Tensor-polarized structure functions of spin-one deuteron

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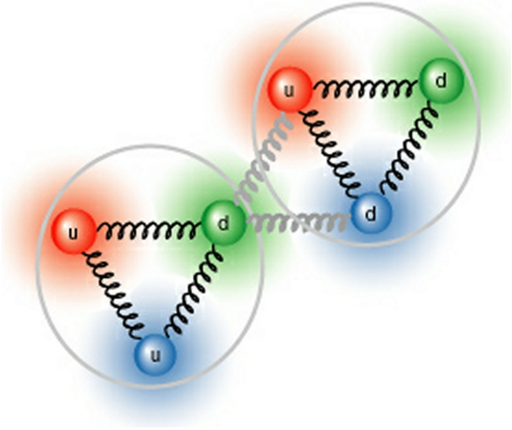
Outline

- Motivation
- Theoretical and experimental status
- Results

Tensor-polarized structure in deuteron

The deuteron was originally considered as proton and neutron in S wave.

Experimental magnetic moment of deuteron is consistent with the S-wave proposal, while the existence of electric quadrupole moment indicates that the deuteron should also contain D wave.



Magnetic Moment(D) $\approx$ Magnetic Moment(p)+Magnetic Moment(n)

$$\text{S wave}: \delta_T q_i(x,Q^2) = q_i^{\,0} - \frac{q_i^{\,1} + q_i^{\,-1}}{2} = 0,\ b_1 = \frac{1}{2}\sum_i e_i^2 (\delta_T q_i(x,Q^2) + \delta_T \bar{q}_i(x,Q^2)) = 0$$

$$\text{S-D Mix}: \delta_T q_i(x,Q^2) = q_i^{\,0} - \frac{q_i^{\,1} + q_i^{\,-1}}{2} \neq 0,\ b_1 = \frac{1}{2}\sum_i e_i^2 (\delta_T q_i(x,Q^2) + \delta_T \bar{q}_i(x,Q^2)) \neq 0$$

where q^m is patron distribution function in hadron spin-m state.

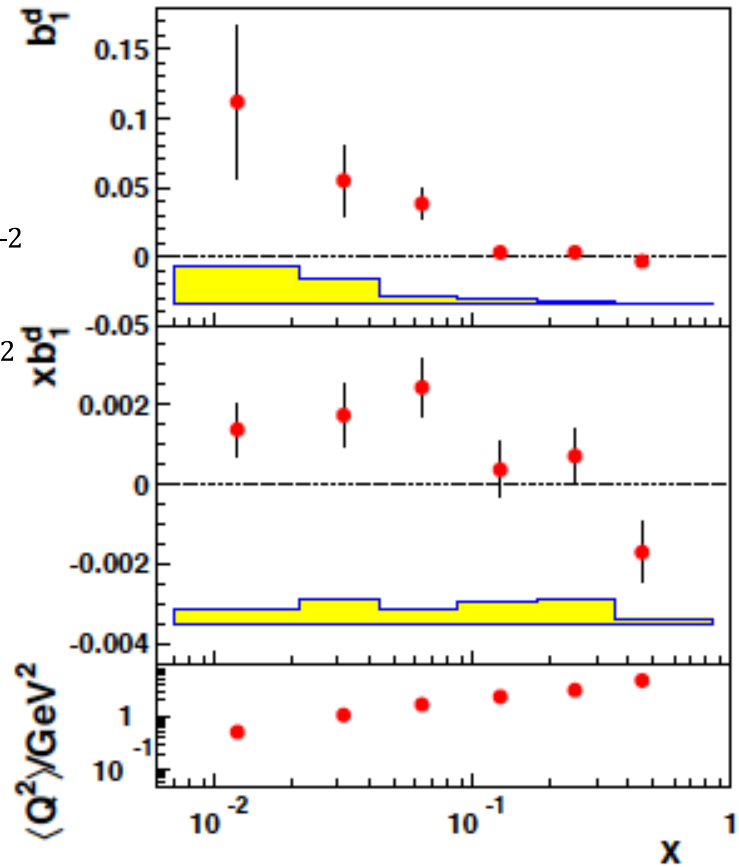
Puzzle of deuteron tensor structure

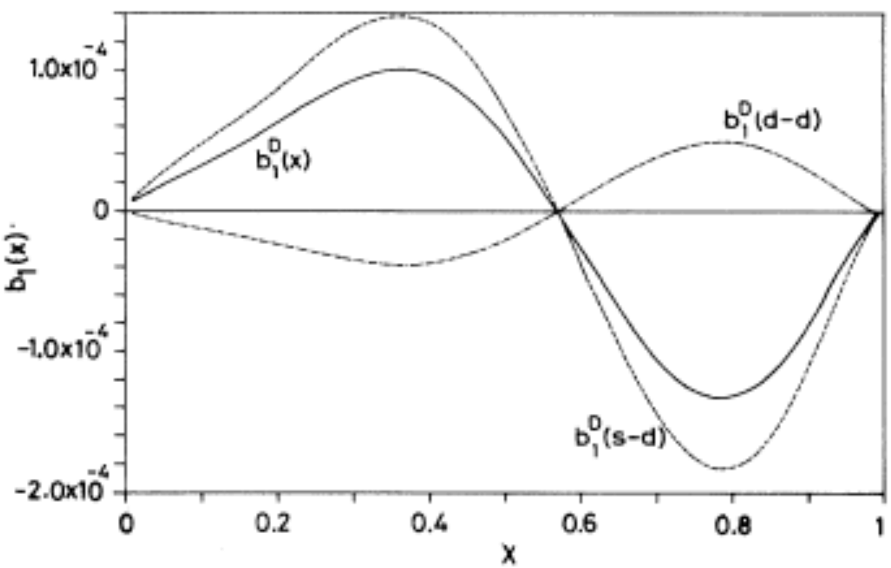
Hermes data show that b_1 is not as small as the prediction for the S-D mixture proposal.

$$\int_{0.002}^{0.85} b_1(x)dx = [1.05 \pm 0.34(stat) \pm 0.35(sys)] \times 10^{-2}$$

$$\int_{0.02}^{0.85} b_1(x)dx = [0.35 \pm 0.10(stat) \pm 0.18(sys)] \times 10^{-2}$$

H.Khan and P. Hoodhoy, PRC 44 (1991) 1219
A. Airapetian *et al.* (HERMES), PRL 95 (2005) 242001.

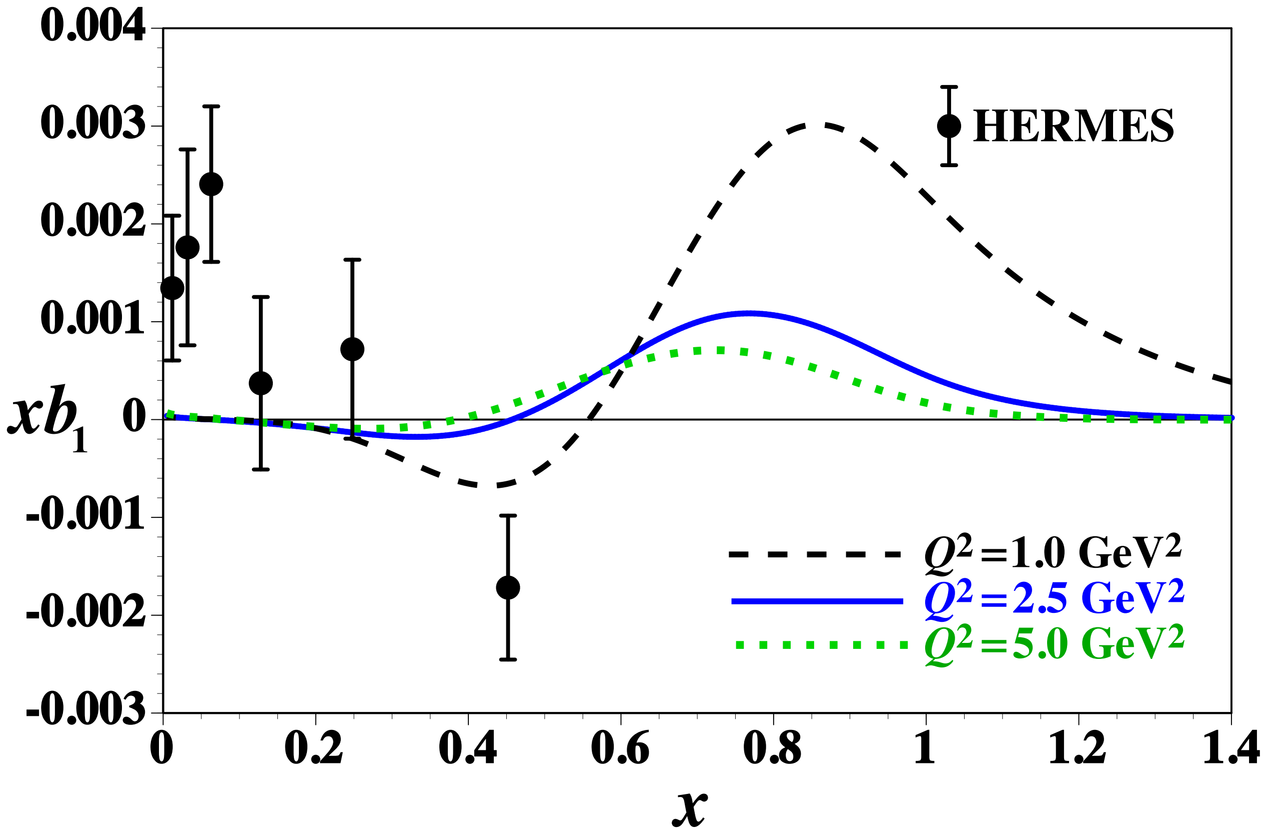




$xb_1 \sim 10^{-4}$

Order of magnitude difference

$xb_1 \sim 10^{-3}$ **in HERMES data**



W. Cosyn, Yu-Bing Dong, S. Kumano and M. Sargsian, PRD 95 (2016) 074036

Standard S-D mixture proposal can not explain the experimental data.

Possible explanations for the unexpected b_1 of the deuteron:

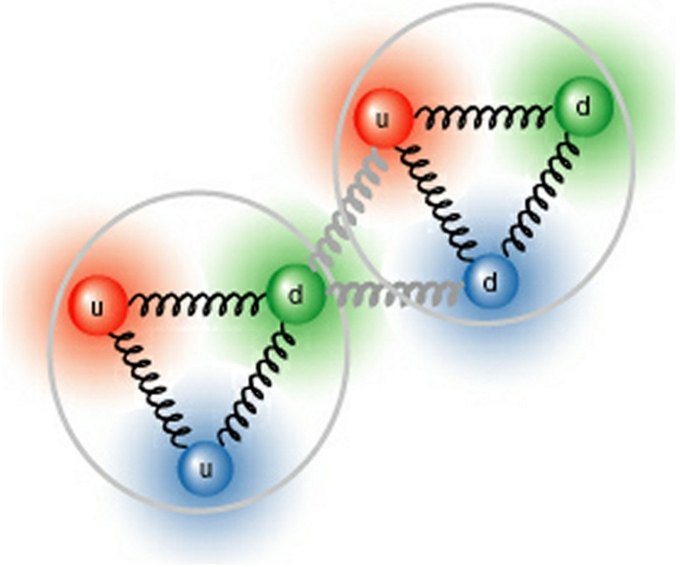
- Six quarks configuration of the deuteron
- Shadowing effects of the nucleus

G. A. Miller, PRC 89 (2014) 045203
N. N. Nikolaev and W. Schafer, PLB 398 (1997) 245
J. Edelmann, G. Piller, and W. Weise, Z. Phys. A 357, 129 (1997)
K. Bora and R. L. Jaffe, PRD 57 (1998), 6906

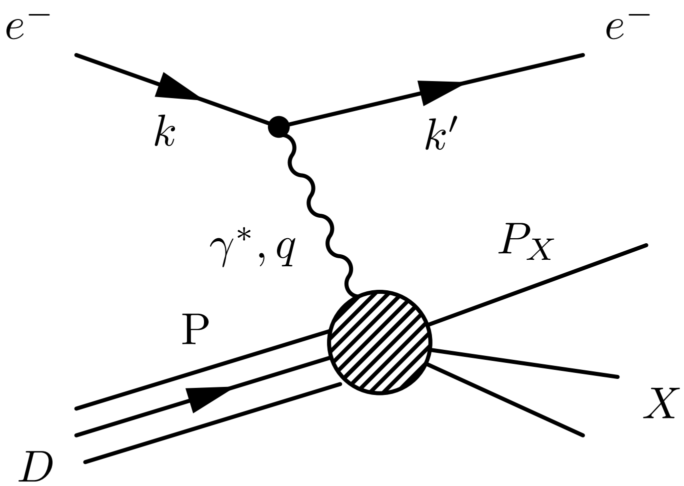
The structure of the deuteron is not well understood!

An introduction to tensor structure of deuteron: theory and experiment

Two ways to investigate the structure of deuteron are
Deep Inelastic Scattering and Drell-Yan Process



Deuteron Structure Function in DIS



DIS for deuteron

$$W_{\mu\nu}^{\lambda_i\lambda_f} = \int \frac{d^4x}{4\pi} e^{iqx} \langle p,\lambda_f | J_\mu(x) J_\nu(0) | p,\lambda_i \rangle$$

$$W_{\mu\nu}^{\lambda_i\lambda_f} = -F_1 \hat{g}_{\mu\nu} + F_2 \frac{\hat{p}_\mu \hat{p}_\nu}{M\nu} + g_1 \frac{i}{\nu} \varepsilon_{\mu\nu\lambda\sigma} q^\lambda s^\sigma + g_2 \frac{i}{\nu^2} \varepsilon_{\mu\nu\lambda\sigma} q^\lambda \left(p\cdot q s^\sigma - s\cdot q p^\sigma\right)$$

$$-b_1 r_{\mu\nu} + \frac{1}{6} b_2 \left(s_{\mu\nu} + t_{\mu\nu} + u_{\mu\nu}\right) + \frac{1}{2} b_3 \left(s_{\mu\nu} - u_{\mu\nu}\right) + \frac{1}{2} b_4 \left(s_{\mu\nu} - t_{\mu\nu}\right)$$

F_1, F_2 ,g_1 and g_2 exist in spin-1/2 hadron, while b_1, b_2, b_3 and b_4 are the new quantities for spin-1 hadron. In total,there are 8 structure functions for deuteron.

$$F_1 = \frac{1}{2} \sum_i e_i^2 (q_i(x,Q^2) + \bar{q}_i(x,Q^2))$$

$$b_1 = \frac{1}{2} \sum_i e_i^2 (\delta_T q_i(x,Q^2) + \delta_T \bar{q}_i(x,Q^2))$$

$$\delta_T q_i(x,Q^2) = q_i^0 - \frac{q_i^1 + q_i^{-1}}{2}$$

The tensor –polarized distributions will disappear if the deuteron is S wave.

P. Hoodbhoy, R. L. Jaffe, and A. Manohar, NP B312 (1989) 571

L. L. Frankfurt and M. I. Strikman, NP A405 (1983) 557.

$$\boxed{\int dx b_1(x) = 0 + \frac{1}{18} \int dx [8\delta_T \bar{u}(x) + 2\delta_T \bar{d}(x) + \delta_T s(x) + \delta_T \bar{s}(x)]}$$

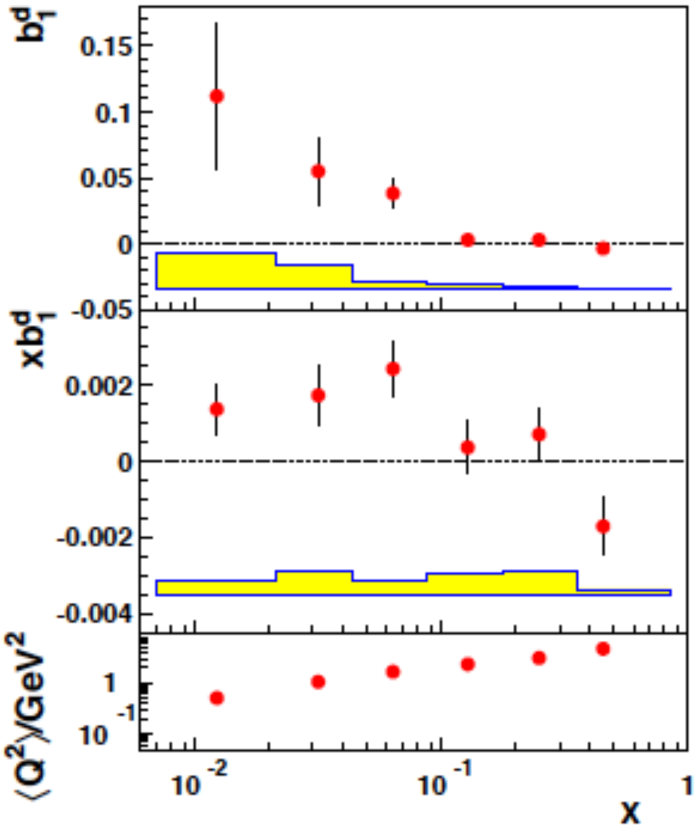
Experiment Status: the measurement of b_1

$$\int dx b_1(x) = 0 + \frac{1}{18}\int dx[8\delta_T\bar{u}(x) + 2\delta_T\bar{d}(x) + \delta_T s(x) + \delta_T\bar{s}(x)]$$

$$\int_{0.002}^{0.85} dx b_1(x) = [1.05 \pm 0.34(stat) \pm 0.35(sys)] \times 10^{-2}$$

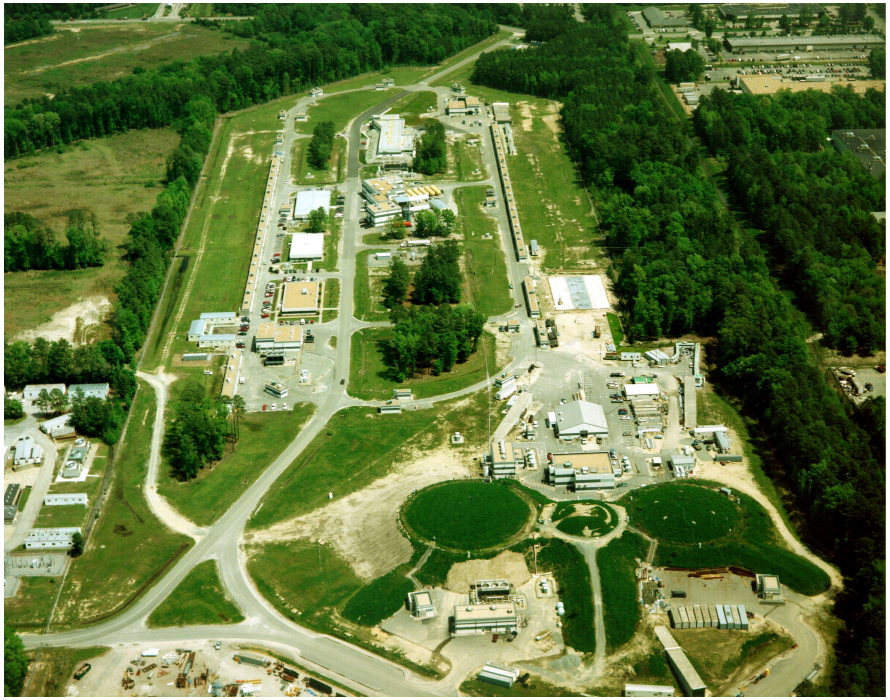
$$\int_{0.02}^{0.85} dx b_1(x) = [0.35 \pm 0.10(stat) \pm 0.18(sys)] \times 10^{-2}$$

The derivation from 0 of the integration will indicate the existence of tensor – polarized distributions for antiquark(sea) quarks.



A. Airapetian *et al.* (HERMES), PRL 95 (2005) 242001.

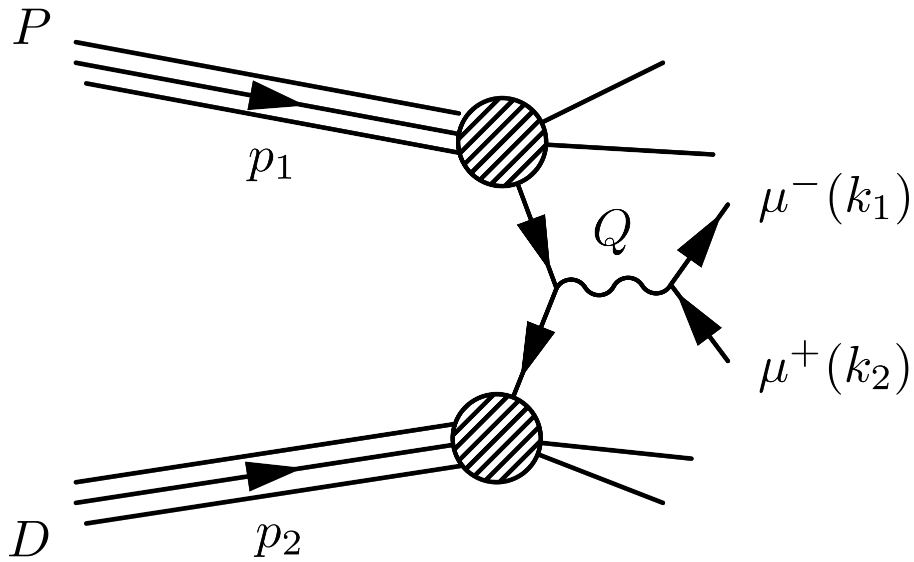
There is an approved experiment E12-13-001 to measure b_1 at JLab (Thomas Jefferson National Accelerator Facility), and this will help us to understand the tensor structure of deuteron.



See Professor Karl Slifer's talk on Wednesday.

Drell-Yan process for proton and deuteron

$$P + D \rightarrow \gamma^* \rightarrow \mu^- \mu^+ + X$$



$$W_{\mu\nu} = \int \frac{d^4\xi}{(2\pi)^4} e^{iQ\xi} \left\langle P_1 S_1 P_2 S_2 \middle| J_\mu(0) J_\nu(\xi) \middle| P_1 S_1 P_2 S_2 \right\rangle$$

The spin asymmetry A_{UQ0} will indicate that existence of tensor –polarized distributions, which are only available in D-wave deuteron. In experiment, the tensor –polarized distributions have been confirmed by Hermes measurements for b_1 of electron-deuteron DIS.

$$A_{UQ_0} = \frac{1}{2\langle\sigma\rangle}[\sigma(\bullet,0) - \frac{\sigma(\bullet,+1)+\sigma(\bullet,-1)}{2}]$$

S. Hino and S. Kumano, PRD 59 (1999) 094026; PRD 60 (1999) 054018

In Parton Model

$$A_{UQ_0} = \frac{\sum_i e_i^2 (q_i(x_1)\delta_T \bar{q}_i(x_2) + \bar{q}_i(x_1)\delta_T q_i(x_2))}{2\sum_i e_i^2 (q_i(x_1)\bar{q}_i(x_2) + \bar{q}_i(x_1) q_i(x_2))}$$

There are 108 structure functions for the hadron tensor of unpolarized proton-polarized deuteron Drell-Yan Process, and the spin asymmetry A_{UQ0} is measured with the tensor polarized deuteron.

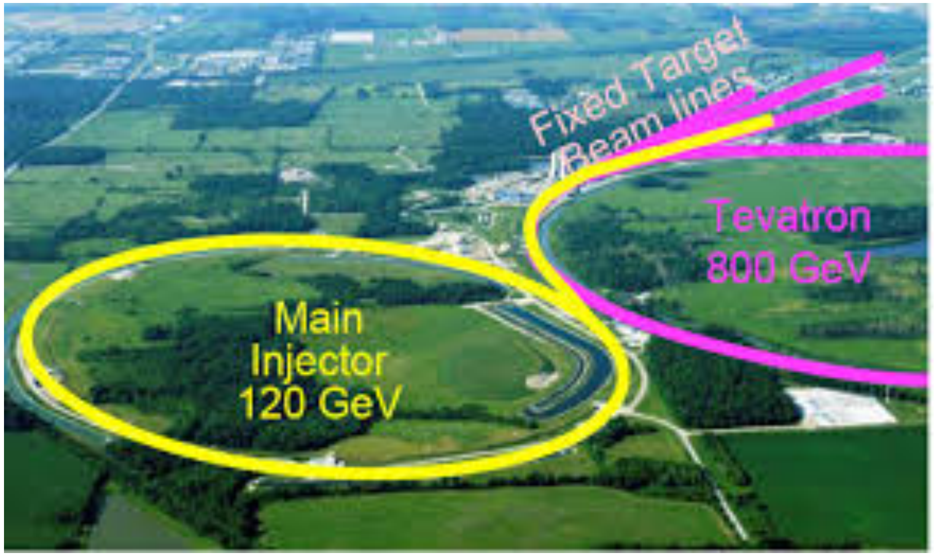
At Large $x_F = x_1 - x_1$:

$$q_i(x_1)\delta_T \bar{q}_i(x_2) \gg \bar{q}_i(x_1)\delta_T q_i(x_2)$$

$$\boxed{A_{UQ_0} = \frac{\sum_i e_{i\,i}^2 (q_i(x_1)\delta_T \bar{q}_i(x_2))}{2\sum_i e_{i\,i}^2 (q_i(x_1)\bar{q}_i(x_2))}}$$

The asymmetry A_{UQ0} at large x_F reflects antiquark tensor-polarized distribution, and it is easier to get the antiquark tensor-polarized distribution from the measurement of the asymmetry A_{UQ0}.

The asymmetry could be measured by Fermilab E-1309 experiment through proton-deuteron Drell-Yan Process. The beam is unpolaried proton(120 GeV, Fermilab Main-Injector) and the target is (tensor) polarized deuteron.



Fermilab Drell-Yan process

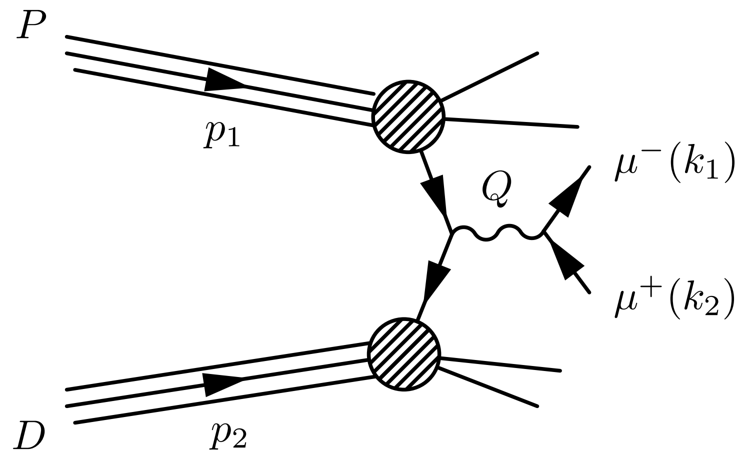
Results: Estimate on tensor-polarized asymmetry for the proton-deuteron Drell-Yan Process

$$P + D \rightarrow \mu^- \mu^+ + X$$

$$E_p = 120\ GeV$$

$$s = (p_1 + p_2)^2 = M_p^2 + M_d^2 + 2M_d E_p$$

$$Q^2 = x_1 x_2 s$$



$$A_{UQ_0} = \frac{\sum_i e_i^2 (q_i(x_1)\delta_T \bar{q}_i(x_2) + \bar{q}_i(x_1)\delta_T q_i(x_2))}{2\sum_i e_i^2 (q_i(x_1)\bar{q}_i(x_2) + \bar{q}_i(x_1) q_i(x_2))}$$

The unpolarized distributions of proton and deuteron q(x, Q^2) can be obtained by MSTW. We use the functional form of parameterizations for the initial tensor-polarized distributions of deuteron (Q^2=2.5GeV^2) based on Hermes data.

A.D. Martin *et al* EPJC 63 (2009) 189
S. Kumano, PRD 82 (2010) 017501

Parameterizations for initial tensor-polarized distributions of deuteron

$$\delta_T q^D(x,\, Q_0^2) = \delta_T w(x) \times q^D(x,\, Q_0^2) = \delta_T w(x) \times \frac{u_v(x,\, Q_0^2) + d_v(x,\, Q_0^2)}{2}$$

$$\delta_T \bar{q}^D(x,\, Q_0^2) = \bar{\alpha} \times \delta_T w(x) \times \bar{q}^D(x,\, Q_0^2) = \bar{\alpha} \times \delta_T w(x) \times \frac{2\bar{u}(x,\, Q_0^2) + 2\bar{d}(x,\, Q_0^2) + s(x,\, Q_0^2) + \bar{s}(x,\, Q_0^2)}{6}$$

$$\delta_T w(x) = a x^b (1-x)^c (x_0 - x)$$

$$Q_0^2 = 2.5 \text{ GeV}^2$$

The existence of the node x_0 satisfies the sum rule $\int dx (b_1)_{Valence} = 0$

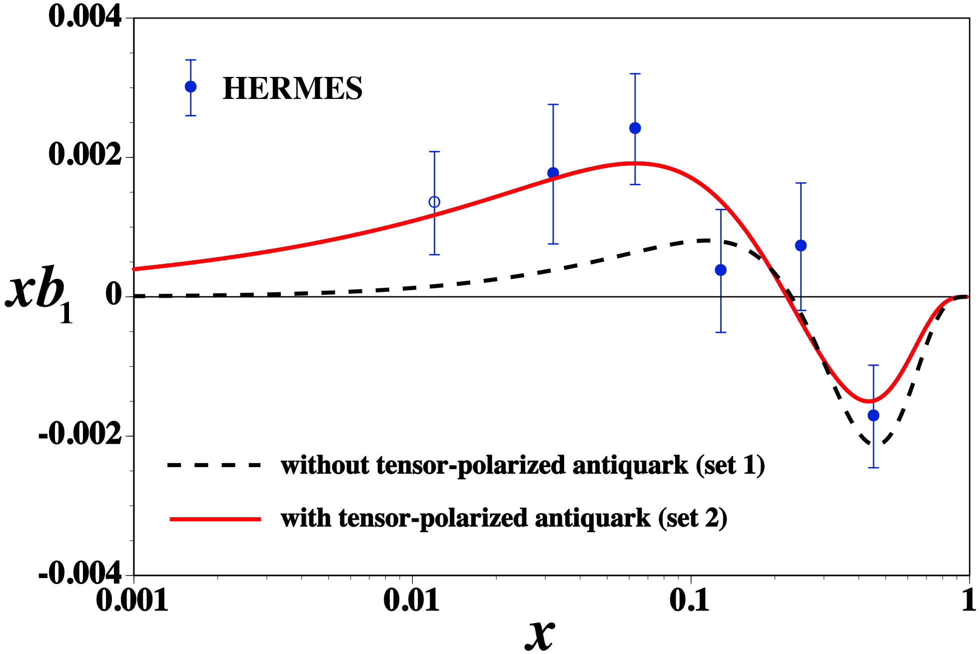
$u_v(x)$ and $d_v(x)$ are the valence quark distributions for the proton,

$\bar{u}(x)$, $\bar{d}(x)$ *and* $\bar{s}(x)$ are antiquark distributions for the proton.

Set 1: $\delta_T \bar{q}^D(x) = 0$ no tensor-polarized antiquark distributions ($\alpha_{\bar{q}} = 0$),

Set 2: $\delta_T \bar{q}^D(x) \neq 0$ finite tensor-polarized antiquark distributions ($\alpha_{\bar{q}} \neq 0$).

S. Kumano, PRD 82 (2010) 017501



Set-1 results of xb_1 can not explain the Hermes data at small x (x<0.1).

Set-2 results can fit the data well enough.

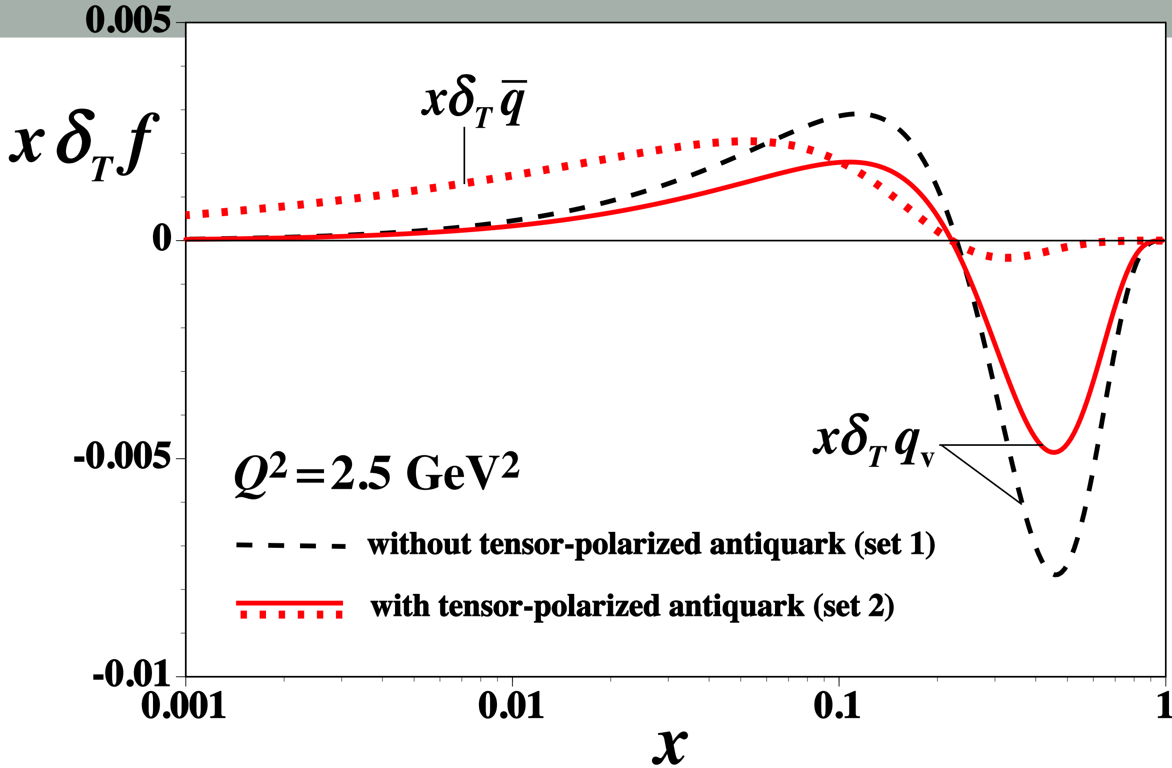
It is better to consider the antiquark tensor-polarized distributions at Q^2=2.5 GeV^2.

$$\int_{0.002}^{0.85} b_1(x)dx = [1.05 \pm 0.34(stat) \pm 0.35(sys)] \times 10^{-2}$$

$$\int_{0.02}^{0.85} b_1(x)dx = [0.35 \pm 0.10(stat) \pm 0.18(sys)] \times 10^{-2}$$

$$\int dx b_1(x) = 0 + \frac{1}{18} \int dx [8\delta_T \bar{u}(x) + 2\delta_T \bar{d}(x) + \delta_T s(x) + \delta_T \bar{s}(x)]$$

Finite antiquark tensor-polarized distributions are necessary!



Tensor-Polarized distributions at Q^2=2.5 GeV^2, the set-2 antiquark tensor-polarized distribution is dominant at small x region (x<0.02). There is a node at x_0=0.229 for set 1 and x_0=0.221 for set 2, and this node is also predicted by standard S-D mixture proposal for deuteron.

P. Hoodbhoy, R. L. Jaffe, and A. Manohar, NPB 312 (1989) 571

H. Khan and P. Hoodbhoy, PRC 44 (1991) 1219

W. Cosyn Yu-Bing Dong, S. Kumano and M. Sargsian, PRD 95 (2016) 074036

The tensor-polarized distributions at other energy scale

The tensor-polarized distributions can be obtained by evolving initial tensor-polarized distributions to any energy scale Q^2. The gluon tensor-polarized distribution is set to be 0 at Q^2=2.5 GeV^2.

$$\delta_T q^D(x_2,\ Q_0^2) \to \delta_T q^D(x_2,\ Q^2)$$

$$\delta_T g^D(x_2,\ Q_0^2) \to \delta_T g^D(x_2,\ Q^2)$$

Q^2 is determined by x_1 and x_2

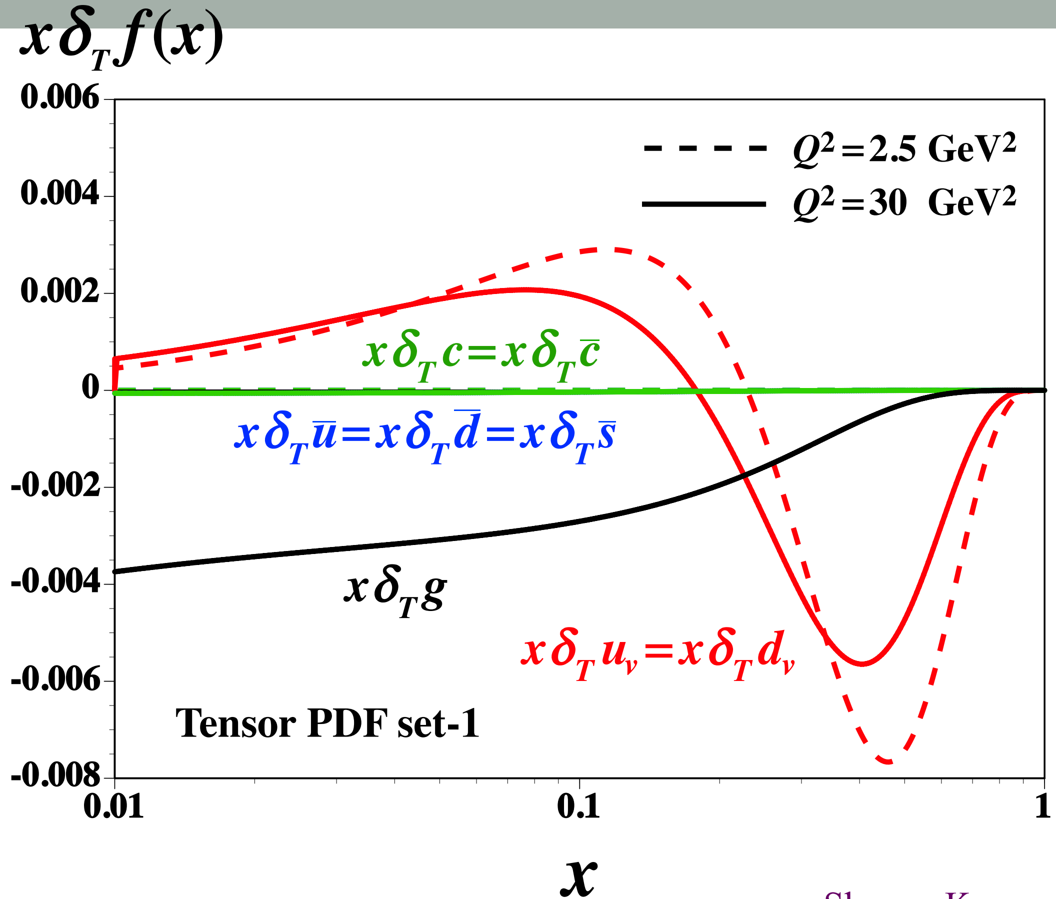
$E_p = 120\ GeV$ **Fermilab Main Injector Proton Beam**

$$s = (p_1 + p_2)^2 = M_p^2 + M_d^2 + 2M_d E_p = 454.545\ GeV^2$$

$$Q^2 = M_{\mu\mu}^2 = x_1 x_2 (2 p_1 p_2) = x_1 x_2 s$$

DGLAP evolution

P. Hoodbhoy et al,NPB 312 (1989) 571

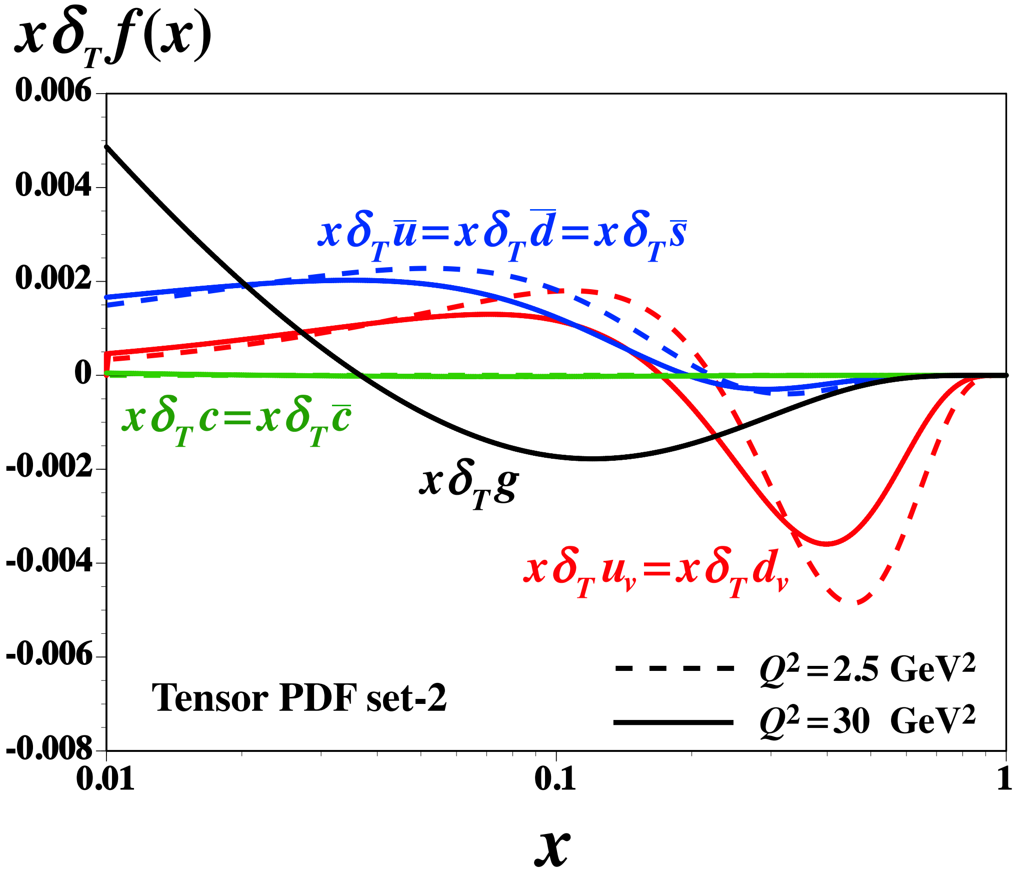


symmetry for antiquarks

$$\delta_T \bar{u} = \delta_T \bar{d} = \delta_T \bar{s} = \delta_T \bar{c}$$

Shunzo Kumano and Qin-Tao Song, PRD **94**, 054022 (2016)

The set-1 tensor-polarized distributions at Q^2=2.5 GeV^2 and Q^2=30 GeV^2 . There also exists the tensor-polarized distribution for gluon, even though it is set to be zero at the initial energy scale Q^2=2.5 GeV^2 .Because there are no antiquark tensor-polarized distributions at Q^2=2.5 GeV^2 ,so the symmetry for antiquarks will hold for any energy scale (leading order).

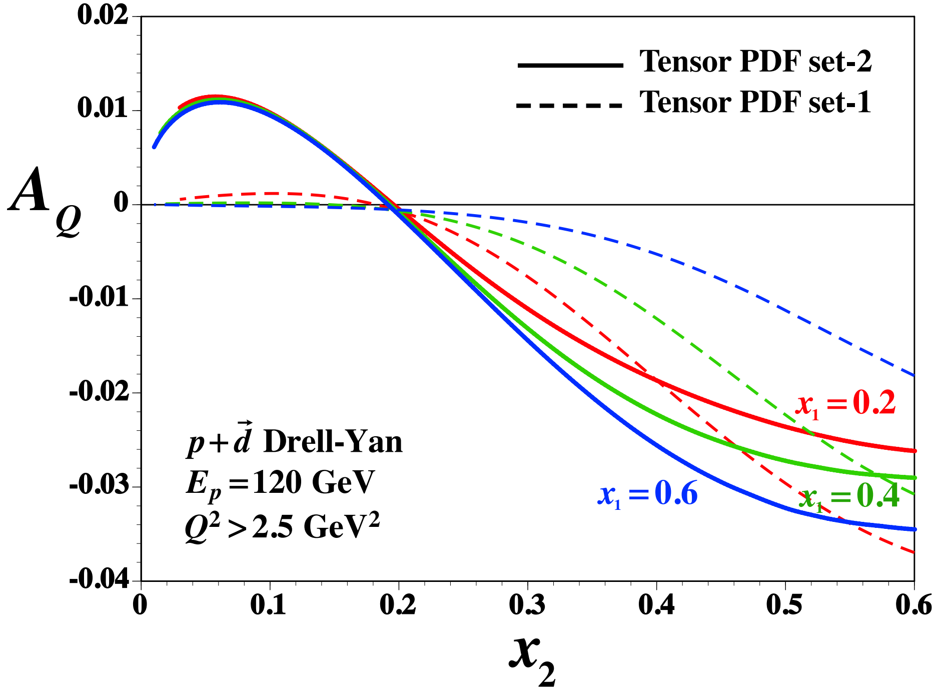


symmetry for antiquarks

$$\delta_T\bar{u} = \delta_T\bar{d} = \delta_T\bar{s} \neq \delta_T\bar{c}$$

The set-2 tensor-polarized distributions at Q^2=2.5 GeV^2 and Q^2=30 GeV^2.

Because there are antiquark tensor-polarized distributions ($\delta_T\bar{u} = \delta_T\bar{d} = \delta_T\bar{s} \neq 0$) at Q^2=2.5 GeV^2, so the antiquark tensor-polarized distributions are SU(3) flavor symmetric for any energy scale (leading order).

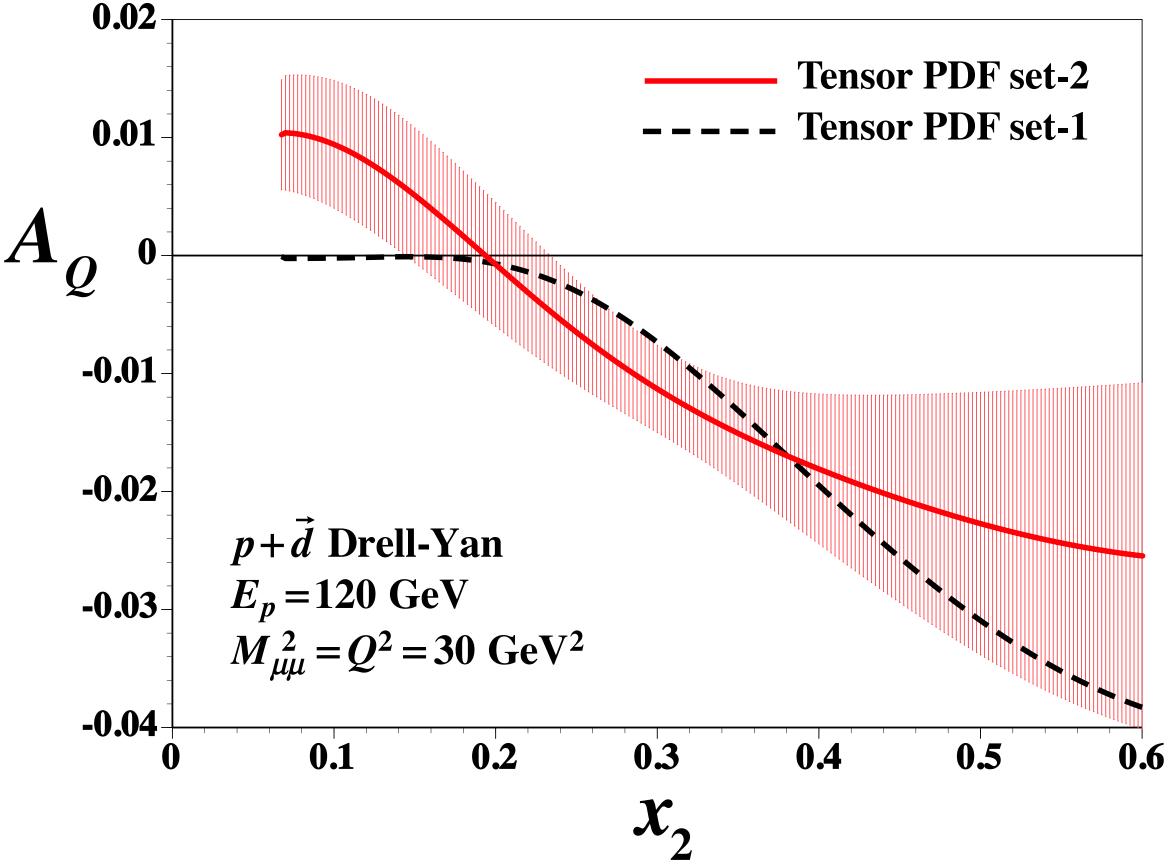


In the figure, tensor-polarized asymmetry A_Q is shown at typical values of x_1=0.2, 0.4 and 0.6.

$$A_Q(x_1, x_2) = 2A_{UQ_0}(x_1, x_2)$$

$$A_{UQ_0} = \frac{\sum_i e_i^2 (q_i(x_1)\delta_T \bar{q}_i(x_2) + \bar{q}_i(x_1)\delta_T q_i(x_2))}{2\sum_i e_i^2 (q_i(x_1)\bar{q}_i(x_2) + \bar{q}_i(x_1) q_i(x_2))}$$

- The values of set-1 and set-2 are both a few percent.
- The set-1 results are so different from those of set-2 at small region of x_2, and this is because that antiquark tensor-polarized distributions are more important when x_2 is small.
- The set-2 results should be more reliable, since the tensor-polarized distributions can also explain the Hermes data well.



Spin asymmetry A_Q at typical energy scale (Q^2=30 GeV^2) with the uncertainties estimate.

Shunzo Kumano and Qin-Tao Song, PRD **94**, 054022 (2016)

Summary

The new structure function b_1 (DIS) and spin asymmetry A_Q (Drell-Yan) of deuteron reflect the tensor-polarized distributions, which have a close relationship with the orbital angular momentum in spin-1 hadrons. In this talk, we give the theoretical estimate of the spin asymmetry A_Q, and it is of the order of a few percent. In the future, those quantities could be measured by Jlab (b_1) and Fermilab (A_Q), which may reveal the puzzle of deuteron.

THANK YOU VERY MUCH