

# Low-energy supersymmetry facing LHC constraints

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# Introduction

## The Minimal Supersymmetric Standard Model

### Chiral supermultiplets

Name	Symbol	spin 0	spin 1/2	$(SU(3)_C, SU(2)_L, U(1)_Y)$
squarks, quarks ( $\times 3$ families)	$Q$	$(\tilde{u}_L, \tilde{d}_L)$	$(u_L, d_L)$	$(3, 2, \frac{1}{6})$
	$\bar{u}$	$\tilde{u}_R^*$	$u_R^\dagger$	$(\bar{3}, 1, -\frac{2}{3})$
	$\bar{d}$	$\tilde{d}_R^*$	$d_R^\dagger$	$(\bar{3}, 1, \frac{1}{3})$
sleptons, leptons ( $\times 3$ families)	$L$	$(\tilde{\nu}, \tilde{e}_L)$	$(\nu, e_L)$	$(1, 2, -\frac{1}{2})$
	$\bar{e}$	$\tilde{e}_R^*$	$e_R^\dagger$	$(1, 1, 1)$
Higgses, Higgsinos	$H_u$	$(H_u^+, H_u^0)$	$(\tilde{H}_u^+, \tilde{H}_u^0)$	$(1, 2, \frac{1}{2})$
	$H_d$	$(H_d^0, H_d^-)$	$(\tilde{H}_d^0, \tilde{H}_d^-)$	$(1, 2, -\frac{1}{2})$

### Gauge supermultiplets

Name	spin 1/2	spin 1	$(SU(3)_C, SU(2)_L, U(1)_Y)$
gluino, gluon	$\tilde{g}$	$g$	$(8, 1, 0)$
winos, W bosons	$\tilde{W}^\pm \quad \tilde{W}^0$	$W^\pm \quad W^0$	$(1, 3, 0)$
bino, B boson	$\tilde{B}^0$	$B^0$	$(1, 1, 0)$

# The MSSM

- ▶ Superpotential  $W = h_e H_d L \bar{e} + h_d H_d Q \bar{d} + h_u Q H_u U^c - \mu H_u H_d$
- ▶ Soft SUSY-breaking mass and interaction terms for MSSM scalars

$$\begin{aligned} \mathcal{L}_{\text{soft-breaking}} = & m_{H_u}^2 H_u^\dagger H_u + m_{H_d}^2 H_d^\dagger H_d + m_Q^2 Q^\dagger Q + m_L^2 L^\dagger L \\ & + m_u^2 \tilde{u}_R^* \tilde{u}_R + m_d^2 \tilde{d}_R^* \tilde{d}_R + m_e^2 \tilde{e}_R^* \tilde{e}_R \\ & + \left( T_e H_d L \tilde{e}_R^* + T_d H_d Q \tilde{d}_R^* + T_u Q H_u \tilde{u}_R^* + B_\mu H_u H_d + h.c. \right) \end{aligned}$$

- ▶ SUSY-soft-breaking gauginos masses

$$\mathcal{L}_G = \frac{1}{2} \left( M_1 \tilde{B} \tilde{B} + M_2 \tilde{W} \tilde{W} + M_3 \tilde{g} \tilde{g} \right) + h.c.$$

## A few phenomenological features

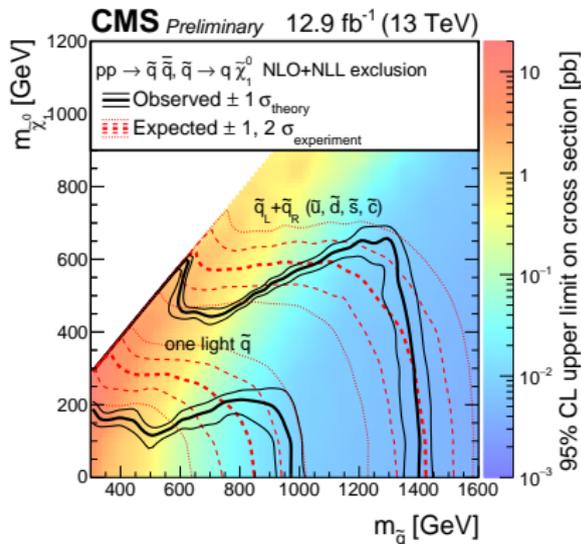
- ▶ After EWSB, gauginos and higgsinos mix to form the neutralinos ( $\tilde{\chi}_{1,2,3,4}^0$ ) and the charginos ( $\tilde{\chi}_{1,2}^\pm$ ).
- ▶ Higgs sector is a two Higgs-doublet (2HDM) of type-II. Physical spectrum is composed of two neutral CP-even Higgs (h and H), one neutral CP-odd Higgs (A) and two charged Higgses ( $H^\pm$ ).
- ▶ The light Higgs mass is *predicted* in the MSSM. Tree level upper bound of  $m_Z$ , however radiative corrections are very important and allow to reach the observable value.





# LHC constraints

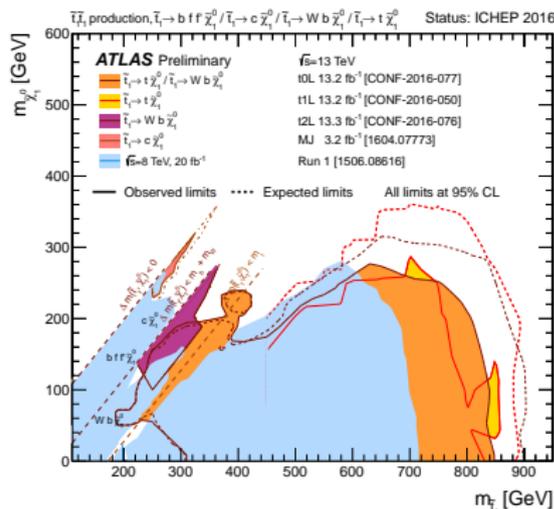
- ▶ A proper interpretation of current results in terms of MSSM parameter space depends strongly on the hierarchy of masses between the different SUSY particles.
- ▶ Different hierarchies implies different decay rate. Some configuration results in difficult experimentally accessible region (e.g. compressed regions).
- ▶ Assumptions that results in the near degeneracy of some states (e.g. first two generation squarks), strongly influence the constraints.
- ▶ If using a simplified model, dependence on its assumptions (BRs, mass of the other particles etc.).



[CMS-PAS-SUS-16-05]

# LHC constraints

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[ATLAS summary plot]

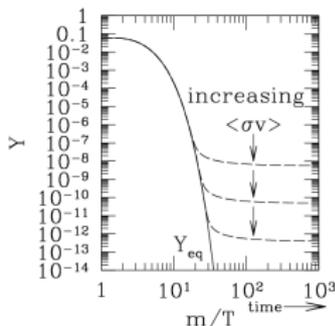
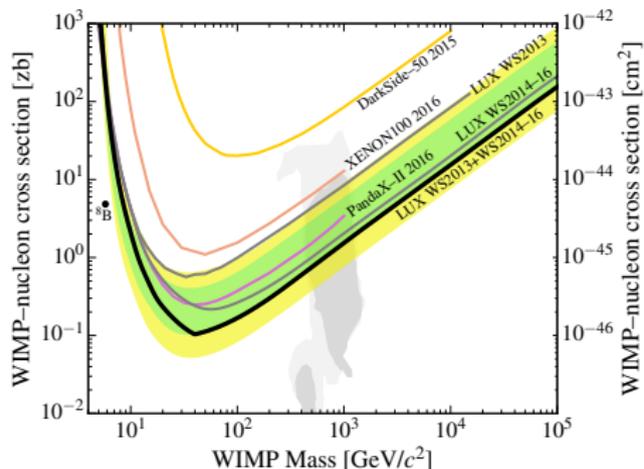
# LHC constraints ... but not only

## Indirect measurements

- ▶  $(g-2)_\mu$ .  $3.4\sigma$  discrepancy may be explained with  $\mathcal{O}(100)$  GeV smuons.
- ▶  $M_W, M_Z, M_b$  and EWPO.
- ▶ Flavor physics observables ( $B_s \rightarrow \mu\mu$ ,  $b \rightarrow s\gamma, \dots$ ).

## Dark matter

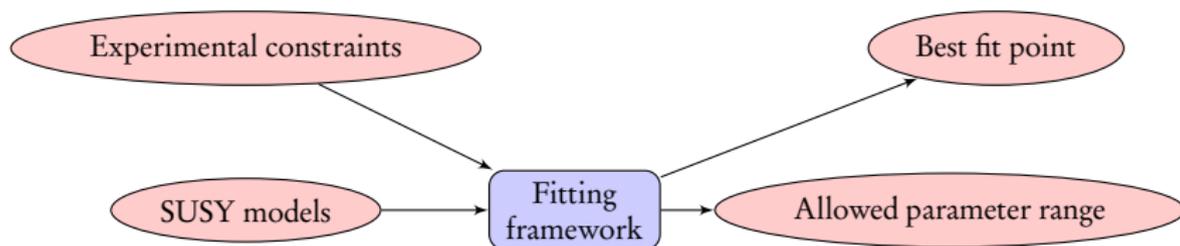
- ▶ Relic density constraint especially important, if assuming that the  $\tilde{\chi}_1^0$  is the only DM component.
- ▶ Strong constraint from direct detection experiment; complementary to the LHC searches.
- ▶ Indirect detection constraints can be important according to the neutralino composition, however large uncertainties in the modeling of the signal.



# Where is SUSY now?

## Global likelihood studies

- ▶ Define a simplified model based on reasonable assumptions and a minor number of free parameters.
- ▶ Use of the available collider data, electro-weak precision observables and DM constraint to fit the best value and the likelihood profile of the model parameters.
- ▶ Effectively implement interplay between different searches (e.g. collider vs direct detection for DM).



# MSSM scenarios

## GUT Models

CMSSM

$$m_0, m_{1/2}, A_0, \tan \beta$$

SU(5)

$$m_{1/2}, m_{\tilde{5}}, m_{10}, m_{H_u}, m_{H_d}, A_0, \tan \beta$$

mAMSB

$$m_0, m_{3/2}, \tan \beta$$

others, e.g NUHM1, NUHM2, ...

- ▶ Introduce correlation between the colored and uncolored sectors.

[1312.5250, 1408.4060, 1610.10084, 1610.10084]

## pMSSM10

$$M_1, M_2, M_3$$

$$m_{\tilde{q}_{1,2}}, m_{\tilde{q}_3}, m_{\tilde{l}}$$

$$A$$

$$M_A, \tan \beta, \mu$$

## pMSSM19

$$M_1, M_2, M_3$$

$$m_{\tilde{Q}_{1,2}}, m_{\tilde{Q}_3}, m_{\tilde{u}_R, \tilde{c}_R}, m_{\tilde{d}_R, \tilde{s}_R}, m_{\tilde{t}_R}, m_{\tilde{b}_R}$$

$$m_{\tilde{L}_{1,2}}, m_{\tilde{L}_3}, m_{\tilde{e}, \tilde{\mu}}, m_{\tilde{\tau}}$$

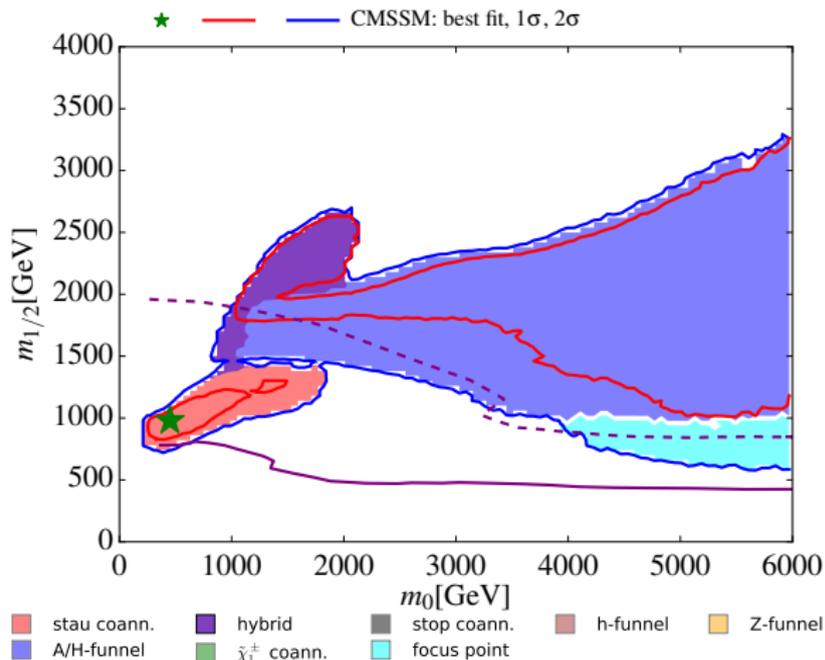
$$A_t, A_b, A_\tau$$

$$M_A, \tan \beta, \mu$$

[1504.03260], [1508.06608, 1605.09502, 1608.05379]

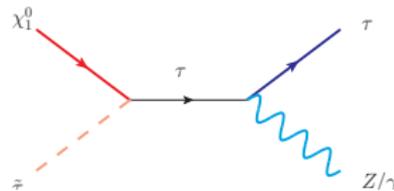
# GUT models

## CMSSM



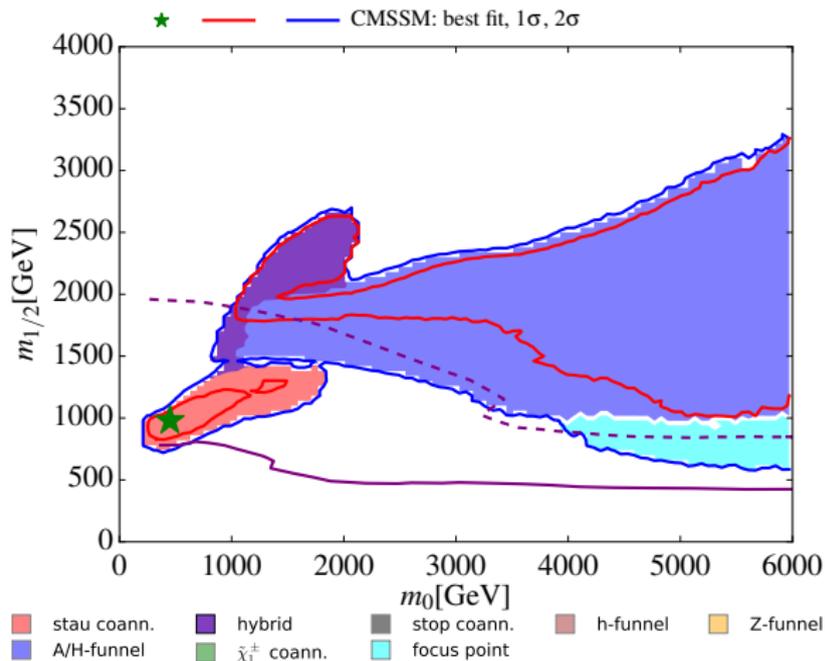
We have several different mechanisms at play.

1.  $\tilde{\tau}$ -coannihilation



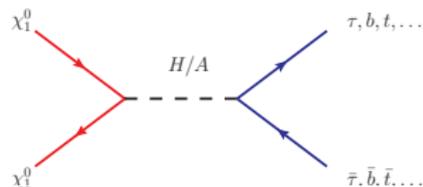
- ▶ Leading mechanism when the mass difference between the  $\tilde{\tau}$  and the  $\tilde{\chi}_1^0$  is of the order of a few GeV.
- ▶  $\tilde{\chi}_1^0$  is Bino-like.
- ▶ Also  $\tilde{\tau} - \tilde{\tau}$  annihilation important in this scenario.

## CMSSM



We have several different mechanisms at play.

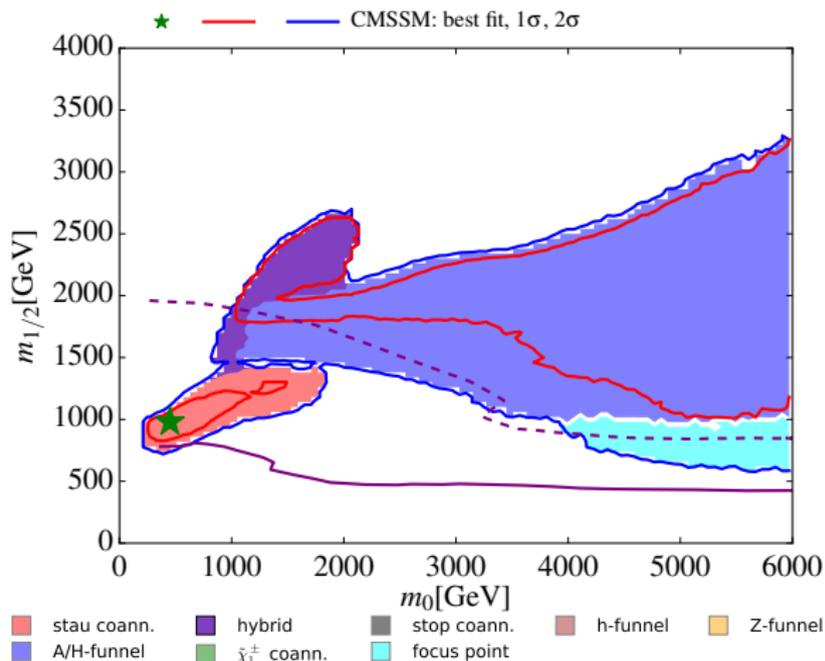
## 2. H/A-funnel.



▶  $\tilde{\chi}_1^0$  is Bino-like.

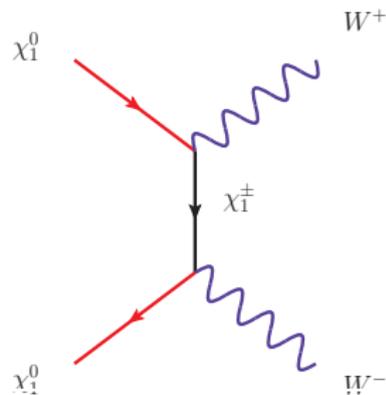
▶ Mass degeneracy condition:  
 $2 \cdot \tilde{\chi}_1^0 \approx M_A/M_H$ .

## CMSSM



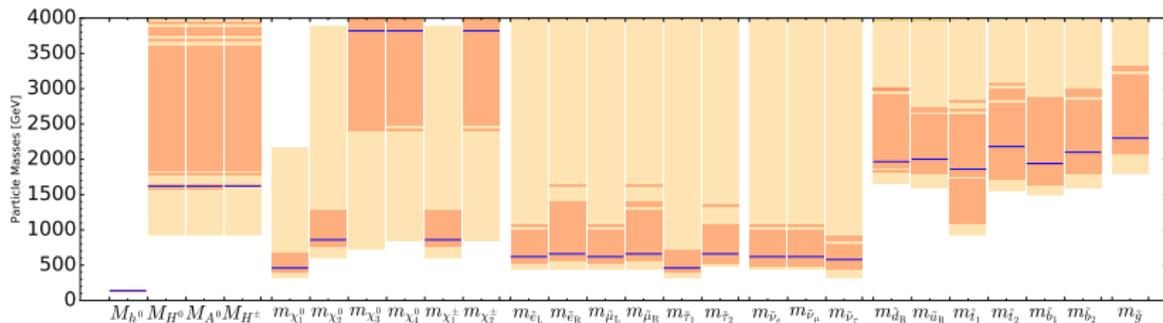
We have several different mechanisms at play.

### 3. Focus point.

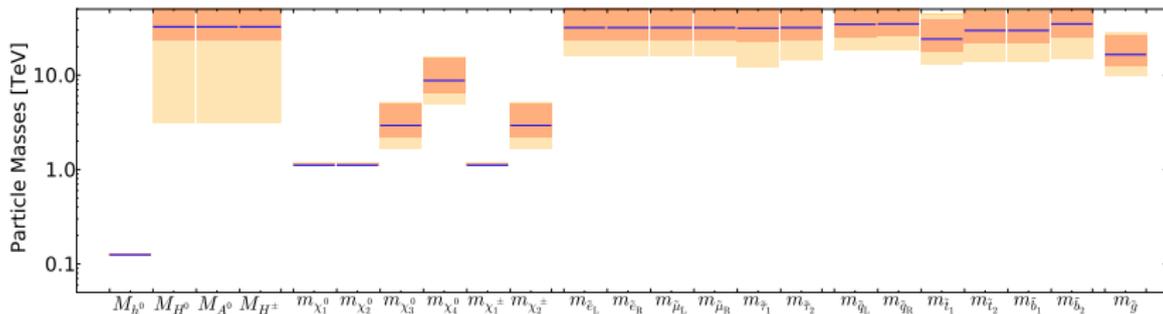


- ▶ Region where RGEs have focussing properties.
- ▶ We have that  $\mu \approx M_1$ , sizable Higgsino component of the  $\tilde{\chi}_1^0$ .

# SU(5) boundary conditions

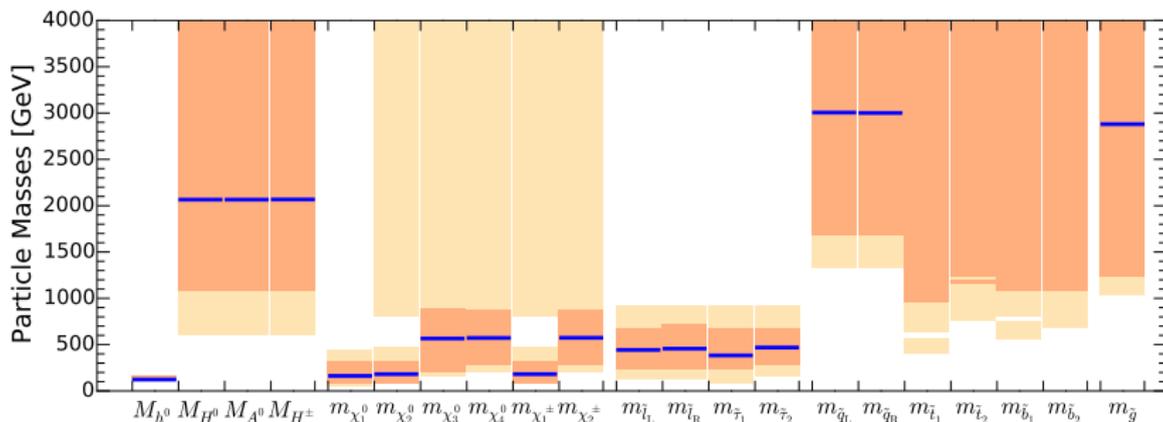


## mAMSB



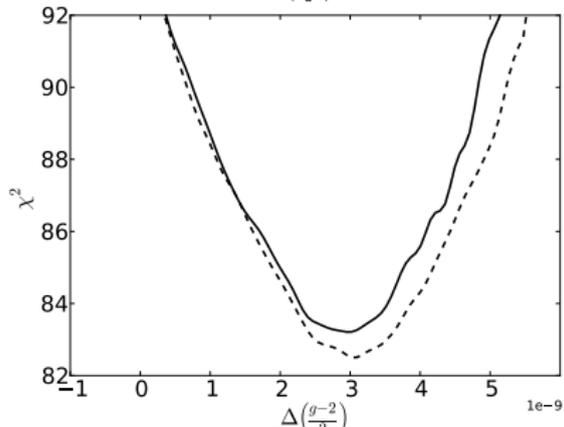
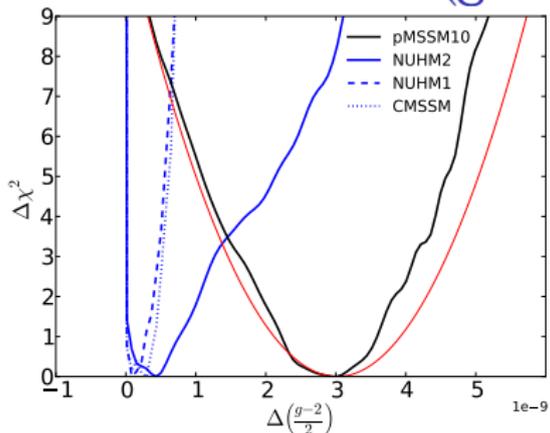
# Phenomenological models

# pMSSM10 mass spectrum



- ▶ Poor determination of the mass of colored sparticles (only lower bound from LHC searches).
- ▶ Larger freedom allow to fulfill the  $(g-2)_\mu$  constraint without being in tension with the LHC searches.
- ▶ Improved fit with respect to the GUT models.

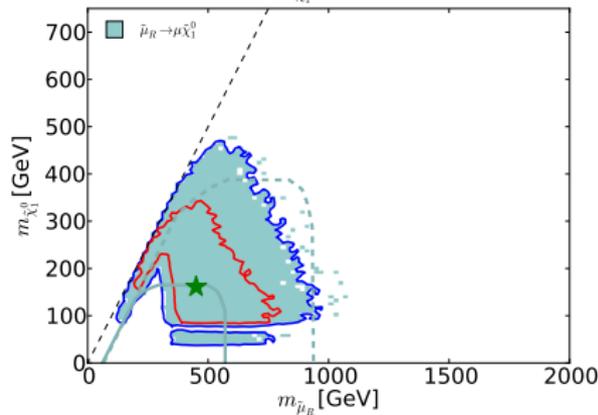
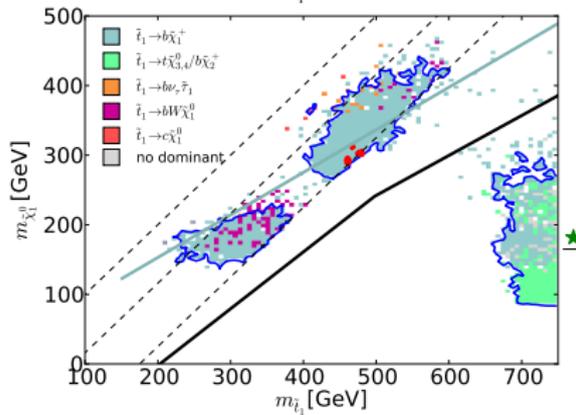
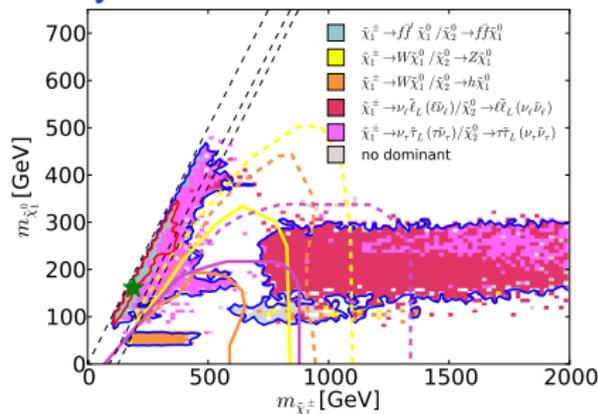
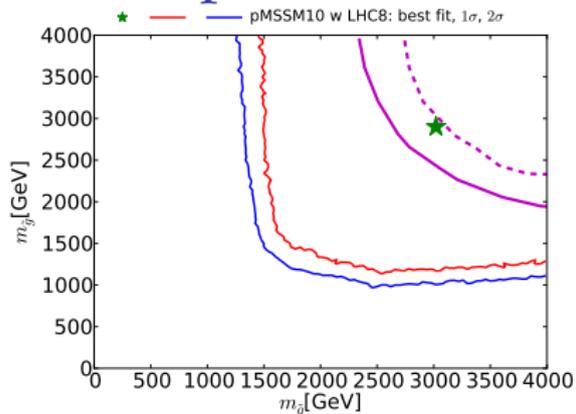
# The $(g-2)_\mu$ constraint



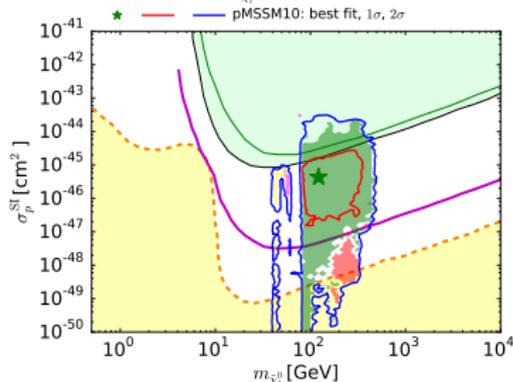
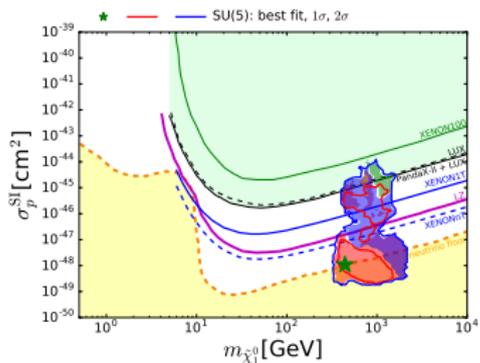
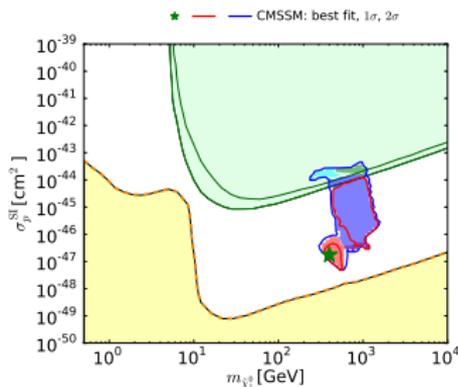
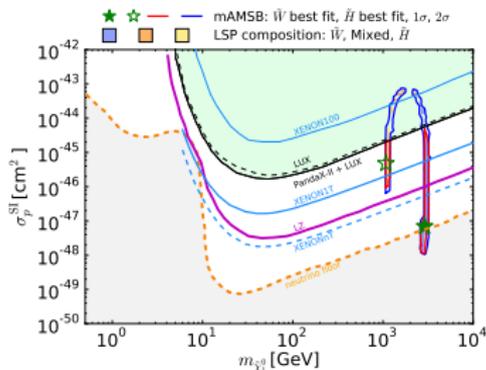
Model	$\chi^2/n_{\text{dof}}$	p-value
CMSSM	32.8/24	11 %
NUHM1	31.1/23	12 %
NUHM2	30.3/22	11 %
pMSSM10	20.5/18	31 %

- ▶  $3.5\sigma$  discrepancy between the SM  $(g-2)_\mu$  value and the measured one.
- ▶ In CMSSM, NUHM1 and NUHM2 there is a tension between the  $(g-2)_\mu$  and LHC constraints from direct searches, due to the universality relations.
- ▶ In the pMSSM10 we are able to fit **perfectly** the  $(g-2)_\mu$ .
- ▶ Impact of LHC8<sub>EWK</sub> constraint limited.

# Perspectives for discovery at LHC run 2

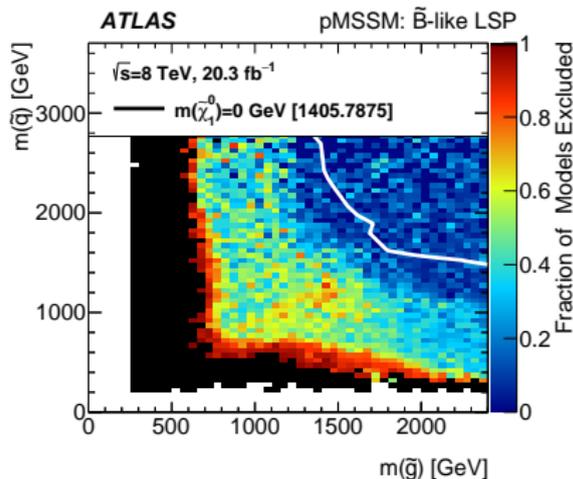
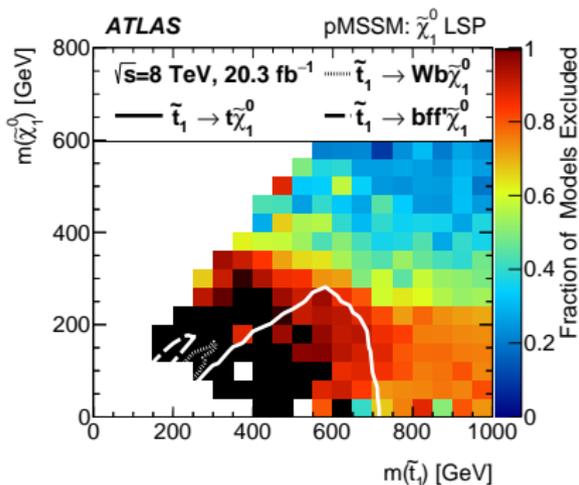


## Interplay between collider and direct detection



## pMSSM19

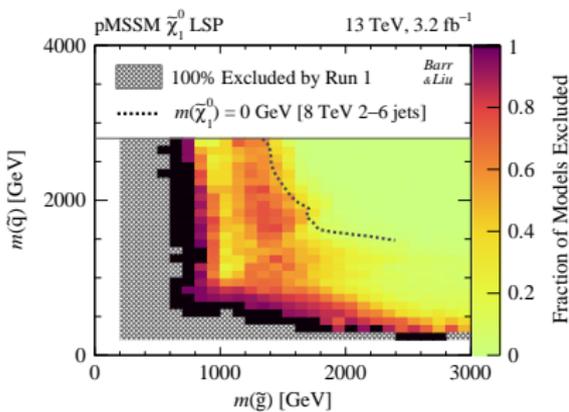
- ▶ ATLAS pMSSM19 scan vs 7/8 TeV searches.
- ▶ Flat-prior random-sampling. Upper and lower bound chosen to maximize coverage of the parameter space accessible to the LHC [1508.06608].



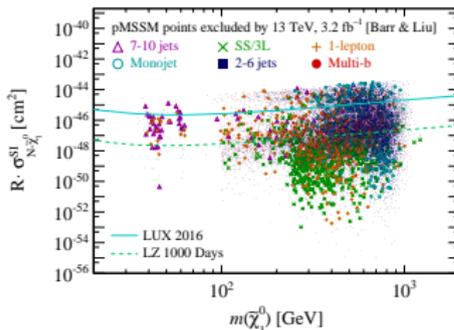
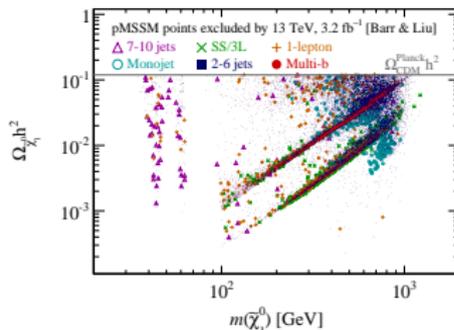
- ▶ SUSY-AI : use results from the ATLAS scan to implement the constraints from the available searches using machine-learning method [1605.02797].

## pMSSM19

- ▶ Exclusion power of the 13 TeV data from Barr et al [1605.09502].
- ▶ Use the models previously found to be allowed by the ATLAS study.
- ▶ Exclude a further 15.7% model points from the set that survived from Run 1 searches.



- ▶ Barr et al [1608.05379], complementarity with DM.



# Conclusions

- ▶ Completely covering Supersymmetry at LHC is difficult, even for the simplest case of the MSSM.
- ▶ Strong dependence of the spectrum (and of the signatures) on the theoretical assumptions of the scenario.
- ▶ GUT models unable to fit  $(g-2)_\mu$  anymore due to the LHC constraints on sparticle production.
- ▶ Interesting complementarity with DM direct-detection searches.
- ▶ Countless other studies not covered in this talk.

# Appendix

# Higgs mechanism in the MSSM

- ▶ Tree level Higgs scalar potential ( $m_u^2 = m_{H_u}^2 + |\mu|^2$  and  $m_d^2 = m_{H_d}^2 + |\mu|^2$ )

$$V_0 = m_u^2 |H_u^0|^2 + m_d^2 |H_d^0|^2 + B_\mu (H_d^0 H_u^0 + \text{h.c.}) + \frac{g^2 + g'^2}{8} (|H_d^0|^2 - |H_u^0|^2)^2$$

- ▶ The two Higgs doublet are supposed to acquire a v.e.v. different from zero
- ▶ Decomposition of the fields

$$H_u^0 = \frac{1}{\sqrt{2}} (v_u + S_u + iP_u), \quad H_d^0 = \frac{1}{\sqrt{2}} (v_d + S_d + iP_d)$$

- ▶ Diagonalization of the pseudoscalar mass matrix (rotation angle  $\beta$ ) give a would-be Goldstone boson eaten by the Z and a pseudoscalar state with a mass

$$m_A^2 = \frac{B_\mu}{\cos \beta \sin \beta}$$

- ▶ Same diagonalization angle for the charged Higgs matrix
- ▶ Pseudoscalar couplings to quarks and leptons are given by

$$g_{Auu} = \cot \beta \frac{m_u}{v}, \quad g_{Add, Aee} = \tan \beta \frac{m_{d,e}}{v}$$

# Higgs mechanism in the MSSM

- ▶ Mass matrix for the scalar sector ( $m_u^2$  and  $m_d^2$  replaced by a combination of  $m_A^2$  and  $\tan\beta$ )

$$\mathcal{M}_0 = \begin{pmatrix} m_A^2 \sin^2 \beta + m_Z^2 \cos^2 \beta & -(m_A^2 + m_Z^2) \sin \beta \cos \beta \\ -(m_A^2 + m_Z^2) \sin \beta \cos \beta & m_A^2 \cos^2 \beta + m_Z^2 \sin^2 \beta \end{pmatrix}$$

- ▶ Diagonalization angle  $\alpha$ .  $m_b^2 \leq m_Z^2 \cos^2(2\beta)$  at tree level.

$$\tan 2\alpha = \left( \frac{m_A^2 + m_Z^2}{m_A^2 - m_Z^2} \right) \tan 2\beta$$



$$m_{b,H} = \frac{1}{2} \left( m_A^2 + m_Z^2 \mp \sqrt{(m_A^2 - m_Z^2)^2 + 4m_Z^2 m_A^2 \sin^2(2\beta)} \right)$$

- ▶ Scalar coupling to the gauge bosons:  $g_{bVV} = \frac{2m_V^2}{v} \sin(\beta - \alpha)$ ,  $g_{HVV} = \frac{2m_V^2}{v} \cos(\beta - \alpha)$
- ▶ Scalar couplings to the quarks and leptons are given by

$$g_{huu} = \frac{\cos \alpha}{\sin \beta} \frac{m_u}{v}, \quad g_{hdd,hee} = -\frac{\sin \alpha}{\cos \beta} \frac{m_{d,e}}{v}$$
$$g_{Hu u} = \frac{\sin \alpha}{\sin \beta} \frac{m_u}{v}, \quad g_{Hdd,hee} = \frac{\cos \alpha}{\cos \beta} \frac{m_{d,e}}{v}$$

# The framework

- ▶ Frequentist fitting framework written in Python/Cython and C++.
- ▶ We use SLHA standard as an interface between the external codes that are used to compute the spectrum and the observables.
- ▶ The `MultiNest` algorithm is used to sample the parameter space.

Parameter	Range	Number of segments
$M_1$	(-1, 1) TeV	2
$M_2$	(0, 4) TeV	2
$M_3$	(-4, 4) TeV	4
$m_{\tilde{q}}$	(0, 4) TeV	2
$m_{\tilde{q}_3}$	(0, 4) TeV	2
$m_{\tilde{l}}$	(0, 2) TeV	1
$M_A$	(0, 4) TeV	2
$A$	(-5, 5) TeV	1
$\mu$	(-5, 5) TeV	1
$\tan\beta$	(1, 60)	1
Total number of boxes		128

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## Codes

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### Spectrum generation

SoftSUSY

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### Higgs sector and $(g-2)_\mu$

FeynHiggs, Higgssignals, Higgsbounds

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### B-Physics

SuFla, SuperISO

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### EW precision observables

FeynWZ

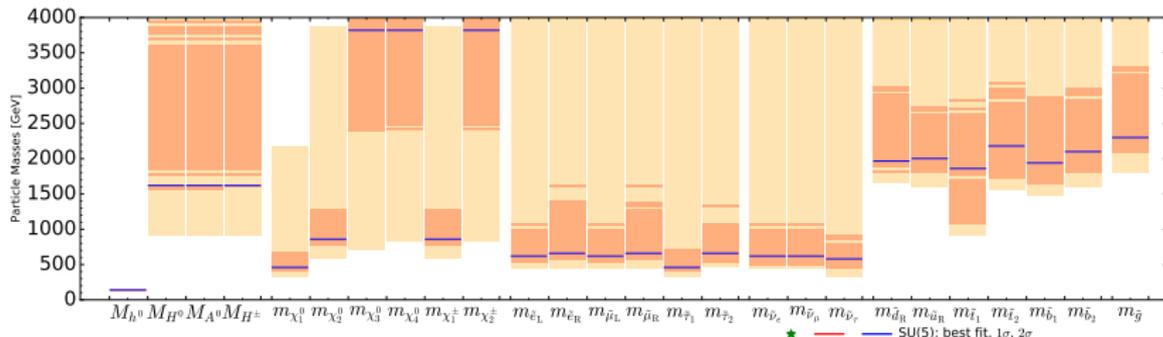
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### Dark matter

MicrOMEGAs, SSARD

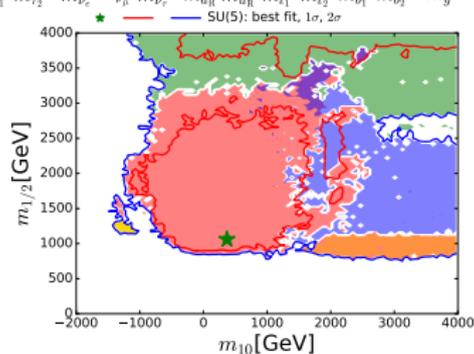
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# SU(5) GUT

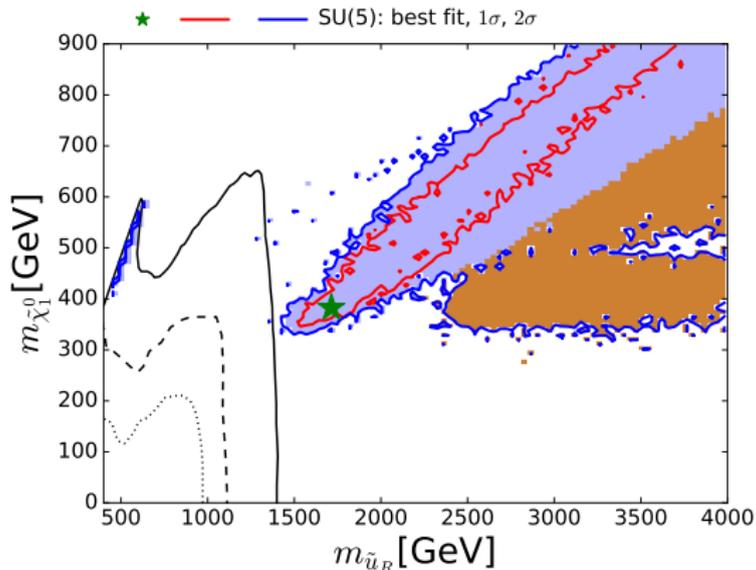


► SU(5) boundary conditions for soft SUSY-breaking terms.

- $(q_L, u_L^c, e_L^c)_i \in \mathbf{10}_i$
- $(\ell_L, d_L^c)_i \in \bar{\mathbf{5}}_i$
- $H_u \in \mathbf{5}_i, H_d \in \bar{\mathbf{5}}_i$
- Universal trilinear  $A_0$ .
- $\tan \beta$ .



# SU(5) GUT



- ▶ CMS simplified models, 100% BR  $\tilde{q} \rightarrow q\tilde{\chi}_1^0$ .
- ▶  $\tilde{u}_L$  and  $\tilde{d}_L$  decays on other hand mainly in  $\tilde{\chi}^\pm + q'$ .
- ▶ We implemented our own recasting of the analysis.

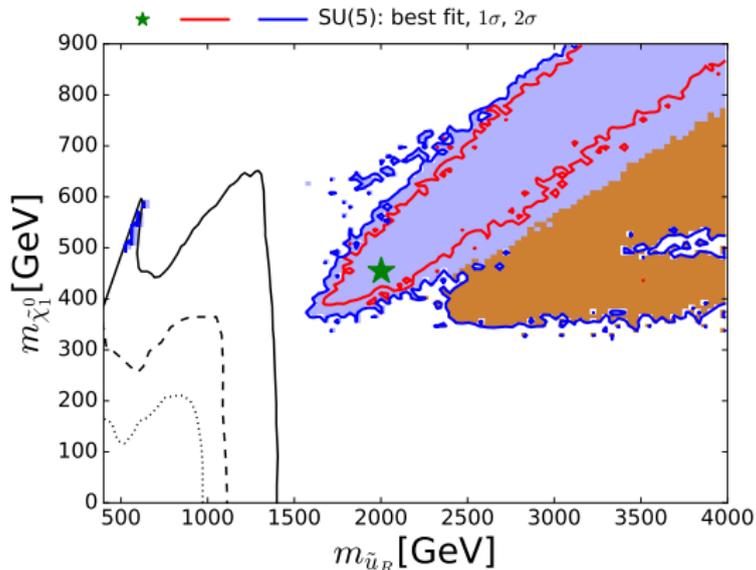


$\tilde{u}_R \rightarrow \tilde{\chi}_1^0 q$



$\tilde{u}_R \rightarrow \tilde{g} q$

# SU(5) GUT



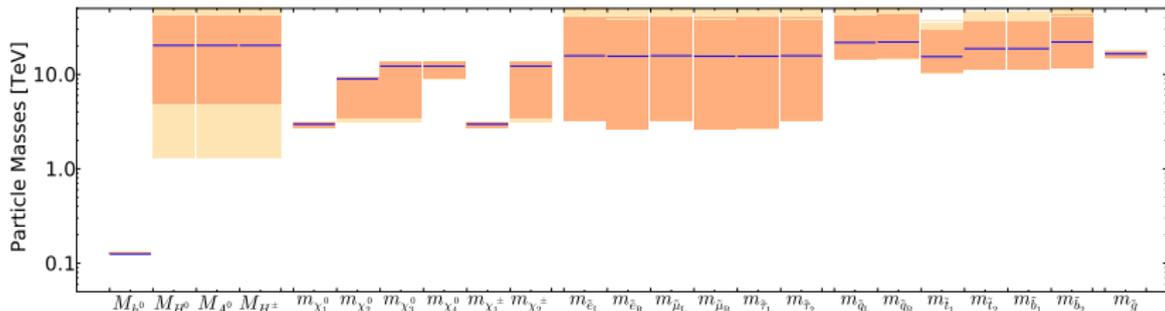
$\tilde{u}_R \rightarrow \tilde{\chi}_1^0 q$



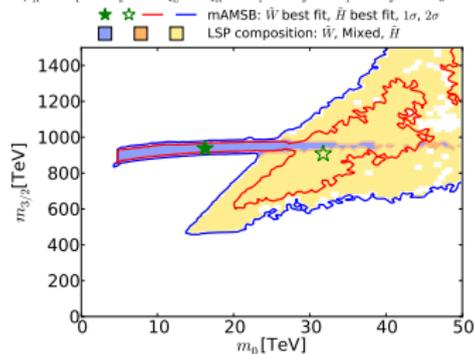
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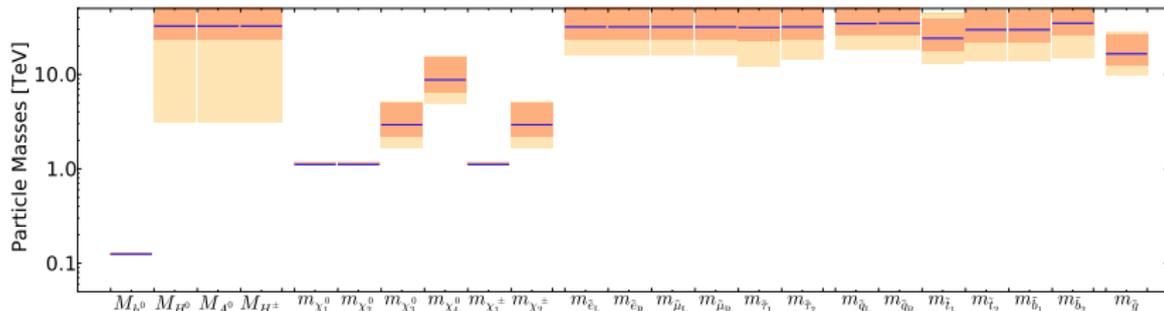
# mAMSB



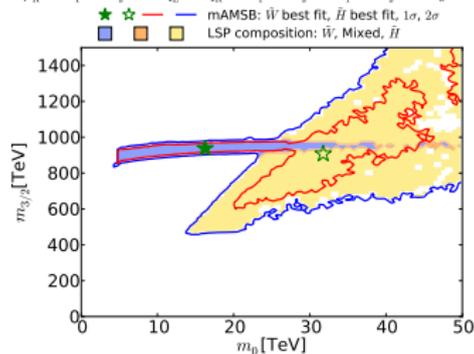
- ▶ SUSY breaking via loop-induced super-Weyl anomaly.
- ▶ Pure AMSB unrealistic (tachionic sleptons), add a term  $m_0$ .
- ▶ Three parameters:  $m_0$ ,  $m_{3/2}$  and  $\tan\beta$ .
- ▶ Sign of  $\mu$  is also free.



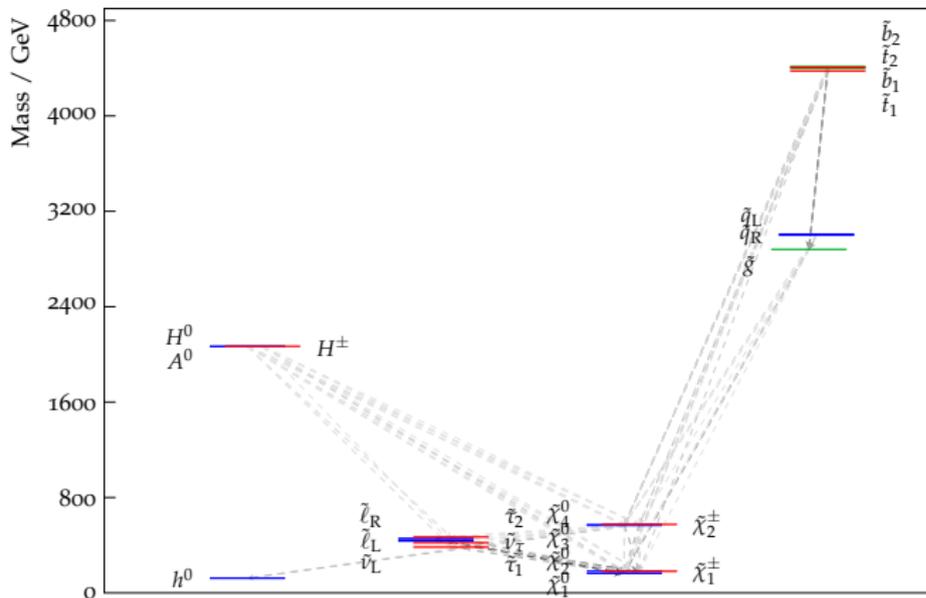
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- ▶ Three parameters:  $m_0$ ,  $m_{3/2}$  and  $\tan\beta$ .
- ▶ Sign of  $\mu$  is also free.



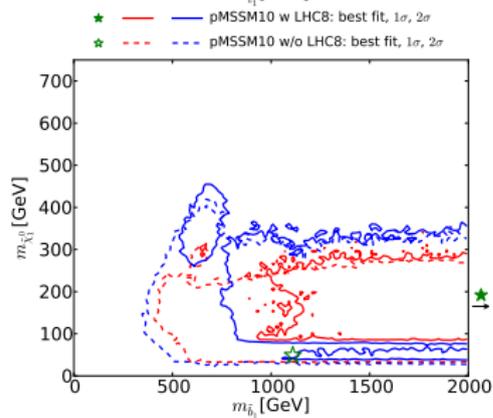
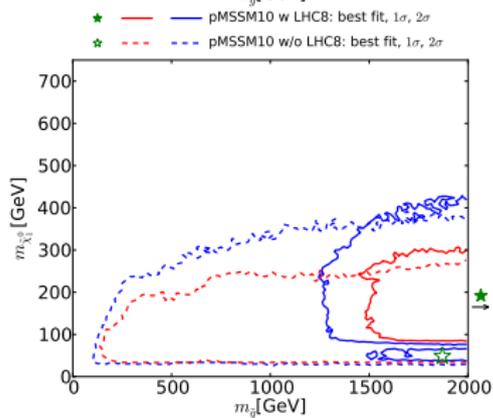
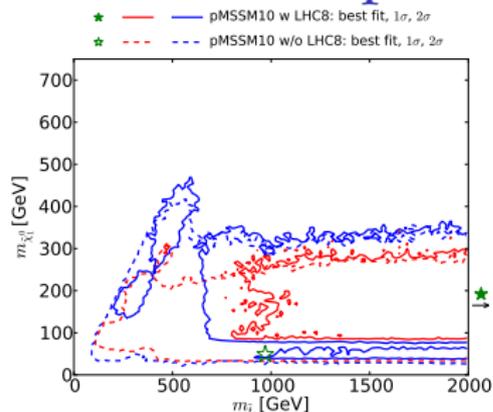
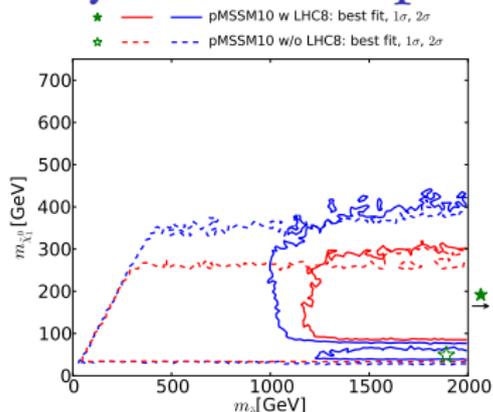
# pMSSM10 best fit point



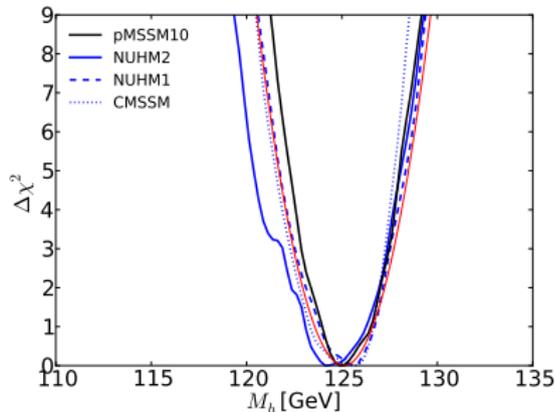
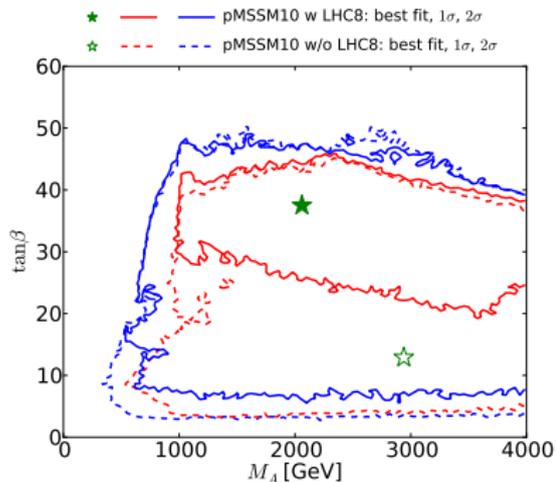
Parameter	Best-fit
$M_1$	170 GeV
$M_2$	170 GeV
$M_3$	2600 GeV
$m_{\tilde{q}}$	2880 GeV
$m_{\tilde{q}_3}$	4360 GeV
$m_{\tilde{l}}$	440 GeV
$M_A$	2070 GeV
$A$	790 GeV
$\mu$	550 GeV
$\tan \beta$	37.6

- ▶ Heavy Higgses, squarks, gluinos are relatively unconstrained.
- ▶ Left-handed fermion decay chains evolve via  $\tilde{\chi}_1^\pm$  and  $\tilde{\chi}_2^0$ .
- ▶ Sleptons are at less than 1 TeV.

# Physical mass planes for the colored sparticles



# Higgs physics



- ▶ pMSSM10 likelihood is very similar to the experimental value smeared by the theoretical uncertainty as given by FeynHiggs.
- ▶ Lower value of  $\tan\beta$  are disfavored at the 68% CL by LHC8<sub>EWK</sub>,  $(g-2)_\mu$  and DM constraints
- ▶ The constraints interplay with the choice of a single soft SUSY-breaking mass-parameter for the sleptons.