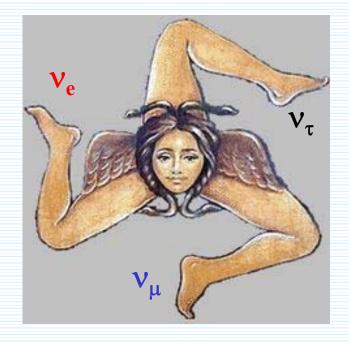
### Conference on Neutrino and Nuclear Physics Monastero dei Benedettini, Catania-Sicily: October 15-21, 2017



## **Favored** 0vββ decay mechanisms and associated nuclear matrix elements Fedor Šimkovic





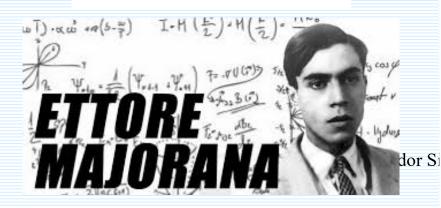


# **Majorana fermion**



https://en.wikipedia.org/wiki/File:Ettore\_Majorana.jpg





### TEORIA SIMMETRICA DELL'ELETTRONE E DEL POSITRONE

Nota di ETTORE MAJORANA

#### Symmetric Theory of Electron and Positron Nuovo Cim. 14 (1937) 171

Sunto. - Si dimostra la possibilità di pervenire a una piena simmetrizzazione formale della teoria quantistica dell'elettrone e del positrone facendo uso di un nuovo processo di quantizzazione. Il significato delle equazioni di DIRAC ne risulta alquanto modificato e non vi è più luogo a parlare di stati di energia negativa; nè a presumere per ogni altro tipo di particelle, particolarmente neutre, l'esistenza di « antiparticelle » corrispondenti ai « vuoti » di energia negativa.

L'interpretazione dei cosidetti « stati di energia negativa » proposta da DIRAC (<sup>1</sup>) conduce, come è ben noto, a una descrizione sostanzialmente simmetrica degli elettroni e dei positroni. La sostanziale simmetria del formalismo consiste precisamente in questo, che fin dove è possibile applicare la teoria girando le difficoltà di convergenza, essa fornisce realmente risultati del tutto simmetrici. Tuttavia gli artifici suggeriti per dare alla teoria una forma simmetrica



- trica, sia iante tali she possinuova via

che conduce più direttamente alla meta.

Per quanto riguarda gli elettroni e i positroni, da essa si può veramente attendere soltanto un progresso formale; ma ci sembra importante, per le possibili estensioni analogiche, che venga a cadere la nozione stessa di stato di energia negativa. Vedremo infatti che è perfettamente possibile costruire, nella maniera più naturale, una teoria delle particelle neutre elementari senza stati negativi.

(<sup>1</sup>) P. A. M. DIEAC, & Proc. Camb. Phil. Soc. », 80, 150, 1924. V. anche W. HEISENBERG, & ZS. f. Phys. », 90, 209, 1934.







I ragazzi di via Panisperna



#### MESONIUM AND ANTIMESONIUM

**B. PONTECORVO** 

Joint Institute for Nuclear Research

Submitted to JETP editor May 23, 1957

J. Exptl. Theoret. Phys. (U.S.S.R.) 33, 549-551 (August, 1957)

INVERSE BETA PROCESSES AND NONCON-SERVATION OF LEPTON CHARGE

#### **B. PONTECORVO**

Joint Institute for Nuclear Research

Submitted to JETP editor October 19, 1957

J. Exptl. Theoret. Phys. (U.S.S.R.) 34, 247-249 (January, 1958)

It follows from the above assumptions that in vacuum a neutrino can be transformed into an antineutrino and vice versa. This means that the neutrino and antineutrino are "mixed" particles, i.e., a symmetric and antisymmetric combination of two truly neutral Majorana particles  $\nu_1$  and  $\nu_2$  of different combined parity.<sup>5</sup>

1968 Gribov, Pontecorvo [PLB 28(1969) 493] oscillations of neutrinos - a solution of deficit of solar neutrinos in Homestake exp.

### **OUTLINE**

- Introduction v-oscillations and v-masses
- The 0 νββ-decay scenarios due neutrinos exchange (simpliest, sterile v, LR-symmetric model)
- DBD NMEs and Quenching of  $g_A$ (nuclear structure issues)
- DBD NMEs within schematic models (SU(4) symmetry, nonlinear QRPA)
   Conclusion

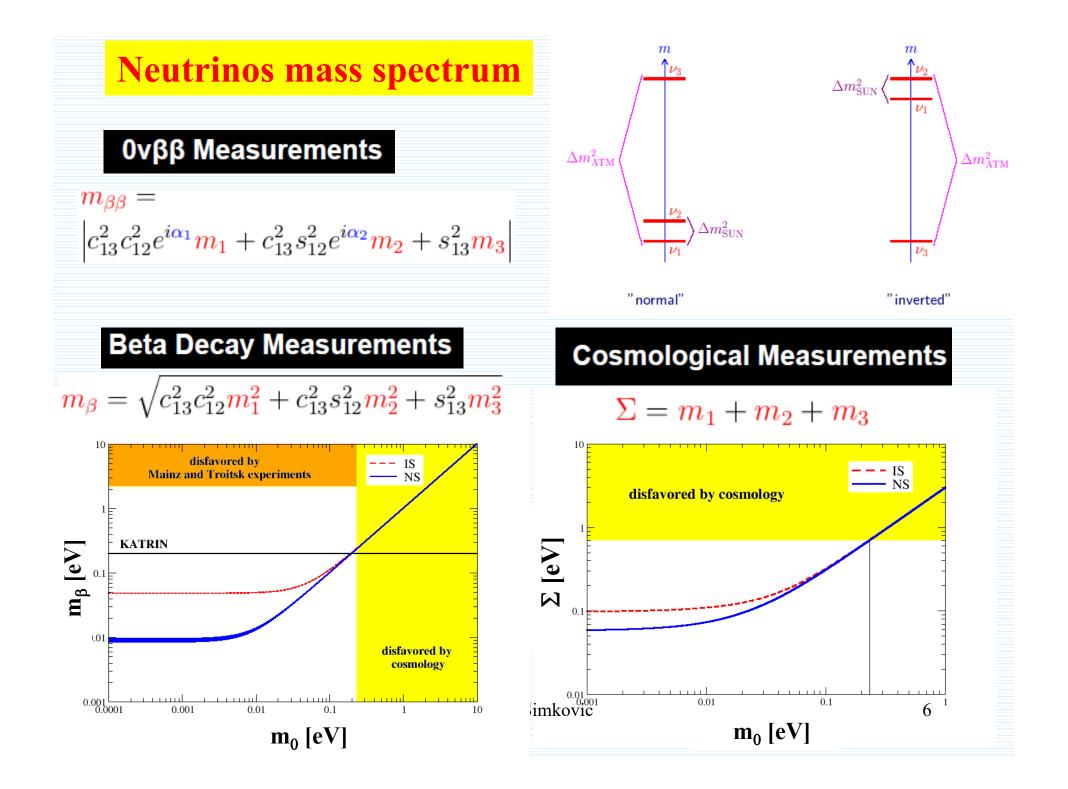
Acknowledgements: A. Faesler (Tuebingen), P. Vogel (Caltech), S. Kovalenko (Valparaiso U.), M. Krivoruchenko (ITEP Moscow), D. Štefánik, R. Dvornický (Comenius U.), A. Babič, A. Smetana, J. Terasaki (IEAP CTU Prague), ... **Observation of v-oscillations = the first prove of the BSM physics** 

mass-squared differences:  $\Delta m^2_{SUN} \cong 7.5 \ 10^{-5} \ eV^2$ ,  $\Delta m^2_{ATM} \cong 2.4 \ 10^{-3} \ eV^2$ 

The observed small neutrino masses (limits from tritium β-decay, cosmology) have profound implications for our understanding of the Universe and are now a major focus in astro, particle and nuclear physics and in cosmology.

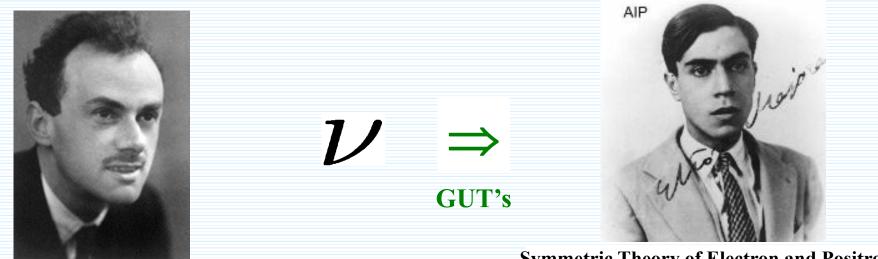
PMNS<br/>unitary<br/>mixing<br/>matrix $\begin{pmatrix} v_e \\ v_{\mu} \\ v_{\tau} \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} v_1 \\ v_2 \\ v_3 \end{pmatrix}$ Iarge off-diagonal valuesImatrix $\begin{pmatrix} v_e \\ v_{\mu} \\ v_{\tau} \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} v_1 \\ v_2 \\ v_3 \end{pmatrix}$  $\begin{pmatrix} 0.82 & 0.54 & -0.15 \\ -0.35 & 0.70 & 0.62 \\ 0.44 & -0.45 & 0.77 \end{pmatrix}$ 

 $3 \text{ angles: } \theta_{12} = 33.36^{\circ} \text{ (solar), } \theta_{13} = 8.66^{\circ} \text{ (reactor), } \theta_{23} = 40.0^{\circ} \text{ or } 50.4^{\circ} \text{ (atmospheric)}$  $U^{PMNS} = \begin{pmatrix} c_{12}c_{13} & c_{13}s_{12} & e^{-i\delta}s_{13} \\ -c_{23}s_{12} - e^{i\delta}c_{12}s_{13}s_{23} & c_{12}c_{23} - e^{i\delta}s_{12}s_{13}s_{23} & c_{13}s_{23} \\ s_{12}s_{23} - e^{i\delta}c_{12}c_{23}s_{13} & -e^{i\delta}c_{23}s_{12}s_{13} - c_{12}s_{23} & c_{13}c_{23} \end{pmatrix} \begin{pmatrix} e^{i\alpha_{1}} & 0 & 0 \\ 0 & e^{i\alpha_{2}} & 0 \\ 0 & 0 & 1 \end{pmatrix}$  $\text{unknown (CP violating) phases: } \delta, \alpha_{1}, \alpha_{2}$ 



The answer to the question whether neutrinos are their own antiparticles is of central importance, not only to our understanding of neutrinos, but also to our understanding of the origin of mass.

### What is the nature of neutrinos?



Symmetric Theory of Electron and Positron Nuovo Cim. 14 (1937) 171

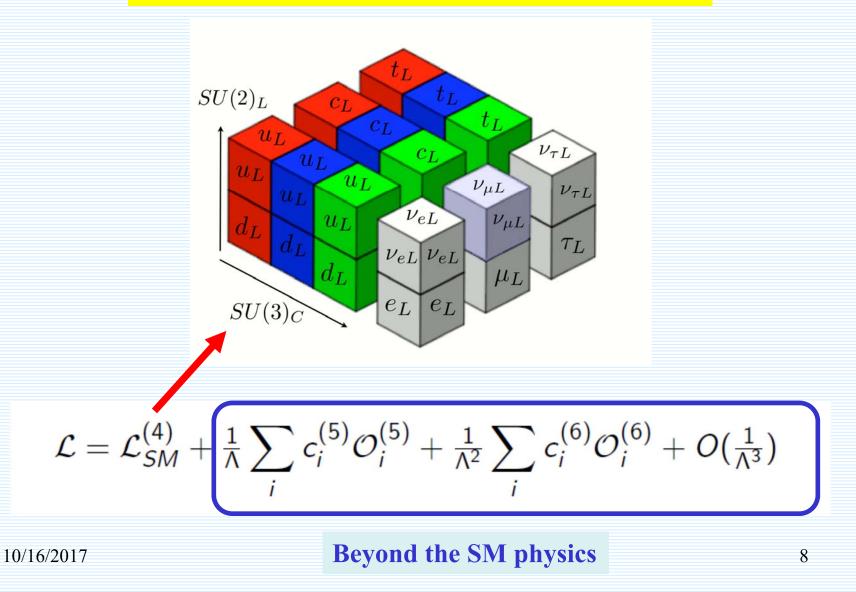
### Only the $0\nu\beta\beta$ -decay can answer this fundamental question

Analogy with kaons: K<sub>0</sub> and K<sub>0</sub>

Fedor Simkovic

Analogy with  $\pi_0$ 

## Beyond the Standard model physics (EFT scenario)



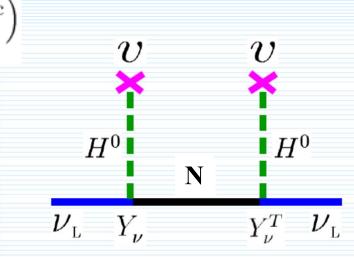
## Minimal SM + EFT

The absence of the right-handed neutrino fields in the Standard Model is the simplest, most economical possibility. In such a scenario Majorana mass term is the only possibility for neutrinos to be massive and mixed. This mass term is generated by the lepton number violating Weinberg effective Lagrangian.

$$\mathcal{L}_{5}^{eff} = -\frac{1}{\Lambda} \sum_{l_{1}l_{2}} \left( \overline{\Psi}_{l_{1}L}^{lep} \widetilde{\Phi} \right) \acute{Y}_{l_{1}l_{2}} \left( \widetilde{\Phi}^{T} (\Psi_{l_{2}L}^{lep})^{e} \right)$$
$$m_{i} = \frac{v}{-} (y_{i}v), \quad i = 1, 2, 3 \qquad \Lambda > 10^{15} \text{ GeV}$$

-1

Heavy Majorana leptons  $N_i (N_i=N_i^c)$ singlet of  $SU(2)_L xU(1)_Y$  group Yukawa lepton number violating int.



The three Majorana neutrino masses are suppressed by the ratio of the electroweak scale and a scale of a lepton-number violating physics.

The discovery of the  $\beta\beta$ -decay and absence of transitions of flavor neutrinos into sterile states would be evidence in favor of this minimal scenario.

## **I.** *The simplest 0 vββ-decay scenario* (SM + EFT scenario)

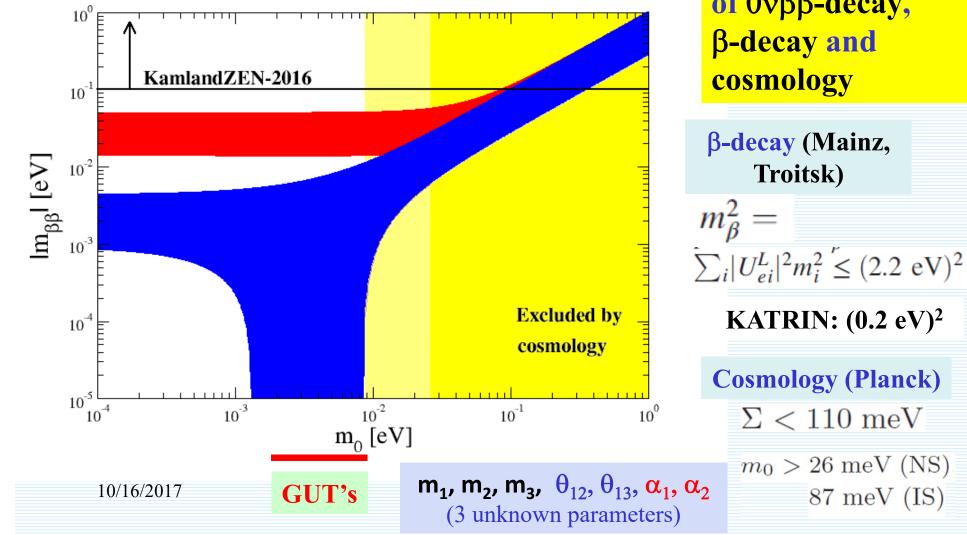
$$\left(T^{0\nu}_{1/2}\right)^{-1} = \left|\frac{m_{\beta\beta}}{m_e}\right|^2 g_A^4 \left|M^{0\nu}_{\nu}\right|^2 G^{0\nu}$$

### $(A,Z) \rightarrow (A,Z+2) + e^- + e^-$

|                      |   | transition                        | $G^{01}(E_0, Z)$  | $Q_{\beta\beta}$                                   | Abund. | $ M^{0\nu} ^2$ |  |
|----------------------|---|-----------------------------------|-------------------|--|--------|----------------|--|
|                      | _ A=const (even) _  |                                   | $	imes 10^{14} y$ | [MeV]  | (%)    |                |  |
| units)               |   | $^{150}Nd \rightarrow ^{150}Sm$   | 26.9              | 3.667  | 6      | ?              |  |
|                      | Z odd   | ${}^{48}Ca \rightarrow {}^{48}Ti$ | 8.04              | 4.271  | 0.2    | ?              |  |
| rary                 |   | ${}^{96}Zr \rightarrow {}^{96}Mo$ | 7.37              | 3.350  | 3      | ?              |  |
| (arbitrary           |   | $^{116}Cd \rightarrow {}^{116}Sn$ | 6.24              | 2.802  | 7      | ?              |  |
| s (ai                |   | $^{136}Xe \rightarrow {}^{136}Ba$ | 5.92              | 2.479  | 9      | ?              |  |
| Atomic mass          | $ \beta^+$ $$   | $^{100}Mo \rightarrow {}^{100}Ru$ | 5.74              | 3.034  | 10     | ?              |  |
| lic 1                |   | $^{130}Te \rightarrow ^{130}Xe$   | 5.55              | 2.533  | 34     | ?              |  |
| ton                  | $ \begin{array}{c c} & & & \\ & & & & \\ & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & $ | $^{82}Se \rightarrow {}^{82}Kr$   | 3.53              | 2.995  | 9      | ?              |  |
| ◄                    | /   | $^{76}Ge \rightarrow ^{76}Se$     | 0.79              | 2.040  | 8      | ?              |  |
|                      | – Z even –  |                                   |                   |  |        |                |  |
|                      |   |                                   |                   |  | -      |                |  |
| $\Delta L = L - L_0$ |   |                                   |                   | ββ-decay must be evaluated<br>Is of nuclear theory |        |                |  |



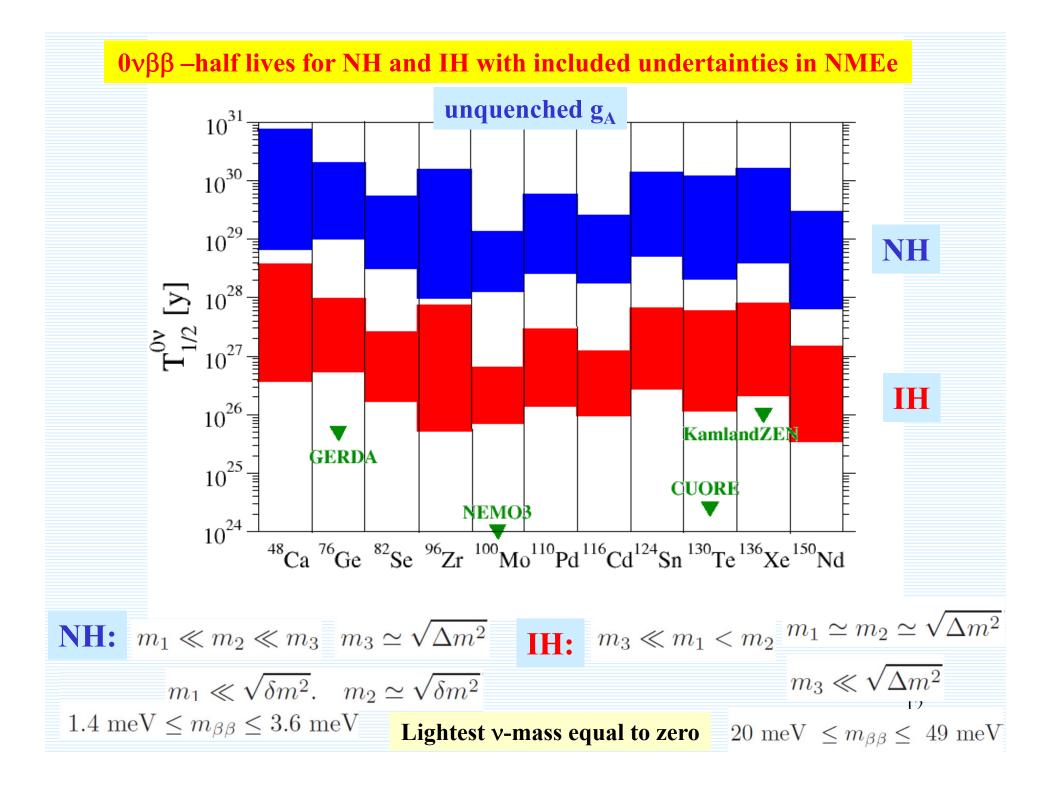
### **Effective mass of Majorana neutrinos**

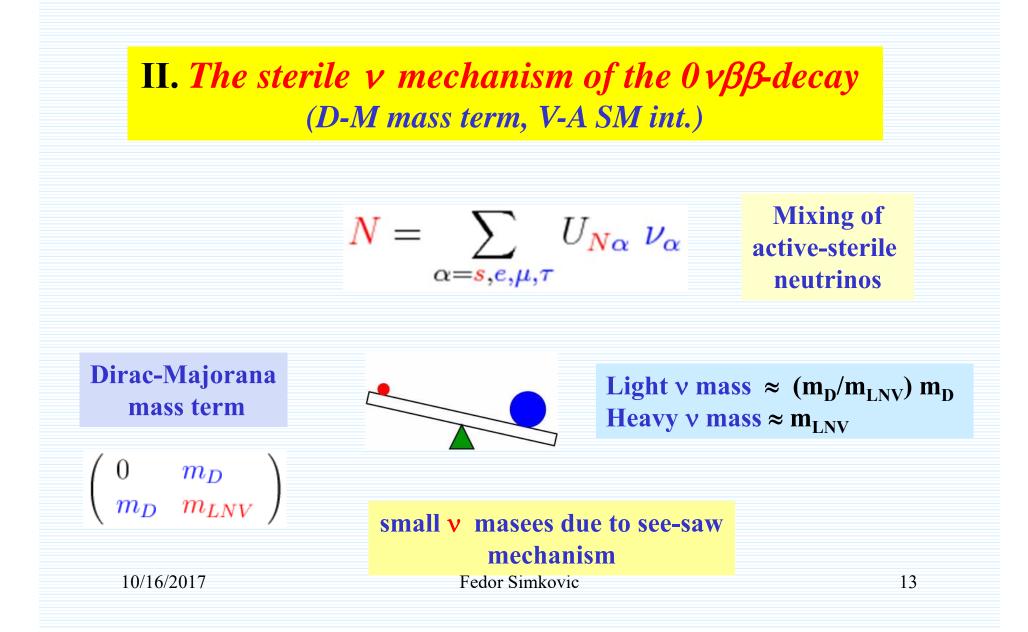


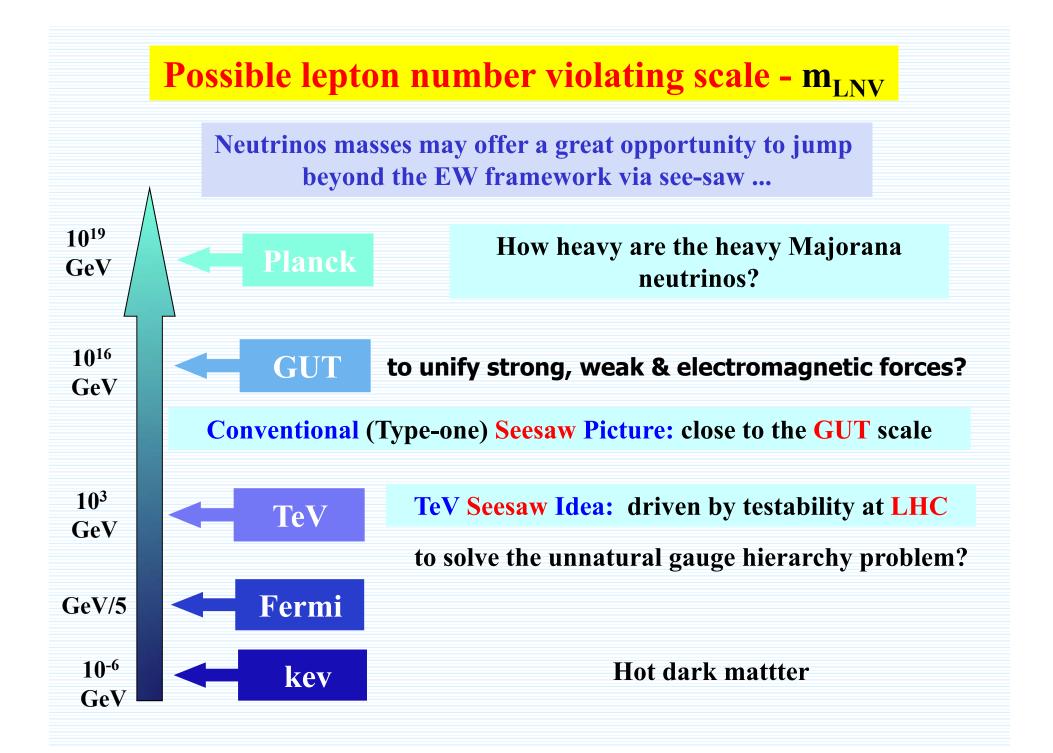
**Complementarity** of  $0\nu\beta\beta$ -decay, **β-decay and** cosmology

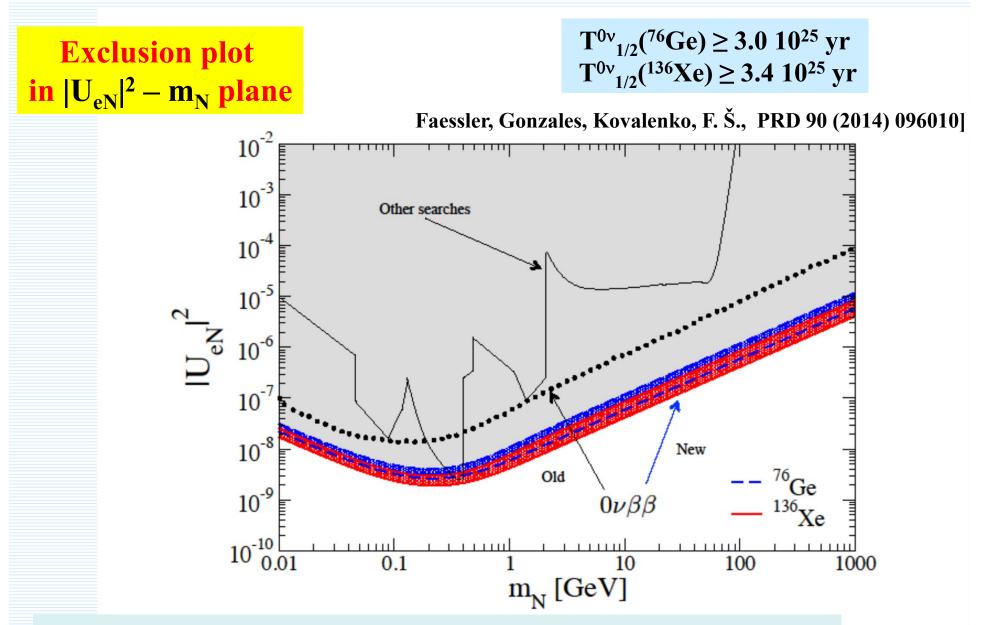
β-decay (Mainz, **Troitsk)** 

87 meV (IS)

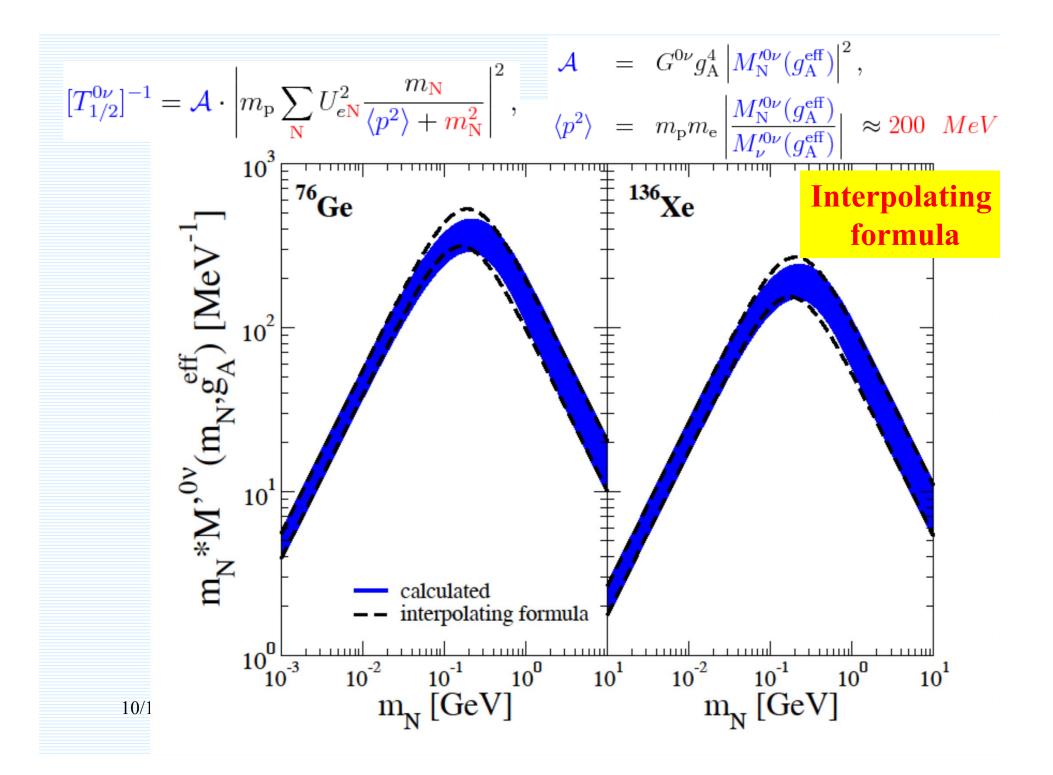








**Improvements:** i) QRPA (constrained Hamiltonian by  $2\nu\beta\beta$  half-life, self-consistent treatment of src, restoration of isospin symmetry ...), ii) More stringent limits on the  $0\nu\beta\beta$  half-life



## **III.** The 0 νββ-decay within L-R symmetric theories (D-M mass term, see-saw, V-A and V+A int., exchange of light neutrinos)

### Effective β-decay Hamiltonian

$$\boldsymbol{H}^{\boldsymbol{\beta}} = \frac{G_{\boldsymbol{\beta}}}{\sqrt{2}} \left[ j_L^{\ \rho} J_{L\rho} + \boldsymbol{\chi} \, j_L^{\ \rho} J_{R\rho} \right]$$

$$+ \quad \eta \; j_R^{\rho} J_{L\rho} + \; \lambda \; j_R^{\rho} J_{R\rho} + h.c. \Big]$$

Mixing of vector bosons  $\boldsymbol{W}_L$  and  $\boldsymbol{W}_R$ 

$$\begin{pmatrix} W_L^- \\ W_R^- \end{pmatrix} = \begin{pmatrix} \cos \zeta & \sin \zeta \\ -\sin \zeta & \cos \zeta \end{pmatrix} \begin{pmatrix} W_1^- \\ W_2^- \end{pmatrix}$$

The  $0\nu\beta\beta$ -decay half-life

10/16/2017

$$\begin{bmatrix} T_{1/2}^{0\nu} \end{bmatrix}^{-1} = \frac{\Gamma^{0\nu}}{\ln 2} = g_A^4 |M_{GT}|^2 \left\{ C_{mm} \frac{|m_{\beta\beta}|^2}{m_e} \right\}^2$$
$$+ C_{m\lambda} \frac{|m_{\beta\beta}|}{m_e} \langle \lambda \rangle \cos \psi_1 + C_{m\eta} \frac{|m_{\beta\beta}|}{m_e} \langle \eta \rangle \cos \psi_2$$

+ 
$$C_{\lambda\lambda}\langle\lambda\rangle^2$$
 +  $C_{\eta\eta}\langle\eta\rangle^2$  +  $C_{\lambda\eta}\langle\lambda\rangle\langle\eta\rangle\cos(\psi_1-\psi_2)$ 

left- and right-handed lept. currents

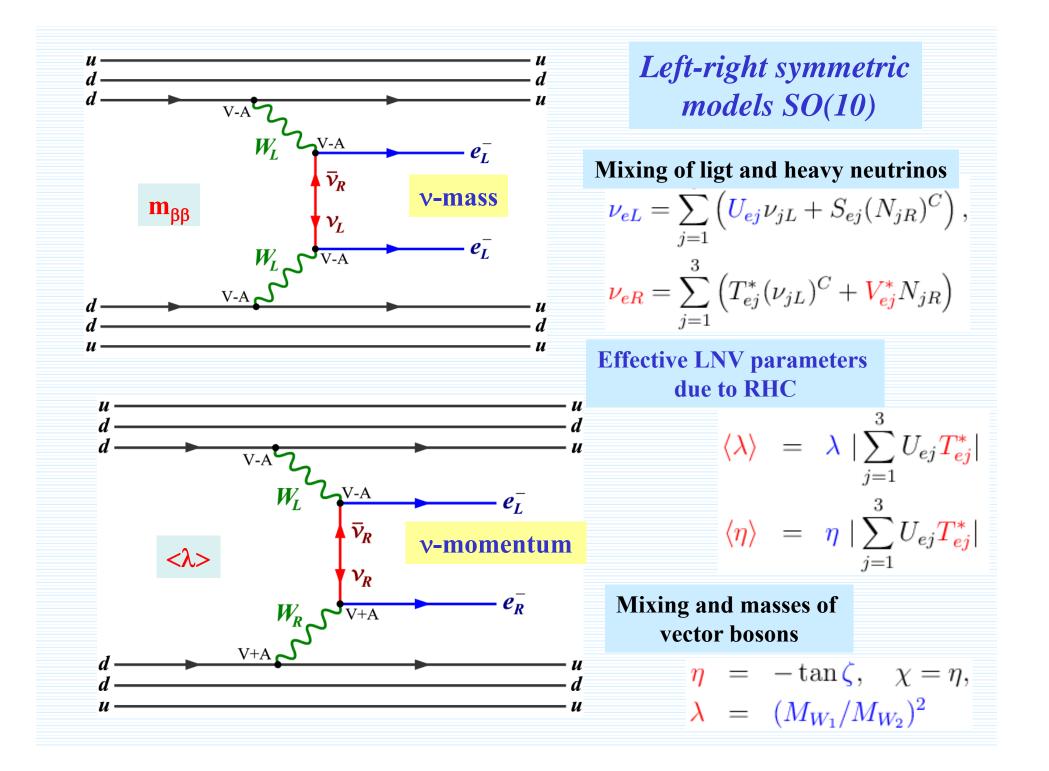
$$egin{array}{rcl} j_L^{\ 
ho} &=& ar e \gamma^
ho (1-\gamma_5) 
u_{eL} \ j_R^{\ 
ho} &=& ar e \gamma^
ho (1+\gamma_5) 
u_{eR} \end{array}$$

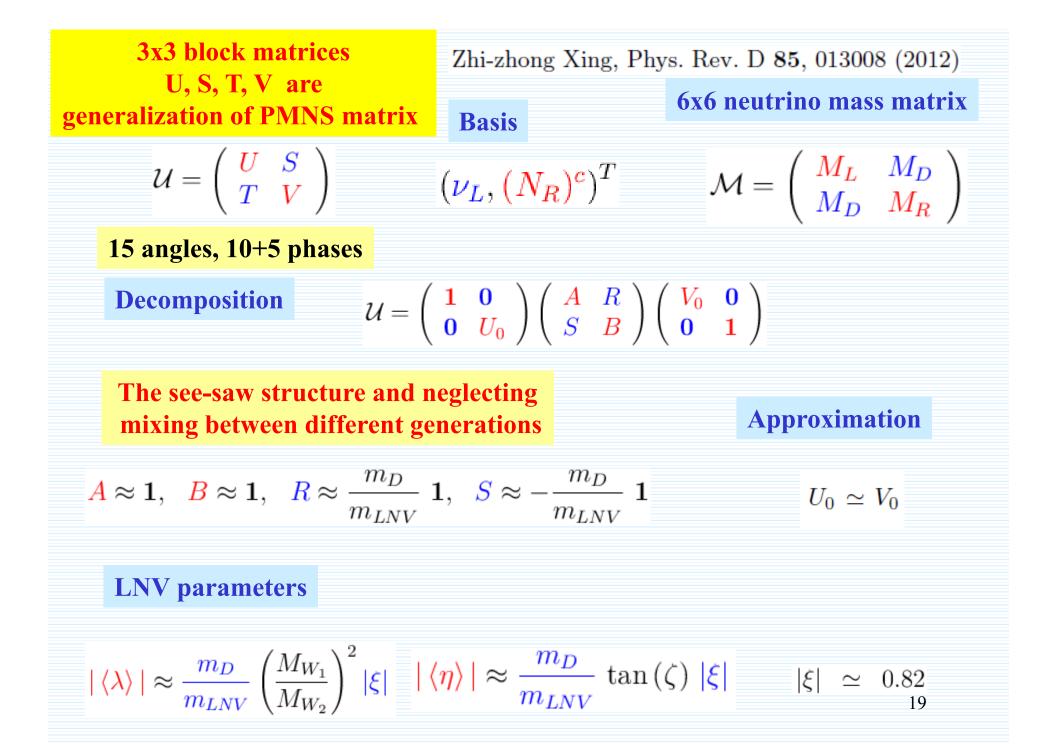
$$\eta = -\tan\zeta, \quad \chi = \eta,$$
  
$$\lambda = (M_{W_1}/M_{W_2})^2$$

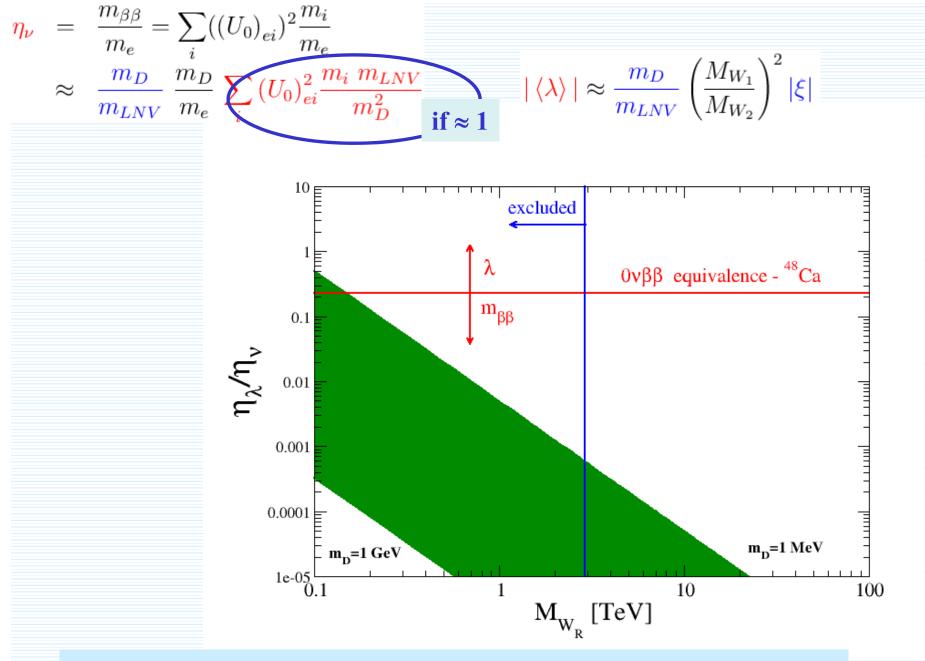
$$<\lambda>$$
 - W<sub>L</sub>-W<sub>R</sub> exch.

$$<\eta>$$
 -  $W_L$  -  $W_R$  mixing

D. Štefánik, R. Dvornický, F.Š., P. Vogel, PRC 92, 055502 (2015)

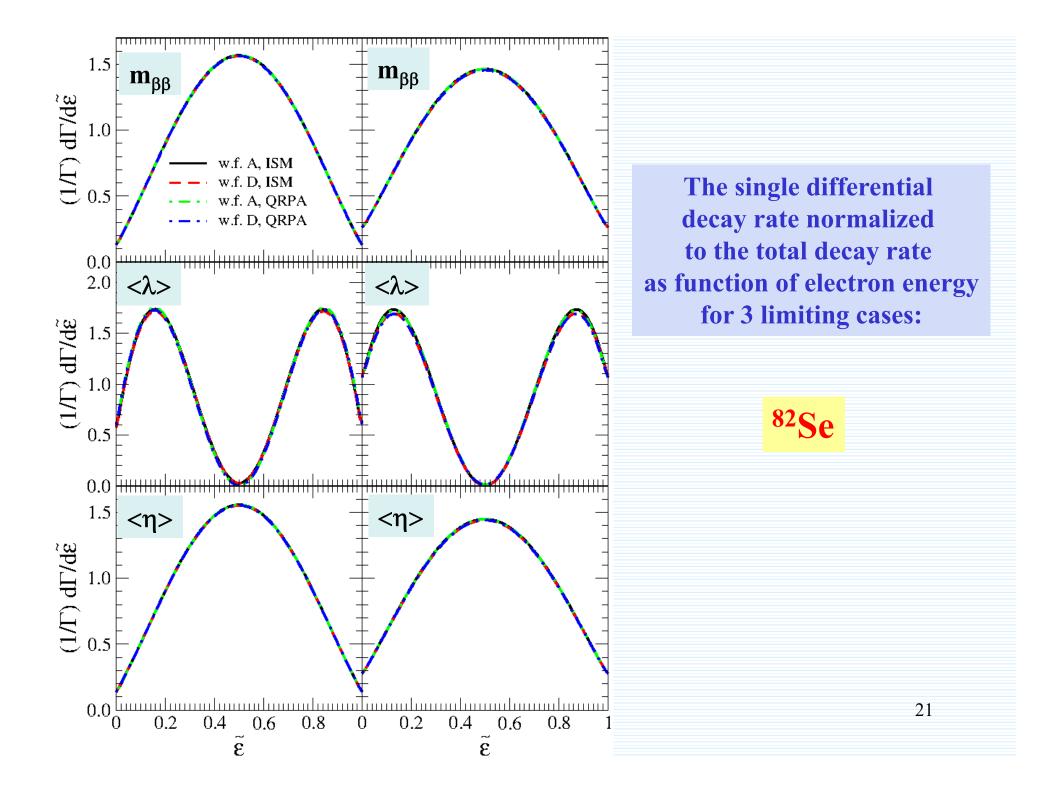


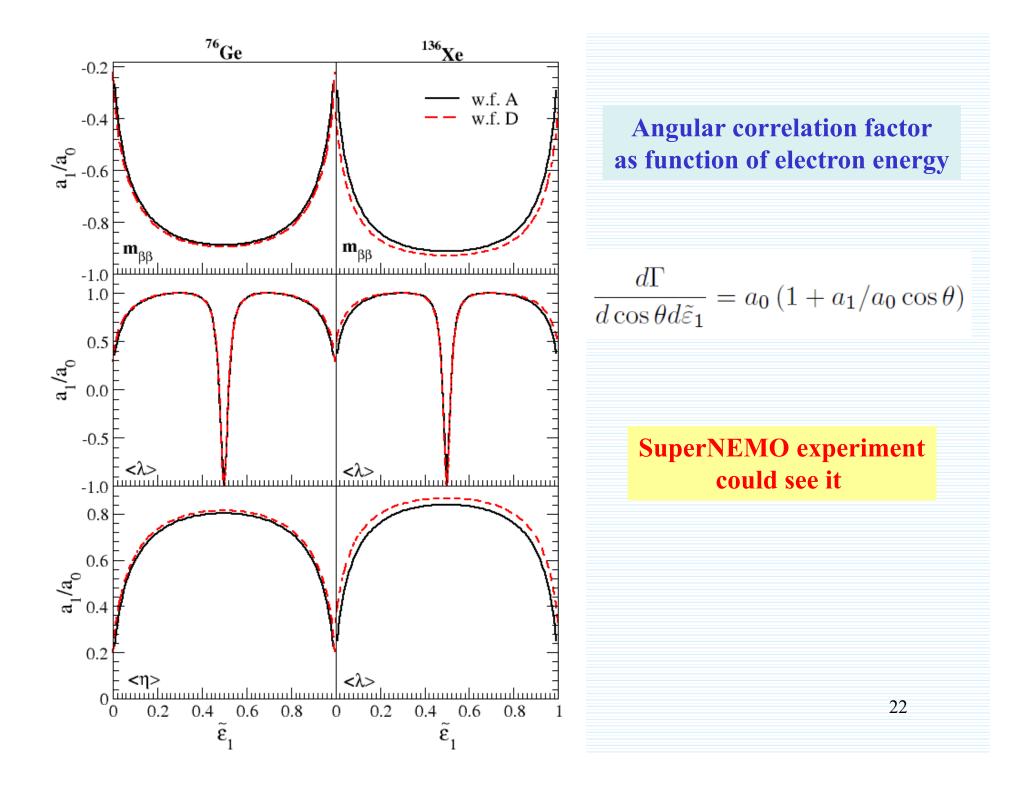


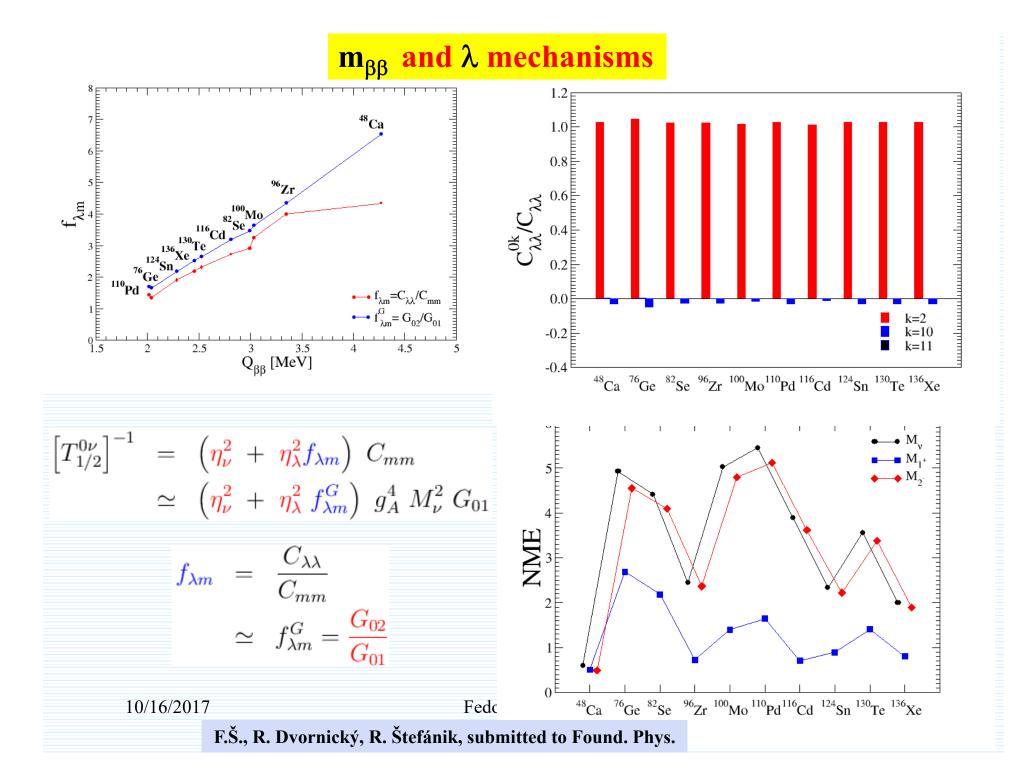


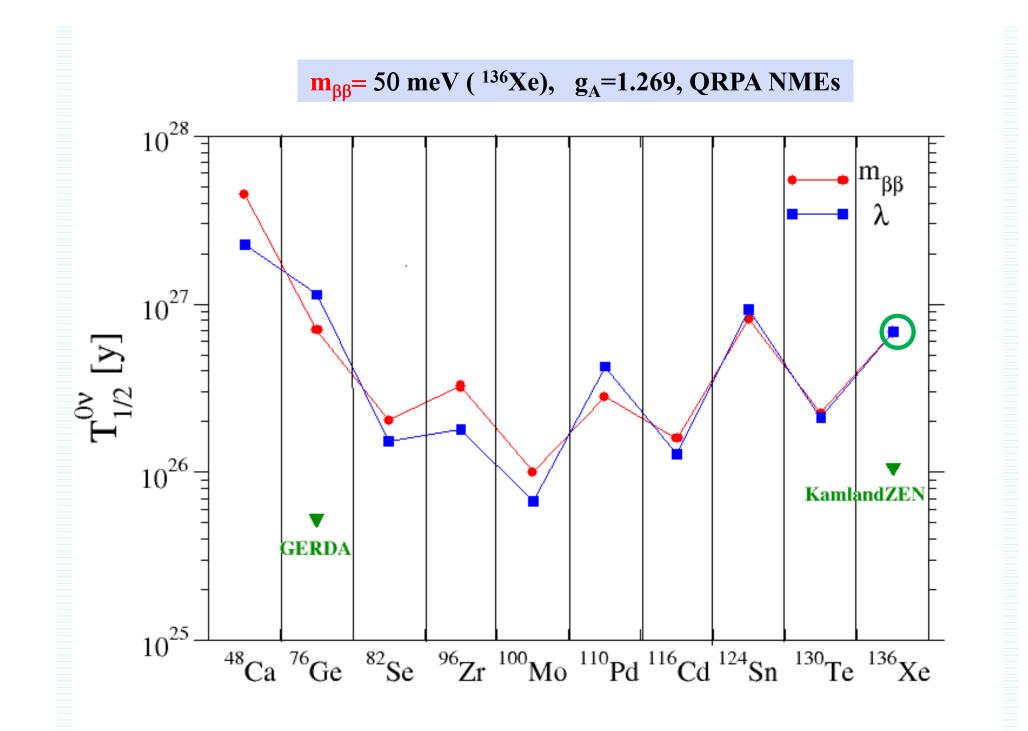
Clear dominance of  $m_{\beta\beta}$  over  $\langle \lambda \rangle$  mechanism by current constraint on mass of heavy vector boson and 1 MeV  $\leq m_D \leq 1$  GeV

20



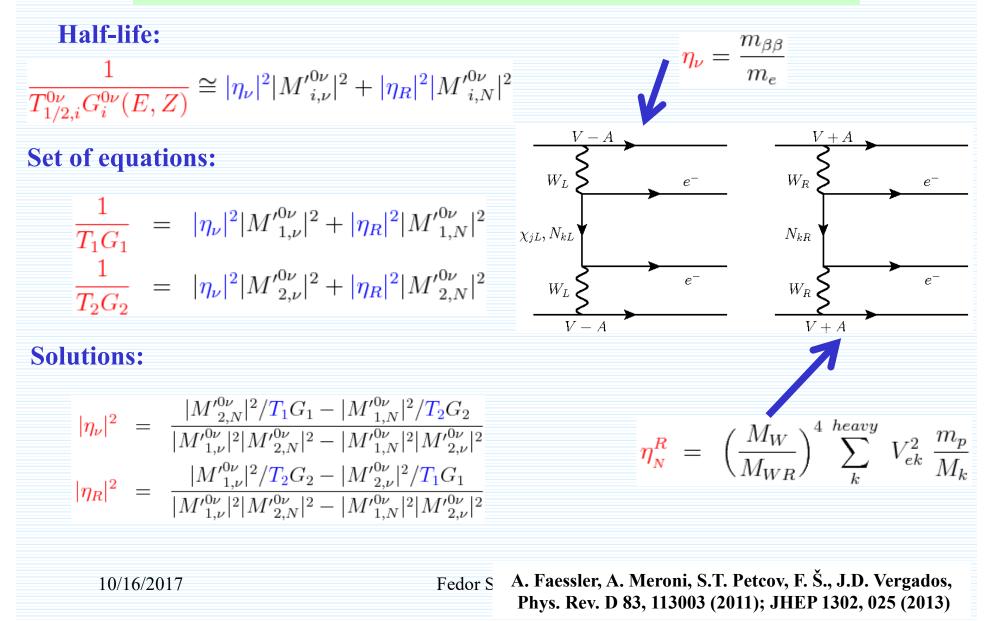


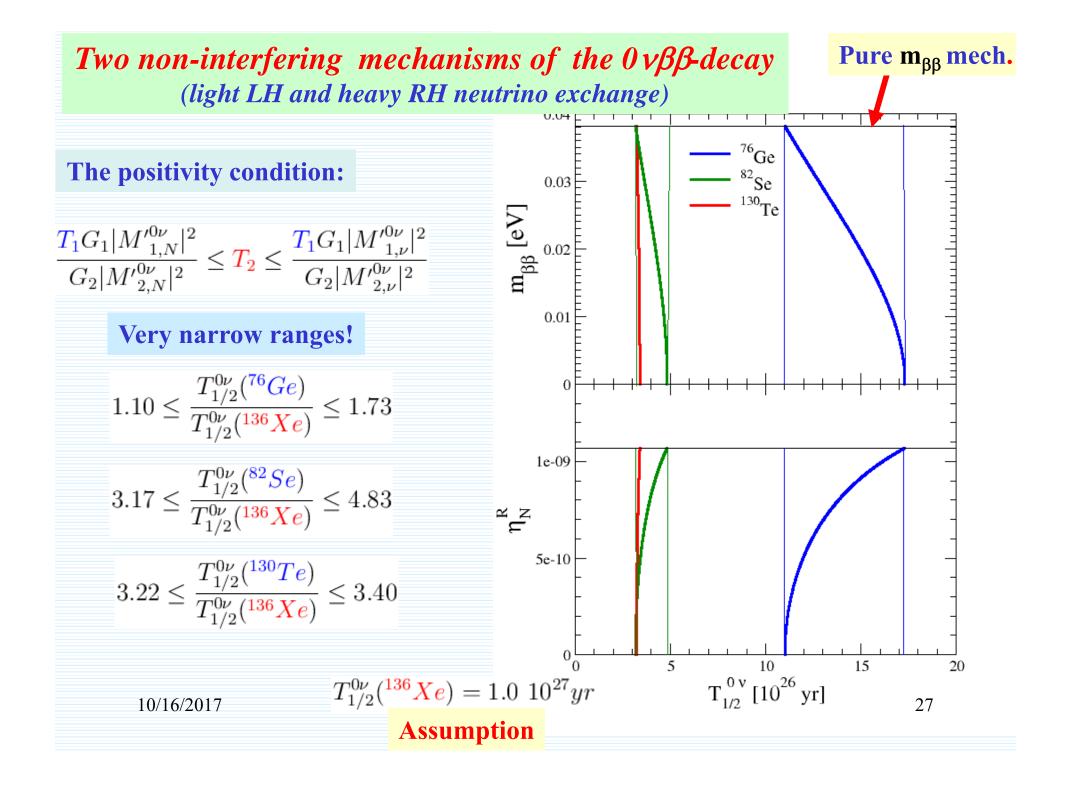


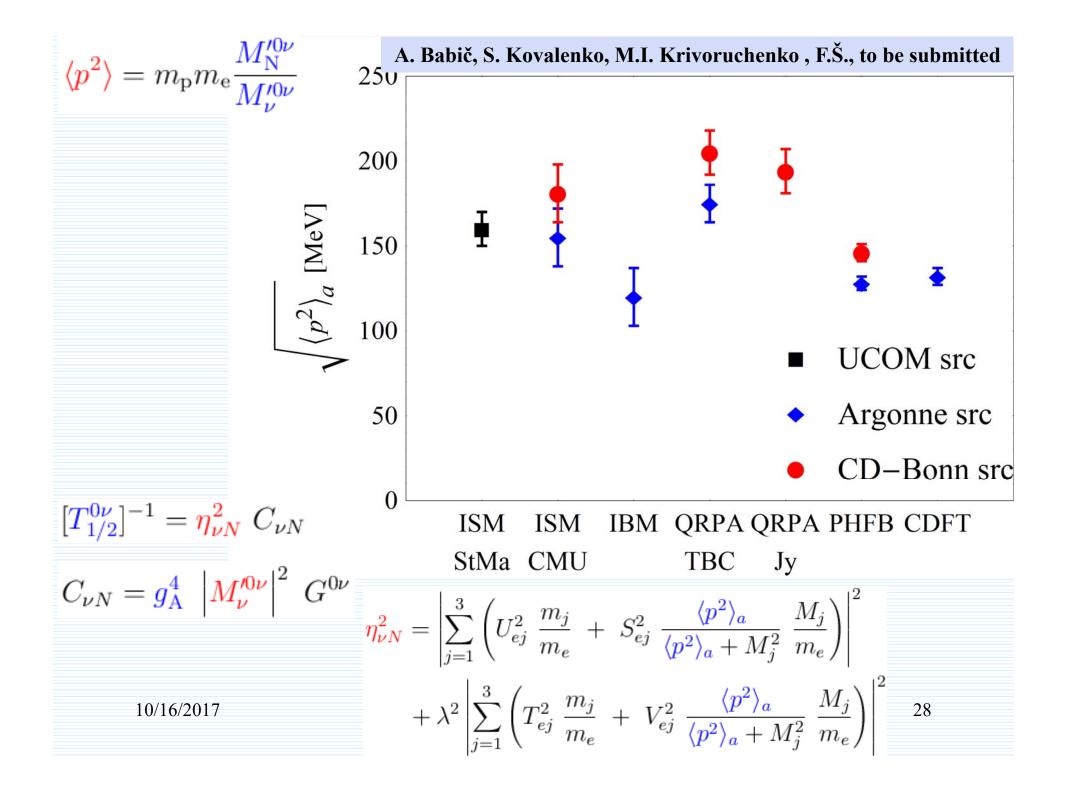


**IV.** The 
$$0 \nu \beta \beta$$
-decay within L-R symmetric theories  
(D-M mass term, see-saw, V-A and V+A int., exchange of heavy neutrinos)  
J.D.Vergados, H. Ejiri, F.Š., Int. J. Mod. Phys. E25, 1630007(2016)  
 $\left(T_{1/2}^{0\nu} G^{0\nu} g_A^2\right)^{-1} = \left|\eta_{\nu} M_{\nu}^{0\nu} + \eta_N^L M_N^{0\nu}\right|^2 + \left|\eta_N^R M_N^{0\nu}\right|^2$   
 $\eta_{\nu} = \frac{m_{\beta\beta}}{m_e} = \sum_i ((U_0)_{ei})^2 \frac{m_i}{m_e} \qquad \eta_N^L = \frac{m_p}{m_{LNV}} \sum_i (U_{ei}^{(12)})^2 \frac{m_{LNV}}{M_i} \qquad \eta_{\nu} >> \eta_N^L$   
 $\approx \frac{m_p}{m_{LNV}} \frac{m_D^2}{m_e m_p} \underbrace{(U_0)_{ei}^2 \frac{m_i m_{LNV}}{m_D^2}}_{-1} \approx \frac{m_p}{m_{LNV}} \left(\frac{m_D}{m_{LNV}}\right)^2 \underbrace{\sum_i \frac{m_{LNV}}{M_i}}_{comparable} -1$   
 $\eta_{\nu}$  and  $\eta^R_N$  might  
be comparable, if e.g.  
 $m_D^{\approx} m_e \sim 5 < 10^{-4}$ 

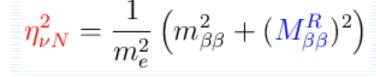
## Two non-interfering mechanisms of the 0vββ-decay (light LH and heavy RH neutrino exchange)

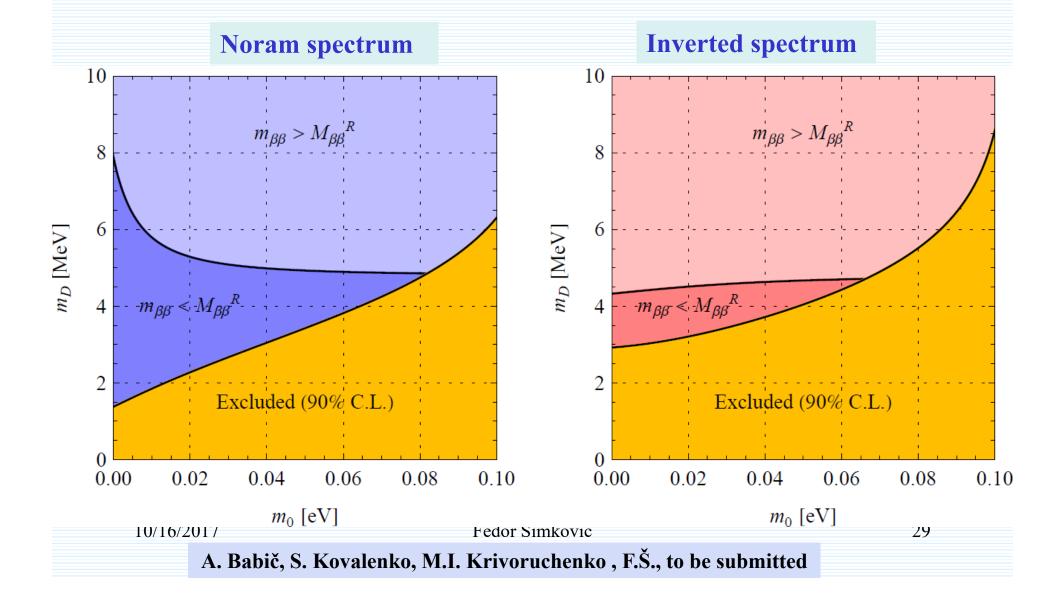






### See-saw scenario





# Calculation of 0vbb decay NMEs

| = | Method   | $g_A$  | src   | $M_{\nu}^{0\nu}$  |  |  |  |   |  |
|---|--|--|---|---|--|--|--|---|--|
|   |  | 0  |   | $^{48}Ca$   | $^{76}\mathrm{Ge}$   | $^{82}Se$  | <sup>96</sup> Zr   | $^{100}\mathrm{Mo}$   | $^{110}\mathrm{Pd}$  |
| - | ISM-StMa   | 1.25   | UCOM  | 0.85  | 2.81   | 2.64   |  |   |  |
|   | ISM-CMU  | 1.27   | Argonne   | 0.80  | 3.37   | 3.19   |  |   |  |
|   |  |  | CD-Bonn   | 0.88  | 3.57   | 3.39   |  |   |  |
|   | IBM  | 1.27   | Argonne   | 1.75  | 4.68   | 3.73   | 2.83   | 4.22  | 4.05   |
|   | QRPA-TBC   | 1.27   | Argonne   | 0.54  | 5.16   | 4.64   | 2.72   | 5.40  | 5.76   |
|   |  |  | CD-Bonn   | 0.59  | 5.57   | 5.02   | 2.96   | 5.85  | 6.26   |
|   | QRPA-Jy  | 1.26   | CD-Bonn   |   | 5.26   | 3.73   | 3.14   | 3.90  | 6.52   |
|   | dQRPA-NC   | 1.25   | without   |   | 5.09   |  |  |   |  |
|   | PHFB   | 1.25   | Argonne   |   |  |  | 2.84   | 5.82  | 7.12   |
|   |  |  | CD-Bonn   |   |  |  | 2.98   | 6.07  | 7.42   |
|   | NREDF  | 1.25   | UCOM  | 2.37  | 4.60   | 4.22   | 5.65   | 5.08  |  |
|   | REDF   | 1.25   | without   | 2.94  | 6.13   | 5.40   | 6.47   | 6.58  |  |
| 1 | Mean value                                       |  |   | 1.34  | 4.55   | 4.02   | 3.78   | 5.57  | 6.12   |
|   | variance   |  |   | 0.81  | 1.20   | 0.91   | 2.49   | 0.58  | 1.78   |
| - | Method   | $g_A$  | src   | $M_{\nu}^{0 u}$   |  |  |  |   |  |
| _ |  |  |   | $^{116}\mathrm{Cd}$   | $^{124}Sn$   | $^{128}\mathrm{Te}$  | <sup>130</sup> Te  | $^{136}$ Xe   | $^{150}\mathrm{Nd}$  |
| - | ISM-StMa   | 1.25   | UCOM  |   | 2.62   |  | 2.65   | 2.19  |  |
|   | ISM-CMU  | 1.27   | Argonne   |   | 2.00   |  | 1.79   | 1.63  |  |
|   |  |  | 0   |   |  |  |  | 1.00  |  |
|   |  |  | CD-Bonn   |   | 2.15   |  | 1.93   | 1.05<br>1.76  |  |
|   | IBM  | 1.27   |   | 3.10  | $2.15 \\ 3.19$   | 4.10   | $1.93 \\ 3.70$   |   | 2.67   |
|   | IBM<br>QRPA-TBC                                  |  | CD-Bonn   | 3.10 $4.04$   |  | $\begin{array}{c} 4.10\\ 4.56\end{array}$                                |  | 1.76  | 2.67   |
|   |  | 1.27   | CD-Bonn<br>Argonne  |   | 3.19   |  | 3.70   | $1.76 \\ 3.05$  | 2.67<br>3.37   |
|   |  | 1.27   | CD-Bonn<br>Argonne<br>Argonne   | 4.04  | $3.19 \\ 2.56$   | 4.56   | $3.70 \\ 3.89$   | $1.76 \\ 3.05 \\ 2.18$  |  |
|   | QRPA-TBC   | $1.27 \\ 1.27$                               | CD-Bonn<br>Argonne<br>Argonne<br>CD-Bonn  | $\begin{array}{c} 4.04 \\ 4.34 \end{array}$                   | $3.19 \\ 2.56 \\ 2.91$   | $4.56 \\ 5.08$   | $3.70 \\ 3.89 \\ 4.37$                                       | $   \begin{array}{r}     1.76 \\     3.05 \\     2.18 \\     2.46   \end{array} $             |  |
|   | QRPA-TBC<br>QRPA-Jy                              | $1.27 \\ 1.27 \\ 1.26$                       | CD-Bonn<br>Argonne<br>Argonne<br>CD-Bonn<br>CD-Bonn                               | $\begin{array}{c} 4.04 \\ 4.34 \end{array}$                   | $3.19 \\ 2.56 \\ 2.91$   | $4.56 \\ 5.08$   | 3.70<br>3.89<br>4.37<br>4.00                                 | $   \begin{array}{r}     1.76 \\     3.05 \\     2.18 \\     2.46 \\     2.91   \end{array} $ | 3.37   |
|   | QRPA-TBC<br>QRPA-Jy<br>dQRPA-NC                  | 1.27<br>1.27<br>1.26<br>1.25                 | CD-Bonn<br>Argonne<br>CD-Bonn<br>CD-Bonn<br>without                               | $\begin{array}{c} 4.04 \\ 4.34 \end{array}$                   | $3.19 \\ 2.56 \\ 2.91$   | 4.56<br>5.08<br>4.92   | 3.70<br>3.89<br>4.37<br>4.00<br>1.37                         | $   \begin{array}{r}     1.76 \\     3.05 \\     2.18 \\     2.46 \\     2.91   \end{array} $ | 3.37<br>2.71   |
|   | QRPA-TBC<br>QRPA-Jy<br>dQRPA-NC                  | 1.27<br>1.27<br>1.26<br>1.25                 | CD-Bonn<br>Argonne<br>Argonne<br>CD-Bonn<br>CD-Bonn<br>without<br>Argonne         | $\begin{array}{c} 4.04 \\ 4.34 \end{array}$                   | $3.19 \\ 2.56 \\ 2.91$   | 4.56<br>5.08<br>4.92<br>3.90   | 3.70<br>3.89<br>4.37<br>4.00<br>1.37<br>3.81                 | $   \begin{array}{r}     1.76 \\     3.05 \\     2.18 \\     2.46 \\     2.91   \end{array} $ | <ul><li>3.37</li><li>2.71</li><li>2.58</li></ul>                                 |
|   | QRPA-TBC<br>QRPA-Jy<br>dQRPA-NC<br>PHFB          | 1.27<br>1.27<br>1.26<br>1.25<br>1.27         | CD-Bonn<br>Argonne<br>CD-Bonn<br>CD-Bonn<br>without<br>Argonne<br>CD-Bonn         | 4.04<br>4.34<br>4.26  | 3.19<br>2.56<br>2.91<br>5.30   | $ \begin{array}{r} 4.56 \\ 5.08 \\ 4.92 \\ 3.90 \\ 4.08 \\ \end{array} $ | 3.70<br>3.89<br>4.37<br>4.00<br>1.37<br>3.81<br>3.98         | $     1.76 \\     3.05 \\     2.18 \\     2.46 \\     2.91 \\     1.55 $                      | <ul><li>3.37</li><li>2.71</li><li>2.58</li><li>2.68</li></ul>                    |
|   | QRPA-TBC<br>QRPA-Jy<br>dQRPA-NC<br>PHFB<br>NREDF | 1.27<br>1.27<br>1.26<br>1.25<br>1.27<br>1.25 | CD-Bonn<br>Argonne<br>CD-Bonn<br>CD-Bonn<br>without<br>Argonne<br>CD-Bonn<br>UCOM | <ul><li>4.04</li><li>4.34</li><li>4.26</li><li>4.72</li></ul> | <ul><li>3.19</li><li>2.56</li><li>2.91</li><li>5.30</li><li>4.81</li></ul> | $ \begin{array}{r} 4.56 \\ 5.08 \\ 4.92 \\ 3.90 \\ 4.08 \\ \end{array} $ | 3.70<br>3.89<br>4.37<br>4.00<br>1.37<br>3.81<br>3.98<br>5.13 | $1.76 \\ 3.05 \\ 2.18 \\ 2.46 \\ 2.91 \\ 1.55 \\ 4.20$  | <ul> <li>3.37</li> <li>2.71</li> <li>2.58</li> <li>2.68</li> <li>1.71</li> </ul> |

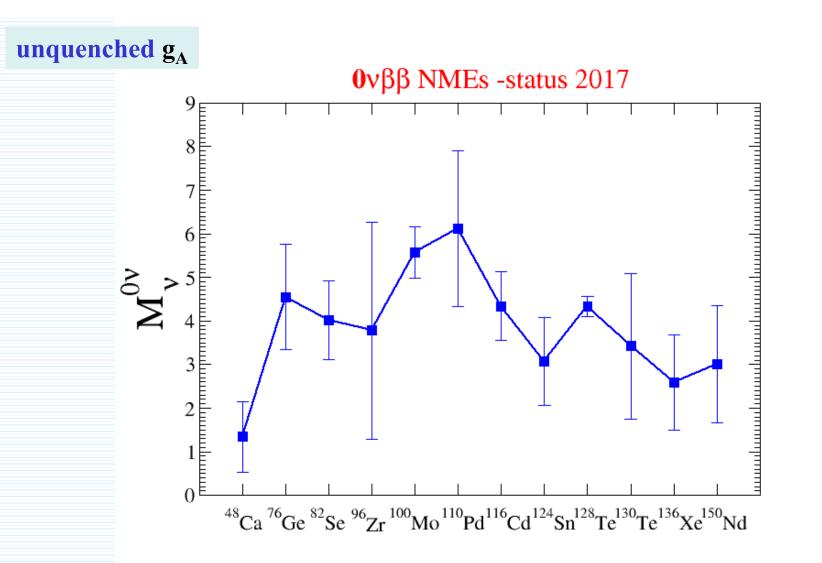
NMEs for unquenched value of g<sub>A</sub>

Mean field approaches (PHFB, NREDF, REDF) ⇒ Large NMEs

Interacting Shell Model (ISM-StMa, ISM-CMU) ⇒ small NMEs

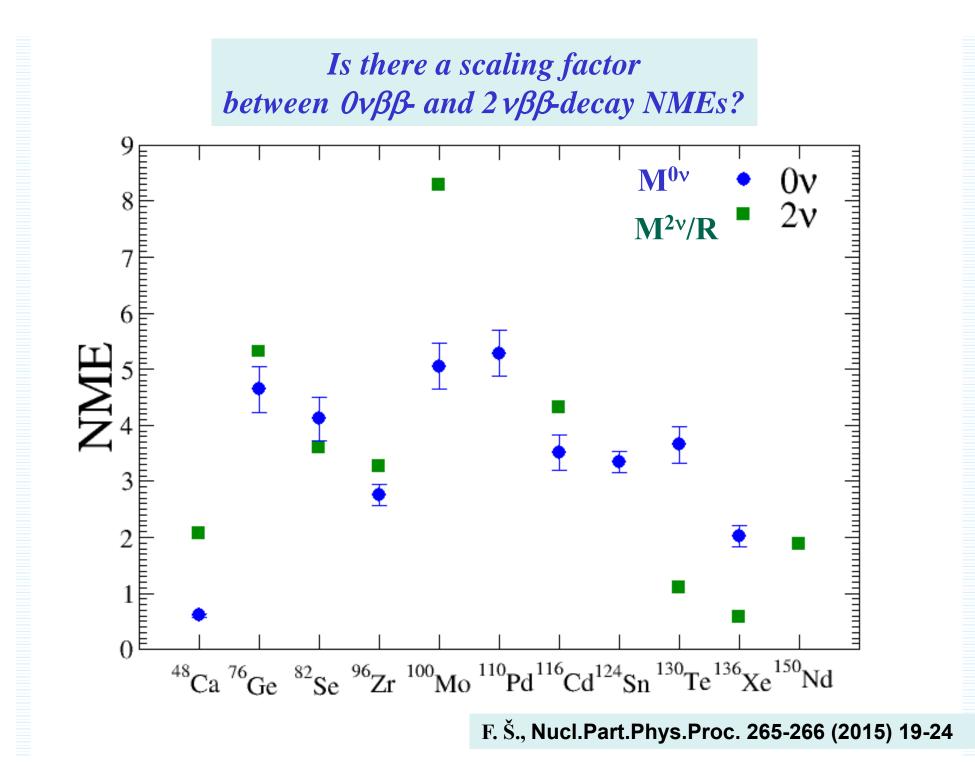
Quasiparticle Random Phase Approximation (QRPA-TBC, QRPA-Jy, dQRPQ-NC) ⇒ Intermediate NMEs

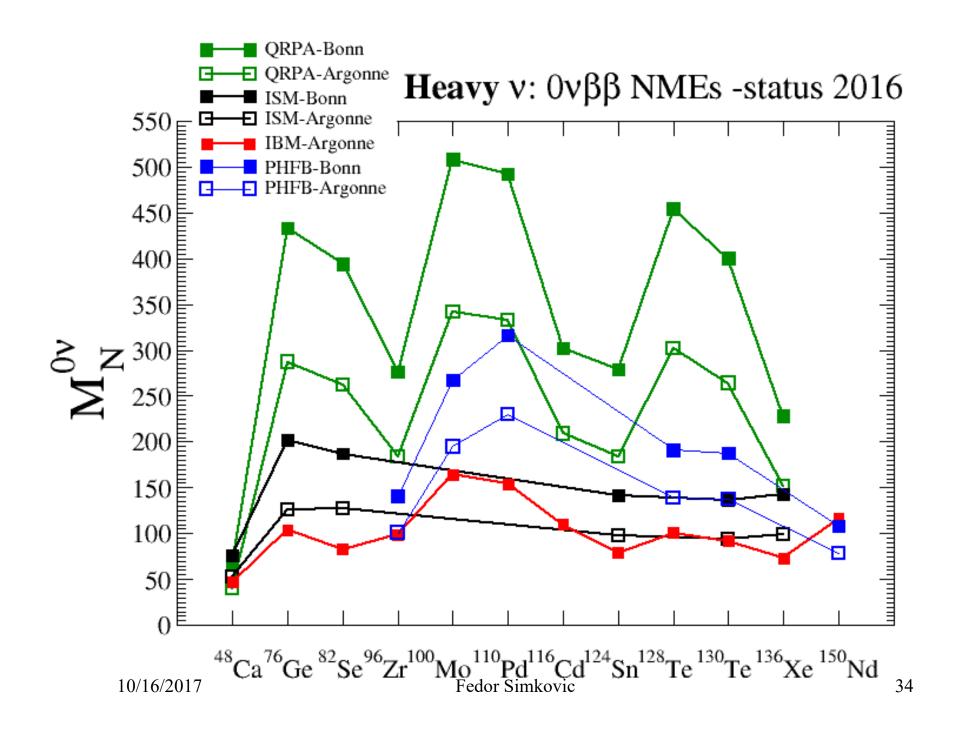
Interacting Boson Model (IBM) ⇒ Close to QRPA results



### J.D.Vergados, H. Ejiri, , F.Š., Int. J. Mod. Phys. E25, 1630007(2016)

|                               | mean field meth. | ISM | IBM        | QRPA       |
|-------------------------------|------------------|-----|------------|------------|
| Large model space             | yes              | no  | yes        | yes        |
| <b>Constr. Interm. States</b> | no               | yes | no         | yes        |
| Nucl. Correlations            | limited          | all | restricted | restricted |





# Quenching of $g_A$

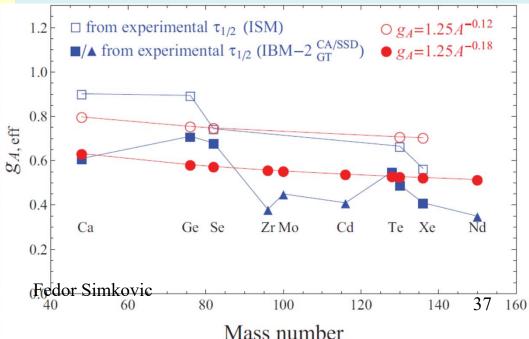
#### $g_{A}^{4} = (1.269)^{4} = 2.6$ Quenching of $g_{A}$ (from exp.: $T_{1/2}^{0\nu}$ up 2.5 x larger) Strength of GT trans. (approx. given by Ikeda sum rule =3(N-Z)) $(g^{eff}{}_{A})^{4} = 1.0$ has to be quenched to reproduce experiment 25 $_{\Box}$ $^{76}_{32}\text{Ge}_{44} \Rightarrow$ standard QRPA $S_{\beta}^{-} - S_{\beta}^{+} = 3(N-Z) = 36$ exp. via (p,n) reaction 20 exp. via (<sup>3</sup>He,t) reaction $\langle 1_m^+ | \beta_{GT}^- | RPA \rangle |^2$ (4) transition virtual 5 76<sub>Ge</sub> <sup>76</sup>As 76<sub>Se</sub> 0 **Pauli blocking** 8 10 12 18 6 14 16 20E [MeV] **Cross-section for charge exchange reaction:** $\left[\frac{d\sigma}{d\Omega}\right] = \left[\frac{\mu}{\pi\hbar}\right]^2 \frac{k_f}{k} \operatorname{Nd} \left|V_{\sigma\tau}\right|^2 \left|\langle f | \sigma\tau| i\rangle\right|^2$ q = 0!!p n n largest at 100 - 200 MeV/A

# **Quenching of g\_A** (from theory: $T_{1/2}^{0\nu}$ up 50 x larger)

 $(g^{eff}_{A})^{4} \simeq 0.66 (^{48}Ca), 0.66 (^{76}Ge), 0.30 (^{76}Se), 0.20 (^{130}Te) and 0.11 (^{136}Xe)$ The Interacting Shell Model (ISM), which describes qualitatively well energy spectra, does reproduce experimental values of  $M^{2\nu}$  only by consideration of significant quenching of the Gamow-Teller operator, typically by 0.45 to 70%.

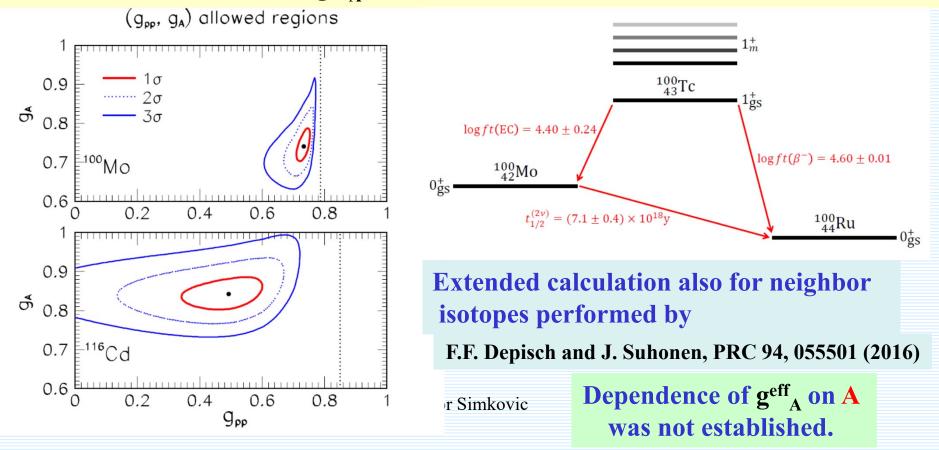
(g<sup>eff</sup><sub>A</sub>)<sup>4</sup> ≃ (1.269 A<sup>-0.18</sup>)4 = 0.063 (The Interacting Boson Model). This is an incredible result. The quenching of the axial-vector coupling within the IBM-2 is more like 60%.
 J. Barea, J. Kotila, F. Iachello, PRC 87, 014315 (2013).

It has been determined by theoretical prediction for the 2vββ-decay half-lives, which were based on within closure approximation calculated corresponding NMEs, with the measured half-lives.



Faessler, Fogli, Lisi, Rodin, Rotunno, F. Š, J. Phys. G 35, 075104 (2008).

 $(g^{eff}{}_{A})^{4} = 0.30$  and 0.50 for <sup>100</sup>Mo and <sup>116</sup>Cd, respectively (The QRPA prediction).  $g^{eff}{}_{A}$  was treated as a completely free parameter alongside  $g_{pp}$  (used to renormalize particl-particle interaction) by performing calculations within the QRPA and RQRPA. It was found that a least-squares fit of  $g^{eff}{}_{A}$  and  $g_{pp}$ , where possible, to the  $\beta$ -decay rate and  $\beta$ +/EC rate of the J = 1<sup>+</sup> ground state in the intermediate nuclei involved in double-beta decay in addition to the  $2\nu\beta\beta$  rates of the initial nuclei, leads to an effective  $g^{eff}{}_{A}$  of about 0.7 or 0.8.



# A novel method to determine effective $g_A$

F. Š., R. Dvornický, D. Štefánik, A. Faessler, to be submitted

10/16/2017

Fedor Simkovic

### **Improved description of the** 0νββ**–decay rate**

$$M_{GT}^{K,L} = m_e \sum_n M_n \frac{E_n - (E_i + E_f)/2}{[E_n - (E_i + E_f)/2]^2 - \varepsilon_{K,L}^2}$$

Let perform Taylor expansion

$$\frac{\varepsilon_{K,L}}{E_n - (E_i + E_f)/2} \quad \epsilon_{K,L} \in \left(-\frac{Q}{2}, \frac{Q}{2}\right)$$

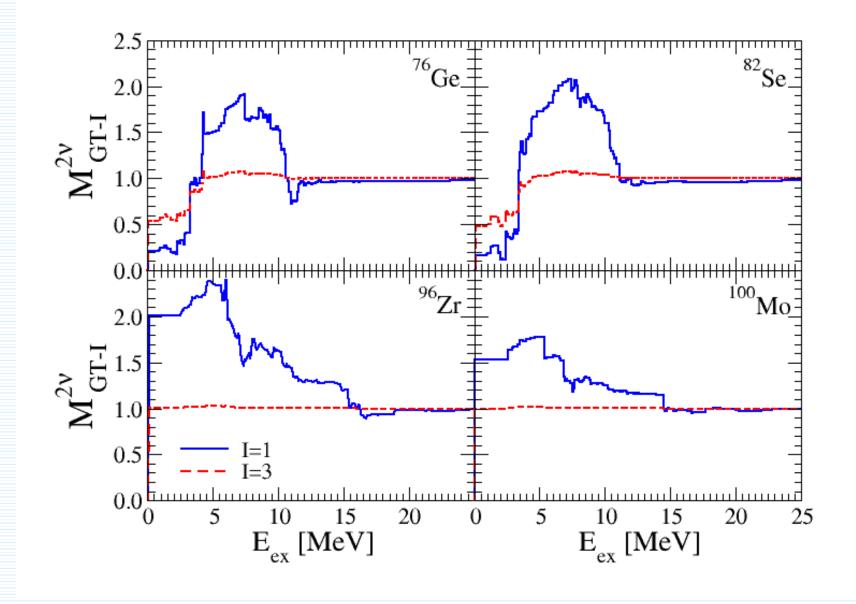
We get

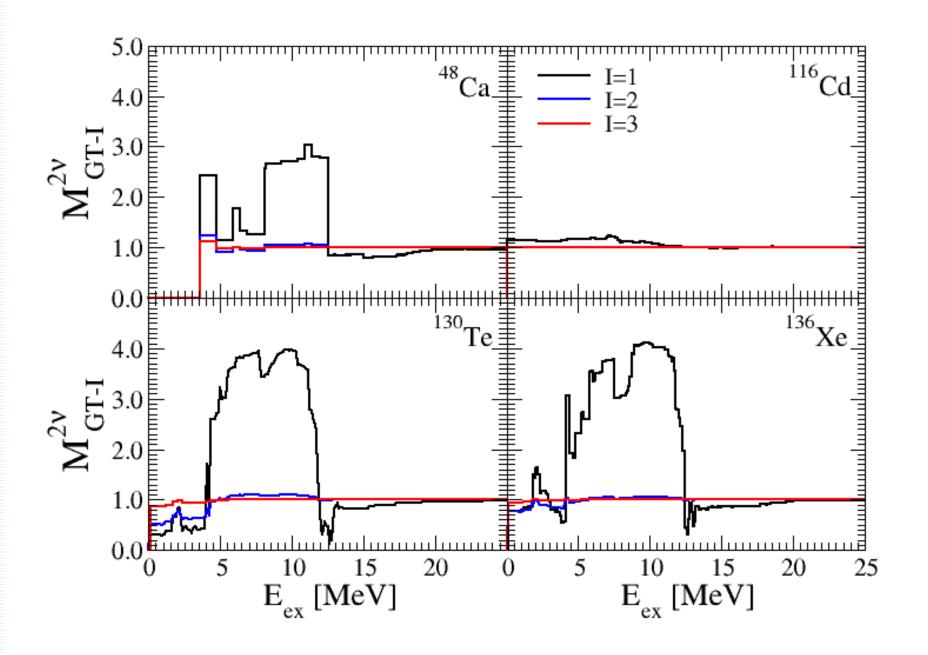
$$\left[T_{1/2}^{2\nu\beta\beta}\right]^{-1} \simeq \left(g_A^{\text{eff}}\right)^4 \left|M_{GT-3}^{2\nu}\right|^2 \frac{1}{\left|\xi_{13}^{2\nu}\right|^2} \left(G_0^{2\nu} + \xi_{13}^{2\nu}G_2^{2\nu}\right)$$

$$M_{GT-1}^{2\nu} = \sum_{n} M_{n} \frac{1}{(E_{n} - (E_{i} + E_{f})/2)}$$
$$M_{GT-3}^{2\nu} = \sum_{n} M_{n} \frac{4 m_{e}^{3}}{(E_{n} - (E_{i} + E_{f})/2)^{3}} \qquad \xi_{13}^{2\nu} = \frac{M_{GT-3}^{2\nu}}{M_{GT-1}^{2\nu}}$$

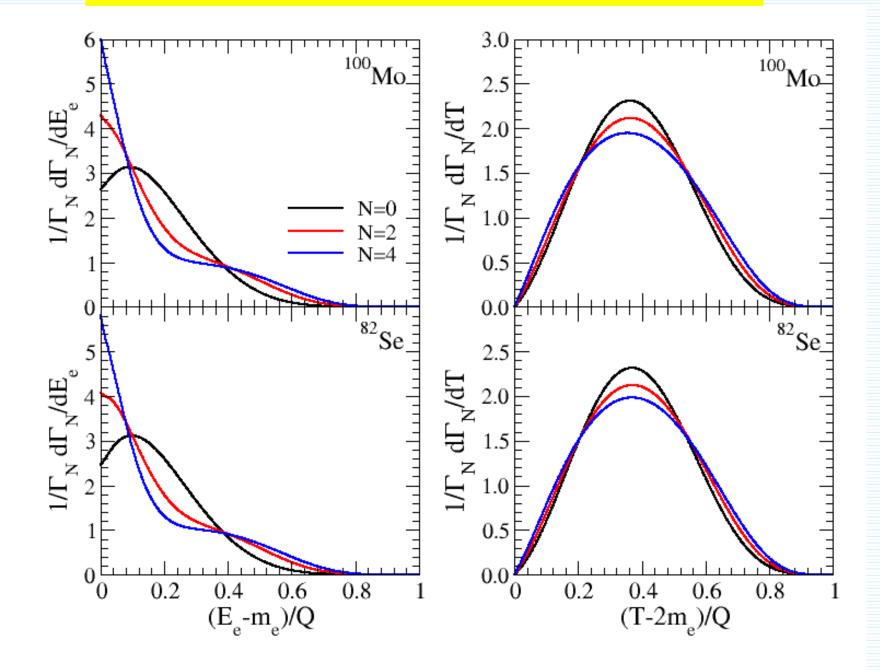
The g<sub>A</sub><sup>eff</sup> can be deterimed with measured half-life and ratio of NMEs and calculated NME dominated by transitions through low lying states of the intermediate nucleus (ISM?)

### The running sum of the $2\nu\beta\beta$ -decay NMEs

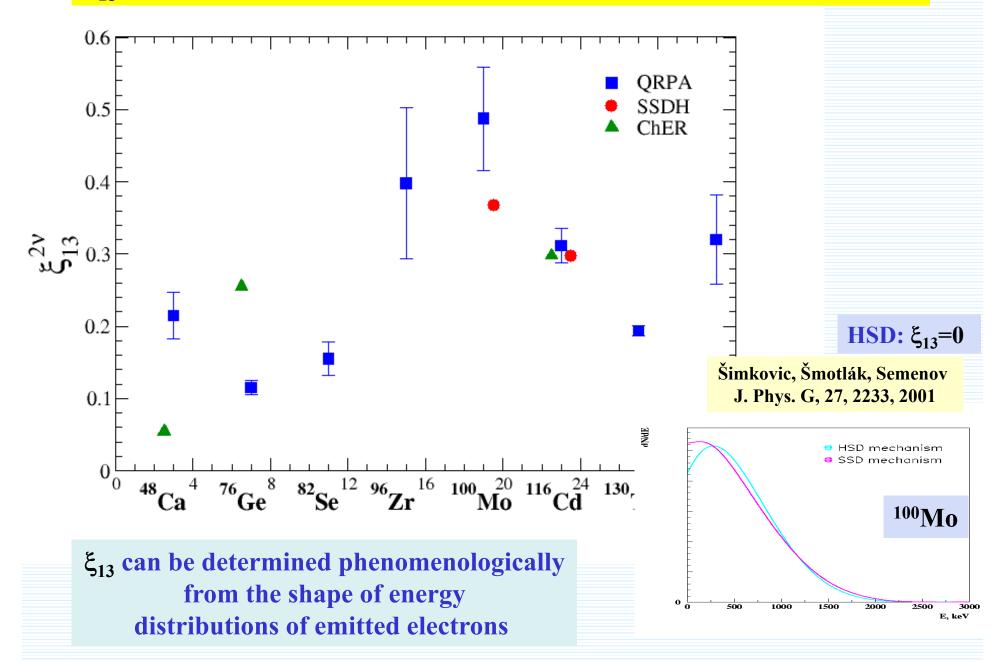


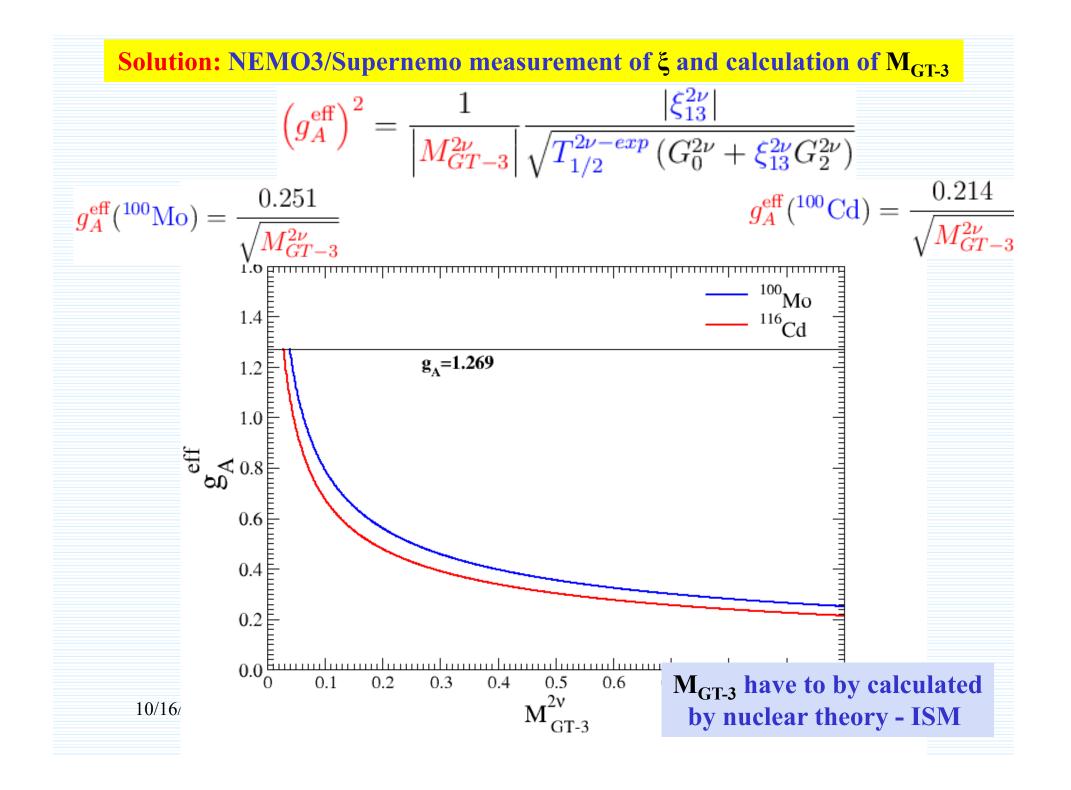


#### Normalized to unity different partial energy distributions



### $\xi_{13}$ tell us about importance of higher lying states of int. nucl.





# Nuclear structure studies within schematic models

10/16/2017

Fedor Simkovic

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Understanding of the  $2\nu\beta\beta$ -decay NMEs is of crucial importance for correct evaluation of the  $2\nu\beta\beta$ -decay NMEs

 $(A,Z) \rightarrow (A,Z+2) + 2e^- + 2\overline{\nu}_e$ 

Both 2νββ and 0νββ operators connect the same states. Both change two neutrons into two protons.

Explaining 2vββ-decay is necessary but not sufficient

There is no reliable calculation of the 2vbb-decay NMEs

Calculation via intermediate nuclear states: **QRPA** (sensitivity to pp-int.) **ISM** (quenching, truncation of model space, spin-orbit partners)

Calculation via closure NME: IBM, PHFB

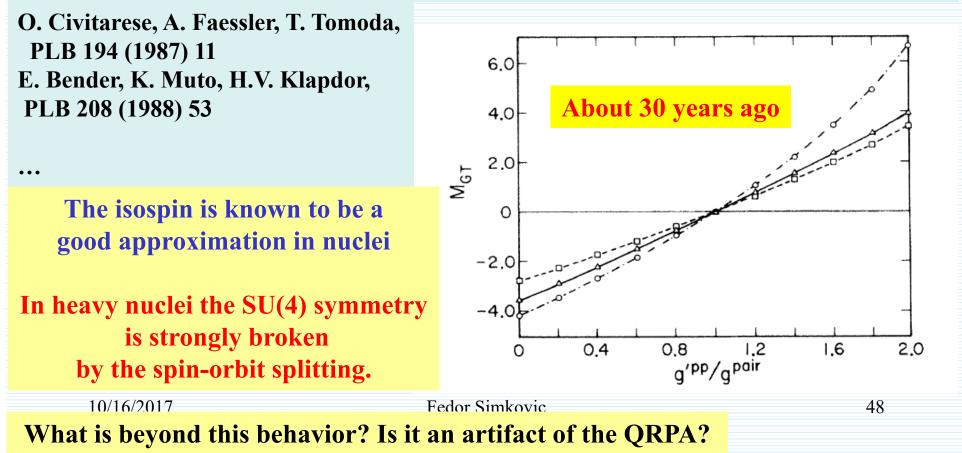
#### No calculation: EDF

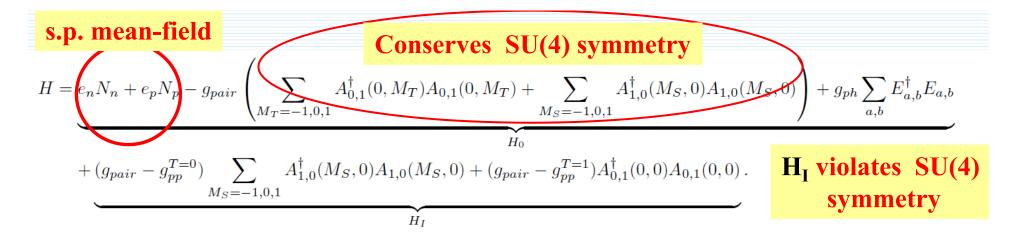
10/16/2017

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*The DBD Nuclear Matrix Elements and the SU(4) symmetry* D. Štefánik, F.Š., A. Faessler, PRC 91, 064311 (2015)

Suppression of the Two Neutrino Double Beta Decay by Nuclear Structure Effects P. Vogel, M.R. Zirnbauer, PRL (1986) 3148



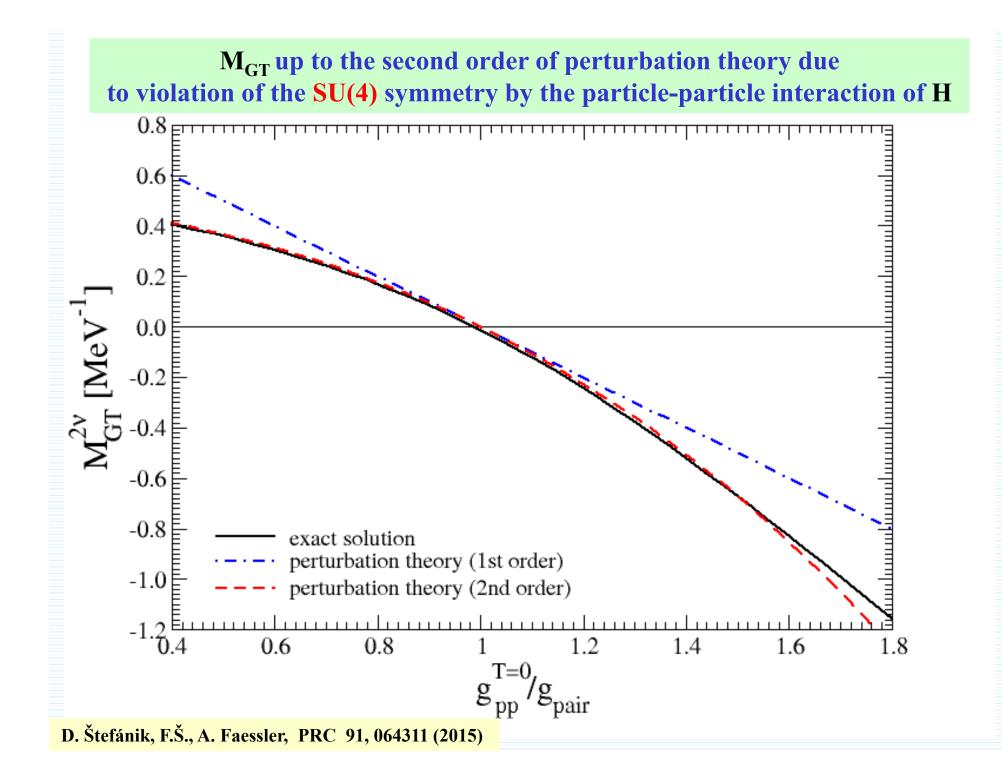


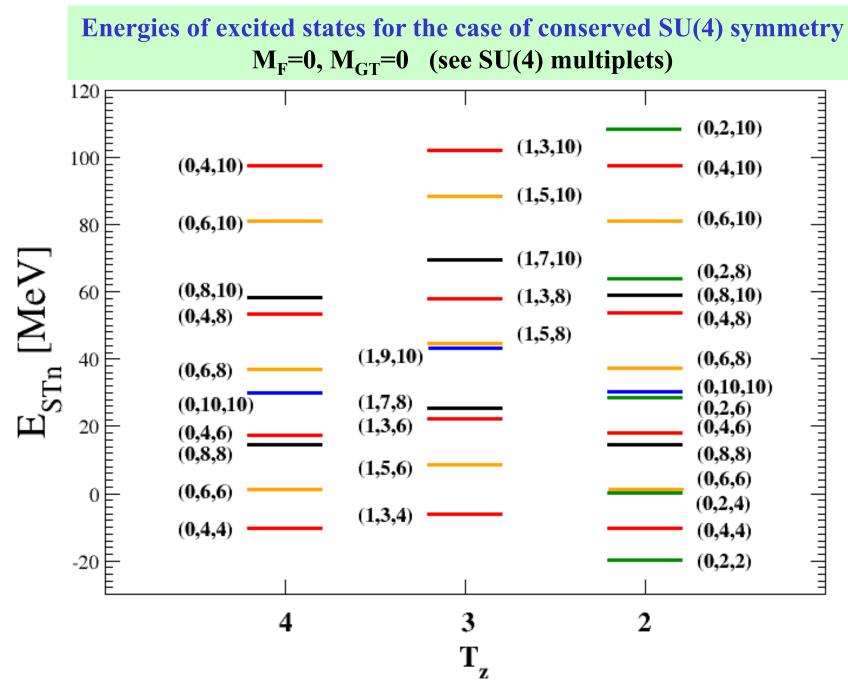
 $\begin{array}{l} g_{pair} \text{-} strength \ of \ isovector \ like \ nucleon \ pairing \ (L=0, \ S=0, \ T=1, \ M_T=\pm 1) \\ g_{pp}^{\ T=1} \text{-} \ strength \ of \ isovector \ spin-0 \ pairing \ (L=0, \ S=0, \ T=1, \ M_T=0 \\ g_{pp}^{\ T=0} \text{-} \ strength \ of \ isoscalar \ spin-1 \ pairing \ (L=0, \ S=1, \ T=0) \\ g_{ph} \text{-} \ strength \ of \ particle-hole \ force \end{array}$ 

M<sub>F</sub> and M<sub>GT</sub> do not depend on the mean-field part of H and are governed by a weak violation of the SU(4) symmetry by the particle-particle interaction of H

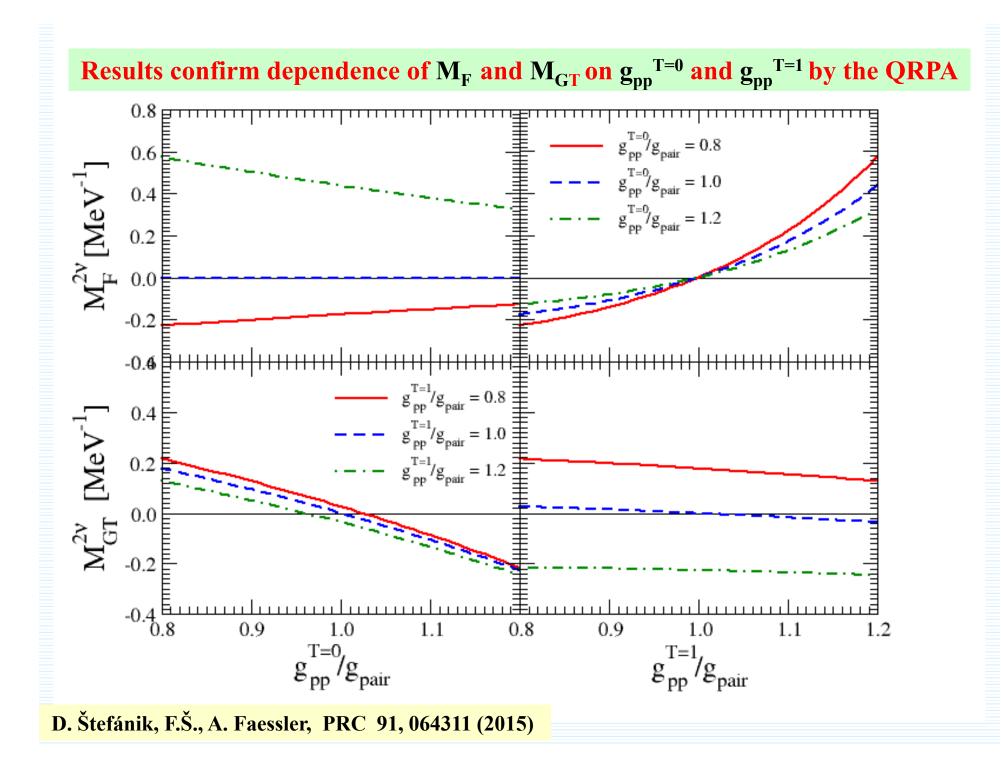
$$\begin{split} M_F^{2\nu} &= -\frac{48\sqrt{\frac{33}{5}}\left(g_{pair} - g_{pp}^{T=1}\right)}{(5g_{pair} + 3g_{ph})(10g_{pair} + 6g_{ph})} \\ M_{GT}^{2\nu} &= \frac{144\sqrt{\frac{33}{5}}}{5g_{pair} + 9g_{ph}} \left\{ \frac{(g_{pair} - g_{pp}^{T=0})}{(10g_{pair} + 20g_{ph})} \right. \\ &+ \frac{2g_{ph}(g_{pair} - g_{pp}^{T=1})}{(10g_{pair} + 20g_{ph})(10g_{pair} + 6g_{ph})} \right\} \end{split}$$

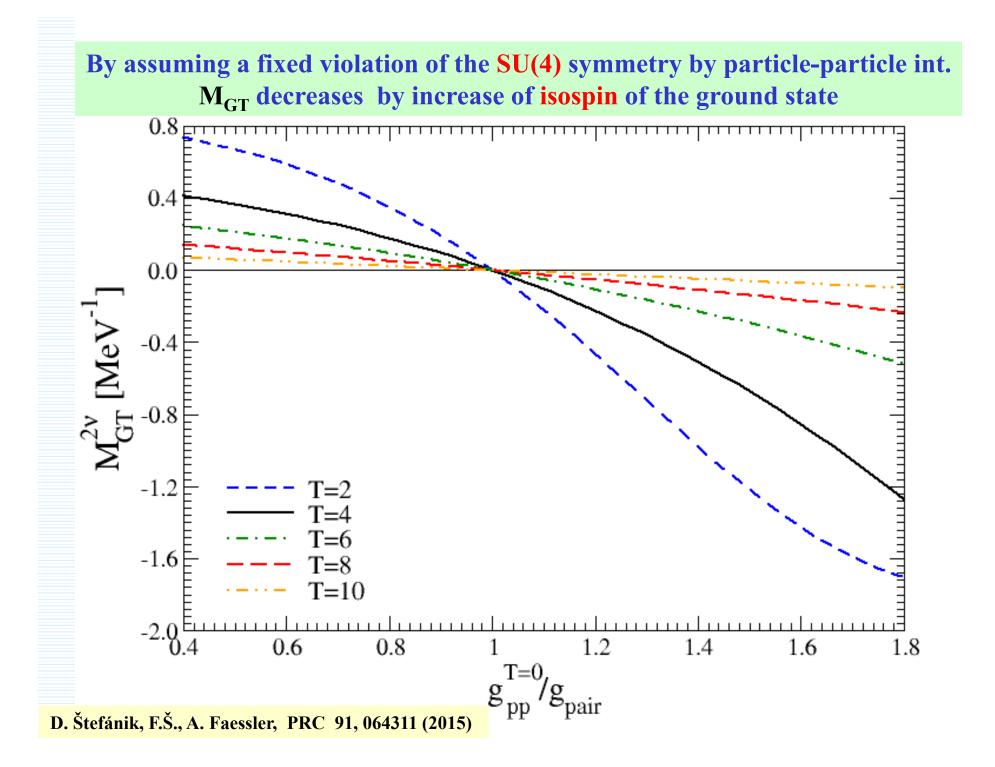
10/16/2017











### **Reproduction of exact solutions of Lipkin model by nonlinear higher random-phase approximation**

J. Terasaki, A. Smetana, F. Š., M.I. Krivoruchenko, arXiv:1701.08368 [nucl-th]

Useful for test of theory<br/>often used.<br/>H.J. Lipkin et al., N.P.<br/>62, 188 (1965)Lipkin model<br/>Level index<br/>1

$$H = \varepsilon J_z + \frac{V}{2} \left( J_+^2 + J_-^2 \right)$$

The nonlinear phonon operator

$$Q_{k}^{o\dagger} = \sum_{l=1}^{n} (X_{2l-1}^{k} \mathcal{J}_{+}^{2l-1} + Y_{2l-1}^{k} \mathcal{J}_{-}^{2l-1})$$
  
(odd-order subspace)  
$$Q_{k}^{e\dagger} = c_{k} + \sum_{l=1}^{n} (X_{2l}^{k} \mathcal{J}_{+}^{2l} + Y_{2l}^{k} \mathcal{J}_{-}^{2l}),$$
  
(even-order subspace)

vel index  
1 Energy  

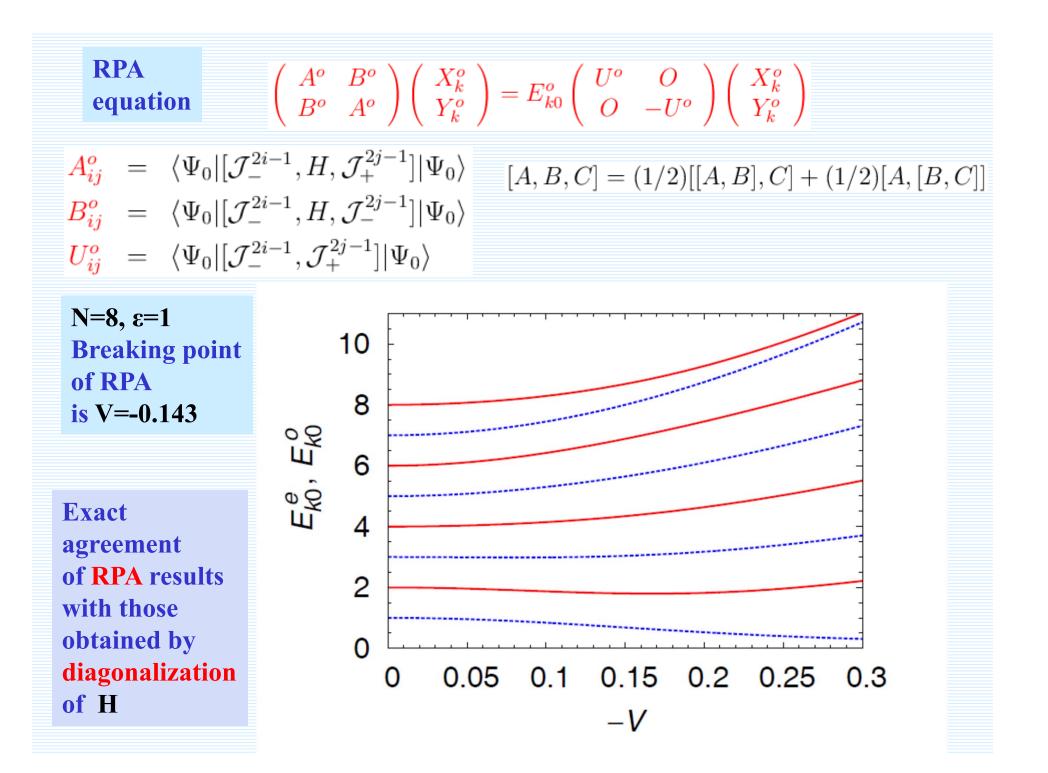
$$\epsilon/2$$
  
0 •••••••  
 $m = 1, \dots N$   $-\epsilon/2$   
Algebra
$$\begin{bmatrix} J_z, J_+ \end{bmatrix} = J_+$$
  
 $\begin{bmatrix} J_z, J_- \end{bmatrix} = -J_-$   
 $\begin{bmatrix} J_+, J_- \end{bmatrix} = 2J_z$   
RPA ground state

 $Q_k |\Psi_0\rangle = 0 \qquad {}_{54}$ 

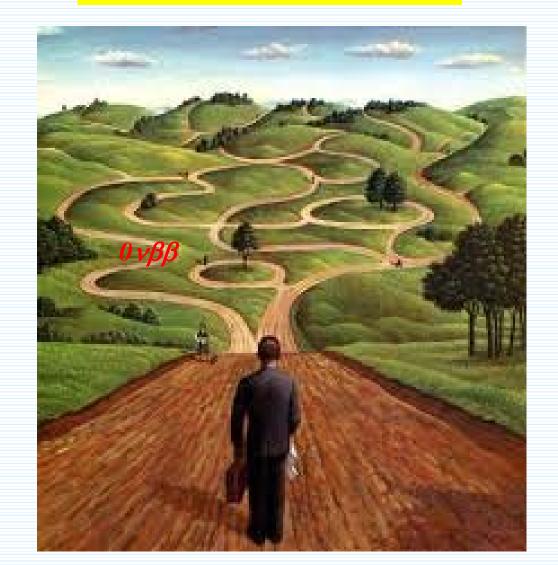
## Eigen states, wave functions, total energies, excitation energies and phonon-creation operators obtained for N=2 by the nonlinear higher RPA.

| Eigenstate         | Wave function  |  | Total energy  |
|--------------------|--|--|---------------|
| Ground             | $ \Psi_{0}\rangle = \frac{V}{\sqrt{2E_{10}^{o}(E_{10}^{o}-\varepsilon)}} \left(1 - \frac{E_{10}^{o}-\varepsilon}{2V}J_{+}^{2}\right) \psi_{0}\rangle$        |  | $-E_{10}^{o}$ |
| Odd-order excited  | $Q_1^{o\dagger} \Psi_0\rangle = \frac{1}{\sqrt{2}}J_+ \psi_0\rangle$   |  | 0             |
| Even-order excited | $Q_1^{e\dagger}  \Psi_0\rangle = \frac{V}{\sqrt{2E_{10}^o(E_{10}^o + \varepsilon)}} \left(1 + \frac{E_{10}^o + \varepsilon}{2V} J_+^2\right)  \psi_0\rangle$ |  | $E_{10}^{o}$  |
| ·                  |  |  |               |
| Eigenstate         | Excitation energy  | Phonon-creation operator   |               |
| Ground             | 0  |  |               |
| Odd-order excited  | $E_{10}^o = \sqrt{\varepsilon^2 + V^2}$  | $Q_1^{o\dagger} = \frac{\sqrt{E_{10}^o}}{2\varepsilon} \left( \frac{V}{ V } \sqrt{E_{10}^o + \varepsilon} J_+ + \sqrt{E_{10}^o - \varepsilon} J \right)$                     |               |
| Even-order excited | $E_{10}^{e} = 2E_{10}^{o}$   | $Q_1^{e\dagger} = \frac{V}{ V } \left( \frac{V}{2\varepsilon} + \frac{E_{10}^o + \varepsilon}{4\varepsilon} J_+^2 + \frac{E_{10}^o - \varepsilon}{4\varepsilon} J^2 \right)$ |               |

J. Terasaki, A. Smetana, F. Š., M.I. Krivoruchenko, arXiv:1701.08368 [nucl-th]



## **Instead of Conclusions**



Progress in nuclear structure calculations is highly required

10/16/2017 We are at the beginning of the BSM Road...

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