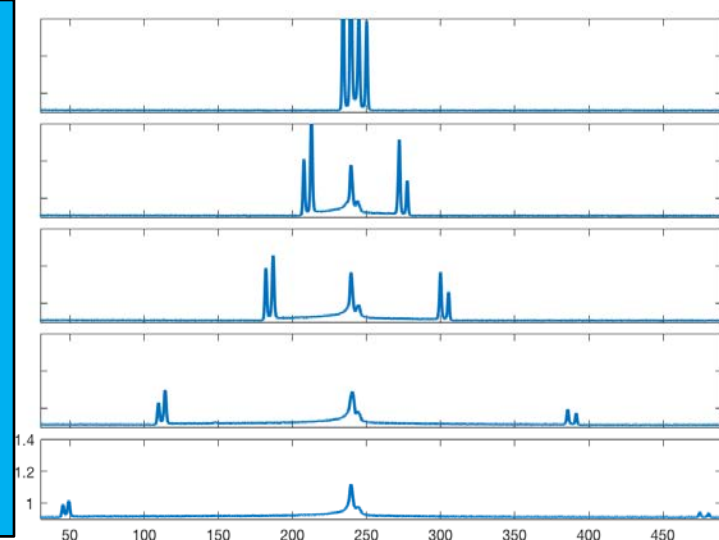
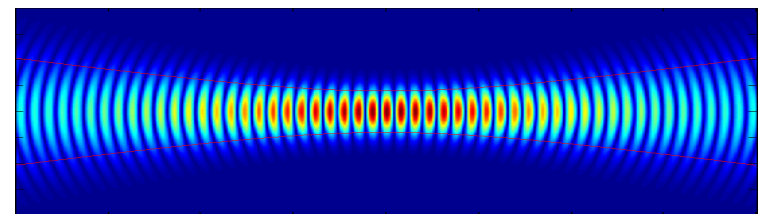


# Precision measurements in fundamental physics



Richard H. Parker,  
Chenghui Yu, Weicheng  
Zhong, Brian Estey, and  
H. Müller



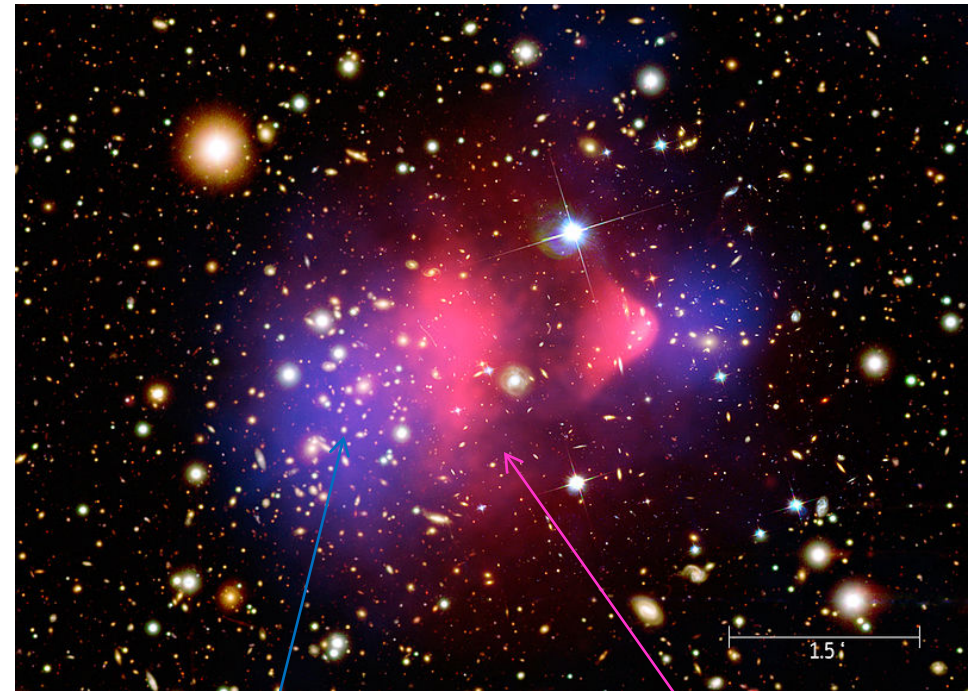
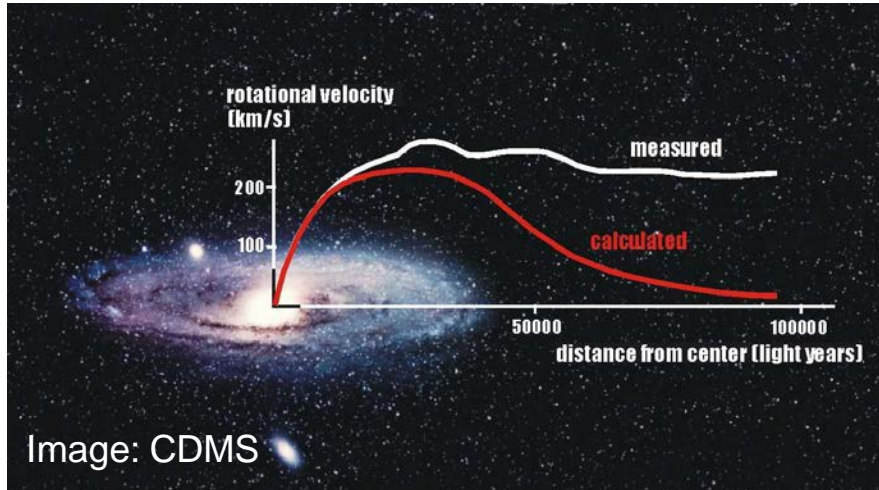
U.C. Berkeley



the David &  
Lucile Packard  
FOUNDATION



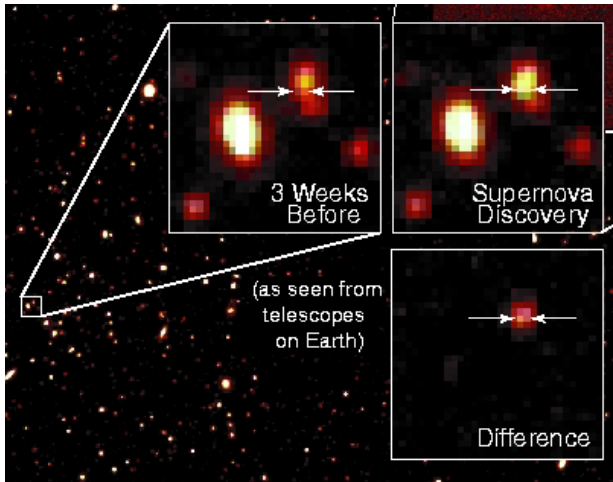
# Dark matter – 23% of all mass



Reconstructed  
mass distribution

Observed  
luminous matter

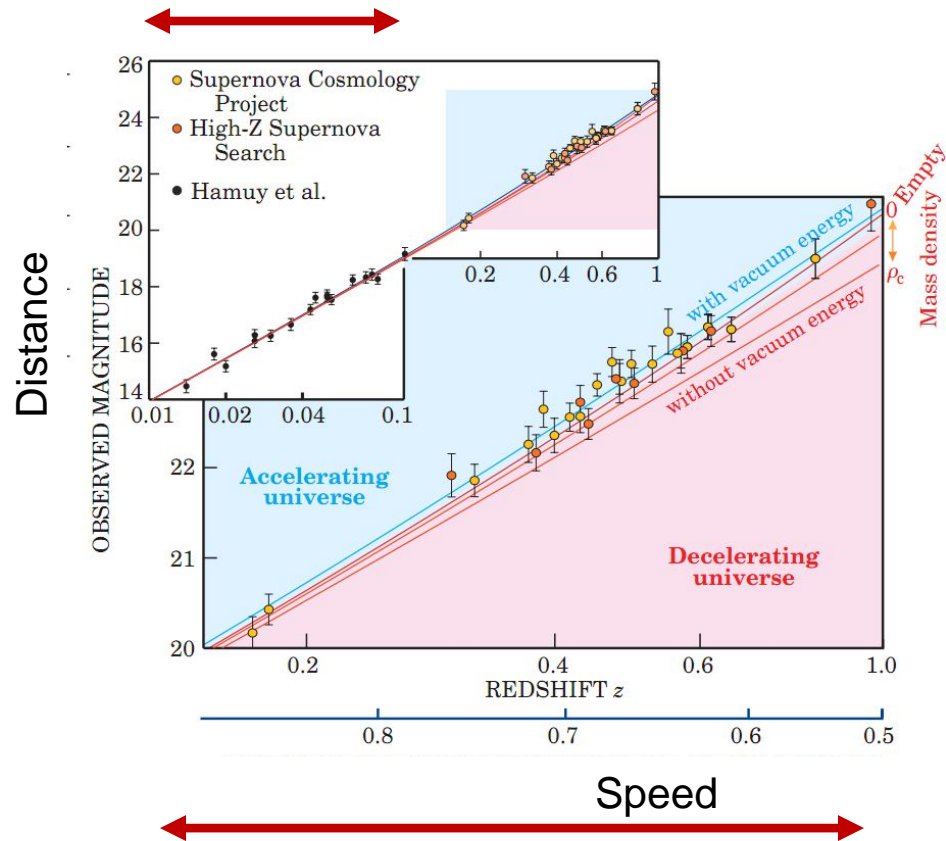
# Dark energy – 73% of all mass



Saul Perlmutter

Brian Schmidt  
Adam Riess

Early 1990's data: nothing special



1998 data:

- 10 times the range
- There may be a discovery behind every order of magnitude.

# The Era of precision uncertainty

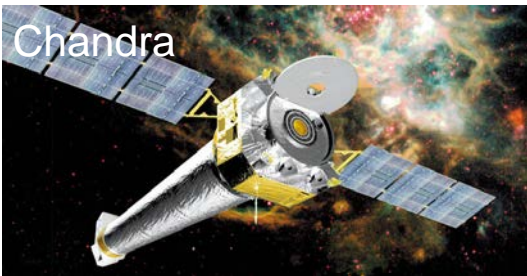
Loud and clear signals from the skies....

...but silence in our detectors

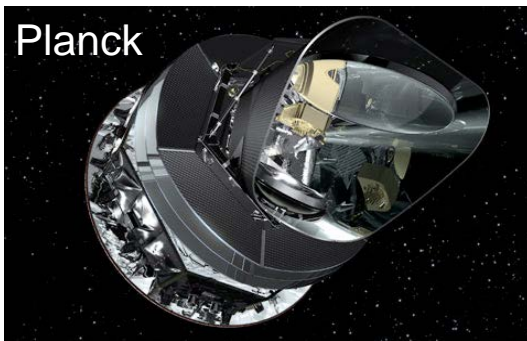
W.M. Keck Observatory



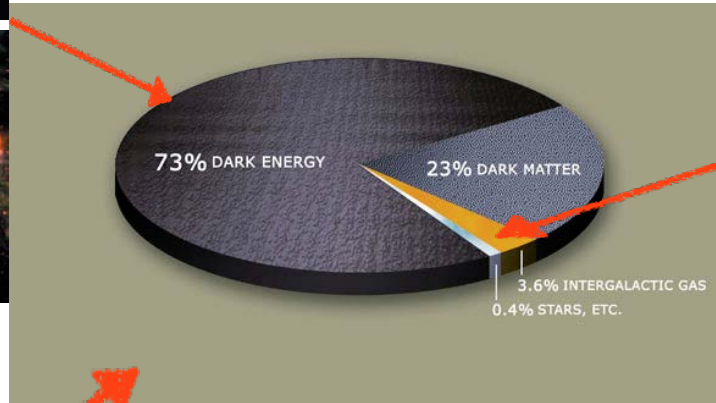
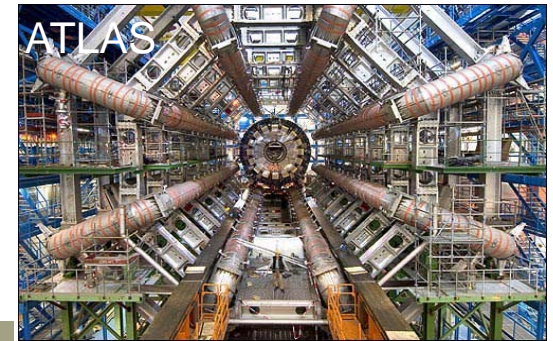
Chandra



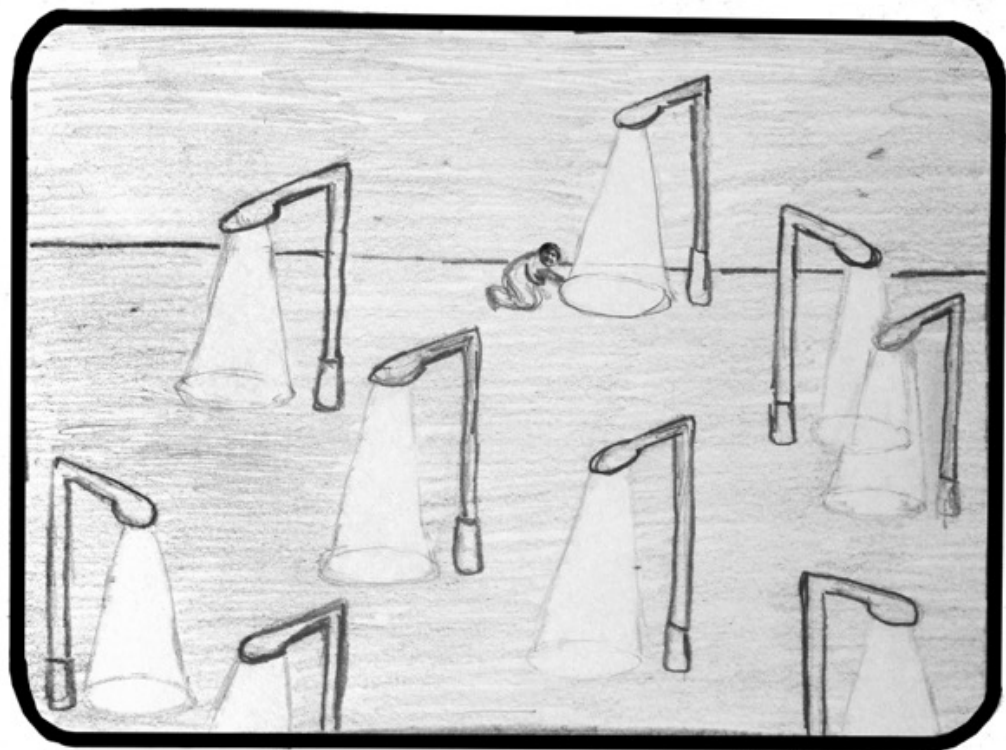
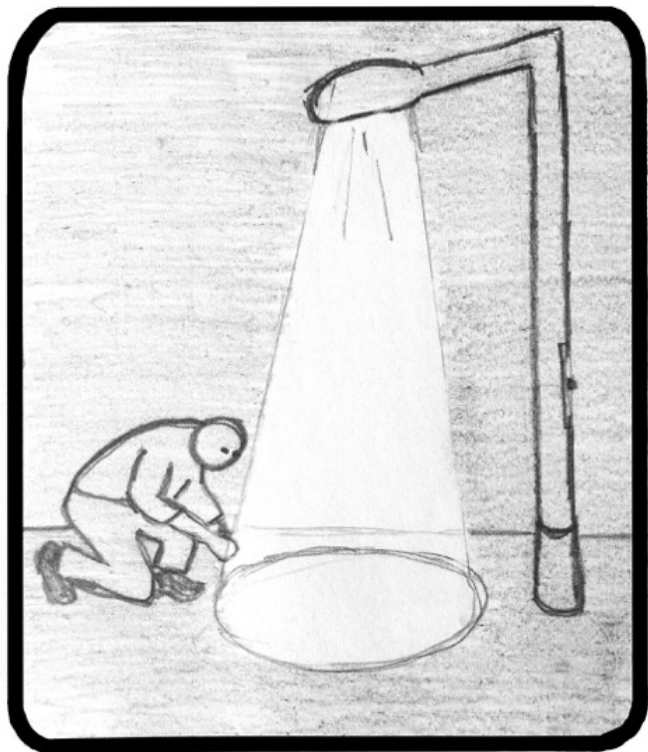
Planck



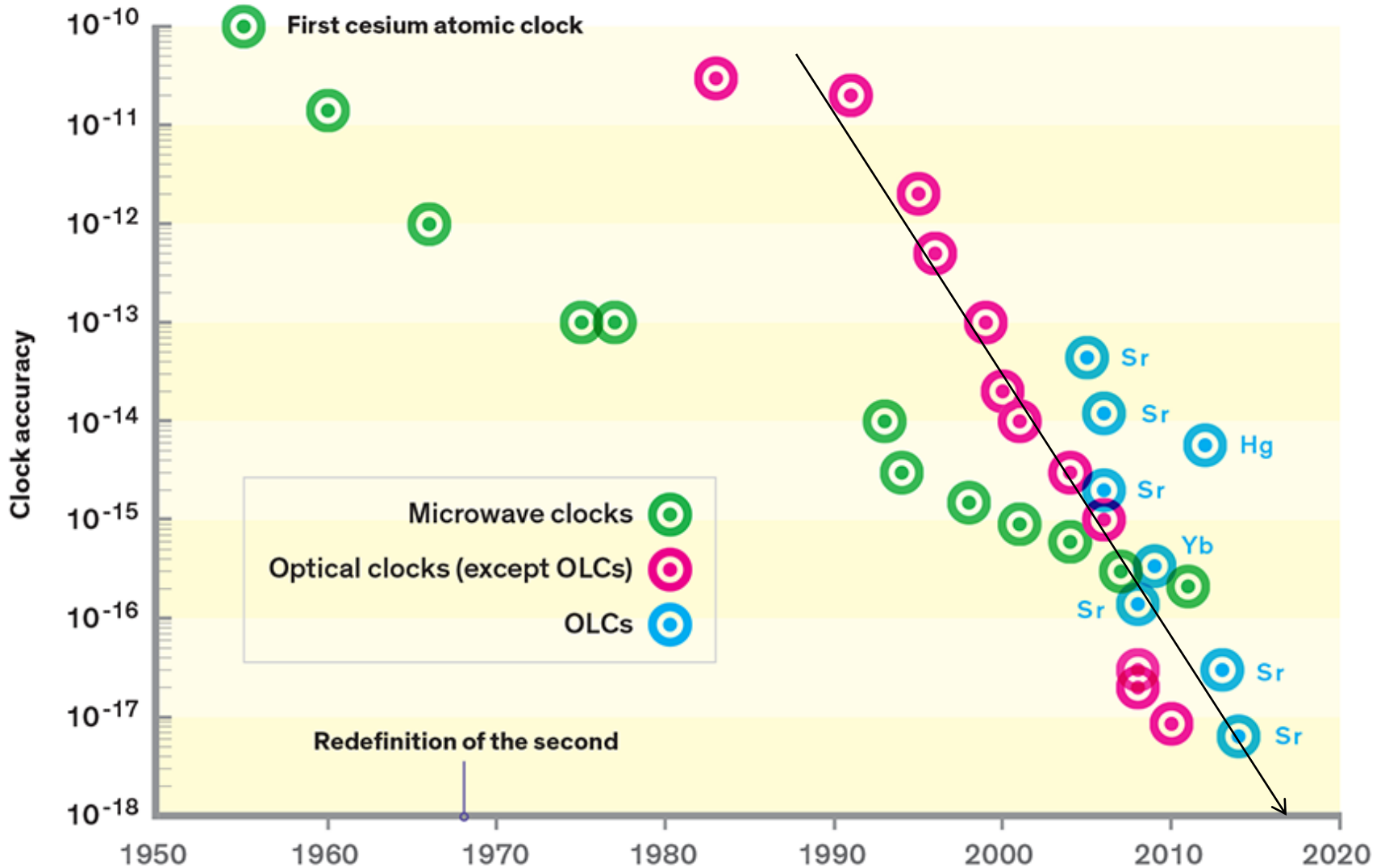
The LHC...THE particle physics experiment



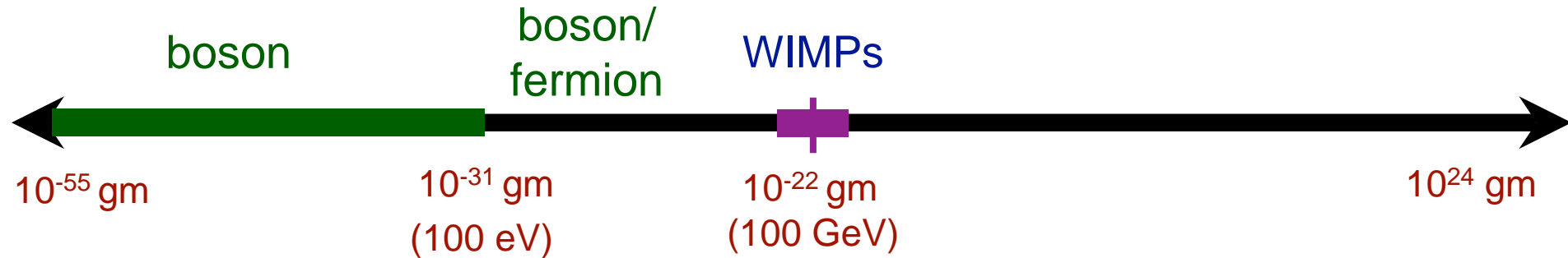
Dark matter detectors



# Moore's law in atomic physics



# The precision frontier



- (Ultra-) light particles are easy to generate, but hard to see.
- Collective forces from a large number of particles
- Forces are the fundamental effect of light particles
- Ultra-sensitive detectors required



# How to best sense the light dark sector

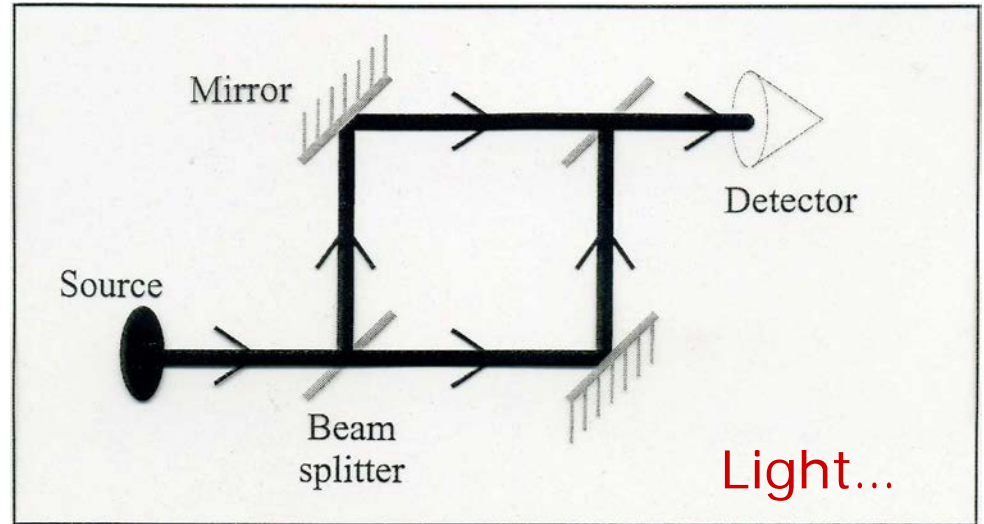
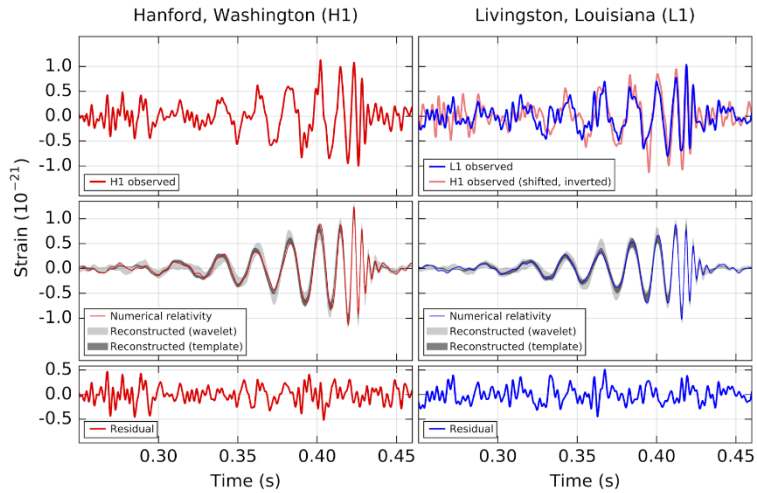
## **Need test particles that are**

- Well understood,
- Light, neutral
- ...and whose motion can be measured with extreme precision

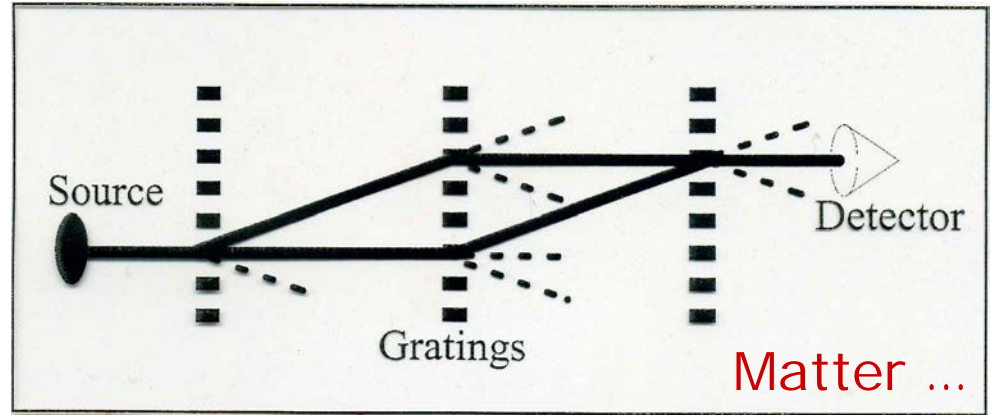
⇒ Interferometry with laser-cooled atoms



# Interferometry...

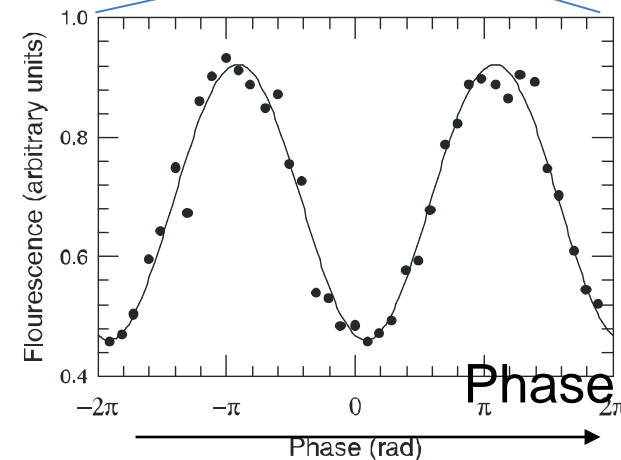
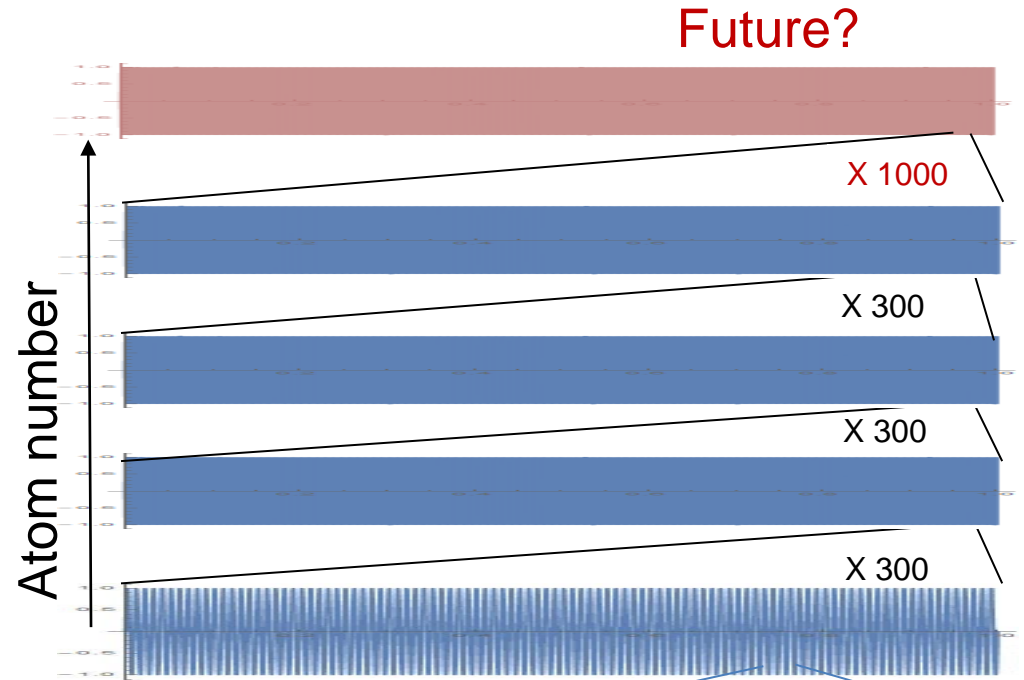
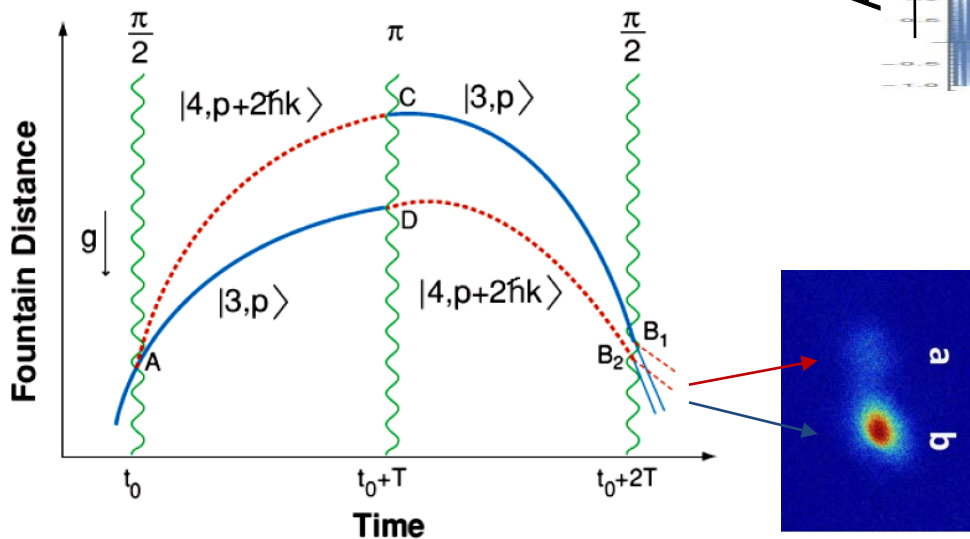


$$\lambda = \frac{h}{mv}$$

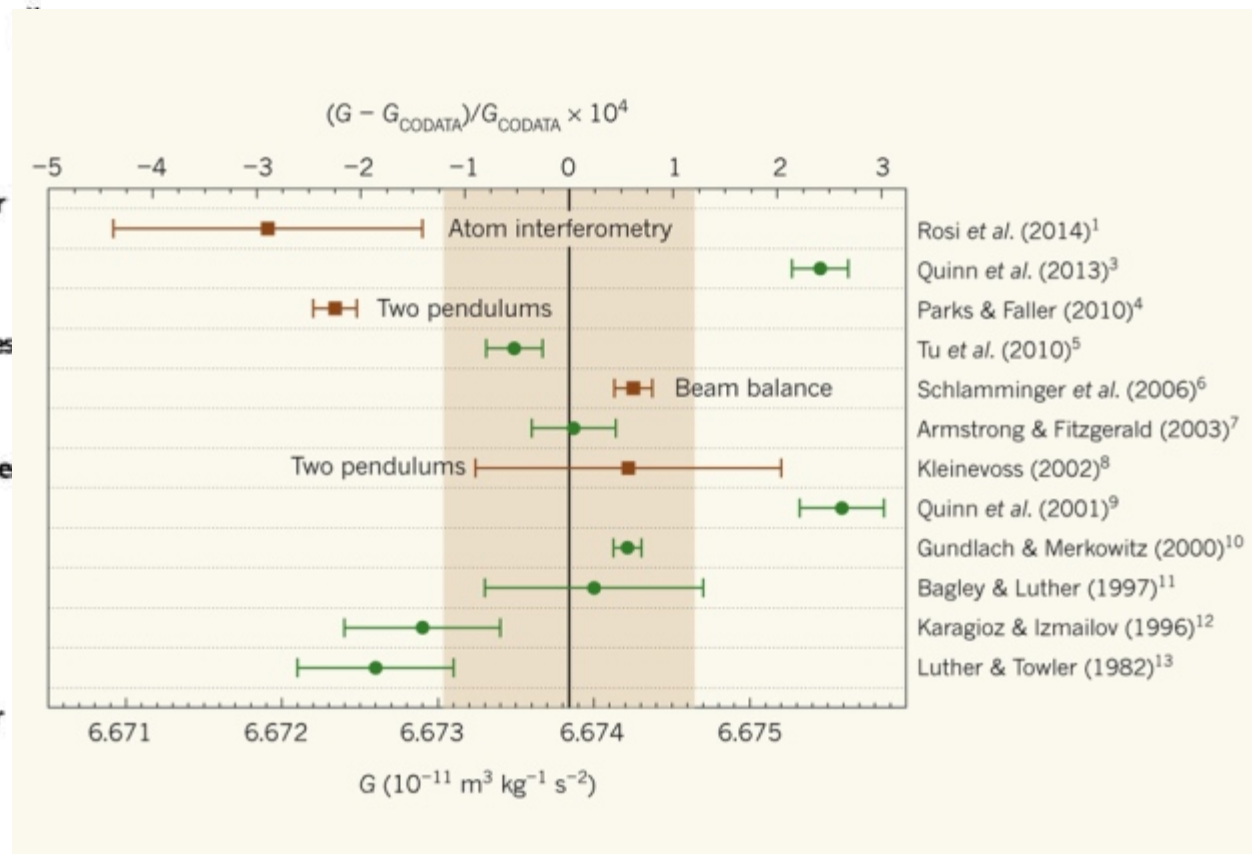
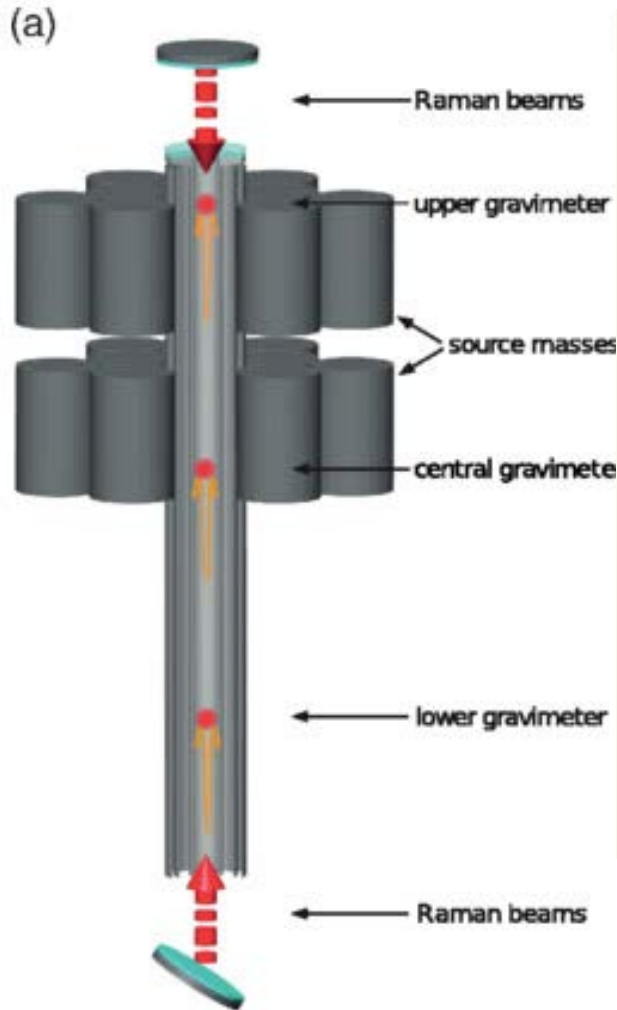


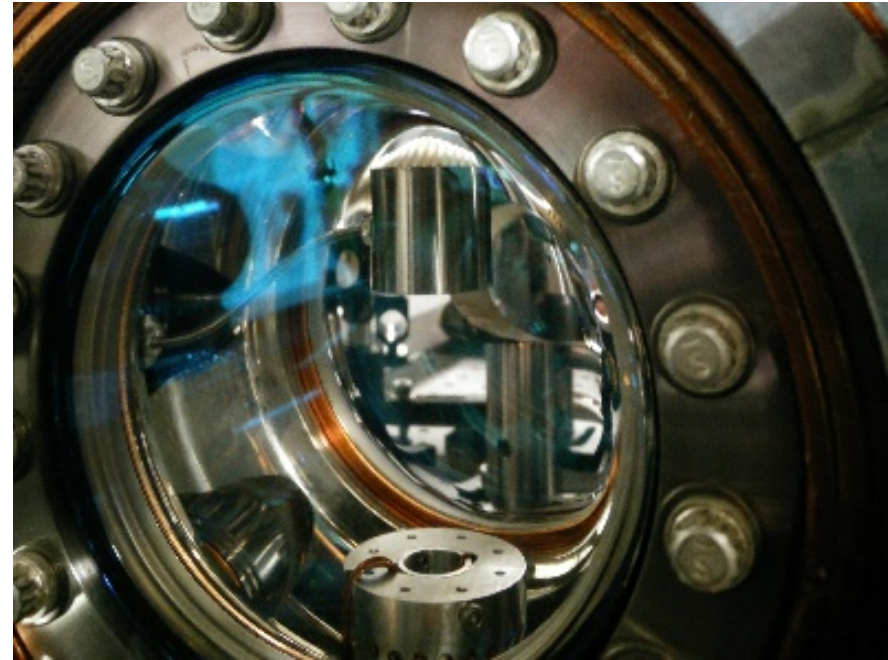
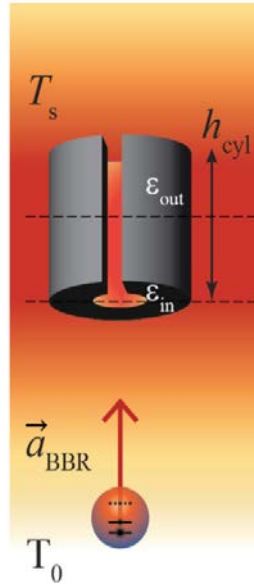
# Light pulse atom interferometer

- Particles / waves
- Forces from the dark sector change deBroglie wavelength
- Laser wavelength as a ruler



# Precision measurement: G



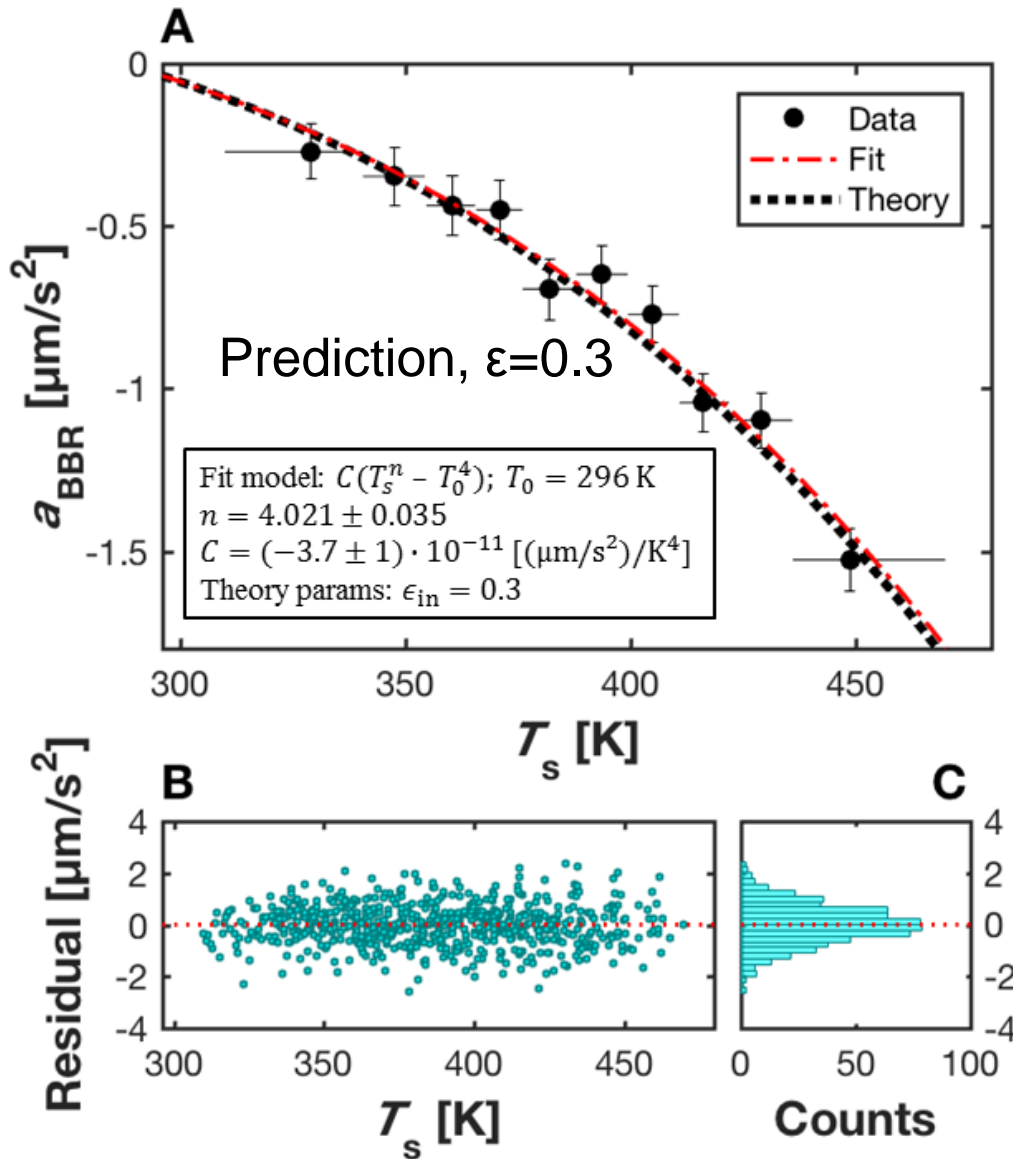


# Attractive force from blackbody radiation

P. Haslinger, M. Jaffe, V. Xu, M. Sonnleithner, H. Ritsch, M. Ritsch & HM

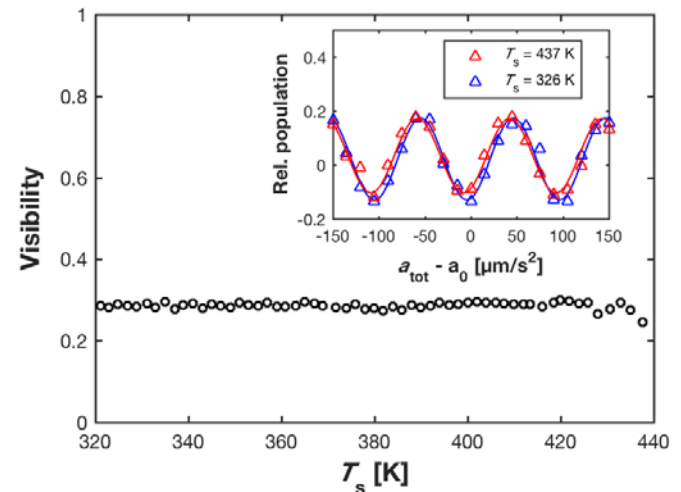
Only one room temp. blackbody photon absorbed every  $10^5$  years...

# Measurement

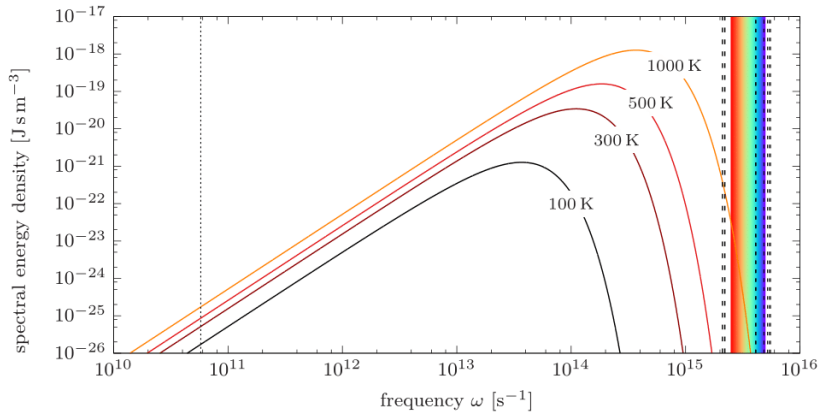


## Systematic Effects Ruled Out:

- Pressure from outgassing (opposite sign,  $\exp(T)$ -dependence, loss of coherence)
- Constant AC Stark effects (e.g., would cancel between interferometer arms)

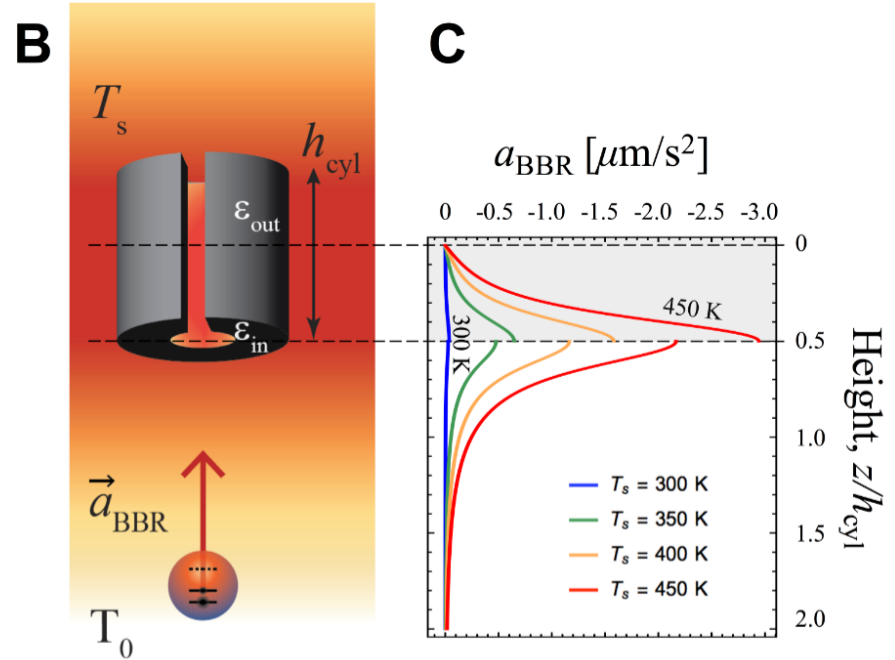


# Theory

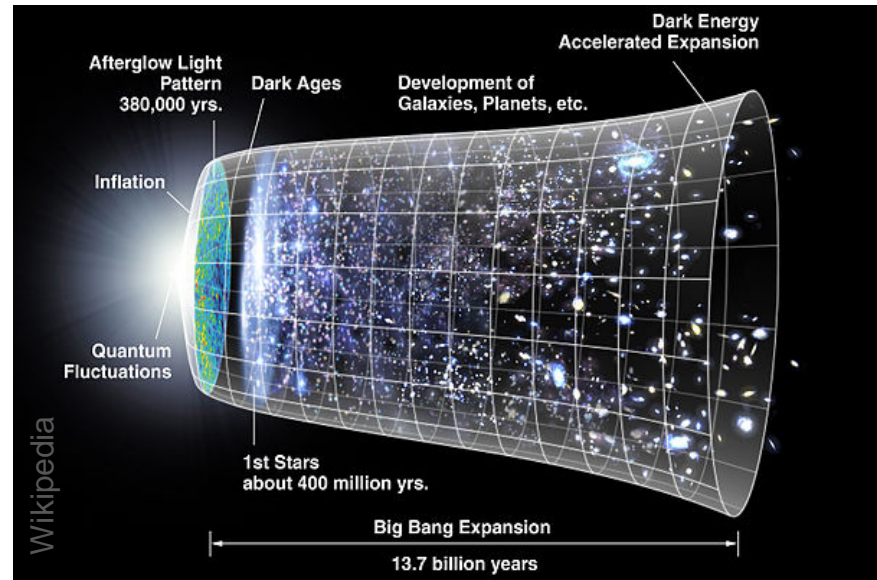


$$\Delta E_0 = -2 \frac{\alpha_{CS} \sigma T_s^4}{c \epsilon_0},$$

$$a = -\alpha_{CS} \frac{\sigma(T_s^4 - T_0^4)}{c \epsilon_0 m_{CS}} \frac{R^2}{r^3}.$$



- Absorptivity  $\alpha$  and emissivity  $\epsilon = \alpha = 0.35 \pm 0.05$  (measured)
- Source and ambient radiation
- Reflections

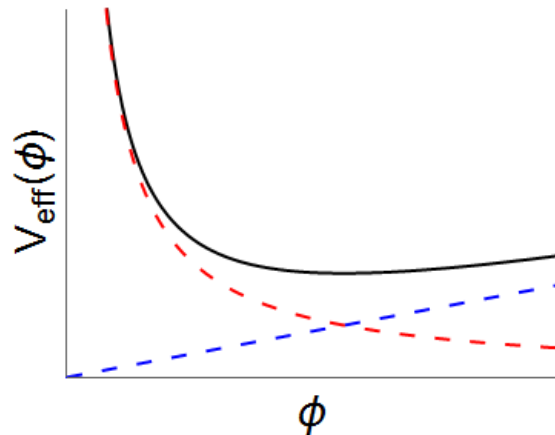


# Dark energy scalar fields

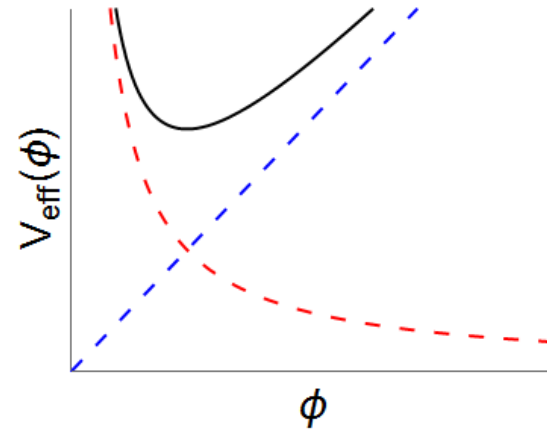
M. Jaffe, P. Haslinger, V. Xu, J. Khoury, B. Elder, M. Upadhye and H. Muller

# Screened DE-matter-coupling

Low density (vacuum)  
Light, long-ranged field

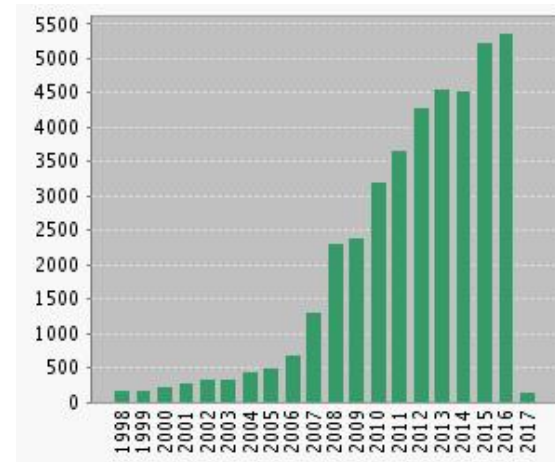


High density (in matter)  
Heavy, short-ranged



- Quintessence can be light in space, yet evade detection
- Chameleons,  $f(R)$ , symmetrons,...
- **Good fit for dark energy, challenging to rule out**

Citations/year



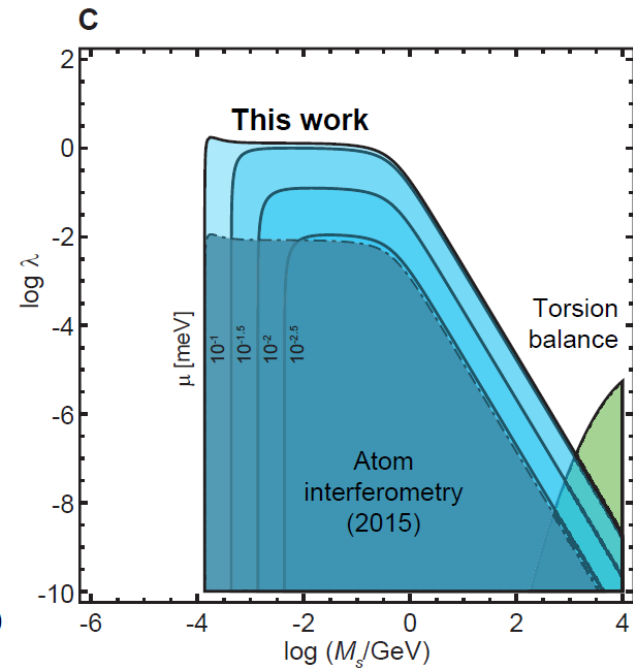
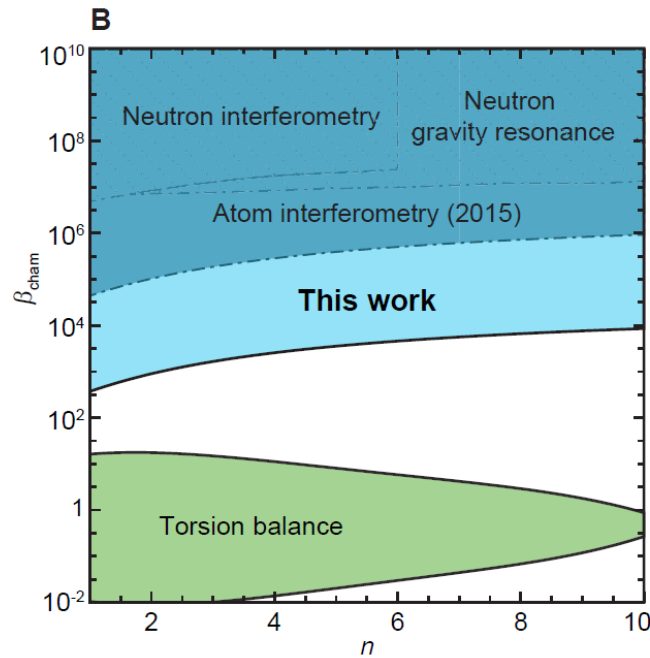
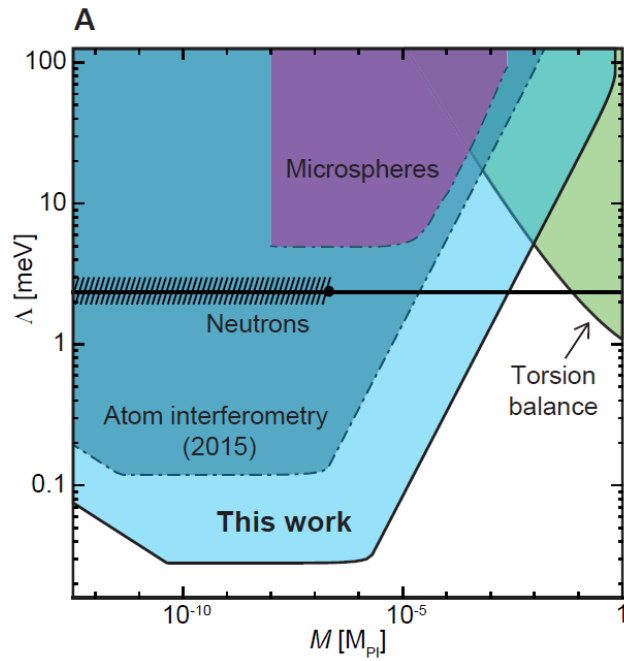




# Limits on dark-energy scalars

## Chameleons

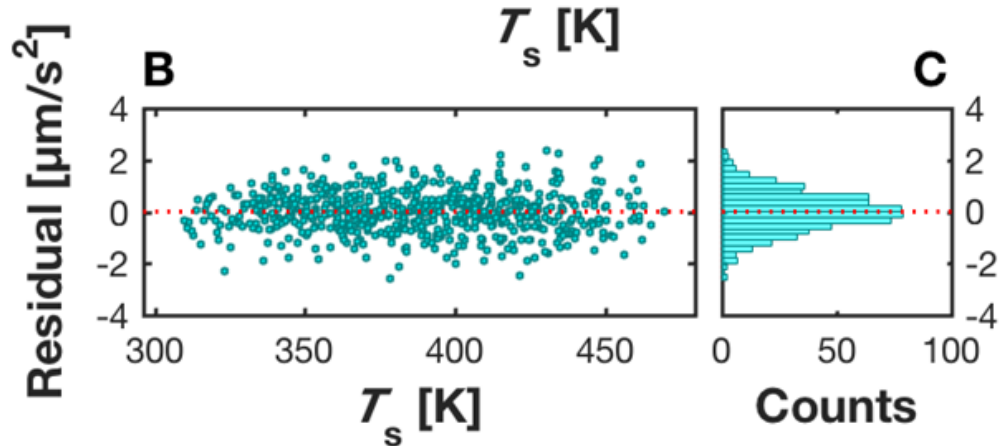
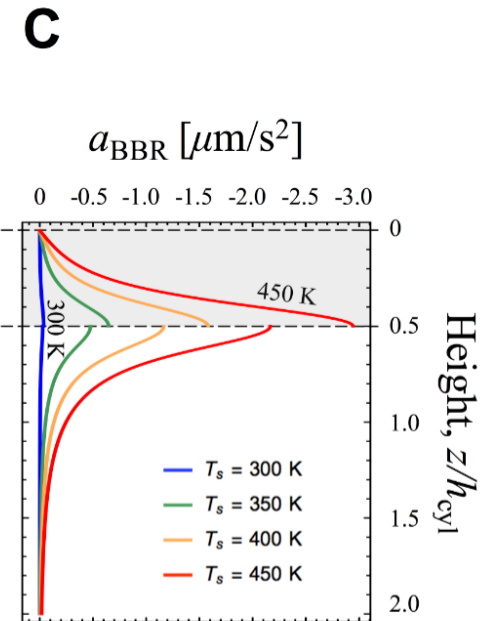
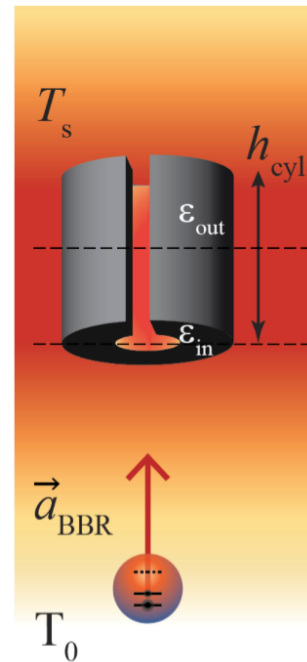
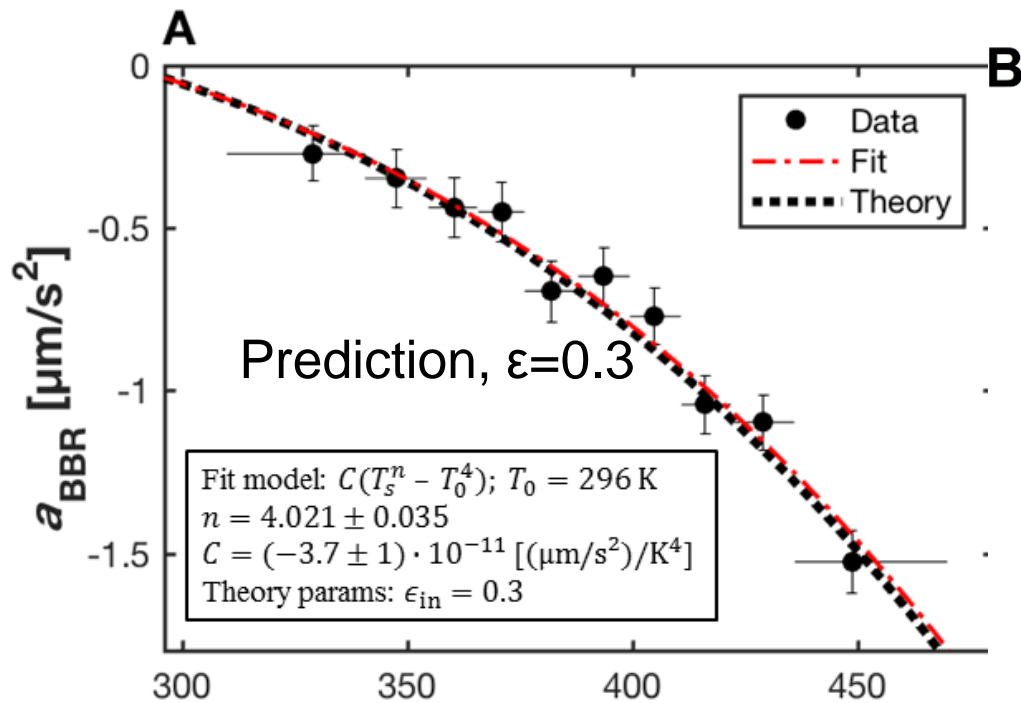
## Symmetrons



Interaction strength

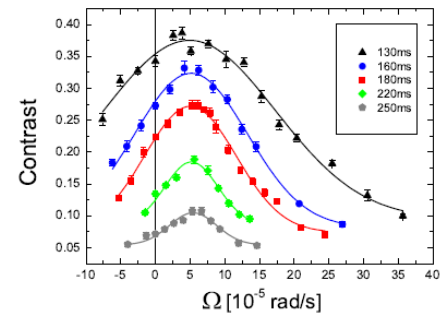
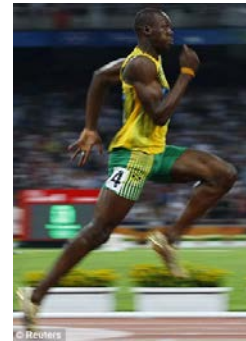
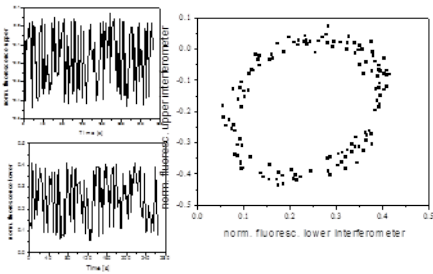
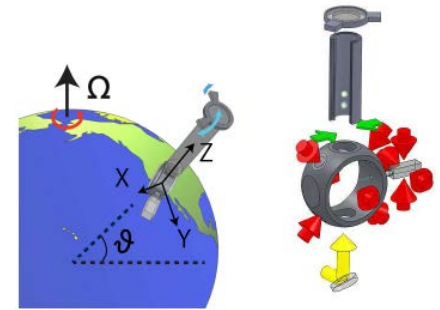
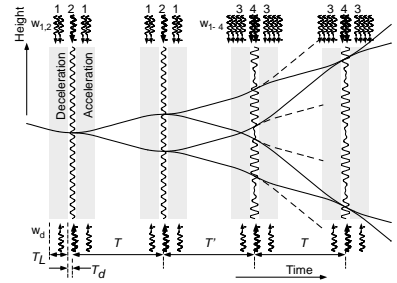
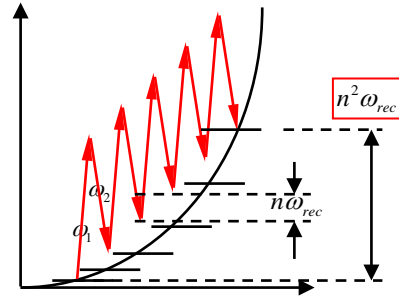
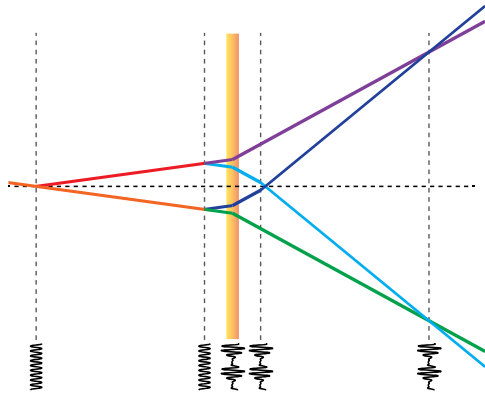
M. Jaffe, P. Haslinger, V. Xu, P. Hamilton, A. Upadhye, B. Elder, J. Khoury, and HM, [Nature Physics](https://doi.org/10.1038/nphys4189), doi: 10.1038/nphys4189

# Force from blackbody radiation



arXiv:1704.03577

# Technology



## Noise rejection

- 2,500 fold gain in sensitivity
- Now used by the Biraben group, LKB Paris
- Chiow et al., PRL 2009

## Multiphoton Bragg diffraction

- Up to 24 photon kicks
- Now used, e.g., at Stanford, Western Australia, Paris, ...
- H.M. et al, PRL 2008

## Optical lattice beam splitter

- Up to 800 photon kicks: record!
- H.M. PRL 2009, Parker, PRL 2015; Estey, PRL 2014

## Coriolis compensation

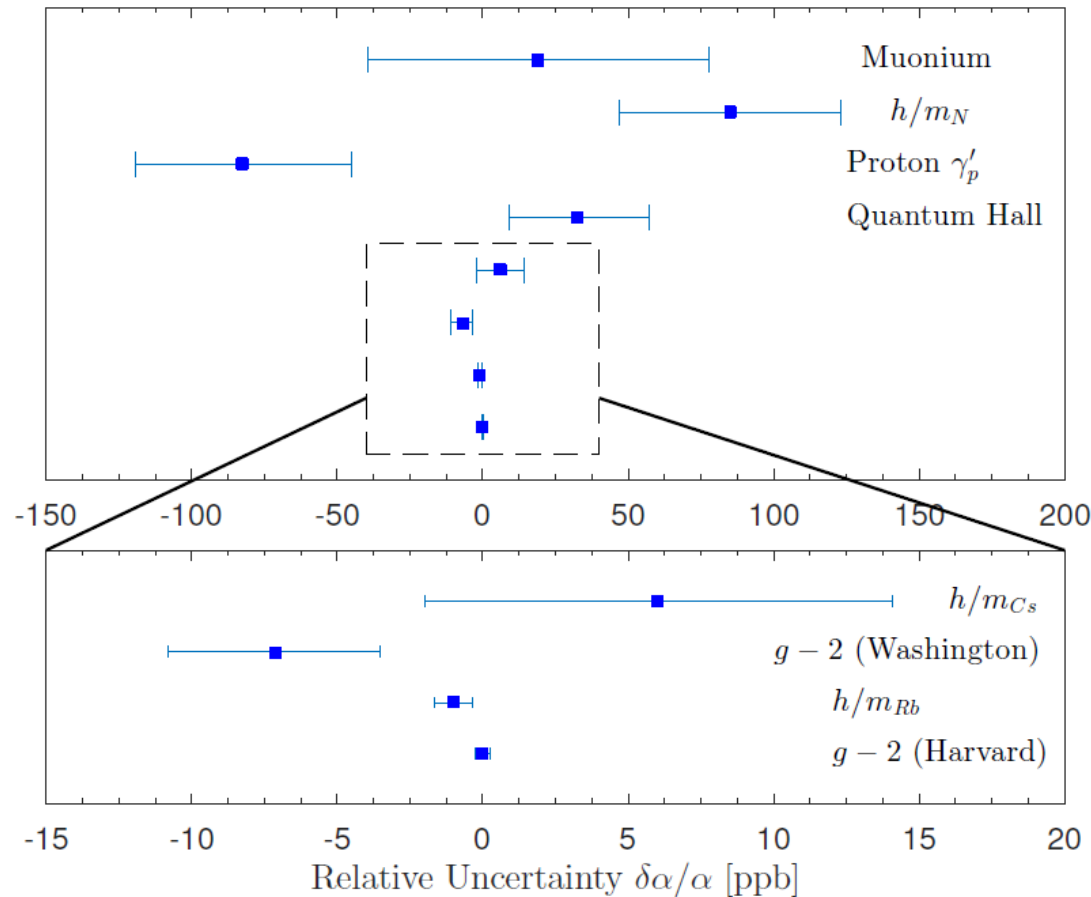
- Needed in world's most sensitive interferometers
- Now used, e.g., at Stanford
- Lan et al., PRL 2012

Fine structure constant

# The Fine Structure Constant

Measures the strength of the electromagnetic interaction

$$\alpha = \frac{1}{4\pi\epsilon_0} \frac{e^2}{\hbar c} = \frac{1}{137.035999139(31)} \quad (0.23\text{ppb}) \quad 2014 \text{ CODATA}$$





# Fine Structure Constant

## Current Status of $\alpha$

Electron's magnetic moment anomaly  $g-2$  : 0.37 ppb

D. Hanneke *et al.* PRL **100**, 120801 (2008 )

$$\frac{g}{2} = 1 + C_2 \left( \frac{\alpha}{\pi} \right) + C_4 \left( \frac{\alpha}{\pi} \right)^2 + C_6 \left( \frac{\alpha}{\pi} \right)^3 + C_8 \left( \frac{\alpha}{\pi} \right)^4 + \dots + a_{\mu,\tau} + a_{\text{hadronic}} + a_{\text{weak}}$$

Photon Recoil Measurement (Rb) : 4.6 ppb M. Cadoret *et al.* PRL **101**, 230801 (2008)

Photon Recoil Measurement (Cs) : 7.4 ppb A. Wicht *et al.*, Phys. Scr. T **102**, 82 (2002).



# Alpha in Atom Recoil Frequency

$$\alpha = \left[ 2 \frac{R_\infty}{c} \frac{u}{m_e} \frac{M}{u} \frac{h}{M} \right]^{1/2}$$

Rydberg Constant

0.007 ppb P. J. Mohr *et al.*,  
Rev. Mod. Phys. **80**, 633 (2008).

Cs mass in u

0.18ppb M. P. Bradley *et al.*, Phys. Rev.  
Lett. **83**, 4510 (1999).

Determined by the atom recoil  
frequency

Electron mass in atomic mass units u

0.43 ppb P. J. Mohr *et al.*, Rev. Mod. Phys. **80**, 633 (2008).

$$\frac{h}{M} = \frac{4\pi c^2 \omega_r}{\omega^2}$$

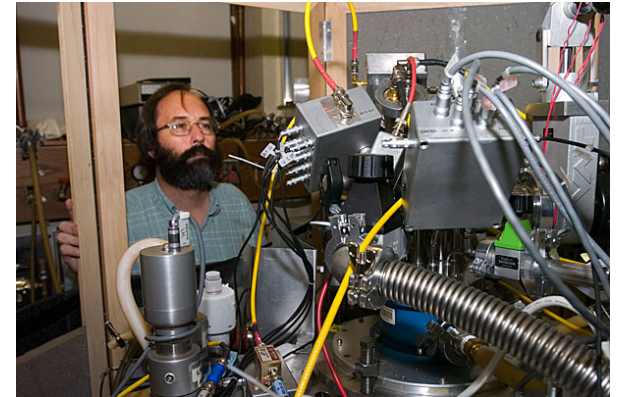
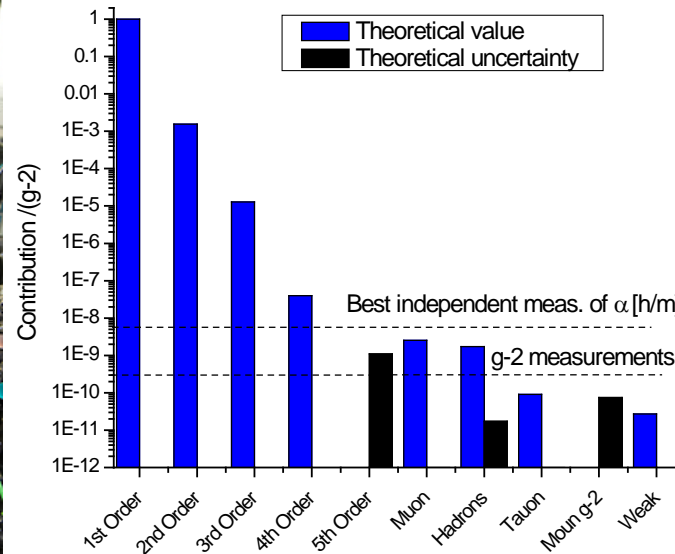
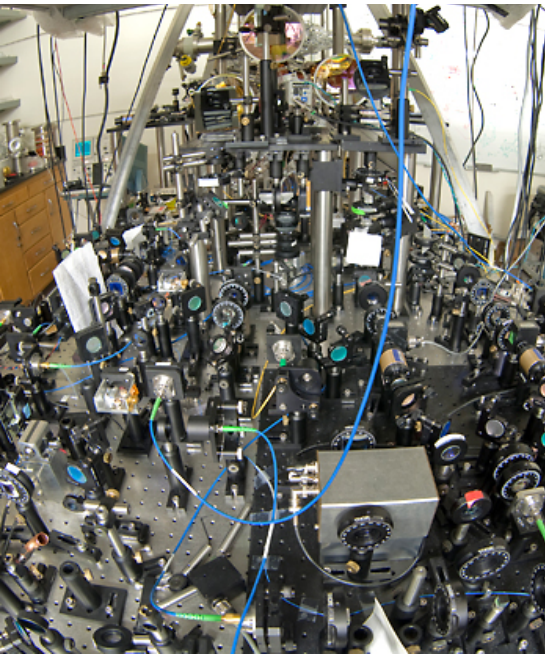
Lowest : 0.23ppb

Cs D2 Transition  
0.015ppb

# The most precise theory/experiment comparison in science

Fine structure constant

Electron gyromagnetic moment

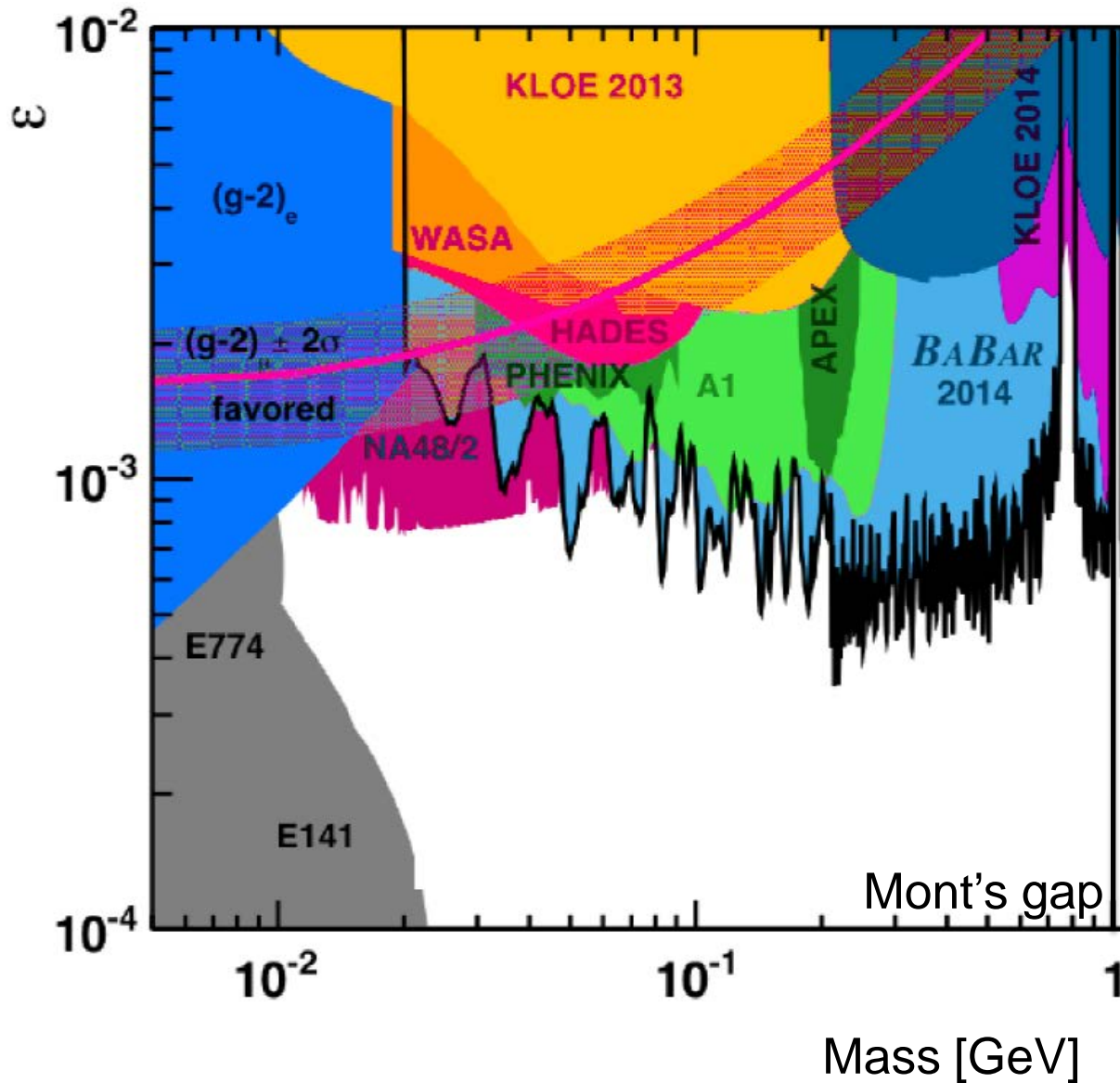


Dark photons shift magnetic moment versus fine structure constant

Measures how strong a magnet an electron is



# Dark photons limits



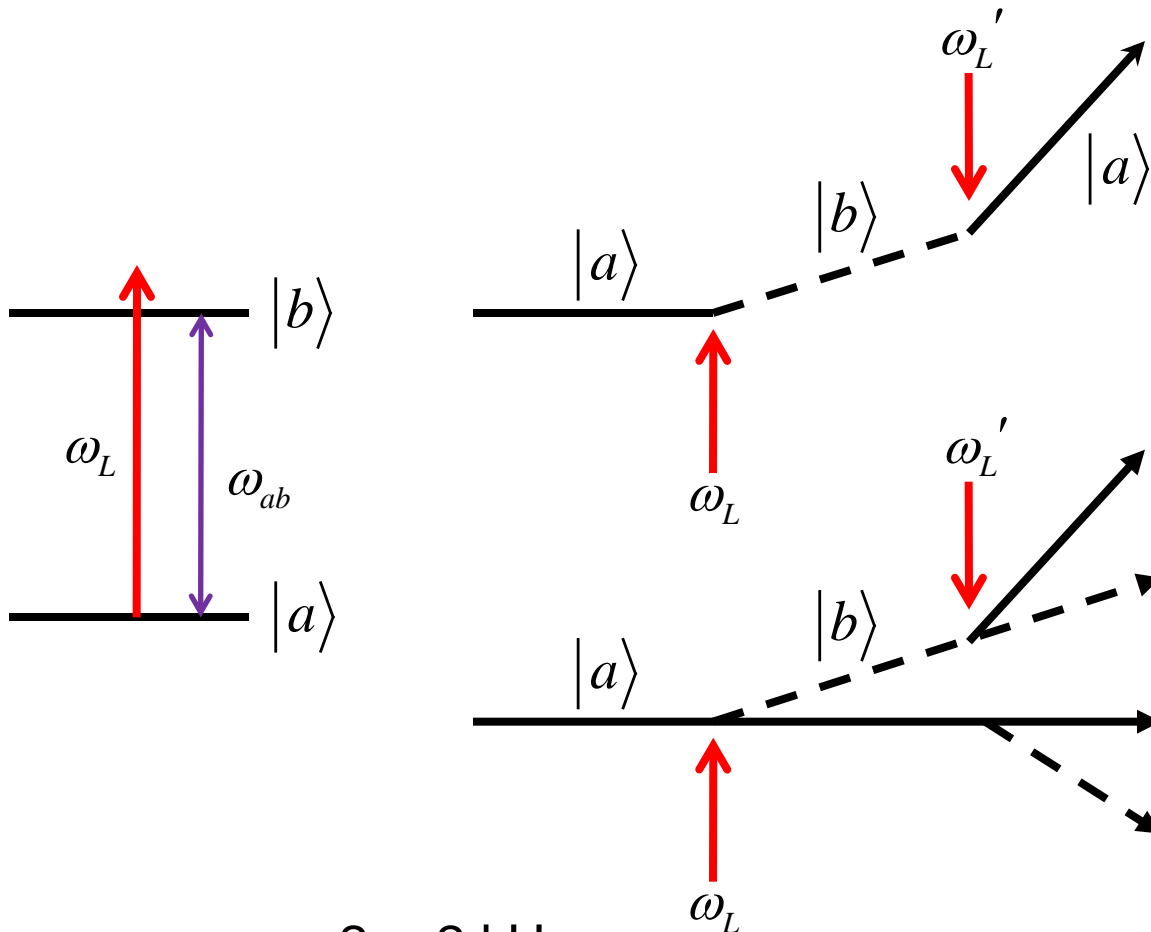
# Impact

- Most precise measurement of the fine structure constant
- Confirms the most precise prediction in all of science
- Search dark photons beyond the reach of colliders
  - Detection: first new particle after Higgs, potentially opening up portal to even more dark sector particles
  - Exclusion would free up enormous resources in collider labs
- First atom interferometer to control systematic errors at  $10^{-12}$  level

Principle



# Photon Recoil Measurement

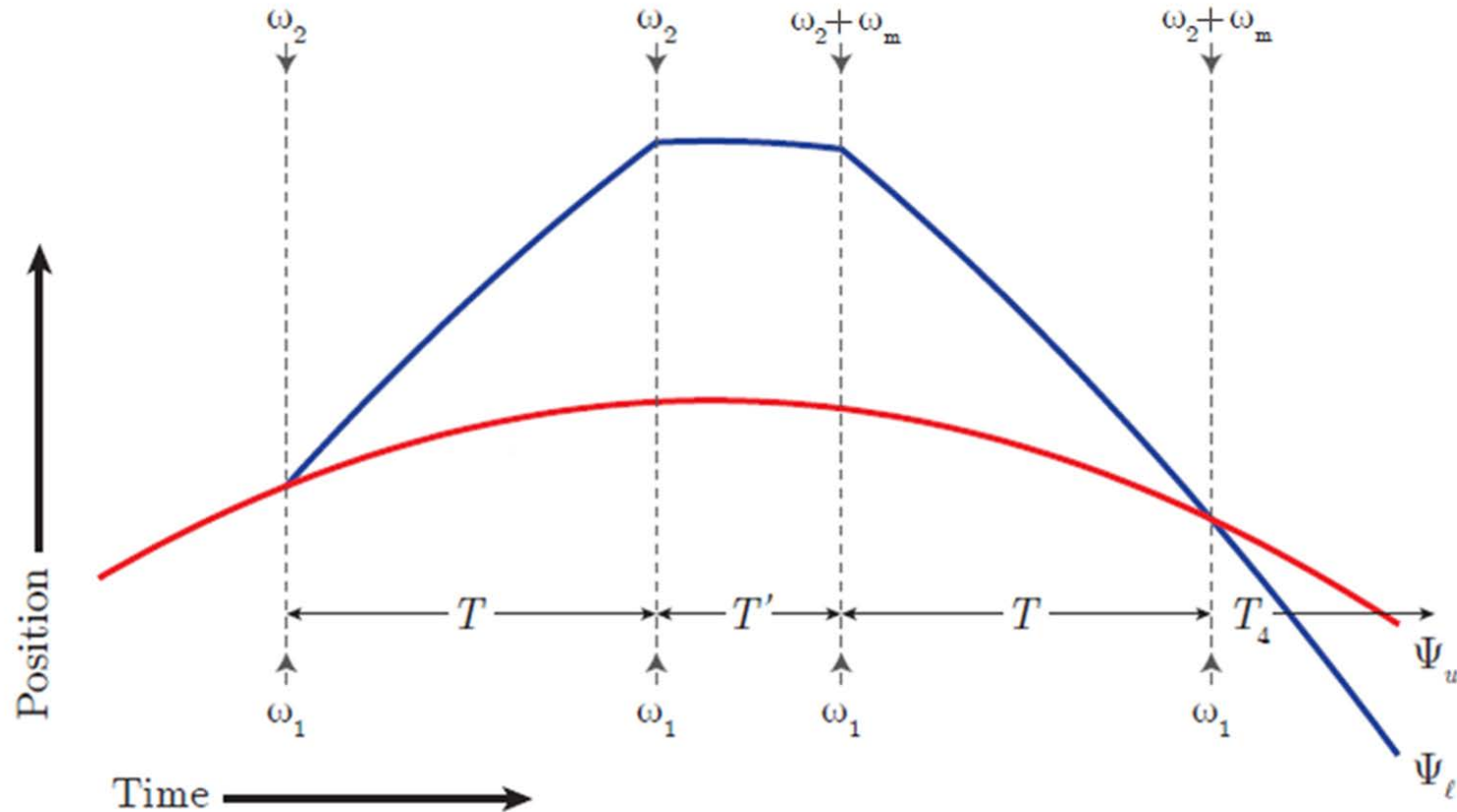


$$\omega'_L(|a\rangle) - \omega'_L(|b\rangle) = 2\omega_{rec}$$

- $\omega r \sim 2\pi \times 2$  kHz,
- Accuracy  $10^{-10}$
- Need to pinpoint resonance to  $0.2 \mu\text{Hz}$  or  $6 \times 10^{-22}$
- 10,000 times better accuracy than precision of best clocks

# Atom-interferometer measurement of $\alpha$

## Ramsey-Bordé Interferometer

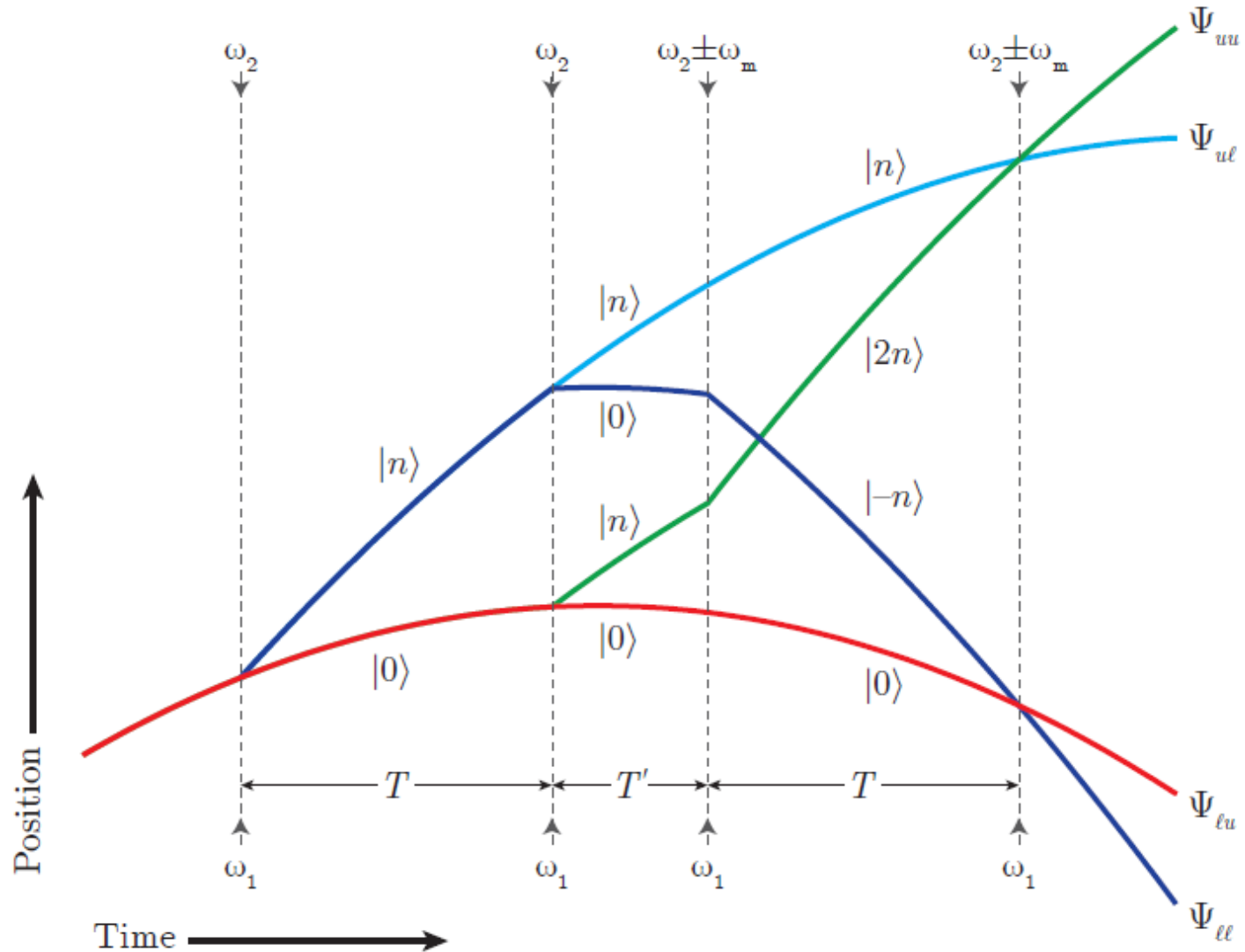


$$\Phi_{RB} = 8n^2 \omega_r T - 2nkg(T + T')T - n\omega_m T$$

$$\frac{1}{2}mv_r^2 = \hbar \left( \frac{\hbar k^2}{2m} \right) = \hbar \omega_r$$

$\omega_r$	$\rightarrow$	$\hbar/m$	$\rightarrow$	$\alpha$
$k$	$\rightarrow$	$\hbar/m$	$\rightarrow$	$\alpha$

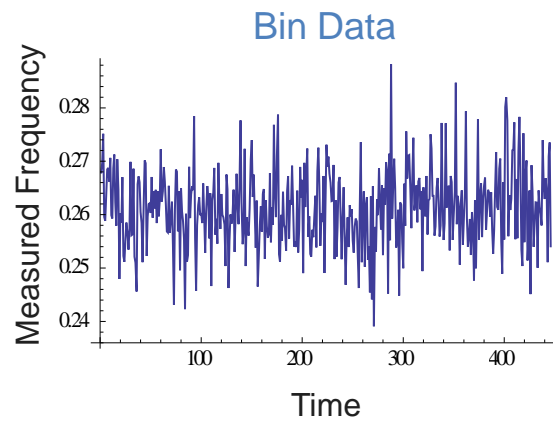
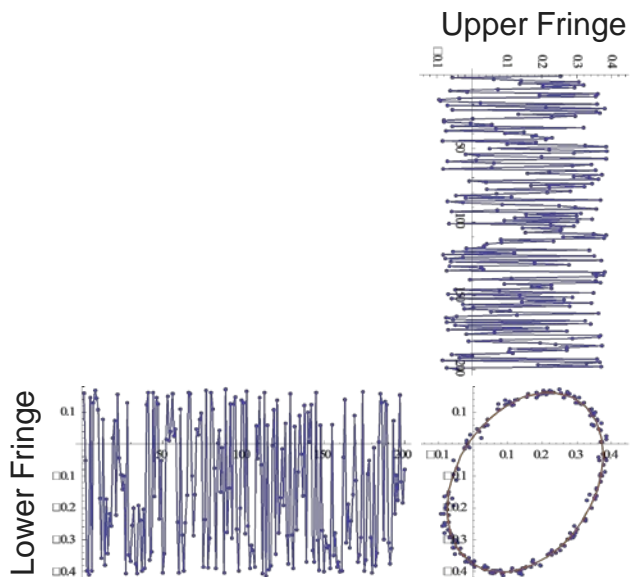
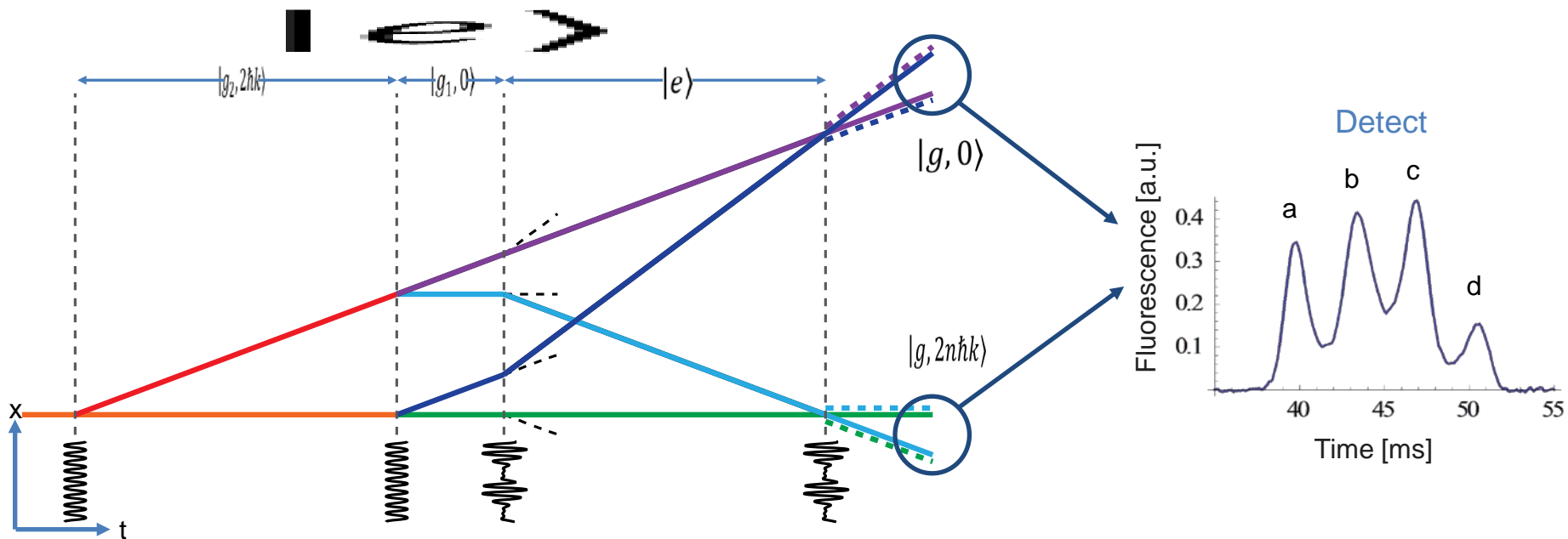
# Simultaneous Conjugate Interferometers



$$\Phi_{RB} = \pm 8n^2 \omega_r T \pm n \omega_m T + 2nkg(T + T')T$$

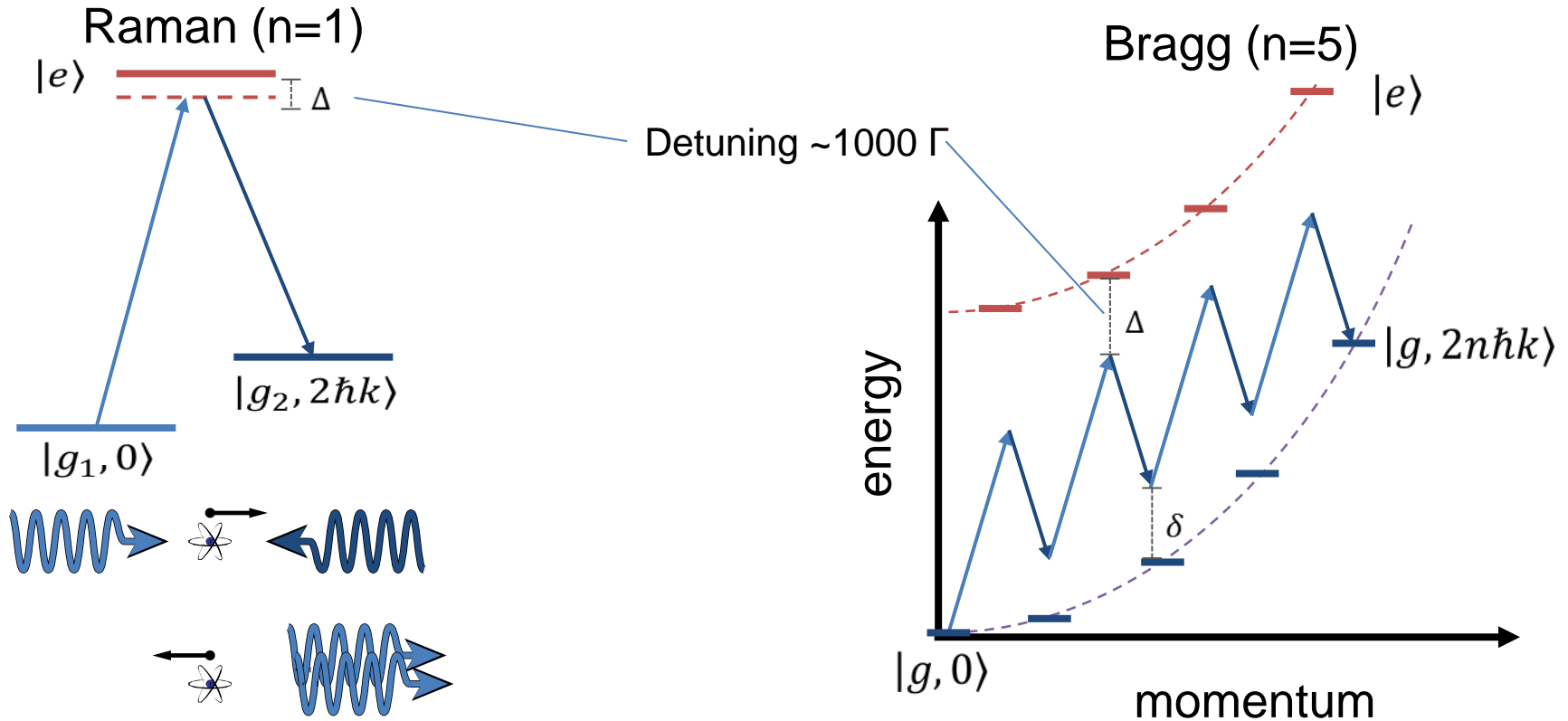
$$\Phi_{RB,Diff} = 16n^2 \omega_r T - 2n \omega_m T$$

# Phase Extraction



# Multi-Photon Bragg Diffraction

$$\Phi_{RB,Diff} = 16n^2\omega_r T - 2n\omega_m T$$

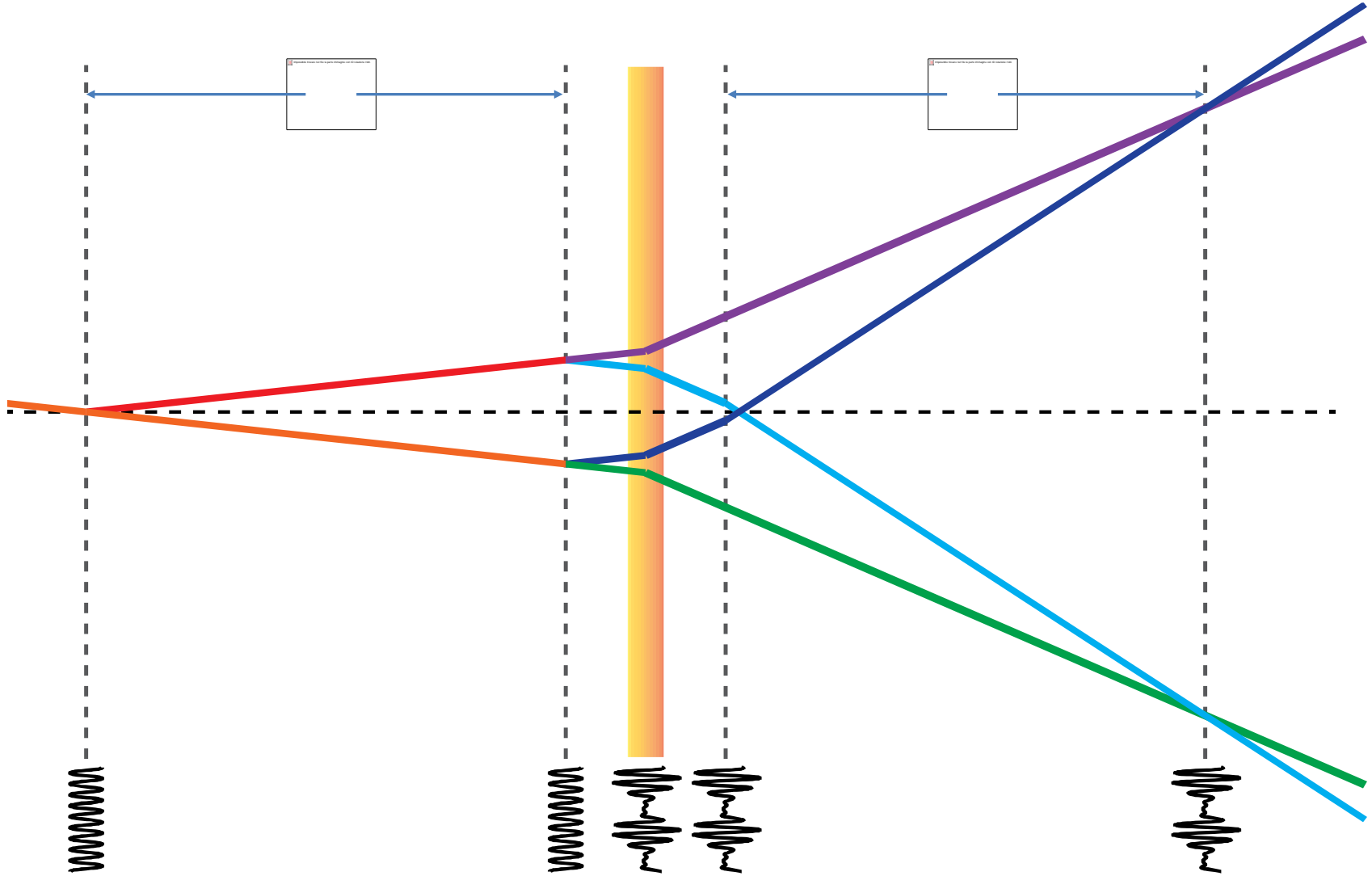


## Bragg gives you:

- More photons transferred per pulse (higher sensitivity)
- Atoms stay in same internal state (Zeeman, AC Stark systematics suppressed)

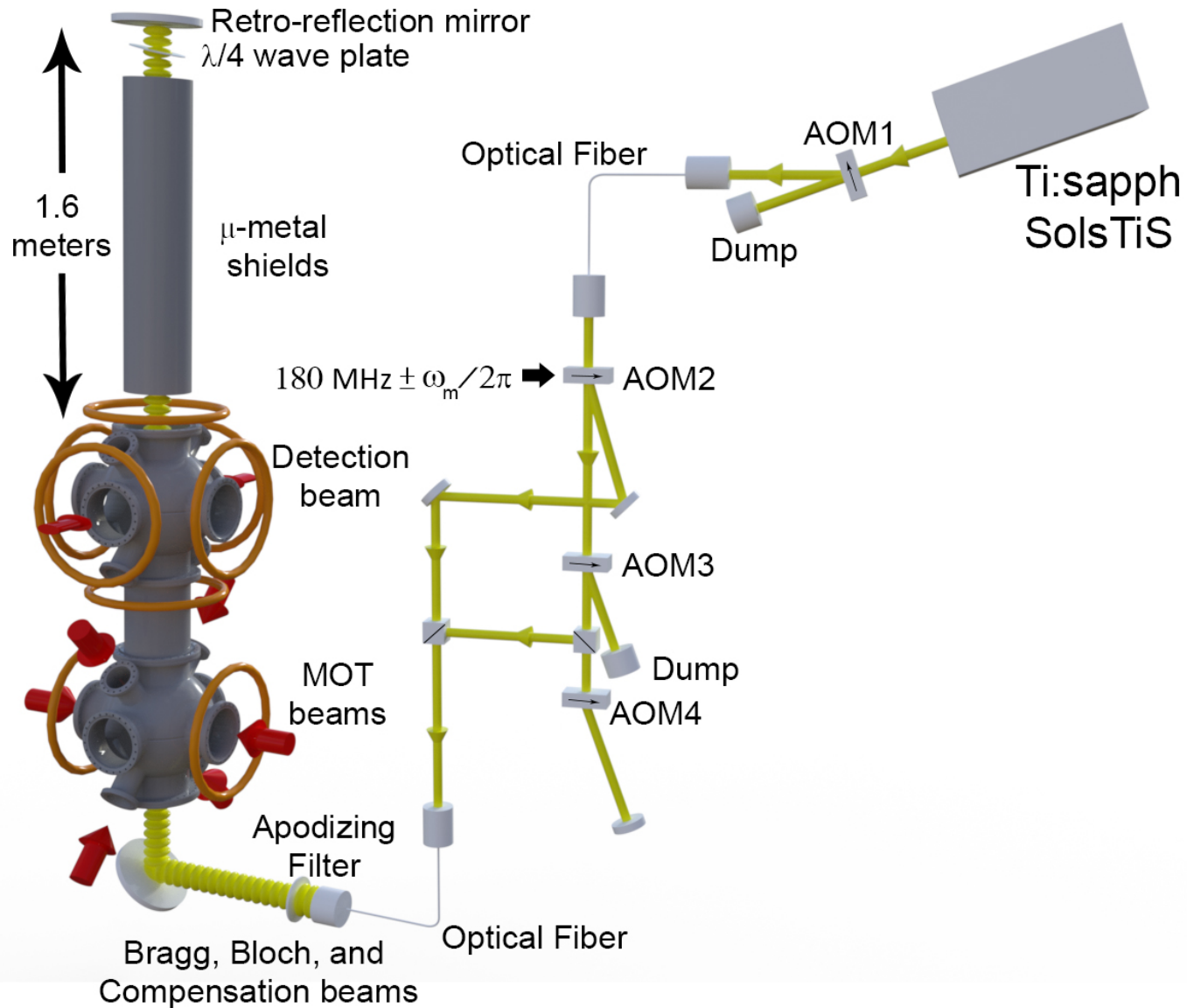


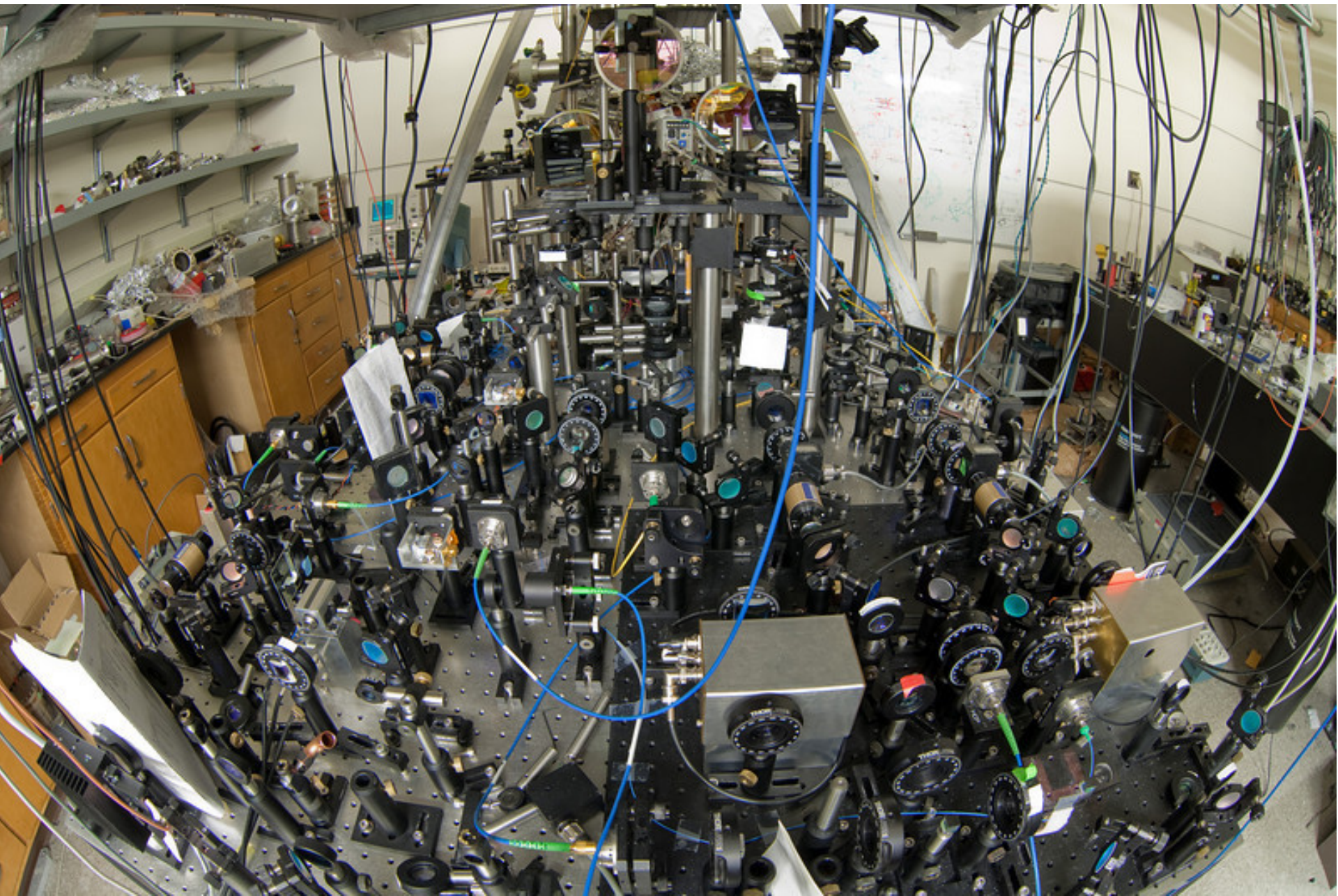
# Bloch Oscillations



$$\Delta\Phi_{RB+Bloch} = 16n(n + N)\omega_r T - 2n\omega_m T$$

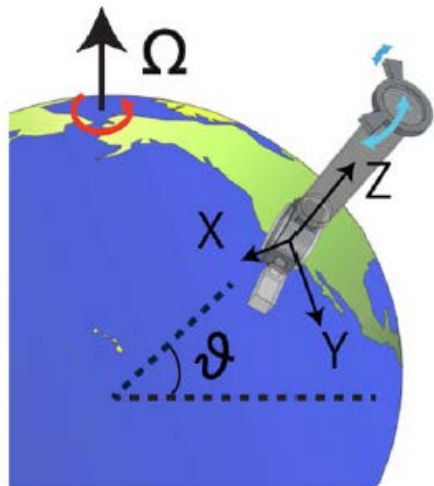
# Setup



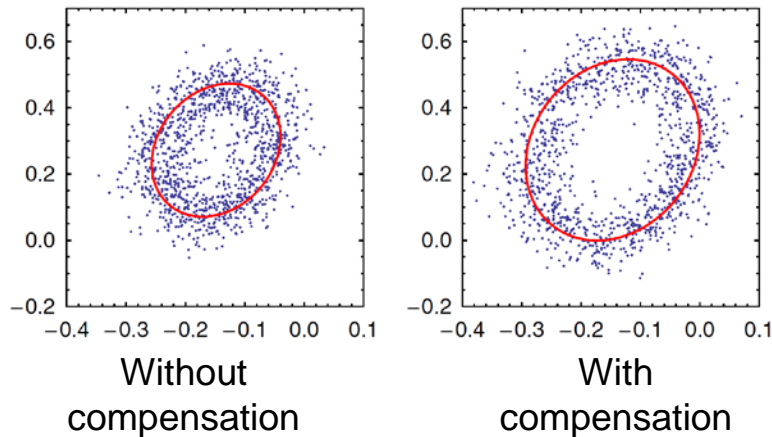


# Tricks for Increased Sensitivity

## Coriolis Compensation



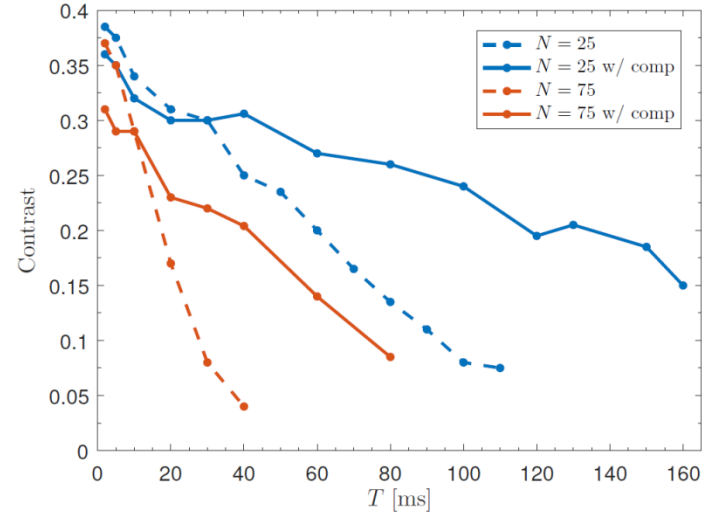
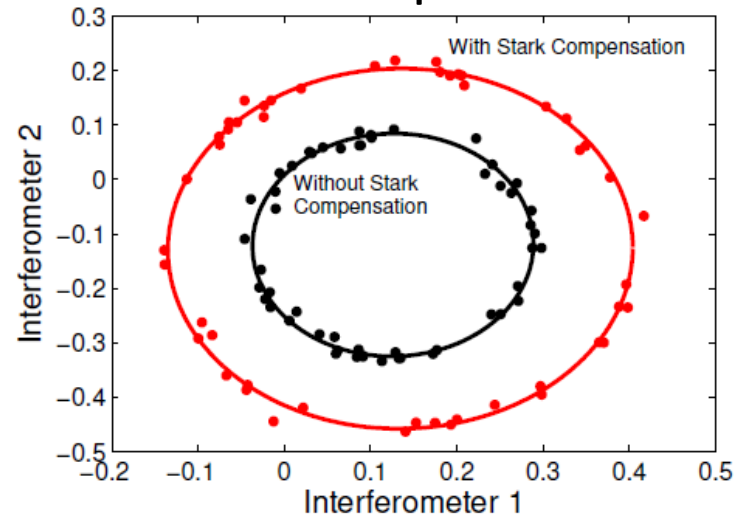
$10\hbar k, T = 180ms$



x3.5 contrast gain

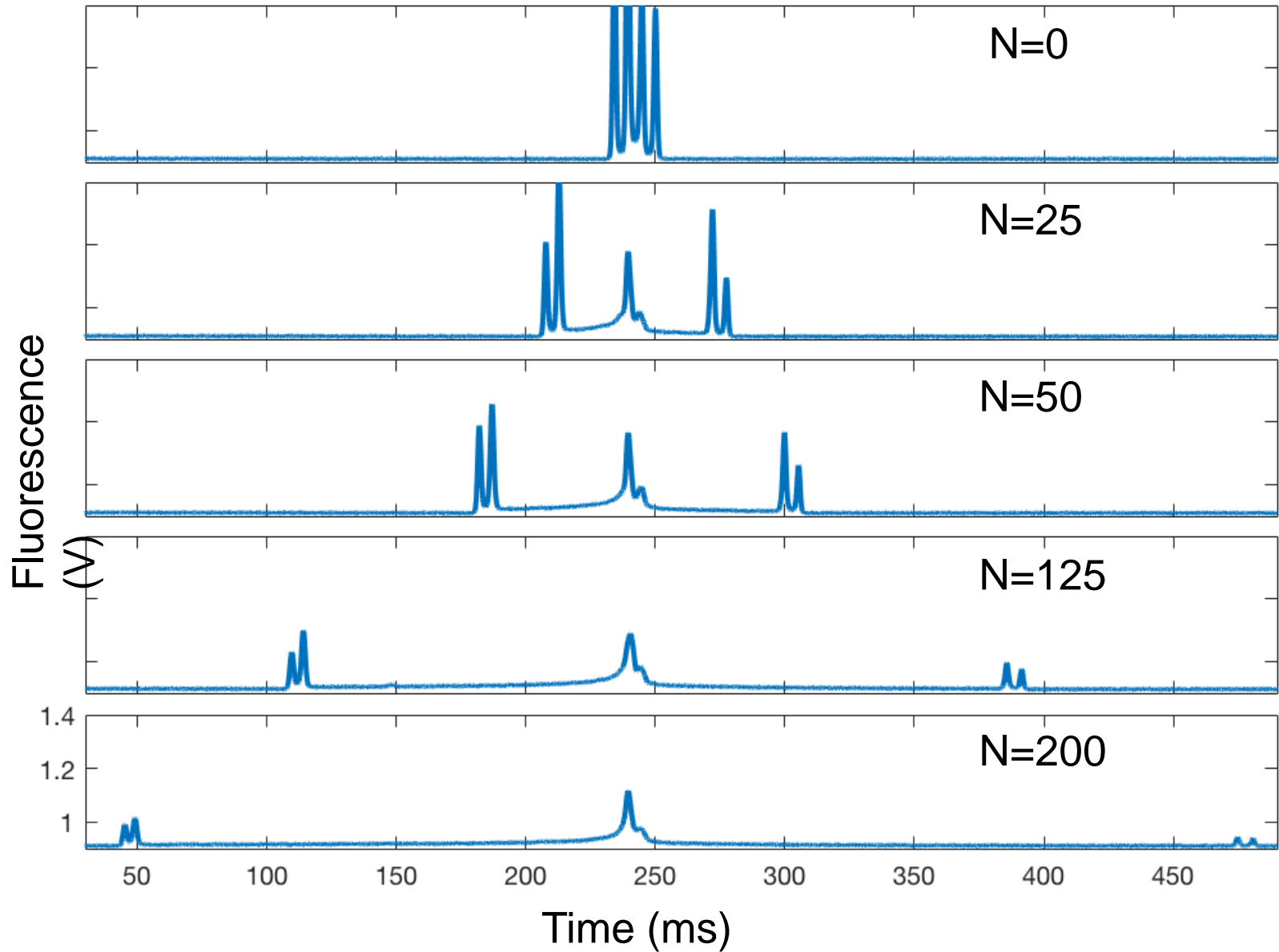
>12Mrad phase diff. measurable!

## Stark Compensation

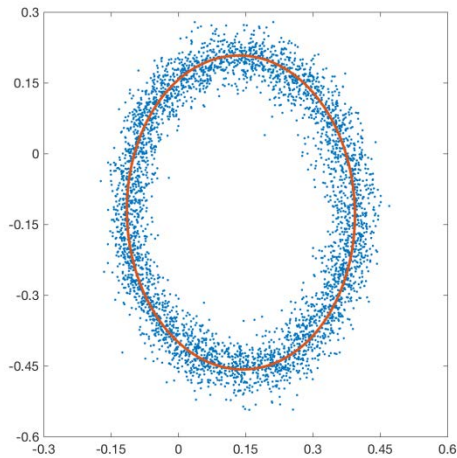


Up to N=200

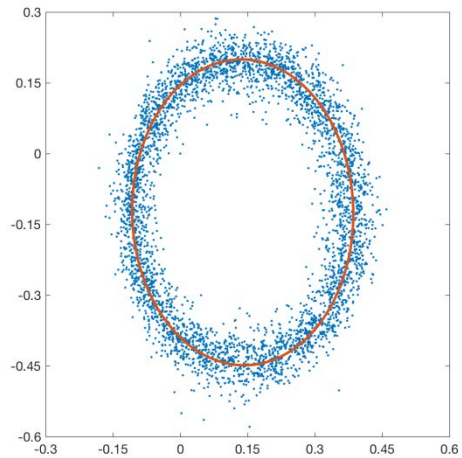
# Fluorescence Traces



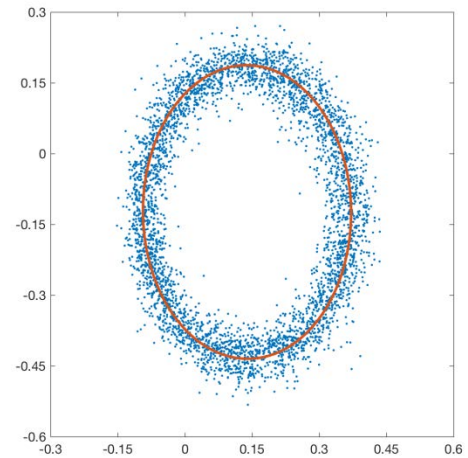
# $n=5, N=125$ Ellipses



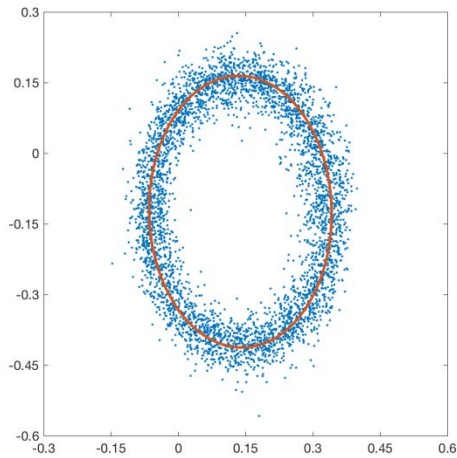
$T=5$  ms



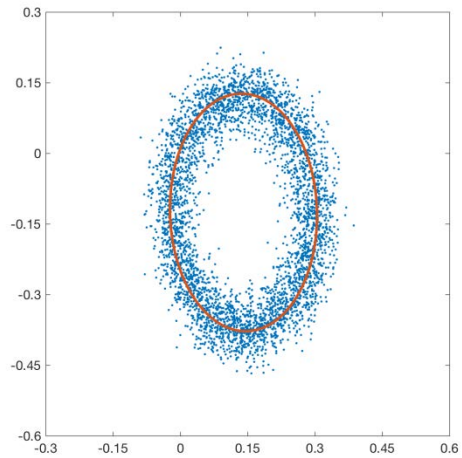
$T=10$  ms



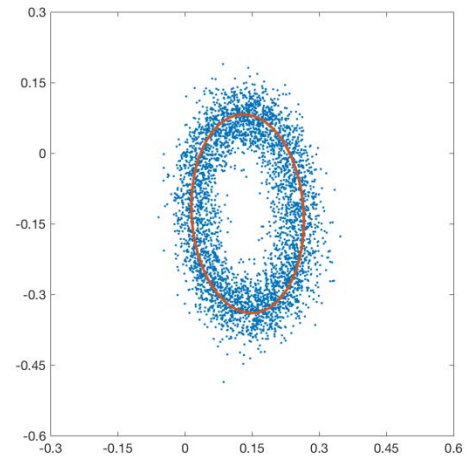
$T=20$  ms



$T=40$  ms



$T=60$  ms

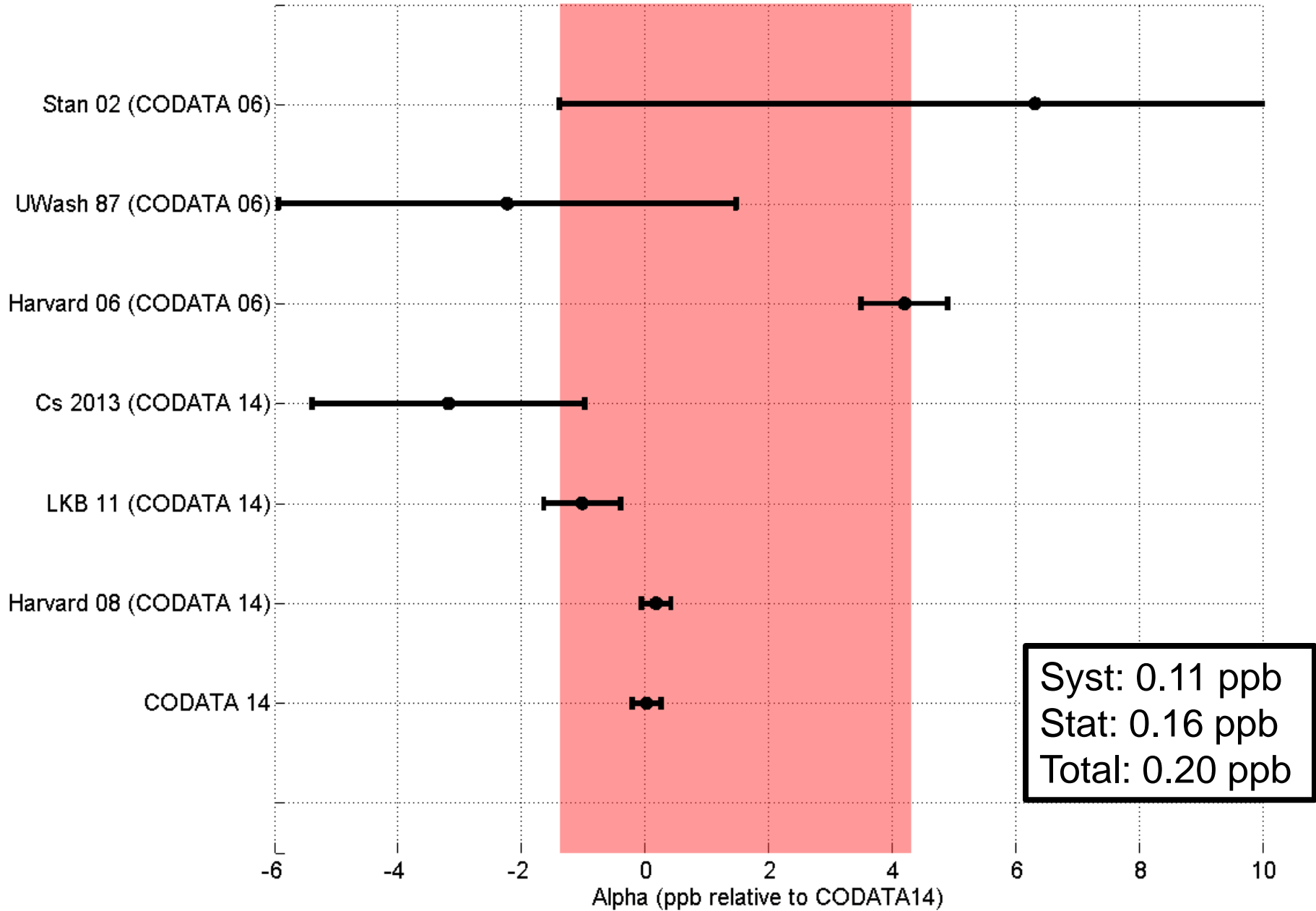


$T=80$  ms

# Suppression of Bias

- Blinding
  - Random number [-1 MHz, +1 MHz] chosen by Rana Adhikari (Caltech)
  - Added to Laser Wavenumber (+/- 3 ppb)
  - Given to us as encrypted file
- Two Independent Data Analysis Programs
  - Same raw datasets
  - Agree

# Blind Analysis

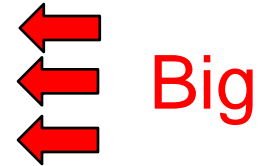




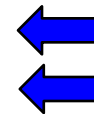
Systematics

# 0.16 ppb systematic errors

Effect	Sect.	Value	$\delta\alpha/\alpha$ (ppb)
Laser Frequency	1	N/A	$-0.24 \pm 0.03$
Acceleration Gradient	4A	$\square \mp (2.13 \pm 0.01) \times 10^{-6} / s^2$	$-1.69 \pm 0.02$
Gouy phase	3	$w_0 = 3.21 \pm 0.008$ mm, $z_0 = 0.5 \pm 1.0$ m	$-3.60 \pm 0.03$
Wavefront Curvature	12	$\langle r^2 \rangle^{1/2} = 0.58$ mm	$0.15 \pm 0.03$
Beam Alignment	5	N/A	$0.05 \pm 0.03$
BO Light Shift	6	N/A	$0 \pm 0.004$
Density Shift	7	$\rho = 10^6$ atoms/cm <sup>3</sup>	$0 \pm 0.003$
Index of Refraction	8	$n_{\text{cloud}} - 1 = 30 \times 10^{-12}$	$0 \pm 0.03$
Speckle Phase Shift	4B	N/A	$0 \pm 0.04$
Sagnac Effect	9	N/A	$0 \pm 0.001$
Mod. Frequency Wavenumber	10	N/A	$0 \pm 0.001$
Thermal Motion of Atoms	11	N/A	$0 \pm 0.08$
Non-Gaussian Waveform	13	N/A	$0 \pm 0.03$
Parasitic Interferometers	14	N/A	$0 \pm 0.03$
Total Systematic Error			$-5.33 \pm 0.12$
Total Statistical Error			$\pm 0.16$
Electron Mass (18)		$5.48579909067 \times 10^{-4}$ u	$\pm 0.02$
Cesium Mass (4,17)		132.9054519615 u	$\pm 0.03$

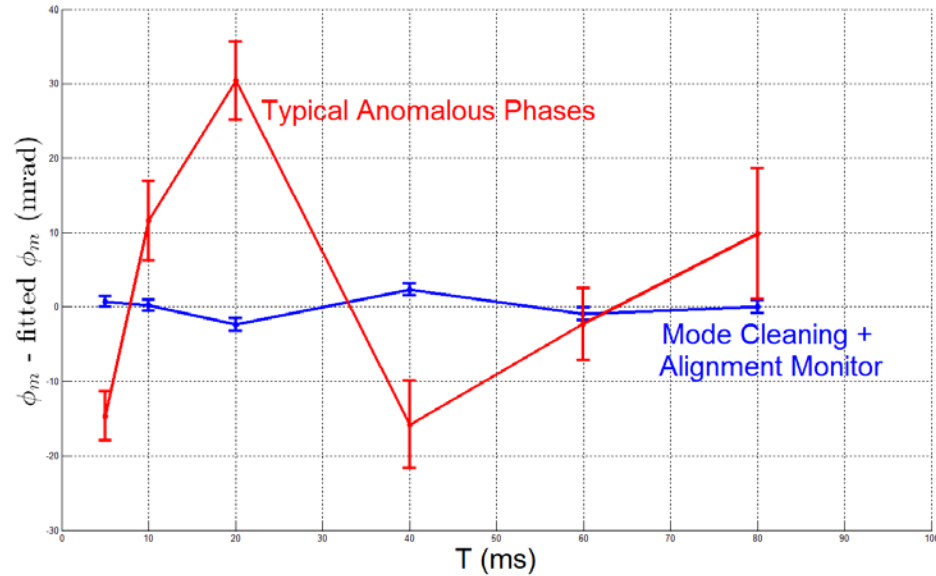
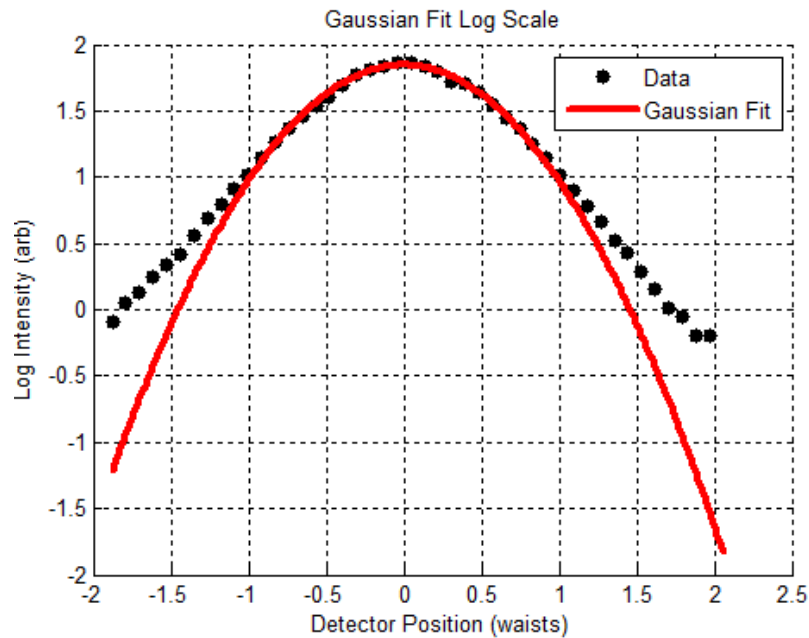


'New'



# Speckle Phase

- 30 mrad anomaly  $\rightarrow$  8 ppb at  $N=0$
- $>10x$  suppression by mode filtering
- 25x suppression by  $N=125$



\$200 Apodizing Filter



- Fiber doesn't make Gaussian beams
- Spatial Filtering via Apodizer + Fountain Alignment Monitor

# Systematic Checks

- Variation of alpha w.r.t.:
  - Bloch order
  - Bloch power
  - Contrast
  - Detection region
  - Pulse intensity: overall and pulse/pulse ratio
  - Speckle phase
  - $\omega_m$  mixing (RF)
  - $\omega_m$  mixing (optics)
  - Delay of interferometer sequence
  - Bias B-field
  - Single-photon detuning
  - Data Analysis parameters (cuts, fitting, etc.)
  - Fountain alignment (launch direction, no spatial filtering)

# Dark photons

Whatever the dark sector is made of, only three interactions are allowed by standard model symmetries

- **Vector portal** “massive photon”
- Higgs portal
- Neutrino portal

## Hints

- Muon  $g-2$
- Proton radius puzzle
- Astrophysical hints?
  - 511 keV line
  - keV gamma-ray excess
  - Galactic center excess



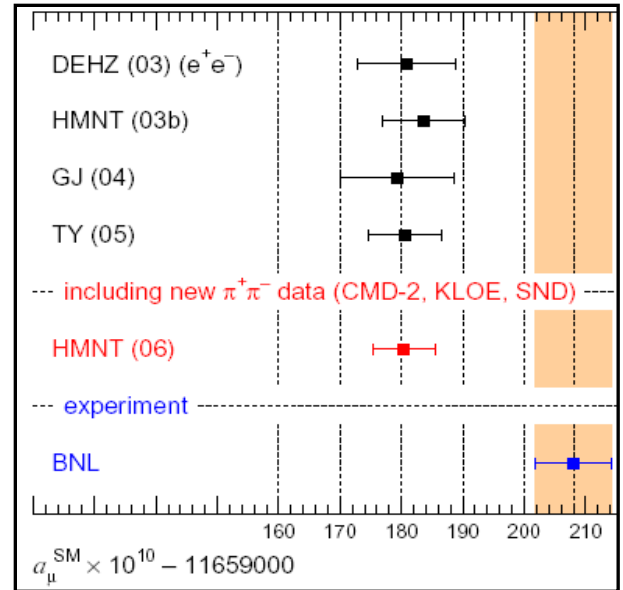
# Dark photons

Whatever the dark sector is made of, only three interactions are allowed by standard model symmetries

- **Vector portal** “massive photon”
- Higgs portal
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## Hints

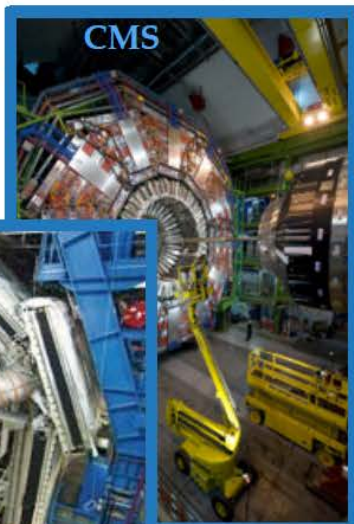
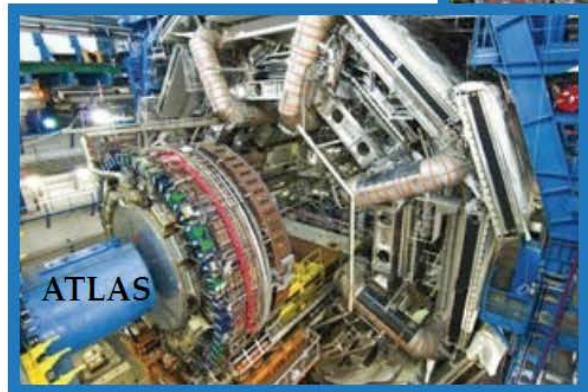
- Muon  $g-2$
- Proton radius puzzle?
- $^8\text{Be}$  decay
- Astrophysical hints?
  - 511 keV line
  - keV gamma-ray excess
  - Galactic center excess



“Arguably, the strongest experimental evidence for physics beyond the standard model” (David Hertzog)

# Ongoing dark photon searches

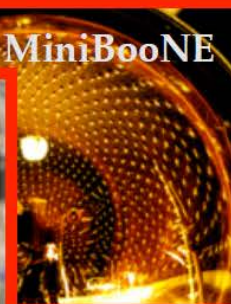
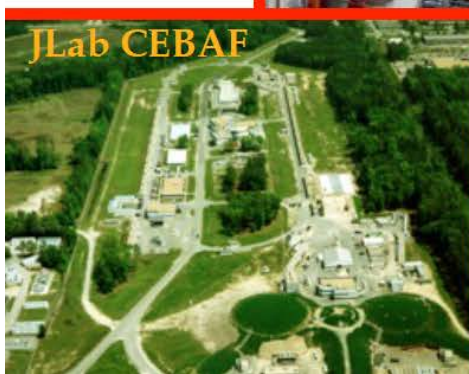
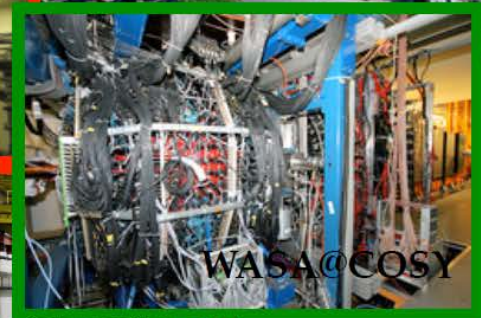
High-energy colliders



High intensity colliders



Fixed Target

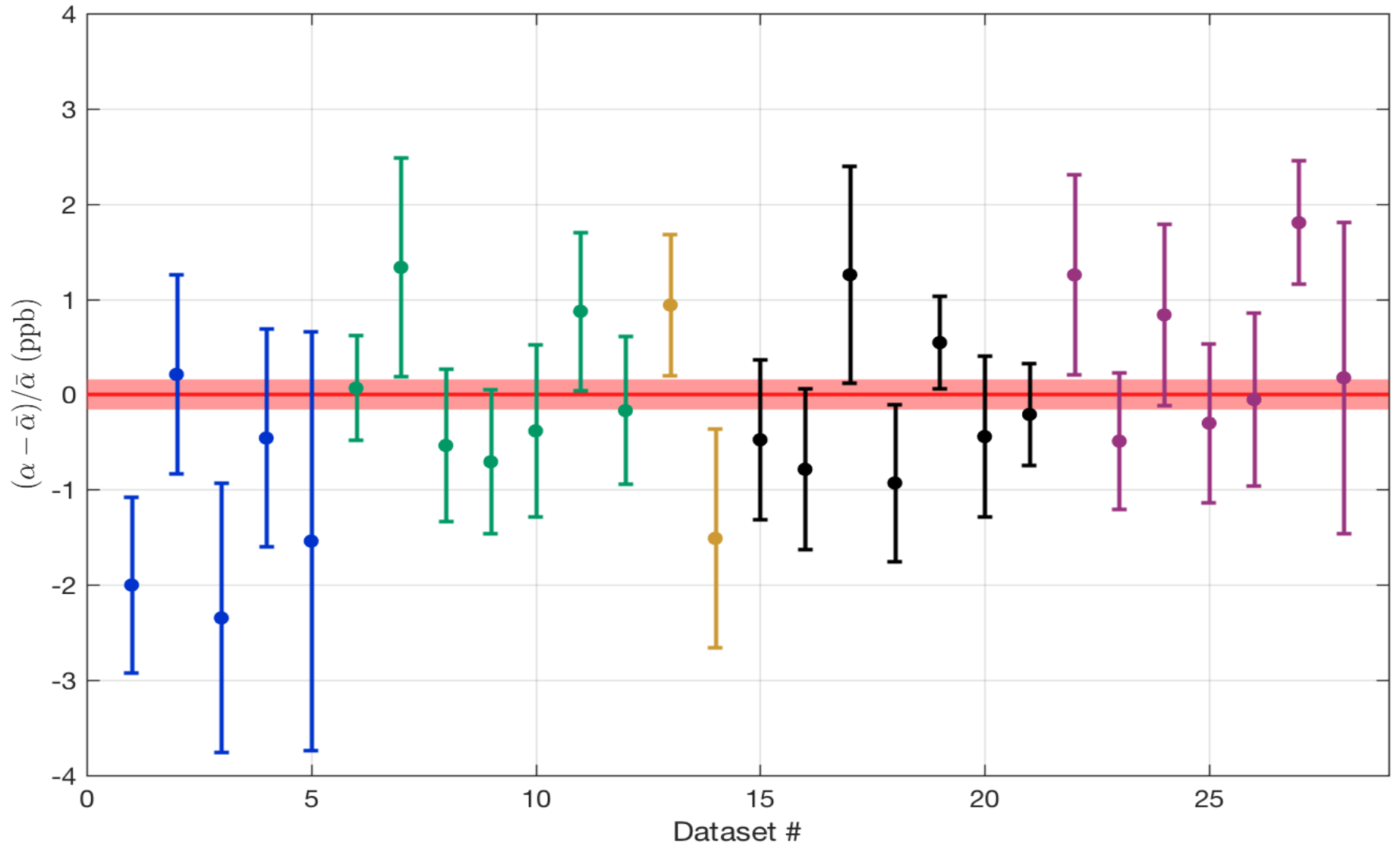


Dave Schuster

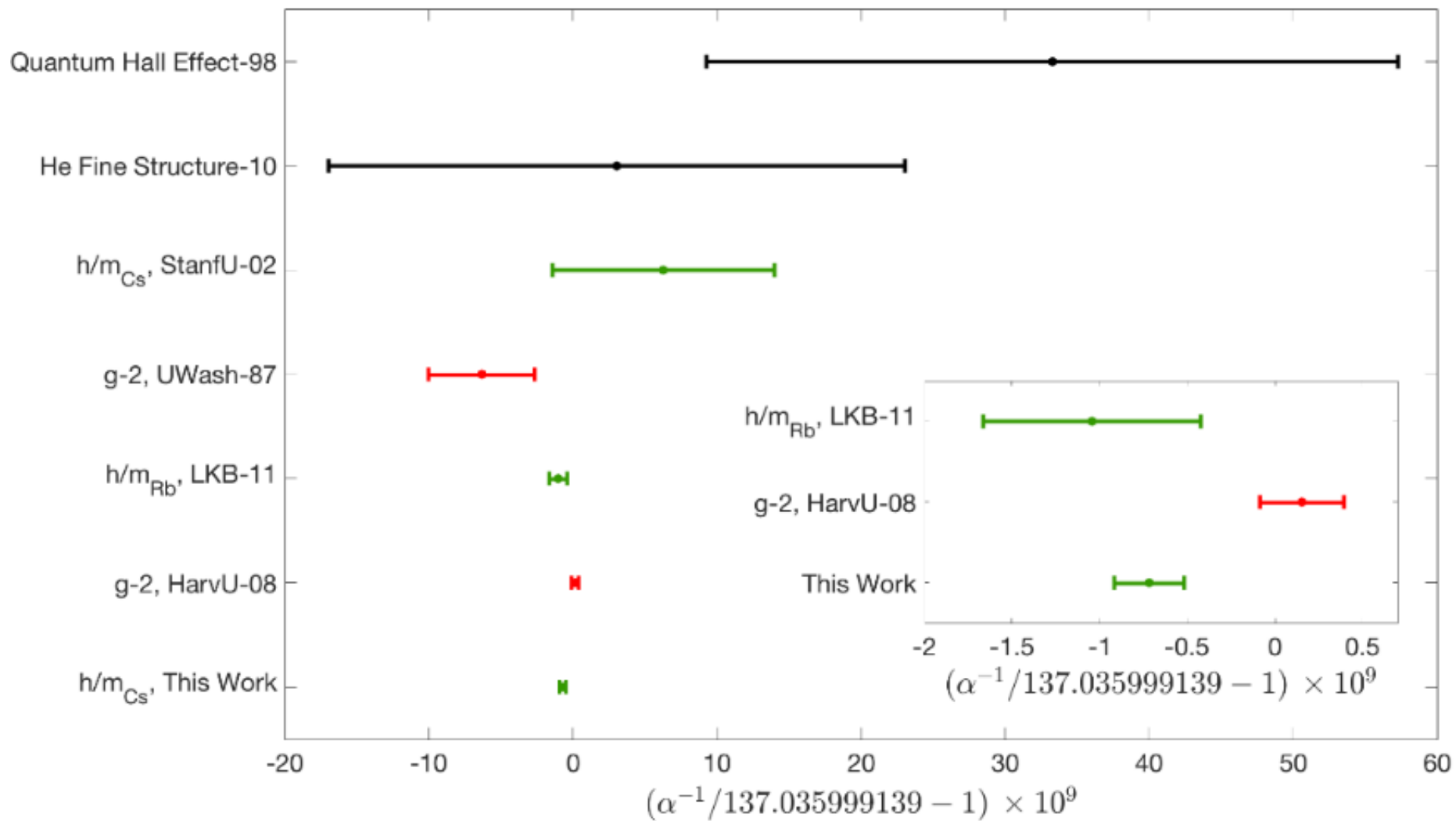
# Results



# Results



# Results



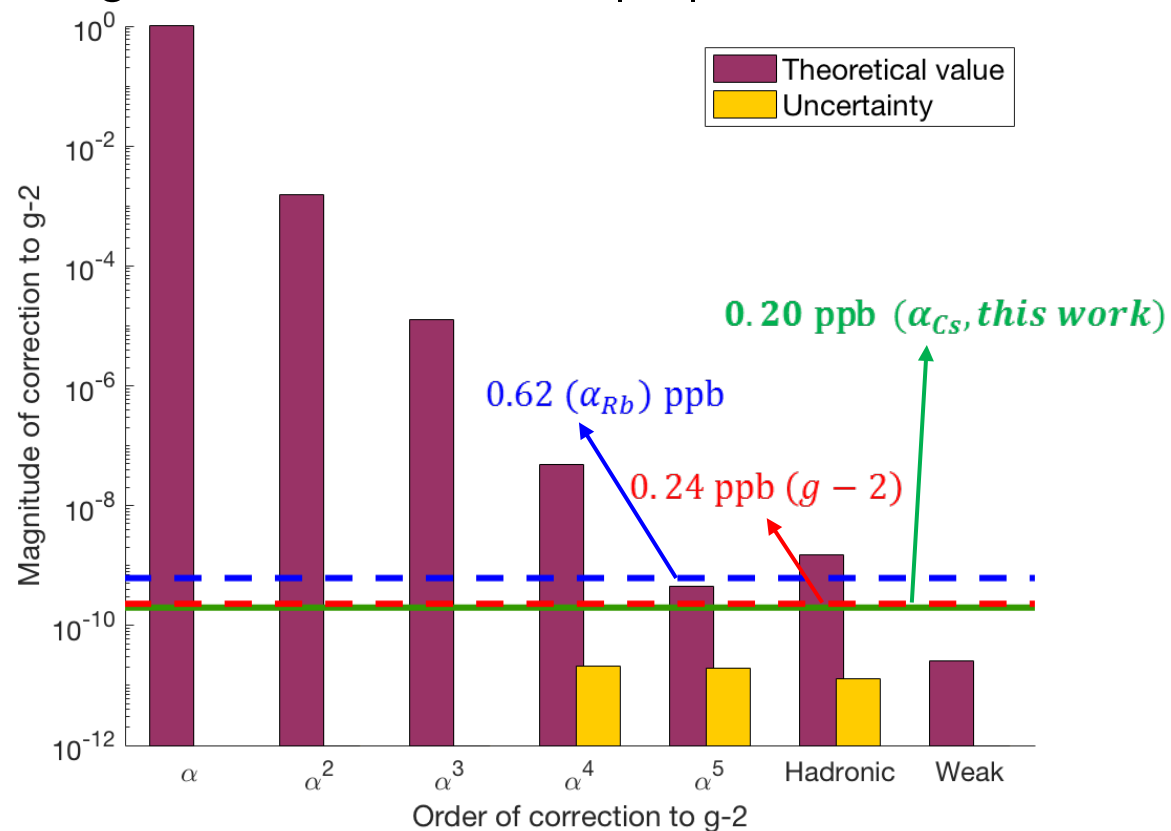
# Results

$$\alpha^{-1} = 137.035999070(27) \text{ (0.20 ppb)}$$

$$a(\alpha) = g/2 - 1 = 0.00115965218149(23)$$

$$\delta a = a_{\text{meas}} - a(\alpha) = -0.76(0.36) \times 10^{-12}$$

1-sigma confidence level  $|\delta a| < 1.1 \times 10^{-12}$



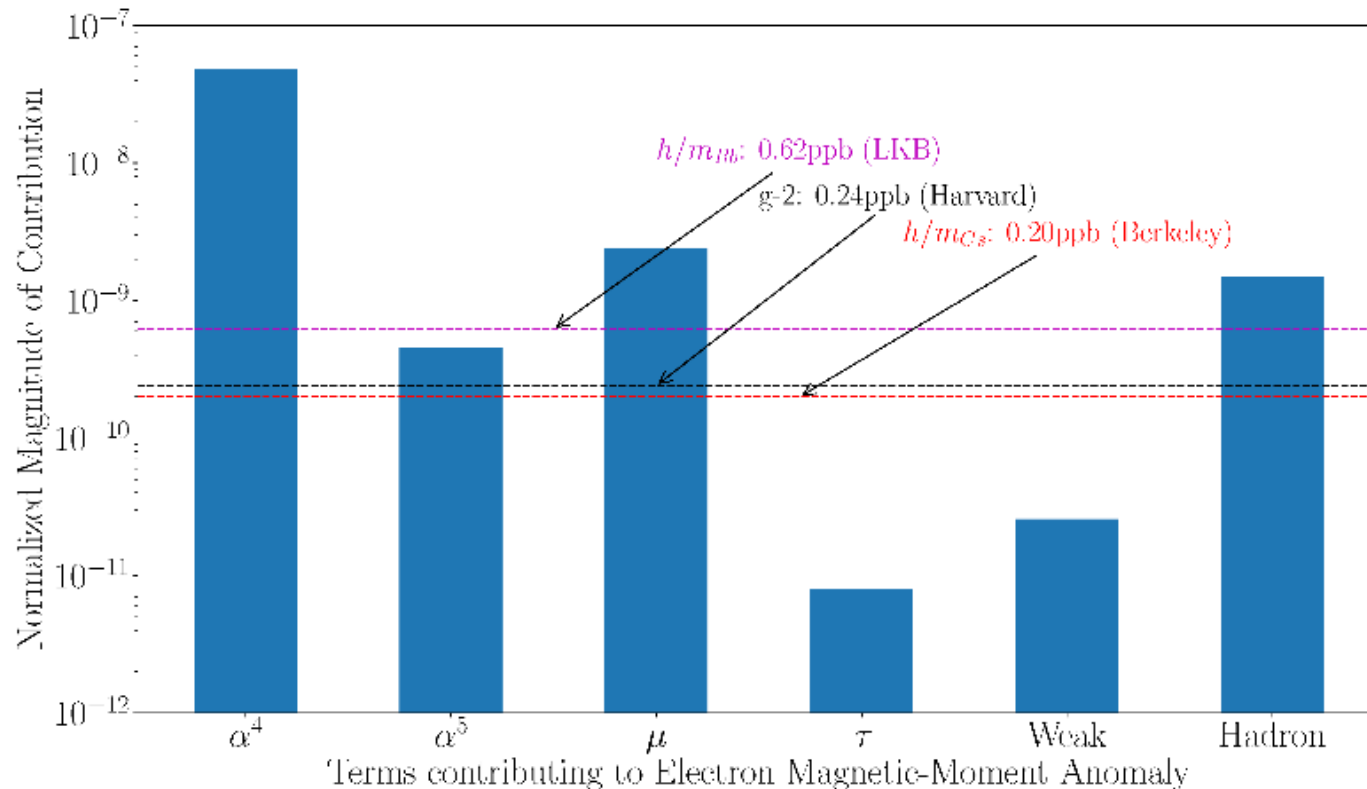
# Results

$$\alpha^{-1} = 137.035999070(27) \text{ (0.20 ppb)}$$

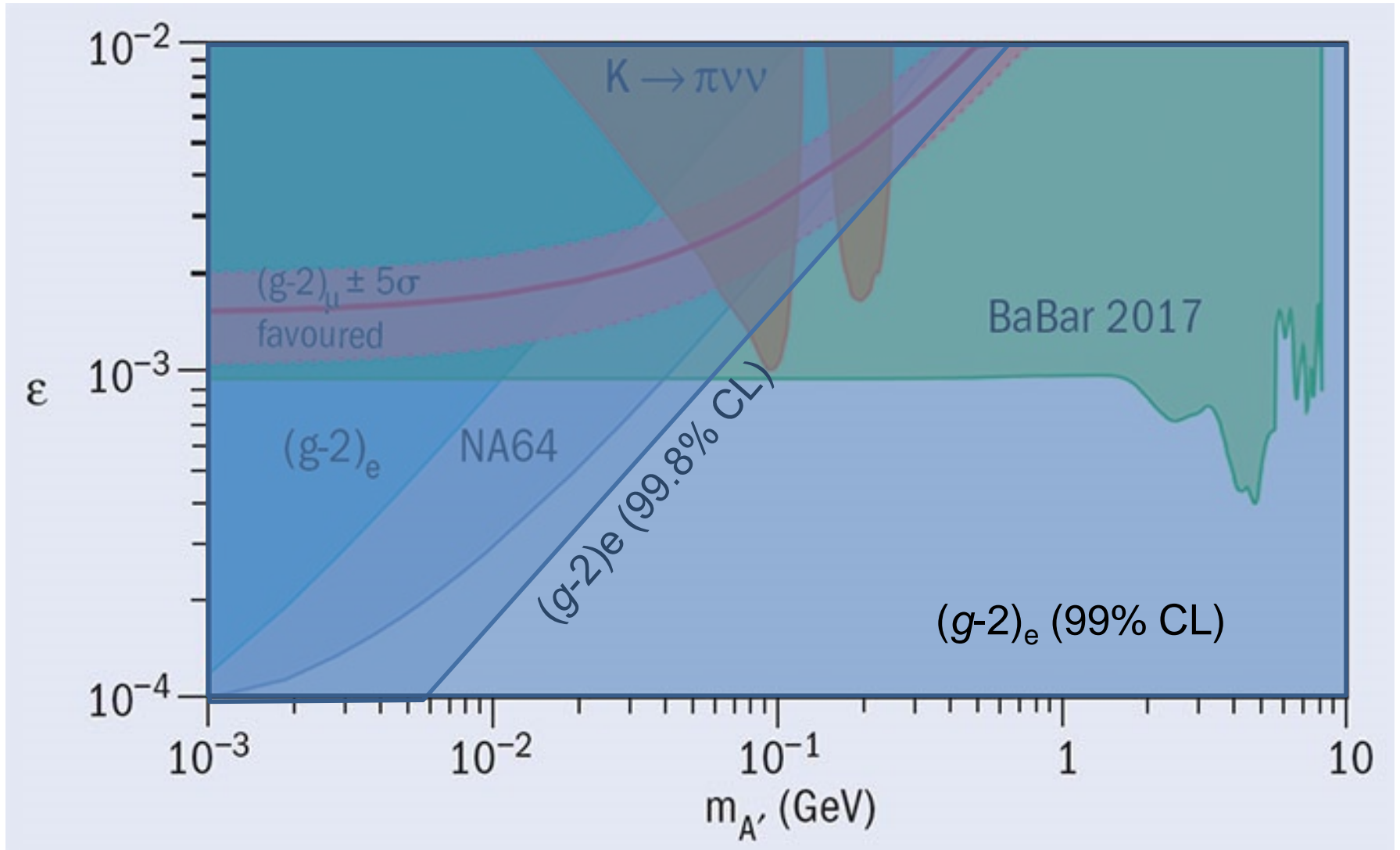
$$a(\alpha) = g/2 - 1 = 0.00115965218149(23)$$

$$\delta a = a_{\text{meas}} - a(\alpha) = -0.76(0.36) \times 10^{-12}$$

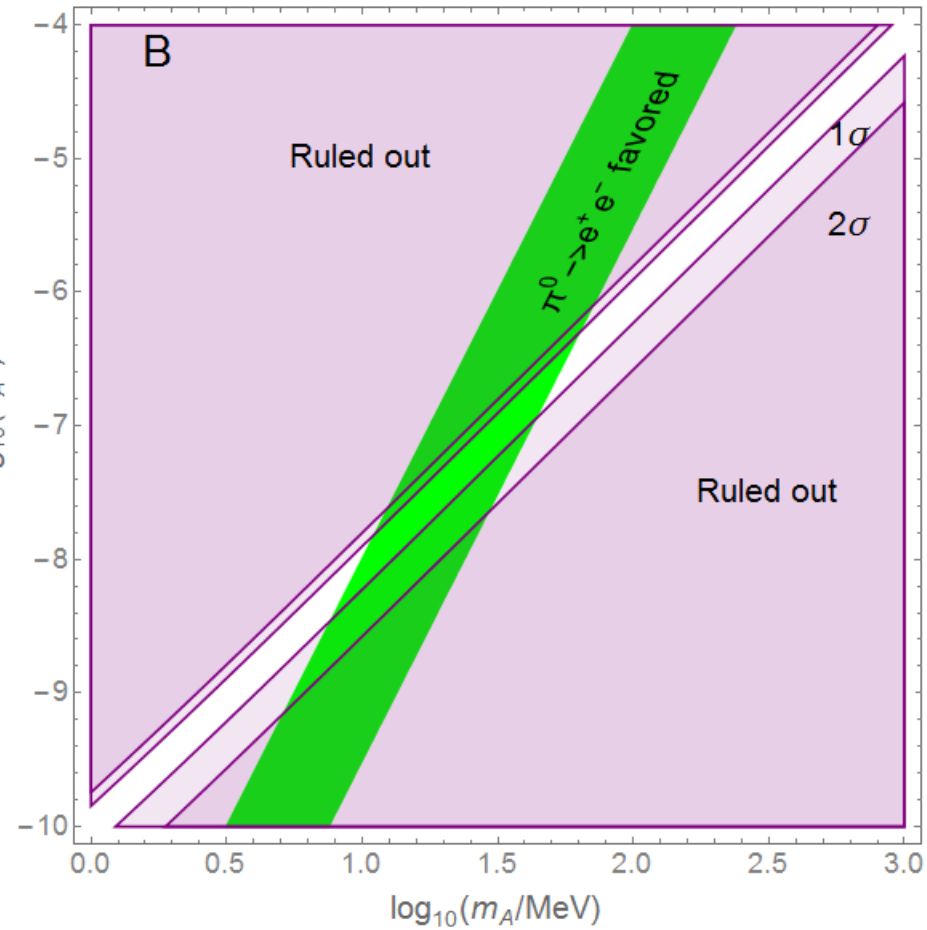
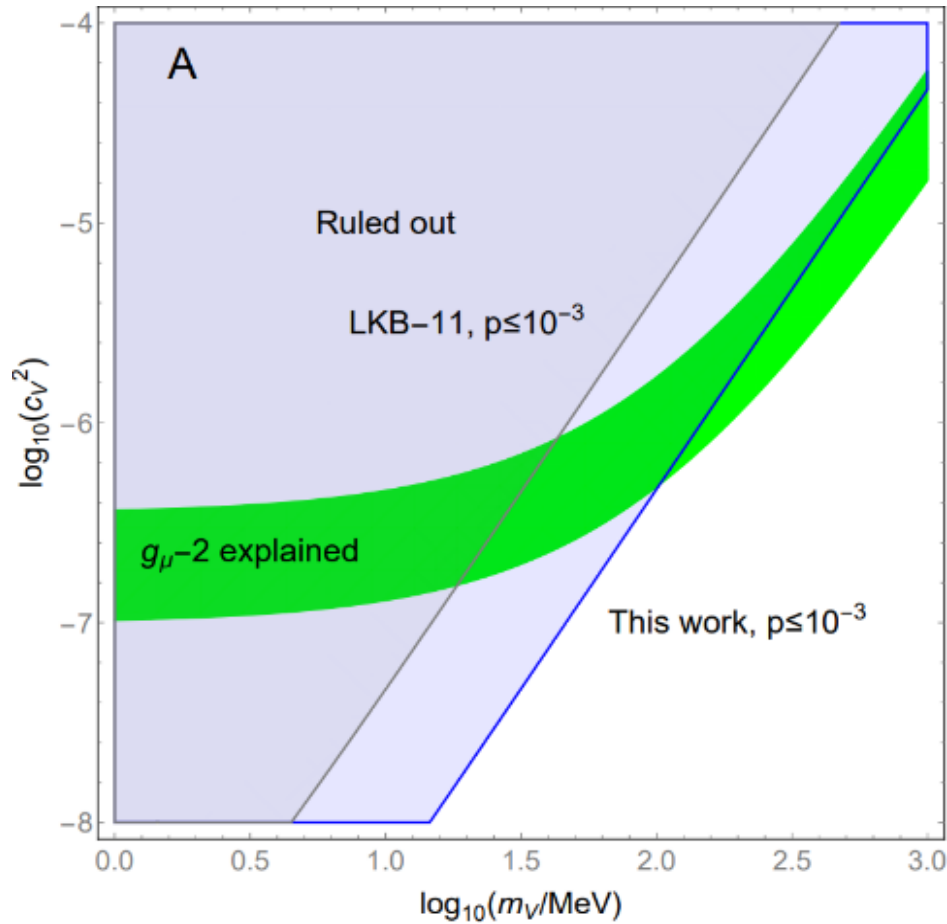
1-sigma confidence level  $|\delta a| < 1.1 \times 10^{-12}$



# Dark photon limits

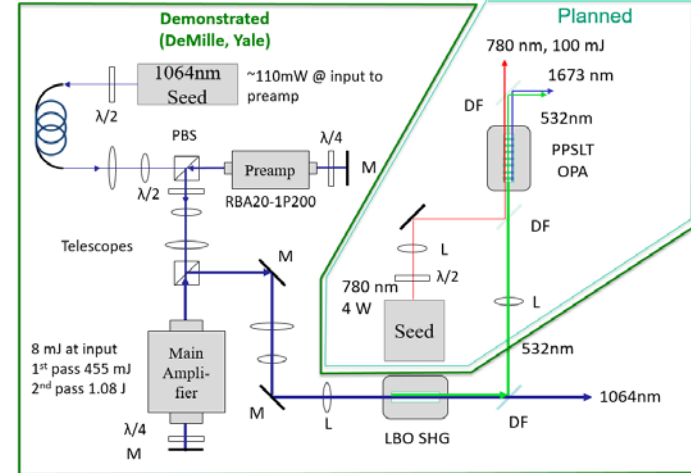


# Dark photons & axial vectors



# Future Upgrades

- Big Vacuum System
  - x20 waist  $\rightarrow$  x400 supp.
- Pulsed Laser
  - x1000 eff. power
- EM/Acoustic Shielded Room
- 2 MOT Chambers
  - Better Fountain Alignment
- Science Chamber
  - Dark Matter studies



# Thank you!

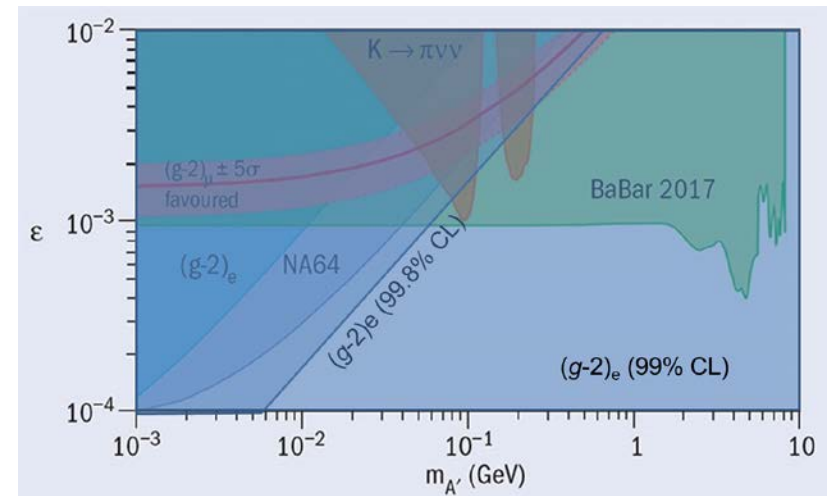
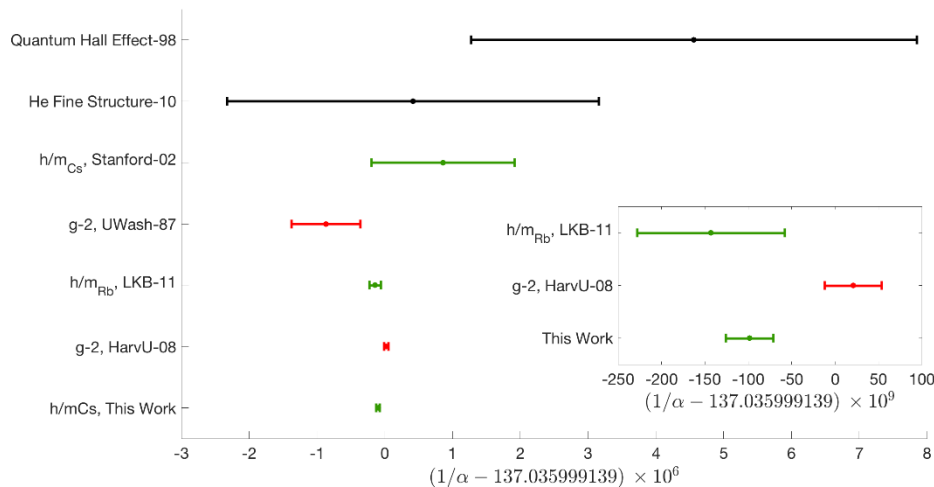
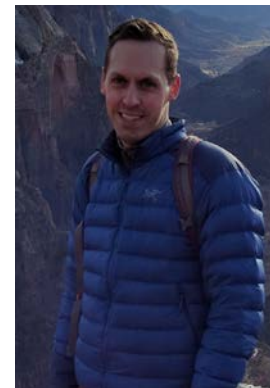
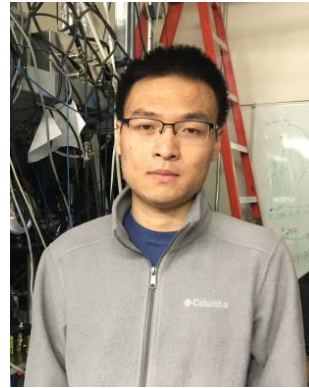
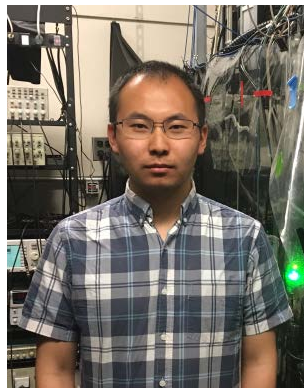
Postdoc:  
R. Parker

Grad:  
Chenghui Yu

Grad:  
Weicheng Zhong

Former Grad:  
Brian Estey

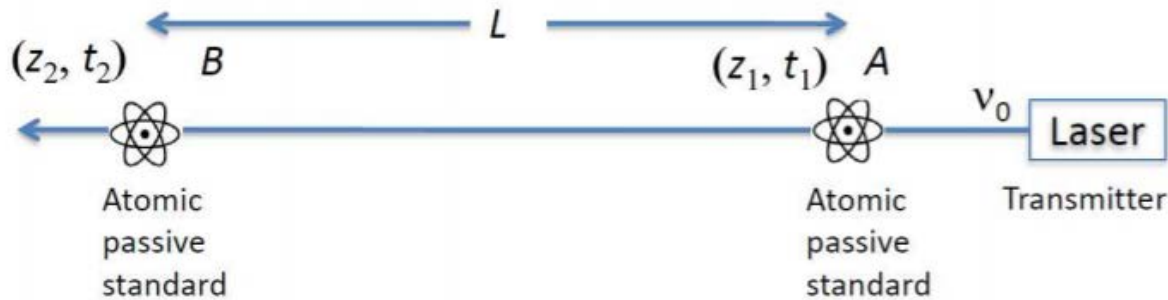
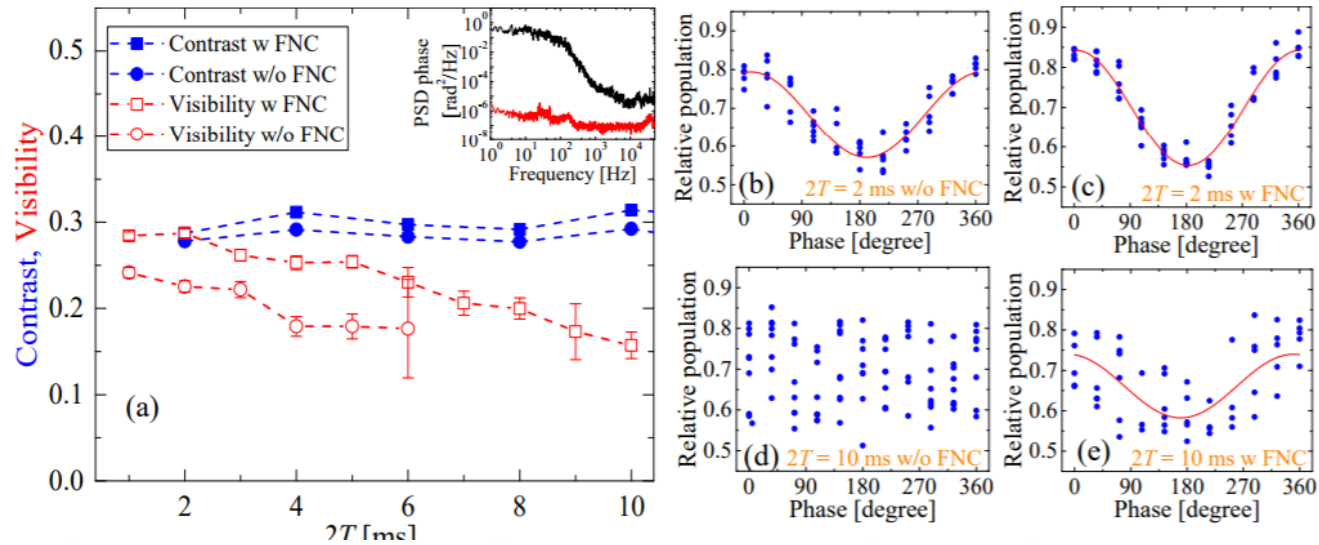
PI: Holger  
Müller





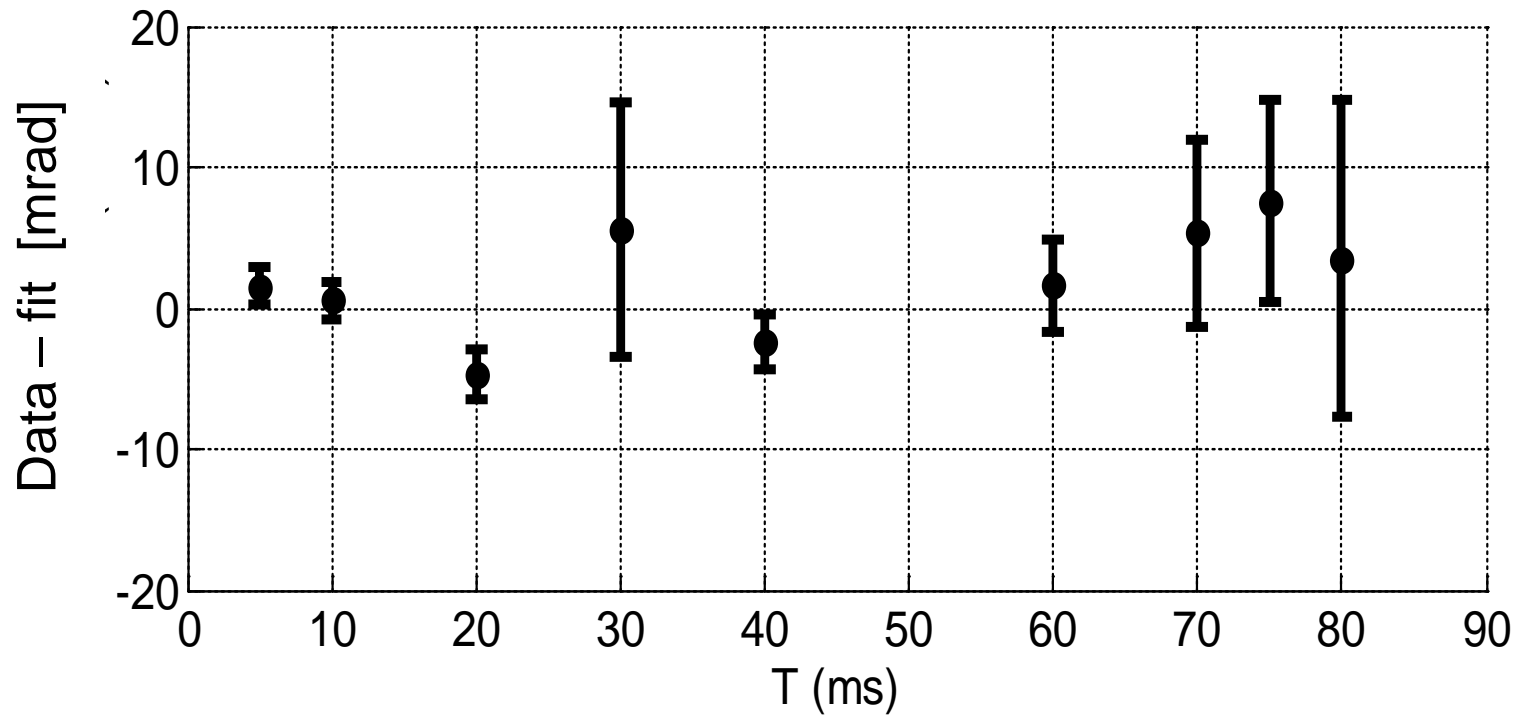
# Atom interferometry with the Sr optical clock transition

Liang Hu,\* Nicola Poli,† Leonardo Salvi, and Guglielmo M. Tino‡  
 Dipartimento di Fisica e Astronomia and LENS - Università di Firenze,  
 INFN - Sezione di Firenze, Via Sansone 1, 50019 Sesto Fiorentino, Italy  
 (Dated: August 18, 2017)

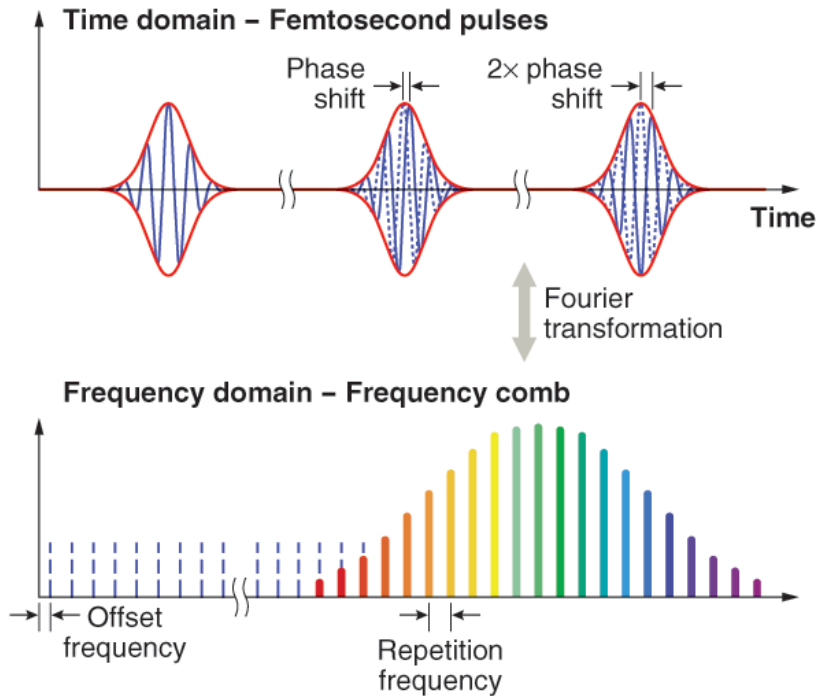


Yu, Tinto  
 2010

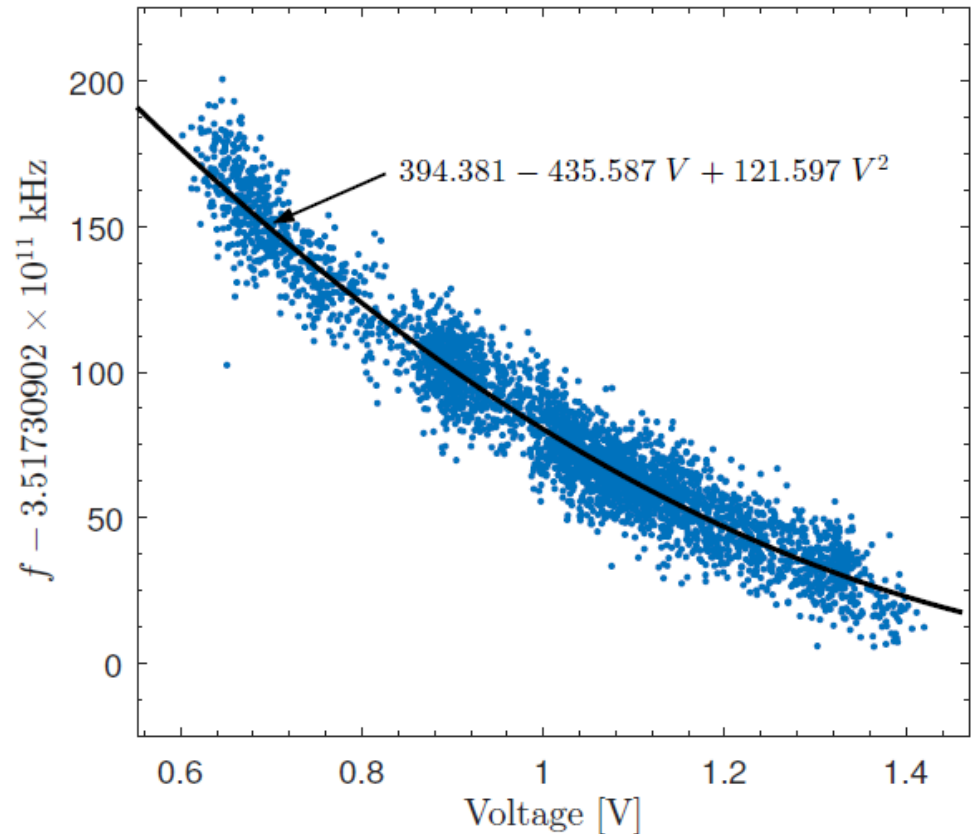
# Residuals (if any) are now unresolved



# Laser Frequency



$$f_n = n f_r + f_{offset}$$

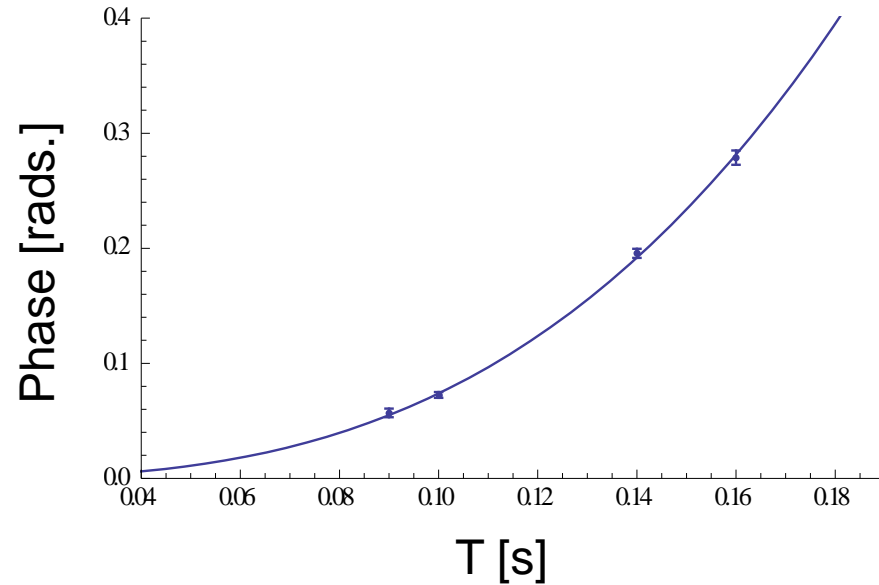
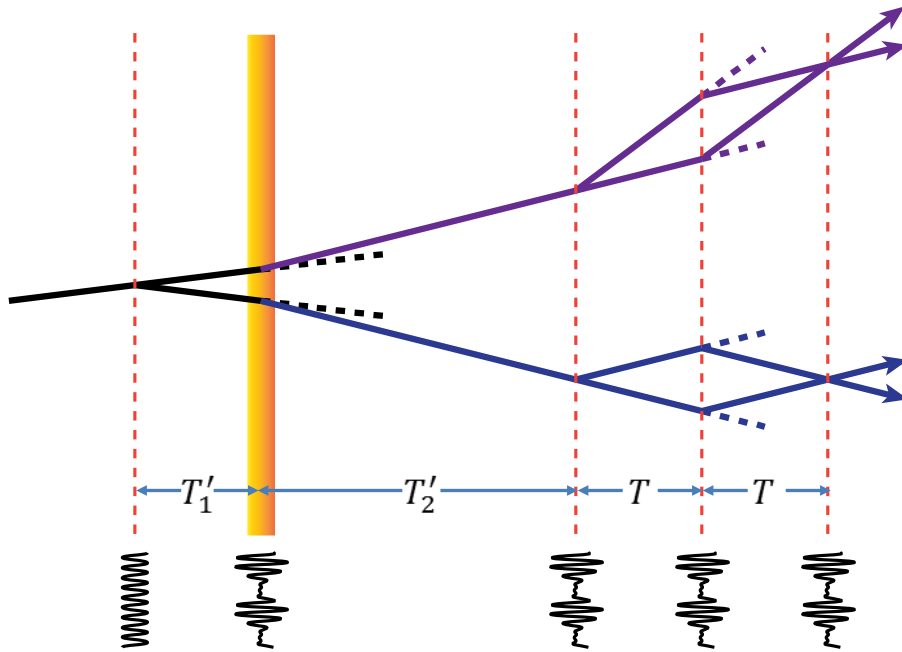


Laser frequency as a function of power send into the spectroscopy

Frequency residual = 10 kHz  $\rightarrow$  0.03 ppb

# Gravity Gradient

$$\Delta\Phi = 16n(n + N)\omega_r T - 2n\omega_m T + \frac{4}{3}n\omega_r\gamma T \left[ n(2T^2 + 3T(T'_1 + T'_2) + 3(T'_1 + T'_2)^2) + N(2T^2 + 6TT'_2 + 6T_2'^2) \right]$$



$$\Delta E_0 = -2 \frac{\alpha_{Cs} \sigma T_s^4}{c \epsilon_n},$$

$$\gamma = 1.295(32) \times 10^{-6} \frac{m}{s^2} \frac{1}{m}$$

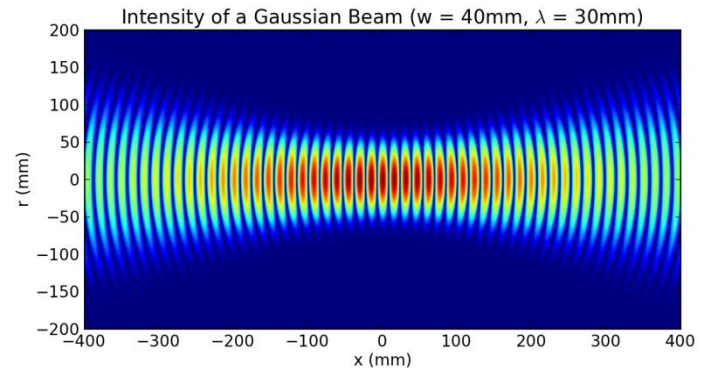
Shift in alpha = -1.41 +/- 0.02 ppb

# Gouy Phase Systematic

$$E(r, z) = E_0 \frac{w_0}{w(z)} e^{-\frac{r^2}{w(z)^2}} e^{-ik(z-z_0) - \frac{ikr^2}{2R(z-z_0)} + i\zeta(z-z_0)}$$

$$z_R = \frac{\pi w_0^2}{\lambda} \sim 50 \text{ m} \quad w(z) = w_0 \sqrt{1 + \frac{z^2}{z_R^2}}$$

$$\zeta(z) = \tan^{-1}\left(\frac{z}{z_R}\right) \quad R(z) = z \left(1 + \frac{z_R^2}{z^2}\right)$$



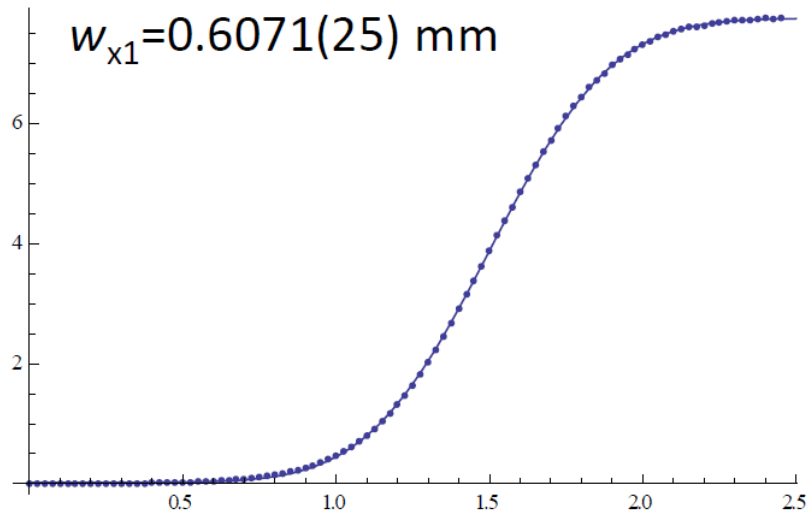
$$k_{eff} = k - \frac{1}{z_R} + \frac{z_0^2}{z_R^3} + \frac{kr^2}{2z_R^2} + \mathcal{O}\left(\frac{z_0^2}{z_R^2}\right)$$

Knife edge  
measured

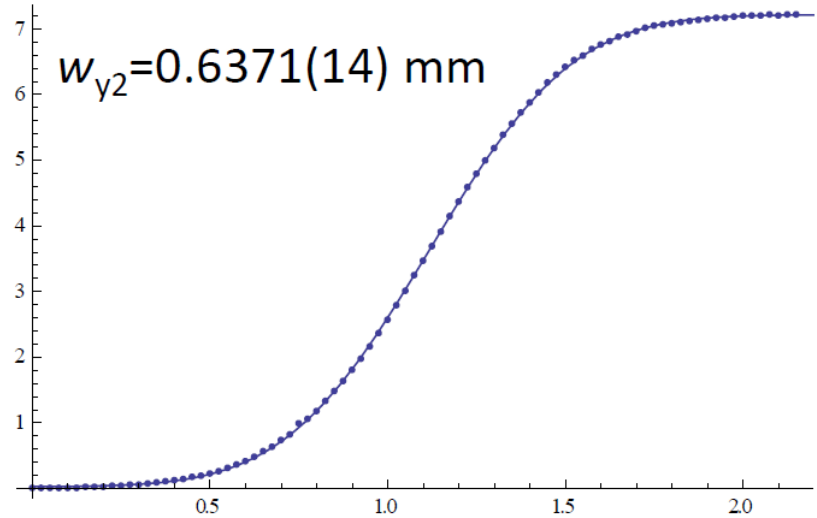
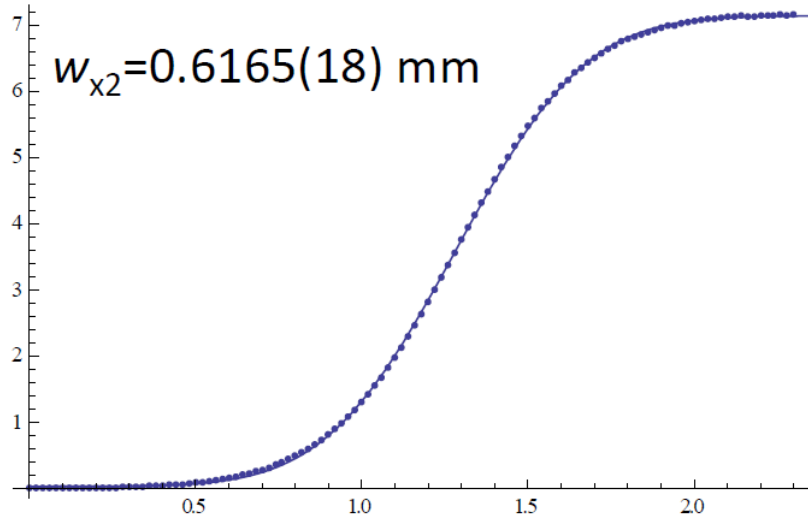
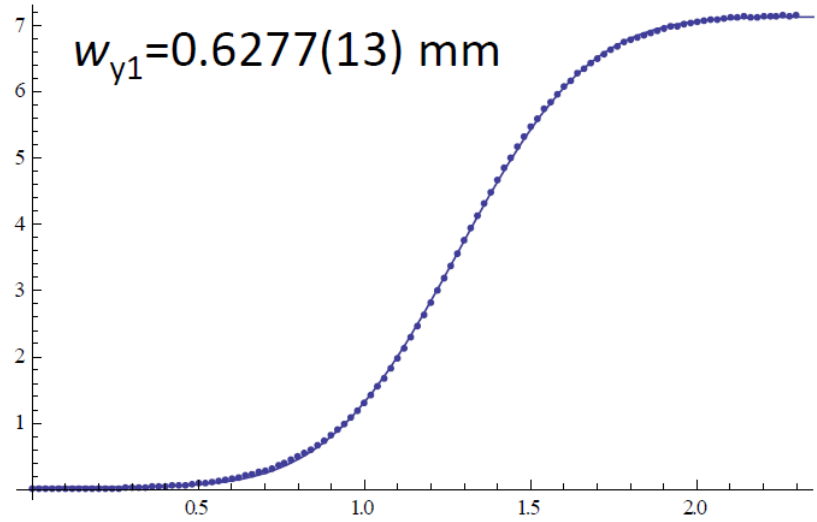
Estimated based on atom  
position using Monte Carlo  
simulation

# Gouy Phase

X

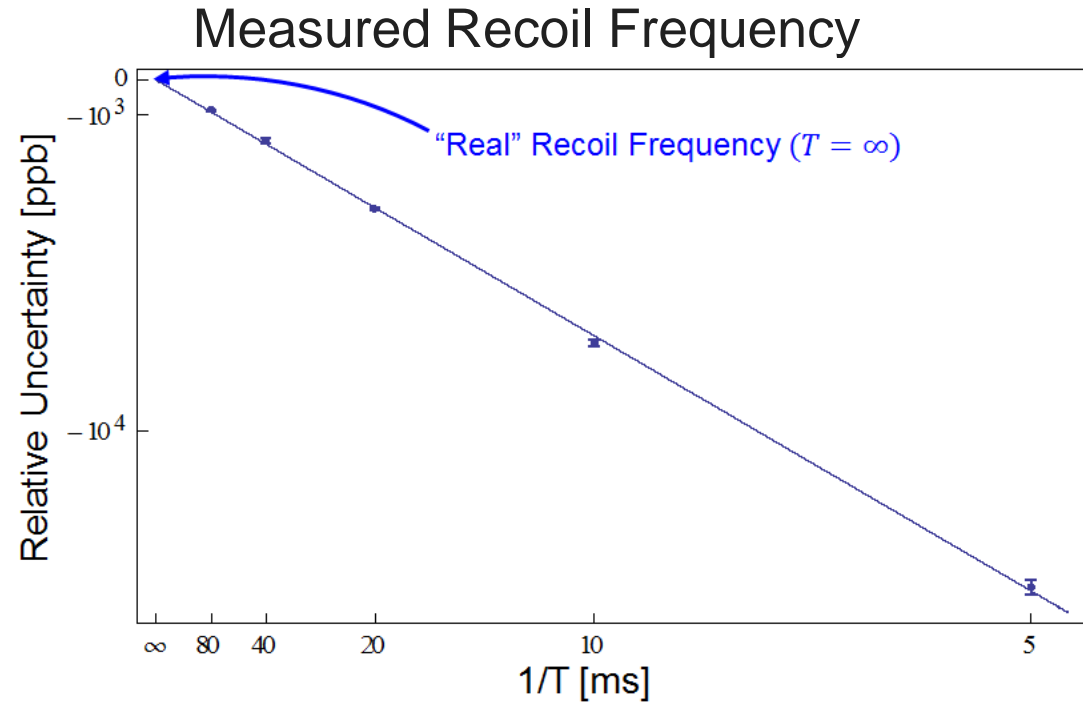
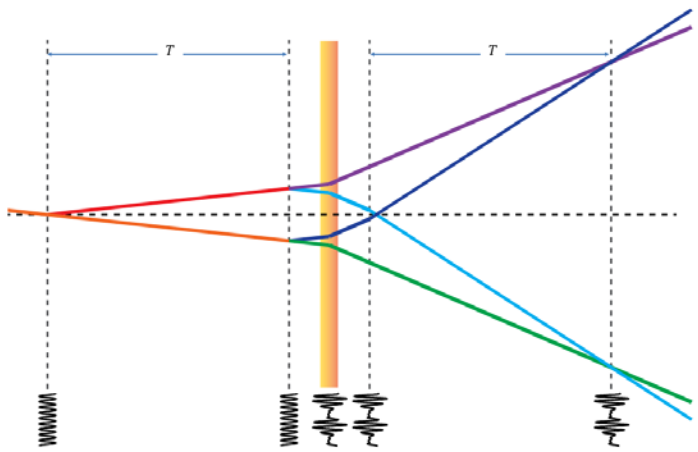


Y



# Diffraction Phase

$$\Delta\Phi_{RB+Bloch} = 16n(n + N)\omega_r T - 2n\omega_m T + \Phi_0$$



Measured Frequency  $\omega_m = 8(n + N)\omega_r + \frac{\Phi_0}{2nT}$

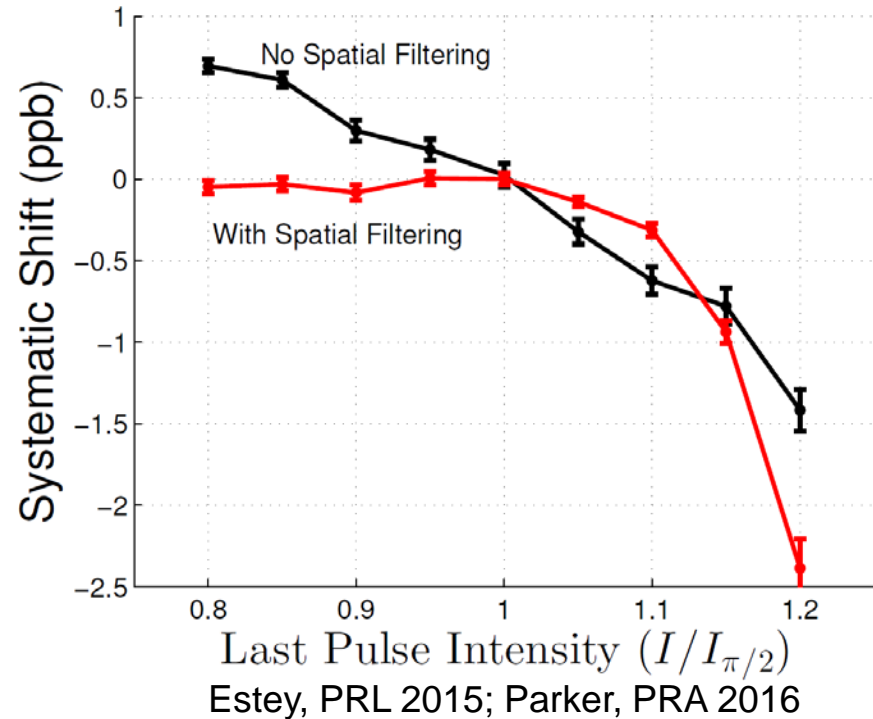
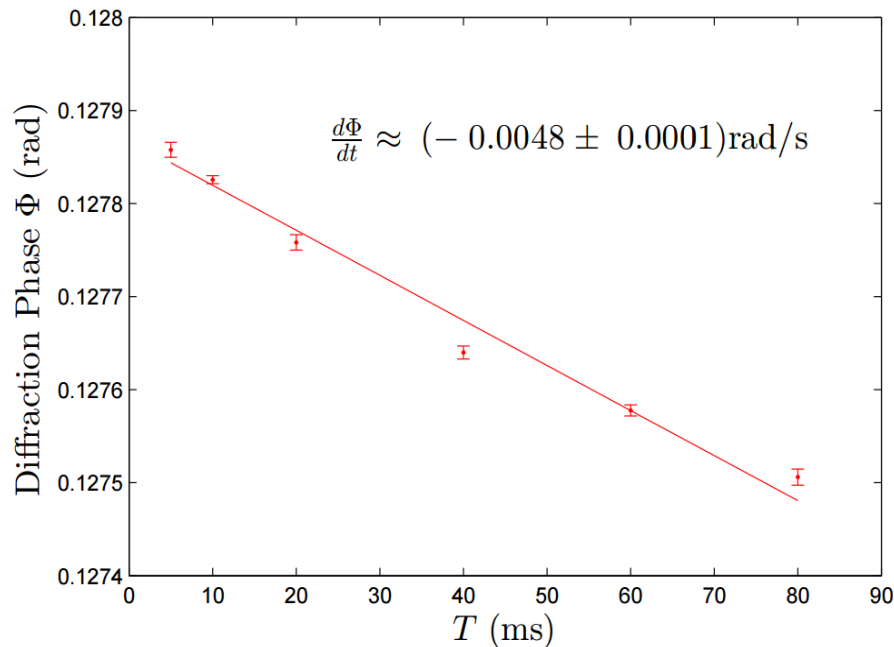
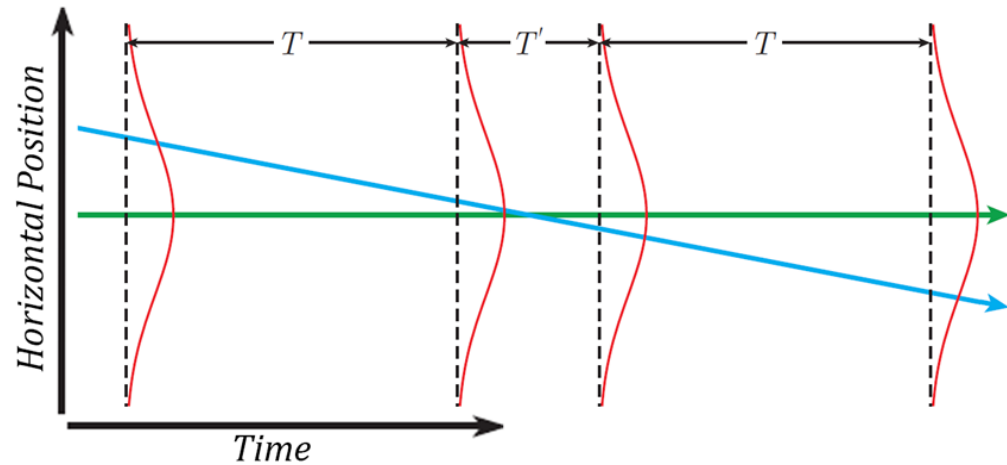
Recoil Frequency  $\omega_r$

Diffraction Phase  $\Phi_0$

# Clipping Phase

$$\Delta\Phi_{RB+Bloch} = 16n(n + N)\omega_r T - 2n\omega_m T + \Phi_0 + \eta T + \dots$$

- Atom Motion  $\rightarrow$  T-dependent diffraction phase
- Sensitive to pulse intensities, detection volume, ...
- 2-point Spatial Filtering
  - Reduce VS waist
  - Reduce detection volume



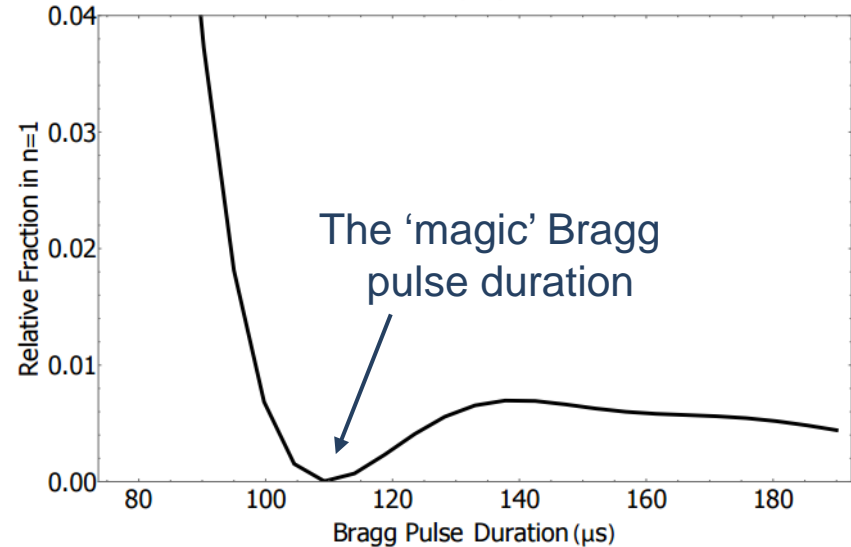
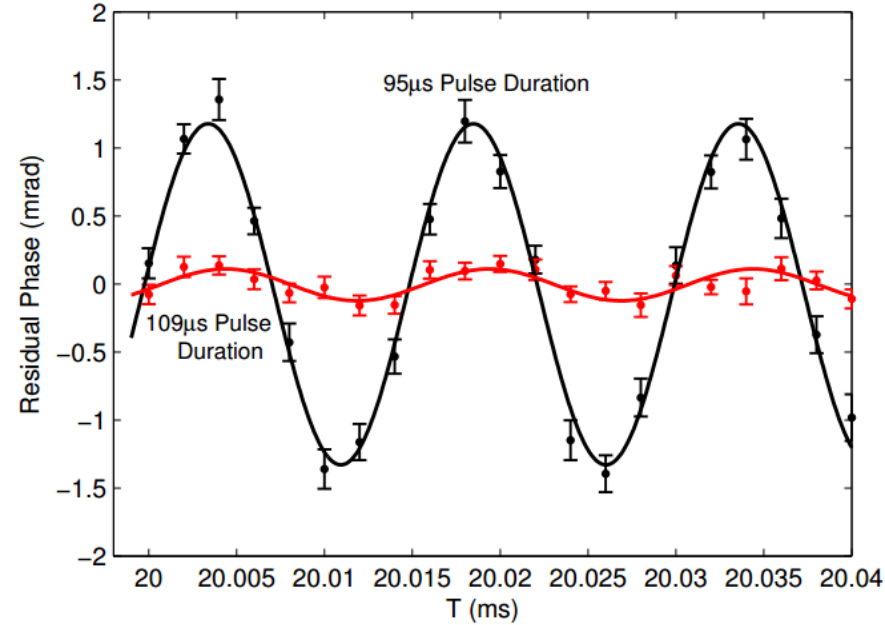
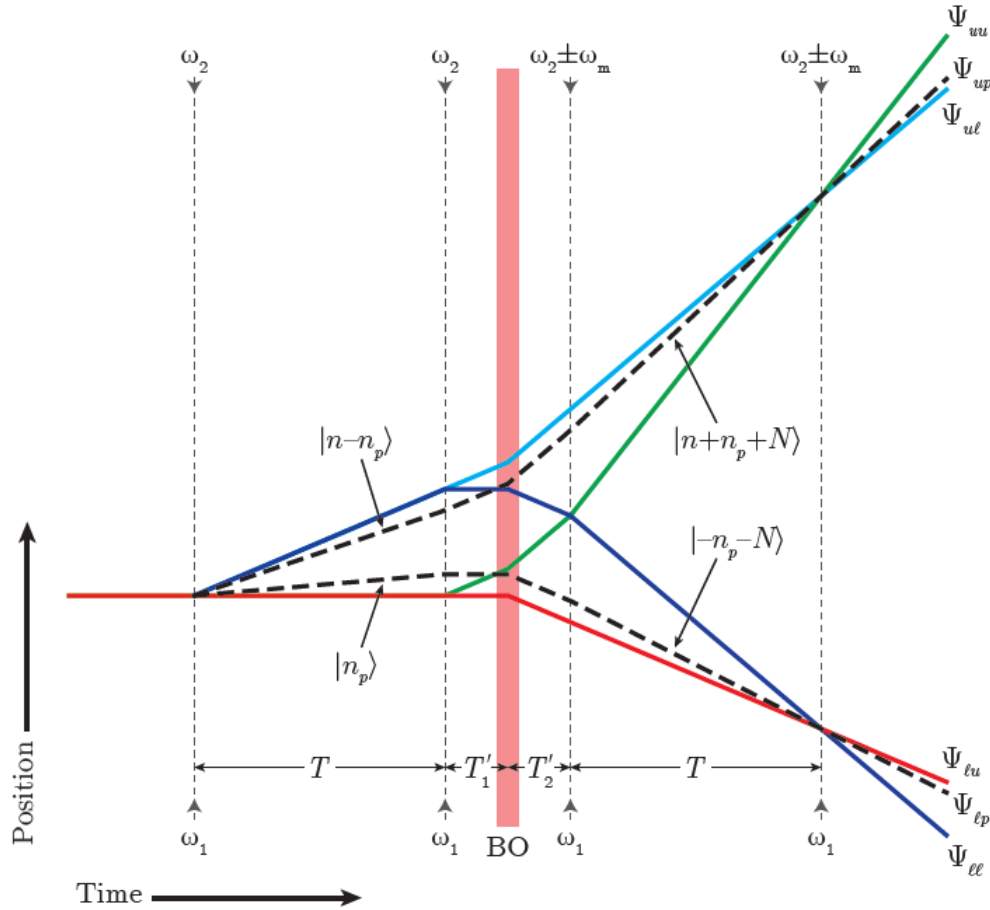


# Atom motion

Effect	Value	$\sigma/\mu$ (ppb)
Cloud radius (mm)	$2.2 \pm 1$	$\pm 0.026$
Vertical velocity width (vr)	$1.5 \pm 0.25$	$\pm 0.031$
Ensemble horizontal velocity (vr)	$0 \pm 0.5$	$\pm 0.032$
Initial horizontal position (mm)	$0 \pm 1$	$\pm 0.034$
Intensity ( $I_{\square 2}$ )	$1.02 \pm 0.02$	$\pm 0.028$
Last pulse intensity ratio	$1.0 \pm 0.02$	$\pm 0.034$

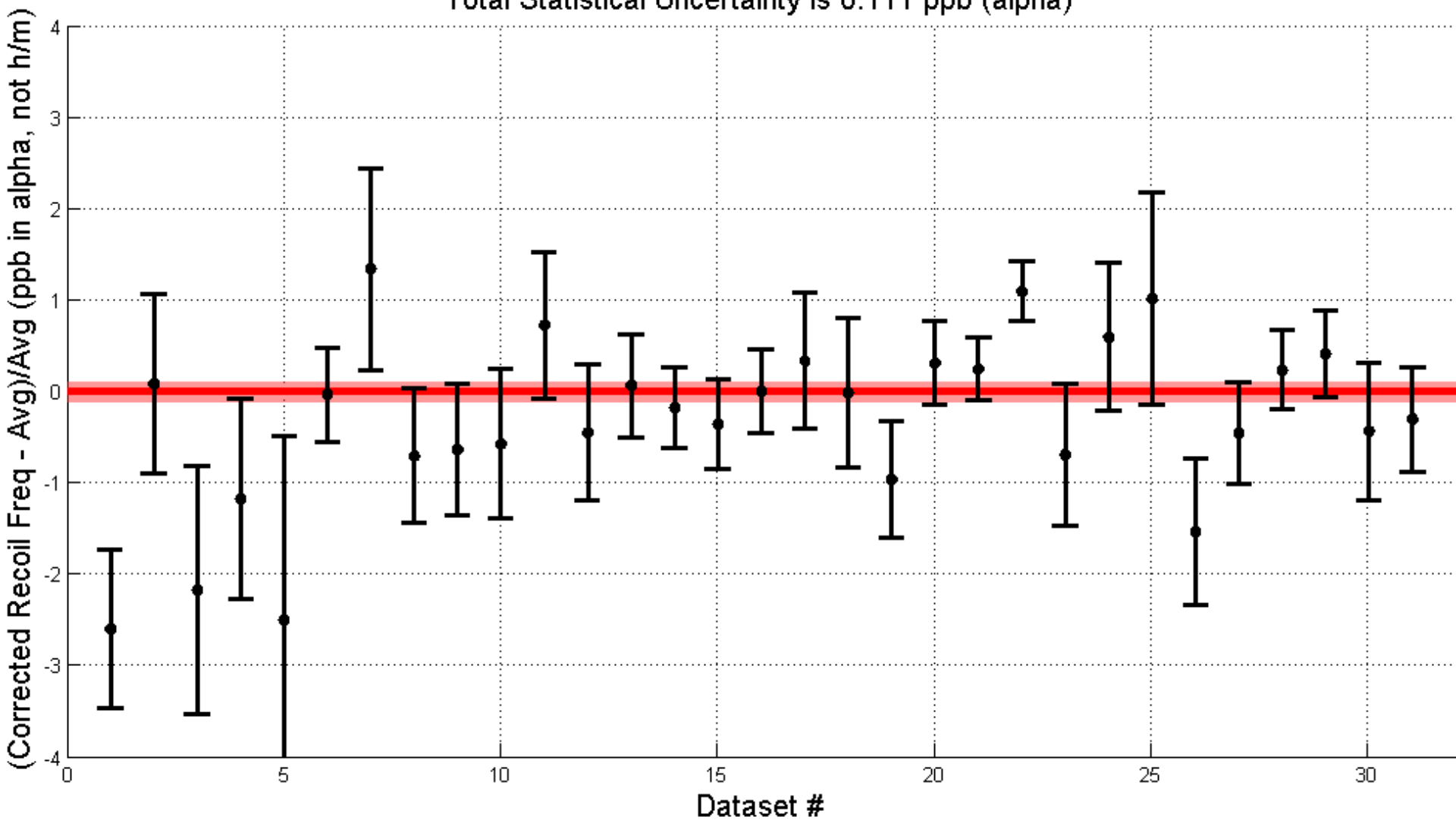
# Parasitic Interferometers

$$\phi_p = \pm 8n_p(n_p + N)\omega_r T \pm n_p\omega_m T + \phi_c(n_p)$$



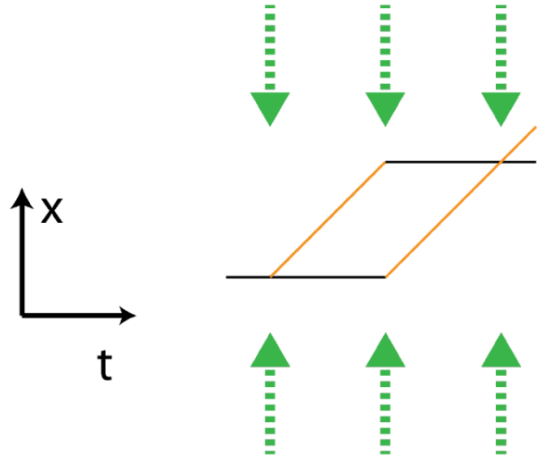
# Recent Data

Total Statistical Uncertainty is 0.111 ppb (alpha)

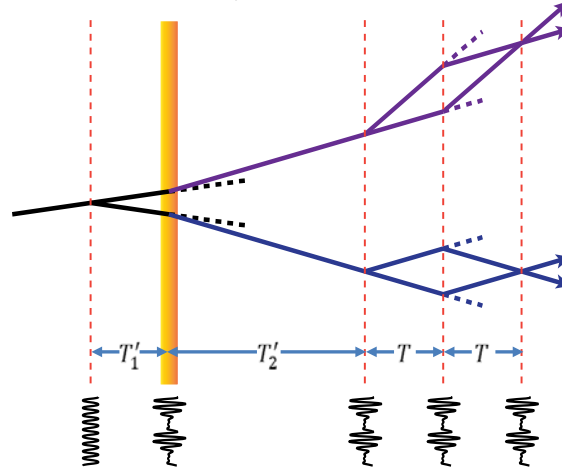


# Matter Wave Interferometry

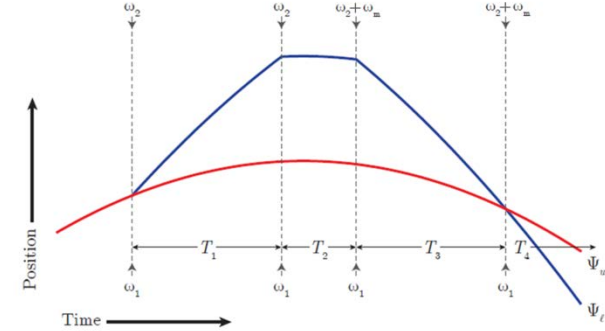
## Local Gravity



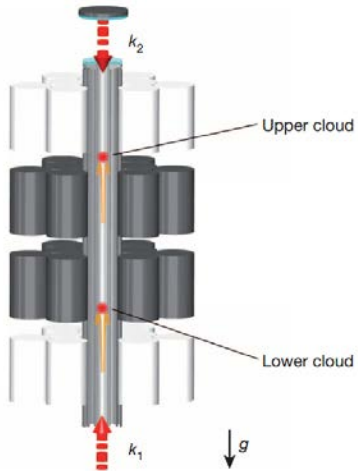
## Gravity Gradients



## Recoil Frequency

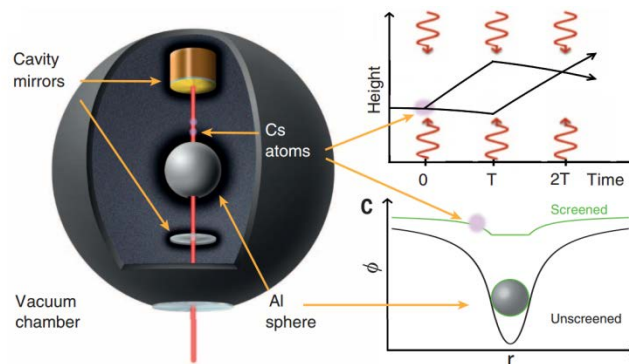


## Newton's G



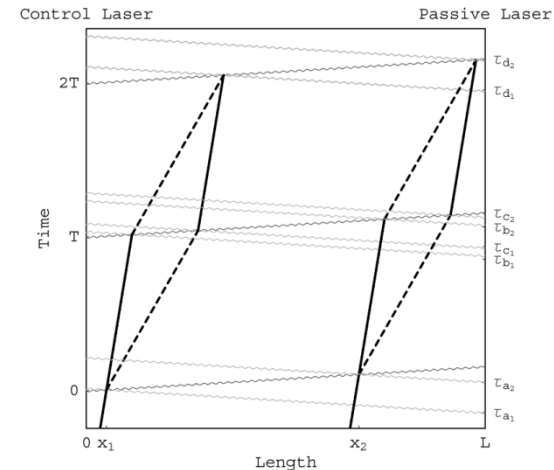
Nature, 510, 518 (2014)

## Dark Energy



Science, 349, 849 (2015)

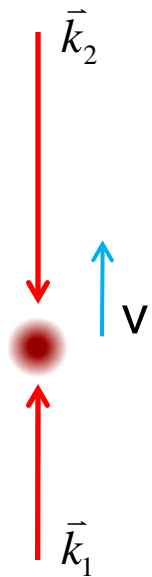
## Gravitational Waves



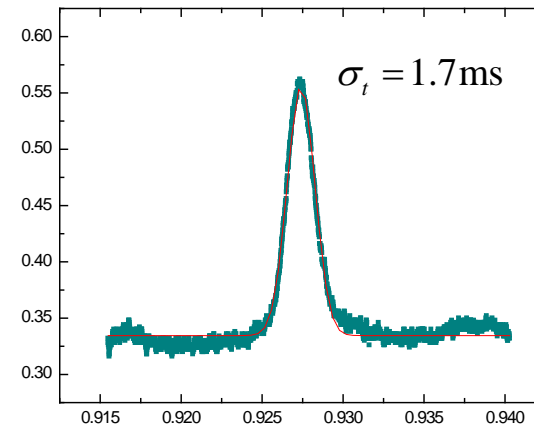
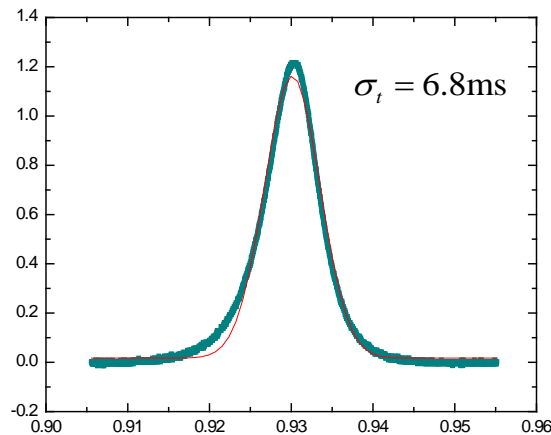
Phys. Lett. B, 678, 1 (2009)



# Velocity Selection



- $2\mu k$  of atoms has velocity spread  $\sim 2\text{cm/sec}$   
After 1s of time of flight, atoms will drift out of interferometer beams
- $100\mu\text{s}$  selection pulse selects about 1/10 of atoms corresponding to hundreds of nK



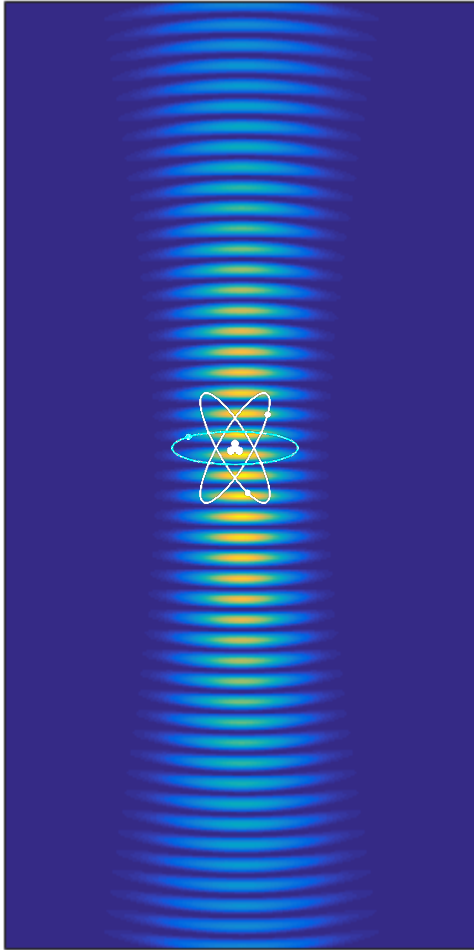
# BO intensity gradient

Six frequencies

$$(I_{\pm}^{\downarrow})' = I_{0,\pm} \frac{z_4 - z_0}{\left(1 + \frac{(z_0 - z_4)^2}{z_R^2}\right)^{3/2} z_R^2},$$

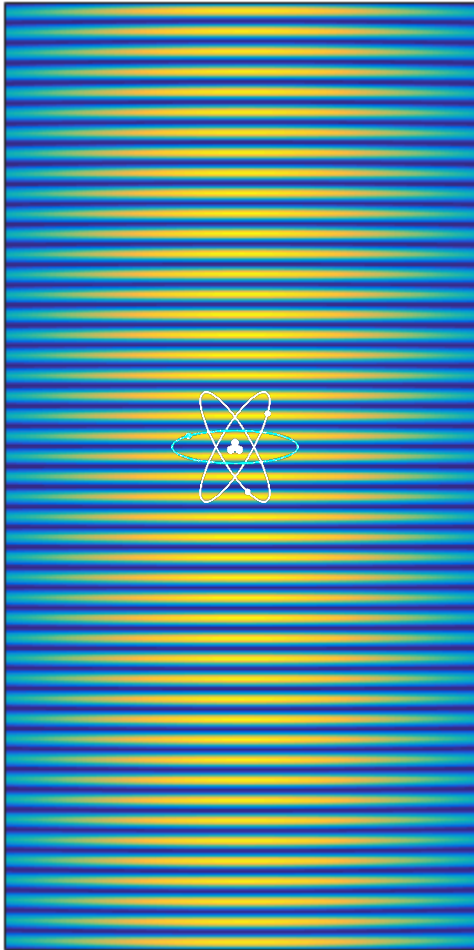
$$\Delta I \approx \left[ (I_+^{\downarrow})' - (I_-^{\downarrow})' \right] d + \tilde{I}'' \delta d + \frac{1}{2} \left[ (I_+^{\downarrow})'' - (I_-^{\downarrow})'' \right] d^2.$$

# Laser beam quality



- 0.3 cm beam radius
- Wavelength errors  $\sim(\lambda/\text{radius})^2$
- Beam splitter losses  $\sim(\lambda/\text{radius})^4$

# A more nearly perfect laser beam

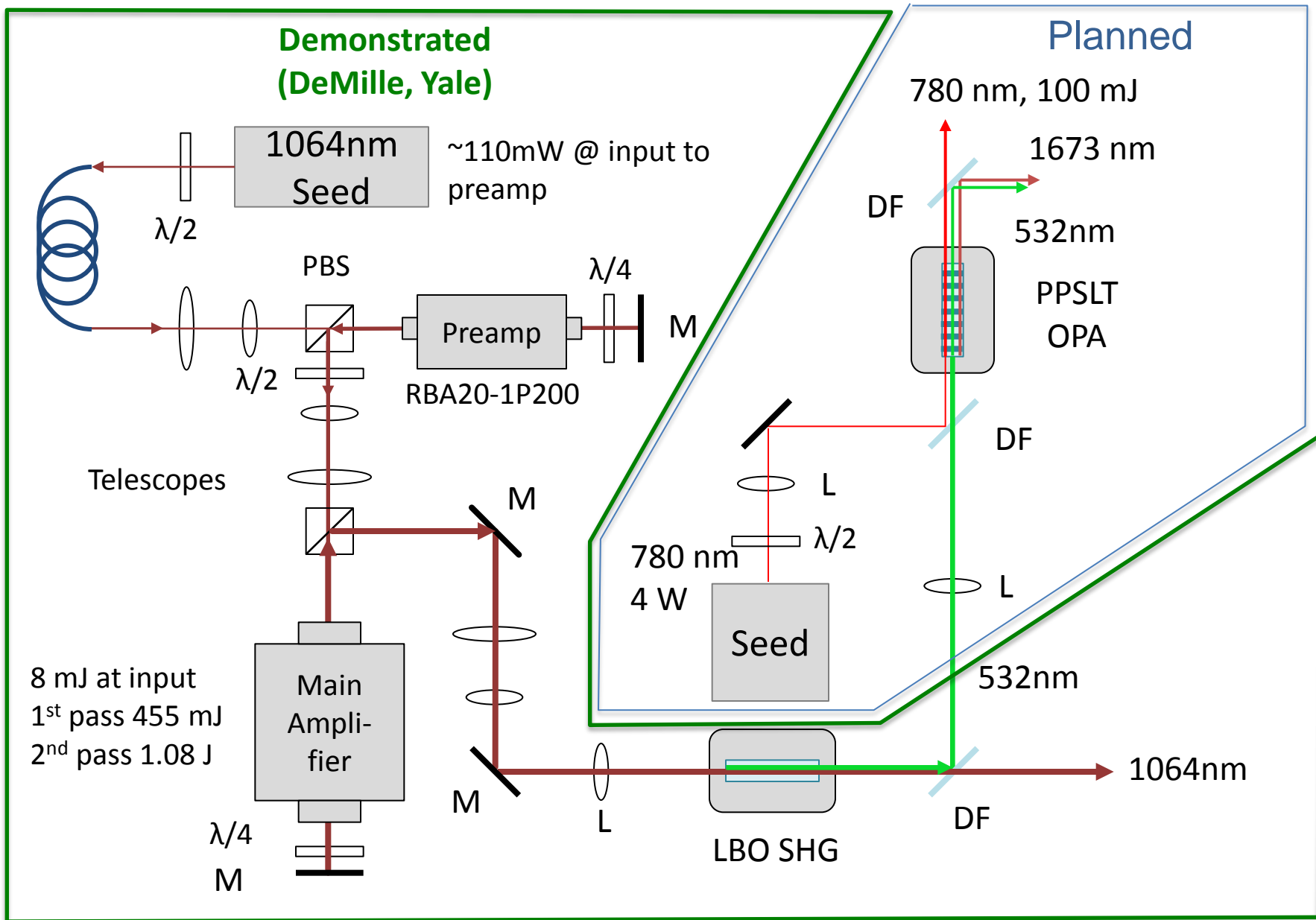


- This project  $\sim 6$  cm radius
- Wavelength errors  $\sim(\lambda/\text{radius})^2$
- 400-fold higher accuracy
- Beam splitter losses  $\sim(\lambda/\text{radius})^4$
- higher momentum transfer, and thus sensitivity

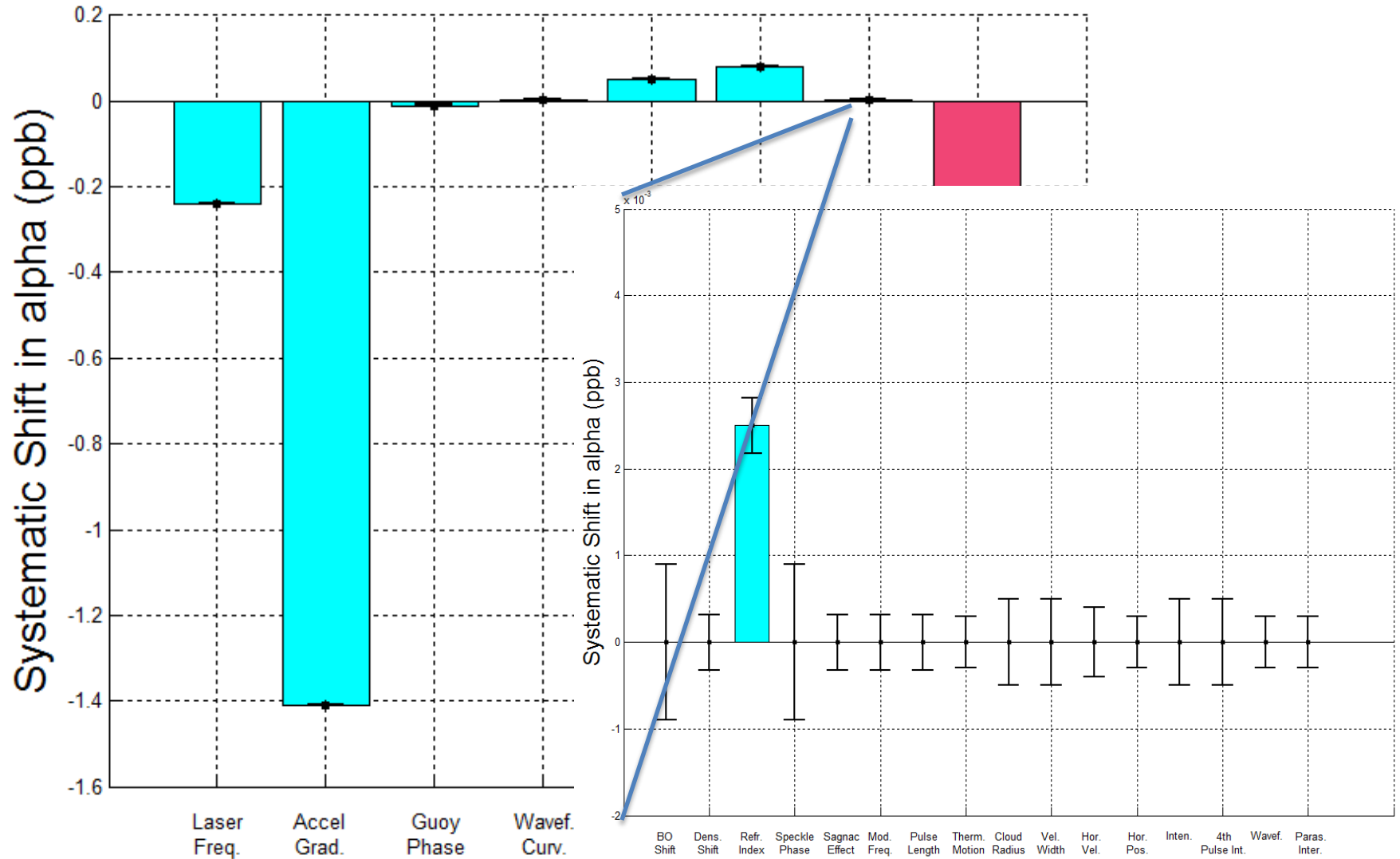
Thick beam will unleash the potential of atom interferometry



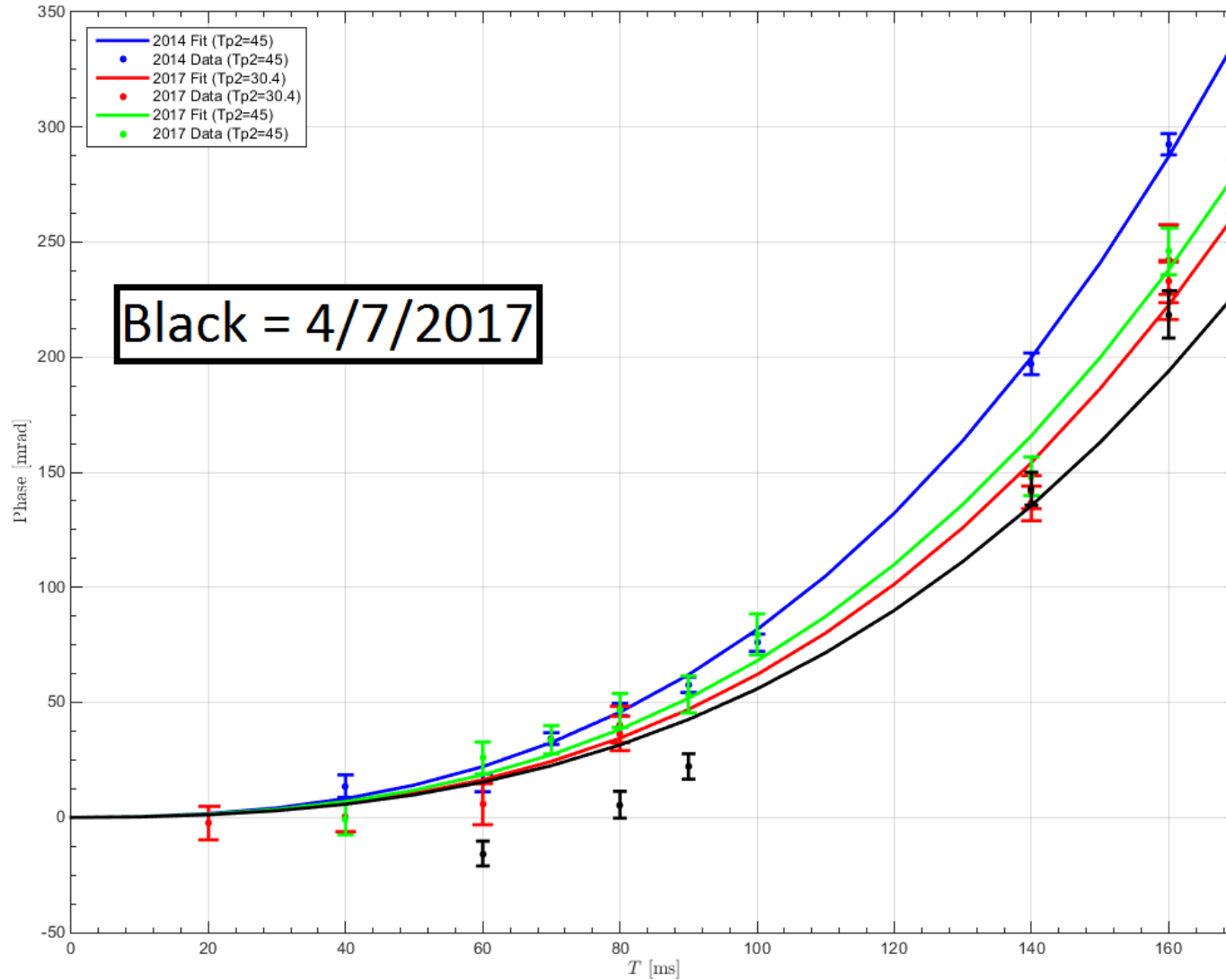
# The death star



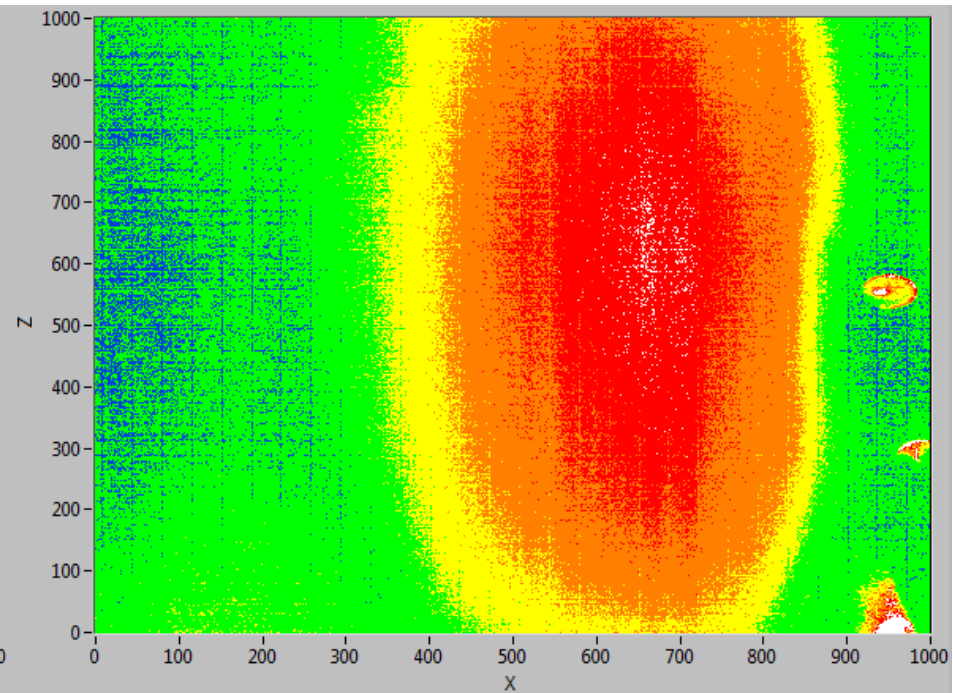
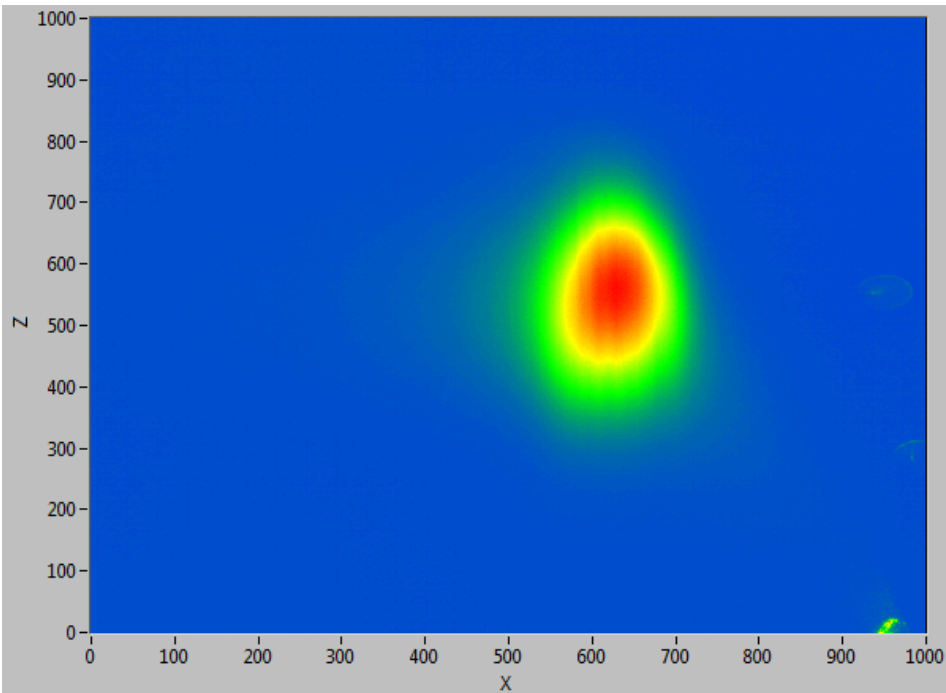
# 0.002 ppb with thick beam



# Gradiometer phase

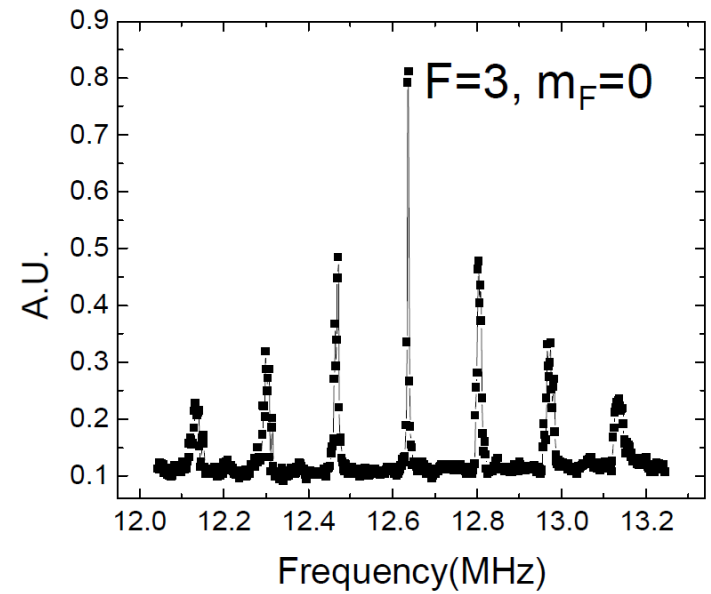
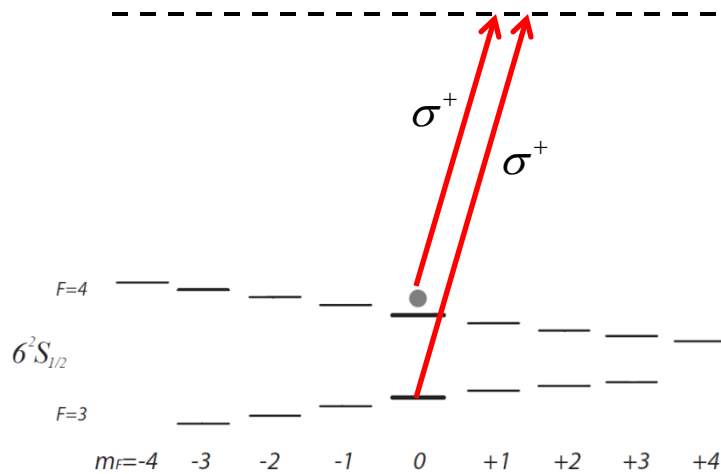
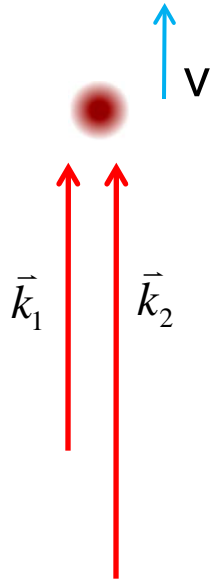


# Atom images

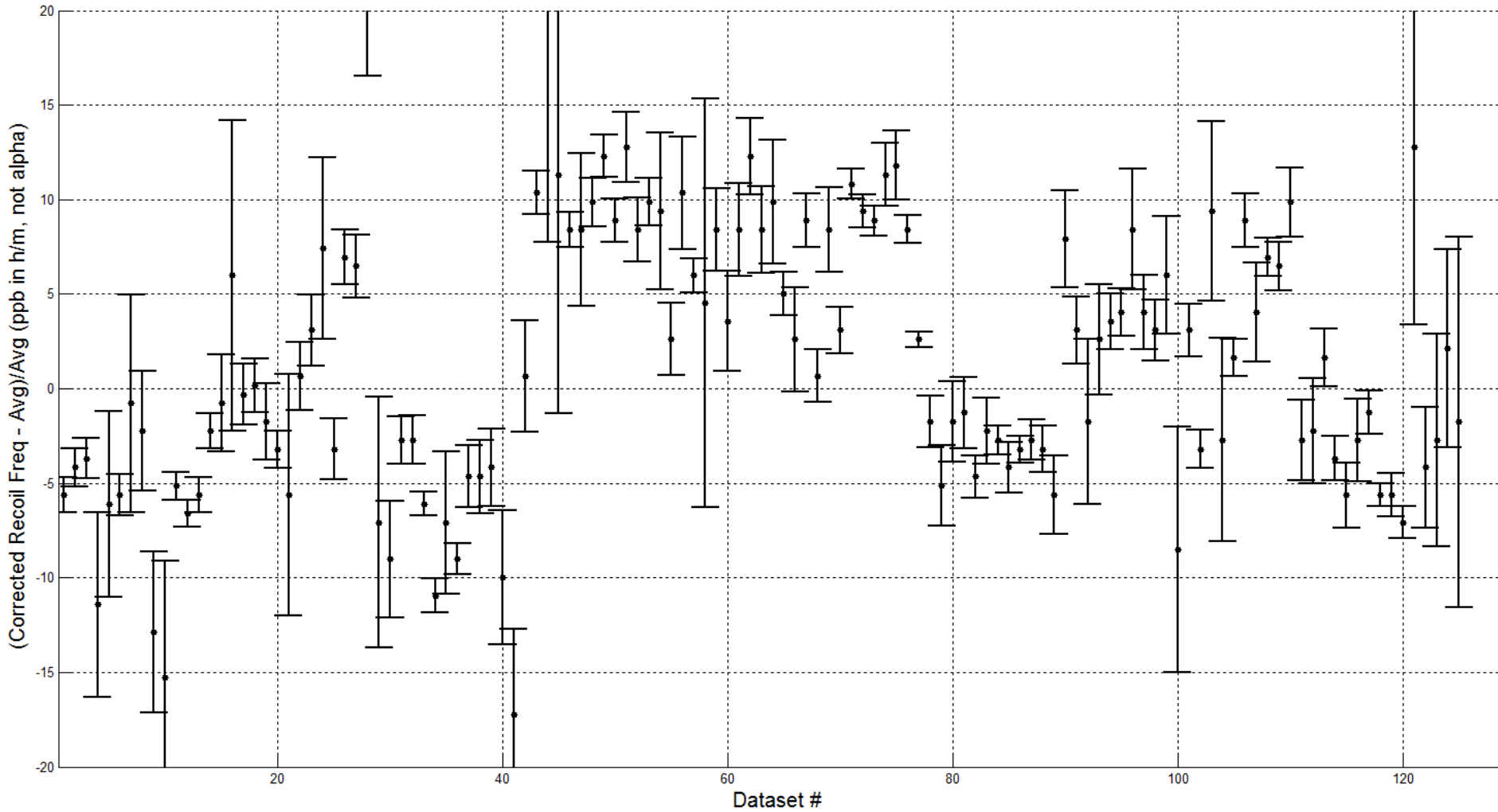




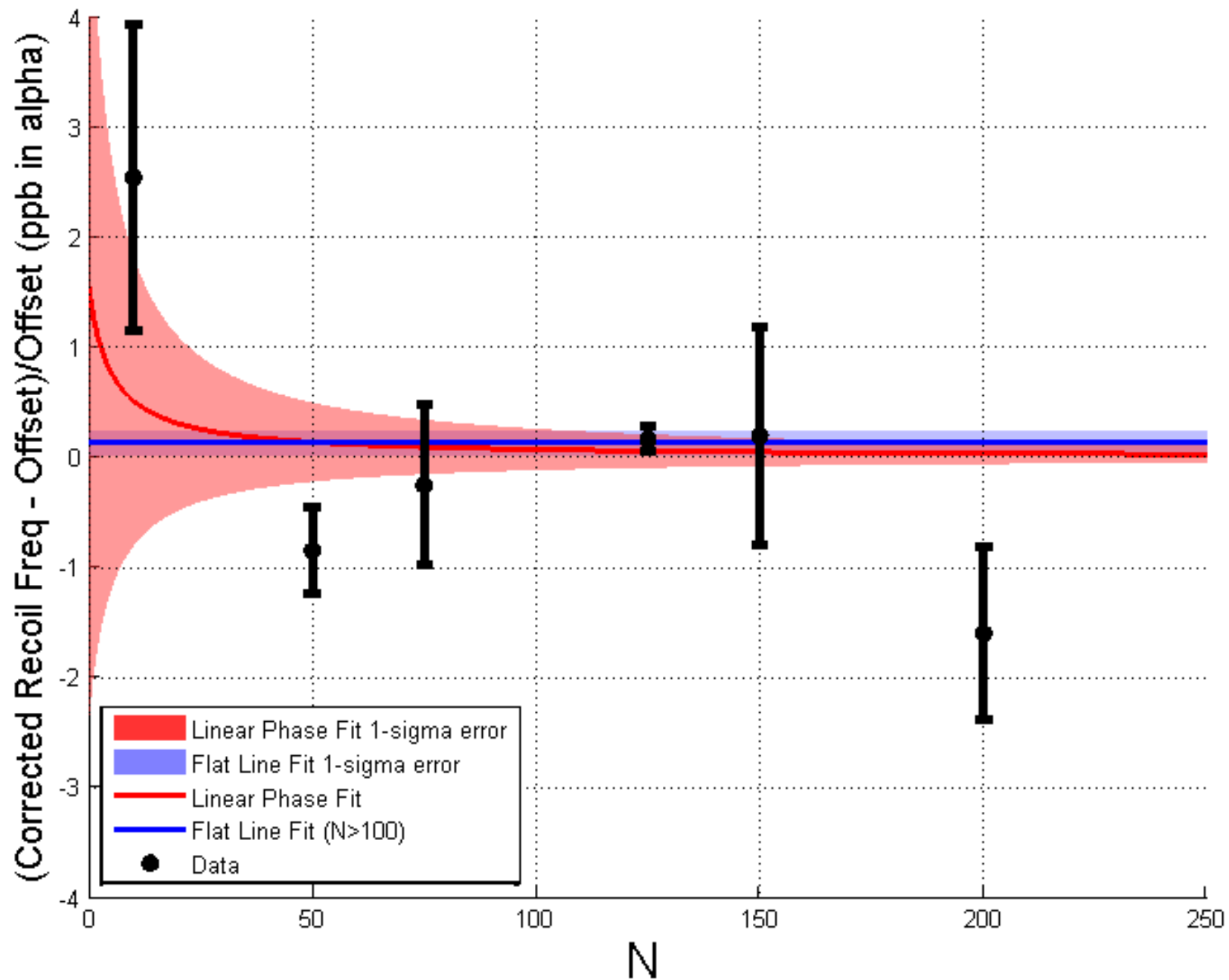
# State Selection



# Ye Olde Data



# $\alpha$ vs Bloch order



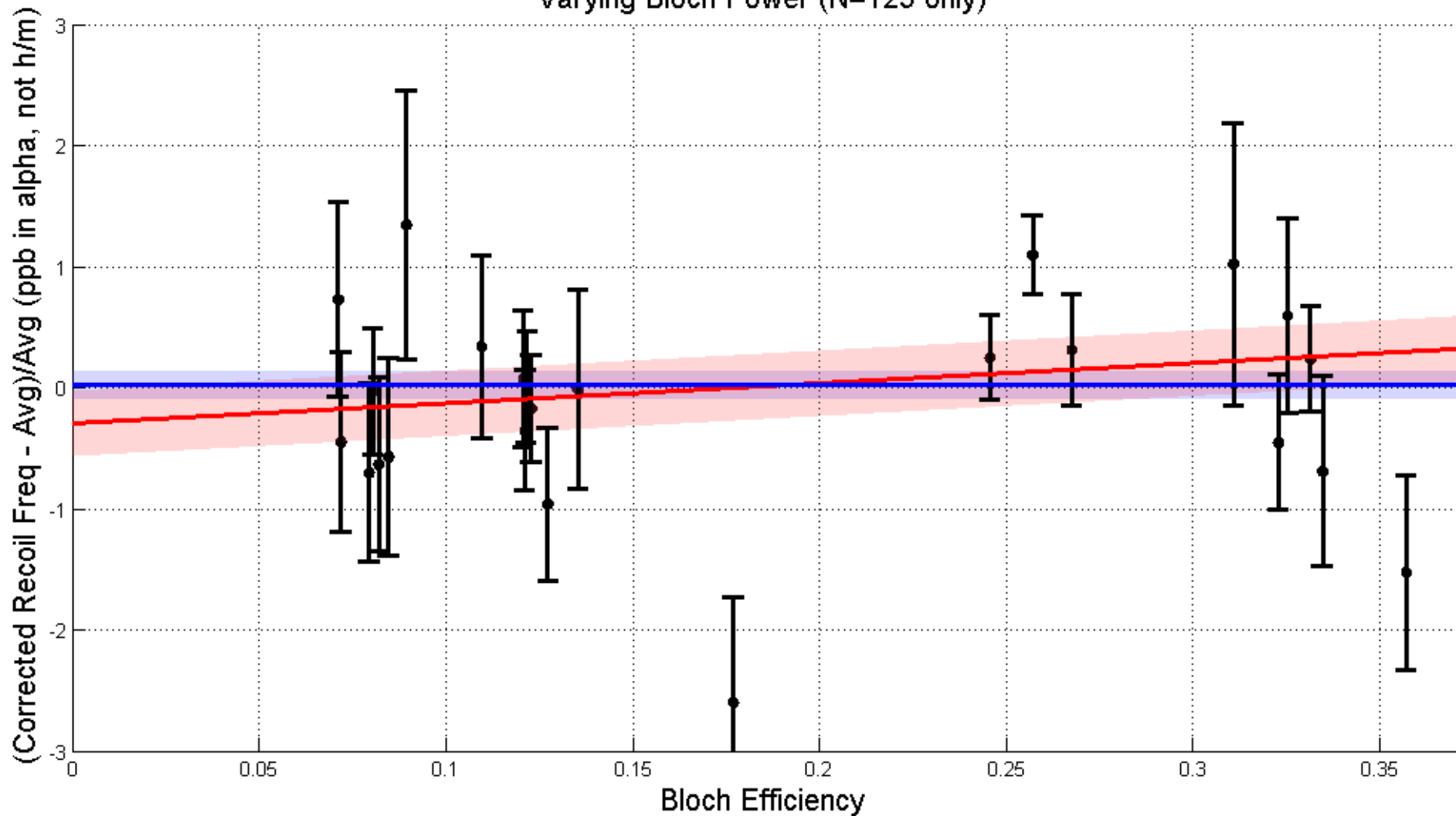
# Clipping systematic vs Bloch order



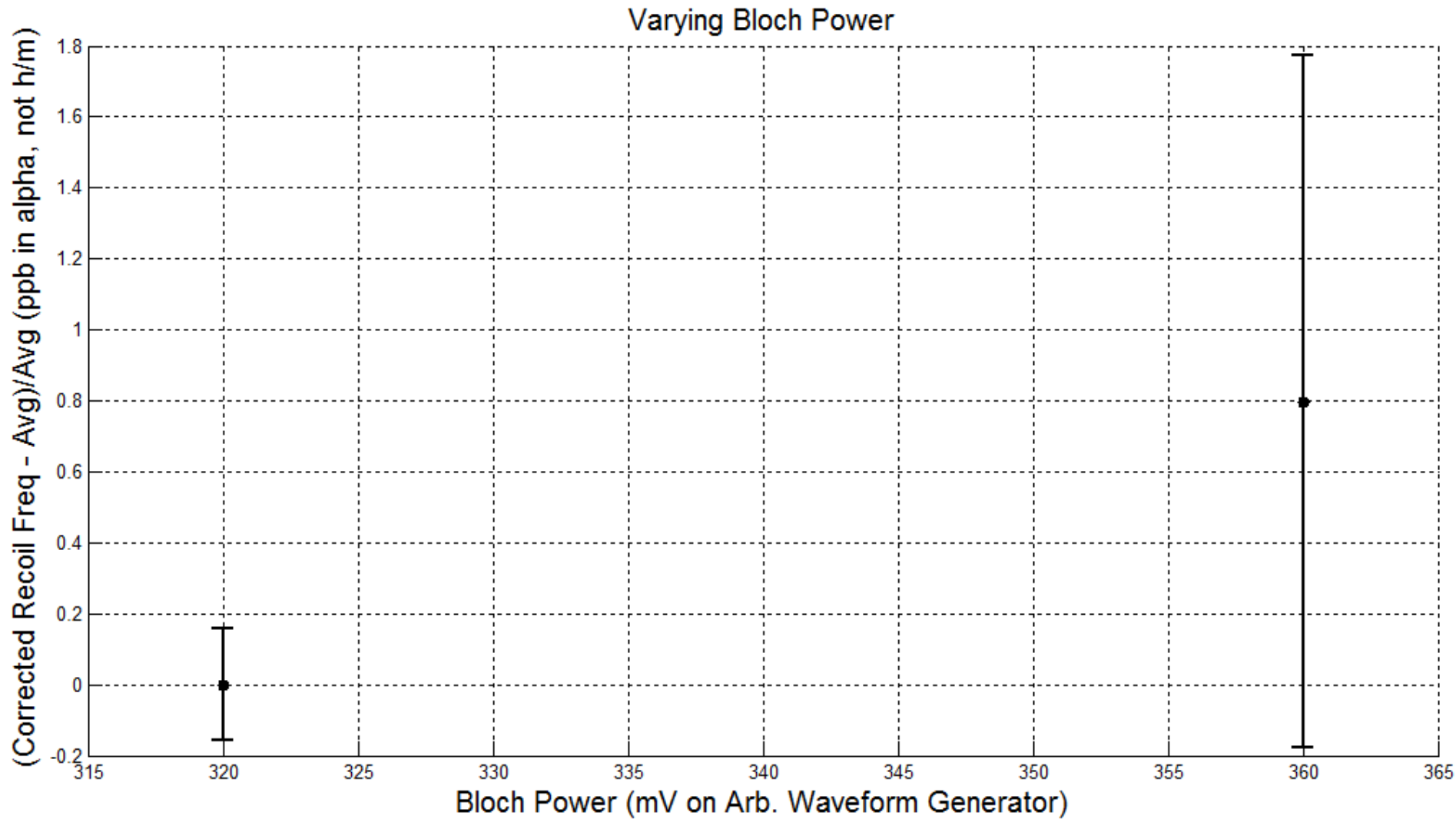


# $\alpha$ vs Bloch power

Varying Bloch Power (N=125 only)

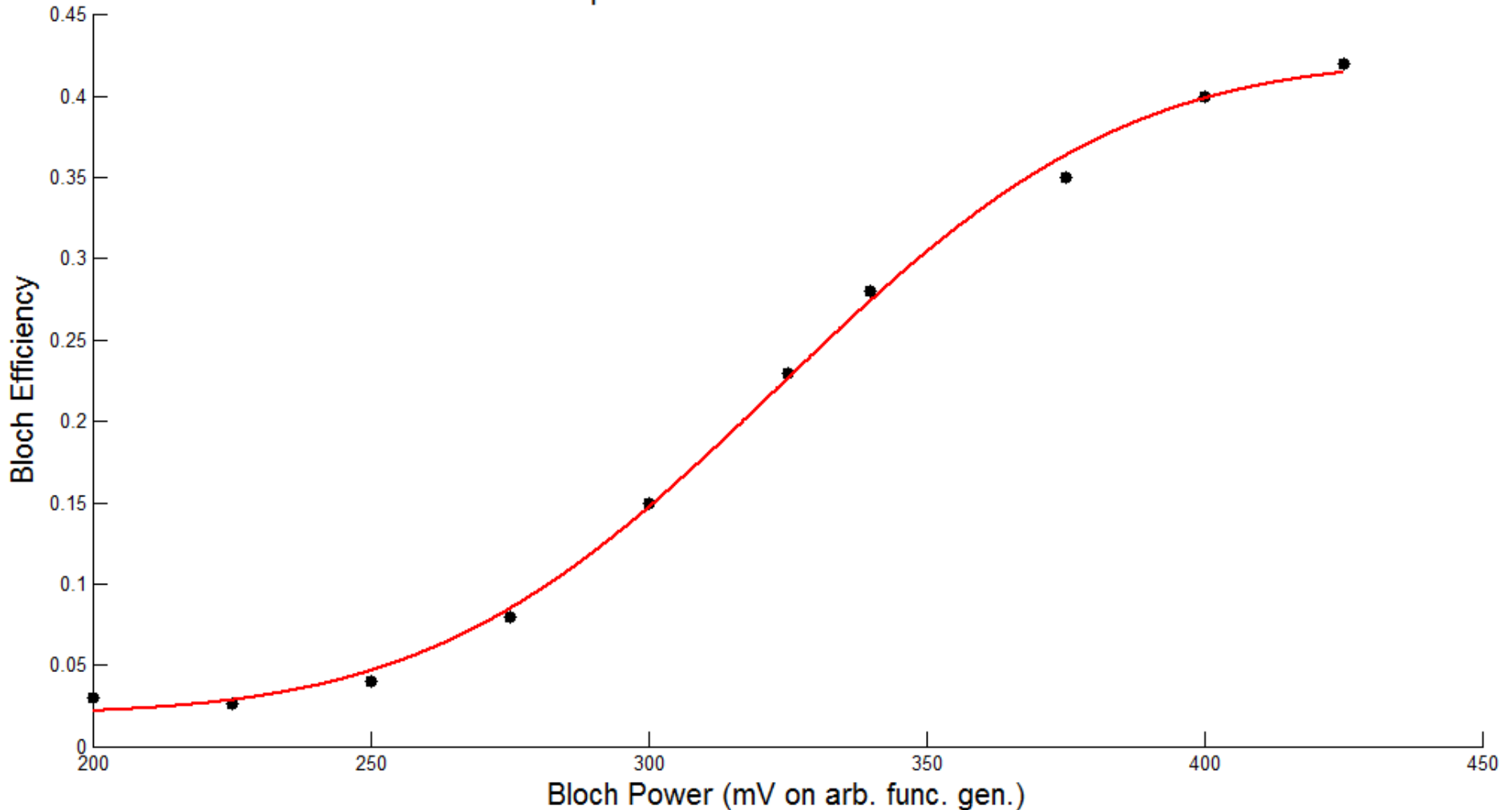


# $\alpha$ vs Bloch Power



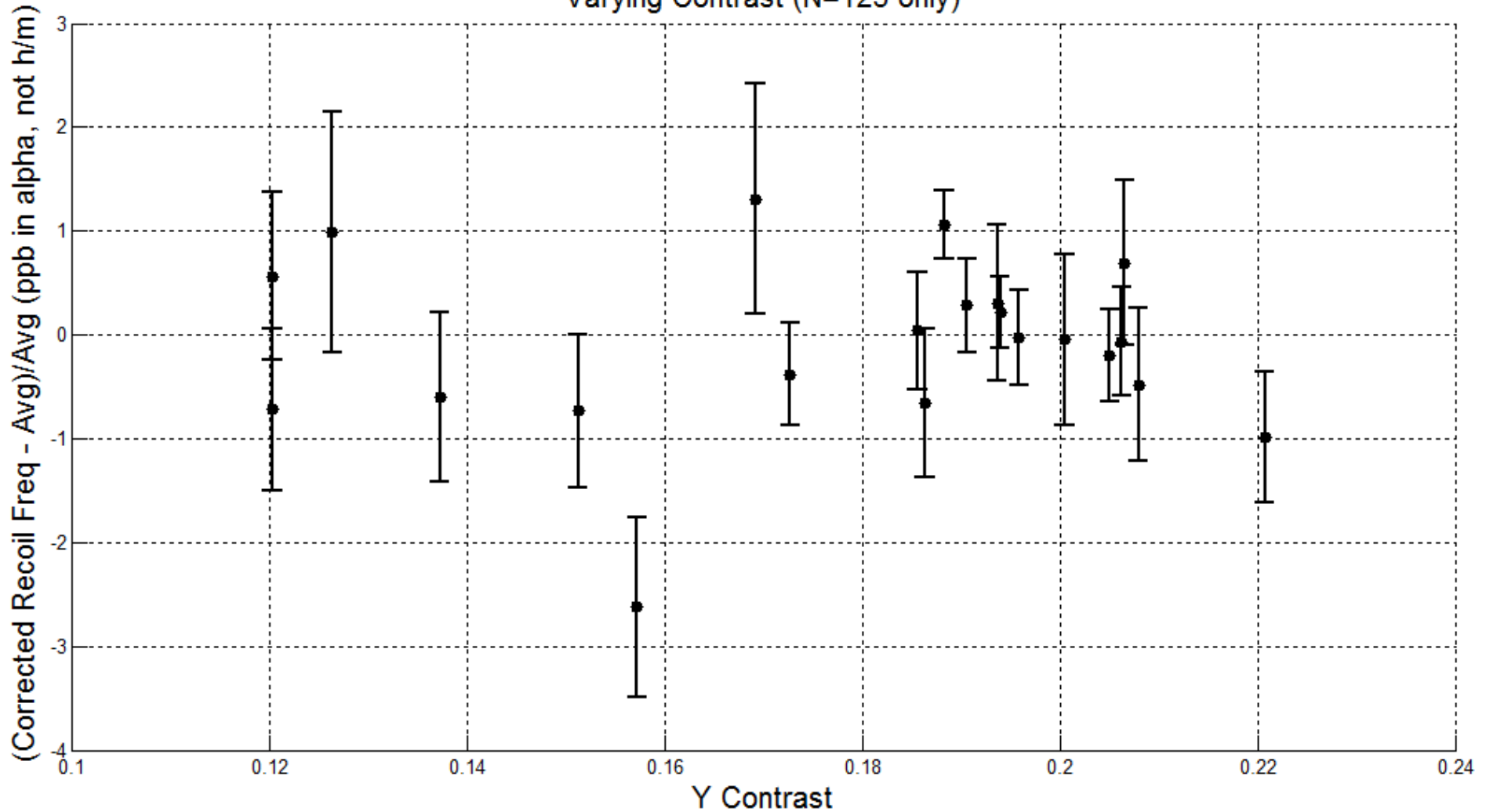
# Bloch efficiency versus power

Empirical Calibration of Bloch Power

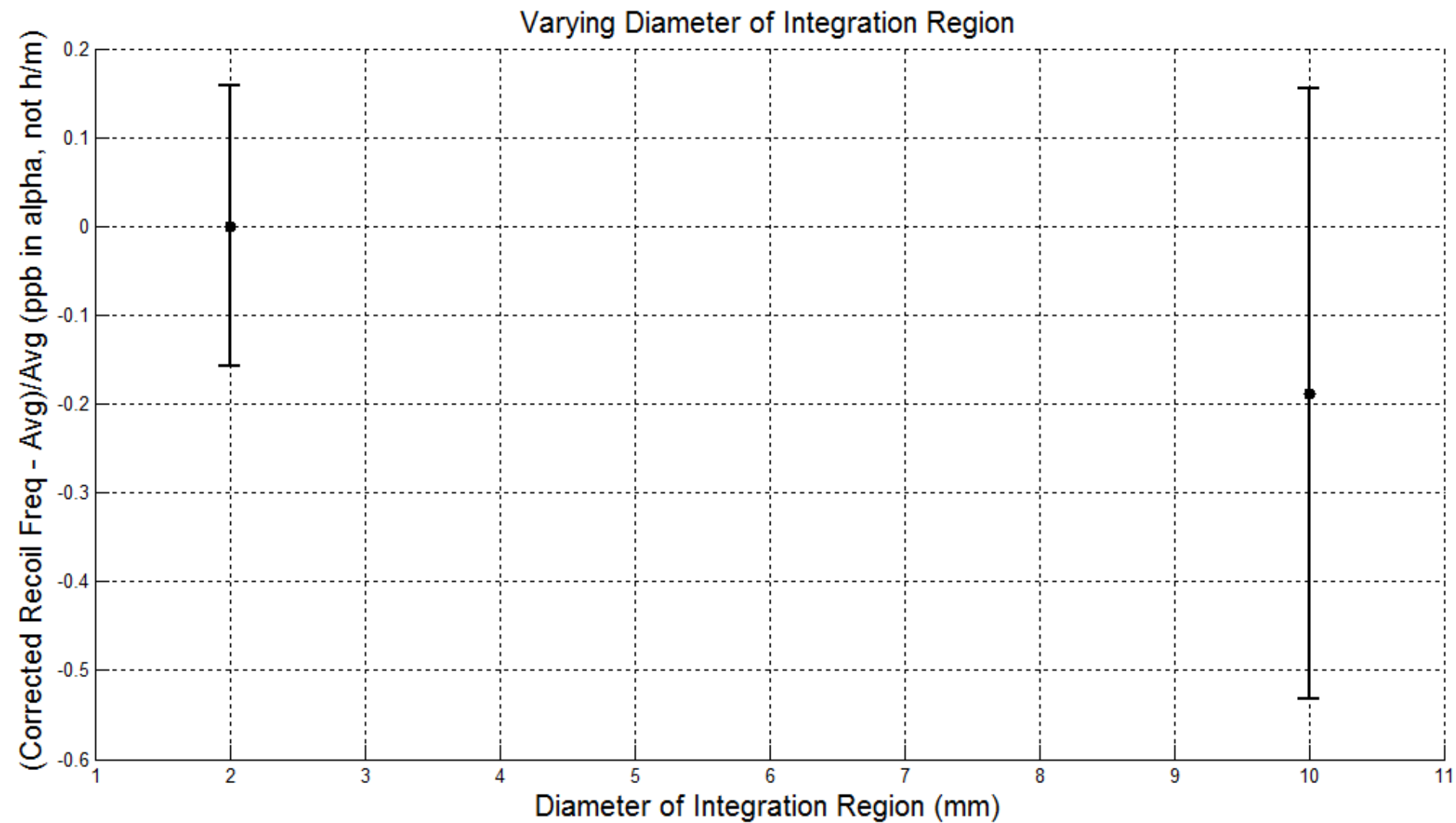


# $\alpha$ vs ellipse contrast

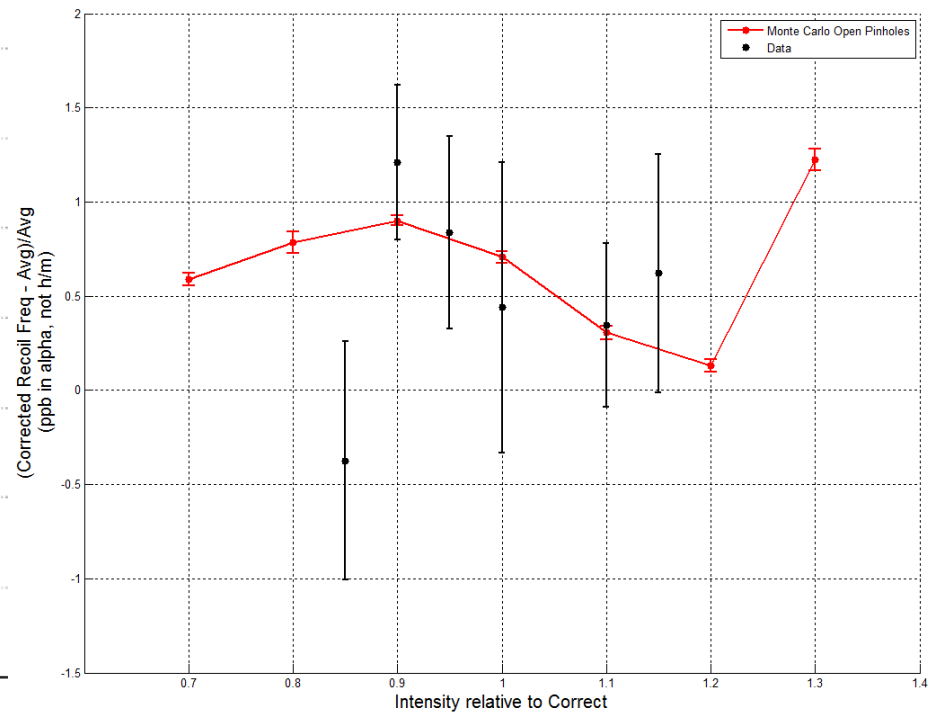
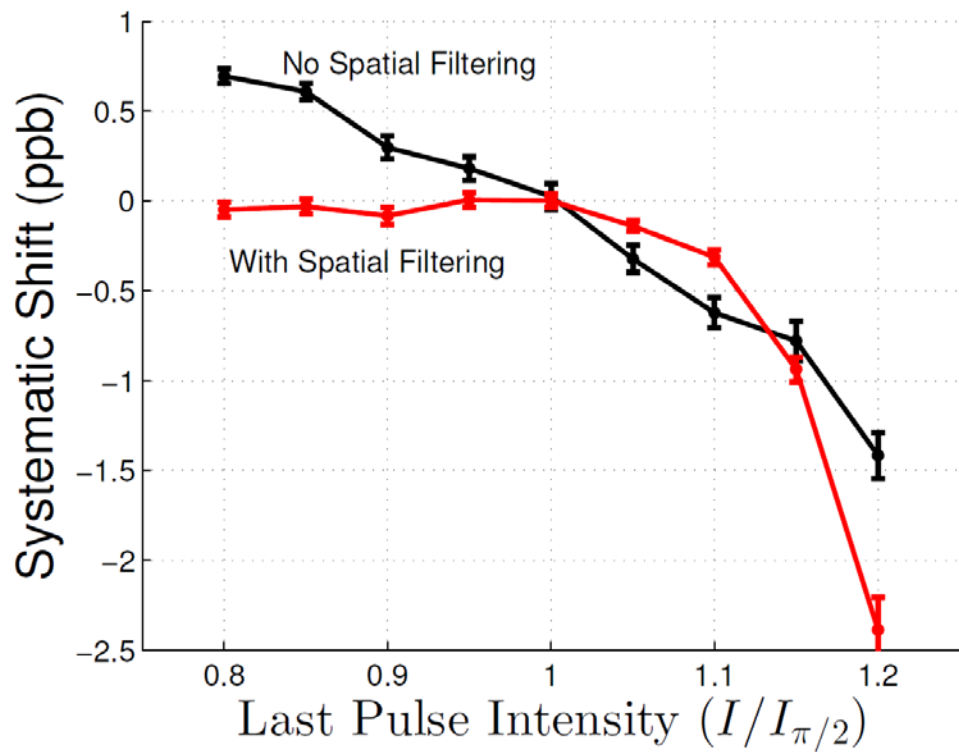
Varying Contrast (N=125 only)



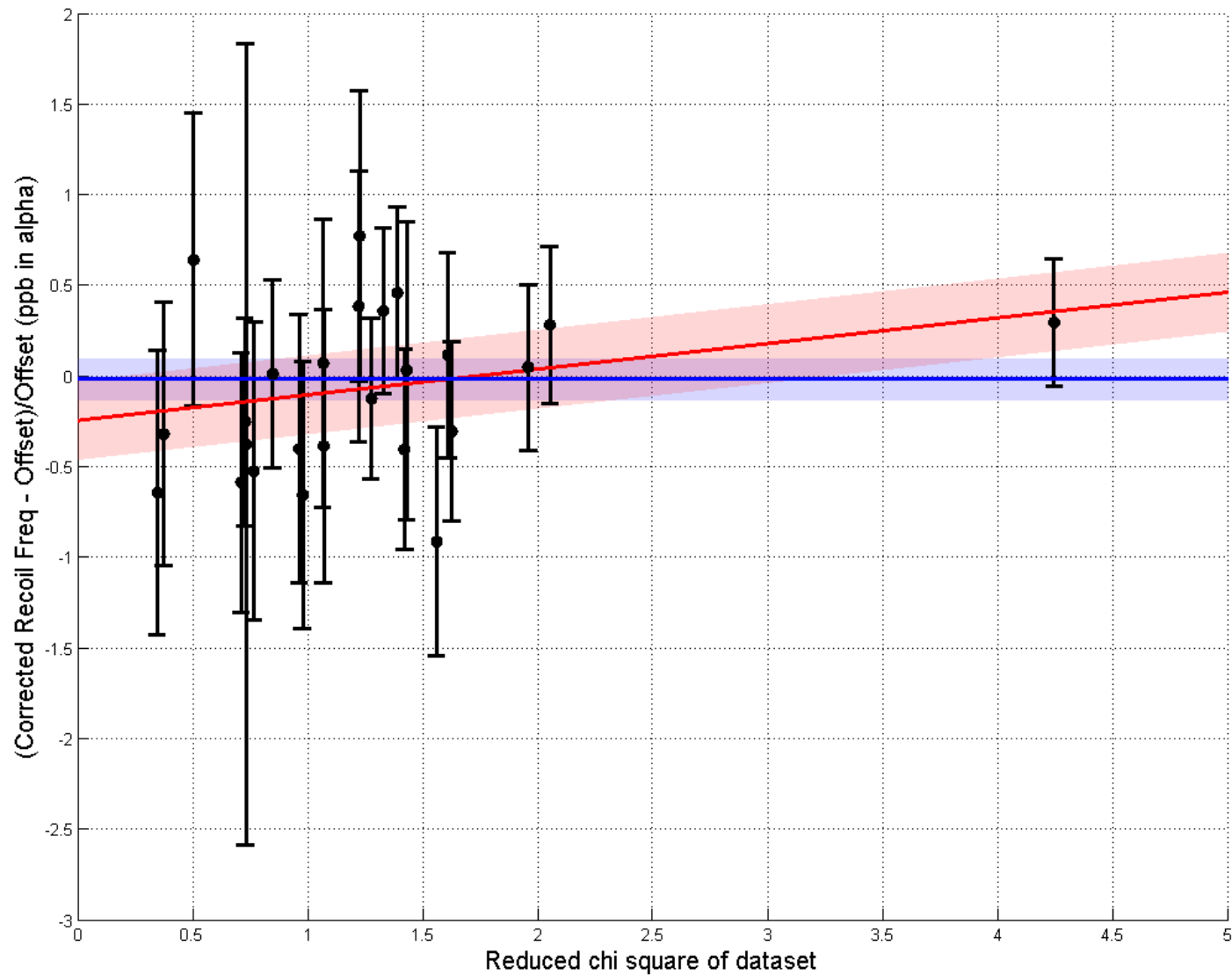
# $\alpha$ vs detection region



# $\alpha$ vs Bragg intensity



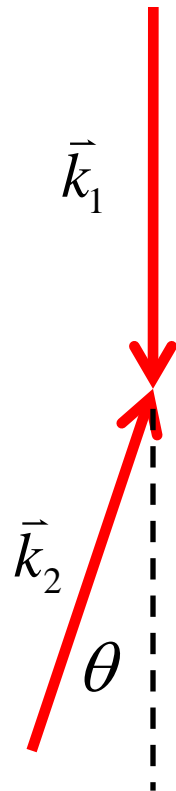
# $\alpha$ vs speckle phase



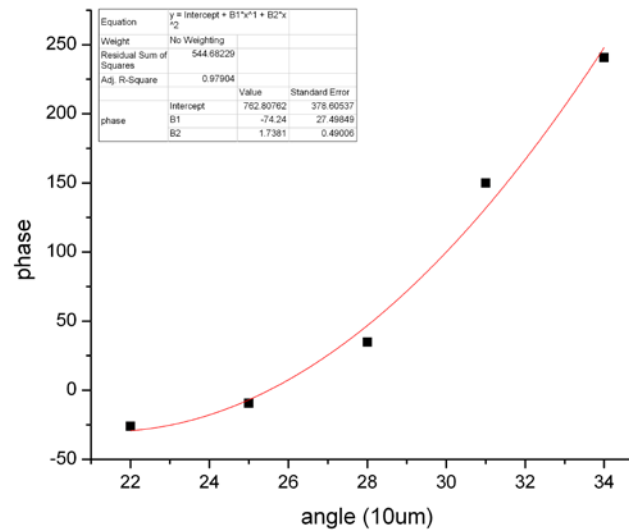


# Systematic Effects

## Beam Misalignment



$$\vec{k}_{eff} = \vec{k}_1 - \vec{k}_2$$
$$|\vec{k}_{eff}|^2 = (2k)^2 \left(1 - \frac{\theta^2}{4}\right)$$





# Experimental Sequence

