

Relaxing Λ

Enrico Trincherini
(Scuola Normale Superiore & INFN, Pisa)

with L. Alberte, P. Creminelli, A. Khmelnitsky and D. Pirtskhalava
1608.05715

The CC problem

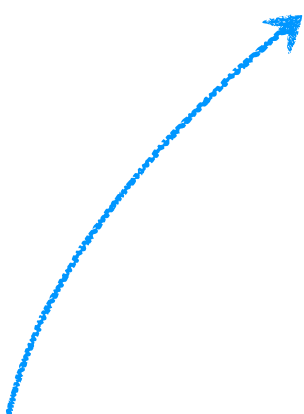
$$\langle T_{\mu\nu} \rangle = -\rho_{\text{vacuum}} g_{\mu\nu}$$

$$\rho_{\text{vacuum}} = \Lambda + \rho_{\text{vacuum}}^{SM} \qquad \simeq (10^{-3} \text{eV})^4$$

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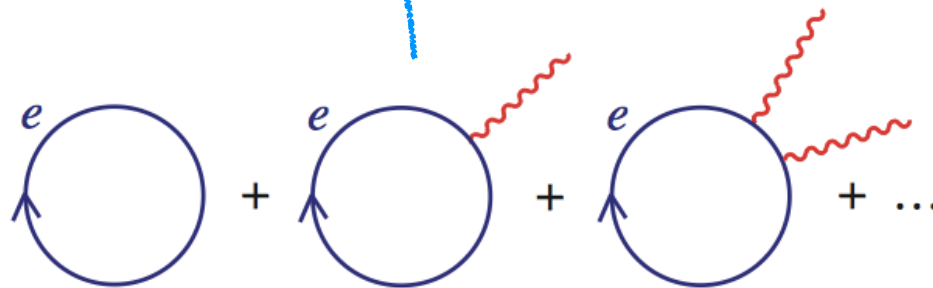
$$\int d^4x \sqrt{-g} (M_{\text{Pl}}^2 R - \Lambda)$$


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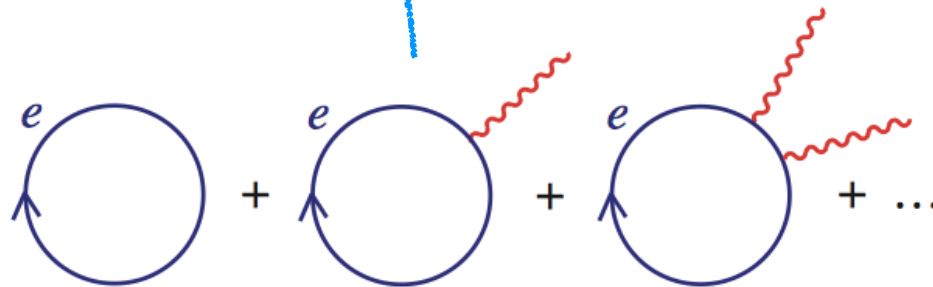
$$\rho_{\text{vacuum}} = \mathcal{O}(M_*^4) + \mathcal{O}(M_*^2 m_e^2) + \mathcal{O}(m_e^4 \log M_*/m_e)$$

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$$\int d^4x \sqrt{-g} (M_{\text{Pl}}^2 R - \Lambda)$$

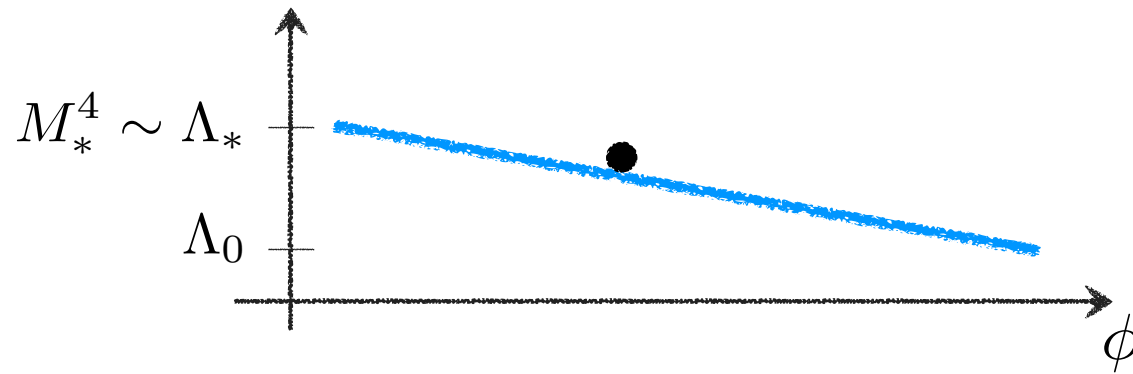


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A simple idea...

Abbott '85

Add a compensating field whose vacuum energy dynamically adjusts itself to cancel the large contribution to the CC

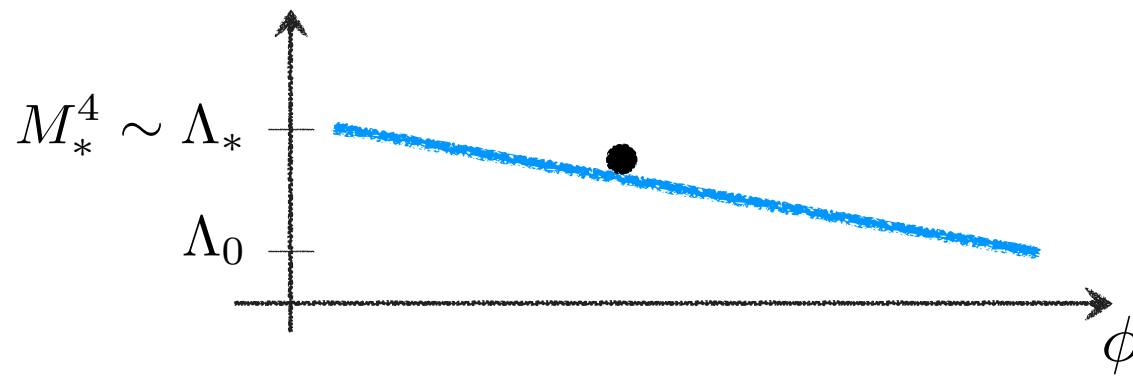


Explain why this dynamics produces the observed value of the CC
Involve very small mass scales: they must be radiatively stable

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...that doesn't work

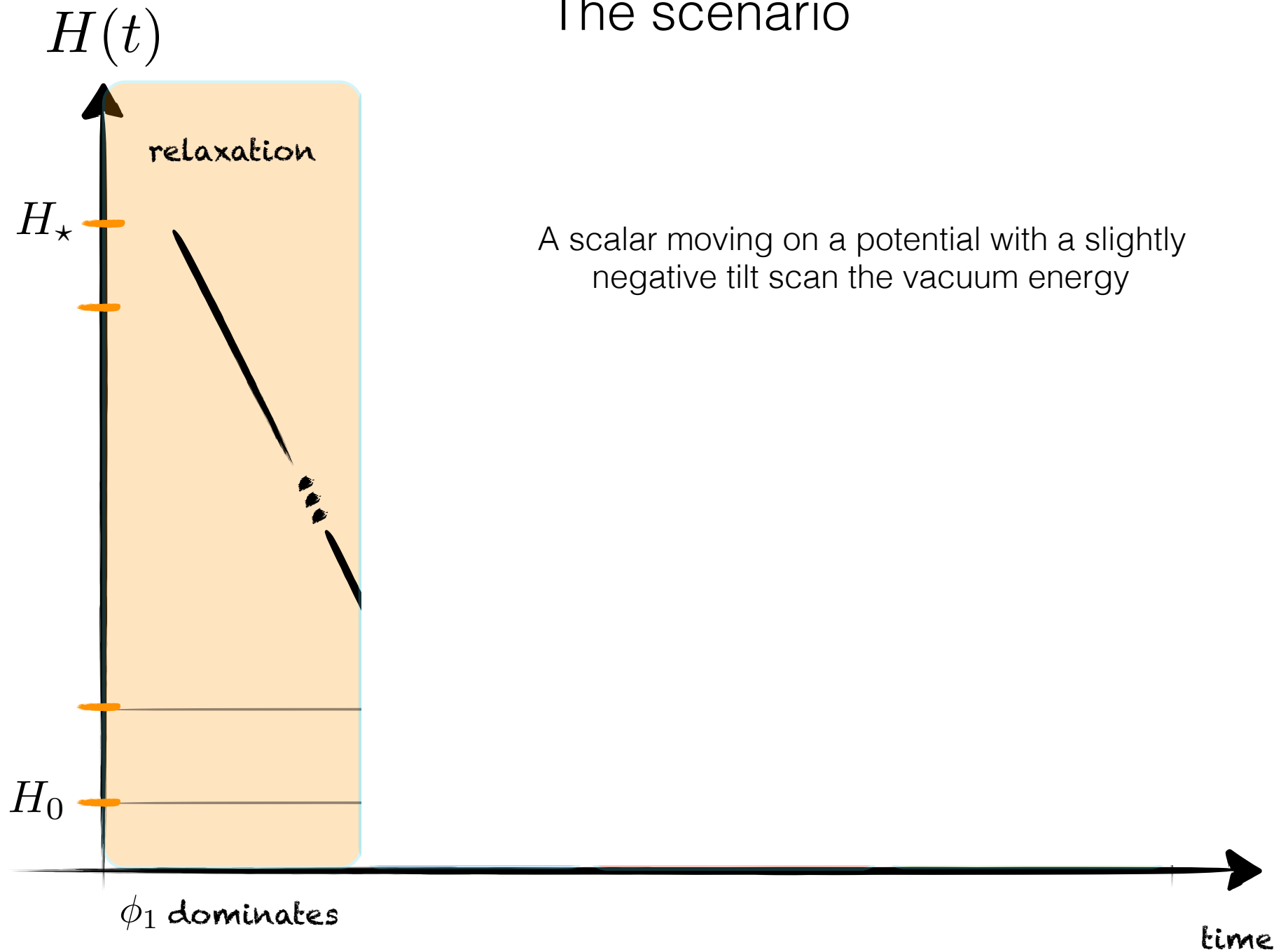
Empty Universe

Sensitive to small Λ only when the Universe is empty

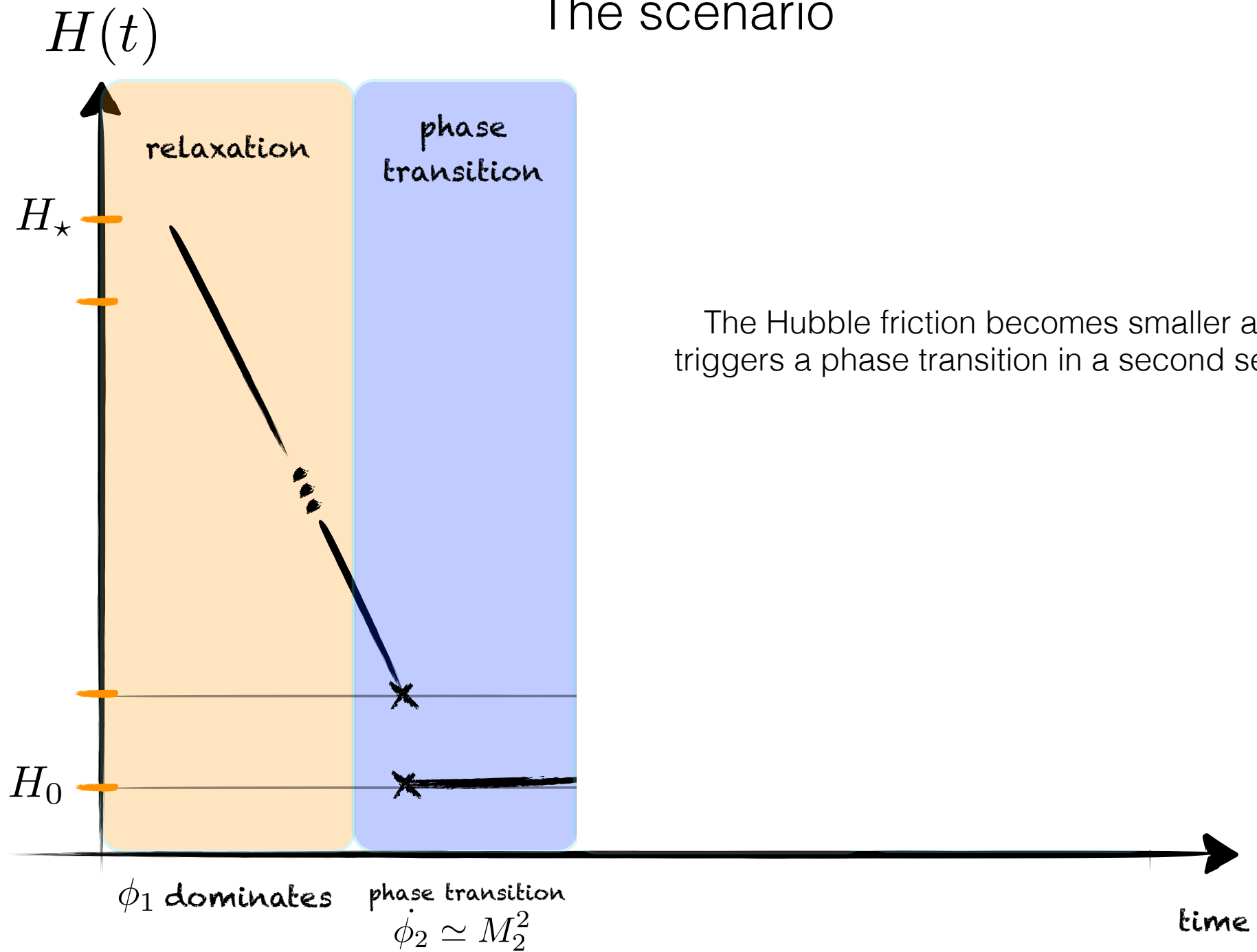
Eternal inflation

In which minimum do we live? Measure problem

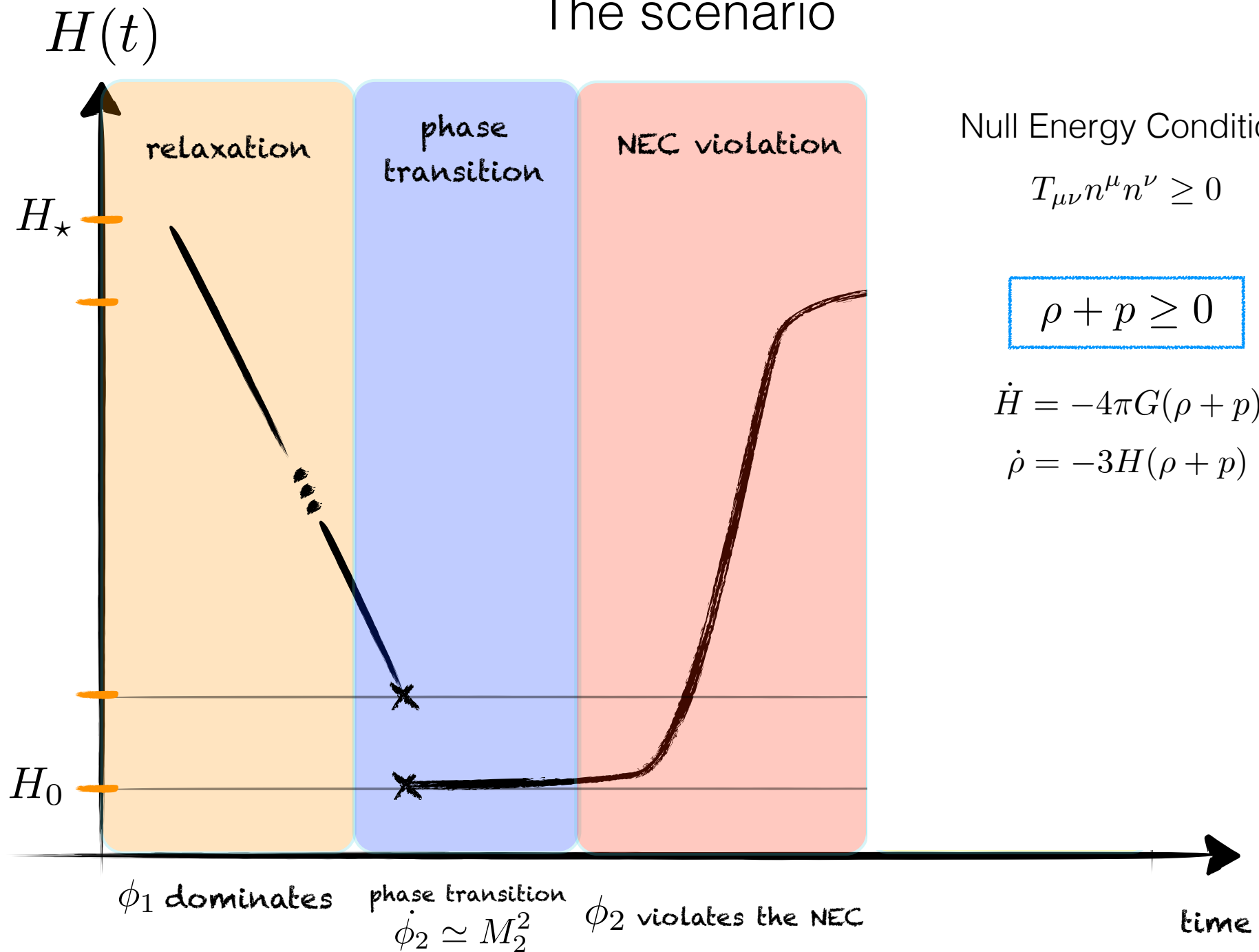
The scenario



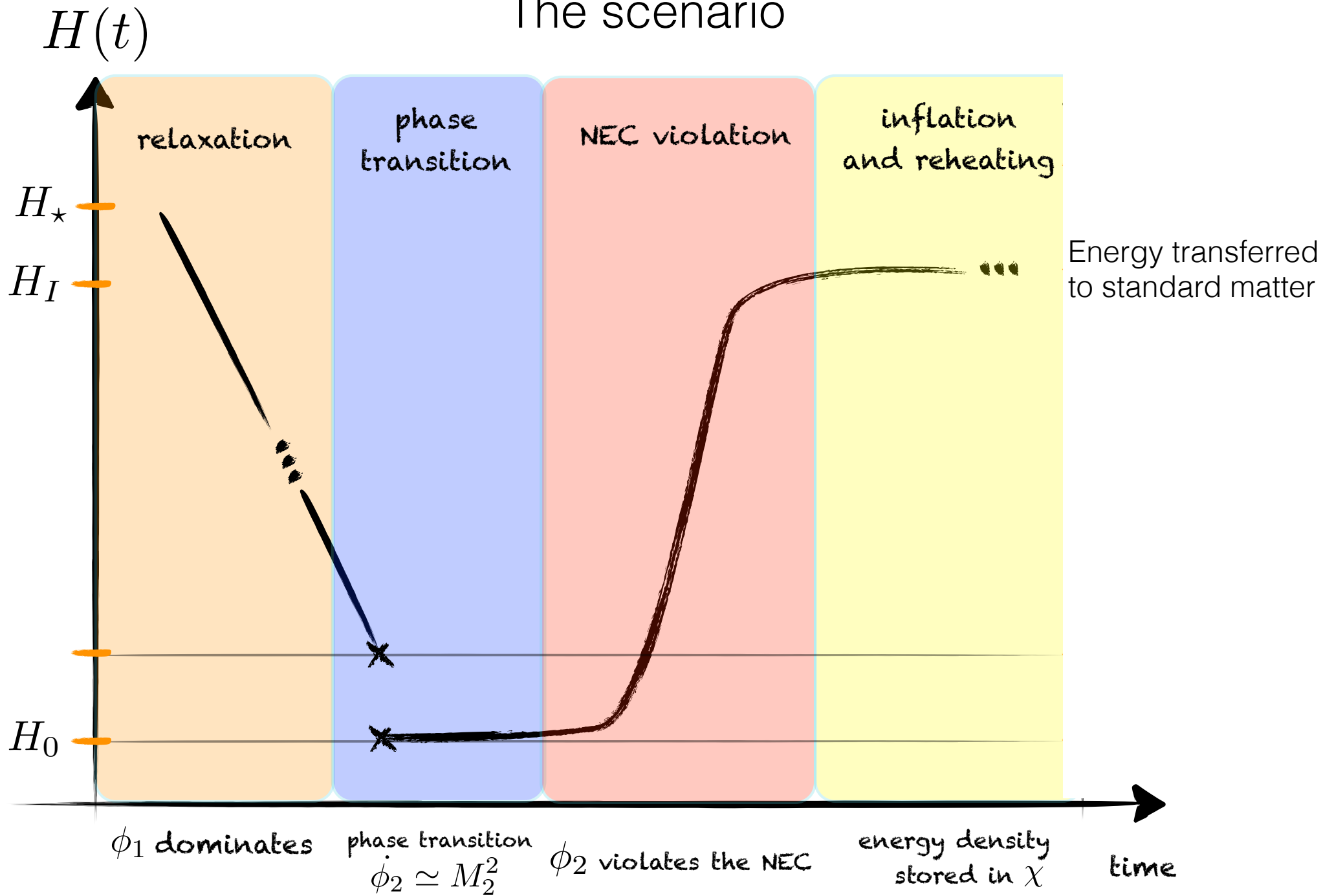
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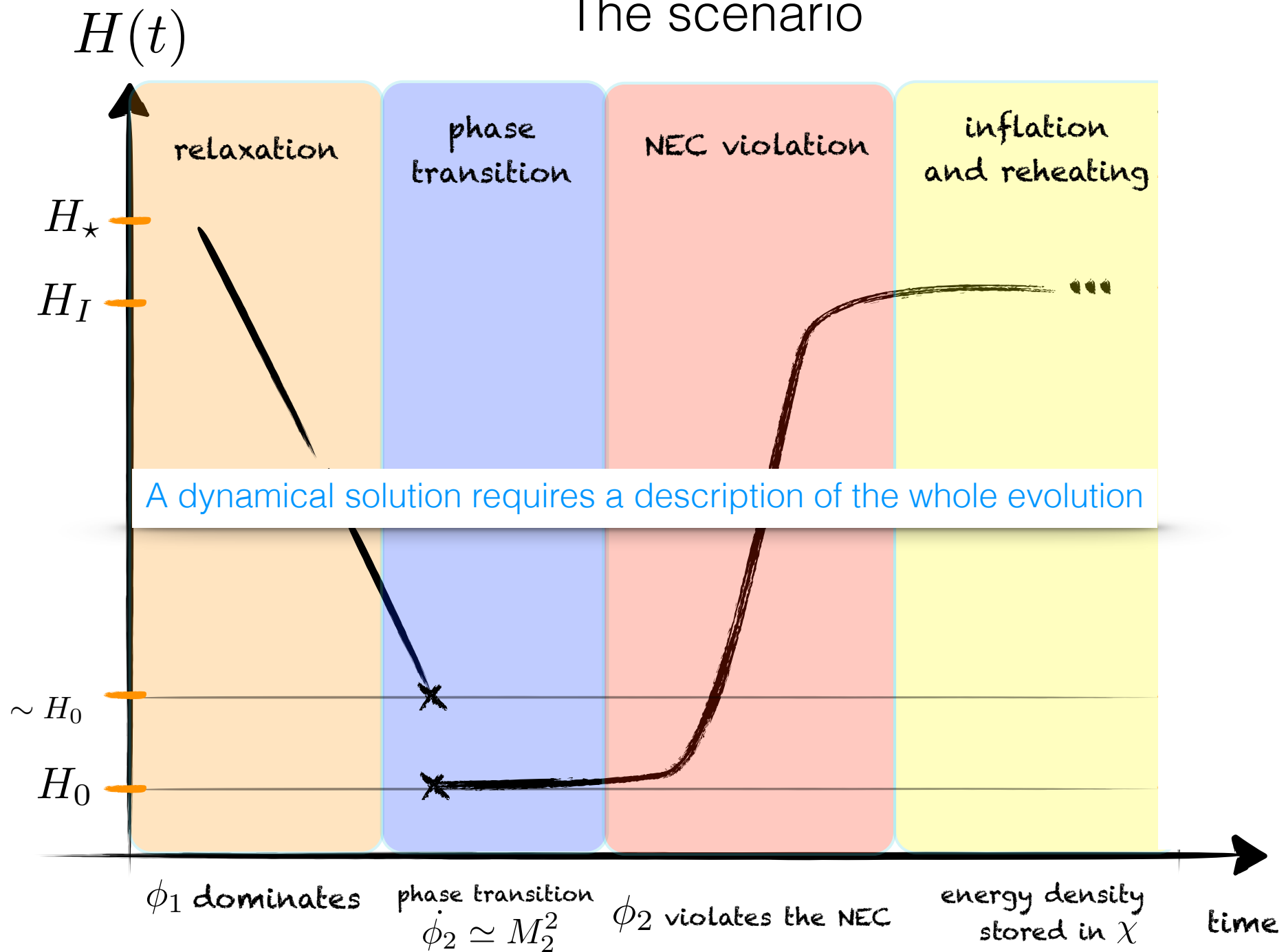
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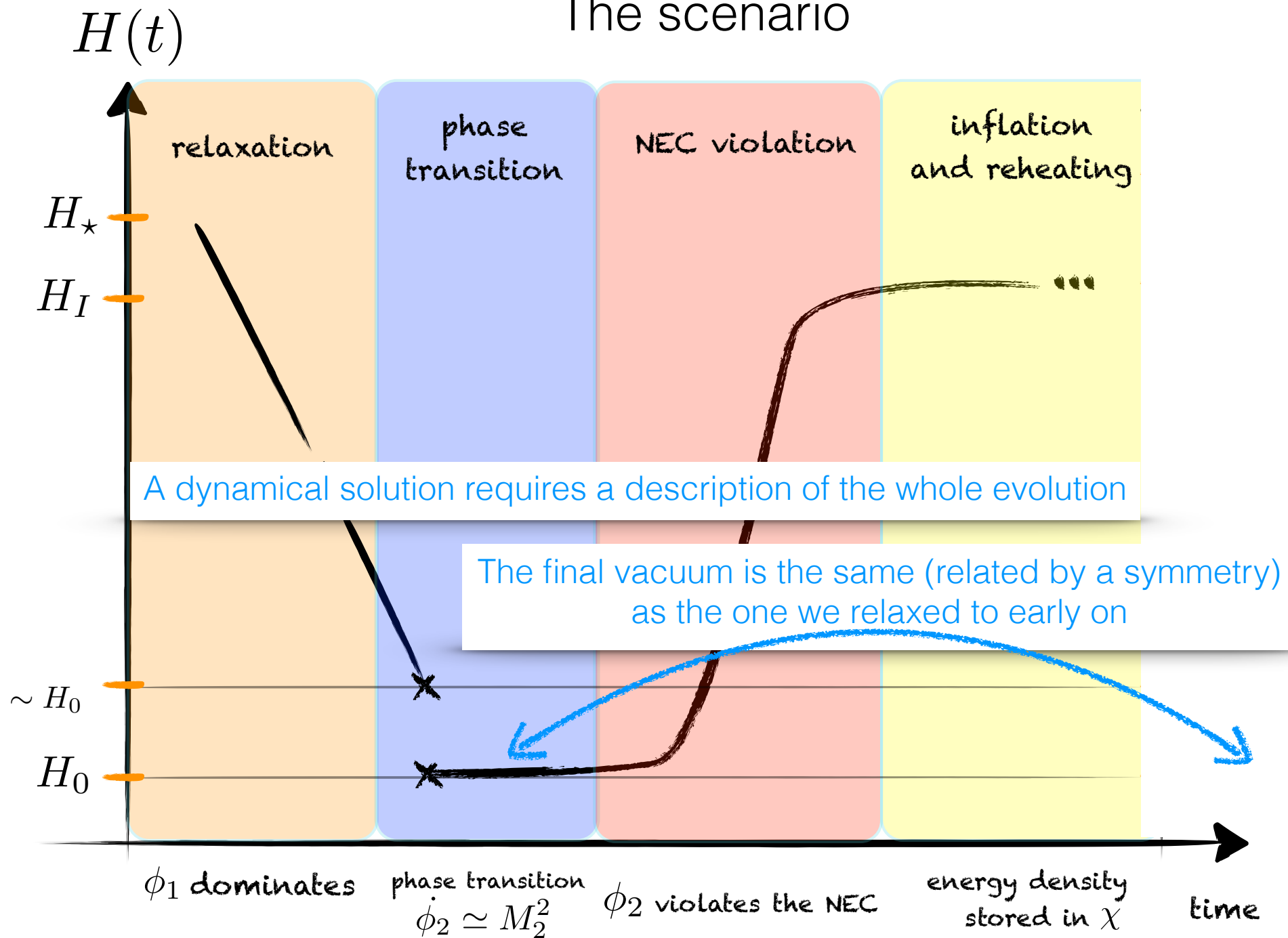
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Additional motivations

The only motivation for dark energy is the CC problem
but no DE model addresses it

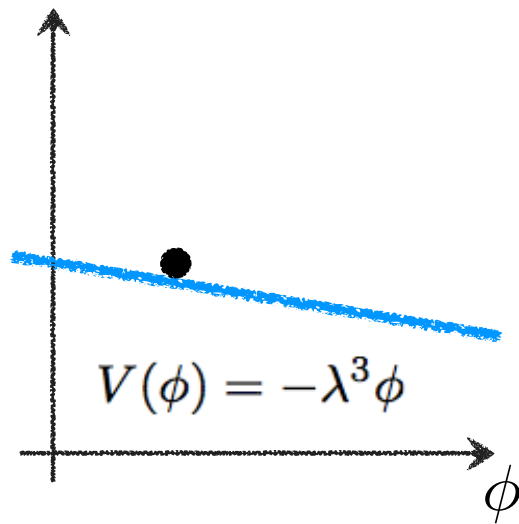
In this scenario two DE component related to the CC problem!

Is NEC violation theoretically consistent? Possible UV obstruction

The relaxing sector

Stable under $O(1)$ variation of Λ_*

Avoid eternal inflation and all the measure related issues



Slow roll

$$\lambda_1^3 \ll M_{\text{Pl}} H^2$$

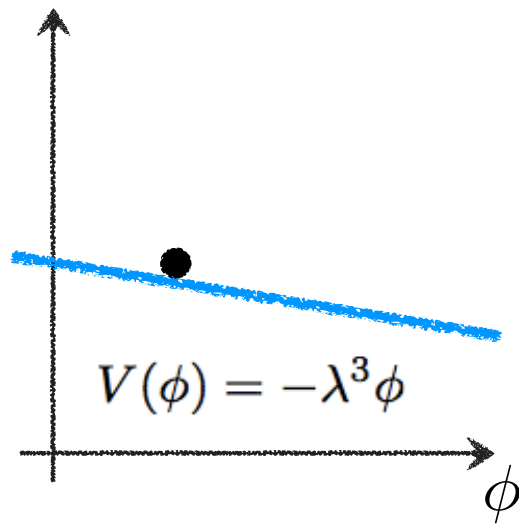
Classical evolution $\dot{\phi}_1 \frac{1}{H} \gg H \Rightarrow \lambda_1^3 \gg H^3$

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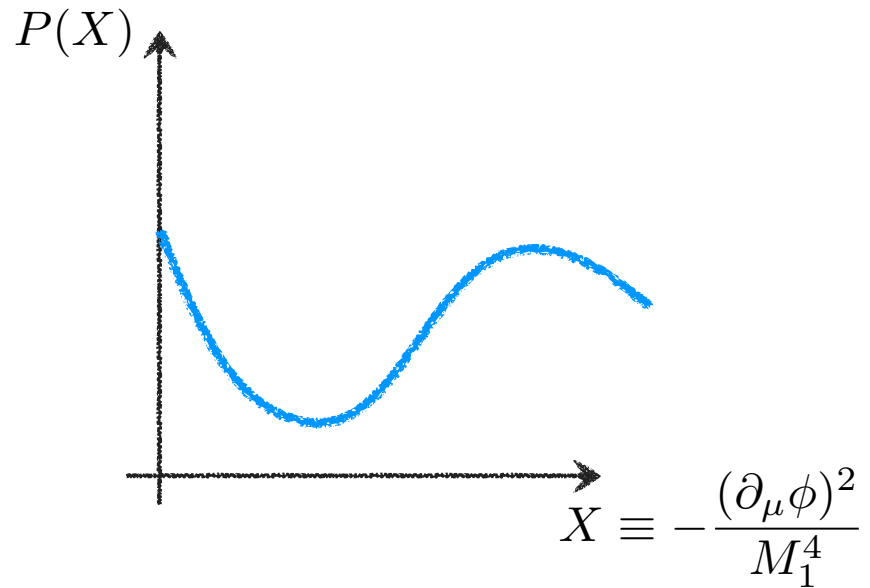
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Keep a classical motion even if $\lambda_1^3 \rightarrow 0$

A scalar field in the “Ghost condensate” regime

The relaxing sector



The ghost condensate

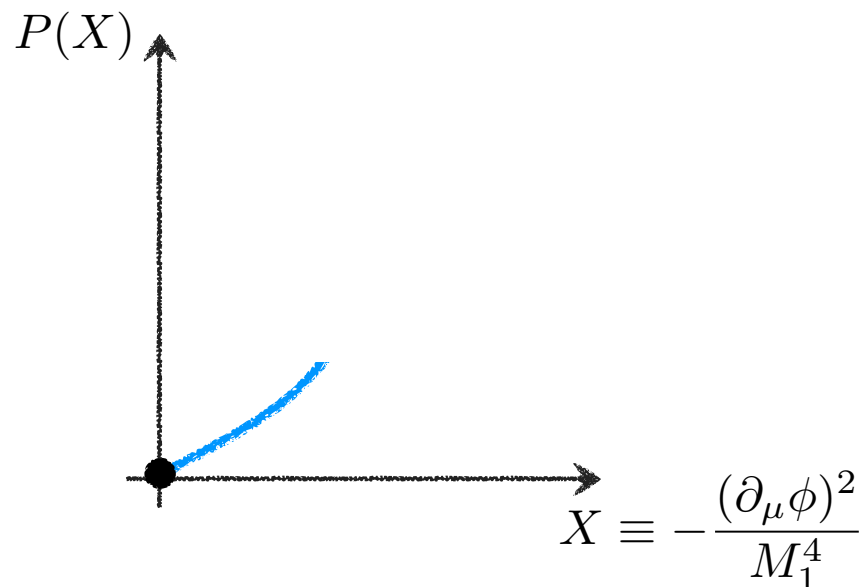
Arkani-Hamed, Cheng, Luty, Mukohyama '03

$$S = \int d^4x \sqrt{-g} \left[M_1^4 P_1(X_1) + \cancel{\lambda_1^3 \phi_1} - \Lambda_\star + \dots \right]$$

The relaxing sector

The ghost condensate

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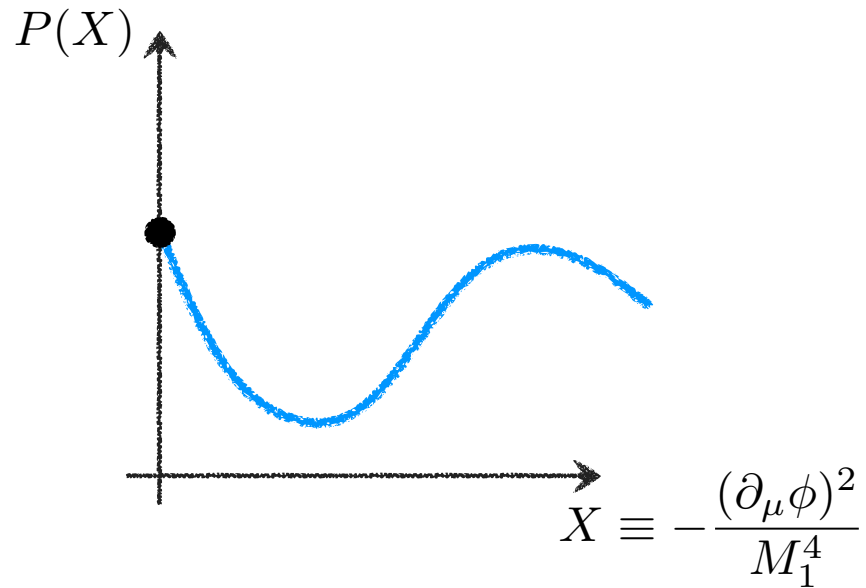


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$-(\partial_\mu \phi_1)^2 + \dots$

A blue arrow points from the term $-(\partial_\mu \phi_1)^2 + \dots$ to the $M_1^4 P_1(X_1)$ term in the action, indicating its identification with X in the potential.

The relaxing sector

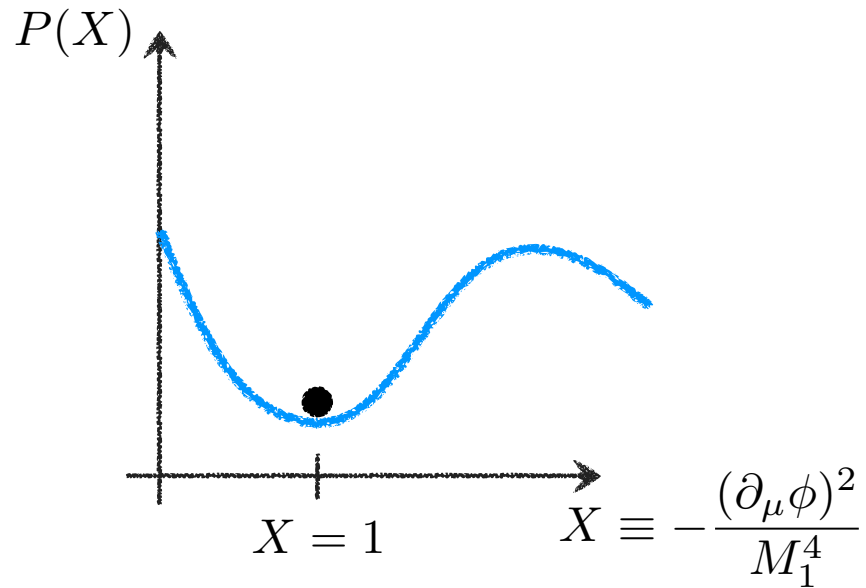


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$$\phi_1 = M_1^2 t + \pi_1(\vec{x}, t) \quad \omega^2 \sim \frac{k^4}{M_1^2}$$

Once minimally coupled to gravity
it sources dS

The relaxing sector

The ghost condensate

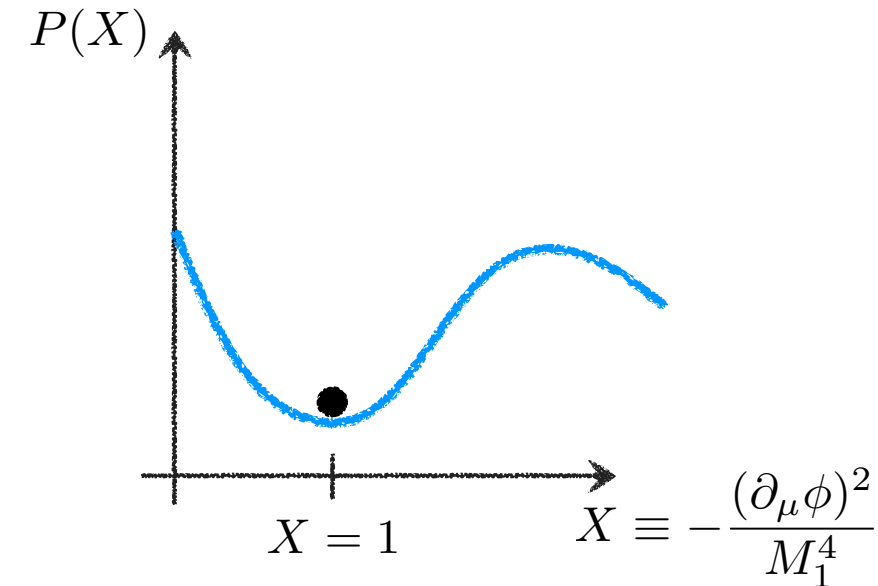
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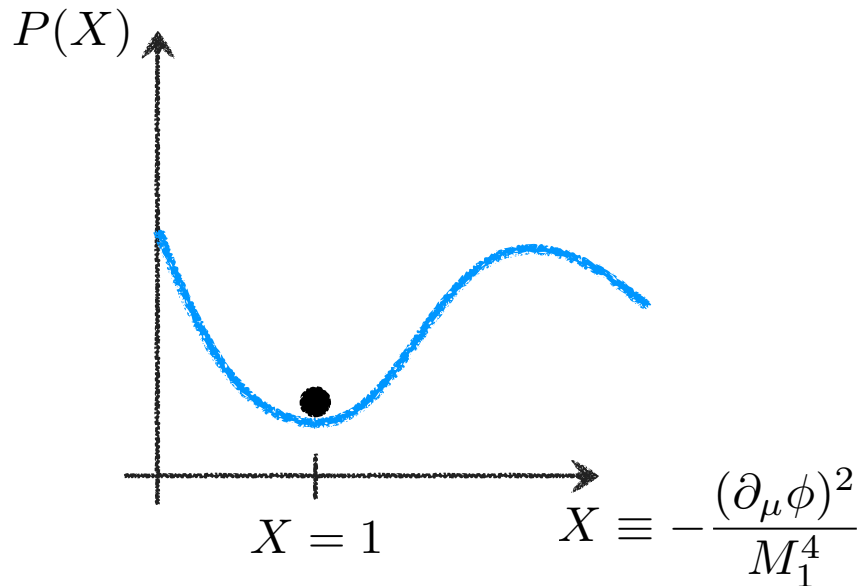
With a **tilted potential**, the solution is perturbed by a homogeneous $\pi_1(t)$ with

It is a small perturbation if $\lambda_1^3 \ll 3H M_1^2$

$$\dot{\pi}_1 \simeq \frac{\lambda_1^3}{3H}$$

$\frac{(\delta\phi_1)_{\text{quant}}}{(\delta\phi_1)_{\text{class}}} \sim \left(\frac{H}{M_1} \right)^{5/4}$ The amplitude of fluctuations is independent of the tilt of the potential

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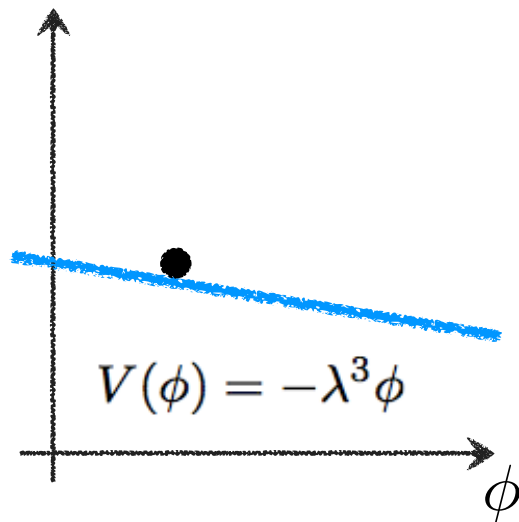
Mixing with gravity introduces a Jeans-like instability for long modes $\omega^2 \sim \frac{k^4}{M_1^2} - \frac{M_1^2}{M_{\text{Pl}}^2} k^2$

Characteristic time of instab longer than H_0 constrains the cutoff $M_1^3 < M_{\text{Pl}}^2 H_0 \sim (10 \text{ MeV})^3$

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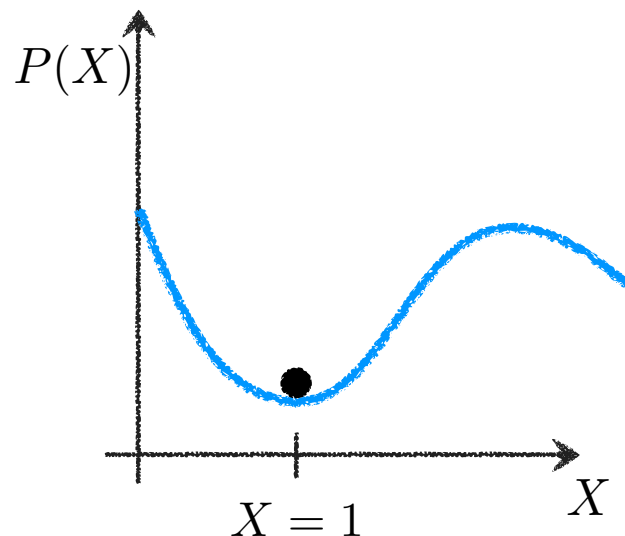


Slow roll

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$$\Lambda_* \sim M_{\text{Pl}}^{8/3} H_0^{4/3} \sim (10 \text{ MeV})^4$$



Classical evolution

No constraints

But relaxation within EFT $H_* < M_1$

$$\Lambda_* \sim M_{\text{Pl}}^{10/3} H_0^{2/3} \sim (10^5 \text{ TeV})^4$$

Slow roll

$$\epsilon_0 \equiv \left(-\frac{\dot{H}}{H^2} \right)_{H=H_0} \sim \frac{\lambda_1^3 m_1^2}{6 M_{\text{Pl}}^2 H_0^3} \ll 1$$

The trigger

The ~~NEC~~ given by a second sector ϕ_2 with UV cutoff M_2

A phase transition $\phi_2 = \text{const} \rightarrow \phi_2 \sim \phi_{\text{NEC}}$ is triggered by ϕ_1 when vacuum energy $\sim \Lambda_0$

The PT will change the vacuum energy $\sim M_2^4$

$$M_2 \simeq \Lambda_0^{1/4} \sim 10^{-3} \text{ eV}$$

The trigger

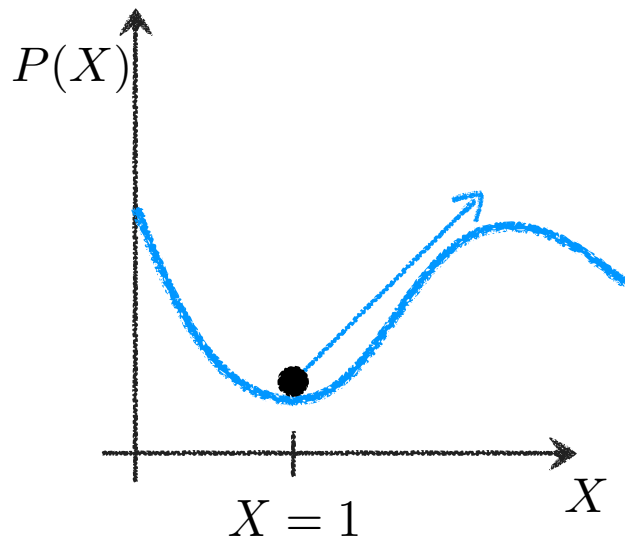
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When is the NEC-violation activated?



π_1 grows with the relaxation of the CC as a result of the reduced Hubble friction

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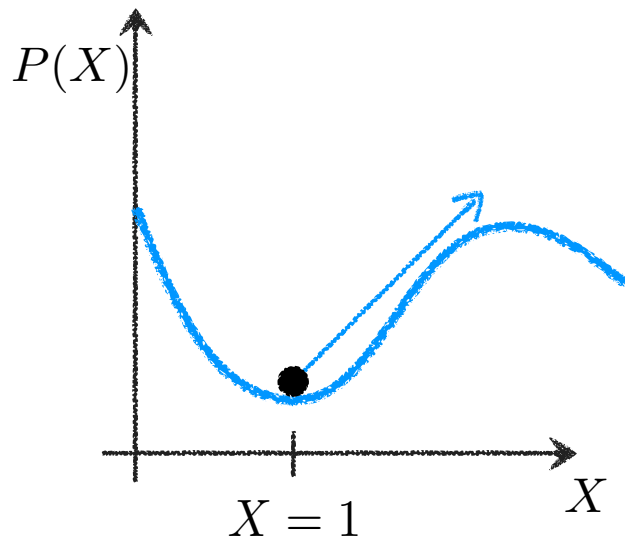
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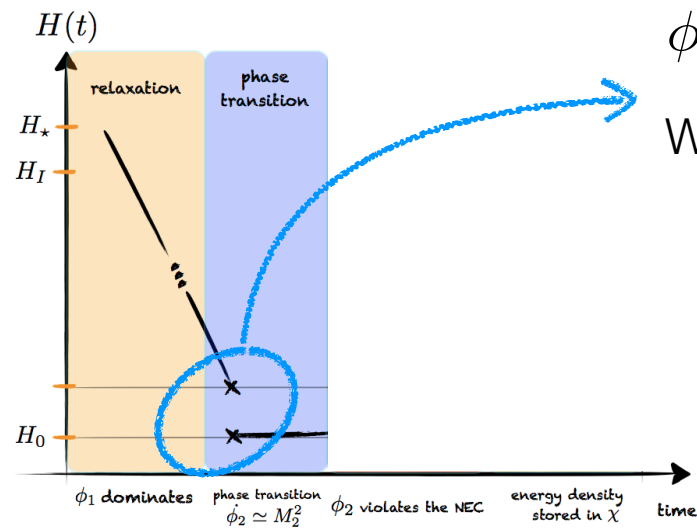
Suppose $\int d^4x \sqrt{-g} M_2^4 P(X_1, X_2)$

This interaction affects significantly the dynamics of the second field when $\dot{\pi}_1 \sim M_1^2$

The observed value of the vacuum energy is fixed in terms of the parameters

$$\Lambda_0 \sim \frac{\lambda_1^6 M_{\text{Pl}}^2}{M_1^4}$$

The trigger



$$\phi_2 = \text{const} \rightarrow \phi_2 \sim \phi_{\text{NEC}}$$

When $\frac{\dot{\pi}_1}{M_1^2} \equiv x \sim 1$

What happens to ϕ_1 ?

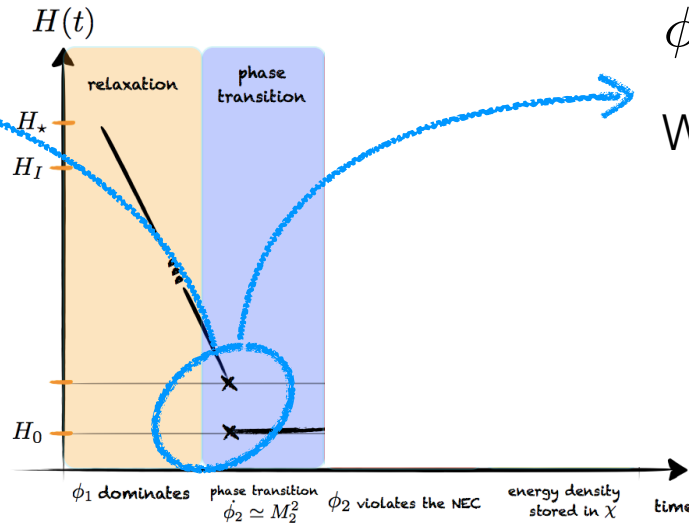
$$\phi_1 = M_1^2 t + \pi_1 \rightarrow \phi_1 = \text{const}$$

The trigger

Jump in vacuum energy $\sim M_1^4$

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Phase transition when $x \sim 1$

The EFT for the scanning field breaks down:

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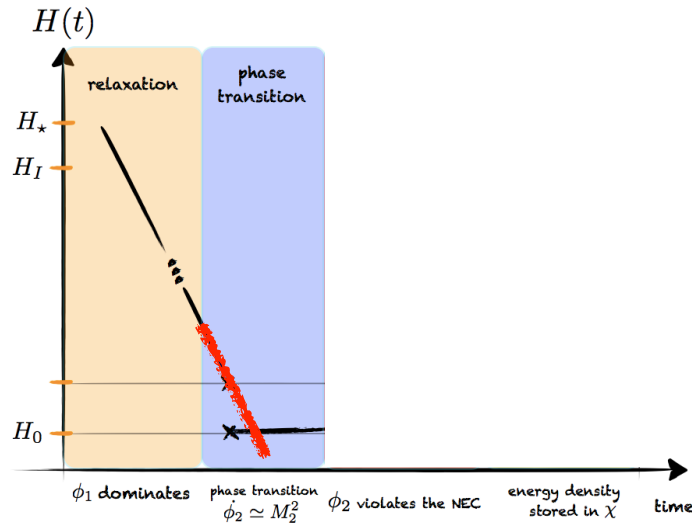
Scanning of the CC stops at Λ_0

Unlimited time for ~~NEC~~

$$M_1 \simeq M_2 \simeq \Lambda_0^{1/4} \sim 10^{-3} \text{ eV}$$

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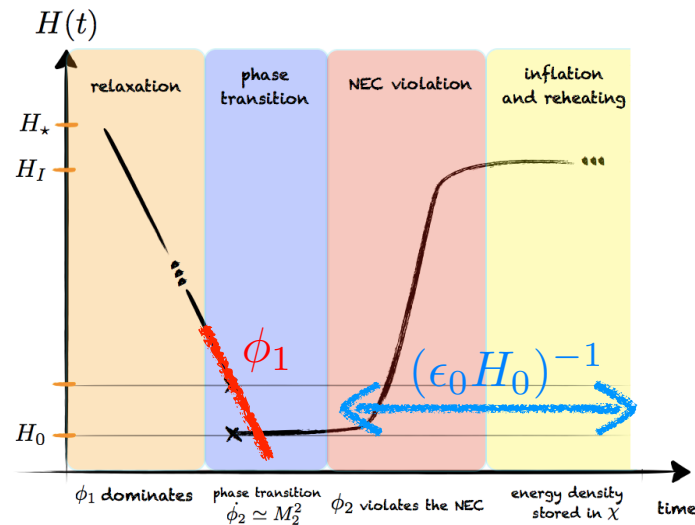
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Scenario 2: Fast ~~NEC~~

Phase transition when $x \lesssim 1$

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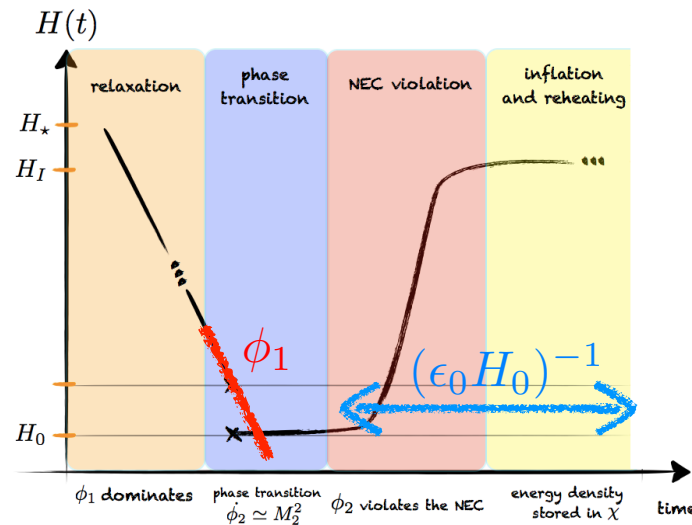
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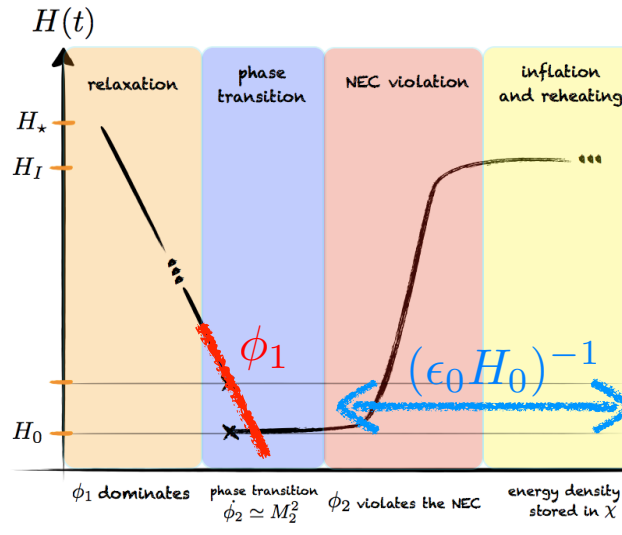
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$$\Lambda_* \lesssim M_{\text{Pl}}^2 M_1^2 \sim (1 \text{ TeV})^4 \left(\frac{\epsilon_0}{x} \right)^{1/2}$$

Constrained by **current** dark energy eq of state

$$\epsilon_0 \lesssim 0.05$$

The trigger



The evolution drives the energy to negative values: contraction and collapse within

$$\epsilon_0^{-1/3} H_0^{-1}$$

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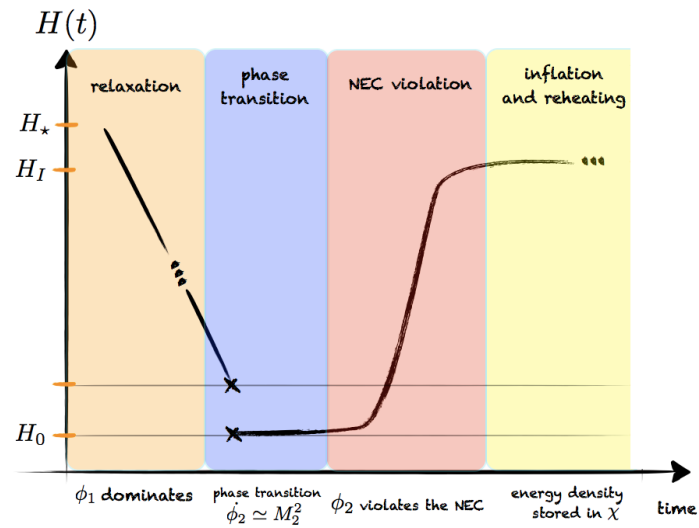
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The model can relax up to $O(\text{TeV})$ CC after huge field excursion $\Delta\phi_1 \sim M_{\text{Pl}} \frac{M_{\text{Pl}}}{H_0}$

NEC violators

$$T_{\mu\nu}k^\mu k^\nu \geq 0 \Rightarrow \rho + p \geq 0 \quad \dot{\rho} = -3H(\rho + p)$$

Usually associated to [instabilities](#)

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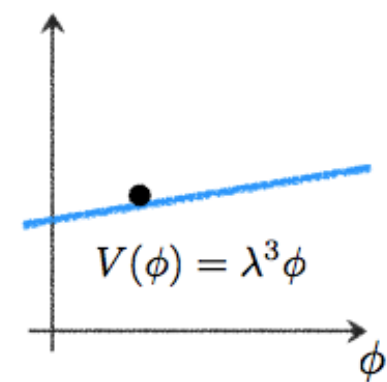
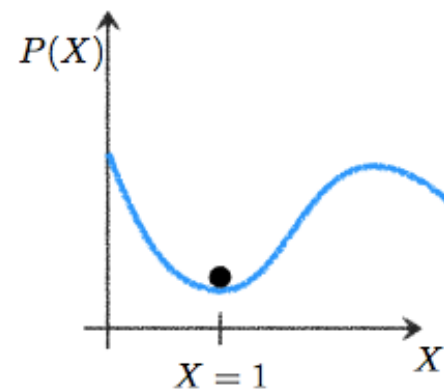
1) The Galileon

[Nicolis, Rattazzi, ET '09](#)

2) The ghost condensate

Deform the theory with a [rising](#) potential

[Creminelli, Luty, Nicolis, Senatore '06](#)

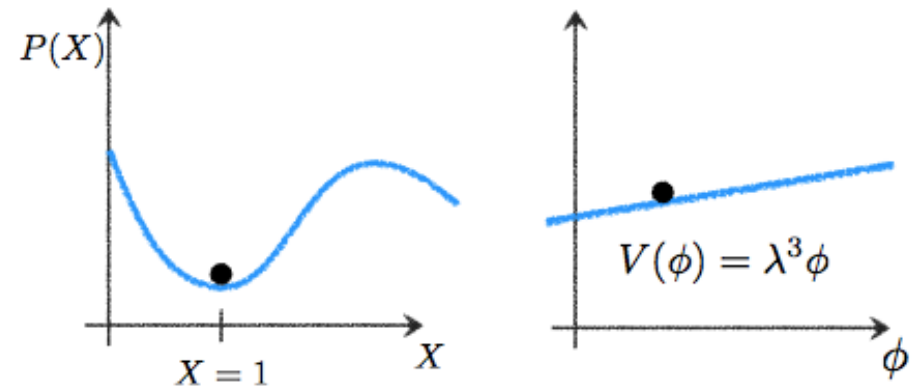


NEC violators

2) The ghost condensate

Deform the theory with a **rising** potential

Creminelli, Luty, Nicolis, Senatore '06



Jeans-like instability

$$\omega_{\text{Jeans}} \sim M_2^3 / M_{\text{Pl}}^2$$



$$M_2 \lesssim (M_{\text{Pl}}^2 H_0)^{1/3} \sim 10 \text{ MeV}$$

Harmless if $\omega < H$

Gradient instability

$$\omega_{\text{grad}} \sim \dot{H} M_{\text{Pl}}^2 / M_2^3$$

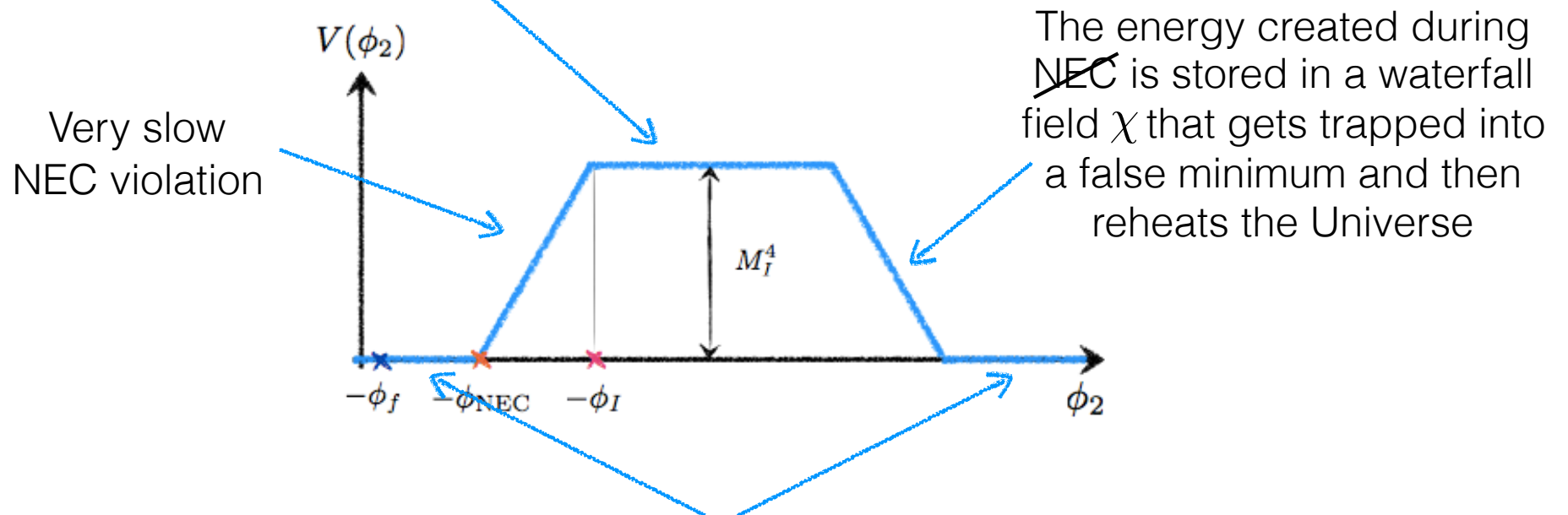
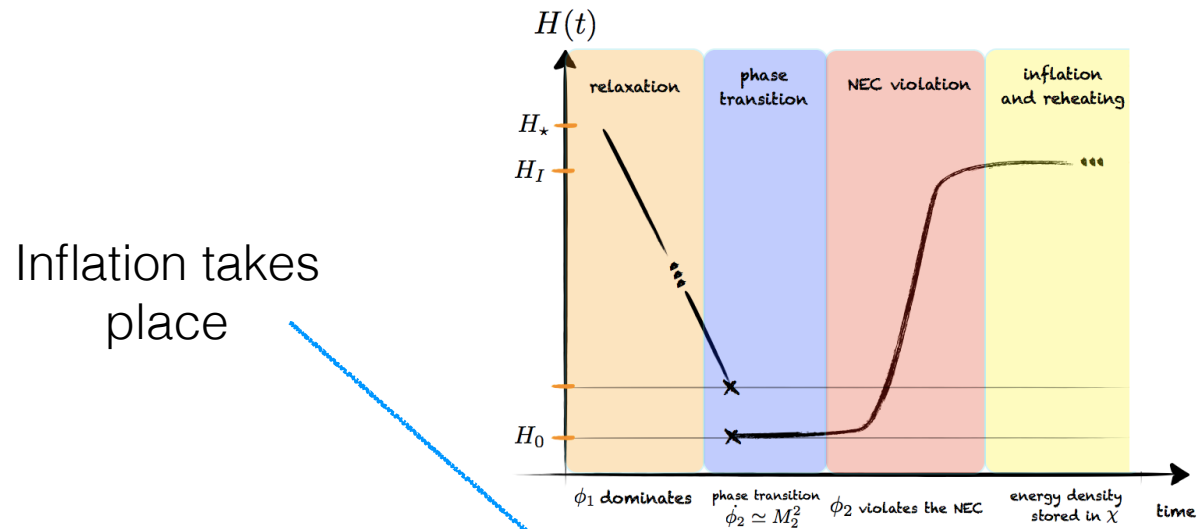
$$\omega^2 \sim \frac{k^4}{M_2^2} - \frac{\dot{H} M_{\text{Pl}}^2 k^2}{M_2^4}$$



$$\lambda_2^3 \lesssim M_2 H_0^2$$

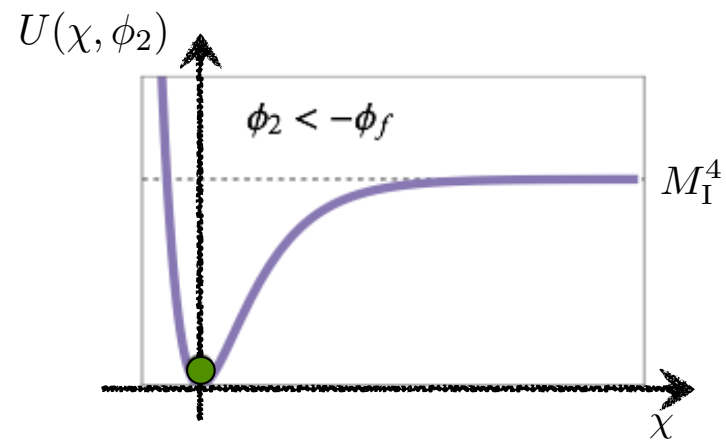
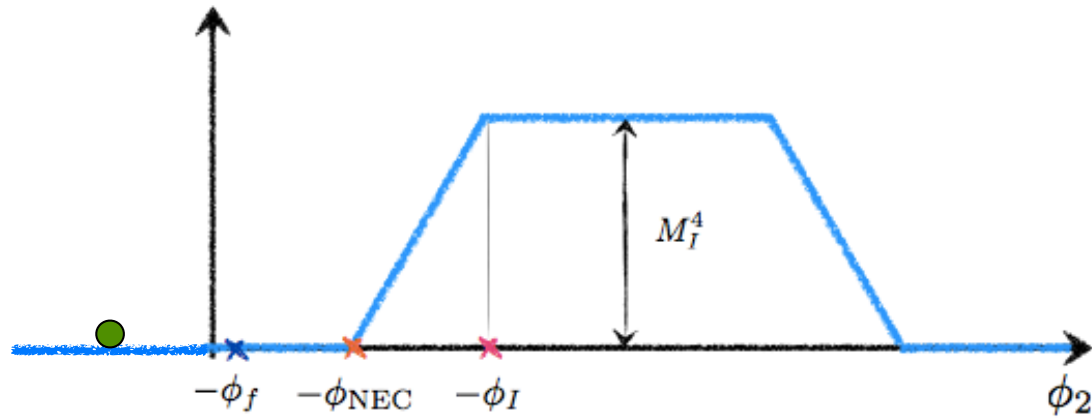
$$\frac{\lambda_2}{M_I} \sim 10^{-35} \quad \text{for maximal } M_I$$

Slow NEC violation

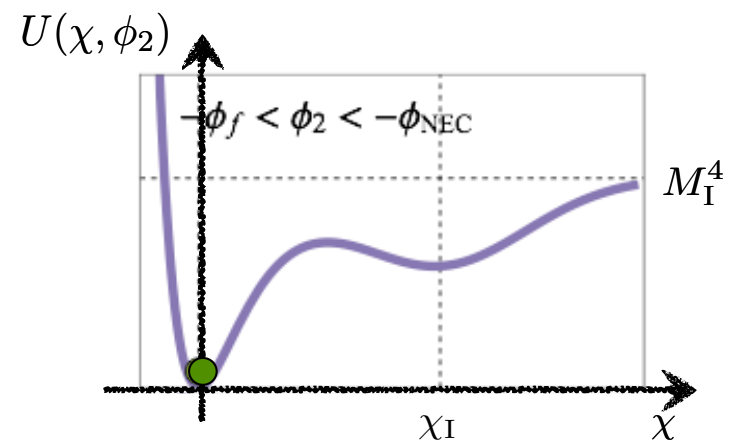
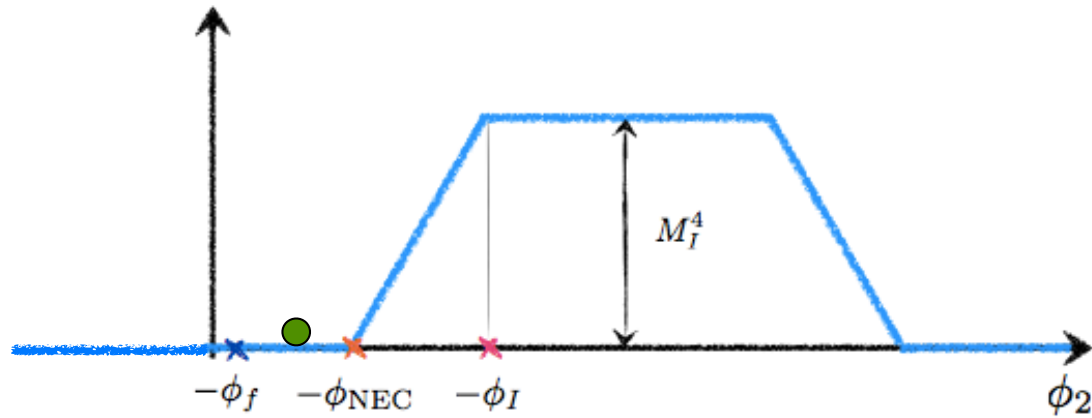


Same CC before and after NEC violation due to a Z_2 symmetry of the action

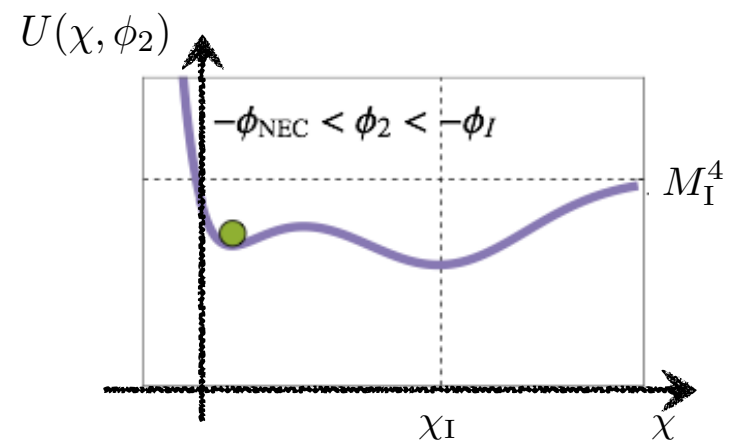
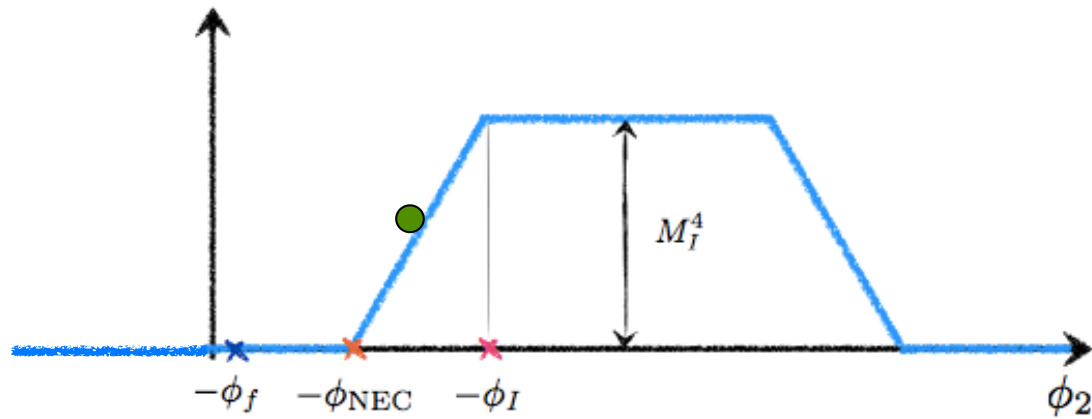
Inflation and Reheating



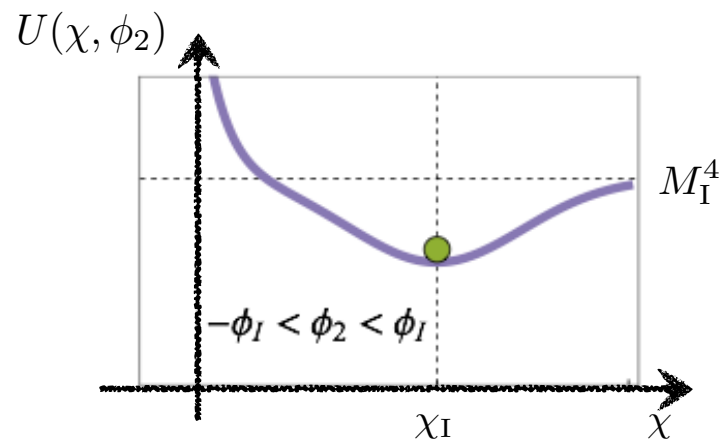
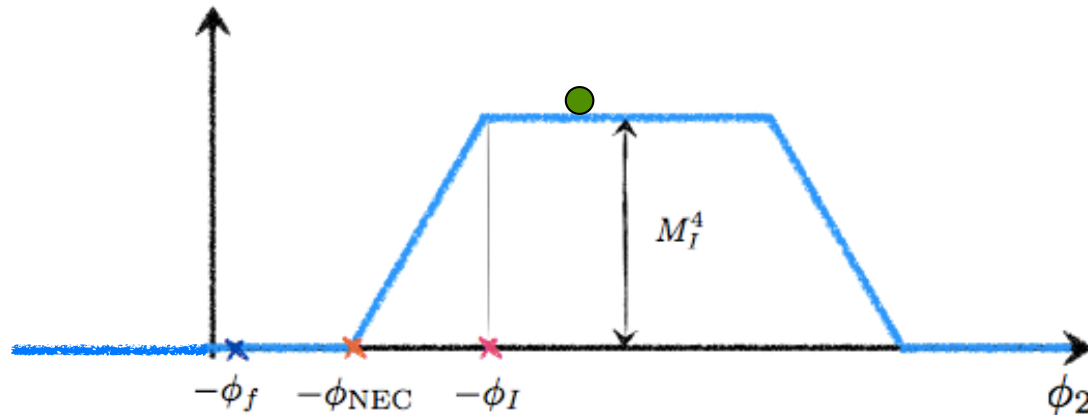
Inflation and Reheating



Inflation and Reheating



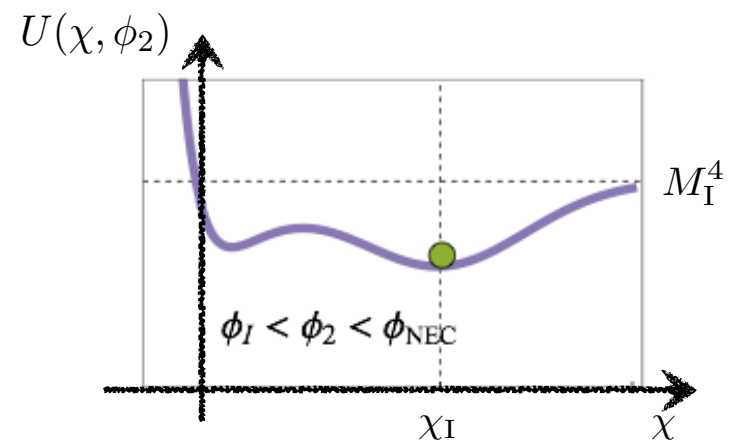
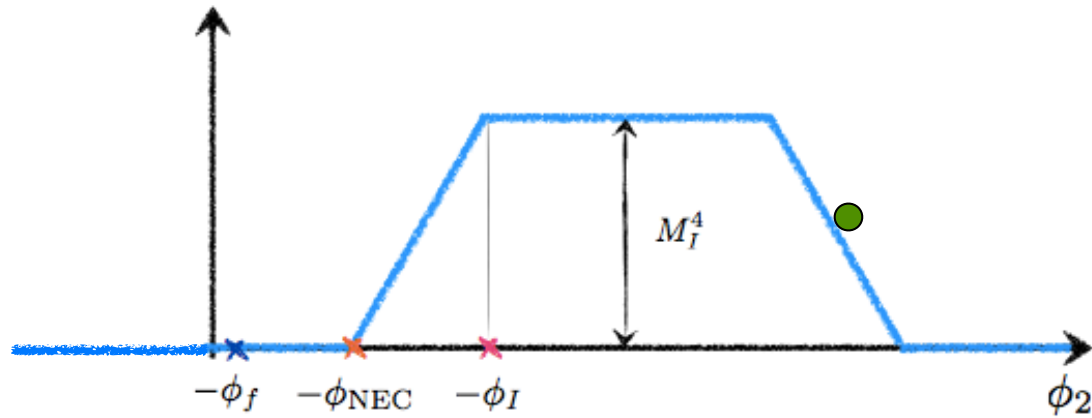
Inflation and Reheating



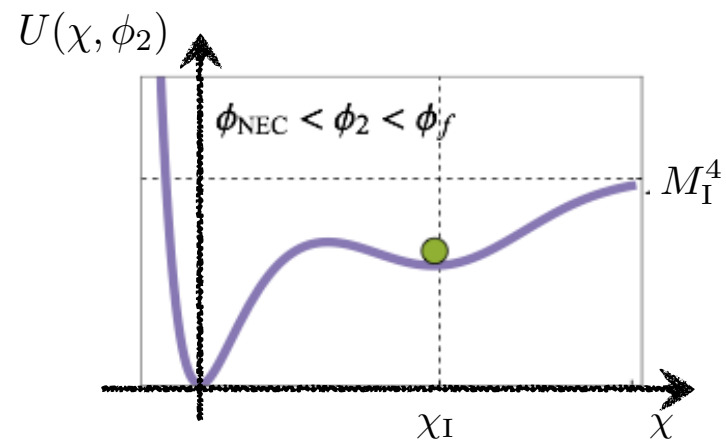
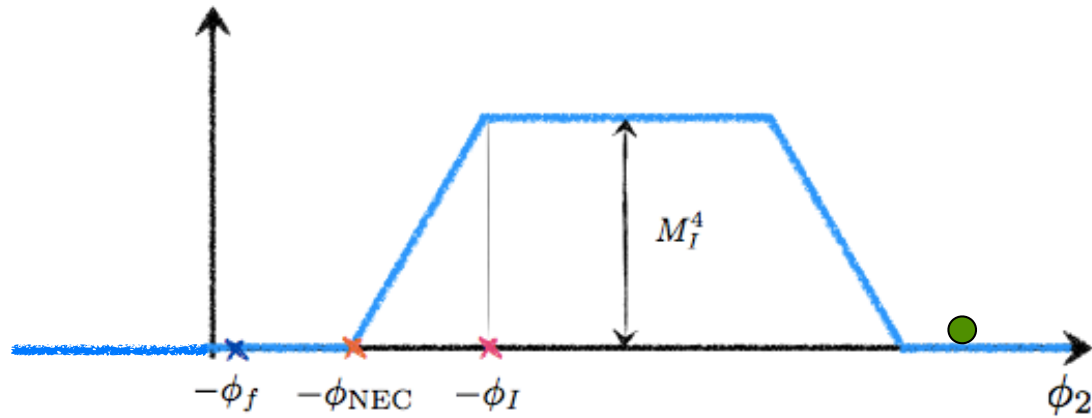
While χ is sitting in the false vacuum, the common potential $U(\chi, \phi_2)$ is nearly flat and the Universe inflates

Ghost inflation \longrightarrow peculiar phenomenology $(H_I M_{\text{Pl}})^2 \sim (10 \text{ GeV})^4$

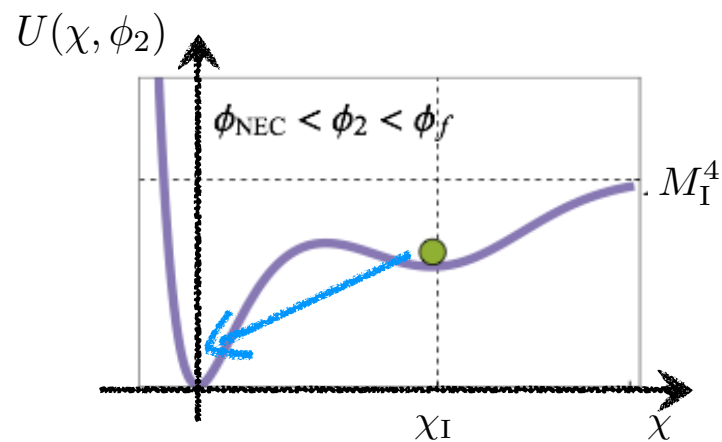
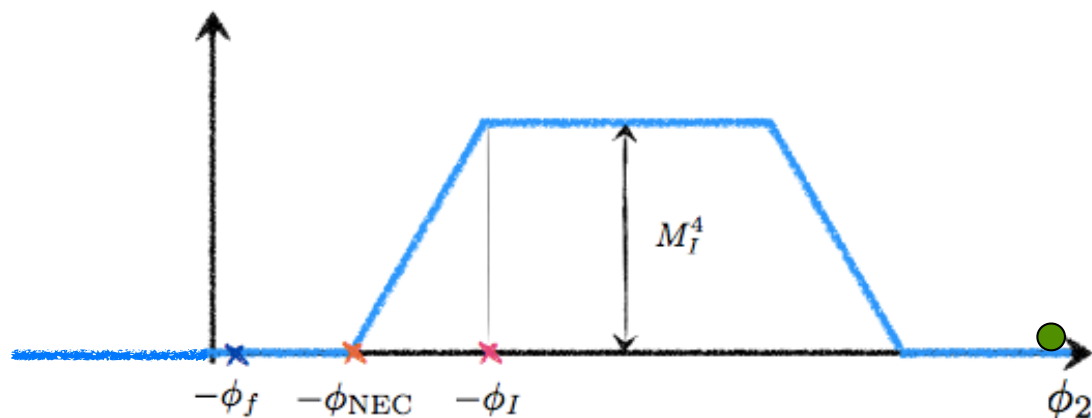
Inflation and Reheating



Inflation and Reheating

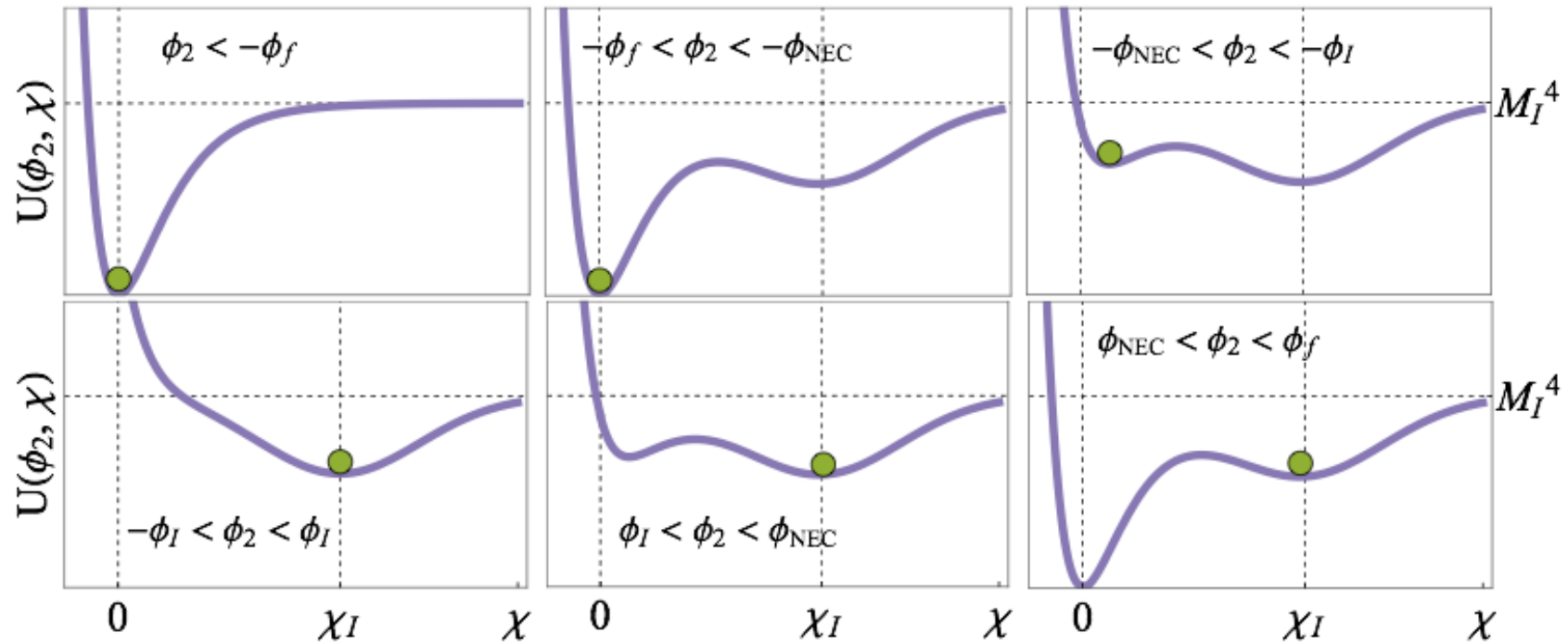


Inflation and Reheating



χ starts rolling back towards the true minimum and oscillates around it, eventually transferring energy to the SM d.o.f.

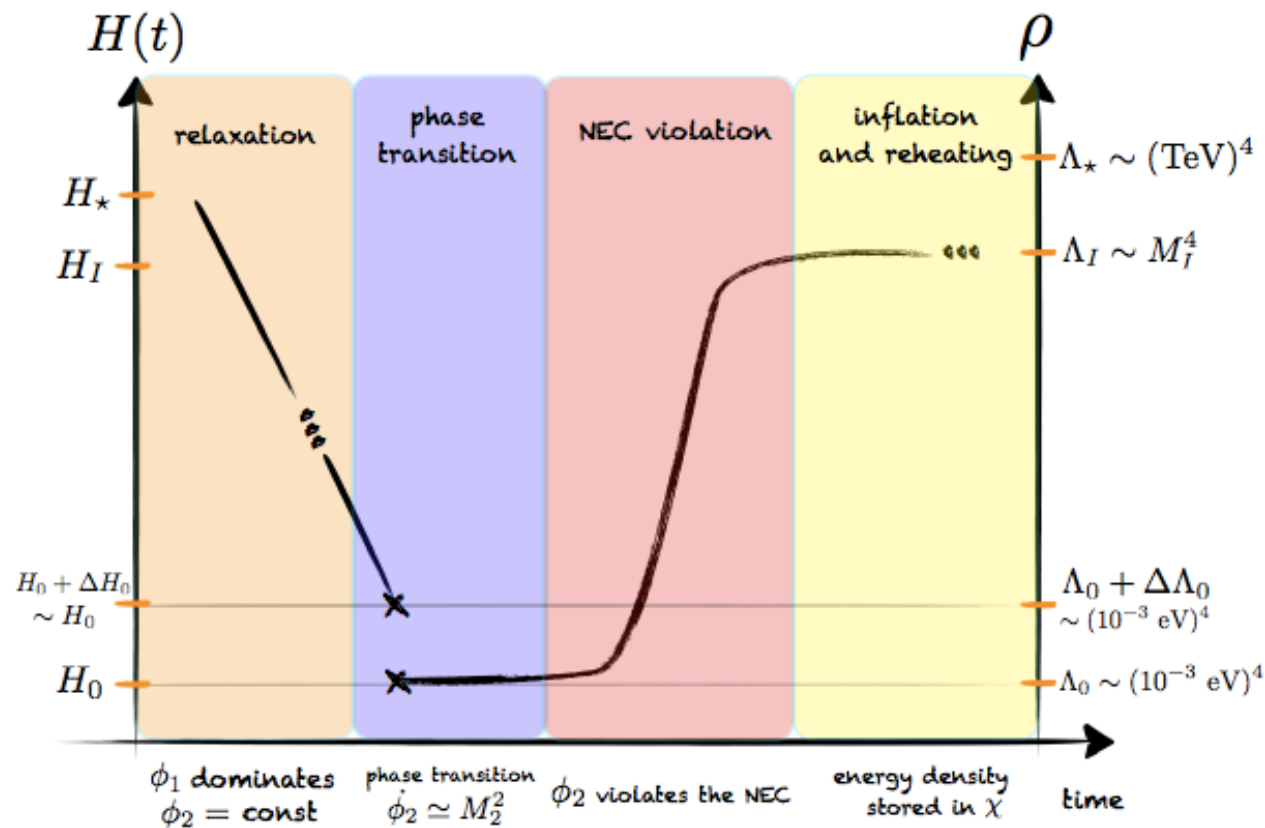
Inflation and Reheating



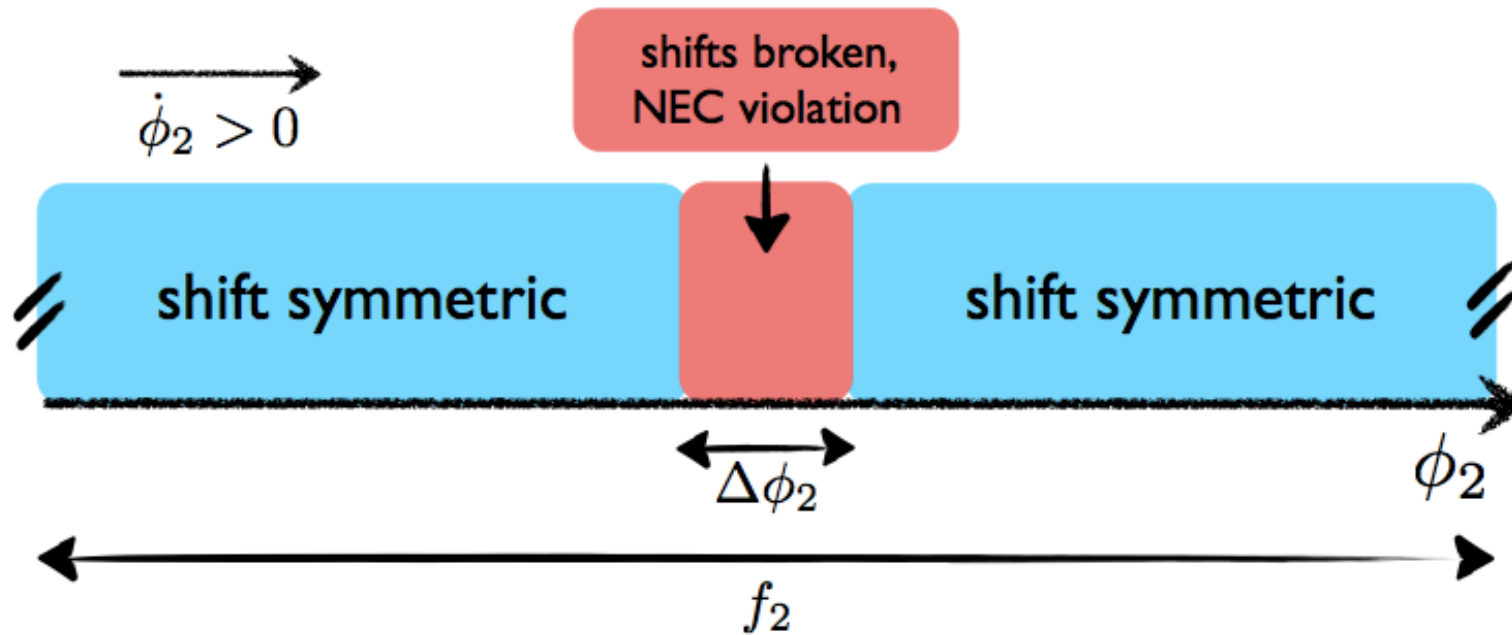
- Back reaction of χ on the dynamics of ϕ_2 should be negligible
- No fluctuations in χ $m_\chi^2 > H_I^2$

Conclusions

- It is possible to relax the CC (the whole evolution of the Universe must be described)
- only IF NEC is violated
- Connection with present dark energy. However it is model dependent



Fast NEC violation



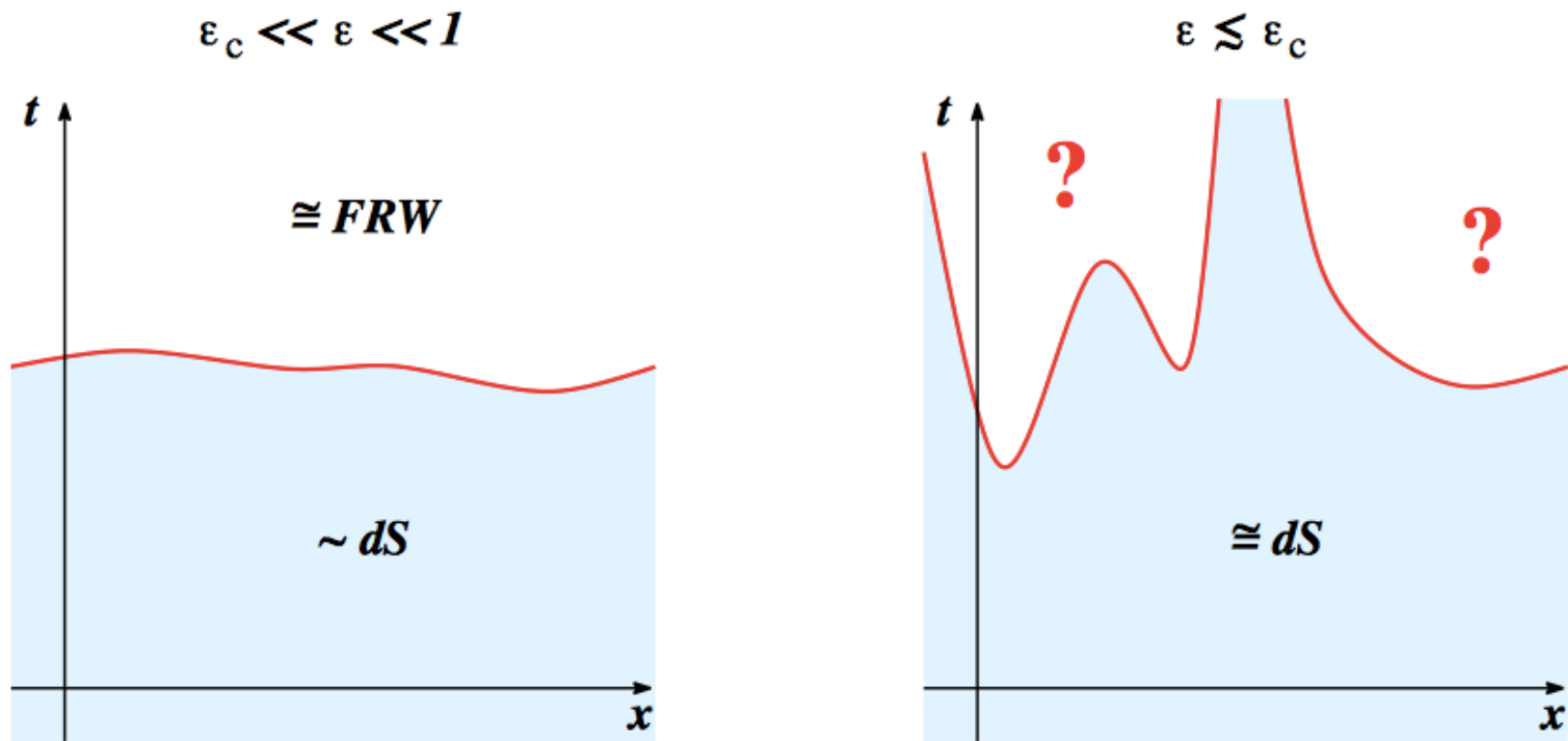
Same CC before and after NEC violation due to periodicity $\phi_2 \rightarrow \phi_2 + f_2$

$$S_\theta = \int d^4x \sqrt{-g} \left[f_2^2 \mathcal{F}_1(\theta) (\partial\theta)^2 + \frac{f_2^3}{M_\theta^3} \mathcal{F}(\theta) (\partial\theta)^2 \square\theta + \frac{f_2^3}{2M_\theta^3} \mathcal{F}_2(\theta) (\partial\theta)^4 - V(\theta) \right]$$

It is possible to create the Universe in H_0^{-1}

- i) Stability
- ii) Cutoff $\gg H_0$
- iii) Subluminality

Slow roll eternal inflation



$$\Delta\phi_{\text{cl}} \sim \dot{\phi}_0 H^{-1} \sim \frac{(-\dot{H} M_{\text{Pl}}^2)^{1/2}}{H}$$

$$\Delta\phi_{\text{quantum}} \sim H$$