



# Nucleon 3D Imaging Program with SoLID at Jefferson Lab

SPIN 2018

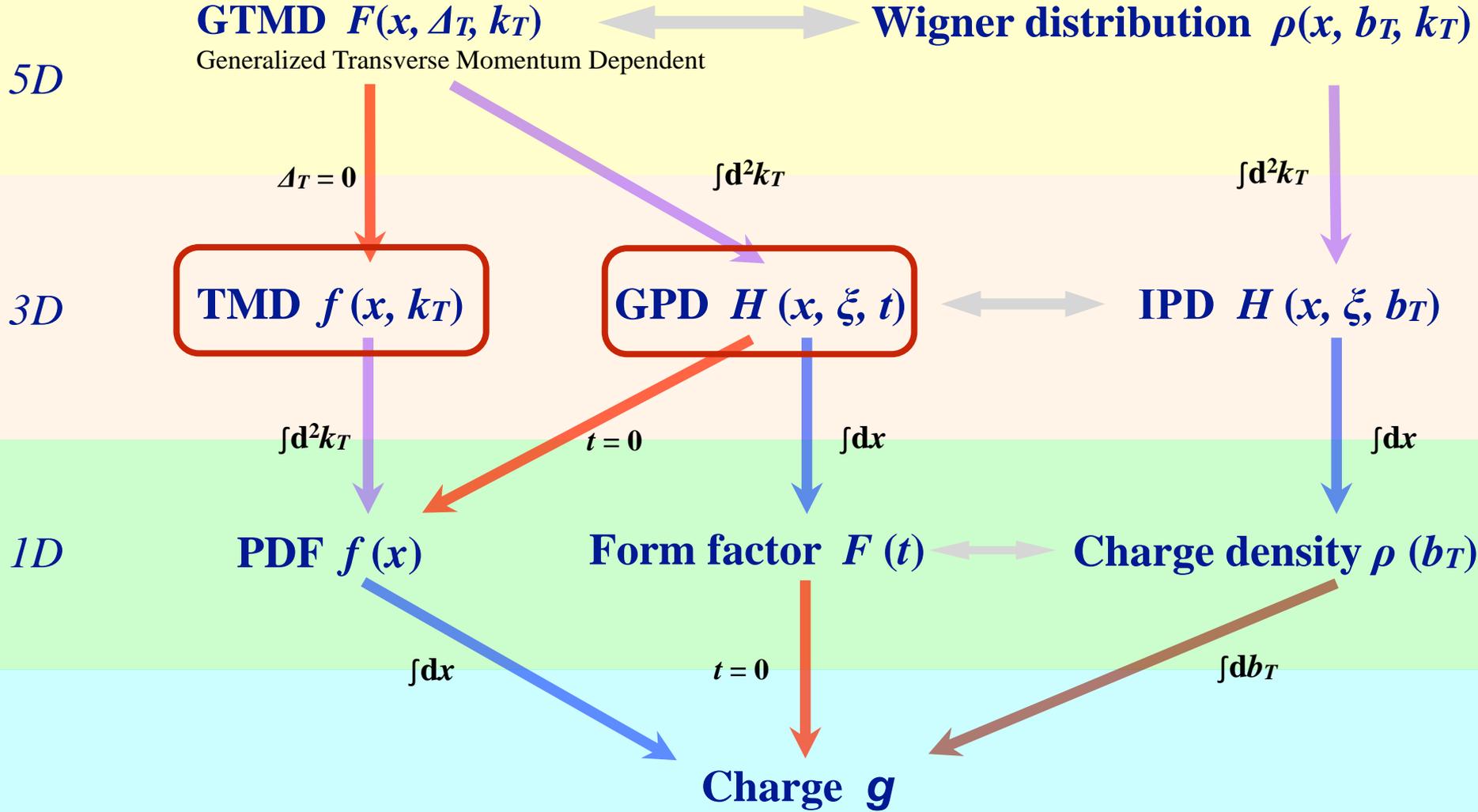
Sep 10-14<sup>th</sup> 2018, Ferrara, Italy

Zhiwen Zhao (*Duke University*)

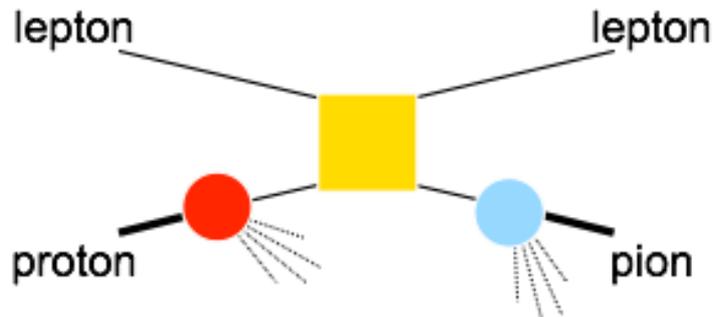
For the **SoLID** Collaboration

# Unified View of Nucleon Structure

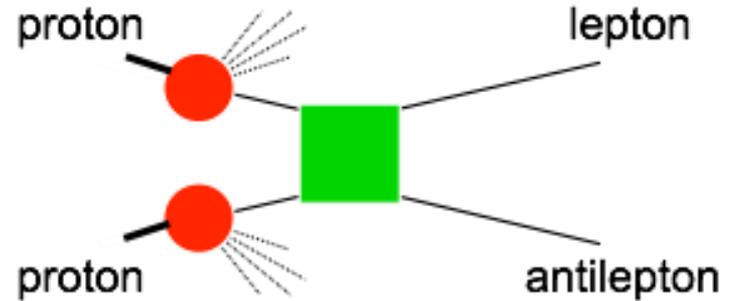
*Light-front wave function  $\Psi(x_i, k_{Ti})$*



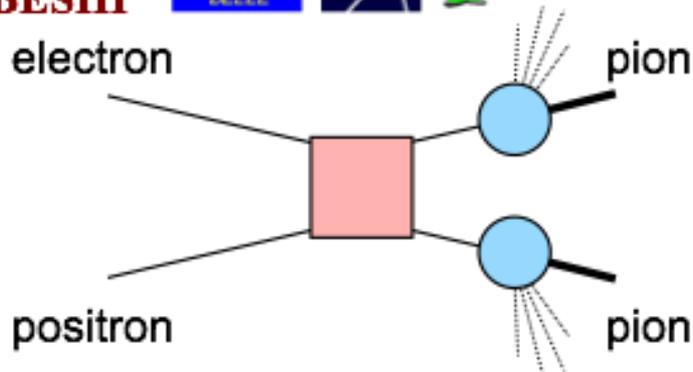
# Access TMDs through Hard Processes



SIDIS



Drell-Yan

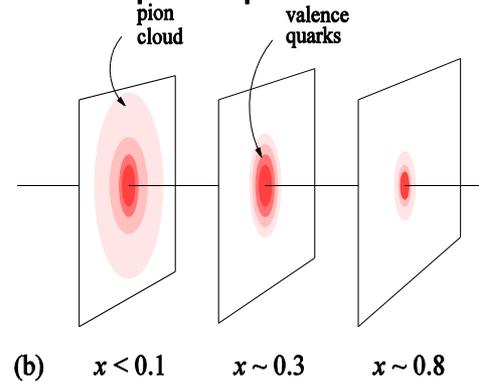
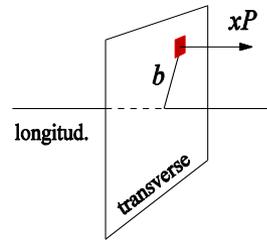
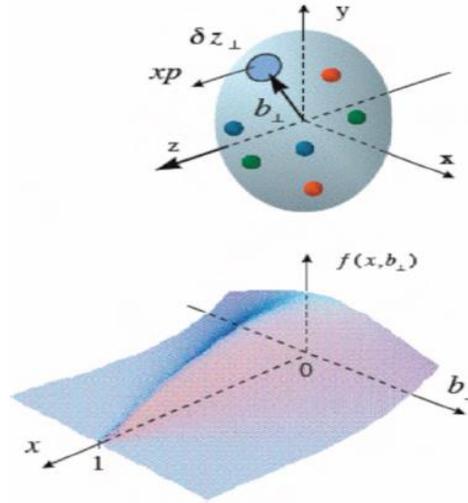


$e^-e^+$  to pions

-  Partonic scattering amplitude
-  Fragmentation amplitude
-  Distribution amplitude

# Generalized Parton Distribution (GPD)

A unified descriptions of partons (quarks and gluons) in the momentum and impact parameter space



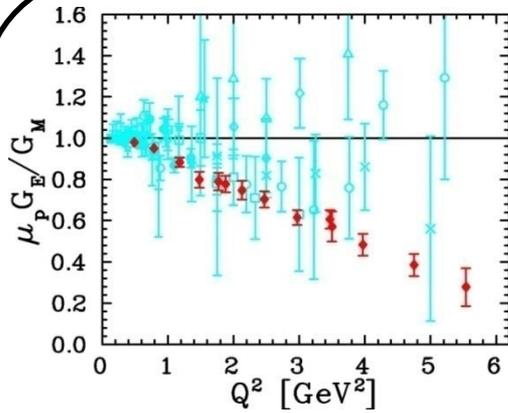
(a)

(b)

$x < 0.1$

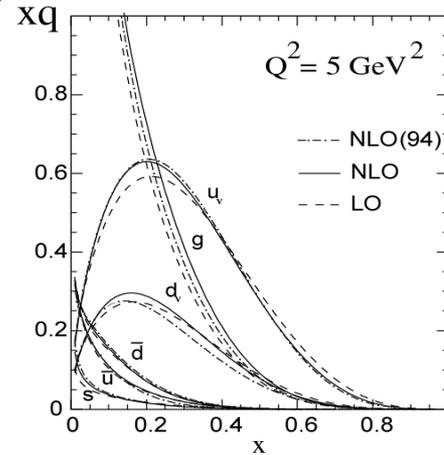
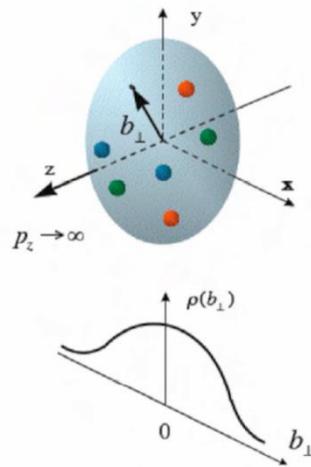
$x \sim 0.3$

$x \sim 0.8$



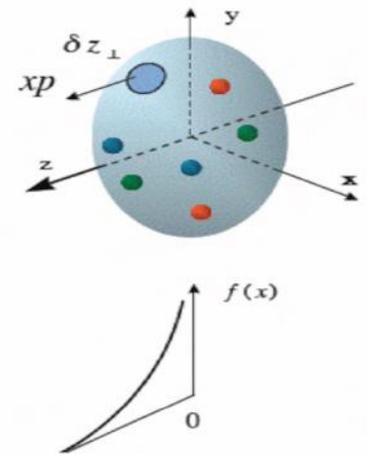
Elastic form factors

Transverse spatial distributions



Parton Distribution Functions

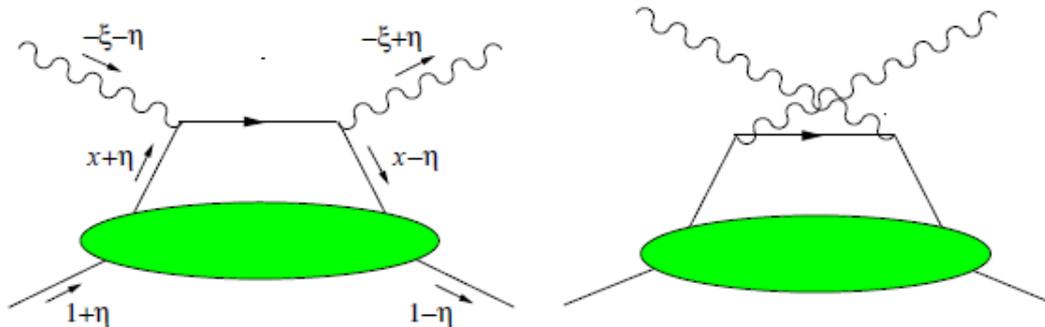
Longitudinal momentum distributions



# General Compton Process accessing GPD

$$\gamma(q) + p(p) \rightarrow \gamma(q') + p(p')$$

$$Q^2 = -q^2, \quad Q'^2 = q'^2, \quad s = (p + q)^2, \quad t = \Delta^2,$$



DVCS	$(\gamma' \rightarrow \gamma)$
TCS	$(\gamma \rightarrow \gamma')$
DDVCS	$(\gamma' \rightarrow \gamma')$

Compton Form Factor (CFF)

$$\mathcal{H}_1(\xi, \eta, t) = \sum_q e_q^2 \int_{-1}^1 dx \left( \frac{H^q(x, \eta, t)}{\xi - x - i\epsilon} - \frac{H^q(x, \eta, t)}{\xi + x - i\epsilon} \right),$$

$$\mathcal{E}_1(\xi, \eta, t) = \sum_q e_q^2 \int_{-1}^1 dx \left( \frac{E^q(x, \eta, t)}{\xi - x - i\epsilon} - \frac{E^q(x, \eta, t)}{\xi + x - i\epsilon} \right),$$

$$\tilde{\mathcal{H}}_1(\xi, \eta, t) = \sum_q e_q^2 \int_{-1}^1 dx \left( \frac{\tilde{H}^q(x, \eta, t)}{\xi - x - i\epsilon} + \frac{\tilde{H}^q(x, \eta, t)}{\xi + x - i\epsilon} \right),$$

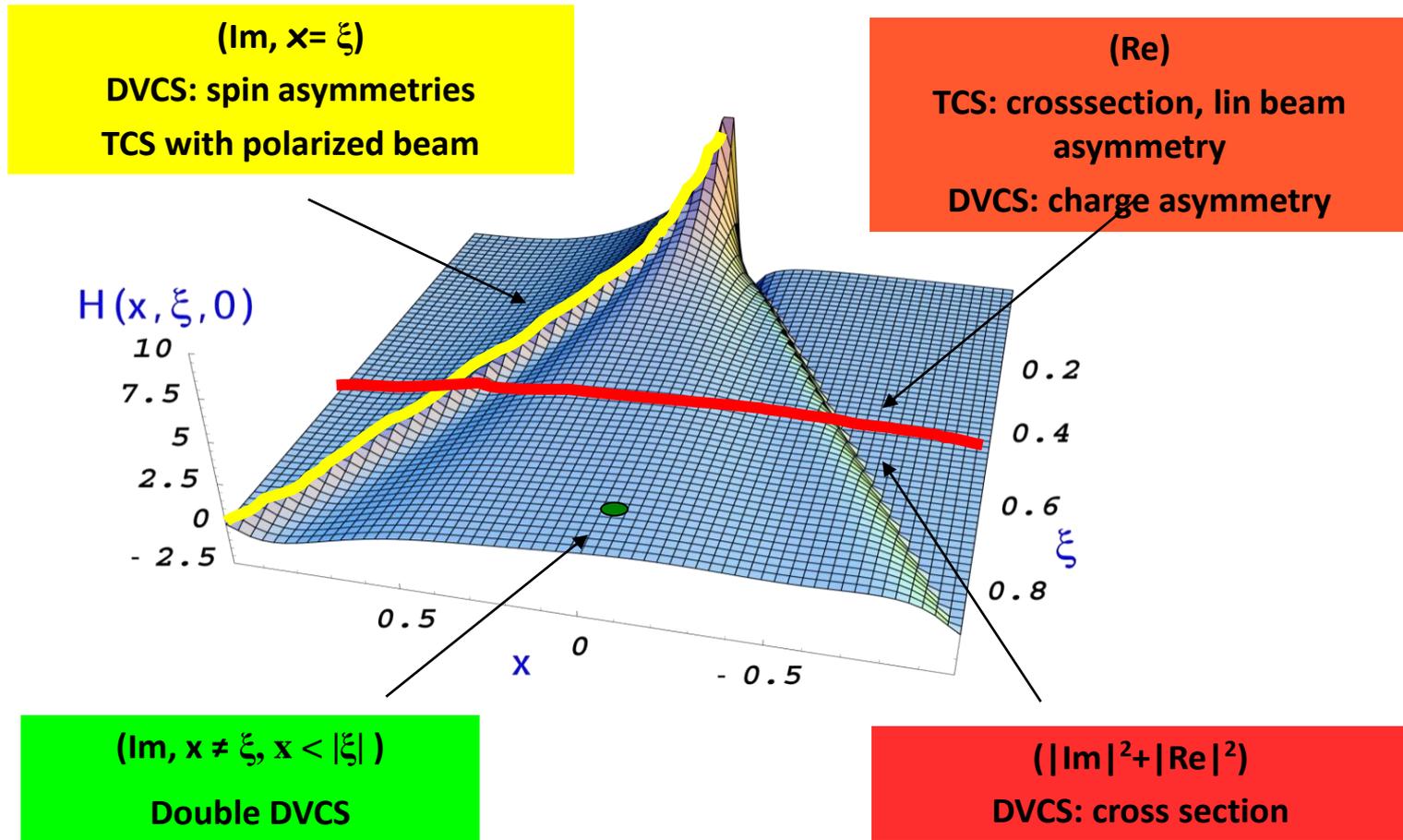
$$\tilde{\mathcal{E}}_1(\xi, \eta, t) = \sum_q e_q^2 \int_{-1}^1 dx \left( \frac{\tilde{E}^q(x, \eta, t)}{\xi - x - i\epsilon} + \frac{\tilde{E}^q(x, \eta, t)}{\xi + x - i\epsilon} \right)$$

$$\xi = -\frac{(q + q')^2}{2(p + p') \cdot (q + q')} \approx \frac{Q^2 - Q'^2}{2s + Q^2 - Q'^2},$$

$$\eta = -\frac{(q - q') \cdot (q + q')}{(p + p') \cdot (q + q')} \approx \frac{Q^2 + Q'^2}{2s + Q^2 - Q'^2},$$

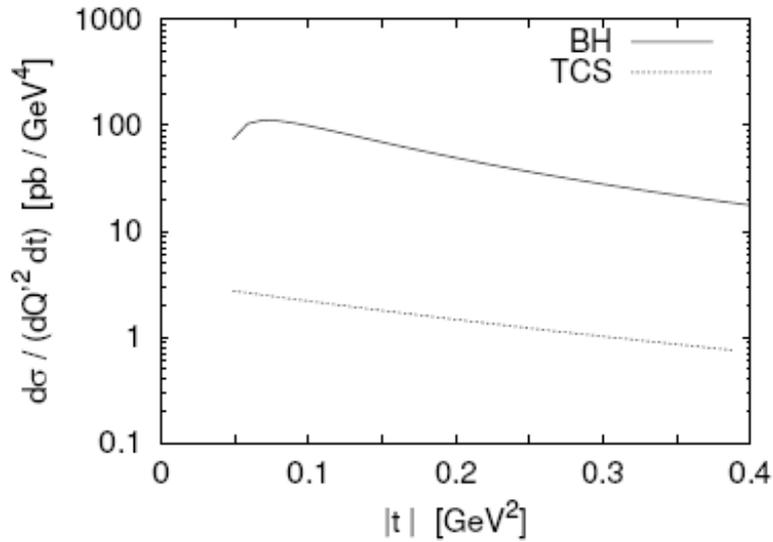
$$x = \frac{(k + k')^+}{(p + p')^+}, \quad \xi \approx -\frac{(q + q')^+}{(p + p')^+}, \quad \eta \approx \frac{(p - p')^+}{(p + p')^+}.$$

# General Compton Process accessing GPD

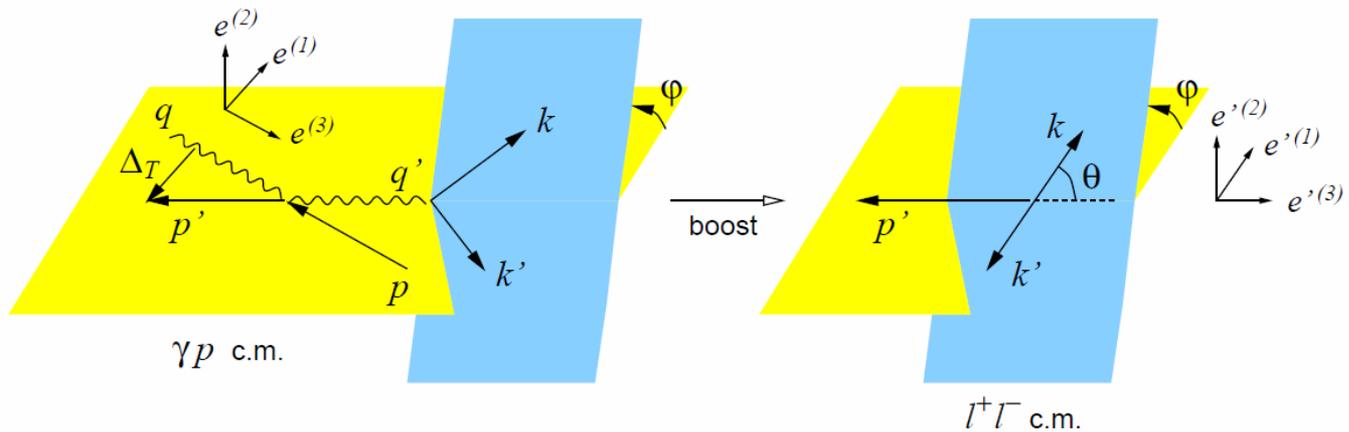
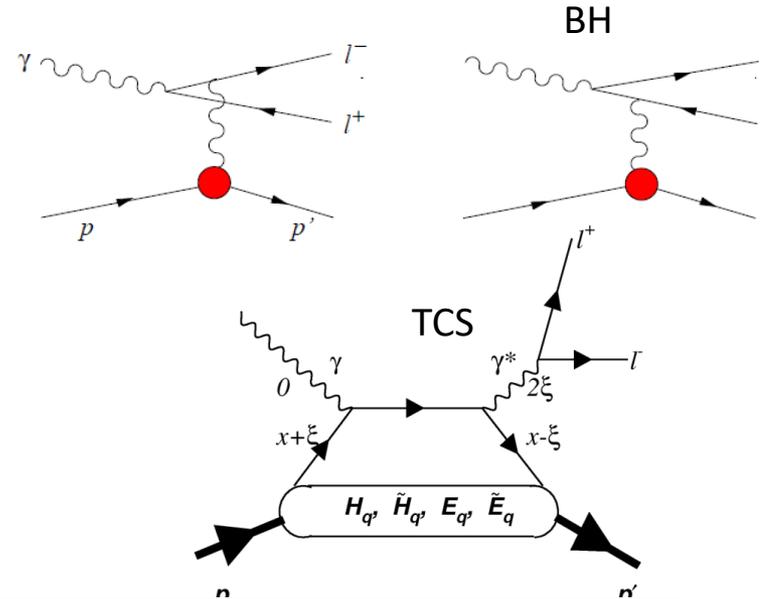


# TCS

Real (imaginary) part of the Compton amplitude can be obtained from photoproduction of lepton pairs using unpolarized (circularly polarized) photons



E. Berger *et al.*, Eur. Phys. J. C23, 675 (2002)



# Deep Exclusive Meson Production

A special kinematic regime is probed in **DEMP**, where the initial hadron emits  $q\bar{q}$  or  $gg$  pair.

- GPD  $\tilde{E}$  not related to an already known parton distribution.
- Experimental information on  $\tilde{E}$  can provide new nucleon structure info unlikely to be available from any other source.
- The most sensitive observable to probe  $\tilde{E}$  is the transverse single-spin asymmetry in exclusive  $\pi$  production

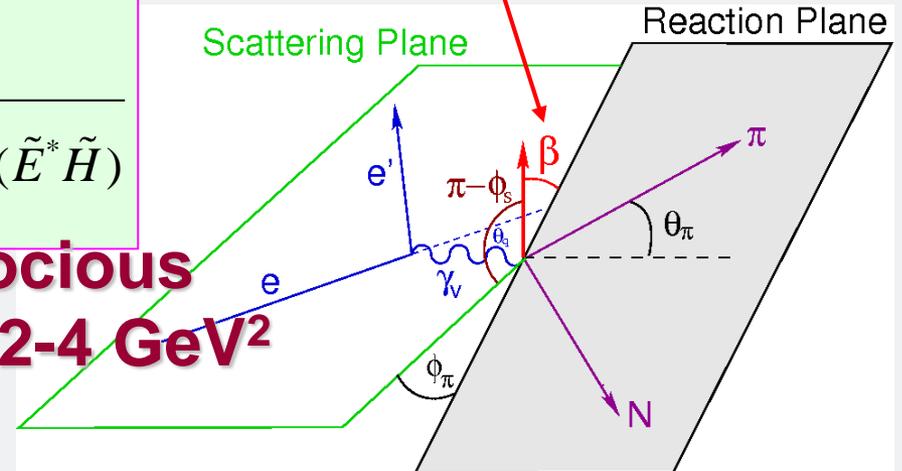
$$A_L^\perp = \frac{\left( \int_0^\pi d\beta \frac{d\sigma_L^\pi}{d\beta} - \int_\pi^{2\pi} d\beta \frac{d\sigma_L^\pi}{d\beta} \right)}{\left( \int_0^{2\pi} d\beta \frac{d\sigma_L^\pi}{d\beta} \right)}$$

$$= \frac{\sqrt{-t'}}{2m_p} \frac{\pi\xi\sqrt{1-\xi^2} \text{Im}(\tilde{E}^* \tilde{H})}{(1-\xi^2)\tilde{H}^2 - \frac{t\xi^2}{4m_p} \tilde{E}^2 - 2\xi^2 \text{Re}(\tilde{E}^* \tilde{H})}$$

$A_L^\perp$  expected to display precocious factorization at moderate  $Q^2 \sim 2-4 \text{ GeV}^2$

Refs: A.V. Belitsky, D. Mueller, PLB513 (2001) 349  
L.L. Frankfurt, et al., PRD 60(1999) 014101

$d\sigma_\pi^L$  = exclusive  $\pi$  cross section for longitudinal  $\gamma^*$   
 $\beta$  = angle between transversely polarized target vector and the reaction plane.



# SoLID (Solenoidal Large Intensity Device)

Full exploitation of JLab 12 GeV upgrade with broad physics program

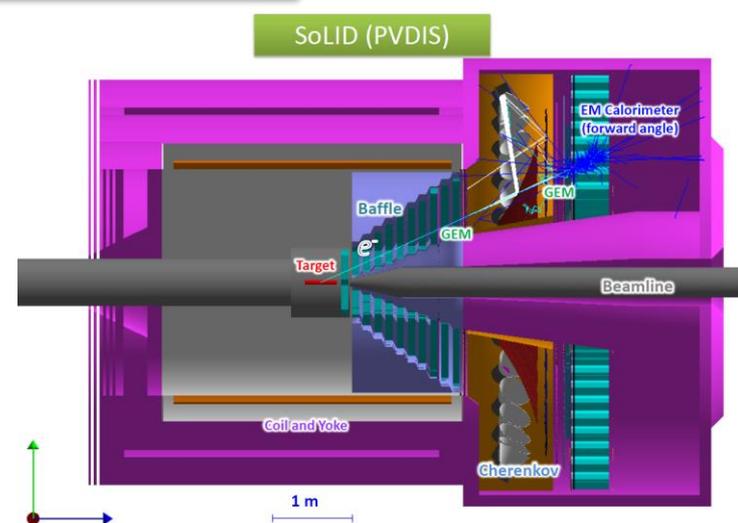
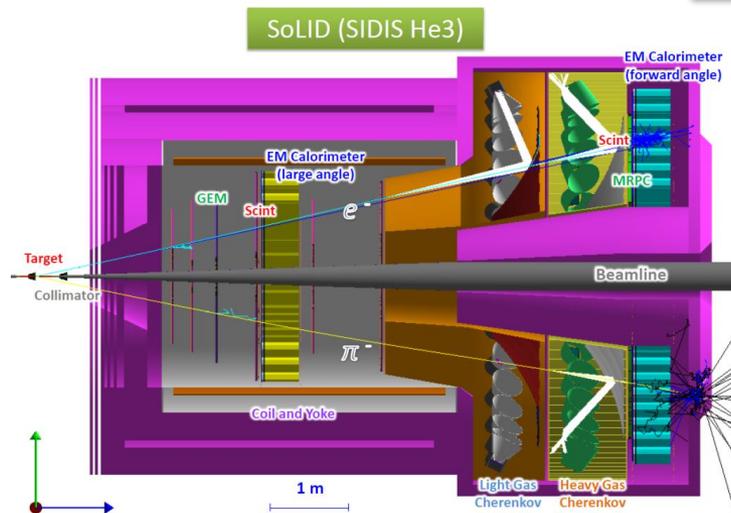
Lumi  $\sim 1e^{37}/\text{cm}^2/\text{s}$  (open geometry)

- 3D hadron structure
  - ❑ TMD (SIDIS on both neutron and proton)
  - ❑ GPD (TCS, DEMP)
- Gluon and nucleon mass
  - ❑  $J/\psi$  production at threshold

Lumi  $\sim 1e^{39}/\text{cm}^2/\text{s}$  (baffled geometry)

- Standard Model test and hadron structure
  - ❑ PVDIS on both deuterium and hydrogen

High Luminosity  
Large Acceptance

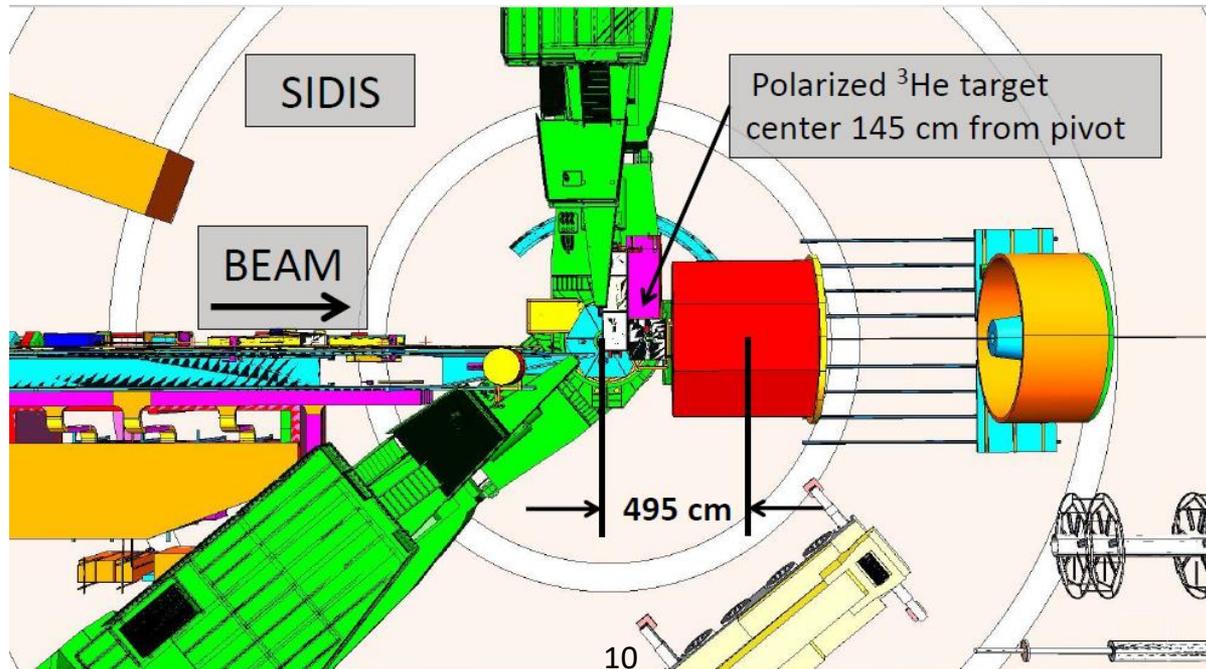


# SoLID Subsystems - Magnet

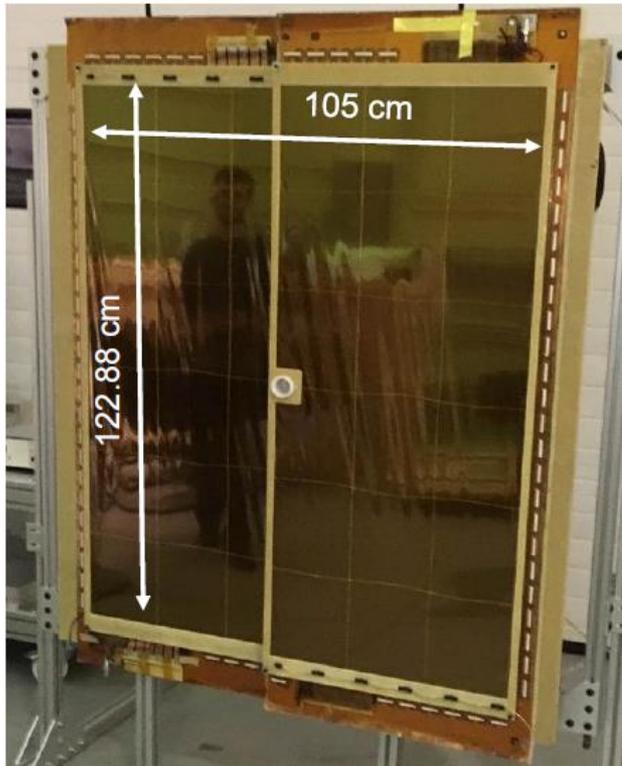
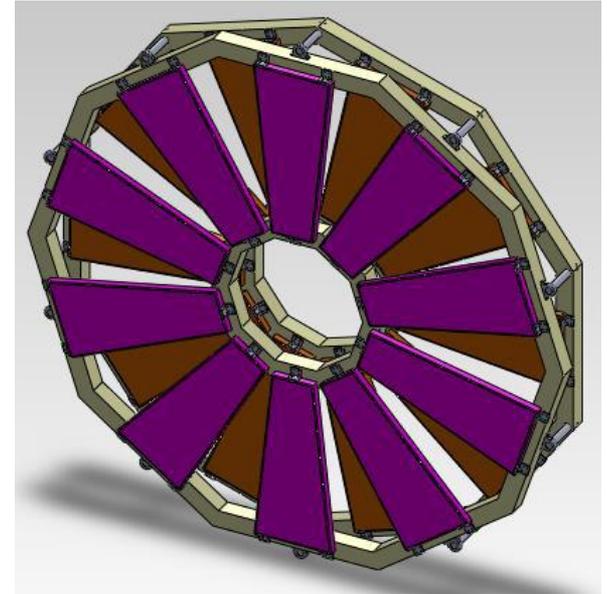
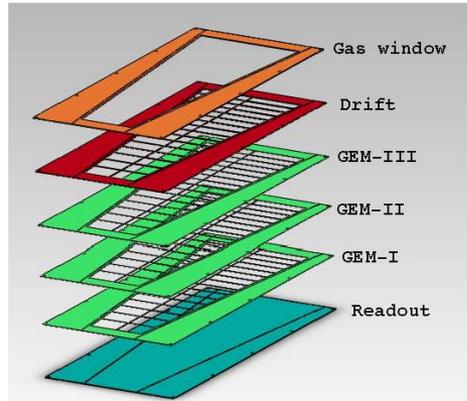
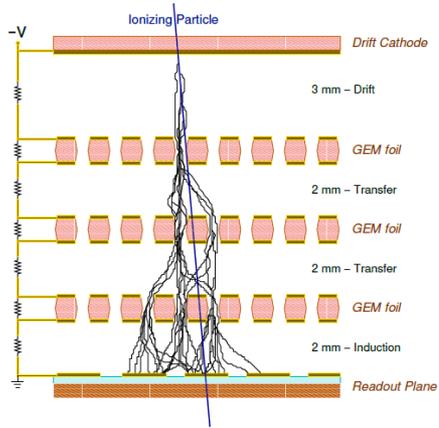


CLEO-II magnet,  
3m diameter, 3.5m long,  
field  $\sim 1.5\text{T}$

moved to Jlab in 2016



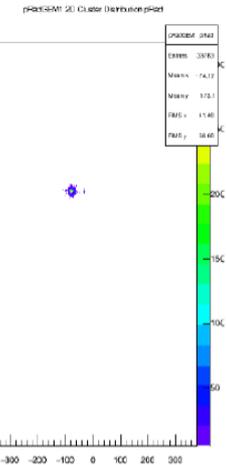
# SoLID Subsystems - GEM



## Gas Electron Multiplier

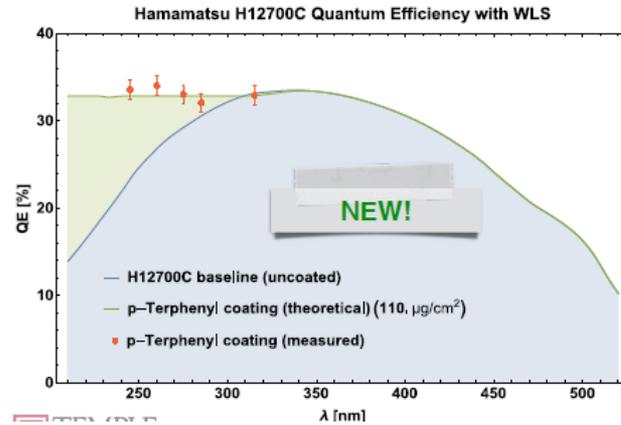
High rate capable trackers with multi-layers and large area

Largest GEM built and ran in experiment, PRad June 2016

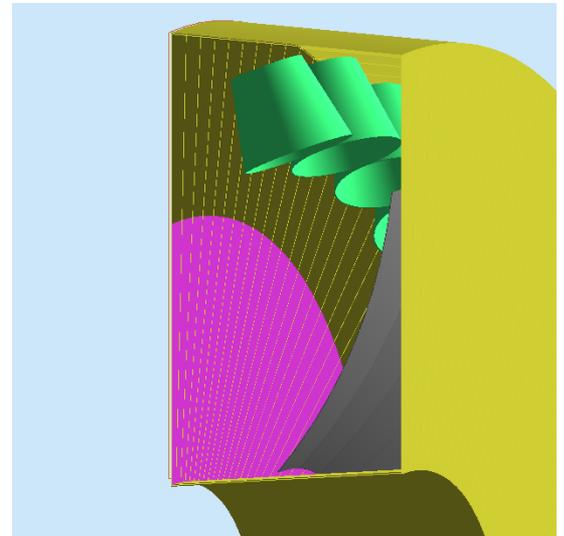
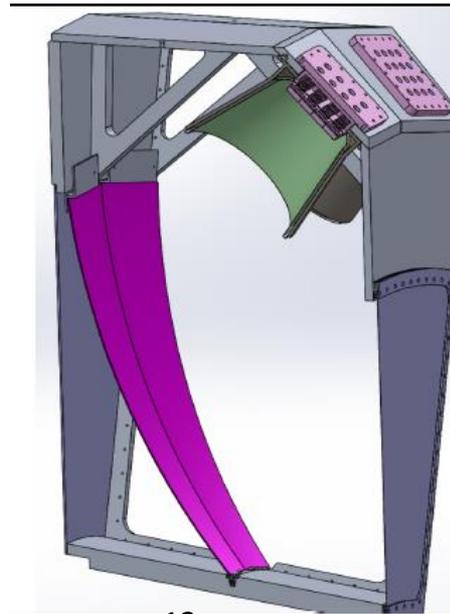


# SoLID Subsystems - Cherenkov

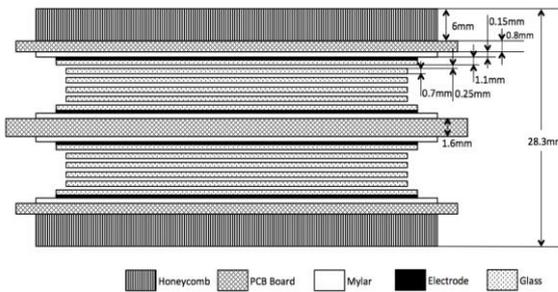
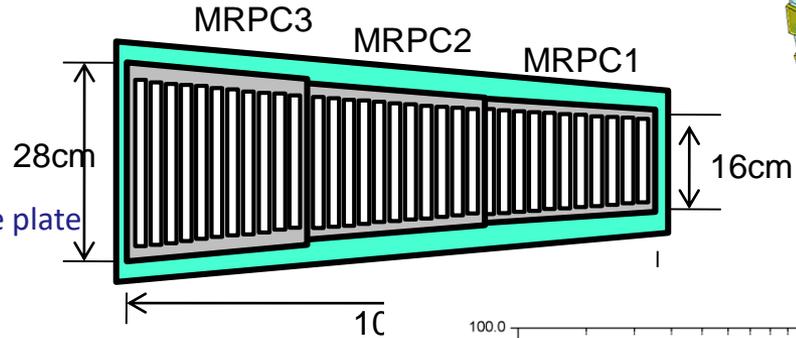
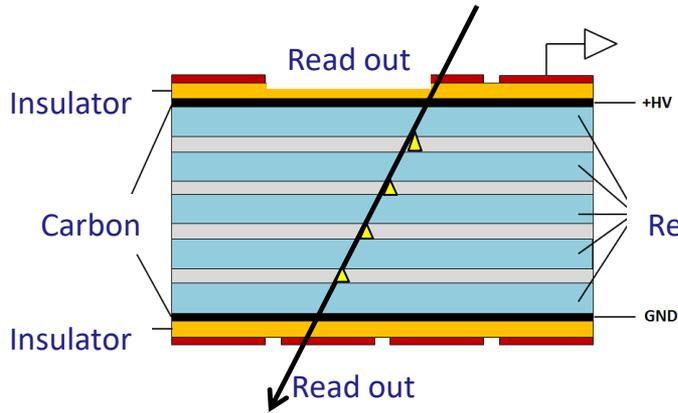
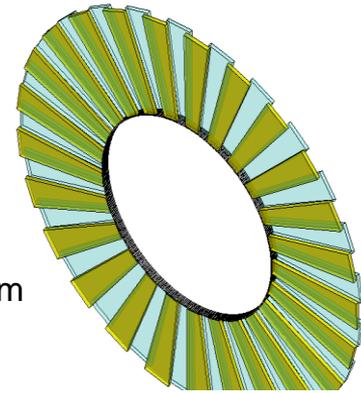
Light gas ( $\text{CO}_2$ )  
identify electrons  
suppress pions



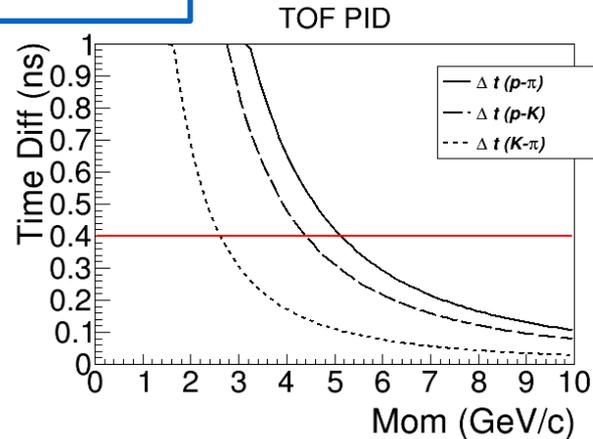
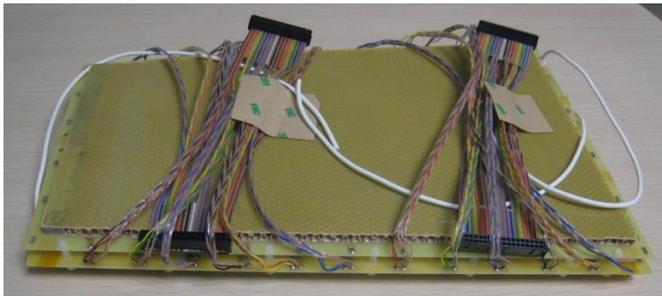
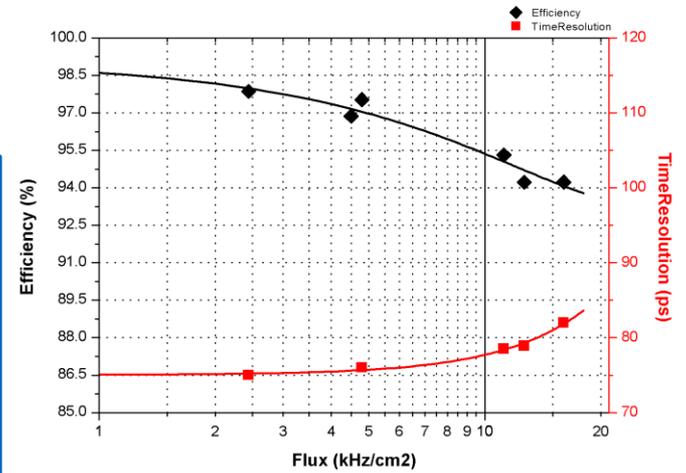
Heavy gas ( $\text{C}_4\text{F}_{10}$ )  
identify pions  
suppress kaons



# SoLID Subsystems - MRPC



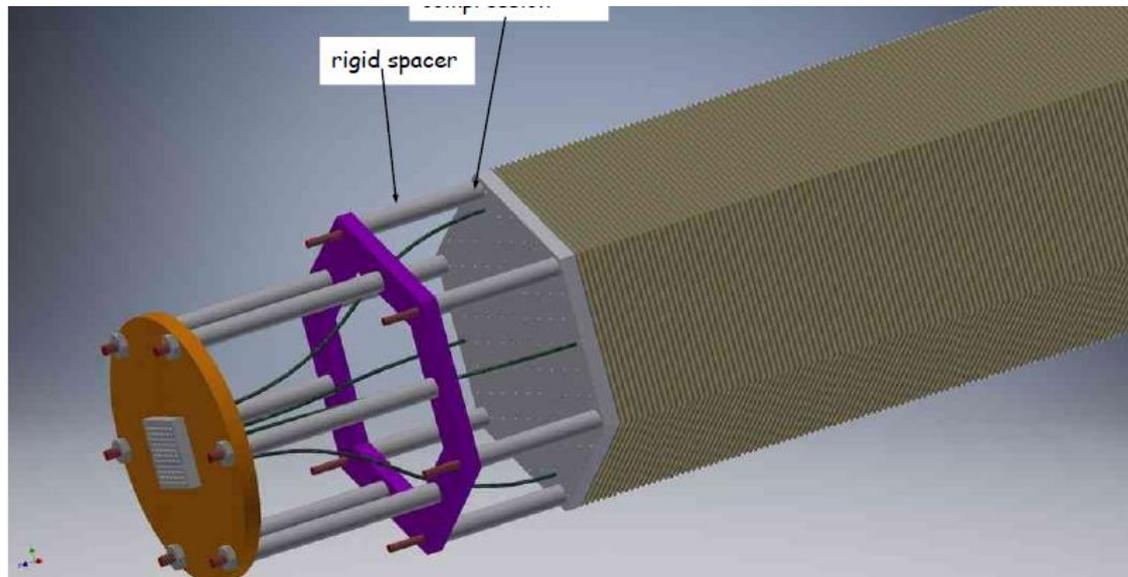
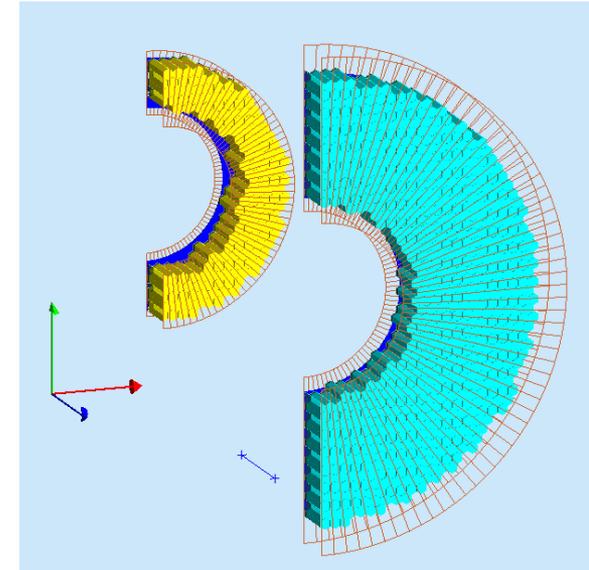
*Multi-gap Resistive Plate Chamber*  
 ~100ps time resolution, fast and high rate capable



# SoLID Subsystems - ECAL



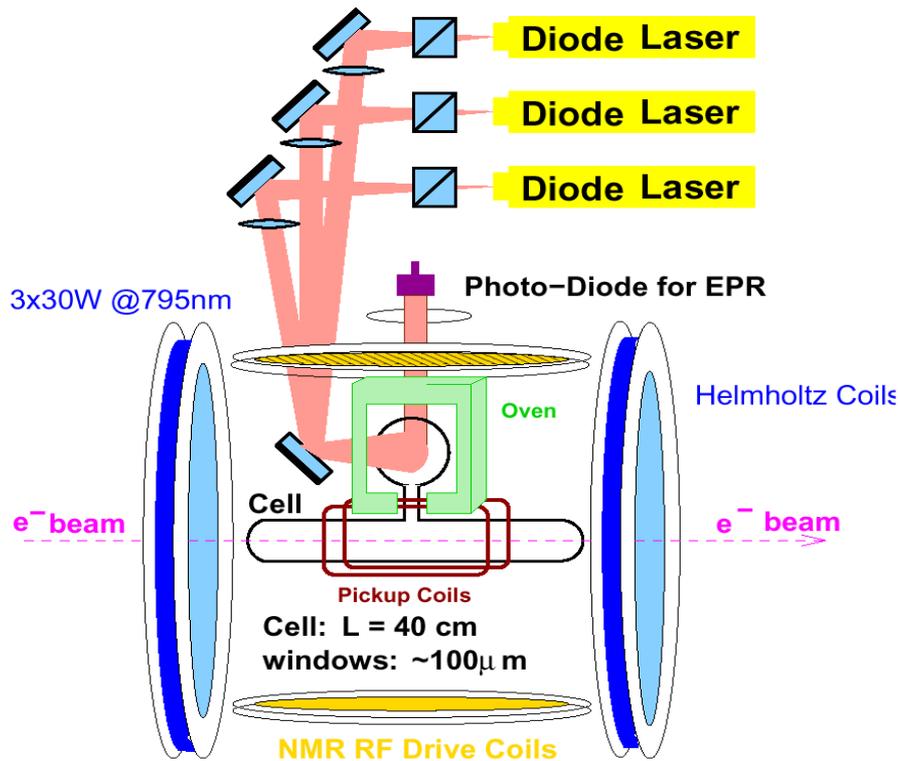
shashlik calorimeter  
, good resolution and  
radiation hardness



# SoLID Subsystems – Target

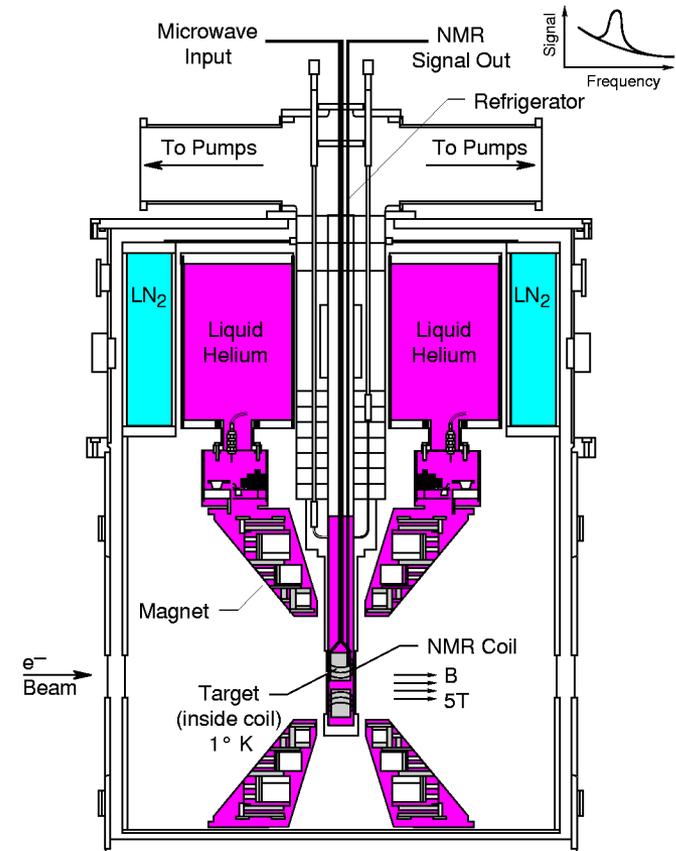
polarized  $^3\text{He}$  target

luminosity  $\geq 10^{36}/\text{cm}^2/\text{s}$  (world record)  
 High in-beam polarization  $\sim 60\%$



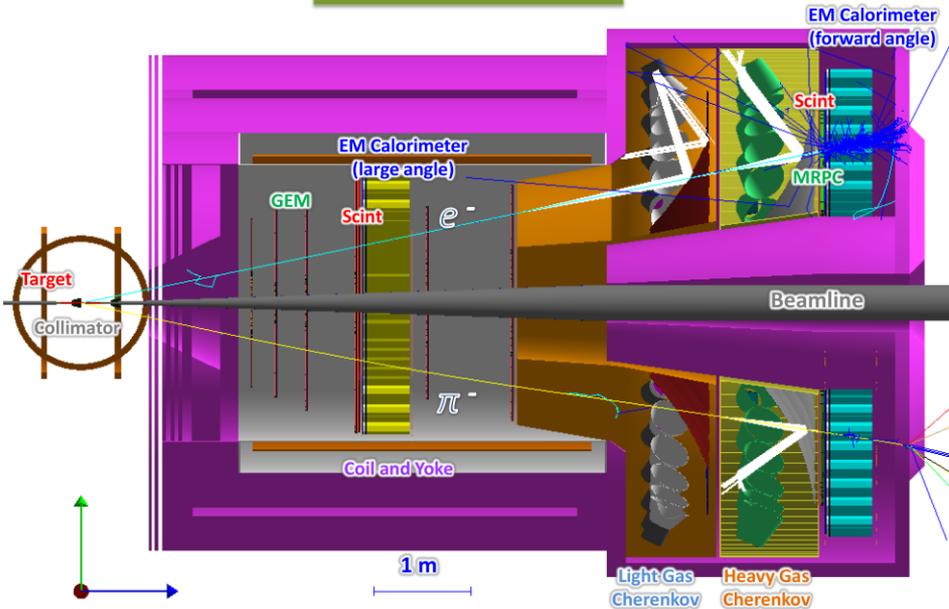
polarized  $\text{NH}_3$  target

luminosity  $\geq 10^{35}/\text{cm}^2/\text{s}$   
 High in-beam polarization  $\sim 70\%$



# SoLID He3 Setup

SoLID (SIDIS He3)



- E12-10-006: Single Spin Asymmetry on transversely polarized  $^3\text{He}$ , 90 days, **rated A**
- E12-11-007: Single and Double Spin Asymmetries on longitudinally polarized  $^3\text{He}$ , 35 days, **rated A**
- Dihadron process as run group

## Detection

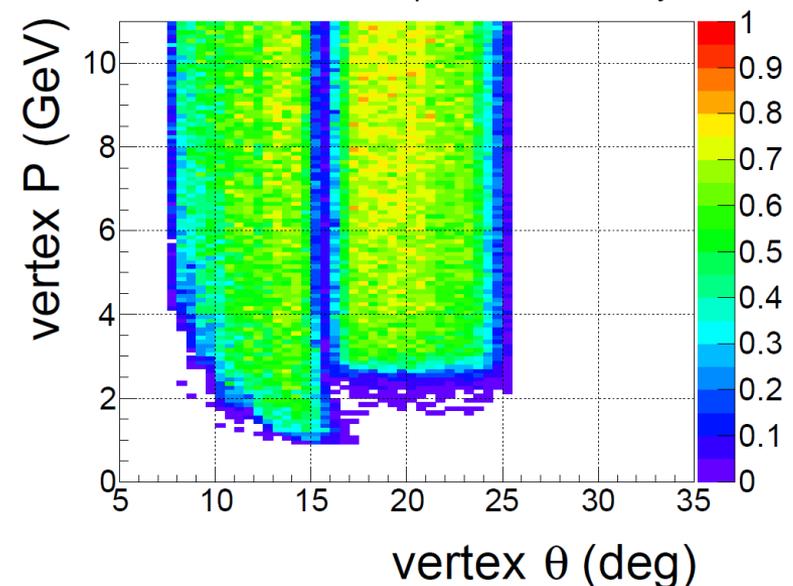
- $e^-$  at forward angle with EC and Cerenkov to reject pions
- $e^-$  above 3GeV detected at large angle with EC to reject pions
- pions detected at forward angle with TOF and Cerenkov to suppress kaons

Polarized lumi  $\sim 1e^{36}/\text{cm}^2/\text{s}$

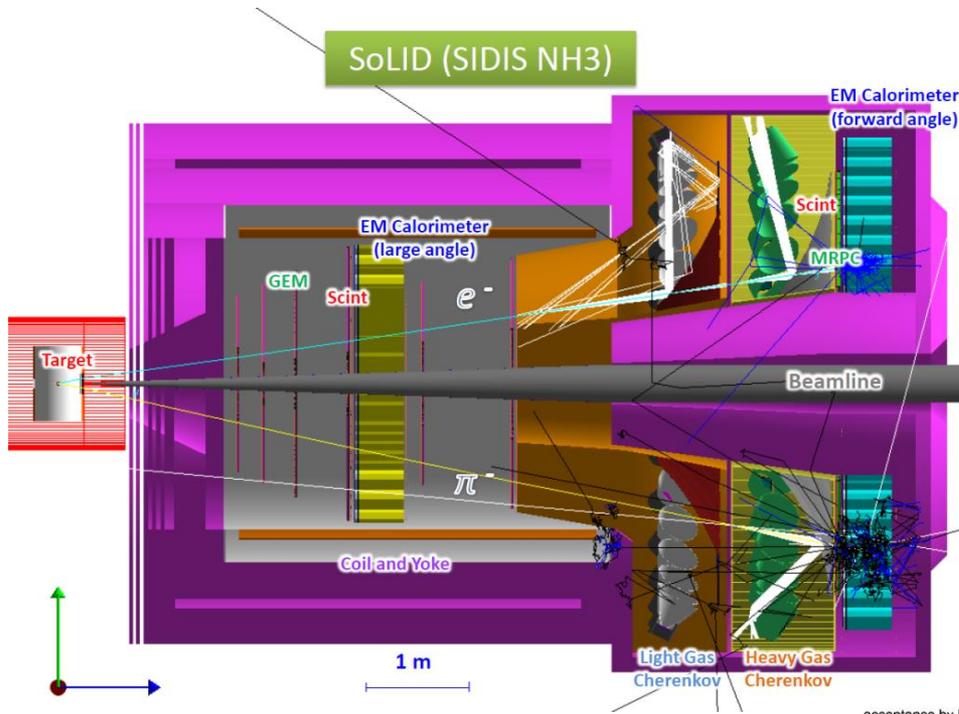
## Coverage

- Polar angle:  $e^-$  8-24 deg,  $\pi^-/\pi^+$  8-15deg
- Azimuthal angle: full
- Mom: 0.8-7GeV

SIDIS electron acceptance & efficiency



# SoLID NH3 Setup



- E12-10-008: Single Spin Asymmetry on transversely polarized proton (NH<sub>3</sub>), 120 days, **rated A**

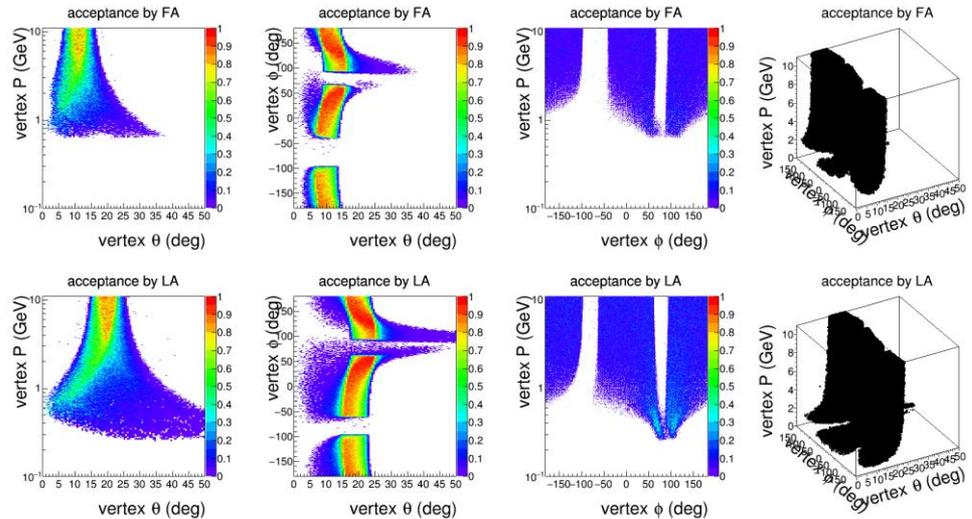
*Detection is similar to He3 setup*

*Coverage is similar to He3 setup except some distortion from the target field*

5T transverse target field  
High radiation sheet of flame areas are cut away

Polarized lumi  $\sim 1e^{35}/\text{cm}^2/\text{s}$

e- acceptance shown  
 $\pi^-$  acceptance is similar  
 $\pi^+$  acceptance is reversed  
along  $\phi=0$  plane



# SoLID SIDIS Kinematic Coverage

$$0.05 < x < 0.6$$

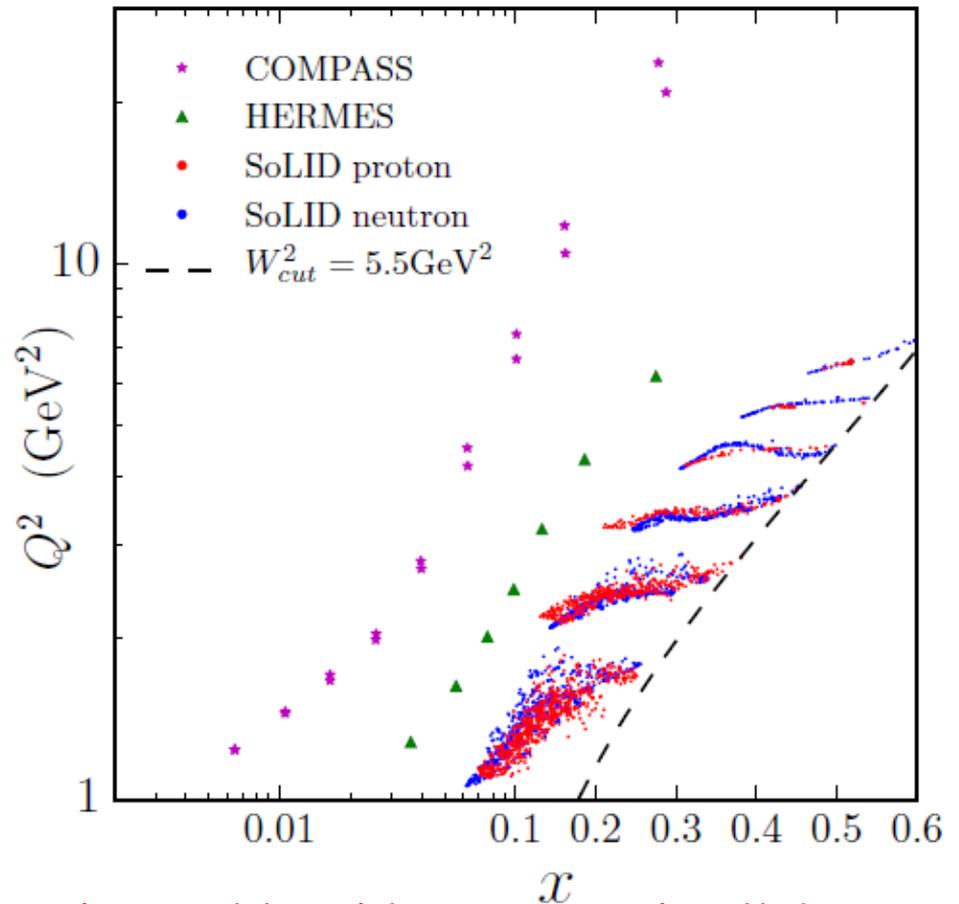
$$1\text{GeV} < Q^2 < 8\text{GeV}$$

$$0.3 < z < 0.7$$

$$0 < P_T < 1.6\text{GeV}$$

~ 2000 bins for n

~ 1000 bins for p



large acceptance and high luminosity enable wide coverage in all 4 kinematic bins with well controlled systematics

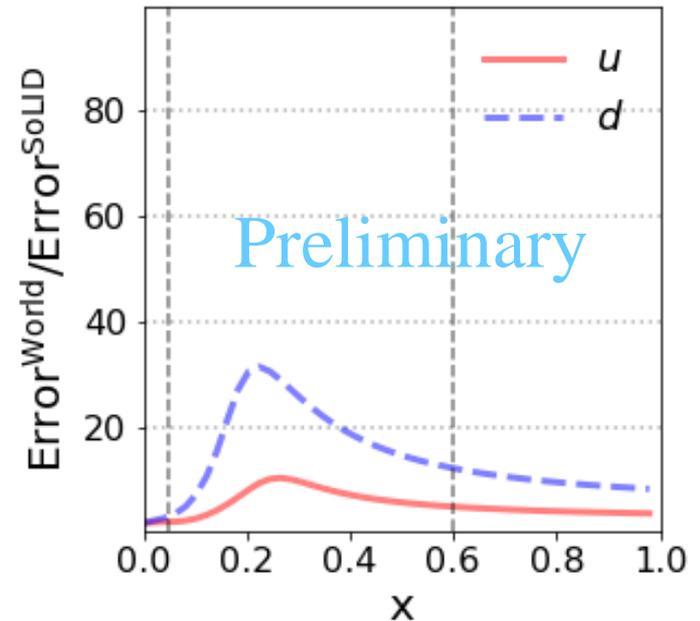
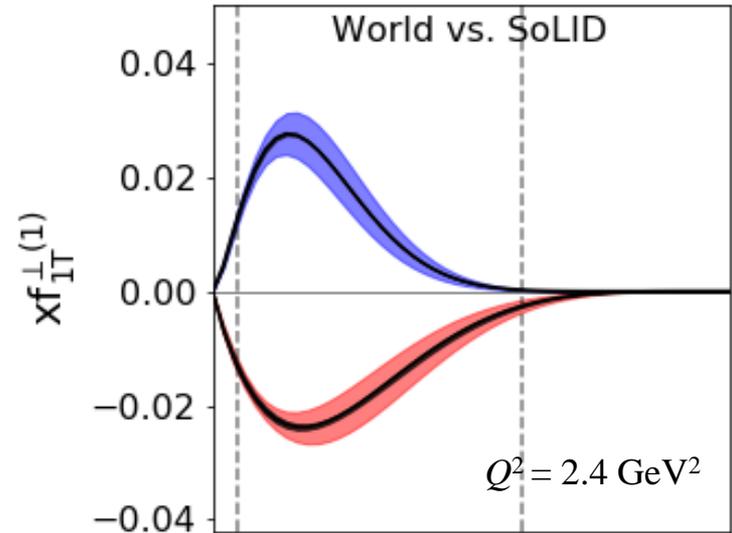
# SoLID Impact on Sivers

Fit SIDIS Sivers asymmetries data from HERMES, COMPASS and Jlab-6 GeV

Monte Carlo method with nested sampling algorithm is applied

TMD evolution is not included

Both statistical and systematic uncertainties are included



# SoLID Impact on Transversity

Fit Collins asymmetries in SIDIS and  $e^+e^-$  annihilation

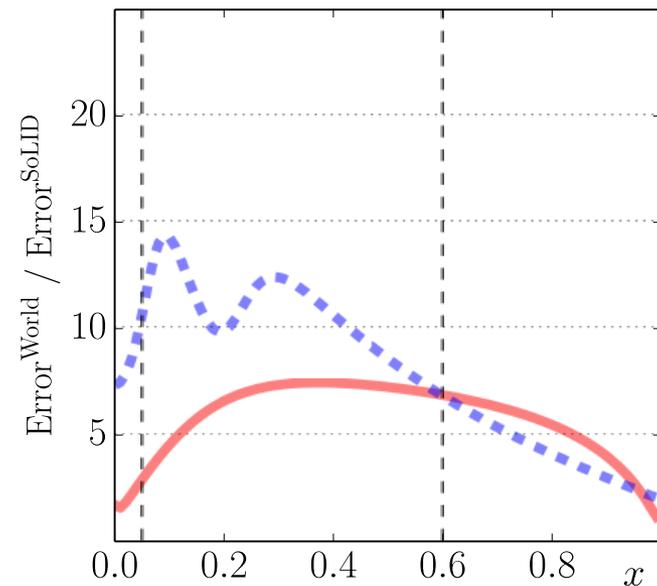
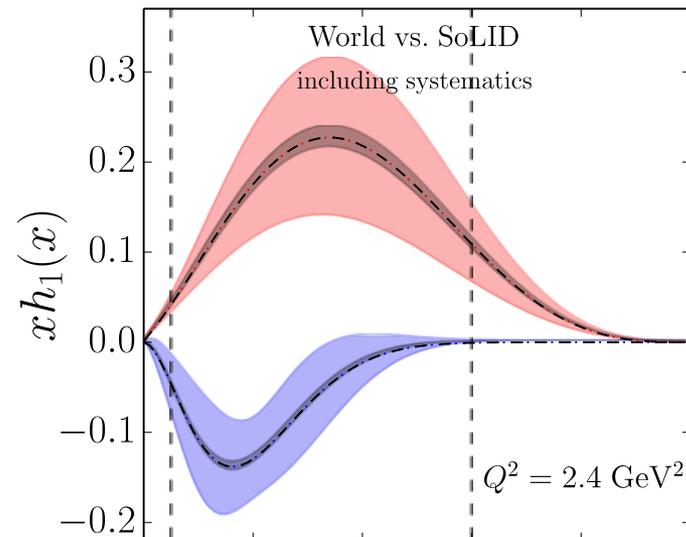
SIDIS data from HERMES, COMPASS and JLab-6 GeV

$e^+e^-$  data from BELLE and BABAR

TMD evolution is included

Both statistical and systematic uncertainties are included

About one order of magnitude improvement



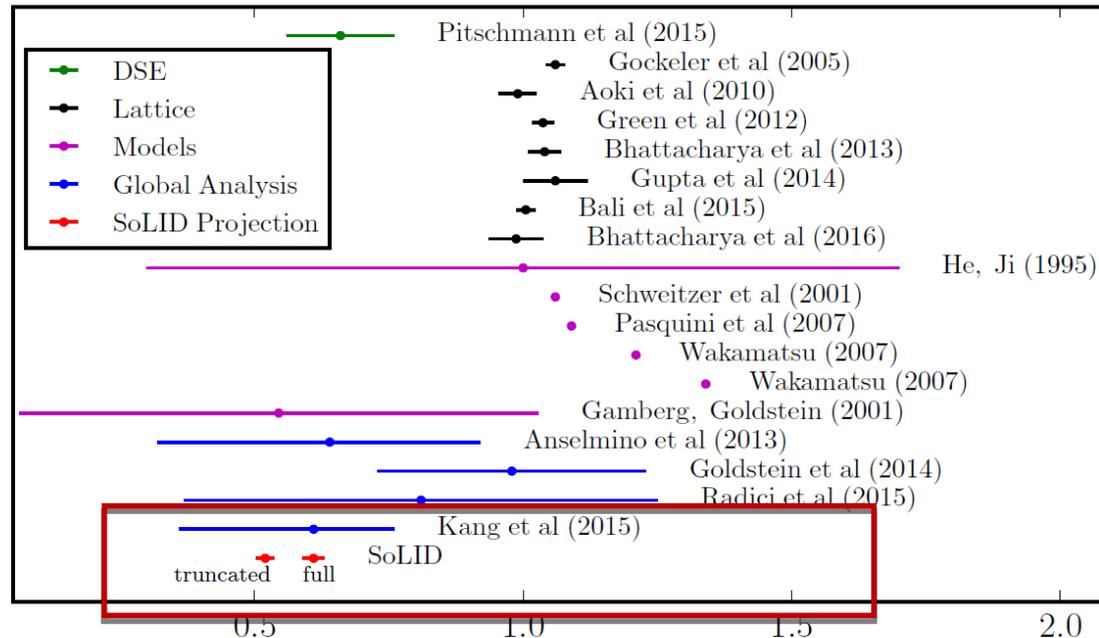
# SoLID Impact on Tensor Charge

## Definition

$$\langle P, S | \bar{\psi}_q i\sigma^{\mu\nu} \psi_q | P, S \rangle = \delta_T q \bar{u}(P, S) i\sigma^{\mu\nu} u(P, S) \quad \delta_T q = \int_0^1 [h_1^q(x) - h_1^{\bar{q}}(x)] dx$$

A fundamental QCD quantity. Matrix element of local operators.  
 Moment of transversity distribution. Valence quark dominant.  
 Calculable in lattice QCD.

1 order  
improvement



Including both  
systematic  
and statistical  
errors

Z. Ye *et al*, Phys. Lett. B 767, 91 (2017)

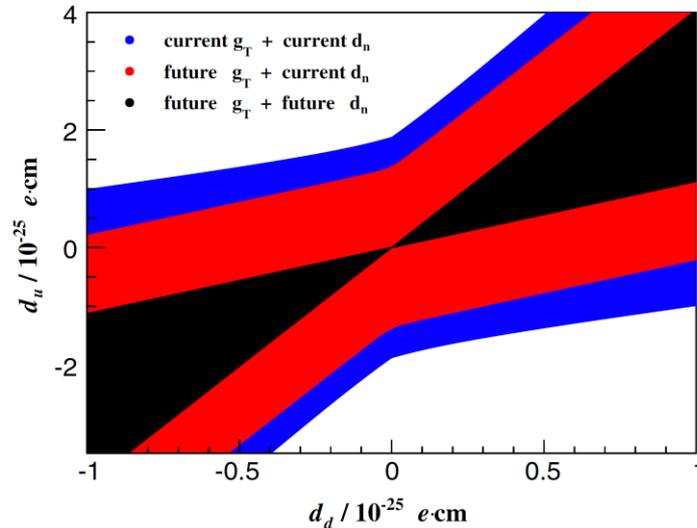
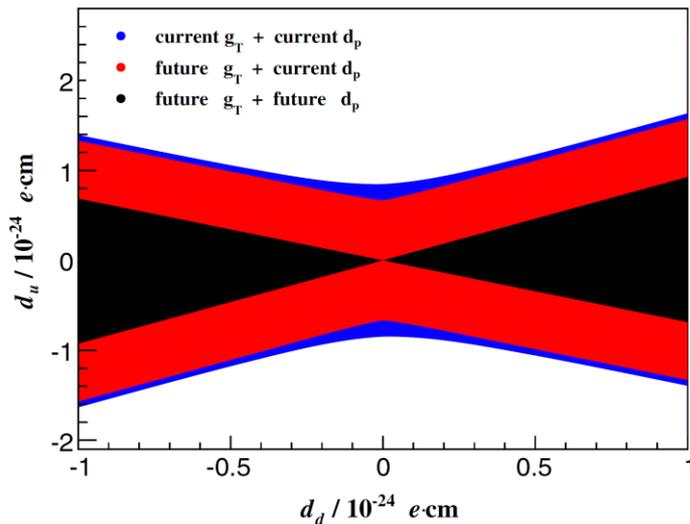
$$g_T = \delta u - \delta d$$

# SoLID Constraint on Quark EDMs with Tensor Charge

Tensor charge and EDM  $d_n = g_T^d d_u + g_T^u d_d + g_T^s d_s$   $g_T^s$  lattice calculation

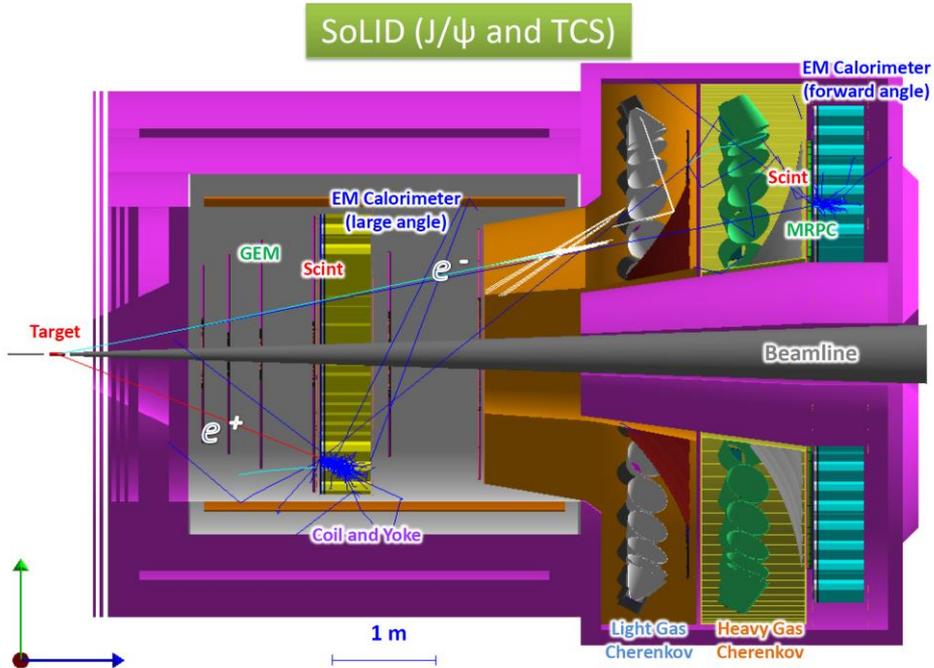
	$d_u$ upper limit	$d_d$ upper limit
Current $g_T$ + current EDMs	$1.27 \times 10^{-24} e \text{ cm}$	$1.17 \times 10^{-24} e \text{ cm}$
SoLID $g_T$ + current EDMs	$6.72 \times 10^{-25} e \text{ cm}$	$1.07 \times 10^{-24} e \text{ cm}$
SoLID $g_T$ + future EDMs	$1.20 \times 10^{-27} e \text{ cm}$	$7.18 \times 10^{-28} e \text{ cm}$

Include 10% isospin symmetry breaking uncertainty



T. Liu, Z.W. Zhao and H. Gao,  
PRD 97, 074018 (2018)

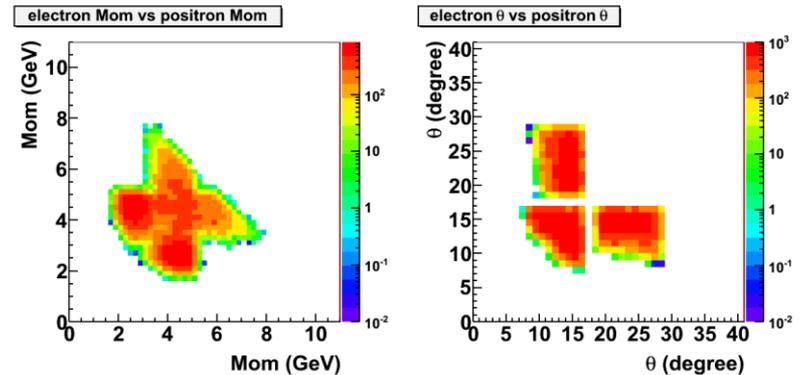
# SoLID TCS Setup



**Target** 15cm LH

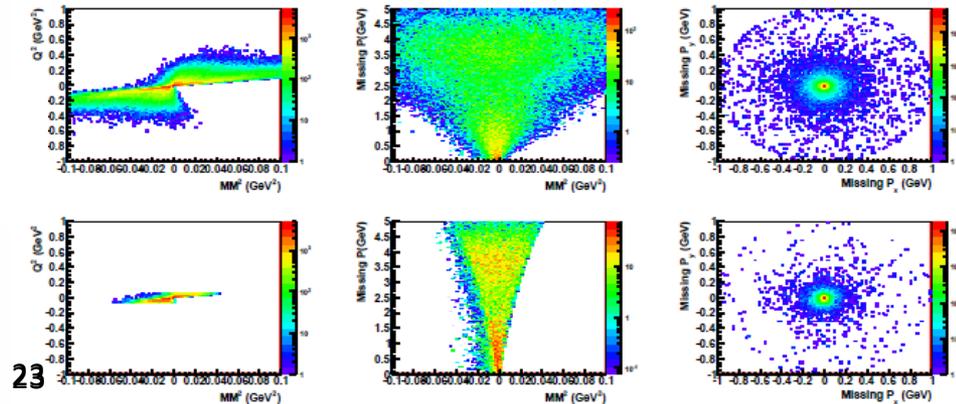
## Detection

- at least one of  $e^-$  and  $e^+$  at forward angle with Cherenkov to reject pions
- proton detected at both forward and large

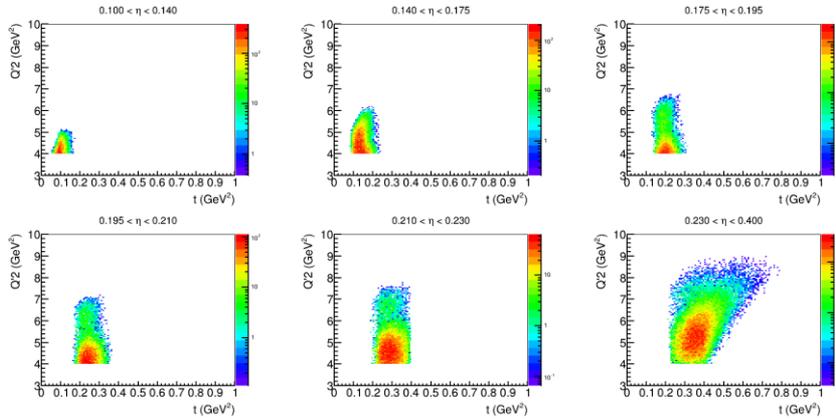


$\text{lumi} \sim 1e^{37}/\text{cm}^2/\text{s}$

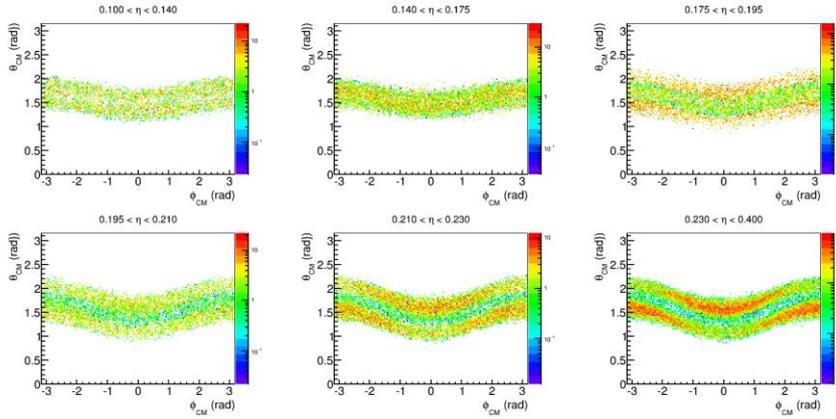
Cut on missing variables to ensure exclusivity



# SoLID TCS Projection



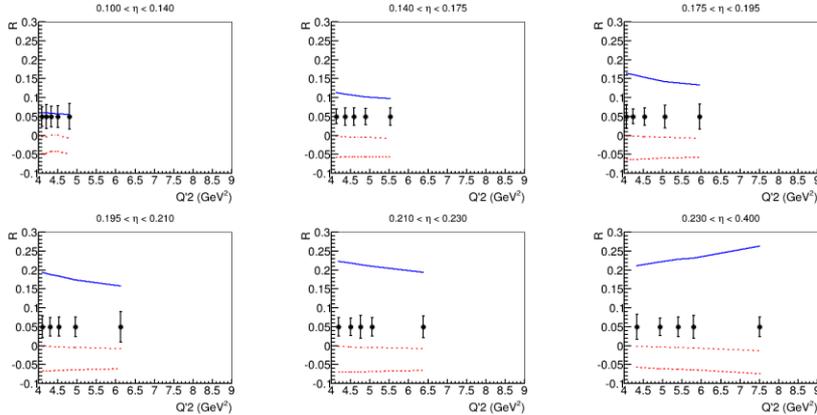
*Enough data for kinematic binning*



*Construct Moment from crosssection*

$$R = \frac{2 \int_0^{2\pi} d\phi \cos \phi \frac{dS}{dQ^2 dt d\phi}}{\int_0^{2\pi} d\phi \frac{dS}{dQ^2 dt d\phi}}$$

$$\frac{dS}{dQ^2 dt d\phi} = \int \frac{L(\theta, \phi)}{L_0(\theta)} \frac{d\sigma}{dQ^2 dt d\phi d\theta} d\theta$$



*Compare to different GPD model*

# SoLID TCS Projection

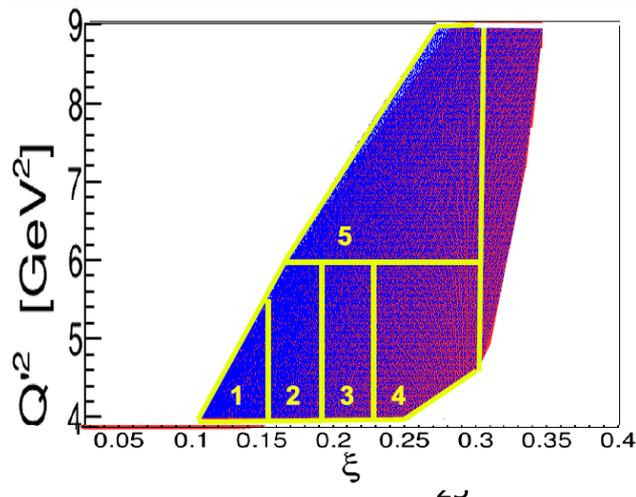
Michel Guidal and Marie Boer

Fit exercise (general)

TCS circular beam asymmetry helps constrain  $\text{Im}\{\mathcal{H}\}$  in fitting

	$(\sigma, \Delta\sigma_{LU})$ DVCS 5%	$(\sigma, \Delta\sigma_{LU})$ DVCS 5% + TCS <sub>ℓ</sub> 15%	$(\sigma, \Delta\sigma_{LU})$ DVCS 5% + TCS <sub>c</sub> 15%	$(\sigma, \Delta\sigma_{LU})$ DVCS 5% + TCS <sub>ℓ</sub> 5%	$(\sigma, \Delta\sigma_{LU})$ DVCS 5% + TCS <sub>c</sub> 5%
$\sigma^+(Re\{\mathcal{H}\})$	+1.21	+0.92	+0.80	+0.54	+0.55
$\sigma^-(Re\{\mathcal{H}\})$	-0.84	-0.79	-0.83	-0.44	-0.45
$\sigma^+(Im\{\mathcal{H}\})$	+0.23	+0.20	+0.15	+0.11	+0.12
$\sigma^-(Im\{\mathcal{H}\})$	-0.50	-0.40	-0.21	-0.27	-0.19

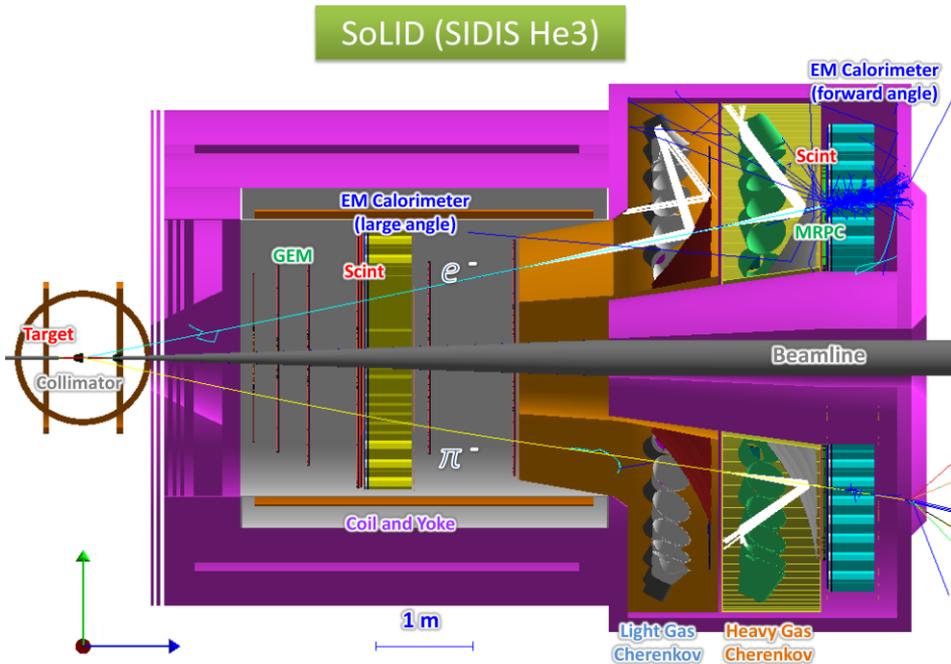
Fit exercise (SoLID TCS)



Go through SoLID simulation to get acceptance and counts for 50 days of running, then fit it

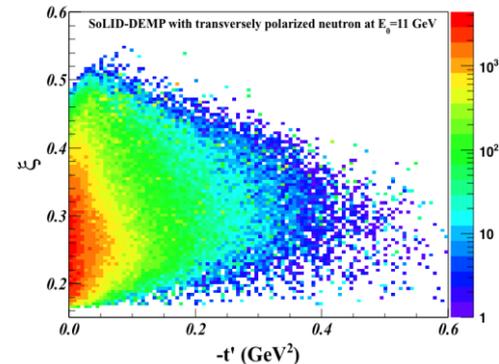
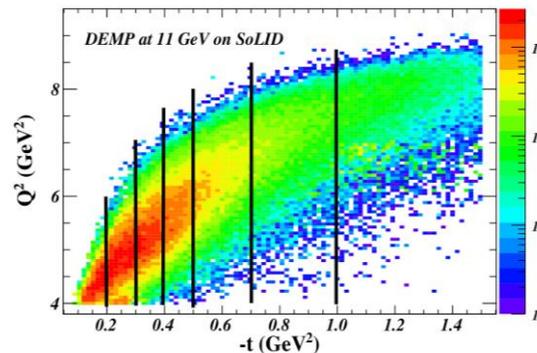
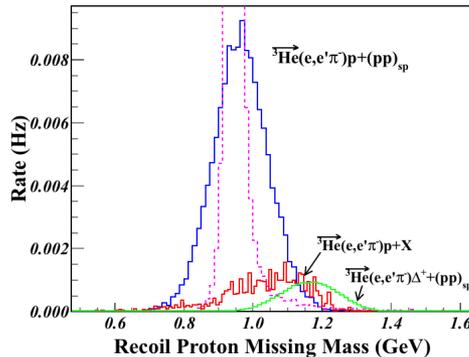
	$(\sigma, \Delta\sigma_{LU})$ DVCS + TCS <sub>c</sub>
$\sigma^+(Re\{\mathcal{H}\})$	+0.82
$\sigma^-(Re\{\mathcal{H}\})$	-0.77
$\sigma^+(Im\{\mathcal{H}\})$	+0.16
$\sigma^-(Im\{\mathcal{H}\})$	-0.40

# SoLID DEMP Setup



- Run group with SIDIS He3 11 GeV
- Proton PID offline, not in trigger
- Complete azimuthal and large polar angle coverage
- **The measurement is valuable as it is the only practical way to obtain  $A_{UT}^{\sin(\varphi-\varphi_s)}$  over a wide kinematic range.**
- We will also measure  $A_{UT}^{\sin(\varphi_s)}$  and its companion moments, as was done by HERMES.
- **Provides vital GPD information not easily available in any other experiment prior to EIC.**

Polarized lumi  $\sim 1e^{36}/\text{cm}^2/\text{s}$

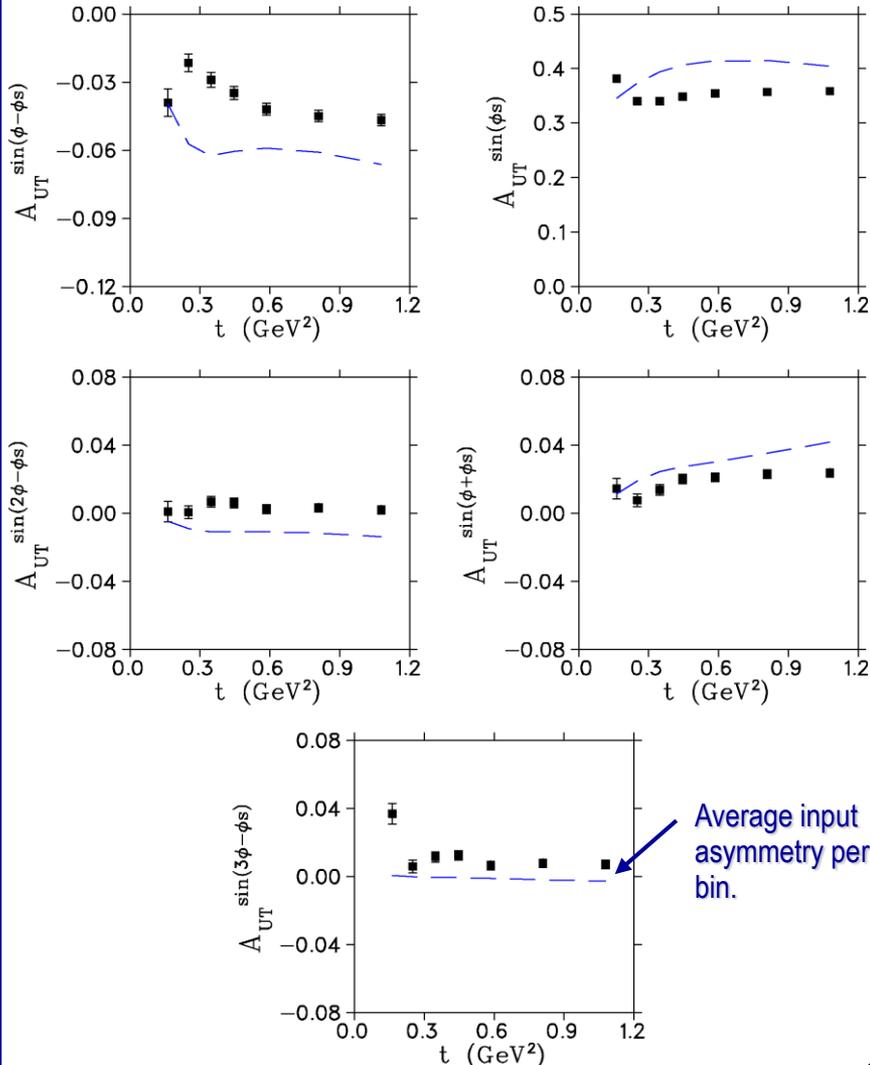


# SoLID DEMP Projection

Unbinned Maximum Likelihood (UML) Method, same as [HERMES PLB 682\(2010\)345](#)

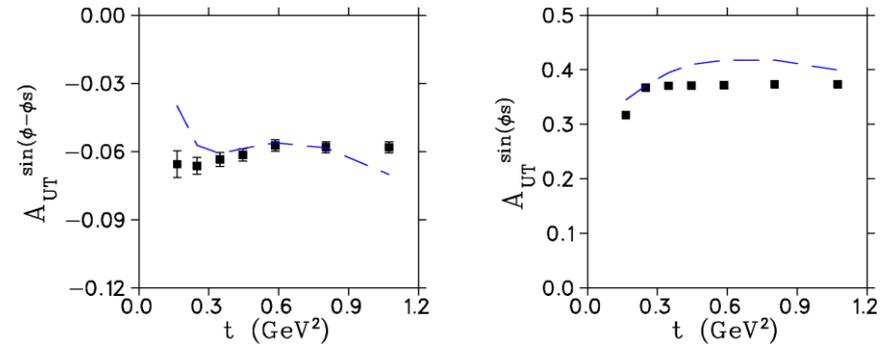
## All effects on.

Includes all scattering, energy loss, resolution and Fermi momentum effects.



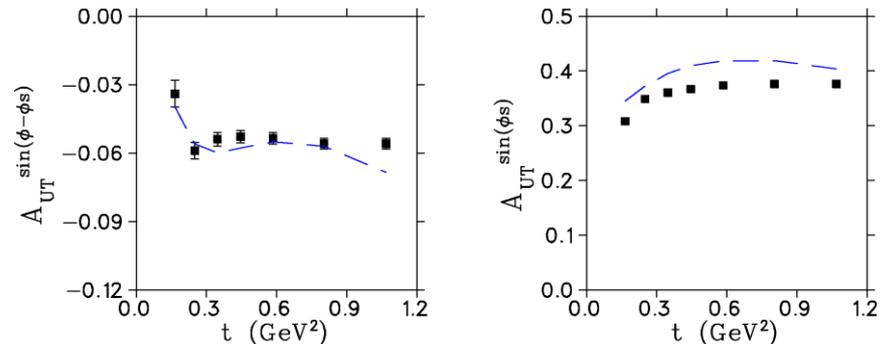
## Only Fermi momentum off.

Includes all scattering, energy loss, resolution effects. Similar to where proton resolution is good enough to correct for Fermi momentum effects.



## All effects off.

- Agreement between input and output fit values is very good. Validates the UML procedure.



# Summary

- Nucleon 3D imaging, including both TMDs and GPDs, will help us understand nucleon and non-perturbative QCD
- SoLID SIDIS program will provide unprecedented precision with multi-dimensional mapping in valence quark region and have great impact on the study of transversity, tensor charge and other TMDs
- SoLID GPD will provide unique opportunity to study TCS and DEMP
- With high luminosity and large acceptance, SoLID will fully exploit the capabilities of JLab 12GeV upgrade

*Thank you!*

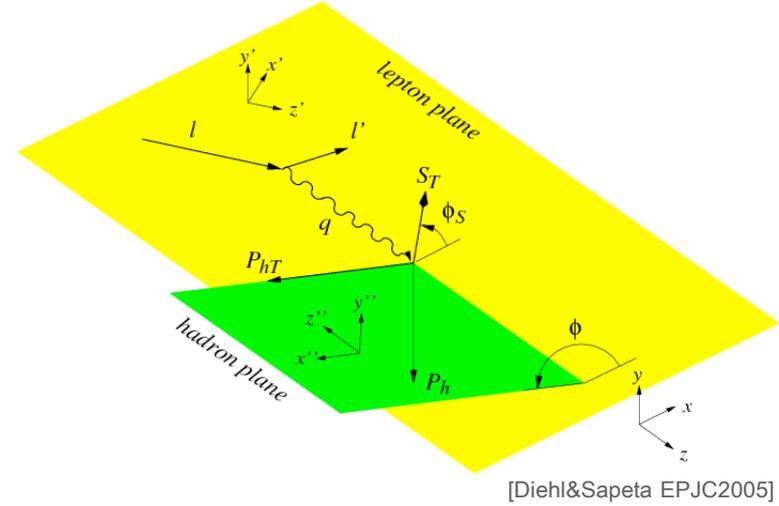
# backup

# Structure Functions

## SIDIS differential cross section

18 structure functions  $F(x, z, Q^2, P_T)$ ,  
model independent. (one photon exchange approximation)

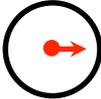
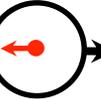
$$\begin{aligned}
 & \frac{d\sigma}{dx dy dz dP_T^2 d\phi_h d\phi_S} \\
 &= \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \\
 & \times \left\{ F_{UU,T} + \epsilon F_{UU,L} + \sqrt{2\epsilon(1+\epsilon)} F_{UU}^{\cos\phi_h} \cos\phi_h + \epsilon F_{UU}^{\cos 2\phi_h} \cos 2\phi_h + \lambda_e \sqrt{2\epsilon(1-\epsilon)} F_{LU}^{\sin\phi_h} \sin\phi_h \right. \\
 & + S_L \left[ \sqrt{2\epsilon(1+\epsilon)} F_{UL}^{\sin\phi_h} \sin\phi_h + \epsilon F_{UL}^{\sin 2\phi_h} \sin 2\phi_h \right] + \lambda_e S_L \left[ \sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} F_{LL}^{\cos\phi_h} \cos\phi_h \right] \\
 & + S_T \left[ (F_{UT,T}^{\sin(\phi_h-\phi_S)} + \epsilon F_{UT,L}^{\sin(\phi_h-\phi_S)}) \sin(\phi_h - \phi_S) + \epsilon F_{UT}^{\sin(\phi_h+\phi_S)} \sin(\phi_h + \phi_S) + \epsilon F_{UT}^{\sin(3\phi_h-\phi_S)} \sin(3\phi_h - \phi_S) \right. \\
 & \quad \left. + \sqrt{2\epsilon(1+\epsilon)} F_{UT}^{\sin\phi_S} \sin\phi_S + \sqrt{2\epsilon(1+\epsilon)} F_{UT}^{\sin(2\phi_h-\phi_S)} \sin(2\phi_h - \phi_S) \right] \\
 & + \lambda_e S_T \left[ \sqrt{1-\epsilon^2} F_{LT}^{\cos(\phi_h-\phi_S)} \cos(\phi_h - \phi_S) \right. \\
 & \quad \left. + \sqrt{2\epsilon(1-\epsilon)} F_{LT}^{\cos\phi_S} \cos\phi_S + \sqrt{2\epsilon(1-\epsilon)} F_{LT}^{\cos(2\phi_h-\phi_S)} \cos(2\phi_h - \phi_S) \right] \left. \right\}
 \end{aligned}$$



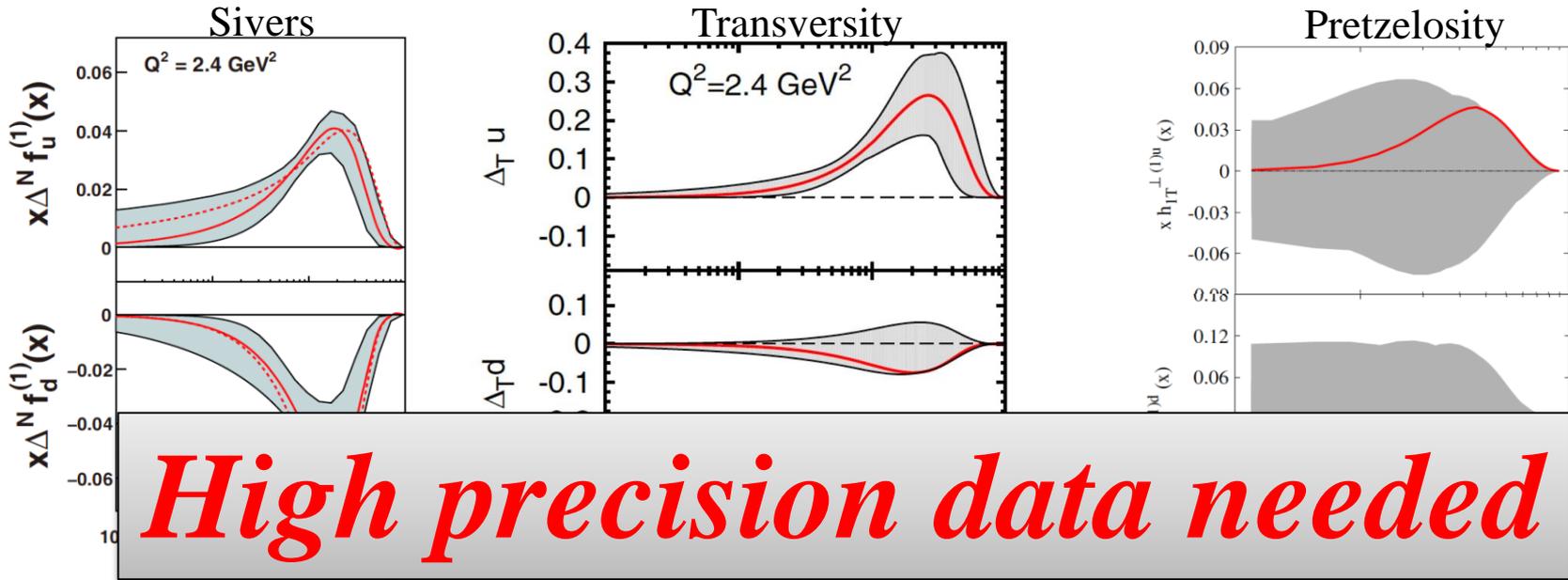
In parton model,  $F(x, z, Q^2, P_T)$ s are expressed as the convolution of TMDs.

# Leading Twist TMDs

 Nucleon Spin  
 Quark Spin

		Quark Polarization		
		U	L	T
Nucleon Polarization	U	$f_1$  unpolarized		$h_1^\perp$  -  Boer-Mulders
	L		$g_{1L}$  -  helicity	$h_{1L}^\perp$  -  longi-transversity (worm-gear)
	T	$f_{1T}^\perp$  -  Sivers	$g_{1T}$  -  trans-helicity (worm-gear)	$h_1$  -  transversity $h_{1T}^\perp$  -  pretzelosity

# Present Status On TMD Extractions



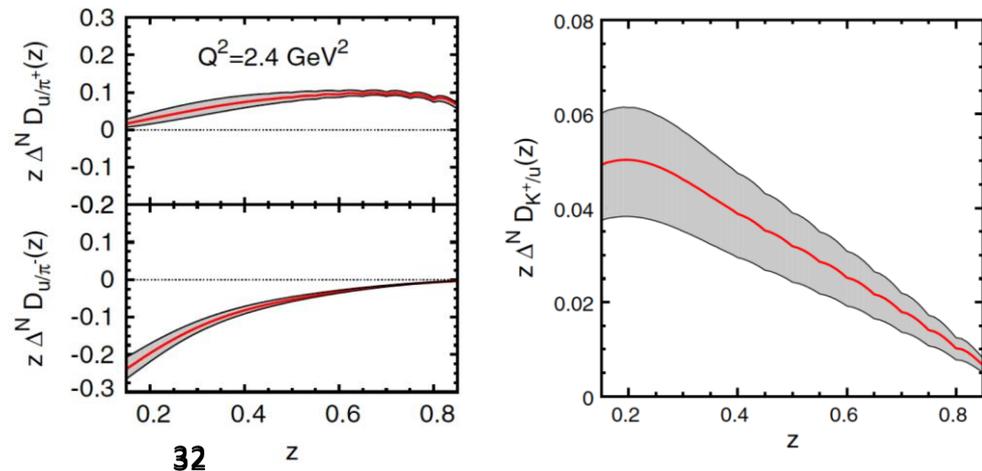
Anselmino et al, EPJA39, 89 (2009)

Anselmino et al, PRD92, 114023 (2015)

Lefky et al, PRD91, 034010 (2015)

## Collins fragmentation

Anselmino et al, PRD92, 114023 (2015)  
PRD93, 034025 (2016)



# SIDIS @ SoLID

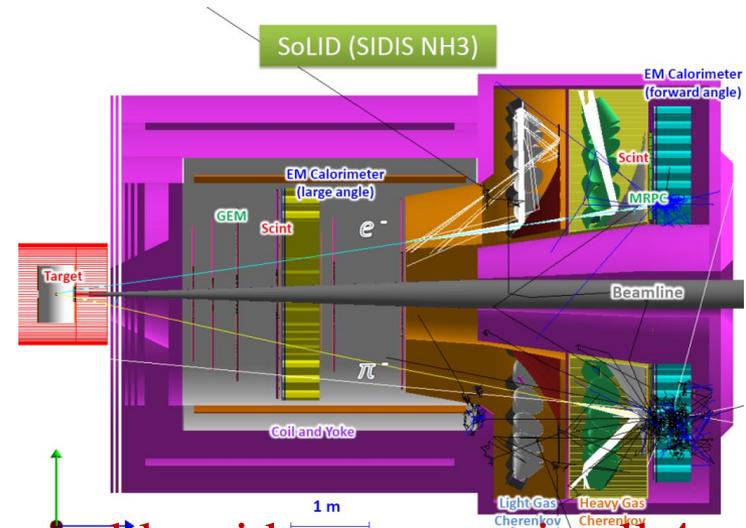
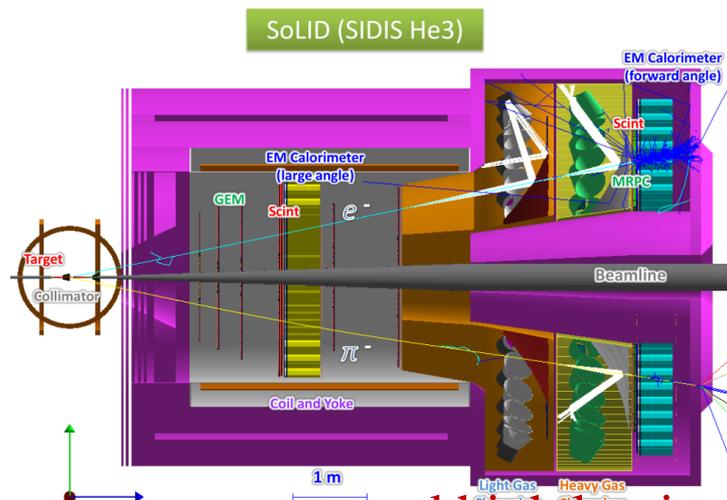
Approved SIDIS experiments rated with A

11/8.8 GeV beam, polar angle  $8^\circ \sim 24^\circ$ , full  $2\pi$  azimuthal angle

- E12-10-006: Single Spin Asymmetry on transversely polarized  $^3\text{He}$ , 90 days, **rated A**
- E12-11-007: Single and Double Spin Asymmetries on longitudinally polarized  $^3\text{He}$ , 35 days, **rated A**

- run group
  - Dihadron process
  - Ay inclusive

- E12-10-008: Single Spin Asymmetry on transversely polarized proton ( $\text{NH}_3$ ), 120 days, **rated A**



large acceptance and high luminosity enable wide coverage in all 4 kinematic bins with well controlled systematics

# SoLID SIDIS Resolution and Error

	$\theta$ angle (mrad)	$\phi$ angle (mrad)	Vertex z (cm)	$p$ (%)
SIDIS $^3\text{He}$ fwd angle ( $e$ )	1.3	5.7	0.9	1.7
SIDIS $^3\text{He}$ fwd angle ( $\pi$ )	1.2	5.2	0.9	1.1
SIDIS $^3\text{He}$ large angle ( $e$ )	1.0	1.7	0.5	1.2
PVDIS ( $e$ )	0.8	1.7	0.3	1.2

Table 21: Averaged resolutions by track fitting with most of material energy loss and without background

$E_{\text{beam}}$ (GeV)	$x$	$z$	$Q^2$ (GeV $^2$ )	$P_{h\perp}$ (GeV)	$\phi_h$ (rad)	$\phi_S$ (rad)
11	0.002	0.003	0.02	0.006	0.015	0.006
8.8	0.002	0.004	0.02	0.006	0.018	0.006

Table 23: Resolution of kinematical variables (in the Trento convention) with the  $^3\text{He}$  target setup.

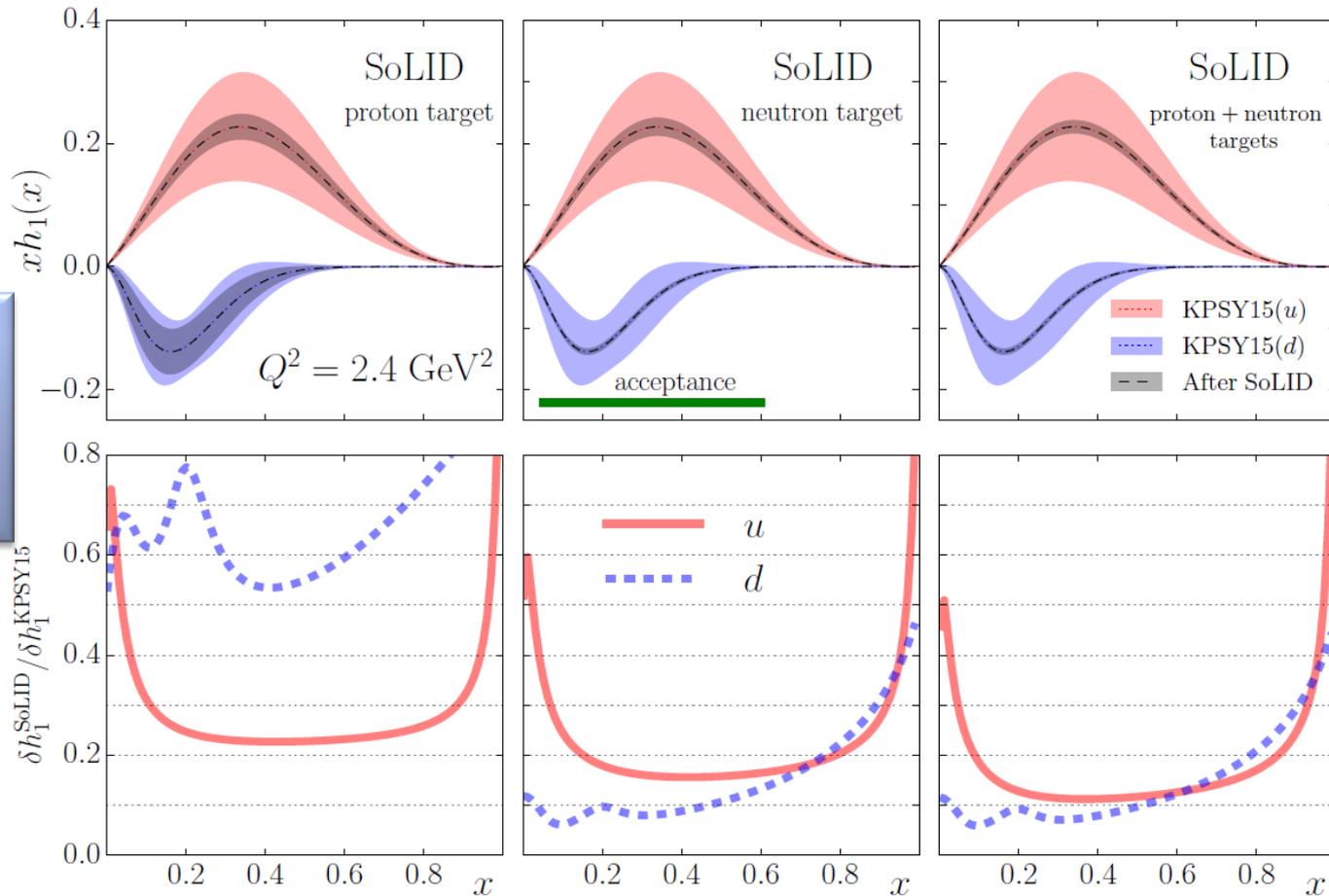
$P_{h\perp}$ (GeV/c)	[0.0, 0.2]	[0.2, 0.4]	[0.4, 0.6]	[0.6, 0.8]	[0.8, 1.0]	[1.0, 1.2]
11 GeV beam ( $\pi^+$ )	110	160	150	105	75	40
11 GeV beam ( $\pi^-$ )	120	160	140	90	70	50
8.8 GeV beam ( $\pi^+$ )	75	95	80	50	45	
8.8 GeV beam ( $\pi^-$ )	65	95	75	50	45	

Table 24: The ratio of SIDIS signal and random coincidence background within 6 ns. These values are estimated with the  $^3\text{He}$  target. Similar results are obtained for the proton target.

Systematic (abs.)		Systematic (rel.)	
Raw asymmetry	0.0014	Target polarization	3%
Detector resolution	< 0.0001	Nuclear effect	(4 – 5)%
		Random coincidence	0.2%
		Radiative correction	(2 – 3)%
		Diffraction meson	3%
Total	0.0014	Total	(6 – 7)%

Table 25: The systematic uncertainties on the asymmetry measurements of SIDIS.

# SoLID Impact on Transversity



1 order  
improvement

Z. Ye *et al*, Phys. Lett. B 767, 91 (2017)

Including both systematic and statistical errors

KPSY 15: Z.-B. Kang *et al*., PR D 93, 014009 (2016).

# Constraint on Quark EDMs

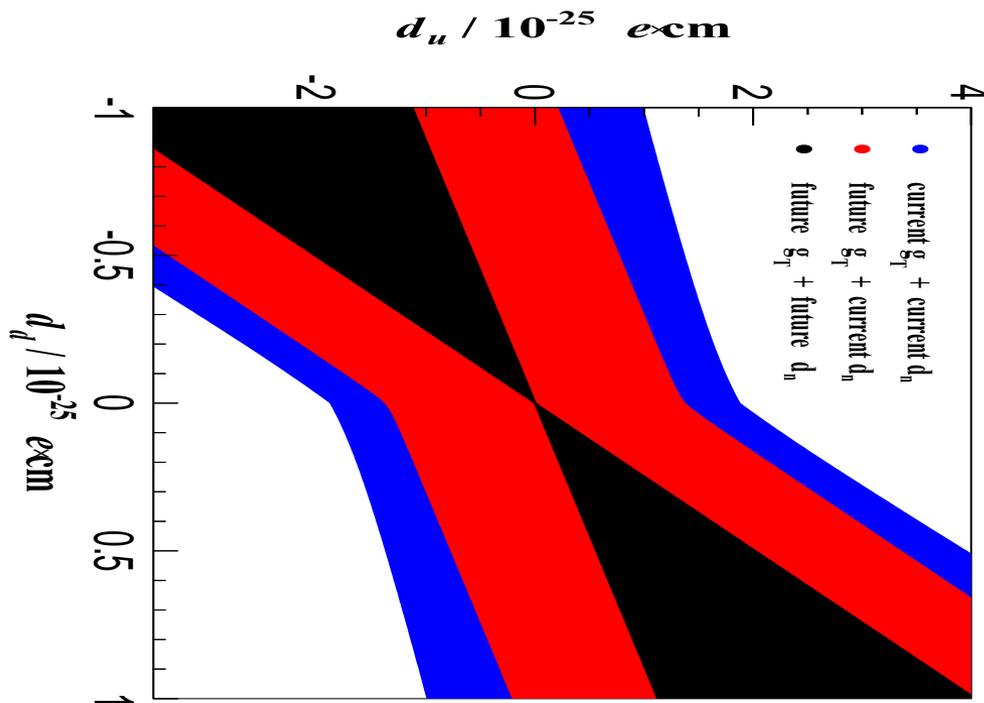
## Current upper limit on the neutron EDM

$$3.0 \times 10^{-26} e \text{ cm} \quad (90\% \text{ CL})$$

J.M. Pendlebury et al., Phys. Rev. D 92, 092003 (2015). [Re-analysis]

C.A. Baker et al., Phys. Rev. Lett. 97, 131801 (2006).

## Constraint on quark EDMs with tensor charge



$$d_n = g_T^d d_u + g_T^u d_d + g_T^s d_s$$

Using  $g_T^s$  from lattice calculation

- Future  $g_T$ : SoLID projected tensor charge
- Future  $d_n$ :  $3.0 \times 10^{-28} e \text{ cm}$

H. Gao, T. Liu, Z. Zhao,  
arXiv:1704.00113, to  
appear in PRD

# Constraint on Quark EDMs

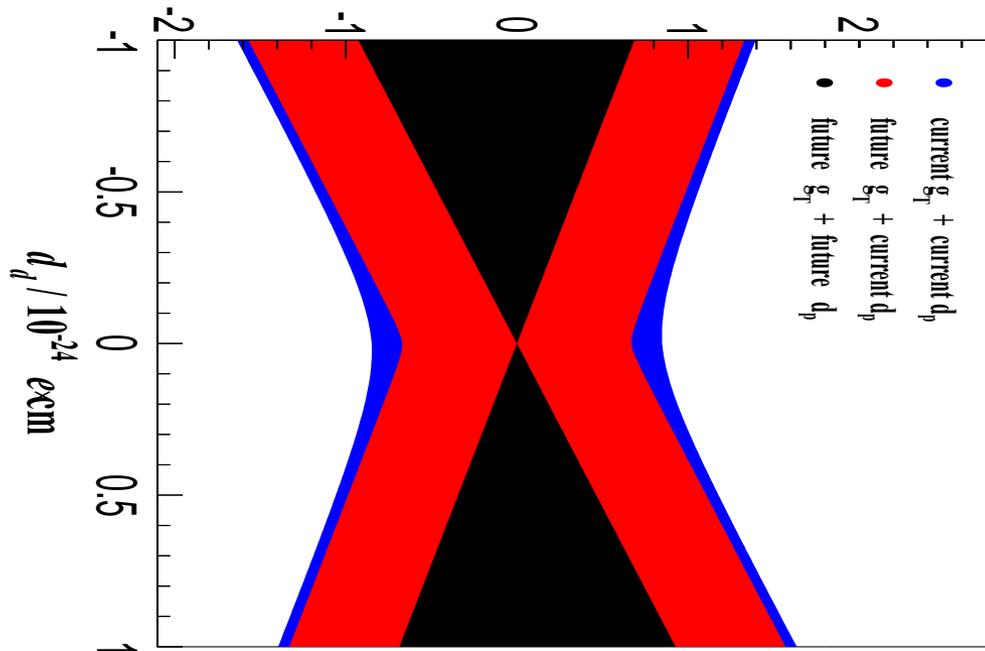
## Current upper limit on the proton EDM

- Mercury atom EDM  
limit:  $7.4 \times 10^{-30} e \text{ cm}$  (95% CL)
- Derived proton EDM  
limit:  $2.6 \times 10^{-25} e \text{ cm}$

B. Graner et al.,  
Phys. Rev. Lett. 116,  
161601 (2016).

Schiff moment method  
including the uncertainty among  
different theoretical models

## Constraint on quark EDMs with tensor charge



$$d_p = g_T^u d_u + g_T^d d_d + g_T^s d_s$$

Using  $g_T^s$  from lattice calculation

- Future  $g_T$ : SoLID  
projected tensor charge
- Future  $d_p$ :  $2.6 \times 10^{-29} e \text{ cm}$

H. Gao, T. Liu, Z. Zhao,  
arXiv:1704.00113, to  
appear in PRD

# Constraint on Quark EDMs (III)

Constraint on quark EDMs with combined proton and neutron EDMs

	$d_u$ upper limit	$d_d$ upper limit
Current $g_T$ + current EDMs	$1.27 \times 10^{-24} e \text{ cm}$	$1.17 \times 10^{-24} e \text{ cm}$
SoLID $g_T$ + current EDMs	$6.72 \times 10^{-25} e \text{ cm}$	$1.07 \times 10^{-24} e \text{ cm}$
SoLID $g_T$ + future EDMs	$1.20 \times 10^{-27} e \text{ cm}$	$7.18 \times 10^{-28} e \text{ cm}$

Include 10% isospin symmetry breaking uncertainty

Sensitivity to new physics

$$d_q \sim \frac{em_q}{(4\pi\Lambda^2)}$$

Three orders of magnitude improvement on quark EDM limit



Probe to 30 ~ 40 times higher scale

Current quark EDM limit:  $10^{-24} e \text{ cm}$



~ 1 TeV

Future quark EDM limit:  $10^{-27} e \text{ cm}$



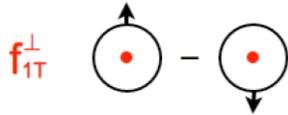
30 ~ 40 TeV

H. Gao, T. Liu, Z. Zhao,  
arXiv:1704.00113, to appear in PRD

# Unpolarized Quark in $p \uparrow$

$$f_{q/p\uparrow}(x, \mathbf{k}_\perp) = f_1^q(x, k_\perp) - f_{1T}^{\perp q}(x, k_\perp) \frac{\hat{\mathbf{P}} \times \mathbf{k}_\perp \cdot \mathbf{S}}{M}$$

## Sivers distribution

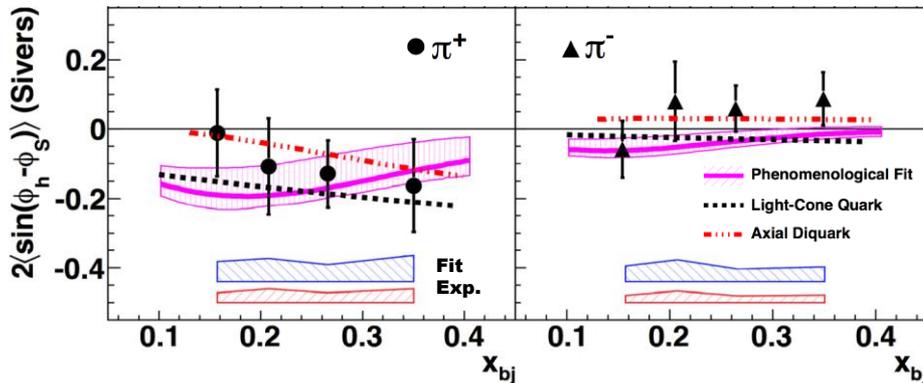


naively time-reversal odd.

$$f_{1T}^{\perp q}(x, k_\perp) \Big|_{\text{SIDIS}} = -f_{1T}^{\perp q}(x, k_\perp) \Big|_{\text{DY}}$$

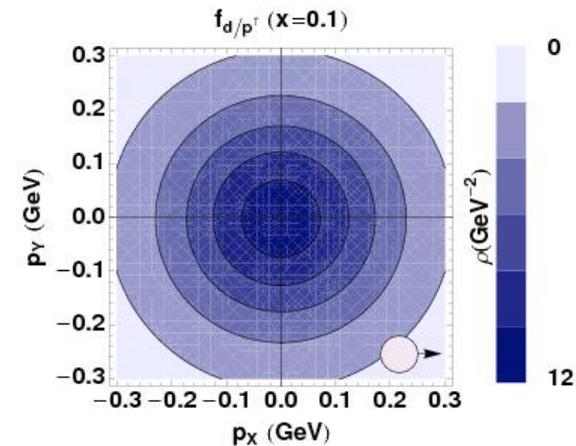
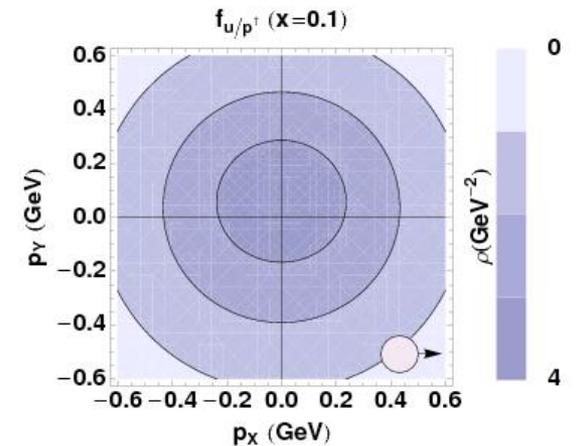
## Measurement in SIDIS

Single spin asymmetry  $A_{UT}^{\sin(\phi_h - \phi_S)} \sim f_{1T}^{\perp}(x, k_\perp) \otimes D_1(z, p_\perp)$   
 (Sivers asymmetry)



6 GeV JLab E06-010, X. Qian *et al.*, PRL 107, 072003 (2011).

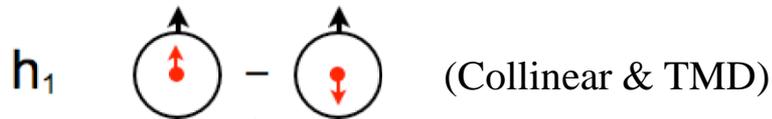
## Model Calculation



Bacchetta, Conti, Radici  
 PR D 78, 074010 (2008).

# Transverse Spin Structure

## Transversity



## Chiral-odd

Unique for the quarks.  
No mixing with gluons.  
Simpler evolution effect.



A transverse counter part to the longitudinal spin structure: helicity  $g_{1L}$

They are NOT the same due to relativity.

NOT accessible via inclusive DIS process.  
Must couple to another chiral-odd function.  
(*e.g.* Collins function  $H_1^\perp$ )

Measured via

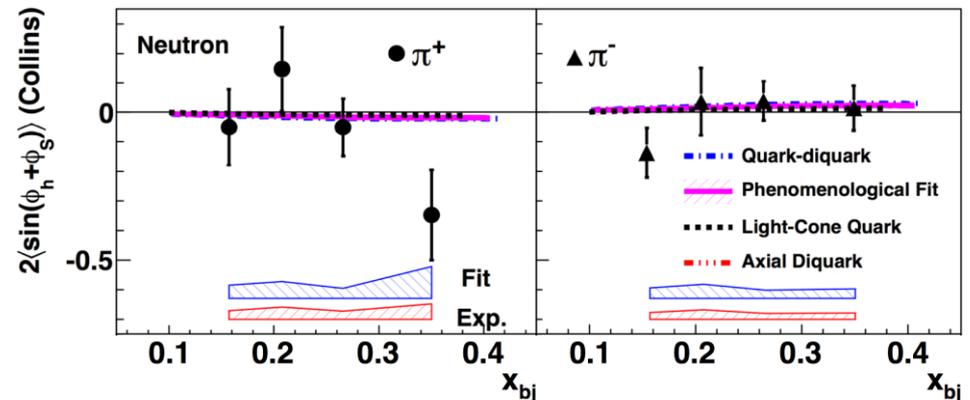
SIDIS (E12-10-006, E12-11-008), Drell-Yan Di-hadron (E12-10-006A)

## Measurement in SIDIS

Single spin asymmetry  
(Collins asymmetry)

$$A_{UT}^{\sin(\phi_h + \phi_S)} \sim h_1(x, k_\perp) \otimes H_1^\perp(z, p_\perp)$$

$H_1^\perp(z, p_\perp)$  Collins fragmentation function



6 GeV JLab E06-010, X. Qian *et al.*, PRL 107, 072003 (2011).

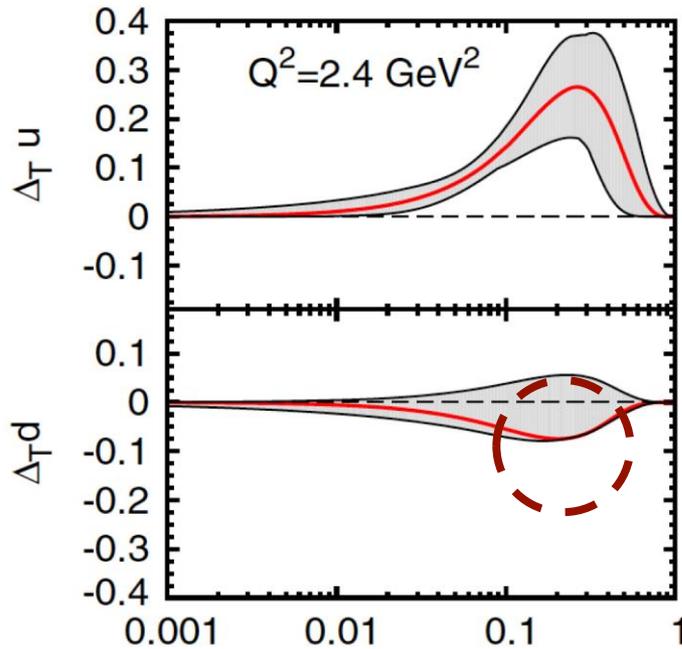
# Soffer's Inequality

## Soffer's bound

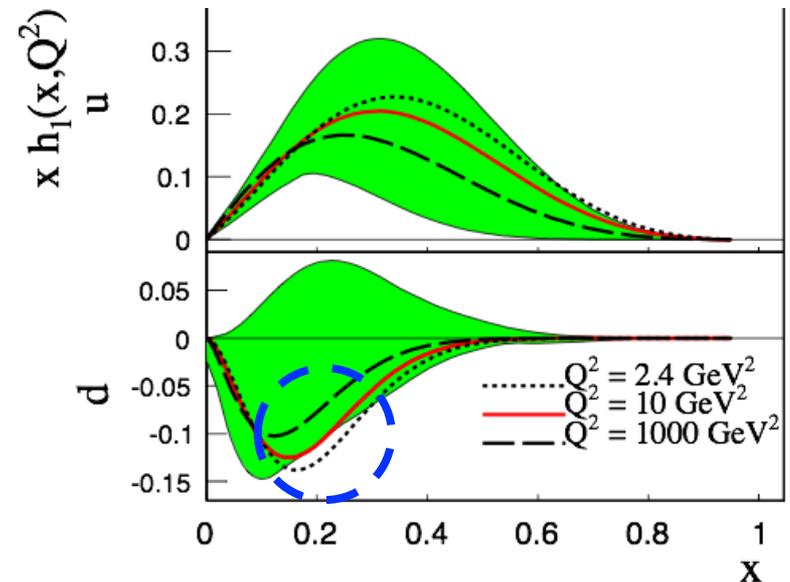
$$|h_1(x)| \leq \frac{1}{2} [f_1(x) + g_{1L}(x)]$$

Derived by using the positivity constraint on the forward scattering helicity amplitude.

## Global fits of transversity



M. Anselmino *et al.*, PR D 92, 114023 (2015).



Z.-B. Kang *et al.*, PR D 93, 014009 (2016).

Test Soffer's inequality @ SoLID

- **Single Spin Asymmetry in Exclusive  $\pi$  Production**  
**Frankfurt et al. have shown  $A_L^\perp$  vanishes if  $\tilde{E}$  is zero**  
 [PRD **60**(1999)014010].
  - **If  $\tilde{E} \neq 0$ , the asymmetry will produce a  $\sin\beta$  dependence.**
- They also argue that precocious factorization of the  $\pi$  production amplitude into three blocks is likely:
  1. overlap integral between  $\gamma$ ,  $\pi$  wave functions.
  2. the hard interaction.
  3. the GPD.
  - **Higher order corrections, which may be significant at low  $Q^2$  for  $\sigma_L$ , likely cancel in  $A_L^\perp$ .**
- **$A_L^\perp$  expected to display precocious factorization at moderate  $Q^2 \sim 2-4 \text{ GeV}^2$ .**

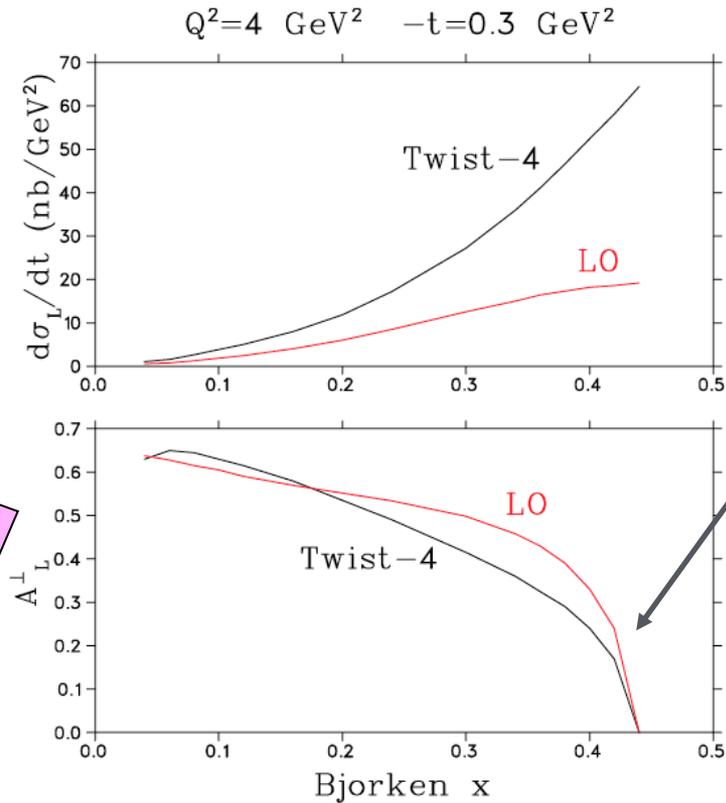
# GPD information in $A_L^\perp$ may be particularly clean

- $A_L^\perp$  is expected to display precocious factorization at only  $Q^2 \sim 2-4 \text{ GeV}^2$ :

- At  $Q^2=10 \text{ GeV}^2$ , Twist-4 effects can be large, but cancel in  $A_L^\perp$

(Belitsky & Müller PLB 513(2001)349).

- At  $Q^2=4 \text{ GeV}^2$ , higher twist effects even larger in  $\sigma_L$ , but still cancel in the asymmetry



This relatively low value of  $Q^2$  for the expected onset of precocious scaling is important, because it is experimentally accessible at Jefferson Lab.

# Transverse Target Single Spin Asymmetry in DEMP



Unpolarized  
Cross section

$$2\pi \frac{d^2 \sigma_{UU}}{dtd\phi} = \varepsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} + \sqrt{2\varepsilon(\varepsilon+1)} \frac{d\sigma_{LT}}{dt} \cos \phi + \varepsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$

Transversely  
polarized cross  
section has  
additional  
components

$$\frac{d^3 \sigma_{UT}}{dtd\phi d\phi_s} = - \frac{P_{\perp} \cos \theta_q}{\sqrt{1 - \sin^2 \theta_q \sin^2 \phi_s}}$$

Gives rise to Asymmetry Moments

$$A(\phi, \phi_s) = \frac{d^3 \sigma_{UT}(\phi, \phi_s)}{d^2 \sigma_{UU}(\phi)}$$

$$= - \sum_k A_{UT}^{\sin(\mu\phi + \lambda\phi_s)_k} \sin(\mu\phi + \lambda\phi_s)_k$$

Unseparated  $\sin\beta = \sin(\varphi - \varphi_s)$  Asymmetry Moment

$$A_{UT}^{\sin(\phi - \phi_s)} \propto \frac{d\sigma_{00}^{+-}}{d\sigma_L \binom{++}{00}} \propto \frac{\text{Im}(\tilde{E}^* \tilde{H})}{|\tilde{E}|^2} \text{ where } \tilde{E} \propto \tilde{H}$$

$$\left( \begin{aligned} & \sin \beta \text{Im}(d\sigma_{++}^{+-} + \varepsilon d\sigma_{00}^{+-}) \\ & + \sin \phi \sqrt{\varepsilon(1+\varepsilon)} \text{Im}(d\sigma_{+0}^{+-}) \\ & + \sin(\phi + \phi_s) \frac{\varepsilon}{2} \text{Im}(d\sigma_{+-}^{+-}) \\ & + \sin(2\phi - \phi_s) \sqrt{\varepsilon(1+\varepsilon)} \text{Im}(d\sigma_{+0}^{-+}) \\ & + \sin(3\phi - \phi_s) \frac{\varepsilon}{2} \text{Im}(d\sigma_{+-}^{-+}) \end{aligned} \right)$$

$\sigma_{mn}^{ij} \rightarrow$  nucleon polarizations  $ij = (+1/2, -1/2)$   
photon polarizations  $mn = (-1, 0, +1)$

Note: Trento convention used for rest of talk

Ref: M. Diehl, S. Sapeta,  
Eur.Phys.J. C41(2005)515.

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# HERMES $\sin(\beta=\varphi-\varphi_s)$ Asymmetry Moment

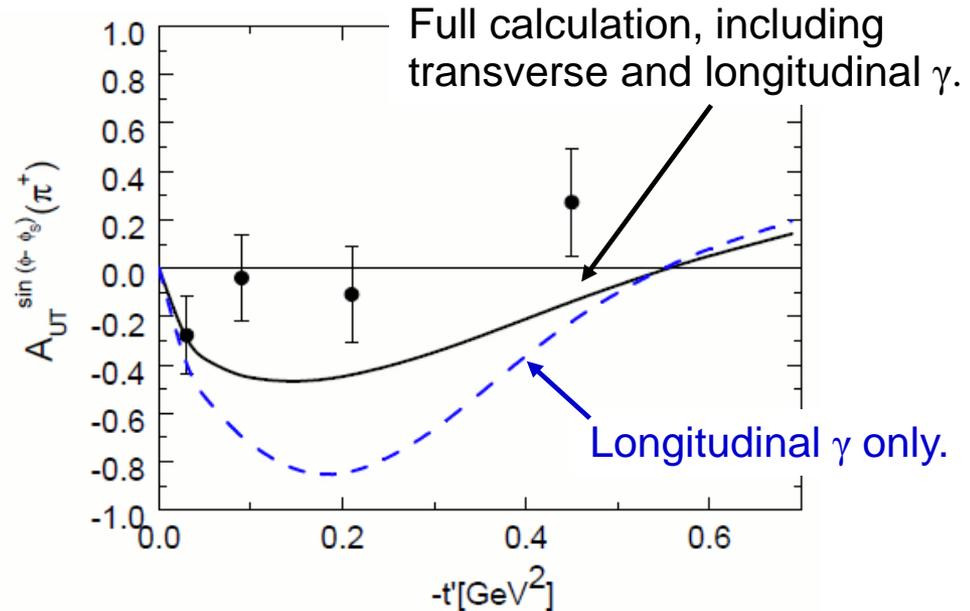


- Exclusive  $\pi^+$  production by scattering 27.6 GeV positrons or electrons from transverse polarized  $^1\text{H}$  **without L/T separation**. [PLB 682(2010)345].

Analyzed in terms of 6 Fourier amplitudes for  $\varphi_\pi, \varphi_s$ .

Asymmetry is diluted by  $\sim 50\%$ .

$\langle x_B \rangle = 0.13$ ,  $\langle Q^2 \rangle = 2.38 \text{ GeV}^2$ ,  
 $\langle -t \rangle = 0.46 \text{ GeV}^2$ .



- Goloskokov and Kroll indicate the HERMES results have significant contributions from transverse photons, as well as from L and T interferences [Eur Phys.J. C65(2010)137].

- Nonetheless, the HERMES data are consistent with GPD models based on the dominance of  $\tilde{E}$  over  $\tilde{H}$  at low  $-t$ .

- In fact, the sign crossing in the model curve at  $-t \approx 0.5 \text{ GeV}^2$  is due to the large contribution from  $\tilde{E}$  demanded by the data.

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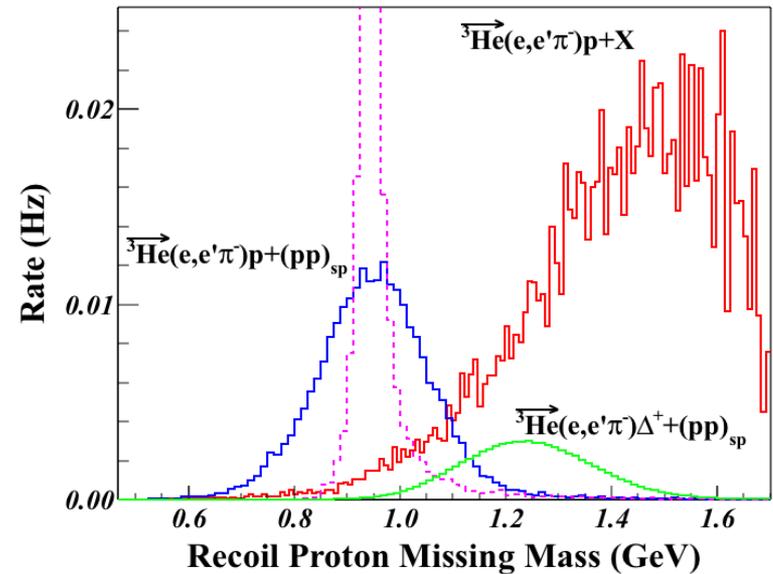
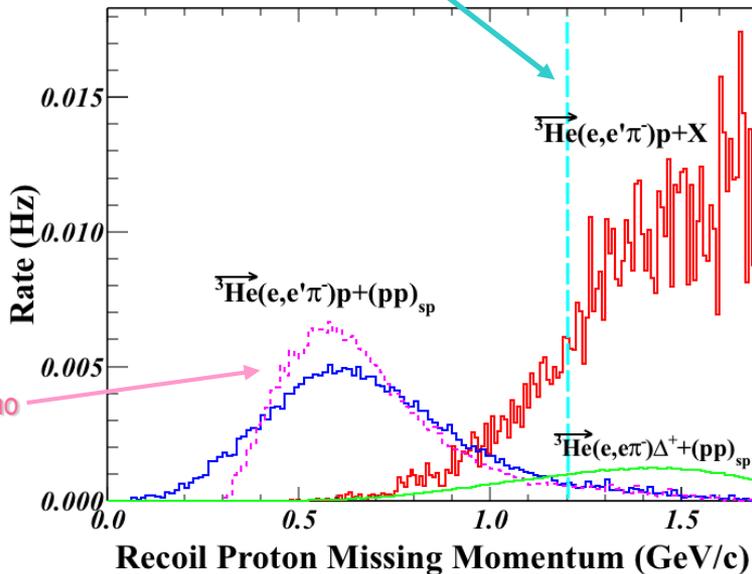
# Example Cuts to Reduce Background



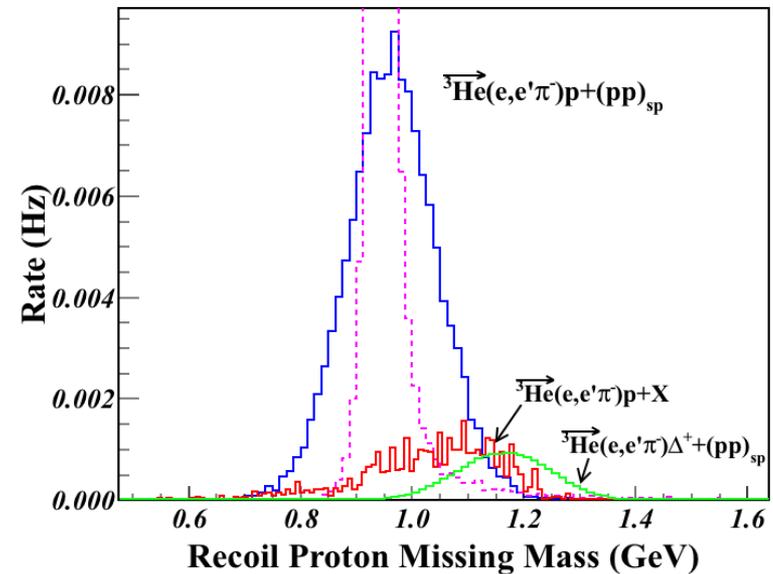
## Two different background channels were simulated:

- SoLID-SIDIS generator  $p(e, e'\pi)X$  and  $n(e, e'\pi^-)X$ , where we assume all  $X$  fragments contain a proton (over-estimate).
- $n \rightarrow \pi \Delta^+ \rightarrow \pi \pi^0 p$  where the  $\Delta^+$  (polarized) decays with  $l=1, m=0$  angular distribution (more realistic).

Apply  $P_{miss} > 1.2$  GeV/c cut



Background remaining after  $P_{miss}$  cut



# Summary



- $A_{UT}^{\sin(\varphi-\varphi_S)}$  transverse single-spin asymmetry in exclusive  $\pi$  production is particularly sensitive to the spin-flip GPD  $\tilde{E}$ . Factorization studies indicate precocious scaling to set in at moderate  $Q^2 \sim 2-4 \text{ GeV}^2$ , while scaling is not expected until  $Q^2 > 10 \text{ GeV}^2$  for absolute cross section.
- $A_{UT}^{\sin(\varphi_S)}$  asymmetry can also be extracted from same data, providing powerful additional GPD-model constraints and insight into the role of transverse photon contributions at small  $-t$ , and over wide range of  $\xi$ .
- **High luminosity and good acceptance capabilities of SoLID make it well-suited for this measurement. It is the only feasible manner to access the wide  $-t$  range needed to fully understand the asymmetries.**
- We propose to analyze the E12-10-006 event files off-line to look for  $e-\pi-p$  triple coincidence events. To be conservative, we assume the recoil proton is only identified, and its momentum is not used to further reduce SIDIS (and other) background.
- **We used a sophisticated UML analysis to extract the asymmetries from simulated data in a realistic manner, just as was used in the pioneering HERMES data. The projected data are expected to be a considerable advance over HERMES in kinematic coverage and statistical precision.**
- SoLID measurement is also important preparatory work for future EIC.

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