



Status of the P2 Experiment

A measurement of the Weak Mixing Angle at Low Energy

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PRISMA



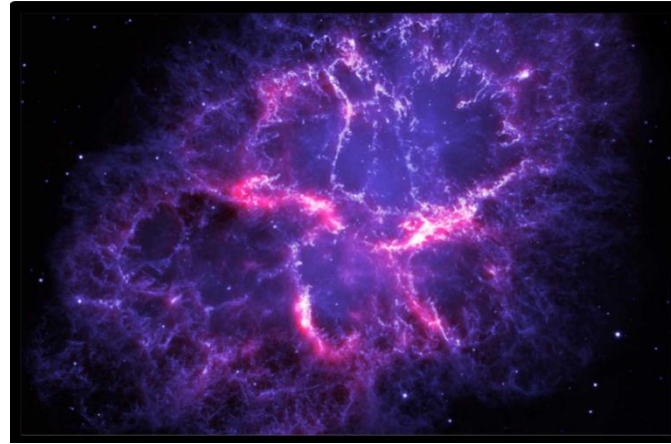


- Introduction:
The Weak Mixing Angle and the Standard Model
- P2 Experiment Design
Achievable precision in $\sin^2\Theta_W$
Spectrometer Design
- Further Physics Program
- Summary



Standard Model: Open questions

- Consistent description of all four fundamental interactions?
- Dark matter, dark energy?

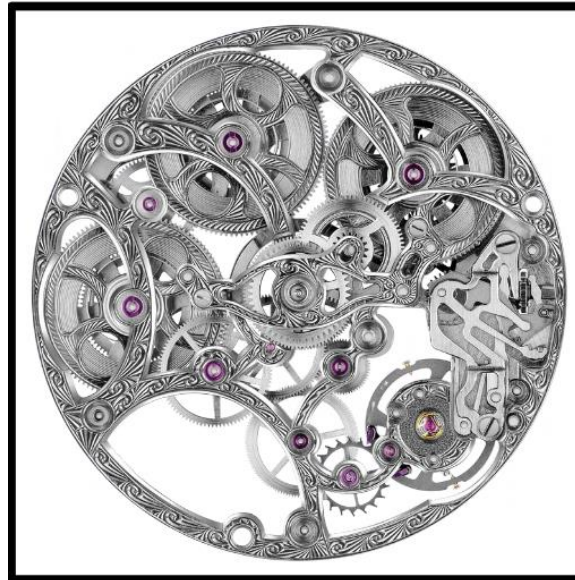


Search for **New Physics**:

Option 1: Direct search for new particles at high energies



Option 2: Precise determination of Standard Model predictions at moderate energies



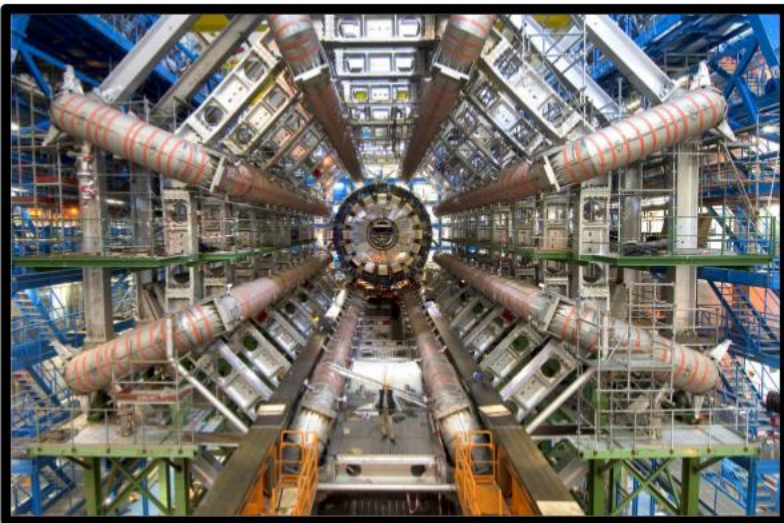
Standard Model: Open questions

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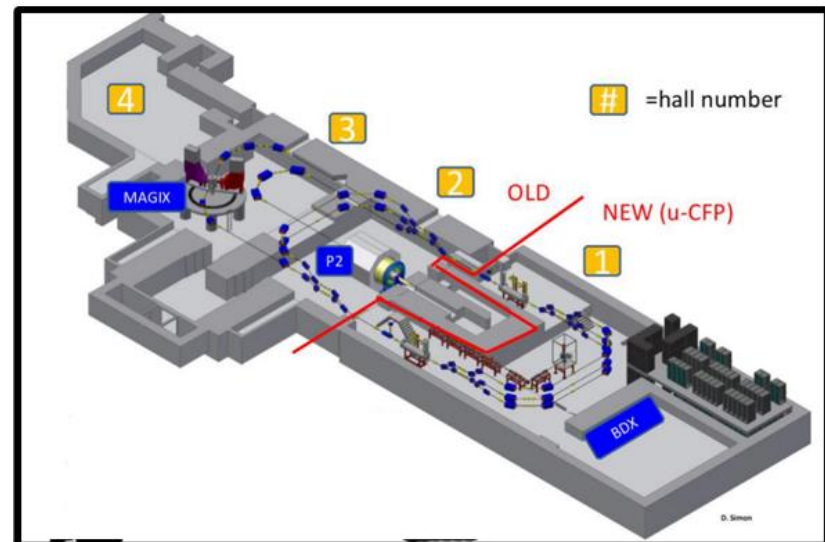


Search for **New Physics**:

Option 1: Direct search for new particles at high energies



Option 2: Precise determination of Standard Model predictions at moderate energies



The weak mixing angle

$\sin^2\Theta_W$: a central parameter in the Standard Model

Tree level relations:

- Electric charge $e = \sqrt{4\pi\alpha} = g_1 \cos \theta_W = g_2 \sin \theta_W$
- Masses of W and Z Boson $\cos \theta_W = M_W / M_Z$
- Myon decay constant $G_\mu = \frac{\pi\alpha}{\sqrt{2} \sin^2 \theta_W M_W^2}$

Standard model relations for the weak mixing angle

Tree level relations:

- Electric charge
- Masses of W and Z Boson
- Myon decay constant

$$e = \sqrt{4\pi\alpha} = g_1 \cos \theta_W = g_2 \sin \theta_W$$

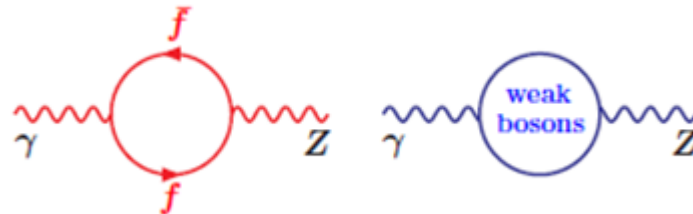
$$\cos \theta_W = M_W / M_Z$$

$$G_\mu = \frac{\pi\alpha}{\sqrt{2} \sin^2 \theta_W M_W^2}$$

Including radiative corrections:

$$G_\mu = \frac{\pi\alpha}{\sqrt{2} \sin^2 \theta_W M_W^2} (1 + \Delta r)$$

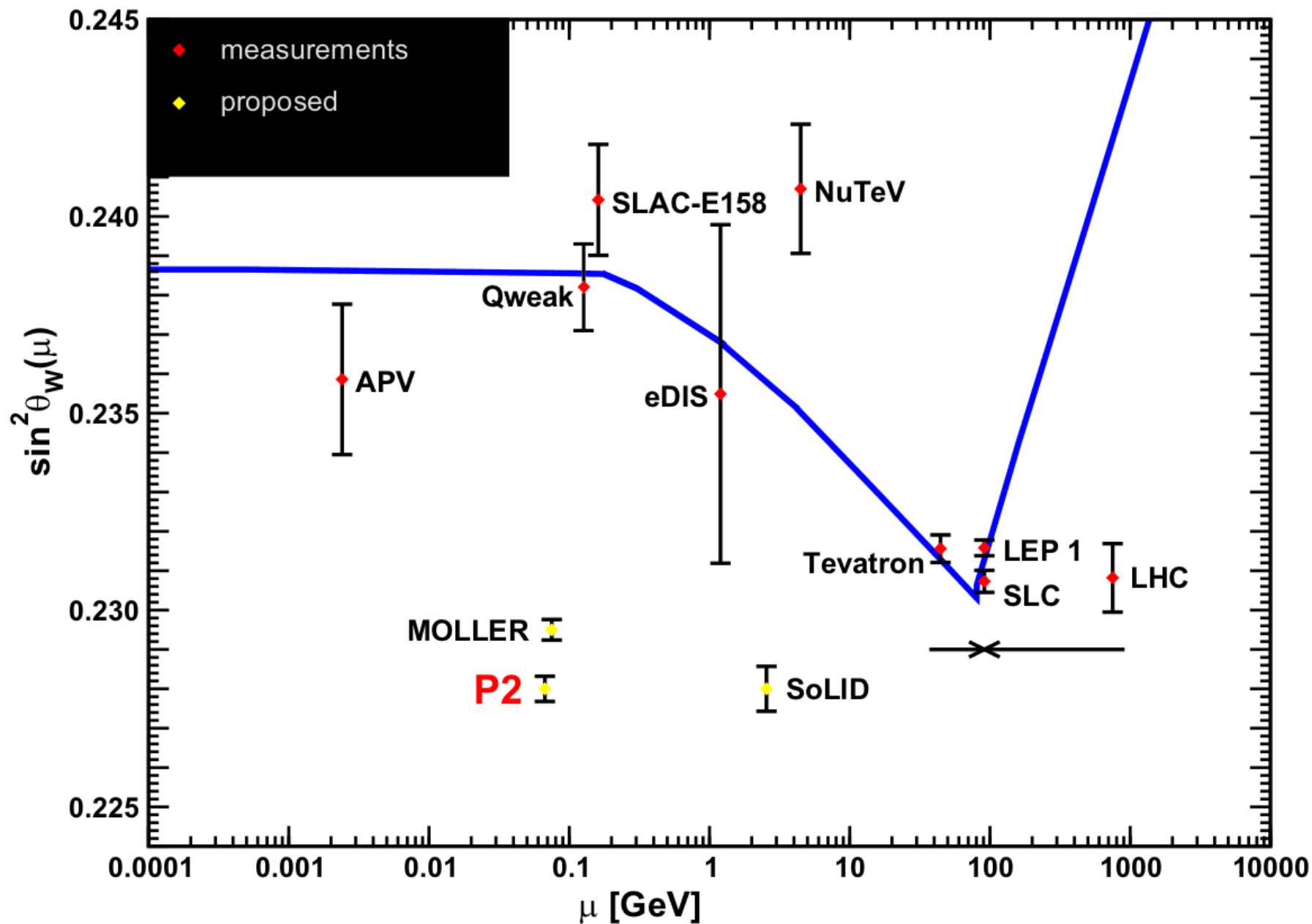
with $\Delta r = \Delta r(\alpha, M_W, \sin \theta_W, m_{top}, M_{Higgs}, \dots)$



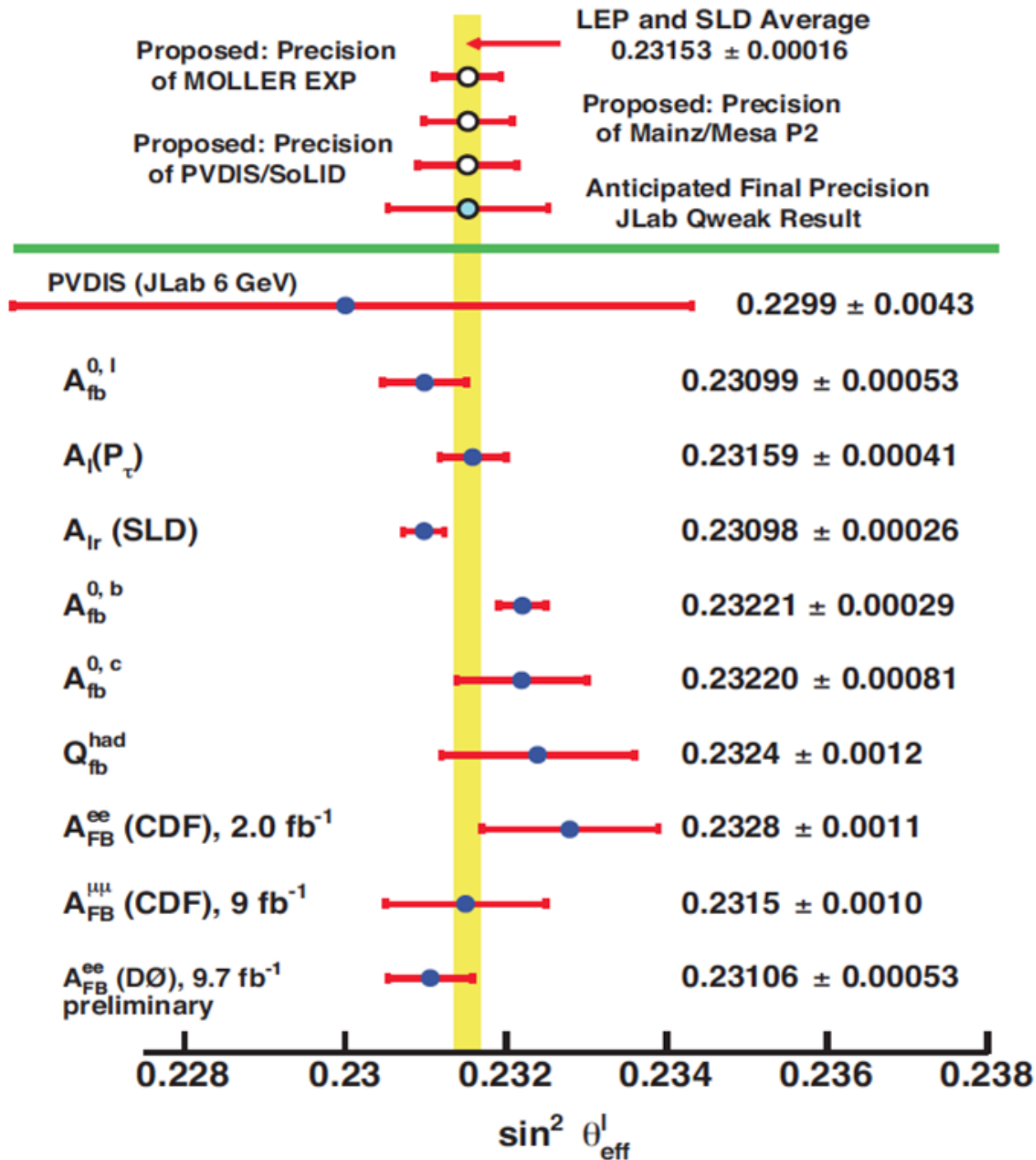
Absorb universal quantum corrections in an **effective, running** weak mixing angle:

$\sin^2 \theta_W \rightarrow \sin^2 \theta_{\text{eff}}$ or $\sin^2 \theta_W(\mu)$ mit μ as energy scale

Scale dependency of $\sin^2\Theta_W$



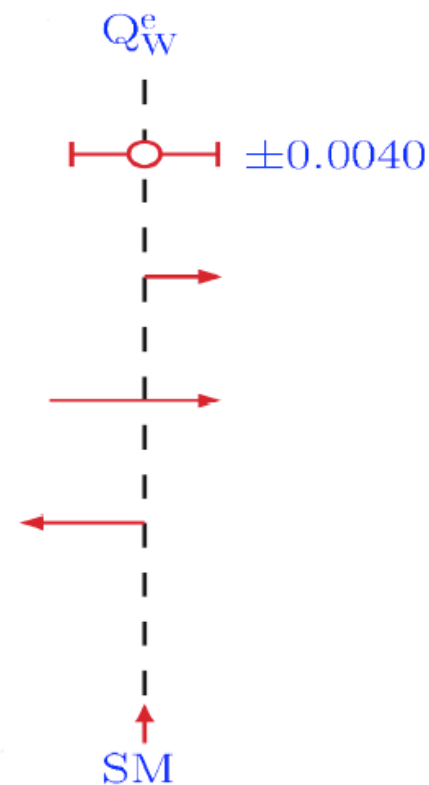
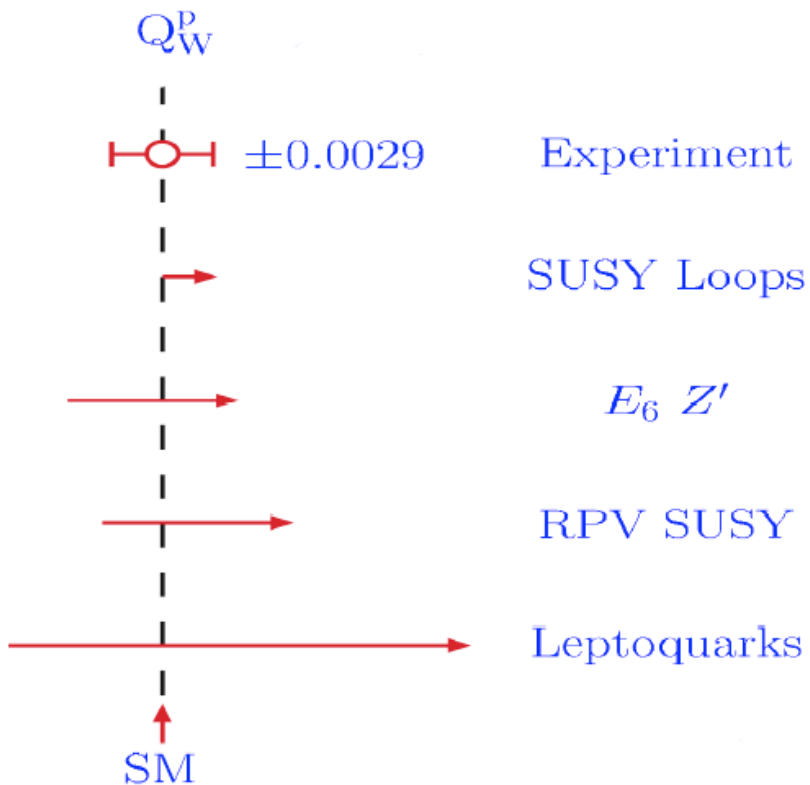
Measurements of $\sin^2 \theta_{\text{eff}}^l$



Physics beyond the Standard Model

Weak charges of proton and electron (tree level):

$$\begin{aligned} \text{Proton} \quad Q_W(p) &= 1 - 4\sin^2\Theta_W \\ \text{Electron} \quad Q_W(e) &= -1 + 4\sin^2\Theta_W \end{aligned}$$

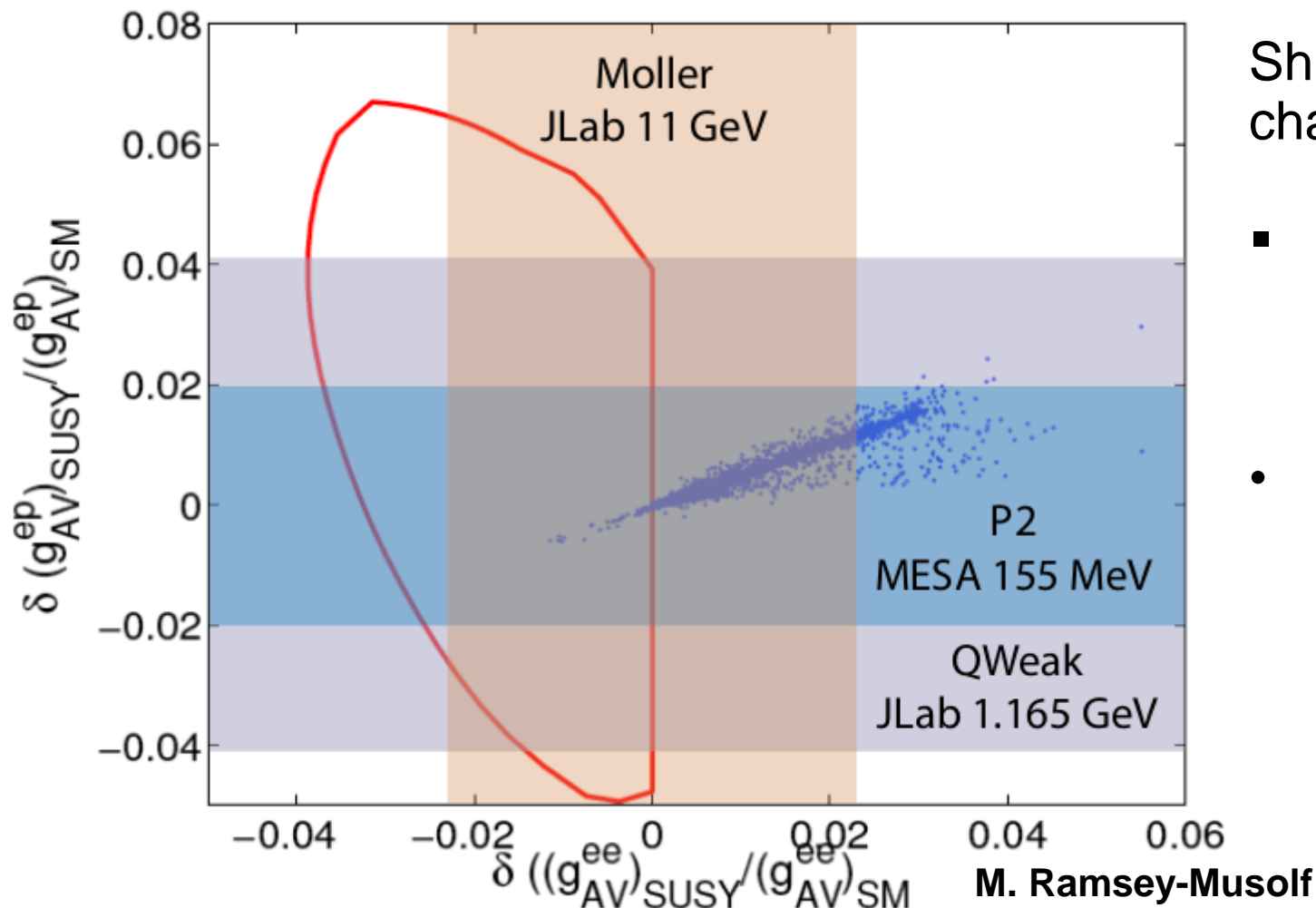


Standard Model extensions:

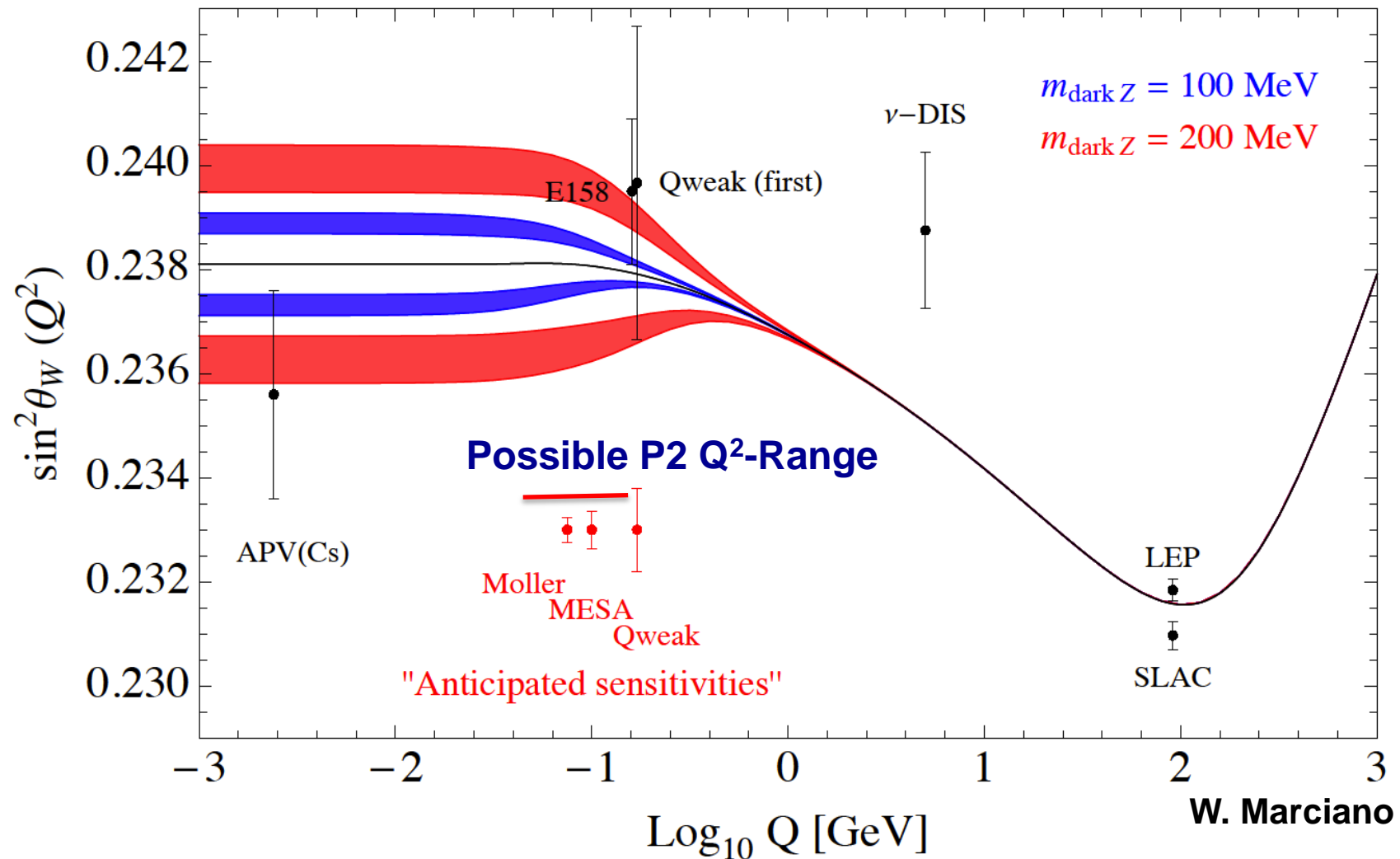
- Characteristic shifts in $Q_W(p)$ and $Q_W(p)$
- Measurements of $Q_W(p)$ and $Q_W(p)$ are complementary

Super Symmetric Models

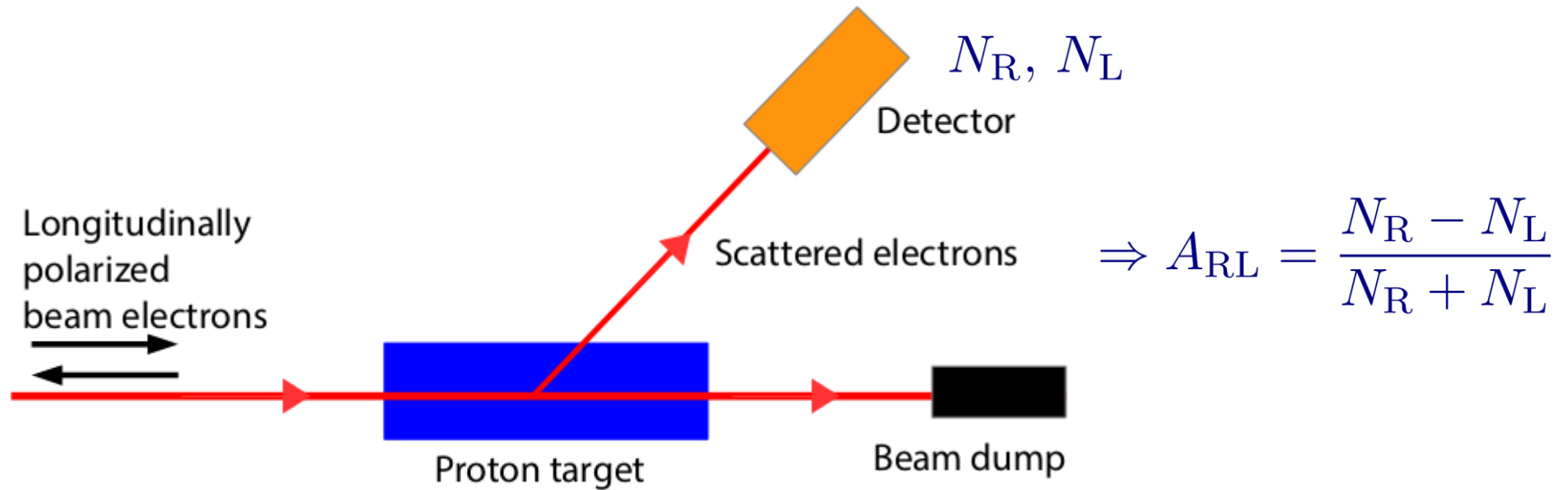
Example: Super symmetric Standard Model extension (SuSy)
with and without R-Parity violation



Running of $\sin^2 \theta_W$ and Dark Parity Violation



Parity violating electron scattering



Cross section: $\sigma_{ep} \sim \left| \begin{array}{c} \text{Diagram 1} \\ + \\ \text{Diagram 2} \end{array} \right|^2 \sim |M_y + M_z|^2$

Diagram 1: A vertex where an incoming electron line (e) and an outgoing electron line (e') meet, connected by a wavy line labeled γ . Below this, an incoming proton line (p) and an outgoing proton line (p') meet at a vertex.

Diagram 2: A vertex where an incoming electron line (e) and an outgoing electron line (e') meet, connected by a dashed line labeled Z_0 . Below this, an incoming proton line (p) and an outgoing proton line (p') meet at a vertex.

The weak interaction is **parity violating**: $M_Z^+ \neq M_Z^- \longrightarrow |M_y + M_Z^+|^2 \neq |M_y + M_Z^-|^2$

$\longrightarrow \boxed{\sigma_{ep}^+ \neq \sigma_{ep}^-}$

Parity violating electron scattering

Asymmetry in the cross section of elastic electron-proton scattering for left- and right-handed polarized electrons

$$A_{LR} = \frac{\sigma(e_{\downarrow}) - \sigma(e_{\uparrow})}{\sigma(e_{\downarrow}) + \sigma(e_{\uparrow})} = -\frac{G_F Q^2}{4\sqrt{2}\pi\alpha} \left(Q_W(\mathcal{N}) - F(Q^2) \right)$$

The weak charge of the proton (tree level):

$$Q_W(p) = 1 - 4 \sin^2 \theta_W$$

$$\frac{\Delta \sin^2 \theta_W}{\sin^2 \theta_W} = \frac{1 - 4 \sin^2 \theta_W}{4 \sin^2 \theta_W} \frac{\Delta Q_W(p)}{Q_W(p)}$$

1.5% precision in $Q_W(p)$ results in a precision of 0.13% in $\sin^2 \theta_W$

Precision Studies

The parity violating asymmetry can be written as

$$A^{\text{PV}} = \frac{-G_{\text{F}}Q^2}{4\pi\alpha_{\text{em}}\sqrt{2}} [Q_{\text{W}}(\text{p}) - F(E_{\text{i}}, Q^2)]$$

with the form factor contribution

$$F(E_{\text{i}}, Q^2) \equiv F^{\text{EM}}(E_{\text{i}}, Q^2) + F^{\text{A}}(E_{\text{i}}, Q^2) + F^{\text{S}}(E_{\text{i}}, Q^2)$$

with

$$F^{\text{EM}}(E_{\text{i}}, Q^2) \equiv \frac{\epsilon G_{\text{E}}^{\text{p},\gamma} G_{\text{E}}^{\text{n},\gamma} + \tau G_{\text{M}}^{\text{p},\gamma} G_{\text{M}}^{\text{n},\gamma}}{\epsilon (G_{\text{E}}^{\text{p},\gamma})^2 + \tau (G_{\text{M}}^{\text{p},\gamma})^2}$$

$$F^{\text{A}}(Q^2) \equiv \frac{(1 - 4 \sin^2 \theta_{\text{W}}) \sqrt{1 - \epsilon^2} \sqrt{\tau(1 - \tau)} G_{\text{M}}^{\text{p},\gamma} G_{\text{A}}^{\text{p},\text{Z}}}{\epsilon (G_{\text{E}}^{\text{p},\gamma})^2 + \tau (G_{\text{M}}^{\text{p},\gamma})^2}$$

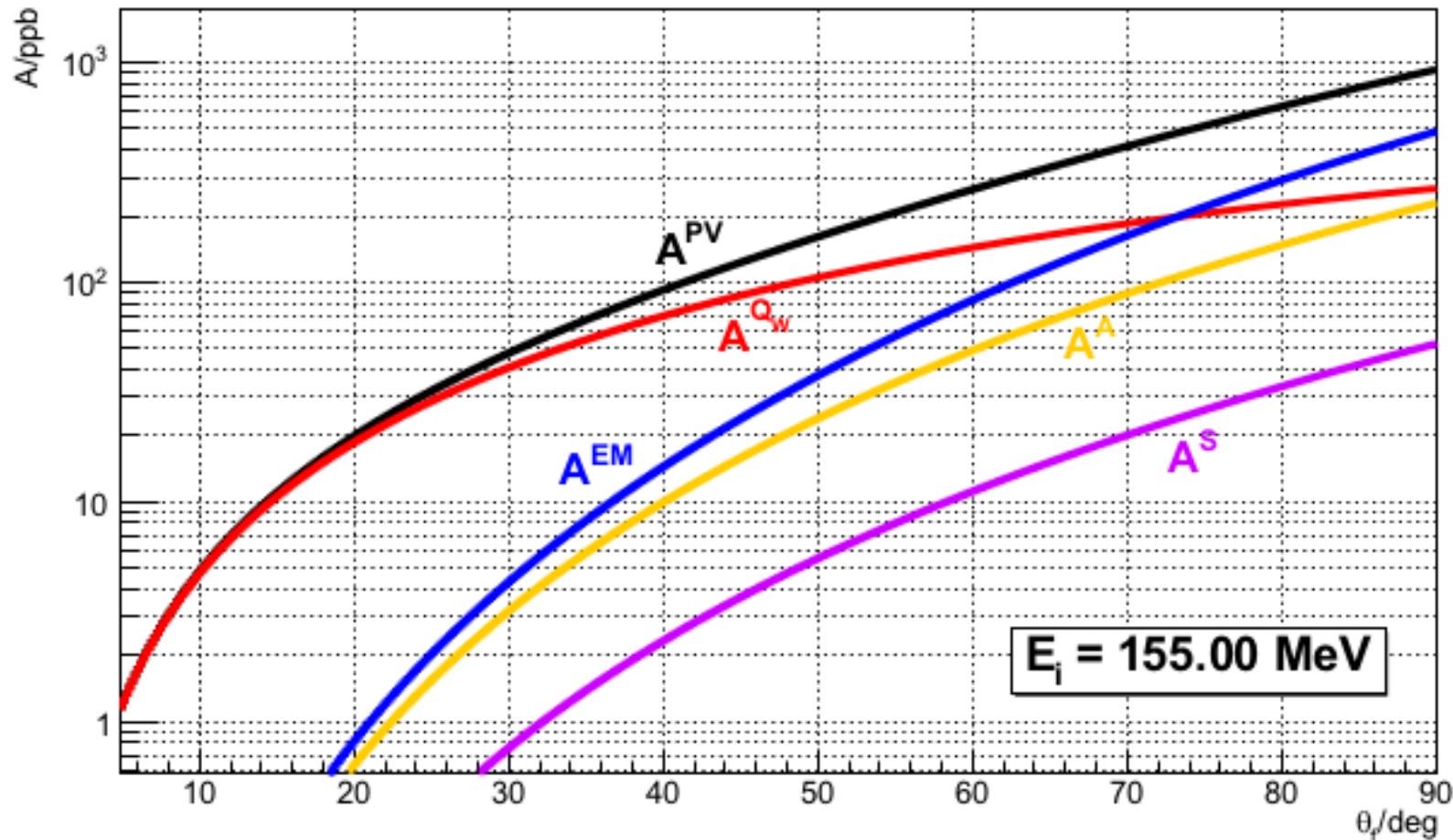
$$F^{\text{S}}(E_{\text{i}}, Q^2) \equiv \frac{\epsilon G_{\text{E}}^{\text{p},\gamma} G_{\text{E}}^{\text{s}} + \tau G_{\text{M}}^{\text{p},\gamma} G_{\text{M}}^{\text{s}}}{\epsilon (G_{\text{E}}^{\text{p},\gamma})^2 + \tau (G_{\text{M}}^{\text{p},\gamma})^2} + \frac{\epsilon G_{\text{E}}^{\text{p},\gamma} G_{\text{E}}^{\text{u,d}} + \tau G_{\text{M}}^{\text{p},\gamma} G_{\text{M}}^{\text{u,d}}}{\epsilon (G_{\text{E}}^{\text{p},\gamma})^2 + \tau (G_{\text{M}}^{\text{p},\gamma})^2}$$

Precision Studies

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Asymmetry contributions for the MESA beam energy of 155 MeV



Precision Studies

The parity violating asymmetry can be written as

$$A^{\text{PV}} = \frac{-G_{\text{F}}Q^2}{4\pi\alpha_{\text{em}}\sqrt{2}} [Q_{\text{W}}(p) - F(E_{\text{i}}, Q^2)]$$

Prediction of the achievable precision:

- The measured asymmetry can be written as

$$\langle A^{\text{raw}} \rangle_{\text{sig}} = P \cdot \langle A^{\text{PV}} \rangle_{\text{sig}} + A^{\text{false}}$$

- Solve this equation for $\sin^2\Theta_{\text{W}}$, denoted here as s_{W}^2

$$s_{\text{W}}^2 = s_{\text{W}}^2(\langle A^{\text{raw}} \rangle_{\text{sig}}, P, E_{\text{beam}}, \bar{\theta}_{\text{f}}, \delta\theta_{\text{f}}, F(\{\kappa_k\}, Q^2), \square_{\gamma\text{Z}})$$

- Perform error propagation calculation based on a Monte Carlo algorithm

Precision Studies

Input parameters for error propagation:

λ_l	$\langle \lambda_l \rangle$	$\Delta \lambda_l$
E_{beam}	variable	0.13 MeV
$\bar{\theta}_f$	variable	0°
$\delta \theta_f$	variable	0.1°
$\delta \phi_f$	360°	0°
I_{beam}	150 μA	0.001 μA
P	0.85	0.00425
L	600 mm	0 mm
T	1×10^4 h	0 h
A^{false}	0	0.1 ppb

Proton form factors of the proton from Bernauer et al.:

$$G_{\text{E}}^{\text{p},\gamma}(Q^2) = G_{\text{dipole}}^{\text{std}}(Q^2) \cdot G_{\text{E}}^{\text{poly}}(Q^2)$$

$$G_{\text{M}}^{\text{p},\gamma}(Q^2) = \mu_{\text{P}}/\mu_{\text{N}} \cdot G_{\text{dipole}}^{\text{std}}(Q^2) \cdot G_{\text{M}}^{\text{poly}}(Q^2)$$

$$G_{\text{F}}^{\text{poly}}(Q^2) = 1 + \sum_{i=1}^8 \left(\kappa_i^{\text{p},\text{F}} \cdot Q^{2i} \right)$$

$$G_{\text{dipole}}^{\text{std}}(Q^2) = \left(1 + \frac{Q^2}{0.71 \text{ GeV}^2} \right)^{-2}$$

Neutron form factors from M. El Yakoubi;

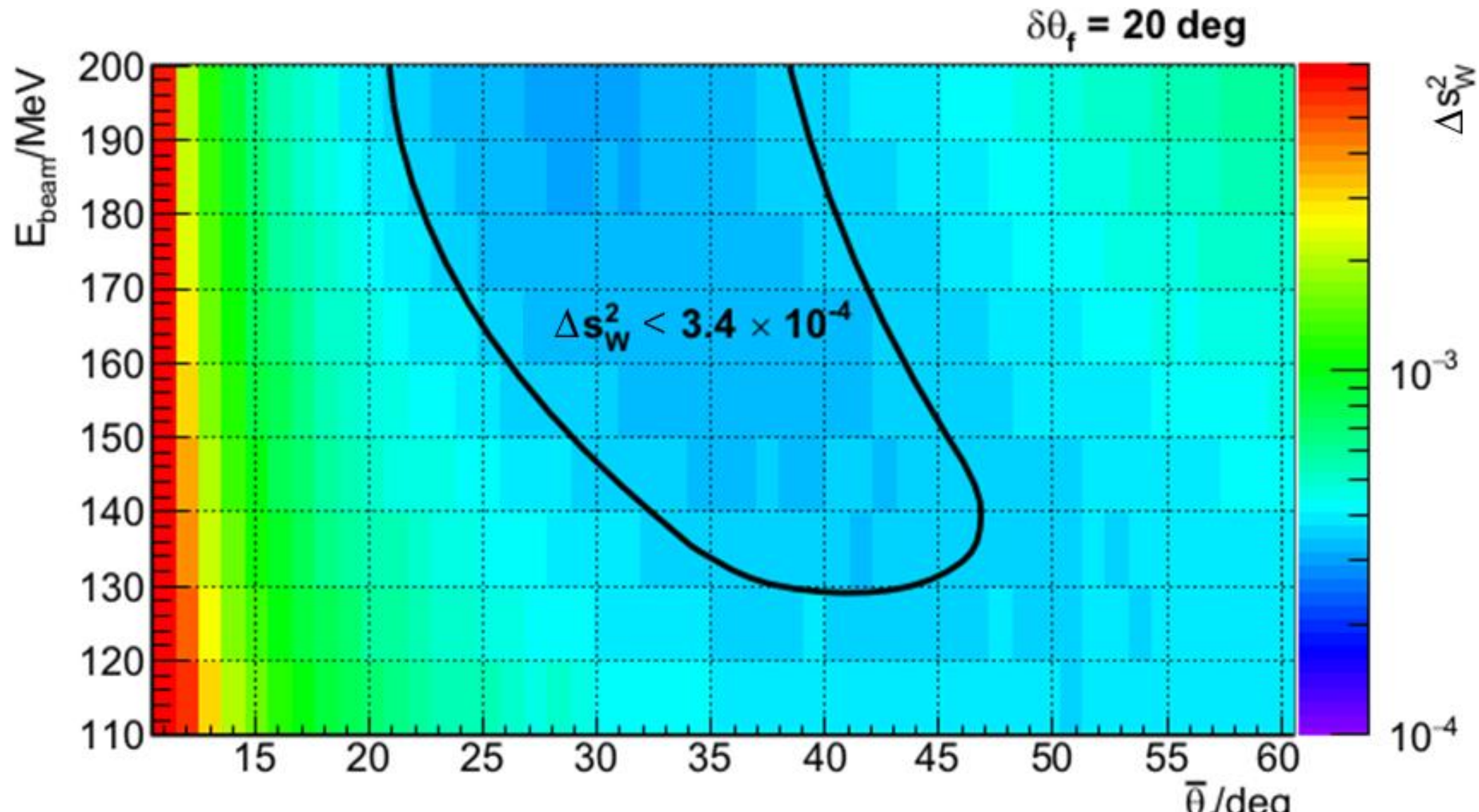
$$G_{\text{E}}^{\text{n},\gamma}(Q^2) = \frac{\tau \kappa_1^{\text{n},\text{E}}}{1 + \tau \kappa_2^{\text{n},\text{E}}} \cdot G_{\text{dipole}}^{\text{std}}(Q^2)$$

$$G_{\text{M}}^{\text{n},\gamma}(Q^2) = \sum_{i=0}^9 \kappa_i^{\text{n},\text{M}} Q^{2i}$$

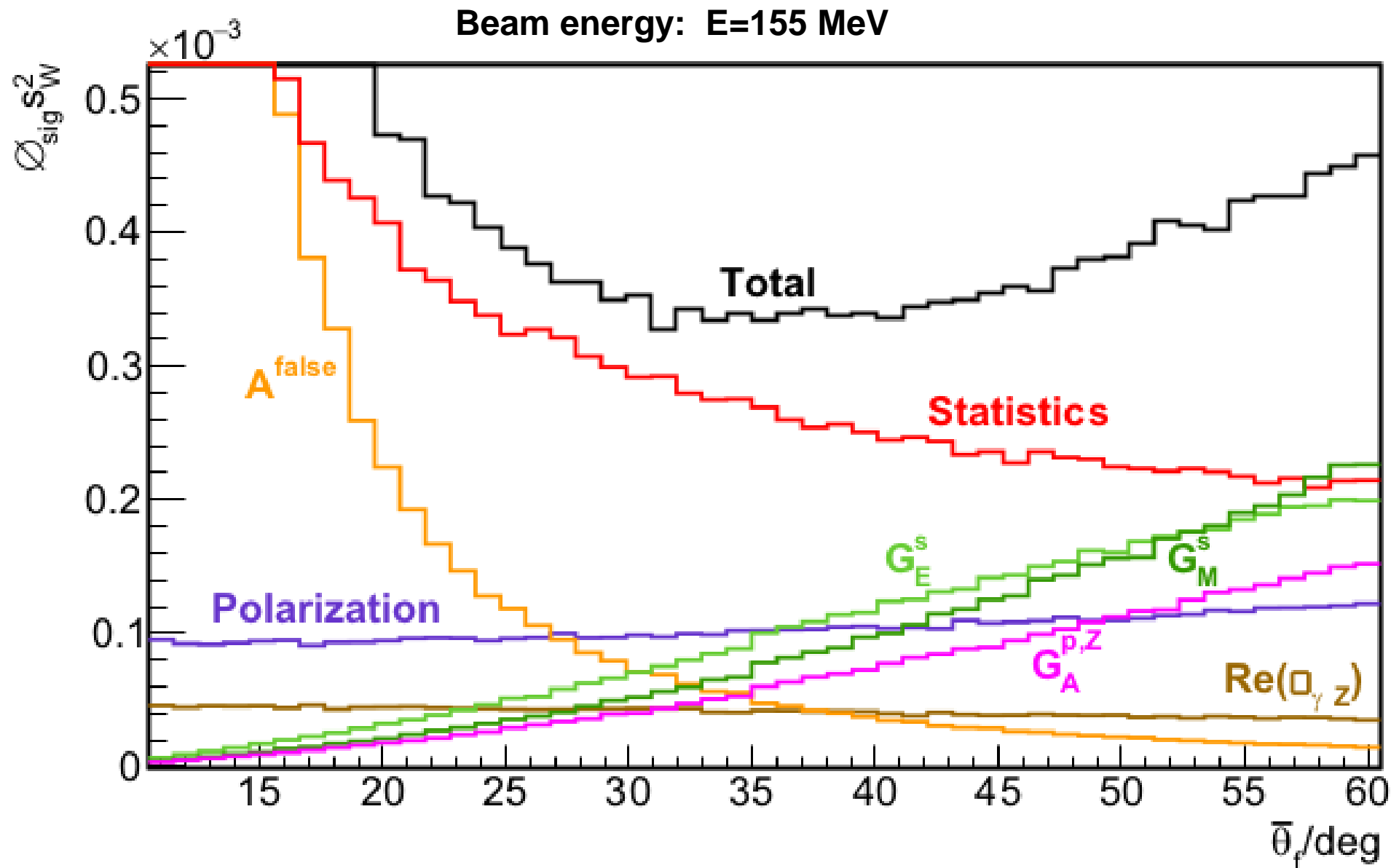
Strangeness and Isobreaking form factors...

Achievable precision in $\sin^2\theta_W$

Find the optimal kinematics for the experiment:
Variation of the scattering angle and the beam energy



Achievable precision in $\sin^2\Theta_W$



Achievable precision in $\sin^2\Theta_W$

E_{beam}	155 MeV
$\bar{\theta}_f$	35°
$\delta\theta_f$	20°
s_W^2	0.231 16
$\Delta_{\text{exp}} s_W^2$	3.7×10^{-4} (0.16 %)
$\Delta_{\text{exp, stat}} s_W^2$	3.1×10^{-4} (0.13 %)
$\Delta_{\text{exp, P}} s_W^2$	0.7×10^{-4} (0.03 %)
$\Delta_{\text{exp, false}} s_W^2$	0.6×10^{-4} (0.03 %)
$\Delta_{\text{exp, t.w.}} s_W^2$	1.2×10^{-4} (0.05 %)
$\Delta_{\text{exp, t.p.}} s_W^2$	0.1×10^{-4} (0.00 %)
$\Delta_{\text{exp, } \square_{\gamma Z}} s_W^2$	0.4×10^{-4} (0.02 %)
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**P2 Experiment
conditions**

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**P2 Achievable
precision**

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Statistics

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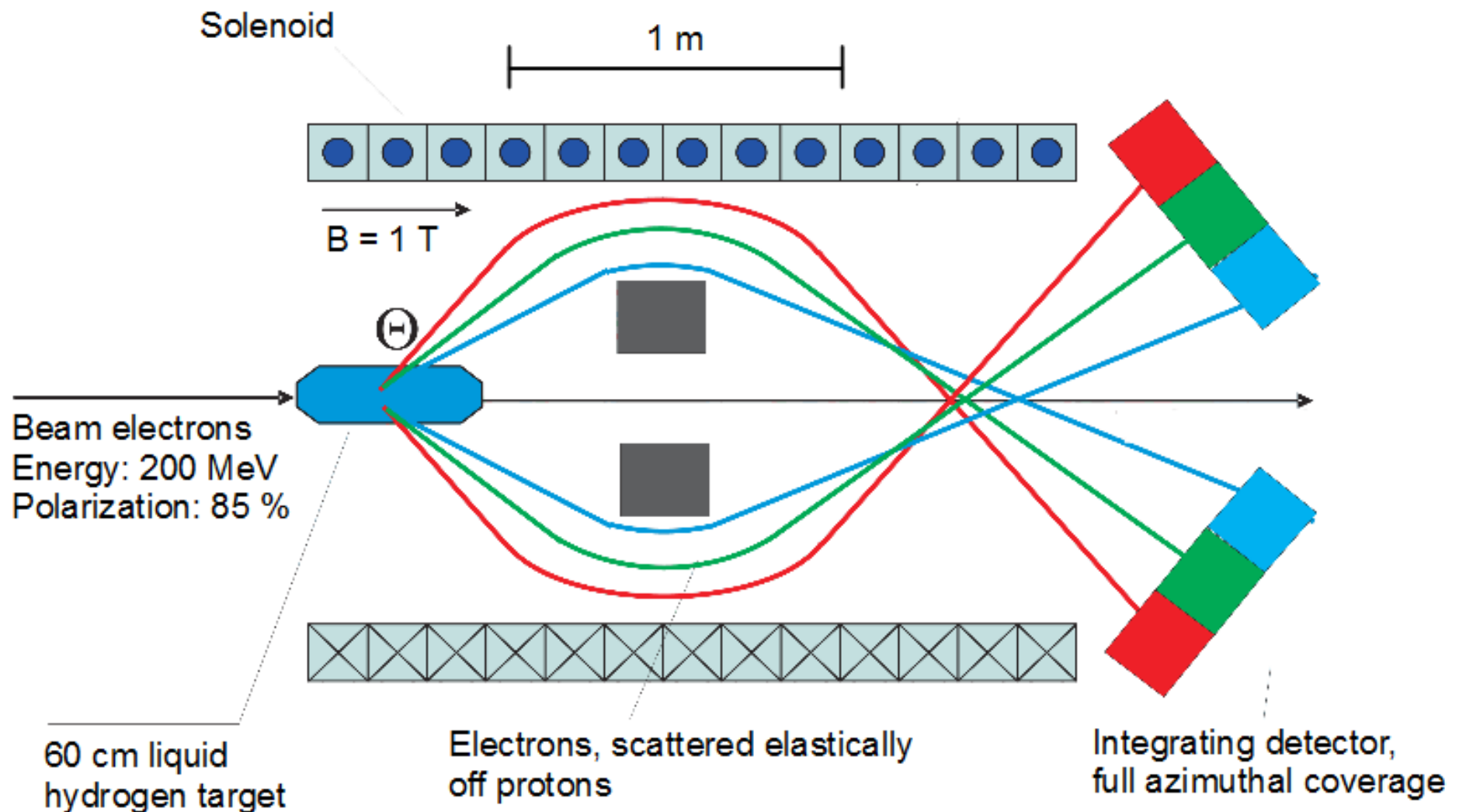
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False	$\Delta_{\text{exp, false}} s_W^2$	0.6×10^{-4} (0.03 %)
Asymmetries	$\Delta_{\text{exp, t.w.}} s_W^2$	1.2×10^{-4} (0.05 %)
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Spectrometer design

Principle:

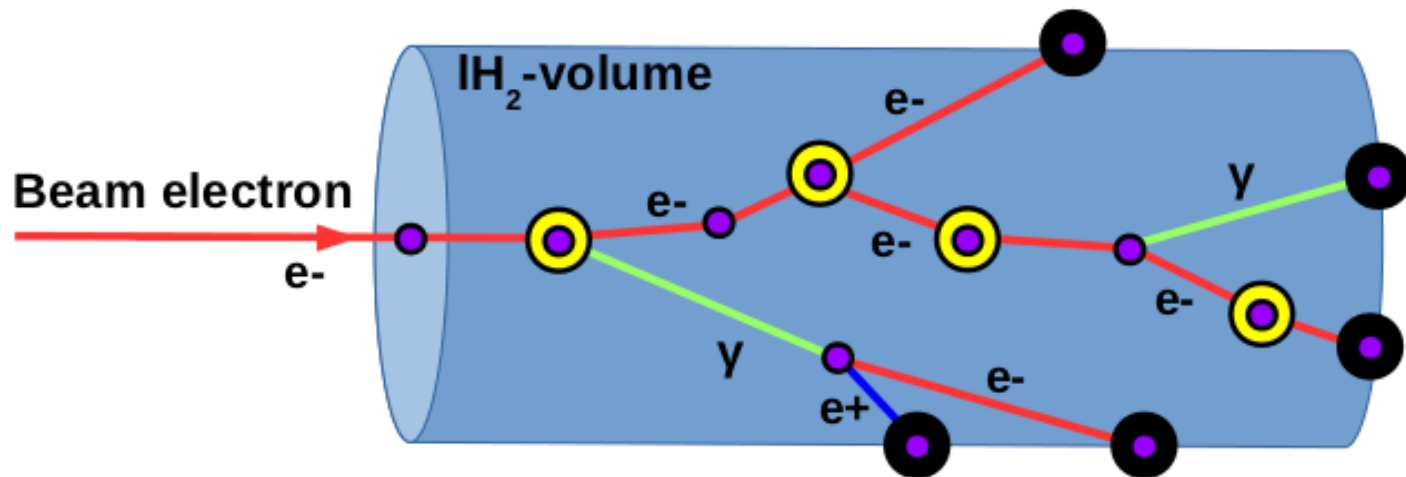
- Detect elastically scattered electrons
- Reject background events



Monte Carlo Studies

Full GEANT4 simulation with CAD Interface

First step: Generate ensemble of initial states in the target



● Endpoint of a propagation step

● Scan initial state of elastic e - p scattering

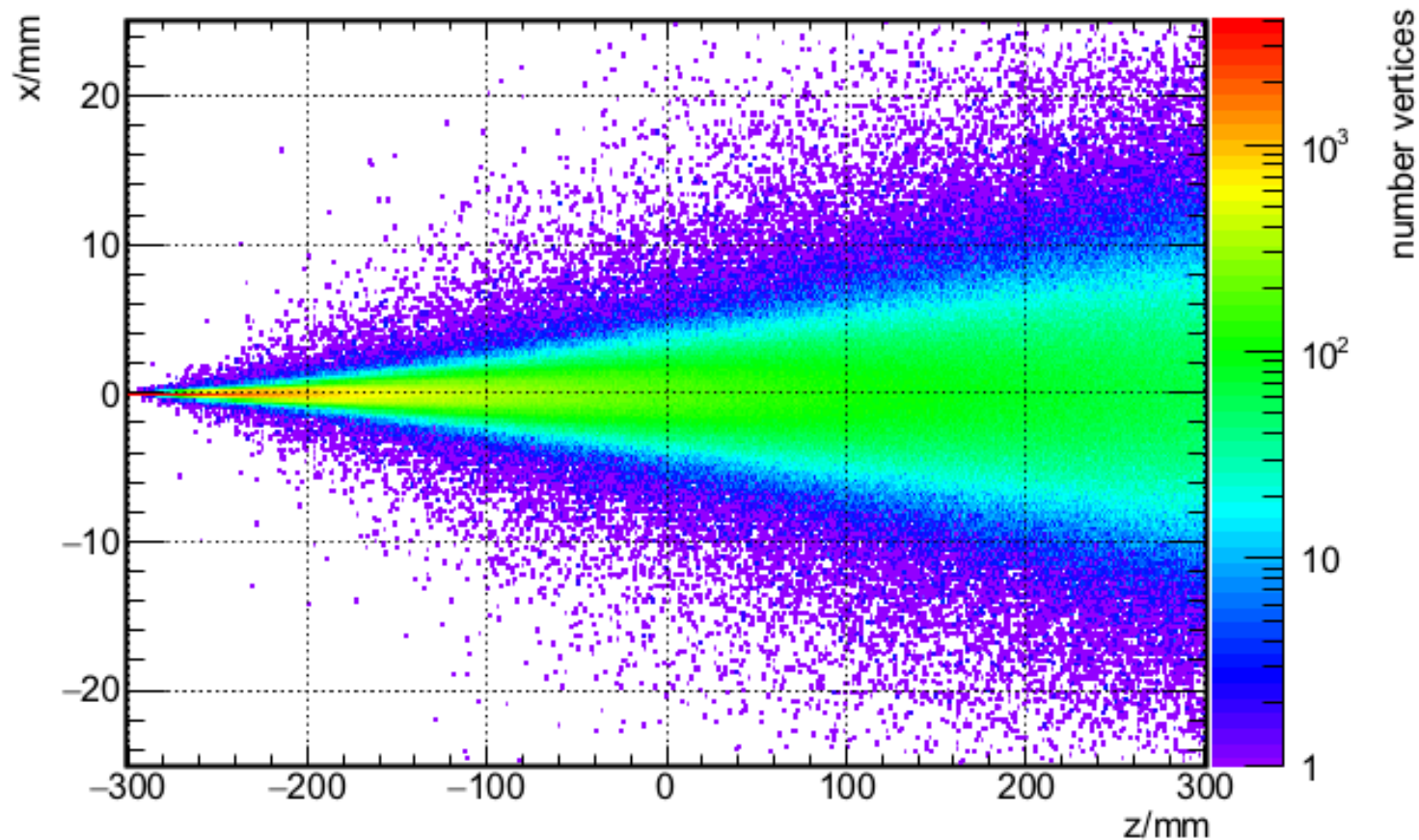
● Scan particle state and stop further propagation

Monte Carlo Studies

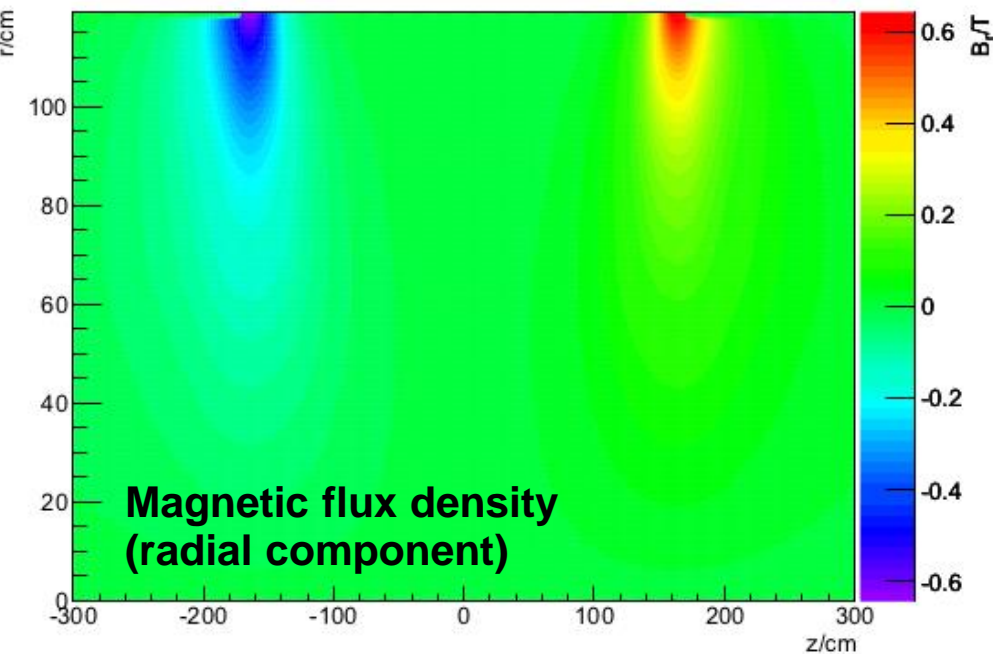
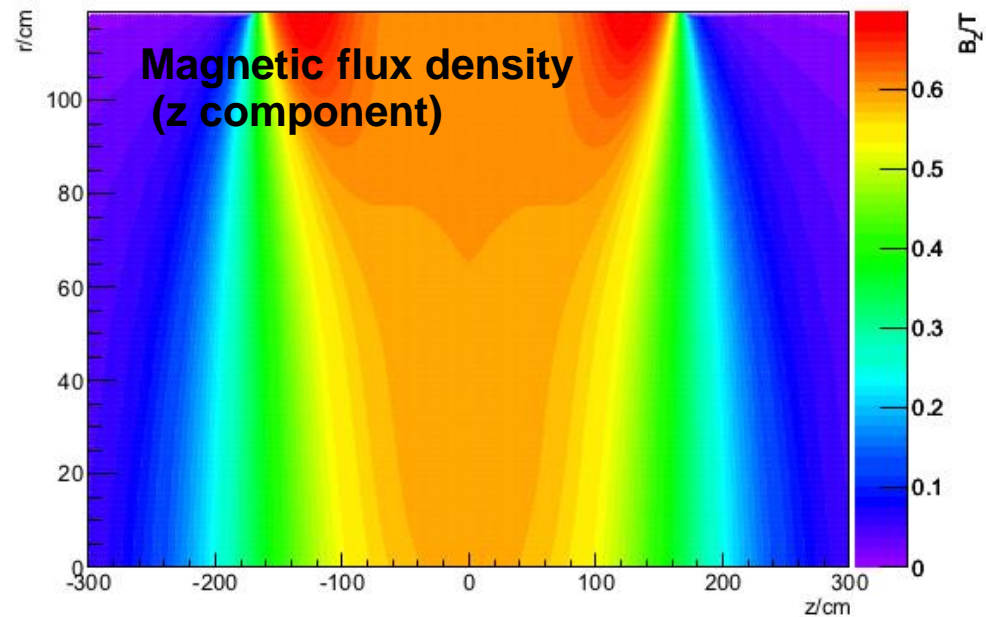
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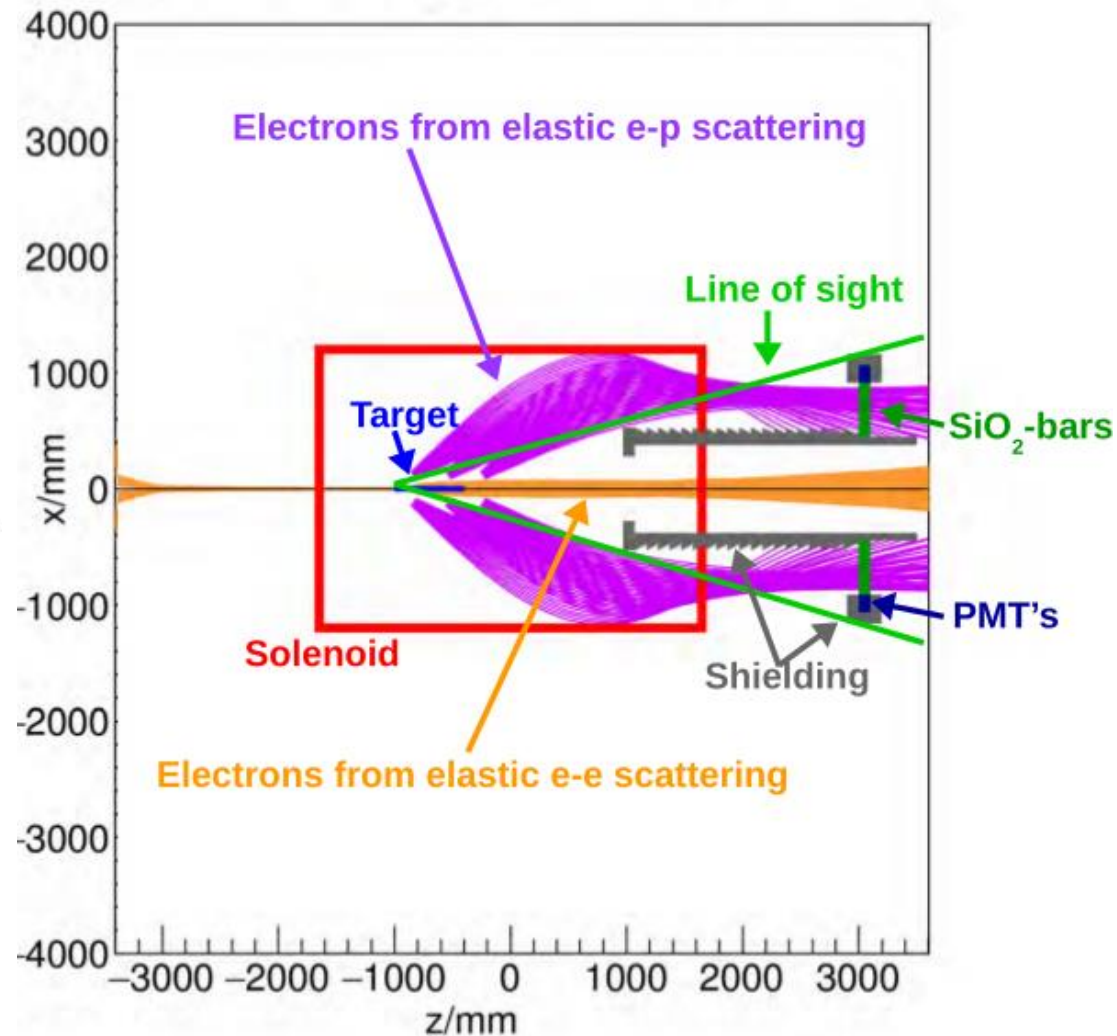
Spatial distribution of sampled vertices for ep scattering in the target



Monte Carlo Studies



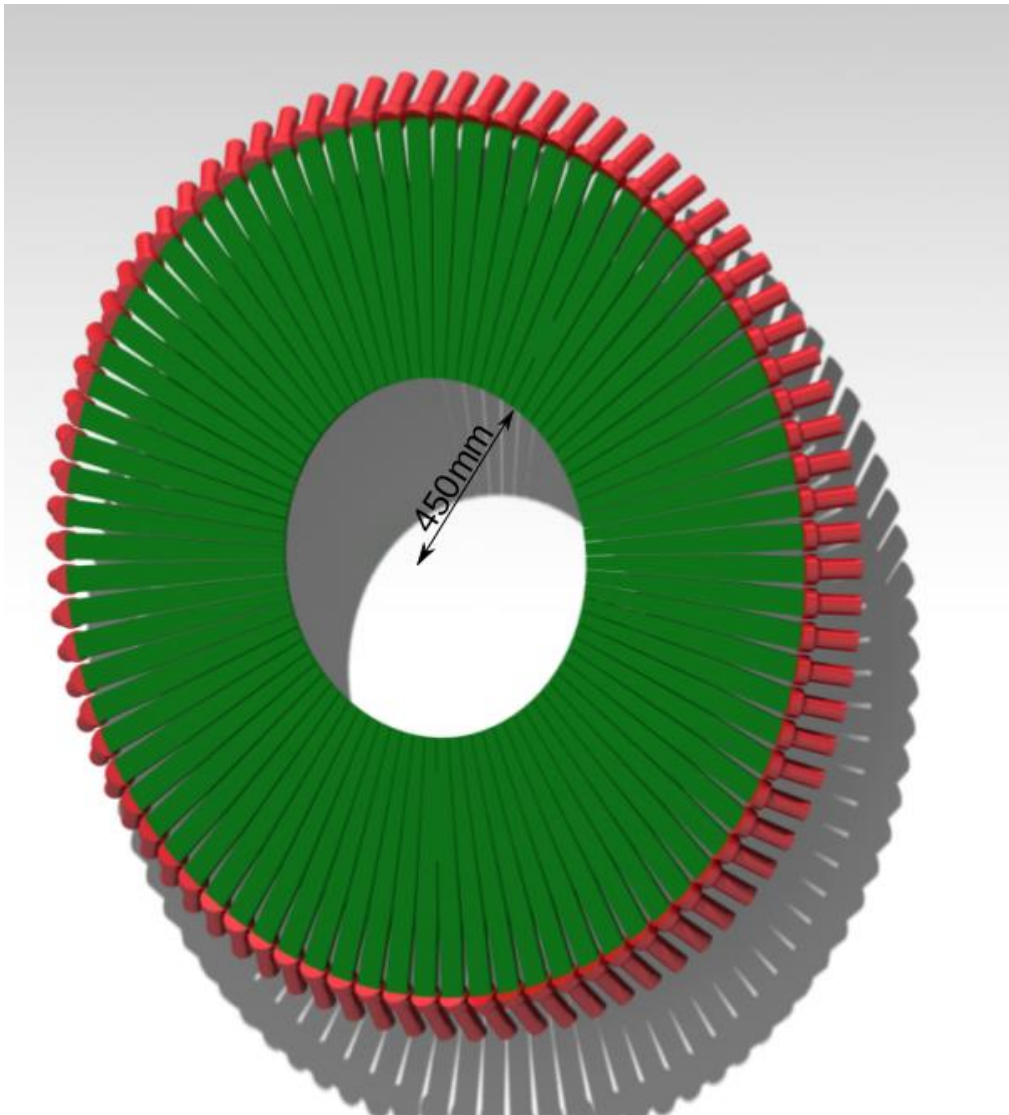
Second step: Particle tracking through the magnetic field



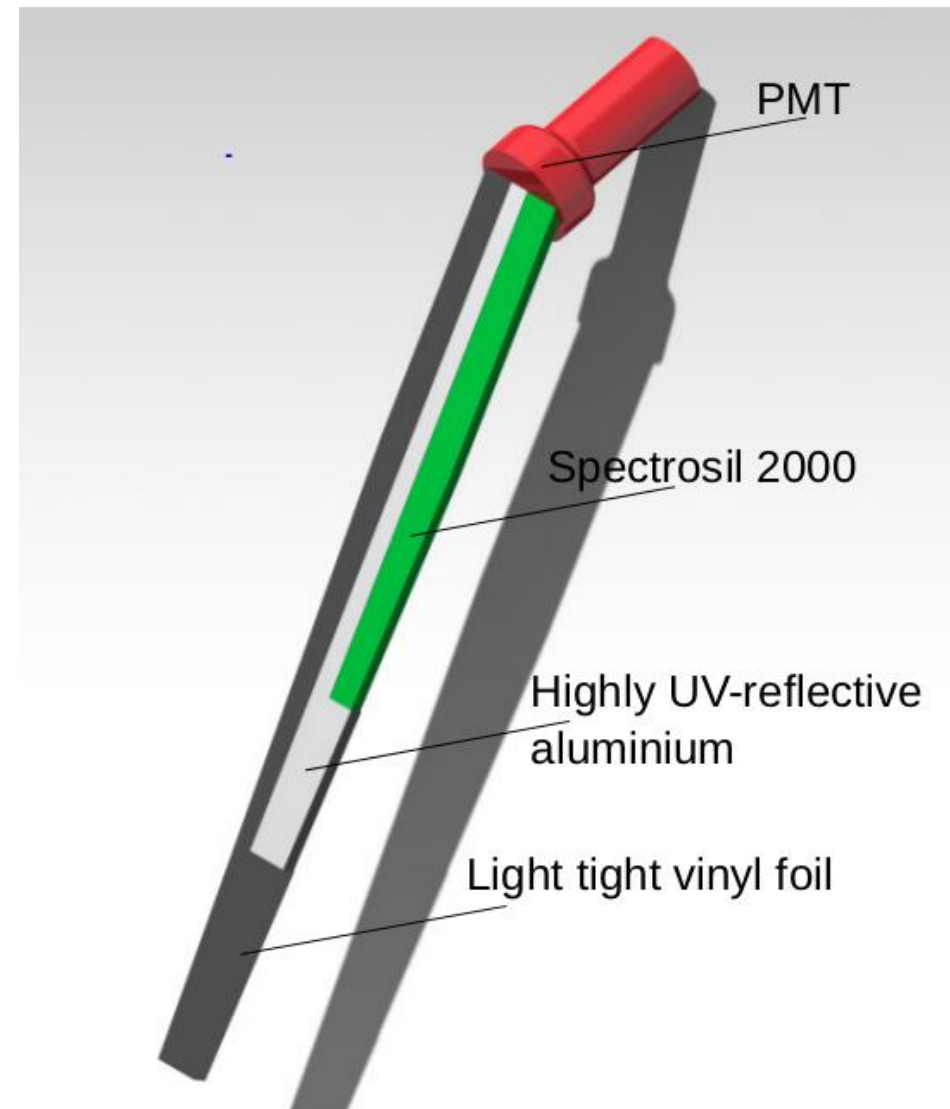
Detector development

Cover the whole azimuth with a radiation hard, fast detector

**Ring detector consisting
of 82 fused silica bars**

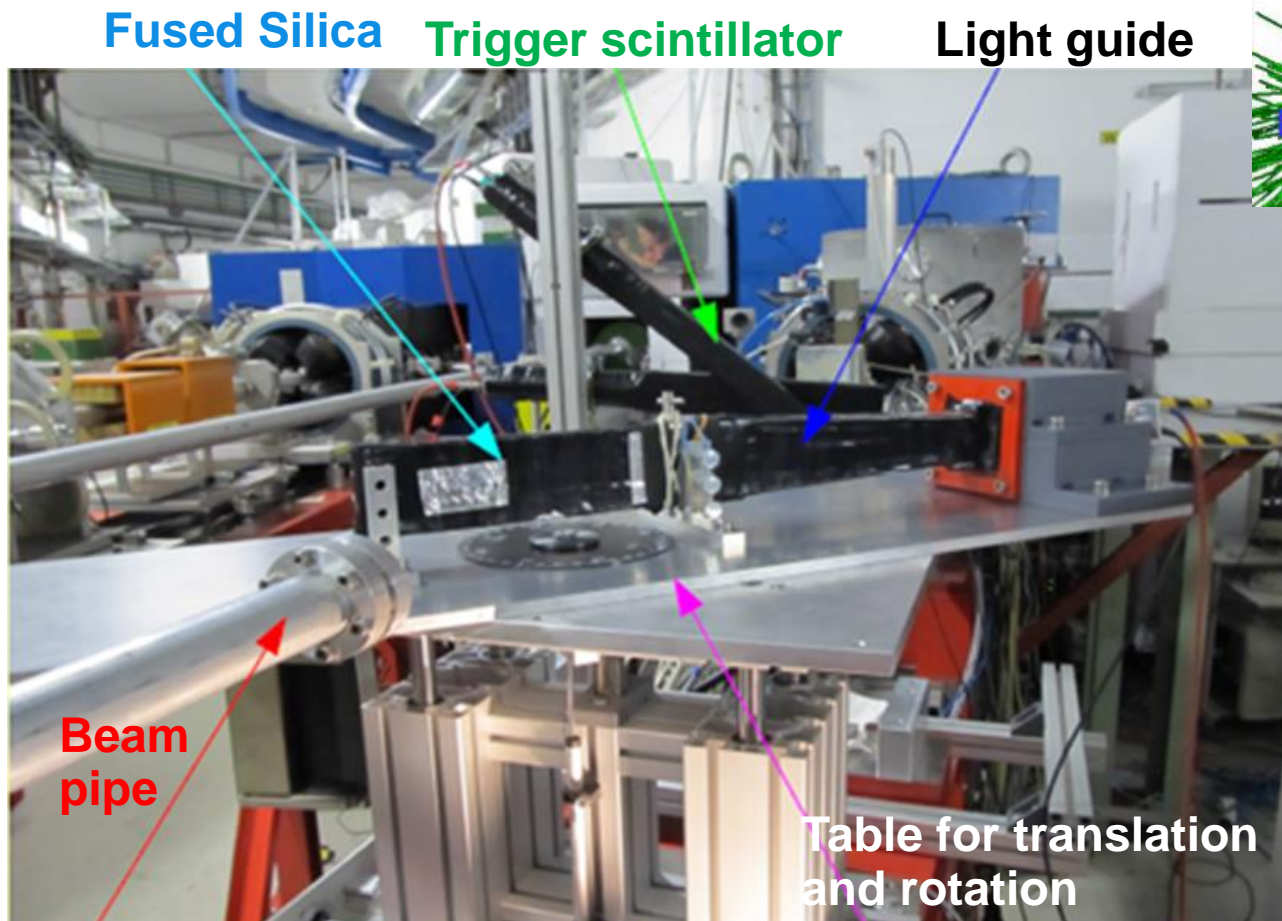
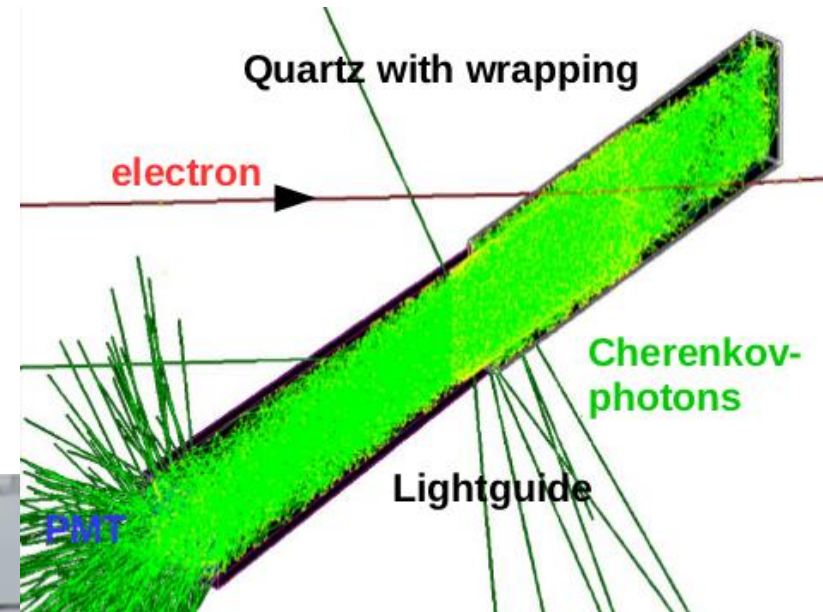


Single detector element



Monte Carlo Studies

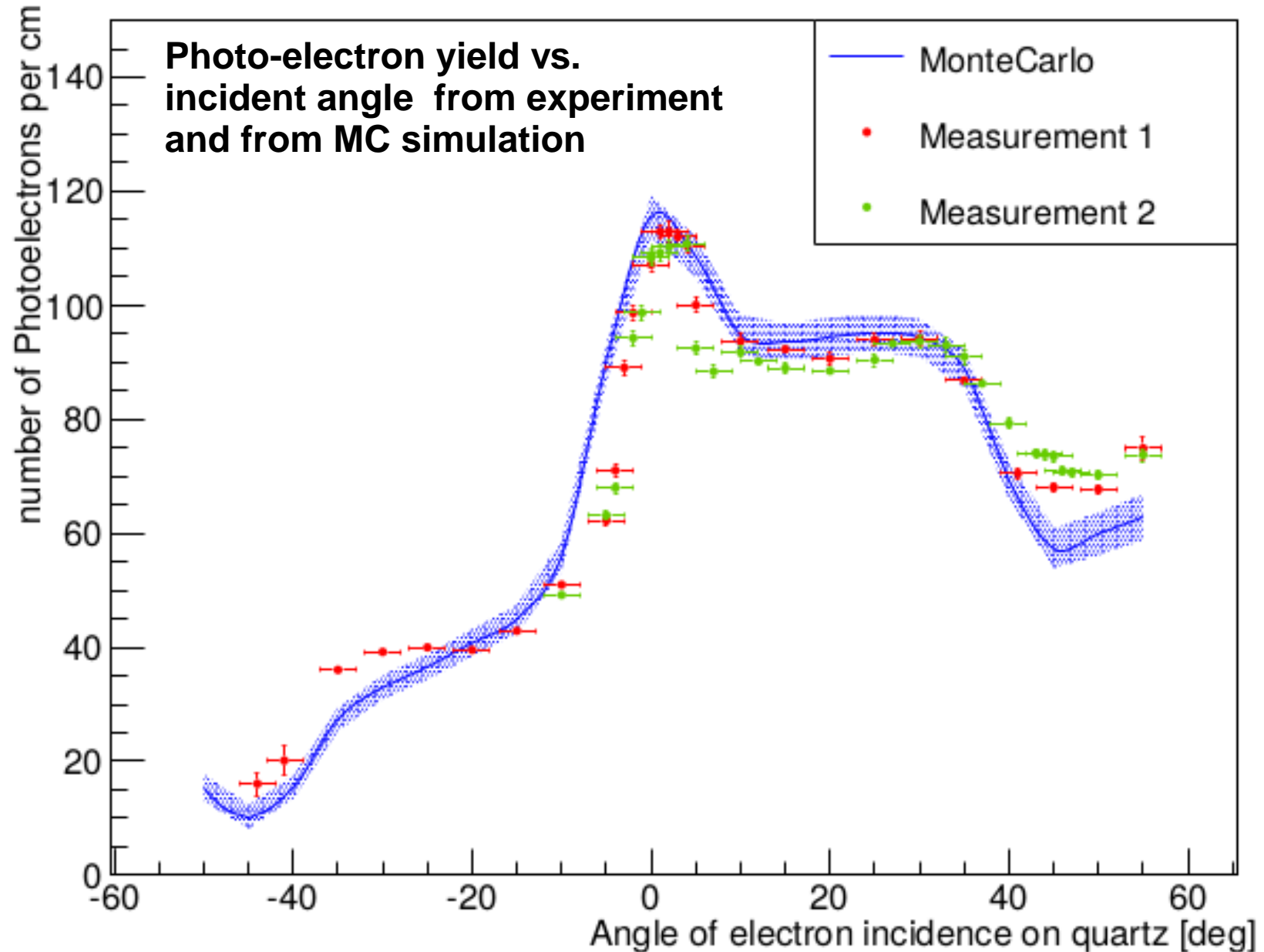
- MC Simulations for generation of Cherenkov light within the fused silica bars and the propagation of the photons in the material



- Beamtests at MAMI
 - electrons
 - photons

Benchmark Simulations with Measurements

Cherenkov detectors: Comparison experiment with MC simulation



Result of Monte Carlo Studies

**Predicted photo currents at the photocathodes from
particles hitting the detector**

Particle type	Photo current/ μA
Elastic ep scattering:	
Primary electrons, $\theta_f \in [25^\circ, 45^\circ]$	8.20×10^{-1} (56.55 %)
Primary electrons, $\theta_f \notin [25^\circ, 45^\circ]$	4.98×10^{-1} (34.34 %)
Secondary electrons	4.92×10^{-2} (3.39 %)
Secondary photons	2.61×10^{-2} (1.80 %)
Secondary positrons	9.88×10^{-3} (0.68 %)
Background processes:	
Electrons	4.07×10^{-2} (2.81 %)
Photons	5.57×10^{-3} (0.38 %)
Positrons	1.28×10^{-3} (0.09 %)
Total	1.45

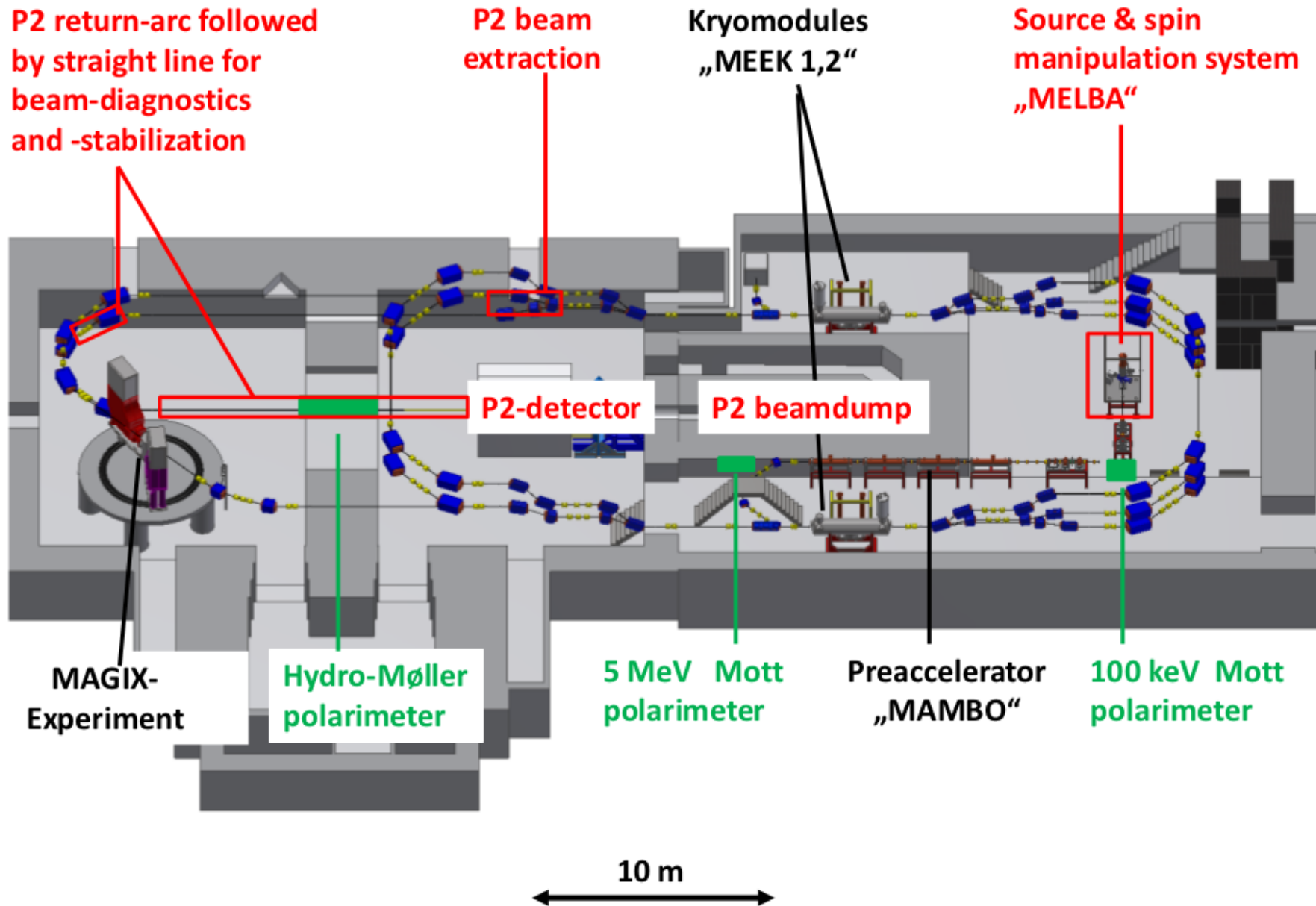
$$\langle Q^2 \rangle_{\text{exp}} = 4.82 \times 10^{-3} (\text{GeV}/c)^2$$

$$\langle A^{\text{raw}} \rangle_{\text{exp}} = -24.03 \text{ ppb}$$

$$\Delta_{\text{tot}} \langle A^{\text{raw}} \rangle_{\text{exp}} = 0.58 \text{ ppb}$$

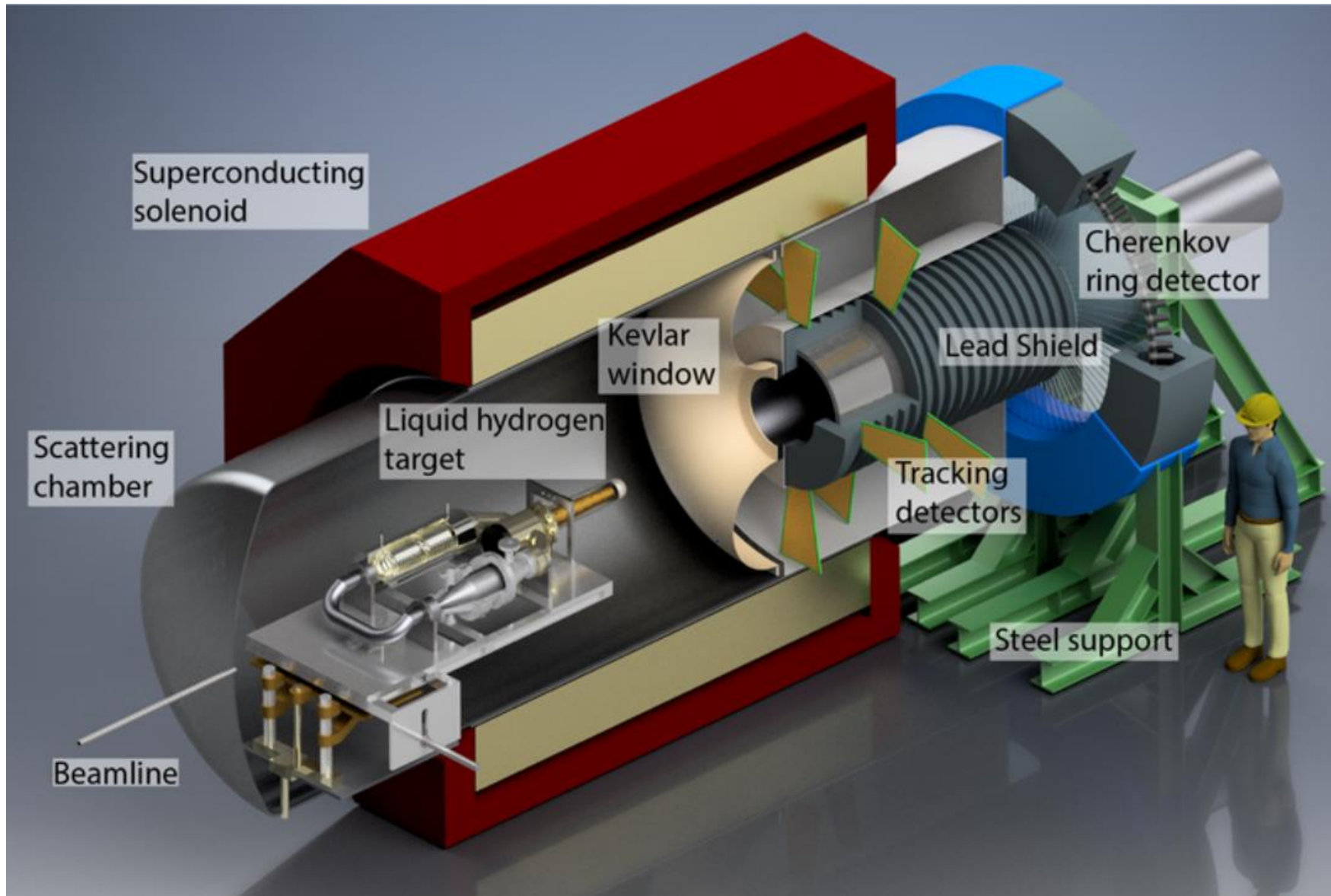
P2 experiment: Installation at a new accelerator facility

Mainz Energy recovering Superconducting Accelerator



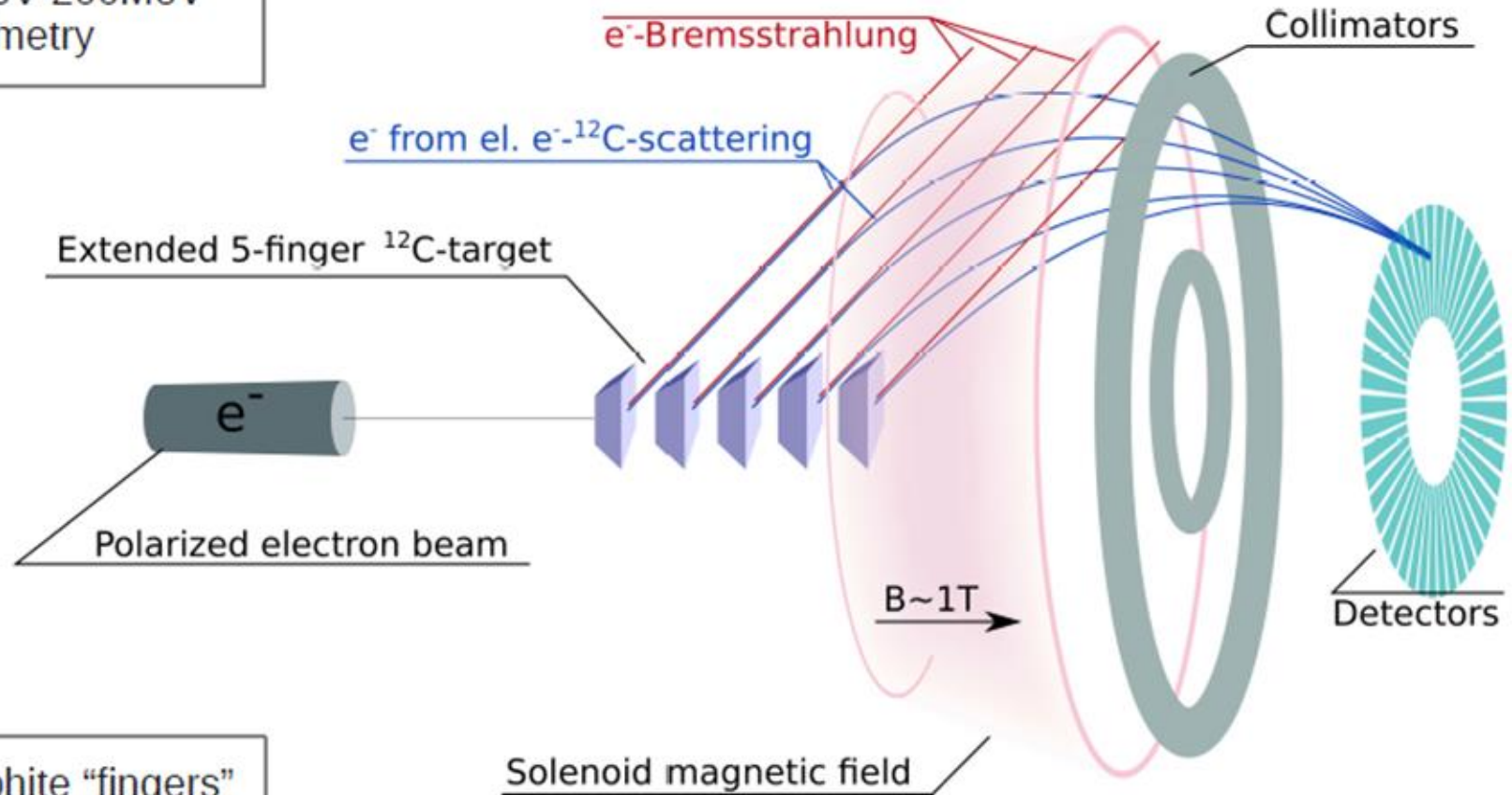
Spectrometer design

Current CAD design of the P2 apparatus



Further physics program: Measurement with ^{12}C

- MESA:
- 150 μA
 - 150 MeV-200 MeV
 - Polarimetry

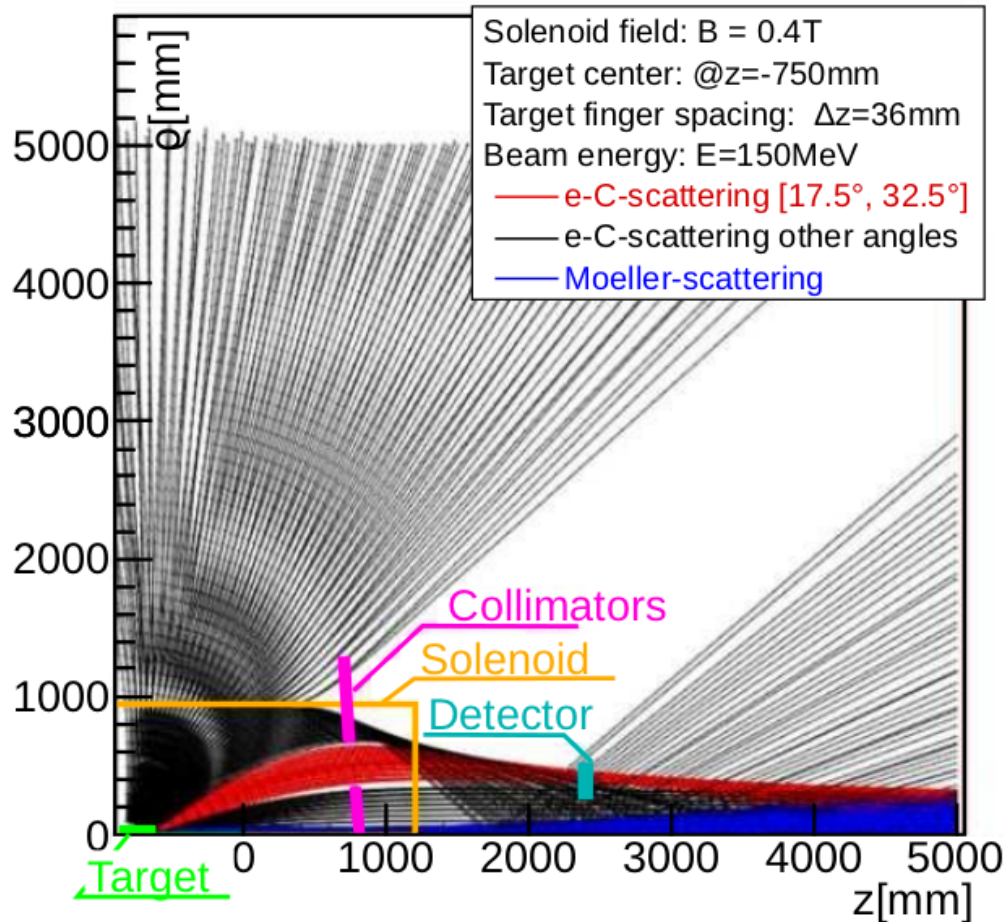


- Target:
- 5 graphite "fingers"
 - 5 g/cm 2 total
 - 36mm spacing

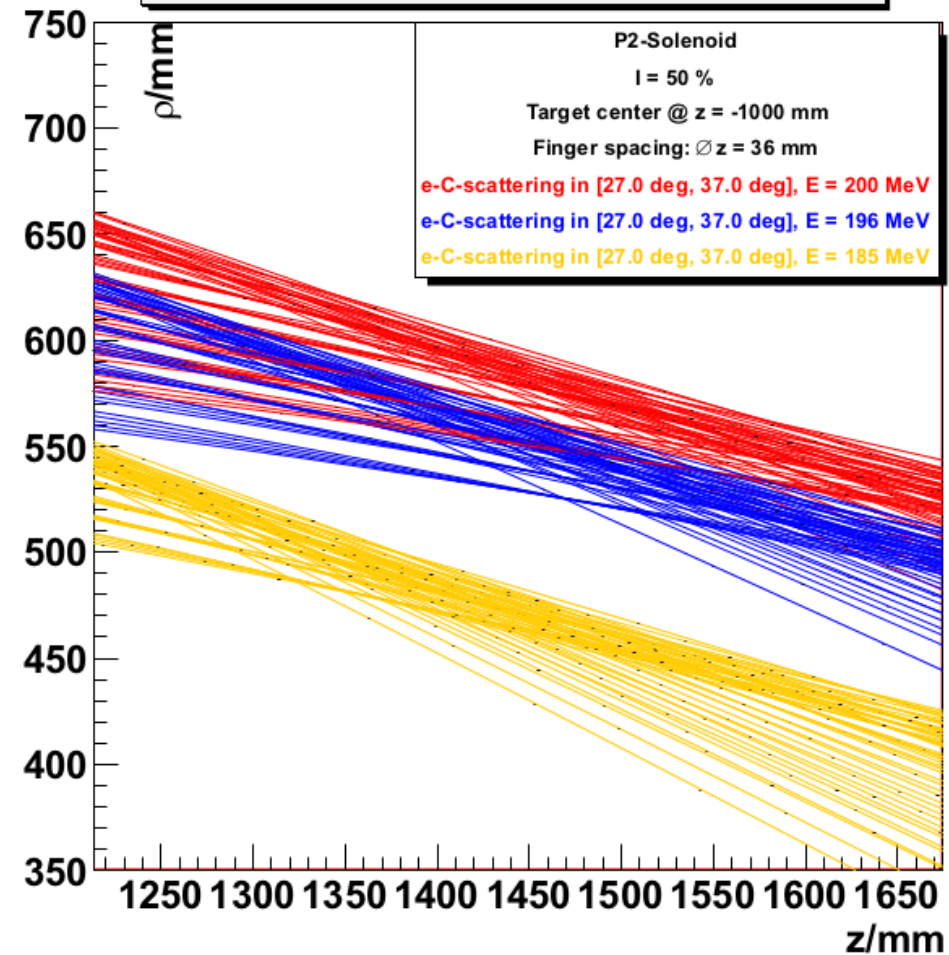
Further physics program: Measurement with ^{12}C

Raytracing study for the P2 solenoid:

Projection of electron trajectories



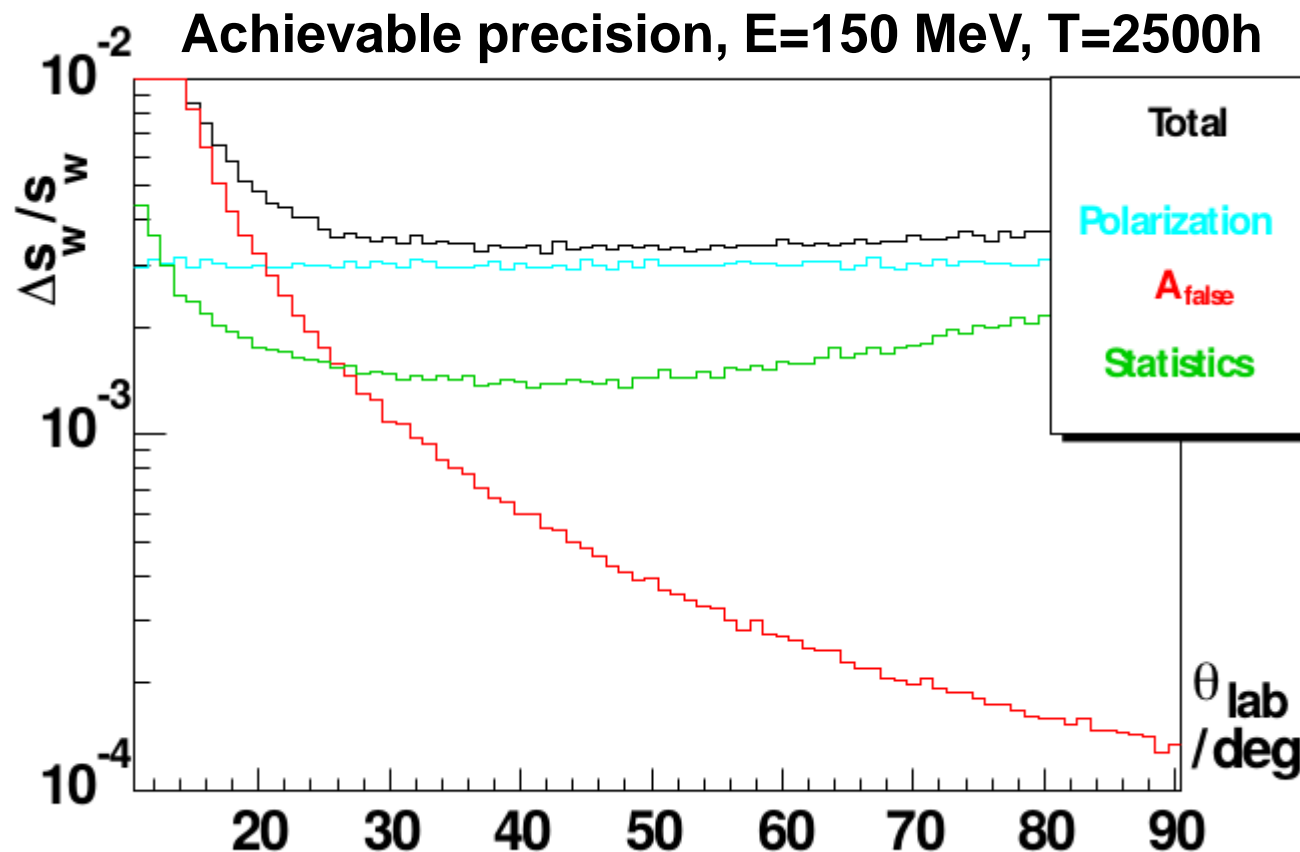
Projection of electron trajectories



Further physics program: Measurement with ^{12}C

Weak charge of the ^{12}C nucleus: $Q_W(^{12}\text{C}) = -24 \sin^2 \theta_W$

Precision in the Weak Mixing Angle is dominated by Polarization uncertainty



Further physics program: Measurement with ^{12}C

- Complimentary sensitivity to certain classes of new physics models
- Weak charged of different targets expressed with the Peskin-Takeuchi parameters:

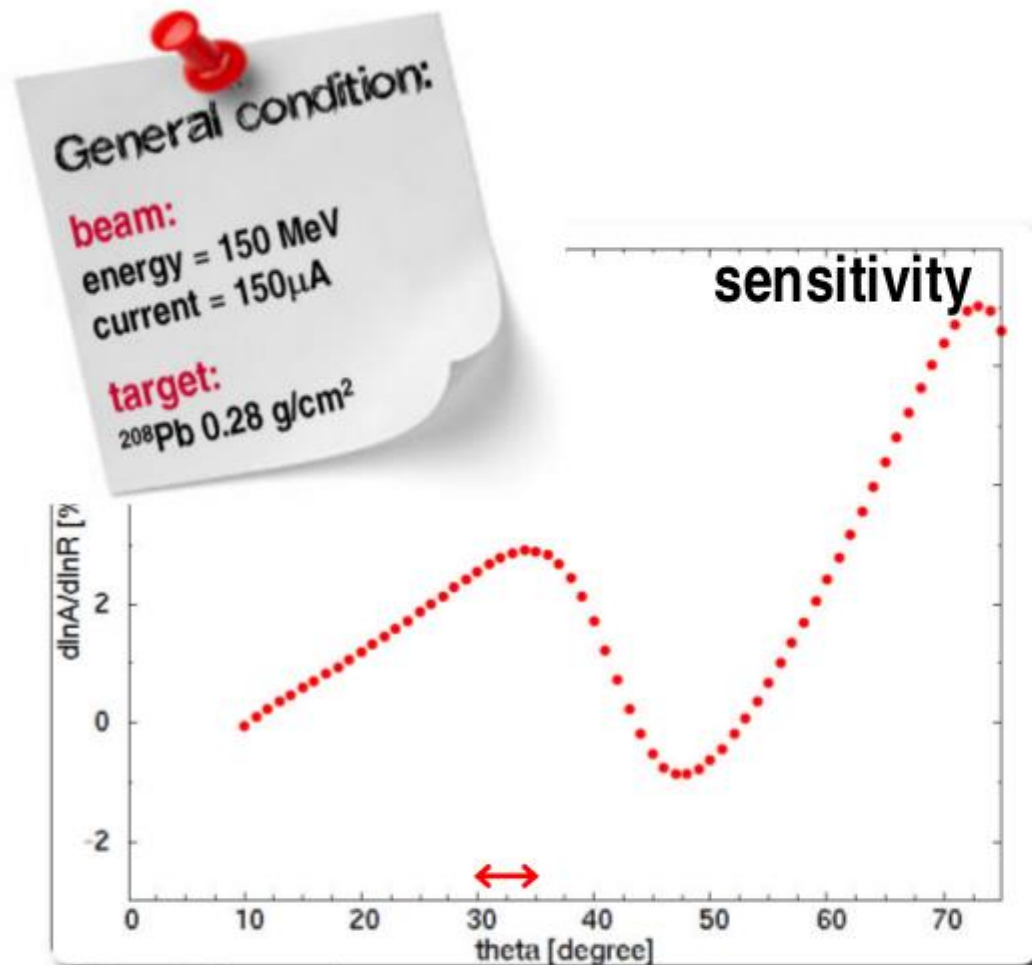
$$Q_W(^{12}\text{C}) = -5.510[1 - 0.003T + 0.016S - 0.033X - \chi],$$

$$Q_W(\text{p}) = +0.0707[1 + 0.15T - 0.21S + 0.43X + 4.3\chi],$$

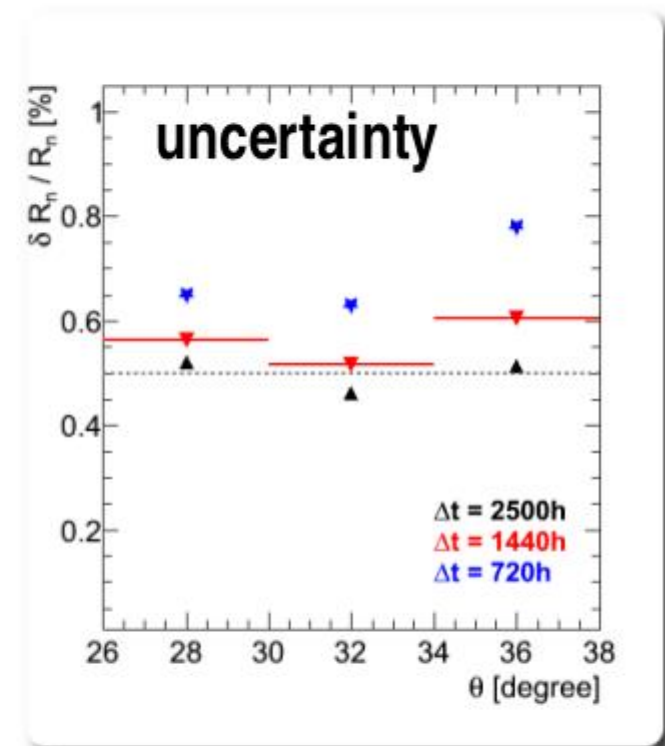
$$Q_W(\text{e}) = -0.0435[1 + 0.25T - 0.34S + 0.7X + 7\chi],$$

$$Q_W(^{133}\text{Cs}) = -73.24[1 + 0.011S - 0.023X - 0.9\chi]$$

Further physics program: Neutron skin



Chuck Horowitz

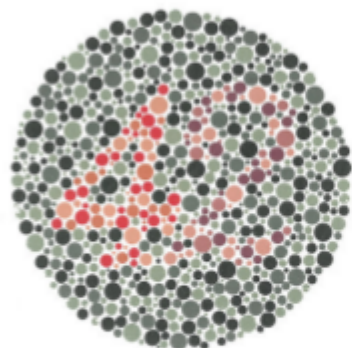


$\Delta\theta=4^\circ$: expected rate = 8.25 GHz, $A_{pV} = 0.66$ ppm, $P = 85\%$, $Q \approx 86$ MeV

$1440\text{h} \rightarrow \delta R_n / R_n = 0.52\% (^{208}\text{Pb} @ 155 \text{ MeV})$

Further physics program: Neutron skin

ray trace simulation



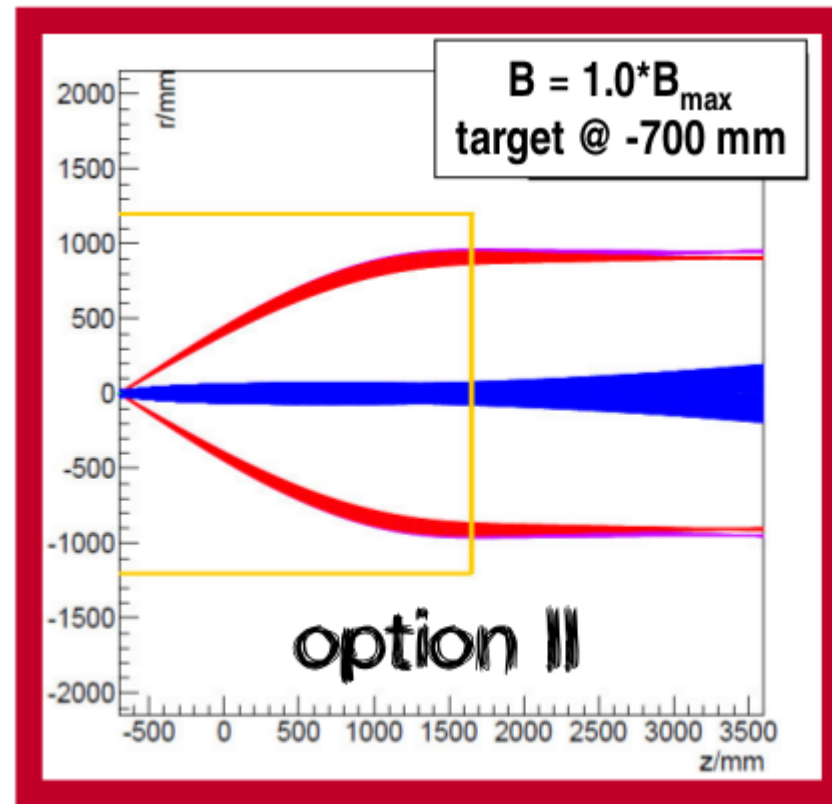
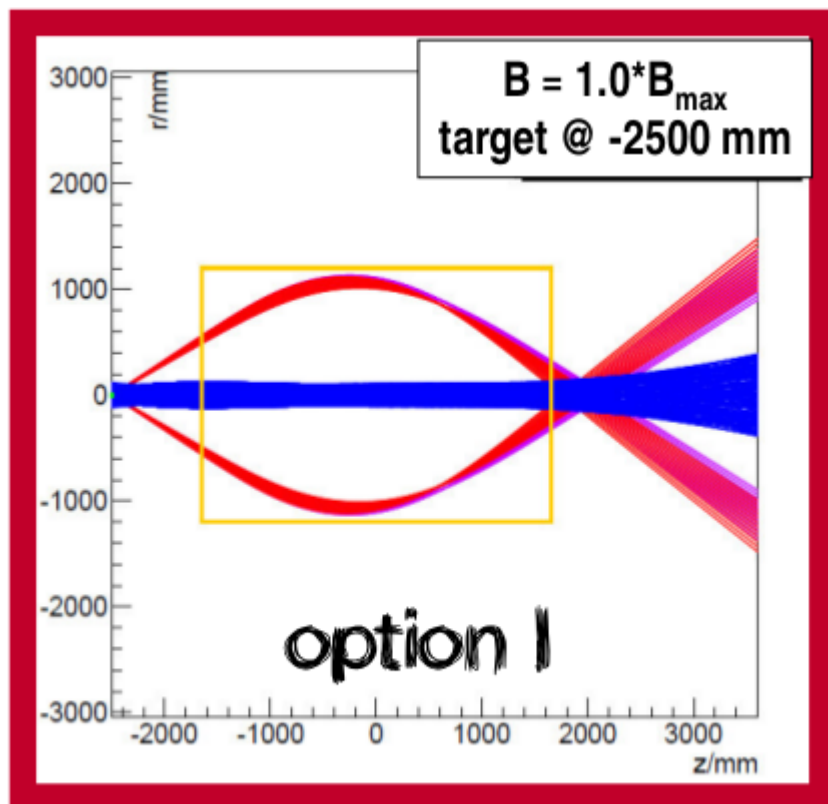
resolve elastic?

$$\Delta E (^{208}\text{Pb}) = 2.7 \text{ MeV}$$

vary magnetic field strength
(0.1 T to 0.6 T)

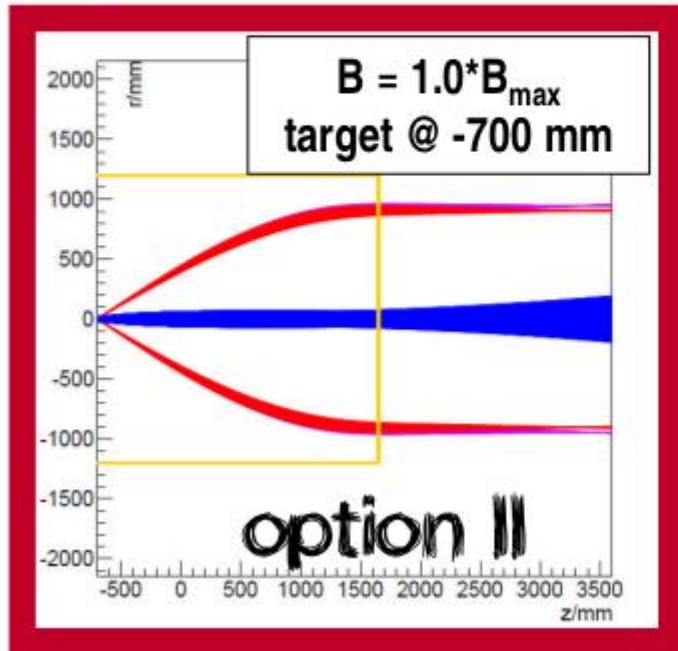


scan of target position
(-2500 mm to 0 mm)



Further physics program: Neutron skin

ray trace simulation



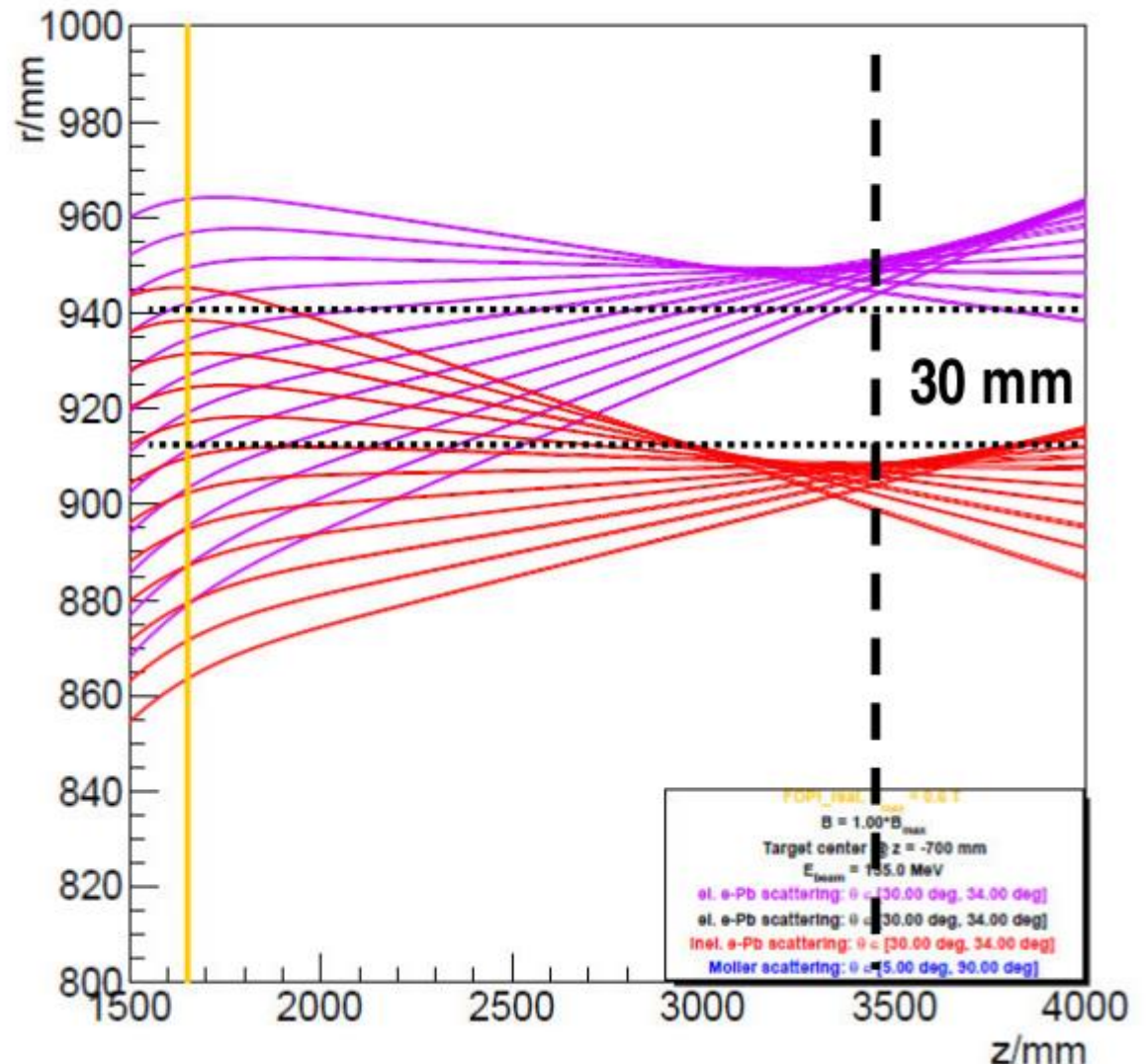
PRO:

similar to P2 design

(maybe) easier shielding

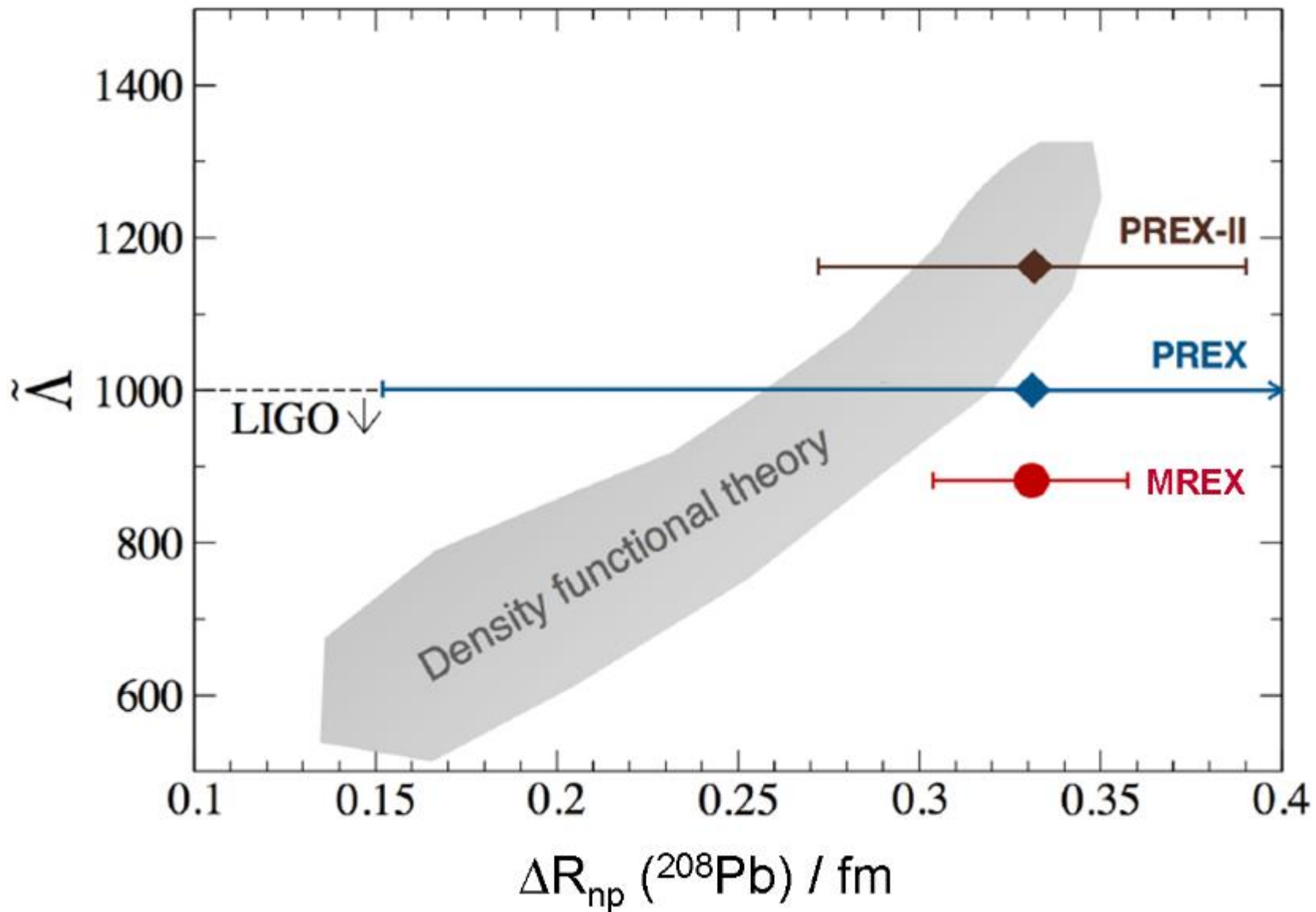
CON:

(maybe) not enough space
after the solenoid



Further physics program: Neutron skin

Projected precision compared to PREX:



Summary and outlook

- P2: A new experiment to measure the weak mixing angle at low energy
- Makes use of the polarized high current electron beam from the new MESA accelerator
- Extensive simulations and beam tests at MAMI
- $\Delta\sin^2\Theta_W=3.7\times 10^{-4}$ (0.16%) expected: Sensitive for BSM physics
- Construction is scheduled to begin end of year 2020