

RECENT RESULTS ON FRAGMENTATION FUNCTIONS FROM E+E- FACILITIES



INDIANA UNIVERSITY

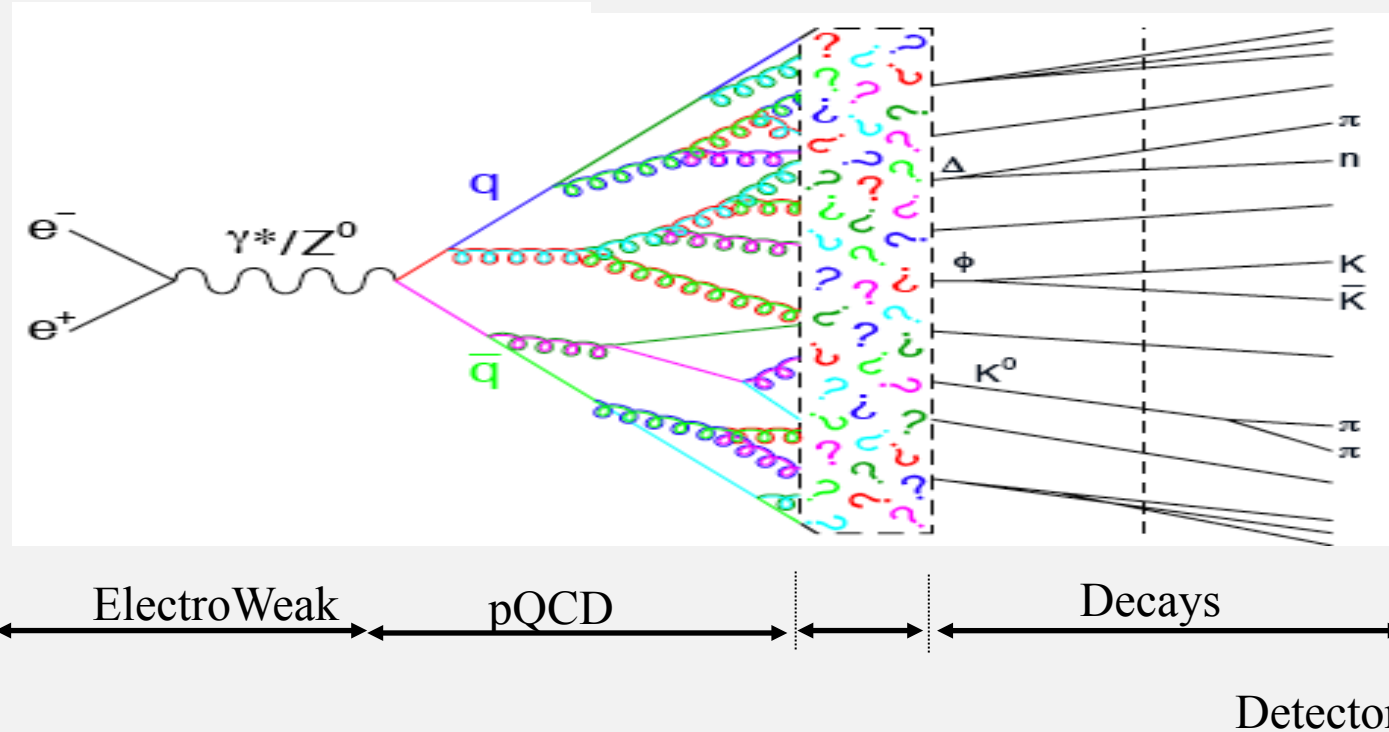
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Transversity 2017, Frascati

Input and slides from
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Fabio Anulli
Yinghui Guan
Ralf Seidl
Matthias Grosse Perdekamp

FACTORIZED QCD: HADRONIZATION DESCRIBED BY FRAGMENTATION FUNCTIONS

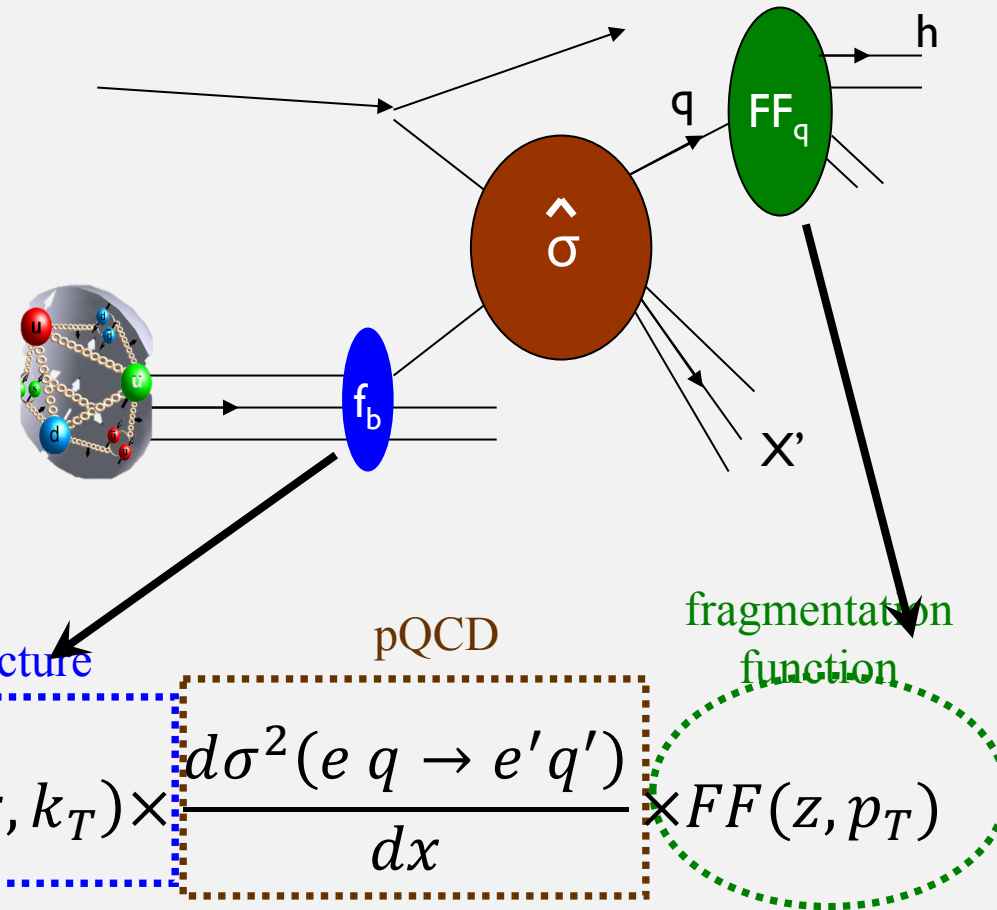
Field, Feynman (1977): Fragmentation functions encode the information on how partons produced in hard-scattering processes are turned into an observed colorless hadronic bound final-state [PRD 15 (1977) 2590]



- Complementary to the study of nucleon structure (PDFs)
- Cannot be computed on the lattice
- Questions to be asked
 - Macroscopic effect (distribution, polarization) of microscopic properties (quantum numbers)?
 - Effect of QCD vacuum the quark is traversing

FRAGMENTATION FUNCTIONS APPEAR ALMOST ALWAYS WHEN ACCESSING PARTONIC STRUCTURE OF THE NUCLEON

- Proton Structure extracted using QCD factorization theorem
- FFs contribute to virtually all processes
- Particular important for transverse spin structure
→ need detailed understanding of FFs to use as 'quark polarimeter'



AMSTERDAM NOTATION FOR FFS WITH QUARK/HADRON POLARIZATION

Observables:

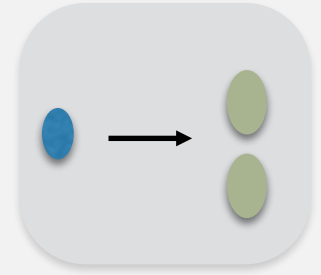
z : fractional energy of the quark carried by the hadron

$p_{h,T}$: transverse momentum of the hadron wrt the quark direction: **TMD FFs**

Parton polarization → Hadron Polarization ↓	Spin averaged	longitudinal	transverse
spin averaged	$D_1^{h/q}(z, p_T) = \left[\bullet \rightarrow \text{red circle} \right]$		$H_1^{\perp h/q}(z, p_T) = \left[\uparrow \bullet \rightarrow \text{blue circle} \right] - \left[\downarrow \bullet \rightarrow \text{blue circle} \right]$
longitudinal		$G_1^{h/q}(z, p_T) = \left[\bullet \rightarrow \text{red circle} \right] - \left[\bullet \leftarrow \text{red circle} \right]$	
Transverse (here Λ)	$D_{1T}^{\perp \Lambda/q}(z, p_T) = \left[\bullet \rightarrow \text{blue circle with } \uparrow \right]$		$H_1^{q/\Lambda}(z, p_T) = \left[\uparrow \bullet \rightarrow \text{red circle with } \uparrow \right] - \left[\downarrow \bullet \rightarrow \text{red circle with } \uparrow \right]$

- Theoretically many more, in particular with polarized hadrons in the final state and transverse momentum dependence → similar to PDFs encoding spin/orbit correlations
- Determining final state polarization needs self analyzing decay (Λ)
- Gluon FFs similar but with circular/linear polarization (not as relevant for e^+e^-)

DI-HADRON FRAGMENTATION FUNCTIONS



Additional Observable:

$$\vec{R} = \vec{P}_1 - \vec{P}_2 :$$

The relative momentum of the hadron pair is an additional degree of freedom:

the orientation of the two hadrons w.r.t. each other and the jet direction can be an indicator of the quark transverse spin

Do not need

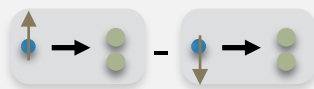
Small \vec{R} : non-perturbative object.

G_1^\perp : T-odd FF



- chiral-even function
- log. polarized q \rightarrow two unp. Hadrons
- \rightarrow connection to jet-handedness and (possibly) QCD vacuum structure

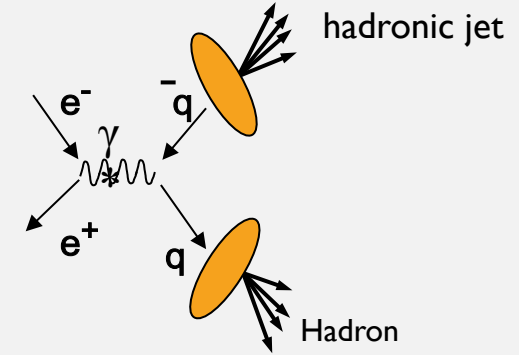
H_1^\leftarrow : T-odd FF



- Chiral-odd function
- Transv. polarized q \rightarrow two unp. Hadrons
- \rightarrow Collinear! (unlike Collins)

ACCESS OF FFS FOR LIGHT MESONS IN E^+E^- (SPIN AVERAGED CASE)

$$\frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^{e^+e^- \rightarrow hX}}{dz} = \frac{1}{\sum_q e_q^2} (2F_1^h(z, Q^2) + F_L^h(z, Q^2))$$

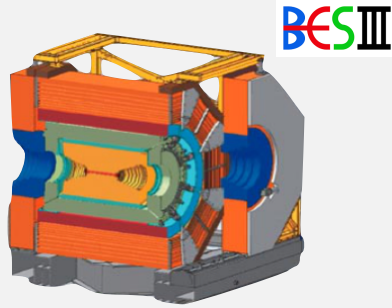


$$2F_1^h(z, Q^2) = \sum_q e_q^2 \left(D_1^{h/q}(z, Q^2) + \frac{\alpha_s(Q^2)}{2\pi} \left(C_1^q \otimes D_1^{h/q} + C_1^g \otimes D_1^{h/g} \right)(z, Q^2) \right)$$

- Cleanest process
- Clean environment, hermetic detectors \rightarrow can reconstruct complex final states, differentiate from feed-down
- Well understood, calculations available at NNLO
- **Limited access to flavor**
 - Use different couplings to γ^* and Z^0
 - Use polarization (SLD) and parity violating coupling
 - Use back-to-back correlations for different flavor combinations \rightarrow see next talk
- **Limited access to gluon FF**
 - From evolution
 - From three jet events (but theory treatment not clear)

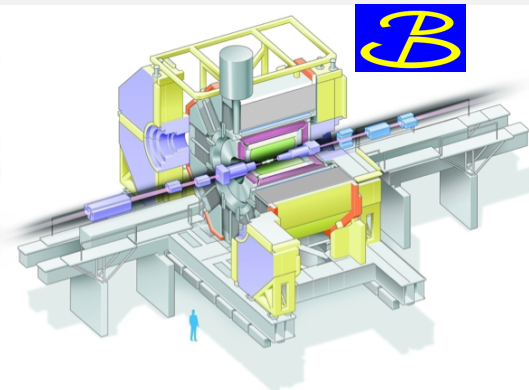
THE BESII, BELLE AND BABAR EXPERIMENTS

NIMA614,345(2010)



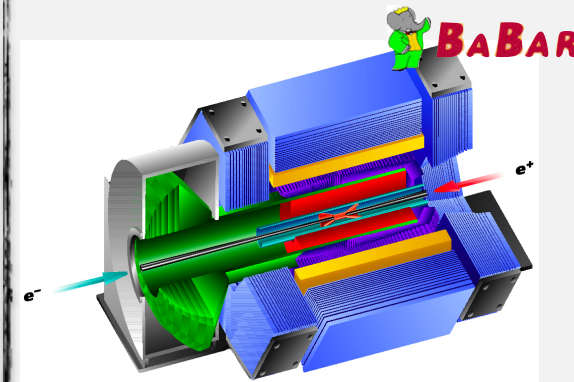
- Symmetric e^+e^- collider
- $\sqrt{s} = [2 - 4.6]$ GeV
- 62 pb^{-1} @ 3.65 GeV used for Collins studies
- Below open-charm threshold

- Asymmetric-energy e^+e^- collider
- $\sqrt{s} \sim 10.6$ GeV ($\Upsilon(4S)$)
- $\beta\gamma=0.425$
- $L \sim 1 \text{ ab}^{-1}$



NIMA479,117(2002)

NIMA729,615(2013)

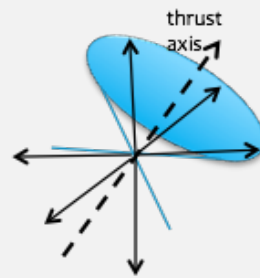


- Asymmetric-energy e^+e^- collider
- $\sqrt{s} \sim 10.6$ GeV ($\Upsilon(4S)$)
- $\beta\gamma=0.65$
- $L \sim 500 \text{ fb}^{-1}$

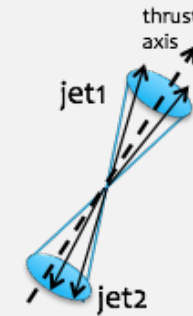
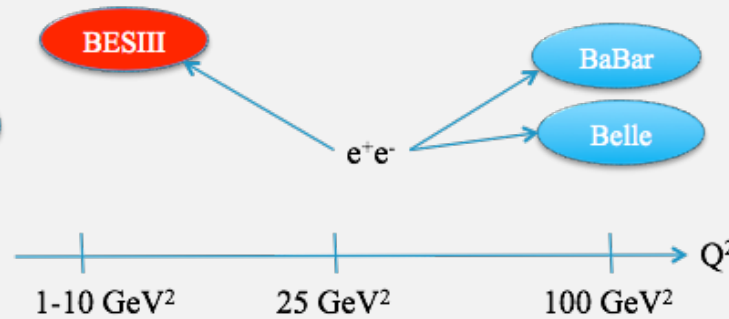
$$T = \sum_i \frac{|\mathbf{P} \cdot \hat{\mathbf{n}}|}{|P|}$$

thrust axis $\equiv \hat{\mathbf{n}}$

$$0.5 \leq T \leq 1$$



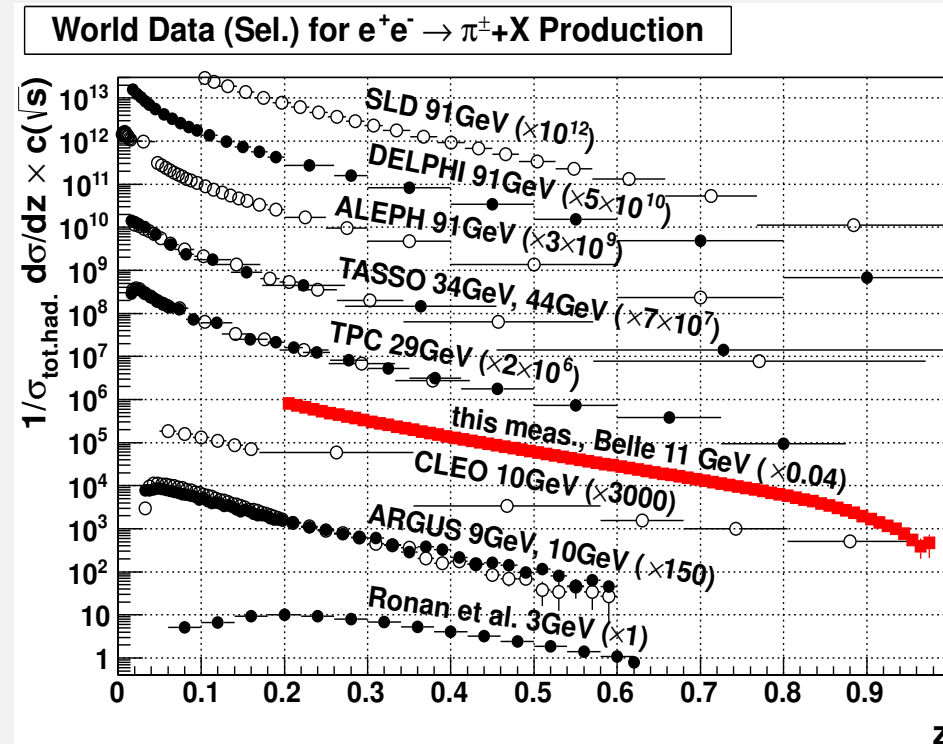
$T \sim 0.5$



$T \sim 1$

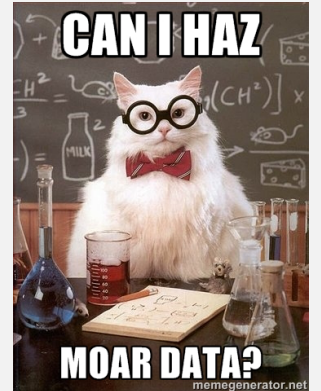
WORLD DATA ON E^+E^-

- Dominated by B factories
- Limited lever arm in \sqrt{s} in particular at high z
- Precision data includes charged single hadrons π , K , ρ , D , Λ , charmed baryons...
- Pairs of π , K , ρ (back-to-back and same hemisphere) \rightarrow See next talk by Gunar
- With B factory data theory and data uncertainties similar, good description by NNLO, some more work tbd at high and low z

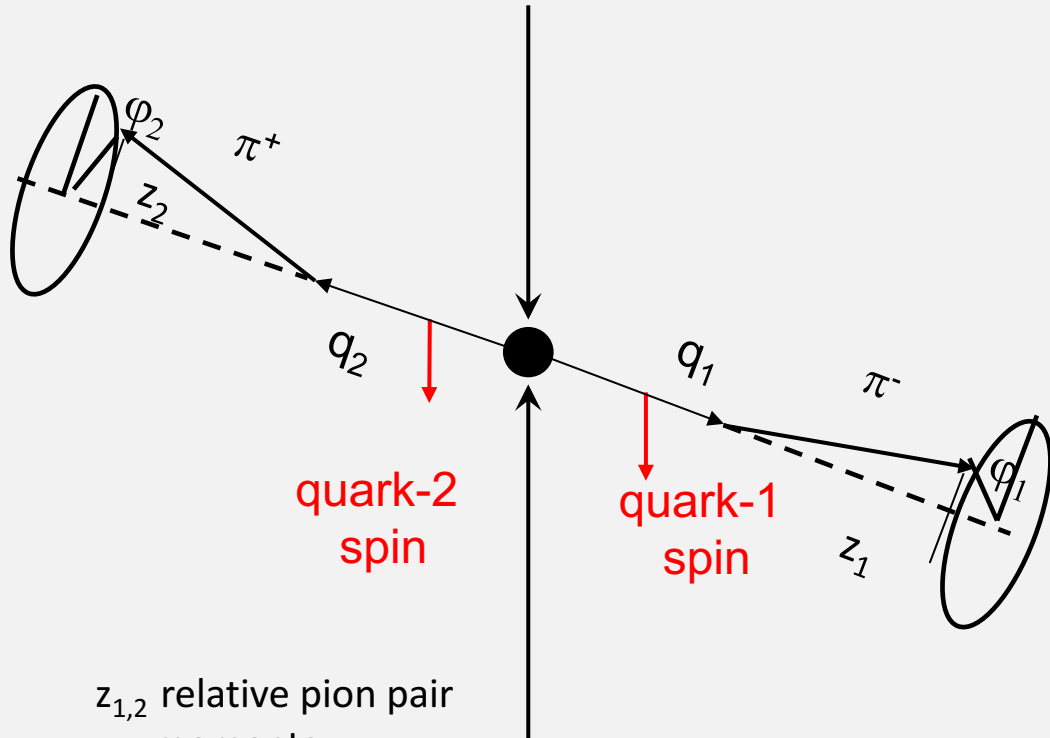


Phys.Rev.Lett. 111 (2013) 062002 (Belle)

Phys.Rev. D88 (2013) 032011 (BaBar)



CORRELATION MEASUREMENTS IN E^+E^-



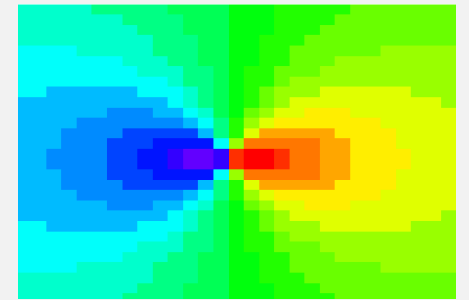
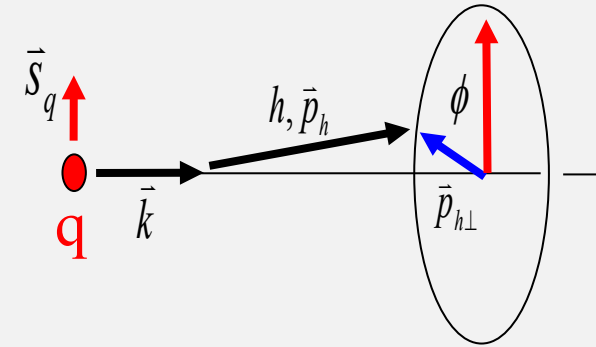
$z_{1,2}$ relative pion pair momenta

$$\text{Cross-section } e^+e^- \rightarrow (h_1 h_2)(\bar{h}_1 \bar{h}_2) + X$$

$$\propto D_1^\perp \bar{D}_1^\perp + H_1^\perp \bar{H}_1^\perp \cos(\phi_1 + \phi_2)$$

J. Collins, Nucl. Phys. B396, (1993) 161

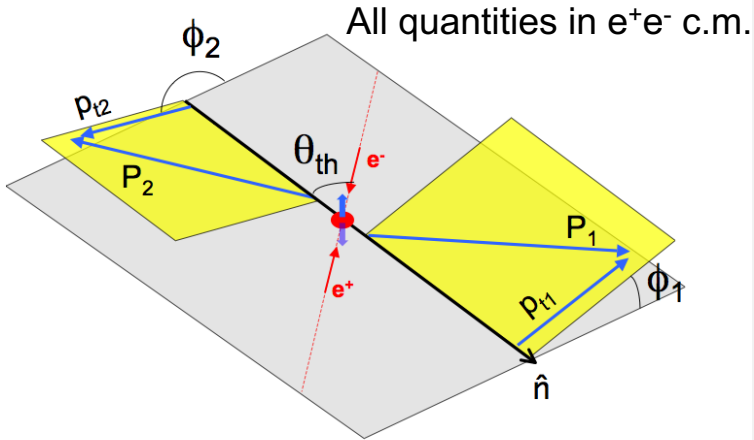
$$D_{q^\uparrow}^h(z, P_{h\perp}) = D_{1,q}^h(z, P_{h\perp}^2) + H_{1,q}^{\perp h}(z, P_{h\perp}^2) \frac{(\hat{\mathbf{k}} \times \mathbf{P}_{h\perp}) \cdot \mathbf{S}_q}{z M_h}$$



- Access spin dependence and p_T dependence (convolution or in jet) without PDF complication
- Made possible by B-factory luminosities

COLLINS EFFECT

RF12 or Thrust RF

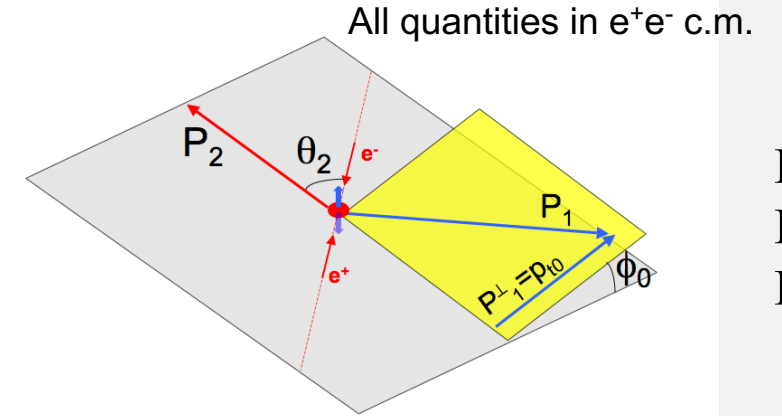


BaBar
Belle
~~BESIII~~

- **Thrust axis** to estimate the $q\bar{q}$ direction
- $\phi_{1,2}$ defined using thrust-beam plane

Normalized cross-section: $e^+e^- \rightarrow (h_1 h_2)(\overline{h_1} \overline{h_2}) + X$
 $\propto 1 + H_1^\perp \cdot \overline{H_1^\perp} \cos(\phi_1 + \phi_2)$

RF0 or Second hadron momentum RF



BaBar
Belle
BESIII

- Use **one track** in a pair
- Very clean experimentally (no thrust axis)

Normalized cross-section: $e^+e^- \rightarrow (h_1 h_2)(\overline{h_1} \overline{h_2}) + X$
 $\propto 1 + H_1^\perp * \overline{H_1^\perp} \cos(2\phi_0)$

Collins Effect vs (z_1, z_2) : comparisons

Unlike/Likesign

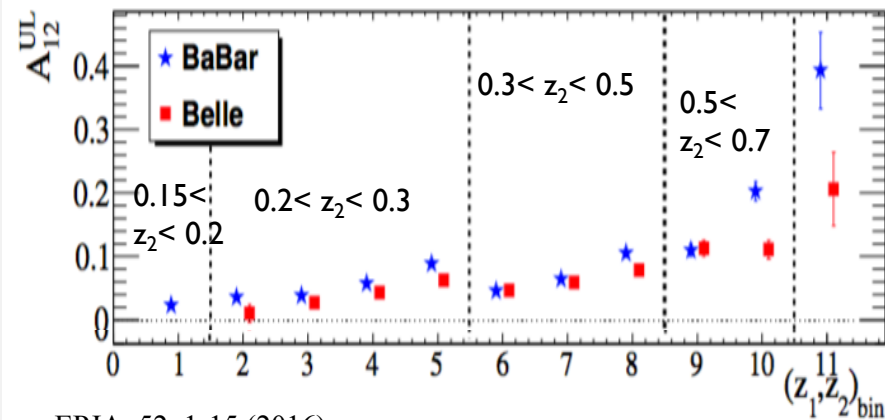
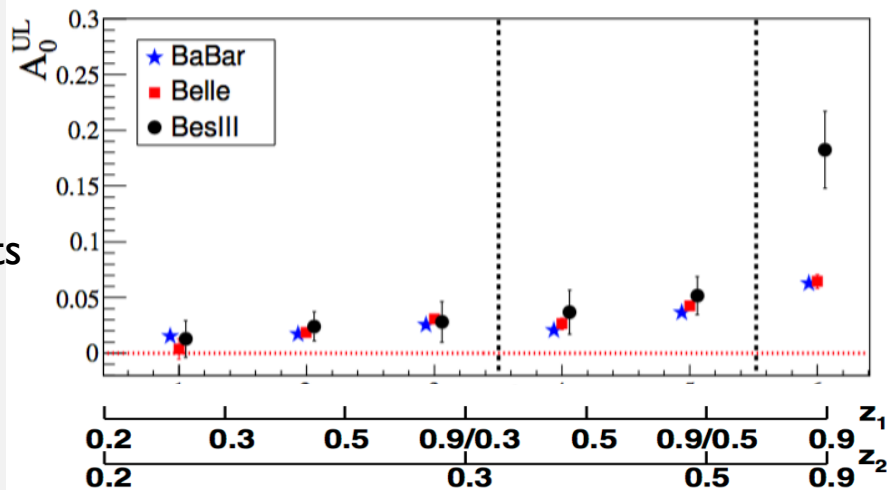
Ratios to cancel acceptance effects

Unlike:

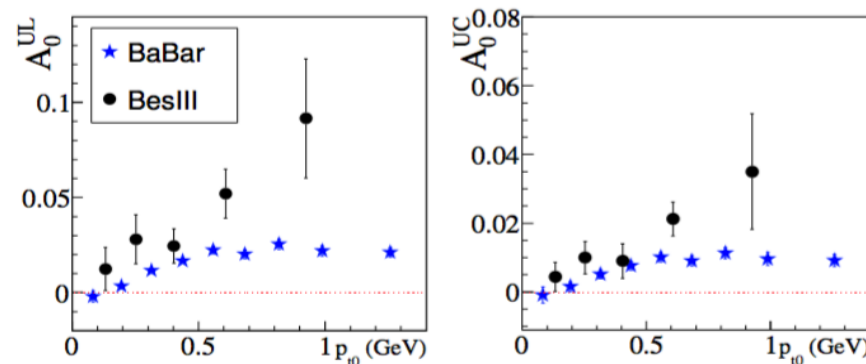
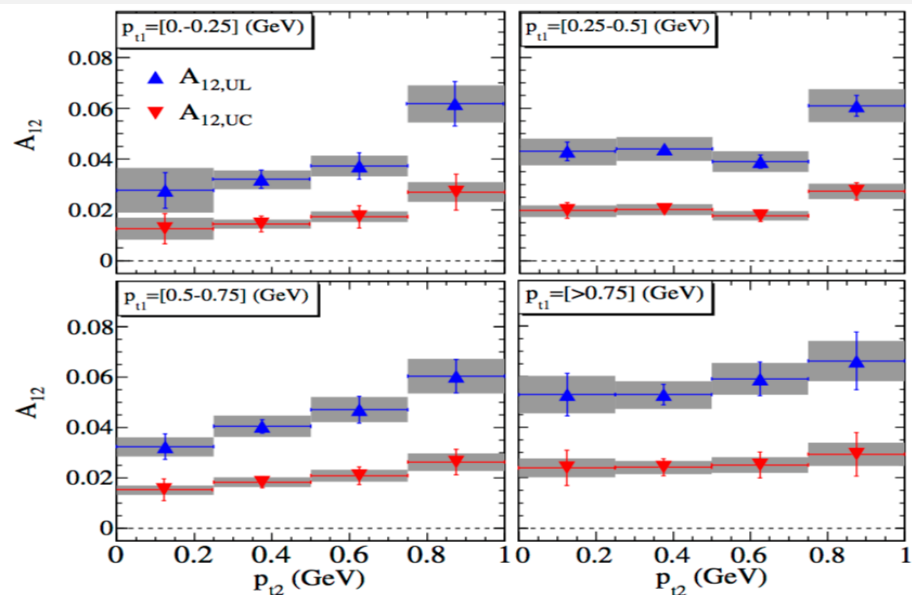
$f_{av} * f_{av} + d_{is} * d_{is}$

Like:

$f_{av} * d_{is}$



EPJA, 52, 1-15 (2016)



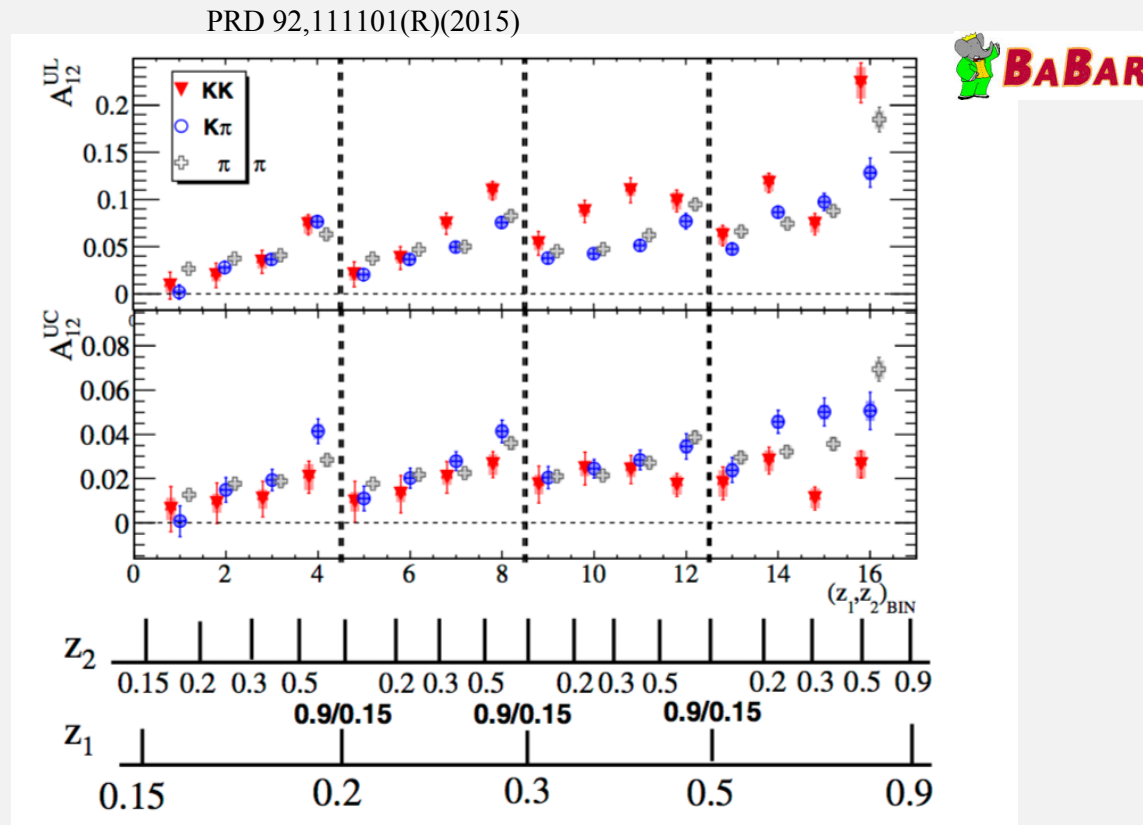
• First non-zero independent measurement of the Collins effect for pion pairs in e^+e^- annihilation by Belle Collaboration @ $\sqrt{s} \sim 10.6$ GeV (PRL 111,062002(2008), PRD 88,032011(2013)) leads to first extraction of transversity (Phys.Rev. D75 (2007) 054032) from SIDIS and e^+e^-

• Confirmed by BaBar @ $\sqrt{s} \sim 10.6$ GeV (PRD 90,052003 (2014); PRD 92,111101(R)(2015) for KK and $K\pi$)

• Measured at BESIII @ $\sqrt{s} = 3.65$ GeV (PRL 116,42001(2016))

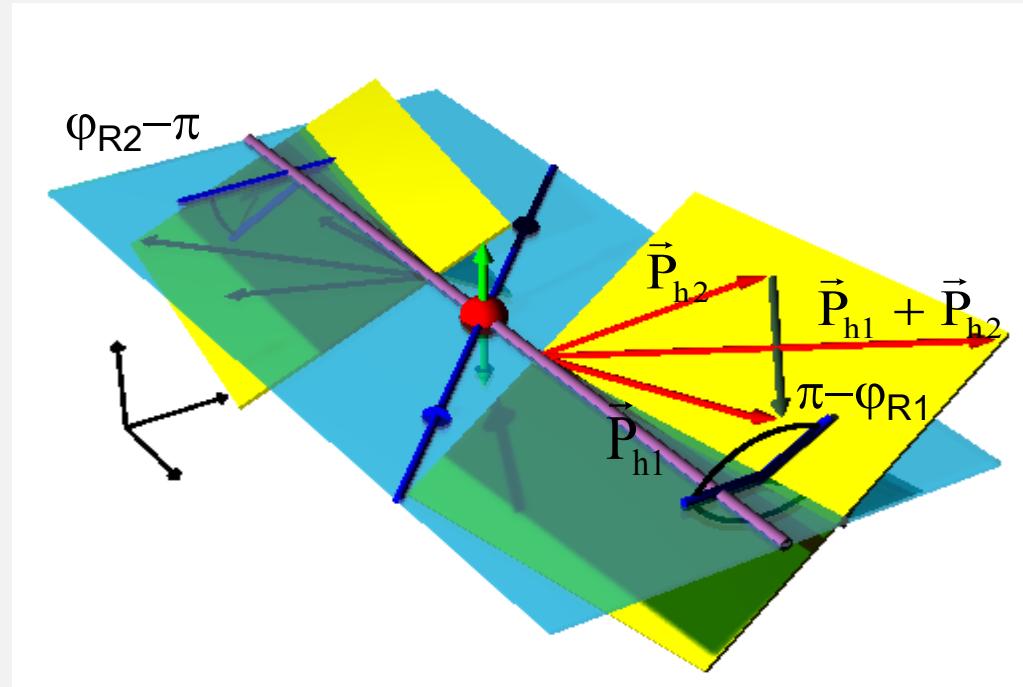
COLLINS EFFECT FOR KAON/PION PAIRS

Simultaneous measurement of KK, K π and $\pi\pi$ Collins asymmetries from BaBar data



- Rise of the asymmetry as a function of z :
- A_{12}^{UL} KK asymmetry slightly higher than pion asymmetry for high z
- KK asymmetry consistent with zero at lower z
- $\pi\pi$ asymmetries consistent with previous measurements (PRD90, 052003)

DI-HADRON ASYMMETRIES

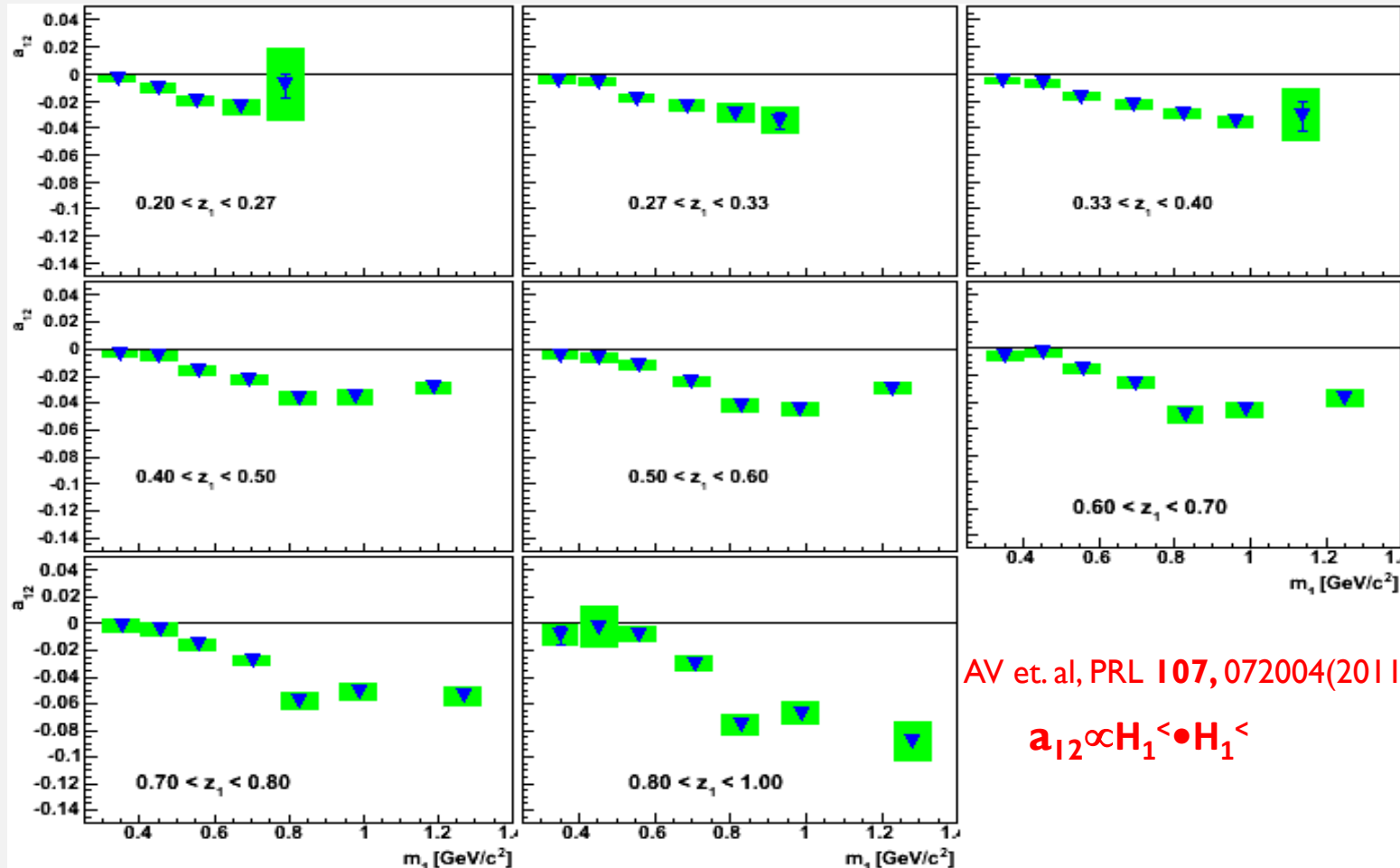


- Conceptually similar measurement as Collins with $\vec{P}_{h\perp} \leftrightarrow \vec{R}_\perp$
- Normalized cross section:

$$e^+e^- \rightarrow (h_1 h_2)(\overline{h_1} \overline{h_2}) + X \propto 1 + H_1^\perp \overline{H_1^\perp} \cos(\phi_{R1} + \phi_{R2}) + G_1^\perp \overline{G_1^\perp} \cos(2(\phi_{R1} - \phi_{R2}))$$
- See talks by Aram and Marco

Extraction of $\cos(\phi_{R_1} + \phi_{R_2})$

First measurement of Interference Fragmentation Function



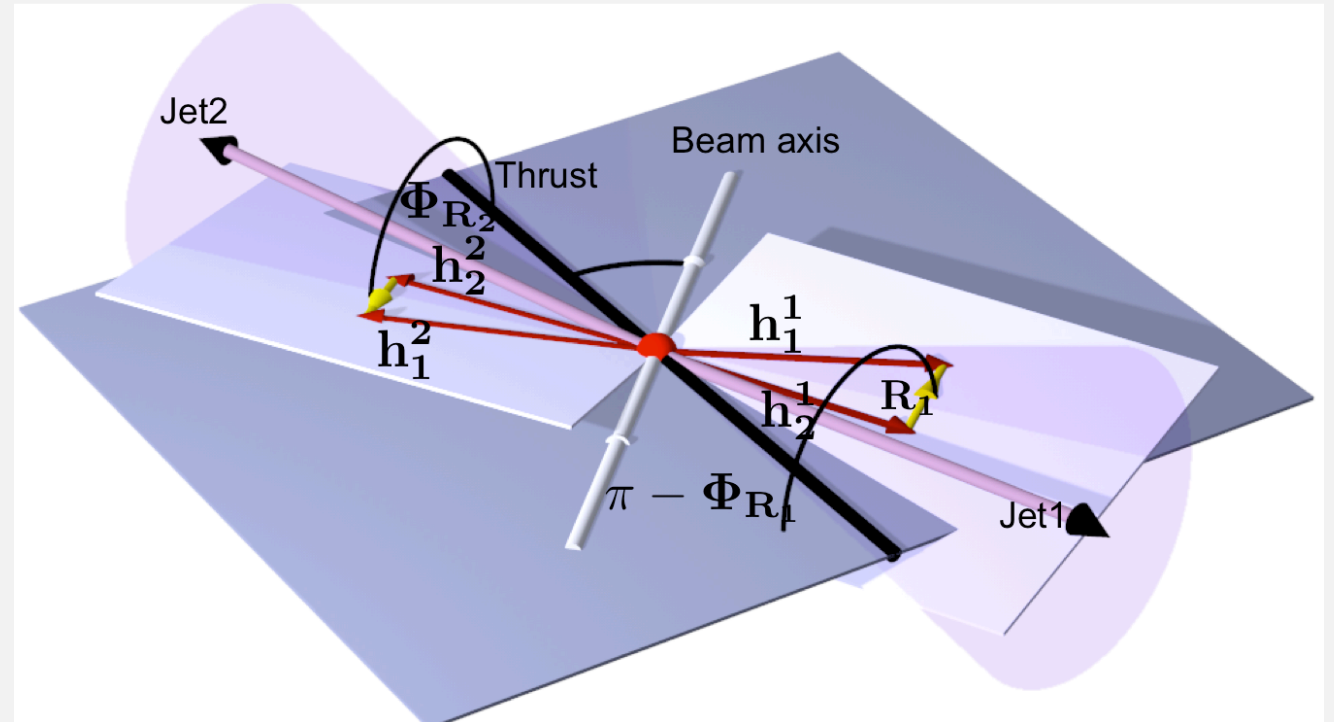
AV et. al, PRL **107**, 072004(2011)

$$a_{12} \propto H_1^{\leftarrow} \bullet H_1^{\leftarrow}$$

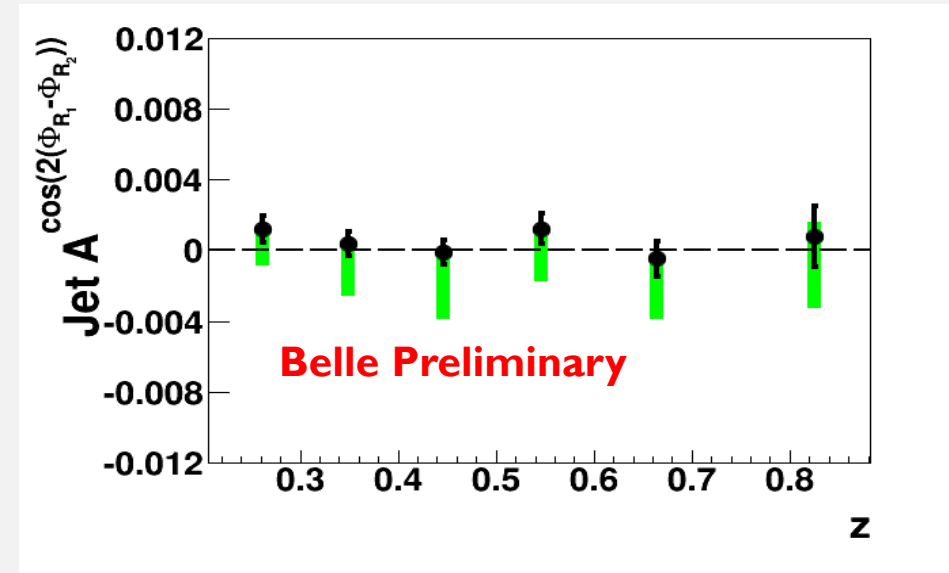
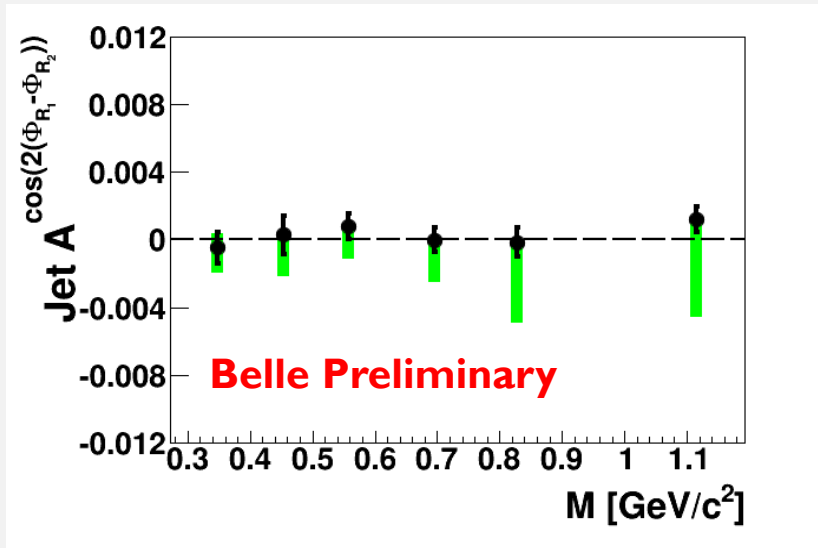
See Marco's talk about
Transversity extraction
From di-hadrons

NEW: USE JET RECONSTRUCTION AT BELLE

- Robust vs. final state radiation
- **De-correlate axis between hemispheres**
 - We use anti-kT algorithm implemented in fastjet
 - Cone radius $R=1.0$
 - Min energy per jet $2.75 \text{ GeV} \rightarrow$ suppress weak decays
- Only allow events with 2 jets passing energy cut (dijet events)
- Only particles that form the jet are
- Thrust cut of $0.8 < T < 0.95$



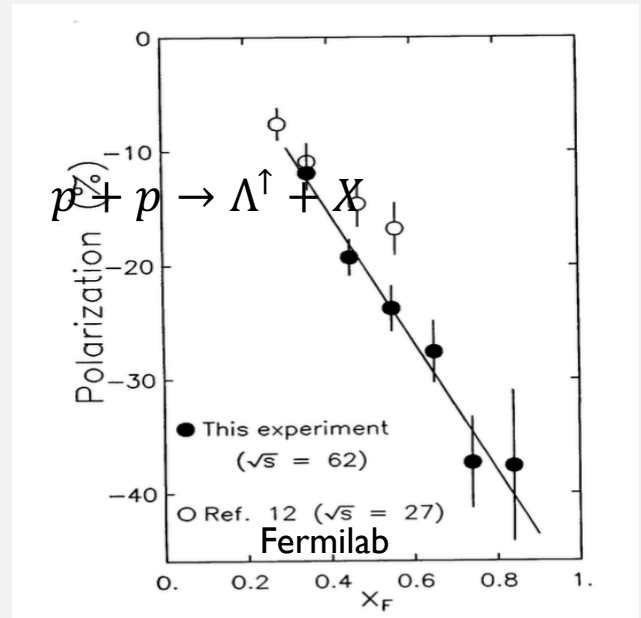
ASYMMETRIES FOR $\cos(2(\phi_{R1}-\phi_{R2}))$ ($G_{I\perp}$) SMALL



- No evidence of local p-odd effects yet
- Next step: partial wave analysis
- See recent NJL model calculations by Matevosyan et al.
 - \rightarrow GIT signal about half of IFF signal, produced by 'worm gear' splitting functions \sim gIT

POLARIZED HYPERON PRODUCTION

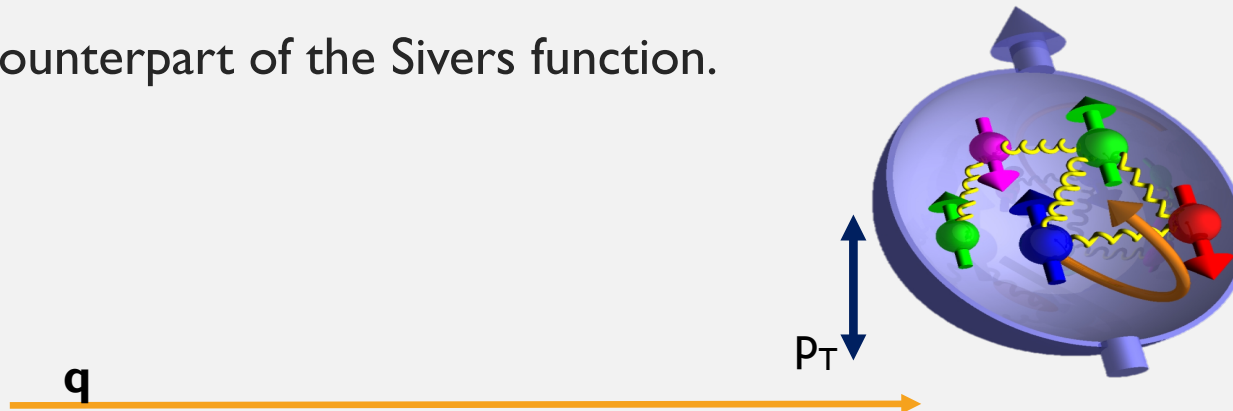
- Large Λ transverse polarization in unpolarized pp collision **PRL36, 1113 (1976); PRL41, 607 (1978)**
- Caused by polarizing FF $D_{1T}^\perp(z, p_\perp^2)$?
- Polarizing FF is chiral-even, has been proposed as a test of universality. **PRL105, 202001 (2010)**
- OPAL experiment at LEP has been looking at transverse Λ polarization, no significant signal was observed. **Eur. Phys. J. C2, 49 (1998)**
- FF counterpart of the Sivers function.



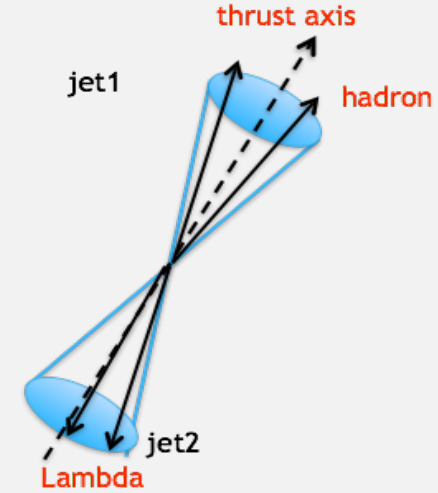
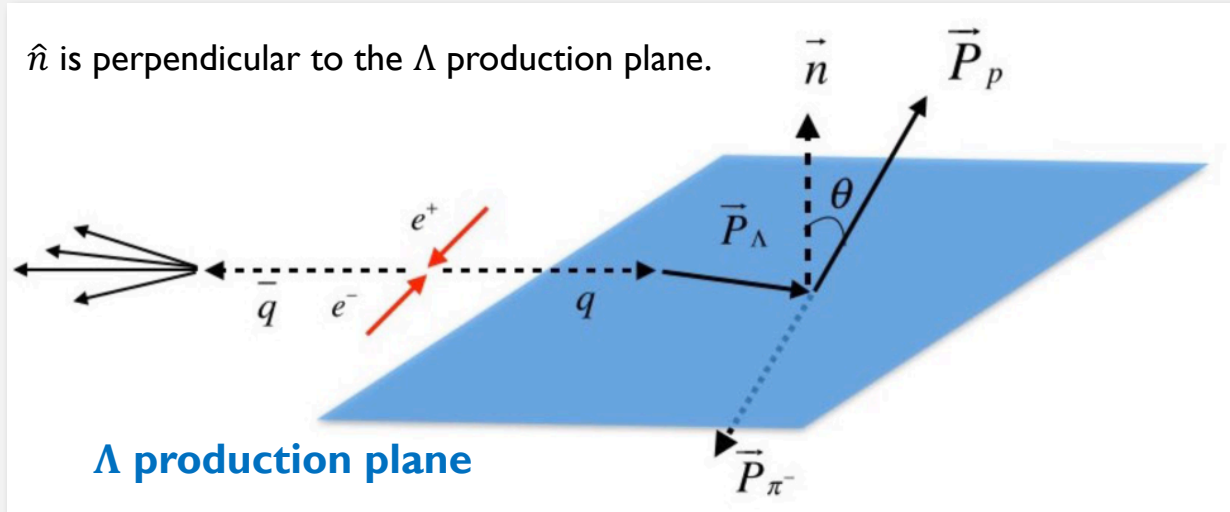
ISR data

(Phys.Lett. B185 (1987) 209)

$$x_F = p_L / \max p_L \sim LO x_1 - x_2 \sim_{forward} x_1$$



OBSERVABLES IN Λ RESTFRAME

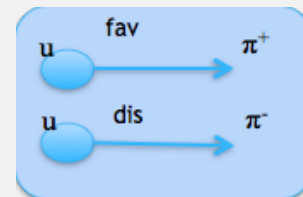
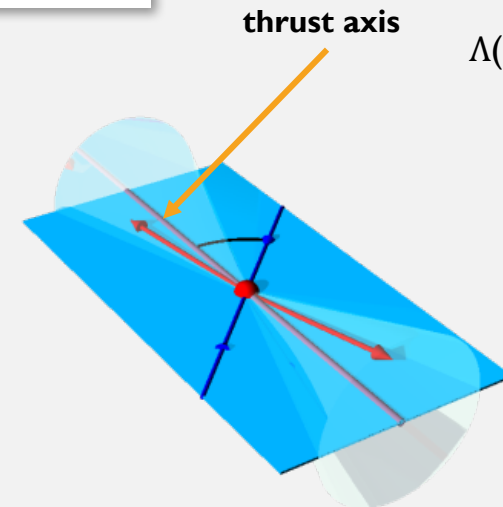


$\Lambda(u\bar{d}s); \pi^+(u\bar{d}); K^+(u\bar{s})$

- Self-analyzing decay leads to polarization dependent distribution

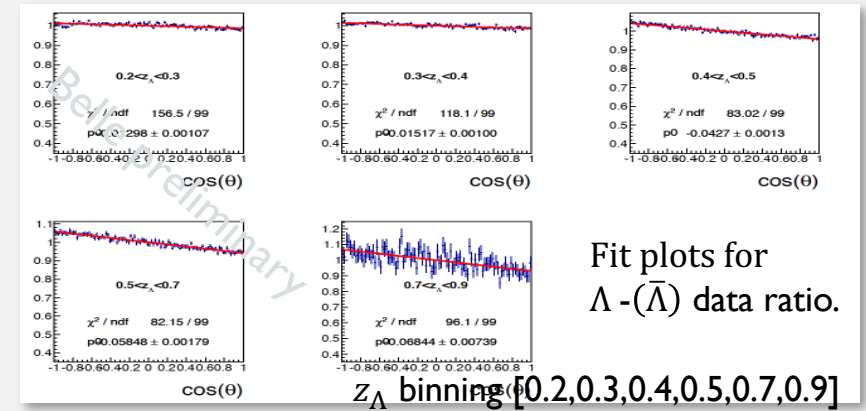
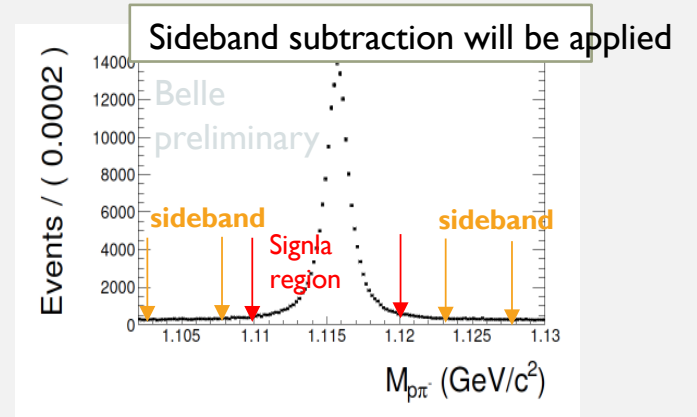
$$\frac{1}{N} \frac{dN}{d\cos\theta} = 1 + \alpha P \cos\theta$$

- where α is the decay parameter: $\alpha_+ = 0.642 \pm 0.013$ for Λ and $\alpha_- = -0.71 \pm 0.08$ for $\bar{\Lambda}$ (PDG).
- The p_t is measured as the transverse momentum of Λ relative to the **thrust axis**

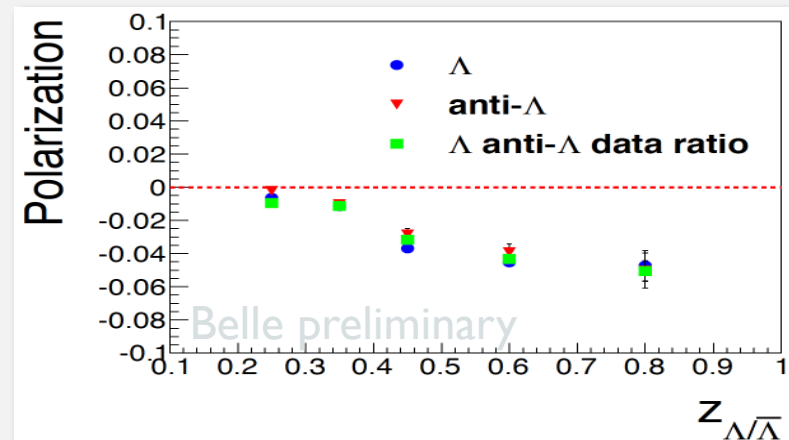


FITS AND POLARIZATION EXTRACTION

- Fit the acceptance corrected $\cos\theta$ distributions with $1 + p_0 \cos\theta$.
- The polarization of interest: p_0/α (decay constant)
- In the data ratio, polarization is obtained via $p_0/(\alpha_+ - \alpha_-)$.
- In data ratios, the slope on the $\cos\theta$ distributions are about two times larger than that in MC-corrected ratios, the $(\alpha_+ - \alpha_-)$ is also about two times larger than $\alpha_+(\alpha_-)$.
- Results from MC-corrected ratio and data ratio are consistent with each other.
- Nonzero polarization**, magnitude rises to about $\sim 5\%$ with $z_\Lambda = 2E_\Lambda/\sqrt{s}$.



Fit plots for $\Lambda - (\bar{\Lambda})$ data ratio.

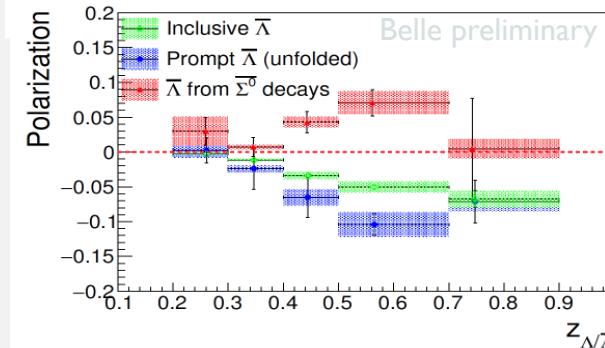
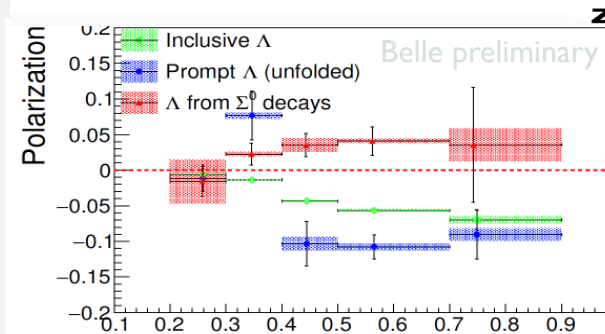
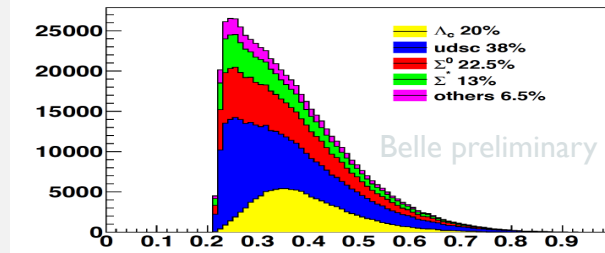


BACKGROUND UNFOLDING

- Σ^* decays to Λ strongly, is included in the signal.
- Feed-down from Σ^0 (22.5%), Λ_c (20%) decays need to be understood.
- The Σ^0 -enhanced ($\Sigma^0 \rightarrow \Lambda + \gamma$) ($\text{Br} \sim 100\%$). and Λ_c -enhanced ($\Lambda_c \rightarrow \Lambda + \pi^+$) ($\text{Br} \sim 1.07\%$) data sets are selected and studied.
- The measured polarization can be expressed as:

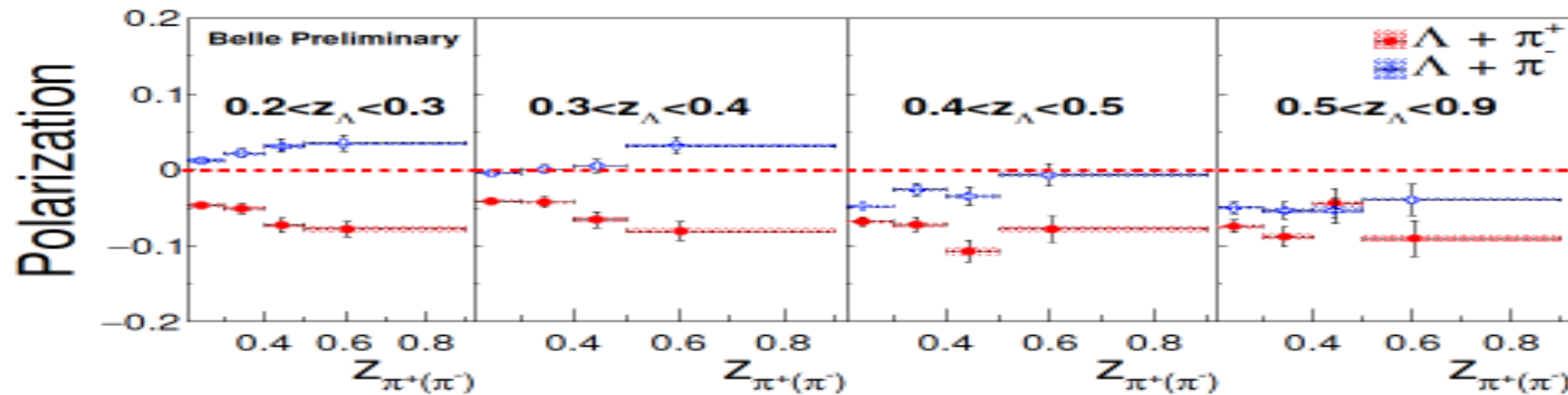
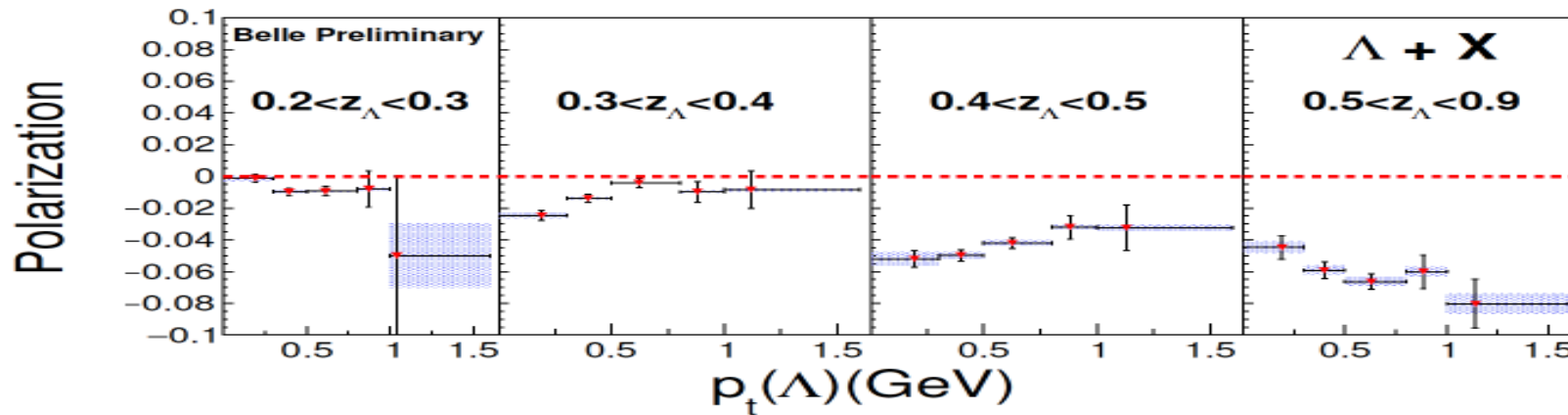
$$P^{mea.} = (1 - \sum_i F_i) P^{true} + \sum_i F_i P_i,$$

- F_i is the fraction of feed-down component i , estimated from MC. P_i is polarization of component i .
- Polarization of Λ from Σ^0 decays is found has opposite sign with that of inclusive Λ .



R. Gatto, Phys. Rev. 109, 610 (1958); Phys.Lett.B303,350(1993)

Z_Λ , P_T DEPENDENCE OF OBSERVED Λ POLARIZATION



- Polarization rises with p_t in the lowest z_Λ and highest z_Λ bin. But the dependence reverses around 1 GeV in the intermediate z_Λ bins \rightarrow **Unexpected!** (might be related to fragmenting quark flavor dependence on z_1, z_2)
- Correlation with opposite hemisphere light meson \rightarrow quark flav/charge dependence
 - Sign of asymmetry dependent on quark charge cf Sivars

KEKB → SUPERKEKB: DELIVER INSTANTANEOUS LUMI X 40

e^+ 4GeV 3.6 A

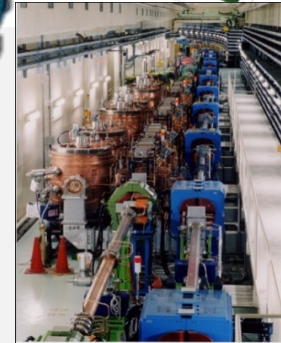
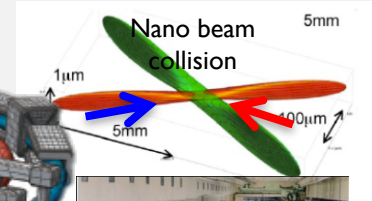
e^- 7GeV 2.6 A

(~2x KEBK)

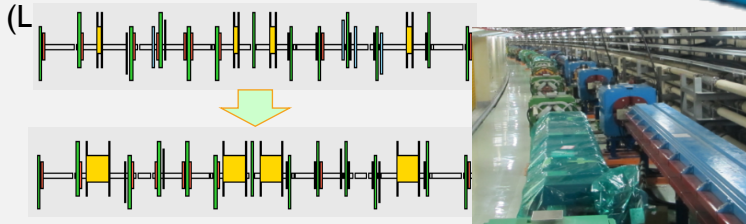
Belle II

New superconducting final focusing quads (QCS) near the IP

SuperKEKB
Target: $L = 8 \times 10^{35} / \text{cm}^2 / \text{s}$



Replace short dipoles with longer ones



Redesign the lattices of HER & LER to squeeze the emittance

TiN-coated beam pipe with antechambers
Cu for wigglers and Al alloy for the rest



Reinforce RF systems for higher beam current

Positron source
New positron target / capture section

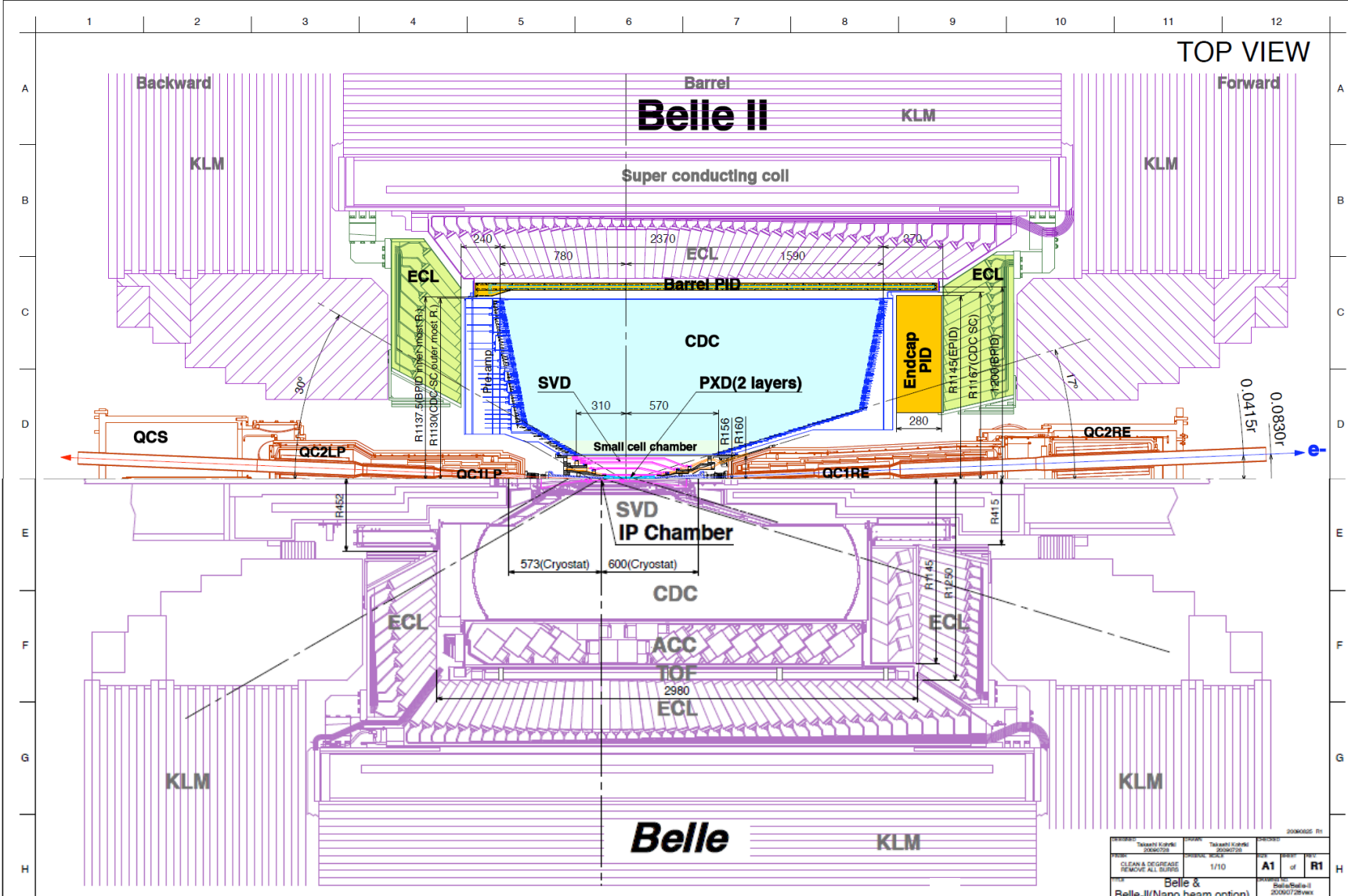
Damping ring (new)

@1.1 GeV
To inject low emittance positrons

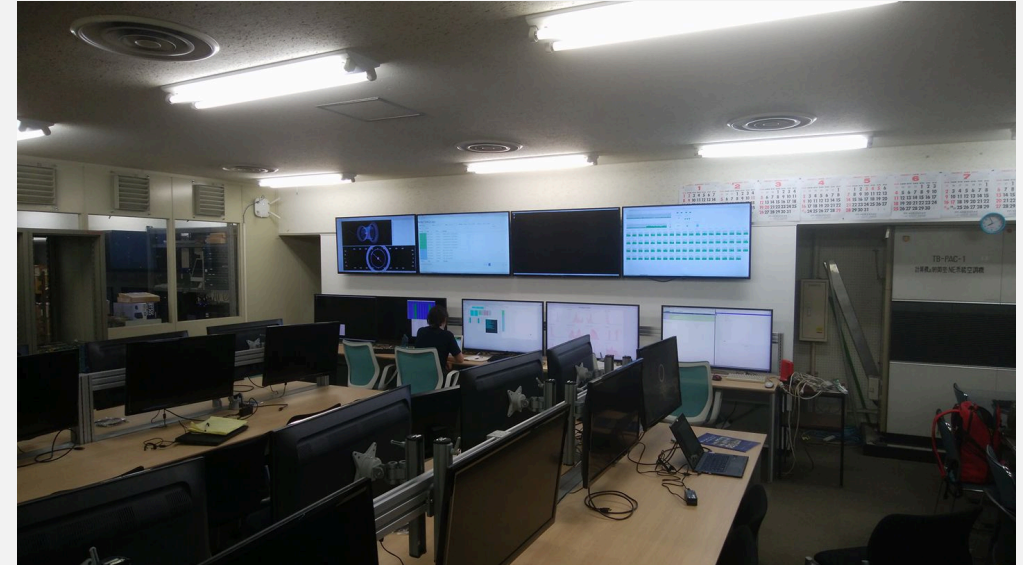
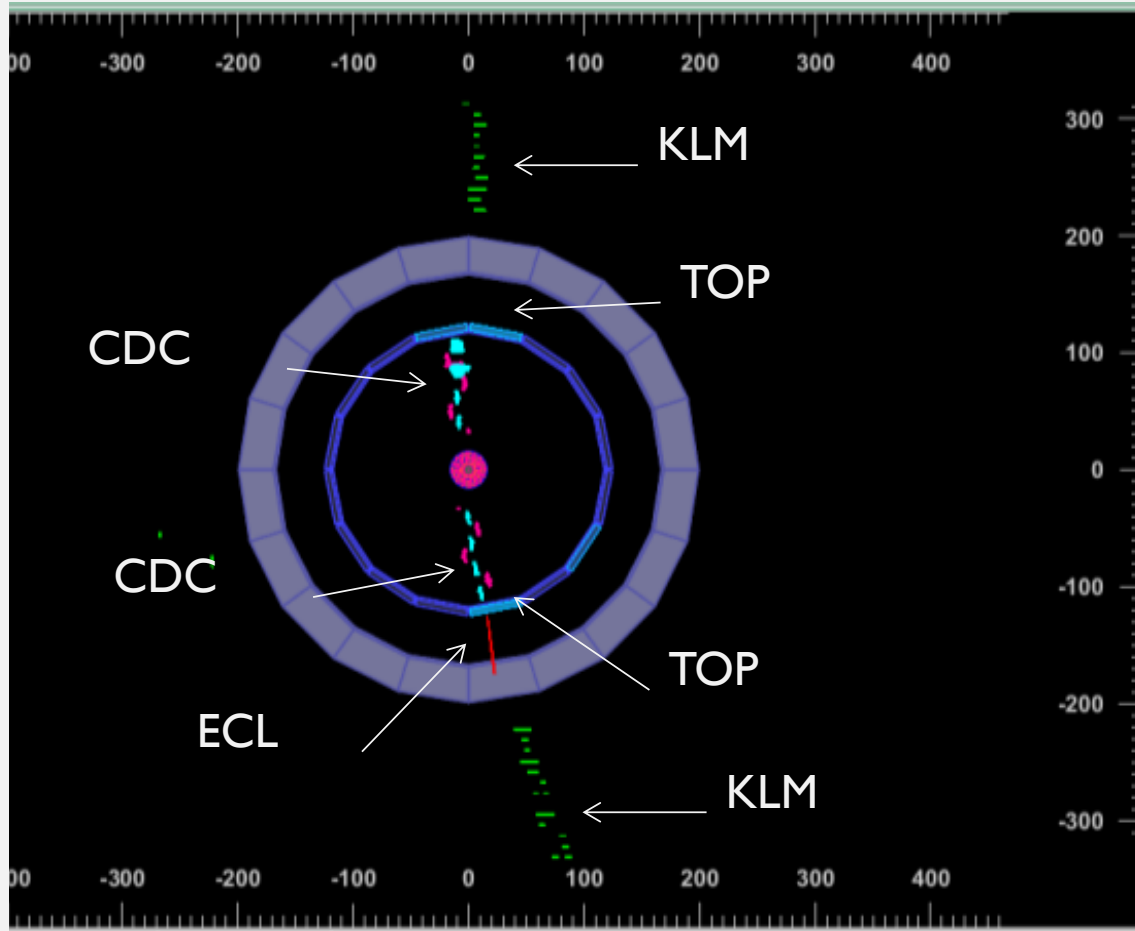
Low emittance gun
To inject low emittance electrons

$$L = \frac{\gamma_{\pm}}{2e r_e} \left(1 + \frac{\sigma_y^*}{\sigma_x^*} \frac{I_{\pm} \xi_{\pm y}}{\beta^*} \frac{R_L}{R_y} \right)$$

BELLE II DETECTOR (COMP. TO BELLE)



READOUT INTEGRATION

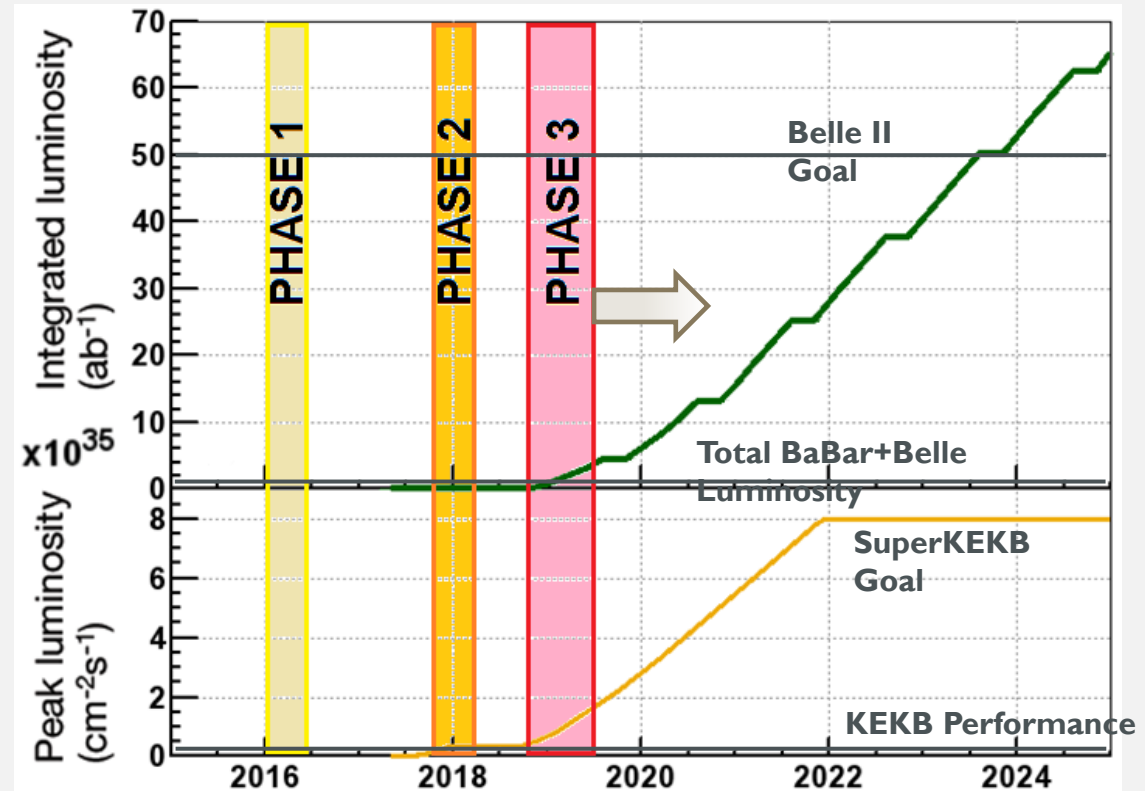


Belle II Control Room

- Readout integration of installed sub-detectors and central DAQ is in progress.
- Combined data taking established in cosmic running

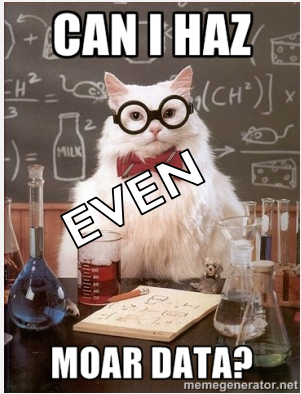
CURRENT STATUS AND SCHEDULE

- Phase I (complete)
 - Accelerator commissioning
- Phase 2 (early 2018)
 - First collisions ($20 \pm 20 \text{ fb}^{-1}$)
 - Partial detector
 - Background study
 - Physics possible
- Phase 3 (“Run I”, early 2019)
 - Nominal Belle II start
- **Ultimate goal: 50 ab^{-1}**



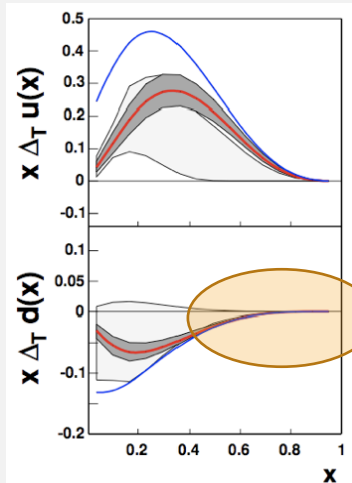
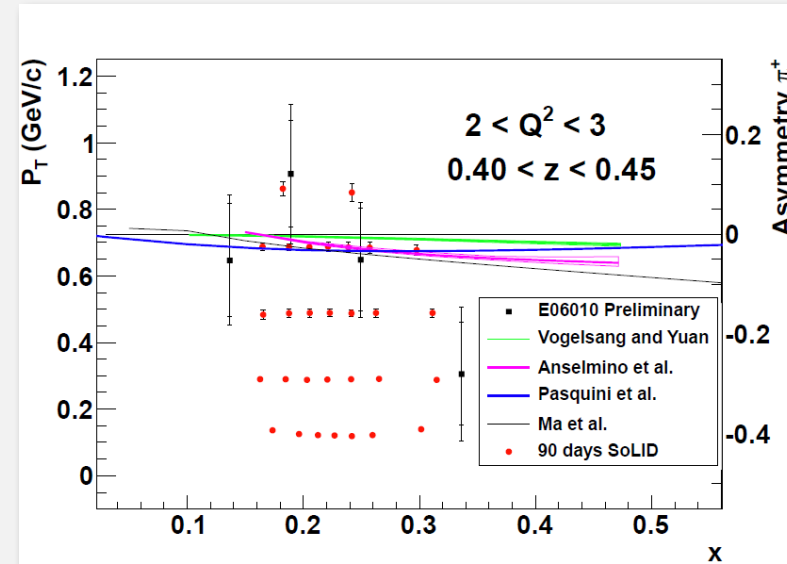
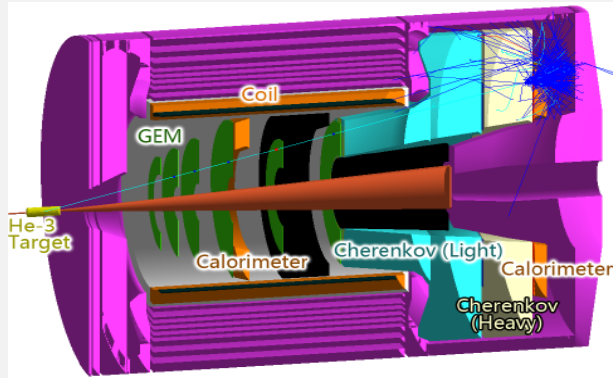
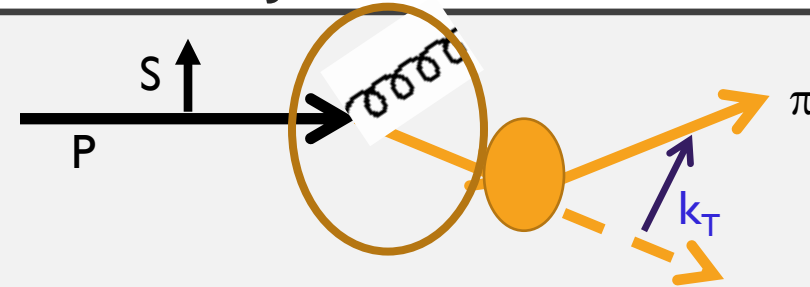
- **Search for New Physics via precision measurements**
 - CPV, (semi-)leptonic/penguin decays, LFV, dark sector, ...

FF PROGRAM AT BELLE II



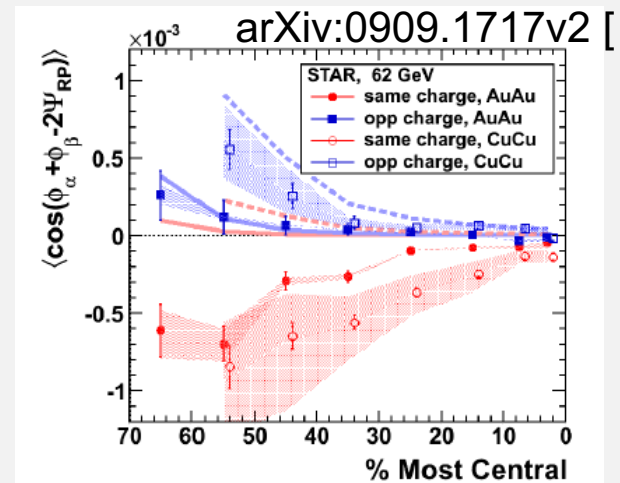
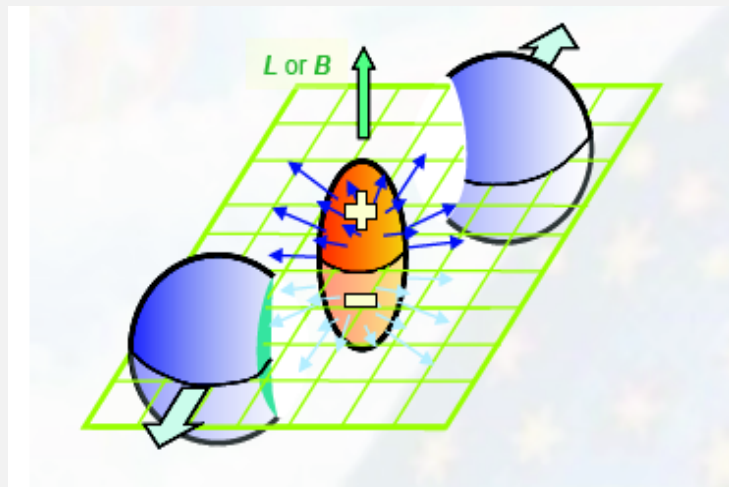
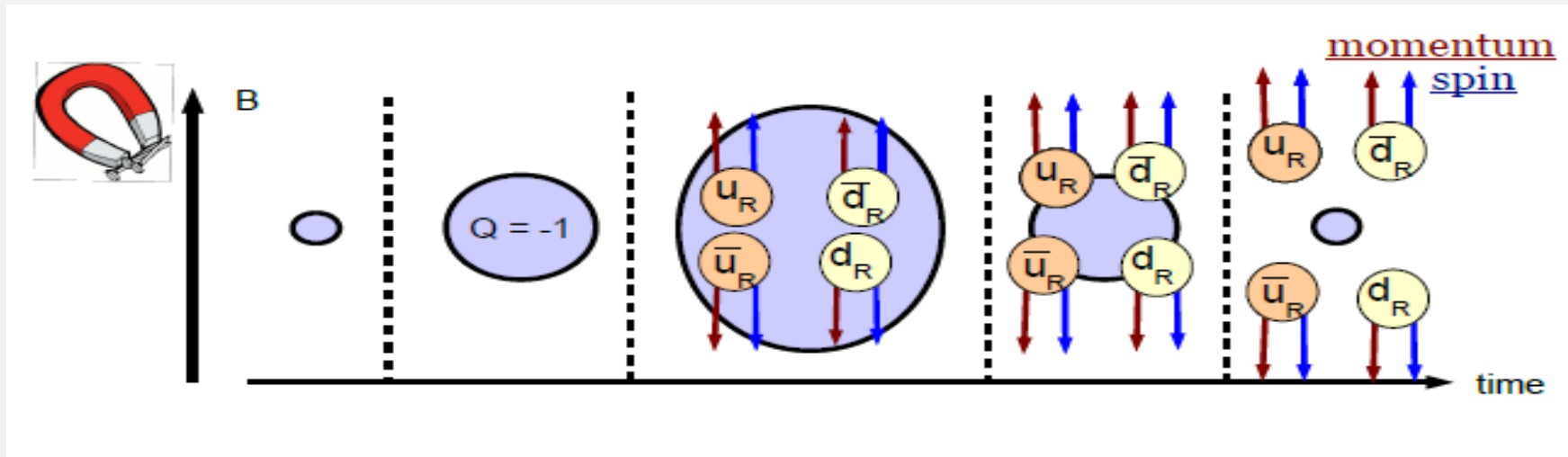
- High Precision measurements of spin dependent Fragmentation Functions
 - Precision back-to-back correlations of less copious hadrons (e.g. Λ)
 - Precision should be on par with anticipated SIDIS data from JLab I2
 - LPV effects in high multiplicity events helped by statistics and increased acceptance for low multiplicity tracks
- State of the Art Detector
 - PID: increase efficiency of e.g. multi kaon final states
 - Vertexing: More efficient charm rejection for FF studies
 - Reduce systematics (in particular charm) and improve PID

TRANSVERSITY AT HIGH X FROM POLARIZED HE3 AT SOLID WITH 12 GEV UPGRADE AT JLAB

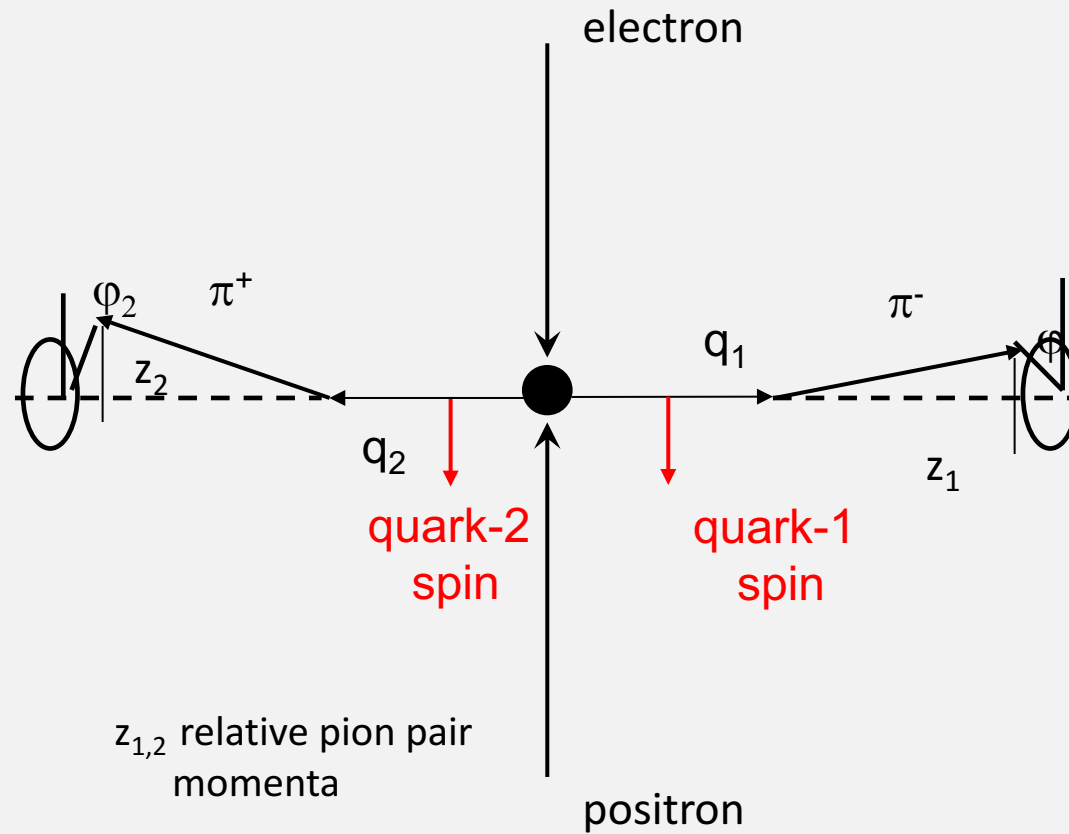


- Precise measurement of p_T dependent Collins effect
- Needs precise measurement of Collins and spin averaged p_T dependent fragmentation functions!

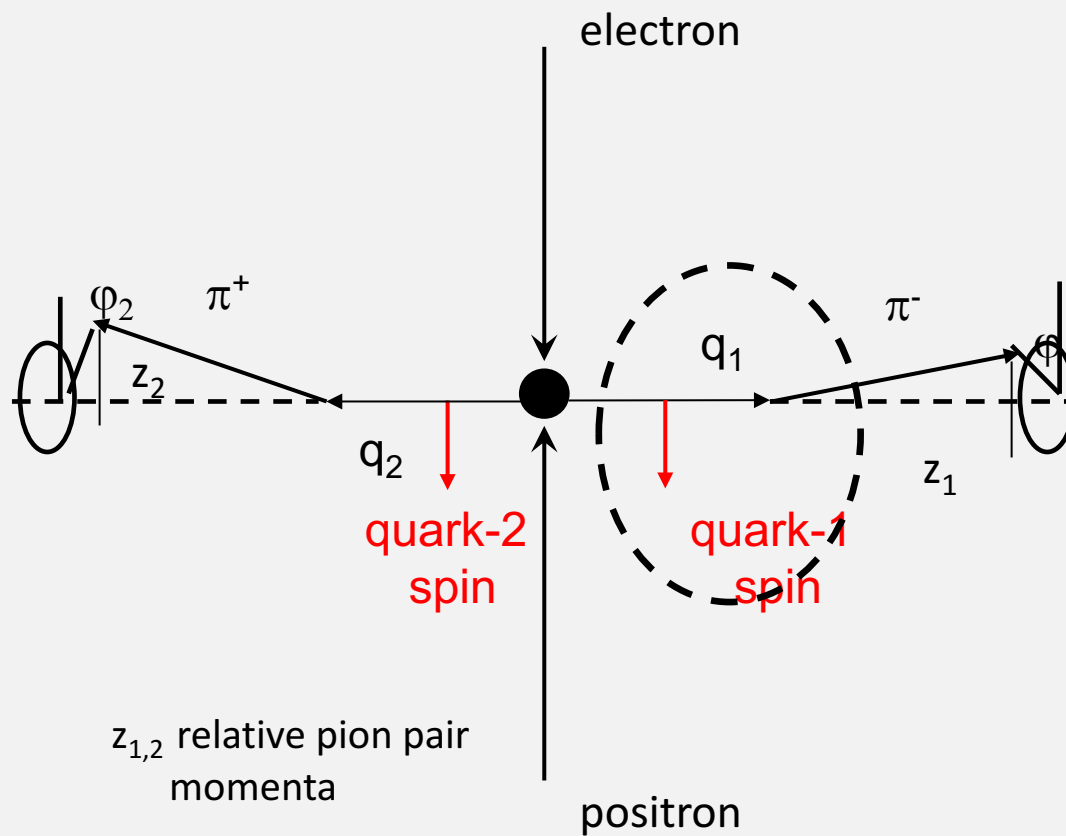
QCD VACUUM TRANSITIONS CARRY CHIRALITY



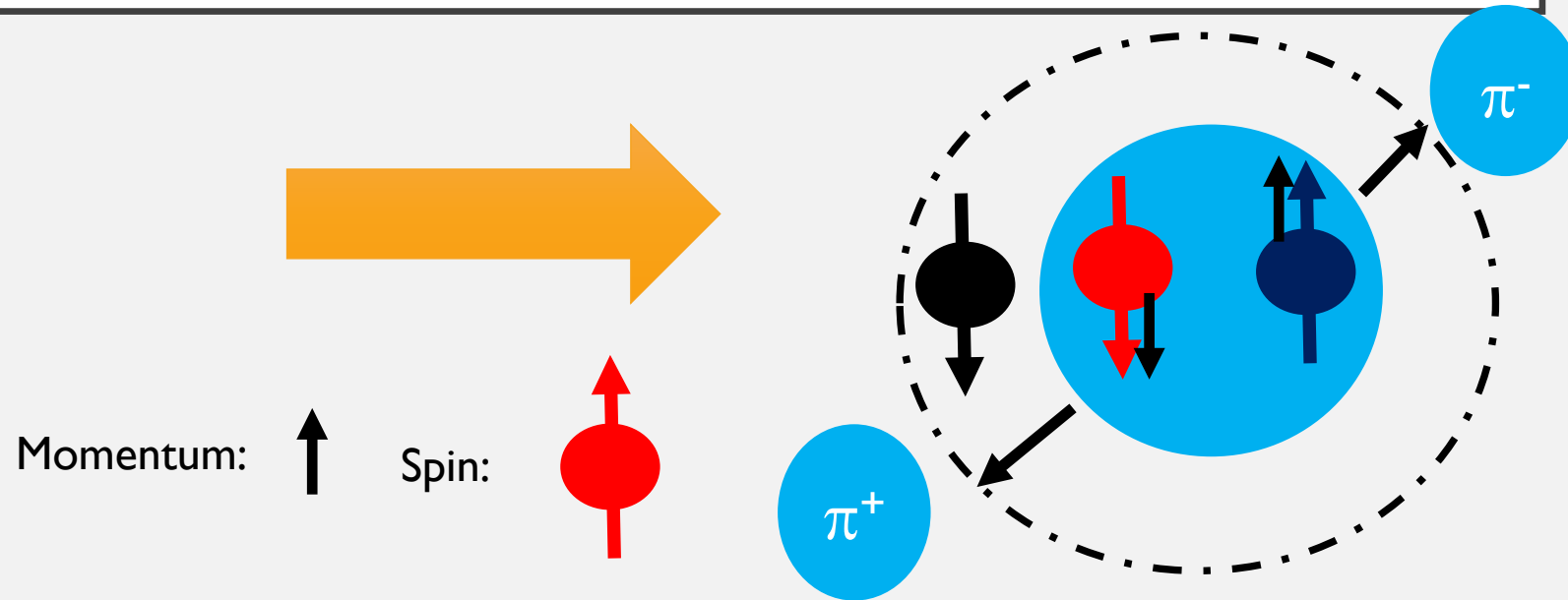
Kharzeev, McLerran and Warringa, arXiv:0711.0950,
 Fukushima, Kharzeev and Warringa, arXiv:0808.3382



$$\sigma \propto H_1^\perp(z_1) \bar{H}_1^\perp(z_2) \cos(\phi_1 + \phi_2) + C$$

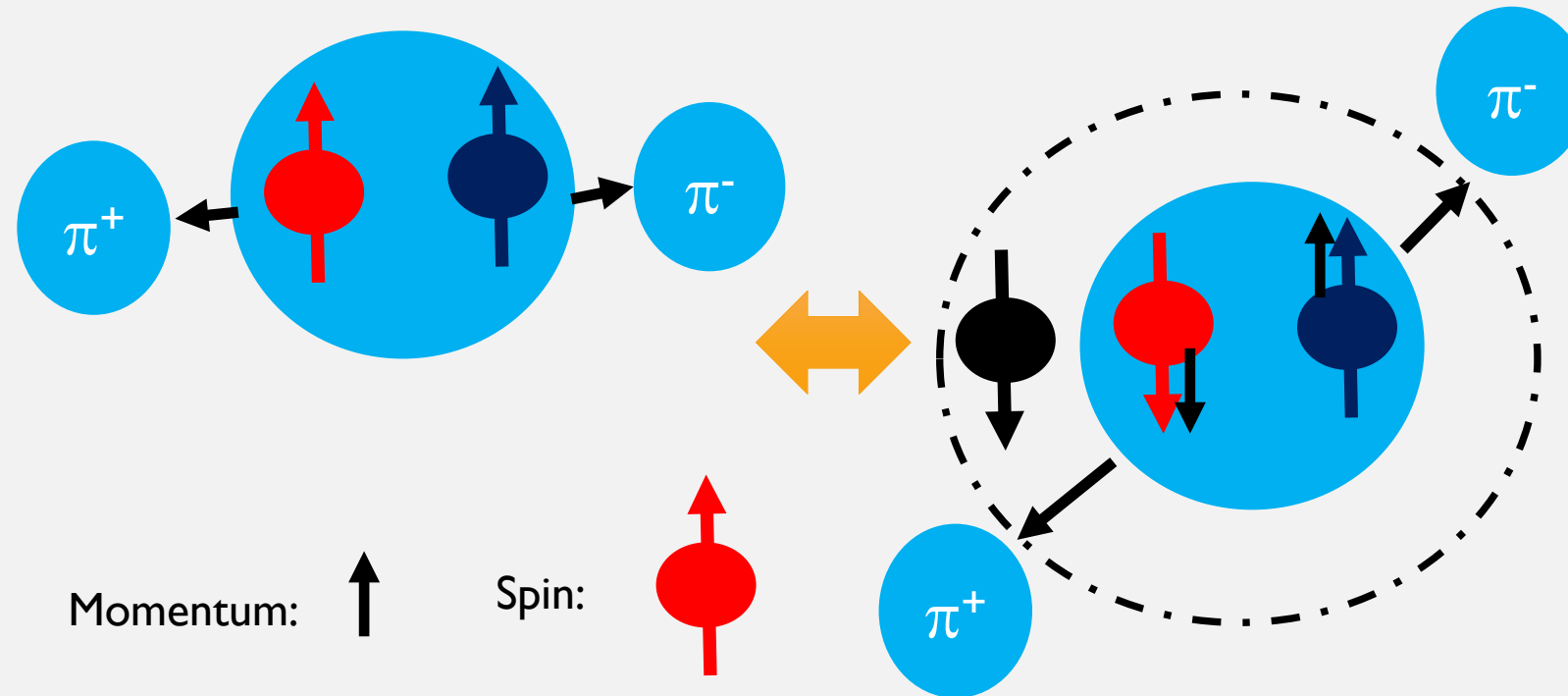


$$\sigma \propto H_1^\perp(z_1) \bar{H}_1^\perp(z_2) \cos(\phi_1 + \phi_2) + C$$



- Fragmentation in P-odd bubble leads spin-momentum correlation
- Difference in 'Winding number' gives effective increment in chirality
- Spin alignment via chromomagnetic-electric effect \rightarrow FF \tilde{H}_1

MIX OF P-ODD FF WITH COLLINS FF LEADS TO EVENT-BY-EVENT ASYMMETRY

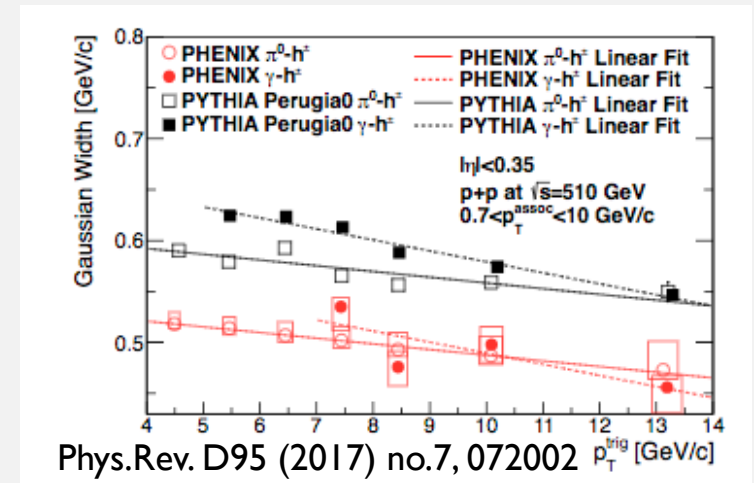
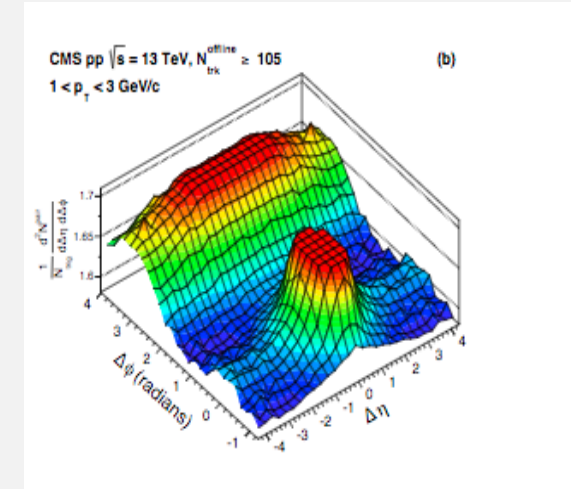


- Fragmentation in P-odd bubble leads spin-momentum correlation (both fragmenting quarks in the ‘bubble’ → G_1^\perp /jet handedness like effect (but conserving parity))
- Difference in ‘Winding number’ gives effective increment in chirality
- Spin alignment via chromomagnetic-electric effect
- Azimuthal **event by event** modulation → **$\sin(\phi_1 + \phi_2)$ modulation**
→ **needs large dataset of high multiplicity events** → **Belle II**
- See Kang, Kharzeev, Phys.Rev.Lett. 106 (2011) 042001

E+E- AS A BASELINE FOR HADRONIC COLLISIONS

Acta Phys.Polon.Supp. 9 (2016) 207-211

- Beyond pQCD there are new phenomena emerging in hadronic collisions
 - Ridge in high multiplicity hadronic collisions
 - pT broadening in back-to-back production
 - ...
- e+e- can provide baseline
- More statistics needed to select e.g. high multiplicity events

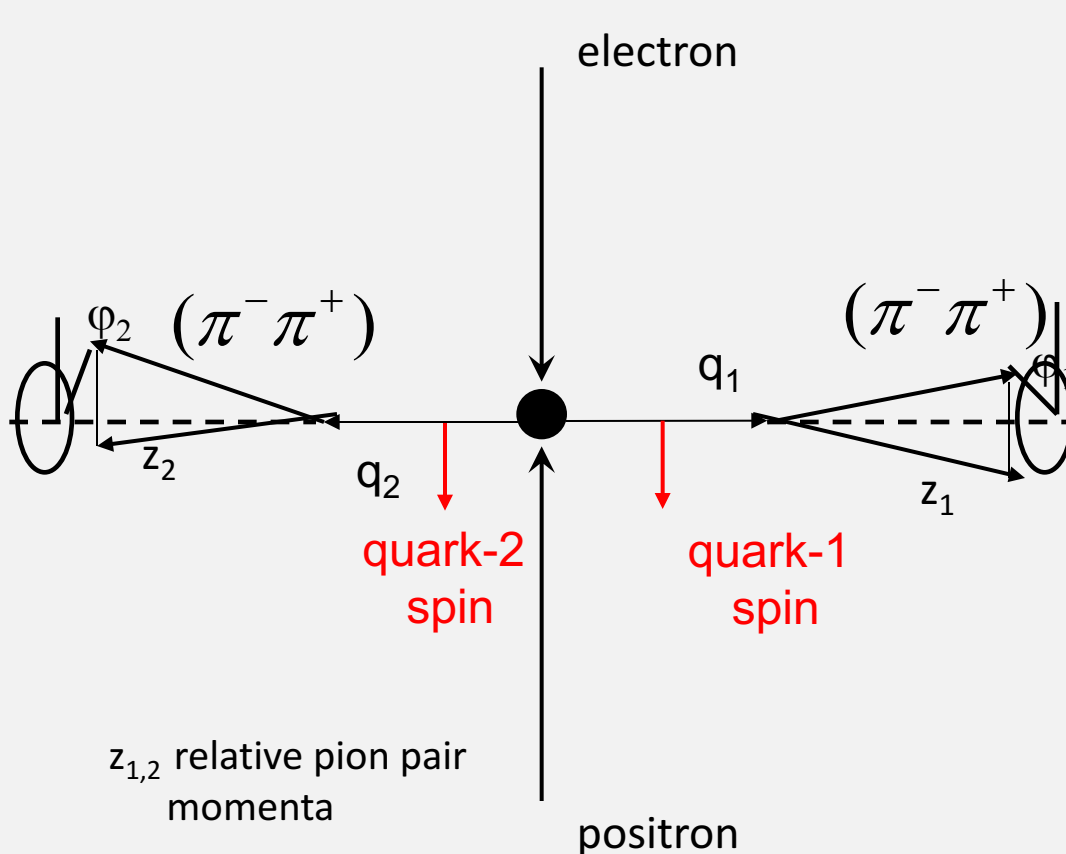


SUMMARY

- **FF programs at Belle, BaBar and BES III has provided key measurements leading to new insights into the spin structure of the nucleon and QCD in general!**
- Results on the horizon include p_T dependence of D_1 , Collins FF for η, π^0
- Belle II will start data taking next year and will quickly surpass Belle data with superior data quality
 - High statistics, multidimensional extraction of $H_1^{\perp h/q}$, LPV effects in high multiplicity events ...
 - Quantification of the impact of precision FF measurements on Jlab12 and EIC program would be helpful to bolster FF program at Belle II



Measuring transverse spin dependent di-Hadron Correlations In unpolarized e^+e^- Annihilation into Quarks



Interference effect in e^+e^- quark fragmentation will lead to azimuthal asymmetries in di-hadron correlation measurements!

Experimental requirements:

- Small asymmetries \rightarrow very large data sample!
- Good particle ID to high momenta.
- Hermetic detector

$$A \propto H_1^\perp(z_1, m_1) \bar{H}_1^\perp(z_2, m_2) \cos(\phi_1 + \phi_2)$$

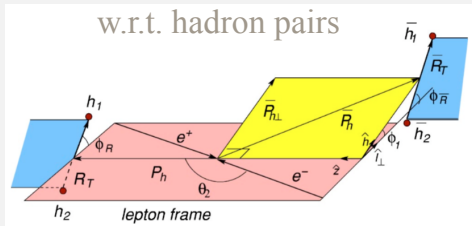


Di-hadron Fragmentation Functions

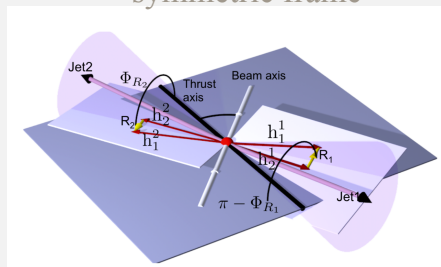
Starting from the fully integrated e^+e^- cross section into four unpolarized hadrons with two leading hadrons in each jet, authors of ref. PRD67, 094003 explicitly derive the asymmetry:

$$A(y, z, \bar{z}, M_h^2 \bar{M}_h^2) = \frac{\langle \cos(2(\phi_R - \phi_{\bar{R}})) \rangle}{\langle 1 \rangle} = \frac{\sum_{a, \bar{a}} e_a^2 \frac{3\alpha^2}{2Q^2} z^2 \bar{z}^2 A(y) \frac{1}{M_1 M_2 \bar{M}_1 \bar{M}_2} G_1^{\perp a}(z, M_h^2) \bar{G}^{\perp a}(\bar{z}, \bar{M}_h^2)}{\sum_{a, \bar{a}} e_a^2 \frac{6\alpha^2}{Q^2} A(y) z^2 \bar{z}^2 D_1^a(z, M_h^2) \bar{D}_1^a(\bar{z}, \bar{M}_h^2)}$$

PRD67,094003
asymmetric frame
w.r.t. hadron pairs



arXiv:1505.08020
symmetric frame



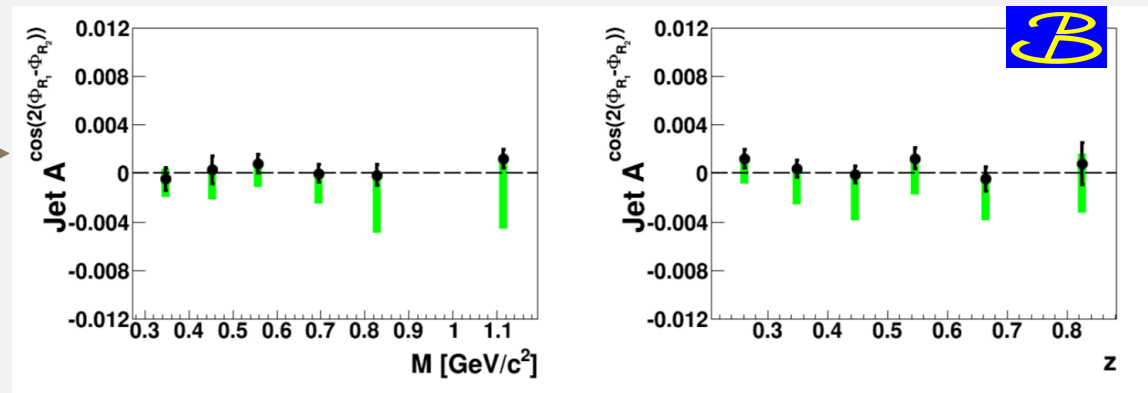
- longitudinally polarized quark IFF G_1^\perp
- chiral-even function related to the jet handedness
- asymmetric reference frame
- experimentally: switch to a symmetric frame
 - Belle preliminary: arXiv:1505.08020
 - angles are computed using the jet axis of di-jet event
 - jet axes reconstructed using anti-kT jet algorithm JHEP0804, 063

Two-dimensional χ^2 fit is performed to the normalized di-pion pairs:

$$1 + A^{\cos(\phi_{R1} + \phi_{R2})} \cos(\phi_{R1} + \phi_{R2}) + A^{\cos(2(\phi_{R1} - \phi_{R2}))} \cos(2(\phi_{R1} - \phi_{R2}))$$

NO SIGNAL observed at Belle

BUT more investigations about the thrust axis method and jet-axes reconstruction are needed



Summary and Conclusions

- Spin-dependent fragmentation functions provide key informations for understanding the hadronic structure and can also be used as a tool for the extraction of parton distribution functions
- e^+e^- annihilation experiments offer the ideal conditions to access FFs

one hadron FF	without k_T	with k_T
spin-0	D_1	H_1^\perp
spin-1/2	D_1, G_1, H_1	$D_{1T}^\perp, H_1^\perp, G_{1T}, H_{1L}^\perp, H_{1L}^\perp$
spin-1	$D_1, D_{1LL}, G_1, H_1, H_{1LT}$	$D_{1T}^\perp, H_1^\perp, G_{1T}, H_{1L}^\perp, H_{1L}^\perp, D_{1T}^\perp, D_{1LT}, D_{1TT}, G_{1LT}, G_{1TT}, H_{1LL}^\perp, H'_{1LT}, H_{1LT}^\perp$
two hadrons FF	without k_T	with k_T
spin-0	D_1, H_1^\perp	G_1^\perp, H_1^\perp

higher twist
T-odd

OTHER PROCESSES NEEDED FOR FLAVOR SEPARATION AND GLUON FF

- e^+e^-
 - back-to-back: flavor and p_T dependence
- SIDIS
 - Inclusive hadrons

$$2F_1^h(x, z, Q^2) = \sum_a e_q^2 \left(f_1^{q/p} D_1^{h/q} + \frac{\alpha_s(Q^2)}{2\pi} \left(f_1^{q/p} \otimes C_1^{qq} \otimes D_1^{h/q} \right. \right.$$

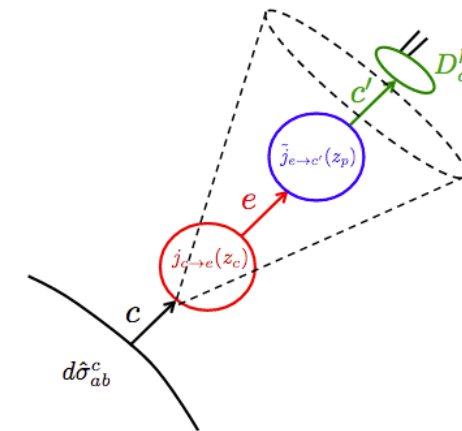
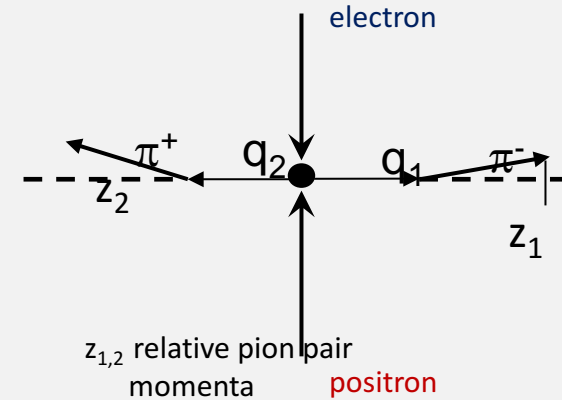
$$\left. \left. + f_1^{q/p} \otimes C_1^{gq} \otimes D_1^{h/g} + f_1^{g/p} \otimes C_1^{qg} \otimes D_1^{h/q} \right) \right|$$

- pp
 - Inclusive

$$\frac{d^3 \sigma^{pp \rightarrow (h, \text{jet}) X}}{dP_T^{\text{jet}} d\eta^{\text{jet}} dz} \propto \sum_{i,j,k} f_1^{i/p_a}(x_a) \otimes f_1^{j/p_b}(x_b) \otimes \hat{\sigma}^{ij \rightarrow k \text{jet}} \otimes D_1^{h/p_k}\left(\frac{z}{z_k}\right)$$

- h-h, Jet-hadron (back-to-back)
- γ -hadron (back-to-back)
- Hadron in jet

$$\frac{E_h d^3 \sigma^{pp \rightarrow hX}}{d^3 P_h} = \sum_{i,j,k,l} \int \frac{dx_a}{x_a} \int \frac{dx_b}{x_b} \int \frac{dz}{z^2} f_1^{i/p_a}(x_a) f_1^{j/p_b}(x_b) D_1^{h/k}(z) \hat{\sigma}^{ij \rightarrow kl} \delta(\hat{s} + \hat{t} + \hat{u}),$$



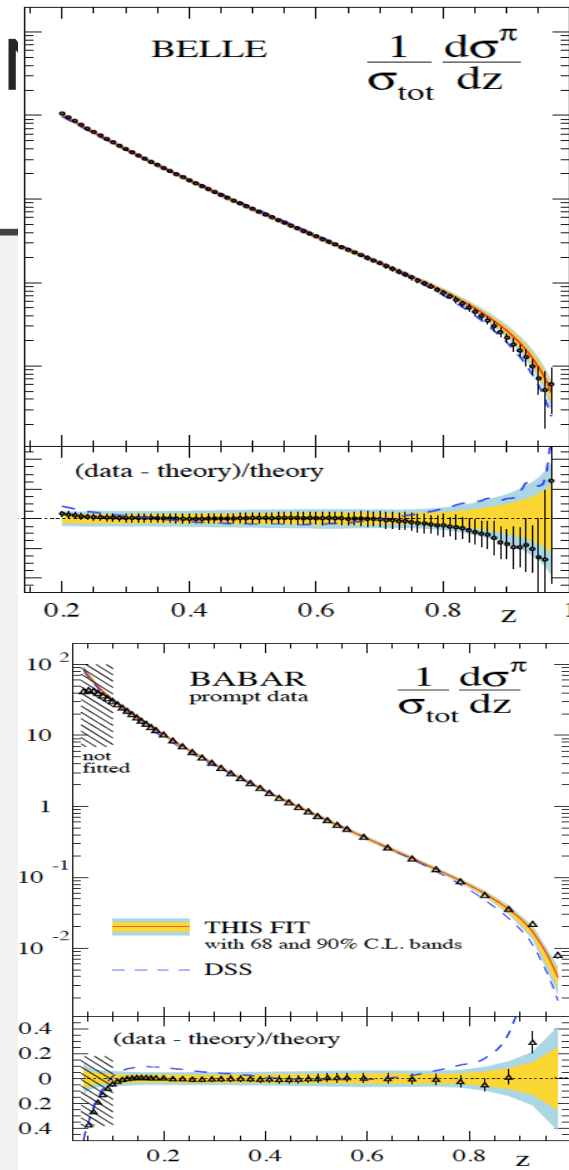
Kaufmann, Mukherjee, Vogelsang,
Phys.Rev. D92 (2015) no.5, 054015

ADVANTAGES OF E+E-

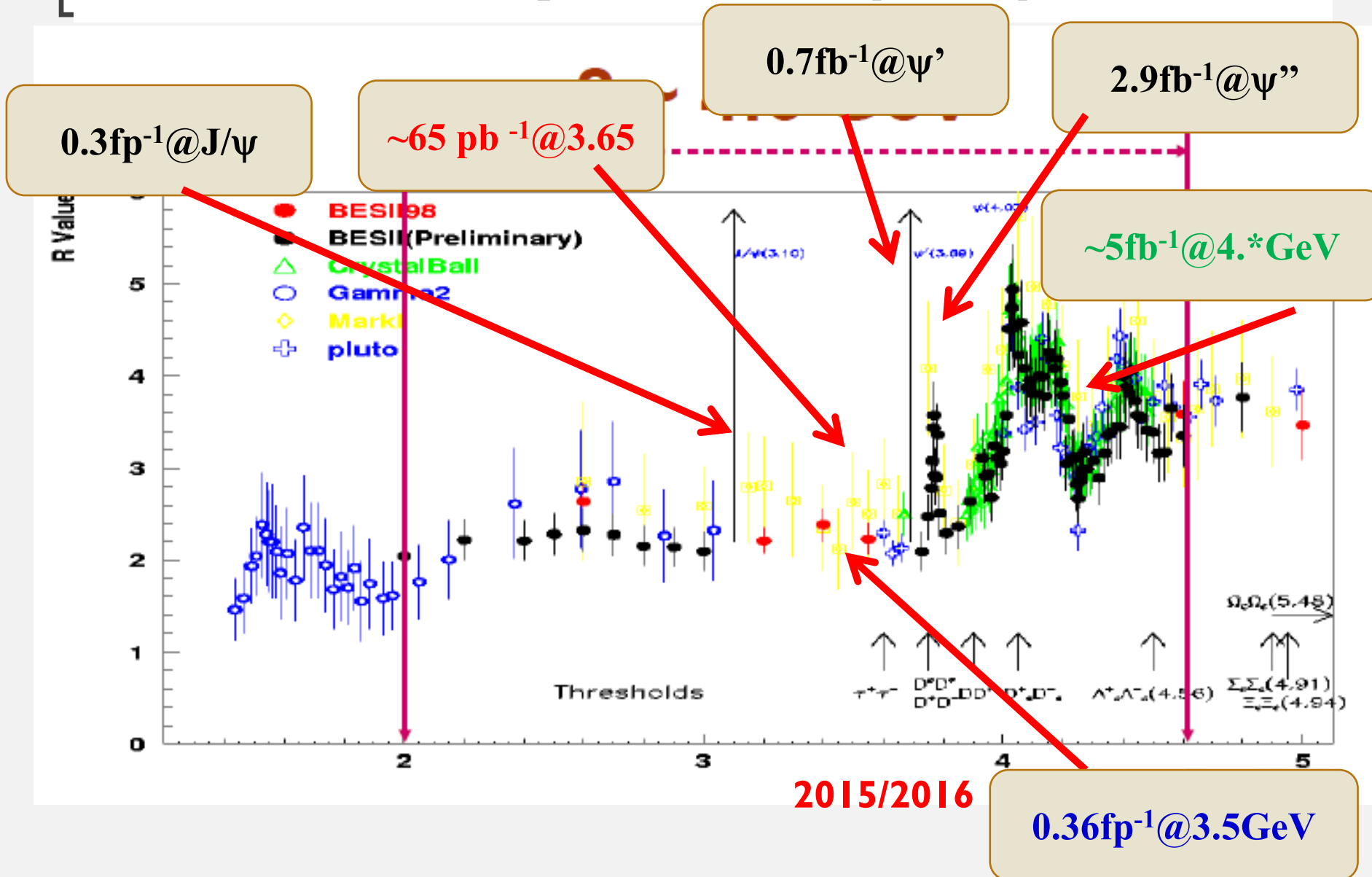
- Reconstruct complex final states (e.g. lambda) with feed-down contributions etc
- Correlations dependent on initial quark spin (not known if quark comes from proton)
- Correlations dependent on pT
- Null-test for back-to-back correlations in pp, HI collisions

COMPARE TO E+E-: AGREE GOOD

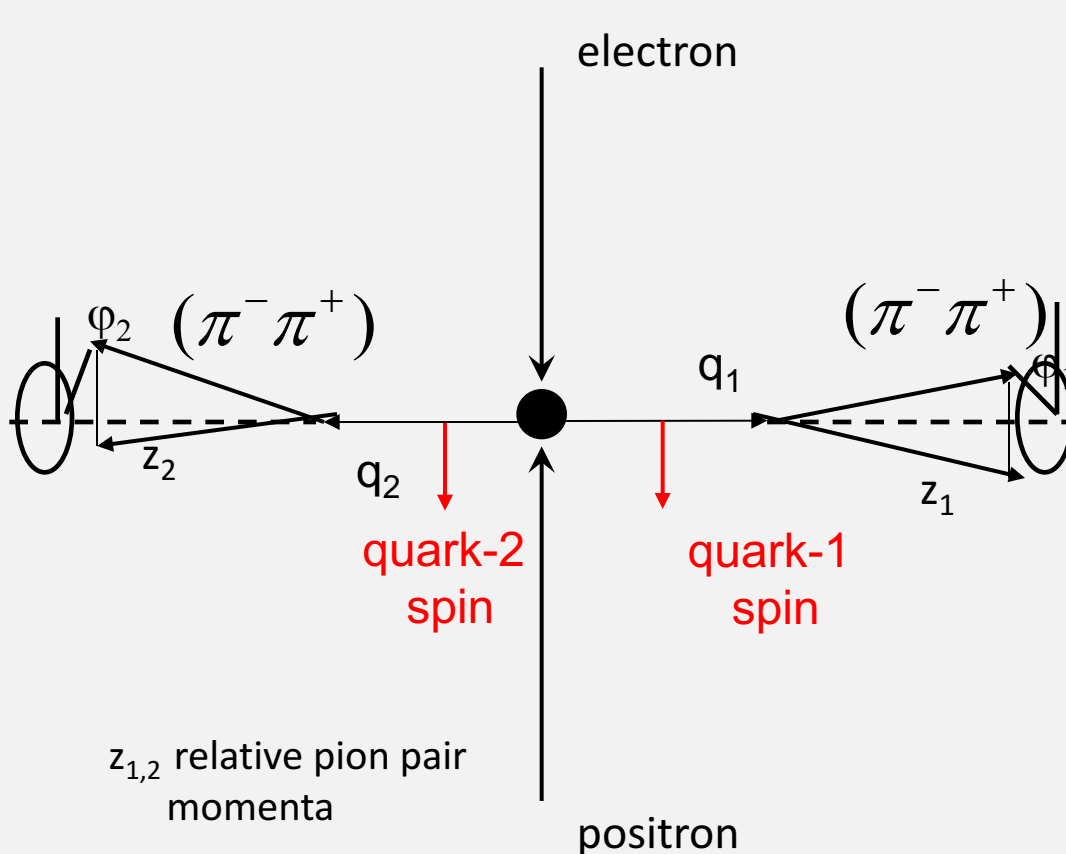
- Fit includes pp, SIDIS data and Babar eFe
- New NNLO calculations (only e+e-)
 - ✦ See talk tomorrow
 - Still need high z resummation and target mass corrections → see also JAM fits
 - Target mass corrections mitigated by high energy at FCC-ee



Data samples we (will) have



Measuring transverse spin dependent di-Hadron Correlations In unpolarized e^+e^- Annihilation into Quarks



Interference effect in e^+e^- quark fragmentation will lead to azimuthal asymmetries in di-hadron correlation measurements!

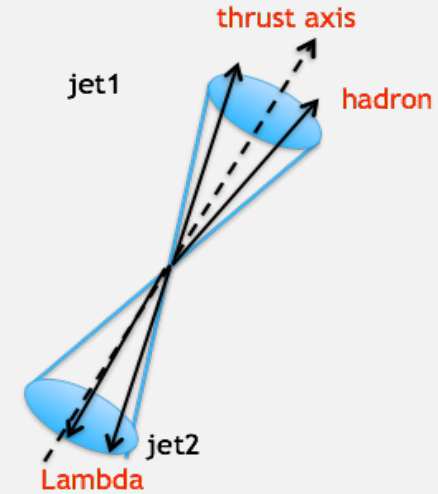
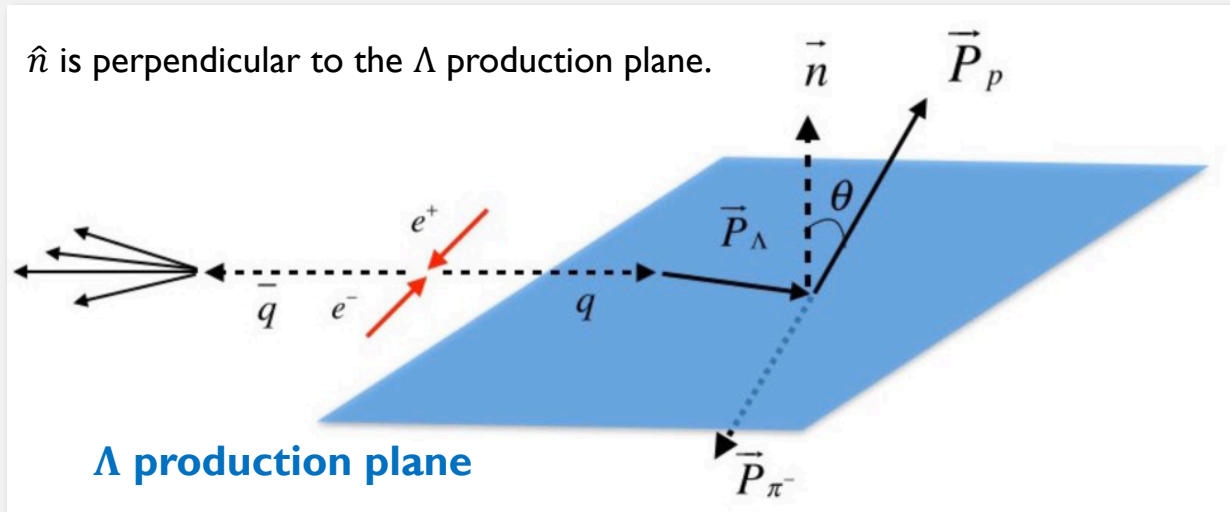
Experimental requirements:

- Small asymmetries \rightarrow very large data sample!
- Good particle ID to high momenta.
- Hermetic detector



Normalized cross section $e^+e^- \rightarrow (h_1 h_2)(\bar{h}_1 \bar{h}_2) + X$
 $\propto 1 + H_1^\perp \overline{H_1^\perp} \cos(\phi_1 + \phi_2) + G_1^\perp \overline{G_1^\perp} \cos(2(\phi_1 - \phi_2))$

OBSERVABLES IN Λ RESTFRAME

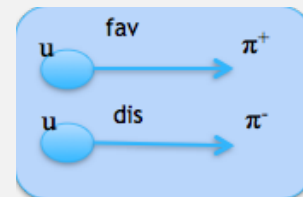
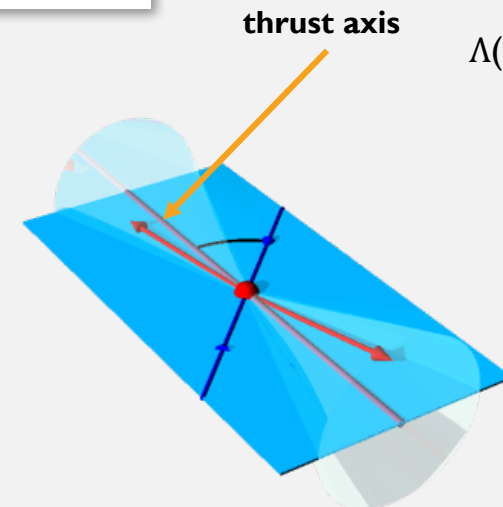


$\Lambda(u\bar{d}s); \pi^+(u\bar{d}); K^+(u\bar{s})$

- Self-analyzing decay leads to polarization dependent distribution

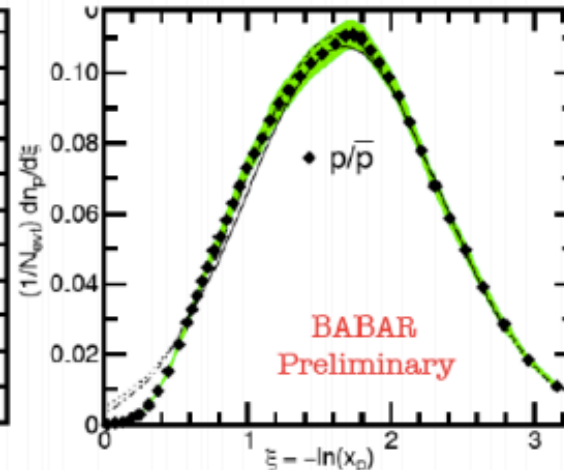
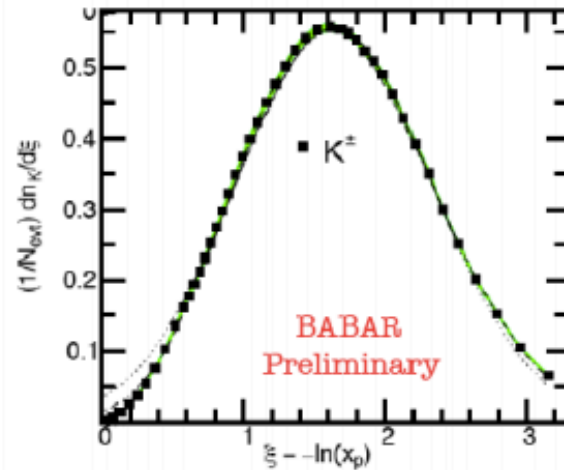
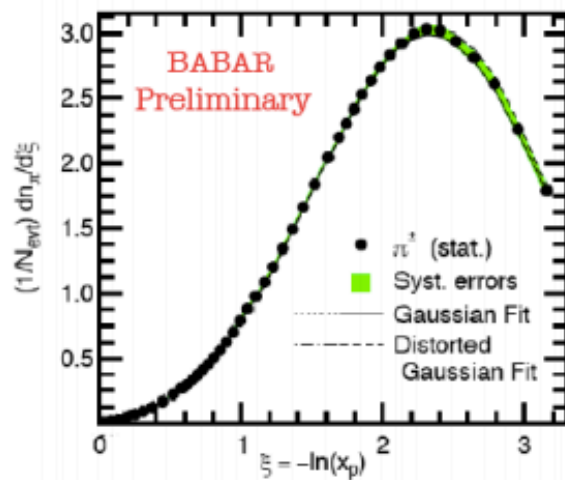
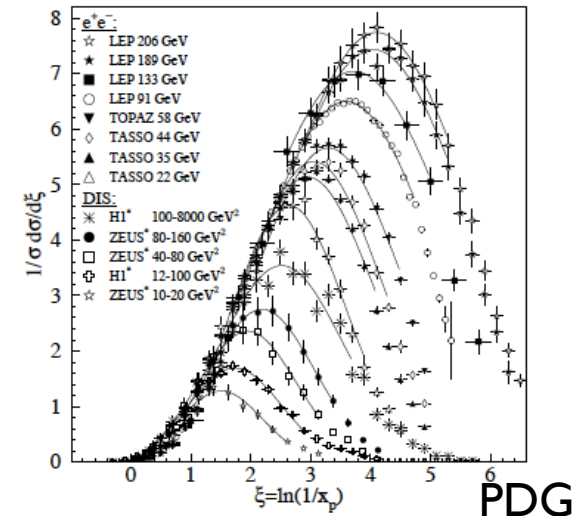
$$\frac{1}{N} \frac{dN}{d\cos\theta} = 1 + \alpha P \cos\theta$$

- where α is the decay parameter: $\alpha_+ = 0.642 \pm 0.013$ for Λ and $\alpha_- = -0.71 \pm 0.08$ for $\bar{\Lambda}$ (PDG).
- The p_t is measured as the transverse momentum of Λ relative to the **thrust axis**

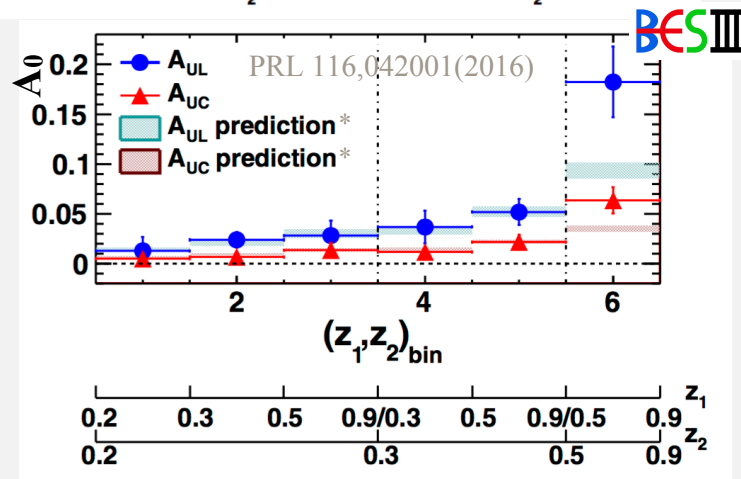
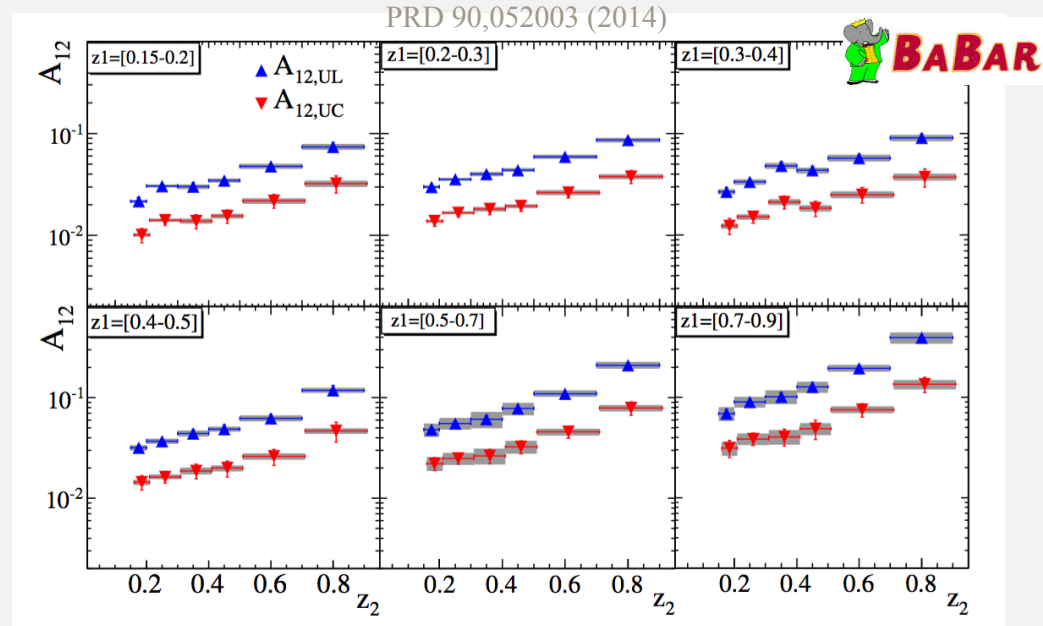
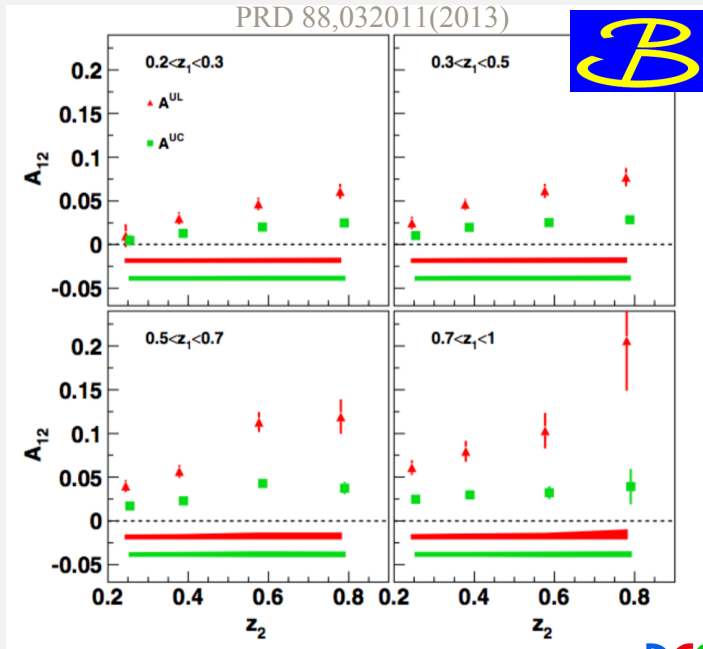


PERTURBATIVE QCD

- Time like splitting functions have singularities ~ 0.1 (unlike space like important for DIS)
- MLLA \rightarrow test for resummation
- Observed shape consistent with QCD calculations (access to α_S)
- FCC-ee might go to lower z . Impact?



Collins Effect vs (z_1, z_2)

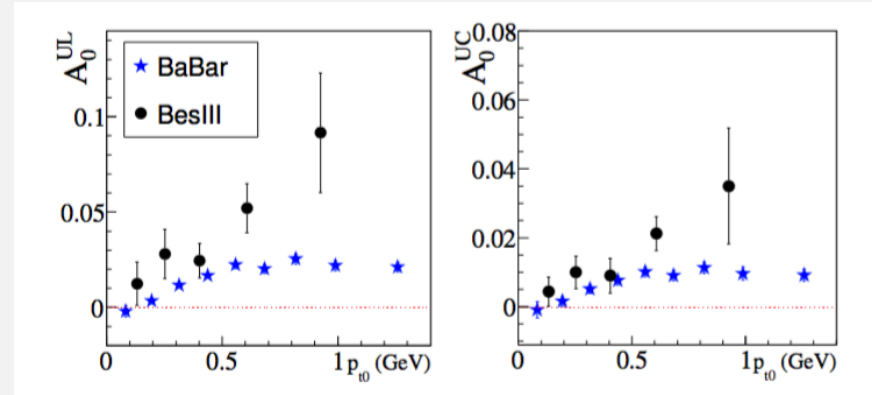
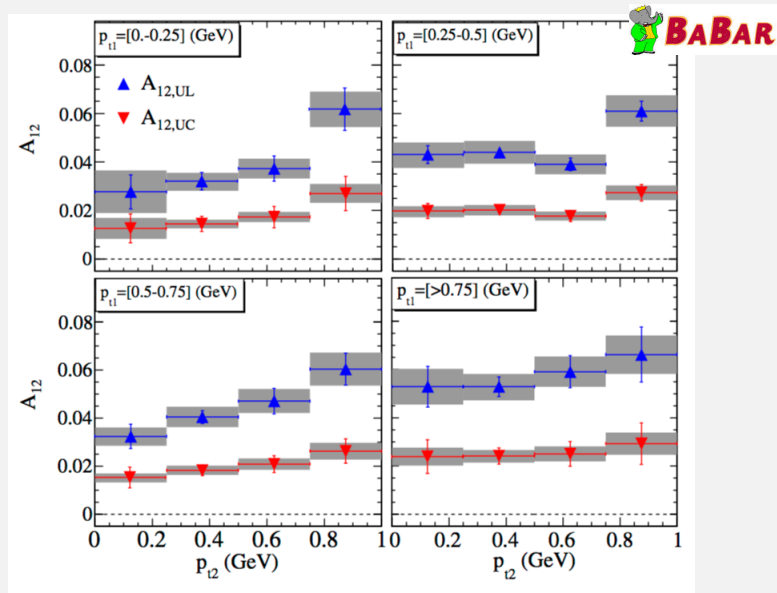


- Significant non-zero asymmetries A_{12} , A_0 in all bins
- Strong dependence on (z_1, z_2) observed in all the experiments
- $A_{UC} < A_{UL}$ as expected; complementary informations about favored and disfavored fragmentation processes

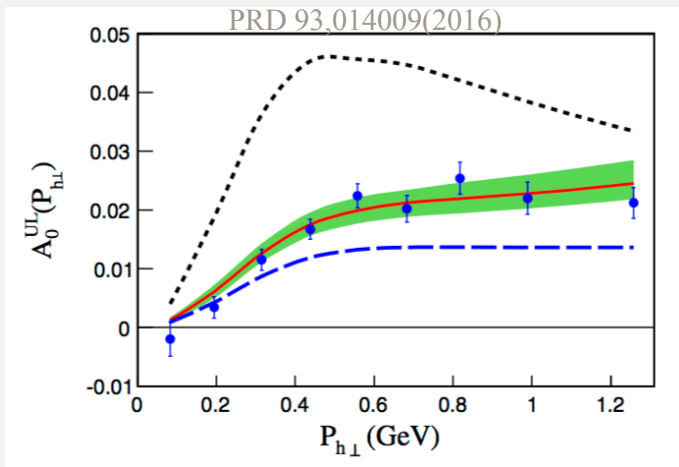
*PRD 93,014009(2016)

COLLINS EFFECT VS PT AND THRUST POLAR ANGLE

Unlike/Likesign
Unlike/Charged
 Ratios to cancel
 acceptance effects
Unlike:
 $\text{fav} \cdot \text{fav} + \text{dis} \cdot \text{dis}$
Like:
 $\text{fav} \cdot \text{dis}$



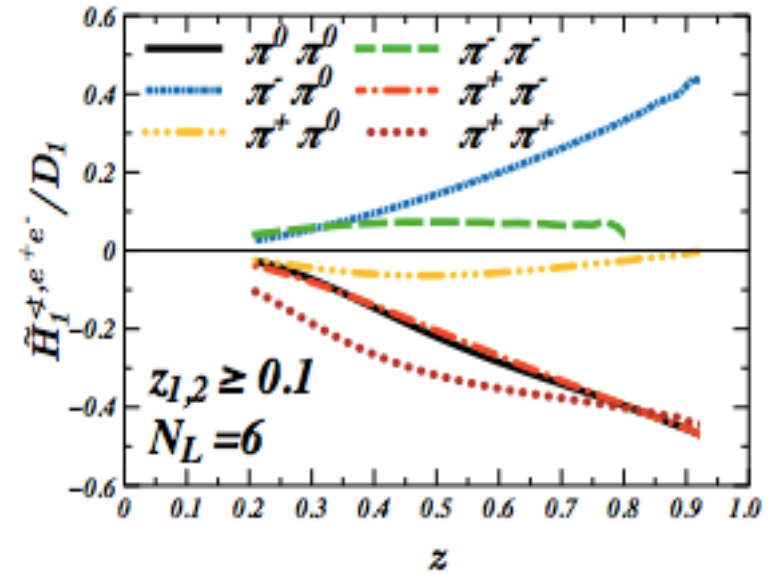
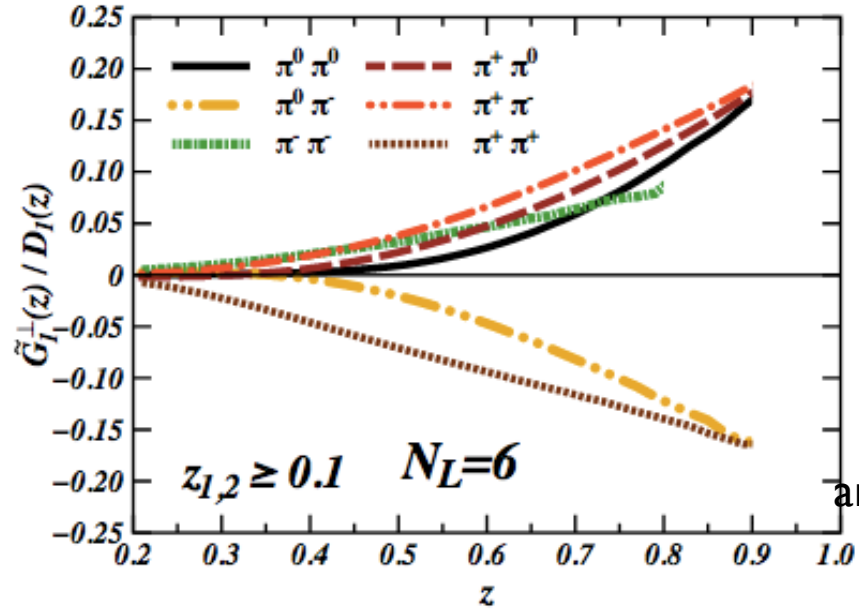
- The asymmetries increase for increasing p_{Tt} :
- less pronounced for A_{12} , but large uncertainties due to the p_{Tt} resolution
 - steeper p_{Tt} dependence for BESIII
 - different kinematic regions: $\langle Z \rangle_{\text{BESIII}} > \langle Z \rangle_{\text{BaBar}}$



— NLL': next-to-leading-logarithm approximation
- - - LL: leading logarithmic calculation
⋯ No TMD evolution
 Calculation performed with fixed parameters from Table I in PRD93,014009

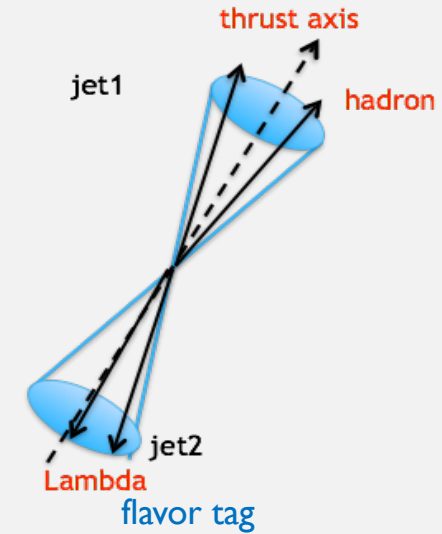
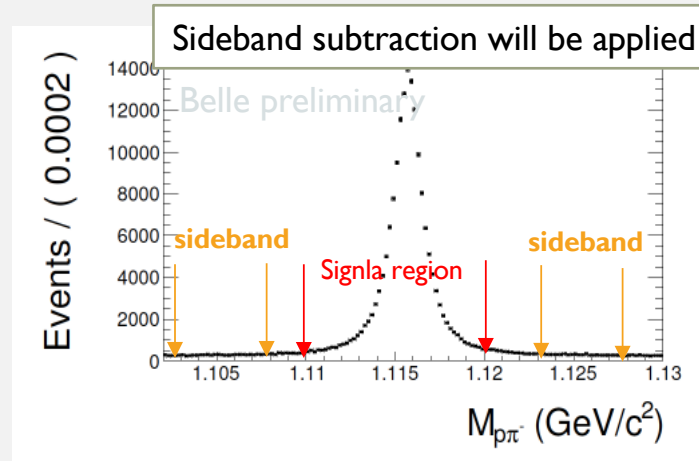
- A^{UL} and A^{UC} asymmetries are described very well
- TMD evolution at NLL' describes e^+e^- and SIDIS data adequately well
- better description including higher orders: improvement of the theoretical uncertainties

ASYMMETRIES FOR $\cos(2(\phi_{R1}-\phi_{R2}))$ ($G_{I\perp}$) SMALL



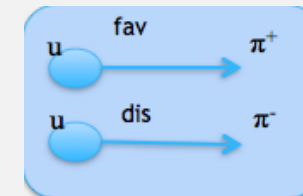
- See recent model calculations by Matevosyan et al. \rightarrow 'worm gear' type splitting function (cmp to glt pdf)

LAMBDA RECONSTRUCTION



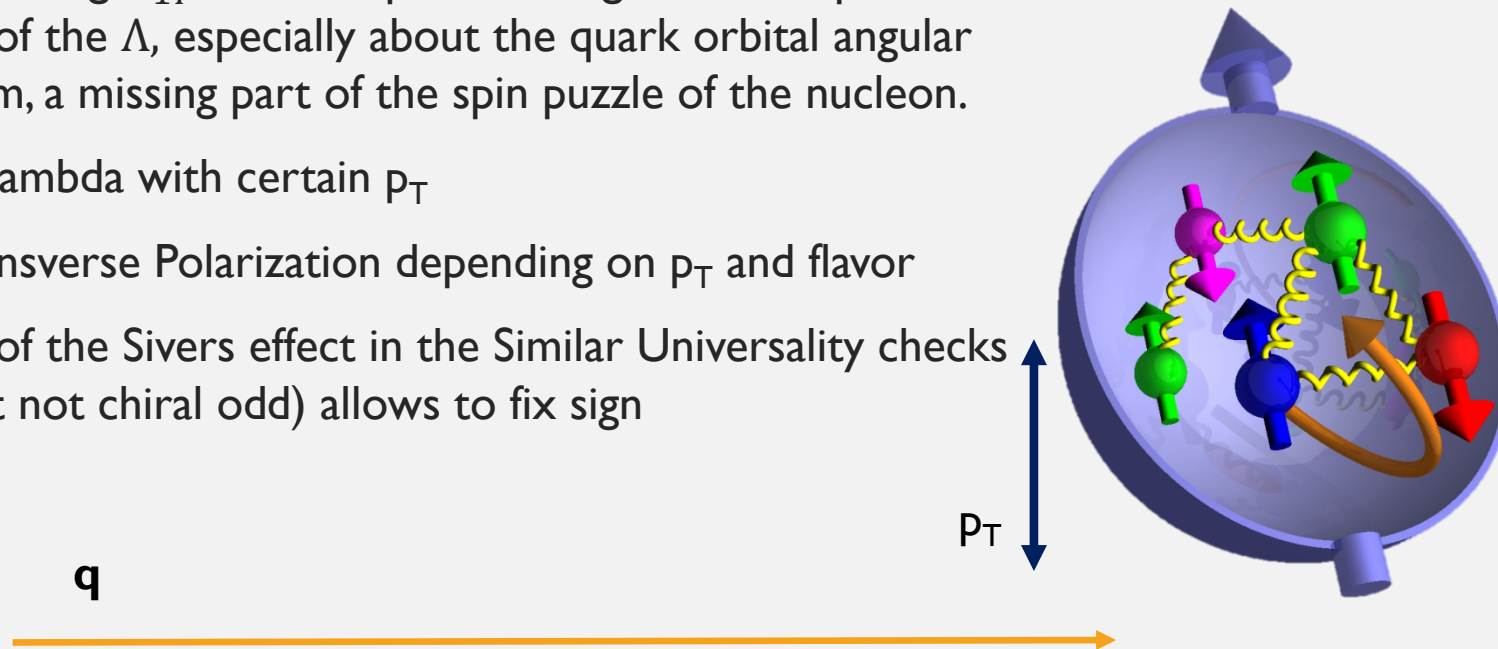
$\Lambda(u ds); \pi^+(u \bar{d}); K^+(u \bar{s})$

- Signal process $\Lambda \rightarrow p \pi^- (\bar{\Lambda} \rightarrow \bar{p} \pi^+)$. Clear Λ peak.
- Detect light hadron (K^\pm, π^\pm) in the opposite hemisphere \rightarrow enhance or suppress different flavors fragmenting in $\Lambda(\bar{\Lambda})$.

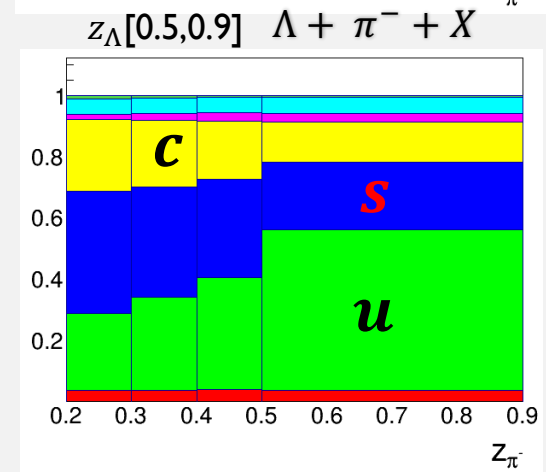
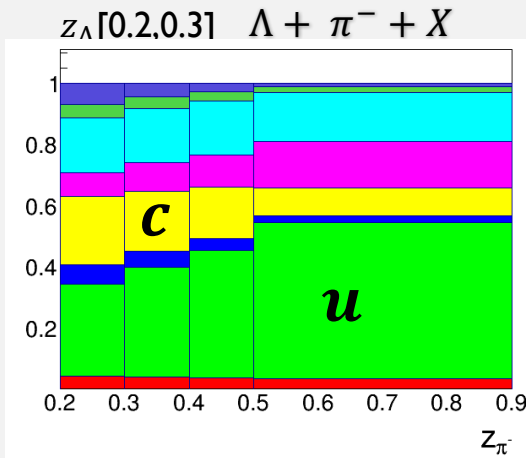
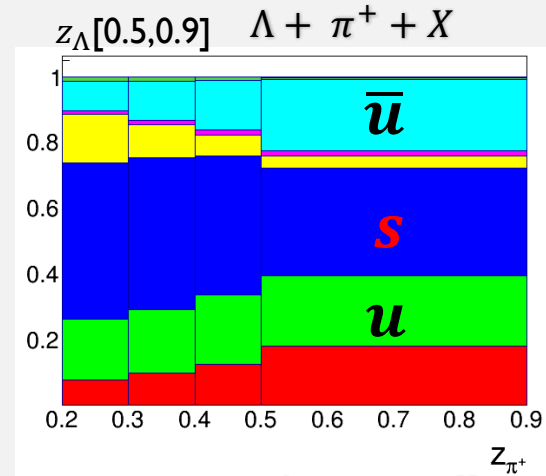
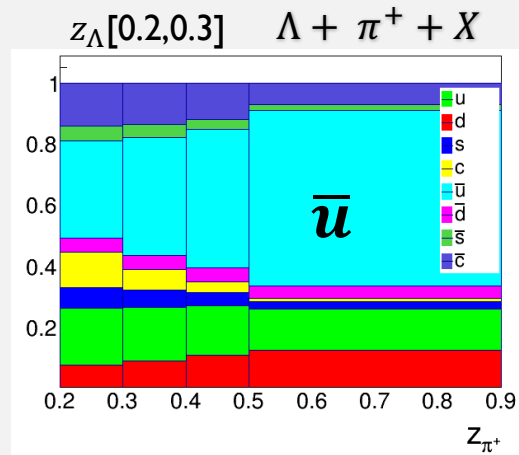


HYPERON PRODUCTION AS A TOOL TO STUDY BARYON SPIN STRUCTURE

- Lambda polarization allows to study spin-orbit correlation of quarks inside Baryon \rightarrow counterpart of the Sivers parton distribution function (k_T dependence of quark distributions in transversely polarized proton)
- A non-vanishing D_{1T}^\perp could help to shed light on the spin structure of the Λ , especially about the quark orbital angular momentum, a missing part of the spin puzzle of the nucleon.
- Produce Lambda with certain p_T
- Check Transverse Polarization depending on p_T and flavor
- Analogue of the Sivers effect in the Similar Universality checks (T-odd but not chiral odd) allows to fix sign

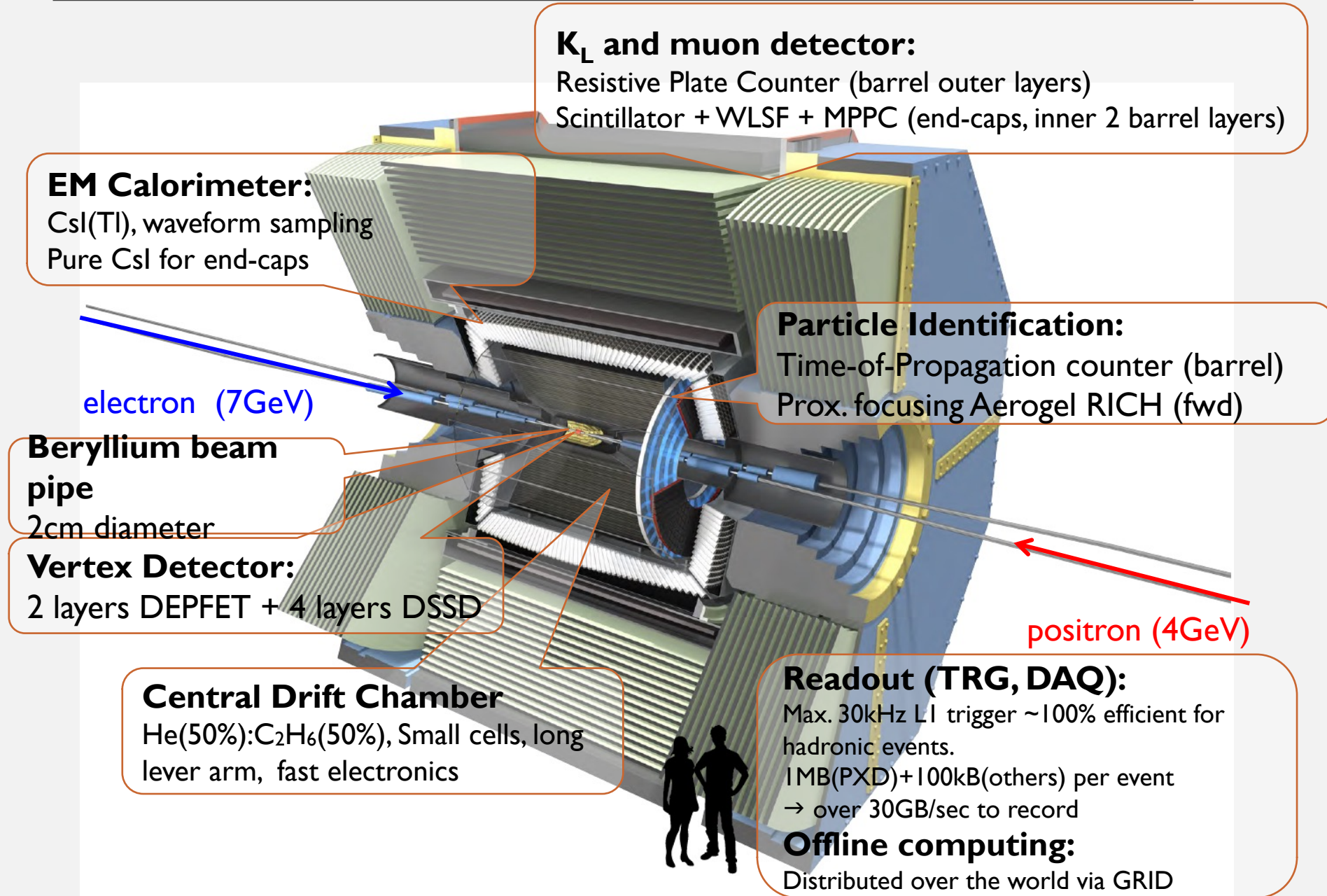


QUARK FLAVOR TAG BY THE LIGHT HADRON

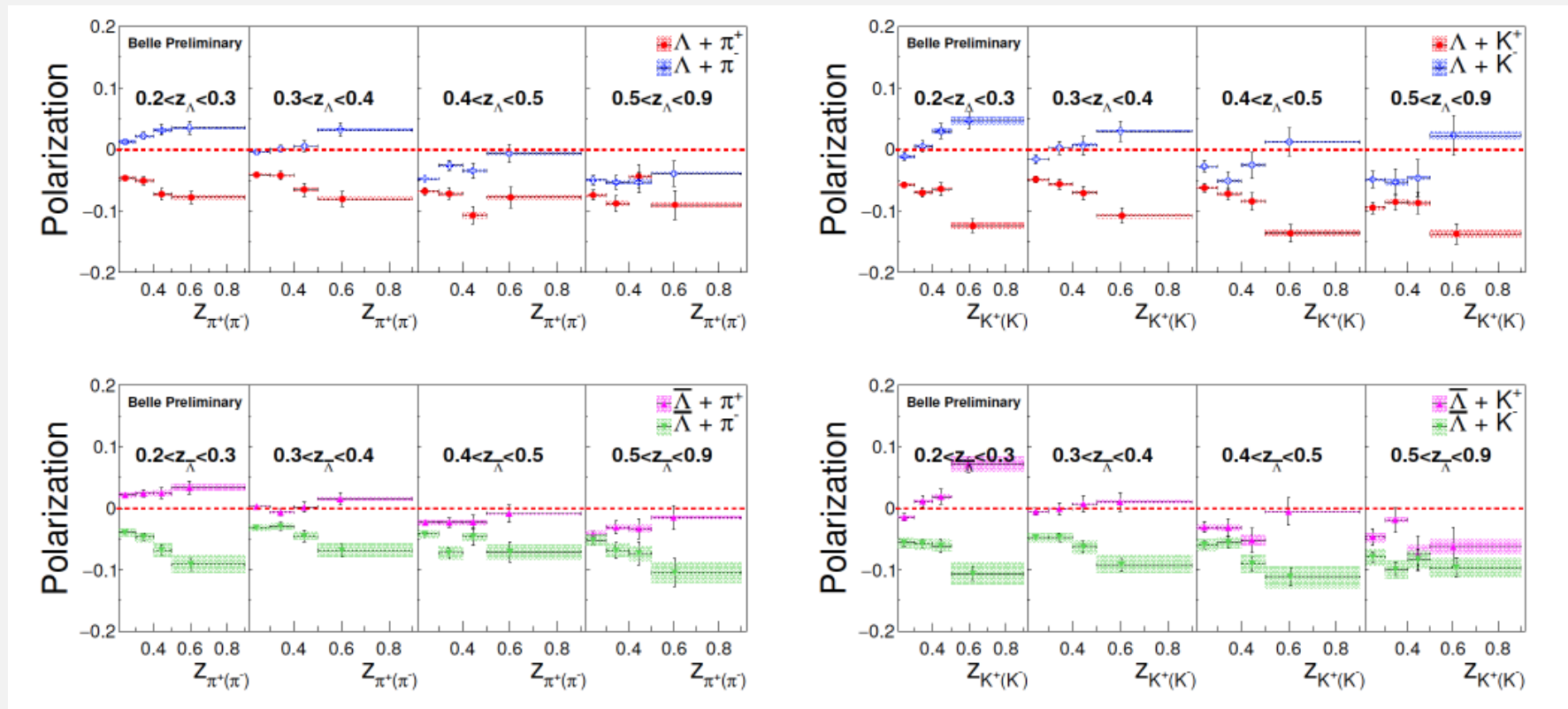


- An attempt to look at the flavor tag effect of the light hadron, based on MC. (Pythia6.2)
- The fractions of various quark flavors going to the Λ 's hemisphere are shown in different $[z_\Lambda, z_h]$ region.
- MC indicates that the tag of the quark flavors is more effective at low z_Λ and high z_h . It explains why at low z_Λ and high z_h , polarization in $\Lambda + h^+$ and $\Lambda + h^-$ have opposite sign.

CUT VIEW OF BELLE II DETECTOR



Π/K TAG IN OPPOSITE HEMISPHERE



- At low z_Λ , polarization in $\Lambda + h^+$ and $\Lambda + h^-$ have opposite sign. The magnitude increases with higher z_h .
- At large z_Λ , the differences between $\Lambda + h^+$ and $\Lambda + h^-$ reduce. Small deviations can still be seen and depend on z_h .

Before

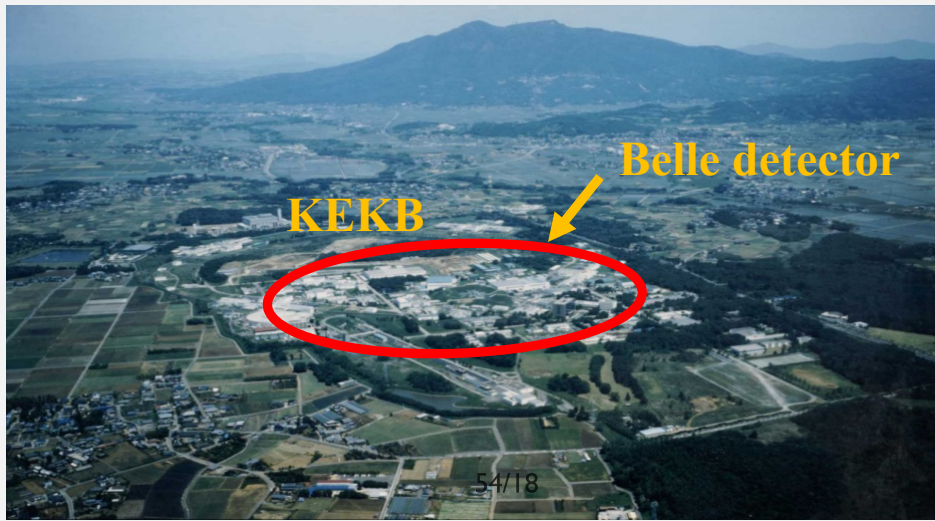


there was



- KEKB: asymmetric e^+ (3.5 GeV) e^- (8 GeV) collider:
 - $\sqrt{s} = 10.58$ GeV, $e^+e^- \rightarrow \Upsilon(nS) \rightarrow B/B + \text{continuum}$
 - $\sqrt{s} = 10.52$ GeV, $e^+e^- \rightarrow q\bar{q}$ (u,d,s,c) 'continuum'
- Ideal (at the time) detector for high precision measurements:
 - tracking acceptance θ [17° ; 150°]: Azimuthally symmetric
 - particle identification (PID): dE/dx, Cherenkov, ToF, EMcal, MuID
- Available data:
 - ~ 1 ab^{-1} total
 - $\sim 1.8 \cdot 10^9$ events at 10.58 GeV,
 - $\sim 220 \cdot 10^6$ events at 10.52 GeV

Experiment	Scans/ Off. Res. fb^{-1}	$\Upsilon(5S)$		$\Upsilon(4S)$		$\Upsilon(3S)$		$\Upsilon(2S)$		$\Upsilon(1S)$	
		10876 MeV fb^{-1}	10^6	10580 MeV fb^{-1}	10^6	10355 MeV fb^{-1}	10^6	10023 MeV fb^{-1}	10^6	9460 MeV fb^{-1}	10^6
CLEO	17.1	0.4	0.1	16	17.1	1.2	5	1.2	10	1.2	21
BaBar	54	R_b scan		433	471	30	122	14	99	-	
Belle	100	121	36	711	772	3	12	25	158	6	102



BELLE Detector (took data till 2010)

