

$d^{12}C$ Elastic Scattering in Three-Body Model

Yuriy Uzikov

Joint Institute for Nuclear Research, Dubna, Russia

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- Motivation: Polarimetry for EDM measurements at COSY (talks on September 11 by N. Nikolaev, A. Nass, A. Kononov).

The deuteron spin rotation in storage ring due to intrinsic EDM will be measured by $\vec{d}^{12}C$ elastic scattering with an accuracy $\sim 10^{-6}$.

/N.P.M. Brantes et al., NIMA 664 (2012) 49/

COSY: "We have to know what is what in the $d^{12}C$ elastic scattering, $d^{12}C$ breakup x-section and figure of merit for different energies (and different targets) ..."

- Capability of the Glauber model for the $\vec{p}\vec{d} \rightarrow pd$ at ~ 100 -200 MeV
- Numerical results for $d^{12}C \rightarrow p(0) + X$ within the IA
- $\vec{d}^{12}C$ - elastic scattering within the Glauber theory similarly to the $\vec{d}p$ -scattering

$d^{12}C \rightarrow p(0) + X$ breakup within the IA

Glauber theory for the reaction $d + A \rightarrow p + X$,

L. Bertocchi, D. Treleani, Nuovo Cim. 36 A, 1 (1976). "The cross section contains:

- i) the deuteron breakup with elastic rescattering of the proton and neutron from the deuteron,
- ii) the neutron absorption cross section, when the neutron participates in inelastic collisions only, while the proton scatters elastically".

In practice after some approximations \implies impulse approximation /A.P. Kobushkin, L. Vizireva, J Phys. G8, 893 (1982)/

Relativistic effects by B.L.G.Backer, L.A. Kondratyuk, M.V. Terentjev NPA (1979):

$$E_p \frac{d^2 \sigma}{d^3 p_p} = \frac{I_2 \mathcal{E}_d (\mathcal{E}_n + \mathcal{E}_p) \varepsilon_p(q)}{I_1 16\pi \mathcal{E}_n^2} \left[\frac{u^2(q) + w^2(q)}{(2\pi)^3} \right] (2J_A + 1) \sigma_{tot}^{MX} (nA \rightarrow X) \quad (1)$$

$$I_1 = p_d \cdot p_A, \quad I_2 = p_n \cdot p_A$$

$d^{12}C \rightarrow p(0^\circ) + X$: search for high-momentum components of the d.w.f.

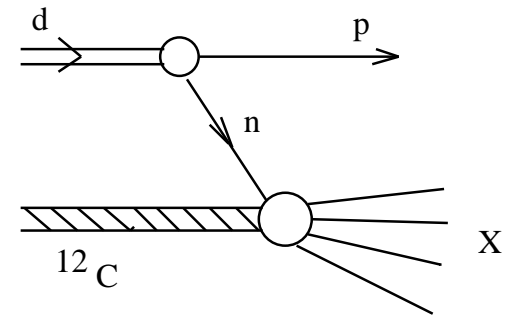
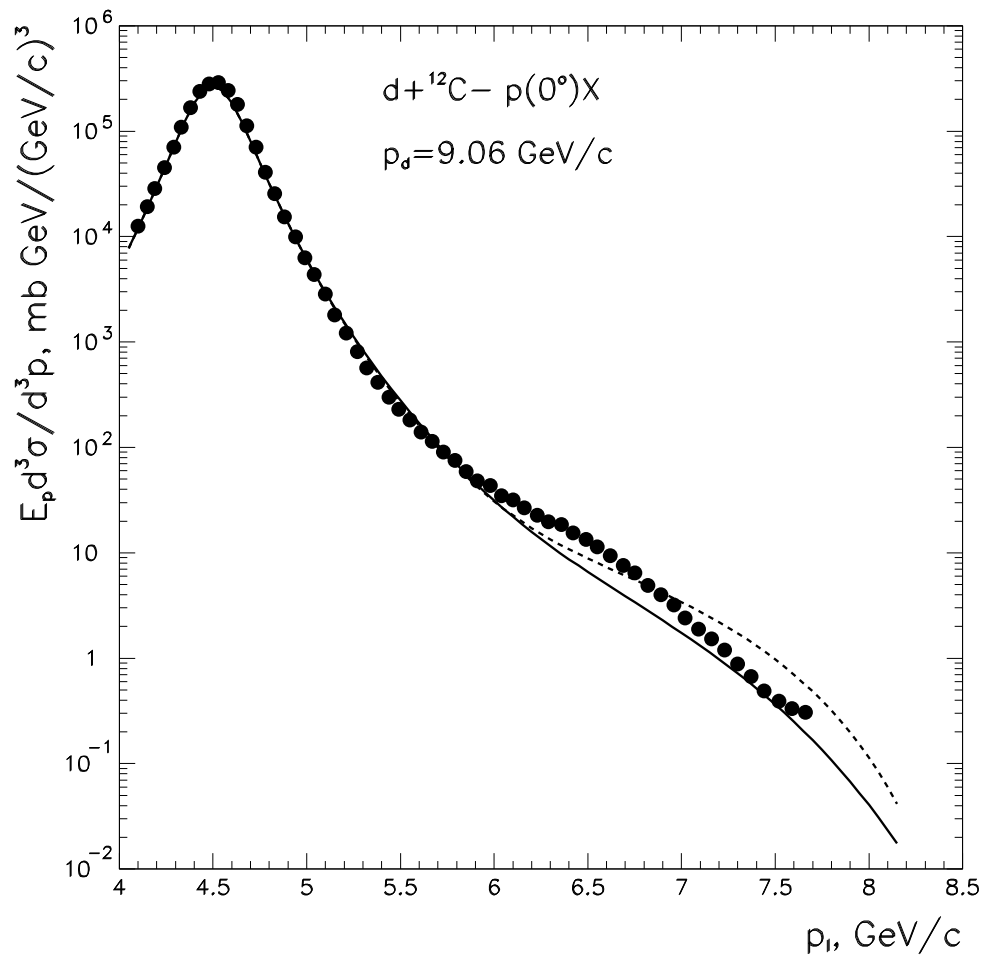
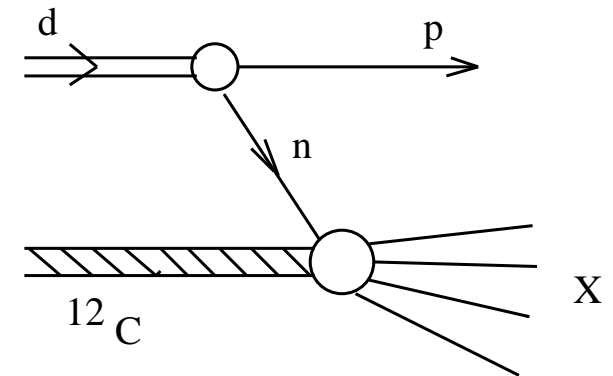
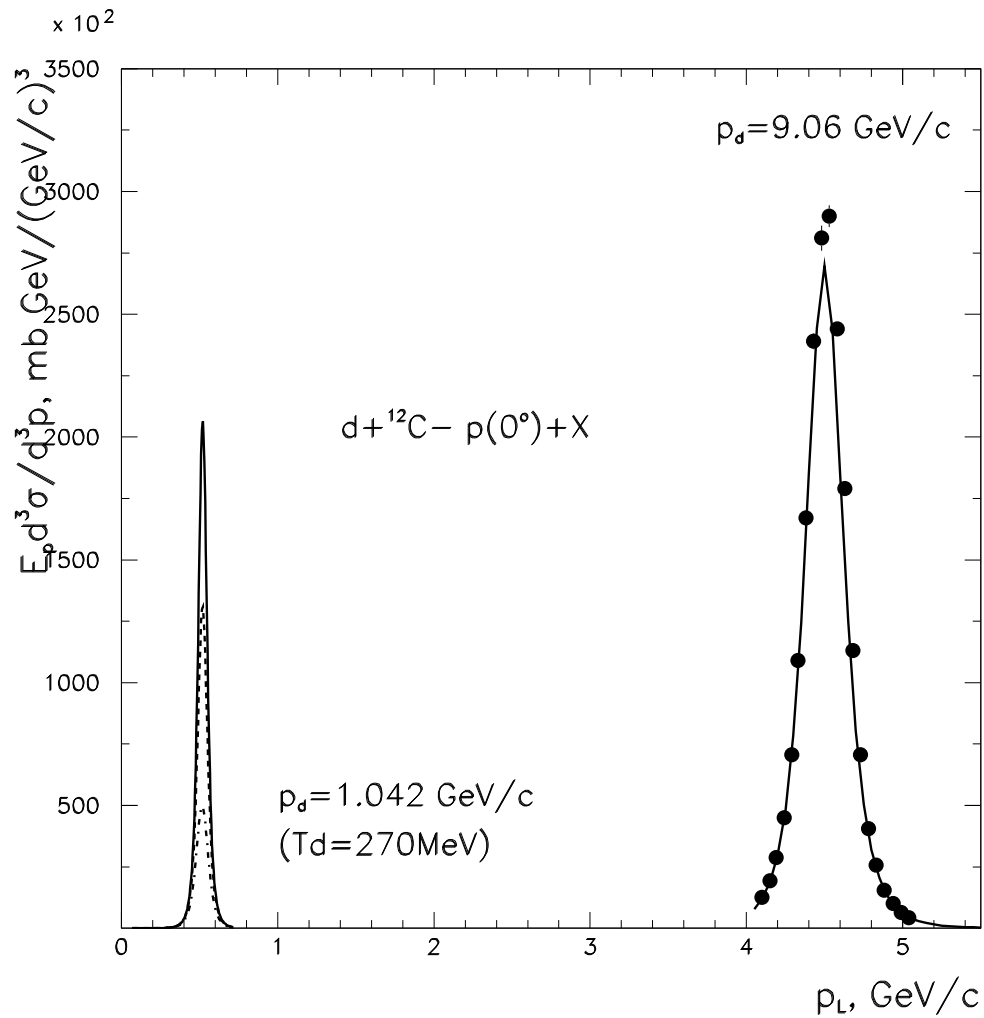


Figure 1: The invariant cross section of the reaction $d + {}^{12}\text{C} \rightarrow p(0^\circ) X$, at $p_d = 9.06 \text{ GeV}/c$ (V. Ableev, 1991) versus lab. momentum of the final proton in comparison with the IA for the CD Bonn (dashed) and Paris (full) d.w.f.

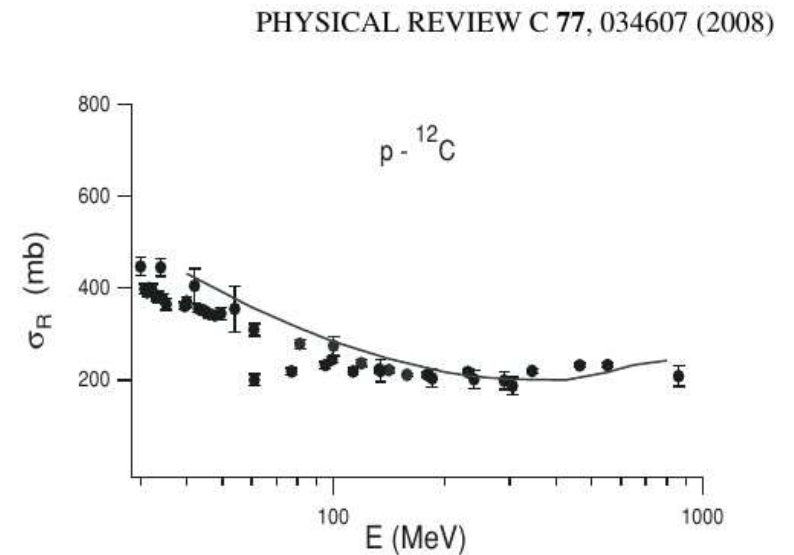
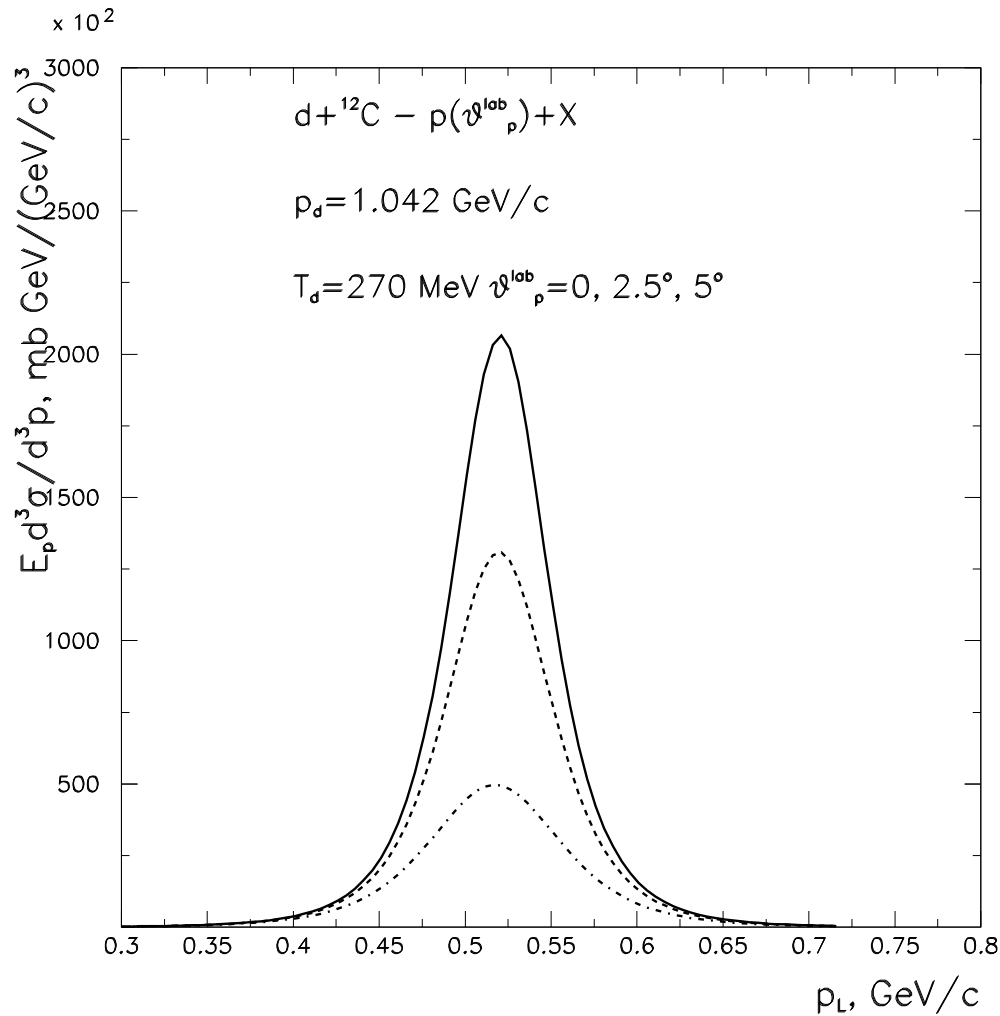
$d^{12}\text{C} \rightarrow p(0^\circ) + X$ within the IA at $T_d = 270 \text{ MeV}$ and $p_d = 9 \text{ GeV}/c$



Curves: the IA calculation

Data at $P_d = 9.06 \text{ GeV}/c$: V.G. Ableev et al. JETP lett. 47, 649 (1988)

$d^{12}C \rightarrow p(0) + X$ within the IA



Curves: the IA calculation at $\theta_p^{\text{lab}} = 0, 2.5^\circ, 5^\circ$

$\sigma_{\text{tot}}^R(n^{12}C \rightarrow X) = 260 \text{ mb}$, B.Abu-Ibrahim et al. PRC 77, 034607 (2008)

ELASTIC pd SCATTERING. Phenomenology of the $pd \rightarrow pd$ transition

$$\frac{1}{2} + 1 \rightarrow \frac{1}{2} + 1$$

$(2 + 1)^2(2\frac{1}{2} + 1)^2 = 36$ transition amplitudes

P-parity \implies 18 independent amplitudes

T-invariance \implies 12 independent amplitudes

Phenomenology of the $pd \rightarrow pd$ transition

$\hat{\mathbf{q}} = (\mathbf{p} - \mathbf{p}')$, $\hat{\mathbf{k}} = (\mathbf{p} + \mathbf{p}')/$, $\hat{\mathbf{n}} = [\mathbf{k} \times \mathbf{q}]$ – unit vect. ($Z \uparrow\uparrow \hat{\mathbf{k}}$, $X \uparrow\uparrow \hat{\mathbf{q}}$ $Y \uparrow\uparrow \hat{\mathbf{n}}$)

$$M = (A_1 + A_2 \boldsymbol{\sigma} \hat{\mathbf{n}}) + (A_3 + A_4 \boldsymbol{\sigma} \hat{\mathbf{n}})(\mathbf{S} \hat{\mathbf{q}})^2 + (A_5 + A_6 \boldsymbol{\sigma} \hat{\mathbf{n}})(\mathbf{S} \hat{\mathbf{n}})^2 + A_7(\boldsymbol{\sigma} \hat{\mathbf{k}})(\mathbf{S} \hat{\mathbf{k}}) + A_8(\boldsymbol{\sigma} \hat{\mathbf{q}}) [(\mathbf{S} \hat{\mathbf{q}})(\mathbf{S} \hat{\mathbf{n}}) + (\mathbf{S} \hat{\mathbf{n}})(\mathbf{S} \hat{\mathbf{q}})] + (A_9 + A_{10} \boldsymbol{\sigma} \hat{\mathbf{n}})(\mathbf{S} \hat{\mathbf{n}}) + A_{11}(\boldsymbol{\sigma} \hat{\mathbf{q}})(\mathbf{S} \hat{\mathbf{q}}) + A_{12}(\boldsymbol{\sigma} \hat{\mathbf{k}}) [(\mathbf{S} \hat{\mathbf{k}})(\mathbf{S} \hat{\mathbf{n}}) + (\mathbf{S} \hat{\mathbf{n}})(\mathbf{S} \hat{\mathbf{k}})]$$

$A_1 \div A_{12}$ T-even P-even:

M. Platonova, V. Kukulín, PRC **81** (2010) 014004

The polarized elastic differential pd cross section

$$\left(\frac{d\sigma}{d\Omega}\right)_{pol} = \left(\frac{d\sigma}{d\Omega}\right)_0 \left[1 + \frac{3}{2} p_j^p p_i^d C_{j,i} + \frac{1}{3} P_{ij}^d A_{ij} + \dots\right]. \quad (2)$$

$$C_{y,y} = Tr M S_y \sigma_y M^+ / Tr M M^+, \quad \dots \quad (3)$$

$$\hat{M}(\mathbf{q}, \mathbf{s}) = \exp\left(\frac{1}{2}i\mathbf{q} \cdot \mathbf{s}\right) M_{pp}(\mathbf{q}) + \exp\left(-\frac{1}{2}i\mathbf{q} \cdot \mathbf{s}\right) M_{pn}(\mathbf{q}) + \frac{i}{2\pi^{3/2}} \int \exp(i\mathbf{q}' \cdot \mathbf{s}) \left[M_{pp}(\mathbf{q}_1) M_{pn}(\mathbf{q}_2) + p \leftrightarrow n \right] d^2\mathbf{q}'.$$

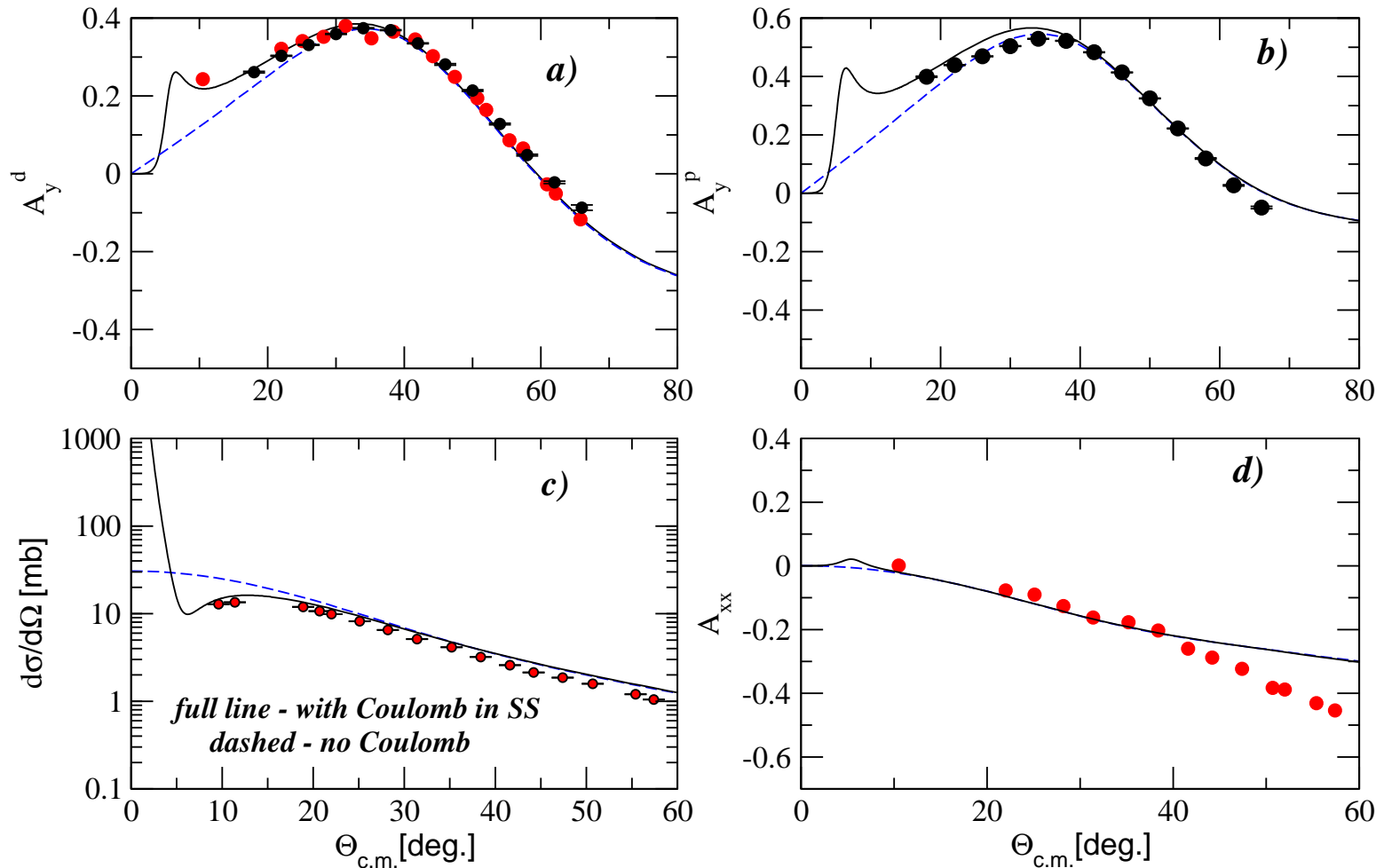
On-shell elastic pN scattering amplitude (**T-even, P-even**, from SAID)

$$M_{pN} = A_N + (C_N \boldsymbol{\sigma}_1 + C'_N \boldsymbol{\sigma}_2) \cdot \hat{\mathbf{n}} + B_N (\boldsymbol{\sigma}_1 \cdot \hat{\mathbf{k}}) (\boldsymbol{\sigma}_2 \cdot \hat{\mathbf{k}}) + (G_N - H_N) (\boldsymbol{\sigma}_1 \cdot \hat{\mathbf{n}}) (\boldsymbol{\sigma}_2 \cdot \hat{\mathbf{n}}) + (G_N + H_N) (\boldsymbol{\sigma}_1 \cdot \hat{\mathbf{q}}) (\boldsymbol{\sigma}_2 \cdot \hat{\mathbf{q}})$$

Spin formalism by [M. Platonova, V. Kukulín, PRC 81 \(2010\)](#) is transformed to the Madison reference frame in: [A. Temerbayev, Yu.N. Uzikov, Yad. Fiz. 78 \(2015\)](#)

Test calculations: pd elastic scattering at 135 MeV

A.A. Temerbayev, Yu.N. Uzikov, Yad. Fiz. **78** (2015) 38 [Phys. At. Nucl. 78 (2015) 35]

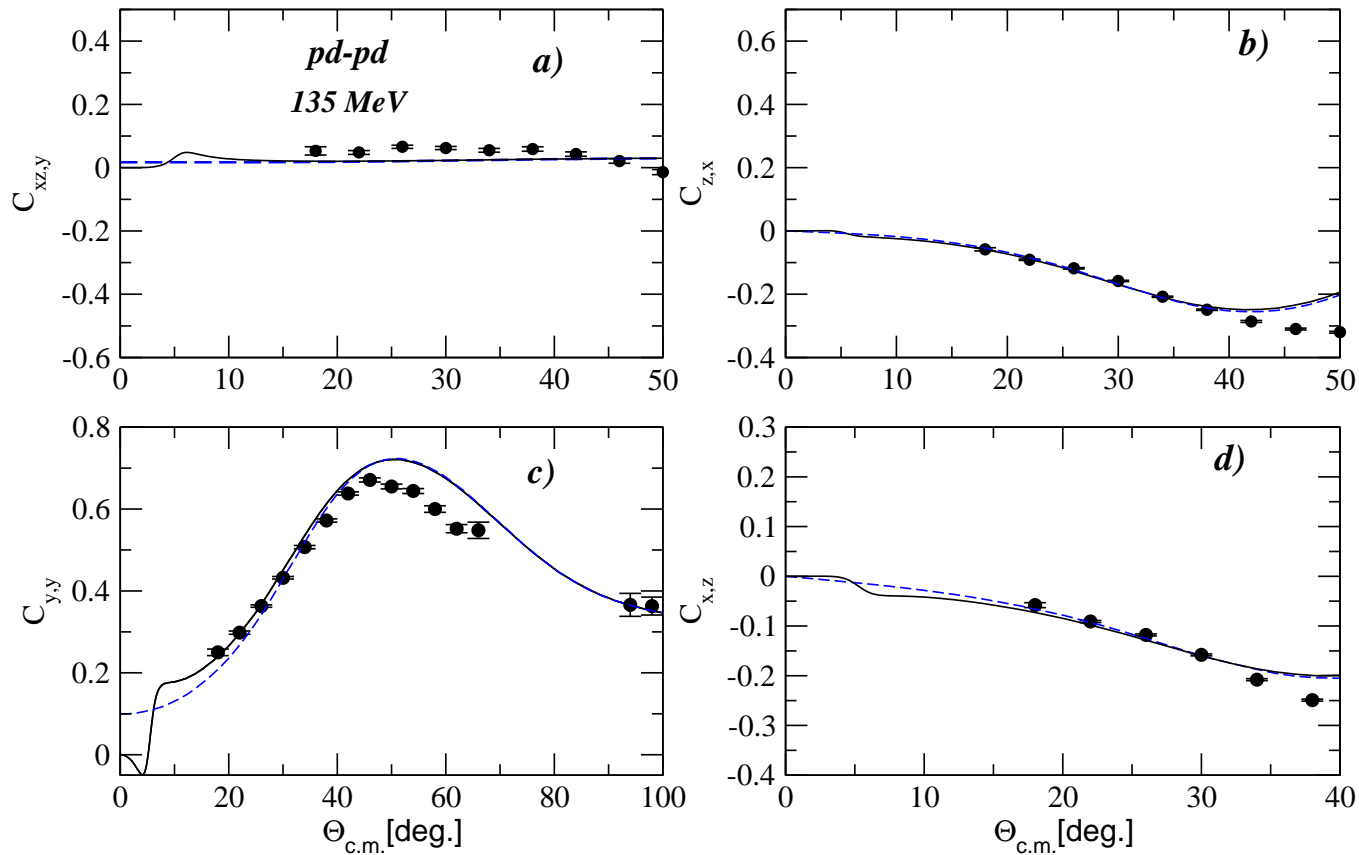


Data: K. Sekiguchi et al. PRC (2002); B. von Przewoski et al. PRC (2006)

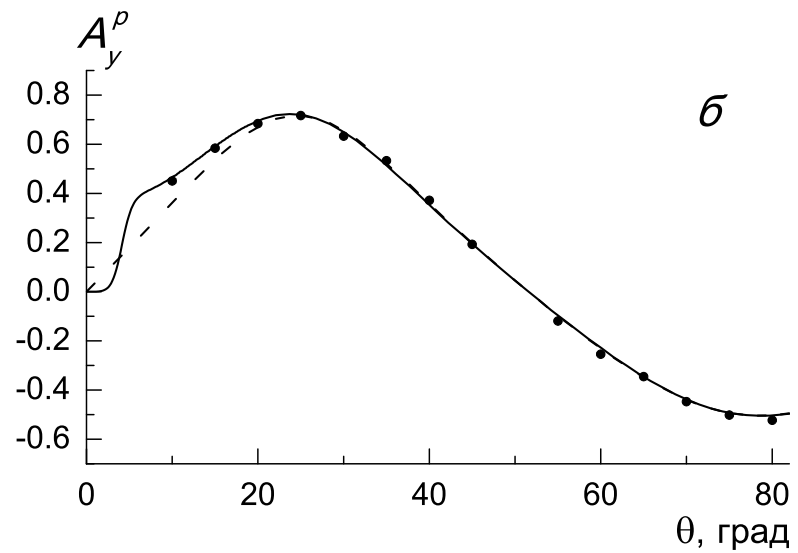
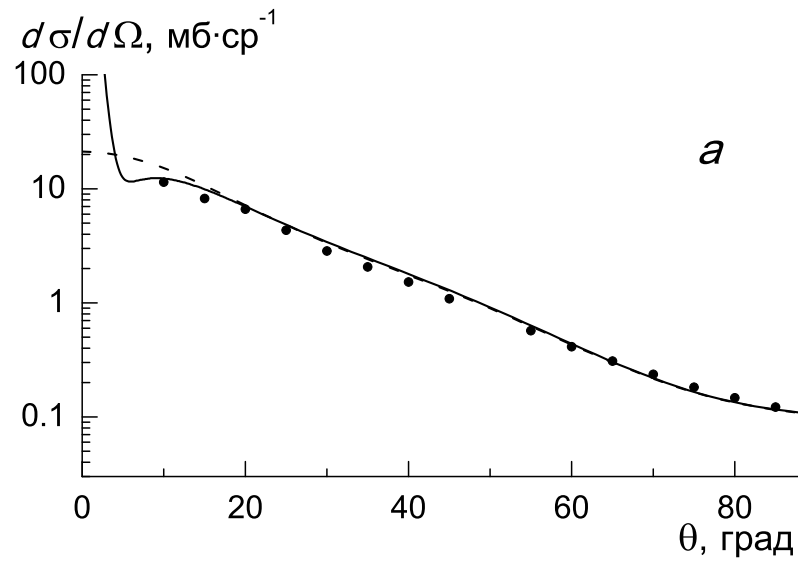
See also **Faddeev calculations**: A.Deltuva, A.C. Fonseca, P.U. Sauer, PRC 71 (2005) 054005.

Test calculations-II: *pd* elastic scattering at 135 MeV

Yu.N. Uzikov, A.A. Temerbavev, Phvs.Rev. C 92 (2015) 014002



Data: von B.Przewoski et al. PRC 74 (2006) 064003 **Curves: the spin-dependent Glauber theory**
Faddeev calculations give very similar results (A.Deltuva, A.C. Fonseca, P.U. Sauer, PRC (2005)).



Phenomenology of the $d^{12}C \rightarrow d^{12}C$ transition

$$\vec{1} + 0 \rightarrow \vec{1} + 0$$

$(2 + 1)^2 = 9$ transition amplitudes

P-parity \implies 5 independent amplitudes

T-invariance \implies 4 independent amplitudes

$$T_{fi} = e_{\beta}^{(\lambda')*} T_{\beta\alpha}(\mathbf{k}, \mathbf{k}') e_{\alpha}^{(\lambda)} \quad (4)$$

$$T_{xx} = A, \quad T_{xy} = 0 \quad T_{xz} = E$$

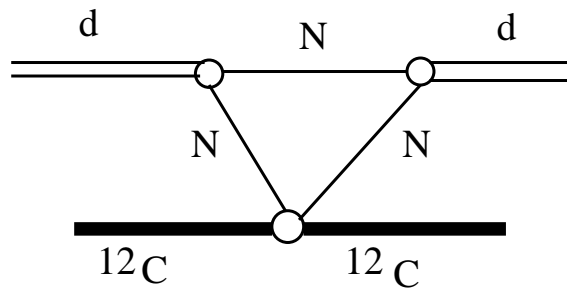
$$T_{yx} = 0 \quad T_{yy} = B \quad T_{yz} = 0$$

$$T_{zx} = D \quad T_{zy} = 0 \quad T_{zz} = C,$$

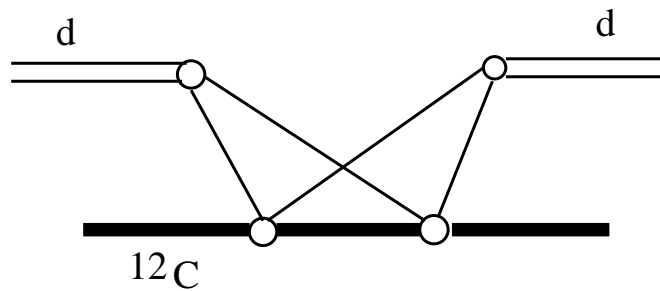
T-invariance:

$$D = E$$

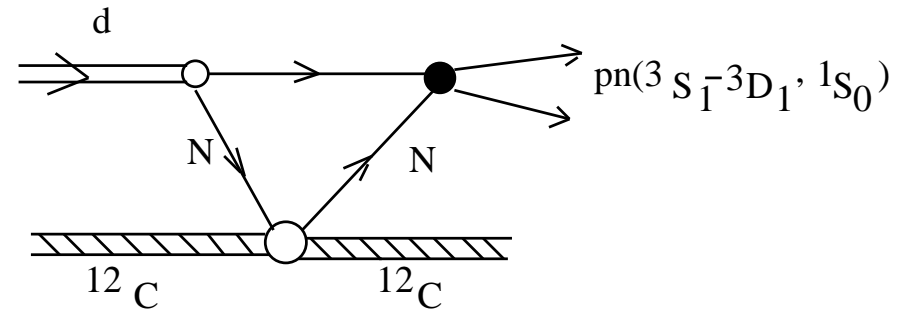
At the next step...



SS



DS



The Glauber formalism

as a modification of the $dp \rightarrow dp$

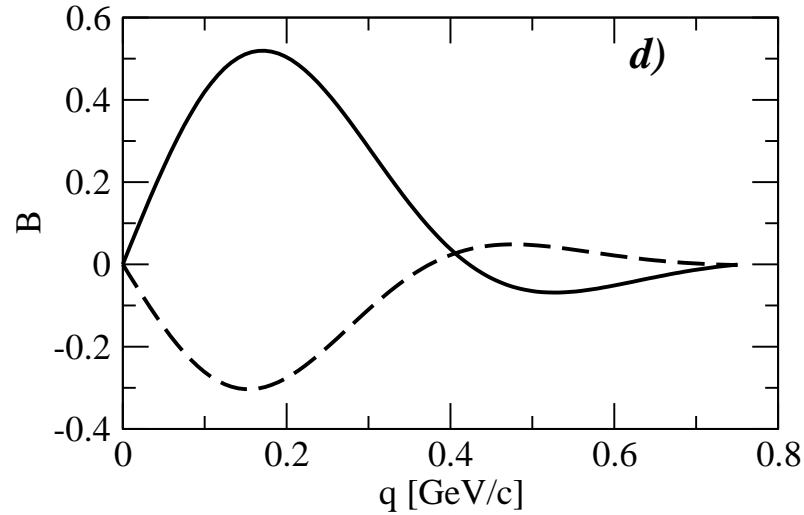
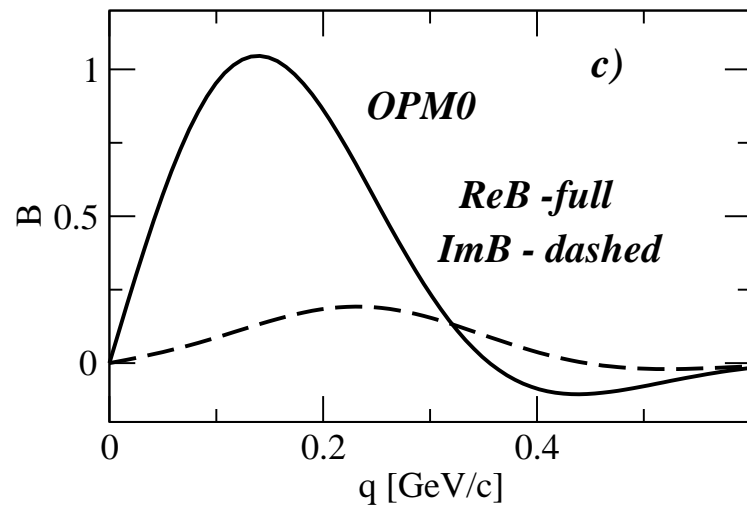
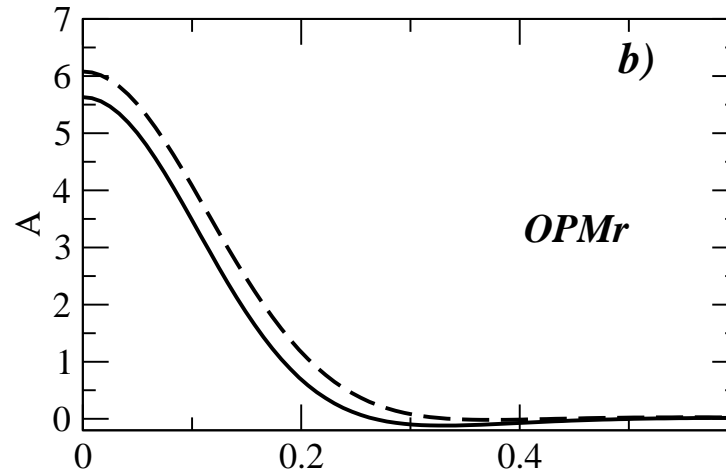
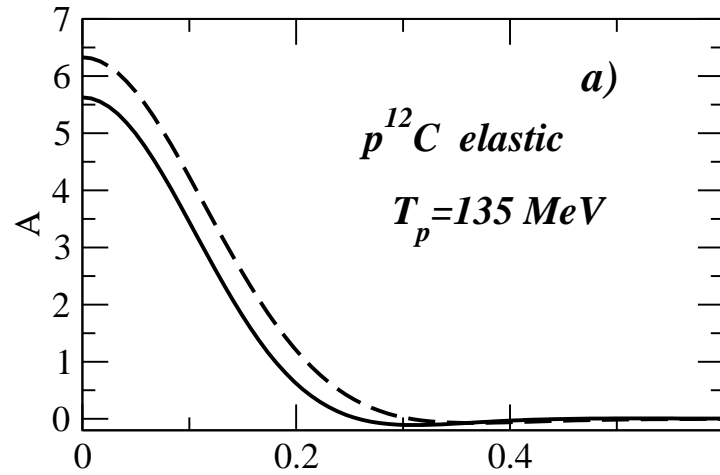
$Np \rightarrow Np$ on-shell $\implies n^{12C}$ on-shell elastic

$^{12}C N$ scattering amplitude

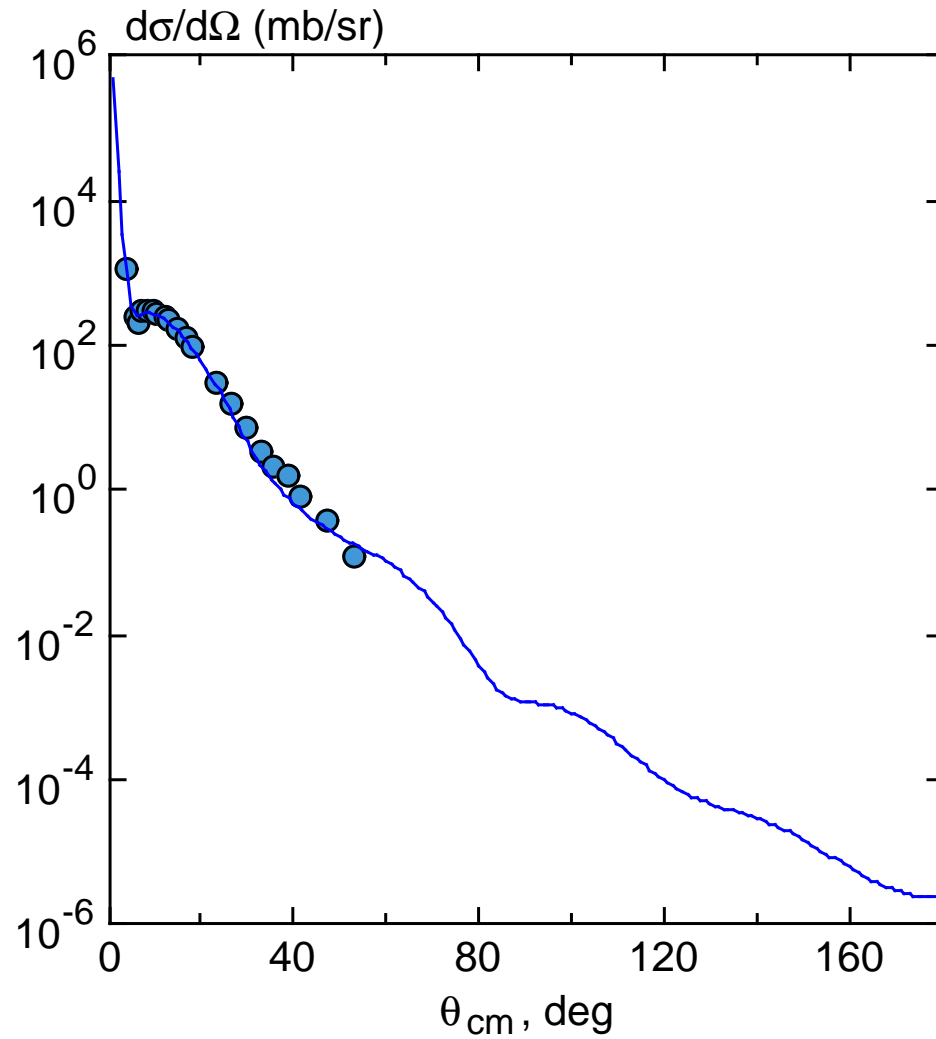
In analogy with the $dp \rightarrow \{pn\}_S + p$

$$M_N(\mathbf{p}, \mathbf{q}; \boldsymbol{\sigma}_N) = A_N + iB_N \boldsymbol{\sigma}_N \cdot \hat{\mathbf{n}}$$

A and B amplitudes of the $p^{12}C$ -elastic scattering (OPM)



E.T. Ibraeva, Yu.N. U. Phys. At. Nucl. 81(2018) 479



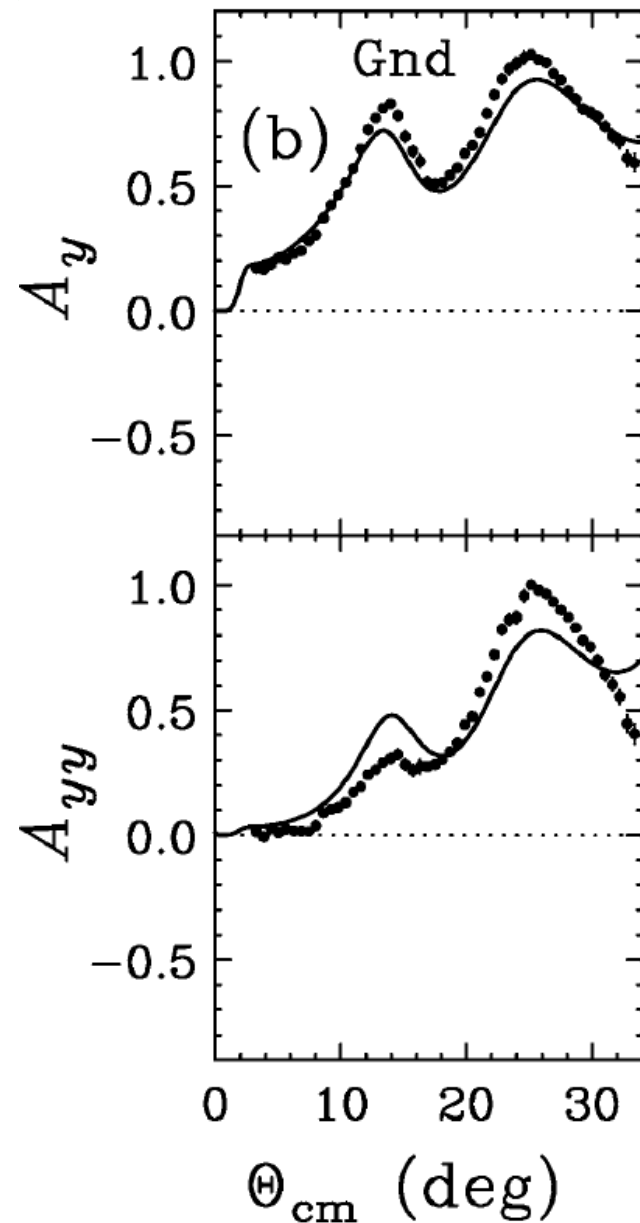
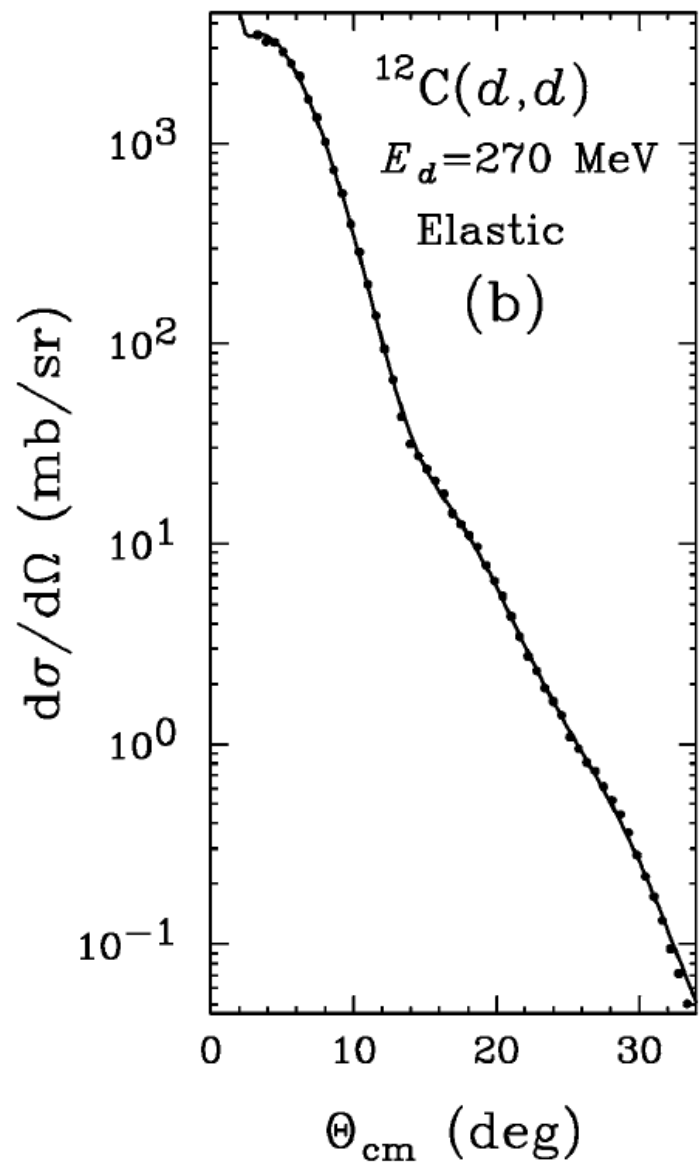
Data – J.L. Comfort, K.C.Karp, PRC 21 (1980) 2162

OPM:

$$U(r) = V_V(r)f(x_R) + iW_V(r)f(x_I) + \left(V_{SO} \frac{1}{r} \frac{d}{dr} f(x_{RSO}) + iW_{SO} \frac{1}{r} \frac{d}{dr} f(x_{ISO}) \right) (\mathbf{L} \cdot \mathbf{s}) - i4a_D W_D \frac{d}{dr} f(x_{RD}) + V_{Coul}(r); \quad (5)$$

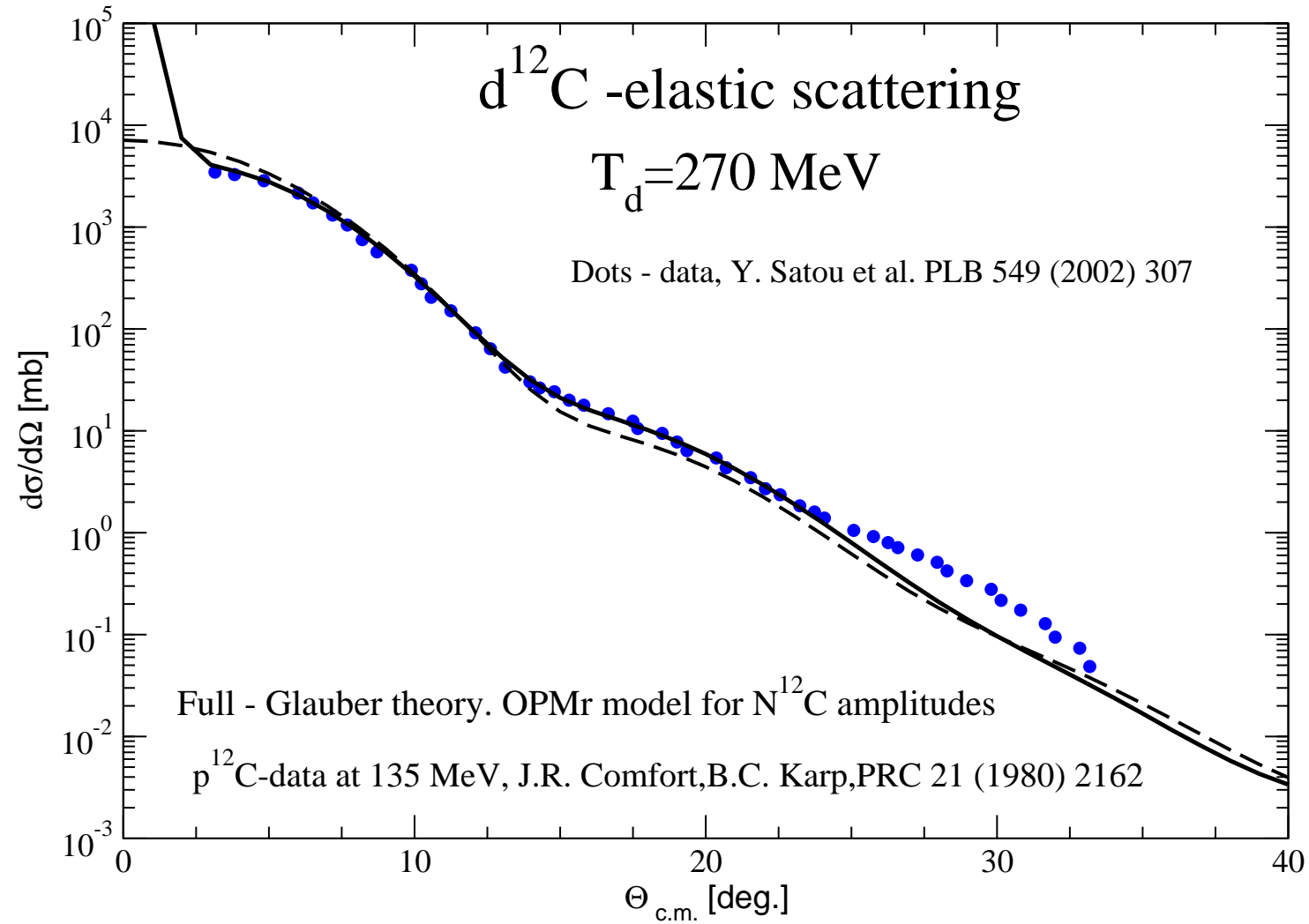
where $f(x_i) = [1 + \exp(x_i)]^{-1}$, $x_i = (r - R_i)/a_i$, $R_i = r_i A^{1/3}$.

[1]. I. Satou et al. Phys.Lett.B 549 (2002) 307: $^{12}\text{C}(d, d')$ at 270 MeV



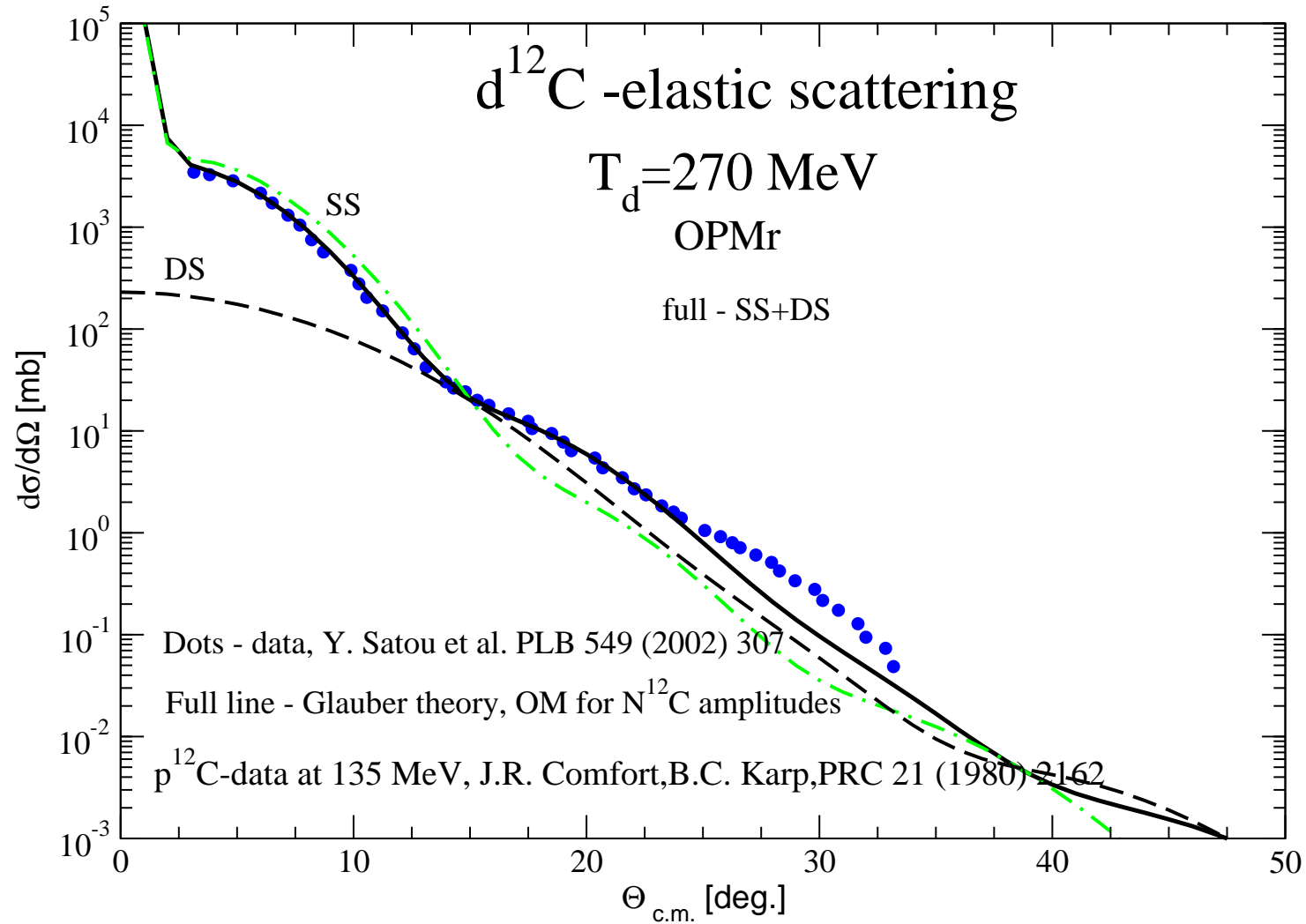
Only optical model was applied to the (elastic) existing $d^{12}\text{C}$ data in Ref.[1].

Glauber theory with the OPM for $N^{12}C$ -elastic- l



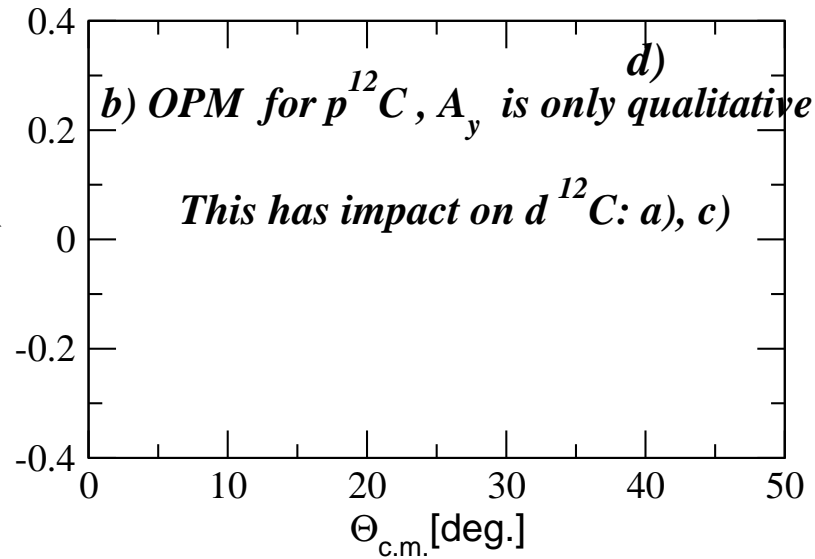
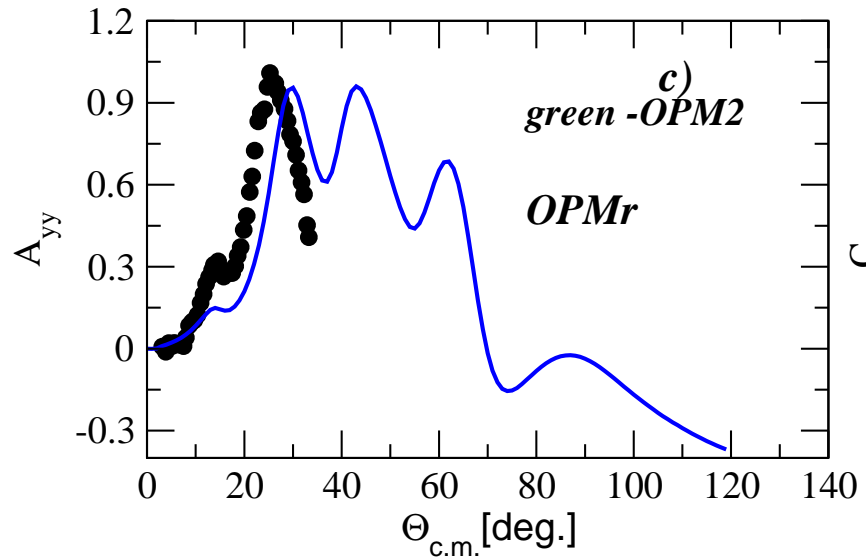
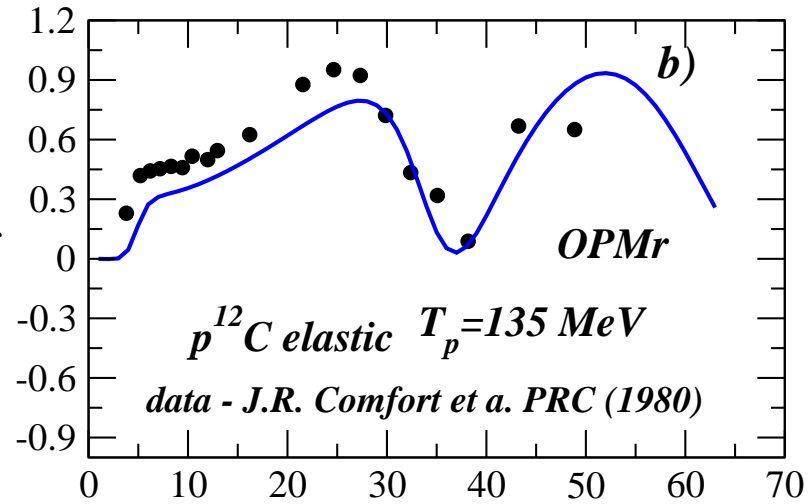
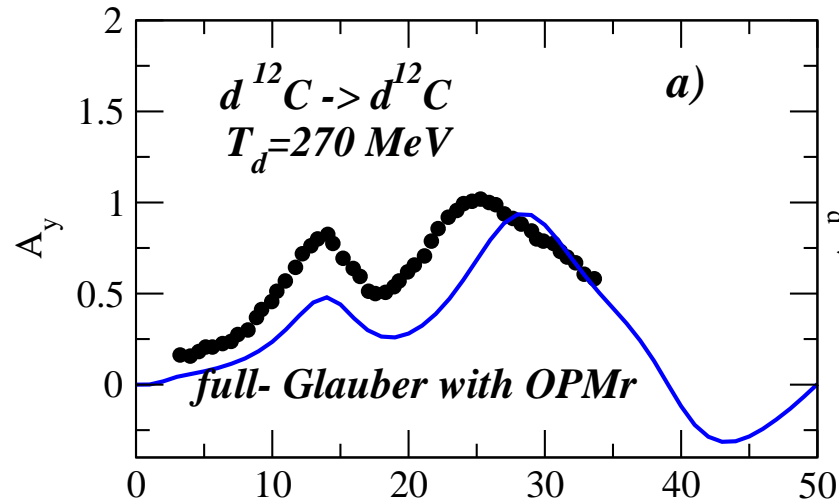
E.T. Ibraeva, Yu.N. Uzikov, Phys.At. Nucl. **81** (2018) 479 [Yad.Fiz. 81(2018) 451]

Glauber theory with the OPM for $N^{12}C$ -elastic -II



E.T. Ibraeva, Yu.N. Uzikov, Phys.At. Nucl. **81** (2018) 479

Glauber theory with the OPM for $N^{12}C$ -elastic -III



SUMMARY and OUTLOOK

- The cross section of the inclusive reaction $d + {}^{12}\text{C} \rightarrow p(0^\circ) + X$ is calculated within the IA at $T_d = 270$ MeV.
- $pd \rightarrow dp$:
Agreement between the Glauber theory (full spin-dependence of the NN plus Coulomb) and the $pd \rightarrow pd$ data on $d\sigma/d\Omega$, A_y , $C_{y,y}$, $C_{xz,y}$ at energy 135 MeV is obtained in forward hemisphere.
- The same approach is used at these energies for the processes $d^{12}\text{C} \rightarrow d^{12}\text{C}$ with a similar accuracy of calculations.
The first results for $d^{12}\text{C} \rightarrow d^{12}\text{C}$ elastic are encouraging.
- **Next step:**
 - ★ Improve OPM for A_y in $p^{12}\text{C} \Rightarrow A_y, A_{yy}$ in $d^{12}\text{C}$.
 - ★ Apply the full Glauber calculation to $p^{12}\text{C}$, $n^{12}\text{C}$ and then $\Rightarrow d^{12}\text{C} \rightarrow d^{12}\text{C}$ and $d^{12}\text{C} \rightarrow \{pn\} + {}^{12}\text{C}$ with $E_{pn} = 0 - 5$ MeV.
 - ★ Consider lower energies $T_p = 70 - 100$ MeV of the proton beam.

THANK YOU FOR ATTENTION!