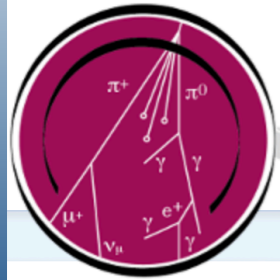


J- AND D-FACTORS DETERMINATION



BAM

WORKSHOP Barolo
Astroparticle Meeting
Sept 3-6, 2017



M. Valli

Istituto Nazionale di Fisica Nucleare

Sezione di Roma

ALSO SUPPORTED BY:



HOW MUCH PRECISELY CAN WE DETERMINE J IN DSPHS?

MNRAS 453 (2015) 849-867

2015

Bonnivard, V. et al.

Quantity	Profile	Parameter	Prior range
DM density	'Einasto' equation (5)	$\log_{10}(\rho_{-2}/M_{\odot} \text{ kpc}^{-3})$	[5, 13]
		$\log_{10}(r_{-2}/\text{kpc})$	$[\log_{10}(r_s^*), 1]$
		α	[0.12, 1]
Anisotropy	'Baes & van Hese' equation (6)	β_0	[-9, 1]
		β_{∞}	[-9, 1]
		$\log_{10}(r_a)$	[-3, 1]
		η	[0.1, 4]

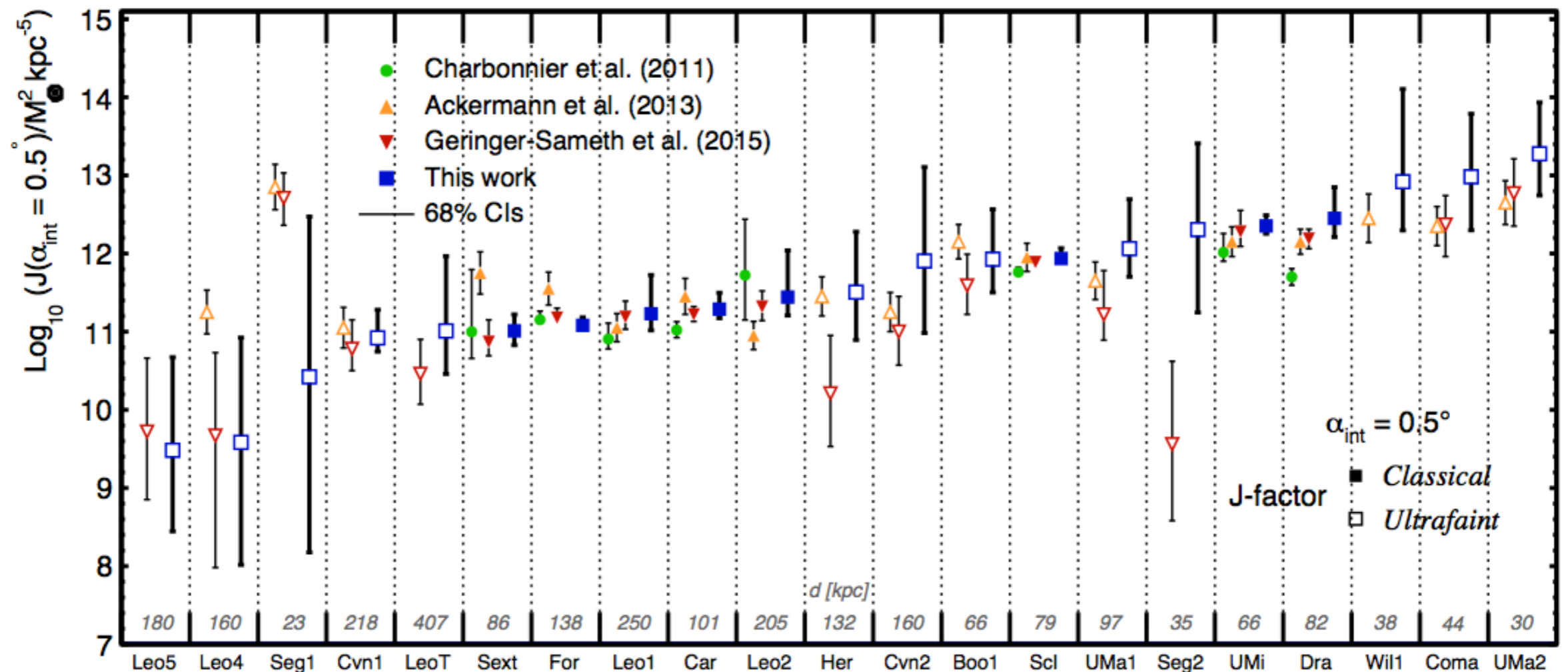
Einasto DM profile

Hernquist-Zhao stellar profile

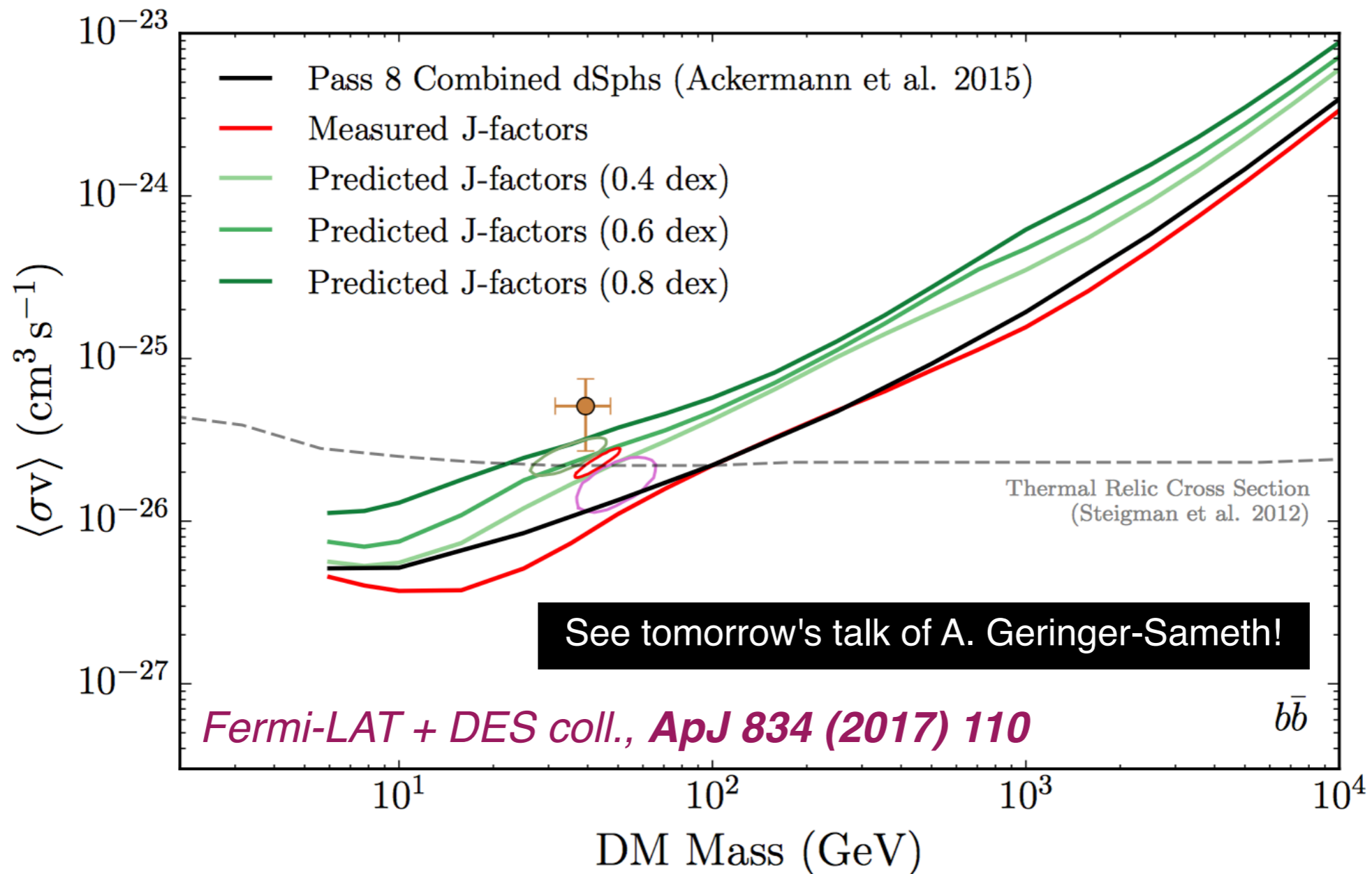
Baes & van Hese anisotropy

$$\beta(r) = \frac{\beta_0 + \beta_{\infty}(r/r_a)^{\eta}}{1 + (r/r_a)^{\eta}}$$

+ phase-space positivity



In light of DES discovery of new Ultra-faint dwarfs, most recent reappraisal of DM particle constraints from gamma-ray observation of MW dwarf satellites:



NOTE: the “measured” J-factors from *Geringer-Sameth et al. '15* include Ultra-faints with (somewhat) smaller errors than what has been found by *Bonnivard et al. '15*. Triaxial systematics not considered!

ROOM FOR MORE CONSERVATIVE / RELIABLE LIMITS! (8 CLASSICALS + Cvn I)

Possible challenges/subtleties even in study of the 8 Classics!

M. Irwin & D. Hatzidimitriou

Different stellar profiles may fit adequately well surface brightness data!

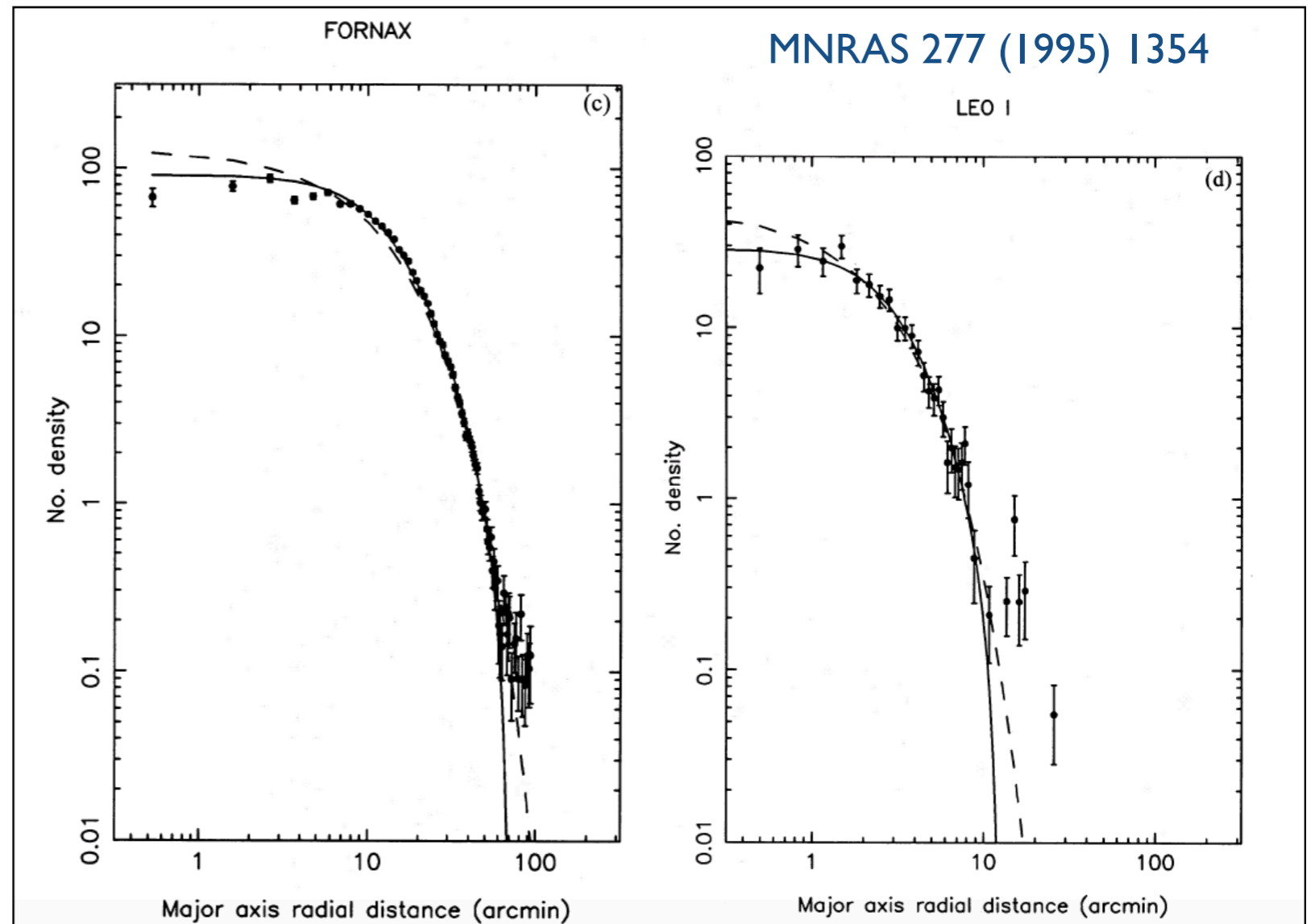
2-PARAMETER MODELS

Plummer, Exponential

> 2-PARAMETER MODELS

King, Sérsic,
Hernquist-Zhao

Slight preference for cored star profiles in the '95 photometric compilation for MW Classics.



URSA MINOR

\mathcal{D} [kpc]	66 ± 3	77 ± 4	76 ± 3
$R_{1/2}$ [kpc]	0.280 ± 15	0.445 ± 44	0.181 ± 27
adopted, e.g., in:	Walker et al. '09	Wolf et al. '10	Geringer-Sameth et al. '15

J (D) -FACTOR DETERMINATION DEPENDS ON DISTANCE + PHOTOMETRIC DATA!

NOTE: systematics present also in $V_{1/2}$ vs $r_{1/2}$ plot of the Too-Big-To-Fail.

Possible challenges/subtleties even in study of the 8 Classics!

—> binning of kinematic data may introduce some bias also in the case of the Classics.

Charbonnier, A. et al., MNRAS 418 (2011) 1526

$$-2 \ln \mathcal{L} = \sum_i^{N_*} \frac{\left(v_{los}^{(obs)}(R_i) - \overline{v_{los}} \right)^2}{\left(\delta v_{los}^{(obs)}(R_i) \right)^2 + \left(\sigma_{los}^{(pred)}(R_i) \right)^2}$$

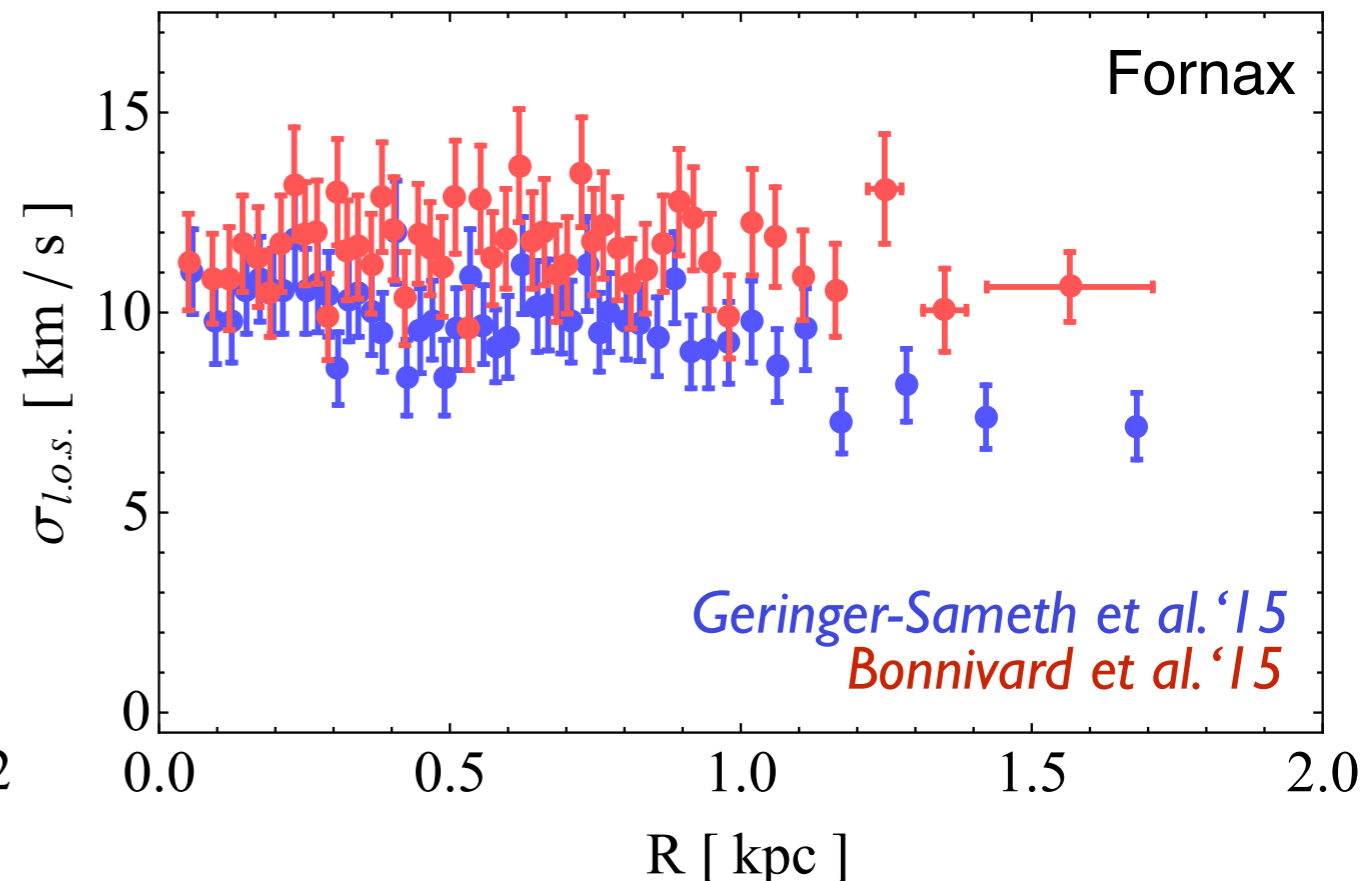
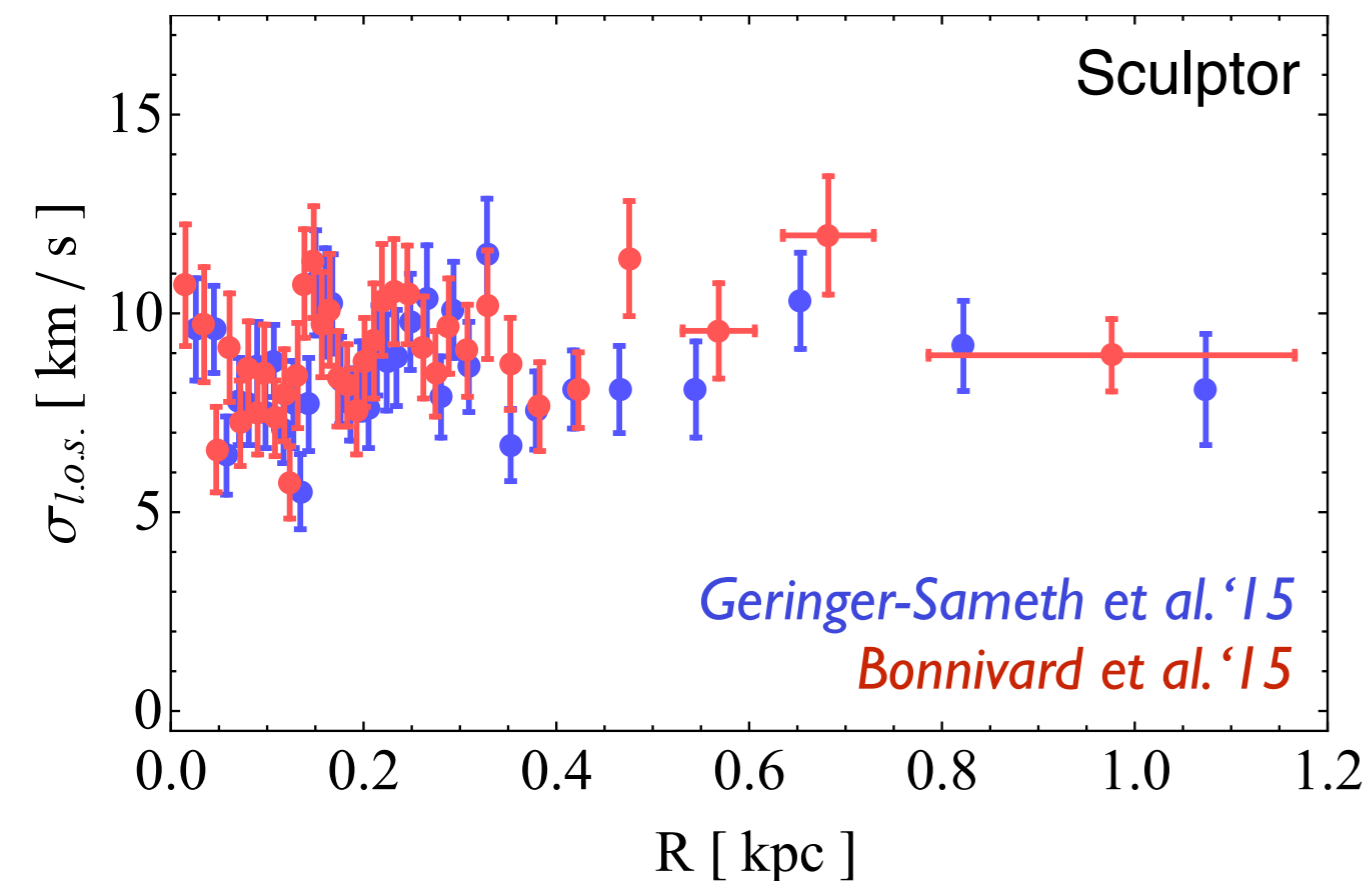
TEST STATISTICS FOR AN UNBINNED ANALYSIS!
 (see, e.g., *Battaglia, G. et al., New Astron. Rev. 57 (2013) 52*)



UNBINNED ANALYSIS ASSUMES GAUSSIAN DISTRIBUTED L.O.S. VELOCITIES ...

l.o.s. kurtosis may provide non-trivial info! See: *Lokas '09, Richardson & Fairbairn '13*

BEYOND TEST STATISTICS: *treatment of membership probability/contaminants seems to represent a non-negligible source of systematics even for the Classical dwarfs!*

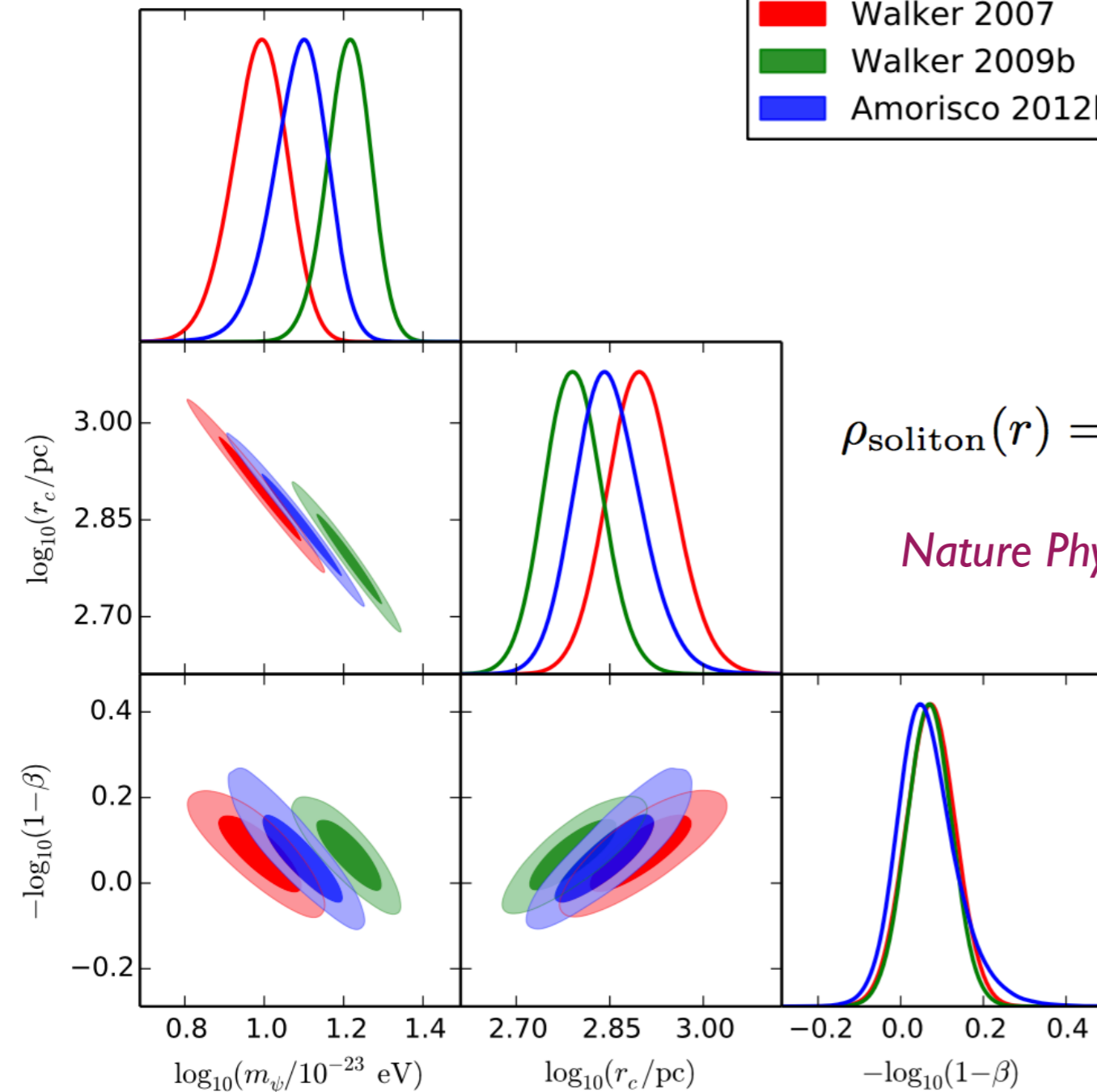
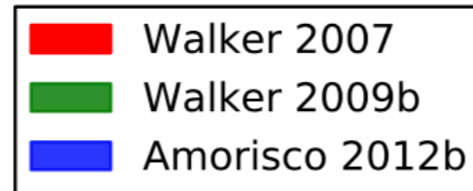
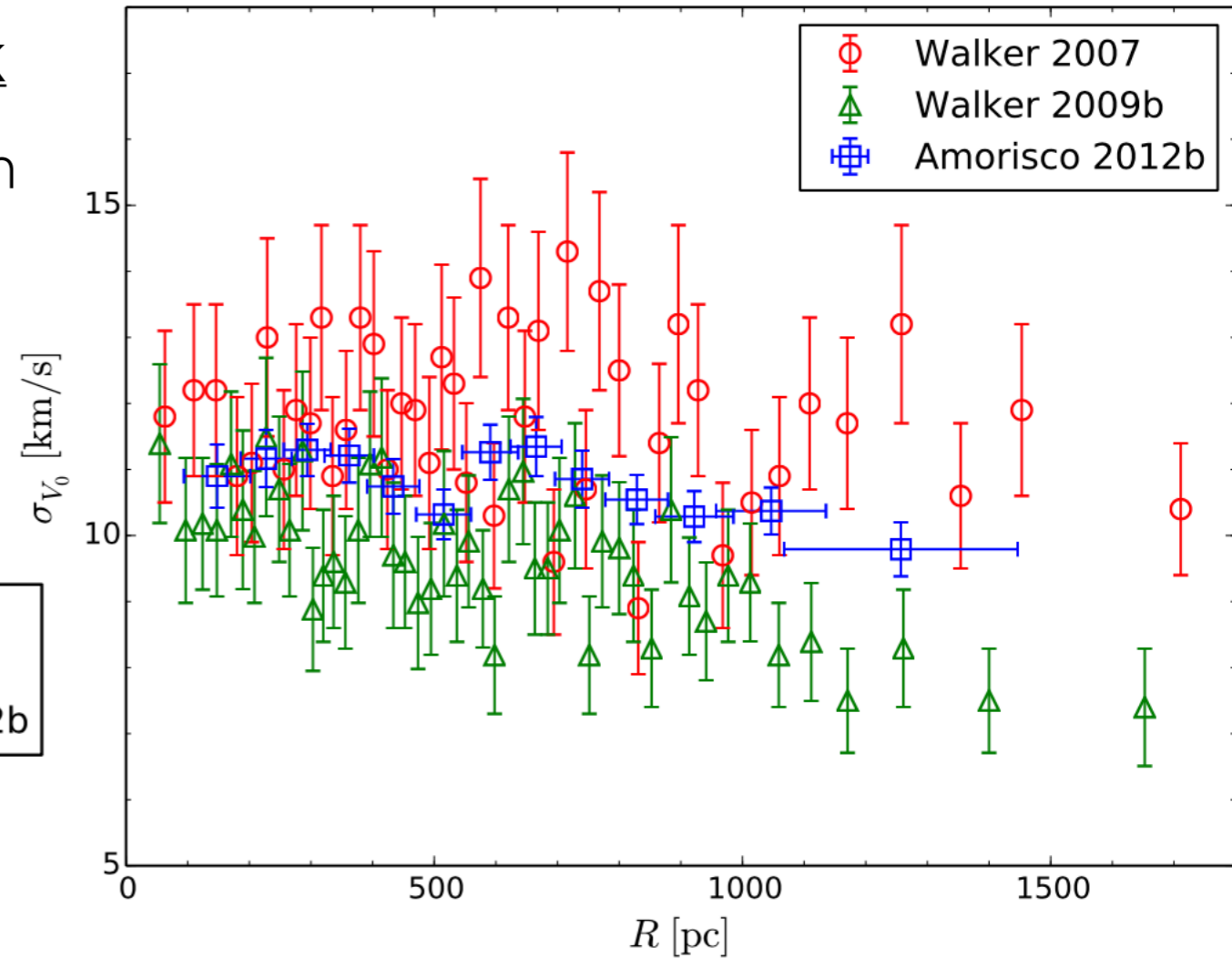


AN EXAMPLE ON THIS SYSTEMATICS AT WORK

Spherical Jeans analysis with axion-like soliton halo profile of Fuzzy / Wave Dark Matter.

MNRAS 468 (2017) 1338-1348, Schive, H.Y. et al.

See tomorrow's talk of A. Gonzalez-Morales!



$$\rho_{\text{soliton}}(r) = \frac{1.9 (m_{\psi}/10^{-23} \text{ eV})^{-2} (r_c/\text{pc})^{-4}}{[1 + 9.1 \times 10^{-2} (r/r_c)^2]^8} 10^{12} M_{\odot} \text{ pc}^{-3}$$

Nature Phys. 10 (2014) 496, PRL 113 (2014) no.26, 261302, Schive, H.Y. et al.

Galaxy	$\log_{10}[m_{\psi}/10^{-23} \text{ eV}]$
Fornax	$1.21^{+0.06(+0.10)}_{-0.05(-0.11)}$
	$0.99^{+0.07(+0.13)}_{-0.07(-0.15)}$

Possible challenges/subtleties even in study of the 8 Classics!

$$0.1 \lesssim \epsilon \equiv 1 - a/b \lesssim 0.5$$

$a := I$ semi-minor axis
 $b := I$ semi-major axis

“Spheroidal” stems from the “small” stellar ellipticity of these 8 galaxies.

Systematics due to a more realistic triaxial-halo shape seems non-negligible, even for Classics.

MNRAS 453 (2015), Bonnivard, V. et al.

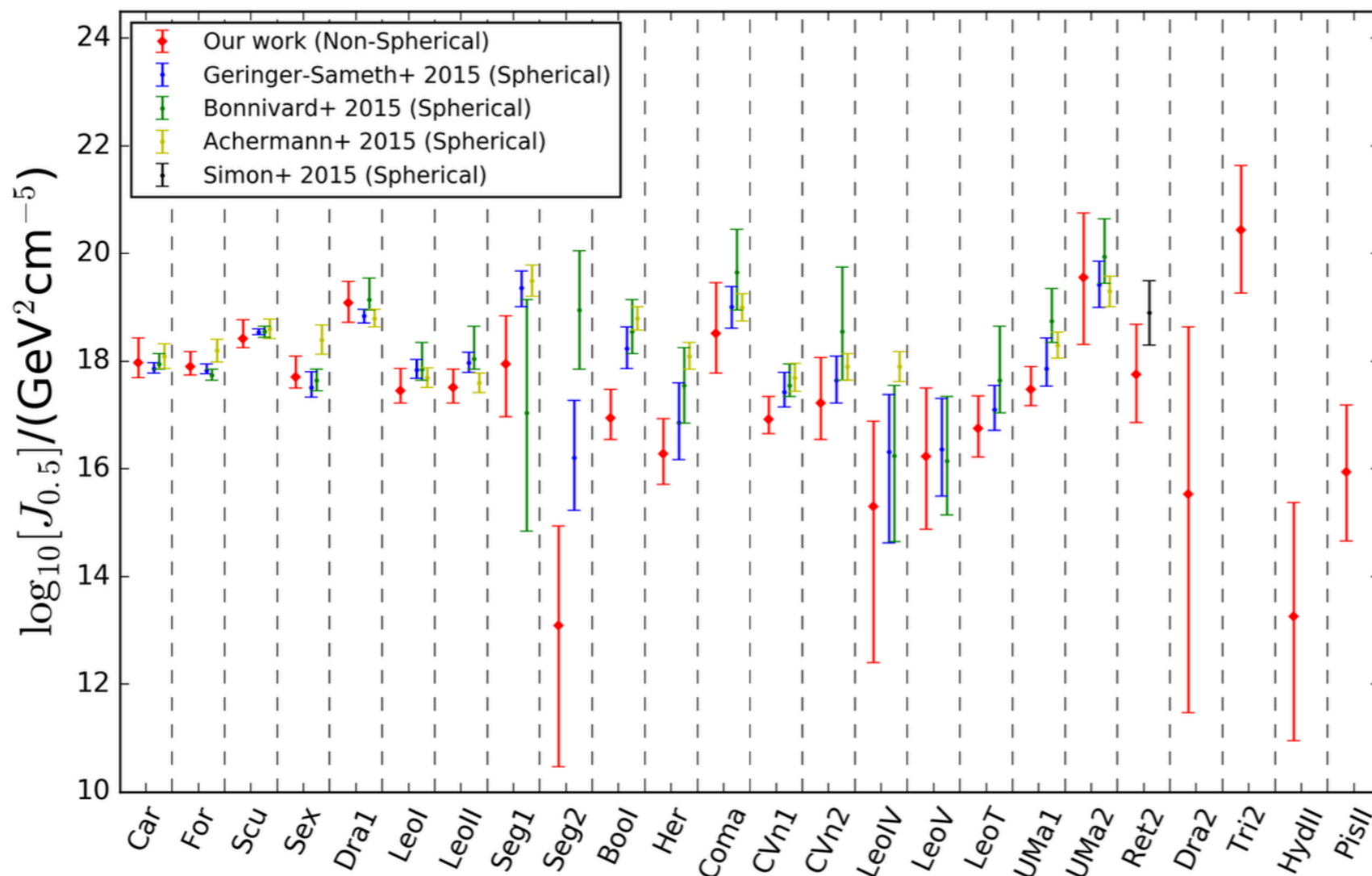
Axi-symmetric Jeans analysis (see *MNRAS 390 (2008) 71, M.Cappellari*) applied in this context highlights **important systematics on Ultra-faint dwarfs** (quite milder effects on Classics).

MNRAS 461 (2016) 2914, Hayashi, K. et al.

ApJ 755 (2012) 145,
ApJ 810 (2015) 22,
 Hayashi & Chiba

See also recent discussion in:
PRD 95 (2017) no.12, 123012
 Klop, N. et al.

Geometric + kinematic corrections to J_s & D_s from “flattening effects” turn out to be small for 8 Classics in:
PRD 94 (2016) no.6, 063521,
 Sanders, J.L. et al.



Mass-Anisotropy degeneracy: An elephant in the room ...

Q: Departures of orders of magnitude from the results presented so far?



Marginalization over an unknown function, with poor theoretical and observational guidance (differently from stellar & DM profiles) ...

I) SEVERAL PARAMETERIZATIONS FROM PHASE-SPACE DENSITY MODELING

$$\beta(r) = \frac{r^2}{r^2 + r_\beta^2} \quad \text{Osipkov '79, Merritt '85} \quad \rightarrow \quad \beta(r) = \frac{\beta_0 + \beta_\infty (r/r_\beta)^\eta}{1 + (r/r_\beta)^\eta} \quad \text{Baes and Van Hese '07}$$

AND FEW THEORETICAL CONSTRAINTS (An, Baes and Van Hese '12)

E.g.: Anisotropy $\leq 1/2$ of Stellar Density Log-Slope (An & Evans '06+ Ciotti & Morganti '10)

II) NO FINAL MESSAGE FROM RECENT N-BODY SIMULATIONS

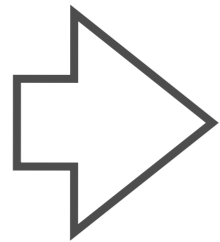
FIRE (El-Badry et al. '17) finds anisotropies well-described by Osipkov-Merritt model

APOSTLE (Campbell et al. '17) leaves room also for tangential bias in the outer region

Next-gen observational programs (see, e.g., **GAIA**, but also **HST astrometry initiative** and proposals such as **Theia**) may reach **sensitivity to** measure **dwarf proper stellar motion**.

dSphs := GOOD LABORATORIES FOR DM PARTICLE LIMITS?

The *impact of mass-anisotropy degeneracy* on the derived DM profile may be the most dramatic systematics ... *are departures of orders of magnitude from outcome of MCMC analyses discussed so far possible?!*



WHAT ABOUT INVESTIGATING THE EFFECT OF THIS SYSTEMATICS WITH A MORE DIRECT APPROACH?

WHAT MAY INDEED BE INTERESTING TO BE ASSESSED ...

$$\phi_{\gamma, \nu, \dots}^{(\text{DM})} \propto \frac{\langle \sigma v \rangle \times J}{(\tau \times D)} \quad \text{DM LIMITS SCALE INVERSELY WITH J}$$

... IS THE “MINIMAL” J-FACTOR VS ANISOTROPY, namely the minimum J-value — statistically allowed by dwarf stellar kinematics — yielding the weakest upper-bound in relation to this systematics.



WE CAN EXPLOIT ABEL INVERSION TO TEST THIS!

$$\hat{f}(y) = \mathbf{A}^{-1}[f(x)] \equiv -\frac{1}{\pi} \int_y^{\infty} \frac{dx}{\sqrt{x-y}} f(x)$$

E.g.: \mathbf{A}^{-1} [surface brightness] \rightarrow stellar density profile

$$\mathbf{A}^{-1} [I (R^2)] \qquad \hat{I} (r^2)$$



WE CAN EXPLOIT ABEL INVERSION TO TEST THIS!

$$\hat{f}(y) = \mathbf{A}^{-1}[f(x)] \equiv -\frac{1}{\pi} \int_y^\infty \frac{dx}{\sqrt{x-y}} f(x)$$

E.g.: \mathbf{A}^{-1} [surface brightness] \rightarrow stellar density profile

\Rightarrow $\hat{P}(r^2) = \mathbf{A}^{-1}[P(R^2) \equiv I \sigma_{los}^2]$ FUNCTION OF L.O.S. OBSERVABLES ONLY

MASS PROFILE FROM INVERSION OF SPHERICAL JEANS EQUATION:

$$\mathcal{M}_\beta(r) = \frac{r^2}{G_N \hat{I}(r)} \left\{ -\frac{d\hat{P}}{dr} [1 - a_\beta(r)] - \frac{a_\beta(r) b_\beta(r)}{r} \int_r^\infty dr' \mathcal{H}_\beta(r, r') \frac{d\hat{P}}{dr'} \right\}$$

$$a_\beta \equiv -\beta/(1 - \beta) \quad , \quad b_\beta(r) \equiv 3 - a_\beta + \frac{d \log a_\beta}{d \log r} \quad ,$$

See, also, previous derivations in:

MNRAS 401(2010), Mamon, G. & Boué, G.,

MNRAS 406(2010), J.Wolf et al.

$$\mathcal{H}_\beta(r, r') \equiv \exp \left(\int_r^{r'} dr'' \frac{a_\beta(r'')}{r''} \right) .$$



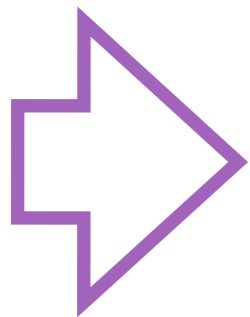
INVERTED SPHERICAL JEANS ANALYSIS IN A NUTSHELL

$$\sigma_{los}(\mathcal{M}, \beta, I) \Rightarrow \mathcal{M}(\beta, \sigma_{los}, I)$$

Some **physical conditions** must supplement the inversion formula.

$$i) \quad \mathcal{M}_\beta(r) > 0, \quad \forall r > 0$$

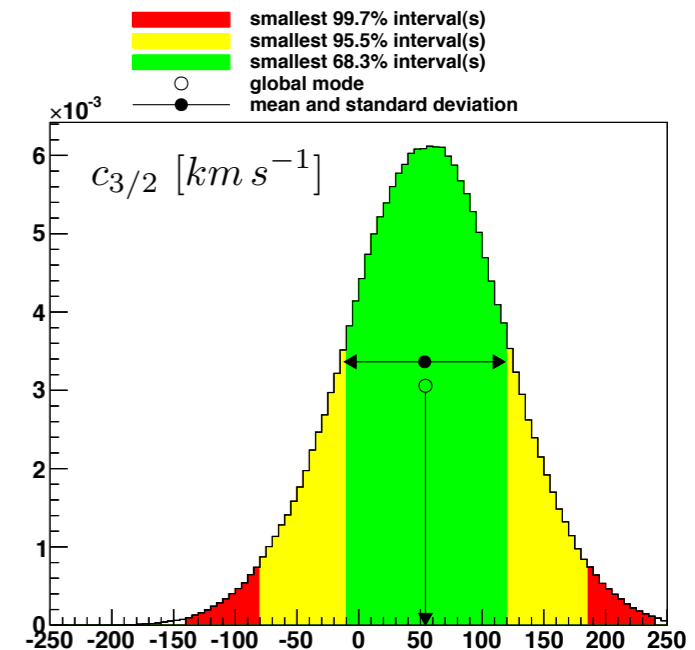
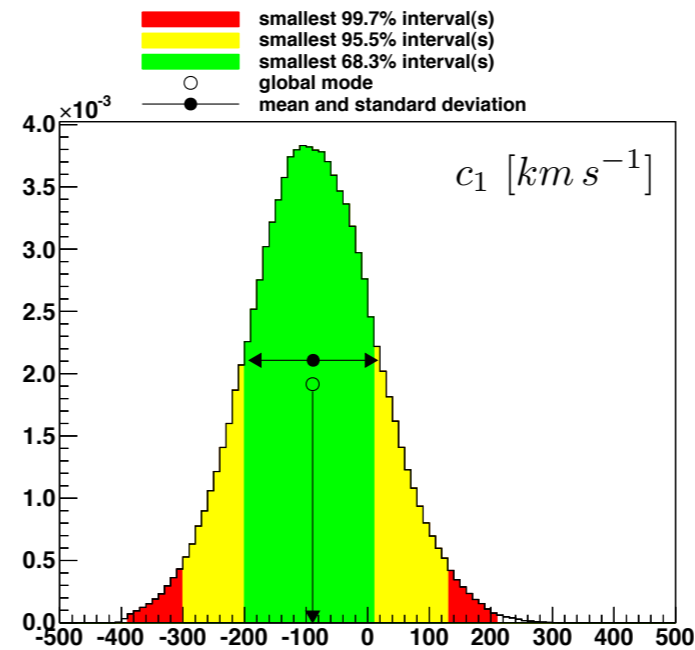
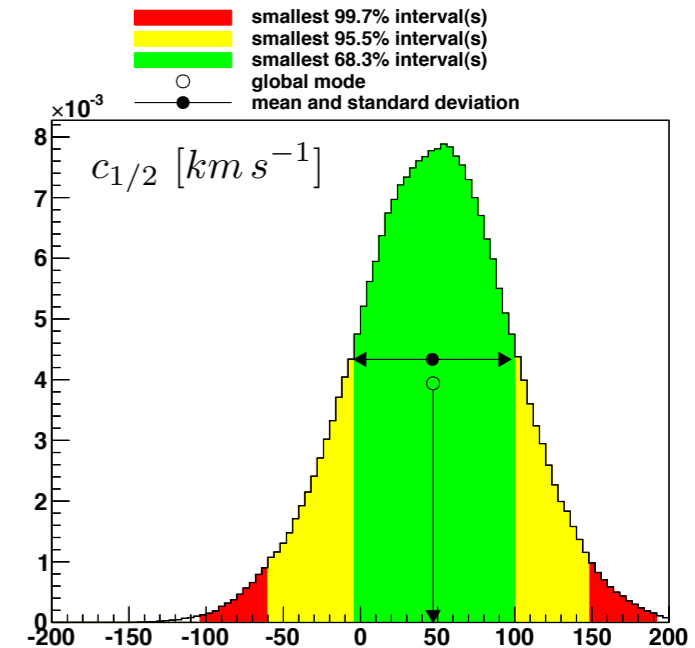
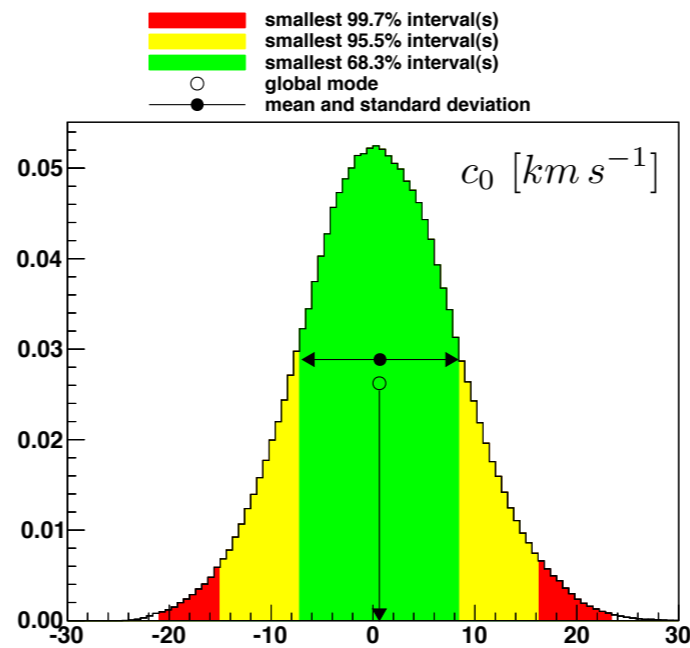
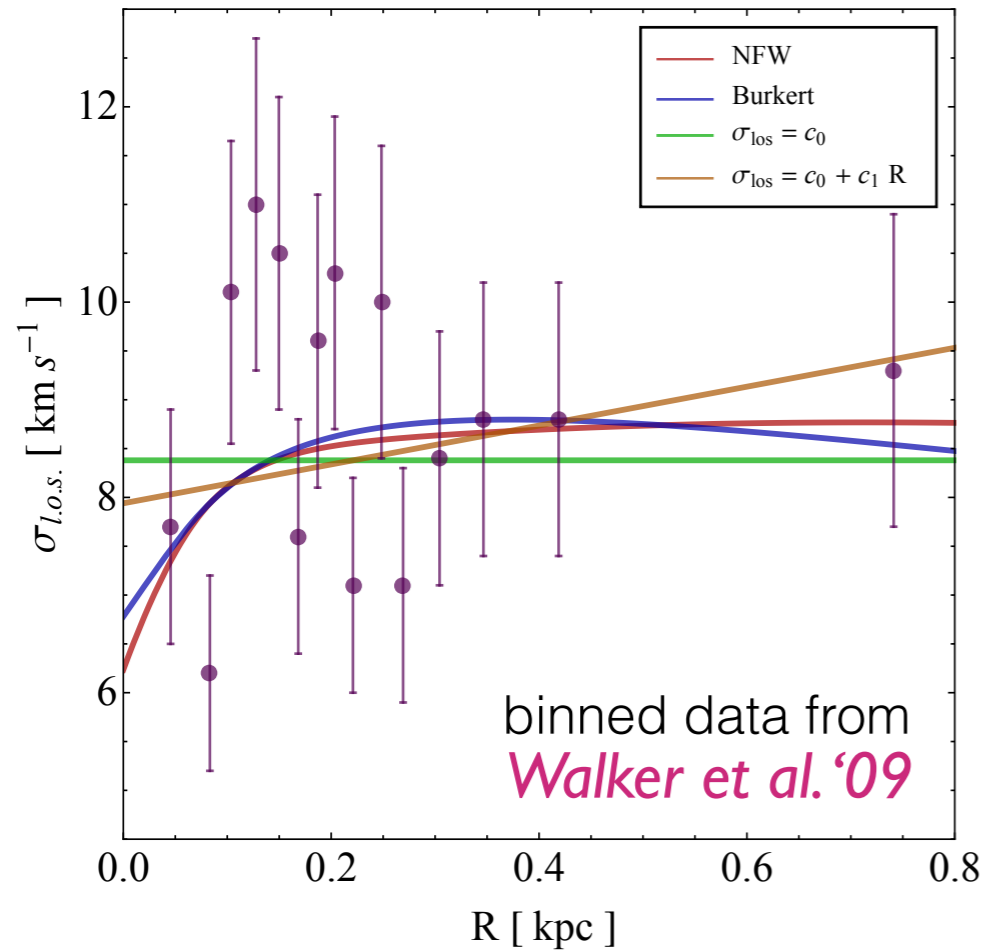
$$ii) \quad \mathcal{M}_\beta(r') \geq \mathcal{M}_\beta(r), \quad \forall r' \geq r.$$



$$\rho_\beta(r) = \frac{1}{4\pi r^2} \frac{d\mathcal{M}_\beta}{dr} \quad \text{DENSITY PROFILE FOR SPHERICAL SYSTEMS}$$

$$iii) \quad \rho_\beta(r') \leq \rho_\beta(r), \quad \forall r' \geq r.$$

THE STUDY CASE OF URSA MINOR



$$\sigma_{los}(R) = \begin{cases} c_0 + c_1 R \\ \sum_{i=0}^3 c_{\frac{i}{2}} R^{\frac{i}{2}} \end{cases}$$

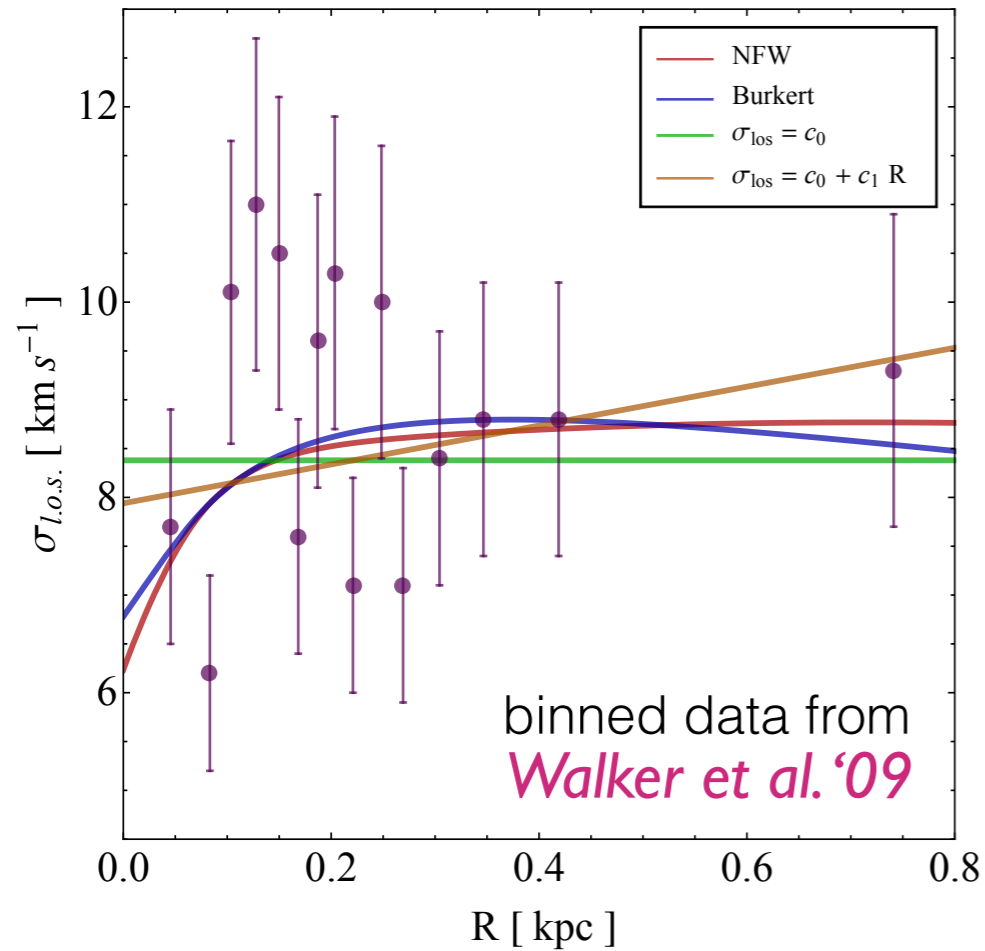
+ Plummer surface brightness

MCMC with



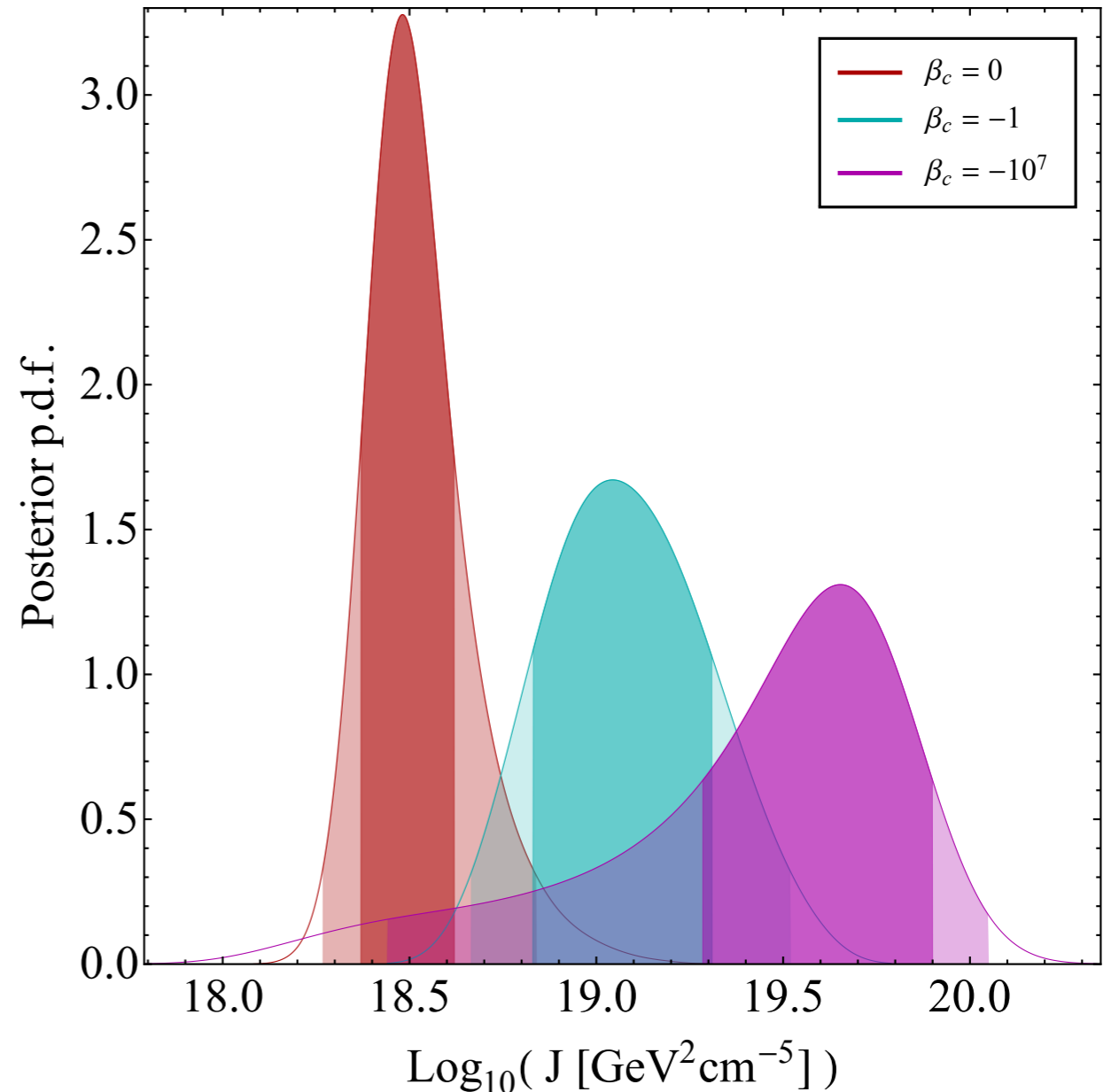
Bayesian
Analysis
Toolkit

THE STUDY CASE OF URSA MINOR



AT EVERY STEP IN THE MCMC, CHECK THE PHYSICAL CONDITIONS. IF SATISFIED:

$$\mathcal{M}_\beta \Rightarrow \rho_\beta \Rightarrow J_\beta$$



$$\sigma_{los}(R) = \begin{cases} c_0 + c_1 R \\ \sum_{i=0}^3 c_{\frac{i}{2}} R^{\frac{i}{2}} \end{cases}$$

+ Plummer surface brightness

THE STUDY CASE OF URSA MINOR

CONSERVATIVE WORKING ASSUMPTION

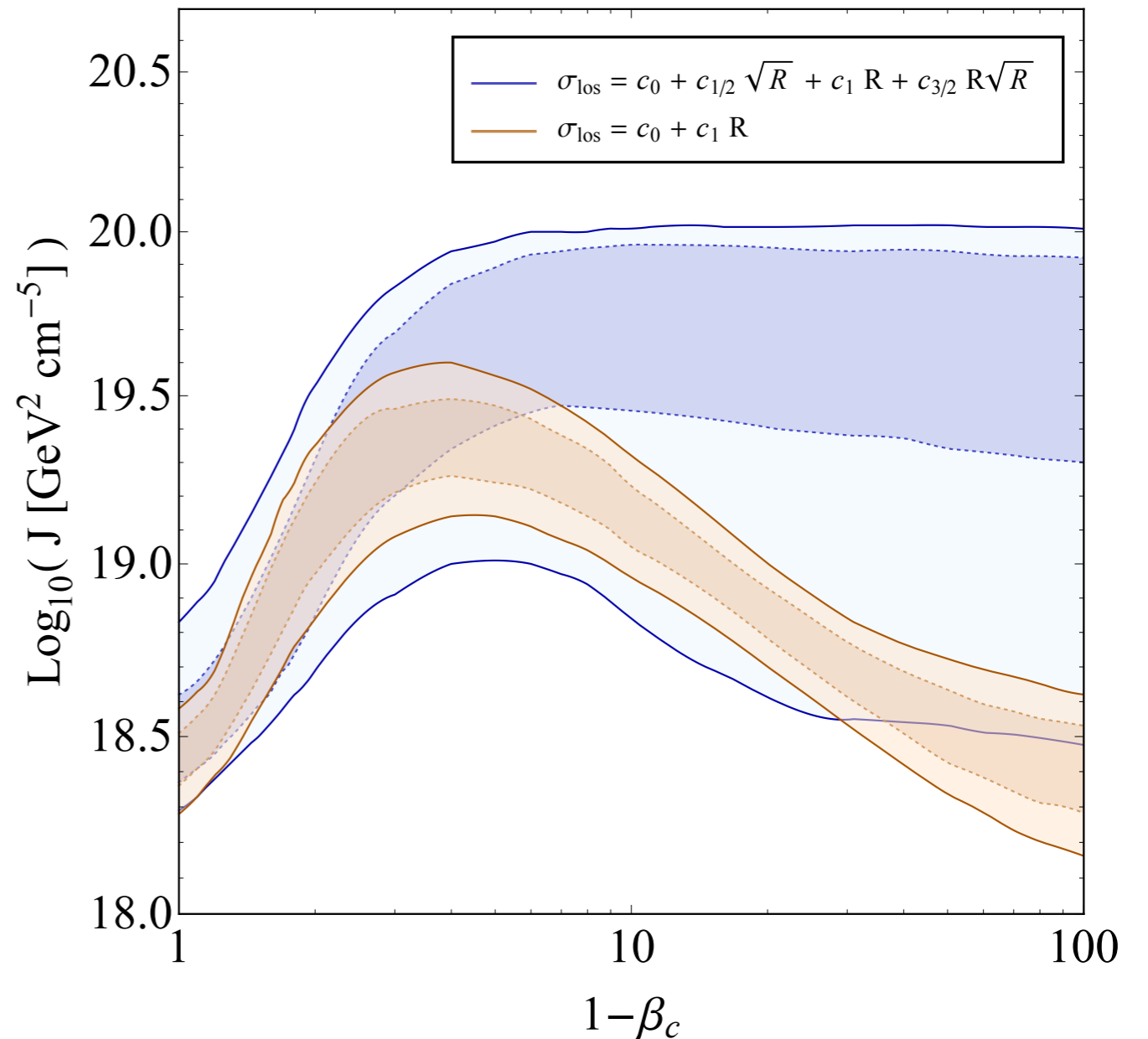
OUR JEANS INVERSION APPROACH IS INTIMATELY CONNECTED TO DATA.



INNER DENSITY (I.E. BELOW FIRST BINNED RADIUS OF DATA) ASSUMED TO BE CONSTANT IN THE EVALUATION OF THE L.O.S. INTEGRAL OF J.

$$\sigma_{los}(R) = \begin{cases} c_0 + c_1 R \\ \sum_{i=0}^3 c_{\frac{i}{2}} R^{\frac{i}{2}} \end{cases}$$

+ Plummer surface brightness



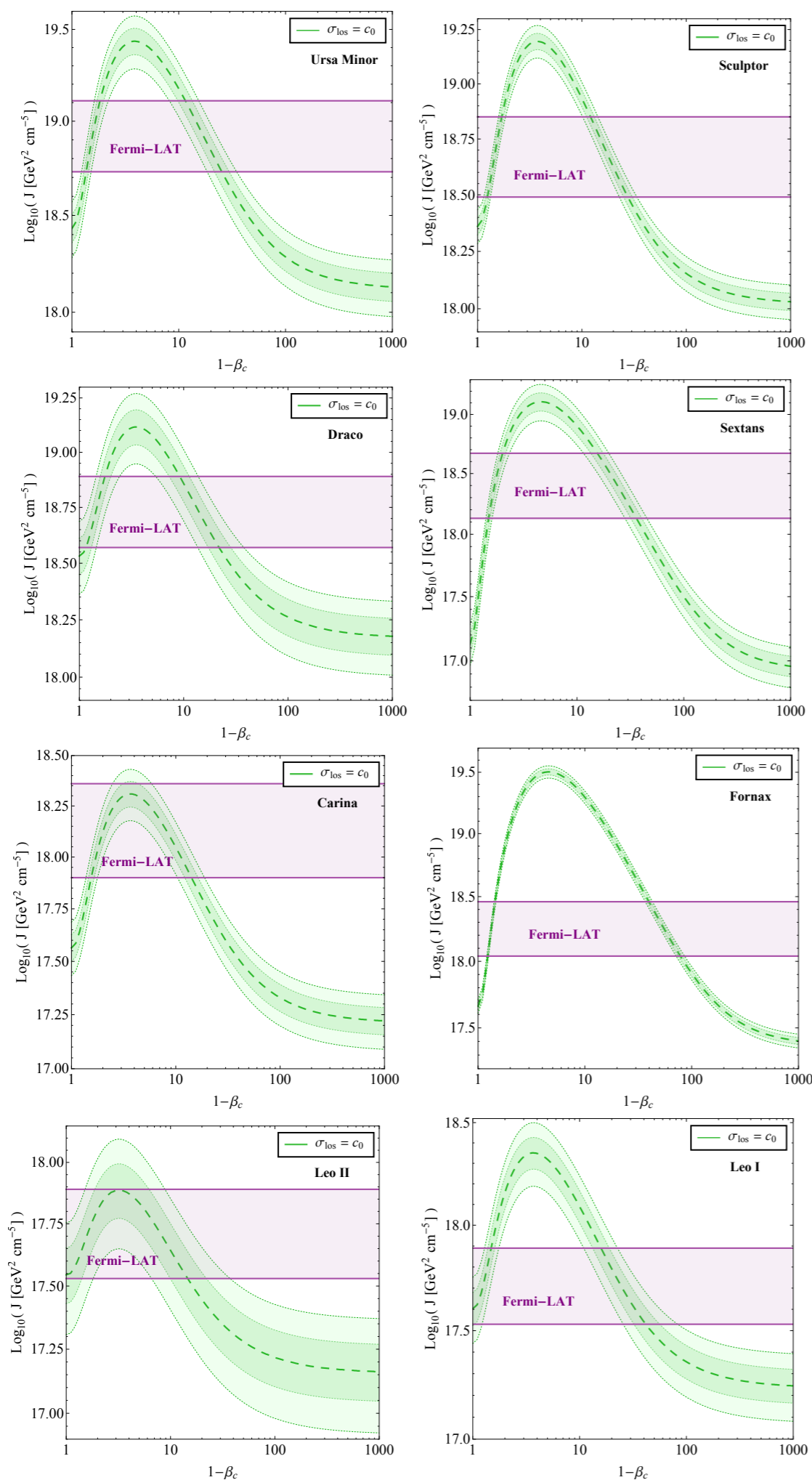
MINIMAL J OBTAINED FOR $\sigma_{LOS} = c_0$ IN THE LIMIT OF STELLAR CIRCULAR MOTION
→ extreme “academic case” under scrutiny
(more details in the backup)



RADICAL CONSERVATIVE
APPROACH CONSIDERED.

AT MOST, FACTOR ~ 4 OF
DIFFERENCE ON MINIMAL J
WRT OTHER ANALYSES.

$X =$ *Ackermann et al.*'13 , *Bonnivard et al.*'15



Classical dSph	$\min J_{@2\sigma}^{(X)} / \min J_{@2\sigma}$	
Ursa Minor	3.80	3.76
Sculptor	2.36	2.64
Draco	2.59	3.36
Sextans	12.88	1.56
Carina	3.94	3.98
Fornax	3.34	1.81
Leo II	2.70	1.43
Leo I	1.91	2.76

Classicals := DM astro-labs that leave **room**
for robust limits in indirect DM searches!

BEYOND THE STANDARD LORE — *J* & *PHASE-SPACE* —

When “particle” & “astro” do not naively factorize anymore ...

Role of velocity dependence in DM phenomenology may be extremely important.

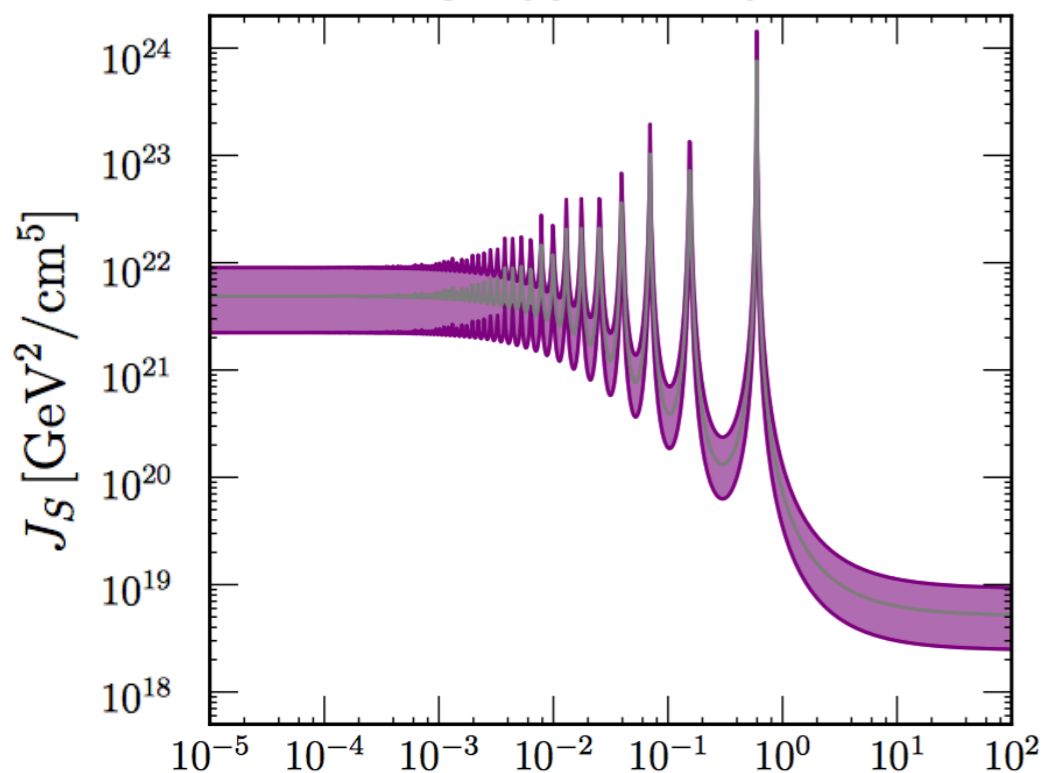
See previous talk by Torsten B.!

—> Sommerfeld-enhanced J-factors & dSphs:

Phys.Rev. D95 (2017) 123008, Boddy, K. et al. (See also: *JCAP 1309 (2013) 005, Ferrer & Hunter*)

$$J_S(\Delta\Omega) \equiv \int_{\Delta\Omega} d\Omega \int d\ell \int d^3v_1 f(r(\ell, \Omega), \vec{v}_1) \int d^3v_2 f(r(\ell, \Omega), \vec{v}_2) S(|\vec{v}_1 - \vec{v}_2|/2)$$

Ursa Minor



$$\epsilon_\phi \equiv \frac{m_\phi}{\alpha_X m_X}$$

Spherical symmetry + isotropy in order to apply Eddington’s formula for both DM & stars.

$$f_{DM, \star}(\epsilon) = \frac{1}{\sqrt{8\pi^2}} \int_\epsilon^0 \frac{d^2 \rho_{DM, \star}}{d\psi^2} \frac{d\psi}{\sqrt{\epsilon - \psi}}$$

Relative potential assumes a NFW profile, while stellar profile matched to Plummer.

Error band obtained using mass-concentration relation from N-body + stellar kinematics:

$$\langle \sigma_{los}^2 \rangle \simeq 3 \frac{\int \langle \sigma_\star^2 \rangle \rho_\star r^2 dr}{\int \rho_\star r^2 dr} = 3 \frac{\int \frac{\int f_\star v^4 dv}{\int f_\star v^2 dv} \rho_\star r^2 dr}{\int \rho_\star r^2 dr}$$

BEYOND THE STANDARD LORE — *J* & *PHASE-SPACE* —

When “particle” & “astro” do not naively factorize anymore ...

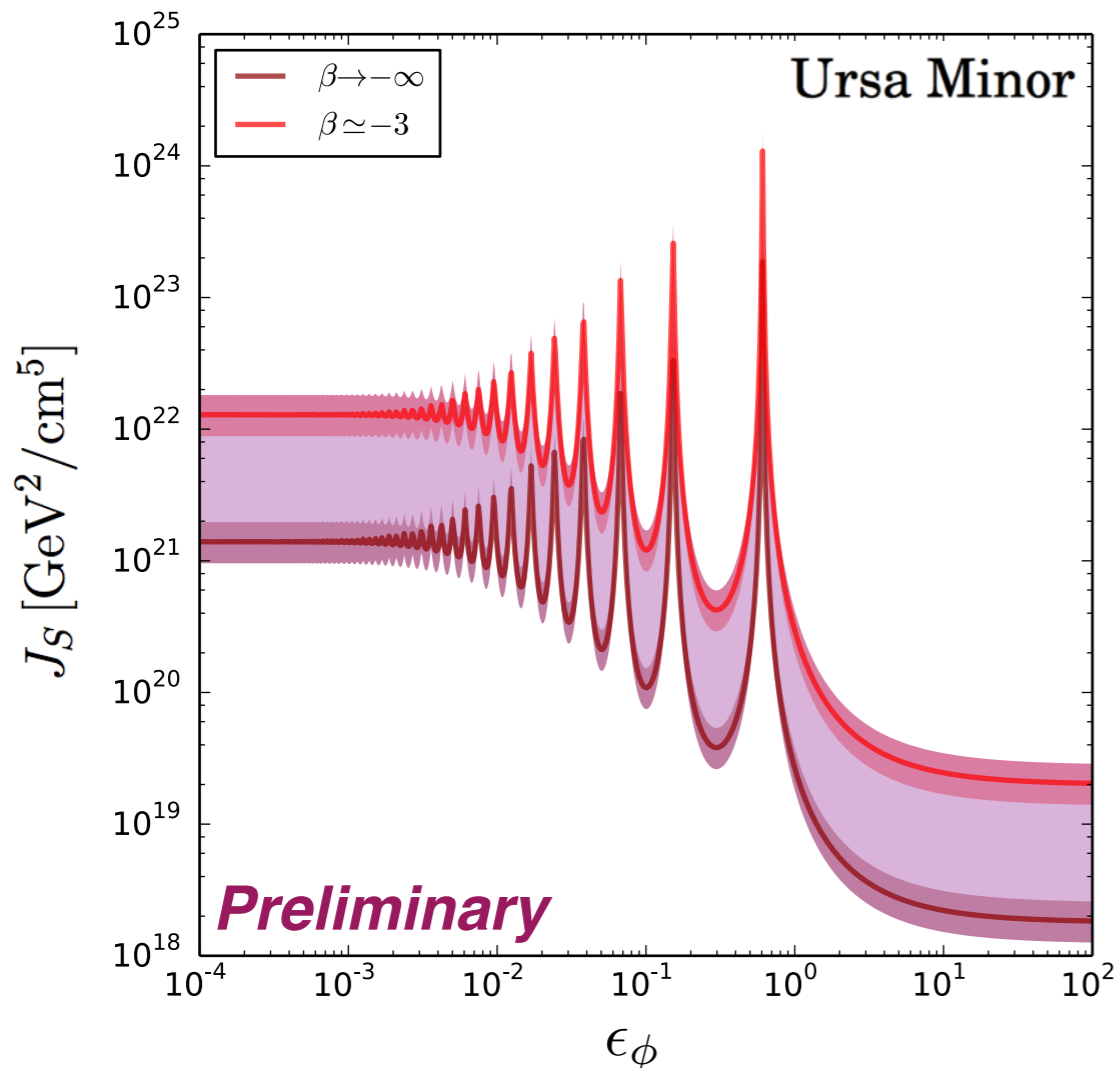
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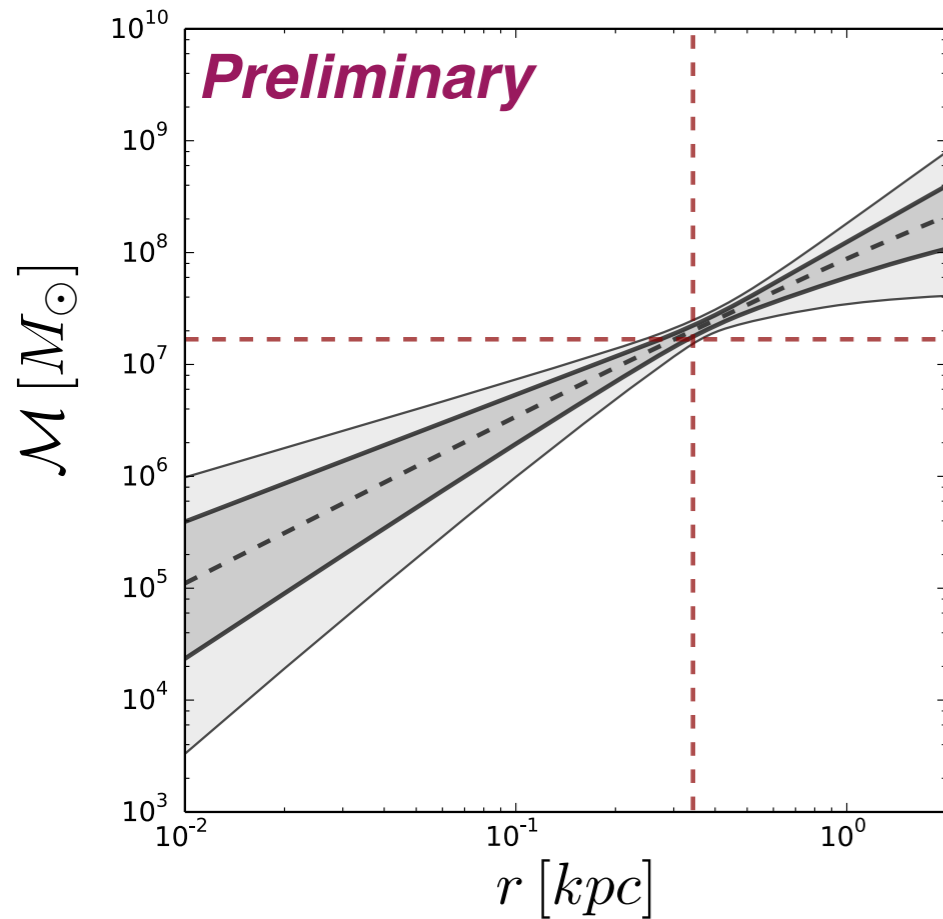
Isotropy for DM particles + spherical symmetry

$$f_{\beta}^{(DM)}(\epsilon) = \frac{1}{\sqrt{8\pi^2}} \int_{\epsilon}^0 \frac{d^2\rho_{\beta}}{d\psi^2} \frac{d\psi}{\sqrt{\epsilon - \psi}}$$

We can join the Jeans inversion formalism to the Eddington’s formula in order to study DM phase-space distribution in terms of the fit to l.o.s. observables!

work in progress,
M. Petac, P.Ullio & M.V.

BEYOND THE STANDARD LORE — DM HALO ESTIMATORS —



IF $\gamma_\beta, \gamma_{\sigma_r^2}$ PHENOMENOLOGICALLY NEGLIGIBLE:

$$\mathcal{M}_\beta(r) - \mathcal{M}_{\beta=0}(r) \simeq \frac{\beta(r) r \sigma_r^2(r)}{G_N} (\gamma_{\hat{I}}(r) - 3)$$

THEN, THE MASS ESTIMATOR IS EXPECTED AT:

$$r_* : \gamma_{\hat{I}}(r_*) = 3 \Rightarrow r_* = \sqrt{3/2} R_{1/2} \simeq r_{1/2}$$

$$\mathcal{M}(r_*) \simeq \mathcal{M}_{\beta=0}(r_*) = \gamma_{\hat{P}}(r_*) \frac{r_* \hat{P}(r_*)}{G_N \hat{I}(r_*)} \simeq 3 \frac{r_*}{G_N} \langle \sigma_{los}^2 \rangle$$

6 parameter MCMC for Ursa Minor

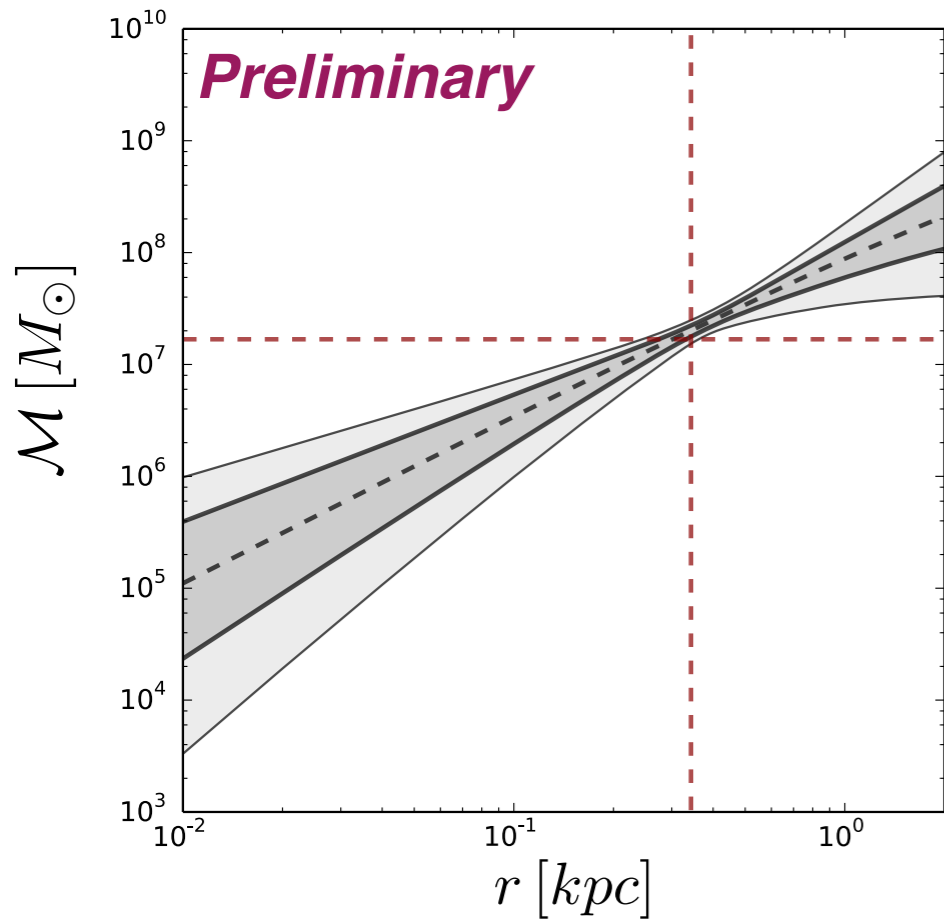
(fit on binned kinematic data)

- Plummer stellar model ($R_{1/2}$ kept fixed)
- Constant orbital anisotropy (1 param) \rightarrow largest range possible: $0 \leq a_\beta \equiv \beta/(\beta - 1) \leq 1$
- Zhao DM profile (5 params) \rightarrow priors as investigated in *Bonnivard et al. '15*

P.S.

Log-slope of \mathcal{O} is: $\gamma_{\mathcal{O}} \equiv -\frac{d \log \mathcal{O}}{d \log r}$

BEYOND THE STANDARD LORE — DM HALO ESTIMATORS —



IF $\gamma_\beta, \gamma_{\sigma_r^2}$ PHENOMENOLOGICALLY NEGLIGIBLE:

$$\mathcal{M}_\beta(r) - \mathcal{M}_{\beta=0}(r) \simeq \frac{\beta(r) r \sigma_r^2(r)}{G_N} (\gamma_{\hat{I}}(r) - 3)$$

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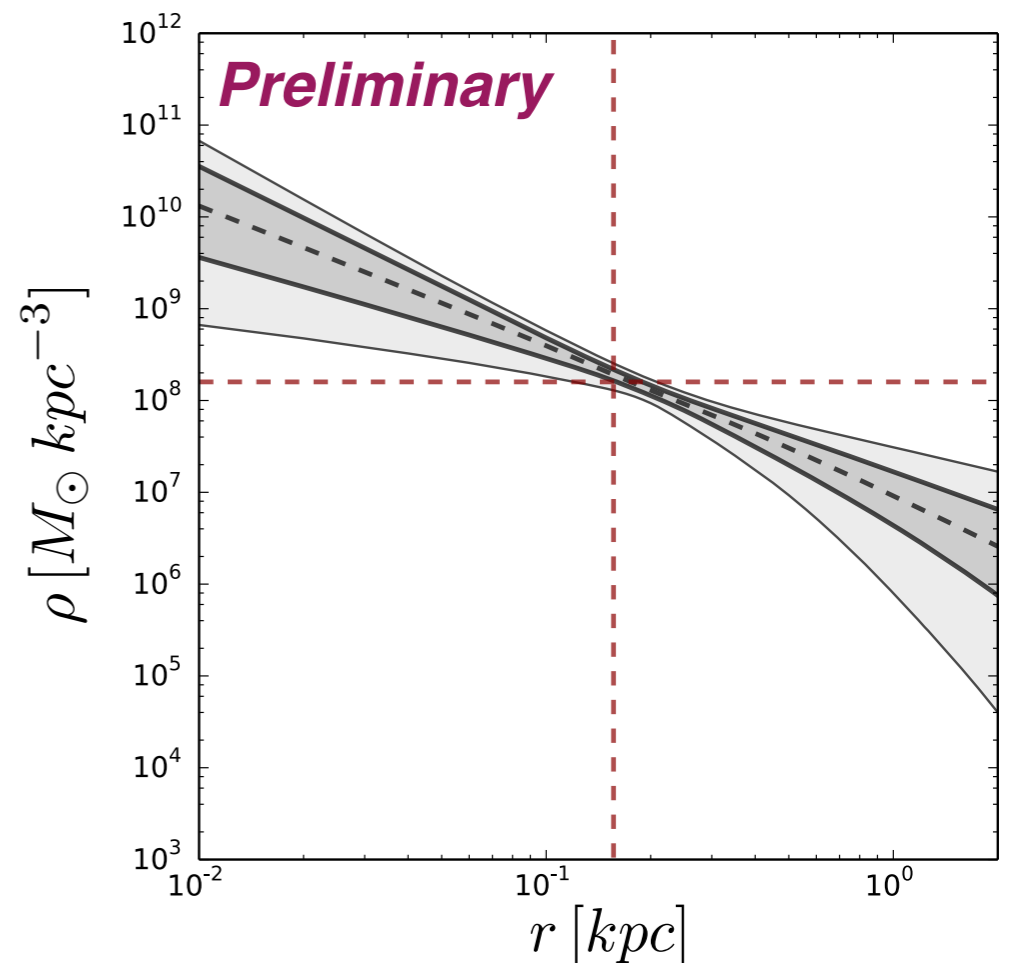
$$r_* : \gamma_{\hat{I}}(r_*) = 3 \Rightarrow r_* = \sqrt{3/2} R_{1/2} \simeq r_{1/2}$$

$$\mathcal{M}(r_*) \simeq \mathcal{M}_{\beta=0}(r_*) = \gamma_{\hat{P}}(r_*) \frac{r_* \hat{P}(r_*)}{G_N \hat{I}(r_*)} \simeq 3 \frac{r_*}{G_N} \langle \sigma_{los}^2 \rangle$$

$$r_{**} : \gamma_{\hat{I}}(r_{**}) (1 - \gamma_{\gamma_{\hat{I}}}(r_{**})) \Rightarrow r_{**} \simeq 2 r_{1/2} / 3$$

$$\rho_{\beta=0}(r_{**}) = \left[\frac{\mathcal{M}_{\beta=0}}{4\pi r^3} (1 - \gamma_{\hat{P}} - \gamma_{\gamma_{\hat{P}}} + \gamma_{\hat{I}}) \right] \Big|_{r=r_{**}}$$

$$\rho(r_{**}) \simeq \frac{\langle \sigma_{los}^2 \rangle}{4\pi r_{**}^2 G_N} \gamma_{\hat{I}}(r_{**}) (1 - \gamma_{\gamma_{\hat{I}}}(r_{**})) = 3 \frac{\langle \sigma_{los}^2 \rangle}{4\pi r_{**}^2 G_N}$$



work in progress, M. Petac, P.Ullio & M.V.

WAY BEYOND THE STANDARD LORE — *SIDM!* —

M.V. & H.B.Yu (in prep.)

MW dSph	$\langle\sigma v\rangle$ [$\text{cm}^3 \text{g}^{-1} \text{s}^{-1}$]	$\langle v\rangle$ [km s^{-1}]	σ/m [$\text{cm}^2 \text{g}^{-1}$]
Ursa Minor	$1.2_{-0.7}^{+2.2} \times 10^2$	52_{-7}^{+11}	$2.9_{-1.8}^{+2.7}$
Sculptor	$0.53_{-0.22}^{+0.22} \times 10^2$	$39.5_{-3.5}^{+3.0}$	$1.23_{-0.37}^{+0.62}$
Draco	$0.65_{-0.28}^{+0.54} \times 10^2$	$45.7_{-5.5}^{+3.7}$	$1.60_{-0.64}^{+0.93}$
Sextans	$0.6_{-0.3}^{+4.0} \times 10^2$	51_{-7}^{+16}	$0.3_{-0.2}^{+8.1}$
Carina	$1.3_{-0.6}^{+1.2} \times 10^2$	$46.9_{-4.8}^{+5.6}$	$2.7_{-1.1}^{+2.3}$
Fornax	$0.28_{-0.09}^{+0.16} \times 10^2$	$30.9_{-1.3}^{+2.5}$	$0.93_{-0.38}^{+0.66}$
Leo II	$2.1_{-1.3}^{+2.0} \times 10^2$	53_{-3}^{+13}	$3.7_{-1.7}^{+2.9}$
Leo I	$1.04_{-0.43}^{+0.76} \times 10^2$	$45.7_{-4.6}^{+3.4}$	$2.4_{-0.9}^{+1.5}$

$$1 \text{ cm}^2 \text{g}^{-1} \lesssim \sigma/m \lesssim 3 \text{ cm}^2 \text{g}^{-1}$$

$$30 \text{ km s}^{-1} \lesssim \langle v \rangle \lesssim 70 \text{ km s}^{-1}$$

Our study on SIDM halo in MW dSphs shows:

I) X-sec range in agreement with current indications from N-body simulations.

Zavala, J. et al. '13, Elbert, O. et al. '15

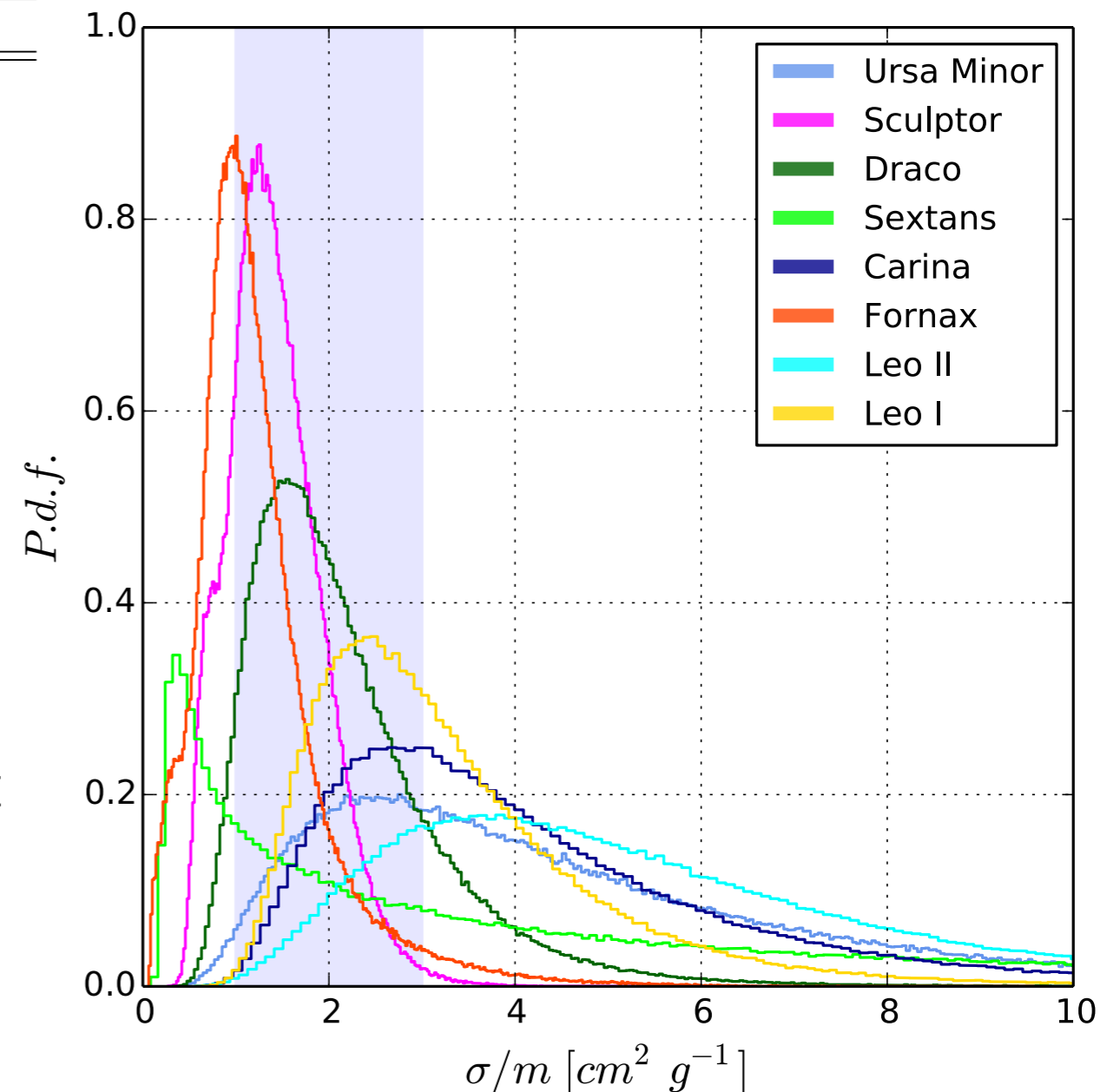
II) Same SIDM ballpark to address “Core VS Cusp” in other kpc-sized systems.

Kaplinghat, M. et al. '16, Kamada, A. et al. '17

III) Some tension left btw goodness of the fit of kinematic data & outer match to CDM.

—> **SIDM ameliorates TBTF problem!**

Vogelsberger, M. et al. '16 (ETHOS)



CONCLUSIONS



Several “basic systematics”: estimate of structural parameters, raw data analysis of stellar kinematics, spherical symmetry ...

FOR CLASSICALS, potential variations up to $\sim 0(50\%)$ on estimated mass at $r_{1/2}$, may naively affect J -factor estimates up to $\Delta J / J \sim 0(1)$.

ABOUT ULTRA-FAINT DWARFS ...

IN DYNAMICAL EQ.?! IF SO, PAUCITY OF KINEMATIC DATA + OTHER OBSERVATIONAL SYSTEMATICS CALL ANYWAY FOR CAUTION ...



—> PROMISING DETECTION TARGETS / POTENTIAL BIAS IN DM LIMITS!

J (D)-factor estimates from *Bonnivard et al. '15* are reasonably conservative against mass-anisotropy degeneracy, take into account uncertainties from stellar fits to photometric data & include triaxial-halo corrections!

Axial-symmetric Jeans analysis from *Hayashi et al. '16* points to comparably “conservative” estimates for J & D (leaving room for further improvements).

PRESENT DM LIMITS FROM MW dSphs CAN BE MADE MORE ROBUST!

Backup

BEYOND J (D) - FACTORS: DISTANCE & HALF-LIGHT RADIUS SYSTEMATICS AT WORK

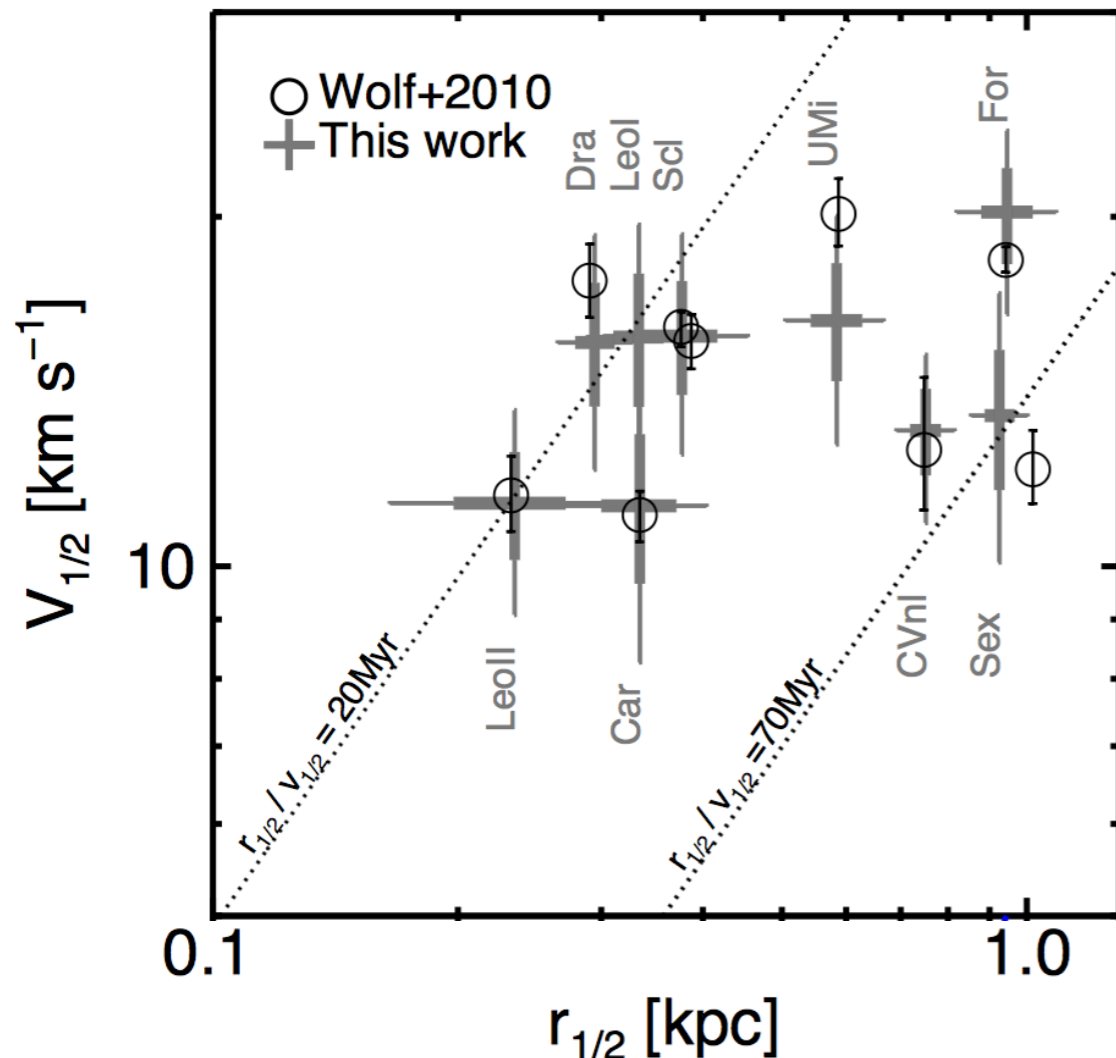
TOO-BIG-TO-FAIL PROBLEM

See previous talk by Manoj K.!

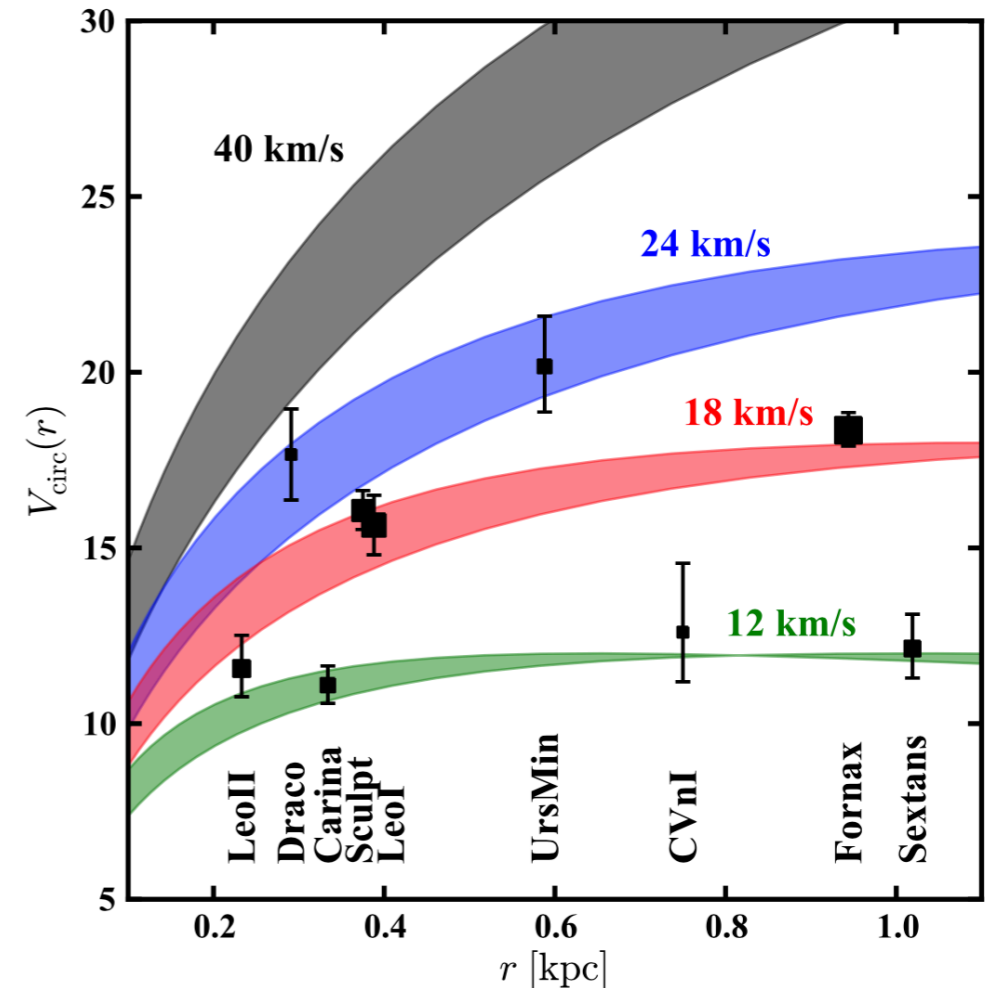
M. Boylan-Kolchin, J.S. Bullock & M. Kaplinghat

MNRAS 415 (2011) L40, MNRAS 422 (2012) 1203

Most massive subhalos in CDM seem to be too dense to host the brightest observed dSphs: so, where are they?



arXiv:1607.06479, Fattahi, A. et al.



To formulate TBTF, it is essential to have a notion of a good “mass estimator” for MW dSphs.

MNRAS 496 (2010) 1220, Wolf, J. et al.

$$\mathcal{M}(r_{1/2}) \Rightarrow V_{circ}(r_{1/2}) = \sqrt{3 \langle \sigma_{los}^2 \rangle}$$

independent of 3D half-light radius ...

... BUT WHEN COMPARING WITH N-BODY, UNCERTAINTIES ON 3D HALF-LIGHT RADIUS SHOULD NOT BE REALLY FORGOTTEN!

Possible challenges/subtleties even in study of the 8 Classics!

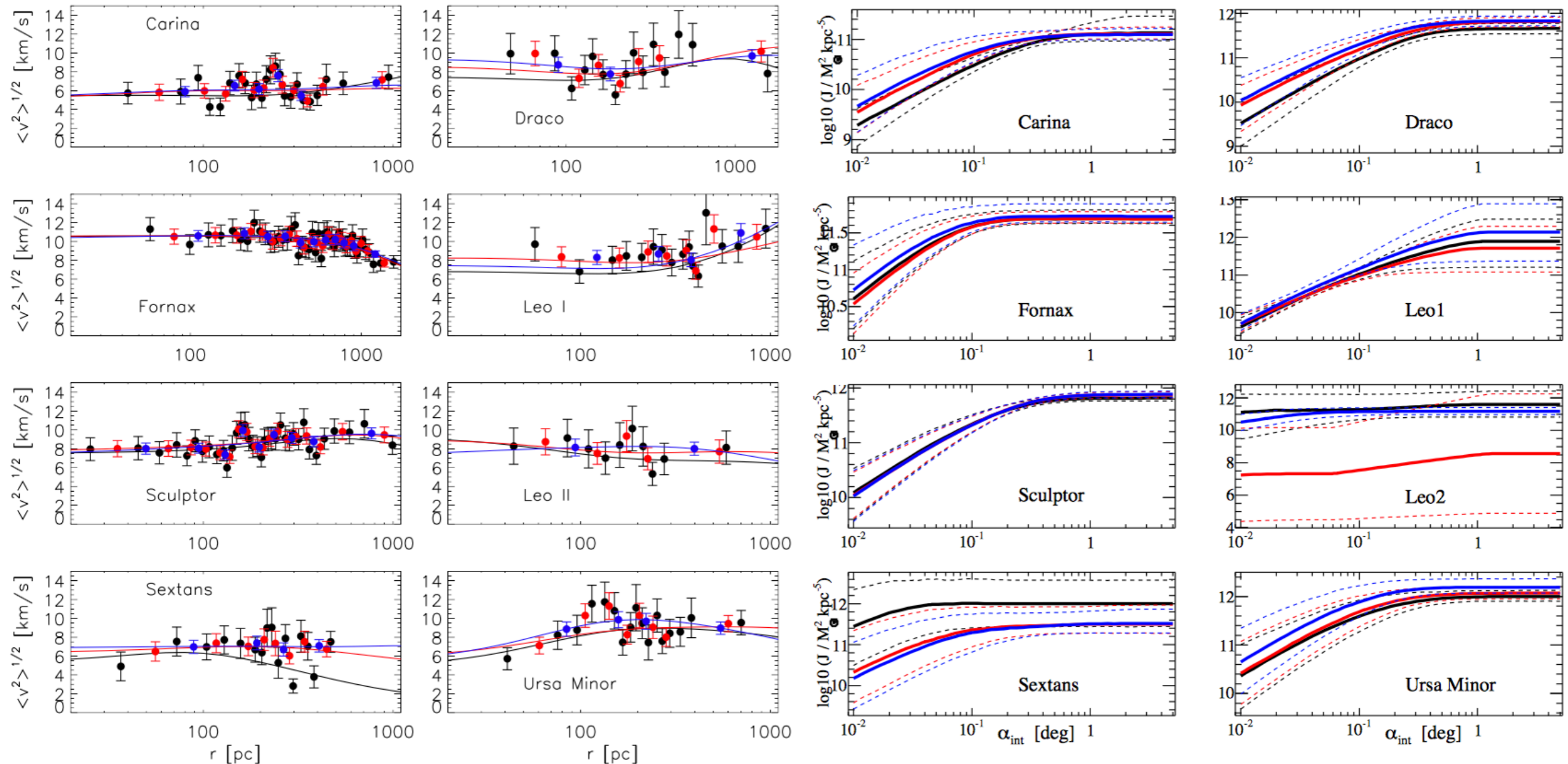
Different choice in binning of l.o.s. velocity dispersions may lead to different results.

$$-2 \ln \mathcal{L} = \sum_i^{N_{bins}} \left(\frac{\sigma_{los}^{(obs)}(R_i) - \sigma_{los}^{(pred)}(R_i)}{\delta \sigma_{los}^{(obs)}(R_i)} \right)^2$$

— $\sqrt{N_*}$ bins
— $\sqrt{N_*}/2$ bins
— $\sqrt{N_*}/4$ bins

$N_* \equiv$ tot star members

MNRAS 418 (2011) 1526, Charbonnier, A. et al.



MASS ESTIMATOR IN DWARF SPHEROIDALS ?

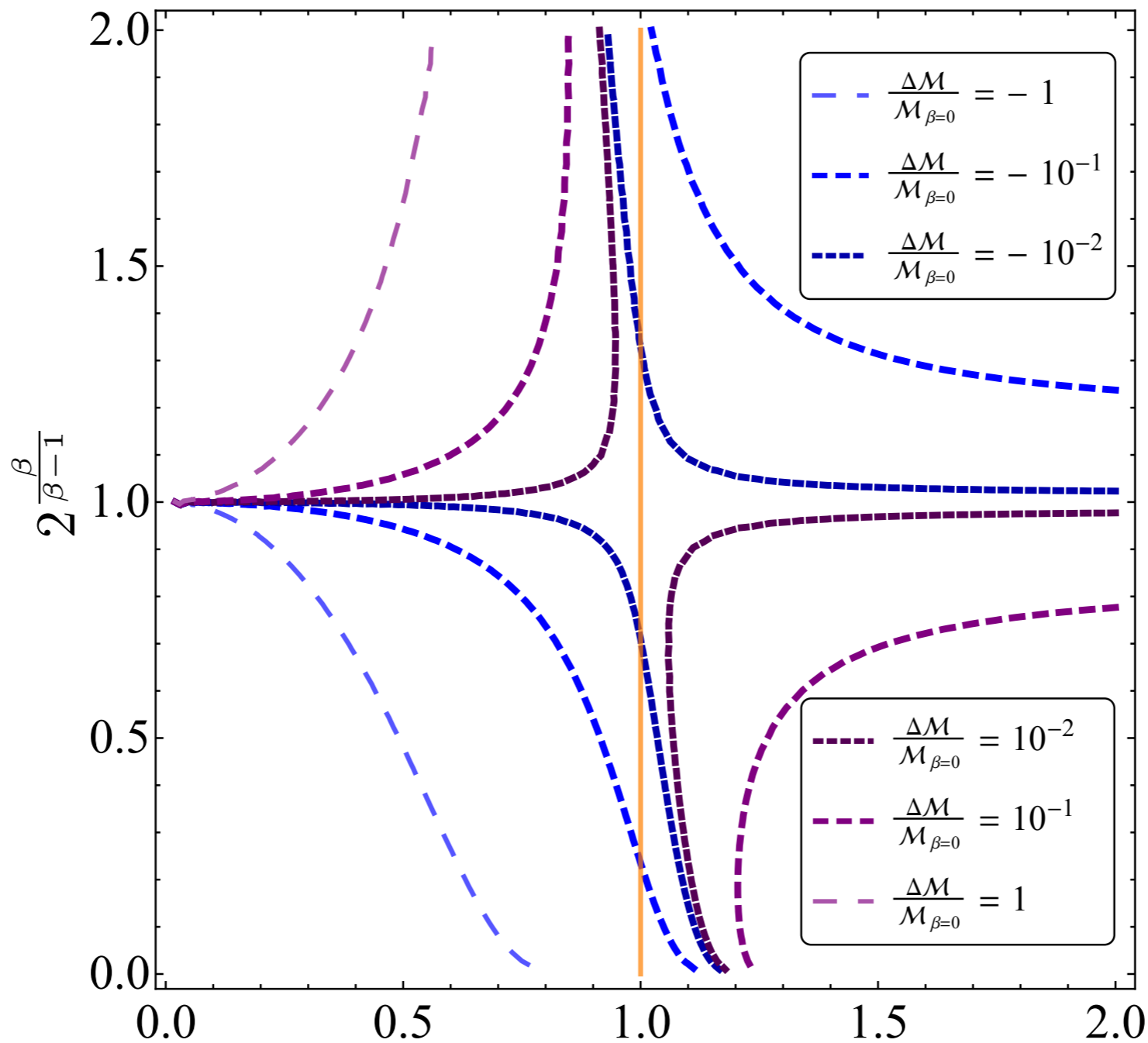
MINIMAL DEPENDENCE ON ANISOTROPY

Nature 454 (2008), Strigari, L. et al.
MNRAS 406 (2010), Wolf, J. et al.



$$\frac{\mathcal{M}_\beta - \mathcal{M}_{\beta=0}}{\mathcal{M}_{\beta=0}} = \text{const.}$$

circular limit
 10%
 isotropic limit
 80%
 radial limit



r/r_* CLOSE TO HALF-LIGHT RADIUS

WORKING HYPOTHESIS

- I) CONST σ_{los} AROUND r_*
- II) CONST β AROUND r_*

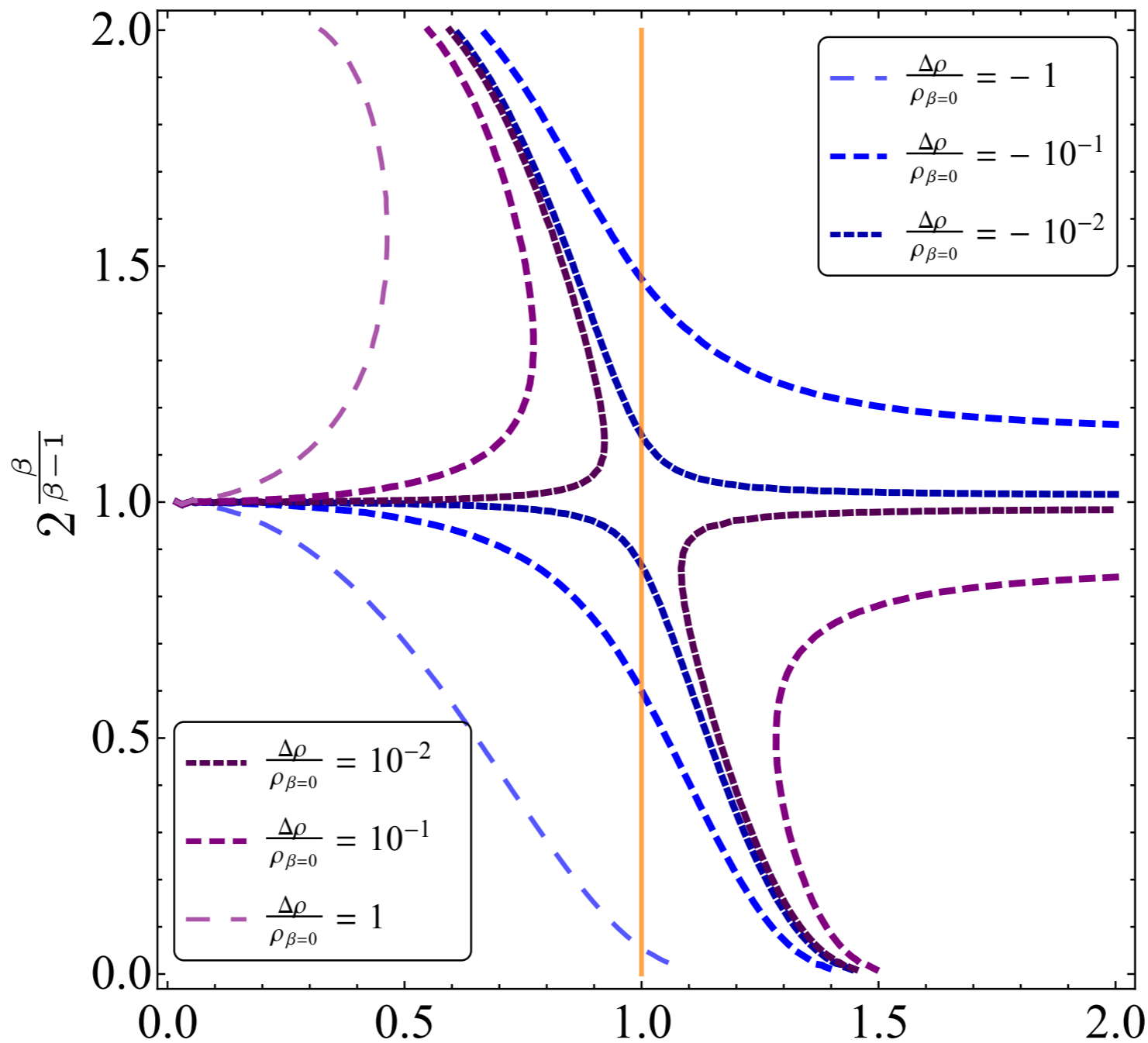
CONCLUSIONS STILL HOLD ALSO BEYOND SUCH FIDUCIAL SCENARIO IF ANISOTROPY IS NOT "FASTLY" VARYING @

DENSITY ESTIMATOR IN DWARF SPHEROIDALS ?

MINIMAL DEPENDENCE ON ANISOTROPY

$$\Rightarrow \frac{\rho_{\beta} - \rho_{\beta=0}}{\rho_{\beta=0}} = \text{const.}$$

circular limit
 $< O(1)$
 isotropic limit
 $\sim O(1)$
 radial limit



WORKING HYPOTHESIS

- I) CONST σ_{los} AROUND r_{**}
- II) CONST β AROUND r_{**}

r / r_{**} CLOSE TO 0.7 x HALF-LIGHT RADIUS

From a well-defined mass estimator we can compute the **minimal J-factor**.

DENSITY AS A SET OF POWER LAWS

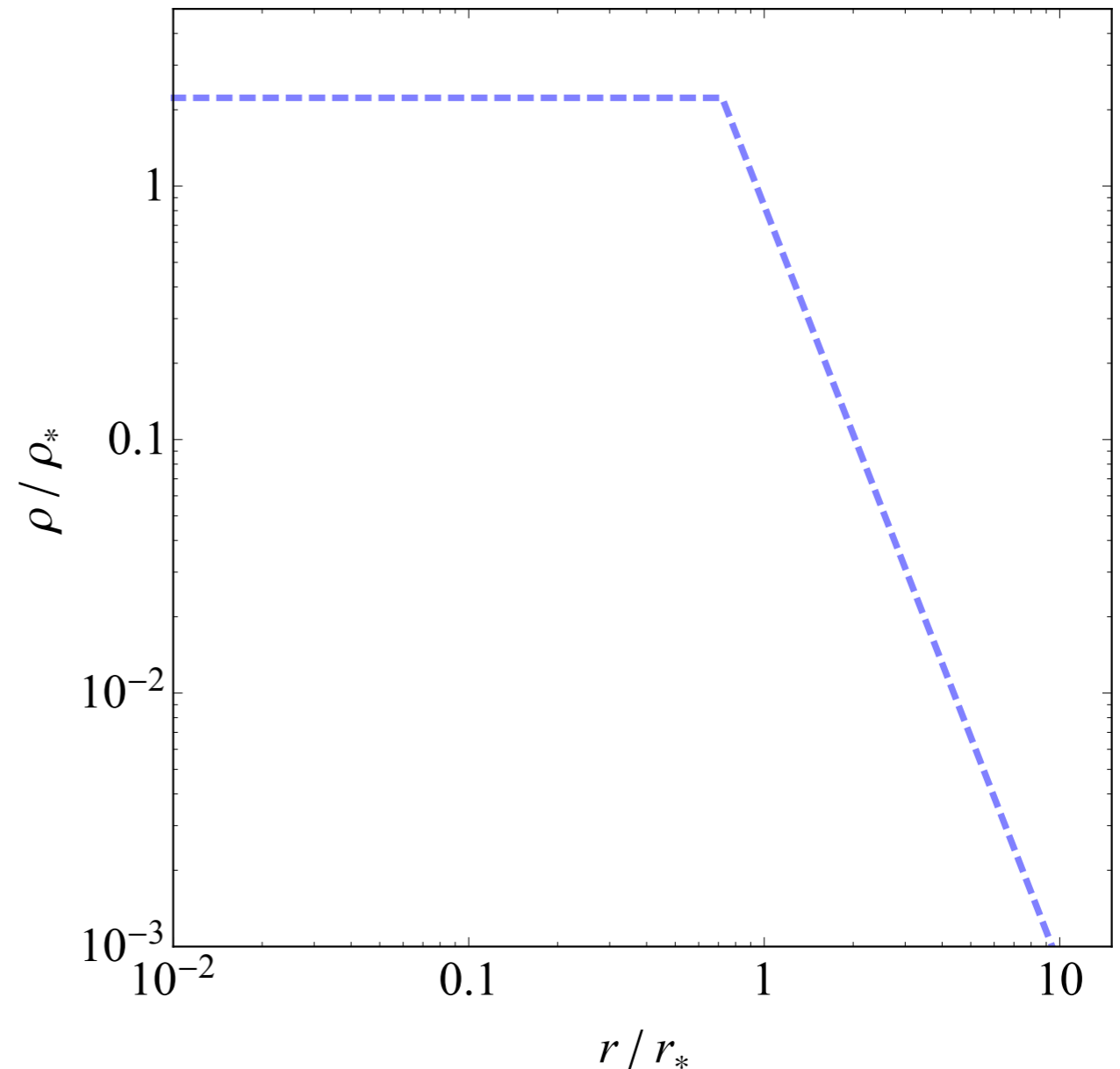
$$\rho \sim r^{-\alpha_i}$$

OVERALL NORMALIZATION FIXED BY

$$4\pi \int_0^{r_*} d\tilde{r} \tilde{r}^2 \rho(\tilde{r}) = \mathcal{M}(r_*)$$

MINIMIZE L.O.S. INTEGRAL OF DENSITY²

$$\min_{\alpha_i} J [\alpha_i]$$



WITHIN THE INTRODUCED **FIDUCIAL MODEL**, **ISOTROPIC ORBITS PREFERRED**

PLUMMER + CONST SIGMA LOS + CONST BETA

From a well-defined mass estimator we can compute the **minimal J-factor**.

DENSITY AS A SET OF POWER LAWS

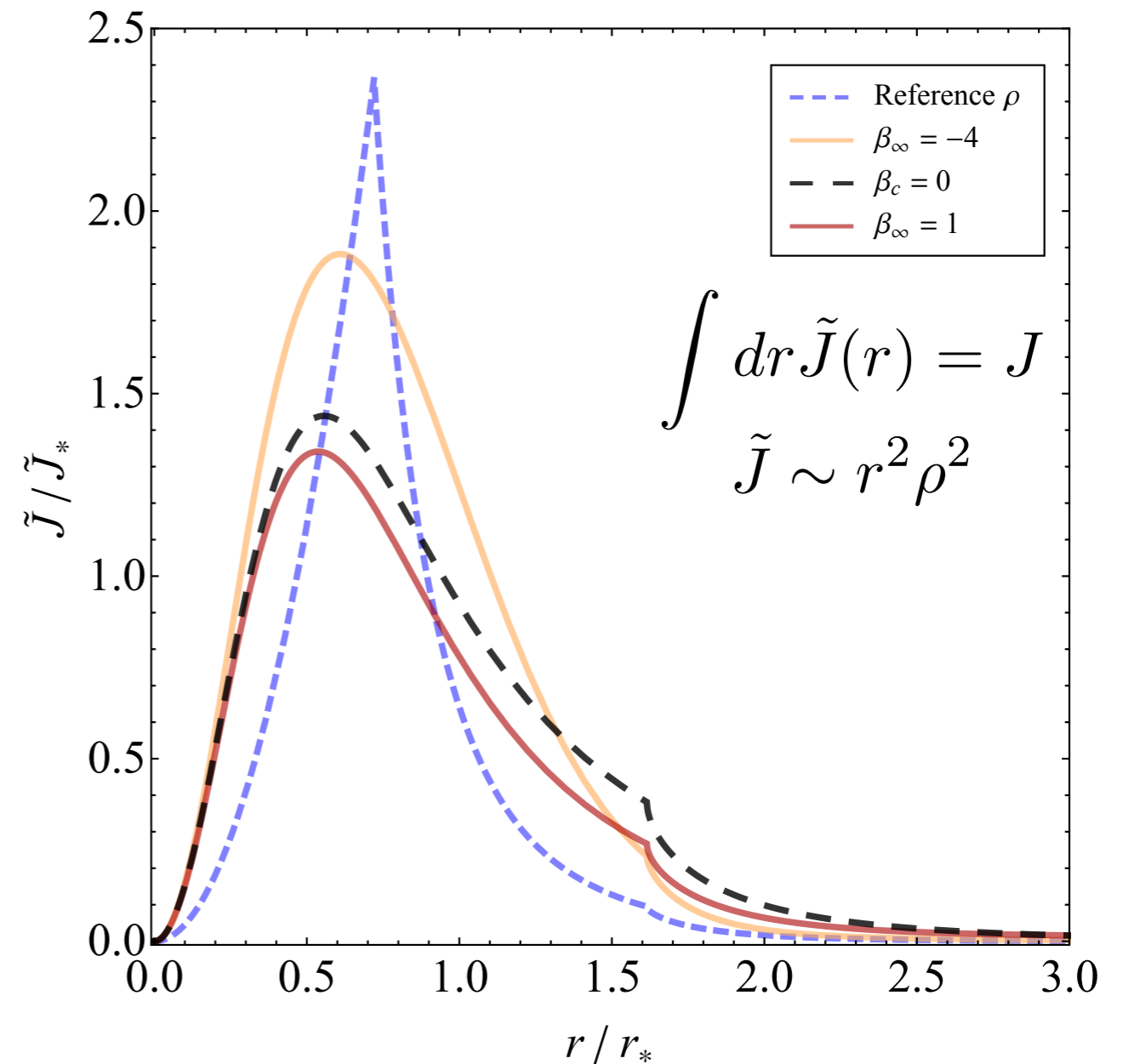
$$\rho \sim r^{-\alpha_i}$$

OVERALL NORMALIZATION FIXED BY

$$4\pi \int_0^{r_*} d\tilde{r} \tilde{r}^2 \rho(\tilde{r}) = \mathcal{M}(r_*)$$

MINIMIZE L.O.S. INTEGRAL OF DENSITY²

$$\min_{\alpha_i} J [\alpha_i]$$

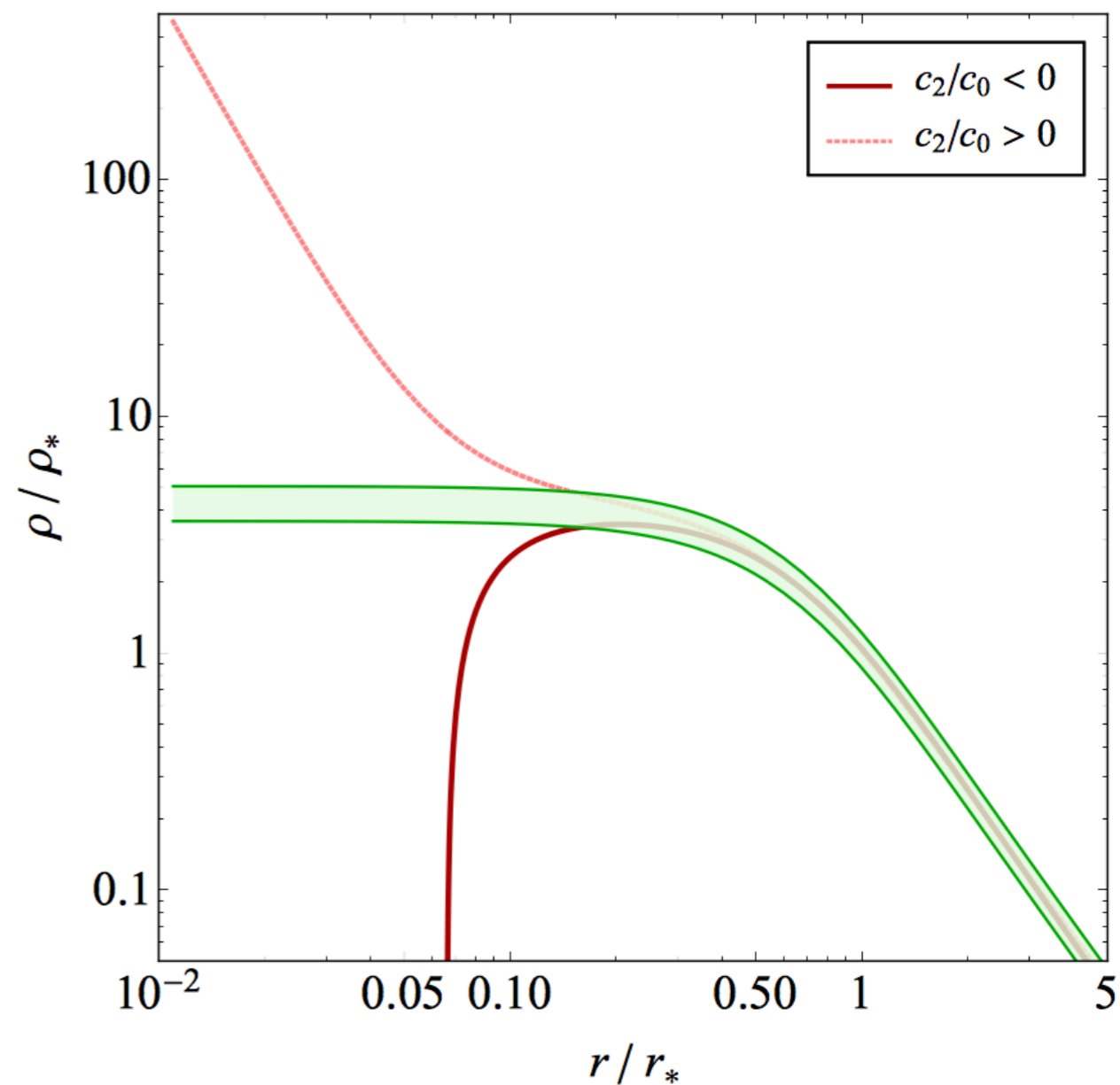
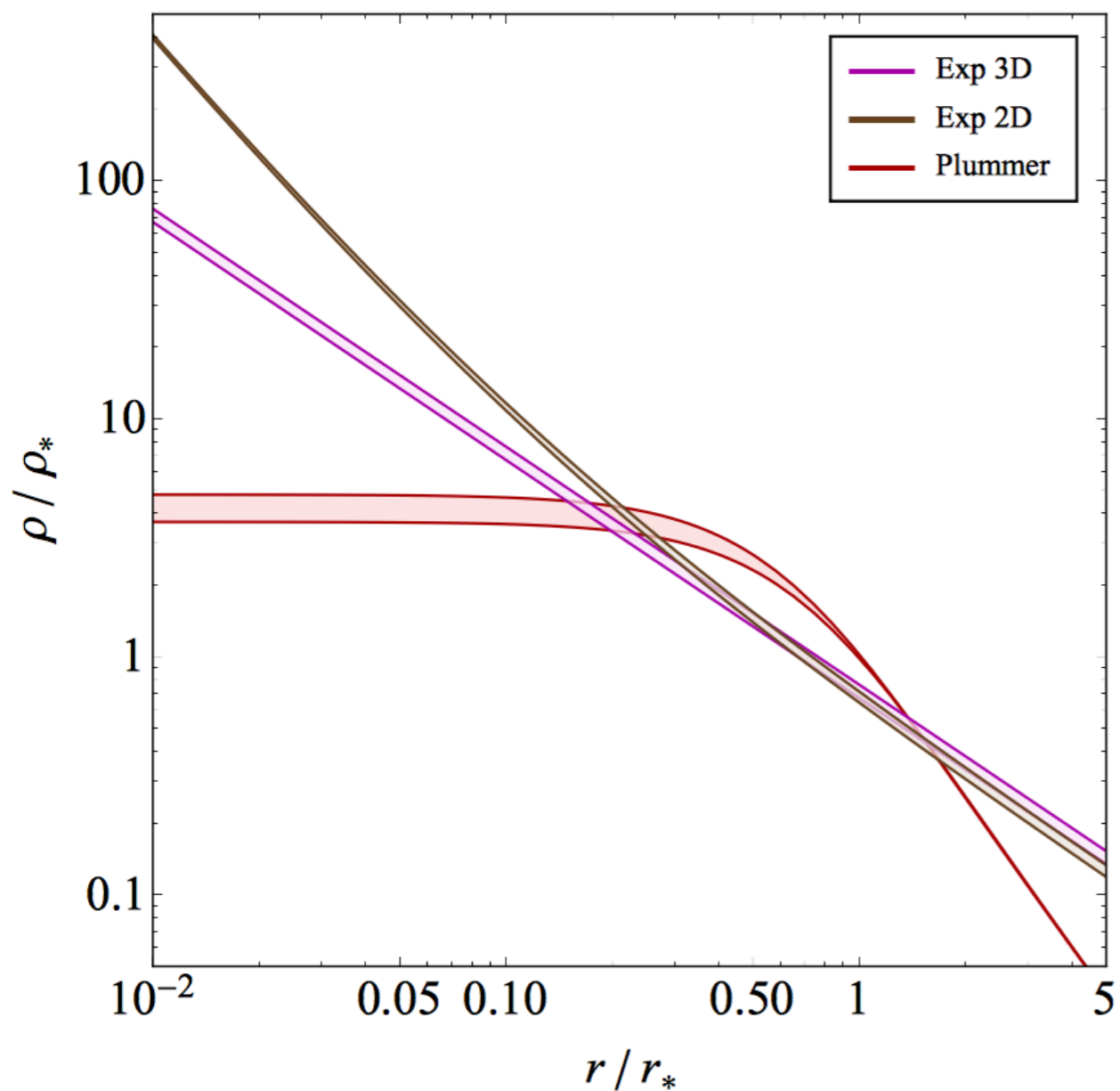


PLUMMER + CONST SIGMA LOS + CONST BETA

WITHIN THE INTRODUCED **FIDUCIAL MODEL**, **ISOTROPIC ORBITS PREFERRED**

$$\beta_c \rightarrow \frac{\beta_0 + \beta_\infty (r/r_a)^\eta}{1 + (r/r_a)^\eta} \quad \text{IMPACTS VERY MILDLY THE MINIMAL J-VALUE}$$

A change of stellar profile in our fiducial model typically increases the minimal J .



Conclusion on minimal J unchanged if we tilt the l.o.s. velocity dispersion profile:

- an inner concave departure from constant σ_{los} increases J
- an inner convex departure from constant σ_{los} yields unphysical density

Departure from isotropic limit corresponds to cuspier profiles (therefore, higher J).

BOTTOM LINE FROM FIDUCIAL MODEL

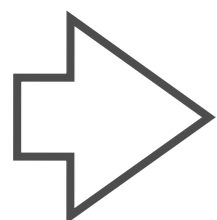
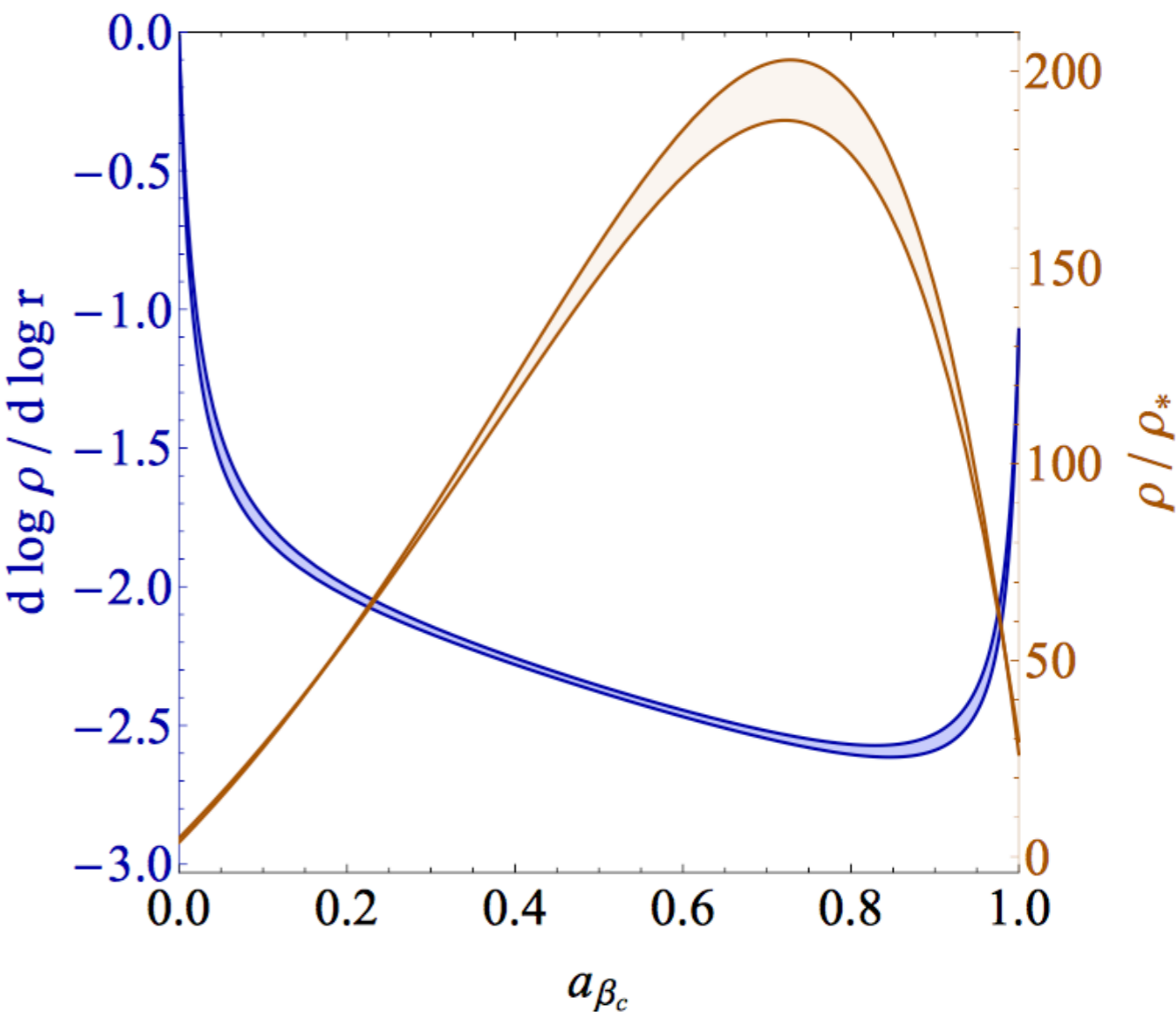


In order to get an inner core in dSph DM density, a cored stellar profile + flattish los sigma require isotropic motion

However, discontinuity of this trend in the limit of perfectly circular stellar orbits:

$$\rho_{a_{\beta} \rightarrow 1}(r = 0) \propto r^{-1}$$

$$\mathcal{M}_{a_{\beta} \rightarrow 1}(r = 0) = \frac{4}{3} \frac{\sigma_{los}^2 R_{1/2}}{G_N}$$



A PHENOMENOLOGICALLY MOTIVATED INNER CUT-OFF ON THE DENSITY SMOOTHES THE DISCONTINUITY WITH THE LIMIT CASE OF NEGATIVE INFINITE ANISOTROPY

IN THIS APPROACH THE MINIMAL J-FACTOR CORRESPONDS NOW TO CIRCULAR-LIKE ORBITS!

Dwarf “spheroidals” → J (D) - factors in spherical symmetry!

$$J = 2\pi \int_0^{\cos \psi_{max}} d \cos \psi \int_{\ell_-(\psi, \mathcal{R})}^{\ell_+(\psi, \mathcal{R})} dl \rho^2(r(\psi, l)) \rightarrow J = 4\pi \int_0^{\mathcal{R}} dr \rho^2(r) \mathcal{A}(r/\mathcal{D}; \psi_{max})$$

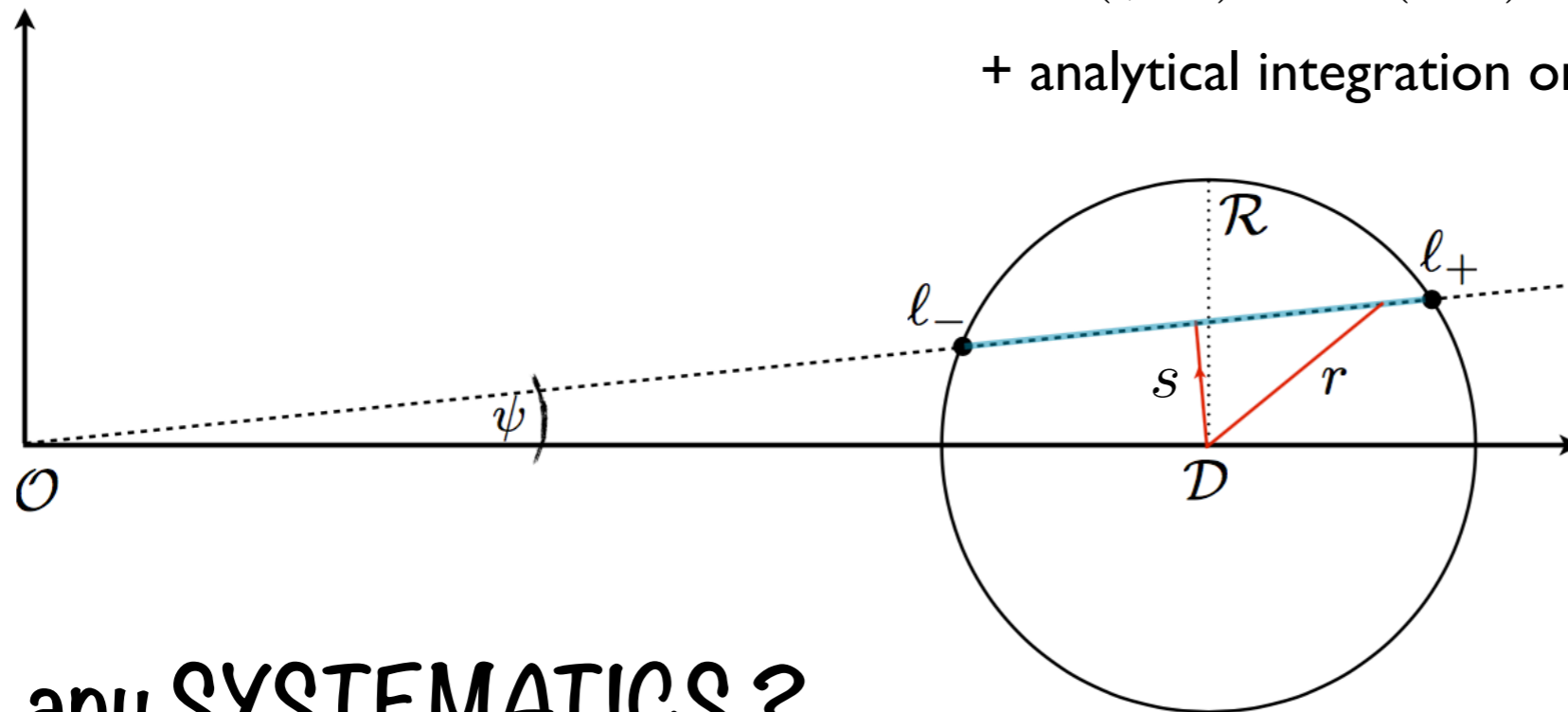
NOTE: for all details, see for example appendix B in *JCAP 1607 (2016) 025*

change of coordinates

$$(\psi, l) \rightarrow (s, r)$$

+ analytical integration on s

$$\left| \int_{\psi_{max}}^{\text{small}} r^2 / \mathcal{D}^2 \right.$$



\mathcal{D}	distance from obs
\mathcal{R}	tidal / outer halo cut
ψ_{max}	obs angular aperture
$\rho(r)$	DM halo density

... any SYSTEMATICS?



DIFFERENT ESTIMATES FOR MW DWARF DISTANCES.

→ see, e.g., *Mateo '98* and *McConnachie '12*

HALO TRUNCATION IS ESSENTIALLY UNKNOWN ...

→ recent investigation in *Geringer-Sameth et al. '15*

... AS BOOST FACTORS FROM SUBSTRUCTURES!

→ DM signal enhancement! See *Strigari et al. '06, Bovy '09*

Dwarf “spheroidals” → J (D) - factors in spherical symmetry!

$$J = 2\pi \int_0^{\cos \psi_{max}} d \cos \psi \int_{\ell_-(\psi, \mathcal{R})}^{\ell_+(\psi, \mathcal{R})} dl \rho^2(r(\psi, l)) \rightarrow J = 4\pi \int_0^{\mathcal{R}} dr \rho^2(r) \mathcal{A}(r/\mathcal{D}; \psi_{max})$$

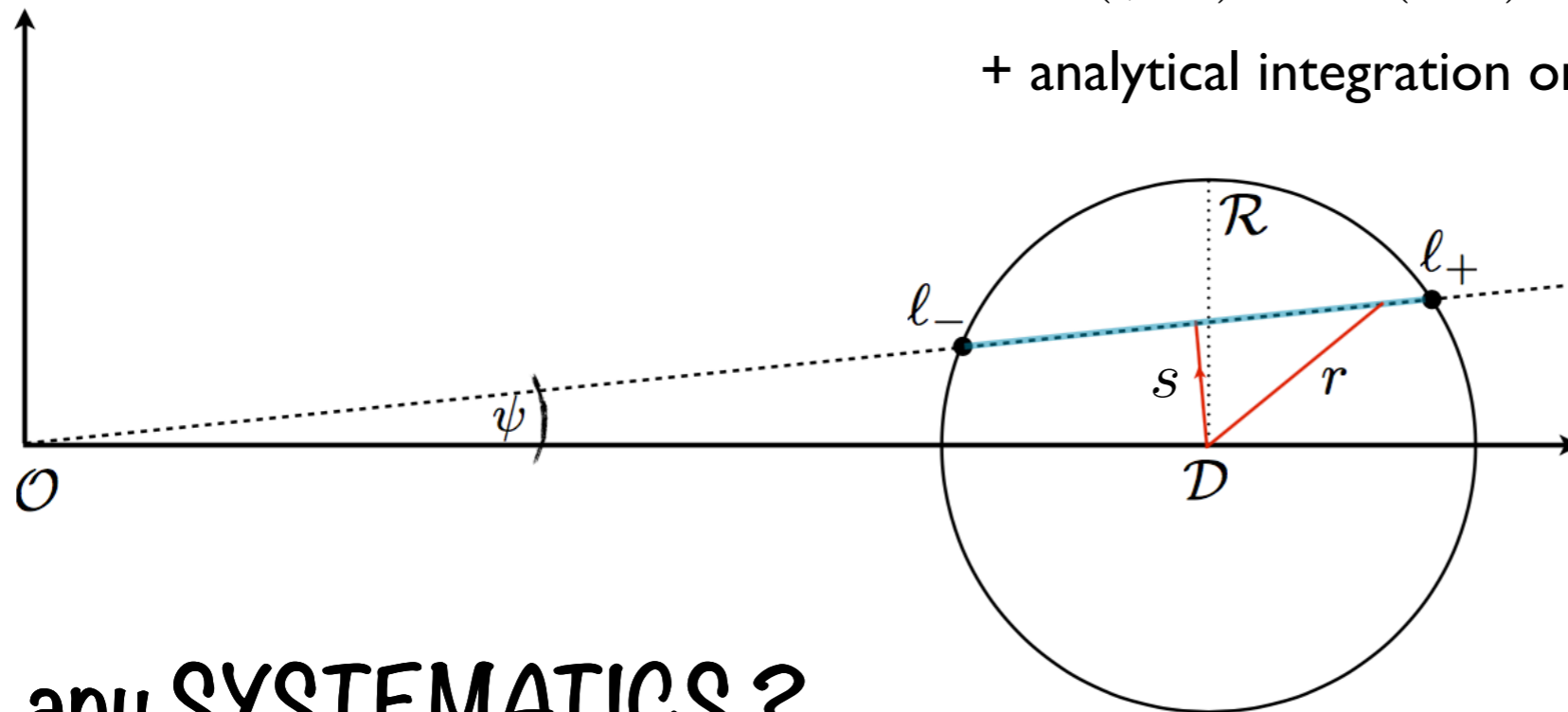
NOTE: for all details, see for example appendix B in *JCAP 1607 (2016) 025*

change of coordinates

$$(\psi, l) \rightarrow (s, r)$$

+ analytical integration on s

$$\left| \mathcal{R} \frac{\text{small } \psi_{max}}{r^2 / \mathcal{D}^2} \right.$$



\mathcal{D}	distance from obs
\mathcal{R}	tidal / outer halo cut
ψ_{max}	obs angular aperture
$\rho(r)$	DM halo density

... any SYSTEMATICS?



DM HALO COMMONLY STUDIED WITH SPHERICAL JEANS EQ.:

$$\sigma_{los} = \sigma_{los}(\mathcal{M}, \beta, I)$$

$\mathcal{M} \sim$ Dark Matter $\beta =$ Stellar Anisotropy $I =$ Surface Brightness

DEGENERACIES AMONG 3 PARAMETRIC PROFILES!

Dwarf “spheroidals” → J (D) - factors in spherical symmetry!

$$J = 2\pi \int_0^{\cos \psi_{max}} d \cos \psi \int_{\ell_-(\psi, \mathcal{R})}^{\ell_+(\psi, \mathcal{R})} dl \rho^2(r(\psi, l)) \rightarrow J = 4\pi \int_0^{\mathcal{R}} dr \rho^2(r) \mathcal{A}(r/\mathcal{D}; \psi_{max})$$

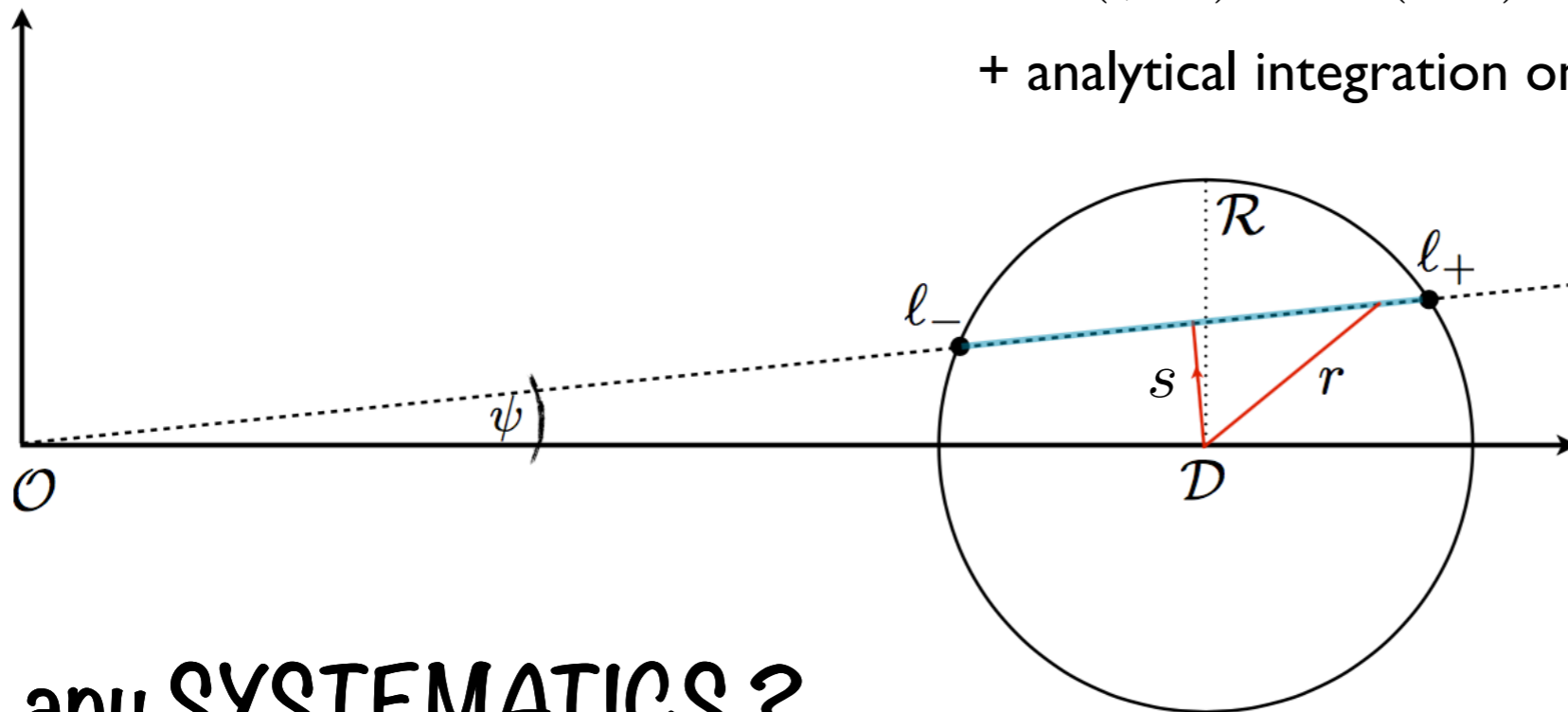
NOTE: for all details, see for example appendix B in *JCAP 1607 (2016) 025*

change of coordinates

$$(\psi, l) \rightarrow (s, r)$$

+ analytical integration on s

$$\left| \mathcal{R} \right| \begin{matrix} \text{small} \\ \psi_{max} \end{matrix} \\ r^2 / \mathcal{D}^2$$



\mathcal{D}	distance from obs
\mathcal{R}	tidal / outer halo cut
ψ_{max}	obs angular aperture
$\rho(r)$	DM halo density

... any SYSTEMATICS?



NUMERICAL EVIDENCES FOR AN OPTIMAL CHOICE:

$$\psi_{max} \simeq \arctan(2 R_{1/2} / \mathcal{D}) \sim 0.5^\circ$$

→ see, e.g., *Walker et al. '11*, *Charbonnier et al. '11*

COMPROMISE BTW UNCERTAINTIES & FLUX DETECTION

... ANY FURTHER INSIGHT (SEE, E.G., THE MASS AT $r_{1/2}$)?