

# SIDIS: most recent results and open issues

XIV International Workshop on Hadron Structure and Spectroscopy

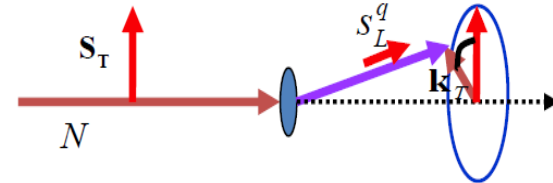
Cortona (Italy), 2 - 5 April 2017

Giulio Sbrizzai – Trieste INFN

Focusing on a selection  
of results mainly on  
transverse momentum dependent effects  
and transverse spin  
in SIDIS  
(and some related open issues)

# The structure of the nucleon

there are **8 TMD PDF** at leading twist appear in the nucleon description taking into account the intrinsic transverse momentum of the quark  $k_{\perp}$



$k_{\perp}$  – intrinsic transverse momentum of the quark

		nucleon polarisation		
		U	L	T
quark polarisation	U	$f_1$ number density $q$		$f_{1T}^{\perp}$ -  Sivers $\Delta_0^T q$
	L		$g_1$ -  helicity $\Delta q$	$g_{1T}$ - $\Delta_T q$
	T	$h_1^{\perp}$ -  Boer Mulders	$h_{1L}^{\perp}$ -	$h_1$ -  transversity $\Delta_T q$ $h_{1T}^{\perp}$ -

# SIDIS: a key process to investigate the structure of the nucleon

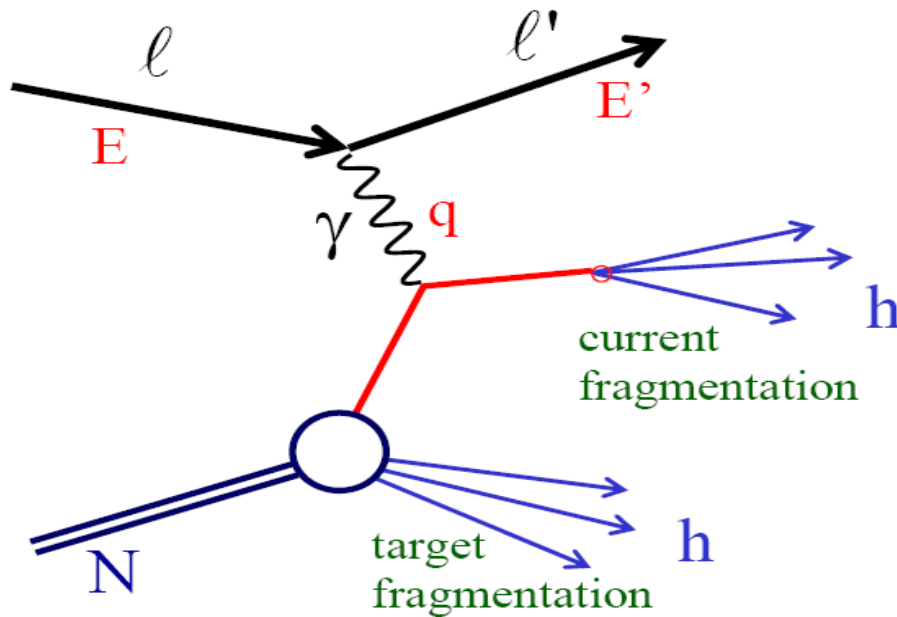
lepton interacts with a **single constituent** of the nucleon ( $Q^2 > 1 \text{ GeV}^2/c^2$ )

$$q = \ell - \ell' \quad x = \frac{Q^2}{2P \cdot q} \quad \text{Bjorken scaling variable}$$

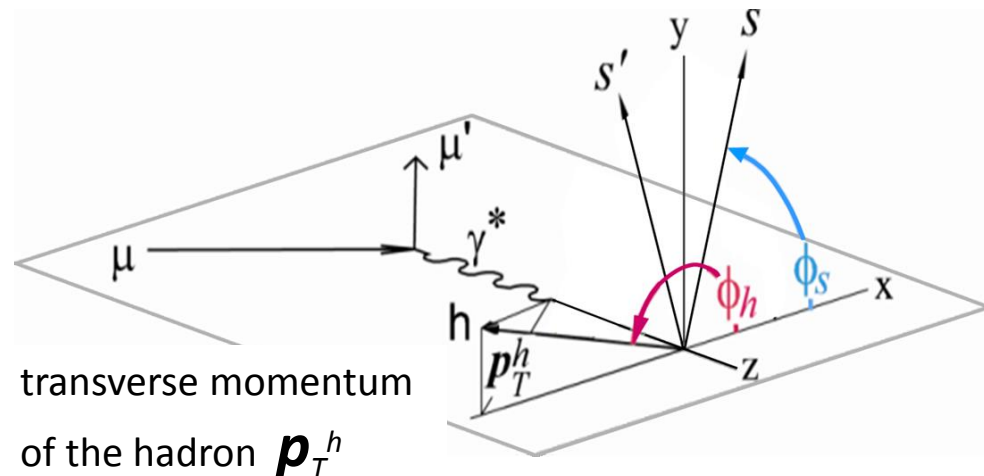
$$Q^2 = -q^2 \quad W^2 = (P + q)^2$$

$$y = \frac{P \cdot q}{P \cdot \ell} =_{LAB} \frac{E - E'}{E}$$

$$z = \frac{P \cdot P_h}{P \cdot q} =_{LAB} \frac{E_h}{E - E'}$$



at least one hadron is detected in the final state  
(information on the **struck quark**)



# polarised SIDIS azimuthal cross section

“one photon exchange approximation”

Bacchetta et al. JHEP 0702:093,2007

$$\begin{aligned}
 \frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = & \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right. \\
 & + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \\
 & + S_{\parallel} \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] + S_{\parallel} \lambda_e \left[ \sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_h F_{LL}^{\cos\phi_h} \right] \\
 & + |S_{\perp}| \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\
 & + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \\
 & + \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \left. \right] \\
 & + |S_{\perp}| \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \\
 & \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \left. \right\},
 \end{aligned}$$

target polarisation

beam polarisation

**14 independent modulations**  
in  $\varphi_h$  and  $\varphi_S$

# polarised SIDIS azimuthal cross section

“one photon exchange approximation”

Bacchetta et al. JHEP 0702:093,2007

$$\begin{aligned}
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 & + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \\
 & + S_{\parallel} \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] + S_{\parallel} \lambda_e \left[ \sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_h F_{LL}^{\cos\phi_h} \right] \\
 & + |S_{\perp}| \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\
 & + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \\
 & + \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \\
 & + |S_{\perp}| \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \\
 & \left. \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \right\},
 \end{aligned}$$

unpolarised part

transverse spin dependent part

target polarisation

beam polarisation

$$F = \sum_q PDF_q(x) \otimes FF_q^h(z)$$

## Why SIDIS?

all these amplitudes can be **extracted simultaneously** from the same data  
all the different **TMD PDFs appear** in the cross section  
and the **different effects** can be **disentangled**

# Outline

- **Unpolarised SIDIS**
  - $P_T^h$  dependent multiplicities
  - azimuthal asymmetries
- **Transversely polarised SIDIS**
  - **Sivers asymmetries**
    - **$P_{Th}$  weighted Sivers asymmetries**
  - **Collins asymmetries**
    - **two hadrons asymmetries**
  - **other 6 asymmetries**

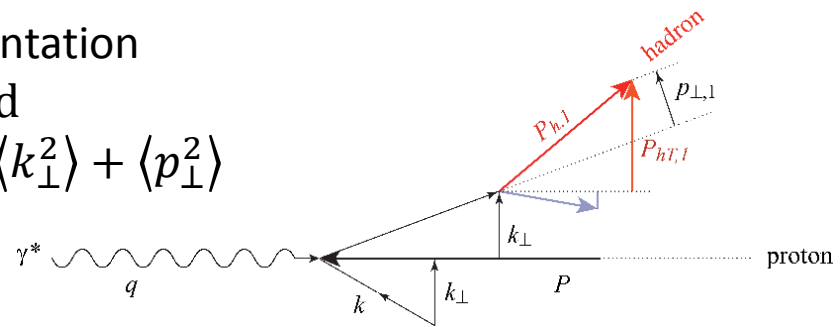


# Unpolarised SIDIS

## hadron multiplicities as function of $(\mathbf{P}_T^h)^2$

- The cross-section dependence from  $P_{hT}$  results from:
  - intrinsic  $k_\perp$  of the quarks
  - $p_\perp$  generated in the quark fragmentation
  - Usual assumptions: Gaussian and

$$\langle P_{hT}^2 \rangle = z^2 \langle k_\perp^2 \rangle + \langle p_\perp^2 \rangle$$



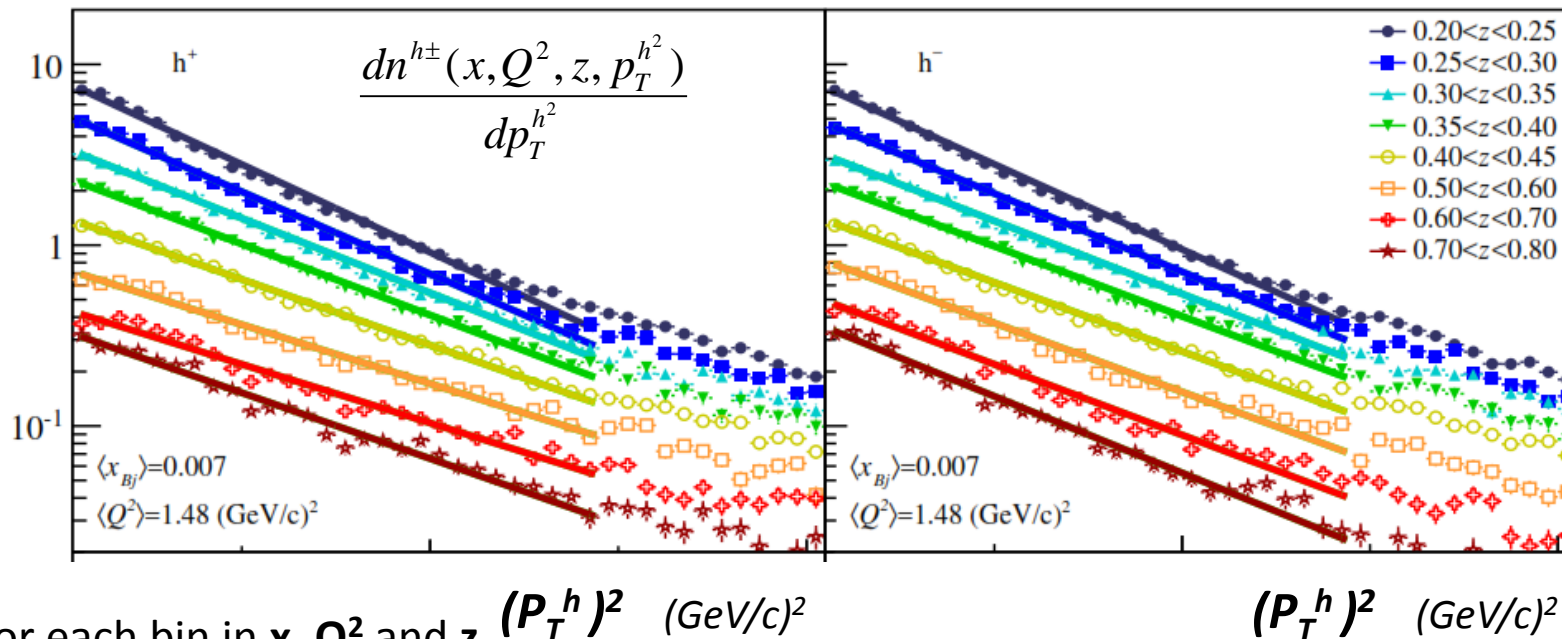
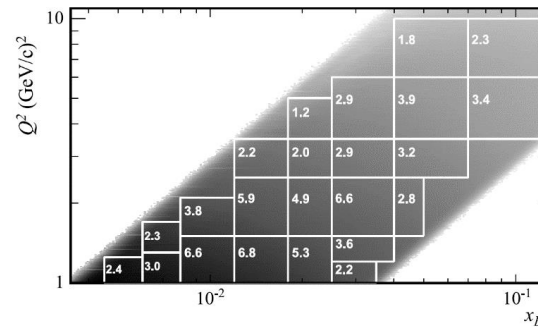
## COMPASS and HERMES have

results on deuteron and on protons (Hermes only)

No COMPASS measurements on  $p$  since on  $NH_3$  nuclear effects may be important

# COMPASS results on deuteron (2004 data)

## hadron multiplicities as function of $(P_T^h)^2$



for each bin in  $x$ ,  $Q^2$  and  $z$   
fit using

→ extract  $A \cdot e^{-P_T^{h^2} / \langle P_T^{h^2} \rangle}$

for  $P_T^h < 0.85 \text{ GeV/c}$   
to stay away from the region  
where transverse momentum  
effects related to gluon radiation  
become relevant

EPJ73 (2013) 2531

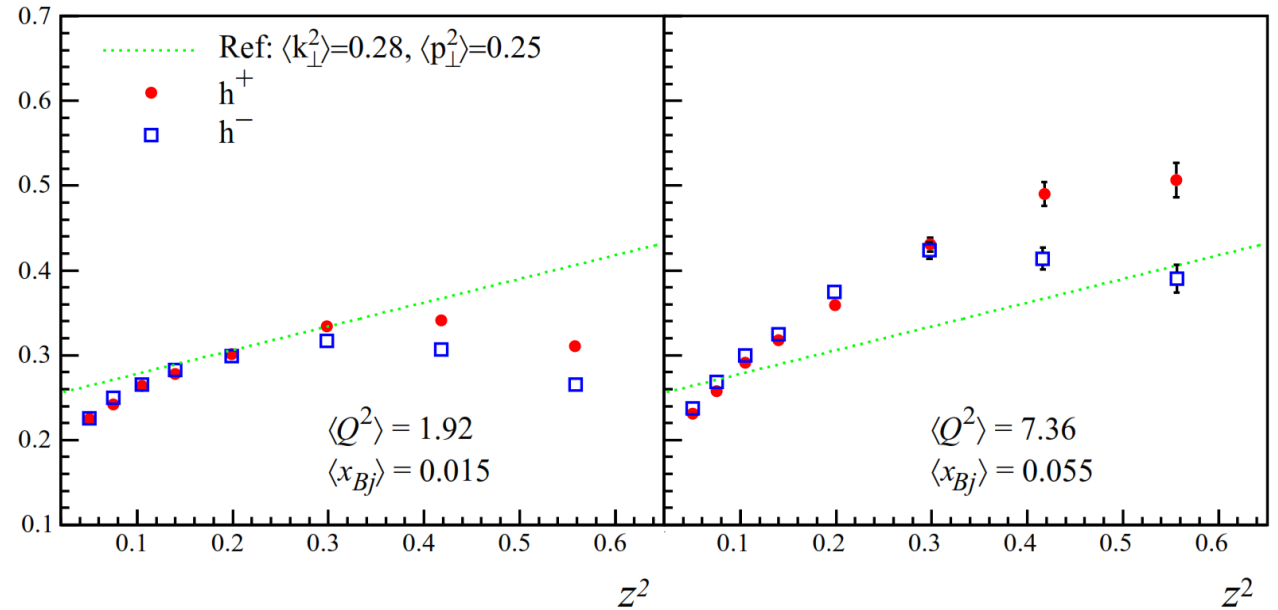


COMPASS results on deuteron  
(2004 data)

$z^2$  dependence

$$\langle P_T^{h^2}(z^2) \rangle$$

EPJ73 (2013) 2531



$$\langle P_T^{h^2}(z) \rangle = \langle P_{\perp}^2(z) \rangle + z^2 \langle k_{\perp}^2 \rangle$$

linear dependence on  $z^2$  does not reproduce data  
effect from fragmentation  $P_{\perp}(z)$  (not so easy to calculate...)

Results given with a 10% uncertainty on the normalization EPJ75 (2015) 94

new results with much better precision from 2006 deuteron data in publication

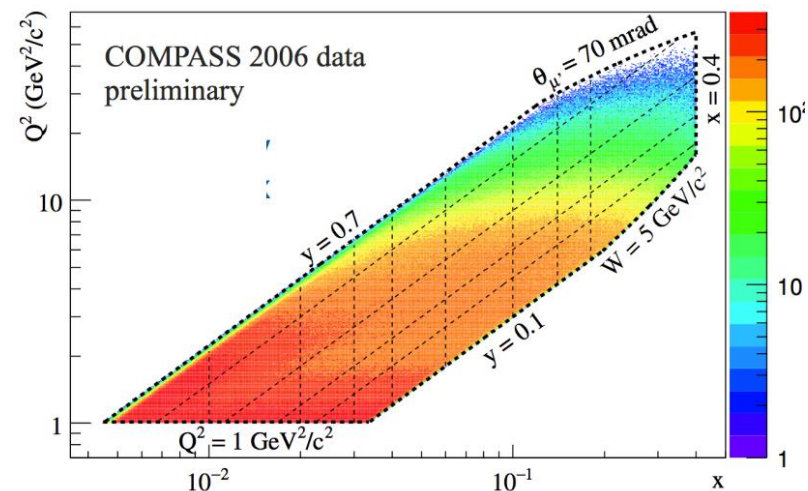
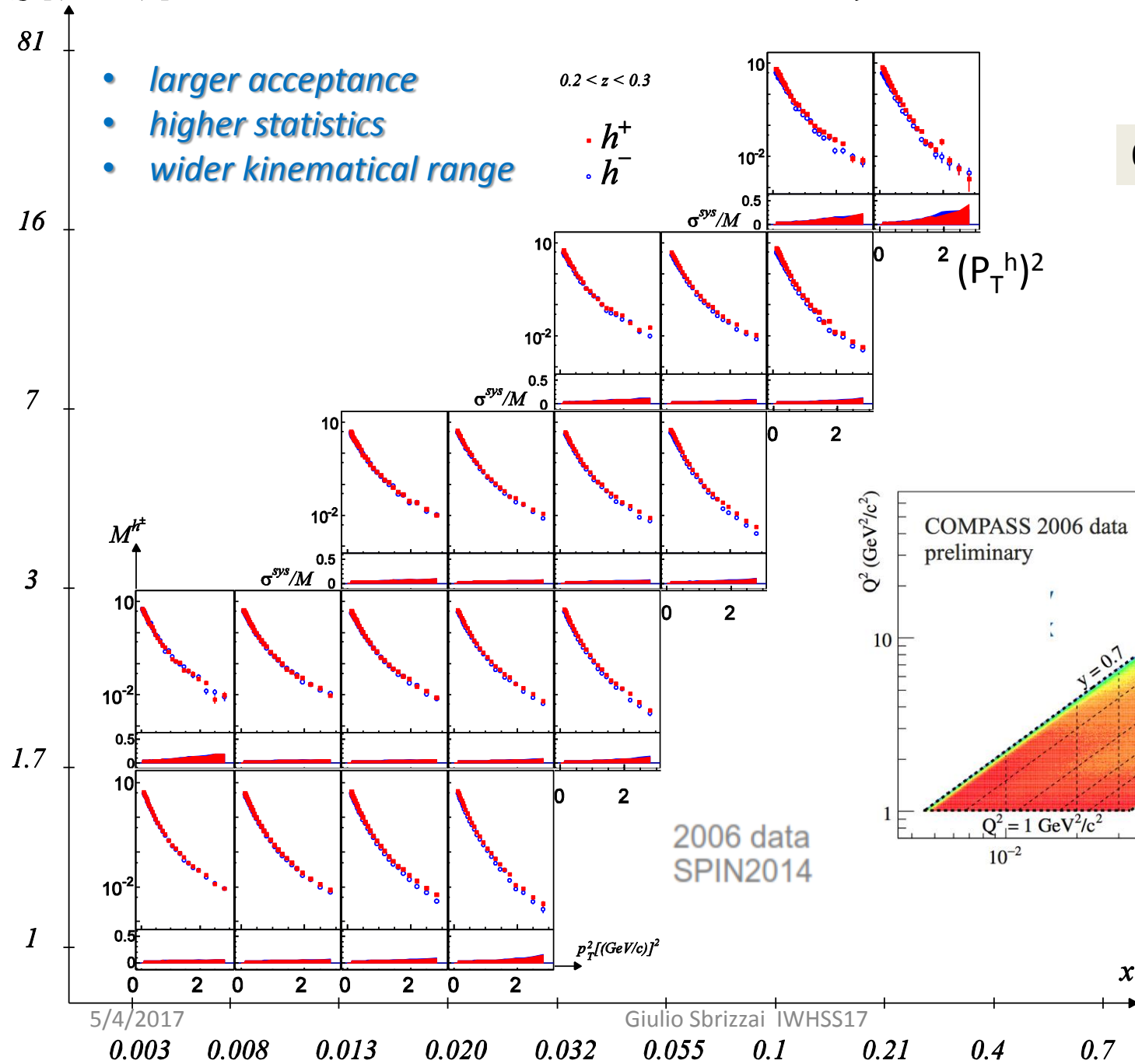
$Q^2 [(\text{GeV}/c)^2]$ 

COMPASS Preliminary

- larger acceptance
- higher statistics
- wider kinematical range

 $0.2 < z < 0.3$ 

•  $h^+$   
•  $h^-$

 $0.2 < z < 0.3$ 

$Q^2 [(GeV/c)^2]$

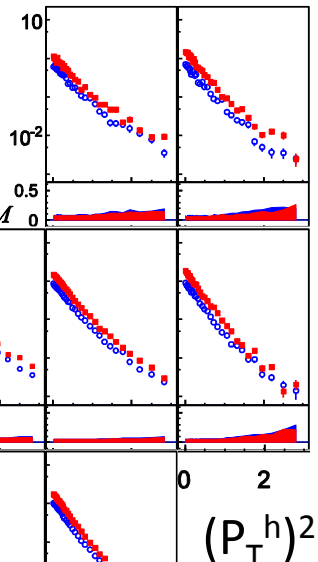
81  
16  
7  
3  
1.7  
1

$0.4 < z < 0.6$

$h^+ / h^-$  difference  
more pronounced  
at large  $x$  and large  $z$

$0.4 < z < 0.6$

$h^+$   
 $h^-$



correction for  
vector meson production  
and radiative corrections  
evaluated

**Total: 4918 points**

*publication on the way*

2006 data  
SPIN2014

$p_T^2 [(GeV/c)^2]$

$x$

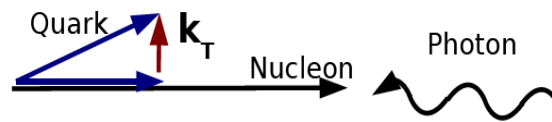
0.003 0.008 0.013 0.020 0.032 0.055 0.1 0.21 0.4 0.7

# Unpolarised SIDIS

- The azimuthal modulations in the unpolarized cross-sections mainly comes from:

mainly **Cahn** effect: **kinematical effect** proportional to the **quark transverse momentum**

$$A_{\cos\phi_h}^{UU} = \frac{F_{\cos\phi_h}^{UU}}{F^{UU}}$$



$$d\sigma^{lq \rightarrow lq} \propto \hat{s}^2 + \hat{u}^2 \propto \left( 1 + \varepsilon_1 \frac{k_{\perp}}{Q} \cos \varphi \right)$$

*pQCD negligible for  $P_T^h < 1 \text{ GeV}/c$*

$$A_{\cos 2\phi_h}^{UU} = \frac{F_{\cos 2\phi_h}^{UU}}{F^{UU}}$$

**Boer-Mulders** (*T-odd* !) function, one of the most famous **TMD PDF**, convoluted with the **Collins FF**



also Cahn effect contribution  $\propto \left( \frac{k_{\perp}}{Q} \right)^2$

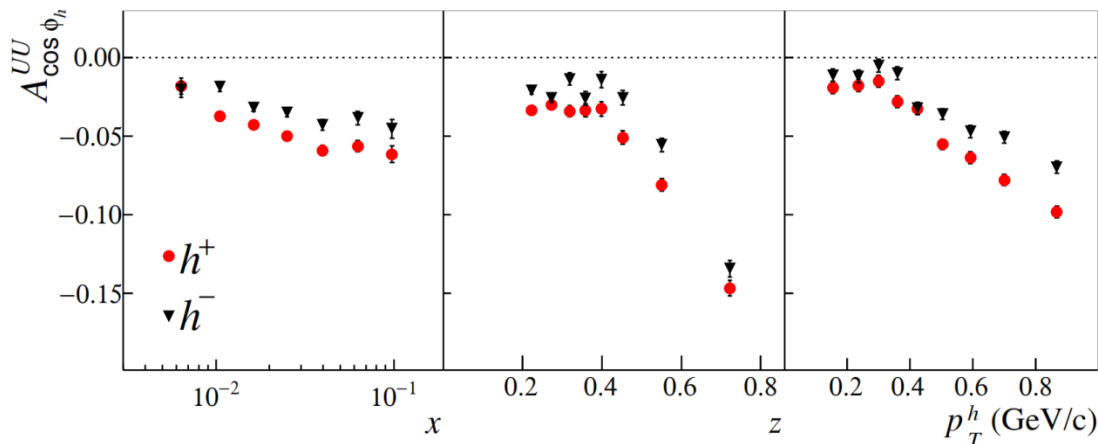
*pQCD negligible for  $P_T^h < 1 \text{ GeV}/c$*

the **Boer-Mulders function** correlates the **quark transverse momentum** and the **quark spin** in an **unpolarized nucleon**

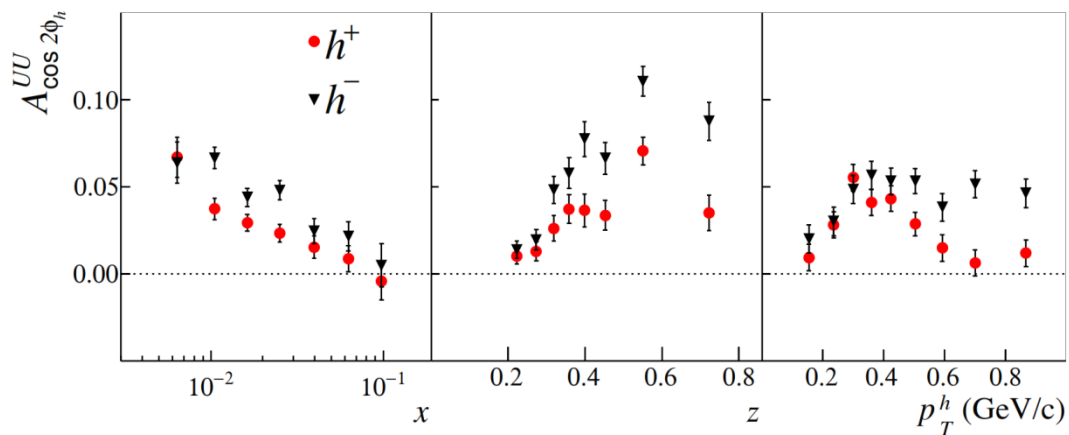
*other higher twist effects can contribute...*

strong kinematic dependencies not understood....

NPB 886 (2014) 1046



$$= \frac{1}{Q} \text{Cahn} + \frac{1}{Q} \text{BM}$$



$$= \text{BM} + \frac{1}{Q^2} \text{Cahn}$$

also CLAS (PRD 80) for  $\pi^+$   
and HERMES (PRD 87)

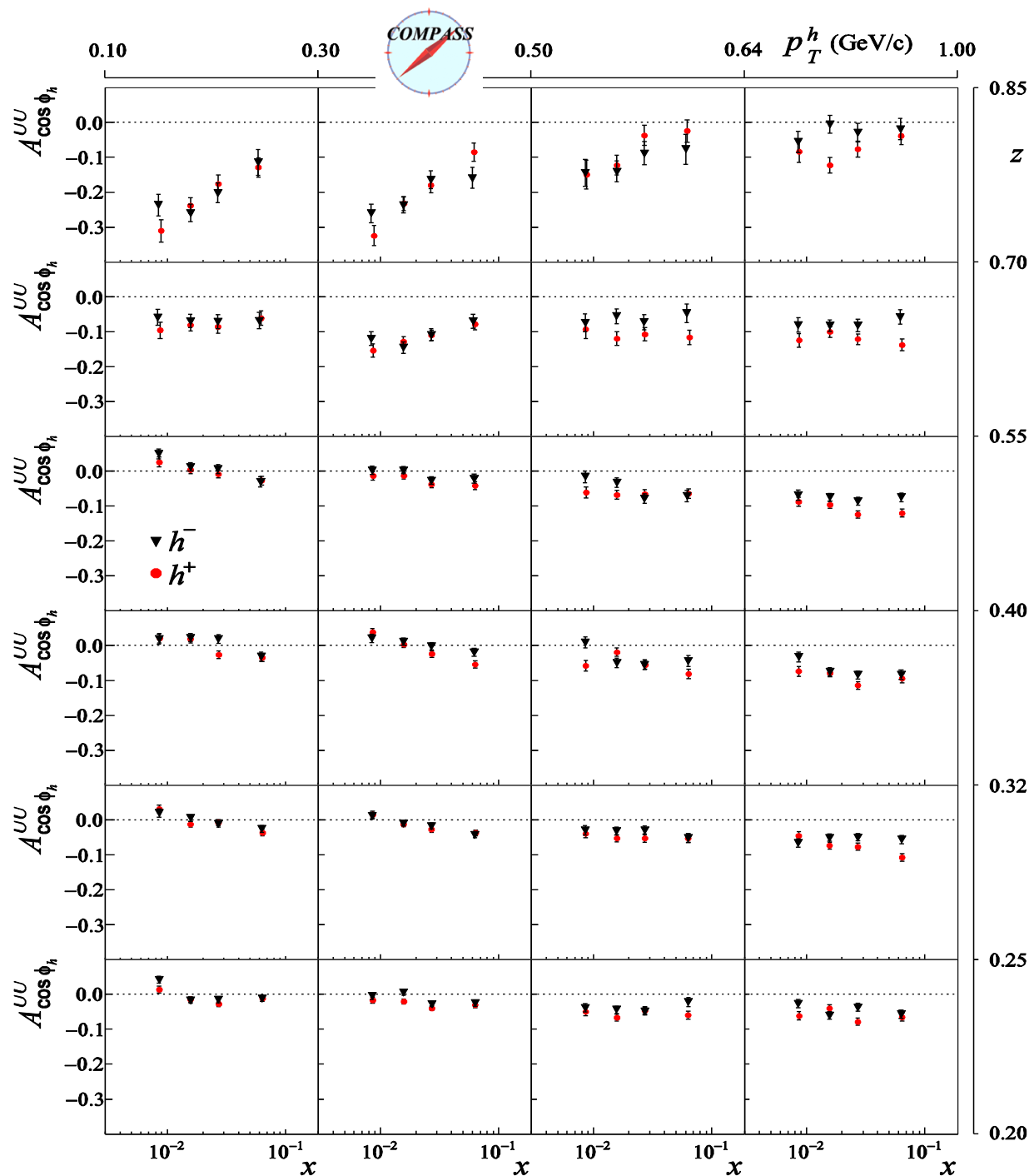
dependencies on  $z$  and on  $P_T^h$  investigated using multiD analysis !

# Unpolarised Azimuthal Asymmetries measured from 2004 deuteron data

$$A_{\cos\phi_h}^{UU} \approx \frac{1}{Q} Cahn + \frac{1}{Q} BM$$

convoluted with  
the Collins FF

multiD  
performed  
both on  
 $\cos\phi$   $\longrightarrow$   
and  $\cos 2\phi$





Using the info from the  $P_T^h$  dependent multiplicities of COMPASS and HERMES data study the azimuthal asymmetries

disentangle  $k_\perp$  and  $p_\perp$  contribution to  $P_T^h$

$P_T^h$  dependencies in different bins of  $z$  and  $x$

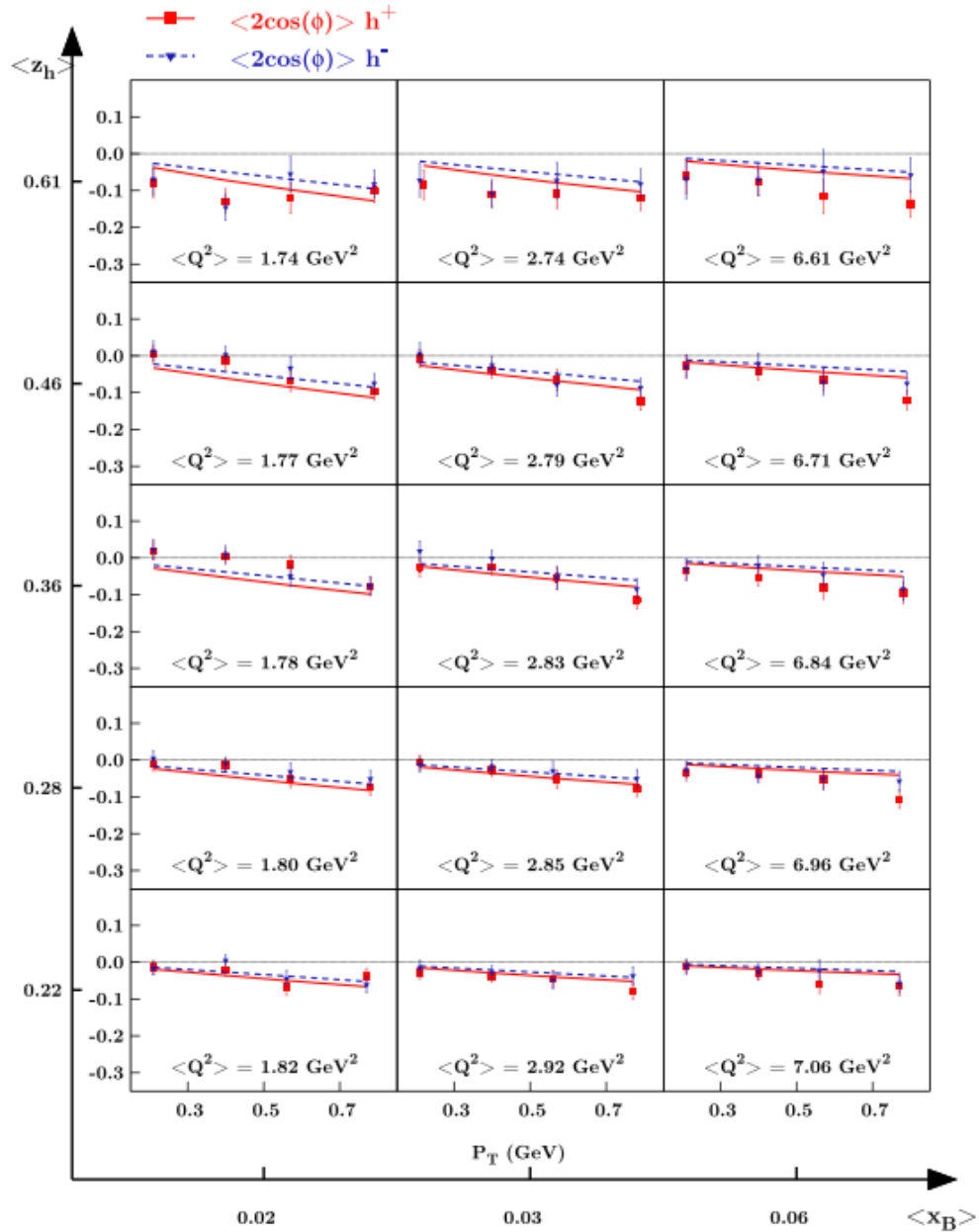
$\cos\phi$  asymmetries

$$A_{\cos\phi_h}^{UU} \approx \frac{1}{Q} \text{Cahn} + \frac{1}{Q} \text{BM}$$

small contribution from  $k_\perp$

neglecting possible dynamic twist-3 contributions

PRD91 (2015) Barone et al



Using the info from the  $P_T^h$  dependent multiplicities of COMPASS and HERMES data study the azimuthal asymmetries

disentangle  $k_\perp$  and  $p_\perp$  contribution to  $P_T^h$

$P_T^h$  dependencies in different bins of  $z$  and  $x$

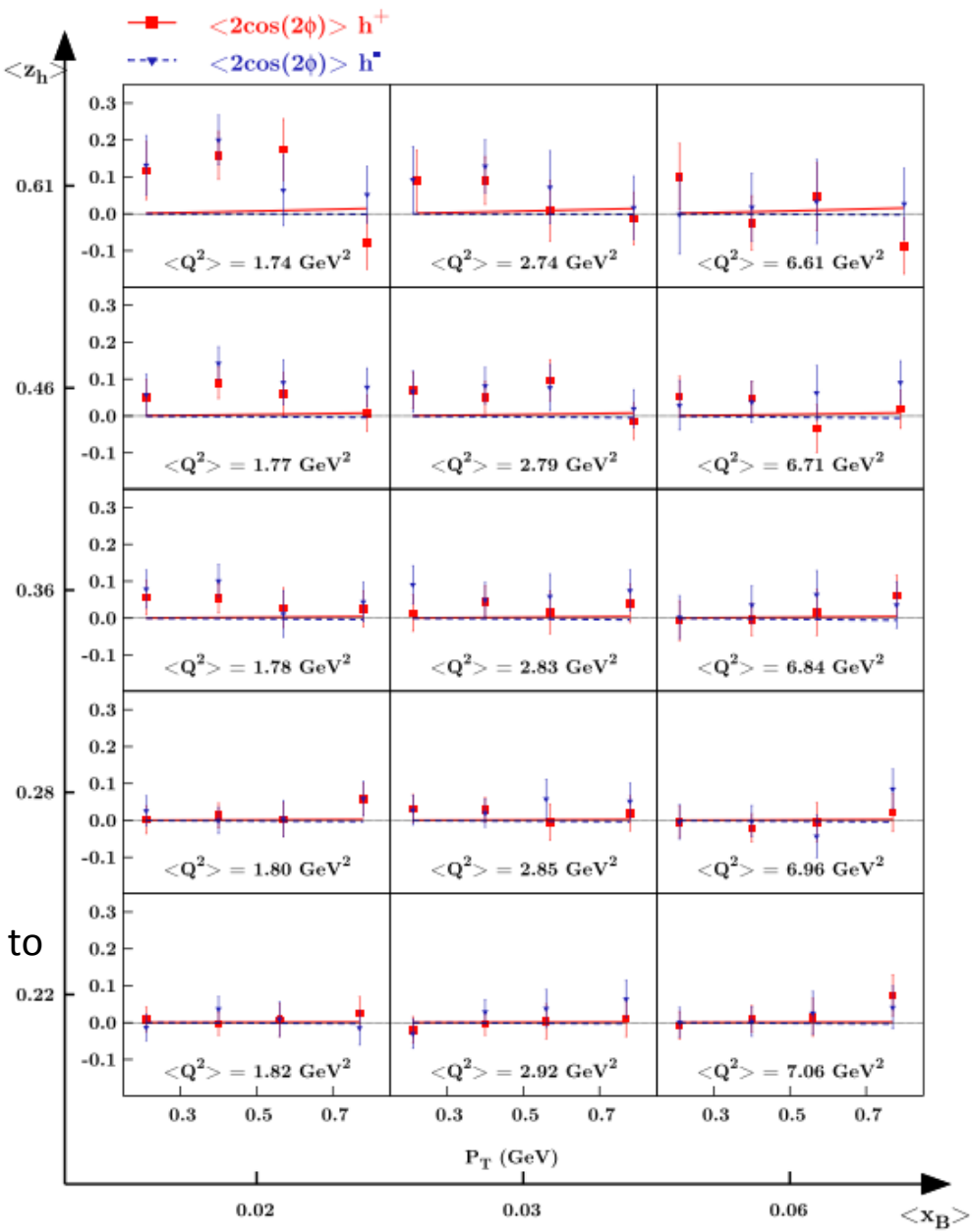
$\cos 2\phi$  asymmetries

$$A_{\cos 2\phi_i}^{UU} \approx \frac{1}{Q^2} \text{Cahn} + \text{BM}$$

fit results give very small asymmetries

discrepancies with data at low  $Q^2$  and large  $z$

It is crucial to have data with different  $Q^2$  in order to disentangle leading twist from higher twist (for example BM in  $\cos 2\phi$ )



more to come from COMPASS:

- unpolarised LH2 (proton) in parallel to the DVCS measurement (2016-2017)
- work started and the analysis is ongoing on the 2016 data

# *Polarised SIDIS*

# The Sivers asymmetry

$$A_{Siv} \approx \frac{\sum_q e_q^2 \cdot f_{1T}^{\perp q}(k_{\perp}^2, x) \otimes D_{1q}^h(p_T^2, z)}{\sum_q e_q^2 \cdot f_1^q(k_{\perp}^2, x) \otimes D_{1q}^h(p_T^2, z)}$$

convolution on the intrinsic  
transverse momentum of the quark



**sivers PDF**

(time odd - final state interactions)

“purely” TMD effect



correlation between the  
nucleon transverse polarisation  
and the **quark transverse momentum**  $k_{\perp}$

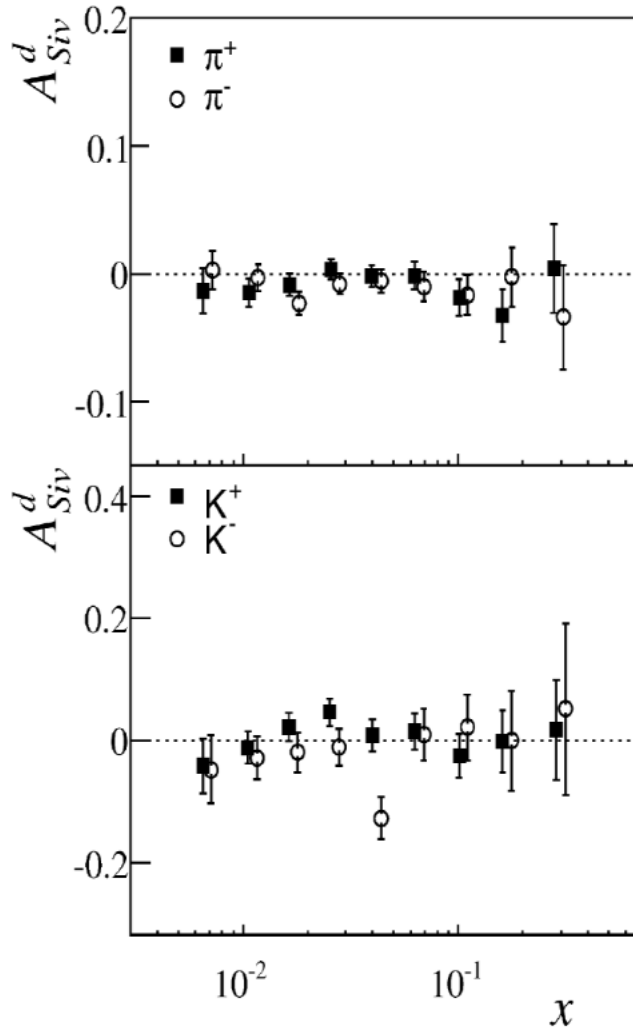


*fundamental prediction pQCD*

*sign change between Sivers TMD measured in SIDIS and in Drell-Yan  
(future measurements from COMPASS)*

# The Sivers asymmetry

- results on polarised deuteron



final results on  
**deuteron**



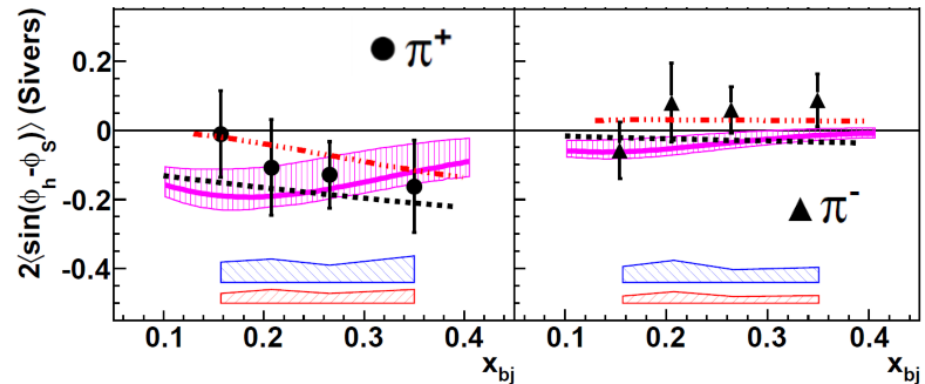
2002-2004 data  
NPB765 2007, PLB673 2009

compatible with zero

and **neutron**

Jefferson Lab

Hall A PRL107, 2011

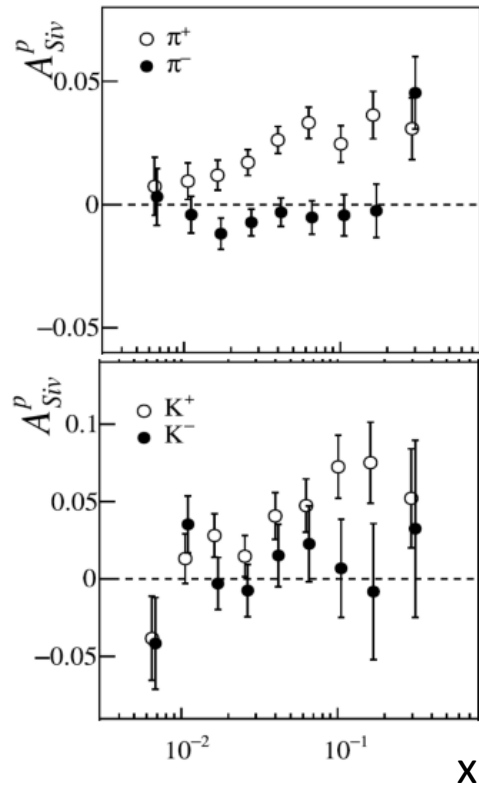


# The Sivers asymmetry

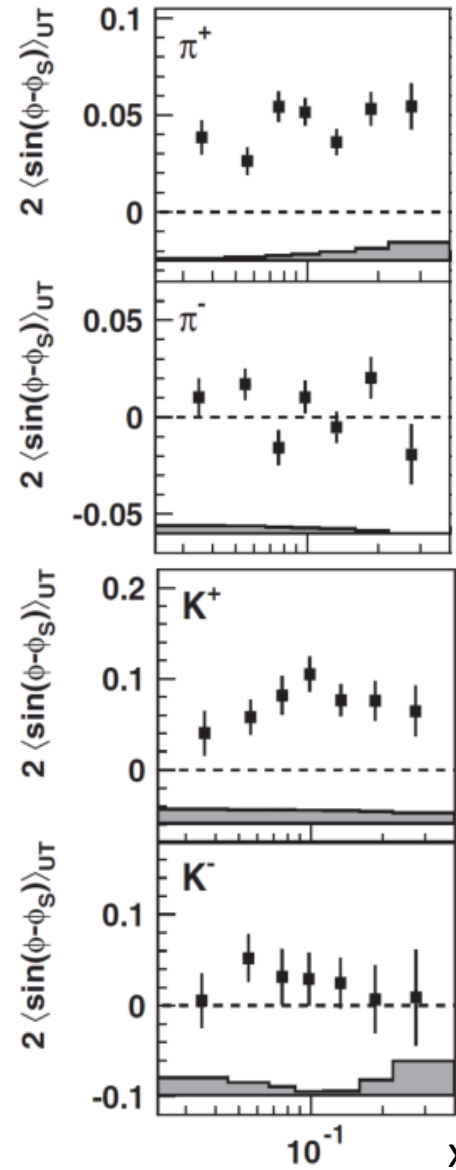
data on **polarised proton**



PLB744 2015

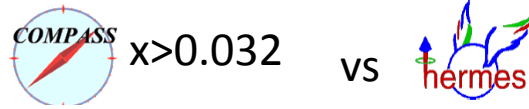


clear signal for positive hadrons  
K asymmetry larger than  $\pi$

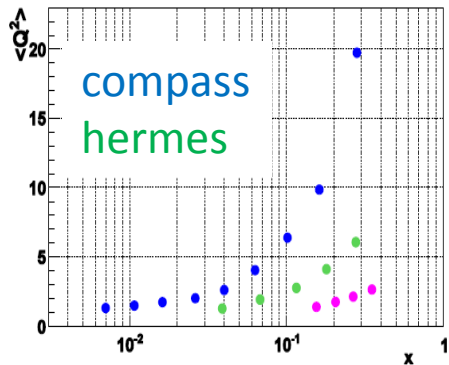


PRL103 2009

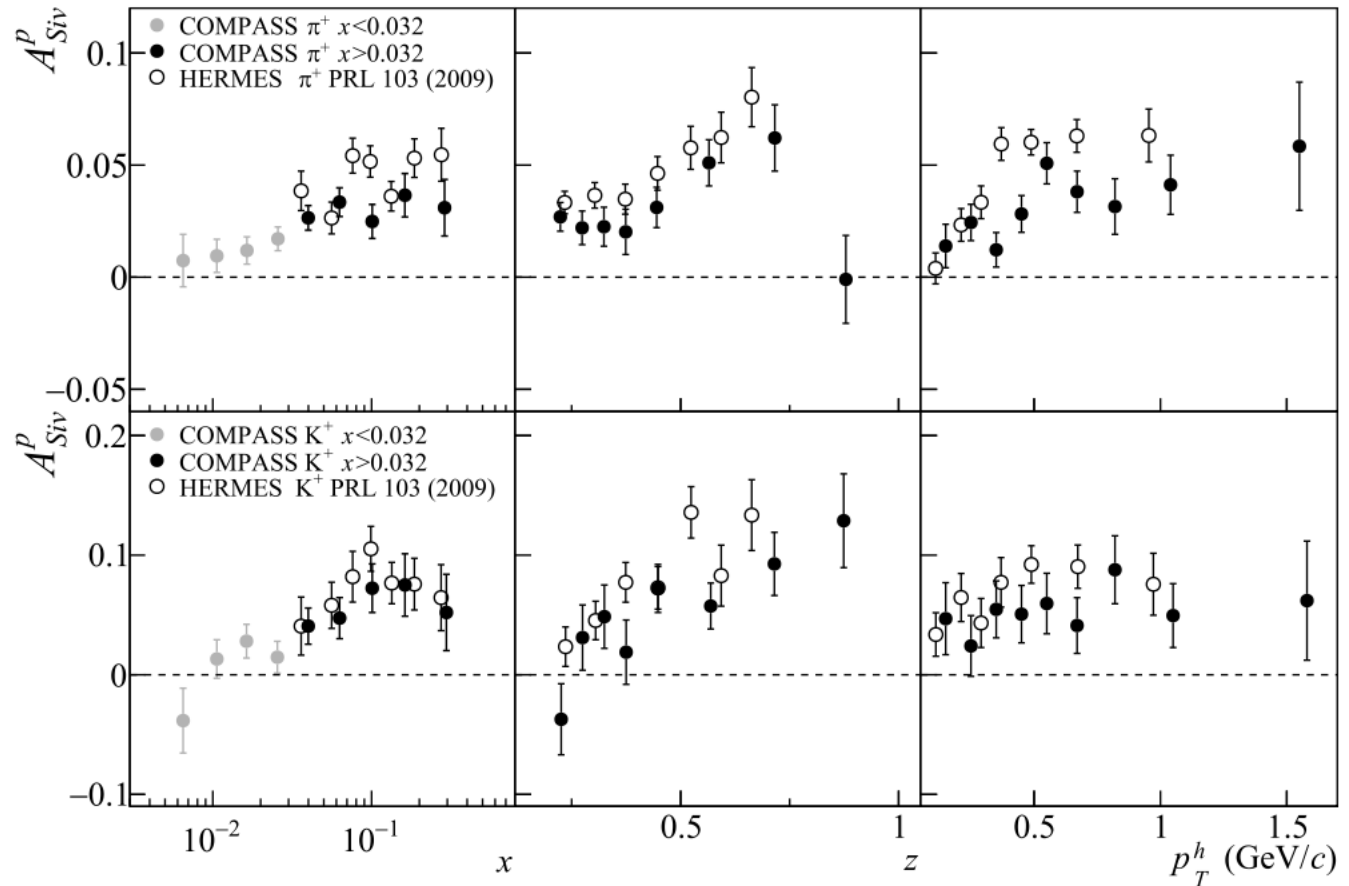
# The Sivers asymmetry



we can have the same range in  $x$  but  $Q^2$  is different



step toward TMD evolution



more info from multi dimensional analysis

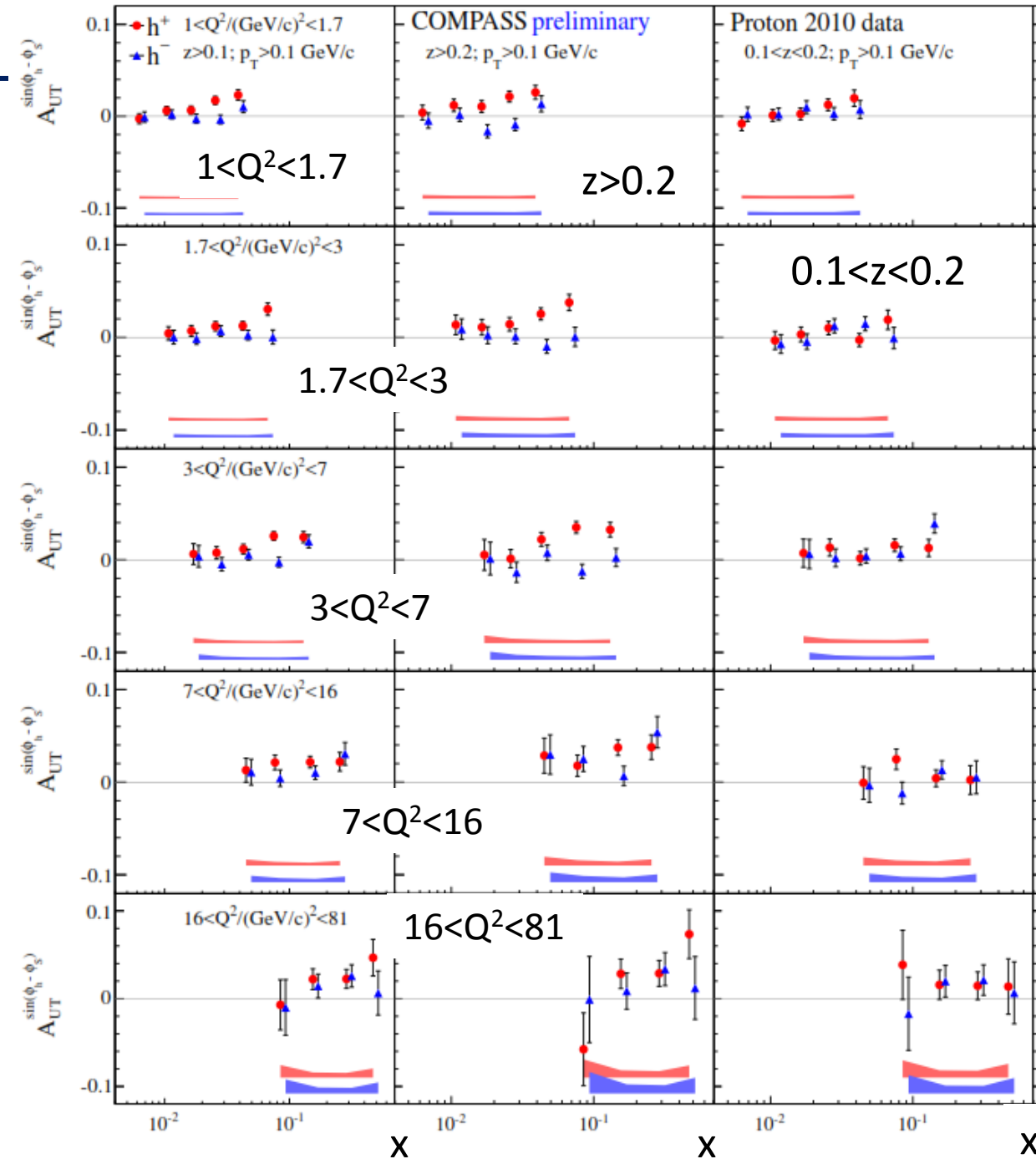


# The Sivers asymmetry

multi dimensional analysis



**no visible  $Q^2$  dependence**  
*(negative hadrons:  
 asymmetries tend to become  
 different from zero at high  $Q^2$ )*



**New measurement:  $P_T^h$  - weighted Siverts Asymmetry**

## $P_T^h$ /zM weighted Siverts Asymmetry

A. Kotzinian and P. J. Mulders, PLB 406 (1997) 373

D. Boer and P. J. Mulders, PRD 57 (1998) 5780

J. C. Collins et al. PRD 73 (2006) 014021

$$f_{1T}^{\perp(1)}(x) = \int d^2 k_T \frac{k_T^2}{2M^2} f_{1T}^{\perp}(x, k_T^2)$$

convolution over TM  $\longrightarrow$  product of first moment Siverts and FF

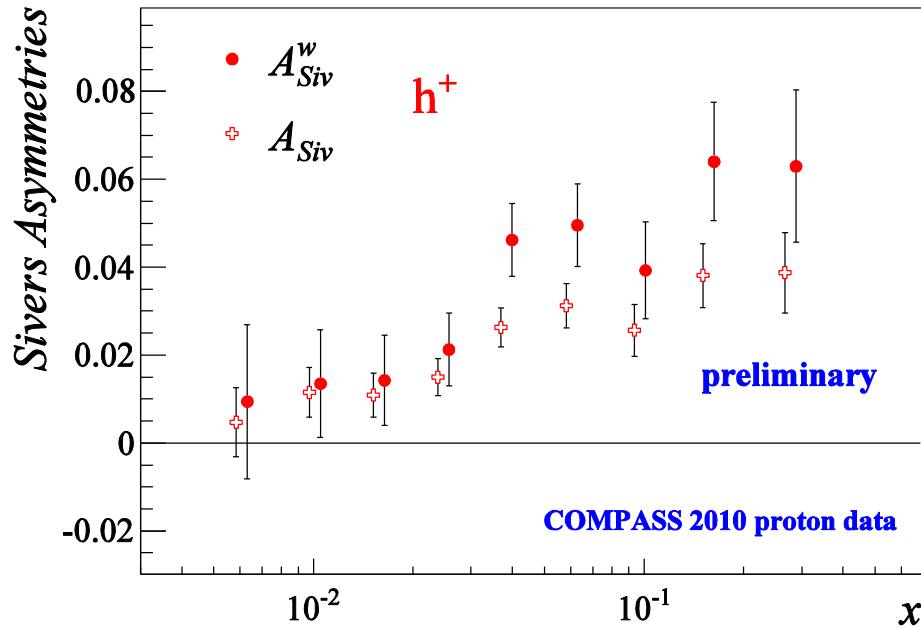
$$A_{Siv}^w(x) = 2 \frac{\sum_q e_q^2 x f_{1T}^{\perp(1)q}(x) \int_{\Omega_z} dz D_1^q(z)}{\sum_q e_q^2 x f_1^q(x) \int_{\Omega_z} dz D_1^q(z)}$$

in a **model independent way** (no assumption on the shape of PDFs and FFs)

COMPASS data from 2010 polarised proton have been analysed  
same sample as the one used for the published standard Siverts asymmetries

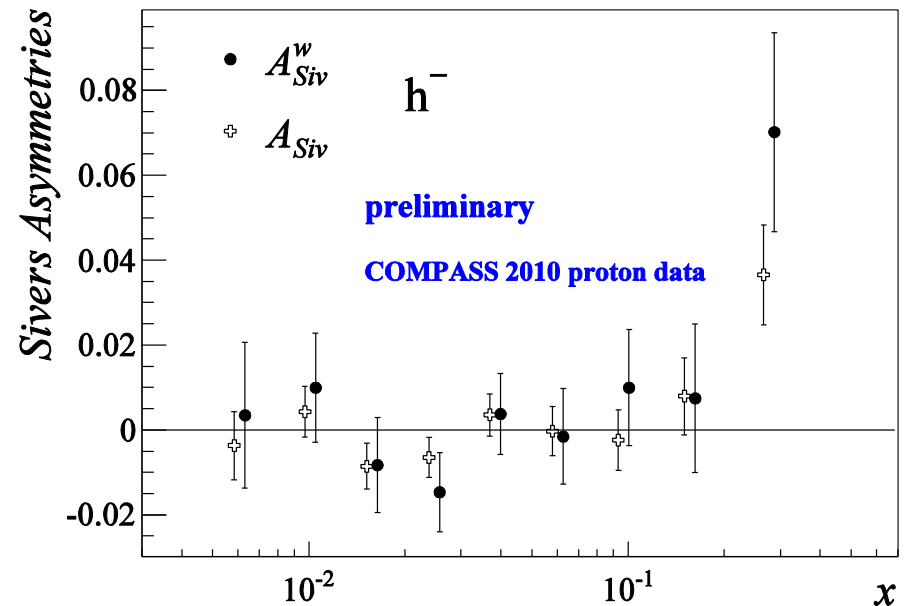
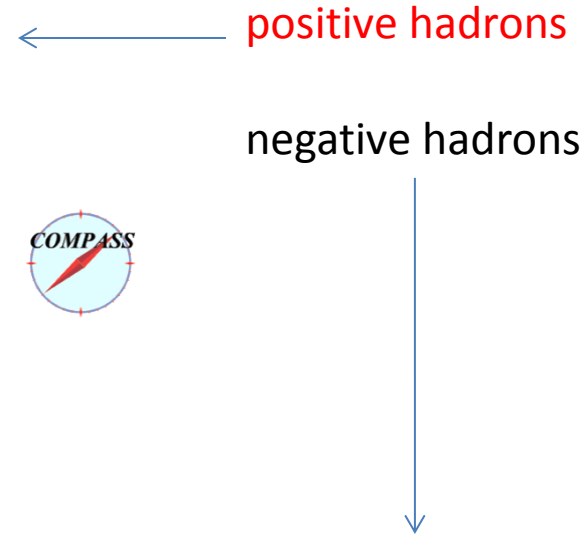
**only spin dependent part of the cross section must be weighted**

Final results ● compared with the standard Sivvers Asymmetries⊕ (PLB 717 (2012) 383)

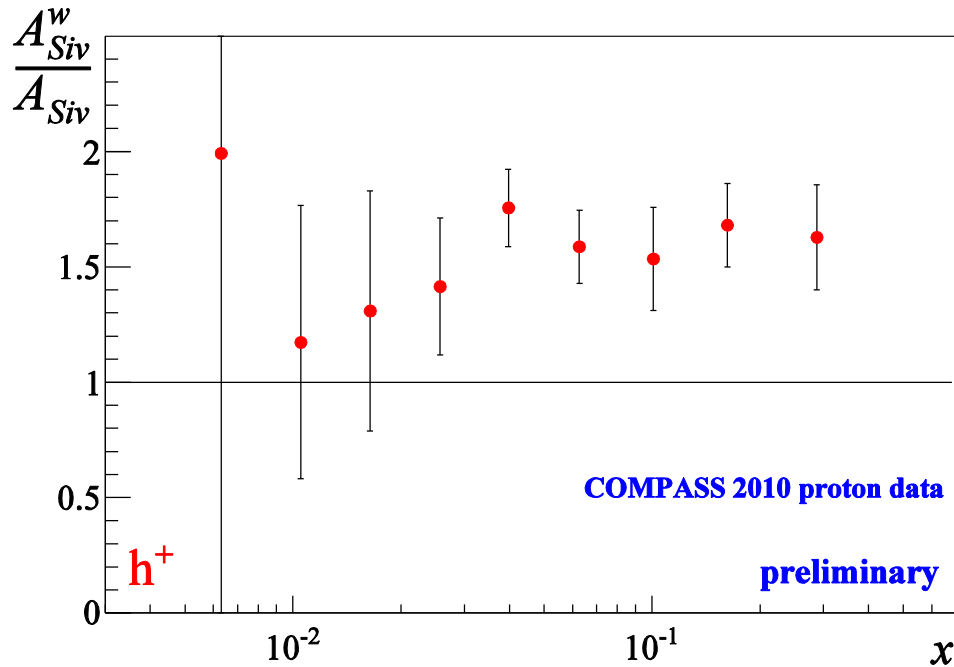


$$A_{Siv}^w(x) \simeq 2 \frac{x f_{1T}^{\perp(1)u}(x)}{x f_1^u(x)}$$

assuming u dominance  
and for  $\pi^+$



# Ratio between weighted and standard Sivers asymmetries



$$A_{Siv}^w(x) \simeq 2 \frac{x f_{1T}^{\perp(1)u}(x)}{x f_1^u(x)}$$

~ constant in x

using **Gaussian** model for the *dependence on the intrinsic transverse momenta of the quarks*

the **standard Sivers asymmetries** can be expressed as (u dominance)

$$A_G(x) \approx \frac{\pi M}{2} \frac{f_{1T}^{\perp(1)u}(x)}{f_1^u(x)} \frac{\int z / P_{T,S}^h D_1^q(z) dz}{\int D_1^q(z) dz}$$

$$(P_{T,S}^h)^2 = z^2 k_{\perp,S}^2 + p_{\perp}^2$$

*Sivers intrinsic quark transverse momentum*



# COMPASS results on the Sivers weighted asymmetries : paper is in preparation

more work done for the paper:

- weighted asymmetries for  $0.1 < z < 0.2$
- weighted asymmetries as function of  $z$
- using  $P_{Th}/M$  instead of  $P_{Th}/zM$



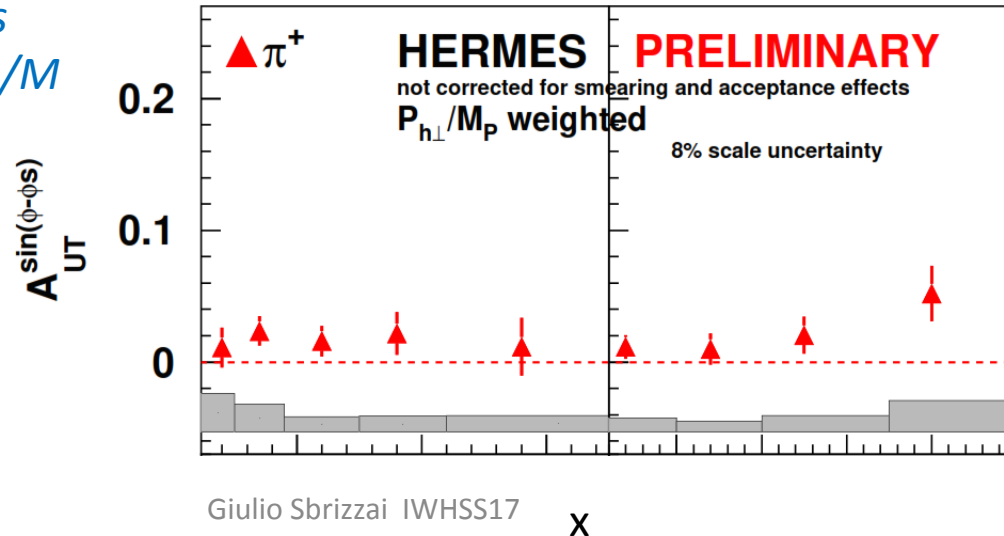
next to come: Bessel weighted Sivers

Also HERMES previously extracted Sivers (and Collins) weighted asymmetries



*HERMES preliminary results  
pion Sivers with weight= $P_T^h/M$*

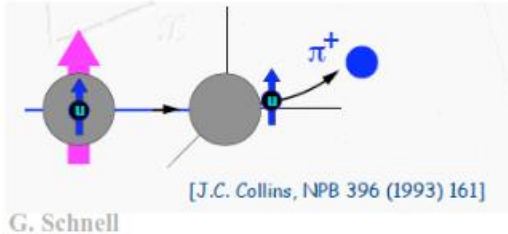
I.M. Gregor , Acta Phys.Polon. B36 (2005) 209



# The Collins asymmetry

$$A_{UT}^{\sin(\phi_h + \phi_S - \pi), h} = \frac{\sum_q e_q^2 h_1^q(k_\perp) \otimes H_1^{\perp q \rightarrow h}(p_\perp)}{\sum_q e_q^2 f_1^q \otimes D_1^{q \rightarrow h}}$$

convolution of **transversity** with **Collins FF**



correlation between  
transverse spin of the fragmenting quark  
and  
transverse momentum of hadrons



2004:  
non-zero values on proton

compatible with zero on deuteron



global fits  
first extraction of  
transversity and Collins FF

*using also e+e- data from Belle*



# The Collins asymmetry

final results on  
deuteron

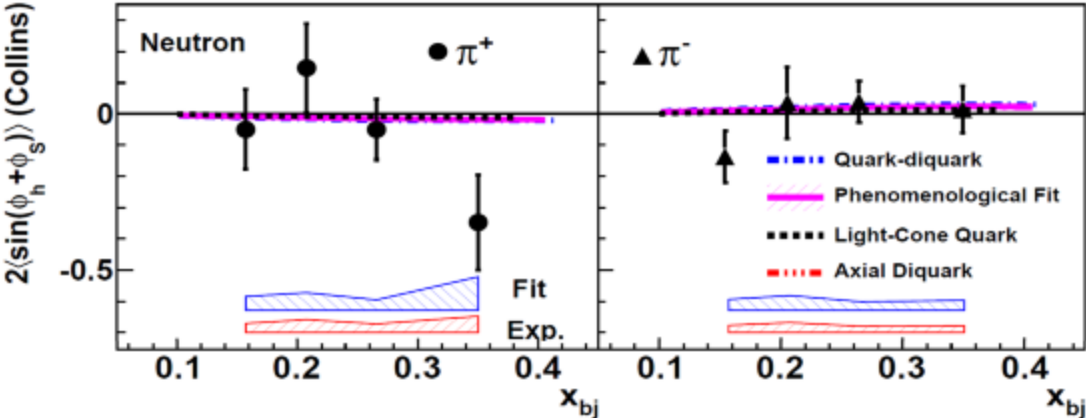
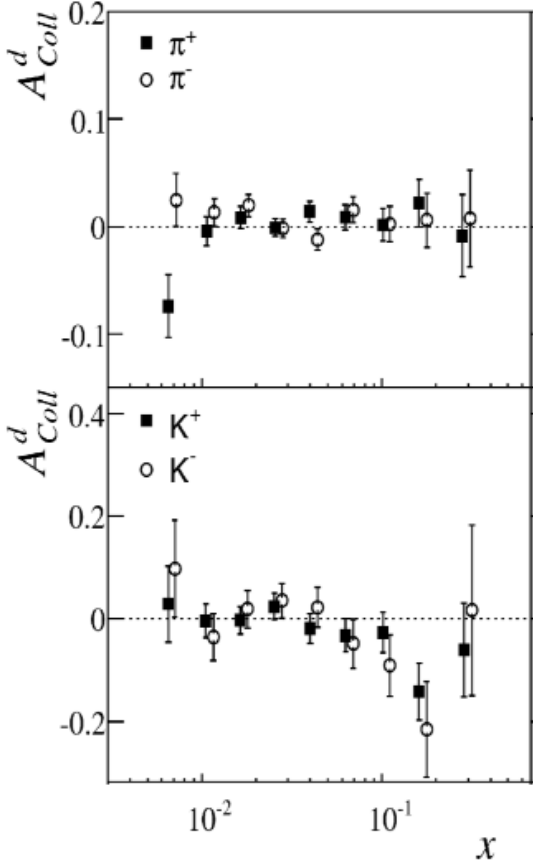


2002-2004 data  
NPB765 2007, PLB673 2009

and neutron

Jefferson Lab

Hall A PRL107, 2011



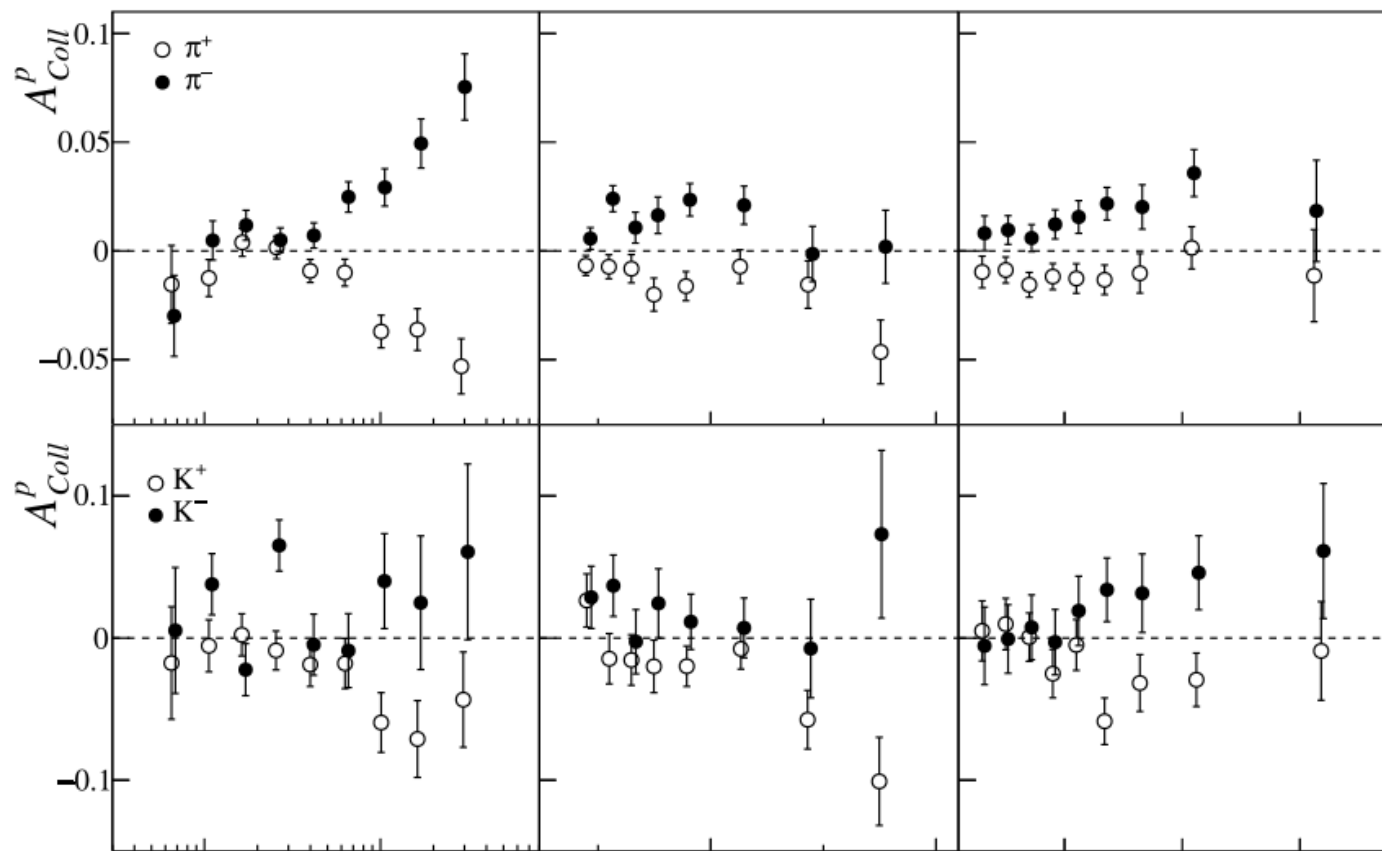


# The Collins asymmetry

1d measurements on transversely polarised proton



PLB744 2015





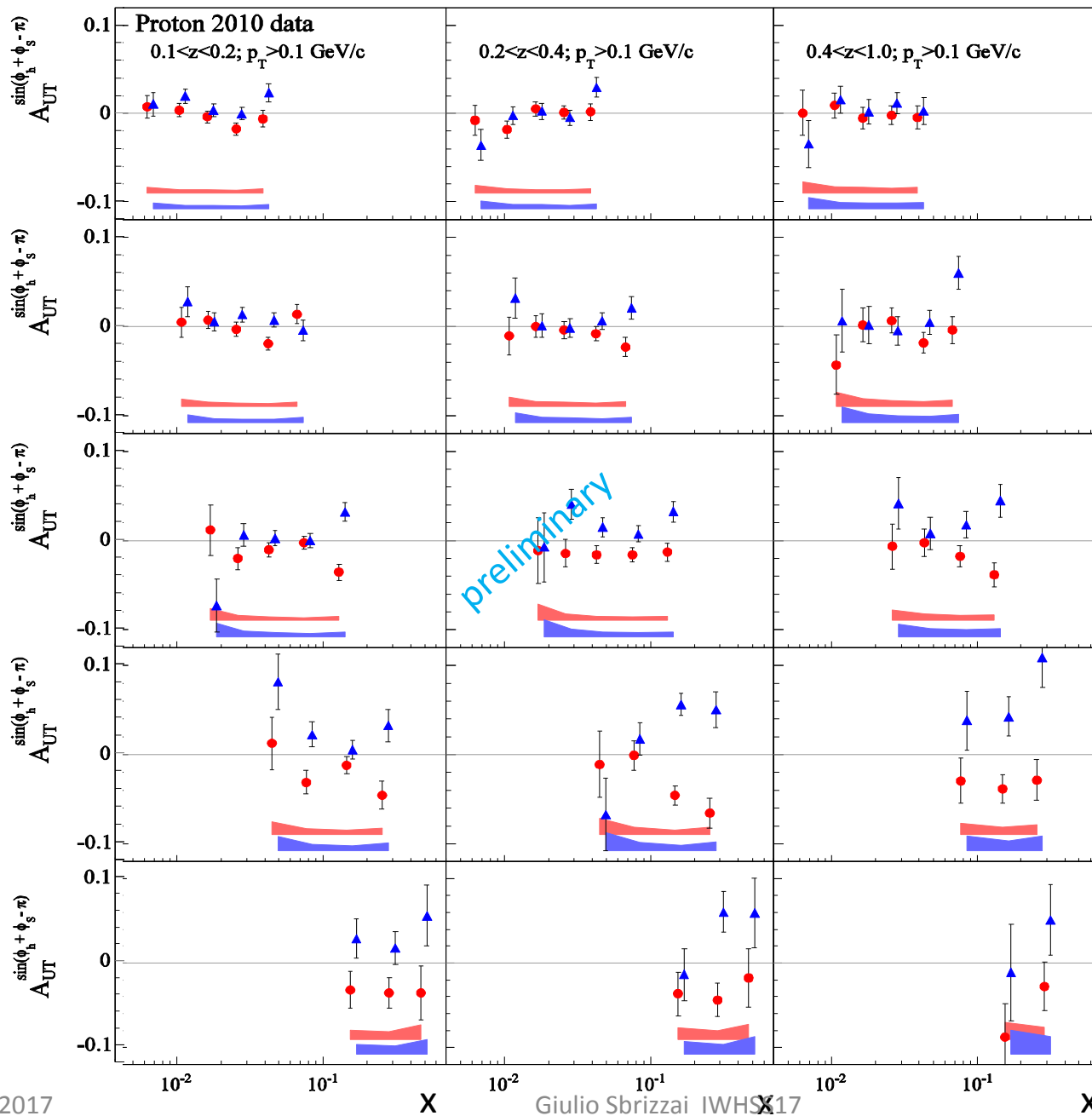
h+  
h-

0.1 < z < 0.2

0.2 < z < 0.4

0.4 < z < 1.0

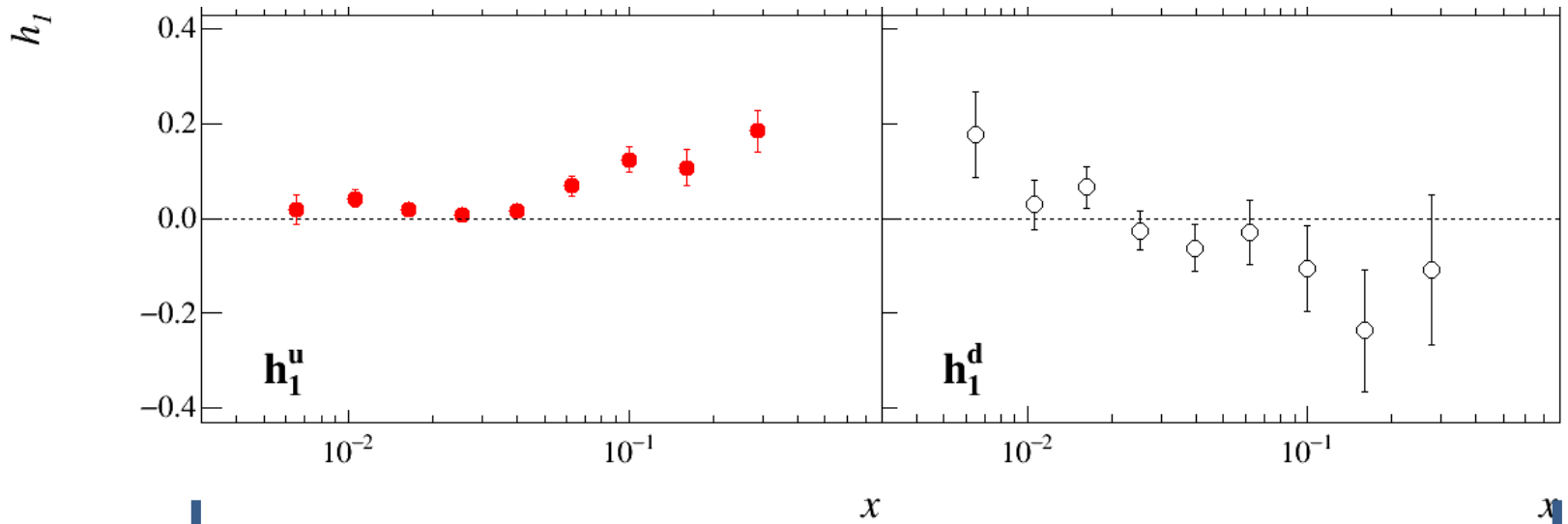
Collins: Multi-D  
approach  
(x: Q<sup>2</sup>: z: p<sub>T</sub>)



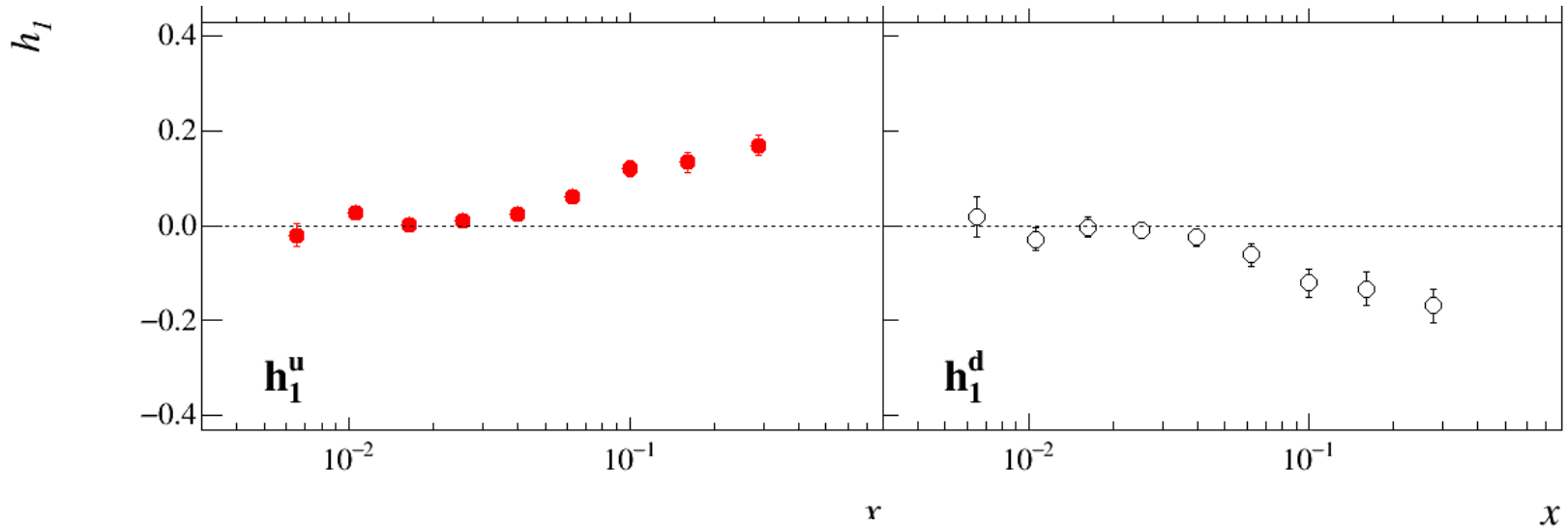
still data on polarised deuteron suffer from statistic  
(wrt data on polarised proton)

affect the error on the extraction of Transversity and Sivers functions  
for the d quark  
(but also other analyses...)

# one example: Transversity

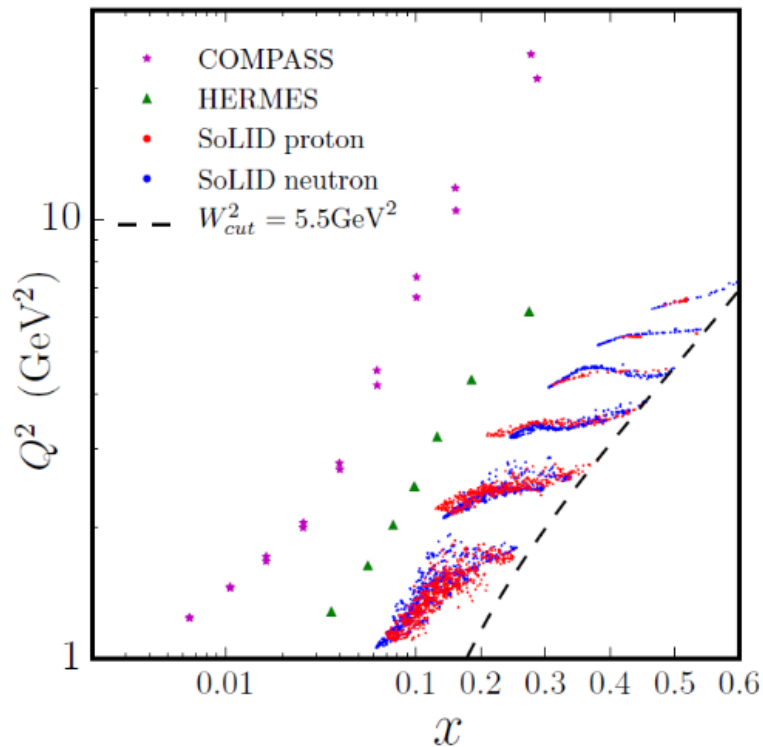


one more year of data taking on polarised deuteron at COMPASS



Projection from A Bressan, COMPASS beyond 2020 Workshop, CERN, March 2016

an enormous amount of data will come from JLab12 experiments  
but in a **different x range!**



Z. Ye et al. JLAB-THY-16-2328

COMPASS:

no competition on precision!

smaller  $x$ , factor  $> 5$  in  $Q^2$ , ...

the kinematical region is relevant  
and new d data coming soon are  
needed

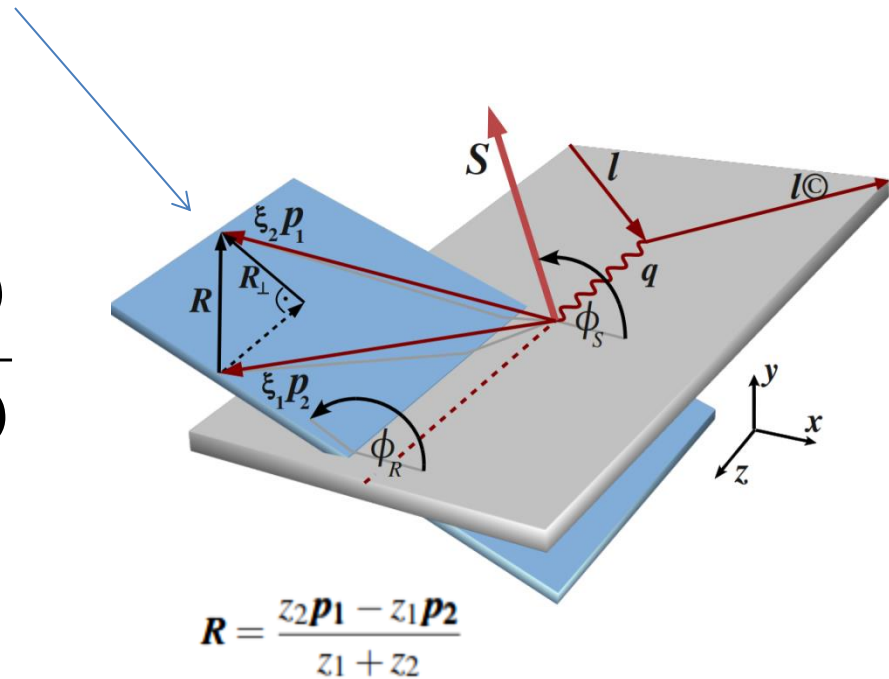
# The dihadron asymmetry

it gives rise to another azimuthal asymmetry in the 2h cross section, on an angle  $\phi_{RS}$  defined as  $\phi_R + \phi_S - \pi$

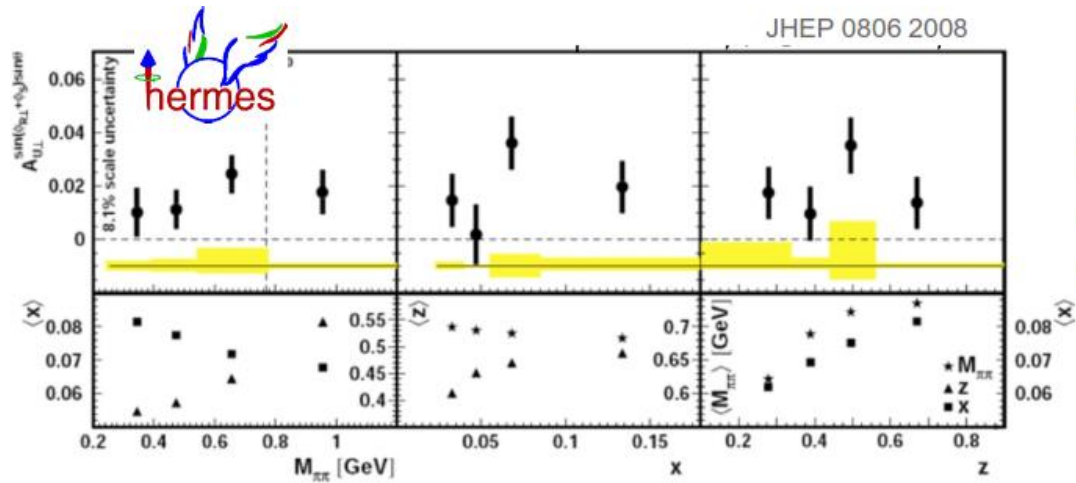
$$A_{h^+h^-}^p \approx \frac{\sum_q e_q^2 \cdot h_1^q(x) \cdot H_{1q}^{\perp}(z, M_{hh}^2)}{\sum_q e_q^2 \cdot f_1^q(x) \cdot D_{1q}^h(z, M_{hh}^2)}$$

product of **transversity** with **dihadron FF**

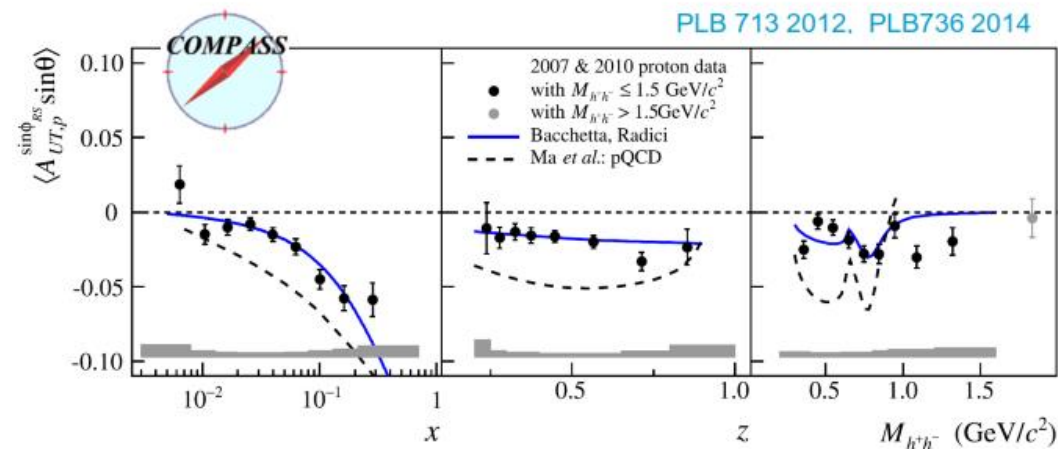
$$A_{Coll} \approx \frac{\sum_q e_q^2 \cdot h_1^q(k_{\perp}^2, x) \otimes H_{1q}^{\perp h}(p_{\perp}^2, z)}{\sum_q e_q^2 \cdot f_1^q(k_{\perp}^2, x) \otimes D_{1q}^h(p_{\perp}^2, z)}$$



# The dihadron asymmetry



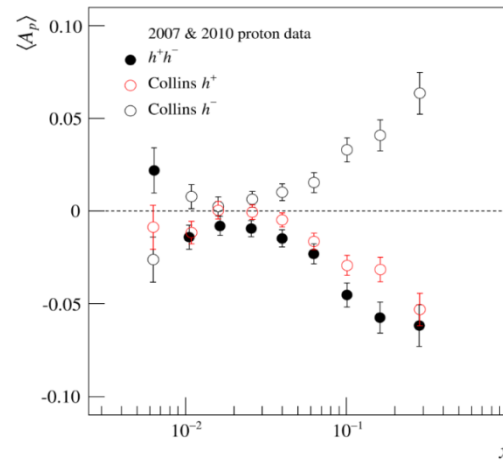
**HERMES proton**  
 first evidence for  
 non-zero dihadron FF,  
 same sign of Collins  
 asymmetry for  $\pi^+$



**COMPASS**  
 deuteron:  
 compatible with zero  
 proton:  
 same sign and shape  
 slightly higher  
 than Collins asymmetry  
 for  $h^+$

# Interesting studies comparing with the Di-hadron Transverse Spin Asymmetries

- Collins asymmetry for  $h^+$  and for  $h^-$  :  
“mirror symmetry”
- dihadron asymmetry vs Collins asymmetry:  
only somewhat larger



analysis of the single hadron and di-hadron asymmetries performed  
**on a common data sample** (2010 transversely polarised proton)



derive the formalism to describe the two asymmetries together

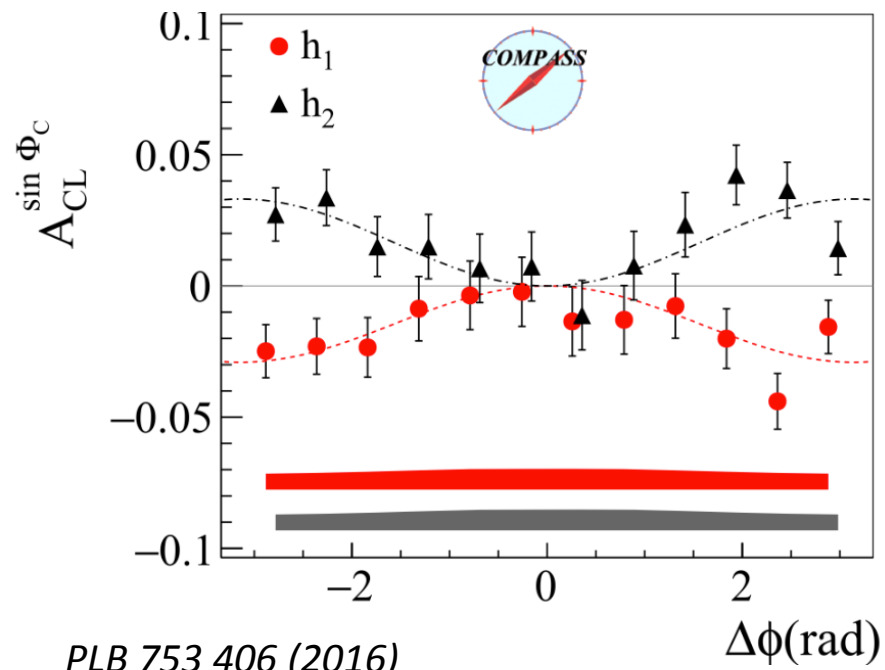


the general expression for the  $lN \rightarrow l' h^+ h^- X$  cross section

$$\frac{d\sigma^{h^+h^-}}{d\phi_{h^+} d\Delta\phi d\phi_S} = \sigma_U^{h^+h^-} + S_T \cdot \left[ \left( \sigma_{1C}^{h^+h^-} + \sigma_{2C}^{h^+h^-} \cos \Delta\phi \right) \sin(\phi_{h^+} + \phi_S - \pi) + \dots \right]$$

$$\Delta\phi = \phi_{h^+} - \phi_{h^-}$$





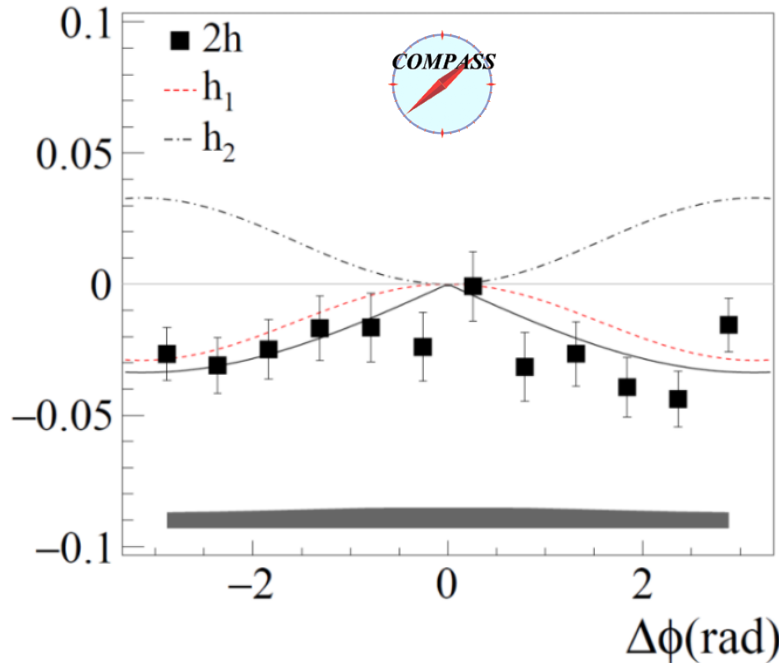
measured Collins asymmetries

$$A_{2CL}^{\sin(\phi_{h^-} + \phi_S - \pi)} = -\frac{\sigma_{1C}^{h^+h^-}}{\sigma_U^{h^+h^-}} \cdot (1 - \cos \Delta\phi)$$

$$A_{1CL}^{\sin(\phi_{h^+} + \phi_S - \pi)} = \frac{\sigma_{1C}^{h^+h^-}}{\sigma_U^{h^+h^-}} \cdot (1 - \cos \Delta\phi)$$

data described assuming mirror asymmetry !

$$\sigma_{1C}^{h^+h^-} = -\sigma_{2C}^{h^+h^-}$$



$$A_{2h,CL}^{\sin(\phi_{2h} + \phi_S - \pi)} = \frac{\sigma_{1C}^{h^+h^-}}{\sigma_U^{h^+h^-}} \cdot \sqrt{2} \cdot (1 - \cos \Delta\phi)$$



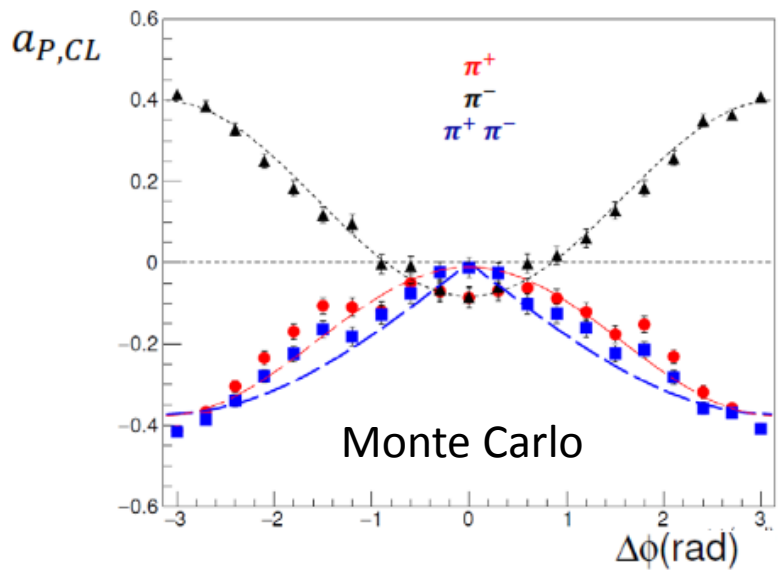
*the same quantity which appear in the single hadron asymmetry*

# Interesting studies comparing with the Di-hadron Transverse Spin Asymmetries

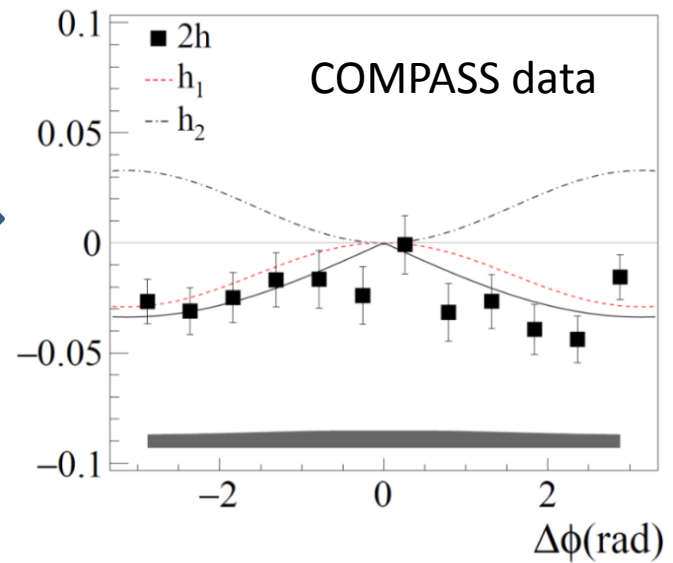
**new:** preliminary results from a Monte Carlo code for transversely polarized quark jet based on the string fragmentation and including, for the first time, the  $^3P_0$  mechanism → X.Artru

1h and 2h  $a_p$  obtained as COMPASS asymmetries from the same sample of generated events

A. Kerbizi talk at SPIN2016



very encouraging results



# Other transverse spin dependent asymmetries

$$\begin{aligned}
 & + |S_{\perp}| \left[ \boxed{\sin(\phi_h - \phi_S)} \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\
 & + \varepsilon \boxed{\sin(\phi_h + \phi_S)} F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \boxed{\sin(3\phi_h - \phi_S)} F_{UT}^{\sin(3\phi_h - \phi_S)} \\
 & \left. + \sqrt{2\varepsilon(1+\varepsilon)} \boxed{\sin\phi_S} F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \boxed{\sin(2\phi_h - \phi_S)} F_{UT}^{\sin(2\phi_h - \phi_S)} \right] \\
 & + |S_{\perp}| \lambda_e \left[ \sqrt{1-\varepsilon^2} \boxed{\cos(\phi_h - \phi_S)} F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \boxed{\cos\phi_S} F_{LT}^{\cos\phi_S} \right. \\
 & \left. + \sqrt{2\varepsilon(1-\varepsilon)} \boxed{\cos(2\phi_h - \phi_S)} F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \Bigg\},
 \end{aligned}$$

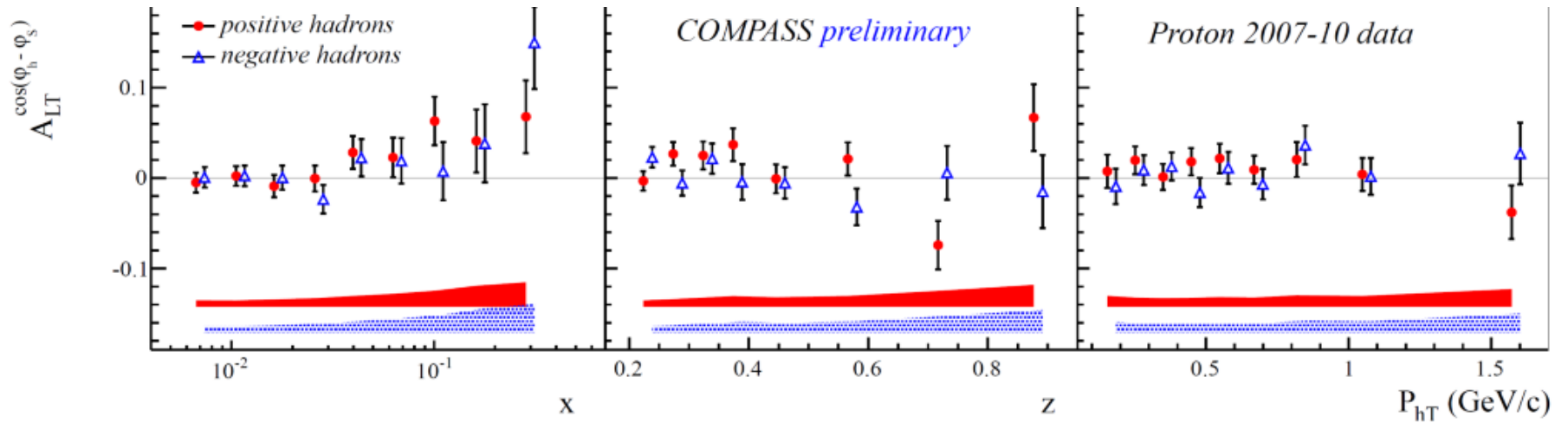
sivers  
collins
pretzelosity
worm-gear

higher twist effects

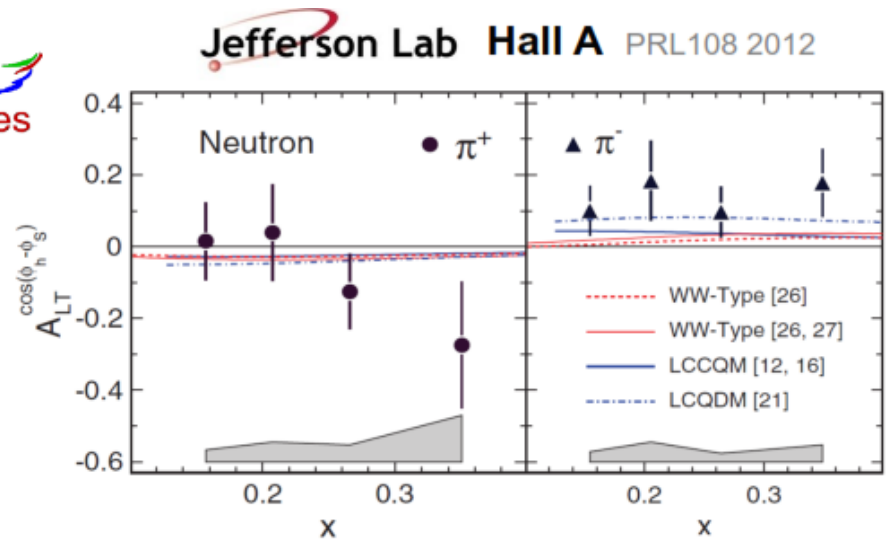
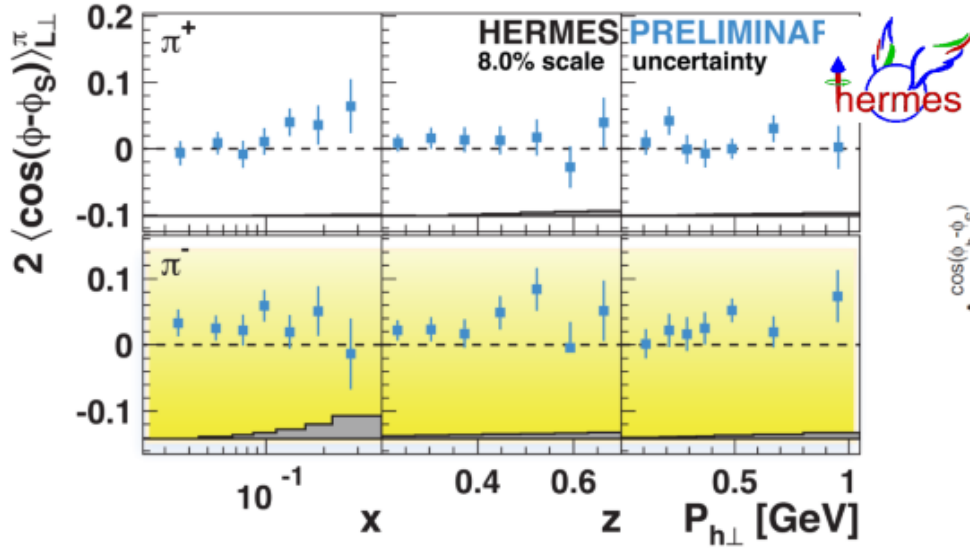
**all of them (and more ...) have been measured on p / d / n by  
COMPASS, HERMES, JLab**

***preliminary results for multidimensional analysis also  
produced at COMPASS and HERMES (SPIN2014)***

$$A_{LT}^{\cos(\phi_h - \phi_s)} \propto g_{1T}^q \otimes D_{1q}^h, \quad \text{worm-gear} \quad g_{1T}^q : \begin{array}{c} \text{---} \odot \text{---} \\ \text{---} \odot \text{---} \end{array}$$



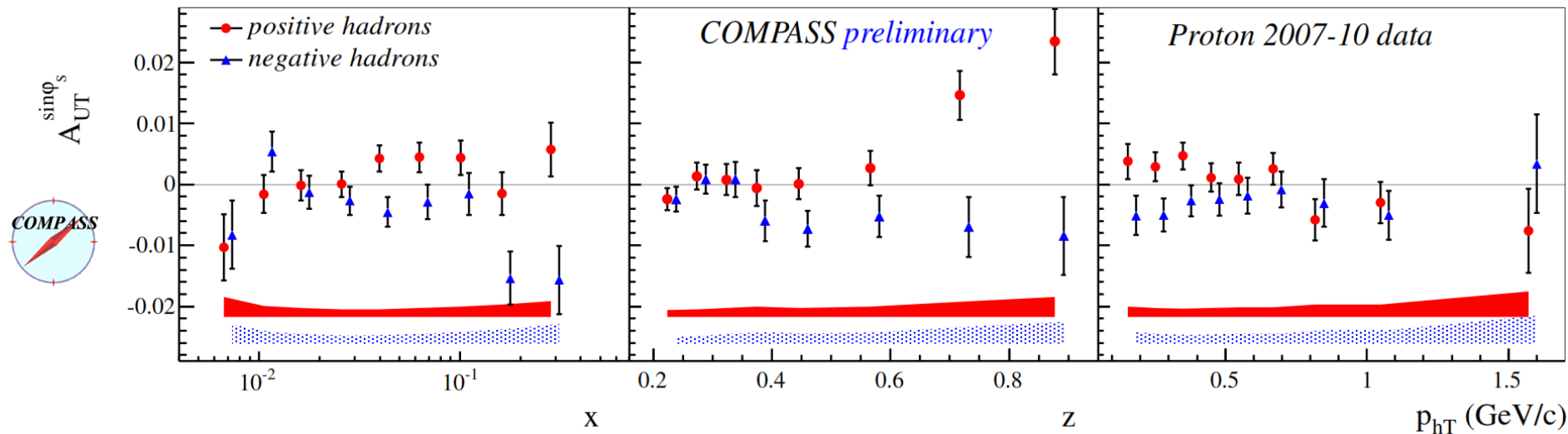
same trend



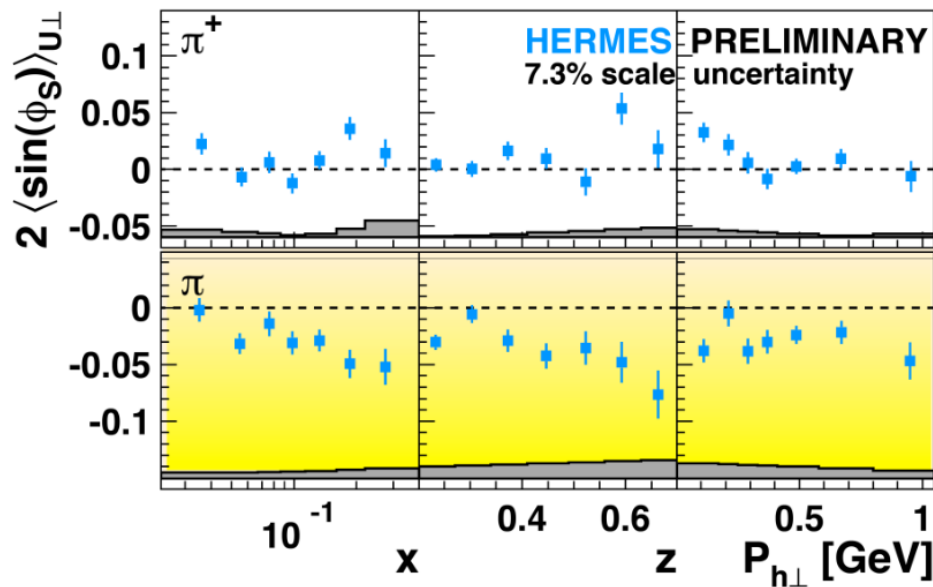
$$A_{UT}^{\sin(\phi_s)} \stackrel{WW}{\propto} Q^{-1} \left( h_1^q \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots \right)$$

twist 3 related to Collins and Sivers  
in WW approximation

compatible with zero on deuteron, but on proton signal different from zero



considerably larger at HERMES  
as expected



Other results:  
**on longitudinal spin azimuthal asymmetries:**

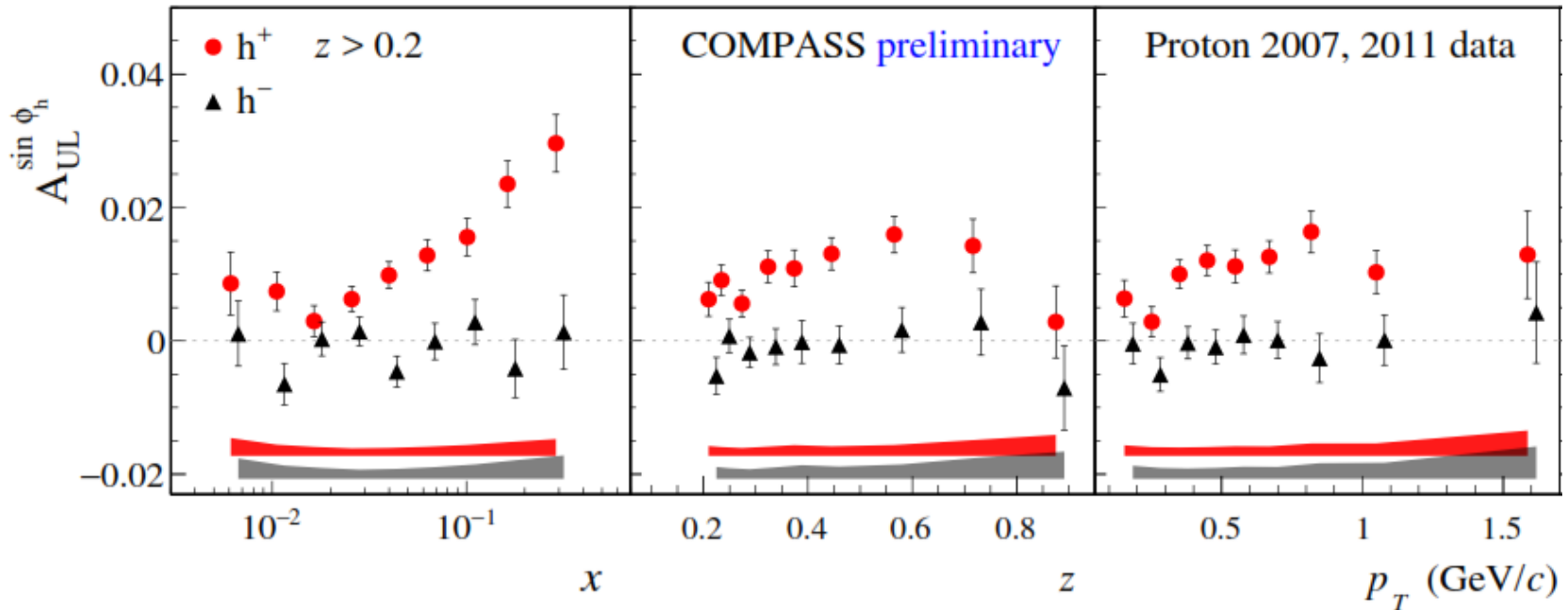
Other results:  
**on longitudinal spin azimuthal asymmetries:**

on deuteron *EPJ C70 (2010)*

*results compatible with zero within statistical accuracy*

**and on proton**

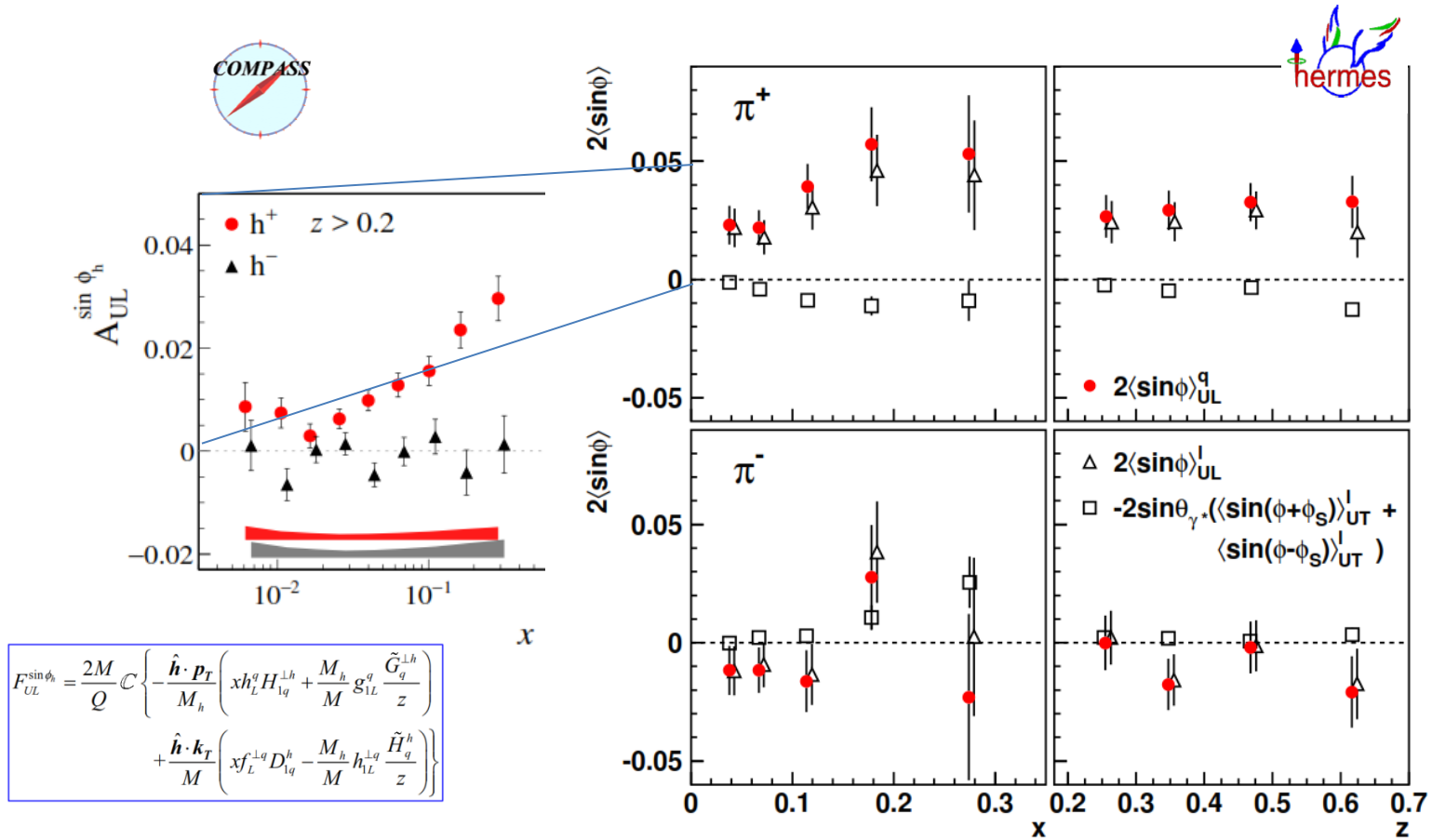
*(first shown at SPIN2016 B.Parsamyan)*



# longitudinal spin azimuthal asymmetries on proton

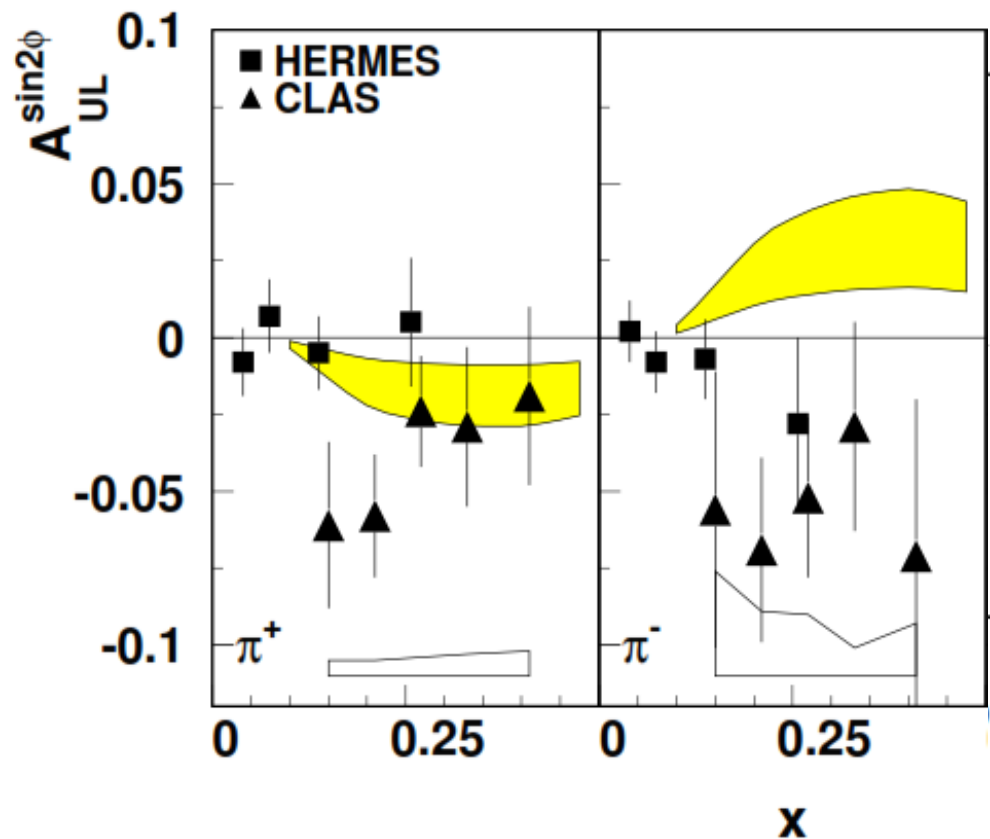
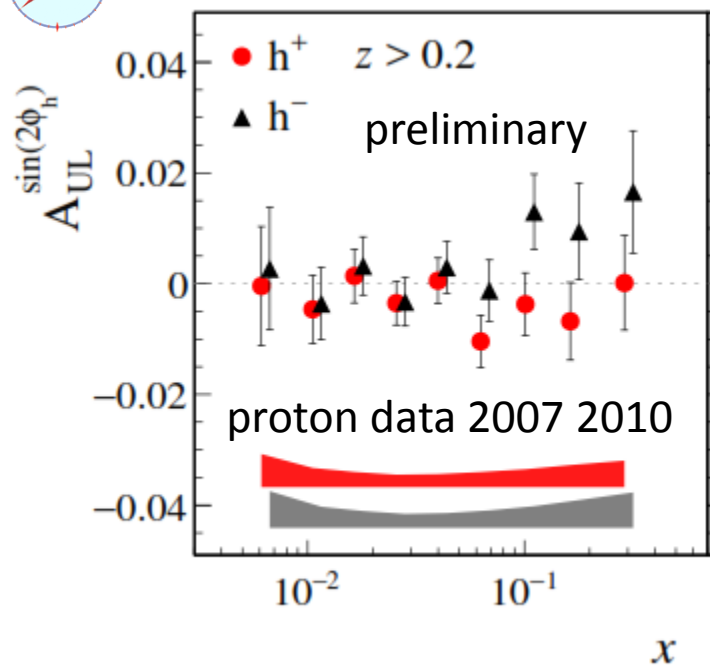
higher twists contributions

smaller signal than in hermes PLB 622 (2015)





# longitudinal spin azimuthal asymmetries on proton



# Conclusions

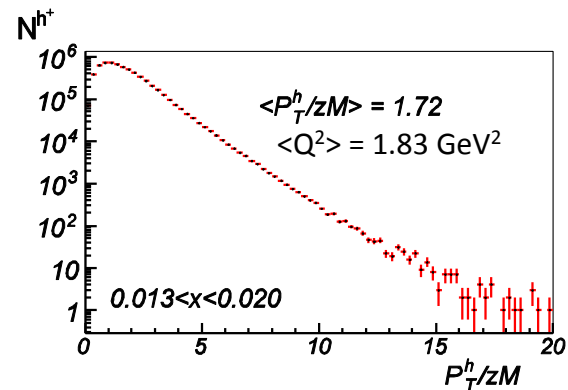
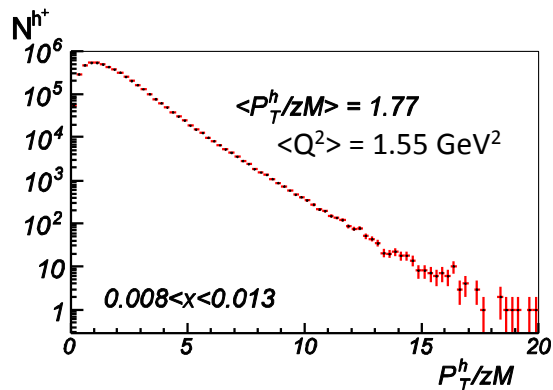
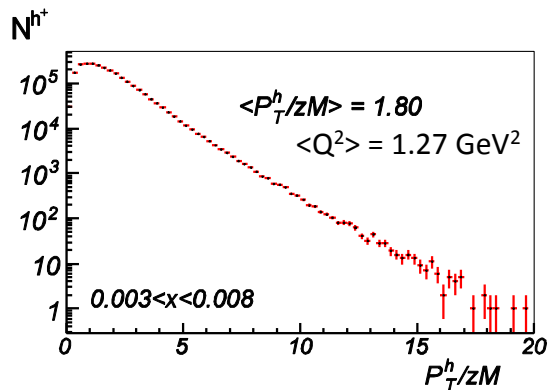
- many SIDIS results, not all easy to explain  
some interesting analysis still going on
- new data on unpolarised SIDIS coming from  
COMPASS LH2 in parallel to DVCS (2016 -2017)
- more data on deuteron are really needed soon....  
one more year on transversely polarised deuteron COMPASS beyond 2020
- new data from JLab12 and EIC...

# SPARES

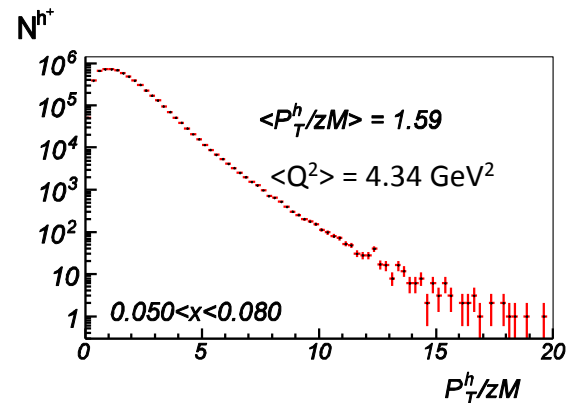
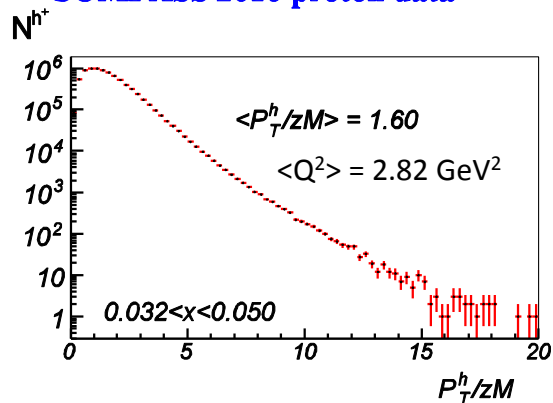
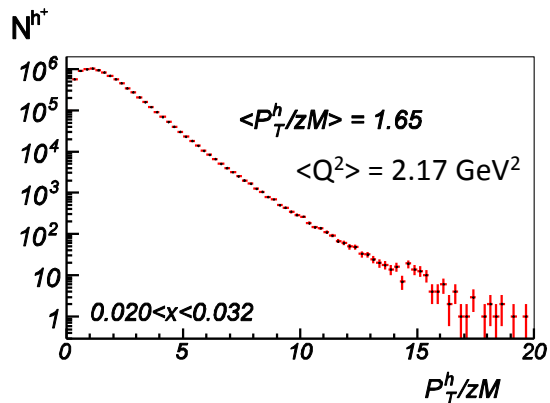


# The $P_T^h/zM$ distributions for each bin of $x$

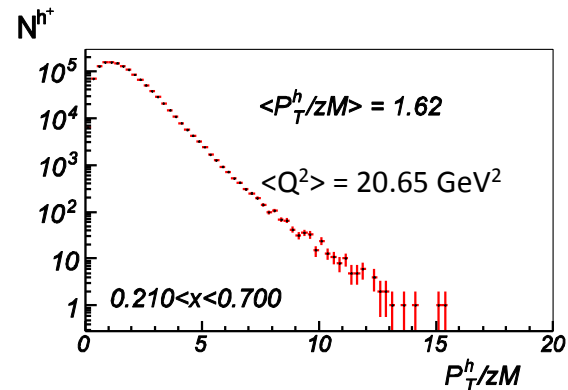
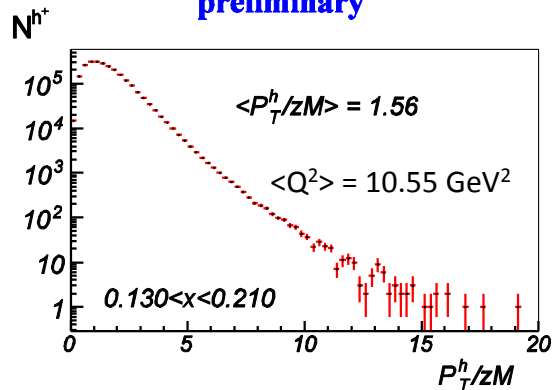
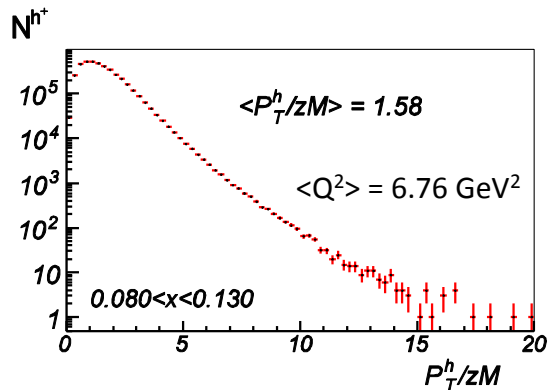
positive hadrons  
not acceptance corrected



COMPASS 2010 proton data



preliminary





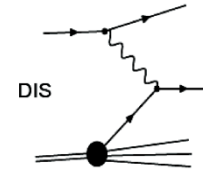
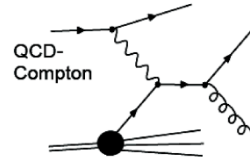
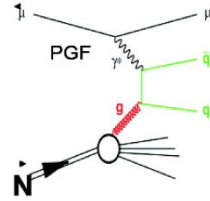
# Gluon Sivers

submitted to PLB

from high- $P_T^h$  two hadrons pairs

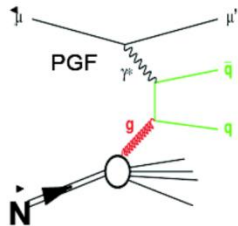
three different contributions:

high  $P_T^h$  hadrons pairs  
enhance contribution from PGF



Neural Network Monte Carlo to tag different processes on COMPASS data

photon-gluon fusion  
(PGF)

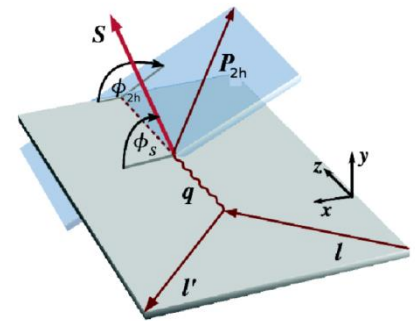


$$\vec{P}_{2h} = \vec{p}_1 + \vec{p}_2$$

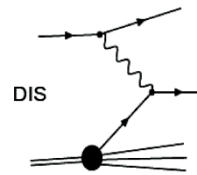
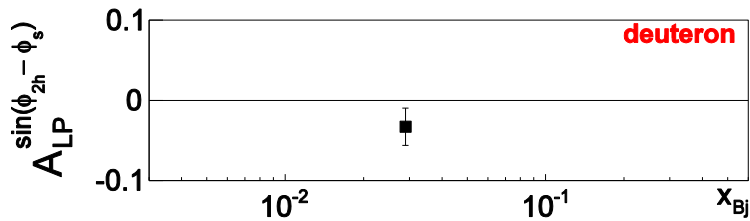
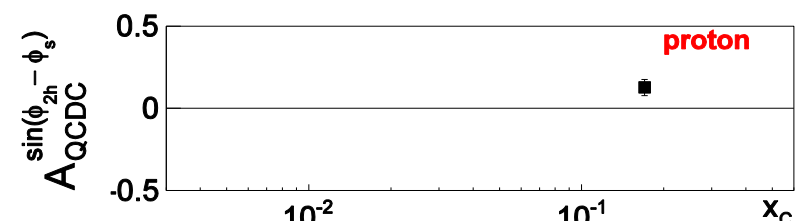
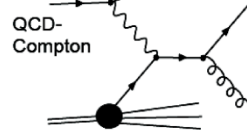
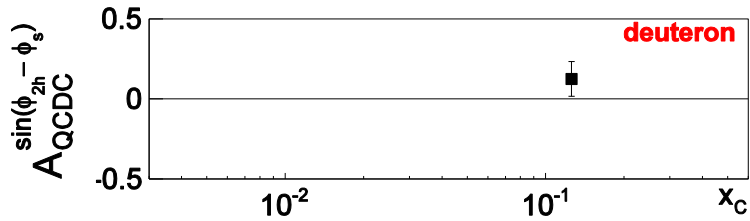
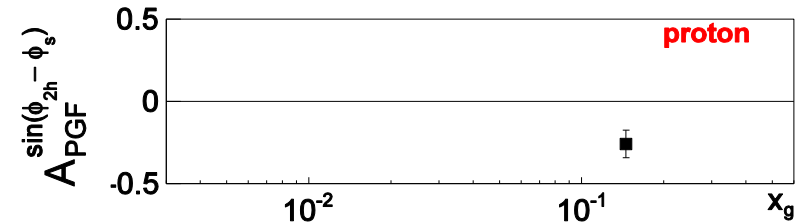
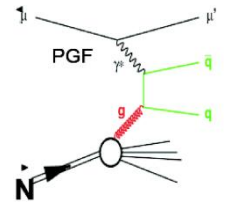
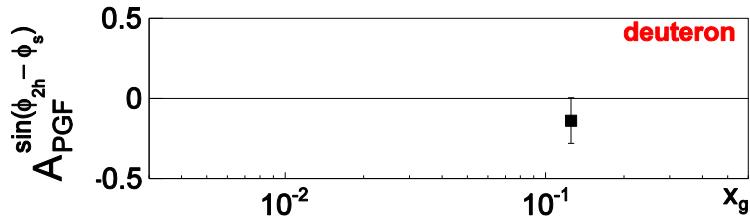
$$\phi = \phi_{2h} - \phi_S$$

$\phi_{2h}$  correlated to  $\phi_{\text{gluon}}$

$$l + N \rightarrow l' + 2h + X$$



# Gluon Sivers from high- $P_T^h$ two hadrons pairs



Limited precision on deuteron. More data needed.

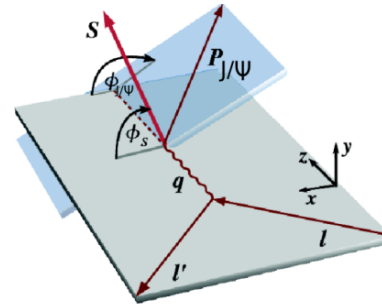
The results for the LP compatible with single hadron measurements

# Gluon Sivers from J/ψ



from 2010 transversely polarised proton data  
in two z bins 0.30 < z < 0.95 and 0.95 < z < 1.05

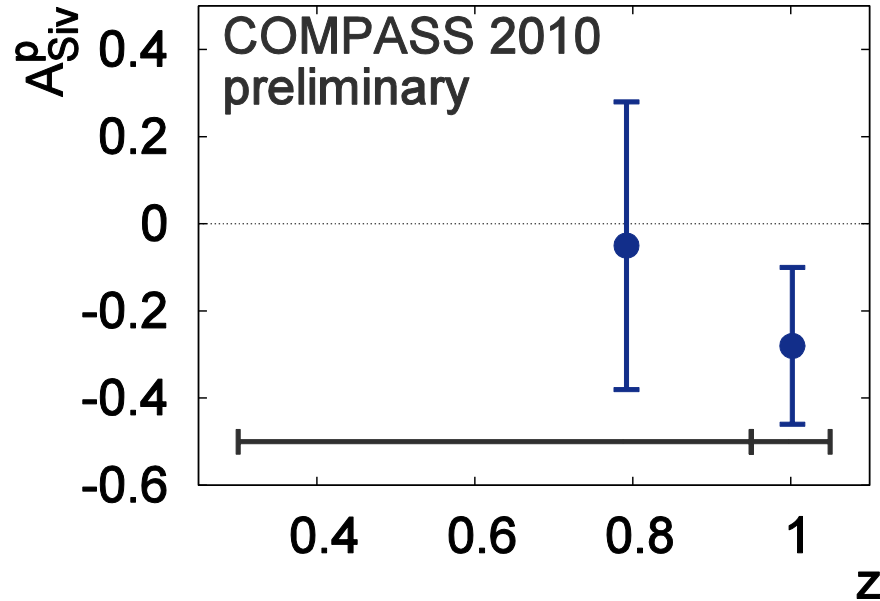
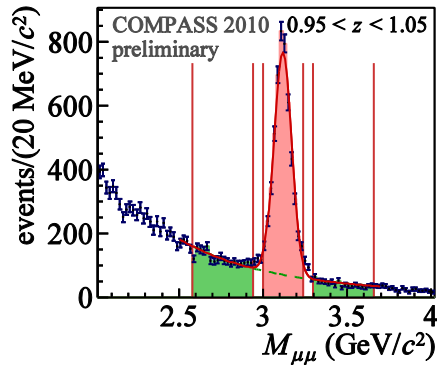
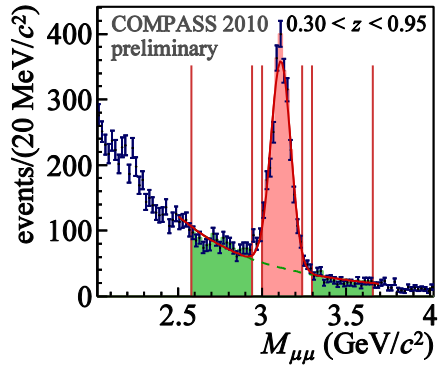
$$\mu^+ + N \rightarrow \mu^+ + J/\psi + X \rightarrow 2\mu^+ + \mu^- + X$$



$$\mathbf{P}_{J/\psi} = \mathbf{p}_{\mu^+} + \mathbf{p}_{\mu^-}$$

$$\phi_{\mu^+\mu^-} = \phi_{J/\psi} = \phi_g$$

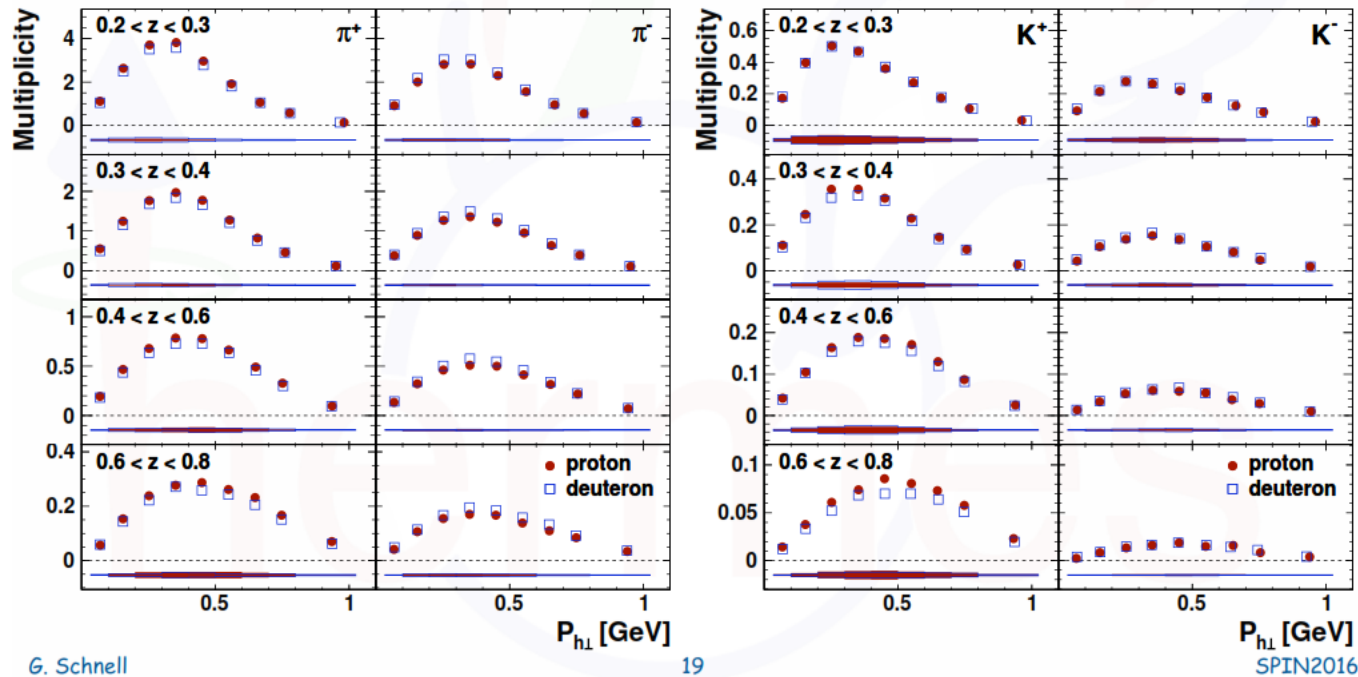
$$\phi = \phi_{\mu^+\mu^-} - \phi_s$$



# Transverse momentum dependence

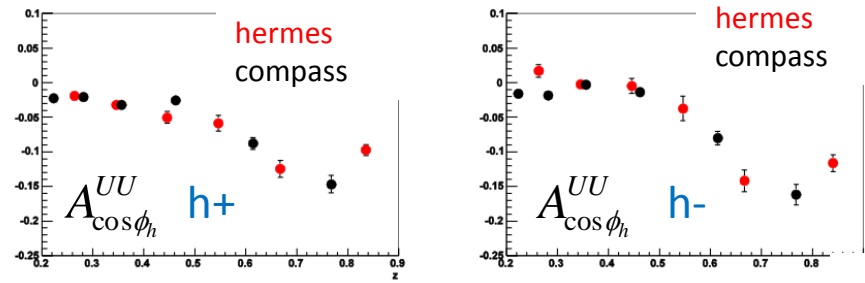
- multi-dimensional analysis allows going beyond collinear factorization
- flavor information on transverse momenta via target variation and hadron ID

[Airapetian et al., PRD 87 (2013) 074029]

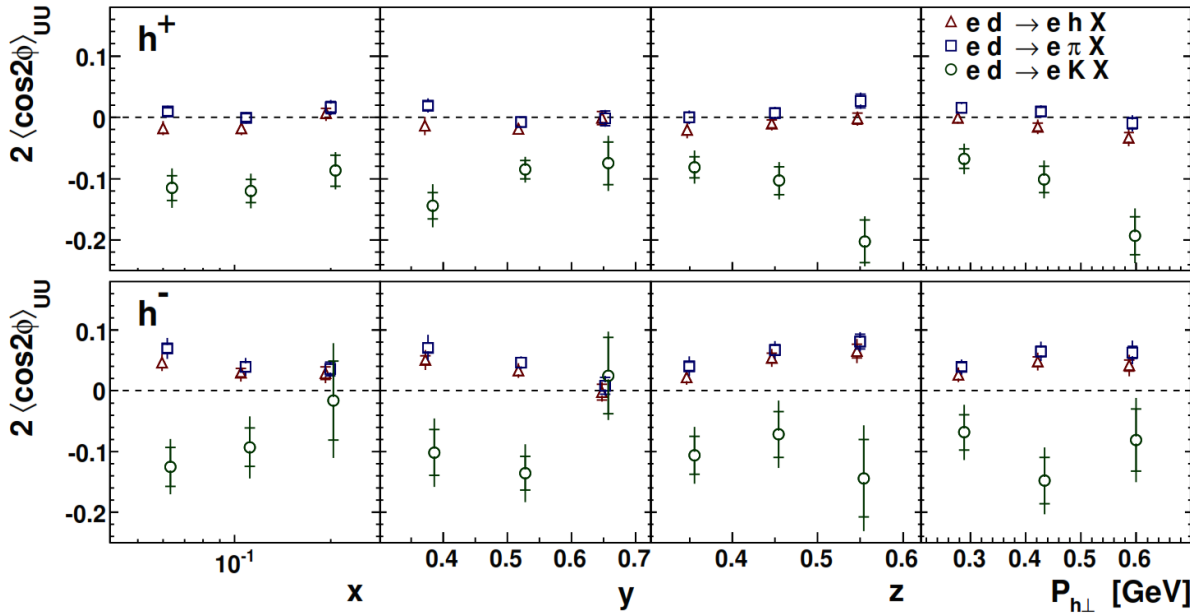
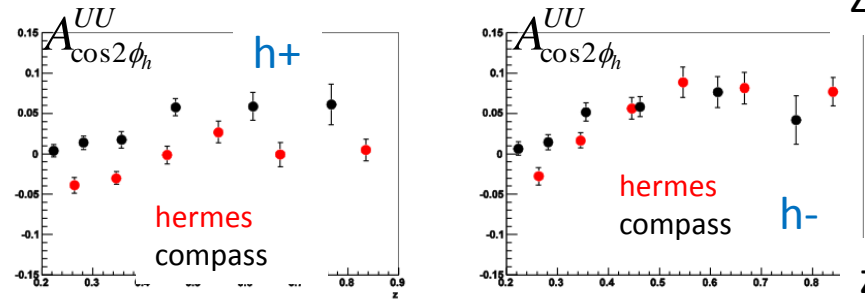




comparison HERMES COMPASS  
in a similar kinematic region



difference for  
pos hadrons not  
well understood yet



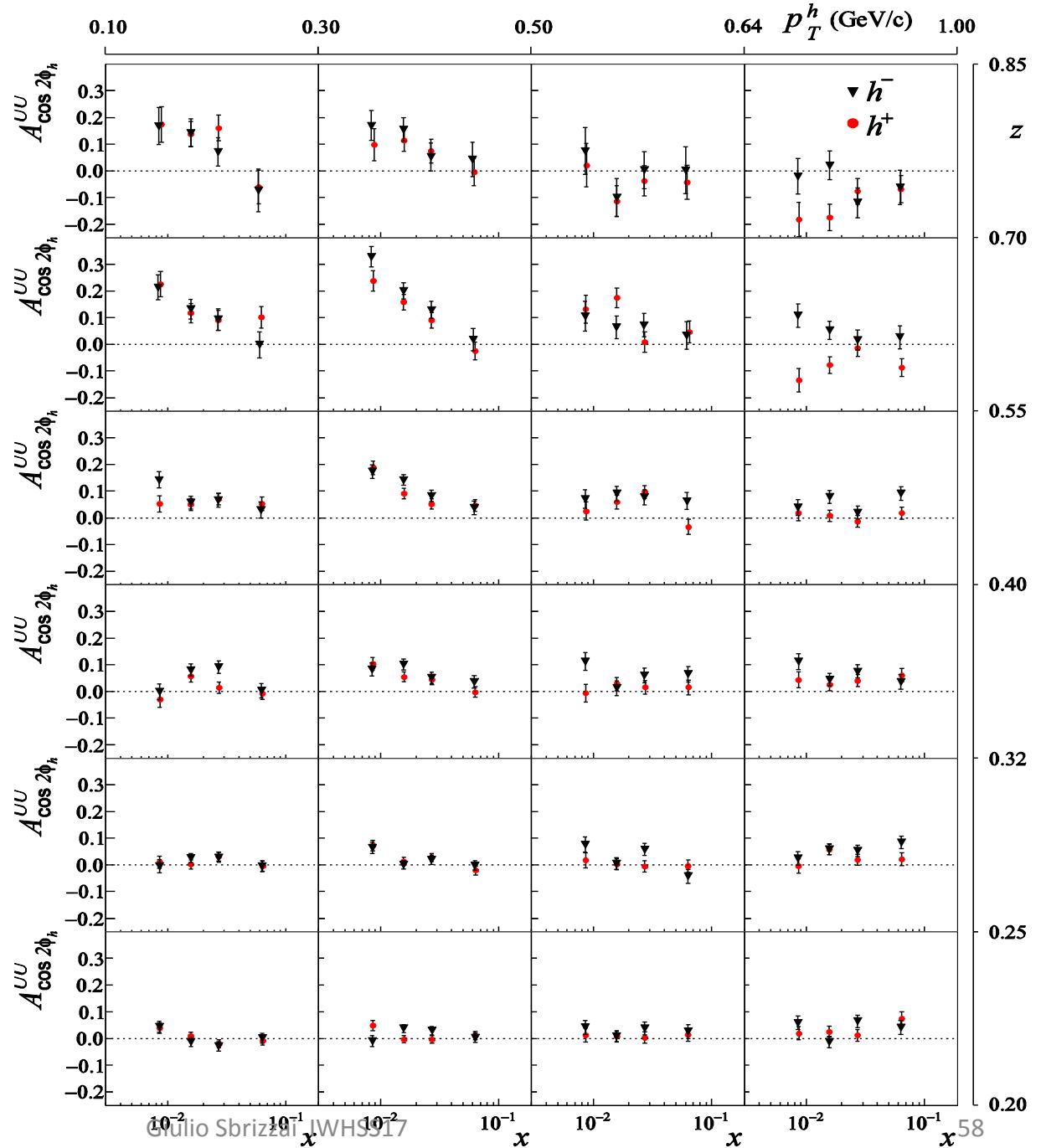
maybe different mixture of  
Kaons and Pions  
in the two experiments...?

# Unpolarised Azimuthal Asymmetries measured from 2004 deuteron data

$$A_{\cos 2\phi_h}^{UU} \approx \frac{1}{Q^2} \text{Cahn} + \text{BM}$$

convoluted with  
the Collins FF

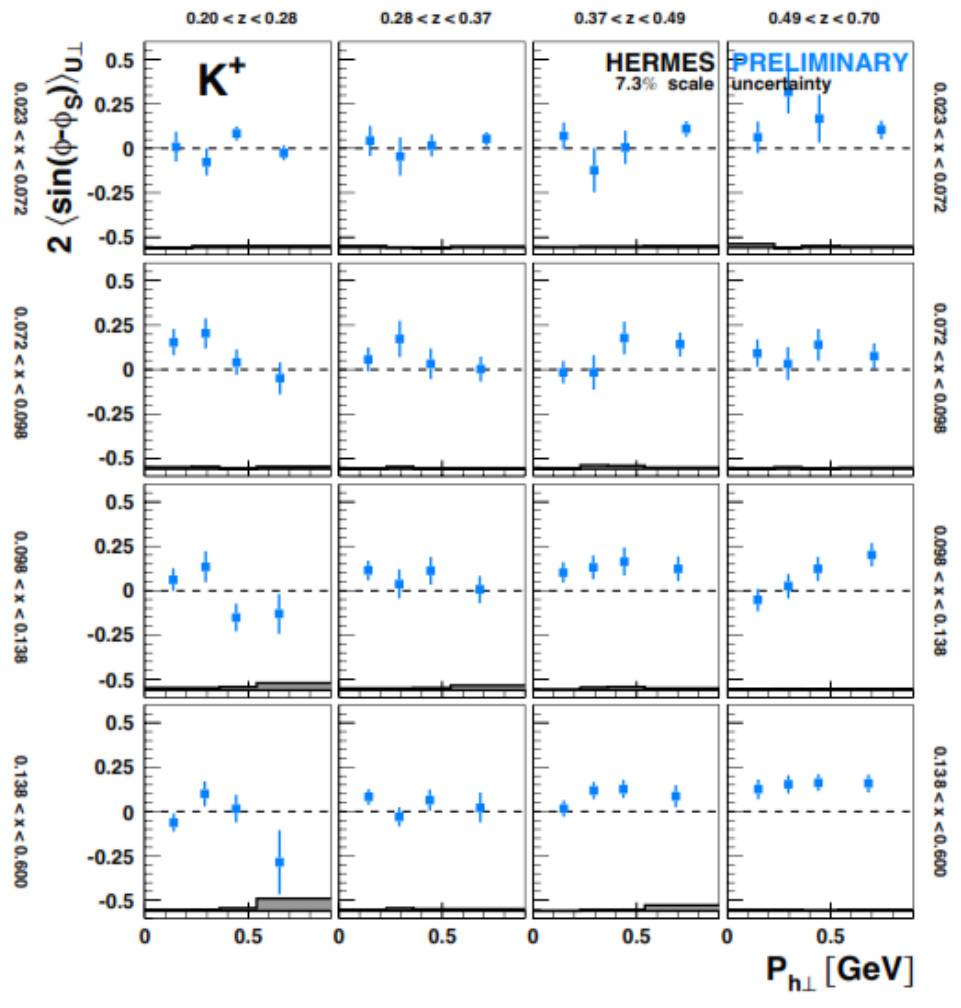
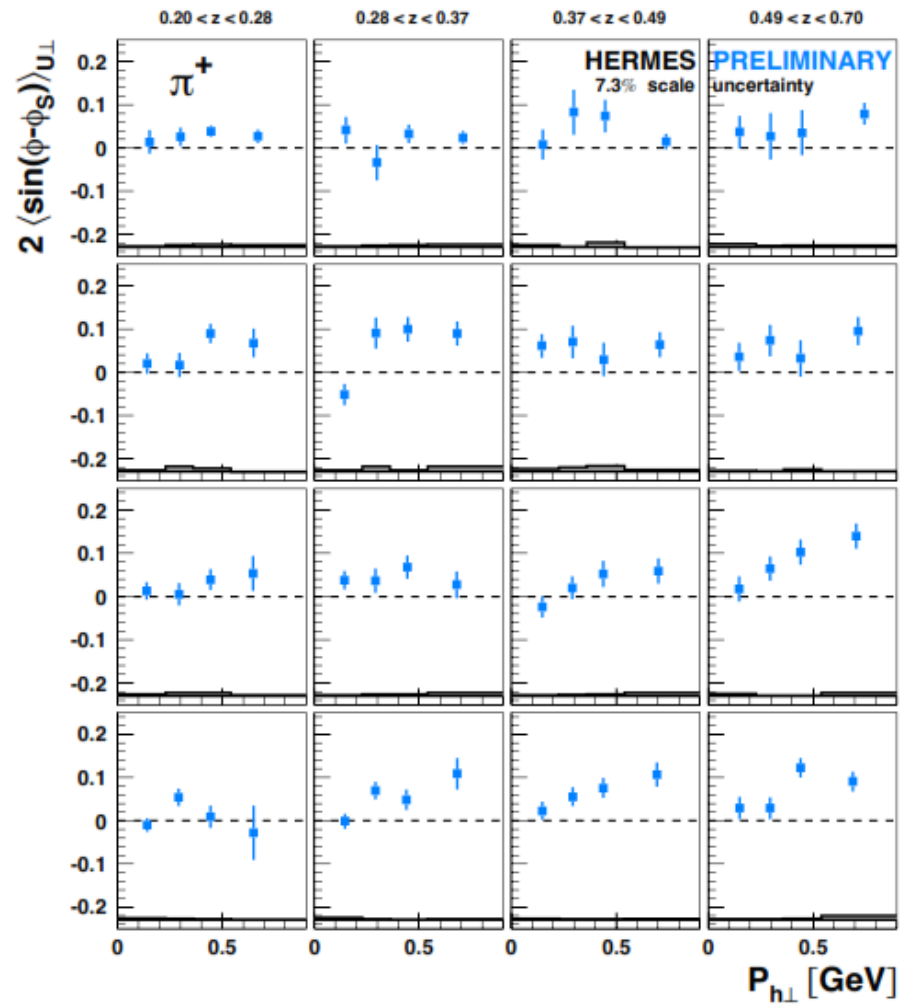
multiD  
performed  
both on  
 $\cos\phi$   
and  $\cos 2\phi$   $\longrightarrow$





# on identified hadrons

Gunar Schnell SPIN 2016



preliminary results produced for all TSA, useful also to compare with 1d results

