Probing Beta-Decay by Heavy Ion Charge Exchange Reactions

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Agenda:

- Investigating nuclear charge changing excitations:
 - single charge exchange (SCE) reactions
 - double charge exchange (DCE) reactions
- "Majorana" DCE reactions:
 - "0v2β" operator structure in hadronic interactions
 - DCE reactions and nuclear matrix elements
- Outlook

Nuclear Reactions as Probes for Nuclear β-Matrix Elements

Charge Exchange Reactions \leftrightarrow Charged Currents: $\Delta q=\pm 1$ excitation of Fermi- (J^{π}=0+,1-...) and GT- (J^{π}=0-,1+...) type states



Operators acting on projectile and target:

$$\left\{ 1_{\sigma}, \vec{\sigma}, \vec{\sigma} imes \vec{q}
ight\} \otimes au_{\pm}$$

Nucleon-Nucleon Interaction and Weak Interaction Vertices

Strong Interaction

Weak Interaction

$$V_{NN} \sim V_{01}(q^{2})\tau_{\pm}\tau_{\mp} \qquad \leftrightarrow \qquad g_{F}(q^{2})\tau_{\pm} \qquad \text{"Fermi"} \\ + V_{11}(q^{2})\sigma_{1}\cdot\sigma_{2} \ \tau_{\pm}\tau_{\mp} \qquad \leftrightarrow \qquad g_{A}(q^{2})\sigma \ \tau_{\pm} \qquad \text{"Gamow-Teller"} \\ + V_{T1}(q^{2})S_{12} \ \tau_{\pm}\tau_{\mp} \qquad \leftrightarrow \qquad g_{M}(q^{2})\sigma \times q \ \tau_{\pm} \qquad \text{"weak magnetic"} \\ + \dots$$

Rank-2 tensor operator:
$$S_{12} = \frac{1}{q^2} \left[3\sigma_1 \cdot \vec{q}\sigma_2 \cdot \vec{q} - \sigma_1 \cdot \sigma_2 q^2 \right]$$

Heavy Ion Single Charge Exchange Reaction (SCE)

Heavy Ion SCE Reactions: Rank-1 Central and Rank-2 Tensor Interaction



CNNP 2017: H. Ejiri, J. Bellone, J.A. Lay, G. Potel...

H. Lenske at al., Phys. Rev. Lett. 62, 1457 (1989)

Initial and Final State Interactions

a+A Initial (ISI) and b+B Final State Interactions (FSI): The reaction coefficient

 $(\rightarrow$ J. Bellone, poster on Thursday)

$$M_{\beta\alpha}(\mathbf{k}_{\alpha},\mathbf{k}_{\beta}) = \langle \chi_{\beta}^{(-)} | \mathcal{U}_{\beta\alpha} | \chi_{\alpha}^{(+)} \rangle$$

$$\mathcal{U}_{\alpha\beta}(\mathbf{r}) = \sum_{ST} \int \frac{d^3p}{(2\pi)^3} e^{-i\mathbf{p}\cdot\mathbf{r}} K^{(ST)}_{\alpha\beta}(\mathbf{p}).$$

$$N_{\alpha\beta}(\mathbf{k}_{\alpha},\mathbf{k}_{\beta},\mathbf{p}) = \frac{1}{(2\pi)^3} \langle \chi_{\beta}^{(-)} | e^{-i\mathbf{p}\cdot\mathbf{r}} | \chi_{\alpha}^{(+)} \rangle.$$

$$M_{\alpha\beta}(\mathbf{k}_{\alpha},\mathbf{k}_{\beta}) = \sum_{ST} \int d^{3}p K_{\alpha\beta}^{(ST)}(\mathbf{p}) N_{\alpha\beta}(\mathbf{k}_{\alpha},\mathbf{k}_{\beta},\mathbf{p}),$$

$$d\sigma_{\alpha\beta} = \frac{m_{\alpha}m_{\beta}}{(2\pi\hbar^2)^2} \frac{k_{\beta}}{k_{\alpha}} \frac{1}{(2J_a+1)(2J_A+1)} \sum_{M_a, M_A \in \alpha; M_b, M_B \in \beta} |M_{\alpha\beta}(\mathbf{k}_{\alpha}, \mathbf{k}_{\beta})|^2 d\Omega.$$

SCE cross section at small momentum transfer NME: b_{LSJ} ~ (B||T_{LSJ}||0)

Fermi-type transition in both nuclei

$$\frac{d\sigma^{FF}}{d\Omega} \sim \frac{q^{2(J_a+J_A)}}{\left[(2J_a+1)!!(2J_A+1)!!\right]^2} \left| V_{01}^{(C)}(0)b_{J_A0J_A}^{AB}b_{J_a0J_a}^{ab} + e^{i\phi_{aA}}V_{11}^{(C)}(0)b_{J_A1J_A}^{(AB)}b_{J_A1J_A}^{(AB)}\right|^2 \mathbf{N}_{\alpha\beta}$$

Gamov-Teller-type transition in both nuclei

$$\begin{split} & \frac{d\sigma^{GG}}{d\Omega} \sim \frac{q^{2(J_a+J_A-2)}}{\left[(2J_a-1)!!(2J_A-1)!!\right]^2} |V_{11}^{(C)}(0)|^2 \\ & \left| b_{J_A-11J_A}^{(AB)} + \frac{q^2}{(2J_A+1)(2J_A+3)} b_{J_A+11J_A}^{(AB)} \right|^2 \left| b_{J_a+11J_a}^{(ab)} + \frac{q^2}{(2J_a+1)(2J_a+3)} b_{J_a+11J_a}^{(ab)} \right|^2 \mathsf{N}_{\alpha\beta} \end{split}$$

...and mixed σ^{FG} and σ^{GF} : e.g. σ^{FG} spin-flip Fermi in a \rightarrow b and GT in A \rightarrow B

Double Charge Exchange Reactions and Double β-Decay

Nuclear Double Beta Decay



Double-SCE Reactions

dSCE:

Double Charge Exchange by sequential Single Charge Exchange

$${}^{18}O + {}^{40}Ca \rightarrow {}^{18}F + {}^{40}K \rightarrow {}^{18}Ne + {}^{40}Ar$$



Reaction Amplitude

$$M_{\alpha\beta}^{(DCE)}(\mathbf{k}_{bB},\mathbf{k}_{\alpha}) == \langle \chi_{\beta}^{(-)}, bB | T_{NN} \mathcal{G}^{(+)}(\omega) T_{NN} | aA, \chi_{aA}^{(+)} \rangle$$

Evaluation of the dSCE Amplitude to a Tractable Form

Bi-Orthogonal set of channel states: $|\gamma\rangle = |cC, \chi_{\gamma}^{(+)}\rangle$, $|\tilde{\gamma}\rangle = |cC, \tilde{\chi}_{\gamma}^{(+)}\rangle$

$$M_{\alpha\beta}^{(DCE)}(\mathbf{k}_{\beta},\mathbf{k}_{\alpha}) = \sum_{c,C} \int \frac{d^{3}k_{\gamma}}{(2\pi)^{3}} M_{bB,cC}^{(SCE)}(\mathbf{k}_{\beta},\mathbf{k}_{\gamma}) G_{cC}(\omega_{\gamma},\omega_{\alpha}) \tilde{M}_{cC,aA}^{(SCE)}(\mathbf{k}_{\gamma},\mathbf{k}_{\alpha})$$

...and making use of the analytic properties of the Green's function

$$M_{\beta\alpha}^{(DCE)}(\mathbf{k}_{\beta}, \mathbf{k}_{\alpha}) = \sum_{S_{1}, S_{2}, T=1} \int \frac{d^{3}k_{\gamma}}{(2\pi)^{3}} \int d^{3}p_{1}d^{3}p_{2}N_{\beta\gamma}(\mathbf{p}_{2})\tilde{N}_{\gamma\alpha}(\mathbf{p}_{1})t_{S_{2}T}(p_{2}^{2})t_{S_{1}T}(p_{1}^{2})$$

$$\times \oint \frac{d\zeta}{2i\pi} \Pi_{S_{2}S_{1}}^{(ba)\dagger}(\frac{1}{2}\tilde{\kappa} - \zeta - i\eta, \mathbf{p}_{2}, \mathbf{p}_{1}) \cdot \Pi_{S_{2}S_{1}}^{(BA)}(\frac{1}{2}\tilde{\kappa} + \zeta + i\eta', \mathbf{p}_{2}, \mathbf{p}_{1})$$

Nuclear CC Polarization Propagator

$$\Pi_{ba}(\mathbf{q}',\mathbf{q},\omega) = \langle 0|T_b^{\dagger}(\mathbf{q}')G(\omega)T_a(\mathbf{q})|0\rangle$$



Nuclear CC Response Functions:

$$R_{ab}(\mathbf{q},\omega) = -\frac{1}{\pi} Im \left[\Pi_{ab}(\mathbf{q},\mathbf{q},\omega) \right].$$

F.T. Baker, H.L. et al. Phys.Rept. 289 (1997) 235

CC Response Functions ${}^{40}Ca \rightarrow {}^{40}K(4^{-})$ and ${}^{18}O \rightarrow {}^{18}F(1^{+})$



Operator:

$$T_{LSJM} = \left(\frac{r}{R_d}\right)^L \left[\boldsymbol{\sigma}^S \otimes Y_L\right]_{JM} \tau_{\pm}$$

"Majorana" DCE and 0v2β Transitions

Weak Interaction $0\nu 2\beta$ decay and Strong Interaction Analogue

weak $0\nu 2\beta$ decay

Hadronic analogue



Nuclear Currents and Matrix Elements

The Target $A \rightarrow B$ coherent DCE Transitions





...a class of diagrams known from nuclear ground state correlations!



...~ 10...20% contribution to nuclear ground states (P. Konrad, H.L. NPA 756 2005).

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The $0\nu 2\beta 0^+ \rightarrow 0^+$ Nuclear Matrix Element

$$M^{0\nu} = \frac{4\pi R}{g_A^2(0)} \sum_{\rm L} \int d^3 x_1 \int d^3 x_2 \int \frac{d^3 q}{(2\pi)^3} \frac{e^{i\mathbf{q}\cdot(\mathbf{x}_1 - \mathbf{x}_2)}}{q(q + E_d)} \langle 0_F^+ | \mathcal{J}_{L,\mu}^{\dagger}(\mathbf{x}_1) \mathcal{J}_{L}^{\mu\dagger}(\mathbf{x}_2) | 0_I^+ \rangle$$

Nuclear charge-changing Currents \mathcal{G}_{L} :

- Vector
- Pseudo-vector
- Axial-vector
- Magnetic

Nuclear CC Currents and CC Transition Amplitude

$$\begin{aligned} \mathcal{J}_{V}^{\mu} &= \bar{\Psi}_{N} \gamma^{\mu} \tau \Psi_{N} \\ \mathcal{J}_{A}^{\mu} &= \bar{\Psi}_{N} \gamma^{\mu} \gamma_{5} \tau \Psi_{N} \\ \mathcal{J}_{S} &= \bar{\Psi}_{N} \gamma_{5} \tau \Psi_{N}. \end{aligned}$$

$$\begin{aligned} \mathcal{M}_{R} \mathcal{T}_{\pi N}^{(CC)} &= \mathcal{T}_{V}(s,t) \mathcal{J}_{V}^{\mu} \\ + \mathcal{T}_{A}(s,t) \mathcal{J}_{A}^{\mu} \\ + \mathcal{T}_{S}(s,t) \mathcal{J}_{S}^{\mu} \\ \mathcal{J}_{A}^{\mu} \\ \mathcal{J}_{A}^{\mu} \\ \mathcal{J}_{A}^{\mu} \\ \mathcal{J}_{A}^{\mu} \\ \mathcal{J}_{A}^{\mu} \\ \mathcal{J}_{A}^{\mu} \\ \mathcal{J}_{B}^{\mu} \\ \mathcal{J}_{$$

The Target DCE^(M) Transition Amplitude

$$M_{AB}^{(\pi\pi)}(k_1, k_2) = T_V^{(\pi\pi)}(s_1) G_{VV}^{(\pi\pi,\pi\pi)}(k_1, k_2) T_V^{(\pi\pi)}(s_2) + T_A^{(\rho\pi)}(s_1) H_{VV}^{(\rho\pi,\rho\pi)}(k_1, k_2) T_A^{(\rho\pi)}(s_2) - T_A^{(\rho\pi)}(s_1) G_{AA}^{(\rho\pi,\rho\pi)}(k_1, k_2) T_A^{(\rho\pi)}(s_2) + T_A^{(\sigma\pi)}(s_1) G_{AA}^{(\sigma\pi,\sigma\pi)}(k_1, k_2) T_A^{(\rho\pi)}(s_2) + T_S^{(\sigma\pi)}(s_1) G_{SS}^{(\sigma\pi,\sigma\pi)}(k_1, k_2) T_S^{(\rho\pi)}(s_2),$$

The full DCE^(M) Transition Amplitu

$$\mathcal{M}_{aA,bB}(k_{1},k_{2}) = M_{AB}^{(\pi\pi)}(k_{1},k_{2}) \langle b | \phi_{\pi^{-}}(k_{1})\phi_{\pi^{-}}(k_{2}) | a \rangle$$

$$+ M_{AB}^{(\rho\rho)\kappa\lambda}(k_{1},k_{2}) \langle b | \phi_{\kappa,\rho^{-}}(k_{1})\phi_{\lambda,\rho^{-}}(k_{2}) | a \rangle$$

$$+ M_{AB}^{(\pi\rho)\lambda}(k_{1},k_{2}) \langle b | \phi_{\pi^{-}}(k_{1})\phi_{\lambda,\rho^{-}}(k_{2}) | a \rangle$$

$$+ M_{AB}^{(\rho\pi)\kappa}(k_{1},k_{2}) \langle b | \phi_{\kappa,\rho^{-}}(k_{1})\phi_{\pi^{-}}(k_{2}) | a \rangle.$$

a →b

p

The Reaction Kernel

$$\mathcal{K}_{\alpha\beta}^{(CC)}(\mathbf{r}) = \int \frac{d^3k_1}{(2\pi)^3} \int \frac{d^3k_2}{(2\pi)^3} e^{-i(\mathbf{k}_1 + \mathbf{k}_2) \cdot \mathbf{r}} \mathcal{M}_{aA,bB}(\mathbf{k}_1, \mathbf{k}_2),$$

The Reaction Amplitude

$$\mathcal{R}_{\alpha\beta}^{(CC)}(\mathbf{k}_{\alpha},\mathbf{k}_{\beta}) = \langle \chi_{\beta}^{(-)} | \mathcal{K}_{aA,bB}^{(CC)} | \chi_{\alpha}^{(+)} \rangle.$$

Plane Wave Limit

$$\mathcal{R}_{\alpha\beta}^{(PW)}(\mathbf{k}_{\alpha},\mathbf{k}_{\beta}) = \int \frac{d^{3}k_{1}}{(2\pi)^{3}} \int \frac{d^{3}k_{2}}{(2\pi)^{3}} (2\pi)^{3} \delta(\mathbf{q}-\mathbf{k}_{1}-\mathbf{k}_{2}) \mathcal{M}_{aA,bB}(\mathbf{k}_{1},\mathbf{k}_{2})$$

Application: $^{18}O+^{40}Ca \rightarrow ^{18}Ne+^{40}Ar$

D. Carbone (Thursday, 2nd plenary): The NUMEN projectJ.-A. Lay (Tuesday, parallel): DCE and TransferJ. Bellone (Thursday, poster): Beta-decay and Heavy Ion SCE

Factorization of Energy and Momentum Dependence

$$T_X^{(xy)}(s,t,u) \sim T_X^{(xy)}(s) F_X^{(xy)}(t,u)$$

(xy)=(π,π), (σπ), (ρπ), (ρρ)..., X = V,A,P,S...



- T_{χ} (s) ~ energy dependent "running scaling" ~ $\sigma_{\pi N}$
- Coupling/vertex form factor $F_X(t,u) \sim F_X(q^2) \sim g_X^2(q^2)$

DCE Cross Section: dSCE and $,,\pi^{-}\pi^{0}\pi^{-}$ **Majorana-DCE**



F. Cappuzzello et al., Eur.Phys.J. A51 (2015) no.11, 145

Predictions and Estimates

• The most direct proof of a DCE^(M) reaction:

$$^{3}H + ^{3}He \rightarrow 3p + 3n$$

• Proof of a DCE^(M) reaction on a heavy target:

$${}^{3}H + A(Z,N) \rightarrow 3p + A(Z-2,N+2)$$
$${}^{3}He + A(Z,N) \rightarrow 3n + A(Z+2,N-2)$$

Rate of DCE^(M)?

- GSC in nuclei ~ 10...20%
- assume 1% of the special type of diagrams
- → DCE^(M) ~ 0.1...1% of all DCE reactions

Summary

- SCE, double-SCE, and Majorana-DCE heavy ion reactions
- Probing $0\nu 2\beta$ -type NME in a hadronic surrogate process:
 - NME of CC nuclear currents
 - Vertices by meson-nucleon T-matrix
- Interface to nuclear structure:
 - Nuclear CC response functions
 - Nuclear form factors
 - Heavy ion elastic interactions

...together with theory section of the NUMEN@LNS collaboration M. Colonna (Catania), E. Santopinto (Genova), J.-A. Lay (Sevilla), J. Lubian (Sao Paolo), N. Auerbach (Tel Aviv)