

# TRANSVERSITY 2017

5<sup>th</sup> International Workshop on Transverse Polarization  
Phenomena in Hard Processes

INFN - FRASCATI NATIONAL LABORATORIES

December 11-15, 2017

## Partonic dynamics and the 3D structure of the nucleon: a global view

**Jianwei Qiu**

*Theory Center, Jefferson Lab*

**Acknowledgement:** Some of the physics presented here are based on the work of EIC White Paper Writing Committee put together by BNL and JLab managements, ...

**Theory Center**

**Jefferson Lab**  
EXPLORING THE NATURE OF MATTER

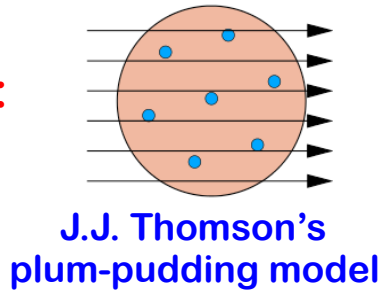
# From 3D atomic structure to quantum world, ...

## □ Atomic structure: dating **back to** Rutherford's experiment :



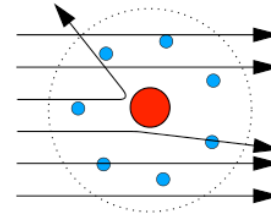
Over 100 years ago

Atom:



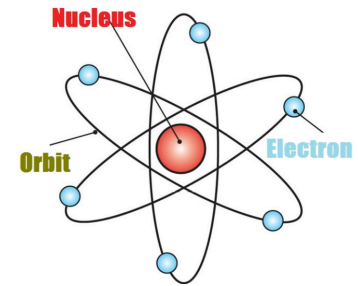
J.J. Thomson's  
plum-pudding model

Experiment



Rutherford's  
Experiment - Data

Theory



Quantum orbitals

**Discovery:** ✧ **Tiny nucleus - *less than 1 trillionth in volume of an atom***  
✧ **Quantum probability - *the Quantum World!***

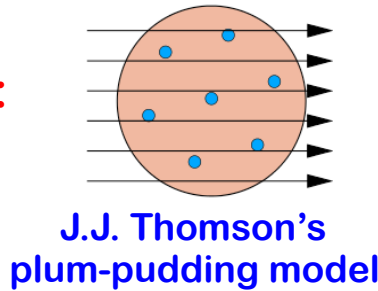
# From 3D atomic structure to quantum world, ...

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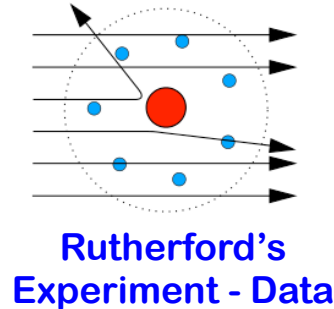


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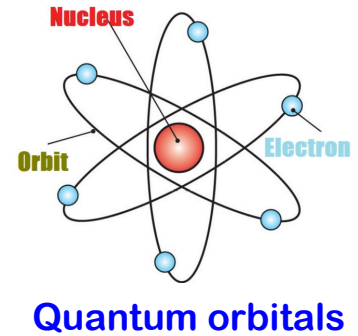
Atom:



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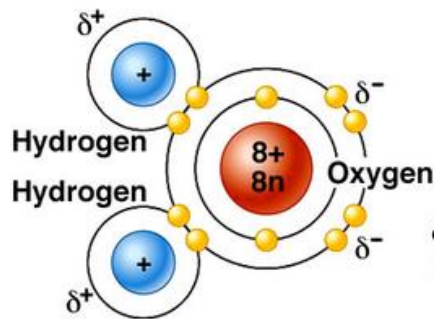


Discovery: ✧ Tiny nucleus - *less than 1 trillionth in volume of an atom*

✧ Quantum probability - *the Quantum World!*

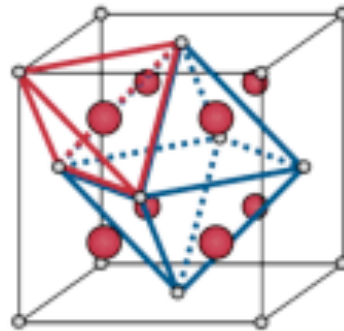
## Localized mass and charge centers – vast “open” space:

Molecule:



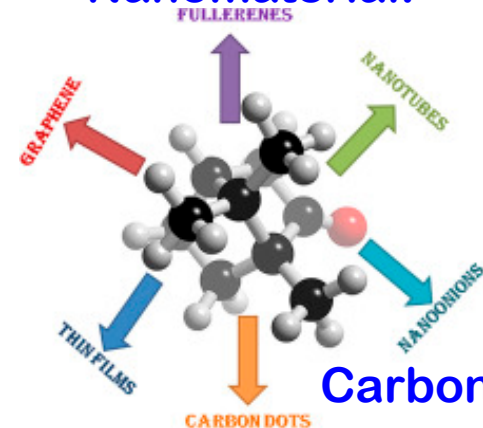
“Water”

Crystal:



Rare-Earth metal

Nanomaterial:



Carbon-based

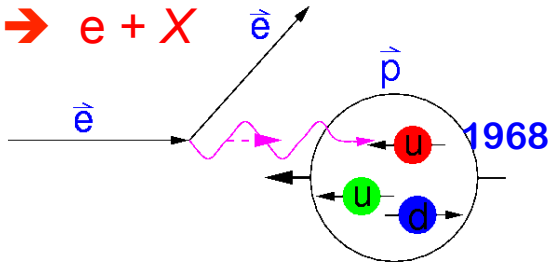


*Infinite opportunities to create & improve ... !*

# From 3D hadron structure to QCD, ...

## □ A modern “Rutherford” experiment (about 50 years ago):

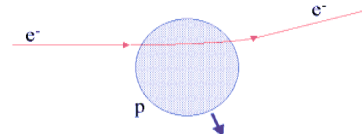
Nucleon: *The building unit of all atomic nuclei*



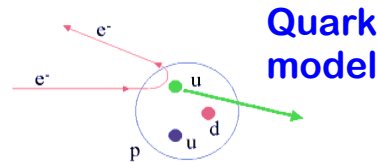
→ *Discovery of quarks!*

### Prediction

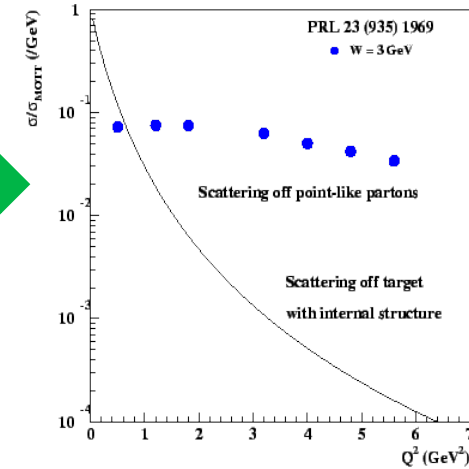
◆ If proton “charge cloud”:



◆ If proton contains point charges, some of time see:



### Discovery

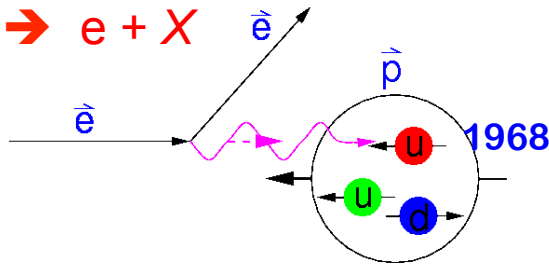


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## □ A modern “Rutherford” experiment (about 50 years ago):

**Nucleon:** *The building unit of all atomic nuclei*

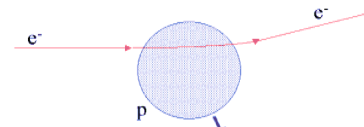
$$e + p \rightarrow e + X \quad \vec{e}$$



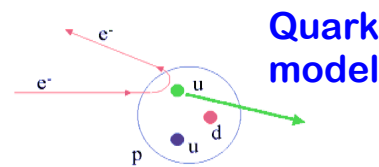
➔ **Discovery of quarks!**

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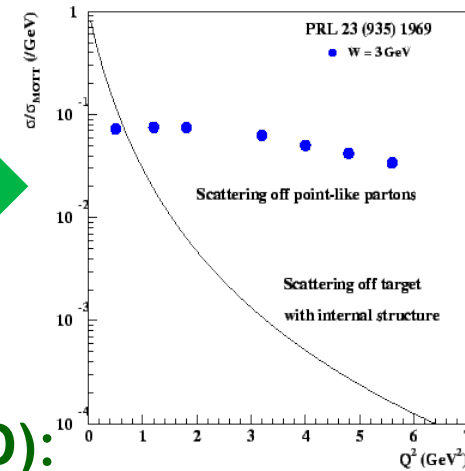


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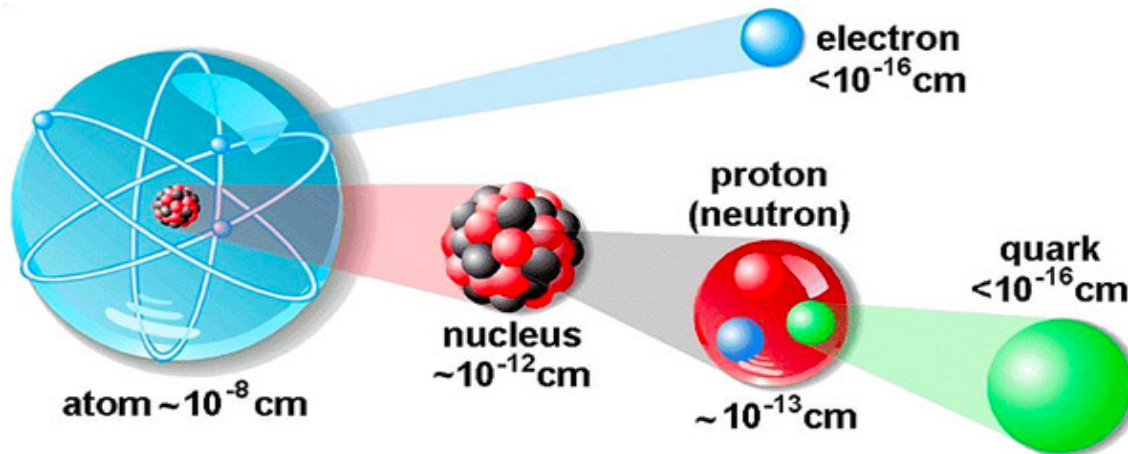


**Quark model**

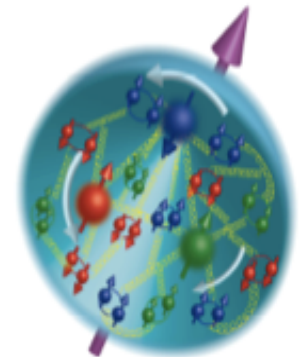
### Discovery



## □ Discovery of Quantum Chromodynamics (QCD):



**Gluons**



**No still picture!  
No fixed structure!**

**Nanometer**

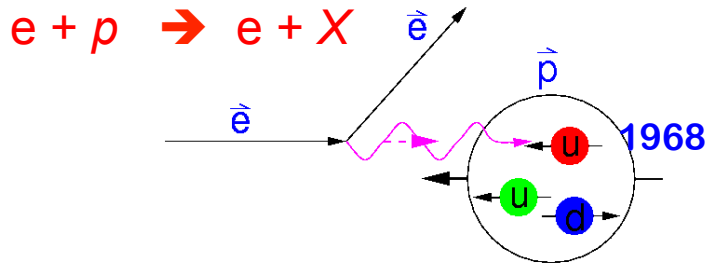
**Femtometer**

**Quantum Probability**

# From 3D hadron structure to QCD, ...

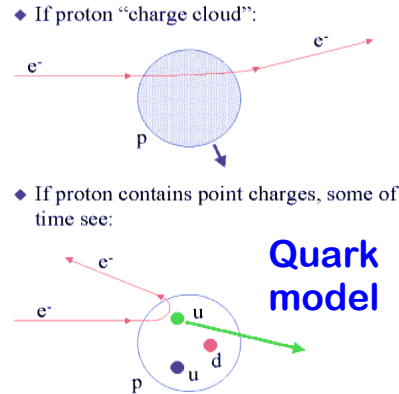
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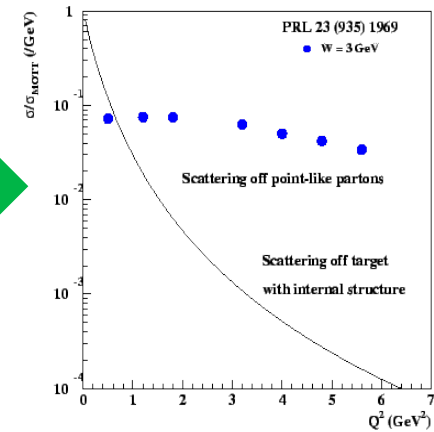


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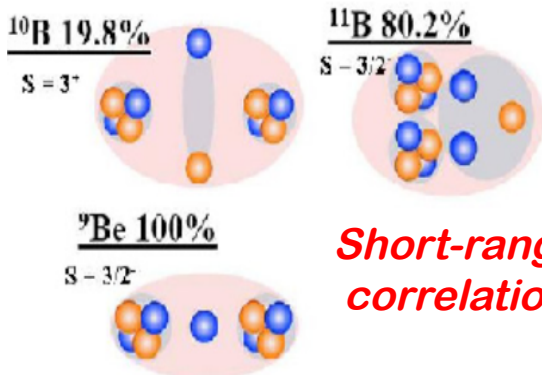


### Discovery



## □ No localized mass and charge centers:

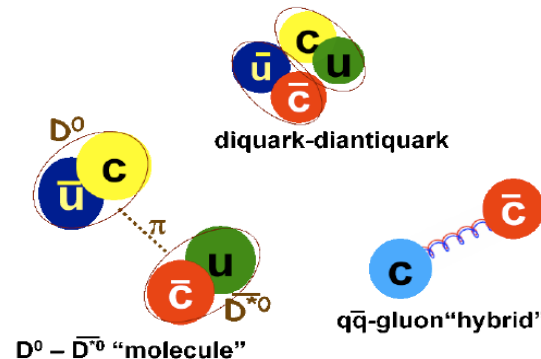
### Nuclei – “Molecule”



**Short-range correlation**

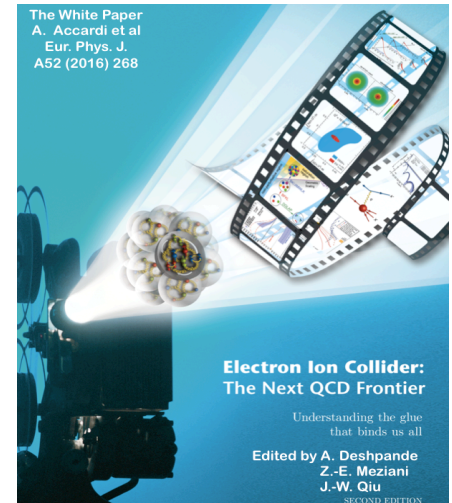
“Light-flavor”

### XYZ – “Nuclei”



“Heavy-flavor”

### “Femtography”



➔ **New frontier of hadron physics ... !**

# Outline of the rest of my talk

## ❑ Next frontier of QCD and hadron physics?

Overarching questions?

## ❑ How to “see” the hadron structure?

See the “unseen”?

## ❑ How to quantify the hadron structure in QCD?

Probabilities to **catch** the parton and its interaction?

## ❑ What do we hope to learn from future facilities?

From JLab 12 GeV to a future Electron-Ion Collider

From Lattice QCD – Complementary to experiments

## ❑ Summary and outlook

# Next frontier of QCD & hadron physics, ...

- How did hadrons, the building blocks of visible world, emerge from quarks and gluons?

Necessary knowledge for understanding  
where and how did we come from following the “Big Bang?”

- What is the internal structure of hadrons, and the dynamics behind the structure?

Necessary knowledge for understanding  
what are we made of, and  
what hold us together, as well as  
how do we improve and move forward – femtotechnology?

- What is the key for understanding color confinement?

Necessary knowledge for understanding  
what is the mother nature of the nonlinear,  
strongly interacting dynamics of the color force?



# How to “see” the hadron structure?

## ❑ Facts:

**Gluons are dark!**

No modern detector has been able to see quarks and gluons in isolation!

## ❑ The intellectual challenge:

*How to probe the quark-gluon dynamics, quantify the hadron structure, study the emergence of hadrons, ..., if we cannot see quarks and gluons?*

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*How to probe the quark-gluon dynamics, quantify the hadron structure, study the emergence of hadrons, ..., if we cannot see quarks and gluons?*

## ❑ Answer to the challenge:

### Theory advances:

QCD factorization – matching the quarks/gluons to hadrons with *controllable approximations!*

### Experimental breakthroughs:

**Jets** – *Footprints of energetic quarks and gluons*

**Quarks** – *Need an EM probe to “see” their existence, ...*

**Gluons** – *Varying the probe’s resolution to “see” their effect, ...*

### Technology improvements:

Energy, luminosity, unprecedented resolution, ...



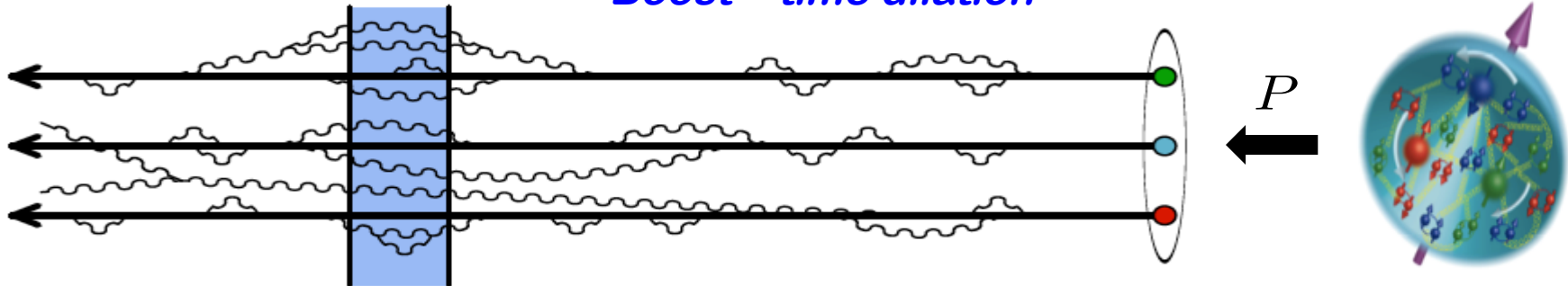
# How to “see” the hadron structure?

- Hard probes to “catch” the **quantum fluctuation**:

*Lorentz invariant cross sections are frame independent  
But, the physical picture of what happened is frame dependent*

**In any frame in which the proton is moving very fast,**

*Boost = time dilation*



**Hard probe ( $t \sim 1/Q < fm$ ) → Probability to “catch” the parton!**

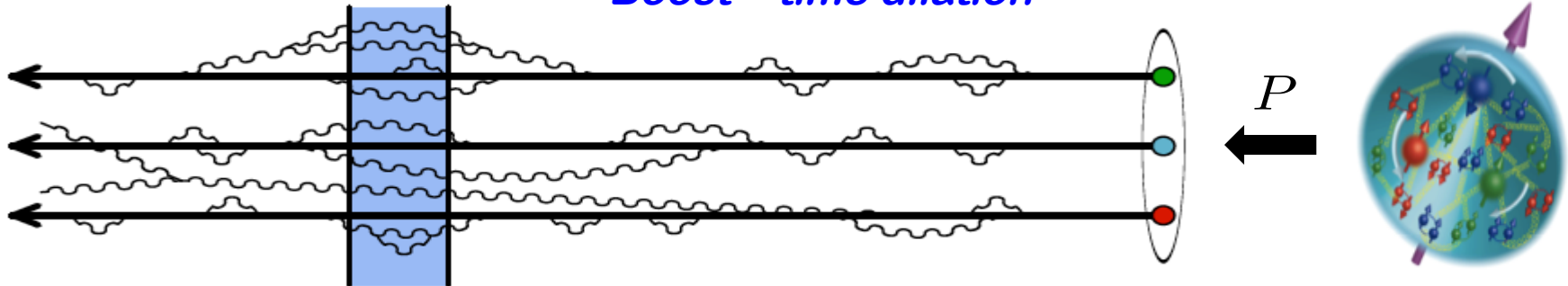
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**Hard probe ( $t \sim 1/Q < fm$ ) → Probability to “catch” the parton!**

✧ Longitudinal momentum fraction –  $x$ :  $xP \sim Q$  **the hard scale!**

✧ Transverse momentum – **confined motion**:  $1/R \sim \Lambda_{QCD} \ll Q$

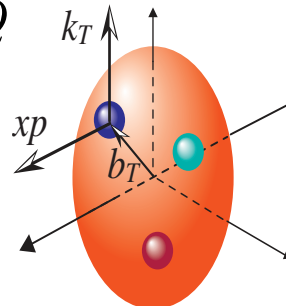
✧ Momentum transfer in diffractive –  $t$ :  $t \ll Q \Rightarrow 1/b_T$



**Spatial imaging:**



**With the collision size:  $\sim 1/Q$**



# How to quantify hadron structure in QCD?

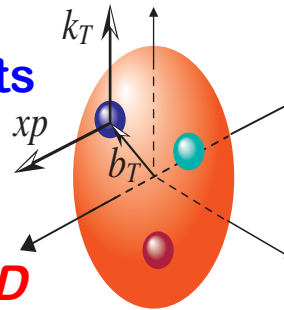
## □ What do we need to know for the structure?

✧ In theory:  $\langle P, S | \mathcal{O}(\bar{\psi}, \psi, A^\mu) | P, S \rangle$  – Hadronic matrix elements  
of all possible operators:  $\mathcal{O}(\bar{\psi}, \psi, A^\mu)$



*Correlations between any number of fields in QCD*

✧ BUT: *None of these matrix elements is a direct physical observable – color confinement!*



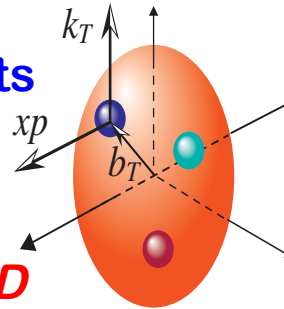
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- ✧ In practice: **Accessible** hadron structure  
= hadron matrix elements of quarks and gluons, **satisfying**

- 1) can be related to physical cross sections of hadrons and leptons with **controllable approximation**; and/or
- 2) can be calculated/extracted from lattice QCD

- ✧ Hard scale: **Wave vs. particle nature of quarks and gluons?**



*Need probes/observables with at least ONE large-scale, & additional controllable small scale(s) to “see” the structure!*

# How to quantify hadron structure in QCD?

□ Matching the **observed** hadron to the caught **partons**:

*Any cross section with identified hadron(s) is NON-Perturbative!*

**Cross section with ONE identified hadron & ONE large momentum transfer:**

$$\sigma_{\text{DIS}}(x, Q^2) = \left| \text{Diagram} \right|^2 = \left| \text{Inclusive DIS Diagrams} \right|^2$$

*Inclusive DIS*

$$\approx c_q \otimes q(x, Q^2) + c_g \otimes g(x, Q^2) + \mathcal{O} \left( \frac{\langle k_T^2 \rangle}{Q^2}, \frac{\langle F^2 \rangle}{Q^2}, \dots \right)$$

Probe     Structure     Probe     Structure

*Most non-perturbative physics are neglected  
Included only those  
in input PDFs!*

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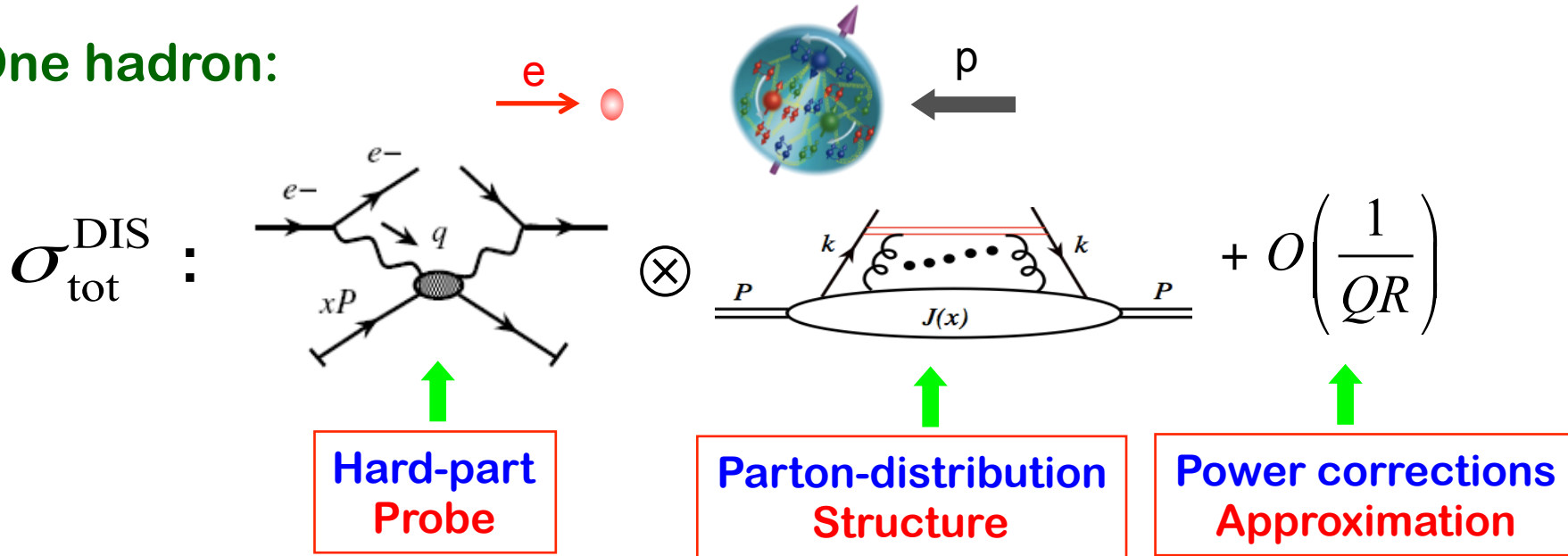
➔ **Leading power/twist factorization**  
– an approximation!

Controllable approximation

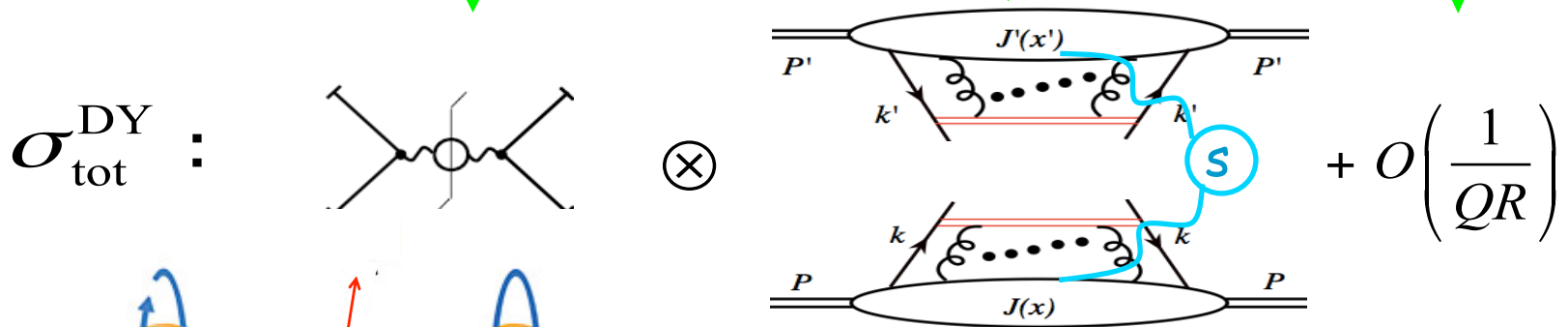


# if there are more than one identified hadron, ...

## One hadron:



## Two hadrons:



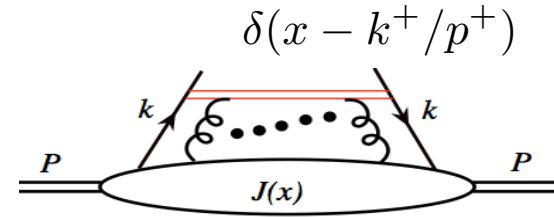
**Predictive power:**  
**Universal Parton Distributions**

# We have learned a lot for 1D structure, ...

## □ General expansion of quark distribution:

must have general expansion in terms of  $P$ ,  $\not{p}$ ,  $\not{S}$  etc.

$$\phi(x) = \frac{1}{2} [q(x)\gamma \cdot P + s_{\parallel} \Delta q(x)\gamma_5 \gamma \cdot P + \delta q(x)\gamma \cdot P \gamma_5 \gamma \cdot S_{\perp}]$$



## □ 3-leading power quark parton distribution:

$$q(x) = \frac{1}{4\pi} \int dz^- e^{iz^- x P^+} \langle P, S | \bar{\psi}(0) \gamma^+ \psi(0, z^-, \mathbf{0}_{\perp}) | P, S \rangle$$

$$\Delta q(x) = \frac{1}{4\pi} \int dz^- e^{iz^- x P^+} \langle P, S | \bar{\psi}(0) \gamma^+ \gamma_5 \psi(0, z^-, \mathbf{0}_{\perp}) | P, S \rangle$$

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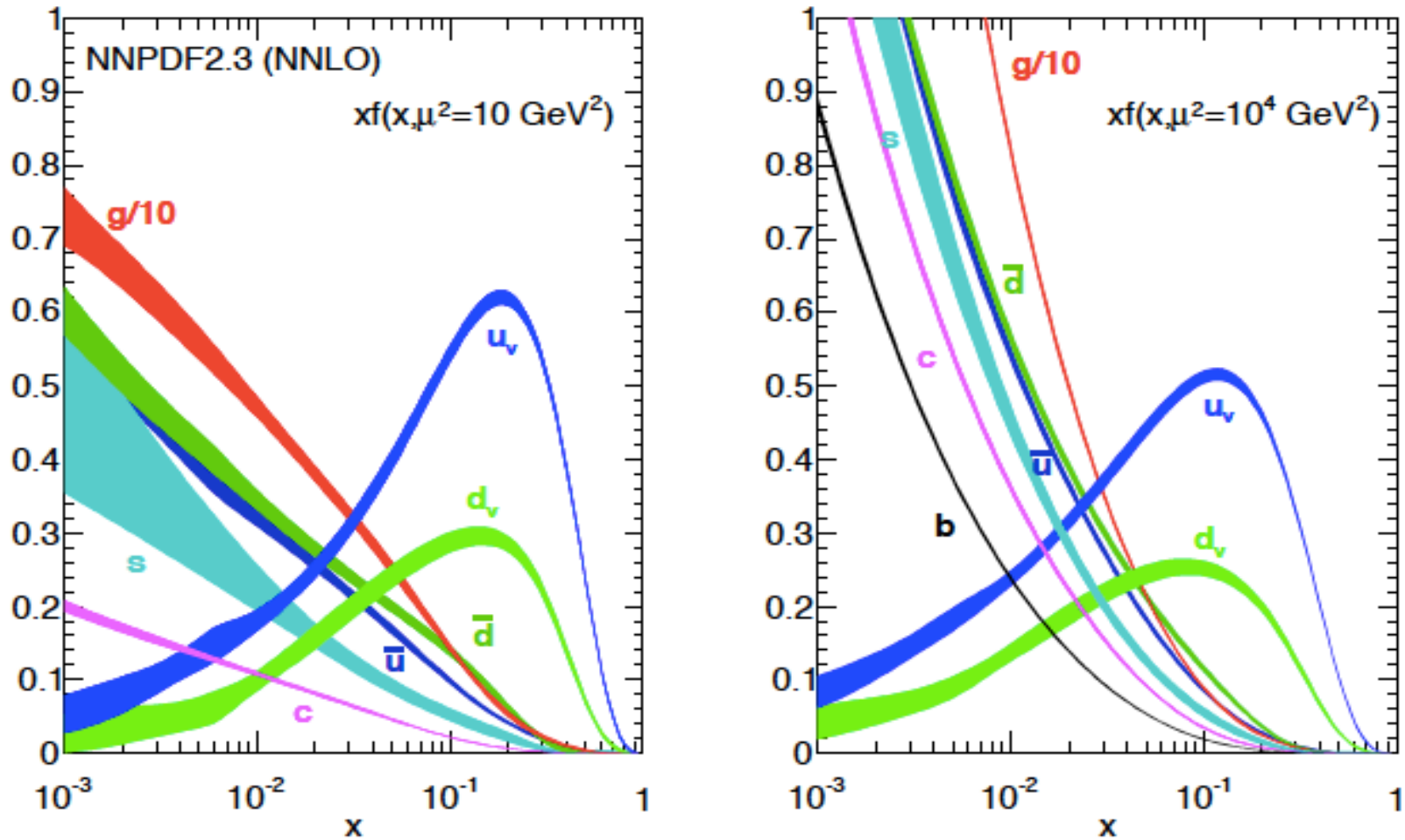
“unpolarized” – “longitudinally polarized” – “transversity”

*Probed with observables with a single-hard scale!*

## □ Similar for gluon density and helicity distributions

# PDFs of a spin-averaged proton

□ Modern sets of PDFs @NNLO with uncertainties:

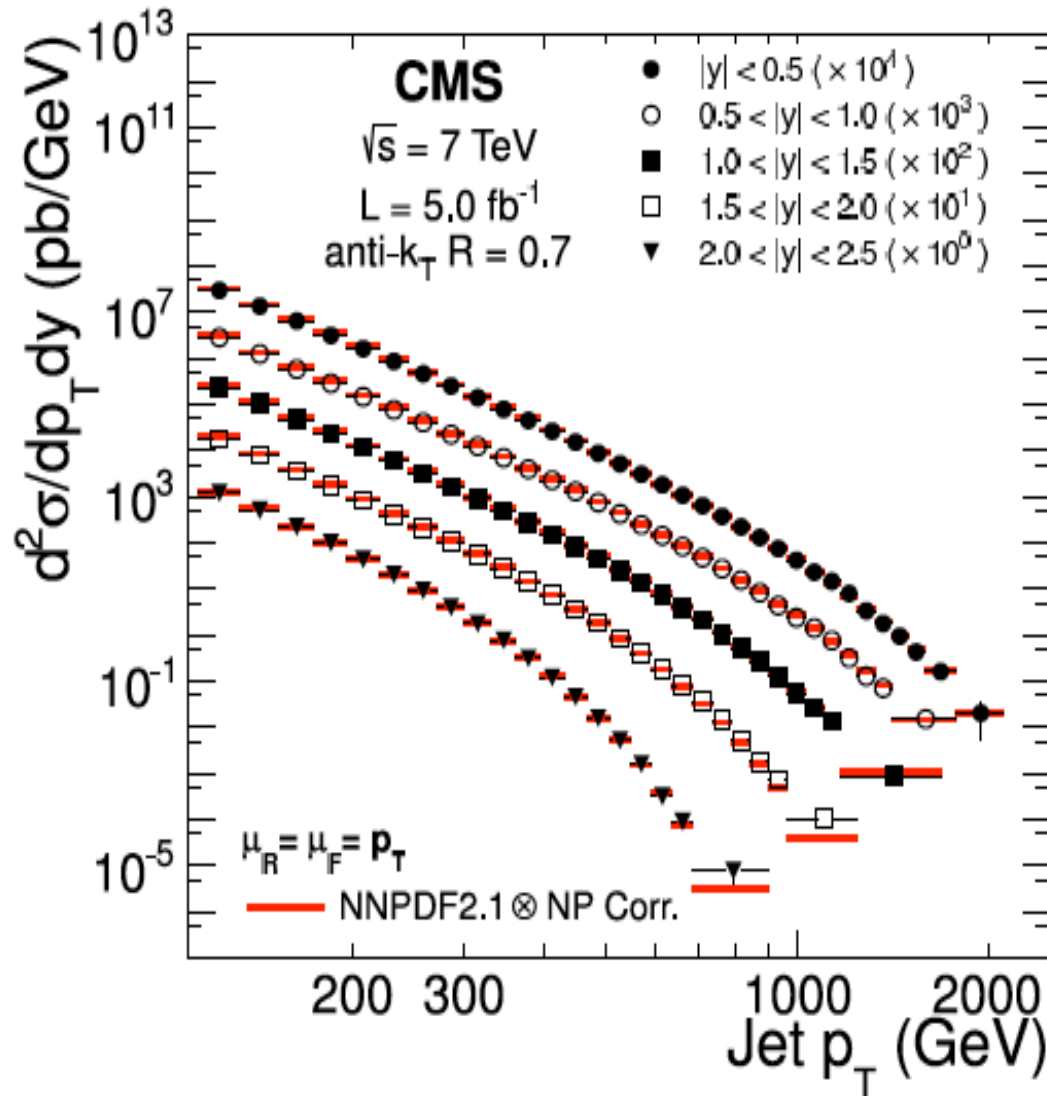


K.A. Olive et al. (Particle Data Group), *Chin. Phys. C*, 38, 090001 (2014)

**Consistently fit almost all data with  $Q > 2\text{GeV}$**

# Role of LHC data

## □ Inclusive jet production at 7 TeV:

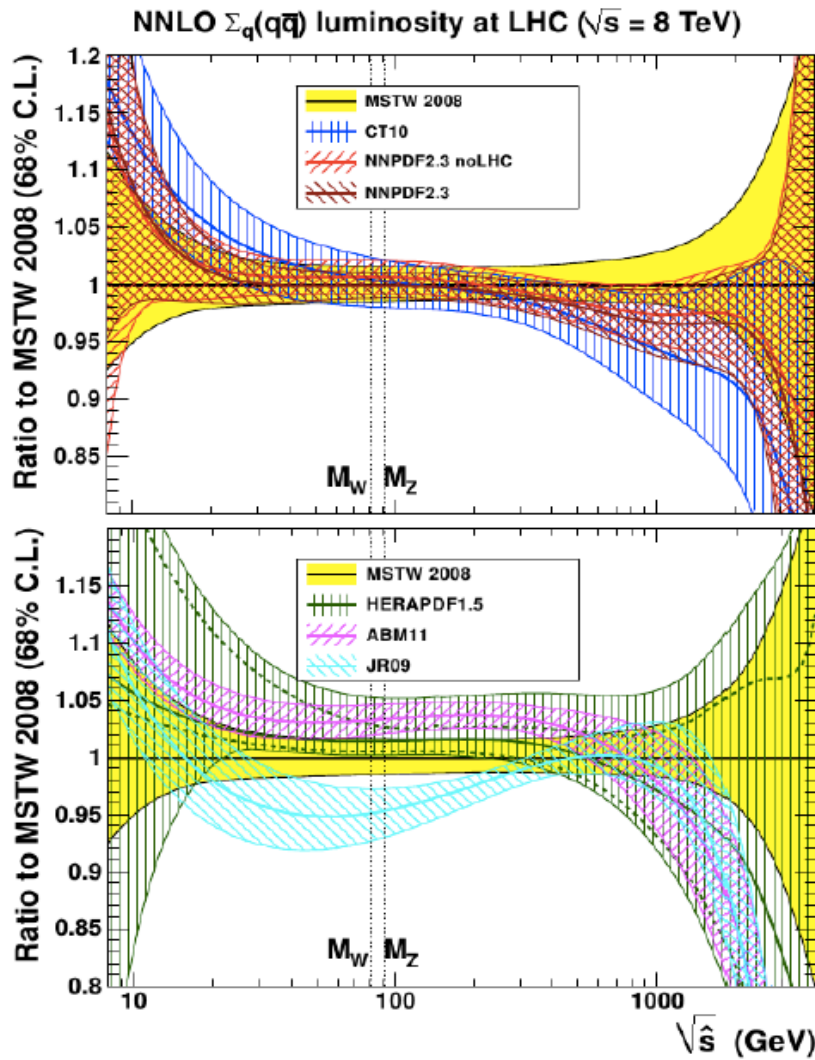


◇ Cross sections span 12 orders of magnitude

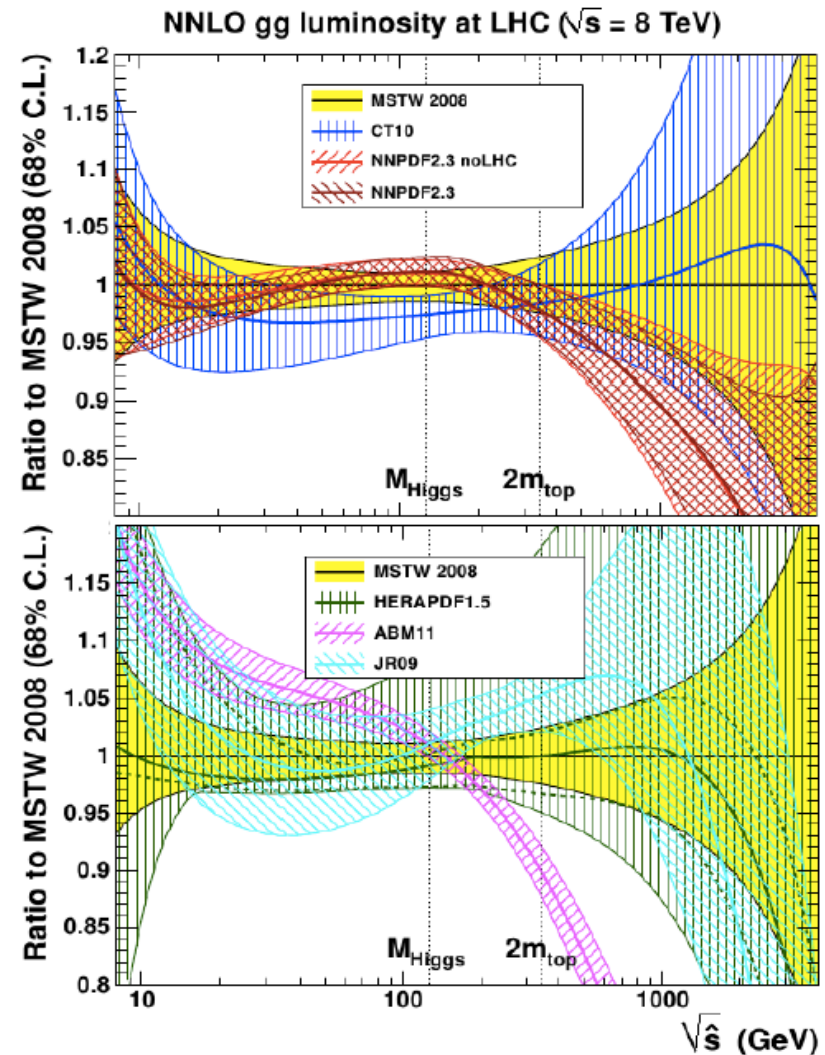
◇ Almost negligible statistical error

# Partonic luminosities – Our discovery potential

q - qbar



g - g

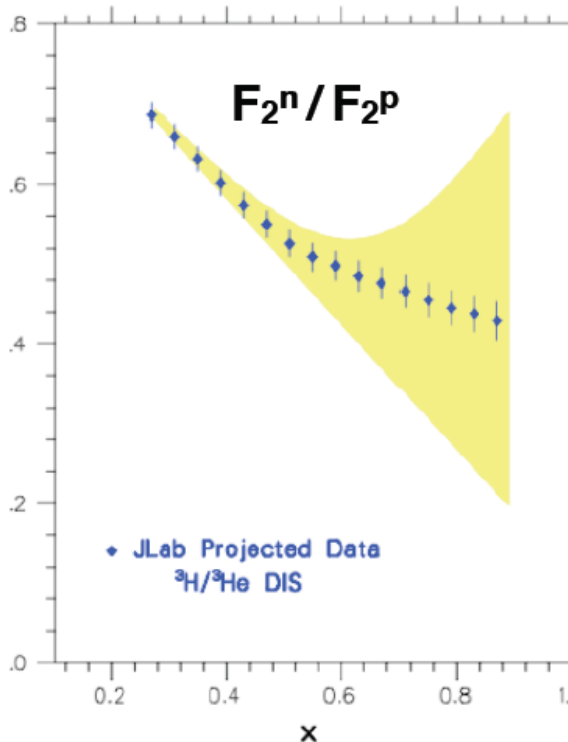


*Uncertainties are mainly in large- & small-x regimes – need both JLab12 & EIC*

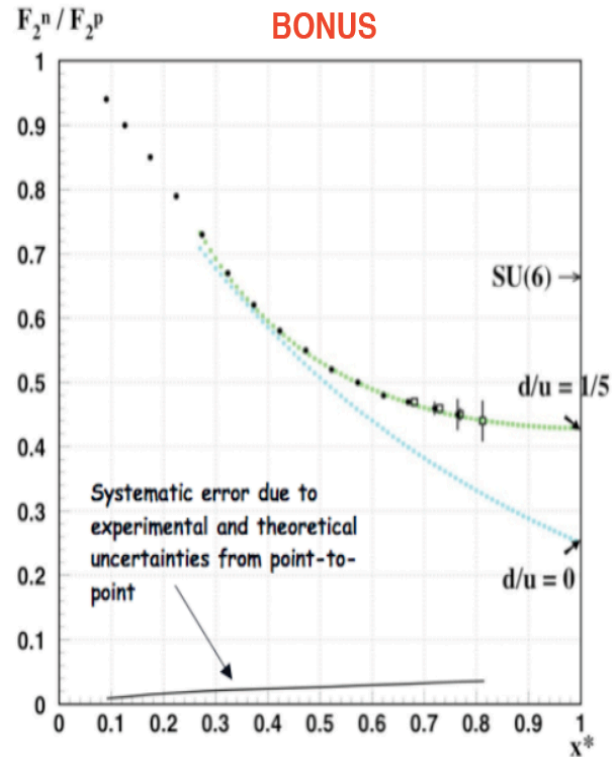
# Future large-x experiments – JLab12

## □ NSAC milestone HP14 (2018):

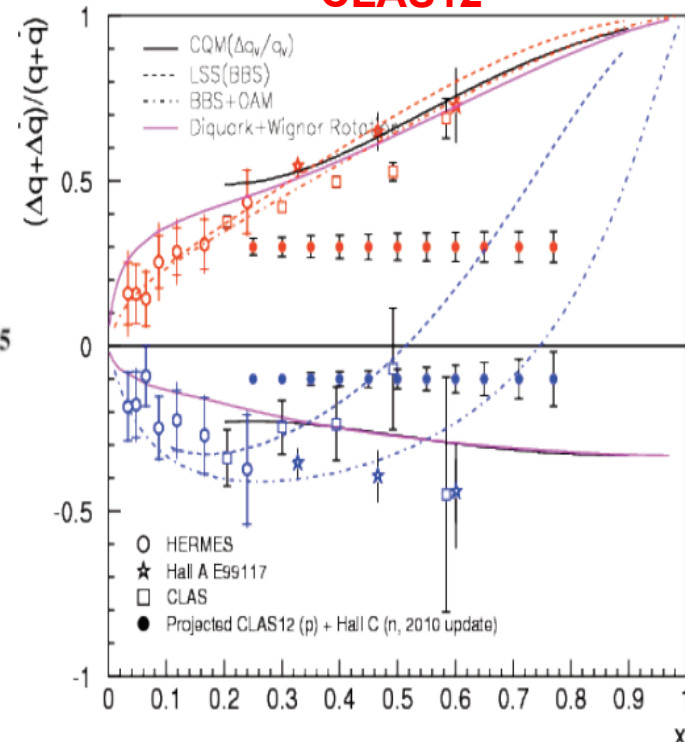
### MARATHON



### BONUS



### CLAS12



## Plus many more JLab experiments:

E12-06-110 (Hall C on  ${}^3\text{He}$ ), E12-06-122 (Hall A on  ${}^3\text{He}$ ),

E12-06-109 (CLAS on  $\text{NH}_3$ ,  $\text{ND}_3$ ), ...

and Fermilab E906, ...

*Future EIC help fix small-x PDFs!*

*Can lattice QCD help large-x?*

# Hadron structure from lattice QCD calculation

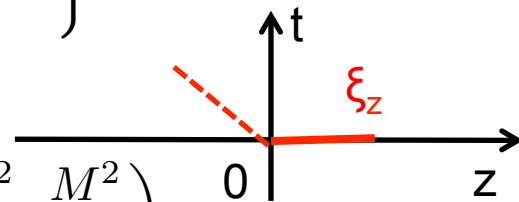
## □ “Quasi” quark distribution (spin-averaged):

See talks by Constantinou and Orginos, ...

$$\tilde{q}(x, \mu^2, P_z) \equiv \int \frac{d\xi_z}{4\pi} e^{-ixP_z\xi_z} \langle P | \bar{\psi}(\xi_z) \gamma_z \exp \left\{ -ig \int_0^{\xi_z} d\eta_z A_z(\eta_z) \right\} \psi(0) | P \rangle + \text{UVCT}(\mu^2)$$

## □ Proposed matching:

$$\tilde{q}(x, \mu^2, P_z) = \int_x^1 \frac{dy}{y} Z \left( \frac{x}{y}, \frac{\mu}{P_z} \right) q(y, \mu^2) + \mathcal{O} \left( \frac{\Lambda^2}{P_z^2}, \frac{M^2}{P_z^2} \right)$$

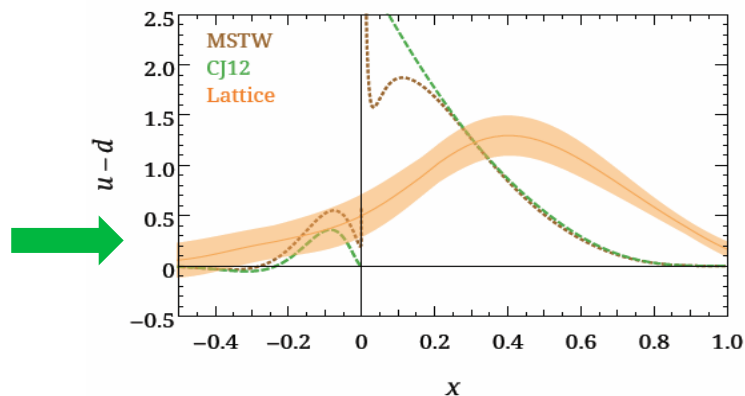
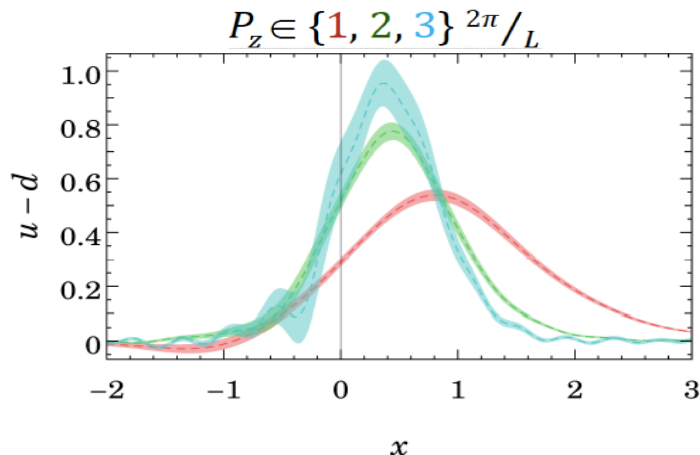


Ji, arXiv:1305.1539

- Power divergence – renormalization?
- Mixing with lower dimension operators cannot be treated perturbatively, ...

## □ Exploratory effort:

Lin et al., arXiv:1402.1462



# Hadron structure from lattice QCD calculation

Ma and Qiu, 2014, 2017

## □ Facts:

- ✧ PDFs are **time-independent**, so as the factorized cross sections!
- ✧ The operators, defining PDFs, located on the light-cone is a consequence of the approximation defining the twist-2 factorization  
*More precisely, the collinear approximation*



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*More precisely, the collinear approximation*

## □ Beyond the quasi- and pseudo-PDFs:

- ✧ NOT try to calculate PDFs **directly** from lattice QCD calculations
- ✧ Calculate a set of **time-independent** (fixed or integrated over time) and **good** single hadron matrix elements – “**lattice cross sections**”

$$\sigma_n(\xi^2, \omega, P^2) = \langle P | T \{ \mathcal{O}_n(\xi) \} | P \rangle \quad \omega = P \cdot \xi$$

with

$$\mathcal{O}_{j_1 j_2}(\xi) \equiv \xi^{d_{j_1} + d_{j_2} - 2} Z_{j_1}^{-1} Z_{j_2}^{-1} j_1(\xi) j_2(0)$$

$$j_S(\xi) = \xi^2 Z_S^{-1} [\bar{\psi}_q \psi_q](\xi), \quad j_G(\xi) = \xi^3 Z_G^{-1} \left[ -\frac{1}{4} F_{\mu\nu}^c F_{\mu\nu}^c \right](\xi)$$

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$$\sigma_n(\xi^2, \omega, P^2) = \langle P | T \{ \mathcal{O}_n(\xi) \} | P \rangle \quad \omega = P \cdot \xi$$

with

$$\mathcal{O}_{j_1 j_2}(\xi) \equiv \xi^{d_{j_1} + d_{j_2} - 2} Z_{j_1}^{-1} Z_{j_2}^{-1} j_1(\xi) j_2(0)$$

$$j_S(\xi) = \xi^2 Z_S^{-1} [\bar{\psi}_q \psi_q](\xi), \quad j_G(\xi) = \xi^3 Z_G^{-1} [-\frac{1}{4} F_{\mu\nu}^c F_{\mu\nu}^c](\xi)$$

- ✧ Derive PDFs from Global Analysis of “**data**” on lattice cross sections

$$\bar{\sigma}_{\text{E}}^{\text{Lat}}(\xi_z, 1/a, P_z) \xleftrightarrow{\mathcal{Z}} \sigma_{\text{E}}(\xi_z, \tilde{\mu}^2, P_z) \quad \text{– Renormalization/continuum limit (lattice QCD expertise, ...)}$$

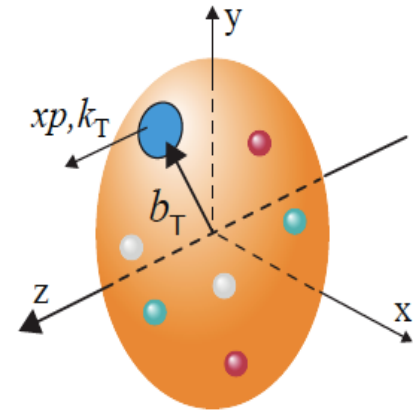
$$\sigma_{\text{M}}(\xi_z, \tilde{\mu}^2, P_z) \xleftrightarrow{\mathcal{C}} f_i(x, \mu^2), \quad \text{– Factorization to PDFs (perturbative QCD, ...)}$$

# Paradigm shift: 3D imaging of hadrons

## □ Cross sections with two-momentum scales observed:

$$Q_1 \gg Q_2 \sim 1/R \sim \Lambda_{\text{QCD}}$$

- ✧ **Hard scale:**  $Q_1$  localizes the probe to see the quark or gluon d.o.f.
- ✧ **“Soft” scale:**  $Q_2$  could be more sensitive to hadron structure, e.g., confined motion

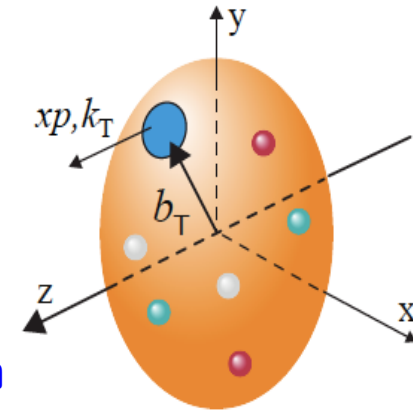


# Paradigm shift: 3D imaging of hadrons

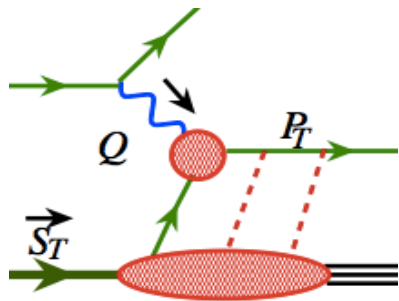
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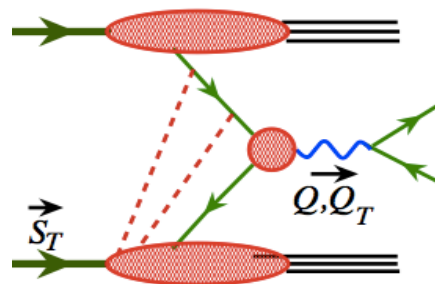


## □ Two-scale observables with the hadron **broken**:



**SIDIS:  $Q \gg P_T$**

+



**DY:  $Q \gg P_T$**

+

**Two-jet momentum imbalance in SIDIS, ...**



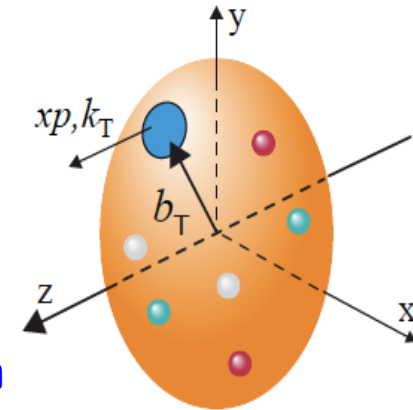
- ✦ **Natural observables with TWO very different scales**
- ✦ **TMD factorization:** partons' confined motion is encoded into TMDs

# Paradigm shift: 3D imaging of hadrons

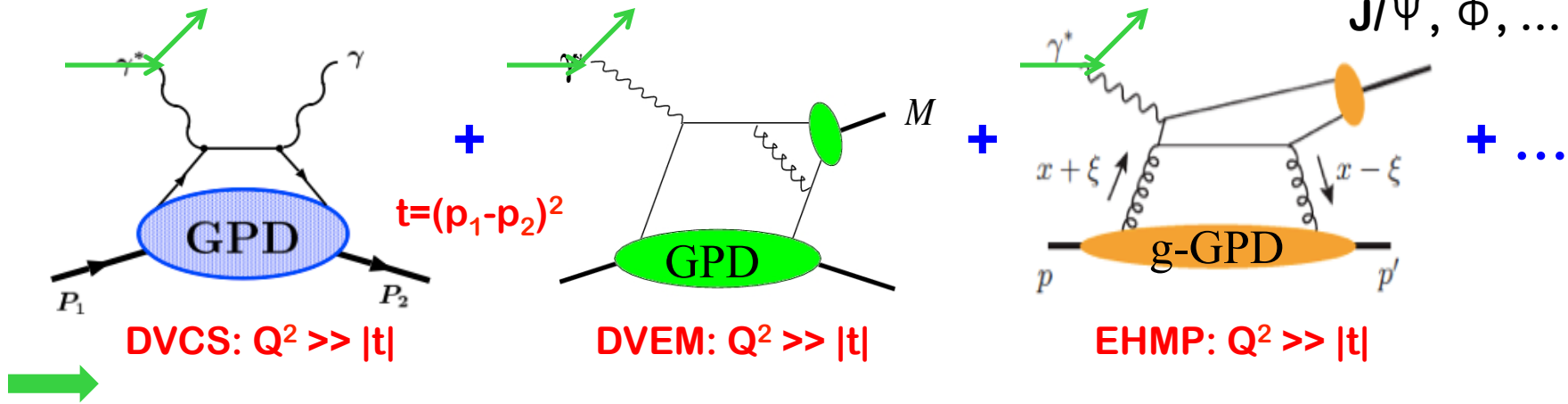
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## □ Two-scale observables with the hadron **unbroken**:



- ✧ **Natural observables with TWO very different scales**
- ✧ **GPDs:** Fourier Transform of  $t$ -dependence gives spatial  $b_T$ -dependence

# Unified description of nucleon structure

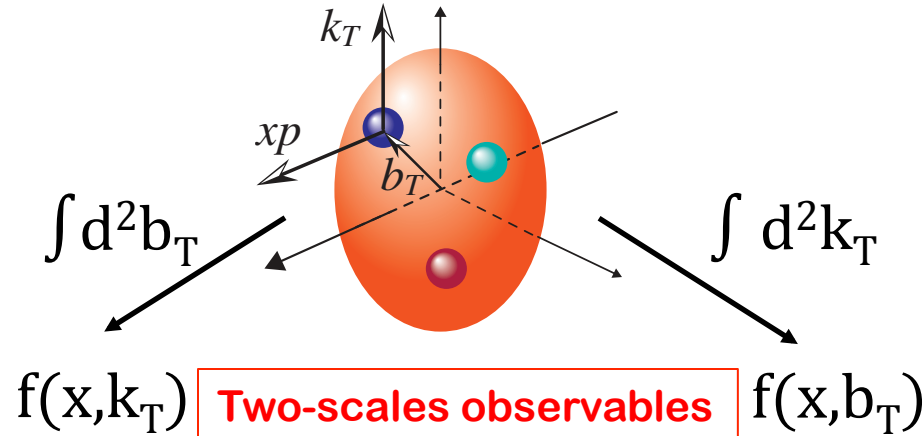
See talks by Pasquini, ...

## □ Wigner distributions in 5D (or GTMDs):

*Momentum  
Space*

*TMDs*

*Confined  
motion*



*Coordinate  
Space*

*GPDs*

*Spatial  
distribution*

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See talks by Pasquini, ...

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Space

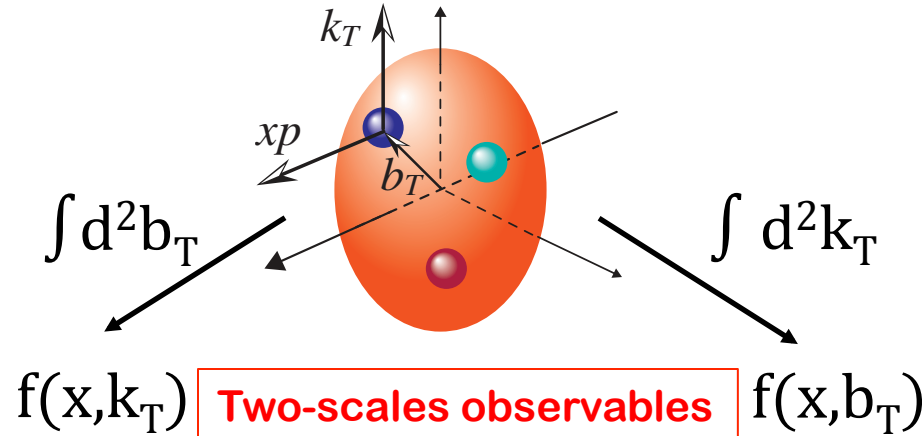
Coordinate  
Space

TMDs

GPDs

Confined  
motion

Spatial  
distribution



## □ Theory is solid – TMDs & SIDIS as an example:

See talks by Rogers,  
Gamberg, Prokudin, ...

### ✧ Low $P_{hT}$ ( $P_{hT} \ll Q$ ) – TMD factorization:

$$\sigma_{\text{SIDIS}}(Q, P_{h\perp}, x_B, z_h) = \hat{H}(Q) \otimes \Phi_f(x, k_\perp) \otimes \mathcal{D}_{f \rightarrow h}(z, p_\perp) \otimes \mathcal{S}(k_{s\perp}) + \mathcal{O}\left[\frac{P_{h\perp}}{Q}\right]$$

### ✧ High $P_{hT}$ ( $P_{hT} \sim Q$ ) – Collinear factorization:

$$\sigma_{\text{SIDIS}}(Q, P_{h\perp}, x_B, z_h) = \hat{H}(Q, P_{h\perp}, \alpha_s) \otimes \phi_f \otimes D_{f \rightarrow h} + \mathcal{O}\left(\frac{1}{P_{h\perp}}, \frac{1}{Q}\right)$$

### ✧ $P_{hT}$ Integrated - Collinear factorization:

$$\sigma_{\text{SIDIS}}(Q, x_B, z_h) = \tilde{H}(Q, \alpha_s) \otimes \phi_f \otimes D_{f \rightarrow h} + \mathcal{O}\left(\frac{1}{Q}\right)$$

### ✧ Very high $P_{hT} \gg Q$ – Collinear factorization:

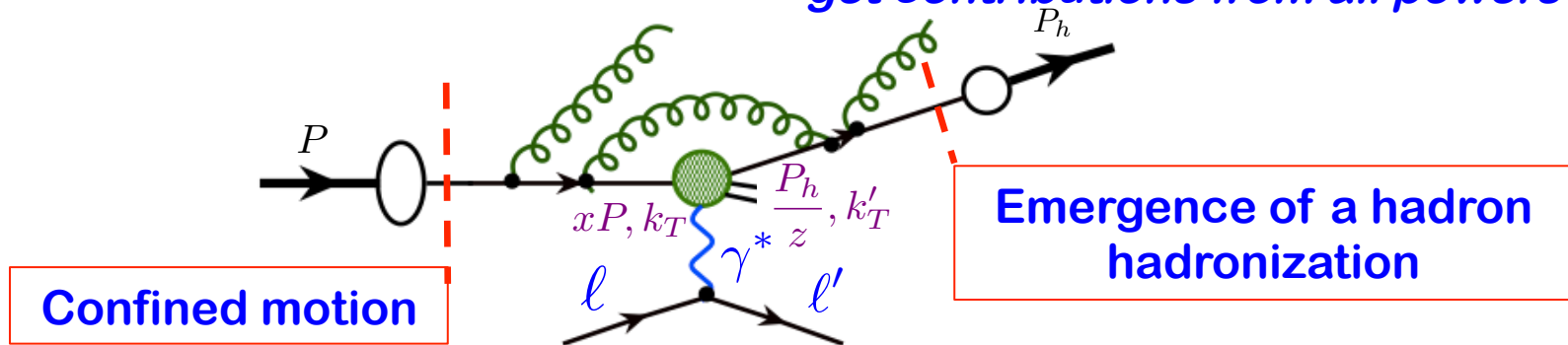
$$\sigma_{\text{SIDIS}}(Q, P_{h\perp}, x_B, z_h) = \sum_{abc} \hat{H}_{ab \rightarrow c} \otimes \phi_{\gamma \rightarrow a} \otimes \phi_b \otimes D_{c \rightarrow h} + \mathcal{O}\left(\frac{1}{Q}, \frac{Q}{P_{h\perp}}\right)$$

# Hadron structure and $Q^2$ -dependence

## □ Variation of $Q^2$ at the hard collision:

*Gluon shower – liberation of confined states*

*– get contributions from all powers*

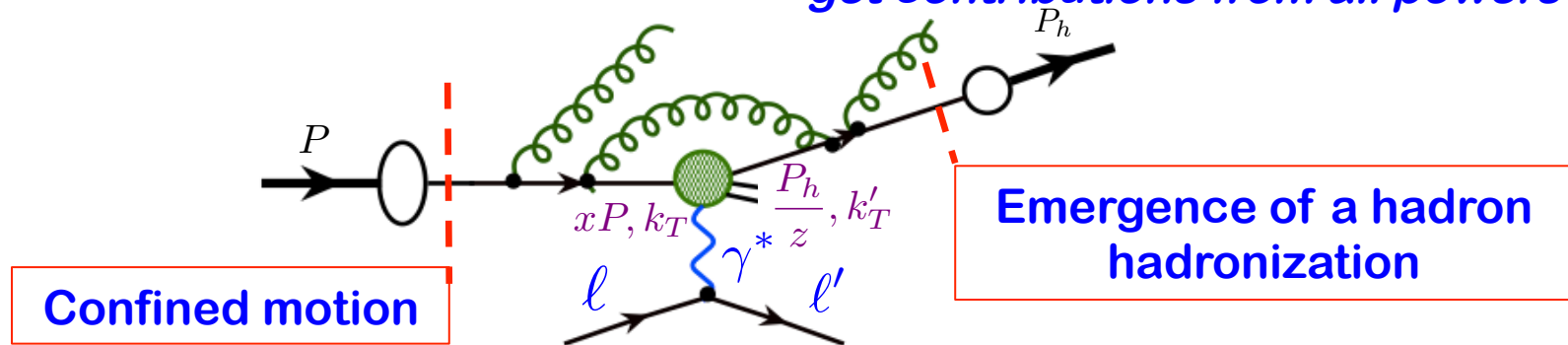




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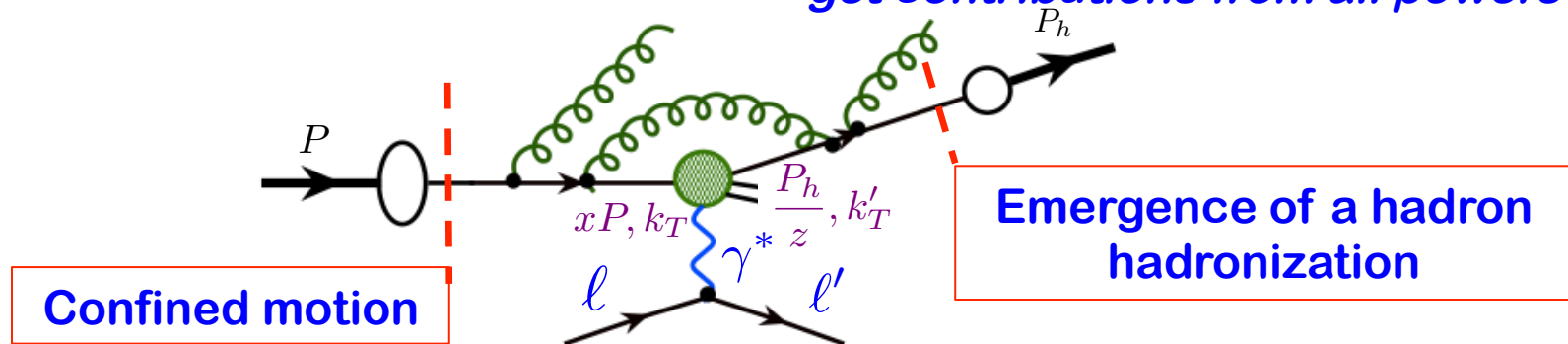
## □ Single hard scale – collinear factorization:

- ✧ DGLAP evolution (LT-approx.) use data at  $Q > Q_0$  to help pin down PDFs at  $Q_0$
- ✧ PDFs at  $Q_0$  carry all non-perturbative structure information

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## □ Two scales – TMD factorization:

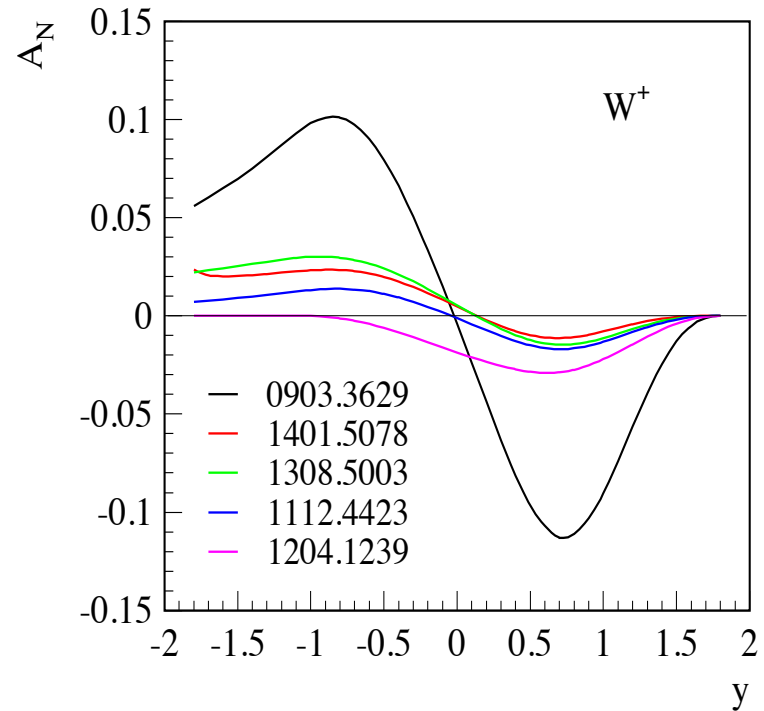
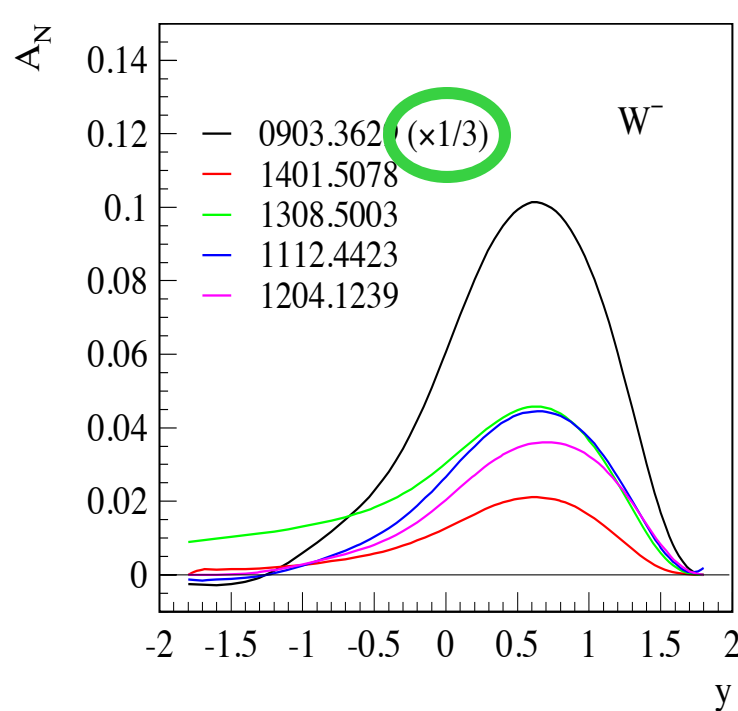
- ✧ TMD factorization valid when  $P_T \ll Q$ , CS evolution in conjugate  $b_T$ -space
- ✧ When TMDs dominated by small  $b_T$ , shower dominated by perturbative logs, CS evolution help use all  $Q > Q_0$  data to fix TMDs at  $Q_0$  ( $Q_0$  large,  $x$  small)
- ✧ When TMDs dominated by large  $b_T$  region, rich N.P. structure information, CS evolution does not help extract TMDs → **models, new challenge!**

# Evolution of the Sivers effect

## □ Sivers Effect:

- ✧ Quantum correlation between the **spin direction** of colliding hadron and the preference of **motion direction** of its confined partons
- ✧ QCD Prediction: **Sign change** of Sivers function from SIDIS and DY

## □ “Prediction” and large uncertainty of QCD evolution:

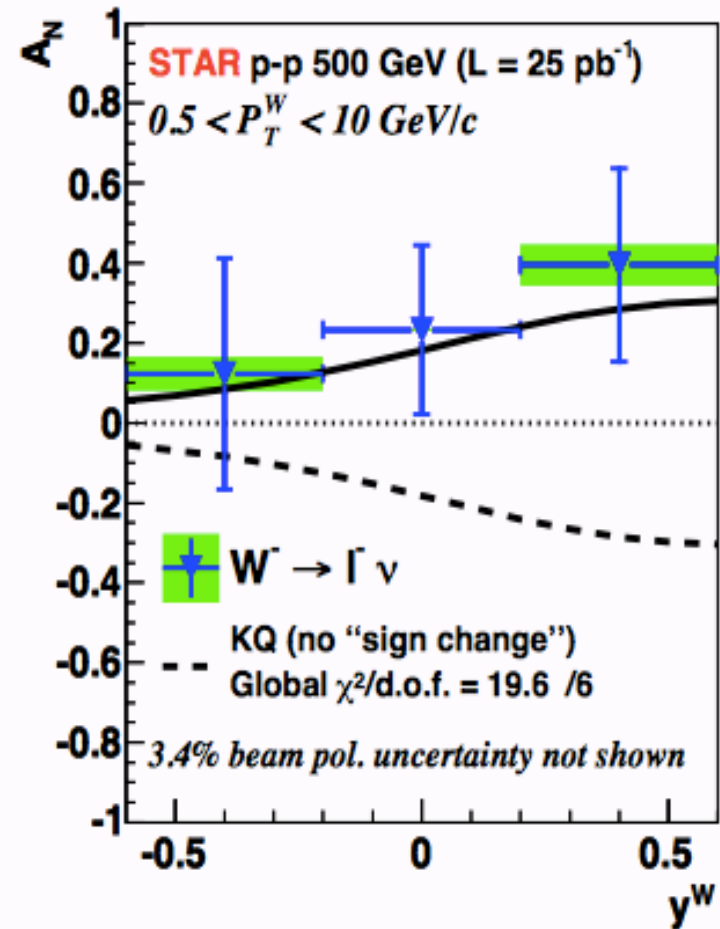
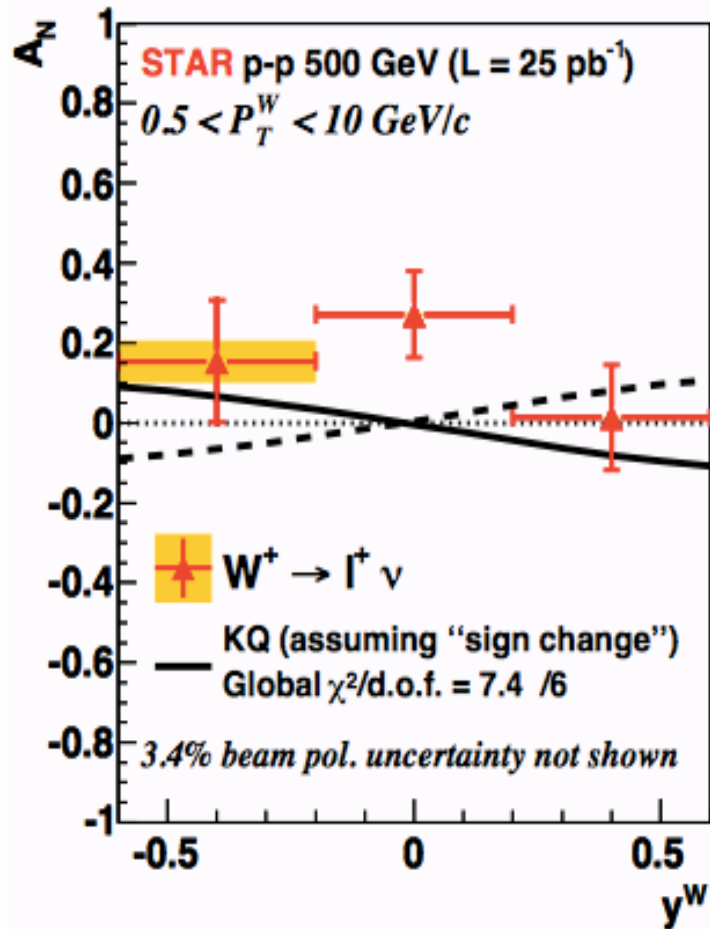


**RHIC is an unique facility to test this (W/Z – DY)!**

# Evolution of the Sivers effect

STAR Collab. Phys. Rev. Lett. 116, 132301 (2016)

See talk by Aschenauer, ...



Theory curves (KQ) = No TMD evolution!

also see M. Anselmino et al.  
JHEP 1704 (2017) 046

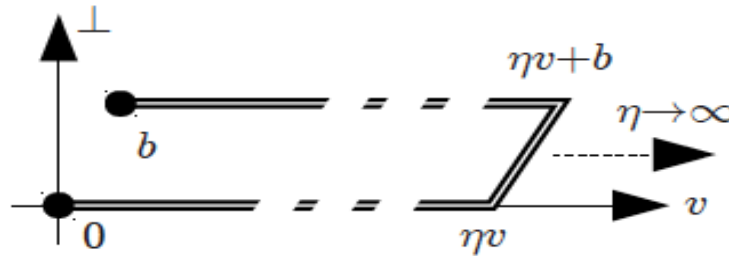
*Data from STAR collaboration on  $A_N$  for  $W$ -production are consistent with a sign change between SIDIS and DY*

# Hint of the sign change from lattice QCD

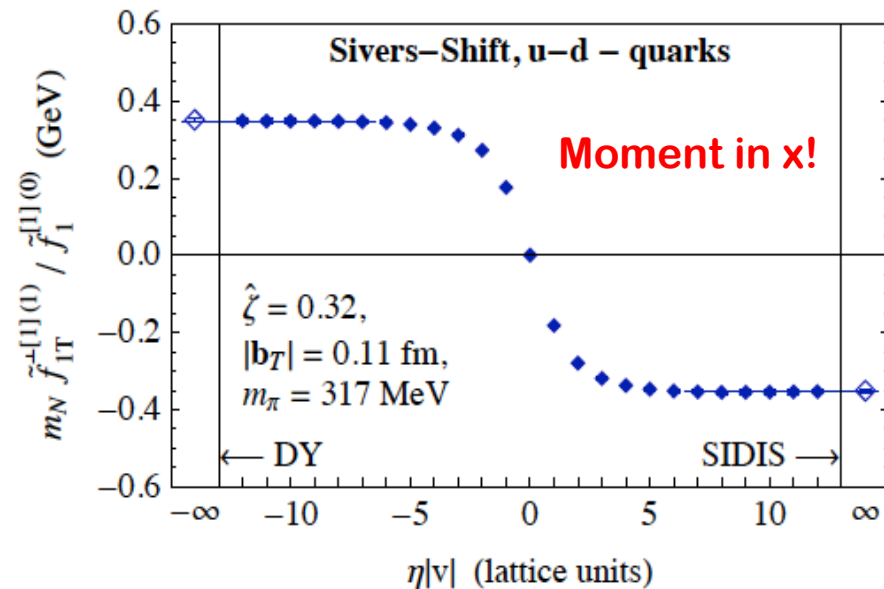
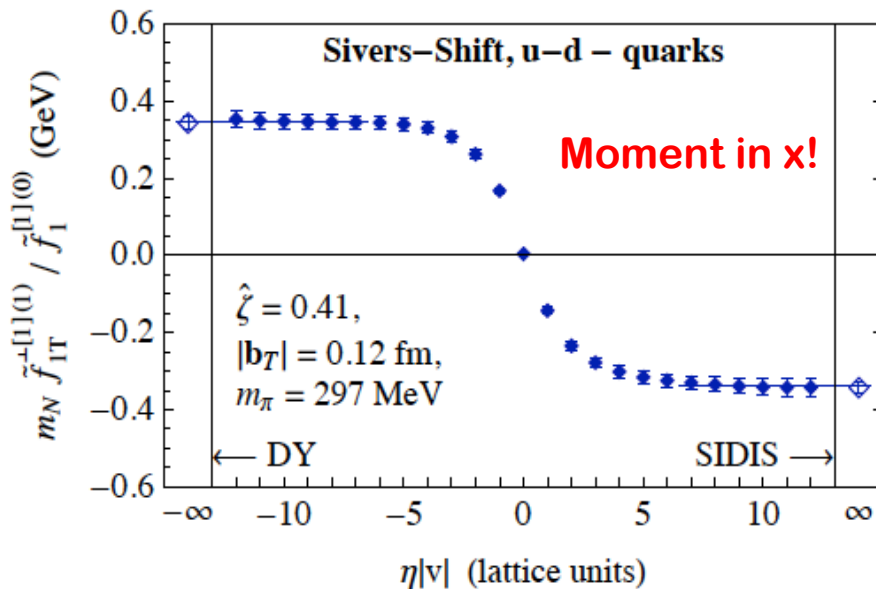
Engelhardt@TMD  
Collaboration meeting

## □ Gauge link for lattice calculation:

Staple-shaped gauge link  $\mathcal{U}[0, \eta v, \eta v + b, b]$



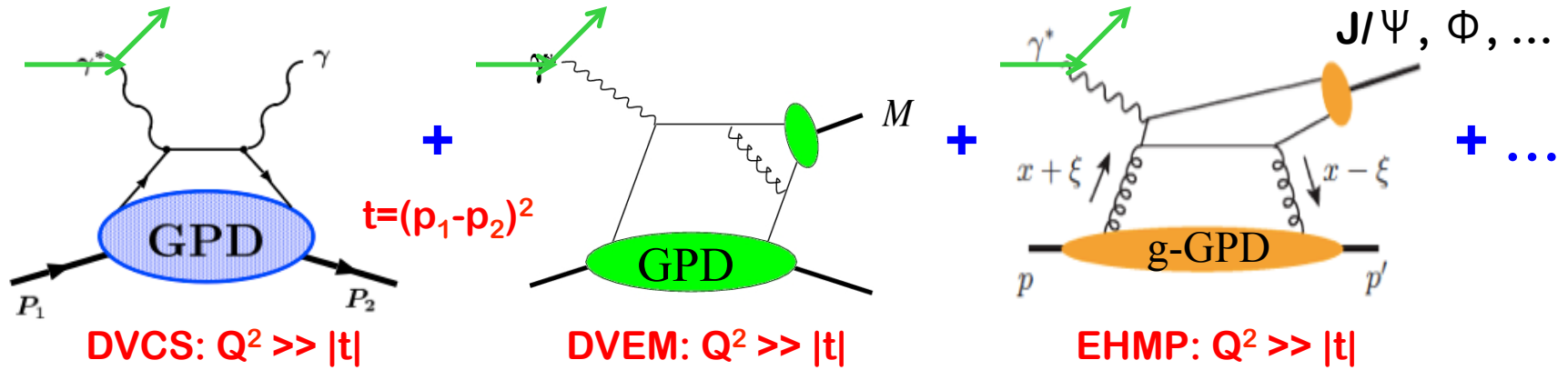
## □ Normalized moment of Sivers function – at given $b_T$ :



# Hunting for GPDs: Exclusive DIS

## □ Experimental access to GPDs:

See talks by Kumericki, Mezrag, Ferrero, Hafidi, Roche, Horn, ...

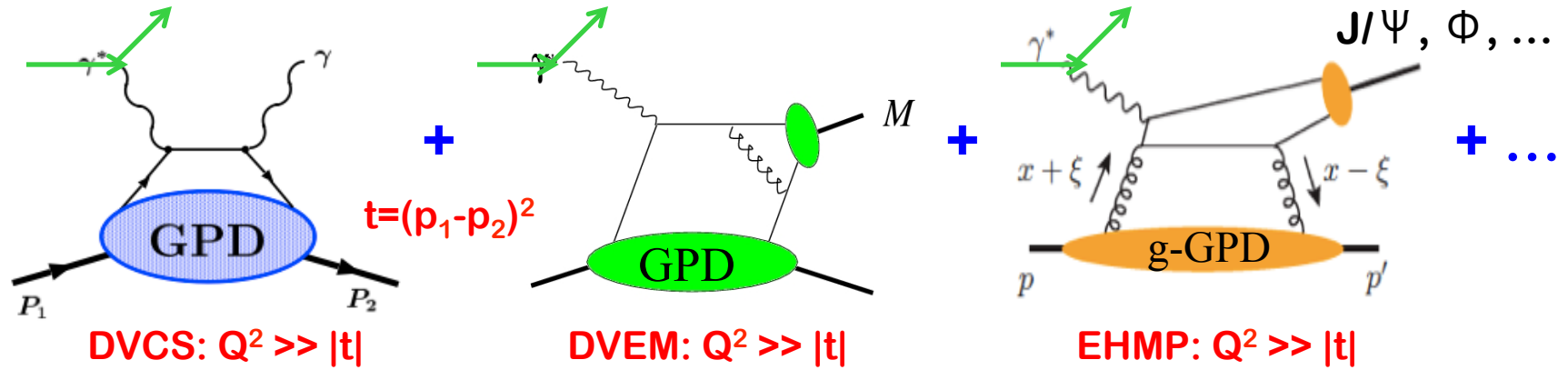


## □ Much more complicated – $(x, \xi, t)$ variables:

✧ Challenge to derive GPDs from data

# Hunting for GPDs: Exclusive DIS

## Experimental access to GPDs:



## Much more complicated – $(x, \xi, t)$ variables:

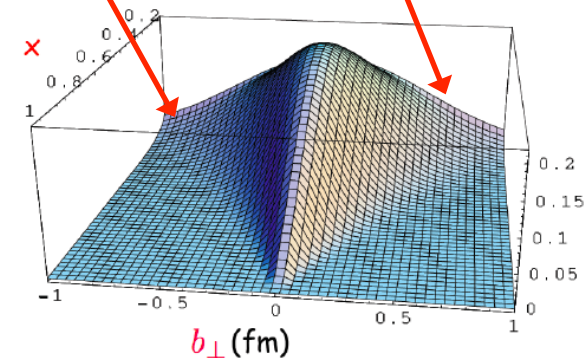
✧ Challenge to derive GPDs from data

## GPDs could tell us:

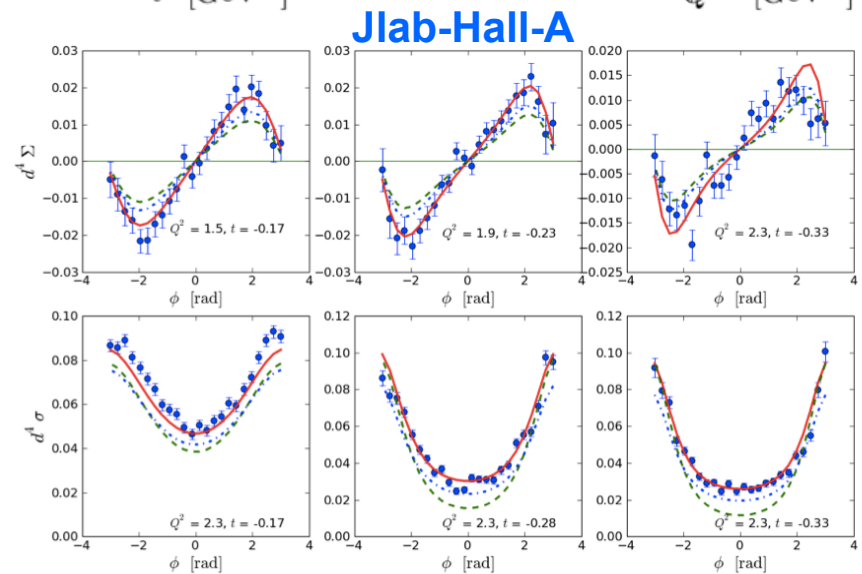
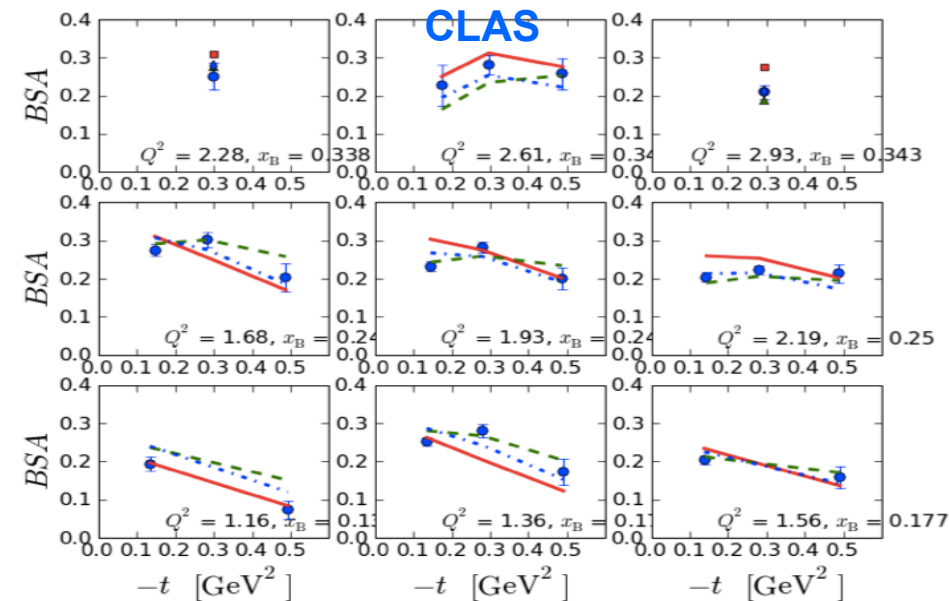
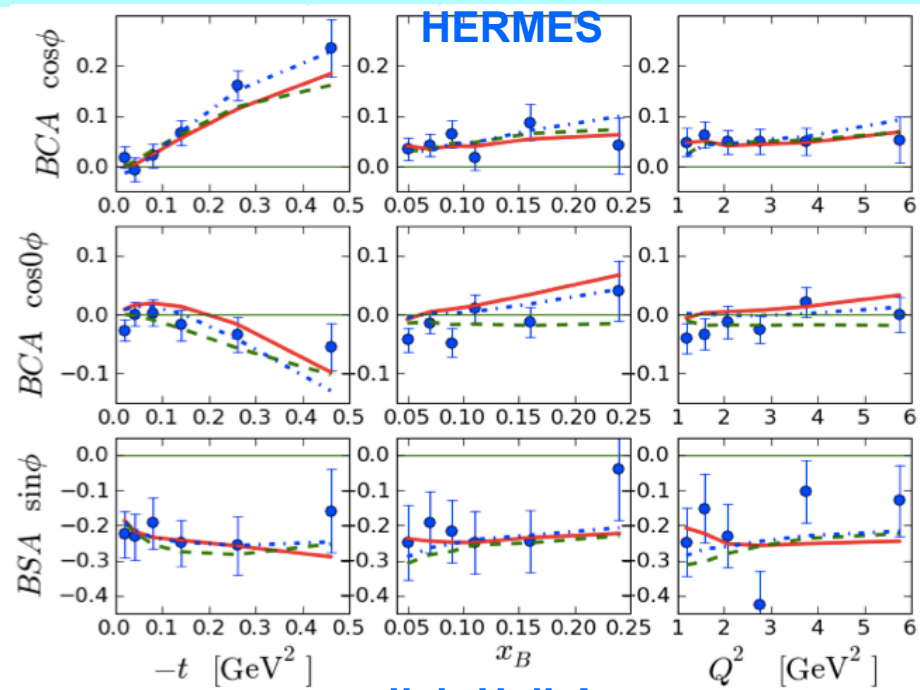
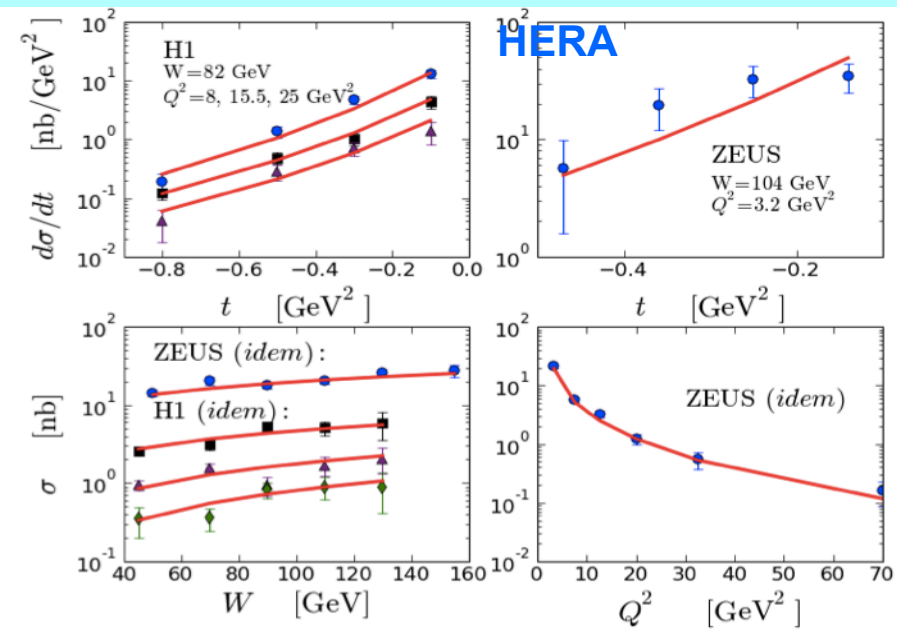
- ✧ Orbital contribution to proton's spin
- ✧ Proton radius of quark & gluon density
- ✧ Hints for color confining radius/mechanism
- ✧ Origin of nuclear force, ...
- ✧ ...

How far does glue density spread?

How fast does glue density fall?



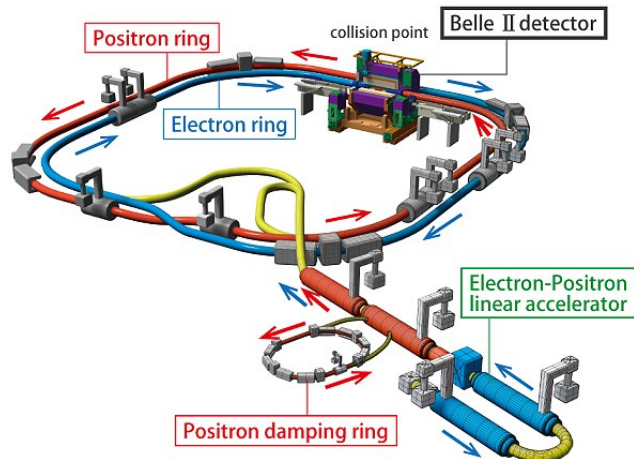
# GPDs: just the beginning



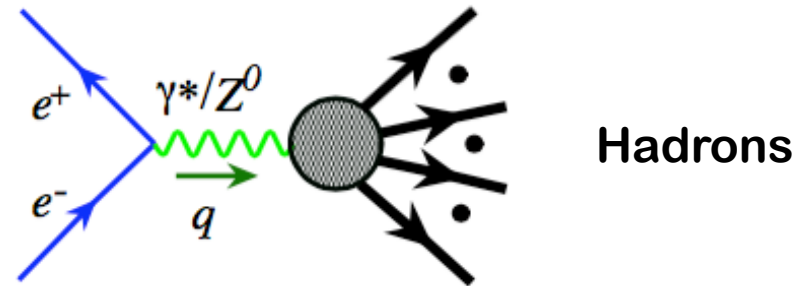


# Hard probes from high energy collisions

## □ Lepton-lepton collisions:



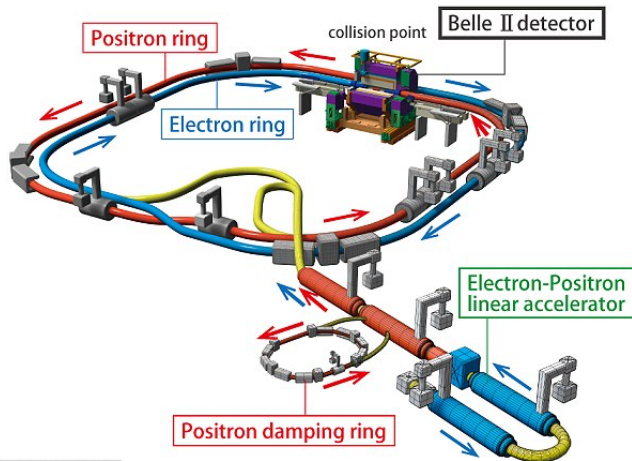
© James Fast/PNNL



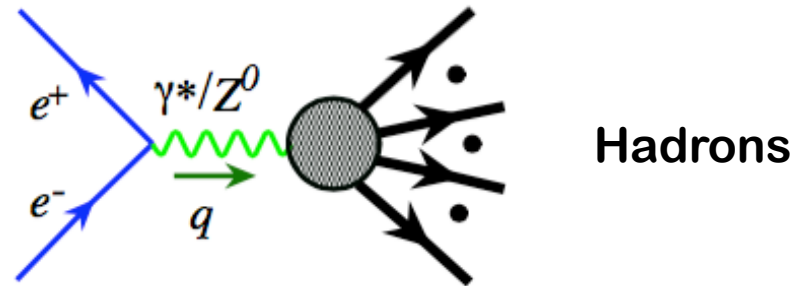
- ✧ No hadron in the initial-state
- ✧ Hadrons are emerged from energy
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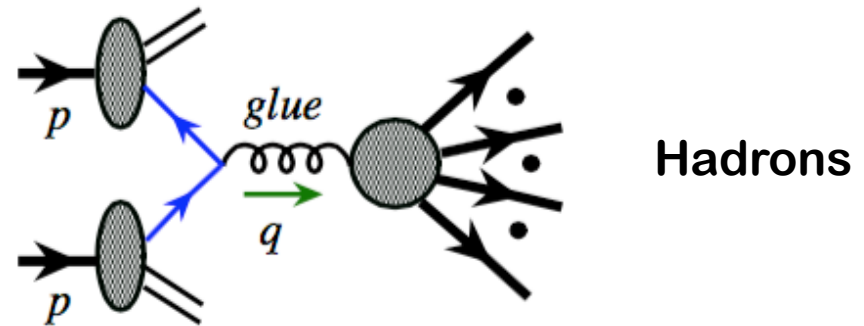
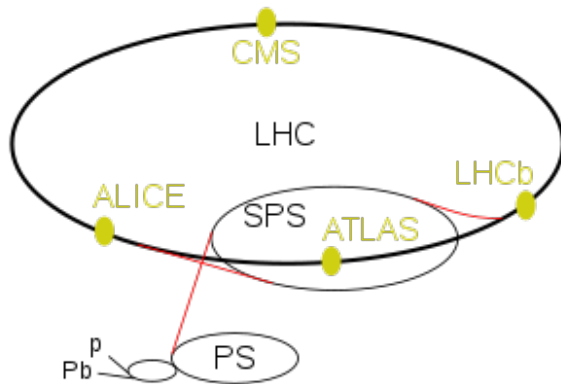


© James Fast/PNNL



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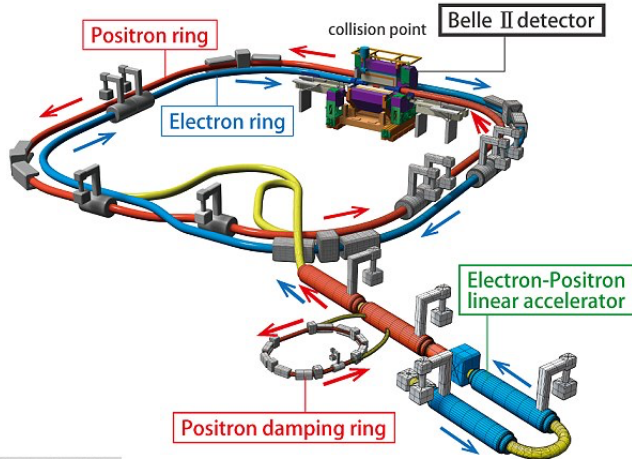
## □ Hadron-hadron collisions:



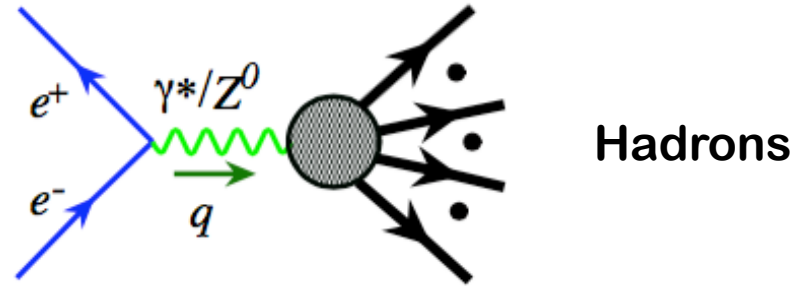
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- ✧ Hadron structure – motion of quarks, ...
- ✧ Emergence of hadrons, ...

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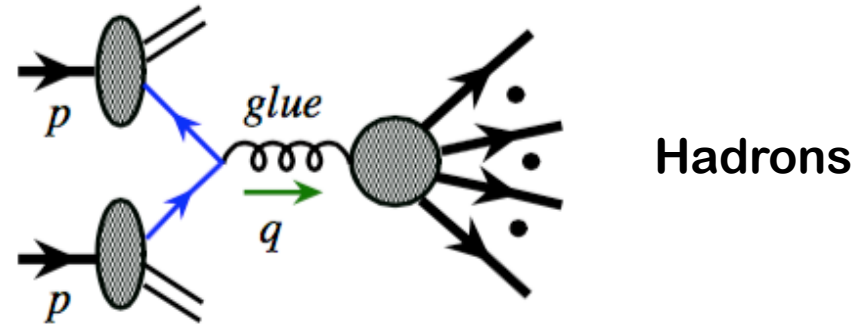
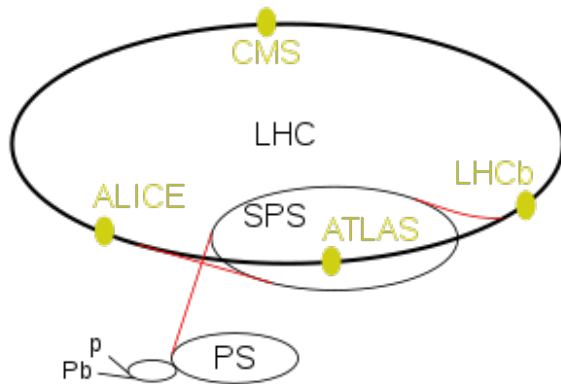


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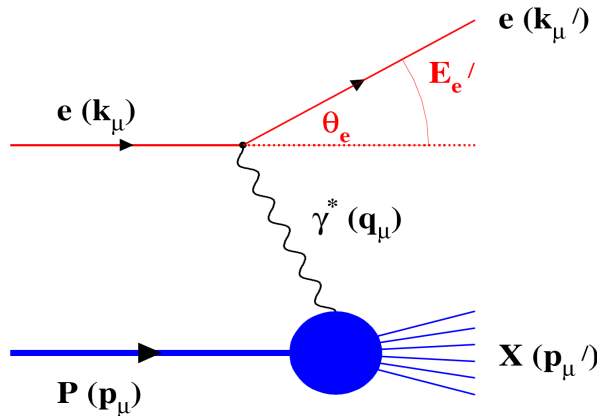
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## □ Lepton-hadron collisions:

Hard collision **without breaking** the initial-state hadron – spatial imaging, ...

# Many complementary probes at one facility

## □ The future “Rutherford” experiment:



$Q^2$  → Measure of resolution

$y$  → Measure of inelasticity

$x$  → Measure of momentum fraction  
of the struck quark in a proton

$$Q^2 = S x y$$

**Inclusive events:**  $e+p/A \rightarrow e'+X$

Detect only the scattered lepton in the detector

(Modern Rutherford experiment!)

**Semi-Inclusive events:**  $e+p/A \rightarrow e'+h(p,K,p,jet)+X$

Detect the scattered lepton in coincidence with identified hadrons/jets

(Initial hadron is broken – confined motion! – cleaner than h-h collisions)

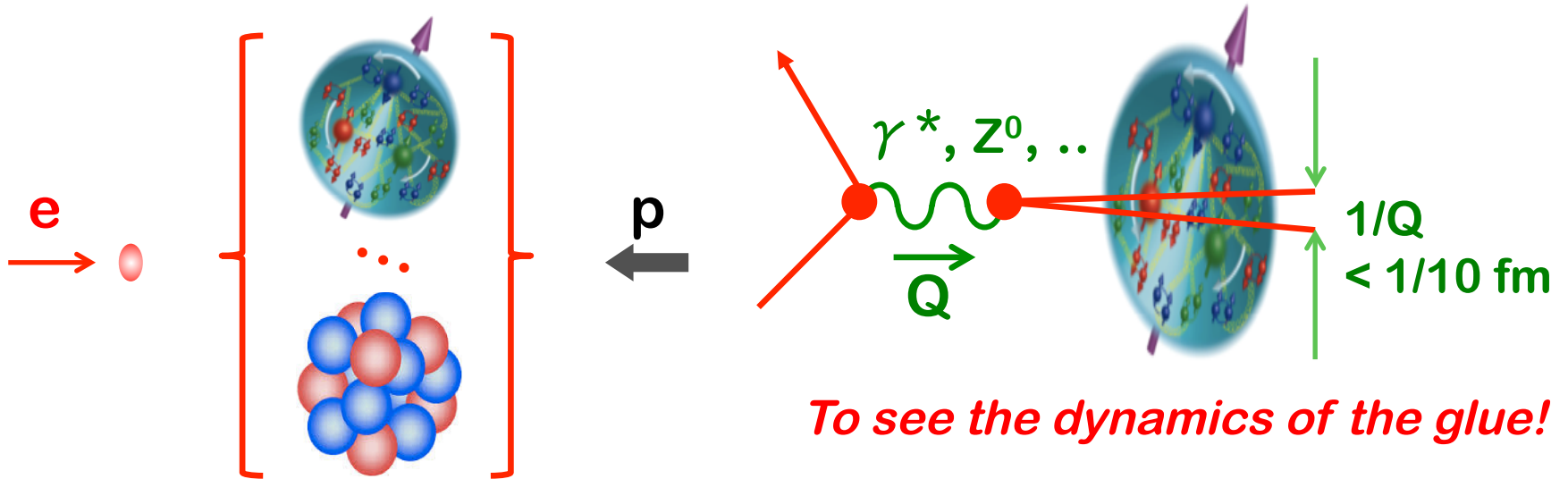
**Exclusive events:**  $e+p/A \rightarrow e'+p'/A'+h(p,K,p,jet)$

Detect every things including scattered proton/nucleus (or its fragments)

(Initial hadron is NOT broken – tomography! – almost impossible for h-h collisions)

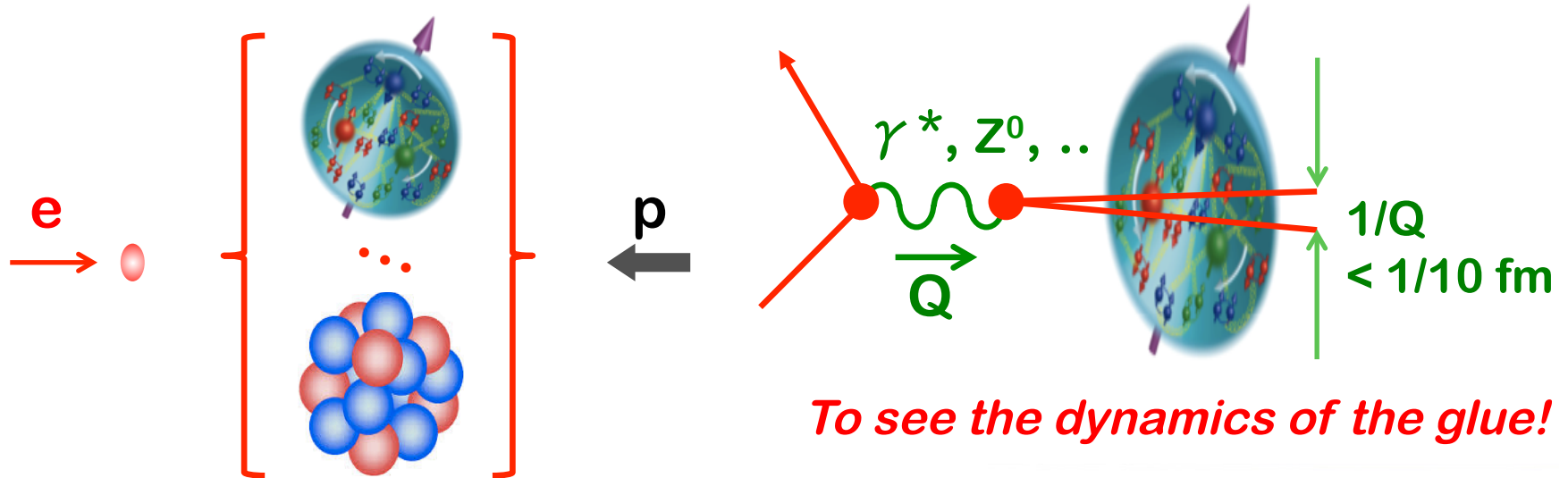
# From JLab12 to Electron-Ion Collider (EIC)

- A giant “Microscope” – “see” quarks and gluons by breaking the hadron



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- A sharpest “CT” – “imagine” quark/gluon structure without breaking the hadron

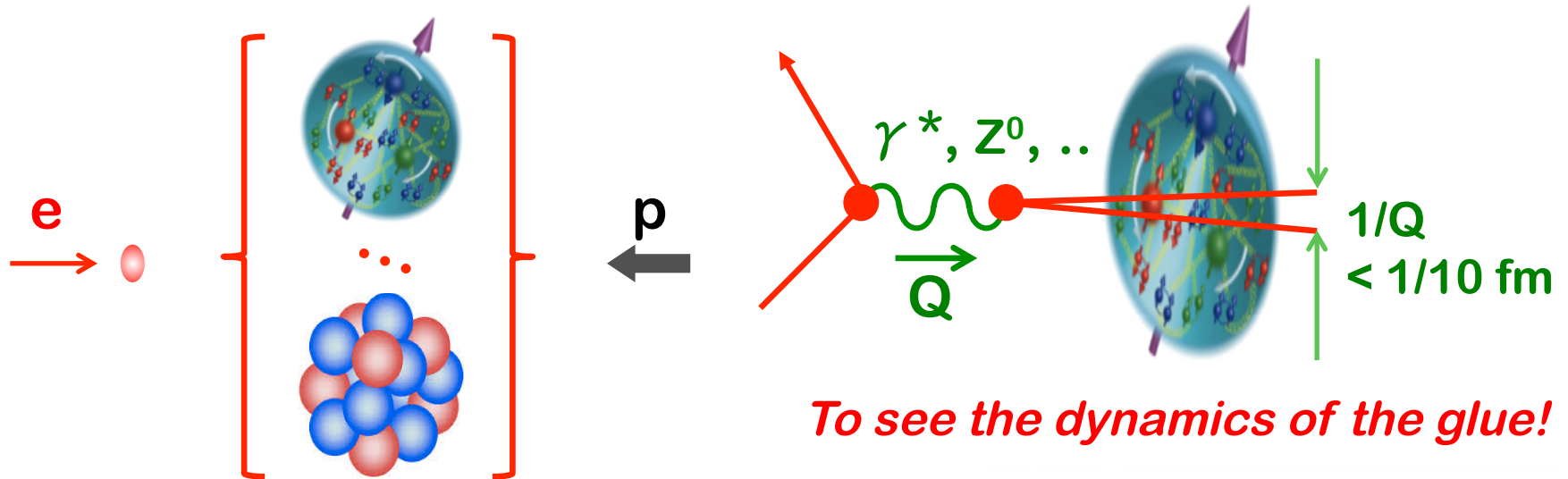
- “cat-scan” the nucleon and nuclei with a better than  $1/10 \text{ fm}$  resolution
- “see” proton “radius” of quark/gluon density as a function of “ $x$ ” – another tunable knob!



→ *To discover color confining radius, hints on confining mechanism!*

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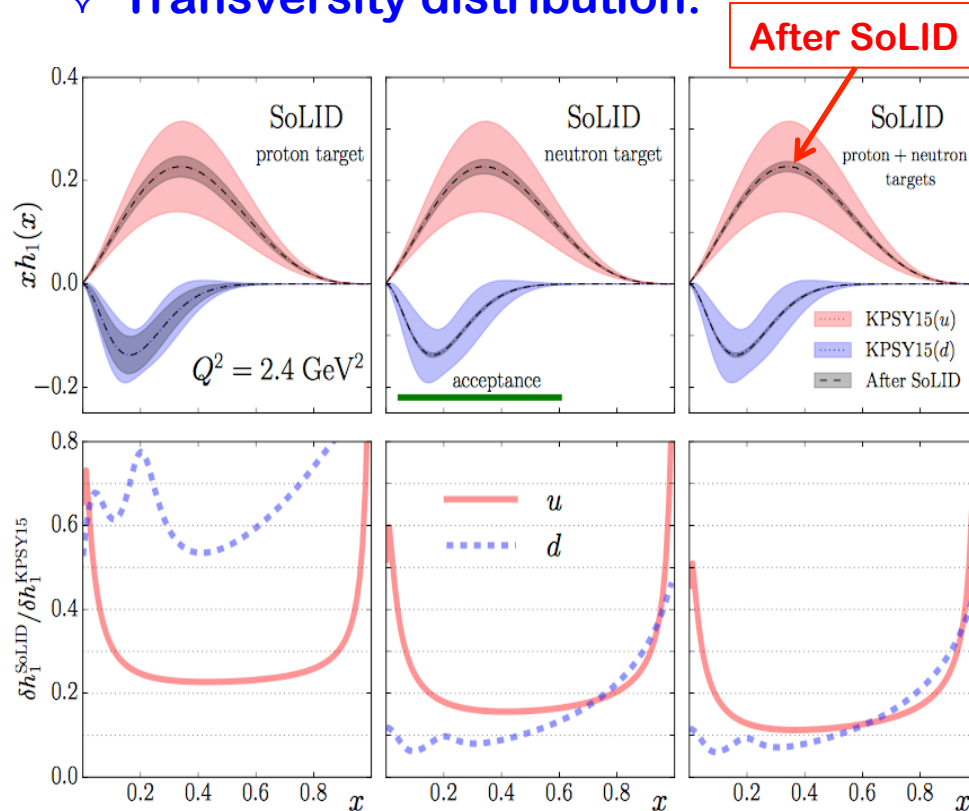
JLab12 – valence quarks, EIC – sea quarks and gluons

# Impact of future SoLID at JLab12

Z. Ye *et al.* Phys Lett. B767, 91 (2017)

## □ Transversity & Tensor charge:

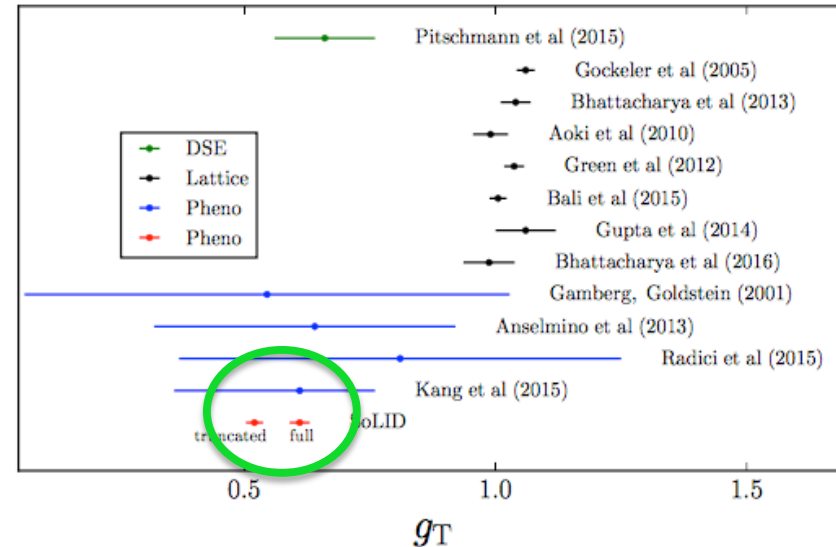
### ✧ Transversity distribution:



### ✧ Tensor charge:

$$\delta q(Q^2) \equiv \int_0^1 dx (h_1^q(x, Q^2) - \bar{h}_1^q(x, Q^2))$$

$$g_T = \delta u - \delta d$$



Bayesian statistics is used to estimate the improvement from new data  
 Current knowledge corresponds to a fit with TMD evolution Kang *et al.*, P.R. D93 (16) 014009

**Order of magnitude improvement in determining the tensor charge!**

“full” is contribution from  $0 < x < 1$  region  
 “truncated” is contribution from  $0.05 < x < 0.6$



# Why US-EIC can do what HERA can't do?

See talks by R. Ent,

## □ Quantum imaging:

- ✧ HERA discovered: 15% of e-p events is diffractive – Proton not broken!
- ✧ US-EIC: 100-1000 times **luminosity** – *Critical for 3D tomography!*

# Why US-EIC can do what HERA can't do?

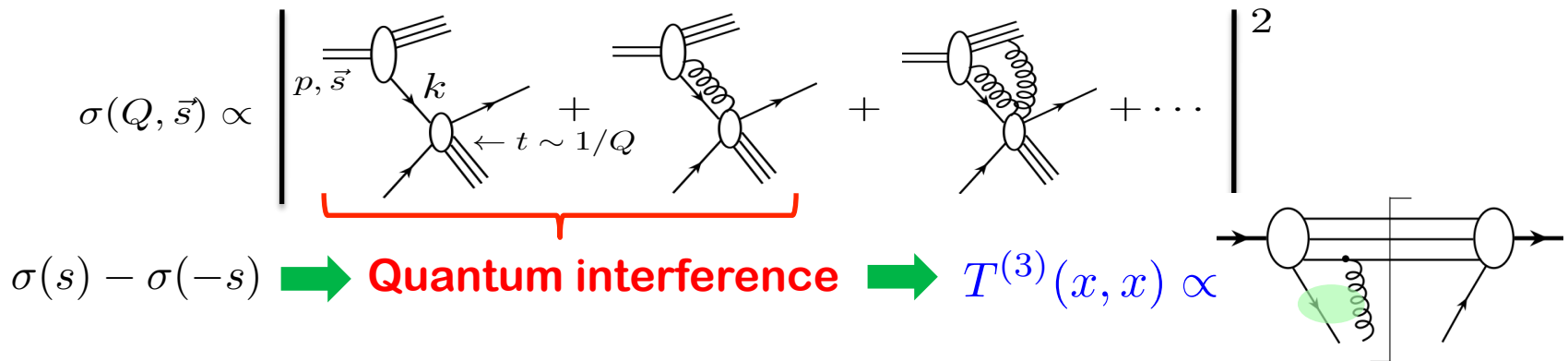
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*Direct access to chromo-quantum interference!*



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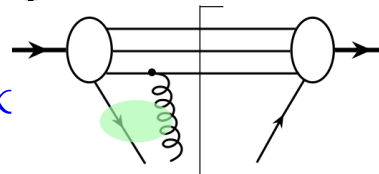
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*Direct access to chromo-quantum interference!*

$$\sigma(Q, \vec{s}) \propto \left| \begin{array}{c} \text{Diagram 1} \\ \text{Diagram 2} \\ \text{Diagram 3} \\ \dots \end{array} \right|^2$$

$\sigma(s) - \sigma(-s) \rightarrow$  **Quantum interference**  $\rightarrow T^{(3)}(x, x) \propto$  

The diagram shows a series of Feynman diagrams for diffractive scattering. The first diagram shows a proton (represented by three lines) interacting with a photon (k) and a proton (t) via a gluon exchange. The second diagram shows a similar process but with a different gluon configuration. The third diagram shows a more complex gluon configuration. The diagrams are summed and squared to give the cross-section. A red bracket underlines the first two diagrams, indicating quantum interference. The final diagram shows a proton with a gluon fluctuation (a green shaded area) and a photon (k) interacting with another proton (t).

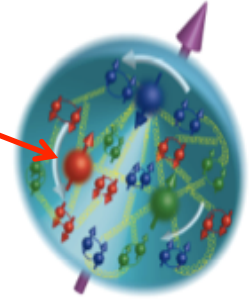
## Nonlinear quantum dynamics:

- US-EIC: Light-to-heavy **nuclear** beams – *Origin of nuclear force, ...*  
*Help Catch the transition from chromo-quantum fluctuation to chromo-condensate of gluons,*  
*Emergence of hadrons (femtometer size detector!),*  
– *“a new controllable knob” – Atomic weight of nuclei*

# Summary

- ❑ QCD has been extremely successful in interpreting and predicting high energy experimental data!
- ❑ But, we still do not know much about hadron structure – work just started!
- ❑ Cross sections with large momentum transfer(s) and identified hadron(s) are the source of structure information
- ❑ QCD factorization is necessary for any controllable “probe” for hadron’s quark-gluon structure!
- ❑ EIC is a ultimate QCD machine, will provide answers to many of our questions on hadron structure, in particular, the confined transverse motions (TMDs), spatial distributions (GPDs), and multi-parton correlations, ...

< 1/10 fm



Round table discussion  
on this Wednesday!

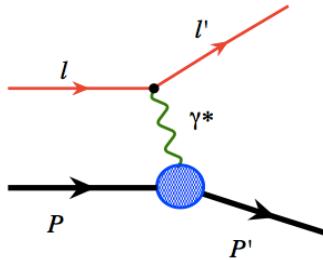
**Thank you!**

**Backup slides**

# What could we learn about hadron structure?

## □ No elastic color current form factor!

QED:

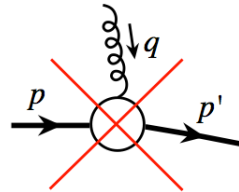


➡ *Form factors*

➡ *Electric charge distribution*

➡ *Proton radius – EM charge*

QCD:



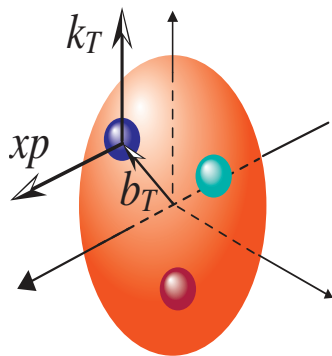
*Gluon carries color!*

➡ *Parton density distributions*

➡ *Proton radius – quark & gluon density distributions*

## □ Single-parton structure “seen” by a short-distance probe:

✧ 5D structure – encoded into the following density distributions:



1)  $\int d^2 b_T$  ➡  $f(x, k_T, \mu)$  – **TMDs**: *2D confined motion!*

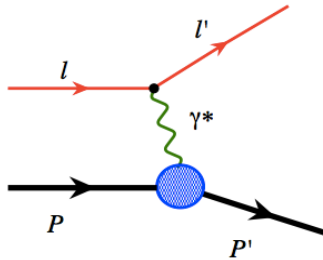
2)  $\int d^2 k_T$  ➡  $F(x, b_T, \mu)$  – **GPDs**: *2D spatial imaging!*

3)  $\int d^2 k_T d^2 b_T$  ➡  $f(x, \mu)$  – **PDFs**: *Number density!*

# What could we learn about hadron structure?

## □ No elastic color current form factor!

QED:

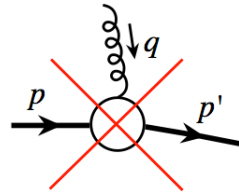


➡ *Form factors*

➡ *Electric charge distribution*

➡ *Proton radius – EM charge*

QCD:



*Gluon carries color!*

➡ *Parton density distributions*

➡ *Proton radius – quark & gluon density distributions*

## □ Multi-parton, quark-gluon corrections:

Single-spin asymmetry:  $\propto [\sigma(Q, \vec{s}) - \sigma(Q, -\vec{s})]$

$$\sigma(Q, \vec{s}) \propto \left| \begin{array}{c} \text{Diagram 1} \\ \text{Diagram 2} \\ \text{Diagram 3} \\ \dots \end{array} \right|^2 \left( \frac{\langle k_{\perp} \rangle}{Q} \right)^n \text{ – Expansion}$$

The diagrams show a proton with momentum  $p$  and spin  $\vec{s}$  interacting with a lepton with momentum  $l$  and outgoing lepton  $l'$ . The diagrams represent different parton-level interactions: a quark line with a gluon loop (Diagram 1), a quark line with a gluon exchange (Diagram 2), and a gluon line with a quark loop (Diagram 3). The momentum transfer is  $Q$ , and the transverse momentum is  $k_{\perp}$ . The expansion is in powers of  $\langle k_{\perp} \rangle / Q$ .

Quantum interference ➡ 3-parton matrix element – not a probability!