

Double Gamow-Teller transitions and its relation to neutrinoless $\beta\beta$ decays

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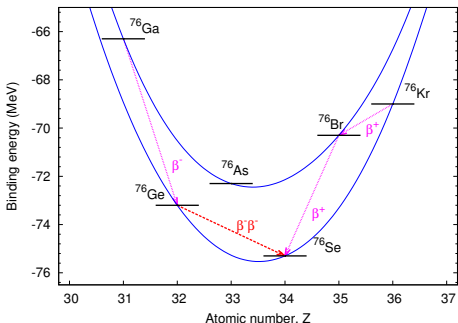


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Nuclear $\beta\beta$ decay

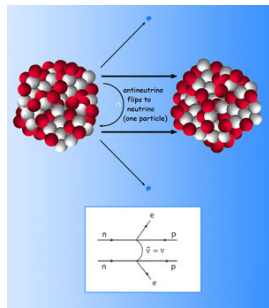
$\beta\beta$ decay second order process observable if β -decay is energetically forbidden or hindered by large ΔJ

Neutrinoless double-beta decay ($0\nu\beta\beta$):
Lepton-number violation, Majorana nature of neutrinos



$$Q_{\beta\beta} > 2\text{MeV}$$

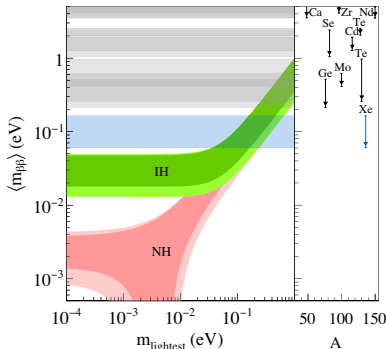
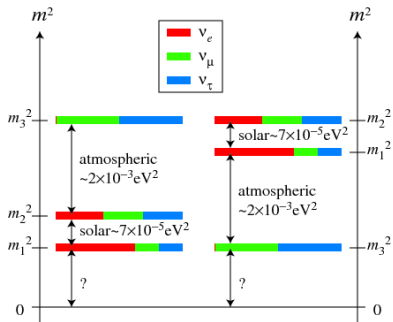
- $^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$
- $^{76}\text{Ge} \rightarrow ^{76}\text{Se}$
- $^{82}\text{Se} \rightarrow ^{82}\text{Kr}$
- $^{96}\text{Zr} \rightarrow ^{96}\text{Mo}$
- $^{100}\text{Mo} \rightarrow ^{100}\text{Ru}$
- $^{110}\text{Pd} \rightarrow ^{110}\text{Cd}$
- $^{116}\text{Cd} \rightarrow ^{116}\text{Sn}$
- $^{124}\text{Sn} \rightarrow ^{124}\text{Te}$
- $^{130}\text{Te} \rightarrow ^{130}\text{Xe}$
- $^{136}\text{Xe} \rightarrow ^{136}\text{Ba}$
- $^{150}\text{Nd} \rightarrow ^{150}\text{Sm}$



$0\nu\beta\beta$ decay matrix elements and experiment

The decay lifetime is $T_{1/2}^{0\nu\beta\beta} (0^+ \rightarrow 0^+)^{-1} = G_{01} |M^{0\nu\beta\beta}|^2 m_{\beta\beta}^2$

sensitive to absolute neutrino masses, $m_{\beta\beta} = |\sum U_{ek}^2 m_k|$, and hierarchy



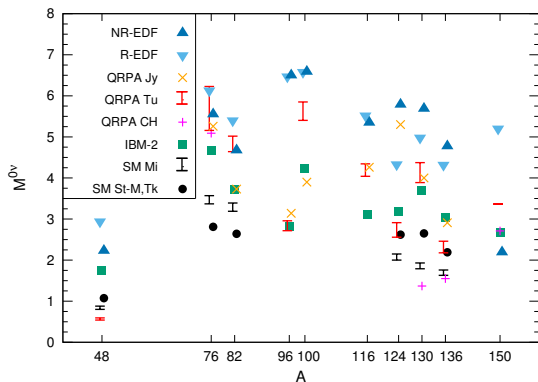
Matrix elements needed to make sure KamLAND-Zen, PRL117 082503(2016) next generation ton-scale experiments fully explore "inverted hierarchy"

$0\nu\beta\beta$ decay nuclear matrix elements

Large difference in nuclear matrix element calculations: factor $\sim 2 - 3$

$$\langle 0_f^+ | \sum_{n,m} \tau_n^- \tau_m^- \sum_X H^X(r) \Omega^X | 0_i^+ \rangle$$

$\Omega^X =$ Fermi ($\mathbb{1}$), GT ($\sigma_n \sigma_m$), Tensor
 $H(r) =$ neutrino potential



How can nuclear matrix elements calculations improve?

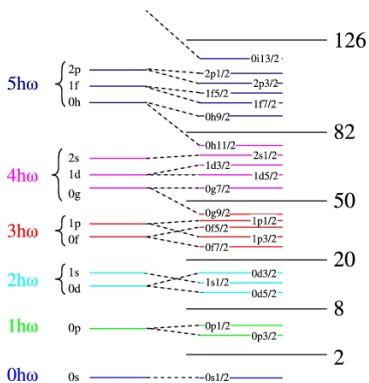
Talks by Simkovic, Coraggio (Mon), Suhonen, Barea (Tue)

Can nuclear structure experiments guide $0\nu\beta\beta$ decay?

Talks by Ejiri (Mon), Freckers (Sat)

Engel, JM, Rep. Prog. Phys. 80 046301 (2017)

Configuration space



Nuclear shell model configuration space only keep essential degrees of freedom

- High-energy orbits: always empty
- Configuration space: where many-body problem is solved
- Inert core: always filled

$$H|\Psi\rangle = E|\Psi\rangle \rightarrow H_{eff}|\Psi\rangle_{eff} = E|\Psi\rangle_{eff}$$

$$|\Psi\rangle_{eff} = \sum_{\alpha} c_{\alpha} |\phi_{\alpha}\rangle, \quad |\phi_{\alpha}\rangle = a_{i_1}^{+} a_{i_2}^{+} \dots a_{i_A}^{+} |0\rangle$$

Shell model codes (1 major oscillator shell)
 $\sim 10^{10}$ Slater dets. [Caurier et al. RMP77 \(2005\)](#)

QRPA calculations suggest
 larger spaces ($\gtrsim 2$ major shells) needed

Dimension \sim

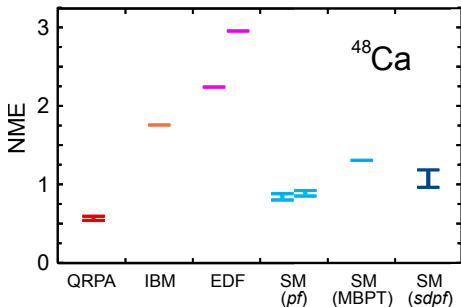
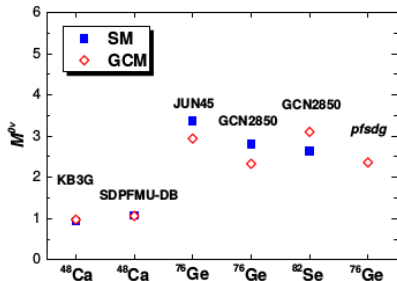
$$\binom{(p+1)(p+2)}{N} \binom{(p+1)(p+2)}{Z}$$

Shell model matrix elements in two shells

$^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$ $0\nu\beta\beta$ decay

Enlarge configuration space
from *pf* to *sdpf*, 4 to 7 orbitals

Test excitation energy of 0_2^+ in
 ^{48}Ca off by 1.3MeV in *pf* shell



Nuclear matrix element
increases moderately 30%

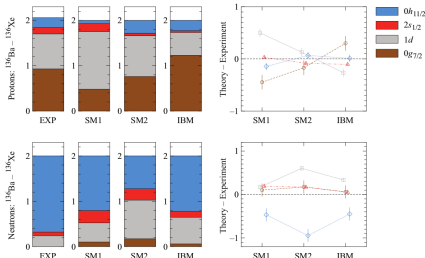
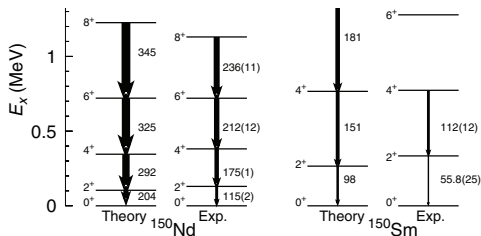
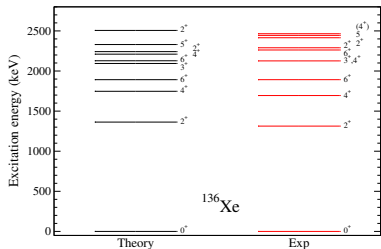
Iwata et al. PRL116 112502 (2016)

Likewise, very mild effect
found in GCM calculations of ^{76}Ge

Jiao et al. arXiv:1707.03940

Tests of nuclear structure

Spectroscopy well described: masses, spectra, transitions, knockout...



Schiffer et al. PRL100 112501(2009)

Kay et al. PRC79 021301(2009)

...

Szwec et al., PRC94 054314 (2016)

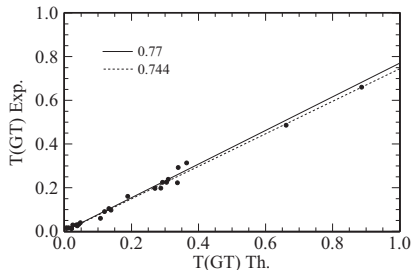
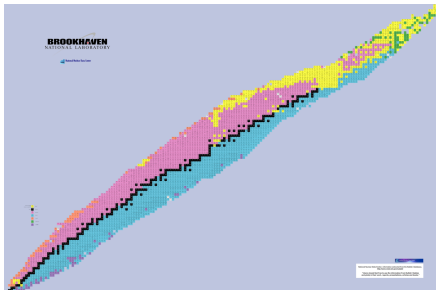
Rodríguez et al. PRL105 252503 (2010)

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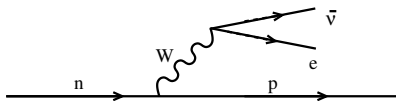
Vietze et al. PRD91 043520 (2015)

Nuclear β decays

β decays (e^- capture) main decay model along nuclear chart
In general well described by nuclear structure theory: shell model...



Martinez-Pinedo et al. PRC53 2602(1996)

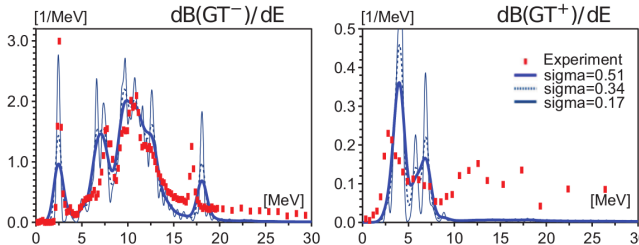
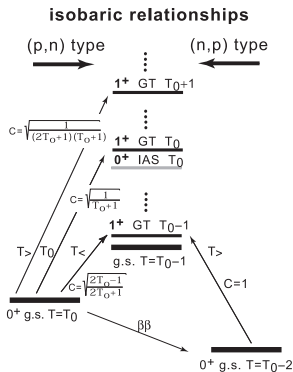


$$\langle F | \sum_i [g_A \sigma_{iT_i}^-]^{\text{eff}} | I \rangle, \quad [\sigma_{iT}^{\text{eff}}] \approx 0.7 \sigma_{iT}$$

Gamow-Teller transitions:
theory needs σ_{iT} "quenching"

Gamow-Teller strength distributions

Gamow-Teller (GT) distributions well described by theory (quenched)



Iwata et al. JPSCP 6 03057 (2015)

$$\langle 1_f^+ | \sum_i [\sigma_i \tau_i^\pm]^{\text{eff}} | 0_{gs}^+ \rangle, \quad [\sigma_i \tau_i^\pm]^{\text{eff}} \approx 0.7 \sigma_i \tau_i^\pm$$

$$M^{2\nu\beta\beta} = \sum_k \frac{\langle 0_f^+ | \sum_n \sigma_n \tau_n^- | 1_k^+ \rangle \langle 1_k^+ | \sum_m \sigma_m \tau_m^- | 0_i^+ \rangle}{E_k - (M_i + M_f)/2}$$

Freckers et al.

NPA916 219 (2013)

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Double Gamow-Teller strength distribution

Measurement of Double Gamow-Teller (DGT) resonance
in double charge-exchange reactions $^{48}\text{Ca}(pp,nn)^{48}\text{Ti}$ proposed in 80's

Auerbach, Muto, Vogel... 1980's, 90's

Recent experimental plans in RCNP, RIKEN (^{48}Ca), INFN Catania

Takaki et al. JPS Conf. Proc. 6 020038 (2015)

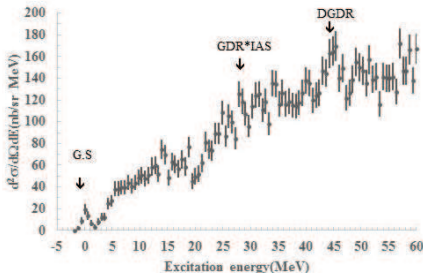
Capuzzello et al. EPJA 51 145 (2015), Takahisa, Ejiri et al. arXiv:1703.08264

Talks by Ejiri, Lenske (Mon), Yako, Lay (Tue), Carbone (Thu)

Promising connection to $\beta\beta$ decay,
two-particle-exchange process,
especially the (tiny) transition
to ground state of final state

Two-nucleon transfers related to
 $0\nu\beta\beta$ decay matrix elements

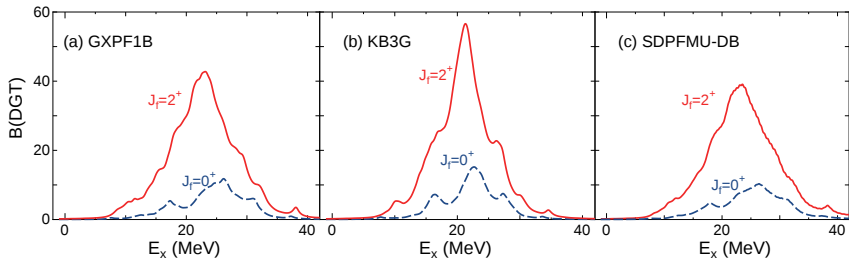
Brown et al. PRL113 262501 (2014)



^{48}Ca Double Gamow-Teller distribution

Calculate with shell model $^{48}\text{Ca } 0_{\text{gs}}^+$ Double Gamow-Teller distribution

$$B(\text{DGT}^-; \lambda; i \rightarrow f) = \frac{1}{2J_i + 1} \left| \left\langle {}^{48}\text{Ti} \left\| \left[\sum_i \sigma_i \tau_i^- \times \sum_j \sigma_j \tau_j^- \right]^{(\lambda)} \right\| \left| {}^{48}\text{Ca}_{\text{gs}} \right\rangle \right|^2$$



Shell model calculation with Lanczos strength function method

Double GT resonances in one and two shells rather similar result

Shimizu, JM, Yako, arXiv:1709.01088

Double Gamow-Teller distribution and pairing

Study the sensitivity of Double GT distribution to pairing correlations

Add/remove pairing

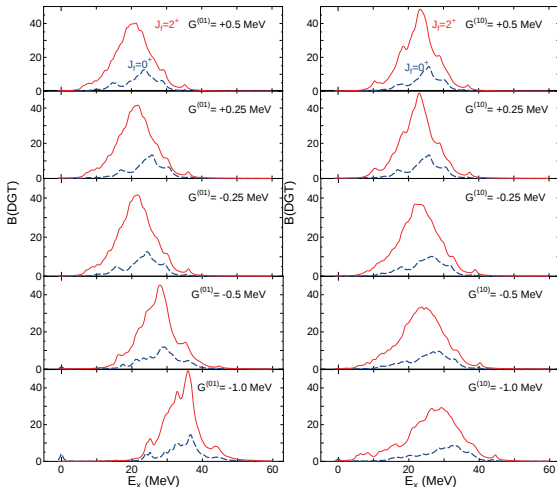
$$H' = H + G^{JT} P^{JT}$$

like-particle ($T=1$) or
proton-neutron ($T=0$)

Position of the
DGT giant resonance
very sensitive to
like-particle pairing

DGT resonance width
probes isoscalar pairing

Shimizu, JM, Yako,
arXiv:1709.01088

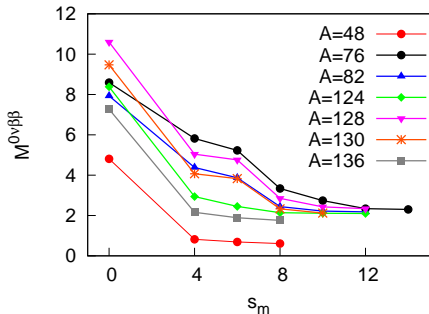


Pairing correlations and $\beta\beta$ decays

$0\nu\beta\beta$ decay favoured by (isovector) pairing, disfavored isoscalar pairing

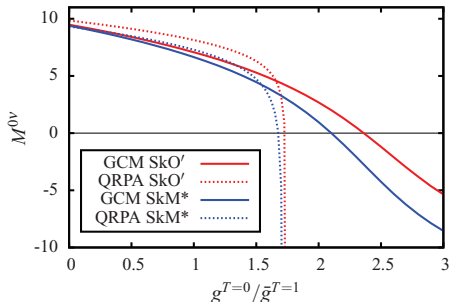
Talk by Hinohara (Fri)

Ideal case: superfluid nuclei reduced with high-seniorities



Caurier et al. PRL100 052503 (2008)

Addition of isoscalar pairing reduces matrix element value

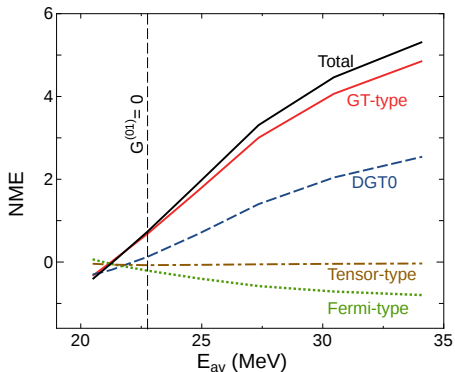


Hinohara, Engel PRC90 031301 (2014)

Related to approximate $SU(4)$ symmetry of the $\sum H(r)\sigma_i\sigma_j\tau_i\tau_j$ operator

^{48}Ca DGT resonance and $0\nu\beta\beta$ decay

Correlation between Double Gamow-Teller resonance in ^{48}Ca and $0\nu\beta\beta$ decay nuclear matrix element



Energy of DGT resonance with accuracy to $\sim 1\text{MeV}$, can give insight on the value of $0\nu\beta\beta$ decay nuclear matrix element

$$E_{av} = \frac{\sum_f E_f B(DGT^-, i \rightarrow f)}{\sum_f B(DGT^-, i \rightarrow f)}$$

Might be feasible in near future

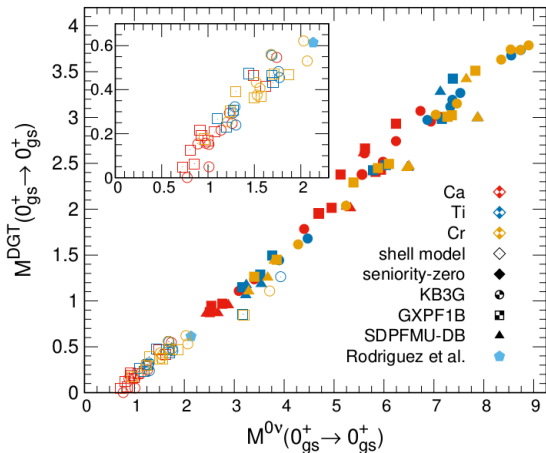
Shimizu, JM, Yako, arXiv:1709.01088

In progress: sensitivity to other nuclear structure correlations

DGT to ground state and $0\nu\beta\beta$ decay

DGT transition to ground state of final nucleus:
Ca, Ti, Cr isotopic chains

$$M^{\text{DGT}} = \langle \text{Final}_{\text{gs}} || [\sum_i \sigma_i \tau_i^- \times \sum_j \sigma_j \tau_j^-]^0 || \text{Initial}_{\text{gs}} \rangle|^2$$

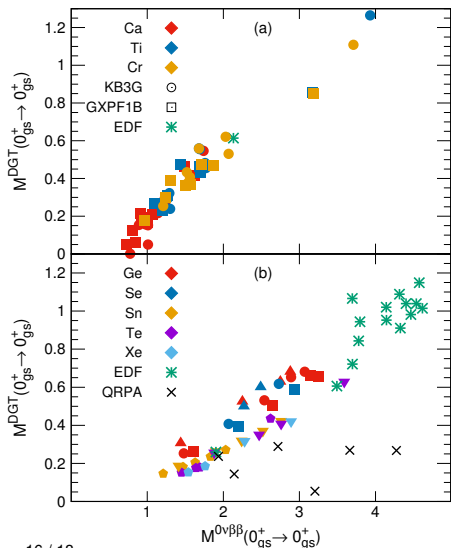


Very good linear correlation between DGT and $0\nu\beta\beta$ decay nuclear matrix elements

Linear correlation holds for ~ 25 transitions studied for simplified wf's (seniority-zero), for different interactions

Shimizu, JM, Yako,
arXiv:1709.01088

DGT and $0\nu\beta\beta$ decay: heavy nuclei



DGT transition to ground state

$$M^{\text{DGT}} = \sqrt{B(\text{DGT}_{-}; 0; 0_{\text{gs}}^+ \rightarrow 0_{\text{gs}}^+)}$$

very good linear correlation
 with $0\nu\beta\beta$ decay
 nuclear matrix elements

Correlation holds
 across wide range of nuclei,
 from Ca to Ge and Xe

Common to shell model and
 energy-density functional theory
 $0 \lesssim M^{0\nu\beta\beta} \lesssim 5$
 disagreement to QRPA

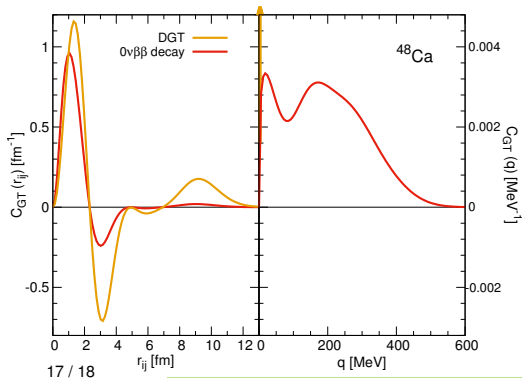
Shimizu, JM, Yako, arXiv:1709.01088

Short-range character of DGT, $0\nu\beta\beta$ decay

DGT transition to ground state same initial, final states with $0\nu\beta\beta$ decay

Correlation between DGT and $0\nu\beta\beta$ decay matrix elements explained by transition involving low-energy states combined with dominance of short distances between exchanged/decaying neutrons

Bogner et al. PRC86 064304 (2012)



$0\nu\beta\beta$ decay matrix element limited to shorter range

Short-range part dominant in double GT matrix element due to partial cancellation of mid- and long-range parts

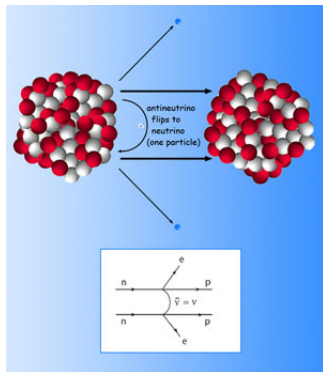
Long-range part dominant in QRPA DGT matrix elements!

Shimizu, JM, Yako, arXiv:1709.01088

Summary

Nuclear matrix elements are key for the design of next-generation tonne-scale $0\nu\beta\beta$ decay experiments and for fully exploiting the experimental results

- Present matrix element calculations disagree
Need improved calculations, guidance from other nuclear experiments
- Shell model nuclear matrix elements in two shells for ^{48}Ca , ^{76}Ge , suggest moderate enhancement ($\lesssim 30\%$)
- Double Gamow-Teller transitions pursued in RIKEN, INFN LNS, RCNP Osaka can provide very useful insight on value of $0\nu\beta\beta$ decay matrix elements



Collaborators



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