

## Bari Theory Xmas Workshop 2016

Dipartimento Interateneo di Fisica Michelangelo Merlin Università degli Studi di Bari Aldo Moro

## Self-propelled droplets through Marangoni Effect

#### F.Fadda, G.Gonnella, A.Lamura (In preparation for *The European Physical Journal E*)

### What is the Marangoni Effect?

The *Marangoni effect* consists in the rise of a force tangential to an interface due to a gradient of surface tension created by anisotropies of temperature (J. of Fluid Mech. 6, 3 (1959)) or surfactant (New J. of Phys. 13 (2011); Soft Matter 10, 7008 (2014)).

Surfactants are examples of tensio-active materials which migrate to the interfaces of systems and have the ability to lower the surface tension there

#### Dynamical equations

$$\mathcal{F} = \int d\mathbf{r} \left[ \frac{a}{2} \phi^2 + \frac{b}{4} \phi^4 + \frac{(B_0 + B_1 c)}{2} (\nabla \phi)^2 + clnc \right]$$
(J. Chem. Phys. **136**, 074904 (2012))

• Continuity equation:

$$\partial_t n + \partial_\alpha (n u_\alpha) = 0$$

• Navier-Stokes equation:

$$\partial_t(nu_{\beta}) + \partial_{\alpha}(nu_{\alpha}u_{\beta}) = -\partial_{\alpha}(P_{\alpha\beta}) + \partial_{\alpha}\{\eta(\partial_{\alpha}u_{\beta} + \partial_{\beta}u_{\alpha} - \delta_{\alpha\beta}\partial_{\gamma}u_{\gamma}) + \zeta\delta_{\alpha\beta}\partial_{\gamma}u_{\gamma}\}$$

• Convection-diffusion equations:

$$\partial_t \phi + \partial_\alpha (u_\alpha \phi) = \nabla^2 \mu$$

$$\partial_t c + \partial_\alpha (u_\alpha c) = \nabla \cdot [Dc \nabla \mu'] - \gamma (c - c_0) + A\Theta(R - |r - r_p|)$$

Simulations performed with hybrid LBM method with cell  $D_2Q_9$ 

### Single self-propelled droplet

(Soft Matter 10, 7008-7022 (2014))



#### Two interacting self-propelled droplets

(J. Fluid Mech. (2016), vol. 806, pp. 205-233)



# Thanks for the attention!!! Merry Christmas and Happy New Year to everybody!!!



