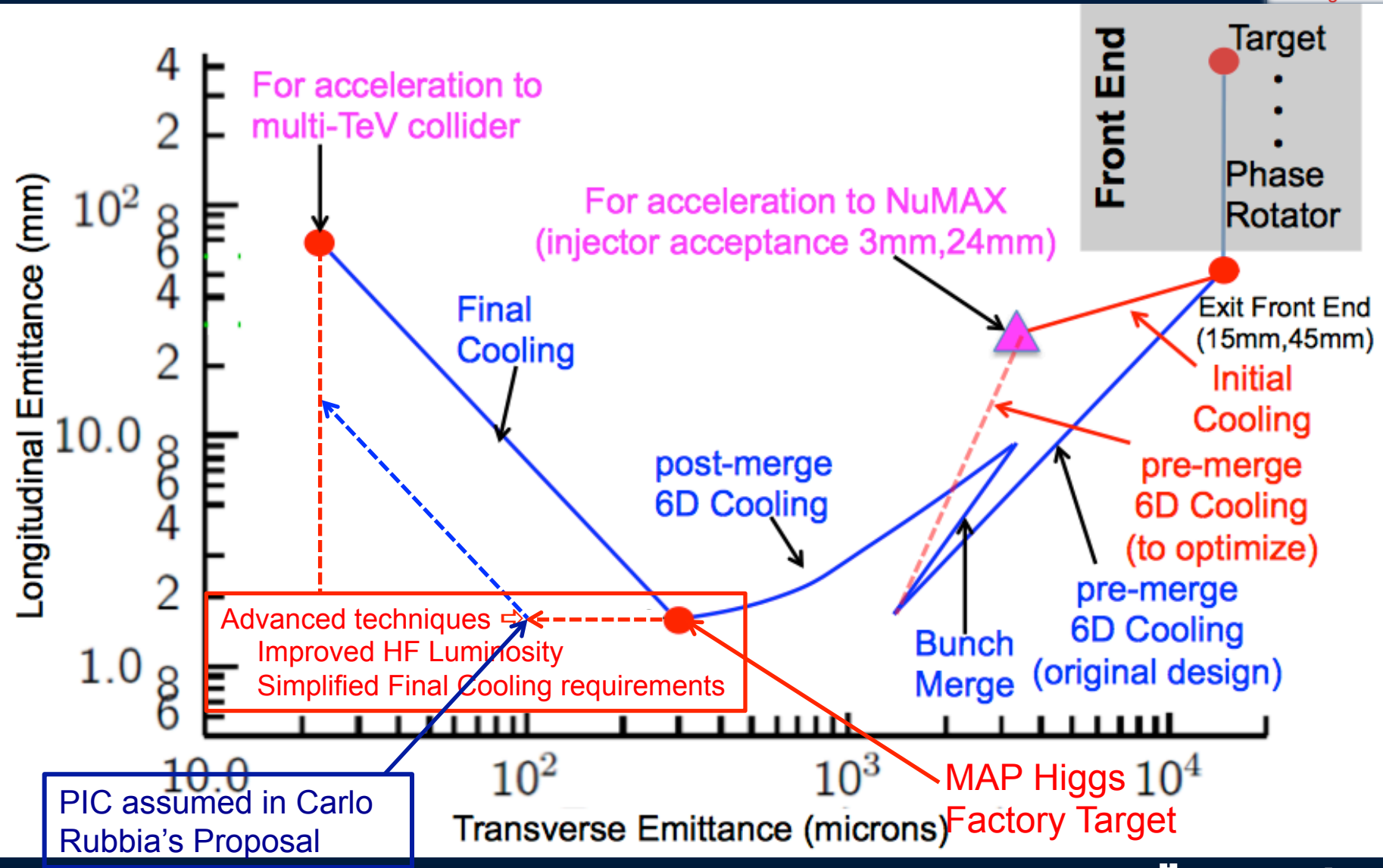
New cavity by LBNL/SLAC for tests in FNAL/MTA

RF cavity filled with gas



No accelerating field degradation up to 3 T
Operation with beam under heavy beam loading

Muon Ionization Cooling

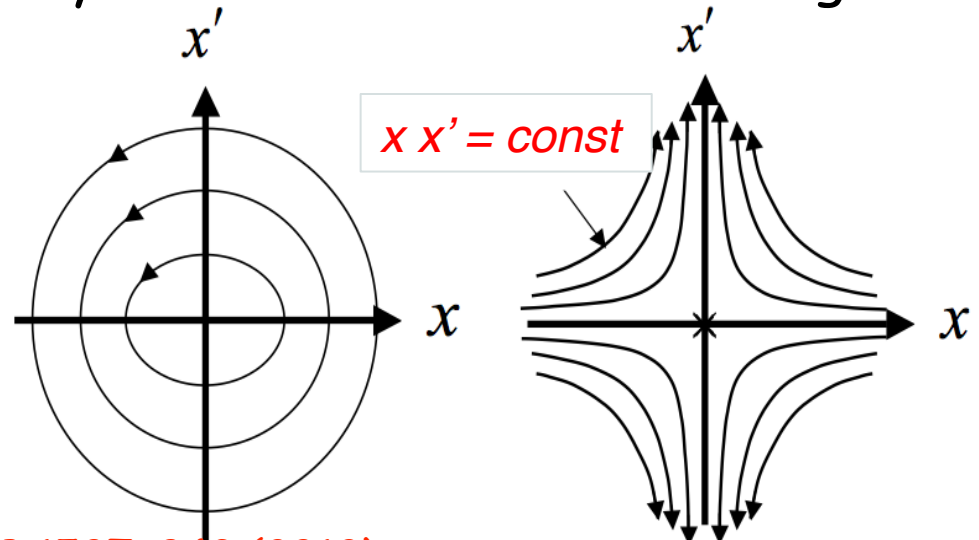


3.-PIC, the Parametric Resonance Cooling of muons

C. Rubbia

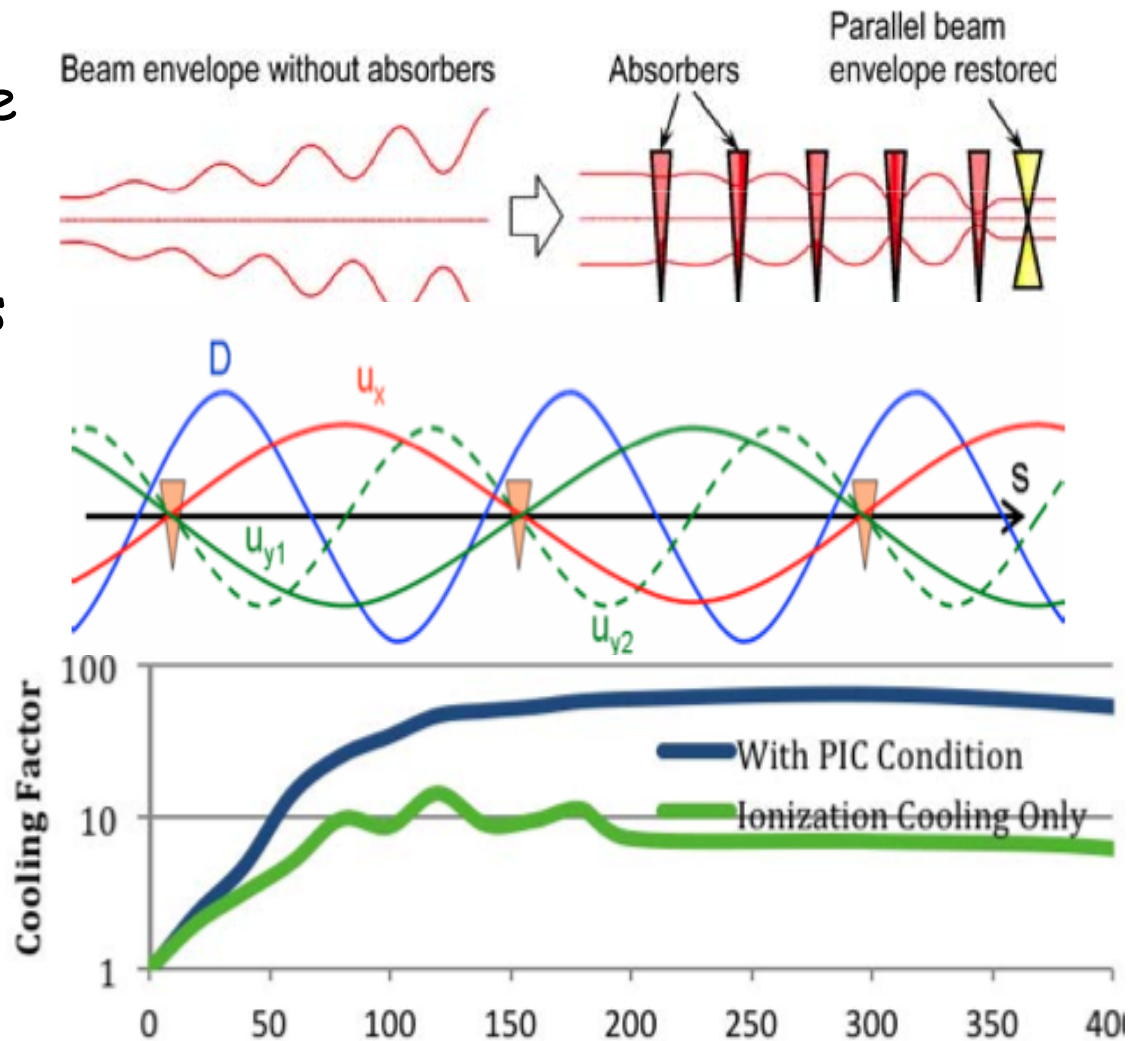
- Combining ionization cooling with parametric resonances is expected to lead to muon with much smaller transv. sizes.
- A linear magnetic transport channel has been designed by Ya.S. Derbenev et al where **a half integer resonance** is induced such that the normal elliptical motion of particles in x - x' phase space becomes **hyperbolic**, with particles moving to smaller x and larger x' at the channel focal points.
- Thin absorbers placed at the focal points of the channel then cool the angular divergence by the usual ionization cooling.

*LEFT ordinary oscillations
RIGHT hyperbolic motion
induced by perturbations
near an (one half integer)
resonance of the betatron
frequency.*



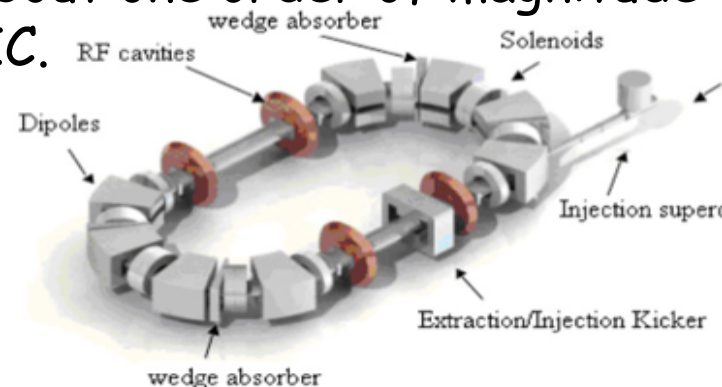
V. S. Morozov et al, AIP 1507, 843 (2012);

- Without damping, the beam dynamics is not stable because the beam envelope grows with every period. Energy absorbers at the focal points stabilizes the beam through the ionization cooling.
- The longitudinal emittance is maintained constant tapering the absorbers and placing them at points of appropriate dispersion, vertical β and two horizontal β .
- Comparison of cooling factors (ratio of initial to final 6D emittance) with and without the PIC condition vs number of cells: more than 10x gain



Parametric Resonance Cooling

- The first muon cooling ring should present no unexpected behaviour and good agreement between calculations and experiment is expected both transversely and longitudinally
- The novel Parametric Resonance Cooling (PIC) involves instead the balance between a strong resonance growth and ionization cooling and it may involve significant and unexpected conditions which are hard to predict.
- Therefore the experimental demonstration of the cooling must be concentrated on such a resonant behaviour.
- On the other hand the success of the novel Parametric Resonance Cooling is a necessary premise for a viable luminosity of the initial proton parameters of the future CERN accelerators since the expected Higgs luminosity is proportional to the inverse of the transverse emittance, hence about one order of magnitude of increment is expected from PIC.



Carlo Rubbia – FNAL May 2015

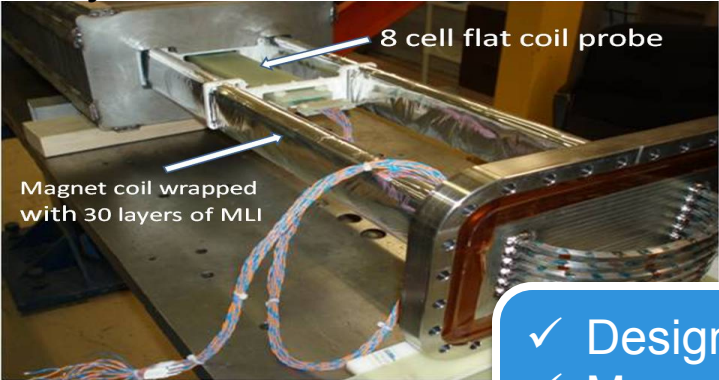
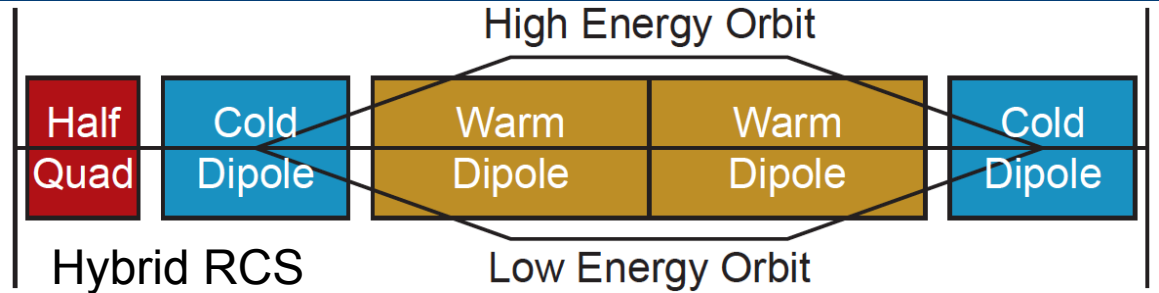
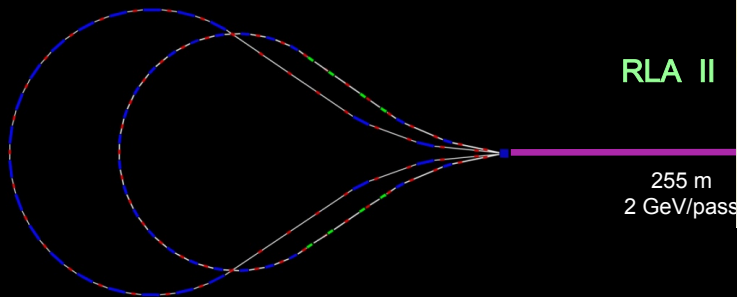
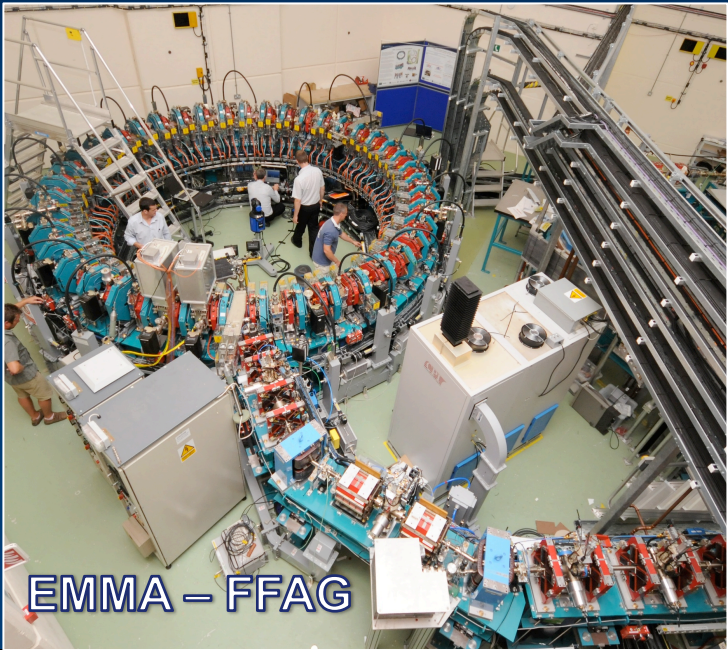
Acceleration Requirements

- Key Issues:
 - Muon lifetime \Rightarrow ultrafast acceleration chain
 - NF with modest cooling \Rightarrow accelerator acceptance
 - Total charge \Rightarrow cavity beam-loading (stored energy)
 - TeV-scale acceleration focuses on hybrid Rapid Cycling Synchrotron \Rightarrow requires rapid cycling magnets
$$B_{\text{peak}} \sim 2\text{T} \quad f > 400\text{Hz}$$

Acceleration

Technologies include:

- Superconducting Linacs (NuMAX choice)
- Recirculating Linear Accelerators (RLAs)
- Fixed-Field Alternating-Gradient (FFAG) Rings
- (Hybrid) Rapid Cycling Synchrotrons (RCS) for TeV energies



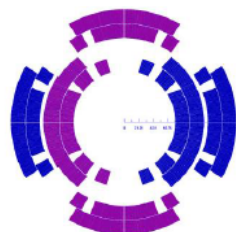
RCS requires
2 T p-p magnets
at $f > 400$ Hz
(U Miss & FNAL)

- ✓ Design concepts in hand
- ✓ Magnet R&D indicates parameters achievable

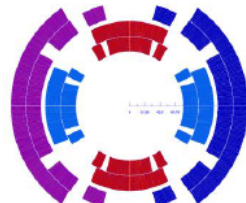
Collider Rings

- Detailed optics studies for Higgs, 1.5 TeV, 3 TeV and now 6 TeV CoM
 - With supporting magnet designs and background studies

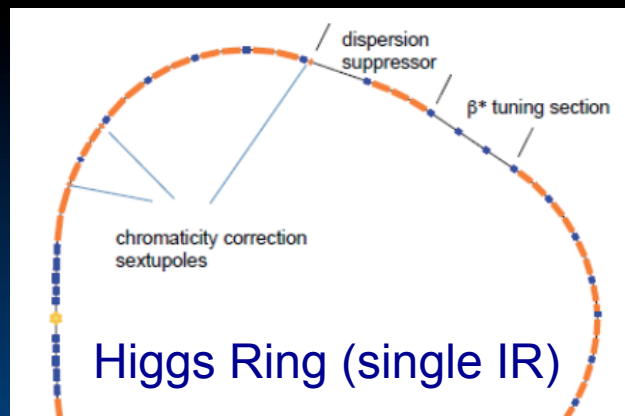
- ✓ Higgs, 1.5 TeV CoM and 3 TeV CoM Designs
 - With magnet concepts
 - Achieve target parameters
- ✓ Preliminary 6 TeV CoM design
 - Key issue is IR design and impact on luminosity
 - Utilizes lower power on target



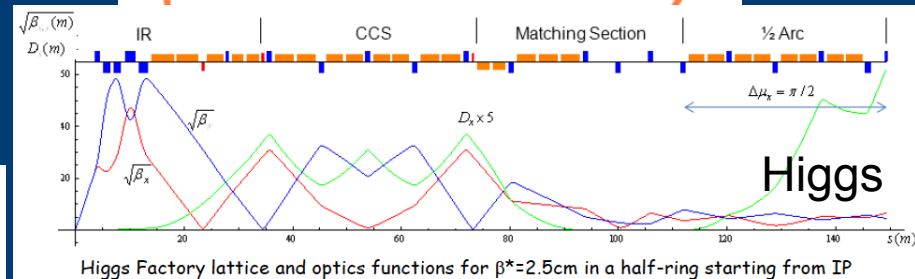
Dipole/Quad



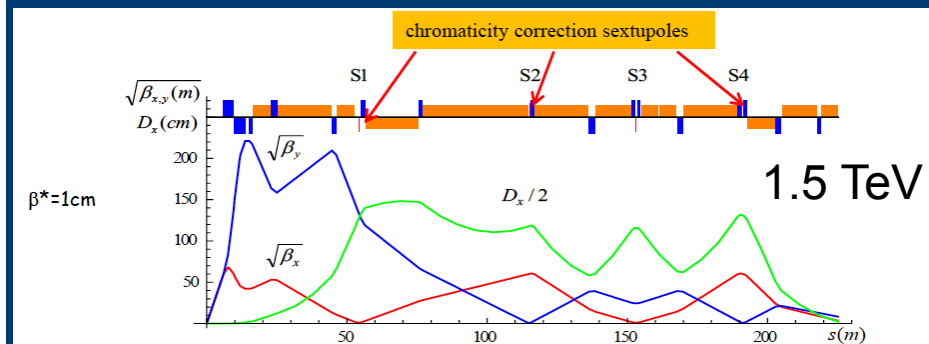
Quad/Dipole



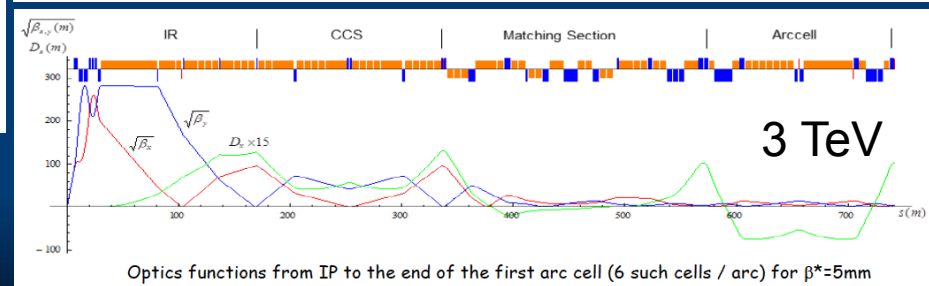
Higgs Ring (single IR)



Higgs Factory lattice and optics functions for $\beta^*=2.5\text{cm}$ in a half-ring starting from IP



1.5 TeV



3 TeV

Optics functions from IP to the end of the first arc cell (6 such cells / arc) for $\beta^*=5\text{mm}$

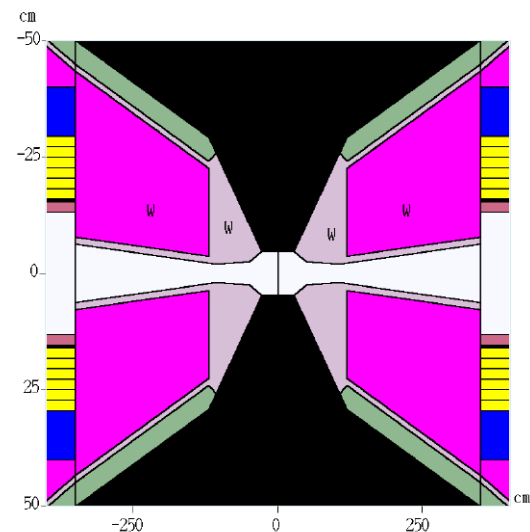
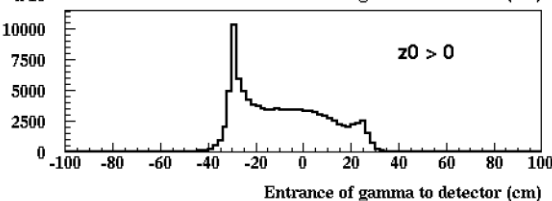
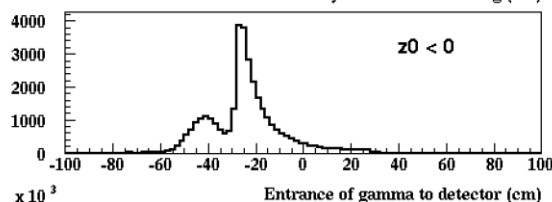
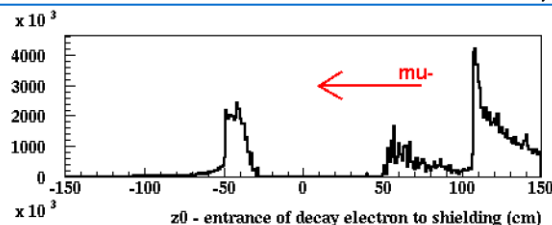
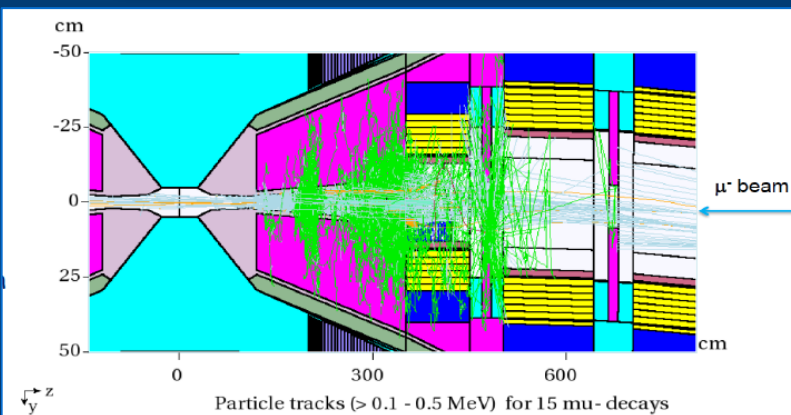
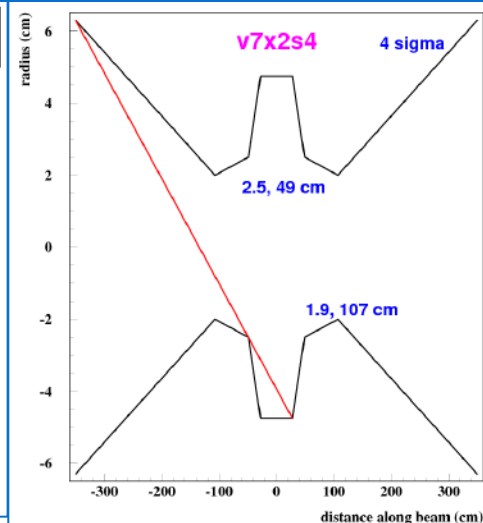
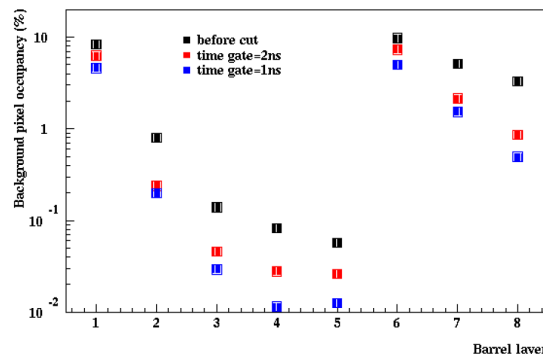
Machine Detector Interface

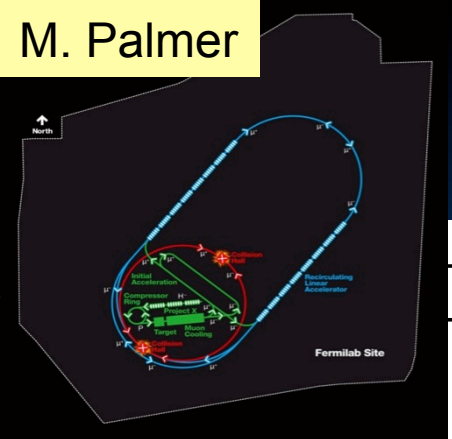


- ✓ Backgrounds appear manageable with suitable detector pixelation and timing rejection
 - ✓ Recent study of hit rates comparing MARS, EGS and FLUKA appear consistent to within factors of <2
- ⇒ Significant improvement in our confidence of detector performance

Pixel occupancy in barrel vs timing cuts.
Pixel - $20 \times 20 \mu\text{m}$ in VXD and $1000 \times 100 \mu\text{m}$ in Tracker

Layer 1-5 are VXD barrel, 6-8 are Tracker barrel





Muon Collider Parameters



Muon Collider Parameters					
Parameter	Units	Higgs	Multi-TeV		
		Production Operation			Accounts for Site Radiation Mitigation
CoM Energy	TeV	0.126	1.5	3.0	6.0
Avg. Luminosity	$10^{34} \text{cm}^{-2} \text{s}^{-1}$	0.008	1.25	4.4	12
Beam Energy Spread	%	0.004	0.1	0.1	0.1
Higgs Production/ 10^7sec		13,500	37,500	200,000	820,000
Circumference	km	0.3	2.5	4.5	6
No. of IPs		1	2	2	2
Repetition Rate	Hz	15	15	12	6
β^*	cm	1.7	1 (0.5-2)	0.5 (0.3-3)	0.25
No. muons/bunch	10^{12}	4	2	2	2
Norm. Trans. Emittance, ϵ_{TN}	$\pi \text{ mm-rad}$	0.2	0.025	0.025	0.025
Norm. Long. Emittance, ϵ_{LN}	$\pi \text{ mm-rad}$	1.5	70	70	70
Bunch Length, σ_s	cm	6.3	1	0.5	0.2
Proton Driver Power	MW	4	4	4	1.6
Wall Plug Power	MW	200	216	230	270

Exquisite Energy Resolution
Allows Direct Measurement
of Higgs Width

Success of advanced cooling concepts
⇒ several $\times 10^{32}$ [Rubbia proposal: 5×10^{32}]

e^+ on target muon source

Idea for low emittance μ beam

Conventional production: from **proton on target**

π , K decays from proton on target have typical $P_\mu \sim 100 \text{ MeV}/c$
(π , K rest frame)

whatever is the boost P_T will stay in Lab frame \rightarrow
very high emittance at production point \rightarrow **cooling needed!**

Direct μ pair production:

Muons produced from $e^+e^- \rightarrow \mu^+\mu^-$ at \sqrt{s} around the $\mu^+\mu^-$ threshold
($\sqrt{s} \sim 0.212 \text{ GeV}$) in asymmetric collisions (to collect μ^+ and μ^-)

NIM A Reviewer: *“A major advantage of this proposal is the lack of cooling of the muons.... the idea presented in this paper may truly revolutionise the design of muon colliders ... ”*

Advantages:

1. **Low emittance possible:** P_μ is tunable with \sqrt{s} in $e^+e^- \rightarrow \mu^+\mu^-$ P_μ can be **very small** close to the $\mu^+\mu^-$ threshold
2. **Low background:** Luminosity at low emittance will allow low background and low ν radiation (easier experimental conditions, can go up in energy)
3. **Reduced losses from decay:** muons can be produced with a relatively high boost in asymmetric collisions
4. **Energy spread:** Muon Energy spread **also small at threshold**, it gets larger as \sqrt{s} increases, one can use correlation with emission angle (eventually it can be reduced with short bunches)

Disadvantages:

- **Rate:** much smaller cross section wrt protons

$$\sigma(e^+e^- \rightarrow \mu^+\mu^-) \sim 1 \mu\text{b at most}$$

i.e. Luminosity(e^+e^-) = $10^{40} \text{ cm}^{-2} \text{ s}^{-1} \rightarrow$ gives μ rates 10^{10} Hz

Possible Schemes

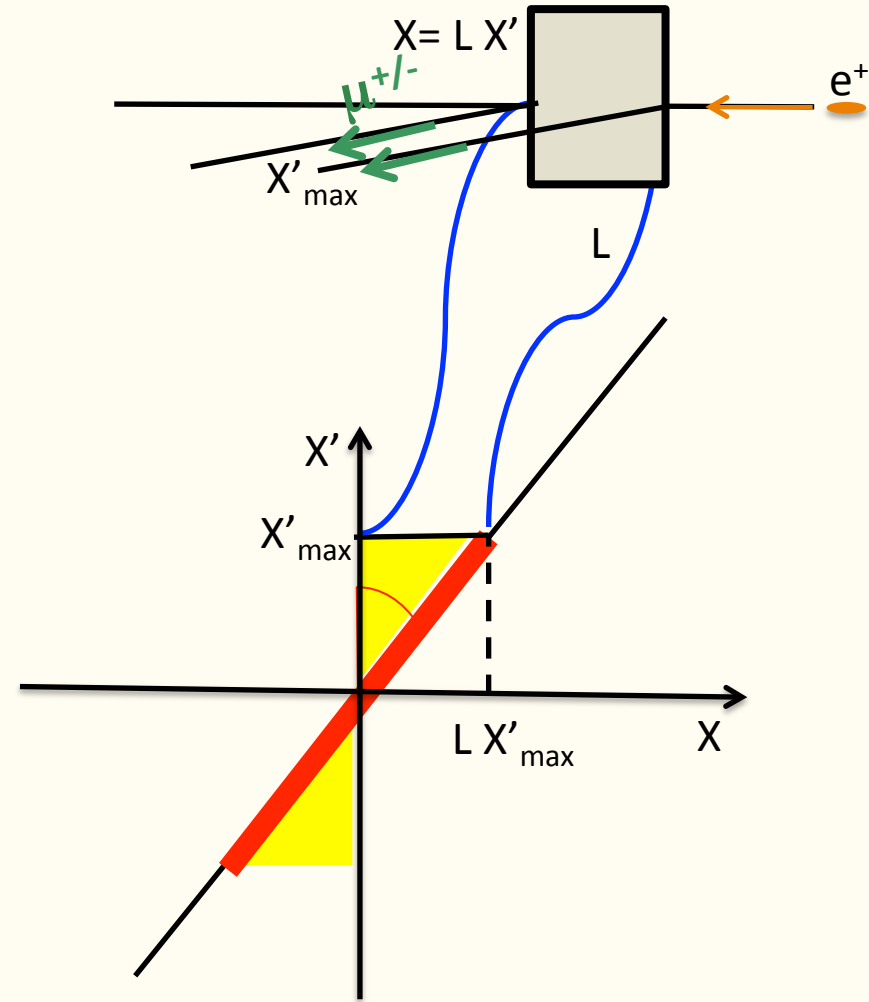
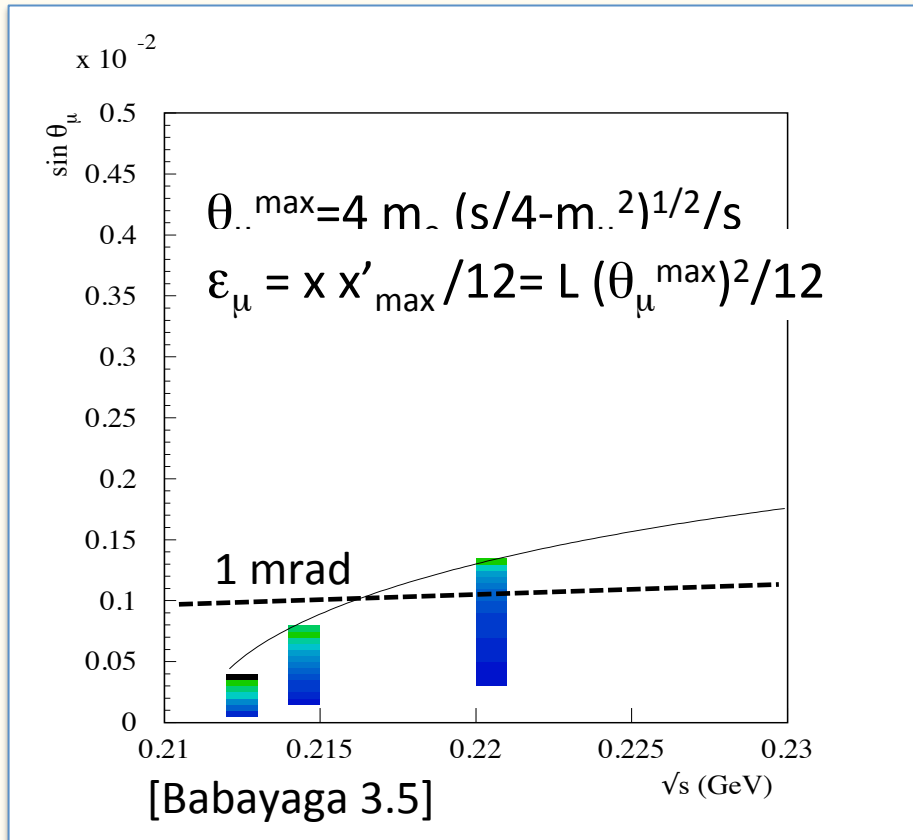
- **Low energy collider with e^+/e^- beam (e^+ in the GeV range):**
 1. Conventional asymmetric collisions (but required luminosity is beyond current knowledge)
 2. Positron beam interacting with continuous beam from electron cooling (too low electron density, 10^{20} electrons/cm³ needed to obtain a reasonable conversion efficiency to muons)
- **Electrons at rest (seems more feasible):**
 3. e^+ on Plasma target
 4. e^+ on standard target, including crystals with channeling
 - Need Positrons of ~ 45 GeV
 - $\gamma(\mu) \sim 200$ and μ laboratory lifetime of about $500 \mu\text{s}$



Ideally muons will *copy* the positron beam

Muons angle contribution to μ beam emittance

The target thickness and c.o.m. energy completely determine the emittance contributions due to muon production angle



Criteria for target design

- **Number of $\mu^+\mu^-$ pairs produced per interaction:**

$$n(\mu^+\mu^-) = n^+ \rho^- L \sigma(\mu^+\mu^-)$$

n^+ = number of e^+

ρ^- = target electron density

L = target length

- **$\rho^- L$ constraints**

- Ideal target (e^- dominated)

$$(\rho^- L)_{\max} = 1/\sigma(\text{radiative bhabha}) \approx 10^{25} \text{ cm}^{-2}$$

(beam lifetime determined by radiative Bhabha)

- With $(\rho^- L)_{\max}$ one has a maximal $\mu^+\mu^-$ production efficiency $\sim 10^{-5}$
- Muon beam emittance increases with L (in absence of intrinsic focusing effects) \rightarrow increase ρ^-
- Conventional target $(\rho^- L)_{\max}$ depends on material (see next slides)

Criteria for target design

Bremsstrahlung on nuclei and multiple scattering (MS) are the dominant effects in real life... X_0 and electron density will matter:

- **Heavy materials**

- minimize emittance (enters linearly) \rightarrow Copper has about same contributions to emittance from MS and $\mu^+\mu^-$ production
- high e^+ loss (Bremsstrahlung is dominant)

- **Very light materials**

- maximize production efficiency (enters quad) \rightarrow H_2
- even for liquid need $O(1m)$ target \rightarrow emittance increase

- **Not too heavy materials(Be, C)**

- Allow low emittance with small e^+ loss

optimal: not too heavy and thin

Application for Multi-TeV Muon Collider as an example

- Use thin target with high efficiency and small e^+ loss
- Positrons in storage ring with high momentum acceptance
- No need of extreme beam energy spread

Possible target: 3 mm Be

45 GeV e^+ impinging beam

- Emittance at $E_\mu = 22$ GeV:

$$\varepsilon_x = 0.19 \cdot 10^{-9} \text{ m-rad}$$

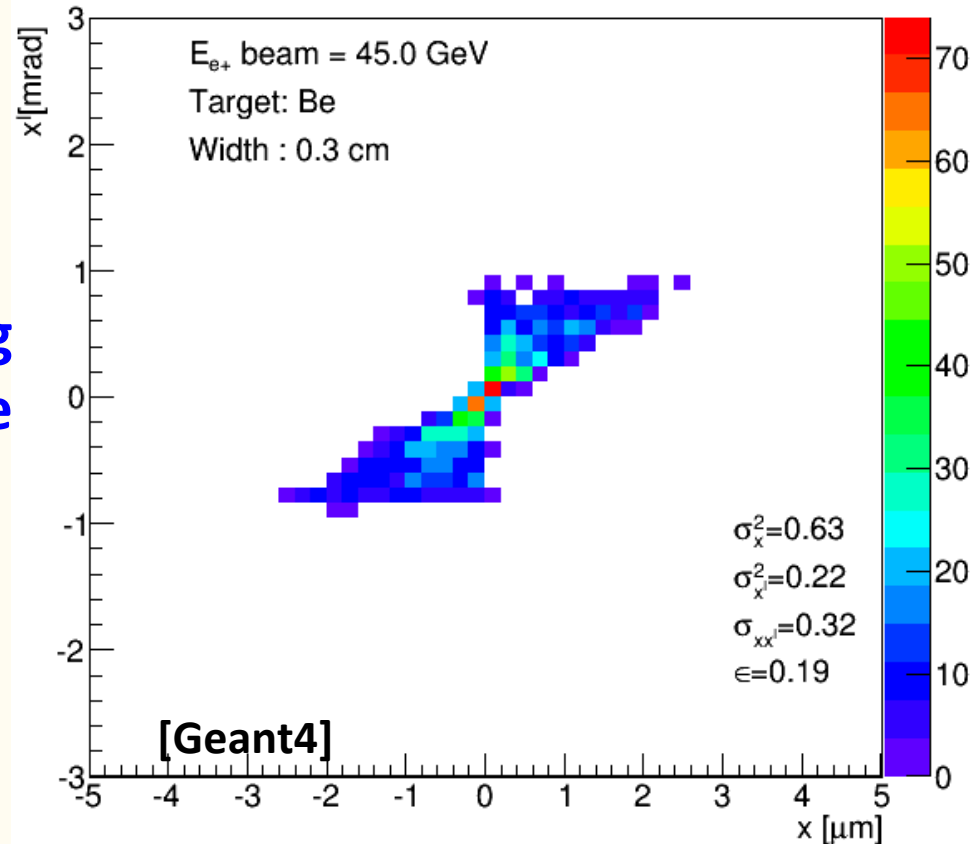
**Multiple Scattering
contribution is negligible**

-> μ after production is not affected by nuclei in target

-> e^+ beam emittance is preserved, not being affected by nuclei in target (see also next slide)

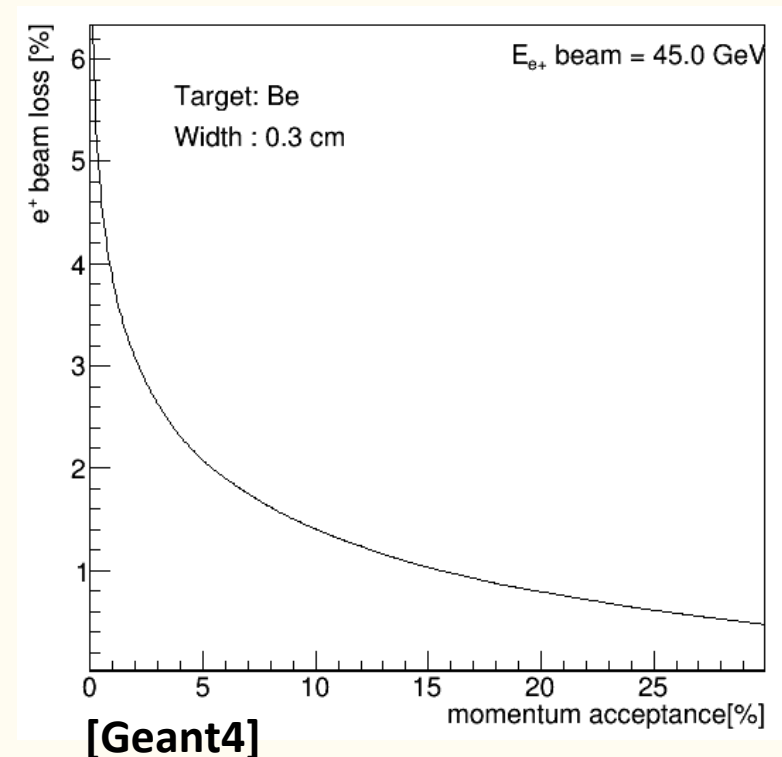
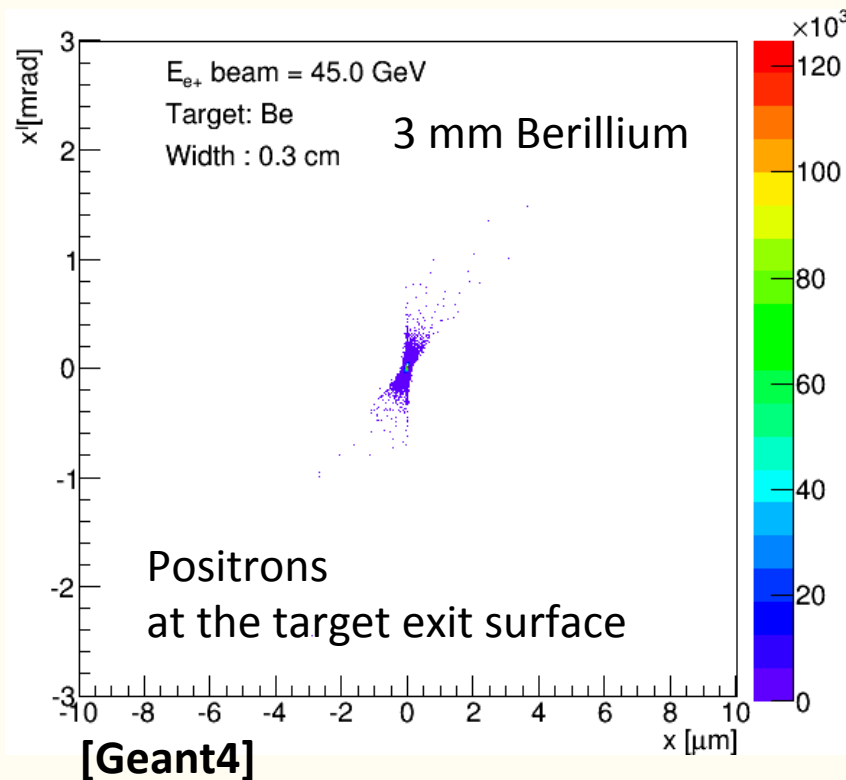
- Conversion efficiency: 10^{-7}
- Muons beam energy spread: 9%

Muons at the target exit surface



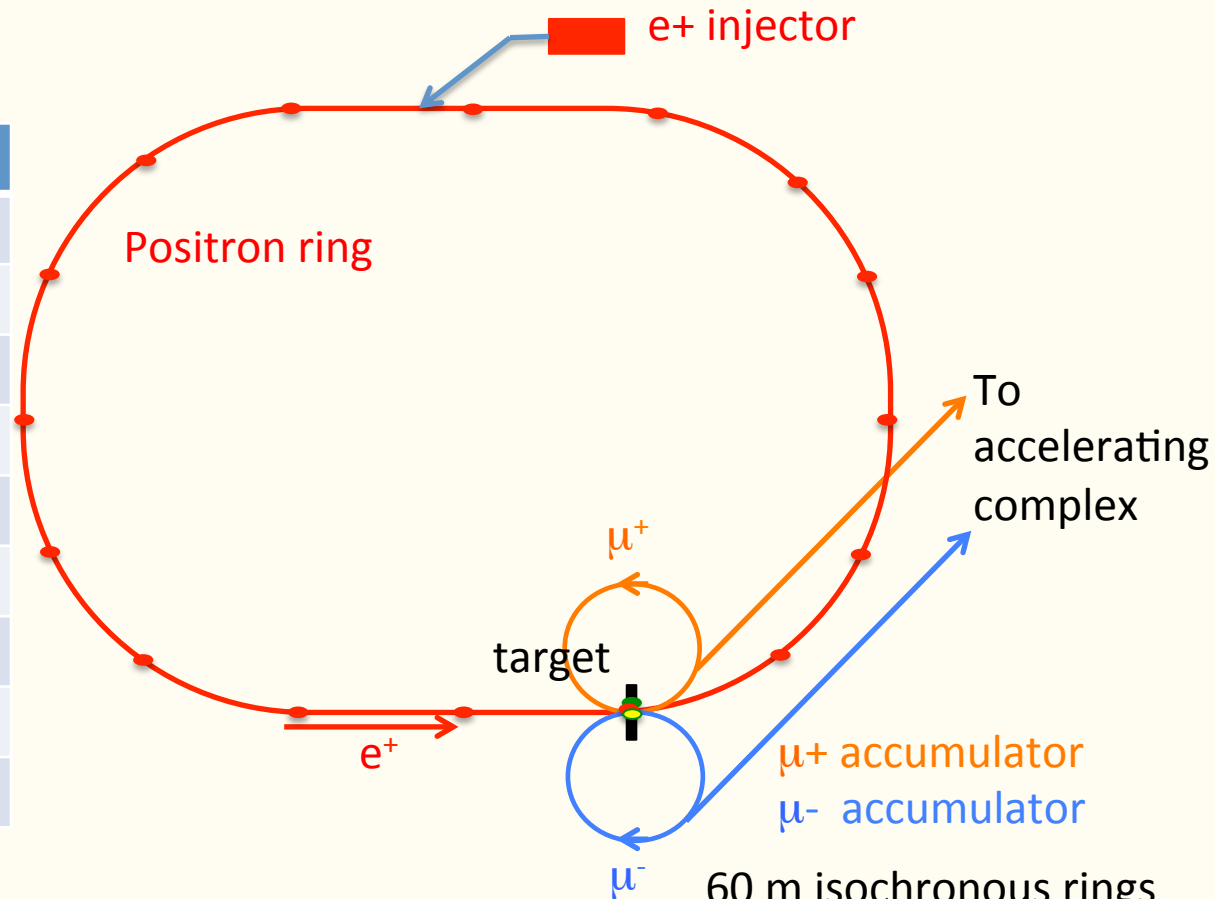
Positrons Storage Ring Requirements

- Transverse phase space almost not affected by target
- Most of positrons experience a small energy deviation:
A large fraction of e^+ can be stored (depending on the momentum acceptance)
 - 10% momentum acceptance will increase the effective muon conversion efficiency (produced muon pairs/produced positrons) by factor 100



Schematic Layout for muon source from e⁺

Circumference	6 km
ρ	0.6 km
number e ⁺ bunches	100
e ⁺ bunch spacing	200 ns
Beam current	240 mA
e ⁺ Particles/bunch	$3 \cdot 10^{11}$
Rate e ⁺ on target	$1.5 \cdot 10^{18}$ e ⁺ /s
U_0	0.58 GeV
P_{tot}	139 MW
B	0.245 T



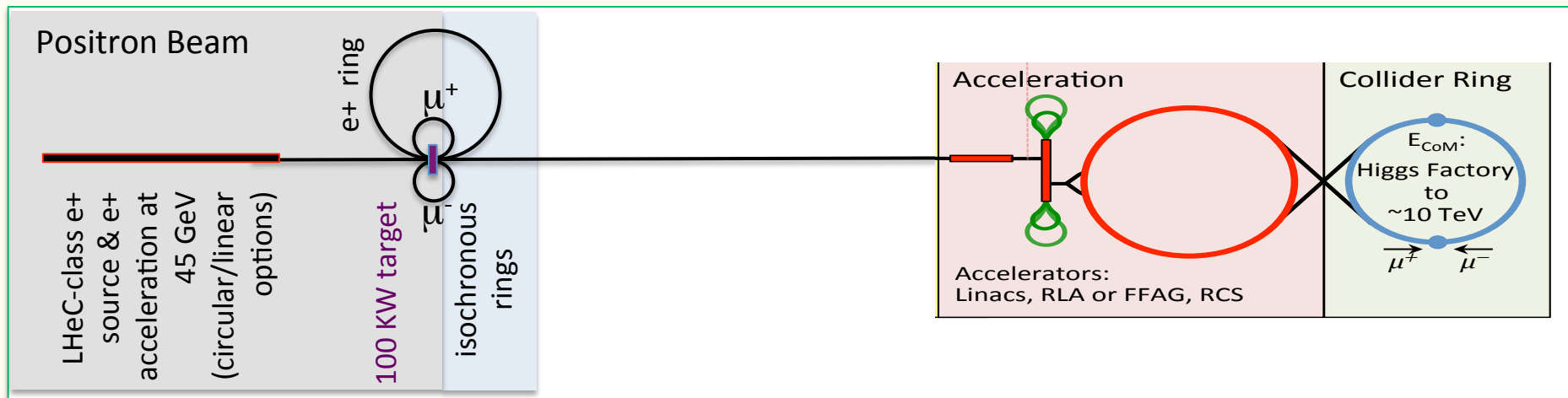
Key point:

Positron source requirements strictly related to the e⁺ ring momentum acceptance

60 m isochronous rings recombine bunches for $\sim 1 \tau_\mu^{\text{lab}} \sim 2500$ turns

$$n_b = \sum_{i=1}^{N_T} e^{-\Delta t(N_T-i)/\tau_\mu^{\text{lab}}}$$

Muon Collider: Schematic Layout for positron based muon source

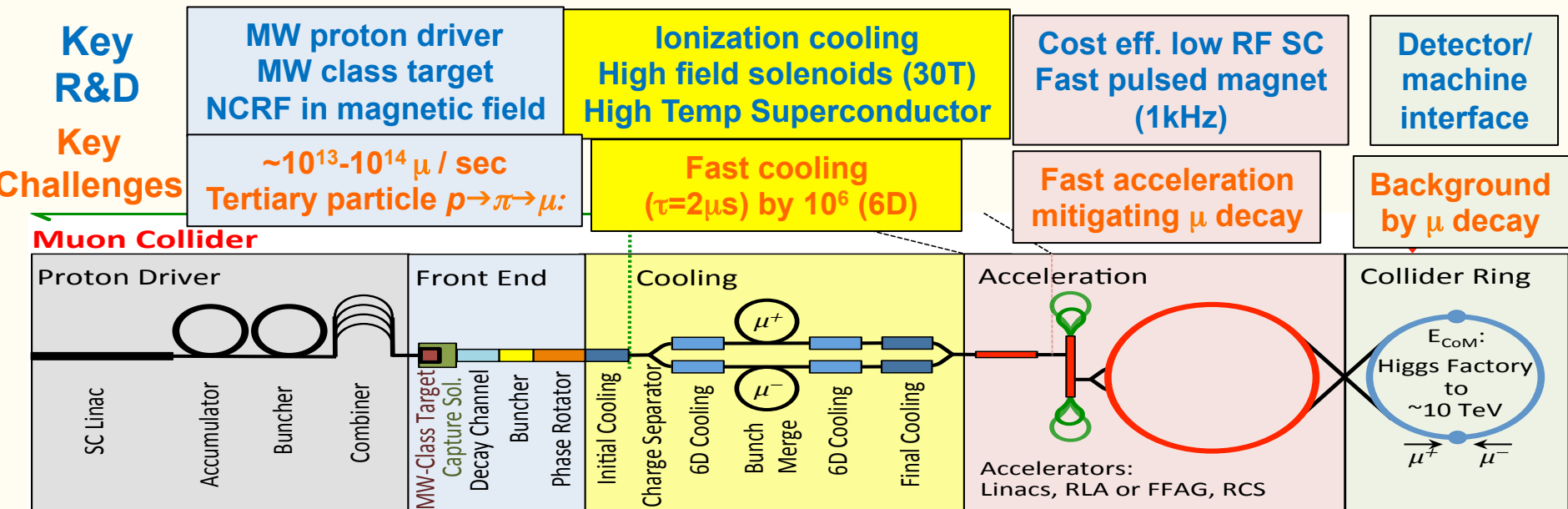


**Key
Challenges**

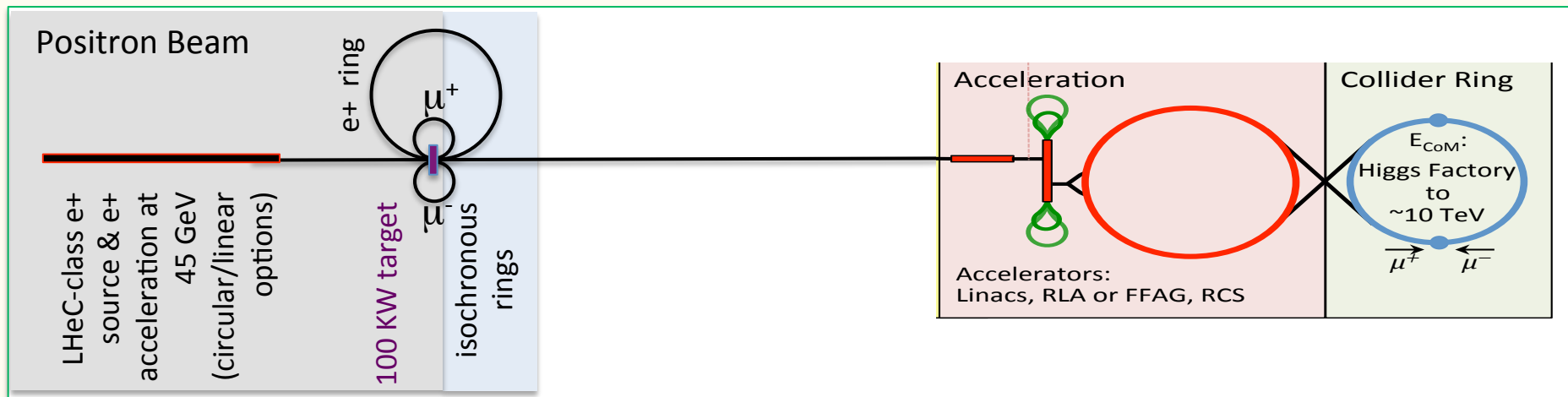
$\sim 10^{11} \mu / \text{sec}$ from $e^+e^- \rightarrow \mu^+\mu^-$

**Key
R&D**

$10^{15} e^+/\text{sec}$, 100 kW class target, NON destructive process in e^+ ring



share the same complex



Key Challenges

$\sim 10^{11} \mu / \text{sec}$ from $e^+e^- \rightarrow \mu^+\mu^-$

Key R&D

$10^{15} e^+/\text{sec}$, 100 kW class target, NON destructive process in e^+ ring

EASIER AND CHEAPER DESIGN, IF FEASIBLE

Muon beam parameters

Assuming

- a positron ring with a total 25% momentum acceptance (10% easily achieved) and
- $\sim 3 \times$ LHeC positron source rate

	positron source	proton source
μ rate[Hz]	$9 \cdot 10^{10}$	$2 \cdot 10^{13}$
μ /bunch	$4.5 \cdot 10^7$	$2 \cdot 10^{12}$
normalised ϵ [$\mu\text{m-mrad}$]	40	25000

Very small emittance, high muon rates but relatively small bunch population:

- The actual number of μ /bunch in the muon collider can be larger by a factor $\sim \tau_{\mu}^{\text{lab}}(\text{HE})/500 \mu\text{s}$ (~ 100 @6 TeV) by topping up.

LEMC Draft Parameters

comparable luminosity with
lower $N\mu$ /bunch
(lower background)
thanks to very small emittance
(and lower beta*)

much higher signal/noise ratio

Of course, a design
study is needed to
define this table

		LEMC-6TeV	LEMC-H
Parameter	Units		
LUMINOSITY/IP	$\text{cm}^{-2} \text{s}^{-1}$	5.09E+34	1.69E+31
Beam Energy	GeV	3000	62.5
Hourglass reduction factor		1.000	1.000
Muon mass	GeV	0.10566	0.10566
Lifetime @ prod	sec	2.20E-06	2.20E-06
Lifetime	sec	0.06	0.00
c*tau @ prod	m	658.00	658.00
c*tau	m	1.87E+07	3.89E+05
1/tau	Hz	1.60E+01	7.68E+02
Circumference	m	6000	150
Bending Field	T	15	15
Bending radius	m	667	14
Magnetic rigidity	T m	10000	208
Gamma Lorentz factor		28392.96	591.52
N turns before decay		3113.76	2594.80
β_x @ IP	m	0.0002	0.0002
β_y @ IP	m	0.0002	0.0002
Beta ratio		1.0	1.0
Coupling (full current)	%	100	100
Normalised Emittance x	m	4.00E-08	4.00E-08
Emittance x	m	1.41E-12	6.76E-11
Emittance y	m	1.41E-12	6.76E-11
Emittance ratio		1.0	1.0
Bunch length (zero current)	mm	0.1	0.1
Bunch length (full current)	mm	0.1	0.1
Beam current	mA	0.048	0.1
Revolution frequency	Hz	5.00E+04	2.00E+06
Revolution period	s	2.00E-05	5.00E-07
Number of bunches	#	1	1
N. Particle/bunch	#	6.00E+09	1.20E+08
Number of IP	#	1.00	1.00
σ_x @ IP	micron	1.68E-02	1.16E-01
σ_y @ IP	micron	1.68E-02	1.16E-01
$\sigma_{x'}$ @ IP	rad	8.39E-05	5.81E-04
$\sigma_{y'}$ @ IP	rad	8.39E-05	5.81E-04

Key Feasibility Issues

Muon Collider Study: Proton Based Source

- **Proton Driver**
- **Target**
- **Front End**
- **Cooling (PIC)**
- **μ Acceleration**
- **Collider Ring**
- **Collider MDI**
- **Collider Detector**

Positron Based Source

Positron Source

Muon Target

Positron Ring

not yet investigated!

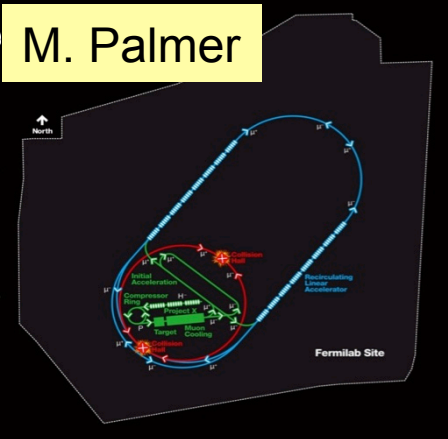
(mostly) independent
on muon source

synergy with the two
options

Conclusions

- **Very low emittance muon beams** can be obtained by means of positron beam on target
- Interesting **muon rates require**:
 - **Challenging positron source** (synergy with LHeC, ILC, FCC-ee...)
 - **Positron ring with high momentum acceptance** (synergy with next generation SL sources)
- Fast muon acceleration concepts deeply studied by MAP
- Final focus design can profit of studies on conventional muon studies

Backup Slides



Muon Collider Parameters



Muon Collider Parameters					
Parameter	Units	Higgs	Multi-TeV		
		Production Operation			Accounts for Site Radiation Mitigation
CoM Energy	TeV	0.126	1.5	3.0	6.0
Avg. Luminosity	$10^{34}\text{cm}^{-2}\text{s}^{-1}$	0.008	1.25	4.4	12
Beam Energy Spread	%	0.004	0.1	0.1	0.1
Higgs Production/ 10^7sec		13,500	37,500	200,000	820,000
Circumference	km	0.3	2.5	4.5	6
No. of IPs		1	2	2	2
Repetition Rate	Hz	15	15	12	6
β^*	cm	1.7	1 (0.5-2)	0.5 (0.3-3)	0.25
No. muons/bunch	10^{12}	4	2	2	2
Norm. Trans. Emittance, ϵ_{TN}	$\pi\text{ mm-rad}$	0.2	0.025	0.025	0.025
Norm. Long. Emittance, ϵ_{LN}	$\pi\text{ mm-rad}$	1.5	70	70	70
Bunch Length, σ_s	cm	6.3	1	0.5	0.2
Proton Driver Power	MW	4	4	4	1.6
Wall Plug Power	MW	200	216	230	270

Exquisite Energy Resolution
Allows Direct Measurement
of Higgs Width

Success of advanced cooling concepts
⇒ several $\times 10^{32}$ [Rubbia proposal: 5×10^{32}]

Conclusion



- NF \Rightarrow precision ν microscopes
- Multi-TeV MC \Rightarrow potentially only cost-effective route to lepton collider capabilities with $E_{\text{CM}} > 5 \text{ TeV}$
- Key technical hurdles have been addressed:
 - High power target demo (MERIT)
 - Realizable cooling channel designs with acceptable performance
 - Breakthroughs in cooling channel technology
 - Significant progress in collider & detector design concepts

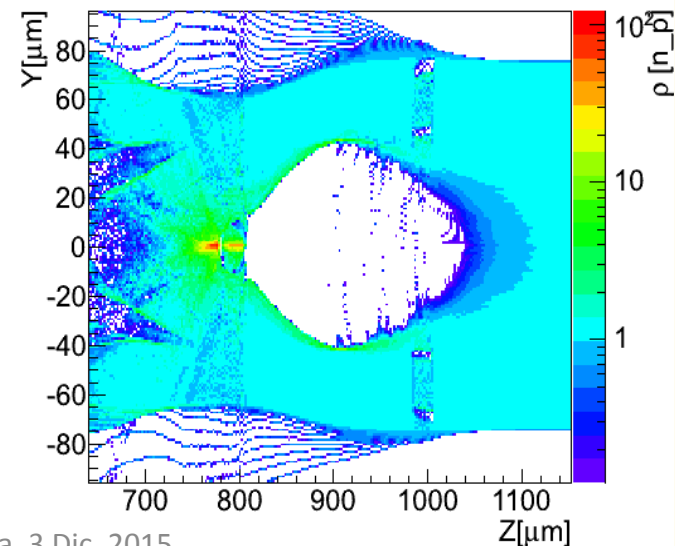
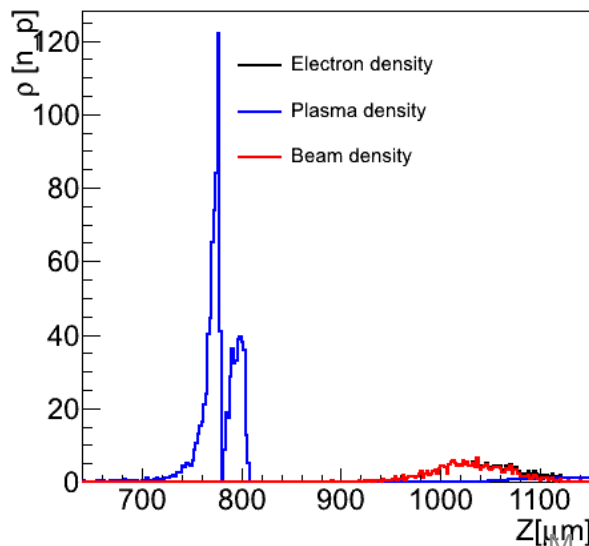
Accelerator	Energy Scale	Performance
Cooling Channel	~200 MeV	Emittance Reduction
MICE	160-240 MeV	5%
Muon Storage Ring	3-4 GeV	Useable μ decays/yr*
ν STORM	3.8 GeV	3×10^{17}
Intensity Frontier ν Factory	4-10 GeV	Useable μ decays/yr*
NuMAX (Initial)	4-6 GeV	8×10^{19}
NuMAX+	4-6 GeV	5×10^{20}
IDS-NF Design	10 GeV	5×10^{20}
Higgs Factory	~126 GeV CoM	Higgs/ 10^7 s
s-Channel μ Collider	~126 GeV CoM	3,500-13,500
Energy Frontier μ Collider	> 1 TeV CoM	Avg. Luminosity
Opt. 1	1.5 TeV CoM	$1.2 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
Opt. 2	3 TeV CoM	$4.4 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
Opt. 3	6 TeV CoM	$12 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

* Decays of an individual species (ie, μ^+ or μ^-)

Muon accelerator capabilities offer unique potential for the future of high energy physics research

Few statements on the plasma option

- Plasma would be a good approximation of an ideal electron target ++ autofocussing by Pinch effect
- enhanced electron density can be obtained at the border of the blow-out region (up x100)
- Simulations for $n_p = 10^{16}$ electrons/cm³ (C. Gatti, P. Londrillo)
- Region size decreases with $1/\sqrt{n_p}$ even don't know if blowout occurs at $n_p \sim 10^{20}$ electrons/cm³



Positron sources: studies on the market

- Summary of e^+ sources projects (all very aggressive):

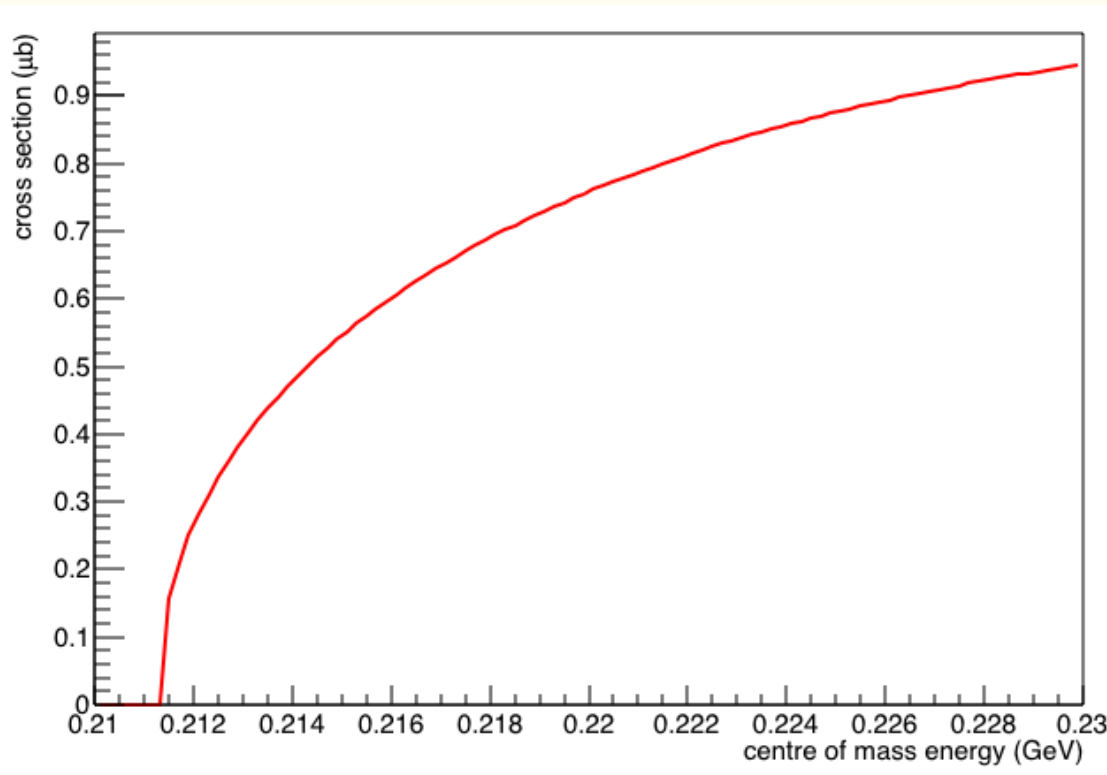
In [F. Zimmermann, et al., '**POSITRON OPTIONS FOR THE LINAC-RING LHeC**', WEPPR076 Proceedings of IPAC2012, New Orleans, Louisiana, USA]

	SLC	CLIC	ILC	LHeC pulsed	LHeC ERL
E [GeV]	1.19	2.86	4	140	60
$\gamma\epsilon_x$ [μm]	30	0.66	10	100	50
$\gamma\epsilon_y$ [μm]	2	0.02	0.04	100	50
$e^+[10^{14}\text{s}^{-1}]$	0.06	1.1	3.9	18	440

➤ This is the most critical issue

Processes at \sqrt{s} around 0.212 GeV

- Bhabha scattering, $\mu^+\mu^-$ production $\gamma\gamma$ (not relevant)
- $e^+e^- \rightarrow \mu^+\mu^-$ cross section:

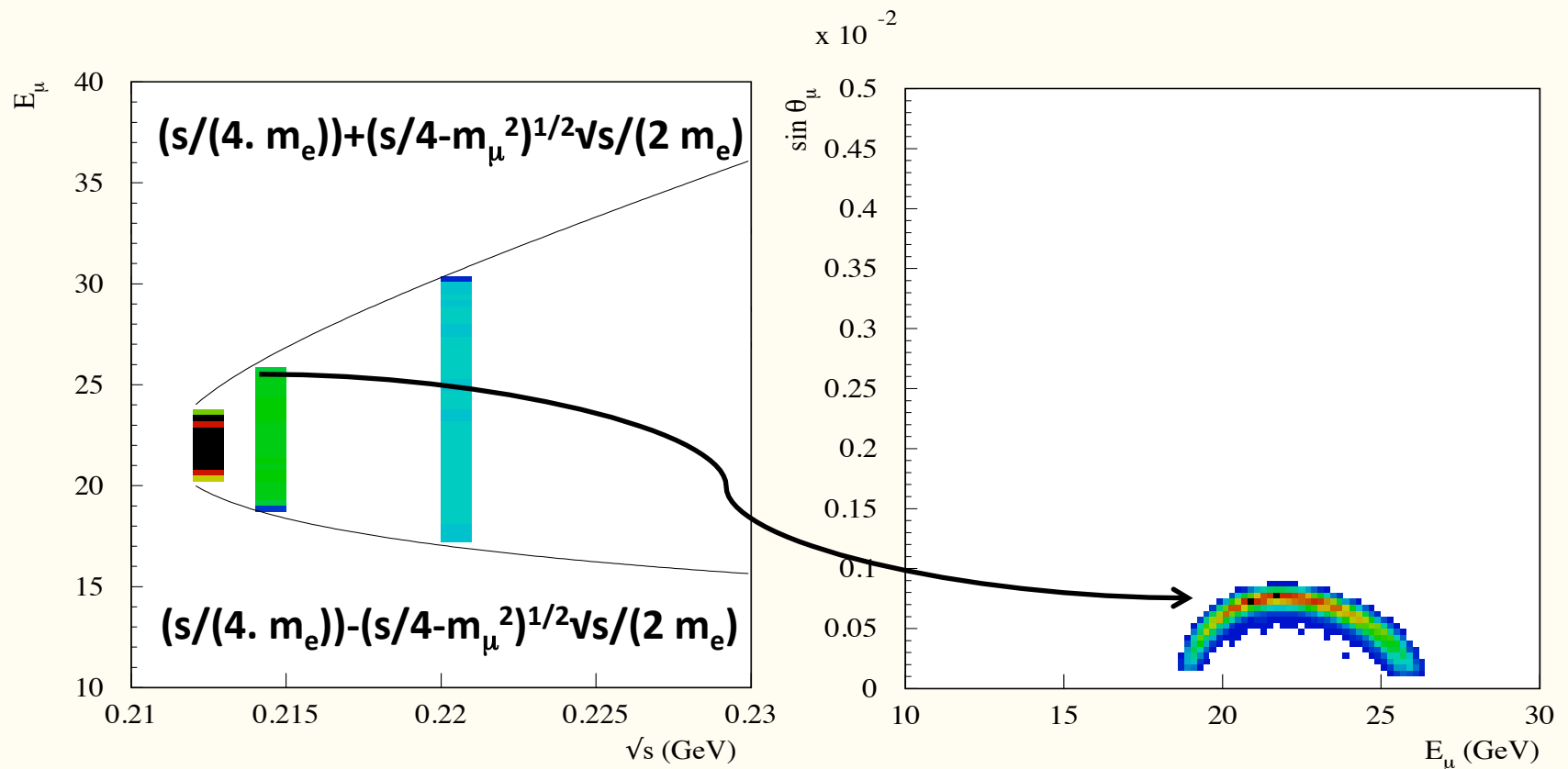


Muonium production also investigated:
huge cross section (mb range)
 10^{-4} eV width

Not viable.... Deeper studies?

Processes at $\sqrt{s} \sim 0.212$ GeV e^+ on target

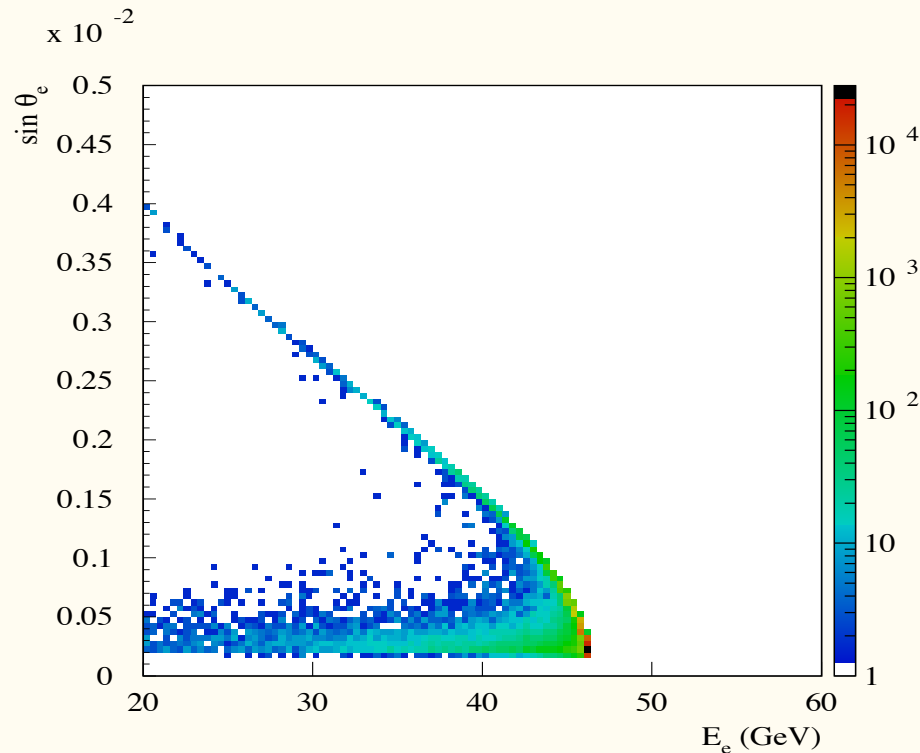
$e^+e^- \rightarrow \mu^+\mu^-$ muons energy spread:



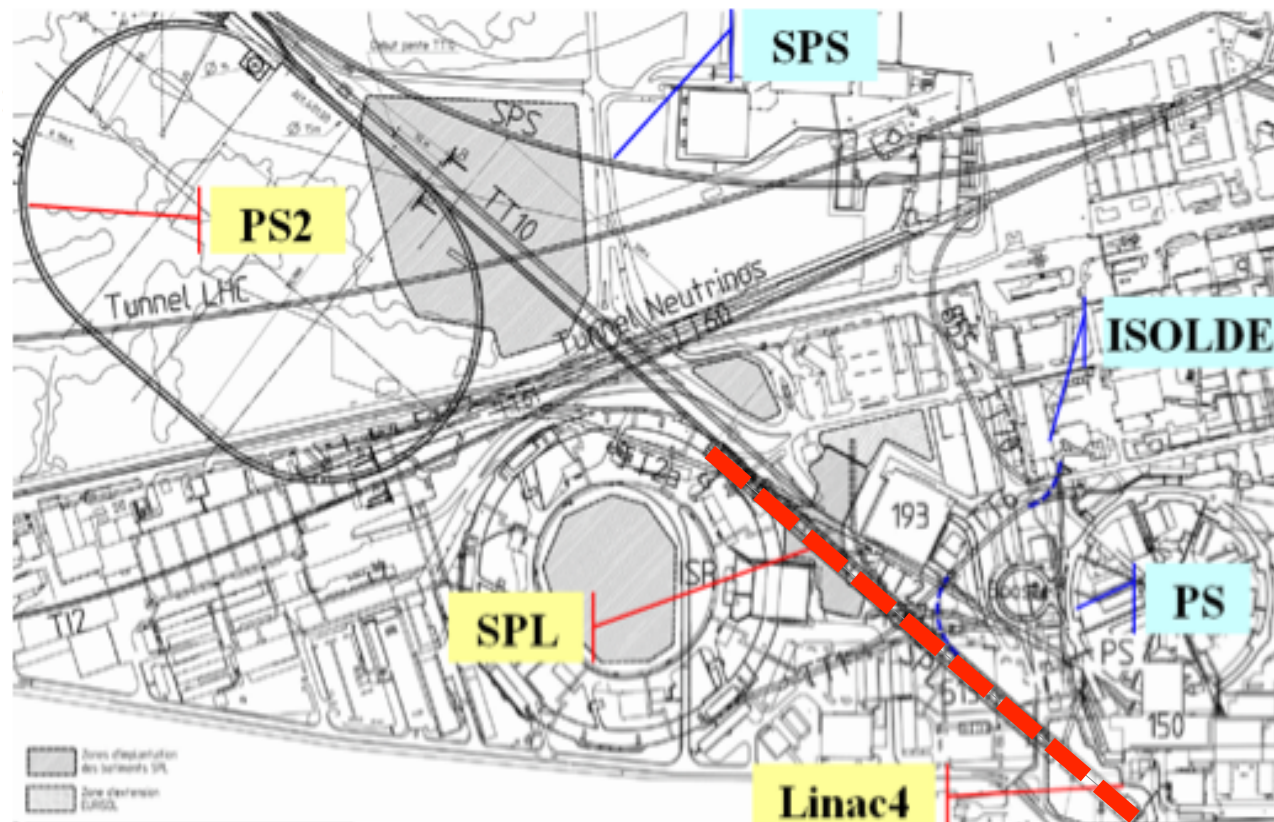
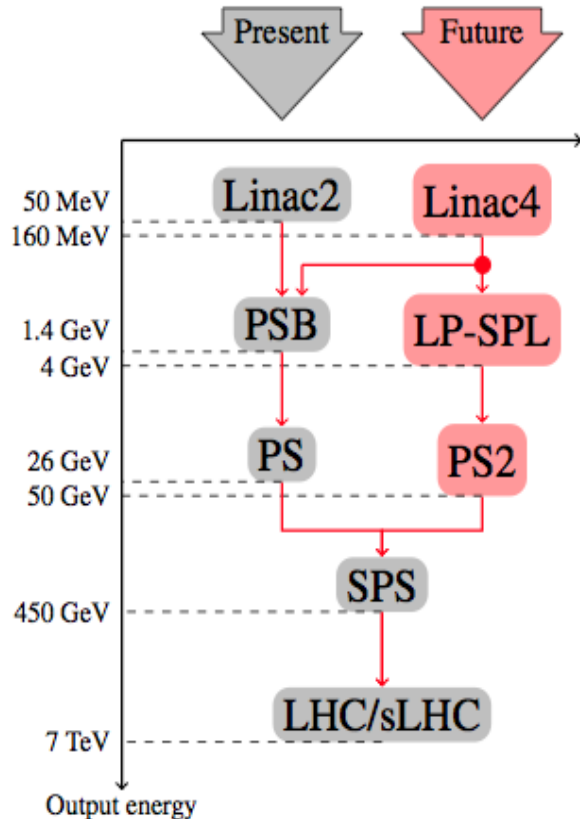
Processes at $\sqrt{s} \sim 0.212$ GeV e^+ on target

$e^+e^- \rightarrow e^+e^-(\gamma's)$ is the dominant process

- Babayaga for “large” angles and
- BBBrems for collinear (dominant $\sigma \sim 150$ mb, $\delta E/E < 2\%$)

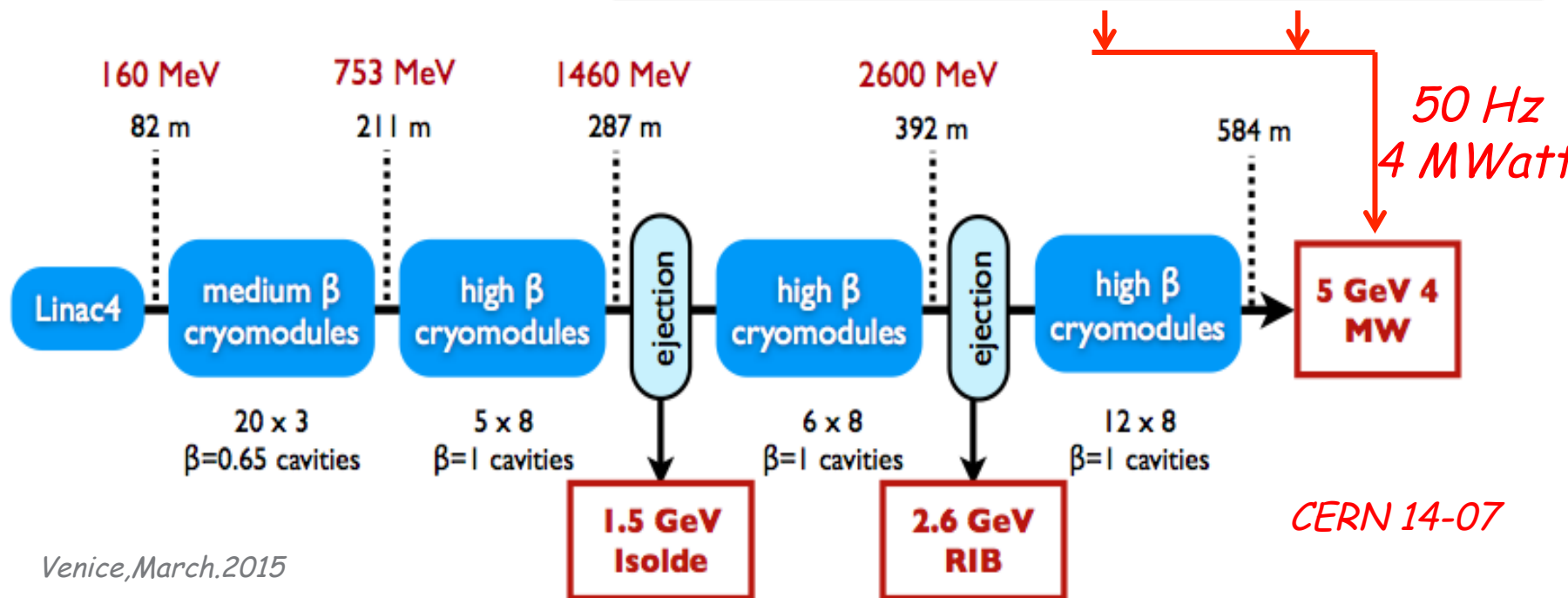


- A new LHC injector complex to increase the collider luminosity 10x with the High Luminosity LHC (HL-LHC)).
- Two accelerators (the LP-SPL and a new 50 GeV synchrotron, PS2) would replace the three existing ones (Linac2, the PSB, and the PS), with the injection of the SPS at 50 GeV,



- Layout of superconducting SPL with intermediate extractions.
- SPL design is very flexible and it can be adapted to the needs of many high-power proton beam applications.

Parameter	Units	HP-SPL		LP-SPL
		Low-current	High-current	
Energy	GeV	5	5	4
Beam power	MW	4	4	0.144
Repetition rate	Hz	50	50	2
Average pulse current	mA	20	40	20
Peak pulse current	mA	32	64	32
Source current	mA	40	80	40
Chopping ratio	%	62	62	62
Beam pulse length	ms	0.8	0.4	0.9
Protons per pulse	10^{14}	1.0	1.0	1.13



- A muon cooled Higgs factory can be easily housed within CERN
- The new 5 GeV Linac will provide at 50 c/s a multi MWatt H- beam with enough pions/muons to supply the muon factory.
- The basic additional accelerator structure will be the following:
 - Two additional small storage rings with $R \approx 50$ m will strip H- to a tight p bunch and compress the LP-SPL beam to a few ns.
 - Muons of both signs are focused in a axially symmetric $B = 20$ T field, reducing progressively pt with a horn and $B = 2$ T
 - A buncher and a rotator compresses muons to ≈ 250 MeV/c
 - Muon Cooling in 3D compresses emittances by a factor 106.
 - Bunches of about 2×10^{12} m^\pm are accelerated to 62.5 GeV
 - Muons are colliding in a SC storage ring of $R \approx 60$ m (about one half of the CERN-PS ,1/100 of LHC) where about 104 Higgs events/y are recorded for each of the experiments.

Staged Neutrino Factory and Muon Colliders main parameters

Neutrino Factory at intensity frontier

System	Parameters	Unit	nuSTORM	NuMAX Commissioning	NuMAX	NuMAX+
Performance	ν_e or ν_μ to detectors/year	-	3×10^{17}	4.9×10^{19}	1.8×10^{20}	5.0×10^{20}
	Stored μ^+ or μ^- /year	-	8×10^{17}	1.25×10^{20}	4.65×10^{20}	1.3×10^{21}
Detector	Far Detector:	Type	SuperBIND	MIND / Mag LAr	MIND / Mag LAr	MIND / Mag LAr
	Distance from Ring	km	1.9	1300	1300	1300
	Mass	kT	1.3	100 / 30	100 / 30	100 / 30
	Magnetic Field	T	2	0.5-2	0.5-2	0.5-2
	Near Detector:	Type	SuperBIND	Suite	Suite	Suite
	Distance from Ring	m	50	100	100	100
	Mass	kT	0.1	1	1	2.7
	Magnetic Field	T	Yes	Yes	Yes	Yes
Neutrino Ring	Ring Momentum	GeV/c	3.8	5	5	5
	Circumference (C)	m	480	737	737	737
	Straight section	m	184	281	281	281
	Number of bunches	-		60	60	60
	Charge per bunch	1×10^9		6.9	26	35
Acceleration	Initial Momentum	GeV/c	-	0.25	0.25	0.25
	Single-pass Linacs	GeV/c	-	1.0, 3.75	1.0, 3.75	1.0, 3.75
		MHz	-	325, 650	325, 650	325, 650
	Repetition	Hz	-	30	30	60
Cooling			No	No	Initial	Initial
Proton Driver	Proton Beam Power	MW	0.2	1	1	2.75
	Proton Beam	GeV	120	6.75	6.75	6.75
	Protons/year	1×10^{21}	0.1	9.2	9.2	25.4
	Repetition	Hz	0.75	15	15	15

Muon Collider at the energy frontier

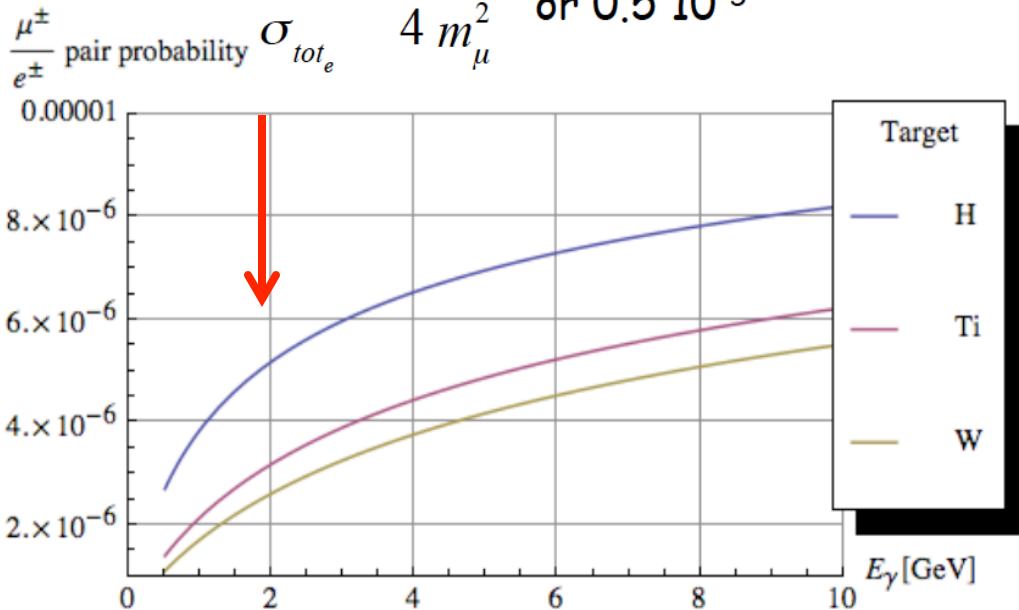
Parameter	Units	Higgs Factory		Top Threshold Options		Multi-TeV Baselines		Accounts for Site Radiation Mitigation
		Startup Operation	Production Operation	High Resolution	High Luminosity			
CoM Energy	TeV	0.126	0.126	0.35	0.35	1.5	3.0	6.0
Avg. Luminosity	$10^{34} \text{ cm}^{-2} \text{ s}^{-1}$	0.0017	0.008	0.07	0.6	1.25	4.4	12
Beam Energy Spread	%	0.003	0.004	0.01	0.1	0.1	0.1	0.1
Higgs* or Top* Production/ 10^7 sec		3,500*	13,500*	7,000*	60,000*	37,500*	200,000*	820,000*
Circumference	km	0.3	0.3	0.7	0.7	2.5	4.5	6
No. of IPs		1	1	1	1	2	2	2
Repetition Rate	Hz	30	15	15	15	15	12	6
β^*	cm	3.3	1.7	1.5	0.5	1 (0.5-2)	0.5 (0.3-3)	0.25
No. muons/bunch	10^{12}	2	4	4	3	2	2	2
No. bunches/beam		1	1	1	1	1	1	1
Norm. Trans. Emittance, ϵ_{TN}	$\pi \text{ mm-rad}$	0.4	0.2	0.2	0.05	0.025	0.025	0.025
Norm. Long. Emittance, ϵ_{LN}	$\pi \text{ mm-rad}$	1	1.5	1.5	10	70	70	70
Bunch Length, σ_z	cm	5.6	6.3	0.9	0.5	1	0.5	0.2
Proton Driver Power	MW	4 ¹	4	4	4	4	4	1.6
Cooling		6D no final		Full 6D				

Muon generation by GeV-scale Compton γ s

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Probability of creating $\mu^+\mu^-$ pairs as a function
of the incident photon energy

$$\frac{\sigma_{tot\mu}}{\sigma_{tot_e}} \approx \frac{1}{4} \frac{m_e^2}{m_\mu^2} \text{ or } 0.5 \cdot 10^{-5}$$



2 GeV γ beam	Pulsed Linac	ERL
e-beam energy [GeV]	36	11
Laser wavelength [μ m]	10	1
Bunch charge [nC]	10	1.5
Rep. rate [kHz]	0.2	20 / 200
Bunches per beam	250	
Average current [mA]	2	30 / 300
e-beam power [MW]	18	330 / 3300
e-to- γ convers. efficiency	3	0.33
γ -beam power [MW]	3	20 / 200
Total AC-to- γ efficiency	10%	20% / 75%
Peak $\mu^+\mu^-$ [per bunch]	10^6	$3 \cdot 10^4$
Average $\mu^+\mu^-$ [per second]	$5 \cdot 10^{10}$	$3 \cdot 10^{11} / 3 \cdot 10^{12}$

- Brightness 10^3 larger than with proton driver
- 10^3 too low with pulsed linac
- 10^2 flux increase with high current ERL
- Approaching intensities desired for NF (but train structure not favorable for collider luminosity, N^2 issue)