

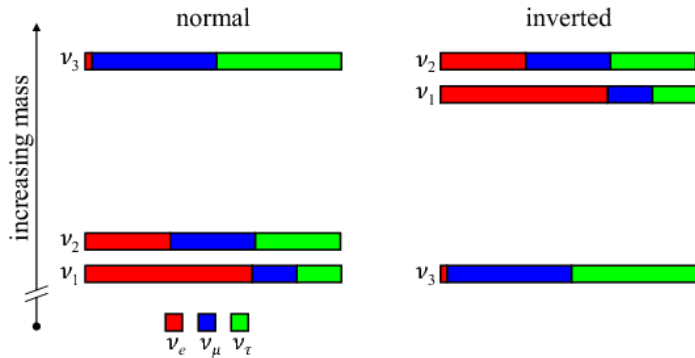
Neutrino Interactions in the few-GeV region and the MiniBooNE anomaly

L. Alvarez Ruso, J. Nieves, E. Saúl Sala, E. Wang



ν oscillation paradigm

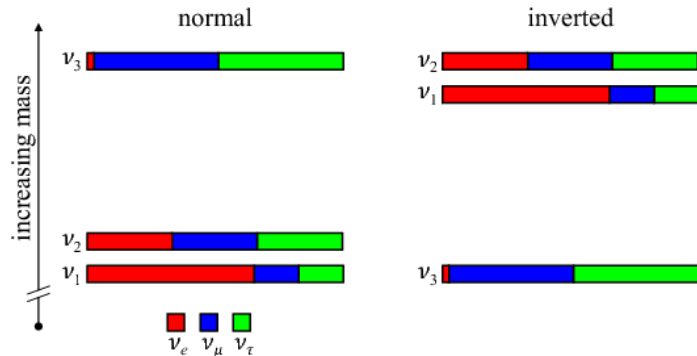
- 3 mixing flavors of mass eigenstates



- supported by solar, atmospheric, reactor and accelerator experiments

ν oscillation paradigm + anomalies

- 3 mixing flavors of mass eigenstates



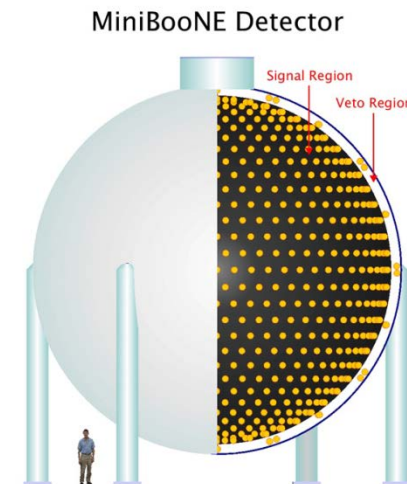
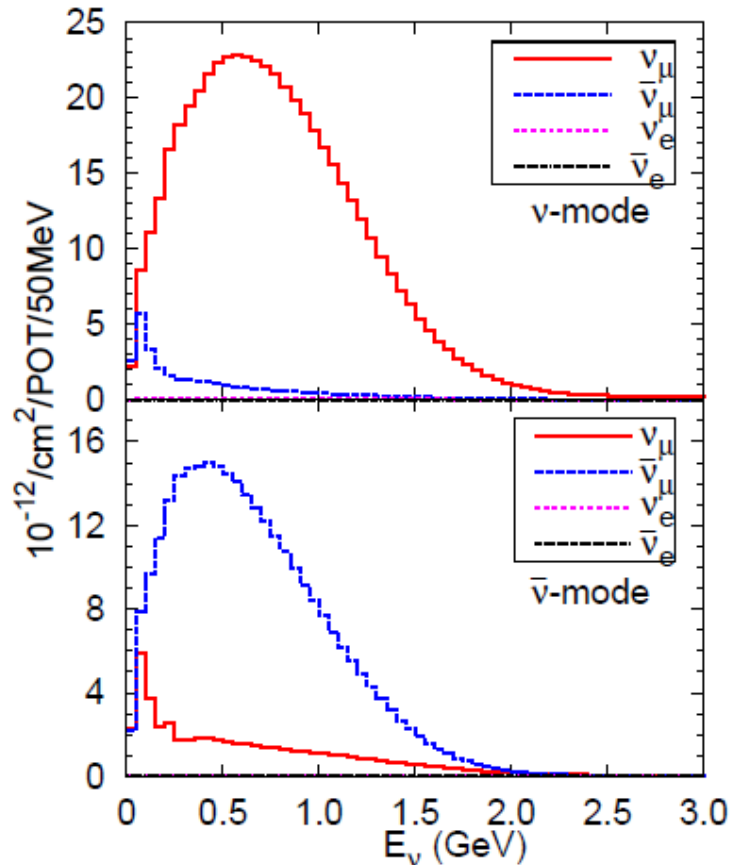
- supported by solar, atmospheric, reactor and accelerator experiments

- **Anomalies**

- reactor
- Gallium radioactive source
- LSND
- **MiniBooNE**

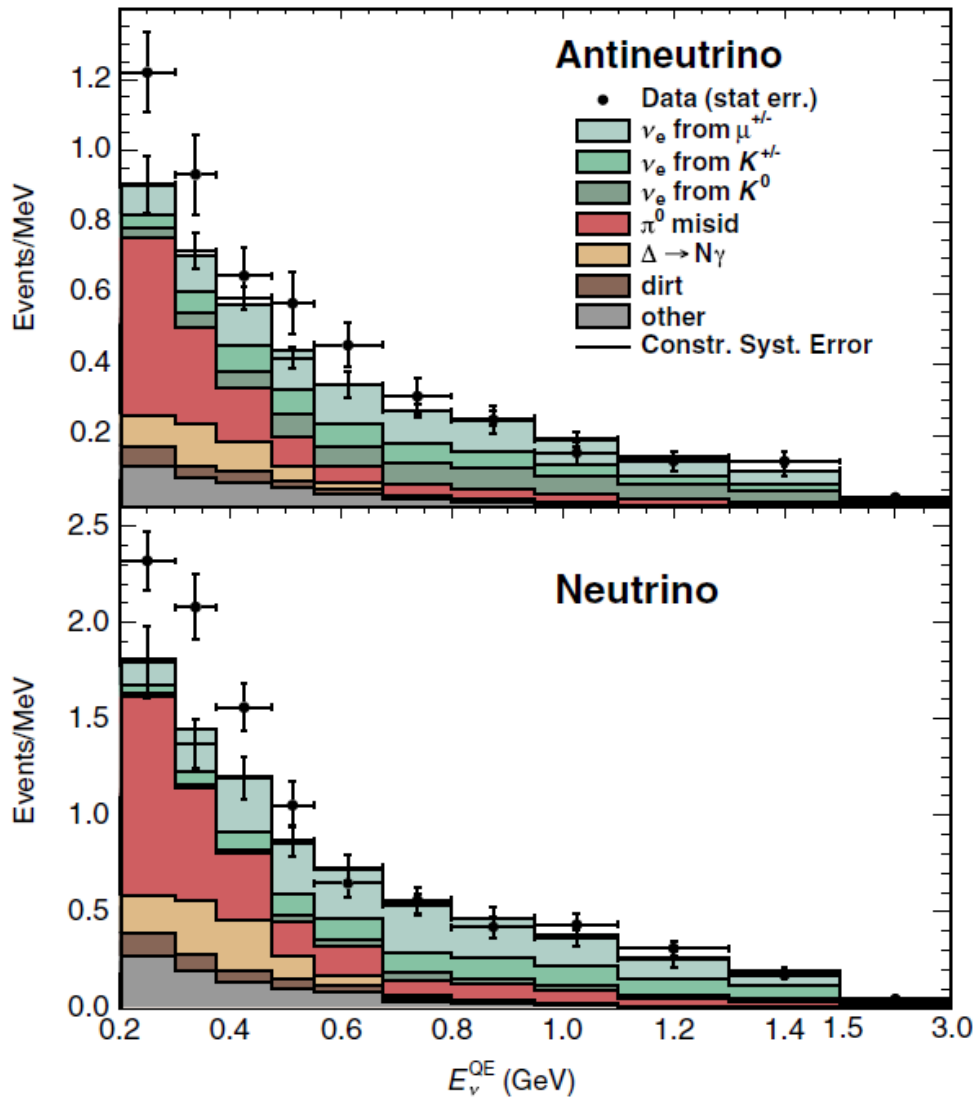
MiniBooNE experiment

- **Target:** CH₂ Aguilar-Arevalo et al, PRL 110 (2013)
- **Mass:** 806 tons
- **Radius:** 611 cm
- **POT:** 6.46 x 10²⁰ (ν mode), 11.27 x 10²⁰ ($\bar{\nu}$ mode)
- **Fluxes:** Aguilar-Arevalo et al, PRD 79 (2009)



MiniBooNE anomaly

■ e-like events in the MiniBooNE $\nu_\mu \rightarrow \nu_e / \bar{\nu}_\mu \rightarrow \bar{\nu}_e$ search:



reconstructed ν energy

$$E_\nu^{QE} = \frac{2m_n E_e - m_e^2 - m_n^2 + m_p^2}{2(m_n - E_e + p_e \cos \theta_e)}$$

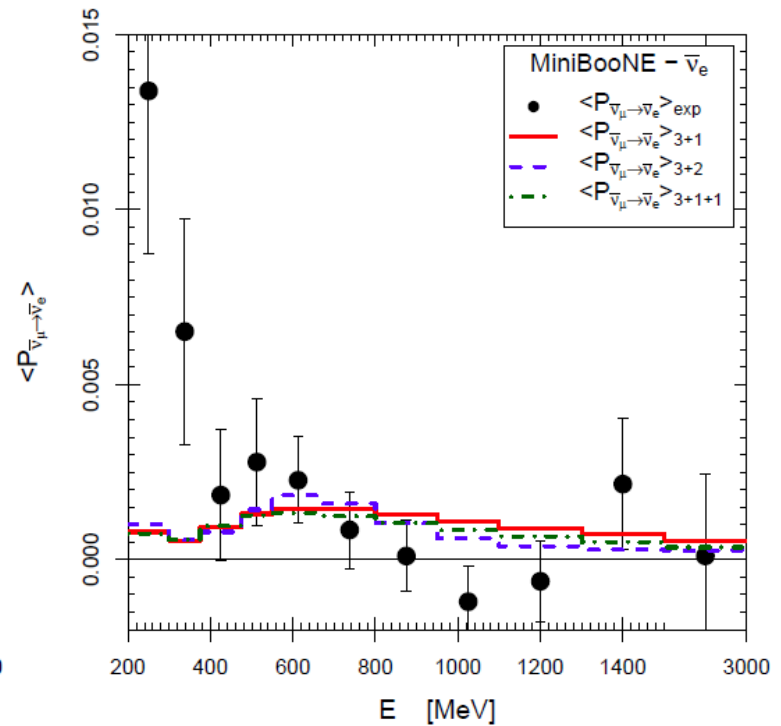
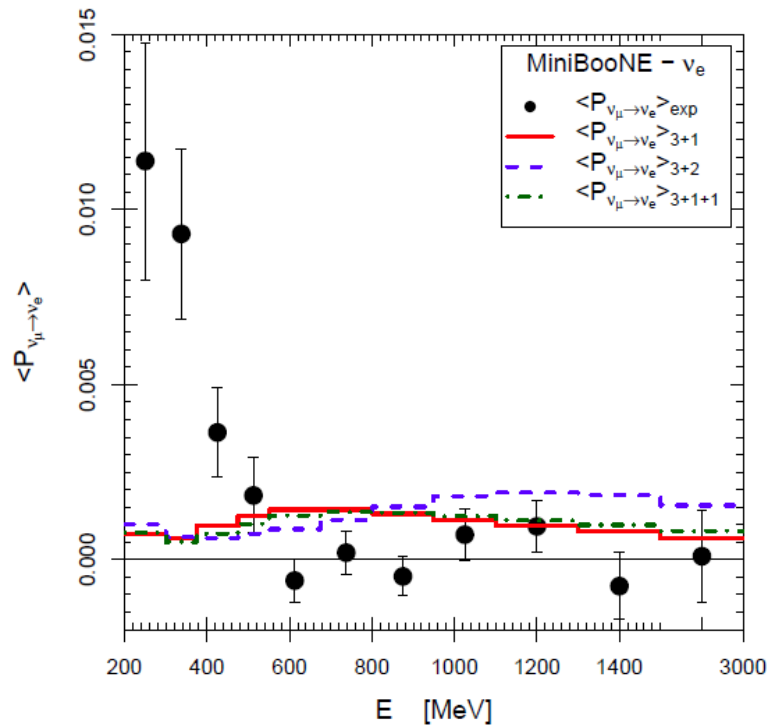
MiniBooNE anomaly

- Origin of **e-like** event excess @ **MiniBooNE**

- **Oscillations: not explained** by 1, 2, 3 families of **sterile neutrinos**

J. Conrad et al., Adv. High Energy Phys. 2013, C. Giunti et al., PRD88 (2013)

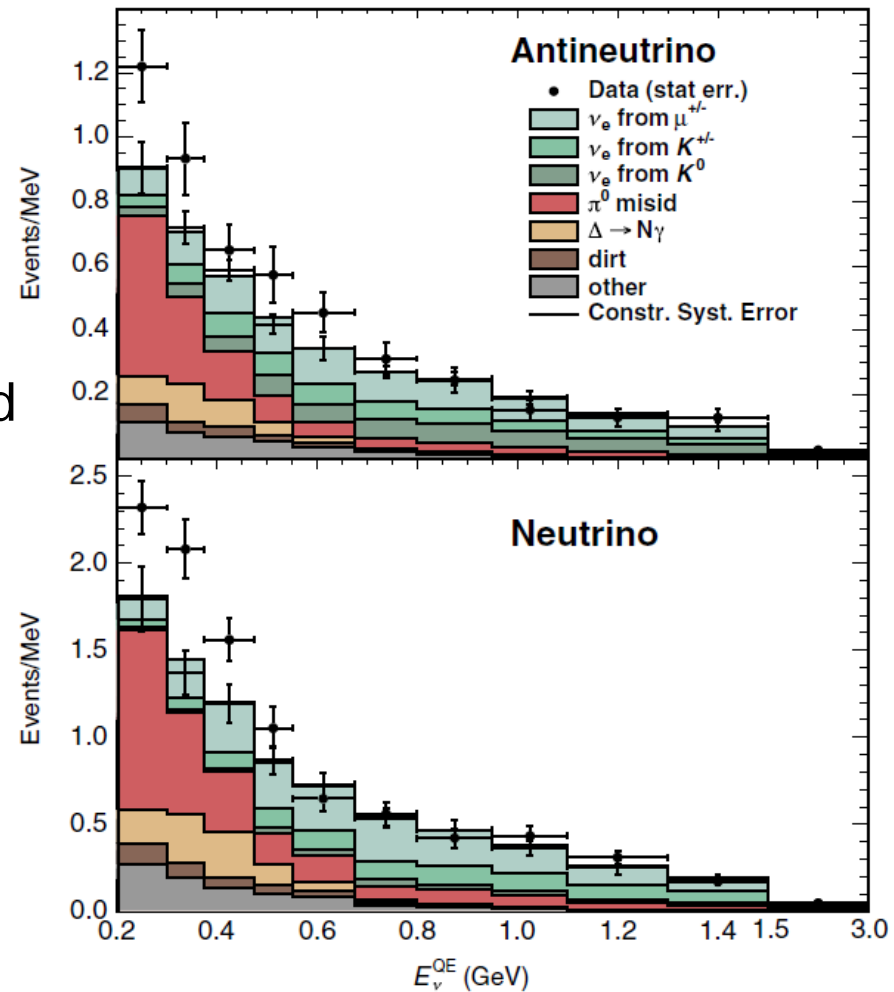
- Even after taking into account multi-nucleon interactions in **E_ν reconstruction** Ericson et al., Phys.Rev. D93 (2016)



The MiniBooNE low-energy anomaly is incompatible with neutrino oscillations
C. Giunti et al., PRD88 (2013)

MiniBooNE anomaly

- e-like **backgrounds** @ **MiniBooNE** are (in principle) constrained **in situ**
- NC π^0
 - **largest** background
 - measured @ **MiniBooNE**
 - Rein-Sehgal **resonance** production model + non-resonant background
 - π Final State Interactions

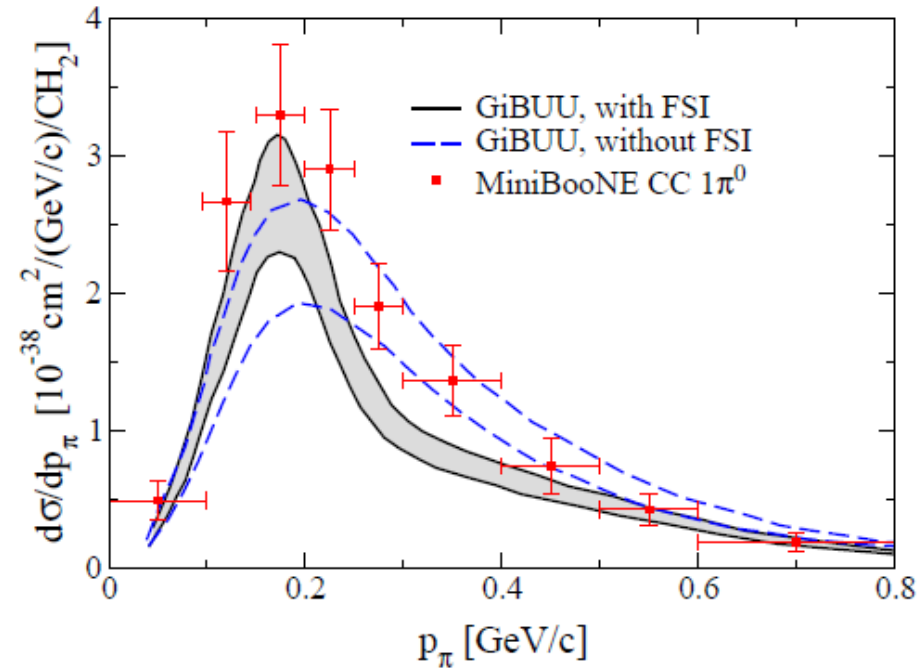


π production on ^{12}C

Comparison to **MiniBooNE**:

Lalakulich, Mosel, PRC87 (2013)

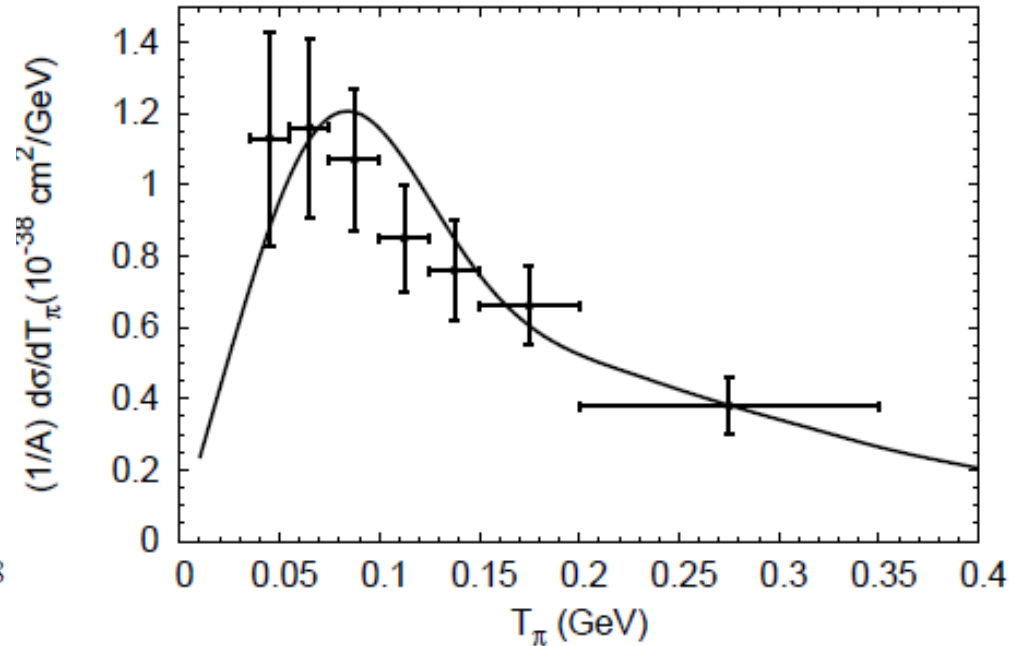
CC π^0 data: Aguilar-Arevalo, PRD83 (2011)



Comparison to **MINERvA**:

Mosel, Gallmeister, PRC96 (2017)

CC π^\pm data: Eberly et al., PRD 92 (2015)



- In spite of flux difference, **MiniBooNE** and **MINERvA** data probe the **same dynamics** and should be strongly **correlated** Sobczyk, Zmuda, PRC 91 (2015)
- This **tension** is **unlikely** to resolve the **MiniBooNE** anomaly

MiniBooNE anomaly

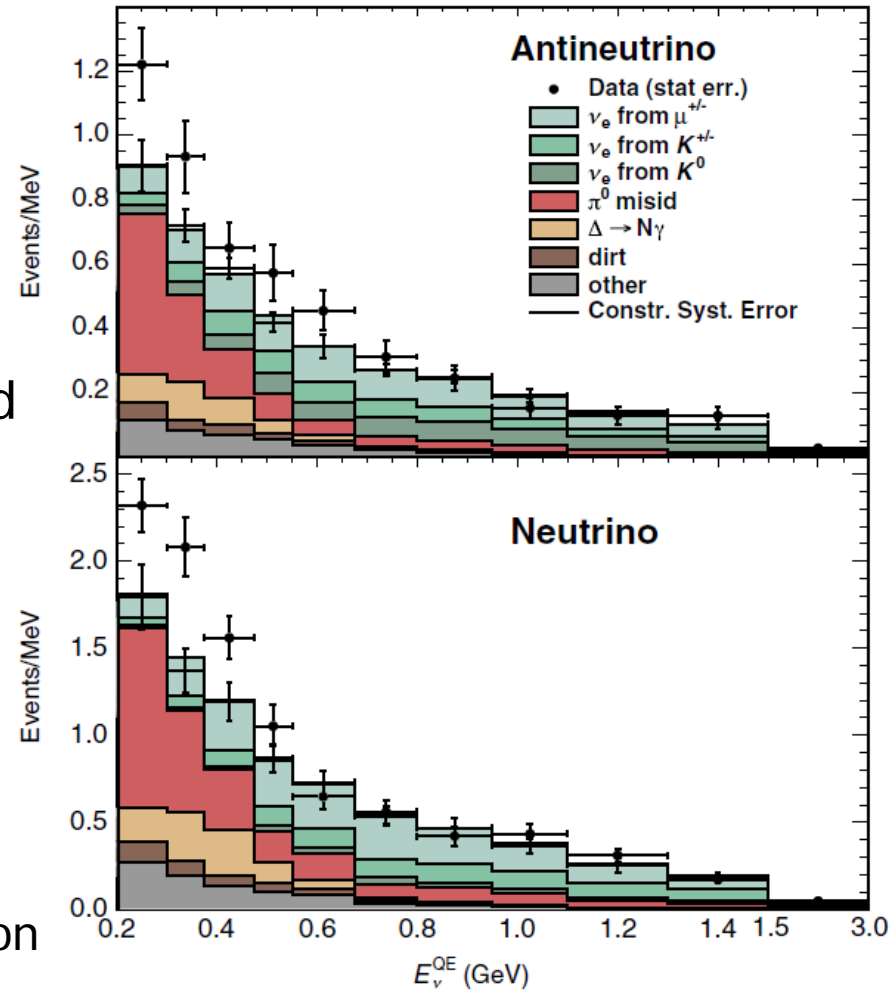
- e-like backgrounds @ MiniBooNE are (in principle) constrained **in situ**

- NC π^0

- **largest** background
- measured @ MiniBooNE
- Rein-Sehgal resonance production model + non-resonant background
- π Final State Interactions

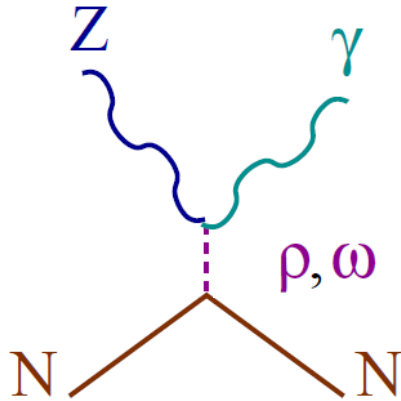
- NC $\Delta \rightarrow N \gamma$

- 2nd **largest** background
- not directly measured
- determined from **measured** NC π^0
 - MC tuning for **resonance** production
 - PDG $R \rightarrow N \gamma$ branching ratios
- Unaccounted **photon** backgrounds?



$NC\gamma$ events at MiniBooNE

- Origin of **e-like** event **excess** @ MiniBooNE
 - Unaccounted **photon** backgrounds?



- Harvey et al., PRL 99 (2007)
- ω favored: large (uncertain) **isoscalar** ωNN coupling

NC γ events at MiniBooNE

■ Photon emission in NC interactions:

■ on nucleons $\nu(\bar{\nu}) N \rightarrow \nu(\bar{\nu}) \gamma N$

■ on nuclei $\nu(\bar{\nu}) A \rightarrow \nu(\bar{\nu}) \gamma X \leftarrow$ incoherent

$\nu(\bar{\nu}) A \rightarrow \nu(\bar{\nu}) \gamma A \leftarrow$ coherent

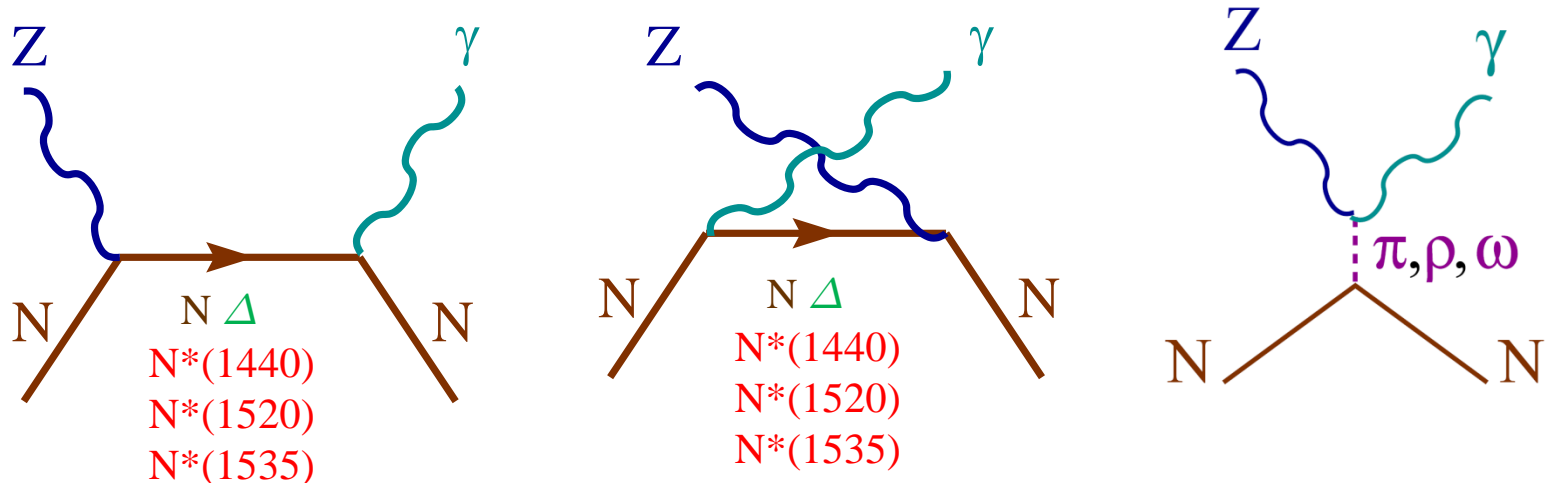
R. Hill, PRD 81 (2010)

Zhang & Serot, PRC 86 (2012)

Wang, LAR, Nieves, PRC 89 (2014)

Photon emission in NC interactions

- on nucleons $\nu(\bar{\nu}) N \rightarrow \nu(\bar{\nu}) \gamma N$



- Weak vector and EM N , N - Δ and N - N^* form factors extracted from electron scattering experiments
- Weak axial N , N - Δ and N - N^* form factors:
 - (off-)diagonal **Goldberger-Treiman** relations for leading couplings
 - e.g. for N - $\Delta(1232)$:

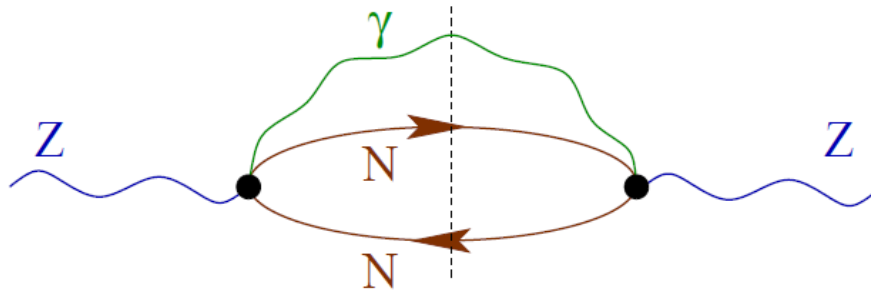
$$C_5^A(0) = \sqrt{\frac{2}{3}} g_{\Delta N \pi} \quad g_{\Delta N \pi} \Leftrightarrow \Gamma(\Delta \rightarrow N \pi) \Leftarrow N \pi \rightarrow N \pi$$

- q^2 dependence consistent with $\nu_\mu d \rightarrow \mu^- \pi^+ p n$ ANL, BNL data

Photon emission in NC interactions

- on nuclei $\nu(\bar{\nu}) A \rightarrow \nu(\bar{\nu}) \gamma X \leftarrow$ incoherent

- 1p1h1 γ excitations in nuclear matter Wang, LAR, Nieves, PRC89 (2014)



- finite nuclei: Local Density approximation: $\rho_F(r) = \left[\frac{3}{2}\pi^2\rho(r)\right]^{1/3}$

- In-medium modification (**broadening**) of the $\Delta(1232)$ resonance

- on nuclei $\nu(\bar{\nu}) A \rightarrow \nu(\bar{\nu}) \gamma A \leftarrow$ coherent

- same microscopic input as for the incoherent process

- Coherent sum over all nucleons:

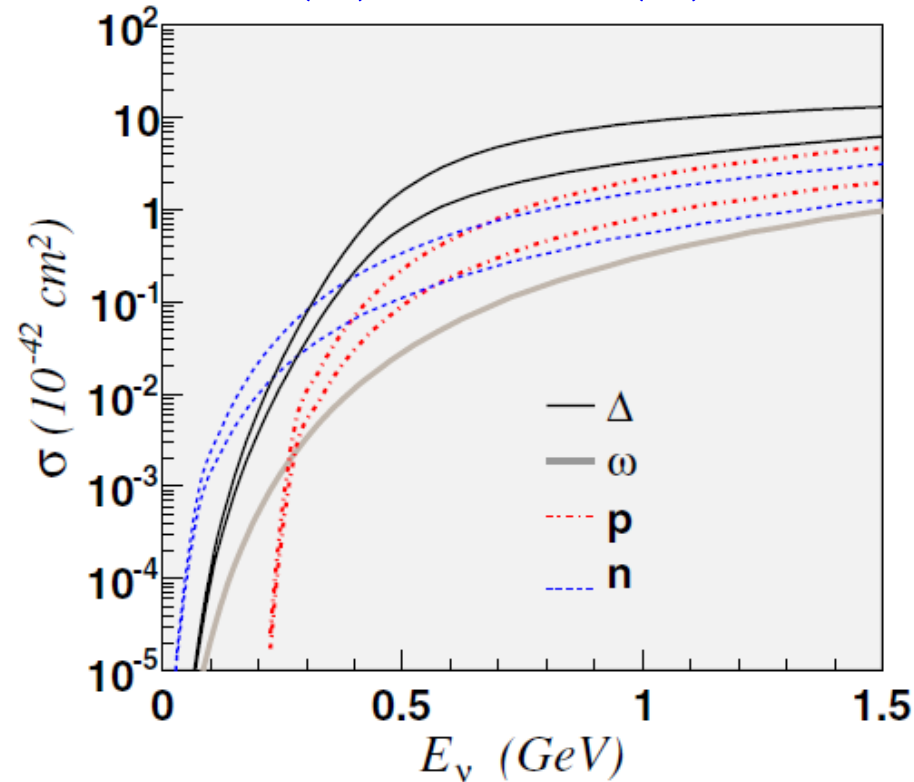
$$\mathcal{M}_r = \frac{G_F e}{\sqrt{2}} \epsilon_\mu^{*(r)} \mathcal{A}^{\mu\alpha} l_\alpha$$

$$\mathcal{A}^{\mu\alpha} = \sum_{r=p,n} \int d\vec{r} e^{i(\vec{q}-\vec{q}_\gamma)\cdot\vec{r}} \rho_r(r) \hat{\Gamma}_r^{\mu\alpha} \quad \hat{\Gamma}_r^{\mu\alpha} = \frac{1}{2} \sum_{i=\text{mech.}} \text{Tr} \left[\bar{u} \Gamma_{i(r)}^\mu u \right]$$

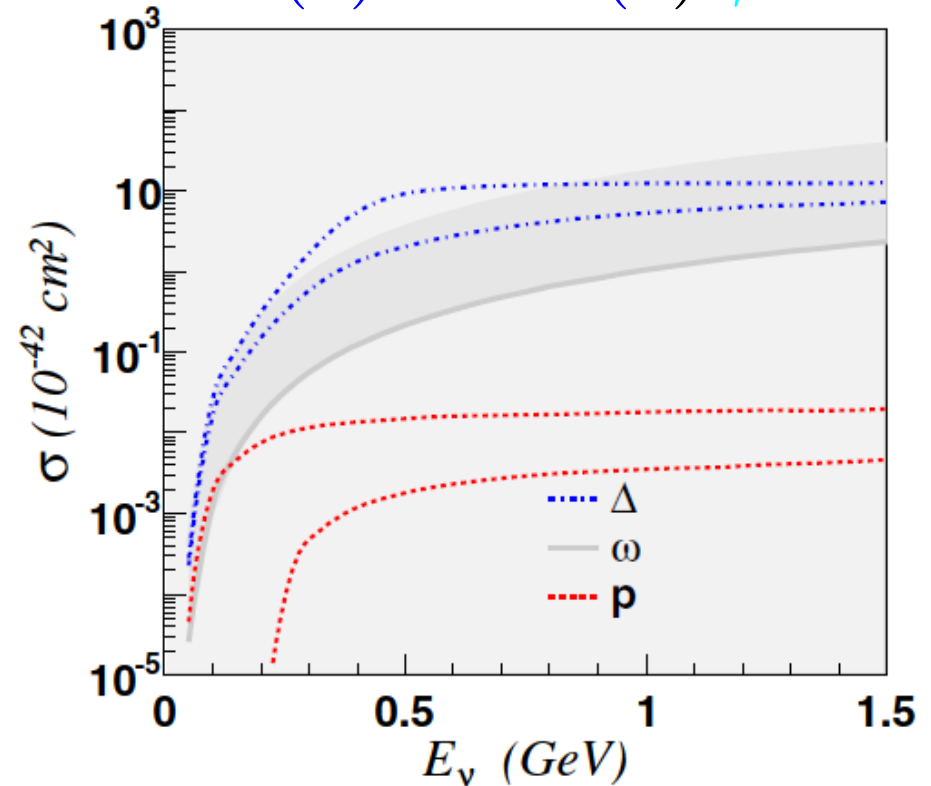
NC γ events at MiniBooNE

■ R. Hill, PRD 81 (2010)

$$\nu(\bar{\nu}) N \rightarrow \nu(\bar{\nu}) \gamma N$$



$$\nu(\bar{\nu}) A \rightarrow \nu(\bar{\nu}) \gamma A$$



■ The ω exchange contribution is **very small**

■ J. Rosner, PRD 91 (2015) \Rightarrow $\frac{1}{4}$ smaller

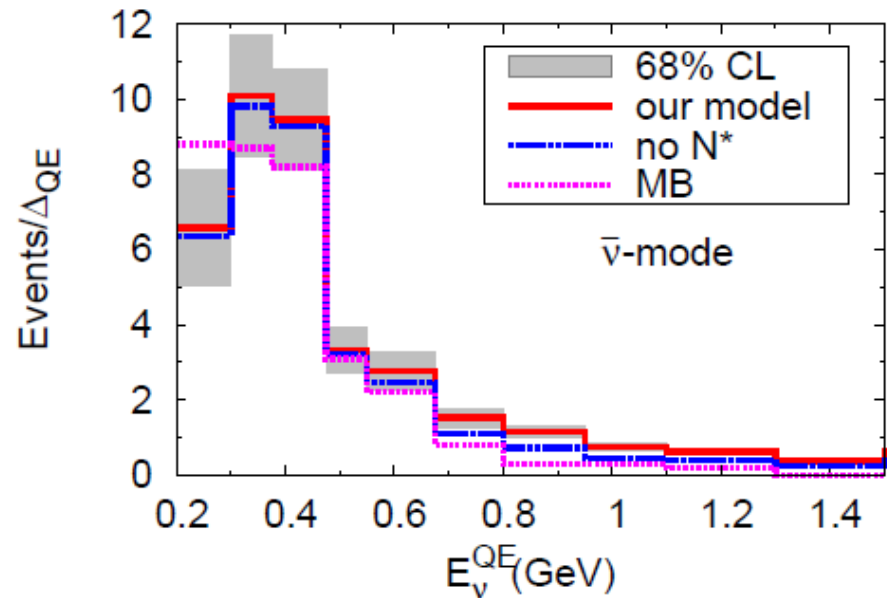
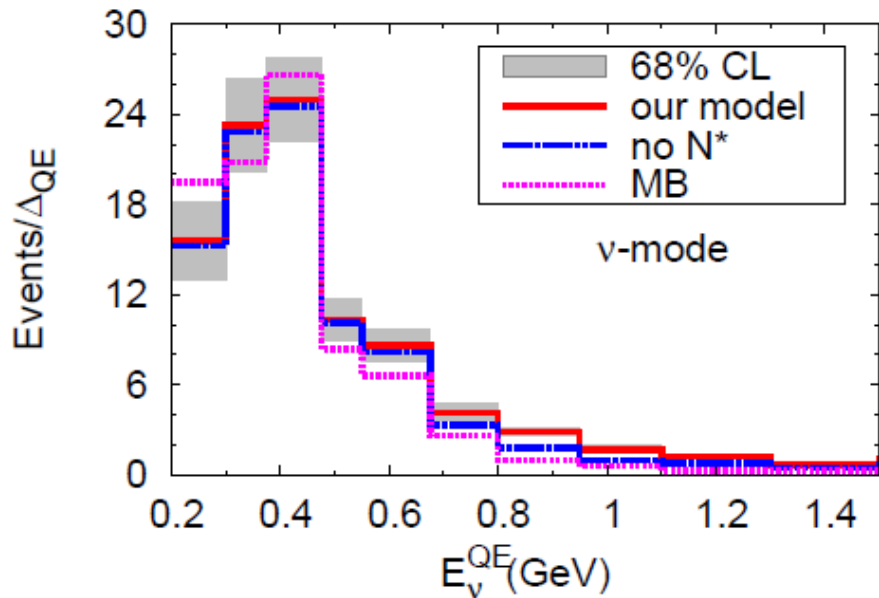
■ Z- ω - γ vertex calibrated by $\tau \rightarrow \nu_\tau a_1$ and $f_1 \rightarrow \rho \gamma$ decays

$NC\gamma$ events at MiniBooNE

- Comparison to the MiniBooNE estimate

- Resonance model (R&S) tuned to π production data

- Only $R \rightarrow N \gamma$



E. Wang, LAR, J. Nieves, PLB 740 (2015)

- $NC\gamma$: insufficient to explain the excess of e-like events at MiniBooNE

- Same conclusion as Zhang, Serot, PLB 719 (2013)

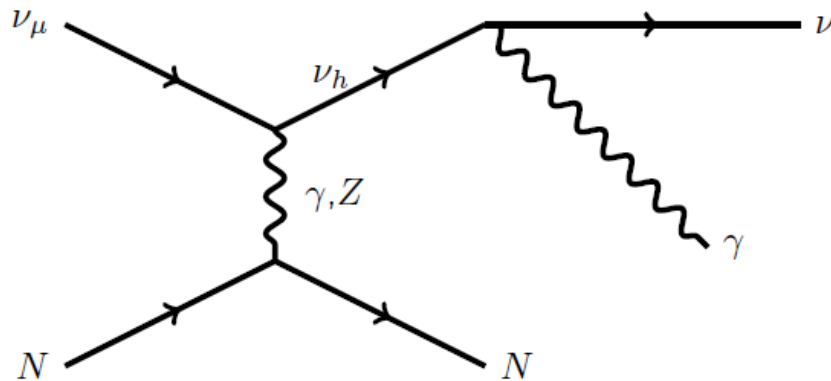
NC γ events at MiniBooNE

- Origin of **e-like** event excess @ MiniBooNE

- Unaccounted **photon** backgrounds?

- **Heavy** (~ 50 MeV) ν produced **weakly** or **EM**, followed by $\nu_h \rightarrow \nu \gamma$

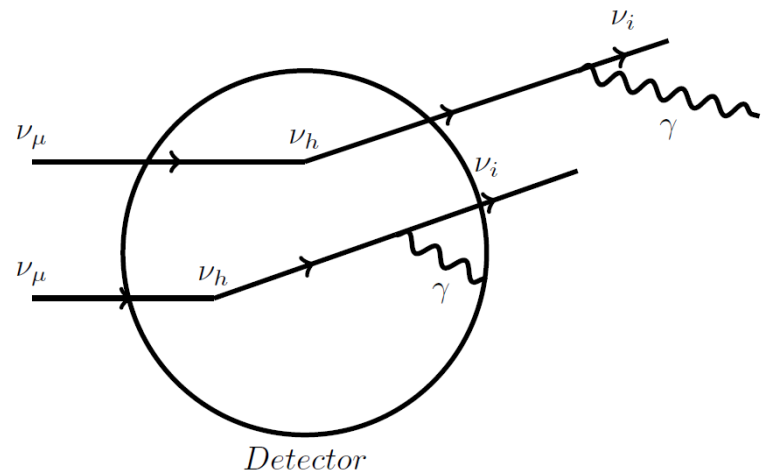
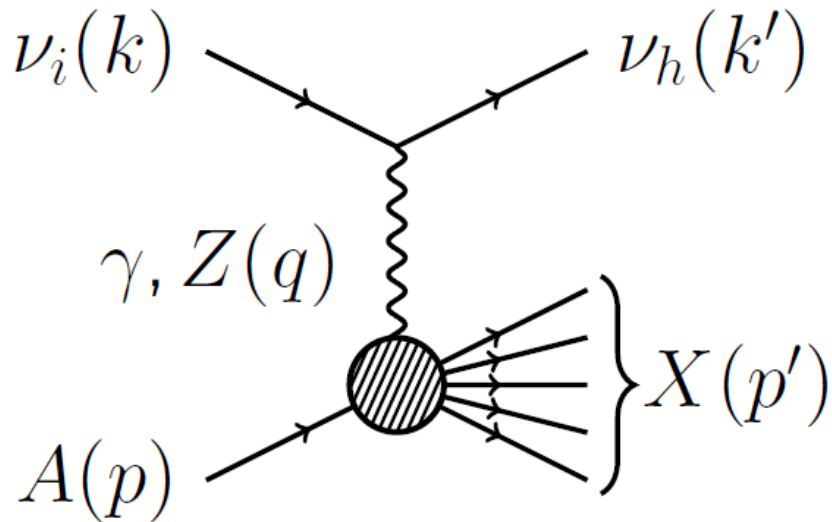
S. Gninenko, PRL 103 (2009), M. Masip et al, JHEP 1301 (2013)



$$\mathcal{L}_{eff} = \frac{1}{2} \mu_{tr}^i [\bar{\nu}_h \sigma_{\mu\nu} (1 - \gamma_5) \nu_i + \bar{\nu}_i \sigma_{\mu\nu} (1 + \gamma_5) \nu_h] \partial^\mu A^\nu$$

$$\frac{d\Gamma_{\nu_h \rightarrow \nu \gamma}}{d \cos \theta_\gamma} = \frac{(\mu_{tr}^i)^2}{32\pi} m_h^3 (1 - \cos \theta_\gamma)$$

ν_h production



- on nucleons $\nu_\mu(\bar{\nu}_\mu) N \rightarrow \nu_h(\bar{\nu}_h) N$
- on nuclei $\nu_\mu(\bar{\nu}_\mu) A \rightarrow \nu_h(\bar{\nu}_h) A \leftarrow$ coherent
- $\nu_\mu(\bar{\nu}_\mu) A \rightarrow \nu_h(\bar{\nu}_h) X \leftarrow$ incoherent

■ $\nu_h =$ Dirac ν with $m \approx 50$ MeV, slightly mixed with ν_μ

■ $A = {}^{12}\text{C}$ (MiniBooNE, CH_2)

LAR, E. Saúl Sala, in preparation, arXiv:1705.00353

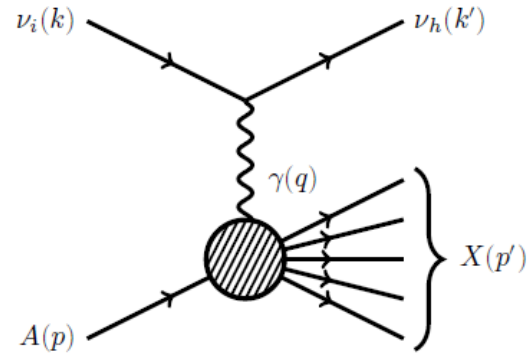
ν_h production by EM interactions

$$\mathcal{L}_{eff} = \frac{1}{2} \mu_{tr}^i [\bar{\nu}_h \sigma_{\mu\nu} (1 - \gamma_5) \nu_i + \bar{\nu}_i \sigma_{\mu\nu} (1 + \gamma_5) \nu_h] \partial^\mu A^\nu$$

- General expression for the **inclusive cross section**

$$\nu_\mu(k) + A(p) \rightarrow \nu_h(k') + X(p')$$

$$\frac{d\sigma}{dk'_0 d\Omega'} = \frac{|\vec{k}'|}{|\vec{k}|} \frac{\alpha (\mu_{tr}^\mu)^2}{4\pi q^4} L_{\mu\nu} W_{EM}^{\mu\nu} \quad \alpha = \frac{e^2}{4\pi} \approx \frac{1}{137}$$



$$\begin{aligned} L_{\mu\nu} &= \frac{1}{4} \text{Tr} [(k' + m_h) \sigma_{\mu\alpha} (1 - \gamma_5) k (1 + \gamma_5) \sigma_{\nu\beta}] q^\alpha q^\beta \\ &= 2(k \cdot k') (k + k')_\mu (k + k')_\nu - 2m_h^2 [2k_\mu k_\nu + g_{\mu\nu} (k \cdot k')] + 2m_h^2 i \epsilon_{\mu\nu\alpha\beta} k^\alpha k'^\beta \end{aligned}$$

$$W_{EM}^{\mu\nu} = W_1 \left(\frac{q^\mu q^\nu}{q^2} - g^{\mu\nu} \right) + \frac{W_2}{M^2} \left(p^\mu - \frac{p \cdot q}{q^2} q^\mu \right) \left(p^\nu - \frac{p \cdot q}{q^2} q^\nu \right)$$

- Structure functions $W_{1,2}$ are

- process specific
- probed in electron elastic and QE scattering

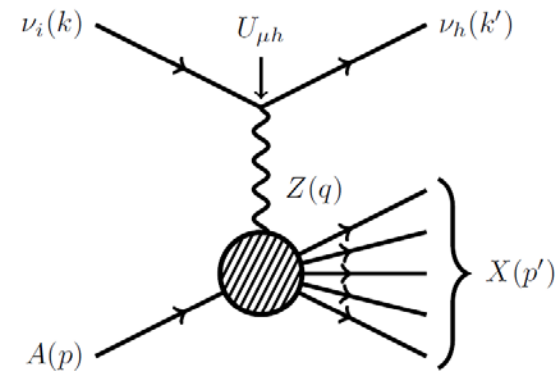
ν_h production by NC interactions

$$\nu_\mu = U_{\mu 1} \nu_1 + U_{\mu 2} \nu_2 + U_{\mu 3} \nu_3 + U_{\mu h} \nu_h + \dots$$

- General expression for the **inclusive cross section**

$$\nu_\mu(k) + A(p) \rightarrow \nu_h(k') + X(p')$$

$$\frac{d\sigma}{dk'_0 d\Omega'} = \frac{|\vec{k}'|}{|\vec{k}|} \frac{|U_{\mu h}|^2 G_F^2}{(2\pi)^2} L_{\mu\nu} W^{\mu\nu}$$



$$\begin{aligned} L_{\mu\nu} &= \text{Tr} [(k' + m_h) \gamma_\mu (1 - \gamma_5) k \gamma_\nu (1 - \gamma_5)] \\ &= 8(k'_\mu k_\nu + k'_\nu k_\mu - g_{\mu\nu} (k \cdot k') + i\epsilon_{\mu\nu\alpha\beta} k'^\alpha k^\beta) \end{aligned}$$

$$\begin{aligned} W_{NC}^{\mu\nu} &= -W_1 g^{\mu\nu} + W_2 \frac{p^\mu p^\nu}{M^2} + W_4 \frac{q^\mu q^\nu}{M^2} + W_5 \frac{p^\mu q^\nu + q^\mu p^\nu}{M^2} \\ &\quad + W_3 i\epsilon^{\mu\nu\alpha\beta} \frac{p_\alpha q_\beta}{2M^2} + W_6 \frac{p^\mu q^\nu - q^\mu p^\nu}{M^2} \end{aligned}$$

- Structure functions $W_{1,2}$ are

- process specific

- probed in electron and neutrino elastic and QE scattering

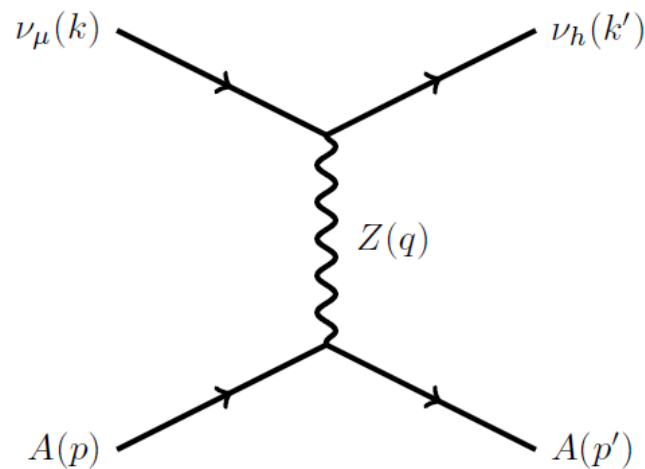
ν_h production by NC interactions

■ $\nu_\mu(k) + A(p) \rightarrow \nu_h(k') + A(p')$

$$W^{\mu\nu} = \frac{1}{2M} \int \frac{d^3 p'}{2E'} \delta^4(k' + p' - k - p) H^{\mu\nu}$$

$$H^{\mu\nu} = J_{NC}^\mu (J_{NC}^\nu)^*$$

$$J_{NC}^\mu = 2 \left(p^\mu - \frac{p \cdot q}{q^2} q^\mu \right) F_W(q^2) \quad \leftarrow \text{as in CE}\nu\text{NS}$$



$$F_W(q^2) = \frac{1}{2} [F_p(q^2)(1 - 4 \sin^2 \theta_W) - F_n(q^2)] \quad F_{p,n}(q^2) = \int d^3 r e^{i\vec{q} \cdot \vec{r}} \rho_{p,n}(r)$$

$$W_1 = 0$$

$$W_2 = \frac{M_A}{E'} \delta(E' + k'_0 - m_N - k_0) F_W(q^2) = 4W_4 = 2W_5$$

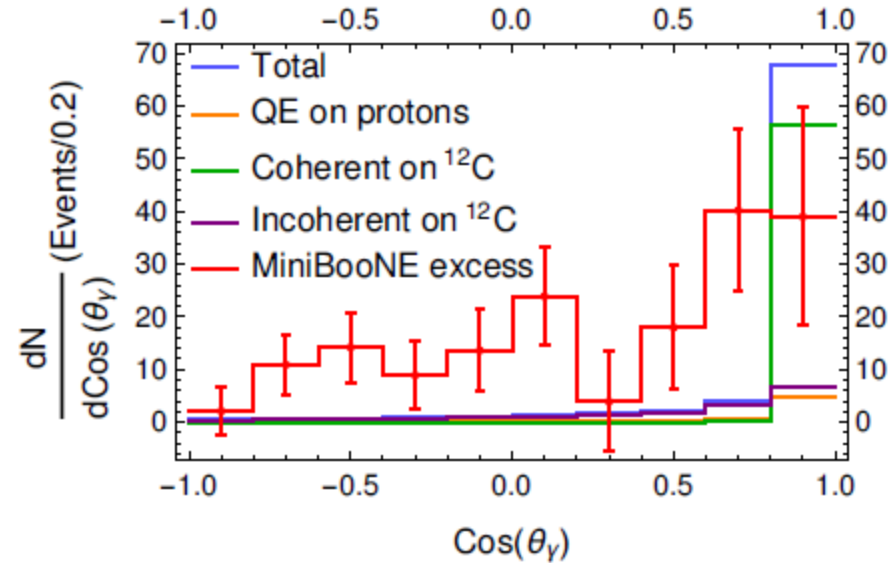
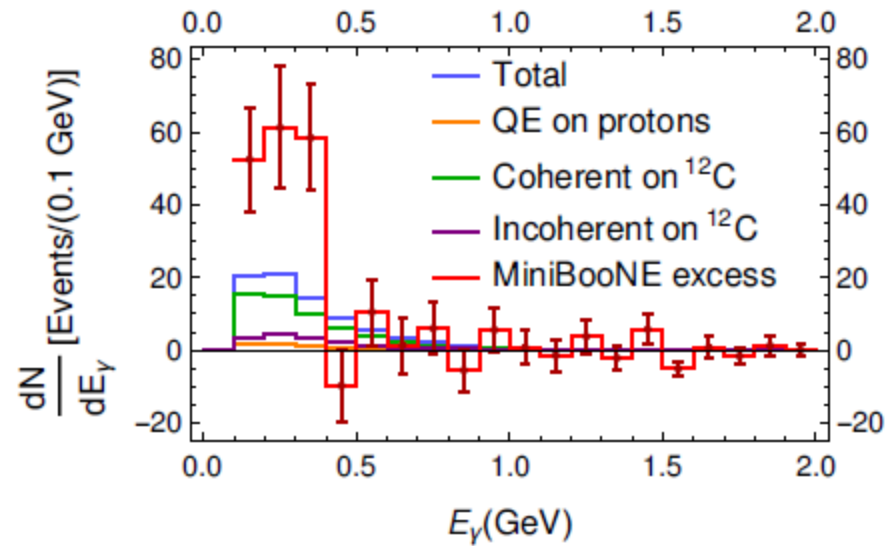
$$\frac{d\sigma}{dt} = \frac{|U_{\mu h}|^2 G_F^2}{8\pi (s - M_A^2)^2} [4(s - M_A^2)^2 + 4st - m_h^2 (4s + t) + m_h^4] F_W^2(t)$$

Results

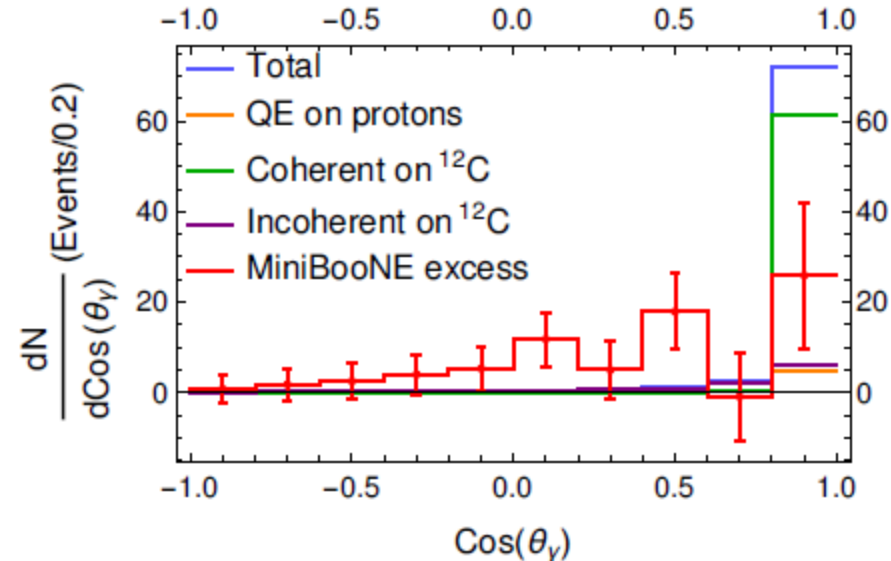
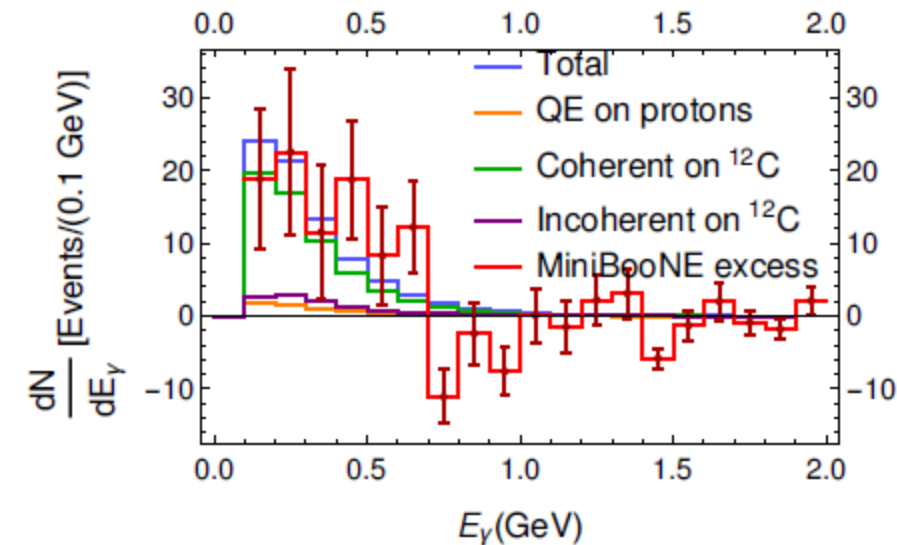
- Choice of parameters from [M. Masip et al, JHEP 1301 \(2013\)](#)
 - $m_h = 50 \text{ MeV}$
 - $\tau_0 = 5 \times 10^{-9} \text{ s}$
 - $\text{BR}(\nu_h \rightarrow \nu_\mu \gamma) = 10^{-2}$
 - $|U_{\mu h}|^2 = 3 \times 10^{-3}$

Events @ MiniBooNE

■ ν mode



■ $\bar{\nu}$ mode



Results

- Choice of parameters from [M. Masip et al, JHEP 1301 \(2013\)](#)
 - $m_h = 50 \text{ MeV}$
 - $\tau_0 = 5 \times 10^{-9} \text{ s}$
 - $\text{BR}(\nu_h \rightarrow \nu_\mu \gamma) = 10^{-2}$
 - $|U_{\mu h}|^2 = 3 \times 10^{-3}$
- **does not explain** the **MiniBooNE excess of events**

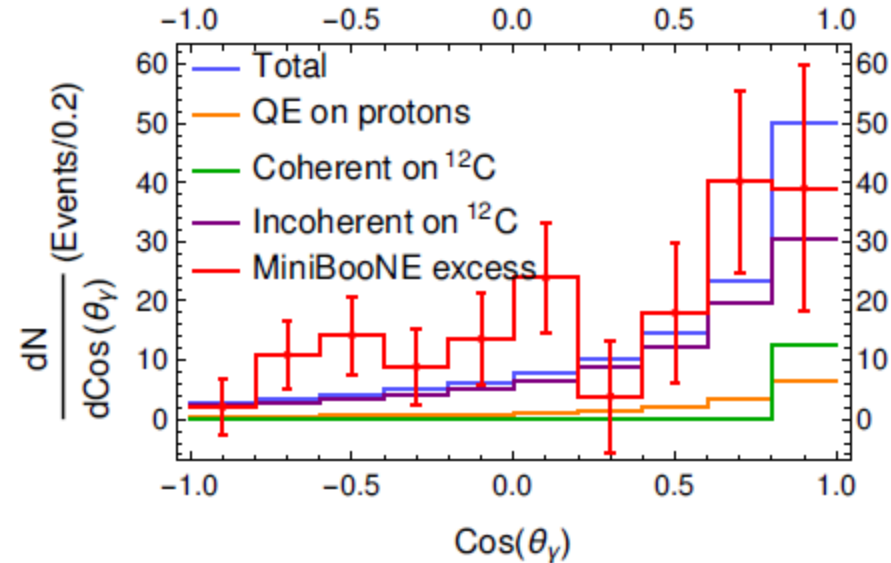
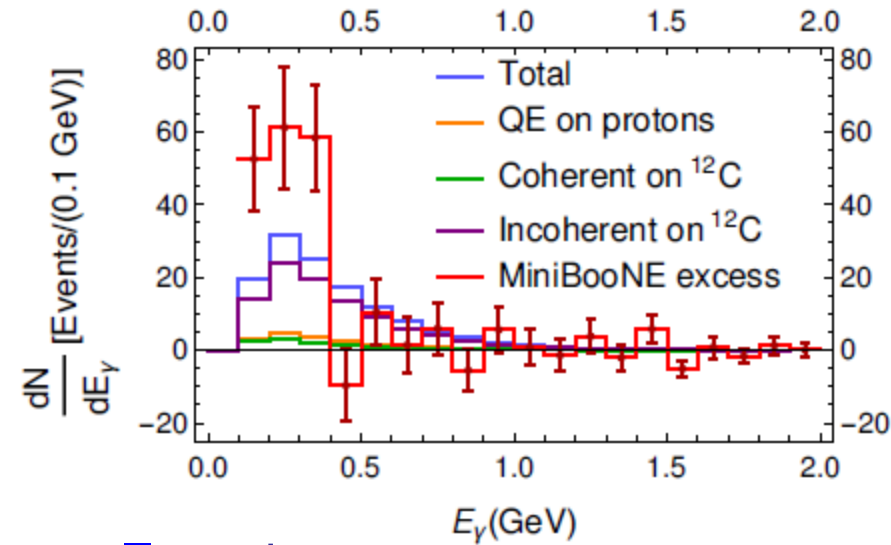
Results

- **LSND** compatible range by **S. Gninenko, PRL 103 (2009)**
 - $m_h > 40$ MeV (**KARMEN**), $m_h < 80$ MeV (**LSND**)
 - $|U_{\mu h}|^2 > 10^{-3}$ (muon lifetime), $|U_{\mu h}|^2 < 10^{-2}$ (**LEP**)
 - $\tau_0 < 10^{-8}$ s (**LSND**)

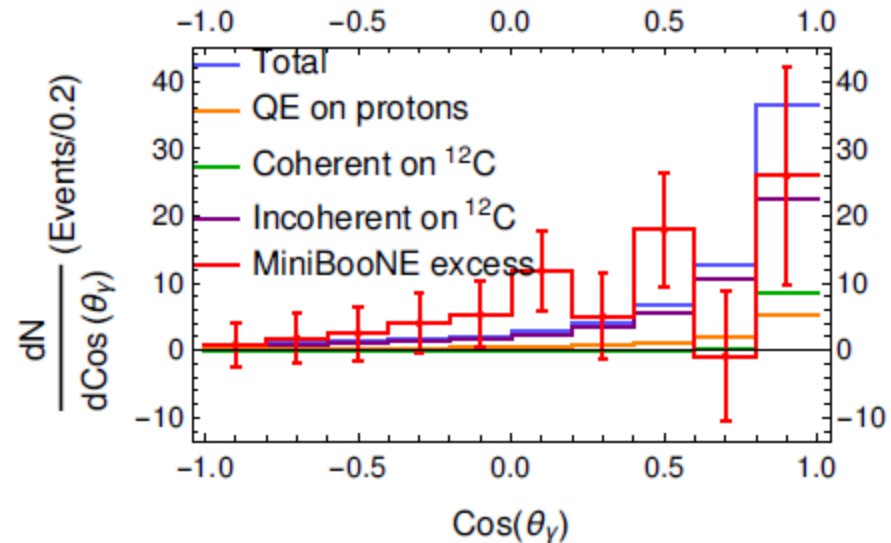
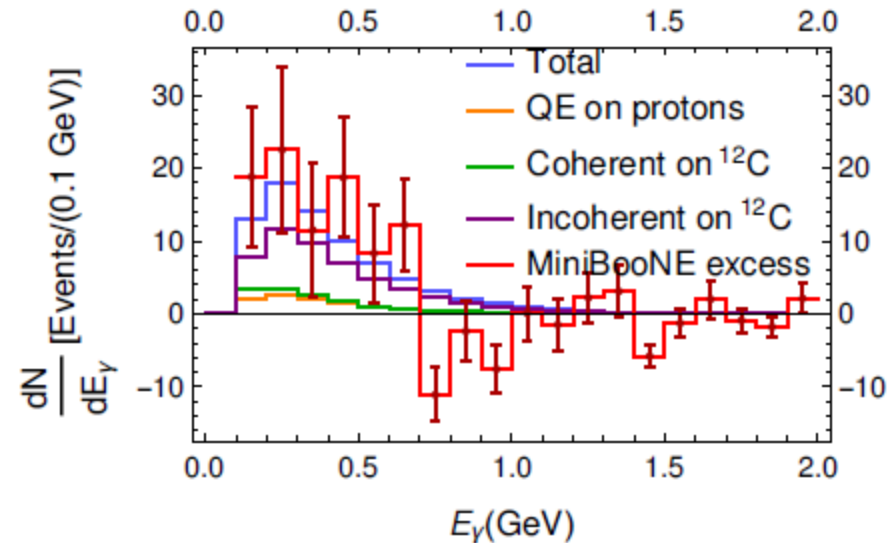
- Our fit: $\chi^2/\text{DoF} = 101/54$
 - $m_h = 68.6$ MeV
 - $\tau_0 = 2.5 \times 10^{-9}$ s
 - $\text{BR}(\nu_h \rightarrow \nu_\mu \gamma) = 8.4 \times 10^{-4} \Leftrightarrow$ EM ν_h production strongly suppressed
 - $|U_{\mu h}|^2 = 10^{-2}$

Events @ MiniBooNE

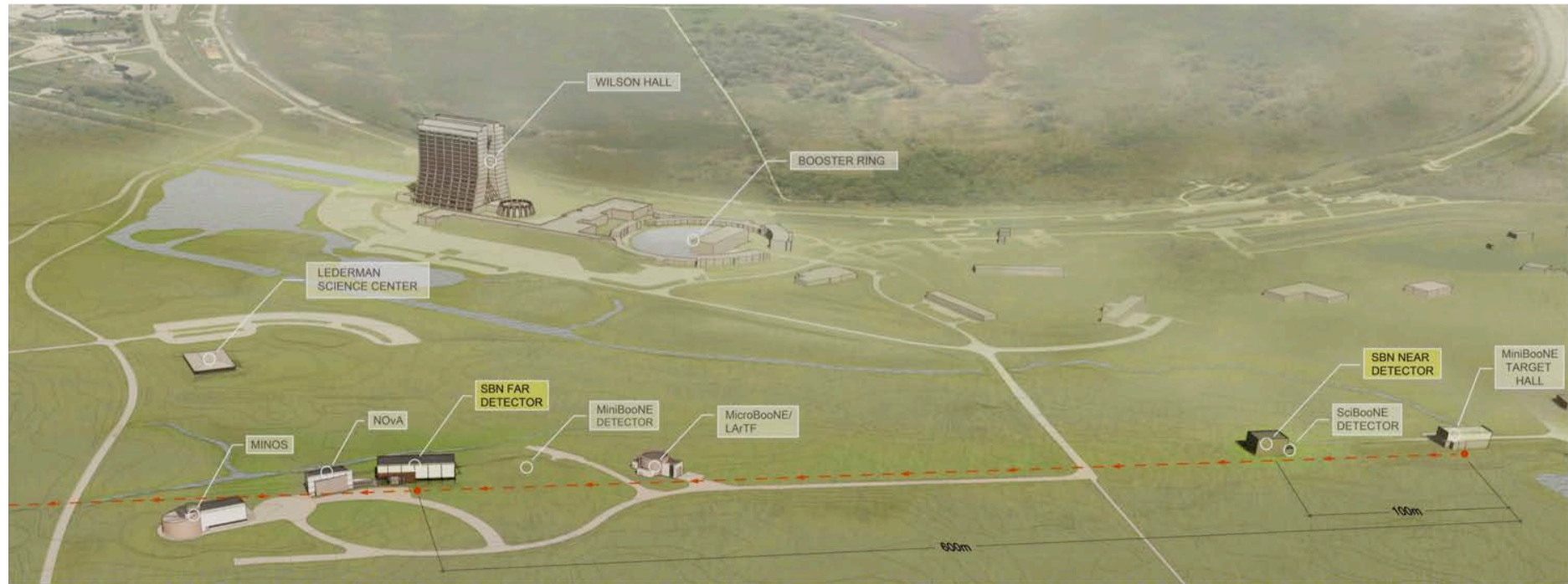
■ ν mode



■ $\bar{\nu}$ mode

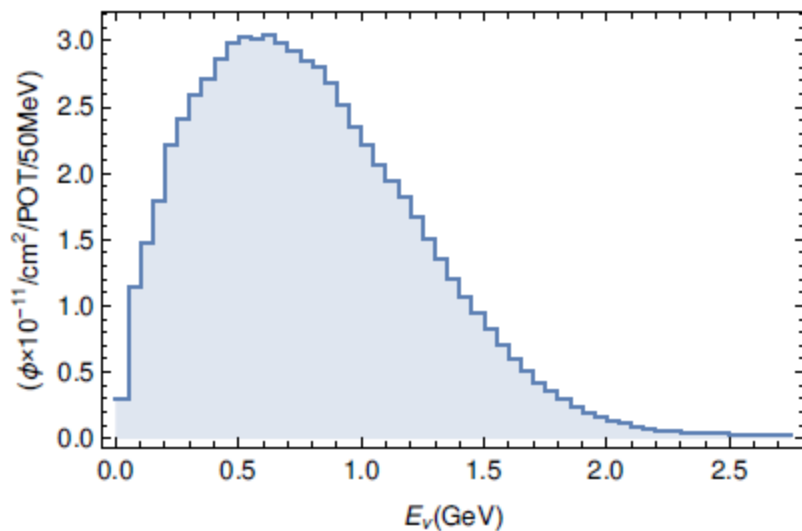


SBN

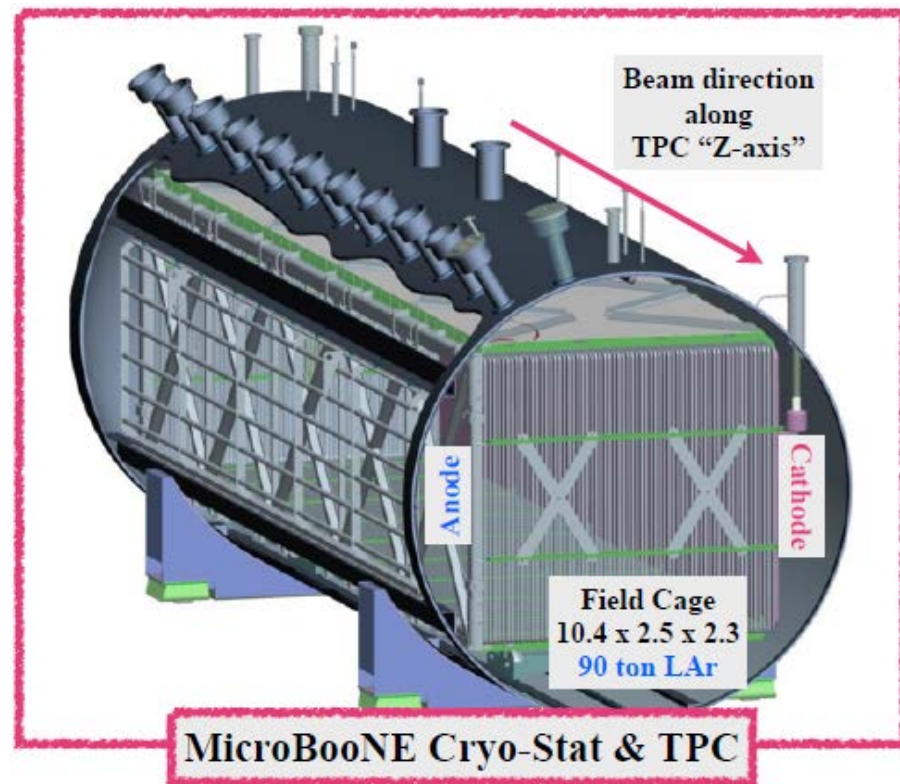


MicroBooNE

- LArTPC
- Active mass: 86.6 tons
- Dimensions: $10.3 \times 2.3 \times 2.3$ m
- Run plan: 6.6×10^{20} POT
- Acciarri et al., arXiv:1503.01520
- Flux prediction:

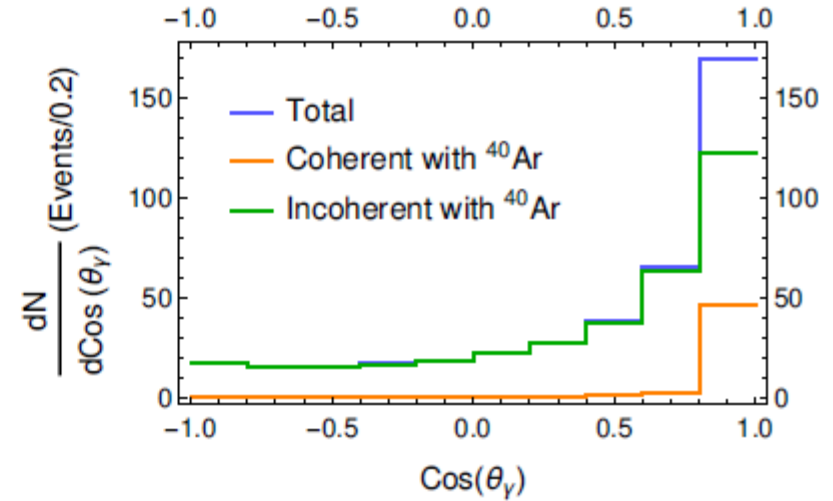
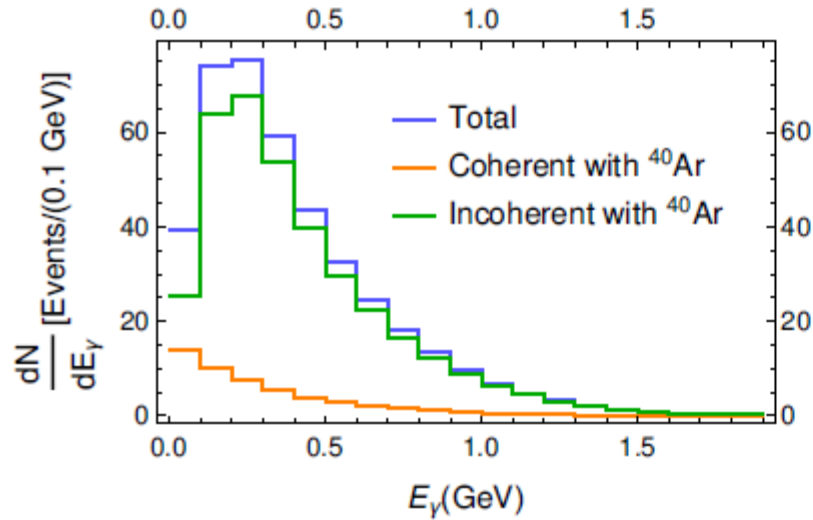


Z. Pavlovic, private communication

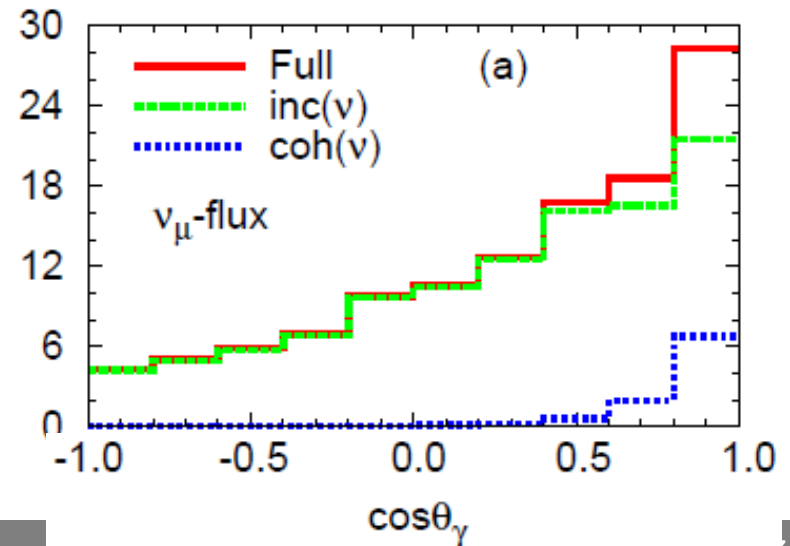
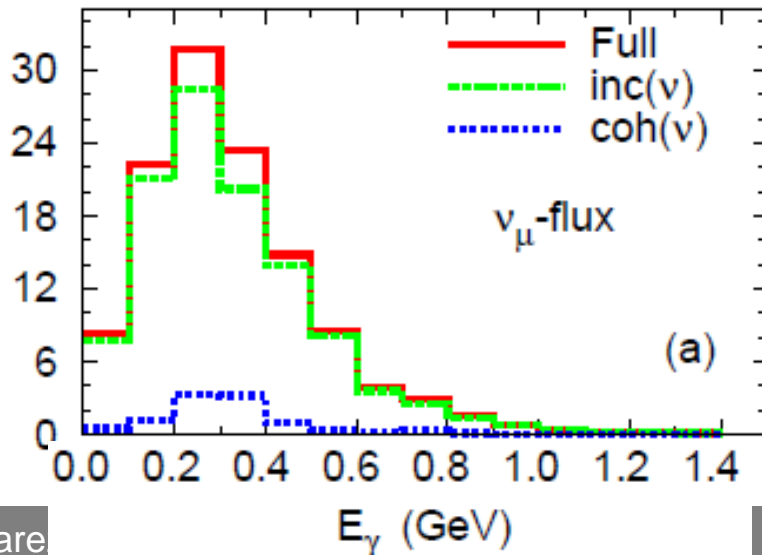


Events @ MicroBooNE

■ ν mode



■ SM prediction LAR & Wang

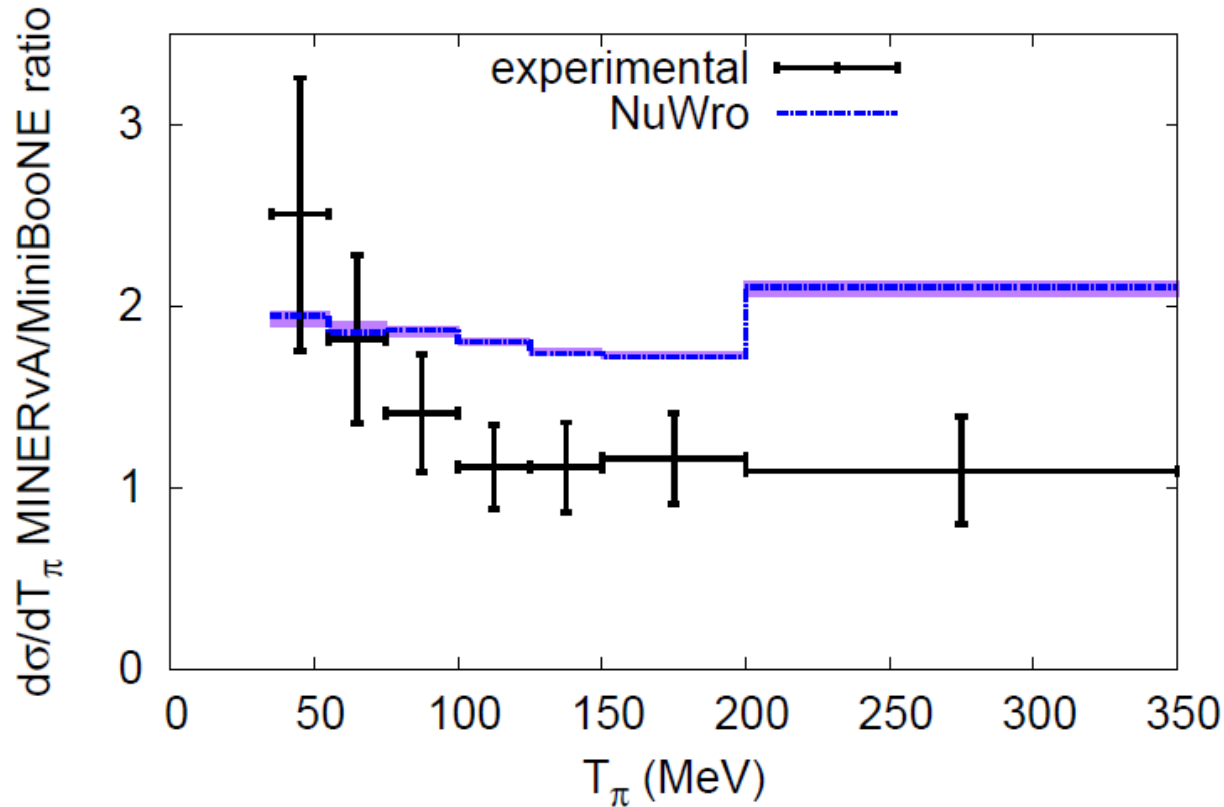


Summary

- The origin of the **MiniBooNE anomaly** is still not understood.
- Hard to reconcile with global oscillation analyses.
- Poorly understood ν **interactions** and/or **unaccounted backgrounds** could be the key
- Standard Model NC_γ : **insufficient** to explain the excess of events
- **Production** and **radiative decay** of **heavy sterile neutrinos** has been proposed as a **possible solution**
 - **not entirely satisfactory** but could still be a sizable contribution.
- Further insight from the **SBN** program at **Fermilab**.

π production on ^{12}C

- Sobczyk, Zmuda, PRC 91 (2015)



- In spite of flux difference, MiniBooNE and MINERvA data probe the same dynamics and should be strongly correlated