

# Experimental Overview of GPDs

Andrea Ferrero, CEA Saclay/IRFU

Transversity 2017, 11-15/12/2017, Frascati

## DVCS on proton -> GPD $H$

Beam Spin Asym: HallA – CLAS - HERMES

Beam Charge Asym: HERMES – H1 – (COMPASS)

Cross section diff and sum: HallA – CLAS – COMPASS

## Proton « tomography »

$t$ -slope of DVCS x-section: H1 – ZEUS – COMPASS

Global fits of CFFs: HallA – CLAS

## Exclusive p0 production: « transversity » GPDs

Cross section measurement: HallA – CLAS – COMPASS

## Hunting the GPD $E$ → ‘Holy grail’ for OAM

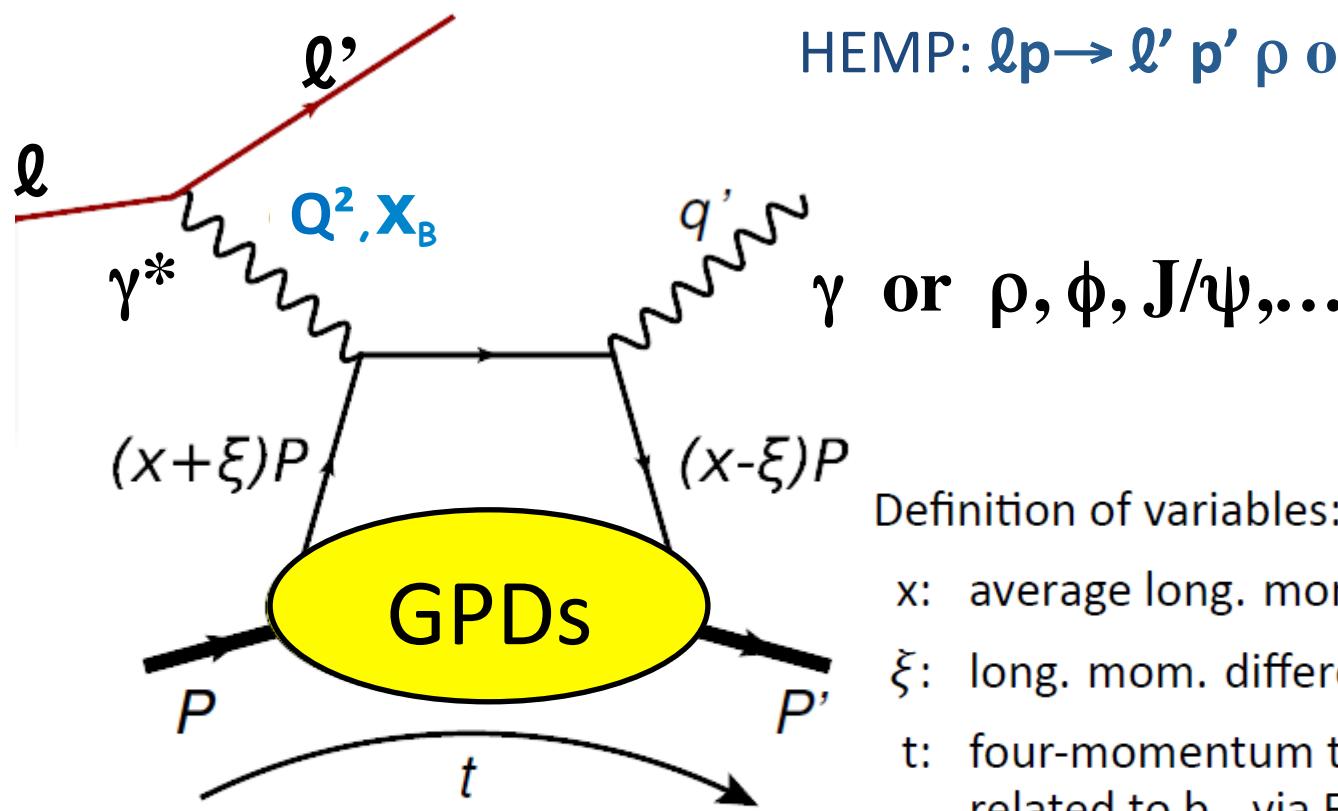
Transv. Pol. Target Asym on the proton - HERMES - (JLab) – (COMPASS)

Beam Spin cross section on the neutron – HallA – (Jlab)

# Exclusive reactions: DVCS and HEMP

DVCS:  $\ell p \rightarrow \ell' p' \gamma$  (« golden » channel)

HEMP:  $\ell p \rightarrow \ell' p' \rho$  or  $\phi$  or  $J/\psi, \dots$



Definition of variables:

$x$ : average long. momentum - NOT ACCESSIBLE

$\xi$ : long. mom. difference  $\simeq x_B/(2 - x_B)$

$t$ : four-momentum transfer  
related to  $b_{\perp}$  via Fourier transform

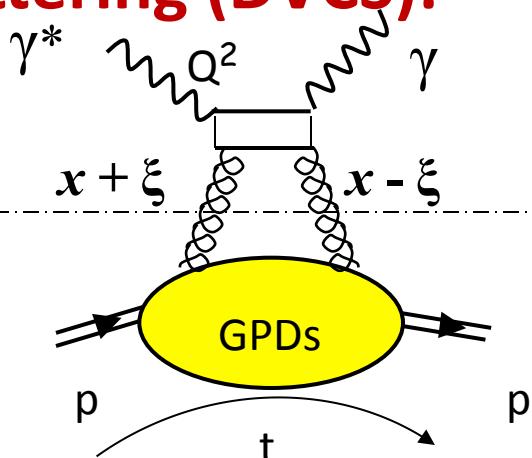
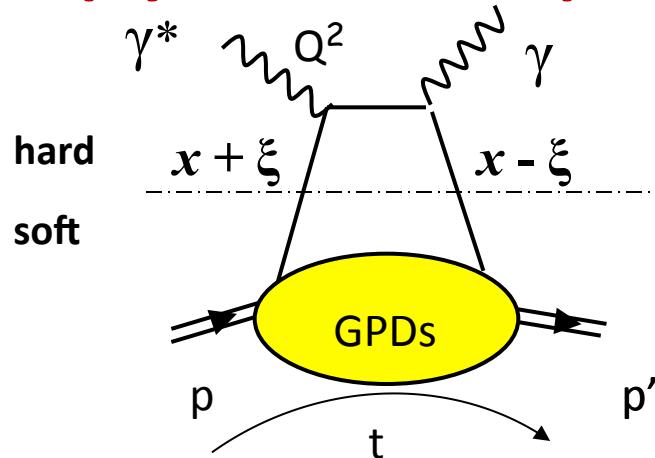
D. Mueller *et al*, Fortsch. Phys. 42 (1994)

X.D. Ji, PRL 78 (1997), PRD 55 (1997)

A. V. Radyushkin, PLB 385 (1996), PRD 56 (1997)

# Exclusive reactions: DVCS and HEMP

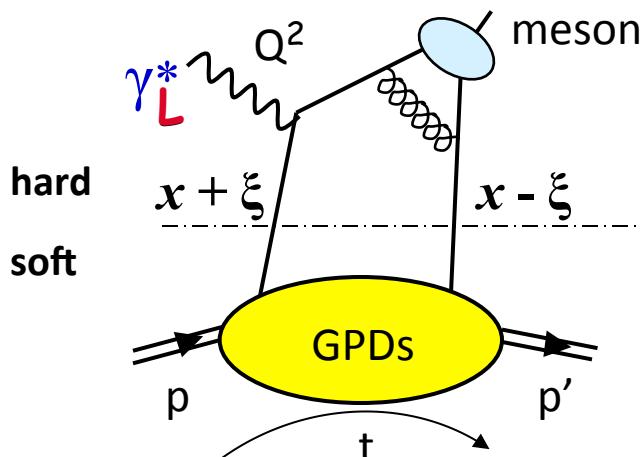
## Deeply Virtual Compton Scattering (DVCS):



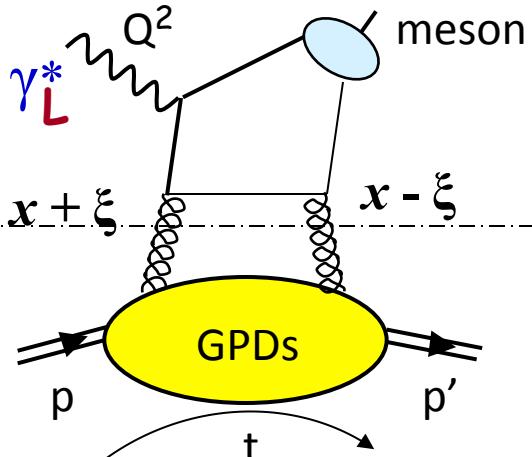
Factorisation:  
Collins *et al.*

$Q^2$  large  
 $t \ll Q^2$

## Hard Exclusive Meson Production (HEMP):



Quark contribution



Gluon contribution

Meson w.f.  
Large power & NLO  
Very slow scaling

8 GPDs



8 TMDs

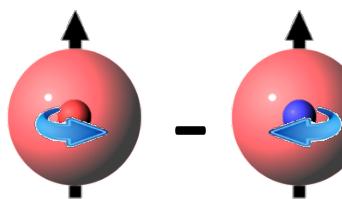
4 Chiral-even

$$H \longleftrightarrow q \text{ or } f_1$$



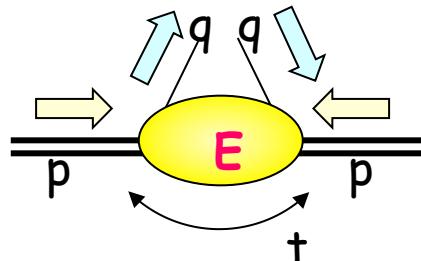
"Elusive"  $E$

$$\sim f_{1T}^\perp$$



**Sivers:** quark  $k_T$   
& nucleon transv. Spin

$$J_i: 2J^q = \int x (H^q(x, \xi, 0) + E^q(x, \xi, 0)) dx$$



## Relation to OAM

+ their partner for polarised quarks

$$\tilde{H} \longleftrightarrow \Delta q \text{ or } g_{1L}$$

$$\tilde{E} \sim g_{1T}$$

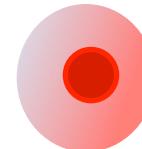
8 GPDs



8 TMDs

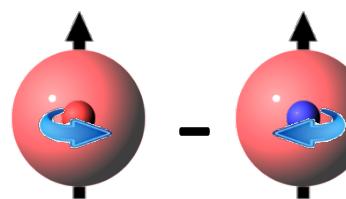
2 of the 4 Chiral-even

$$H \longleftrightarrow q \text{ or } f_1$$



"Elusive"  $E$

$$f_{1T}^\perp$$

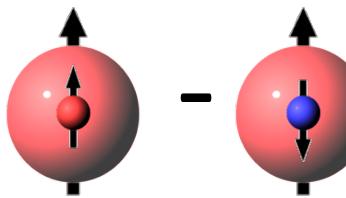


**Sivers:** quark  $k_T$   
& nucleon transv. Spin

$$J_i: 2J^q = \int x (H^q(x, \xi, 0) + E^q(x, \xi, 0)) dx$$

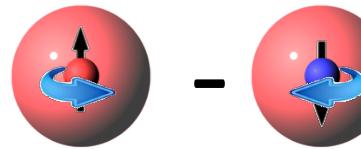
2 of the 4 Chiral-odd

$$H_T \longleftrightarrow h_1$$



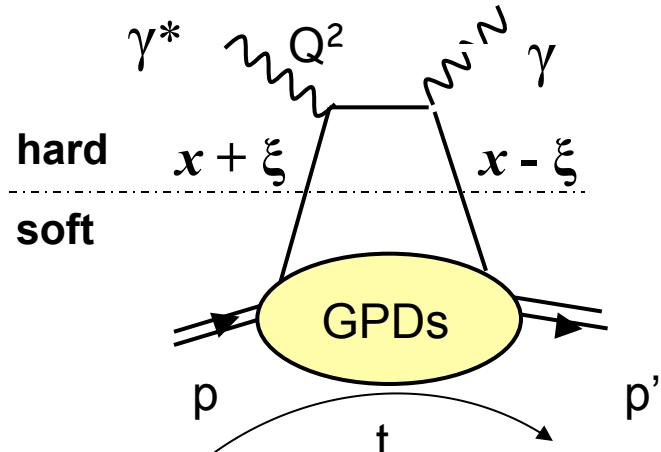
**Transversity:** quark spin  
& nucleon transv. spin

$$\bar{E}_T = 2\tilde{H}_T + E_T \sim h_1^\perp$$



**Boer-Mulders:** quark  $k_T$   
& quark transverse spin

# From DVCS to Compton Form Factors

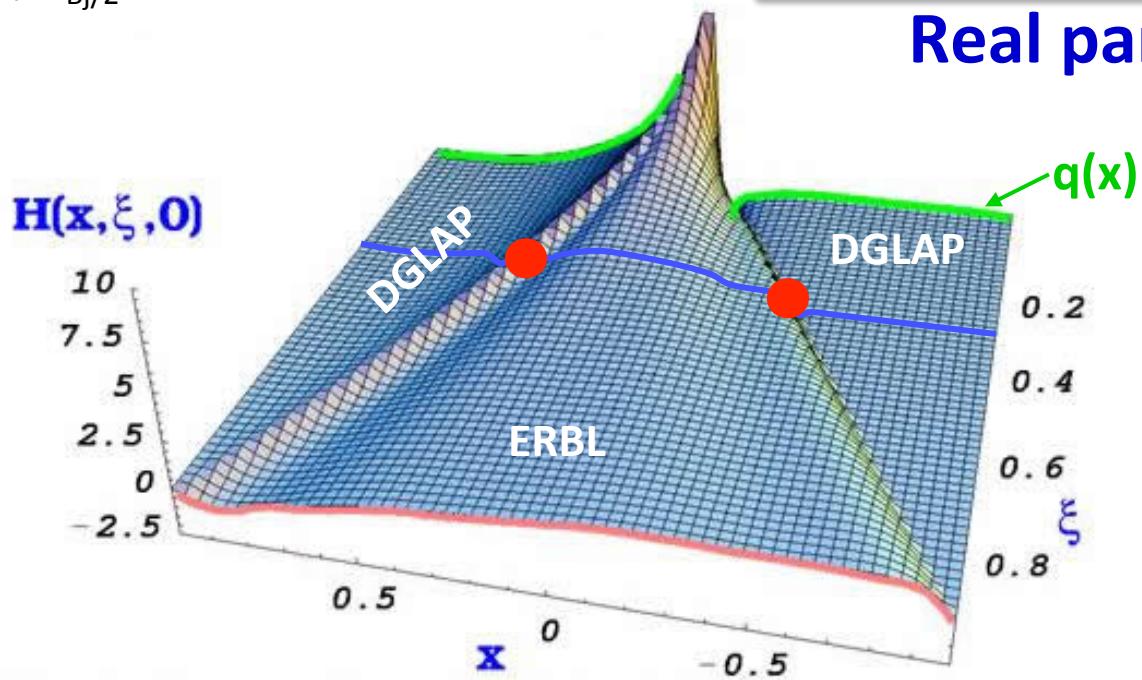


The DVCS amplitude at LT & LO in  $\alpha_S$ :

$$\mathcal{H} = \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi + i\epsilon} = \mathcal{P} \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi} - i\pi H(x = \xi, \xi, t)$$

**Real part**

**Imaginary part**

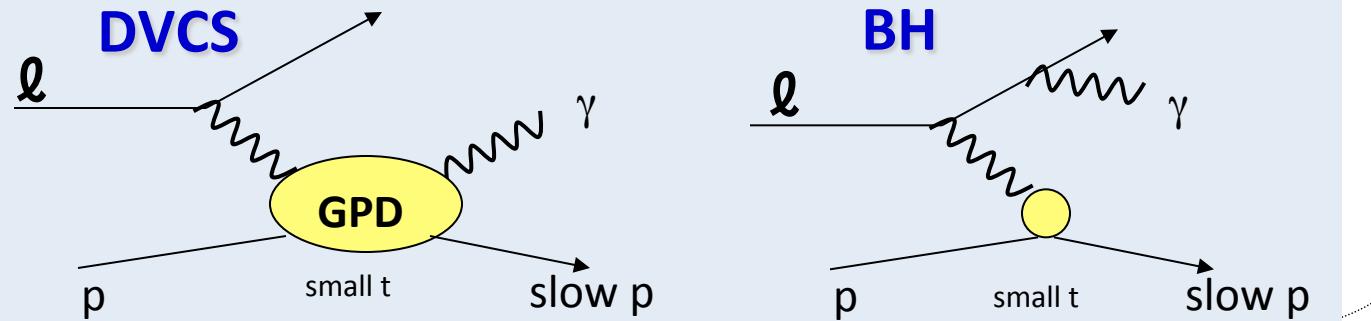


Im part measured in  
Beam Spin  
or Target Spin asymmetries

Real part measured in  
Beam Charge asymmetry  
or cross section

# DVCS (golden channel) → CFF → GPD H (E)

Exclusive Single Photon production  $\ell p \rightarrow \ell' p' \gamma$

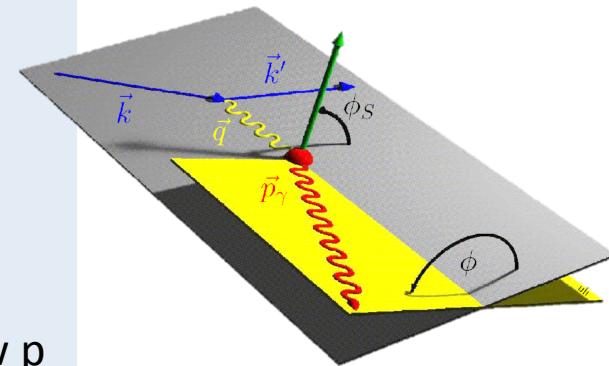
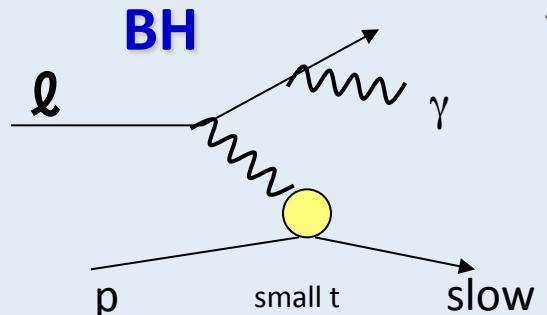
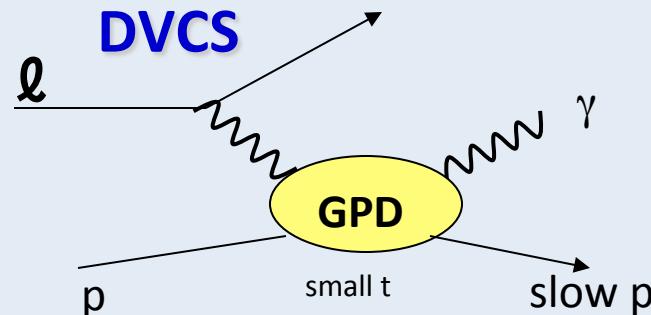


$$d\sigma \propto |\mathcal{T}^{\text{BH}}|^2 + \text{Im}(\mathcal{T}^{\text{DVCS}}) \cdot \mathcal{T}^{\text{BH}} + \text{Re}(\mathcal{T}^{\text{DVCS}}) \cdot \mathcal{T}^{\text{BH}} + |\mathcal{T}^{\text{DVCS}}|^2$$

Known to 1 %      Linear combination of GPDs      bilinear combination of GPDs

# DVCS (golden channel) → CFF → GPD H (E)

Exclusive Single Photon production  $\ell p \rightarrow \ell' p' \gamma$



$$d\sigma \propto |\mathcal{T}^{BH}|^2 + \text{Im}(\mathcal{T}^{DVCS}) \cdot \mathcal{T}^{BH} + \text{Re}(\mathcal{T}^{DVCS}) \cdot \mathcal{T}^{BH} + |\mathcal{T}^{DVCS}|^2$$

Known to 1 %

Linear combination of GPDs

bilinear combination of GPDs

**Beam Charge** Difference on proton

$$A_C^{\cos\phi} = \text{Re} (F_1 \mathcal{H} + \xi (F_1 + F_2) \tilde{\mathcal{H}} - t/4m^2 F_2 \mathcal{E}) \rightarrow \text{Re} (F_1 \mathcal{H})$$

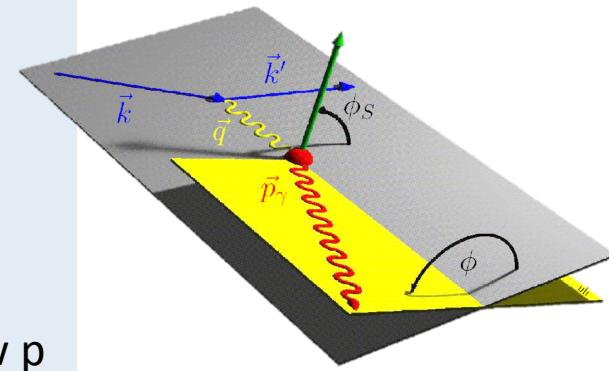
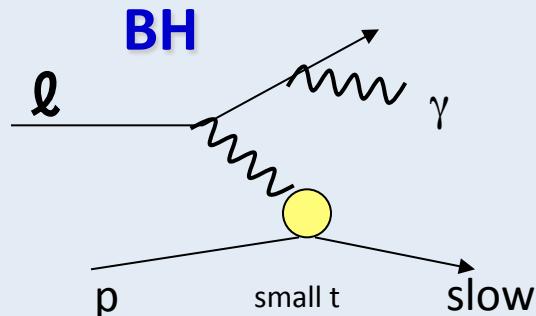
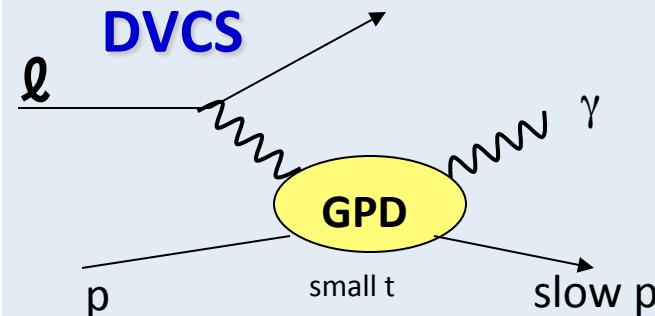
small  $x_B$

**Beam Spin** Difference on proton

$$A_{LU}^{\sin\phi} = \text{Im} (F_1 \mathcal{H} + \xi (F_1 + F_2) \tilde{\mathcal{H}} - t/4m^2 F_2 \mathcal{E}) \rightarrow \text{Im} (F_1 \mathcal{H})$$

# DVCS (golden channel) → CFF → GPD H (E)

Exclusive Single Photon production  $\ell p \rightarrow \ell' p' \gamma$



$$d\sigma \propto |\mathcal{T}^{BH}|^2 + Im(\mathcal{T}^{DVCS}) \cdot \mathcal{T}^{BH} + Re(\mathcal{T}^{DVCS}) \cdot \mathcal{T}^{BH} + |\mathcal{T}^{DVCS}|^2$$

Known to 1 %

Linear combination of GPDs

bilinear combination of GPDs

**Beam Spin Asym on neutron**

$$A_{LU} \sin\phi \rightarrow Im(F_{1n}\mathcal{H} - F_{2n}\mathcal{E})$$

$\mathcal{H}$  and  $\mathcal{E}$   
On the same footing

**Transv. Target Spin Asym on proton**

$$A_{UT} \sin(\phi - \phi_S) \cos\phi \rightarrow Im(F_2\mathcal{H} - F_1\mathcal{E})$$

# HEMP → (MFF)<sup>2</sup>→ filter of GPDs and flavors

## Hard Exclusive Meson Production (HEMP):

Vector meson production ( $\rho, \omega, \phi, J/\psi \dots$ )  $\Rightarrow H$  &  $E$

Pseudo-scalar production ( $\pi, \eta \dots$ )  $\Rightarrow \tilde{H}$  &  $\tilde{E}$

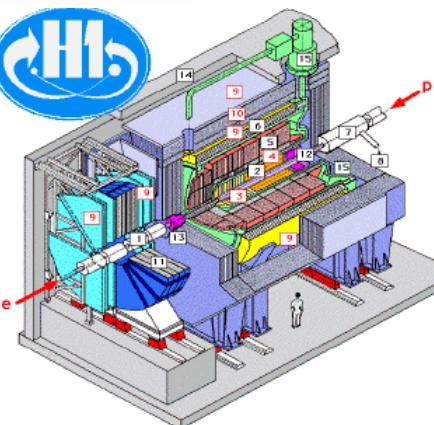
$$H\rho^0 = 1/\sqrt{2} (2/3 H^u + 1/3 H^d + 3/8 H^g)$$

$$H\omega = 1/\sqrt{2} (2/3 H^u - 1/3 H^d + 1/8 H^g)$$

$$H\phi = -1/3 H^s - 1/8 H^g$$

See talk by C. Van Hulse  
On Monday

# The past and future experiments



**Collider mode e-p** forward fast proton

**HERA: H1 and ZEUS**

Polarised 27 GeV e-/e+

Unpolarized 920 GeV proton

~ Full event reconstruction

**Fixed target mode** slow recoil proton

**HERMES:** Polarised 27 GeV e-/e+

Long, Trans polarised p, d target

Missing mass technique

2006-07 with recoil detector



Hall A

spectrometers

**Jlab: Hall A, C, CLAS** High lumi, polar. 6 & **12 GeV e-**

Long, (Trans) polarised p, d target

Missing mass technique



CLAS

Large acceptance  
detector

**COMPASS @ CERN:** Polarised **160 GeV  $\mu^+/\mu^-$**

p target, (Trans) polarised target

2012-17 with recoil detection



recoil proton  
detector  
CAMERA

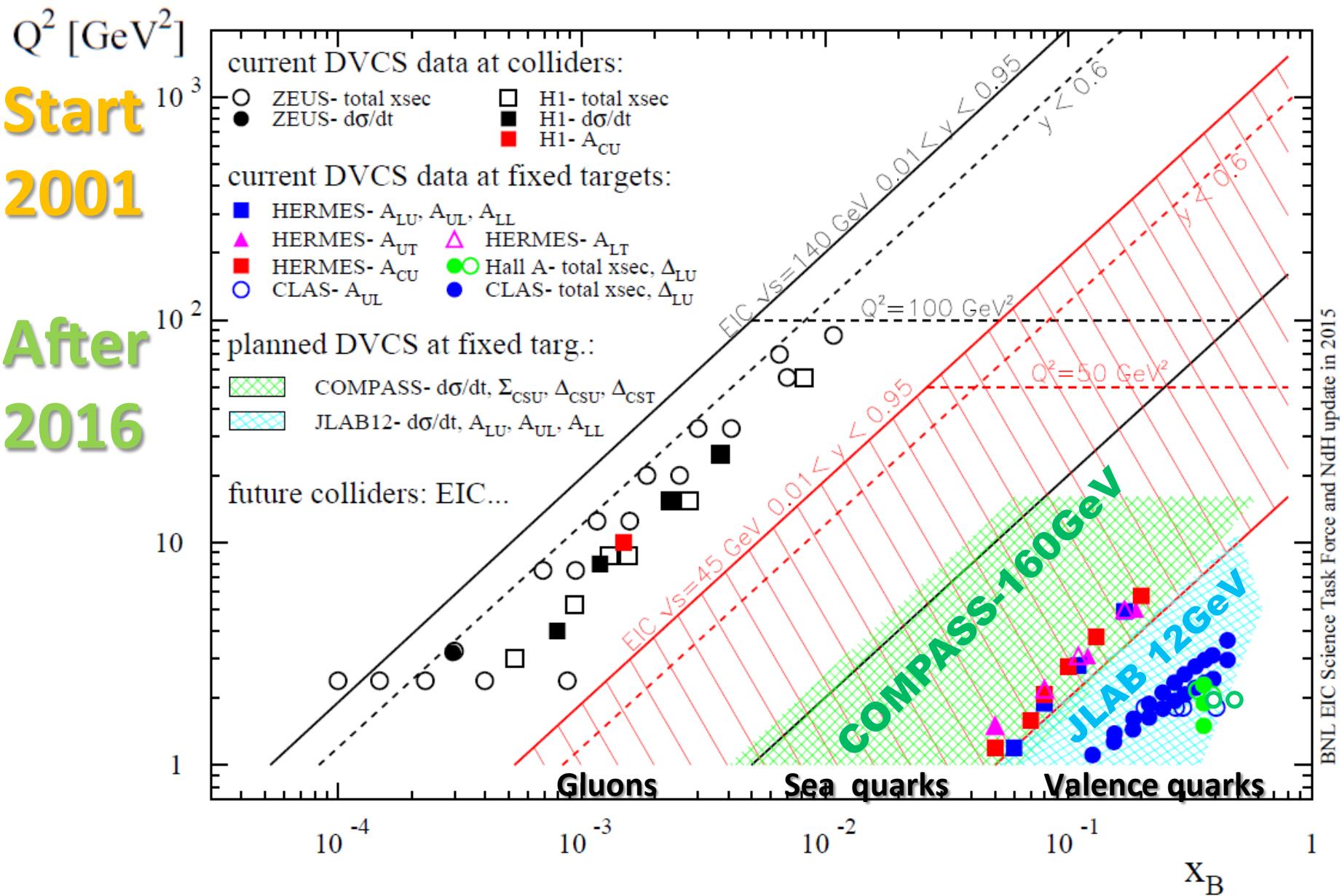
ECALO  
+ 60m long magnetic spectrometer  
of large acceptance  
with 3 EM Calos

COMPASS

# The past and future DVCS experiments

**Start  
2001**

**After  
2016**



# DVCS-BH interference on the proton

- $\text{Im DVCS}$  with Beam Helicity Dependent X-sect.
- $\text{Re DVCS}$  with Beam Charge Difference  
and Unpolarized X-section
  - mainly constrains on the GPD H

Beam Charge or Spin Asymmetries

→ easier to measure, harder to interpret

Beam Charge or Spin x-section diff./sum

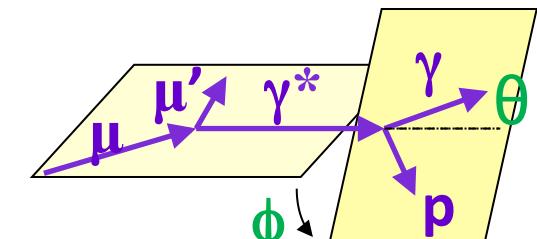
→ harder to measure, more direct to interpret

# Azimuthal dependence of BH+DVCS

$$\frac{d^4\sigma(\ell p \rightarrow \ell p \gamma)}{dx_B dQ^2 d|t| d\phi} = d\sigma^{BH} + \left( d\sigma_{unpol}^{DVCS} + P_\ell d\sigma_{pol}^{DVCS} \right) + (e_\ell \text{Re } I + e_\ell P_\ell \text{Im } I)$$

Well known

$d\sigma^{BH}$	$\propto c_0^{BH} + c_1^{BH} \cos \phi + c_2^{BH} \cos 2\phi$
$d\sigma_{unpol}^{DVCS}$	$\propto c_0^{DVCS} + c_1^{DVCS} \cos \phi + c_2^{DVCS} \cos 2\phi$
$d\sigma_{pol}^{DVCS}$	$\propto s_1^{DVCS} \sin \phi$
$\text{Re } I$	$\propto c_0^I + c_1^I \cos \phi + c_2^I \cos 2\phi + c_3^I \cos 3\phi$
$\text{Im } I$	$\propto s_1^I \sin \phi + s_2^I \sin 2\phi$



Twist-2 >>

- Twist-3,
- Twist-2

double helicity flip  
for gluons

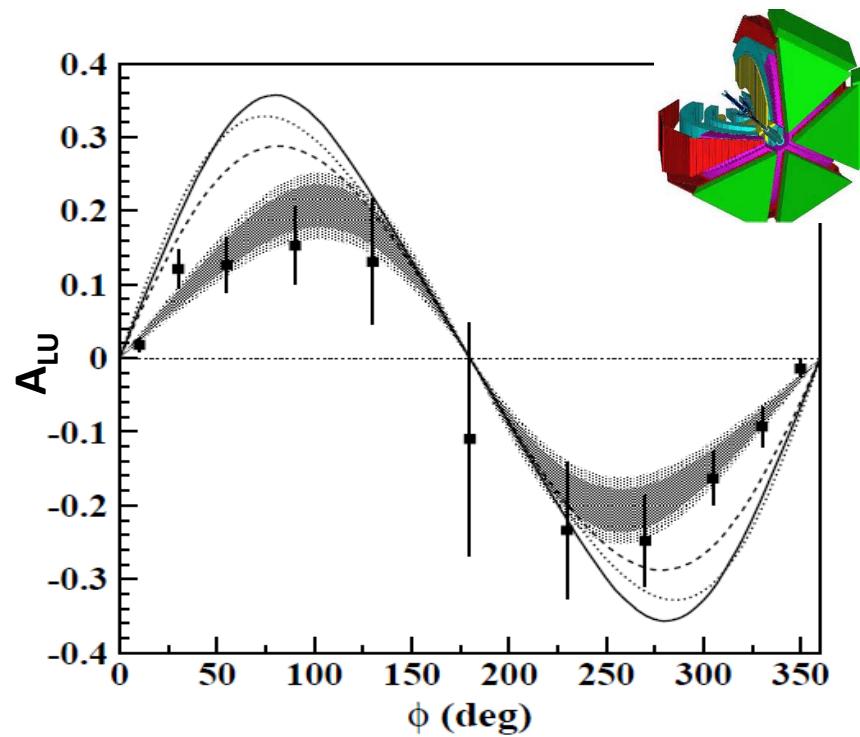
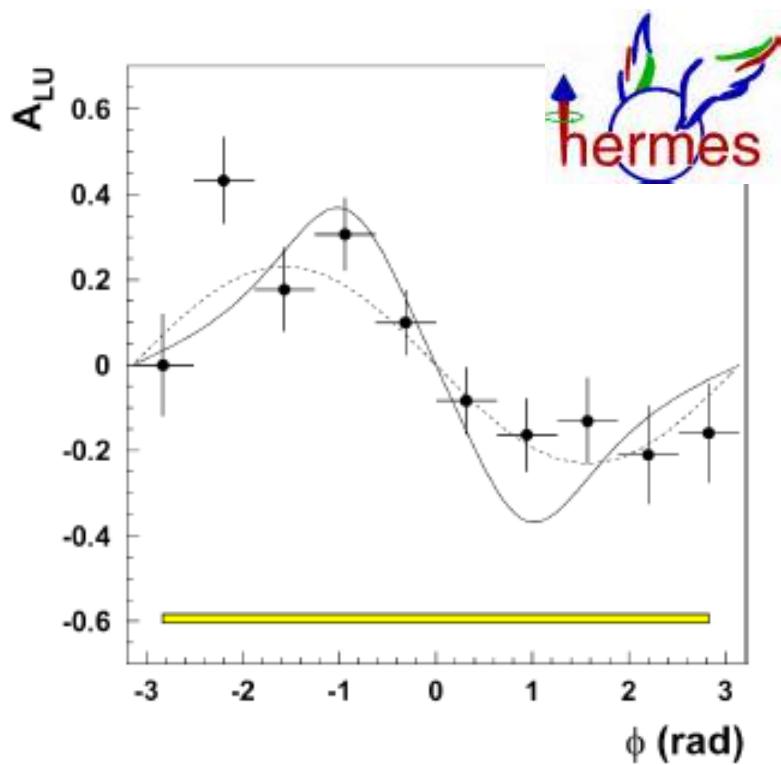
$$s_1^I = \text{Im } \mathcal{F} \quad c_1^I = \text{Re } \mathcal{F}$$

$$\mathcal{F} = F_1 \mathcal{H} + \xi (F_1 + F_2) \tilde{\mathcal{H}} - t/4m^2 F_2 \mathcal{E} \quad \xrightarrow{\text{at small } x_B} \quad F_1 \mathcal{H} \quad \text{for proton}$$

NB: to extract  $\mathcal{E}$  use a neutron (deuteron) target or a transversely pol. target  
to extract  $\tilde{\mathcal{H}}$  use a longitudinally polarized target

# First DVCS interference signals

BSA asymmetries – PRL87 (2001)



Validate the dominance of the handag contribution  
(Fit and VGG model)

# BSA and BCA with HERMES

Last analyses with the complete set of data including 2006-07

Combined analysis of charge and polarisation observables  
to separate interference term and DVCS<sup>2</sup> contributions

$$\sigma_{LU}(\phi; P_l, e_l) = \sigma_{UU}(\phi) \cdot \{ 1 + P_l A_{LU}^{\text{DVCS}}(\phi) + e_l P_l A_{LU}^I(\phi) + e_l A_C(\phi) \}$$

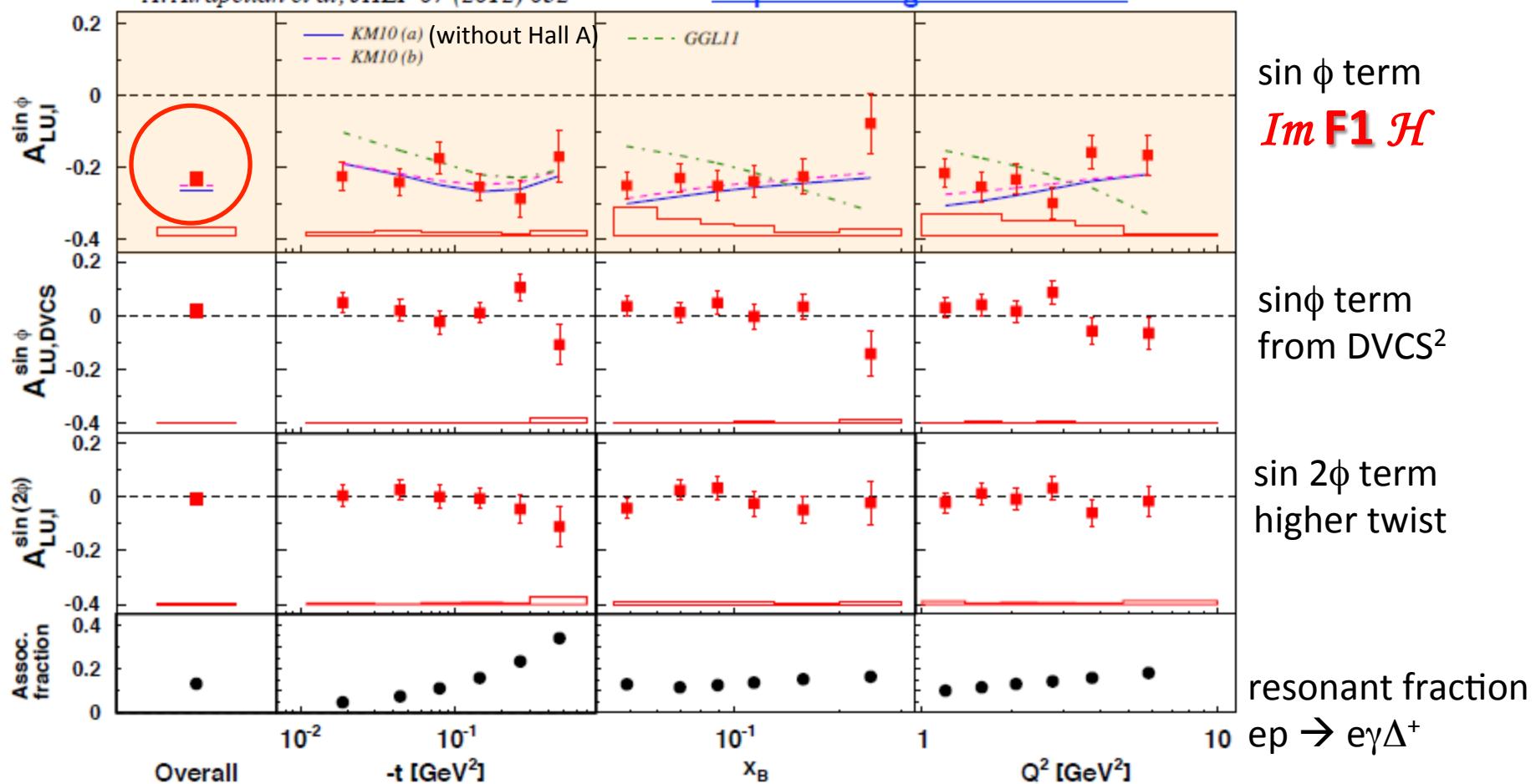
The equation shows the total cross-section  $\sigma_{LU}(\phi; P_l, e_l)$  as a product of the unpolarized cross-section  $\sigma_{UU}(\phi)$  and a sum of four terms. The first term is 1. The second term is  $P_l A_{LU}^{\text{DVCS}}(\phi)$ , which is highlighted with a blue circle and has an arrow pointing to the term  $s_1^{\text{DVCS}} \sin(\phi)$ . The third term is  $e_l P_l A_{LU}^I(\phi)$ , highlighted with a blue circle and has an arrow pointing to the term  $\sum_{n=1}^2 s_n^I \sin(n\phi)$ . The fourth term is  $e_l A_C(\phi)$ , highlighted with a blue circle and has an arrow pointing to the term  $\sum_{n=0}^3 c_n^I \cos(n\phi)$ .

# Beam Spin Asymmetry - HERMES

Complete data set including 2006-07

A. Airapetian et al, JHEP 07 (2012) 032

<http://arxiv.org/abs/1203.6287>



KM: <http://arxiv.org/abs/0904.0458>

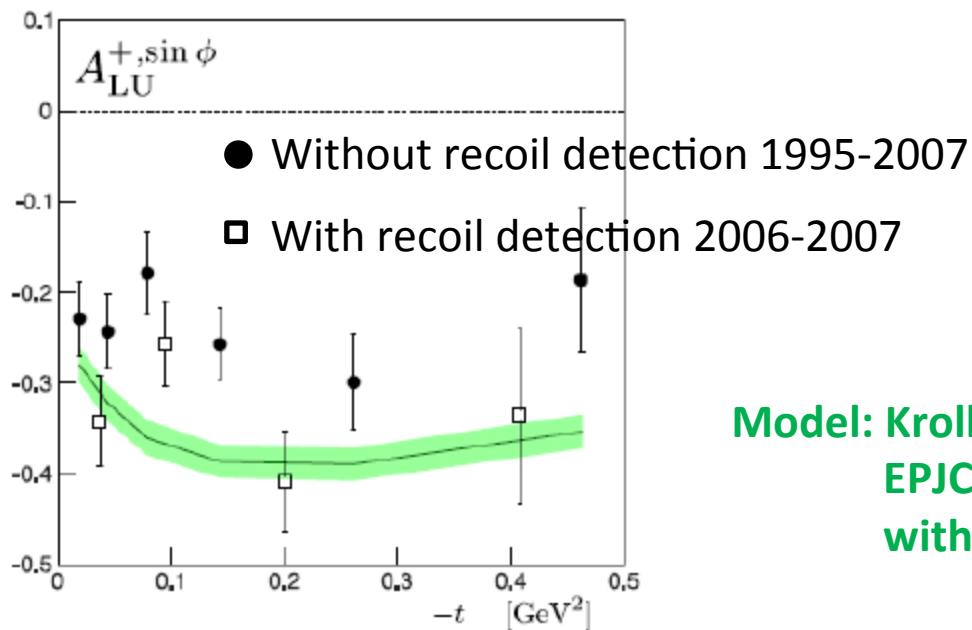
Kumerički and Müller, Nucl. Phys. **B841** (2010)

GHL11: flexible parameterization

<http://arxiv.org/abs/1012.3776>

G. Goldstein, J. Hernandez and S. Liuti, Phys. Rev. D84 (2011)

# BSA with recoil detector - HERMES



Model: Kroll, Moutarde, Sabatié,  
EPJC73 (2013)  
with GPDs from GK model

High-purity event selection shows that there is only  
a small influence on the extracted BSA amplitude  
from events involving an  $\Delta$  particle (associated DVCS)

The leading asymmetry has increased by  $0.054 \pm 0.016$

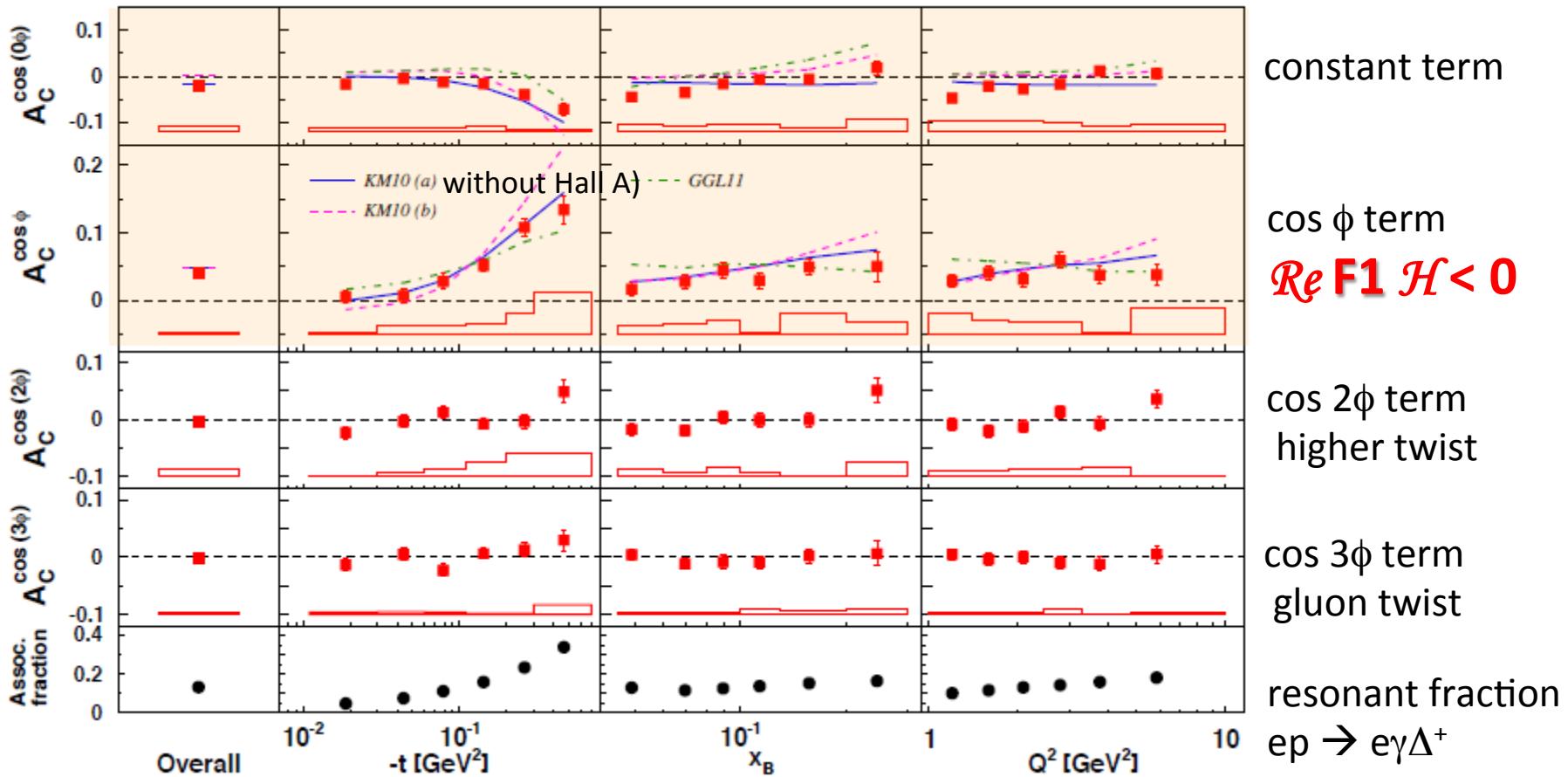
Mainly dilution due to the associated DVCS

# Beam Charge Asymmetry - HERMES

Complete data set including 2006-07 without recoil detection

A. Airapetian et al, JHEP 07 (2012) 032

<http://arxiv.org/abs/1203.6287>



KM: <http://arxiv.org/abs/0904.0458>

Kumerički and Müller, Nuc. Phys. **B841** (2010)

GHL11:

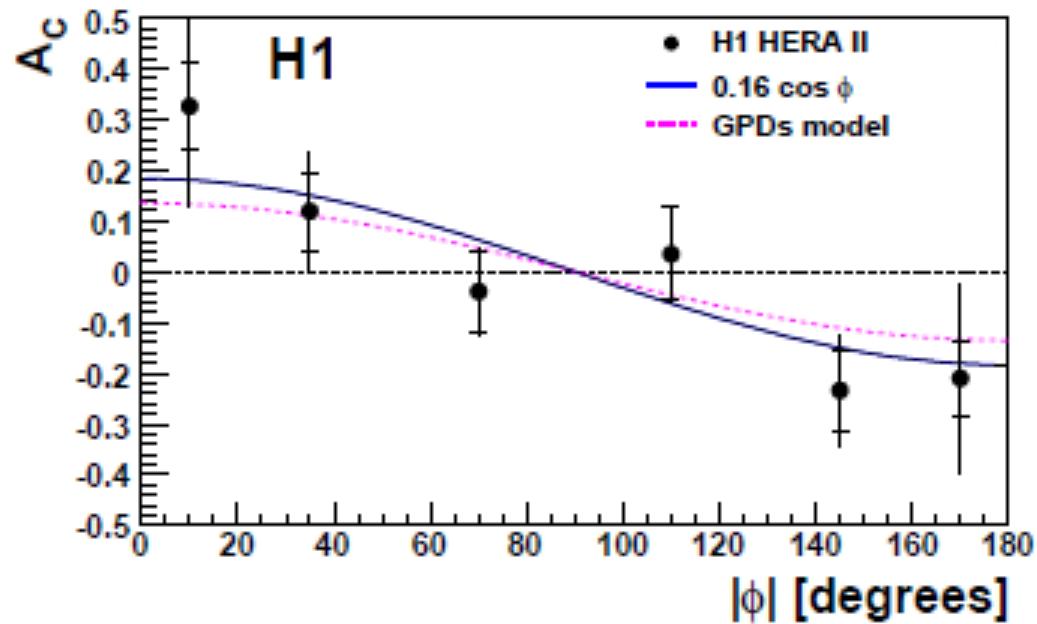
<http://arxiv.org/abs/1012.3776>

G. Goldstein, J. Hernandez and S. Liuti, Phys. Rev. D84 (2011)

# Beam Charge Asymmetry - H1

First measurement at a collider

- Low  $x_B = 10^{-4} - 10^{-2}$
- $65 < Q^2 < 80 \text{ GeV}^2$
- $30 < W < 140 \text{ GeV}$
- $|t| < 1 \text{ GeV}^2$



Positive  $\cos\phi$  amplitude  
Sign change compared to HERMES

$\Re \mathcal{H} > 0$  at H1

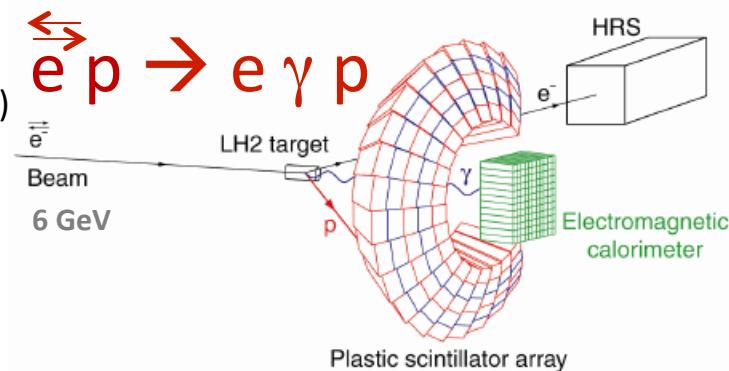
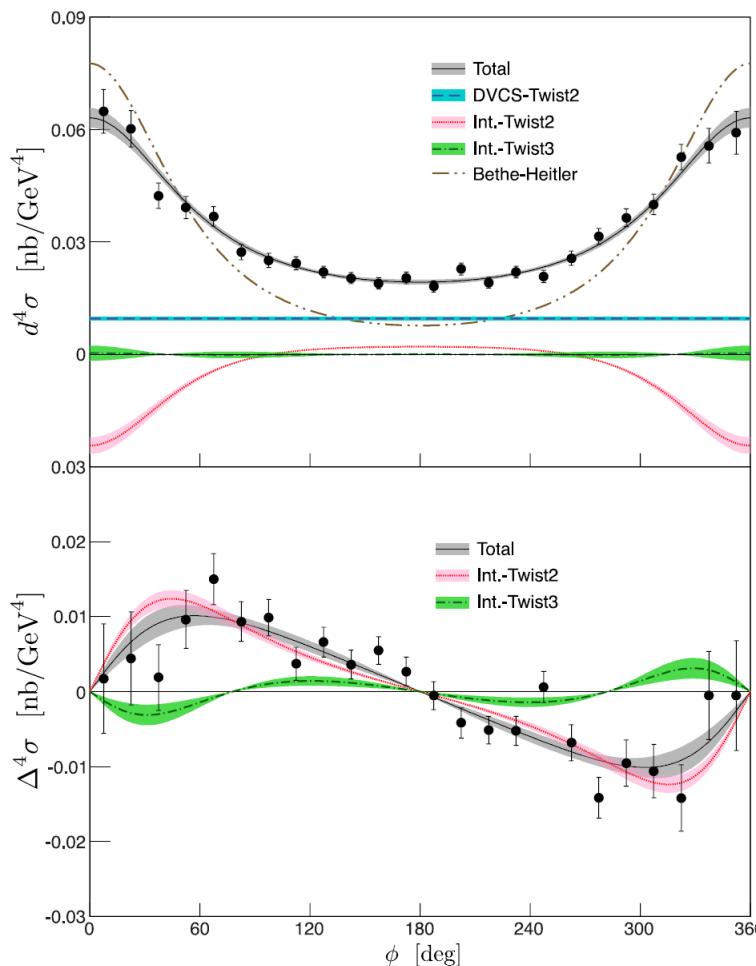
# Beam Spin Sum and Diff of DVCS - HallA

E00-110 pioneer experiment with magnetic spectrometer

$x_B = 0.36$ ,  $Q^2 = 1.5, 1.9, 2.3 \text{ GeV}^2$  Defurne et al. PRC92, 055202 (2015)

$x_B = 0.34, x_B = 0.39$ ,  $Q^2 = 2.1 \text{ GeV}^2$

$x_B = 0.36$ ,  $Q^2 = 2.3 \text{ GeV}^2$ ,  $-t = 0.32 \text{ GeV}^2$



## Unpolarized cross section

$$\begin{aligned} d\sigma^\leftarrow + d\sigma^\rightarrow &\propto d\sigma^{BH} + d\sigma_{unpol}^{DVCS} + \text{Re } I \\ &\rightarrow d\sigma^{BH} + c_0^{DVCS} + c_0^I + c_1^I \cos \phi + c_2^I \cos 2\phi \end{aligned}$$

Further separation  $\rightarrow$  need of different beam energies

## Helicity Dependent cross section

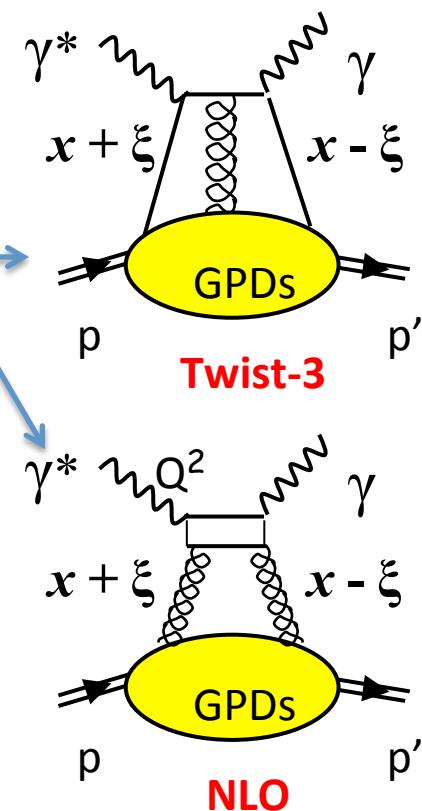
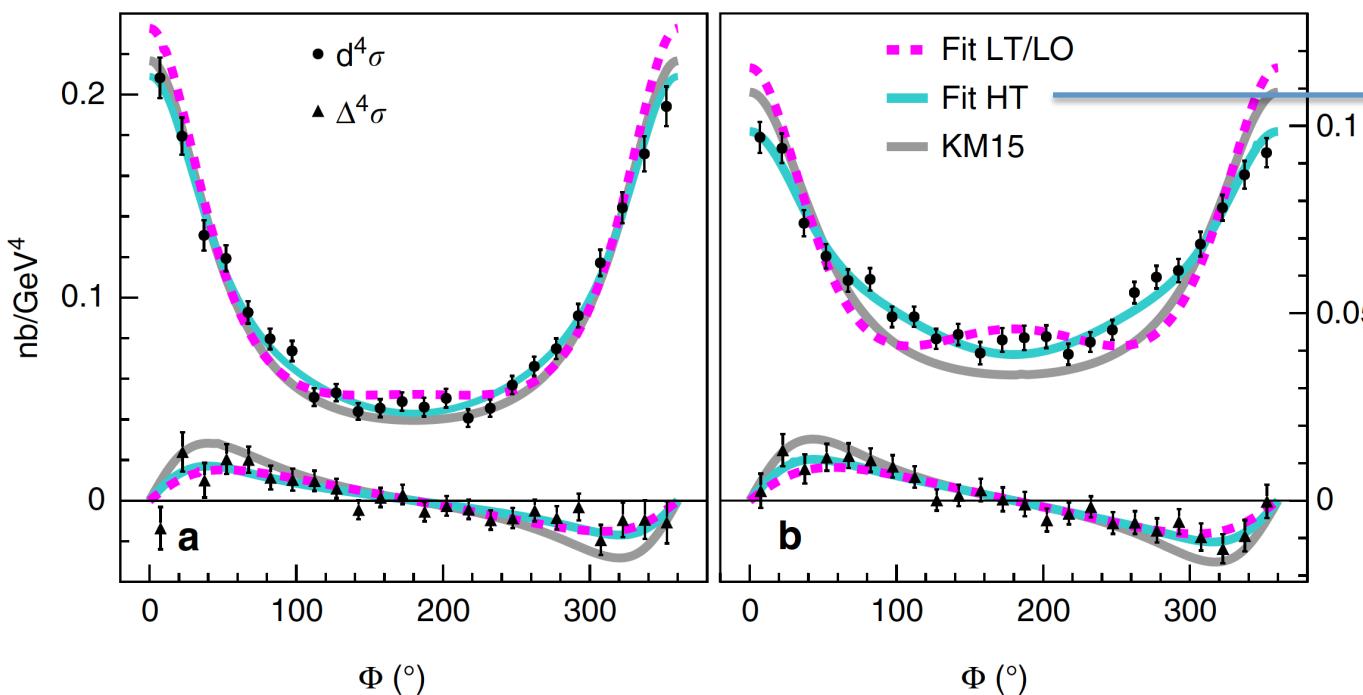
$$\begin{aligned} d\sigma^\leftarrow - d\sigma^\rightarrow &\propto d\sigma_{pol}^{DVCS} + \text{Im } I \\ &\rightarrow s_1^I \sin \phi + s_2^I \sin 2\phi \end{aligned}$$

# New high-precision Hall-A data

Hall-A experiment **E07-007** (2010) M. Defurne et al., Nat. Comm. 8 (2017) 1408

Fixed  $x_B = 0.36$ ,  $Q^2 = 1.5, 1.75, 2.0$

Two different beam energies  $\rightarrow$  BH-DVCS separation

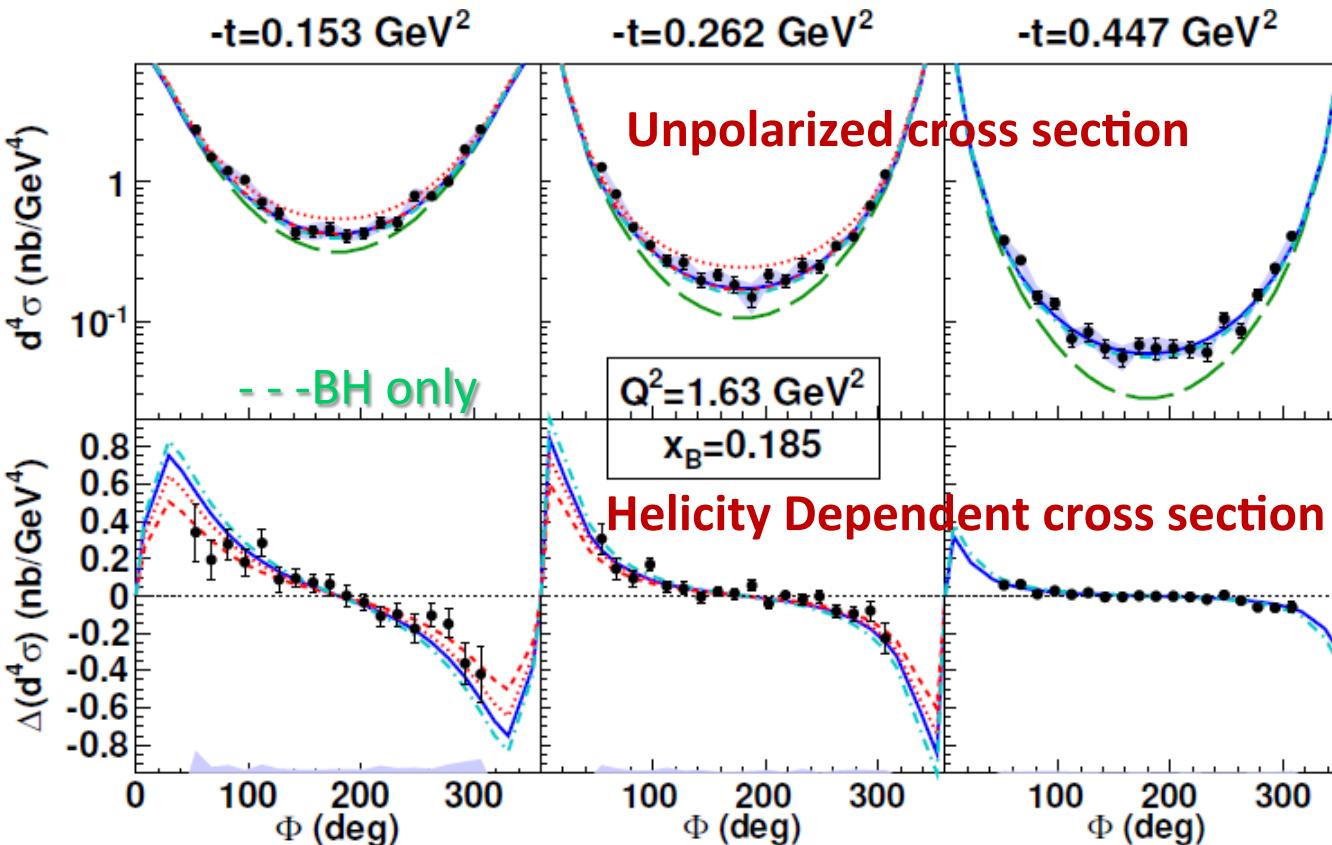
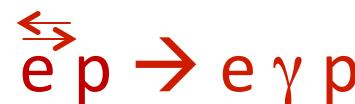


Either **NLO** or **twist-3** terms are needed to properly fit the Beam-helicity independent & dependent cross-sections

# Beam Spin Sum and Diff of DVCS - CLAS

21 bins in  $(x_B, Q^2)$  or 110 bins  $(x_B, Q^2 t)$

- Jo et al. PRL115, 212003 (2015)



**KM10a** - - - **KM10** ..... Kumericki, Mueller, NPB (2010) 841

Flexible parametrization of the GPDs based on both a Mellin-Barnes representation and dispersion integral which entangle skewness and  $t$  dependences

**Global fit** on the world data ranging from H1, ZEUS to HERMES, JLab

models:

**VGG** Vanderhaeghen, Guichon, Guidal  
PRL80(1998), PRD60(1999),  
PPNP47(2001), PRD72(2005)

1rst model of GPDs  
constant evolution

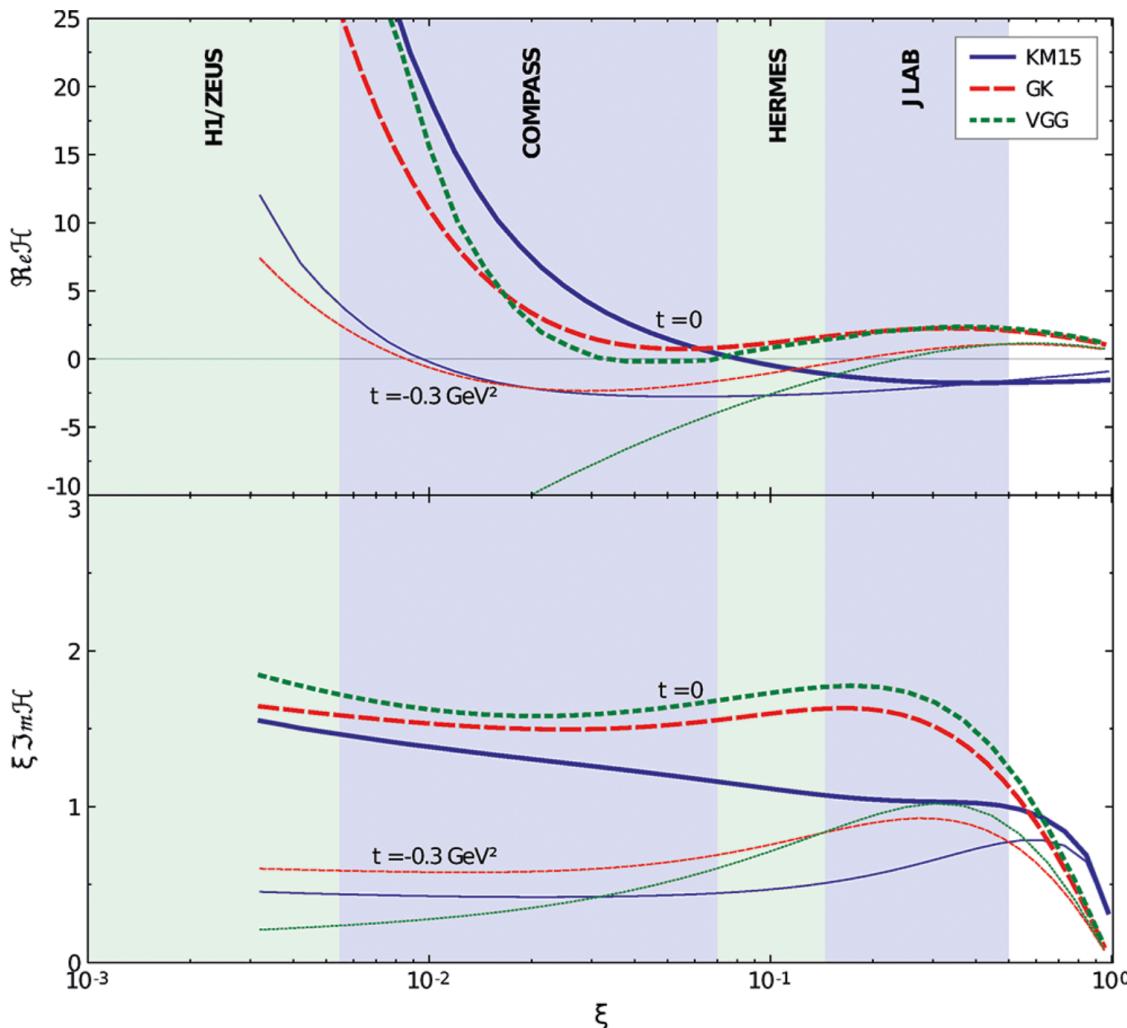
**KMS12** Kroll, Moutarde,  
Sabatié, EPJC73 (2013)

using the **GK** model  
Goloskokov, Kroll,  
EPJC42,50,53,59,65,74

for GPD adjusted on  
the hard exclusive  
meson production at  
small  $x_B$

"universality" of GPDs

# Summary of $Re\mathcal{H}$ and $Im\mathcal{H}$ from global analyses



$Re\mathcal{H}$   
Still poorly constrained

$Im\mathcal{H}$  Better known?

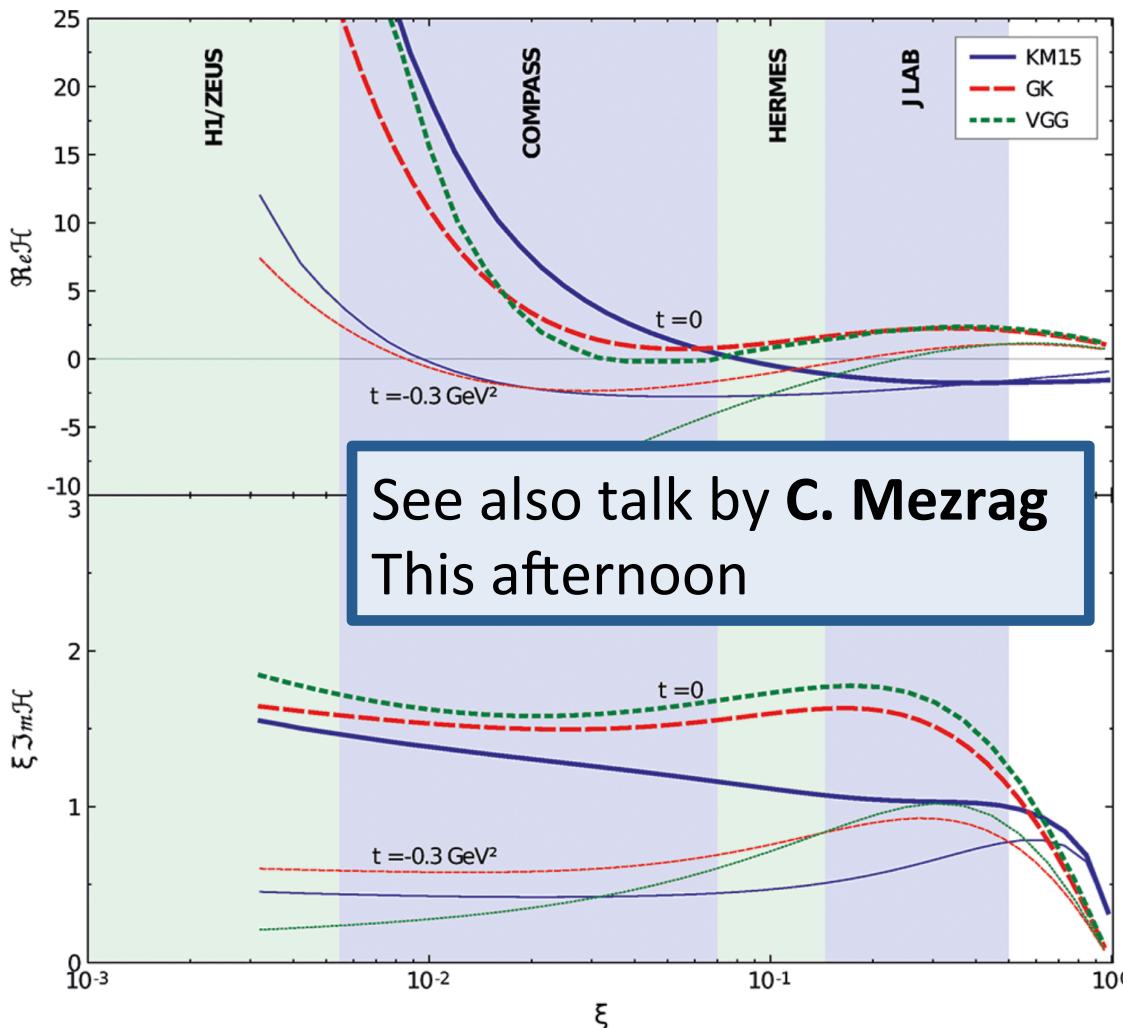
- FUTURE:**
- COMPASS:**  
fill gap at intermediate  $x$
  - JLab12:**  
extended kin. coverage  
increased precision
  - EIC:**  
“ultimate machine”?

**KM15** K Kumericki and D Mueller [arXiv:1512.09014v1](https://arxiv.org/abs/1512.09014v1)

**GK** S.V. Goloskokov, P. Kroll, EPJC53 (2008), EPJA47 (2011)

**VGG** M. Vanderhaeghen, P. A. M. Guichon, and M. Guidal, PRD60 (1999), PRD72(2005)

# Summary of $Re\mathcal{H}$ and $Im\mathcal{H}$ from global analyses



**KM15** K Kumericki and D Mueller [arXiv:1512.09014v1](https://arxiv.org/abs/1512.09014v1)

**GK** S.V. Goloskokov, P. Kroll, EPJC53 (2008), EPJA47 (2011)

**VGG** M. Vanderhaeghen, P. A. M. Guichon, and M. Guidal, PRD60 (1999), PRD72(2005)

$Re\mathcal{H}$   
Still poorly constrained

$Im\mathcal{H}$  Better known?

## FUTURE:

- COMPASS:**  
fill gap at intermediate  $x$
- JLab12:**  
extended kin. coverage  
increased precision
- EIC:**  
“ultimate machine”?

# COMPASS @ CERN – Data Taking in 2016/17

cross-sections on proton for  $\mu^{+\downarrow}, \mu^{-\uparrow}$  beam with opposite charge & spin ( $e_\mu$  &  $P_\mu$ )

$$d\sigma = d\sigma^{BH} + d\sigma_{unpol}^{DVCS} + P_\mu d\sigma_{pol}^{DVCS} + e_\mu a^{BH} \text{Re } A^{DVCS} + e_\mu P_\mu a^{BH} \text{Im } A^{DVCS}$$

$$d\sigma^{BH} \propto c_0^{BH} + c_1^{BH} \cos \phi + c_2^{BH} \cos 2\phi$$

$$d\sigma_{unpol}^{DVCS} \propto c_0^{DVCS} + c_1^{DVCS} \cos \phi + c_2^{DVCS} \cos 2\phi$$

$$d\sigma_{pol}^{DVCS} \propto s_1^{DVCS} \sin \phi$$

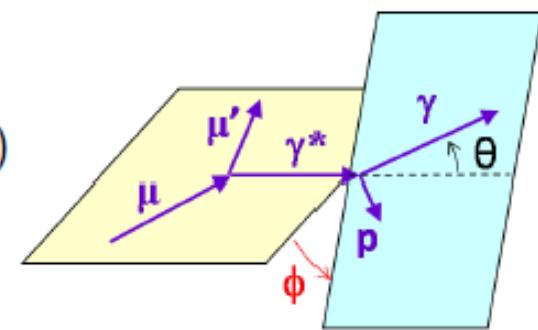
$$a^{BH} \text{Re } A^{DVCS} \propto c_0^I + c_1^I \cos \phi + c_2^I \cos 2\phi + c_3^I \cos 3\phi$$

$$a^{BH} \text{Im } A^{DVCS} \propto s_1^I \sin \phi + s_2^I \sin 2\phi$$

Twist-2  $>>$  (Twist-3, Twist-2 gluon)

$$\mathcal{D}_{cs,u} \equiv d\sigma(\mu^{+\downarrow}) - d\sigma(\mu^{-\uparrow}) \rightarrow \text{Re F1 H}$$

$$\mathcal{S}_{cs,u} \equiv d\sigma(\mu^{+\downarrow}) + d\sigma(\mu^{-\uparrow}) \rightarrow \text{Im F1 H}$$

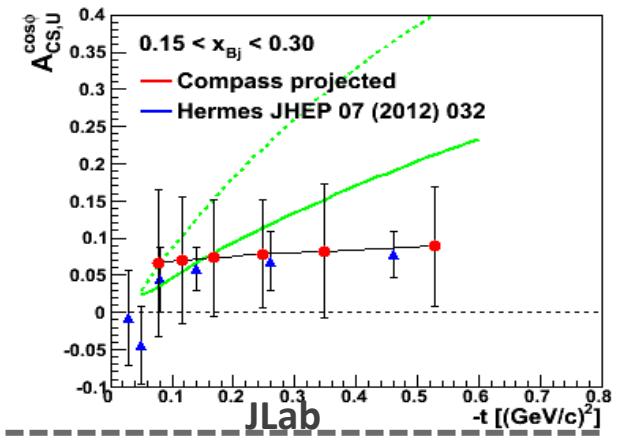
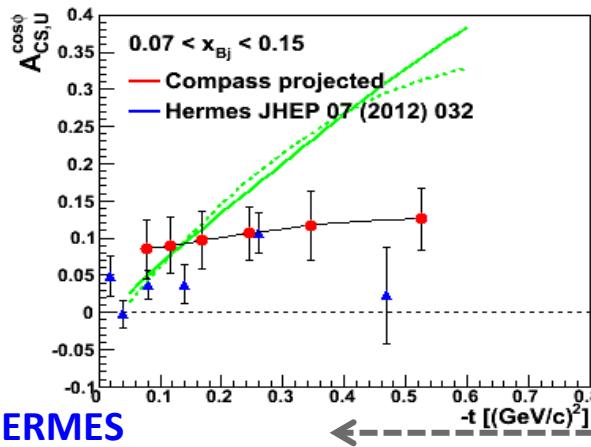
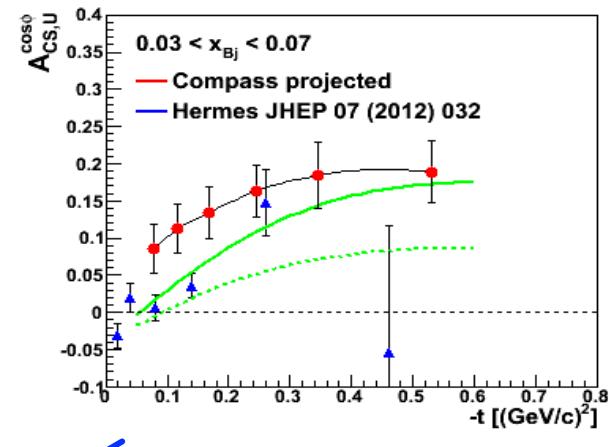
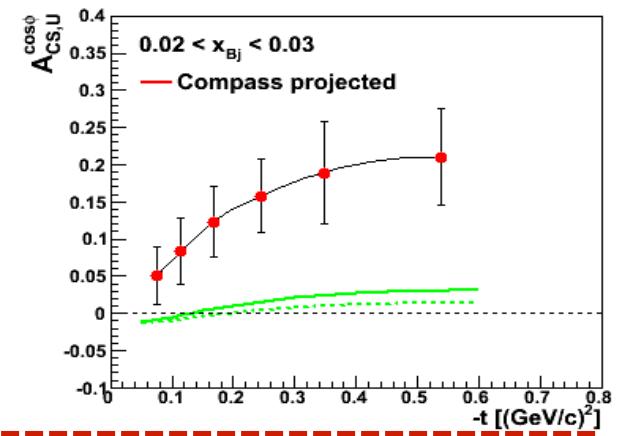
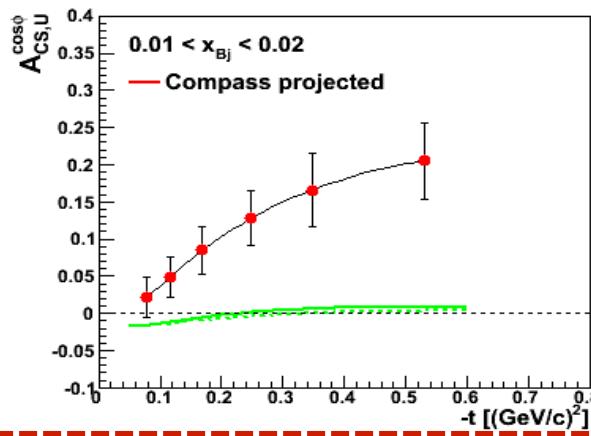
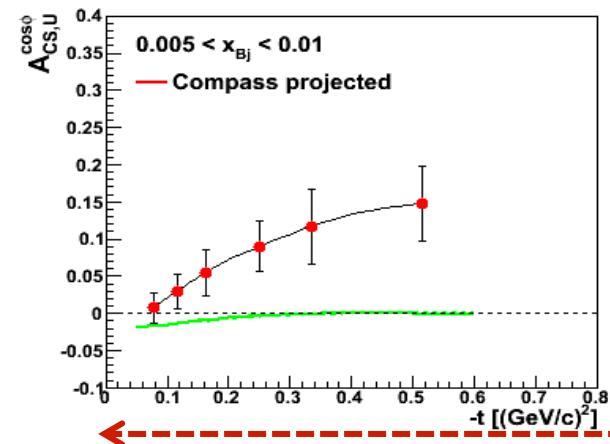


$$\mathcal{D}_{CS,U} = d\sigma(\mu^{\pm\downarrow}) - d\sigma(\mu^{\mp\uparrow}) \propto c_0^{Int} + c_1^{Int} \cos\varphi \quad \text{and} \quad c_{0,1}^{Int} \sim F_1 \Re \mathcal{H}$$

$A_{CS,U}^{\cos\phi}$  related to  $c_1^{Int}$

### Predictions with VGG and D.Mueller

$\Re \mathcal{H} > 0$  at H1  
 $< 0$  at HERMES/JLab  
 Value of  $x_B$  for the node?

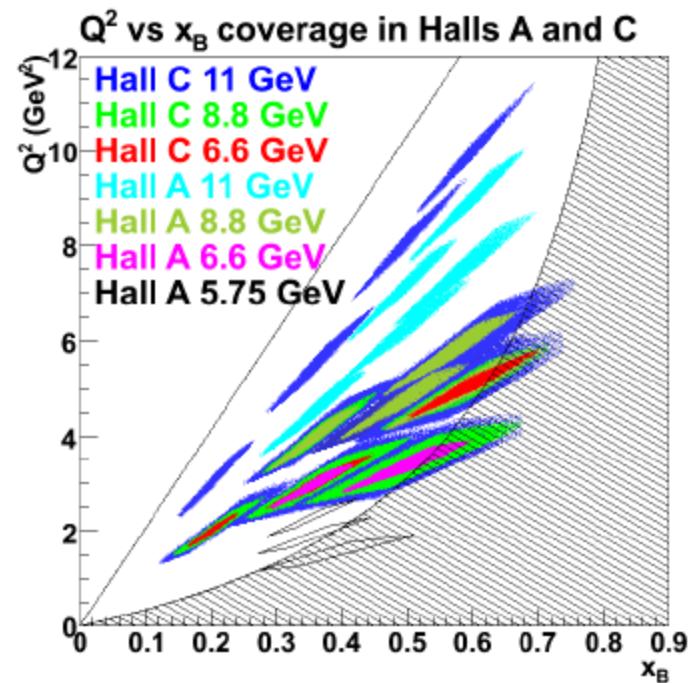
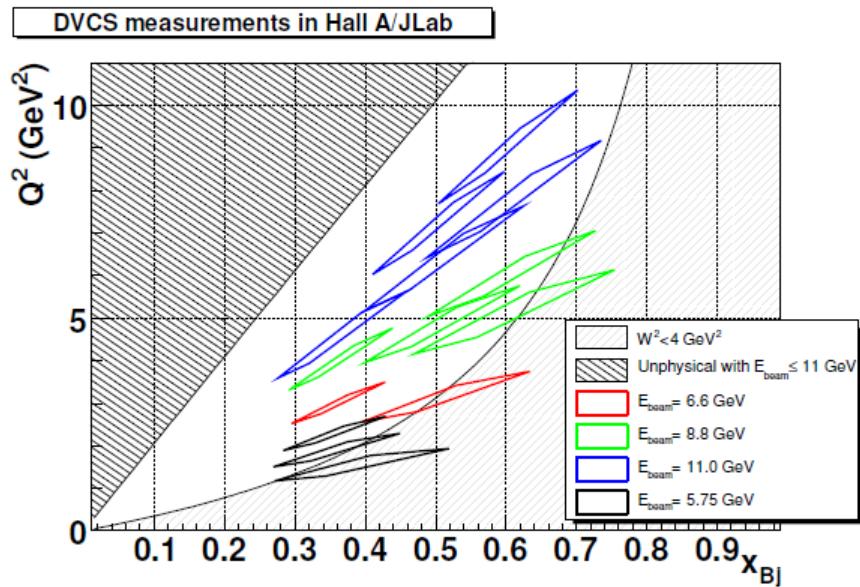


COMPASS 2 years of data  $E\mu = 160$  GeV  $1 < Q^2 < 8$  GeV $^2$  with ECAL2 + ECAL1 + ECAL0

# FUTURE: HALL-A & HALL-C @ Jlab12

with magnetic spectrometer + Calorimeter

JLab12 with 3, 4, 5 pass beam  
(6.6, 8.8, 11.0 GeV beam energy)



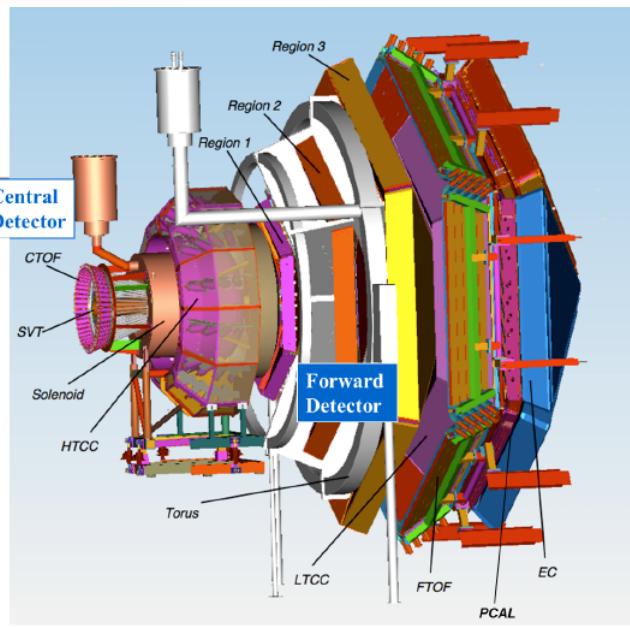
- Absolute cross-section measurements
- Test of scaling:  $Q^2$  dependence of  $d\sigma$  at fixed  $x_{Bj}$
- Increased kinematical coverage

- Energy separation of the DVCS cross section
- Higher  $Q^2$ : measurement of higher twist contributions
- Low- $x_B$  extension (thanks to sweeping magnet)

First run after the 12GeV upgrade  
Now 2014

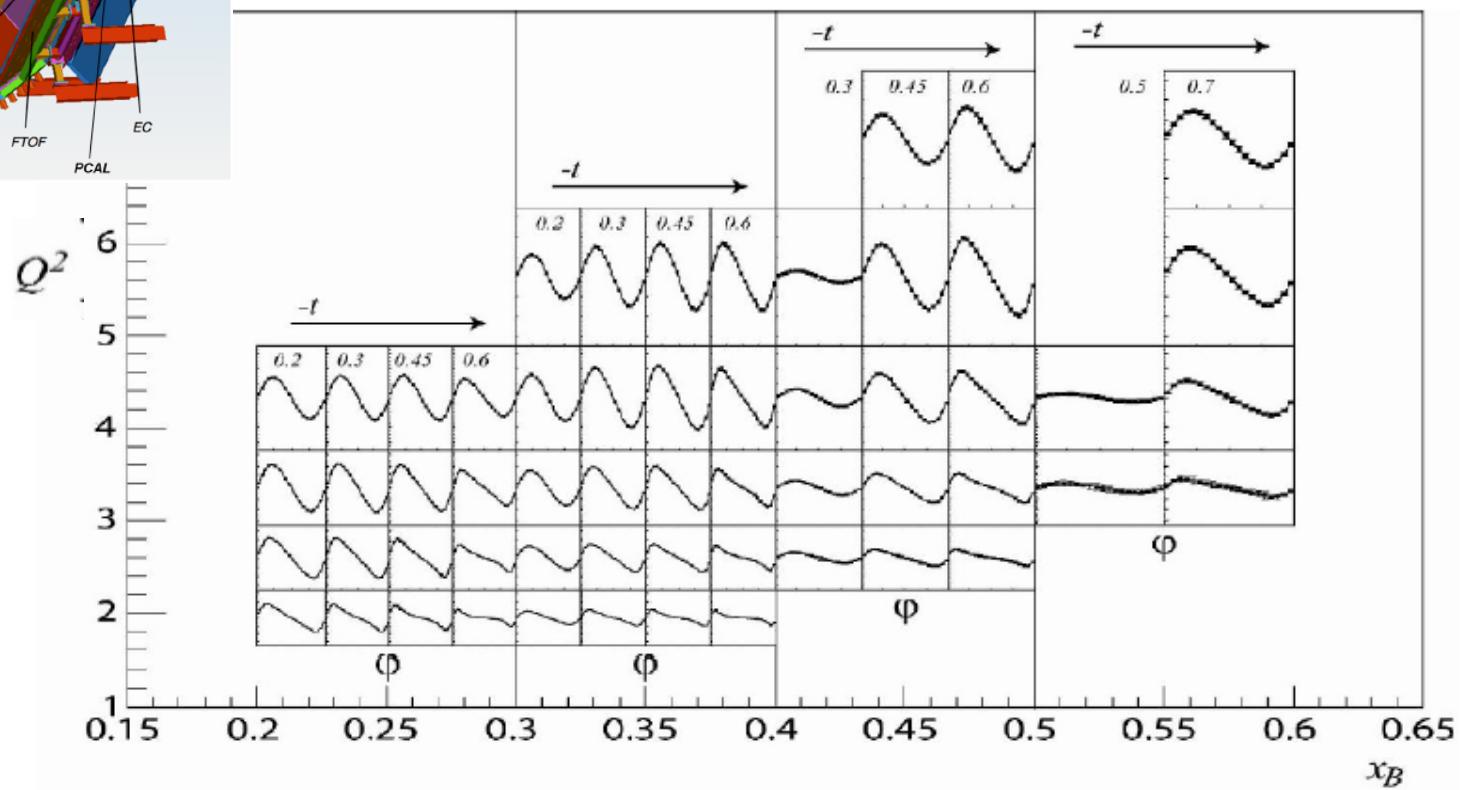
Need a new challenging Calo  
~ 2018

# FUTURE: CLAS12 @ Jlab



Approved experiment E12-06-119

LH<sub>2</sub> Target and Long. Pol. Target  
Extended ( $Q^2, x_B$ ) coverage  
Planned for 201?

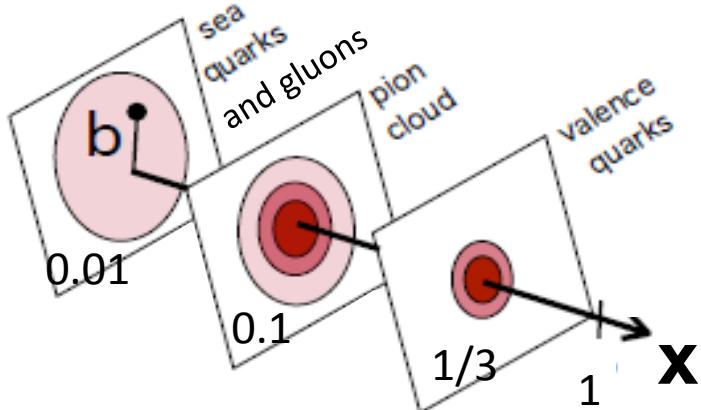


# Nucleon « tomography »

- t-slope of DVCS x-section
- Global fits of DVCS **CFFs**

# Nucleon « tomography »

x-dependent spatial distribution of partons in the transverse plane



$$\langle b_\perp^2(x) \rangle^f = -4 \frac{\partial}{\partial t} \ln H^f(x, 0, t) \Big|_{t=0}$$

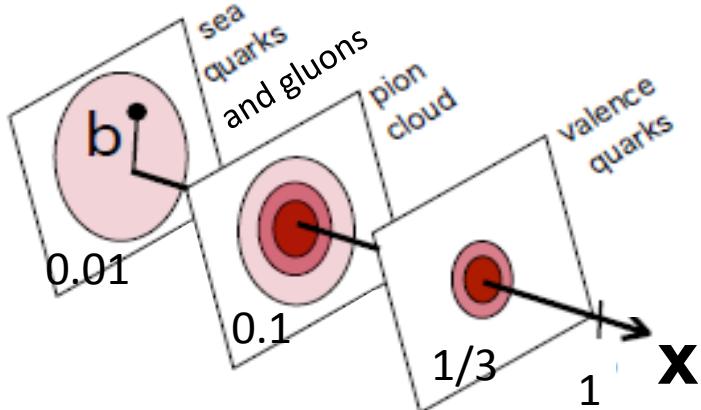
$$H(x, 0, t) \propto e^{-B_0(x)/t}$$



$$\langle b_\perp^2(x) \rangle = 4B_0(x)$$

# Nucleon « tomography »

x-dependent spatial distribution of partons in the transverse plane



$$\langle b_\perp^2(x) \rangle^f = -4 \frac{\partial}{\partial t} \ln H^f(x, 0, t) \Big|_{t=0}$$

$$H(x, 0, t) \propto e^{-B_0(x)/t}$$



$$\langle b_\perp^2(x) \rangle = 4B_0(x)$$

**Unpol. DVCS x-section** mostly sensitive to

$$Im \mathcal{H}(\xi, t) \propto H(x=\xi, \xi, t)$$

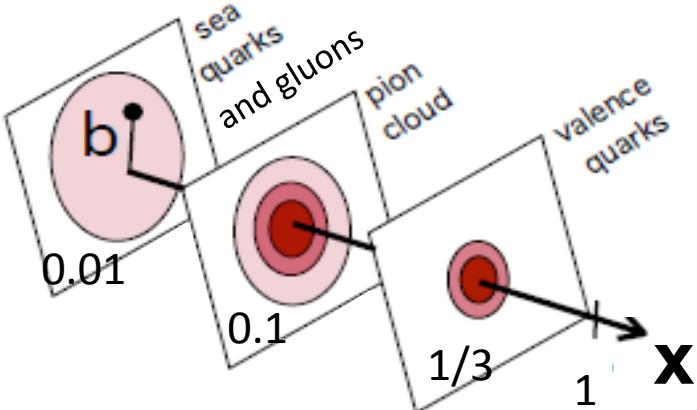
$$H(x=\xi, \xi, t) \propto e^{-B(\xi)/t}$$



$$\langle r_\perp^2(\xi) \rangle = 4B(\xi)$$

# Nucleon « tomography »

x-dependent spatial distribution of partons in the transverse plane



$$\langle b_\perp^2(x) \rangle^f = -4 \frac{\partial}{\partial t} \ln H^f(x, 0, t) \Big|_{t=0}$$

**Unpol. DVCS x-section** mostly sensitive to

$$Im \mathcal{H}(\xi, t) \propto H(x=\xi, \xi, t)$$

$$H(x, 0, t) \propto e^{-B_0(x)/t}$$



$$\langle b_\perp^2(x) \rangle = 4B_0(x)$$

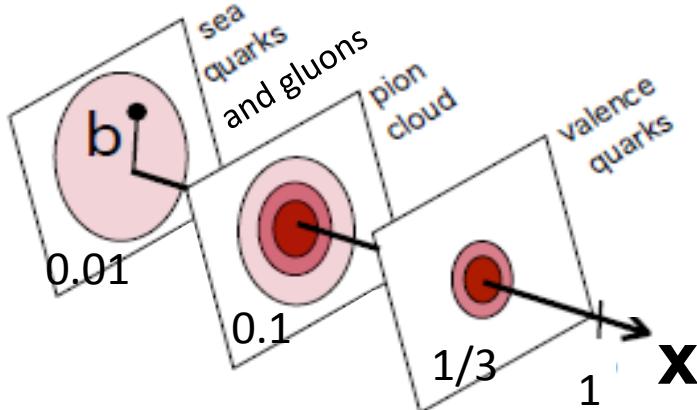
model dependent

$$H(x=\xi, \xi, t) \propto e^{-B(\xi)/t}$$



$$\langle r_\perp^2(\xi) \rangle = 4B(\xi)$$

# Nucleon « tomography »



x-dependent spatial distribution of partons in the transverse plane

$$\langle b_\perp^2(x) \rangle^f = -4 \frac{\partial}{\partial t} \ln H^f(x, 0, t) \Big|_{t=0}$$

$$H(x, 0, t) \propto e^{-B_0(x)/t}$$



$$\langle b_\perp^2(x) \rangle = 4B_0(x)$$

**Unpol. DVCS x-section** mostly sensitive to

$$Im \mathcal{H}(\xi, t) \propto H(x=\xi, \xi, t)$$

model dependent

$$H(x=\xi, \xi, t) \propto e^{-B(\xi)/t}$$



$$\langle r_\perp^2(\xi) \rangle = 4B(\xi)$$

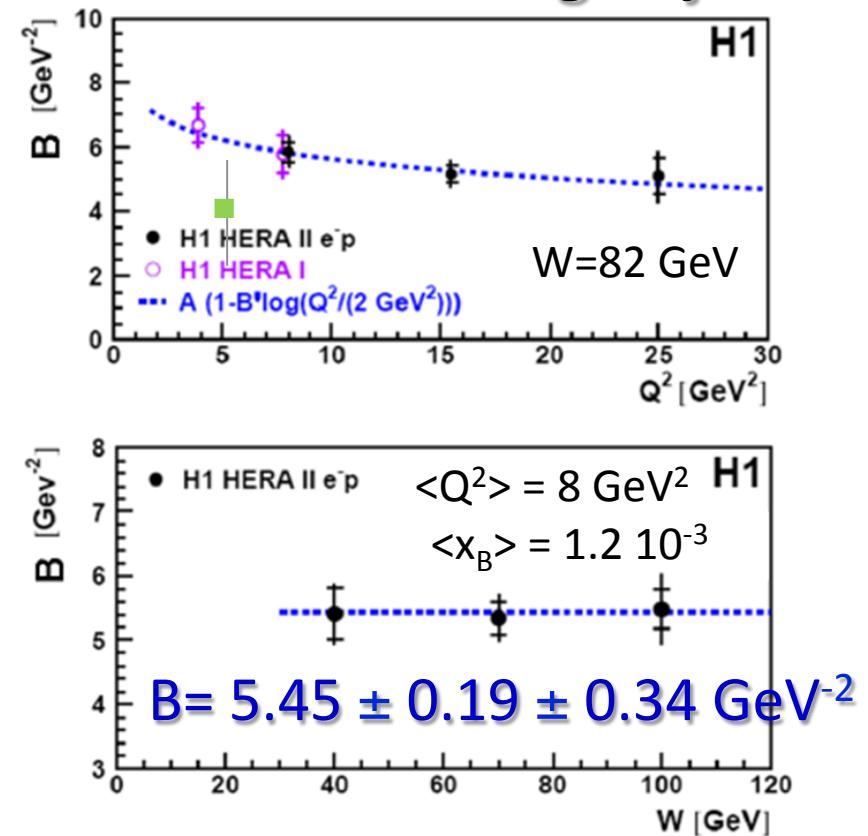
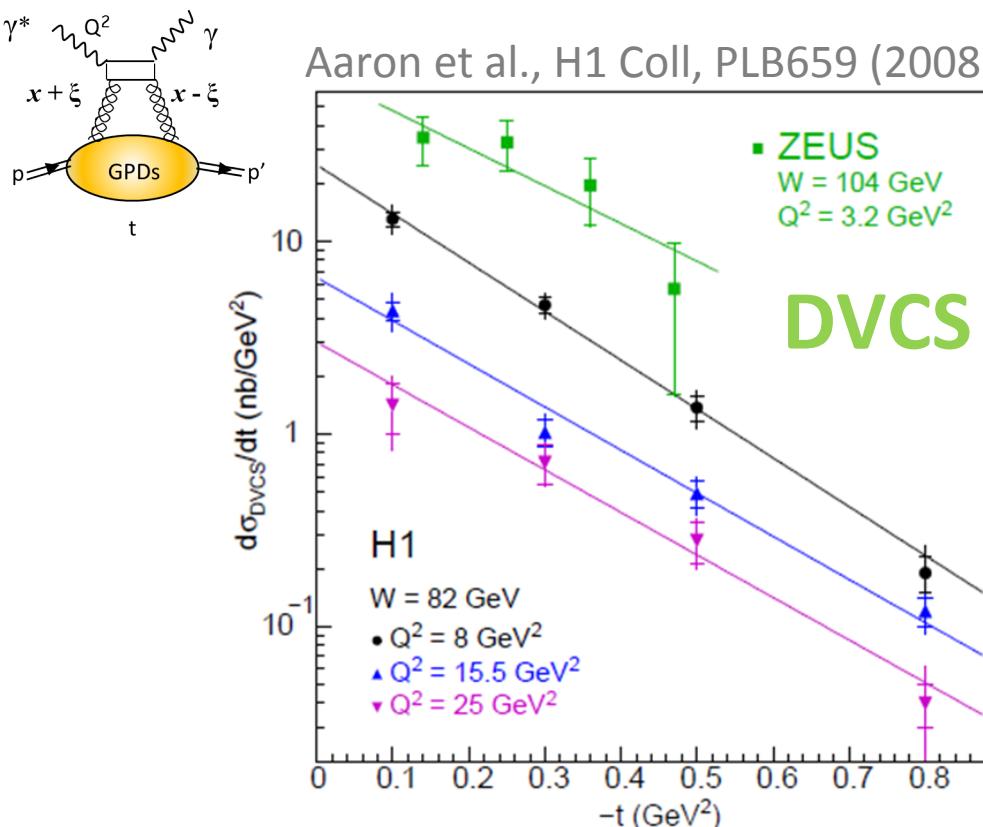
$$d\sigma_{DVCS}/dt \propto e^{-B'(x_B)/t} \rightarrow \langle r_\perp^2(x_B) \rangle \approx 2B'(x_B)$$

$$\xi \approx x_B/2$$

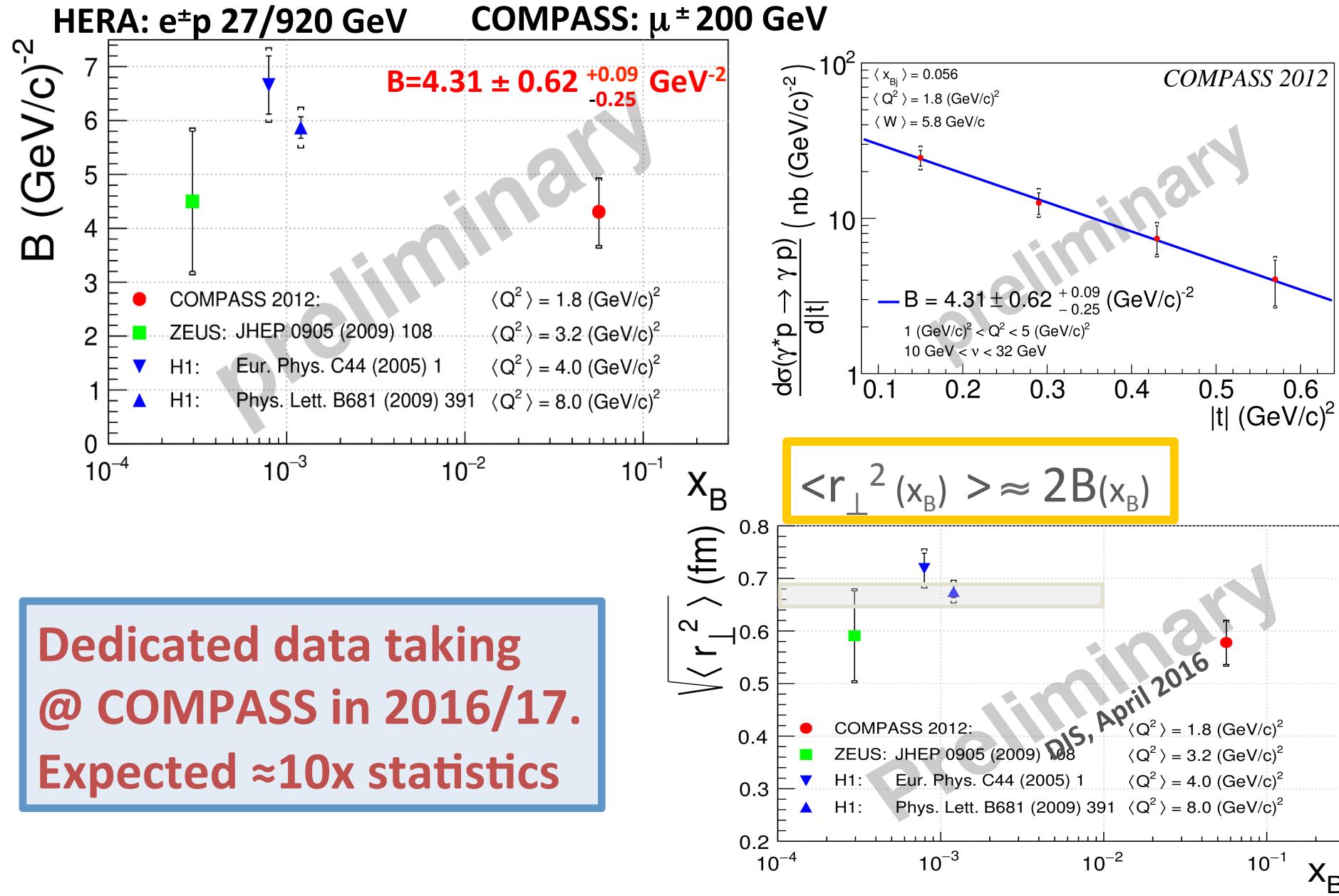
# Gluon imaging @ HERA

$$d\sigma^{\text{DVCS}}/dt = e^{-B|t|}$$

B is related to the transversed size of the scattering objects



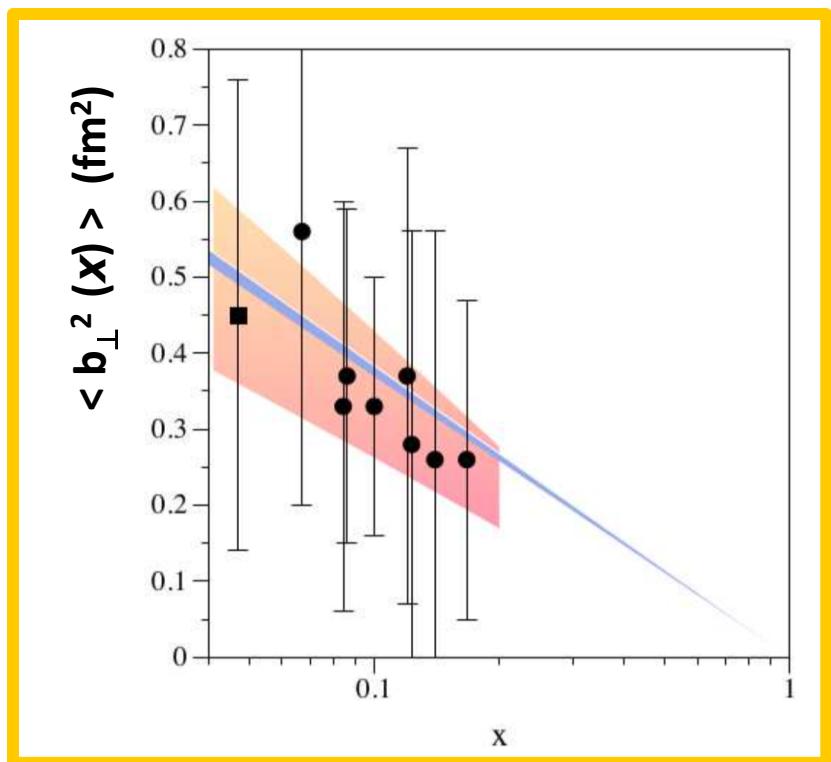
# Sea quark imaging @ COMPASS



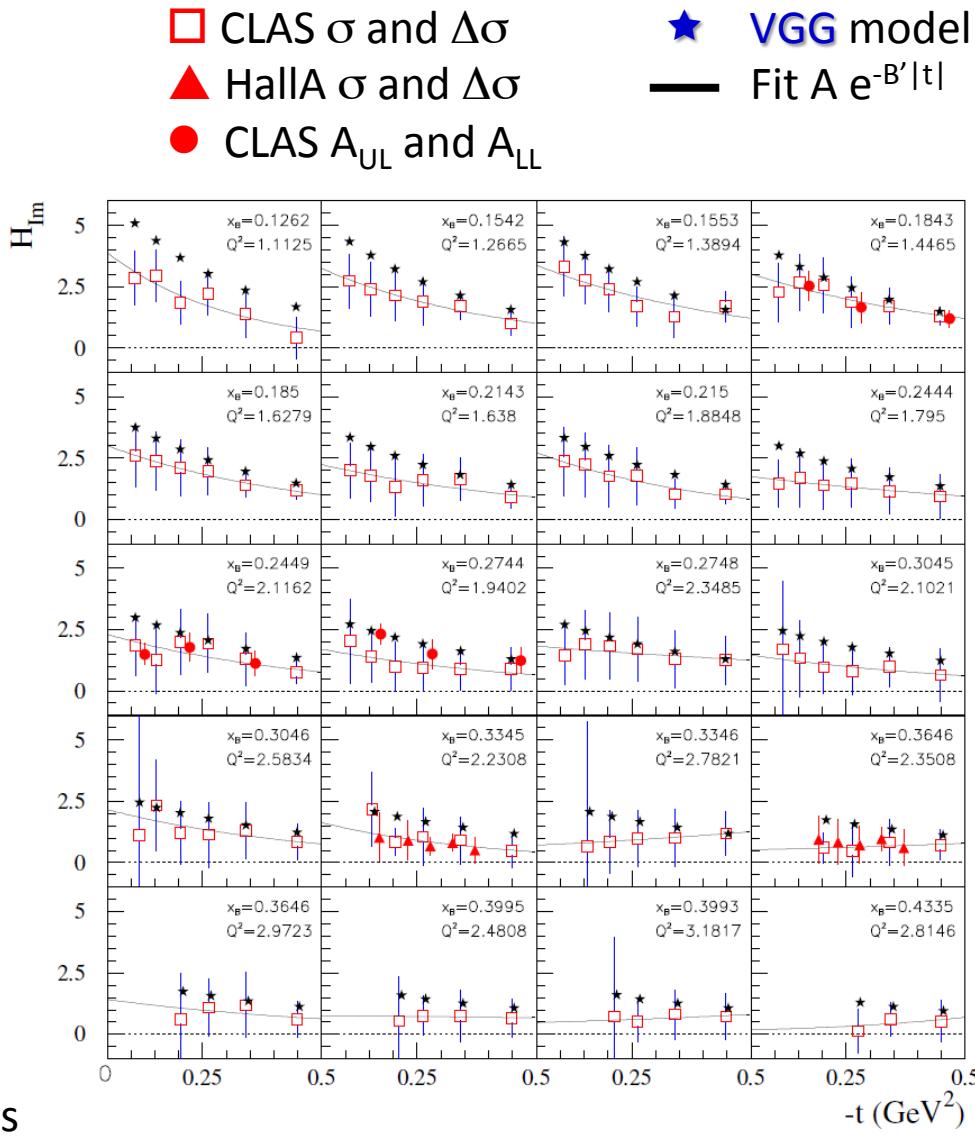
# Valence quark imaging at Jlab

Fit of 8 CFFs at L.O and L.T.

Dupré, Guidal, Niccolai, Vanderhaeghen  
 Eur.Phys.J. A53 (2017) no.8, 171



Error bars dominated by model uncertainties  
 In the fitting procedure



# Exclusive $\pi^0$ production and chiral-odd GPDs

- $\pi^0$  cross-sections – CLASS & COMPASS
- Rosembuth separation – HALL A

# Excl. $\pi^0$ and the chiral-odd $H_T$ and $E_T$ – Jlab CLAS

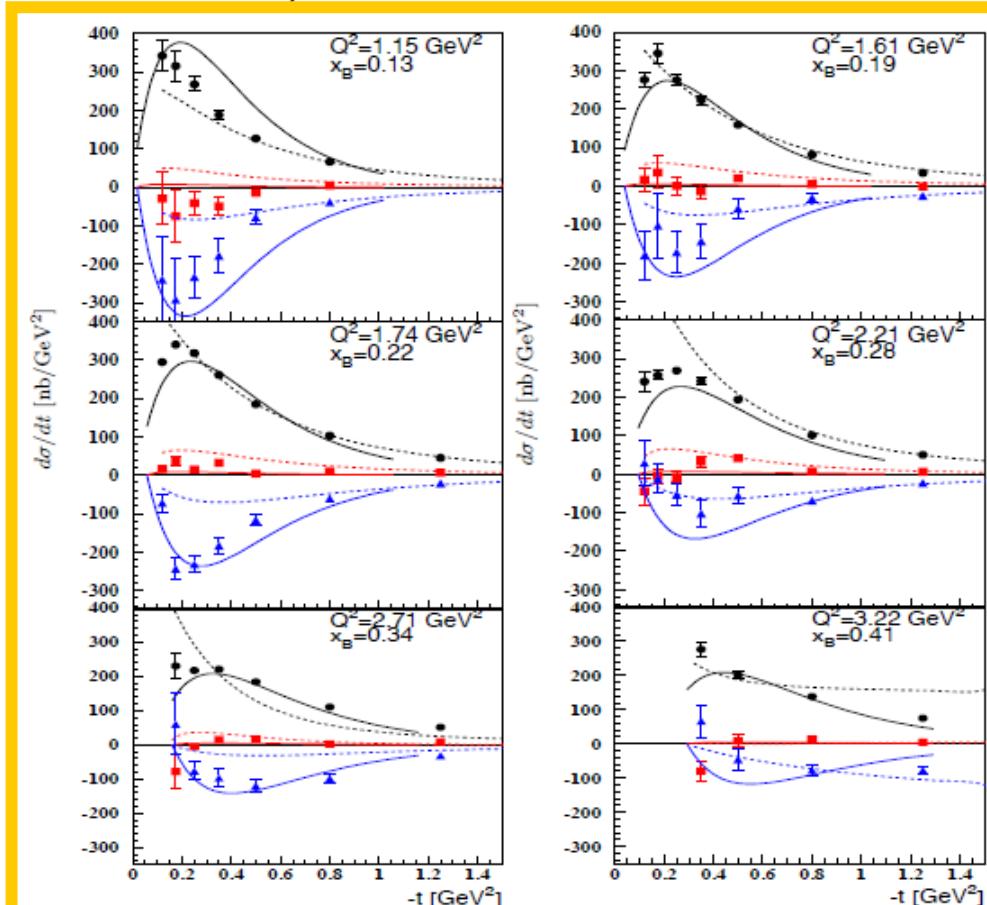
$$e p \rightarrow e \pi^0 p \quad \frac{d^2\sigma}{dt d\phi_\pi} = \frac{1}{2\pi} \left[ \left( \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right) + \epsilon \cos 2\phi_\pi \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi_\pi \frac{d\sigma_{LT}}{dt} \right]$$

$$\frac{d\sigma_L}{dt} = \frac{4\pi\alpha}{k'} \frac{1}{Q^6} \left\{ (1-\xi^2) |\langle \tilde{H} \rangle|^2 - 2\xi^2 \text{Re} [\langle \tilde{H} \rangle^* \langle \tilde{E} \rangle] - \frac{t'}{4m^2} \xi^2 |\langle \tilde{E} \rangle|^2 \right\} \approx \text{only a few \% of } \frac{d\sigma_T}{dt}$$

$$\frac{d\sigma_T}{dt} = \frac{4\pi\alpha}{2k'} \frac{\mu_\pi^2}{Q^8} \left[ (1-\xi^2) |\langle H_T \rangle|^2 - \frac{t'}{8m^2} |\langle \bar{E}_T \rangle|^2 \right]$$

- $\frac{d\sigma_{LT}}{dt} = \frac{4\pi\alpha}{\sqrt{2}k'} \frac{\mu_\pi}{Q^7} \xi \sqrt{1-\xi^2} \frac{\sqrt{-t'}}{2m} \text{Re} [\langle H_T \rangle^* \langle \tilde{E} \rangle]$

- $\frac{d\sigma_{TT}}{dt} = \frac{4\pi\alpha}{k'} \frac{\mu_\pi^2}{Q^8} \frac{t'}{16m^2} |\langle \bar{E}_T \rangle|^2$



Large impact of  $\overline{E}_T$   
clearly visible in  $\sigma_{TT}$   
and in the dip at small  $t$  of  $\sigma_T$

solid lines : **GK** EPJA47 (2011)

Dotted lines: **GHL** JPG:NPP39 (2012)

# Excl. $\pi^0$ and the chiral-odd $H_T$ and $E_T$ – Jlab CLAS

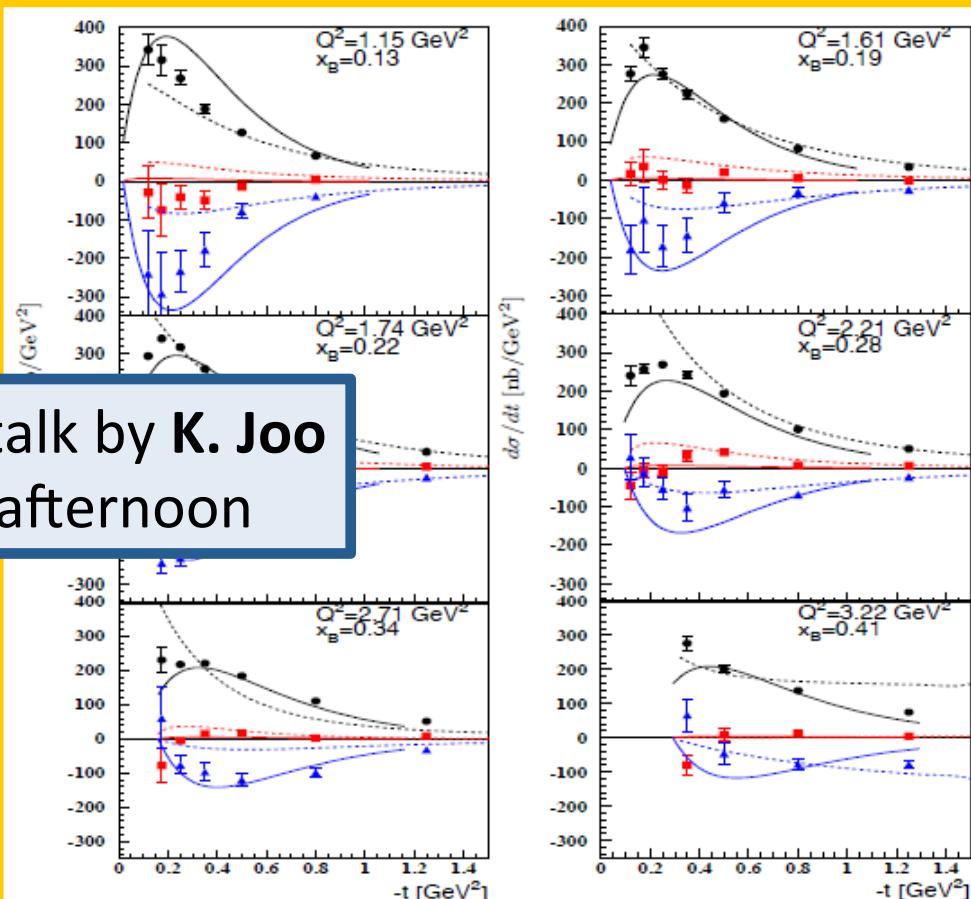
$$e p \rightarrow e \pi^0 p \quad \frac{d^2\sigma}{dt d\phi_\pi} = \frac{1}{2\pi} \left[ \left( \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right) + \epsilon \cos 2\phi_\pi \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi_\pi \frac{d\sigma_{LT}}{dt} \right]$$

$$\frac{d\sigma_L}{dt} = \frac{4\pi\alpha}{k'} \frac{1}{Q^6} \left\{ (1-\xi^2) |\langle \tilde{H} \rangle|^2 - 2\xi^2 \text{Re} [\langle \tilde{H} \rangle^* \langle \tilde{E} \rangle] - \frac{t'}{4m^2} \xi^2 |\langle \tilde{E} \rangle|^2 \right\} \approx \text{only a few \% of } \frac{d\sigma_T}{dt}$$

$$\frac{d\sigma_T}{dt} = \frac{4\pi\alpha}{2k'} \frac{\mu_\pi^2}{Q^8} \left[ (1-\xi^2) |\langle H_T \rangle|^2 - \frac{t'}{8m^2} |\langle \bar{E}_T \rangle|^2 \right]$$

- $\frac{d\sigma_{LT}}{dt} = \frac{4\pi\alpha}{\sqrt{2}k'} \frac{\mu_\pi}{Q^7} \xi \sqrt{1-\xi^2} \frac{\sqrt{-t'}}{2m} \text{Re} [\langle H_T \rangle^* \langle \tilde{E} \rangle]$

- $\frac{d\sigma_{TT}}{dt} = \frac{4\pi\alpha}{k'} \frac{\mu_\pi^2}{Q^8} \frac{t'}{16m^2} |\langle \bar{E}_T \rangle|^2$



Large impact of  $\bar{E}_T$   
 clearly visible in  $\sigma_{TT}$   
 and in the dip at small  $t$  of  $\sigma_T$

solid lines : **GK** EPJA47 (2011)

Dotted lines: **GHL** JPG:NPP39 (2012)

CLAS Coll, Bedlinskiy et al., PRC90(2014)2-025205

# Excl. $\pi^0$ and the chiral-odd $H_T$ and $E_T$ – Jlab HALL-A

$$e p \rightarrow e \pi^0 p \quad \frac{d^2\sigma}{dt d\phi_\pi} = \frac{1}{2\pi} \left[ \left( \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right) + \epsilon \cos 2\phi_\pi \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi_\pi \frac{d\sigma_{LT}}{dt} \right]$$

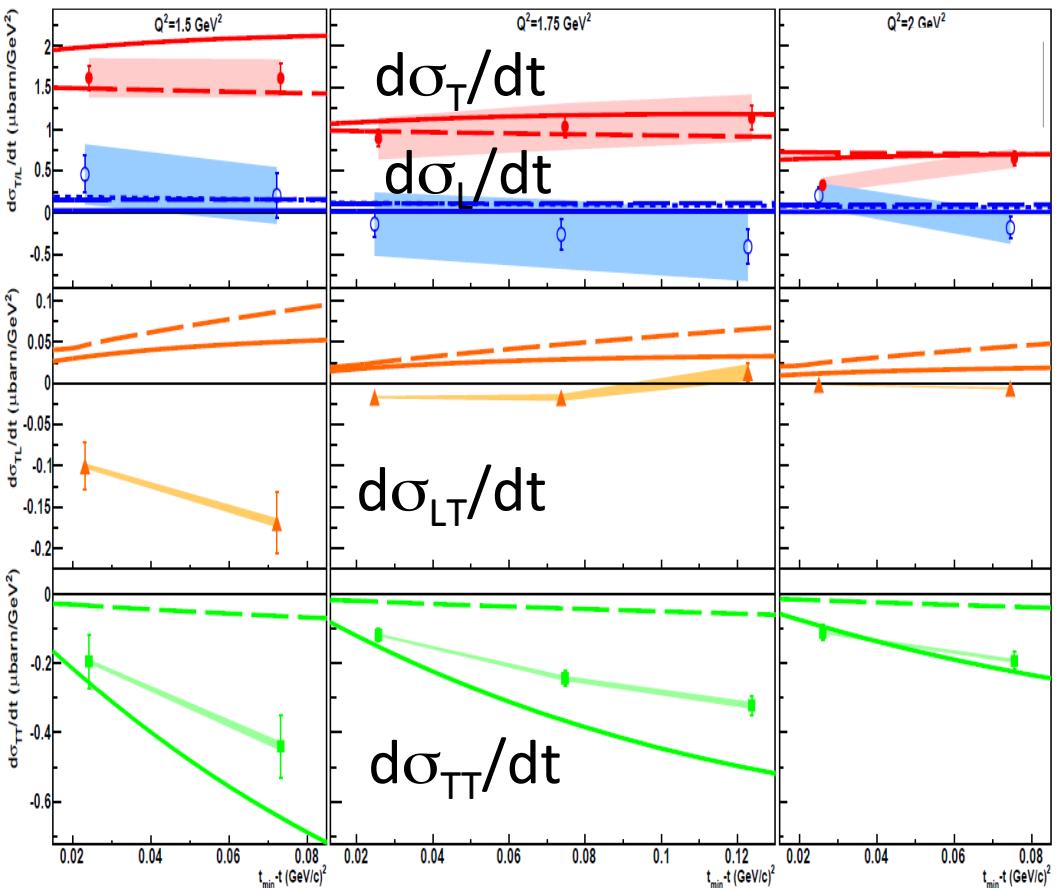
$$\frac{d\sigma_L}{dt} = \frac{4\pi\alpha}{k' Q^6} \frac{1}{Q^6} \left\{ (1 - \xi^2) |\langle \tilde{H} \rangle|^2 - 2\xi^2 \text{Re} [\langle \tilde{H} \rangle^* \langle \tilde{E} \rangle] - \frac{t'}{4m^2} \xi^2 |\langle \tilde{E} \rangle|^2 \right\} \ll \frac{d\sigma_T}{dt}$$

**Confirmation -HallA**

$$\frac{d\sigma_T}{dt} = \frac{4\pi\alpha}{2k' Q^8} \mu_\pi^2 \left[ (1 - \xi^2) |\langle H_T \rangle|^2 - \frac{t'}{8m^2} |\langle \bar{E}_T \rangle|^2 \right]$$

$$\frac{d\sigma_{LT}}{dt} = \frac{4\pi\alpha}{\sqrt{2}k' Q^7} \mu_\pi \xi \sqrt{1 - \xi^2} \frac{\sqrt{-t'}}{2m} \text{Re} [\langle H_T \rangle^* \langle \tilde{E} \rangle]$$

$$\frac{d\sigma_{TT}}{dt} = \frac{4\pi\alpha}{k' Q^8} \frac{\mu_\pi^2}{16m^2} \frac{t'}{16m^2} |\langle \bar{E}_T \rangle|^2$$



Hall A:  $\sigma L$  and  $\sigma T$  separation

Defurne et al. ArXiv:1608.01003

solid lines : **GK** EPJA47 (2011)

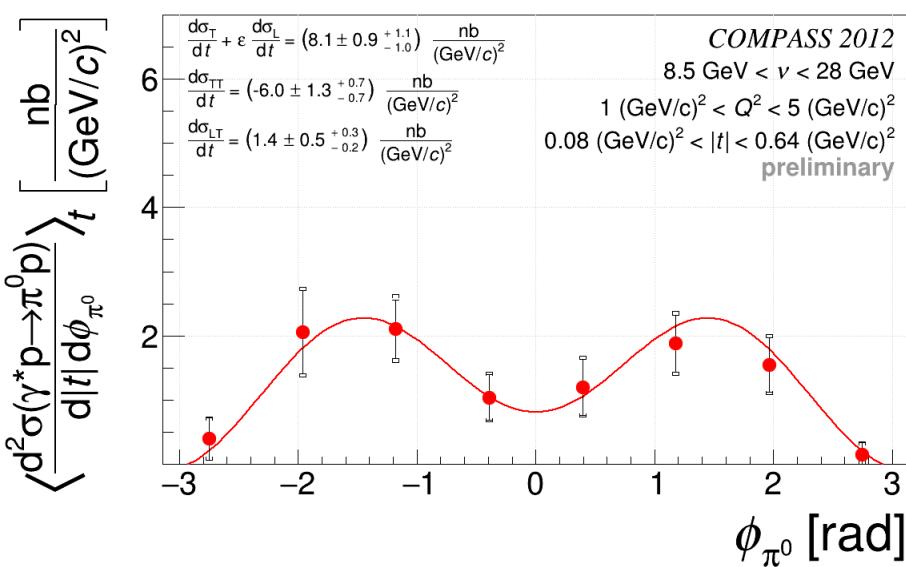
Dashed lines: **GHL** JPG:NPP39 (2012)

# Excl. $\pi^0$ and the chiral-odd $H_T$ and $E_T$ - COMPASS

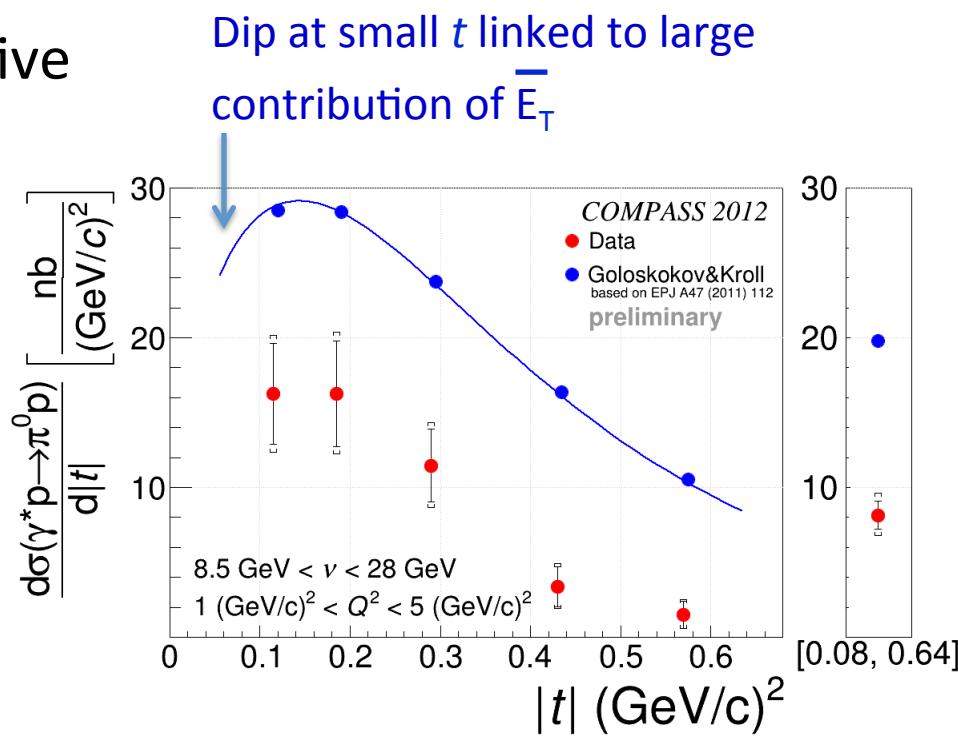
$$e p \rightarrow e \pi^0 p \quad \frac{d^2\sigma}{dt d\phi_\pi} = \frac{1}{2\pi} \left[ \left( \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right) + \epsilon \cos 2\phi_\pi \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi_\pi \frac{d\sigma_{LT}}{dt} \right]$$

$\frac{\sigma_{TT}}{dt} = -6.0 \pm 1.3 \rightarrow$  sizeable and negative, same trend as JLab

$\frac{\sigma_{LT}}{dt} = 1.4 \pm 0.5 \rightarrow$  small but positive



solid lines : GK EPJA47 (2011)



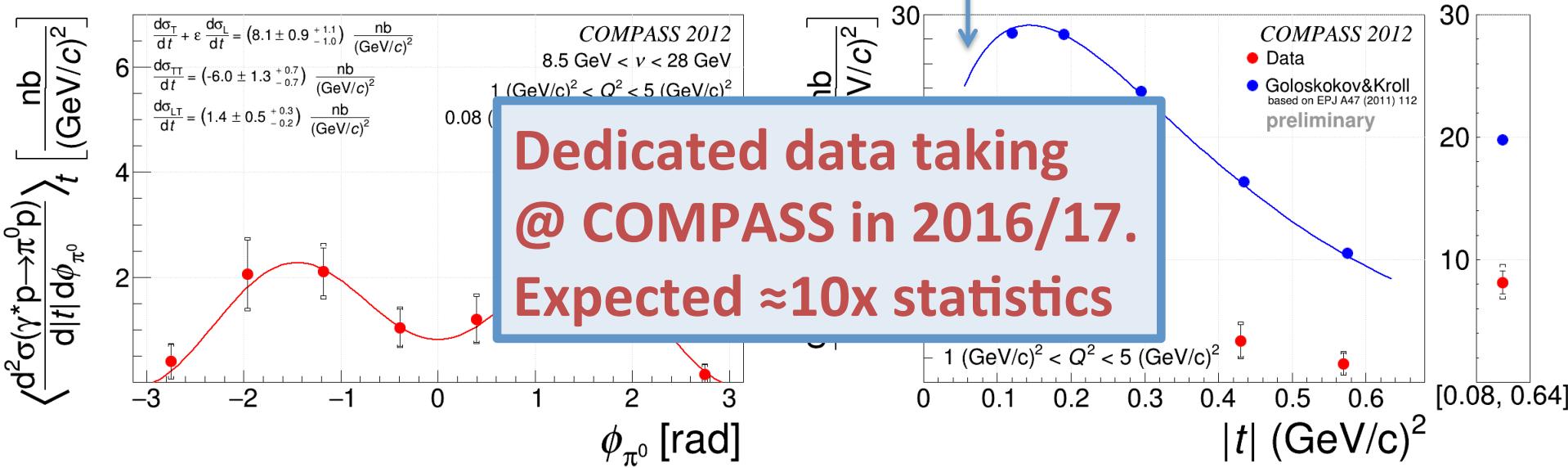
# Excl. $\pi^0$ and the chiral-odd $H_T$ and $E_T$ - COMPASS

$$e p \rightarrow e \pi^0 p \quad \frac{d^2\sigma}{dt d\phi_\pi} = \frac{1}{2\pi} \left[ \left( \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right) + \epsilon \cos 2\phi_\pi \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi_\pi \frac{d\sigma_{LT}}{dt} \right]$$

$\frac{\sigma_{TT}}{dt} = -6.0 \pm 1.3$  -> sizeable and negative, same trend as JLab

$\frac{\sigma_{LT}}{dt} = 1.4 \pm 0.5$  -> small but positive

Dip at small  $t$  linked to large contribution of  $\bar{E}_T$

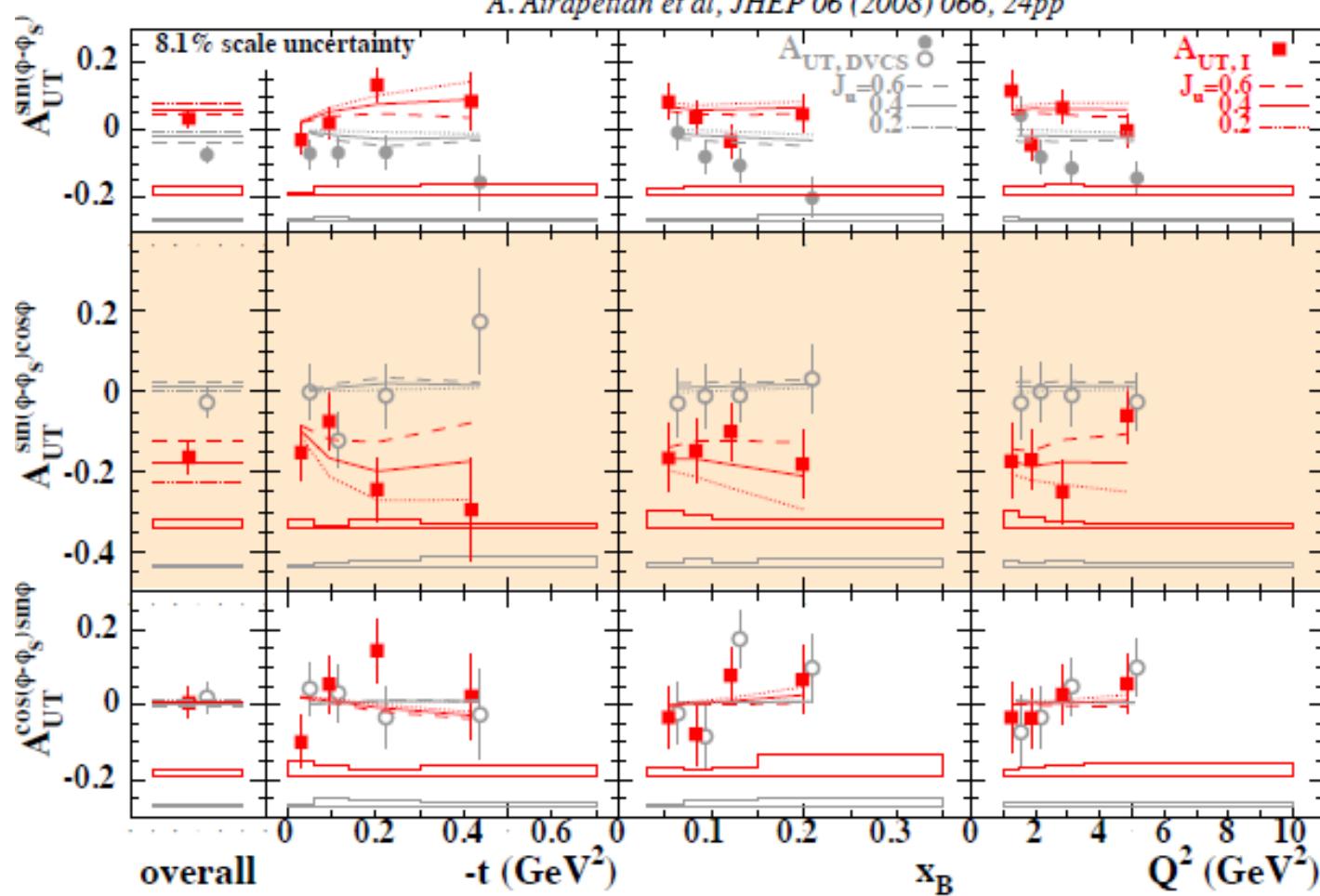


solid lines : GK EPJA47 (2011)

# The Quest for the GPD E

- Transv. Target Spin Asymm. of DVCS – HERMES
- Future: CLAS12, COMPASS

# Trans. Target Spin Asymm. on a proton – HERMES



But also Large  
 $A_{UT,DVCS} \sin(\phi - \phi_S)$   
 With strong  $x_B$  depend.

Large  
 $A_{UT,I} \sin(\phi - \phi_S) \cos \phi$   
 Sensitive to  $J_u, J_d$   
 (VGG model)

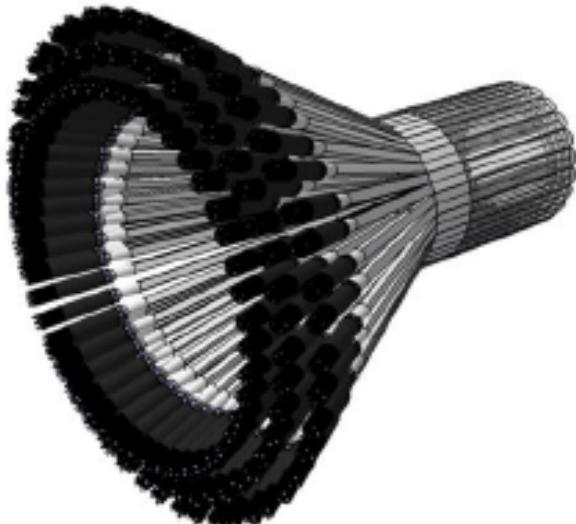
# The Future Quest for the GPD E

## CLAS12 at Jlab

$$\vec{e} d \rightarrow e n \gamma(p) \quad E12-11-003$$

$$\Delta\sigma_{LU} \sim Im (F_{1n} \mathcal{H} - F_{2n} \mathcal{E})$$

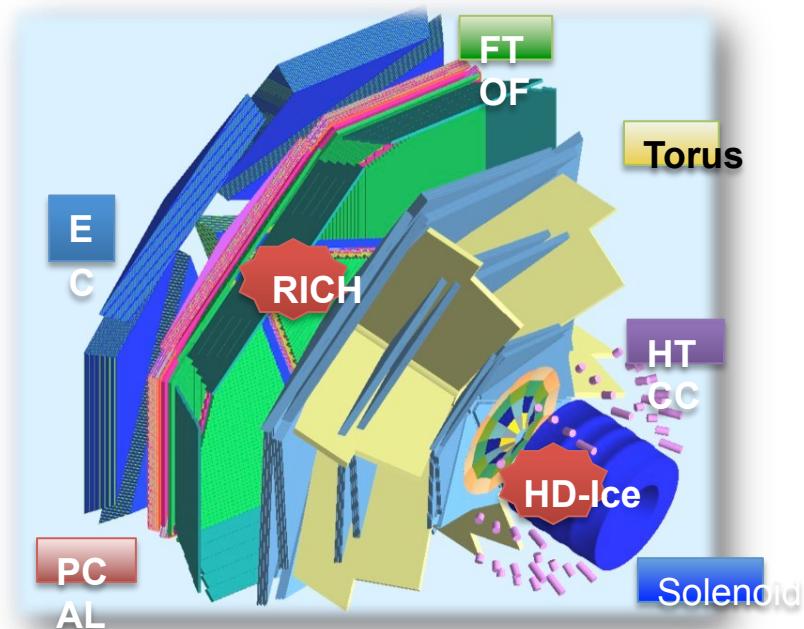
With LD2 target + CLAS12  
+ Forward Calorimeter  
+ Neutron Detector ToF



$$\vec{e} p \uparrow \rightarrow e p \gamma \quad E12-12-010$$

$$\begin{aligned}\Delta\sigma_{UT} \sin(\phi - \phi_s) \cos \phi &= Im (F_2 \mathcal{H} - F_1 \mathcal{E}) \\ \Delta\sigma_{LT} \sin(\phi - \phi_s) \cos \phi &= Re (F_2 \mathcal{H} - F_1 \mathcal{E})\end{aligned}$$

With the HD ice target  
(transv pol =60% H )



# The Quest for the GPD E

## CLAS12 at Jlab

$\vec{e} d \rightarrow e n \gamma(p)$  E12-11-003

$$\Delta\sigma_{LU} \sim Im (F_{1n} \mathcal{H} - F_{2n} \mathcal{E})$$

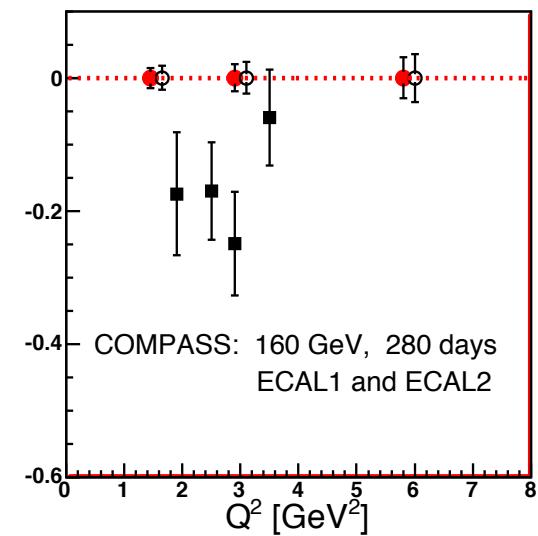
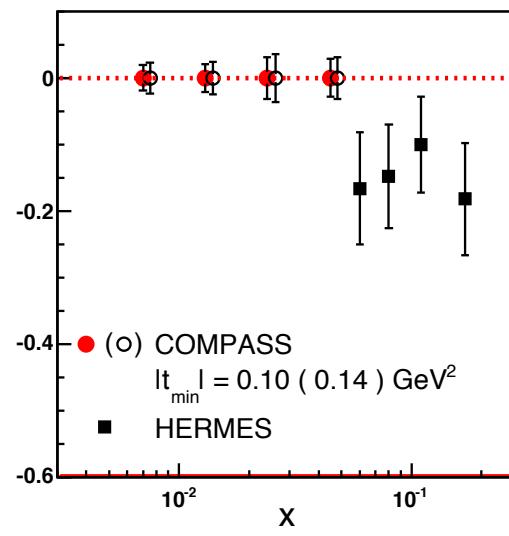
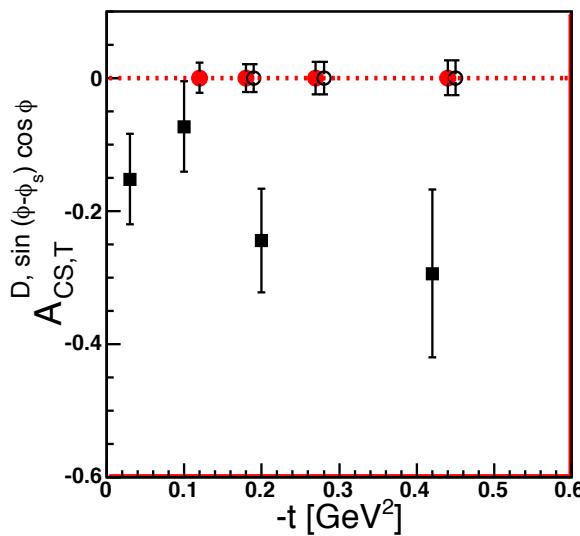
With LD2 target + CLAS12  
+ Forward Calorimeter  
+ Neutron Detector ToF

$\vec{e} p \uparrow \rightarrow e p \gamma$  E12-12-010

$$\begin{aligned}\Delta\sigma_{UT} \sin(\phi - \phi_s) \cos \phi &= Im (F_2 \mathcal{H} - F_1 \mathcal{E}) \\ \Delta\sigma_{LT} \sin(\phi - \phi_s) \cos \phi &= Re (F_2 \mathcal{H} - F_1 \mathcal{E})\end{aligned}$$

With the HD ice target  
(transv pol = 60% H )

$\vec{e} p \uparrow \rightarrow e p \gamma$  @ COMPASS (part of LOI in preparation)



# Conclusions and perspectives

Large worldwide experimental effort for DVCS and HEMP

- Dominance of the GPD **H**:  $\text{Im}\mathcal{H}$  rather well known,
- $\text{Re}\mathcal{H}$  poorly constrained  $\Rightarrow$  Beam Charge Diff. and cross section measurements
- The GPD **E** poorly constrained  $\Rightarrow$  Transversely Pol. Target measurements on proton or measurements on neutron

Precise data on the widest possible kinematic range are needed  
→ High priority for Jlab12, COMPASS and future EIC

Global fits needed to interpret  
the existing and forthcoming measurements

Important complementary information  
from excl. Meson production (only briefly touched in my talk)

A lot of work is ahead of us...

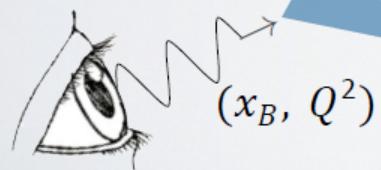
# **BACKUP**

# From PDFs to TMDs and GPDs

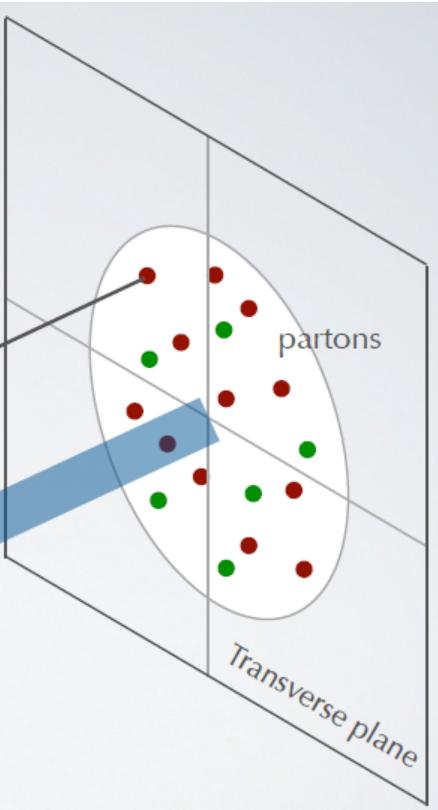
PDFs: 1-D structure

PDF ( $x$ )

Longitudinal momentum  
 $k^+ = xP^+$



A. Bacchetta



PDF measured in Deep Inelastic Scattering

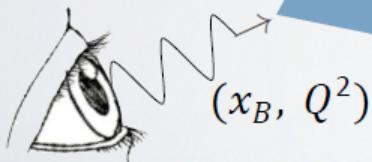
$$\ell p \rightarrow \ell' X$$

# From PDFs to TMDs and GPDs

Wigner distributions  
 $\rho(x, \vec{k}_T, \vec{b}_T)$

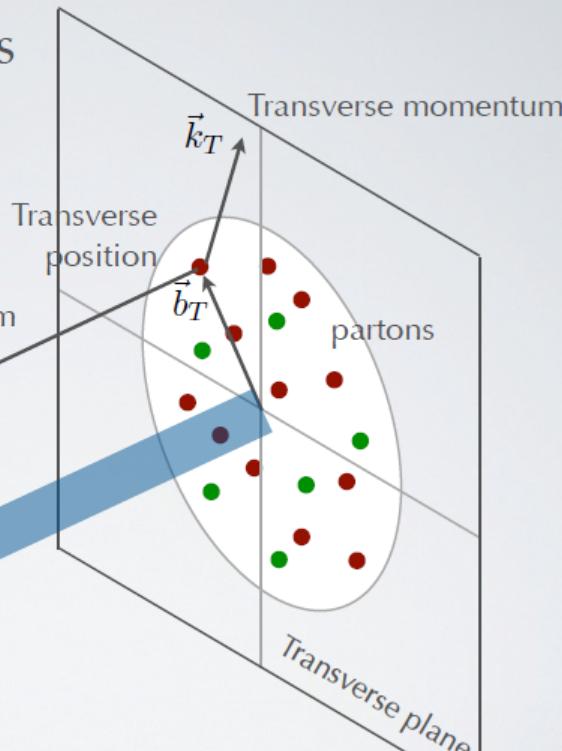
5-D correlations

Longitudinal momentum  
 $k^+ = xP^+$



A. Bacchetta

see, e.g., C. Lorcé, B. Pasquini, M. Vanderhaeghen, JHEP 1105 (11)



**3-dimensional nucleon structure**  
in momentum and configuration space:

**GPD ( $x, b_\perp$ ) :**

Generalised Parton Distribution  
(position in the transverse plane)

**TMD ( $x, k_\perp$ ) :**

Transverse Momentum Distribution  
(momentum in the transv. plane)



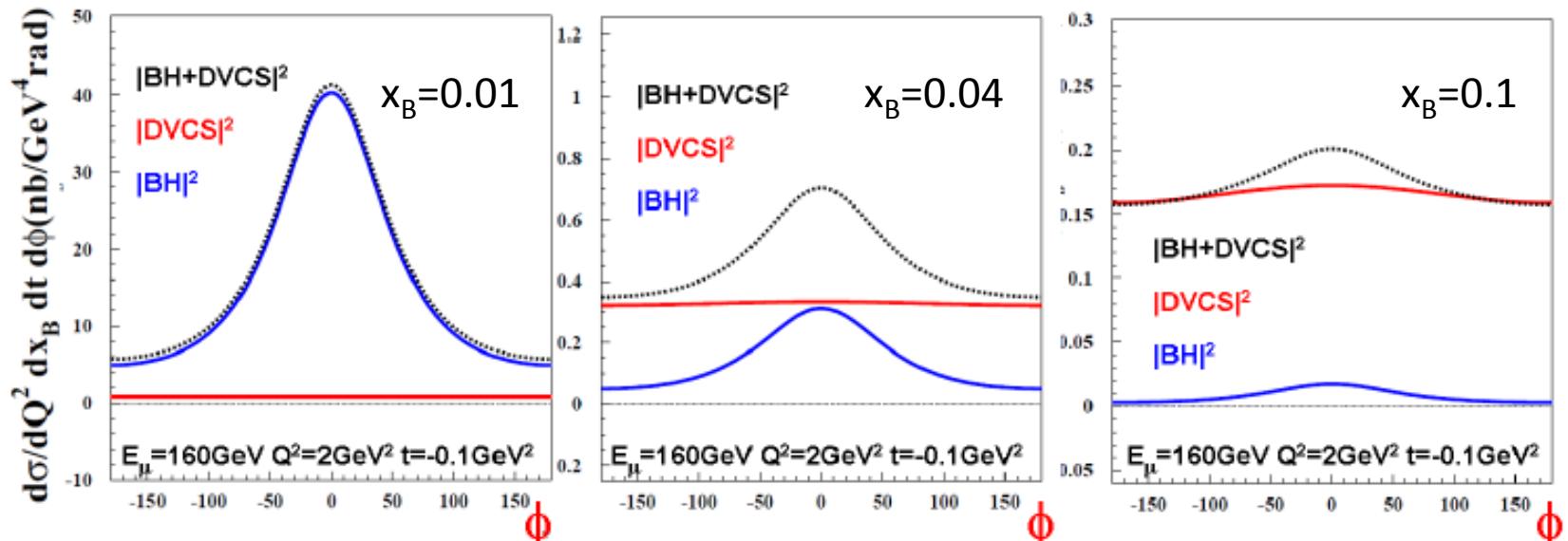
TMD accessible in **SIDIS** and **DY**

GPD in **Exclusive reactions**  
**DVCS** and **HEMP**

# High Beam Energy

Example at  $E_\ell = 160 \text{ GeV}$

$x_B$  ↗  
BH ↘

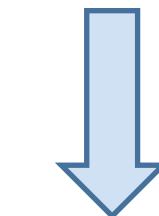


BH dominates  
Reference yield

Access to DVCS ampl.  
Via interference

DVCS dominates  
Study of  $d\sigma/dt$

$E_\ell$  ↘ BH ↗



Jlab  
HERMES, H1  
COMPASS



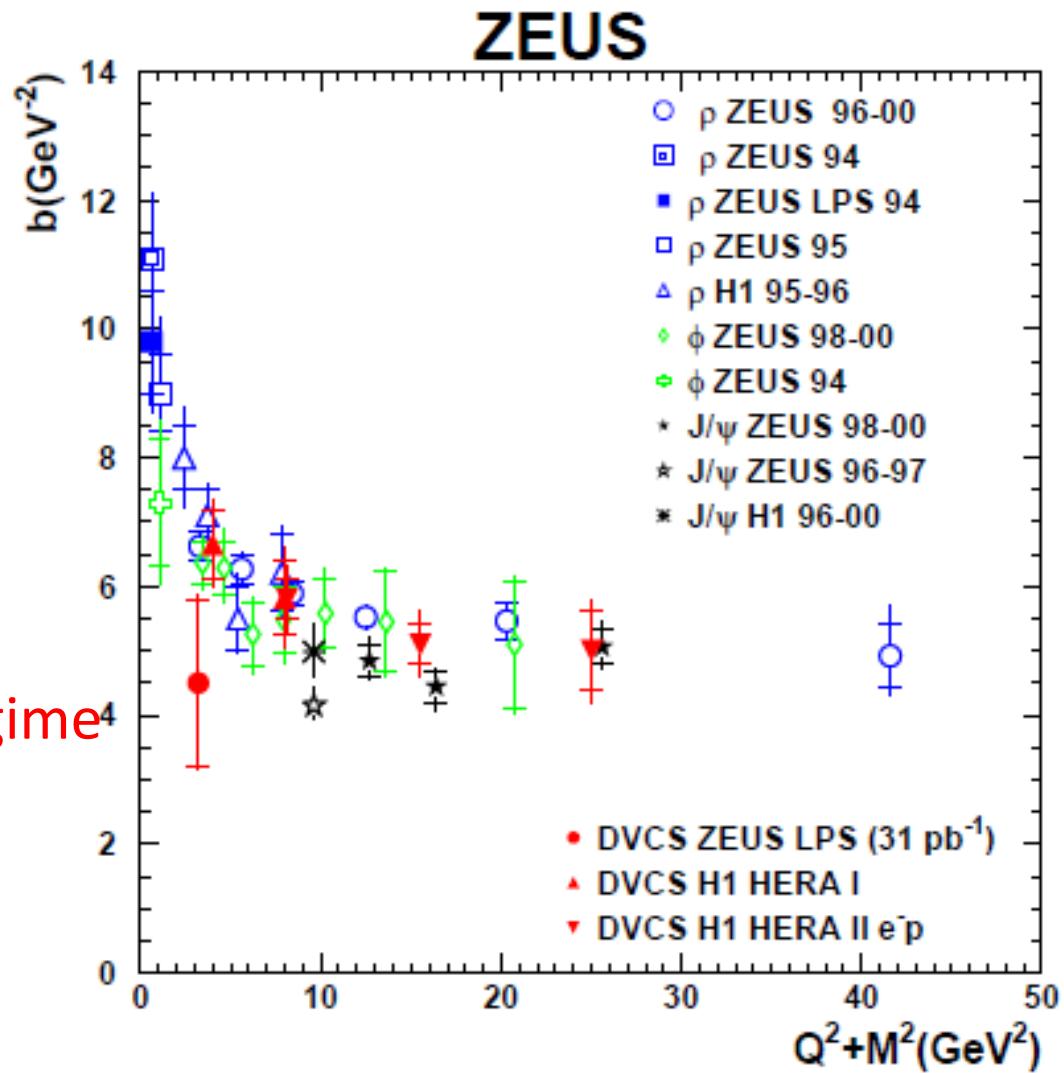
Only for high energy  
H1 & ZEUS  
COMPASS

# Cross sections and t dependence

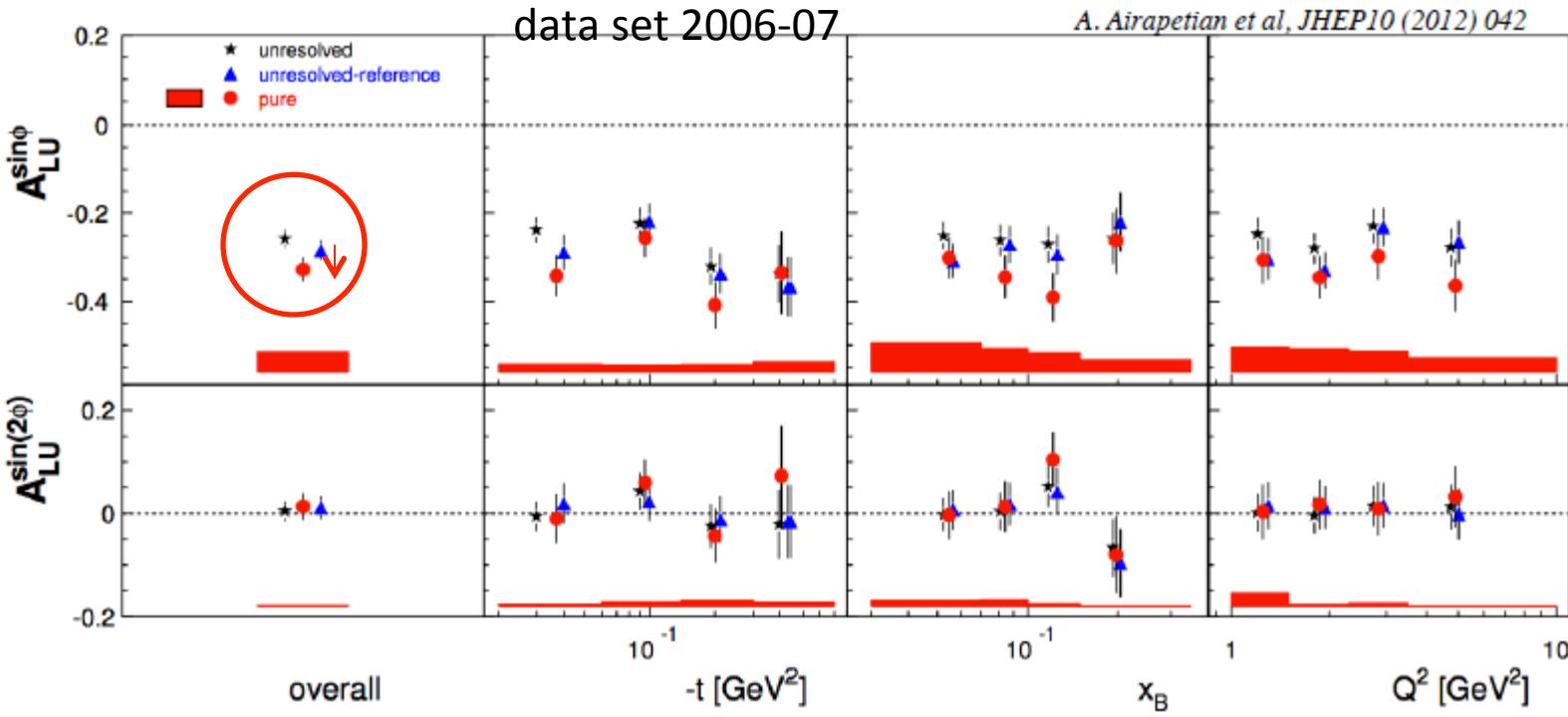
$$\frac{d\sigma}{dt} \propto e^{-b|t|}$$

sensitivity  
to the nucleon transverse size  
+ to the meson transverse size

J/ $\psi$  and DVCS in the hard regime  
at small  $Q^2$



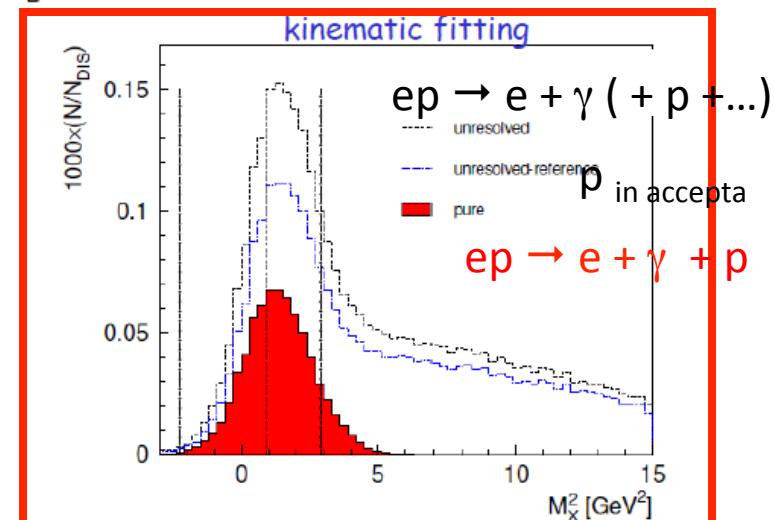
# BSA with recoil detector with HERMES



High-purity event selection shows that there is only a small influence on the extracted BSA amplitude from events involving a  $\Delta$  particle (associated DVCS)

The leading asymmetry has increased by  $0.054 \pm 0.016$

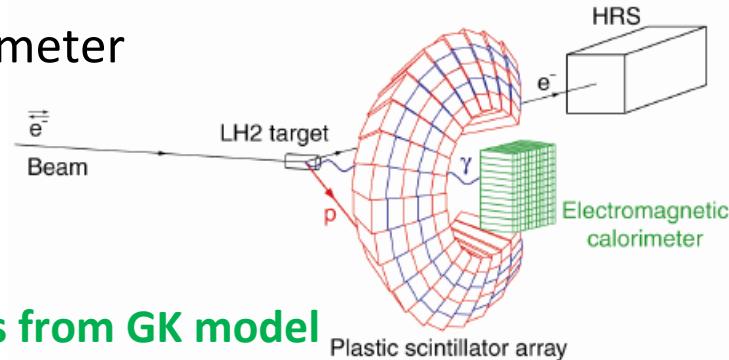
Mainly dilution due to the associated DVCS



# Beam Spin Sum and Diff of DVCS - HallA

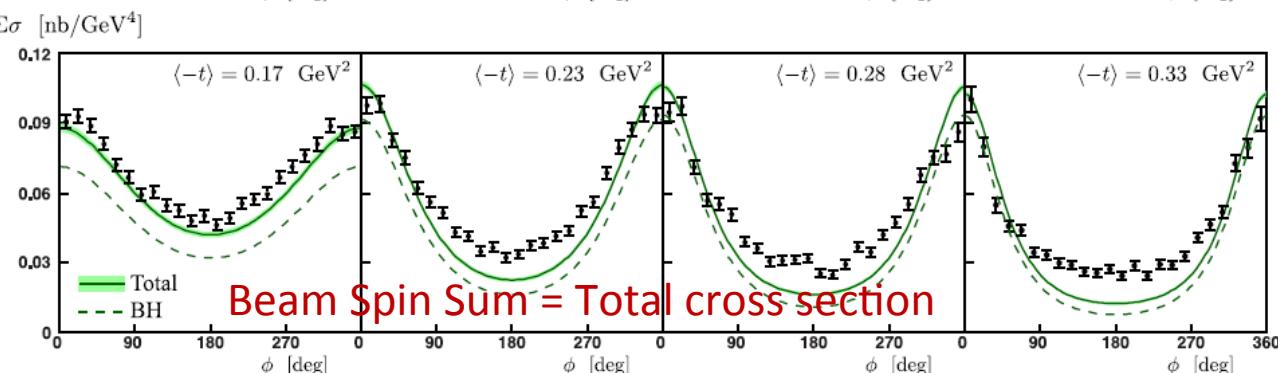
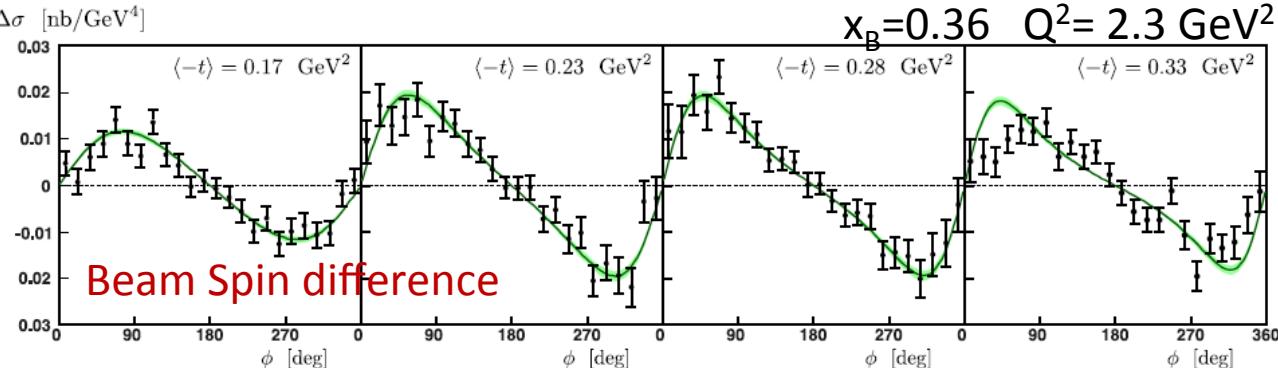
E00-110 pioneer experiment with magnetic spectrometer

3 measurements:  $x_B=0.36$   $Q^2= 1.5, 1.9, 2.3 \text{ GeV}^2$



Data: Munoz et al. PRL97, 262002 (2006)

Model: Kroll, Moutarde, Sabatié, EPJC73 (2013) with GPDs from GK model



Do we understand Hall A data?

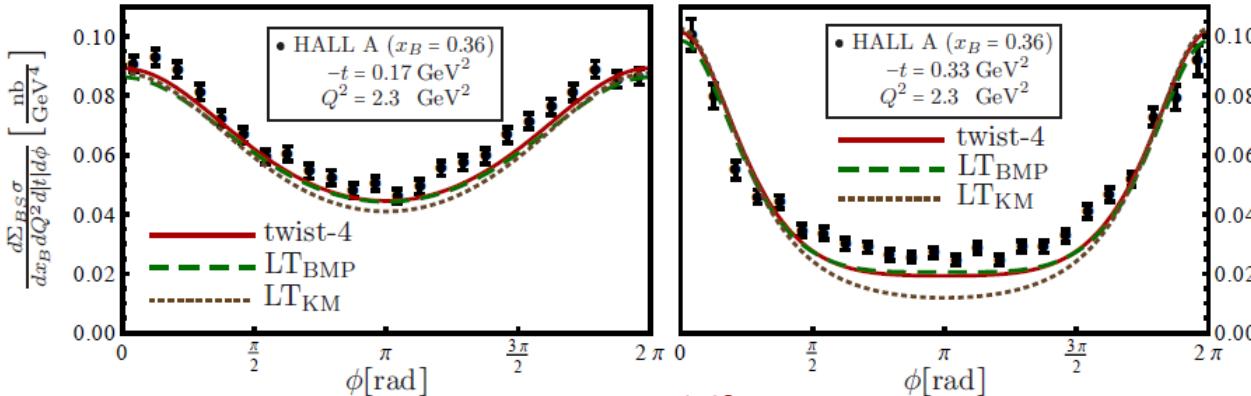
# Beam Spin Sum and Diff of DVCS - HallA

Data: Munoz et al. PRL97, 262002 (2006)

Model: Braun, Manashov, Pirnay, Mueller PRD79 (2014)

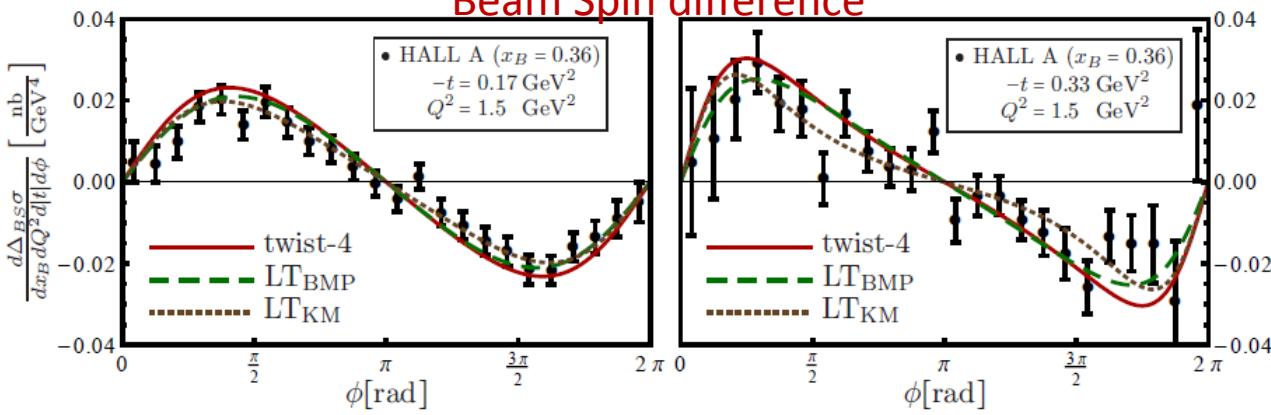
GK12 model evaluated  
with KM and BMP  
prescription

Beam Spin Sum = Total cross section



including  
kinematic corrections  
(finite-t, target mass corr.)

Beam Spin difference



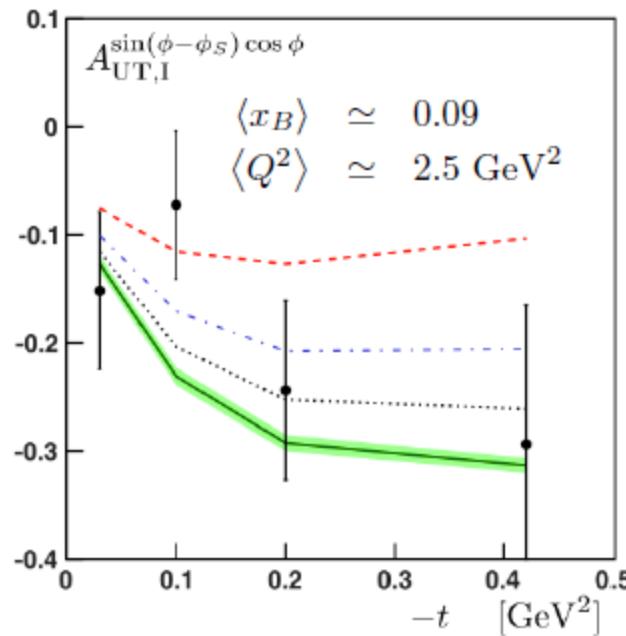
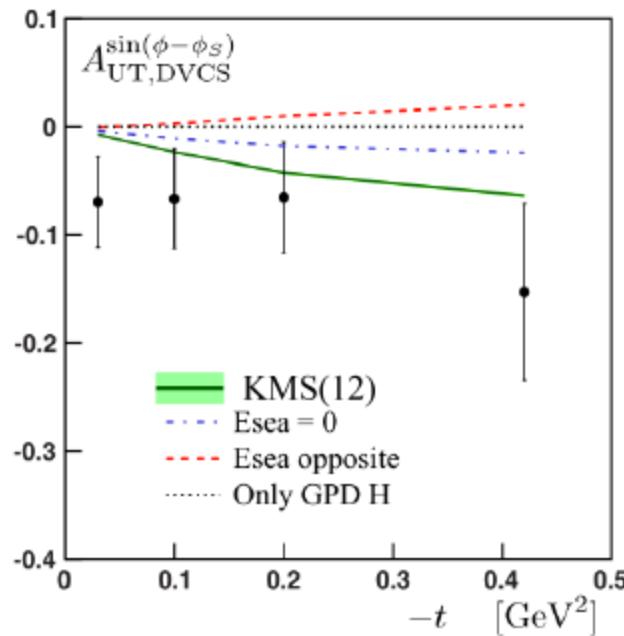
News:

- 2010: run E07-007  
Rosenbluth-like DVCS<sup>2</sup>/Int sparation
- 2014: HallA with 11 GeV
- 2018: HallC with 11 GeV

Do we understand Hall A data?

# Trans. Target Spin Asymmetry on a proton – HERMES

Model: Kroll, Moutarde, Sabatié, EPJC73 (2013) with GPDs from GK model



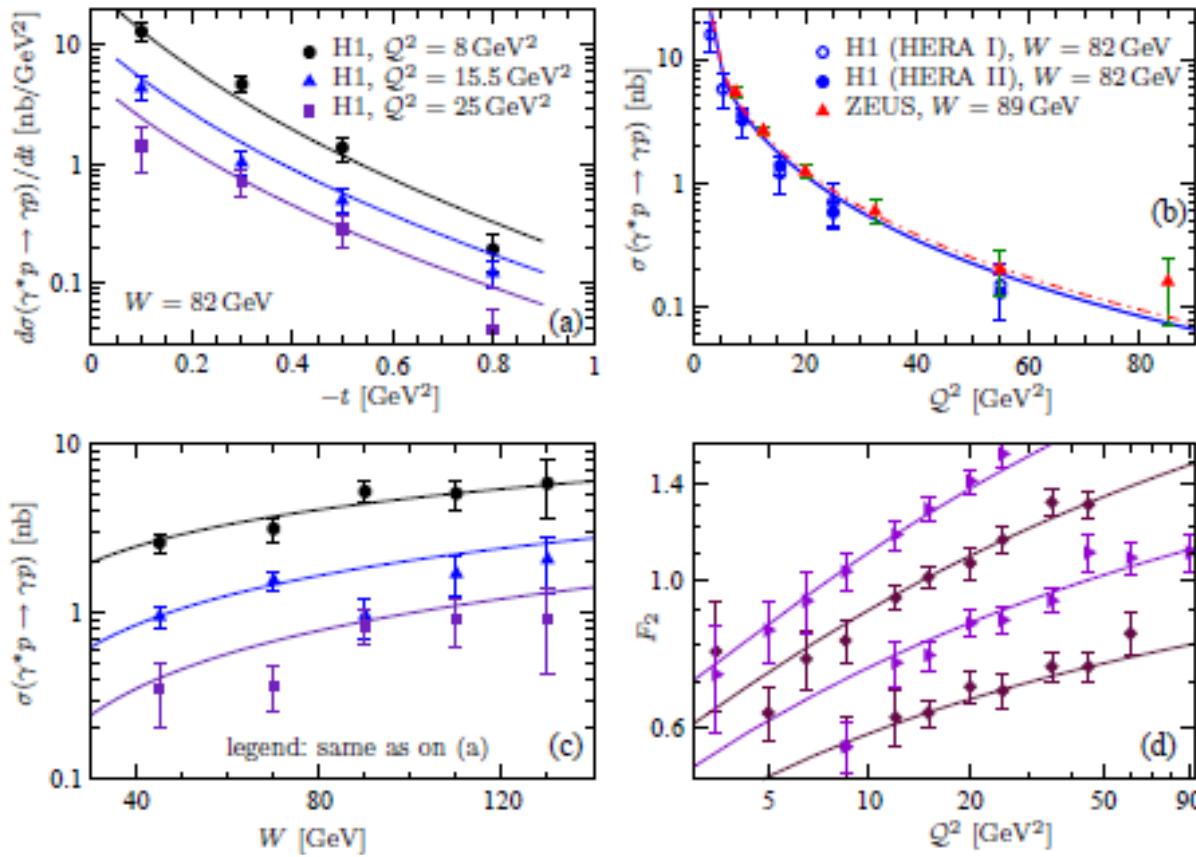
$$A_{\text{UT},\text{DVCS}}^{\sin(\phi-\phi_S)} \sim \text{Im}[\mathcal{E}^* \mathcal{H}]$$

$$A_{\text{UT},\text{DVCS}}^{\sin(\phi-\phi_S)} \neq 0 \implies \mathcal{E} \neq 0$$

cancellation between  $\mathcal{E}^s$  and  $\mathcal{E}^g$  does not occur as for  $\rho^0$  asymmetry,  
DVCS observables are very sensitive to  $E_{\text{sea}}$

**E sea < 0 is favored by HERMES data**

# Predictions for DVCS from KM model

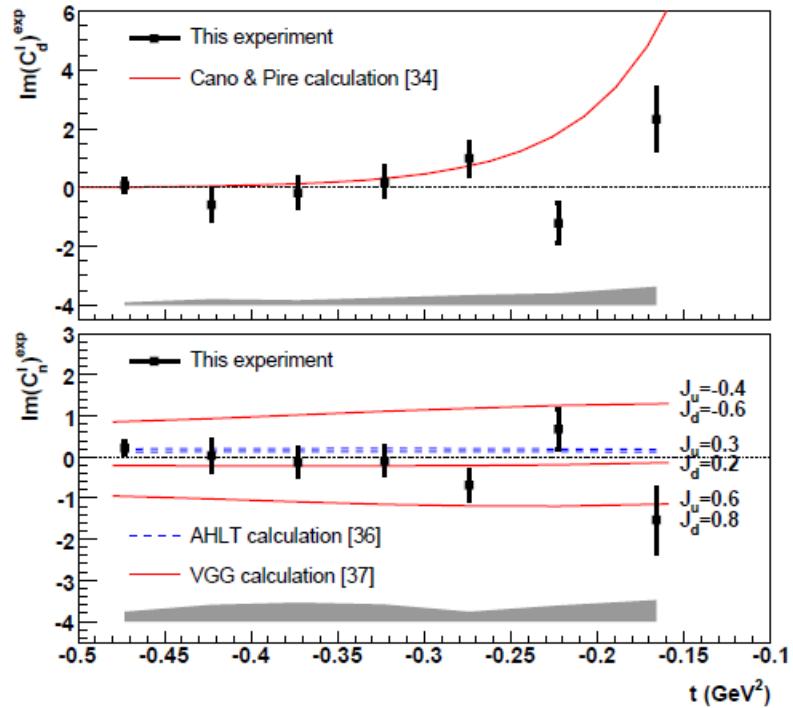
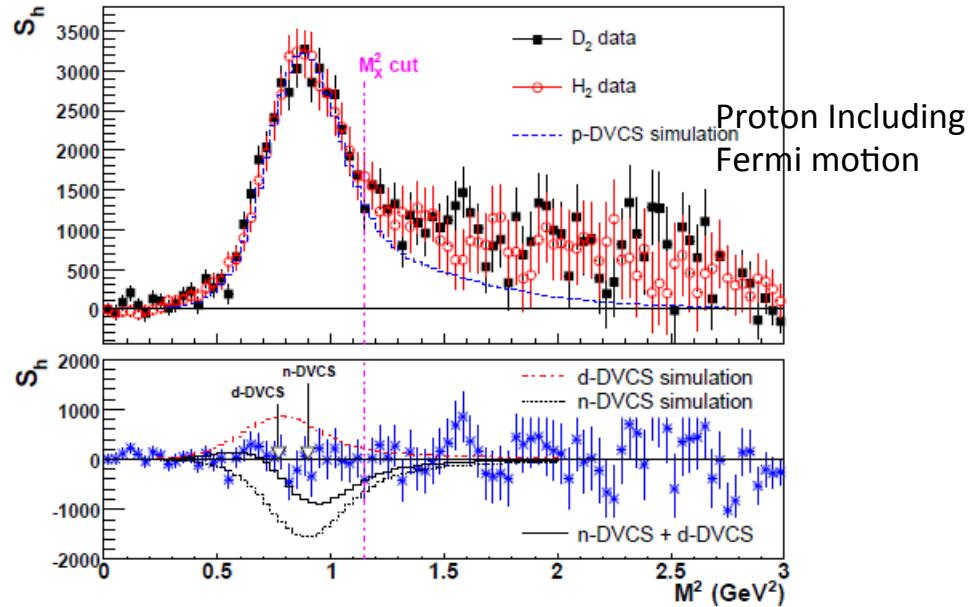


**KM10:** Kumericki and Mueller NPB (2010) 841; arXiv:0904.0458

one of the most general parameterization of GPDs based on their mathematic properties fit to the DVCS data and DIS

# DVCS on a neutron – HALL A

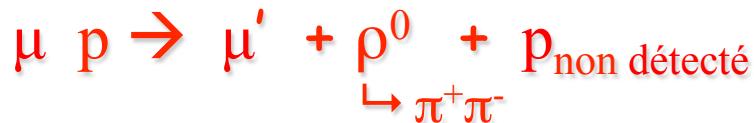
DVCS on LD2 target= DVCS on quasi-free proton + quasi-free neutron + coherent DVCS on D



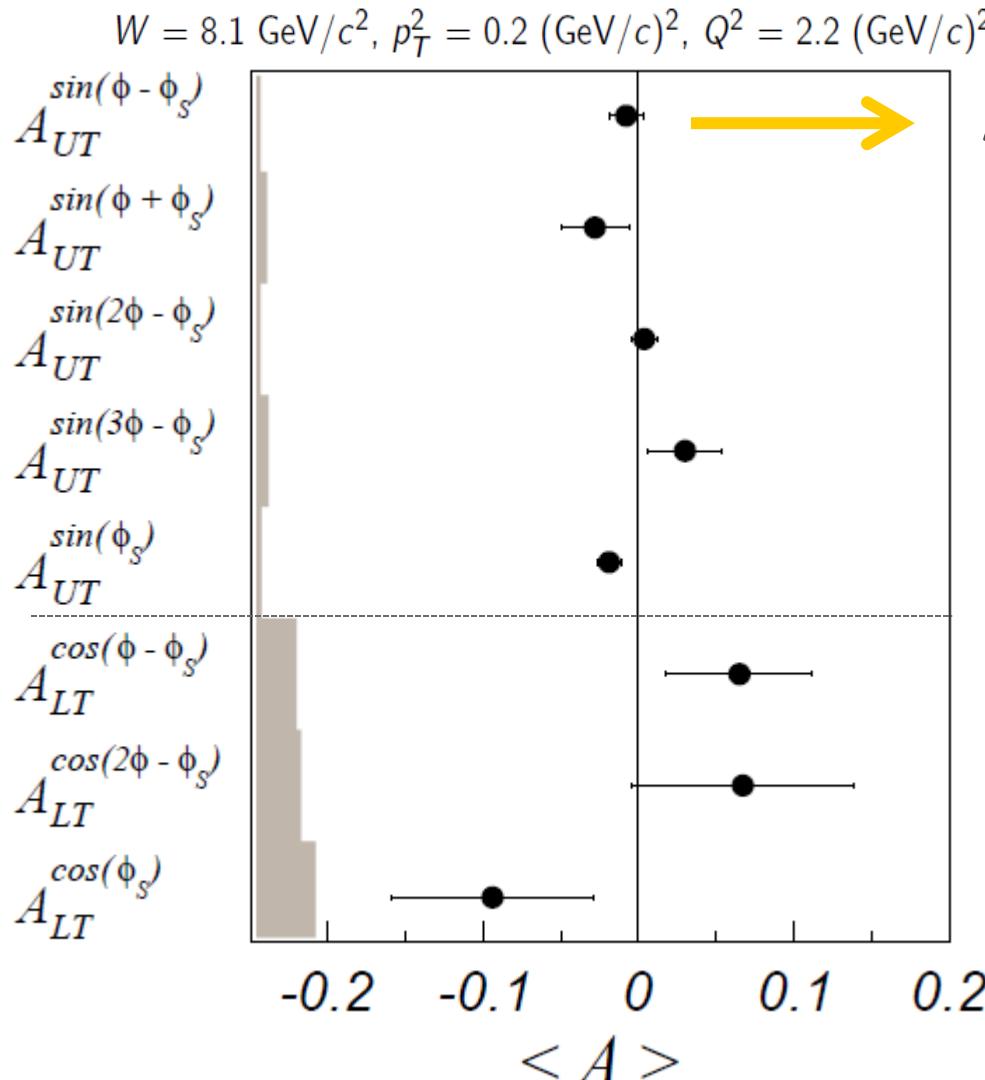
Next:

- 2010: run E08-025 with LD2 target  
Rosenbluth-like DVCS<sup>2</sup>/Int separation
- 2018: CLAS12 with 11 GeV with LD2 target + neutron detector (ToF)

# exclusive $\rho^0$ production with Transv. Polar. Target



COMPASS 2007-2010, with transv. polar. NH3 target,  
without recoil detector



$$A_{UT}^{\sin(\phi - \phi_s)} \propto \text{Im}(\mathcal{E}^* \mathcal{H})$$

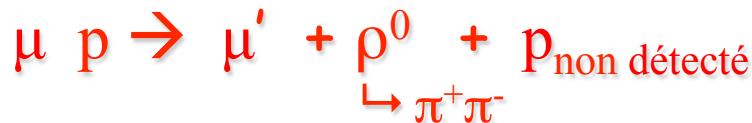
$$E\rho^0 \propto 2/3 E^u + 1/3 E^d + 3/8 E^g$$

Cancellation between gluon and sea contributions and  $E^u \text{ val} \sim -E^d \text{ val}$

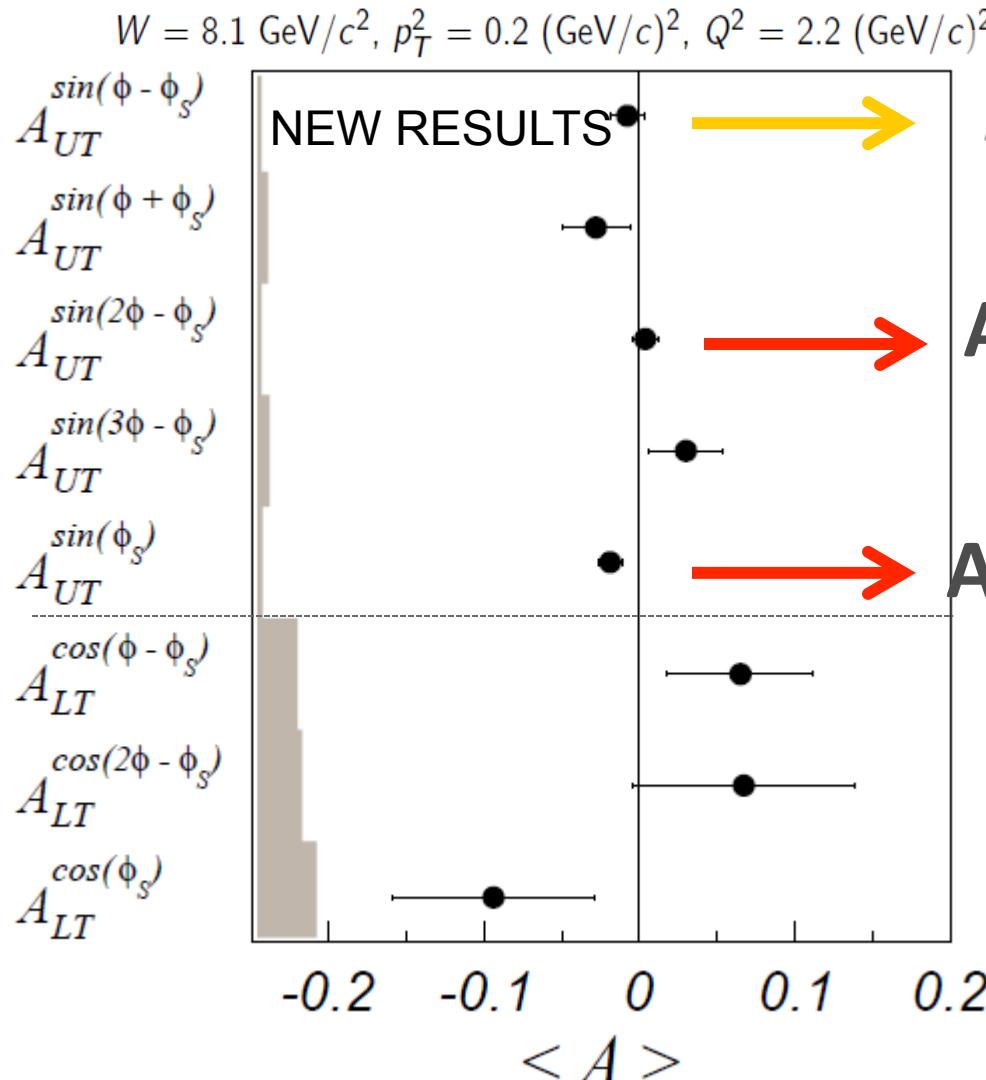
COMPASS, NPB865 (2012) 1-20  
(similar res HERMES PLB679(2000) 100)

$\omega$  production very interesting  
analysis on going

# exclusive $\rho^0$ production with Transv. Polar. Target



COMPASS 2007-2010, without recoil detector



$$A_{UT}^{\sin(\phi - \phi_s)} \propto \text{Im}(\mathcal{E}^* \mathcal{H})$$

$$A_{UT}^{\sin(2\phi - \phi_s)} \propto \text{Im}(\mathcal{E}^* \bar{\mathcal{E}_T})$$

$$A_{UT}^{\sin(\phi_s)} \propto \text{Im}(\mathcal{E}^* \bar{\mathcal{E}_T} - \mathcal{H}^* \bar{\mathcal{H}_T})$$

→  $H_T$  should not be small

COMPASS, PLB 731 (2014) 96