

Production and decay of charmed baryons

Atsushi Hosaka

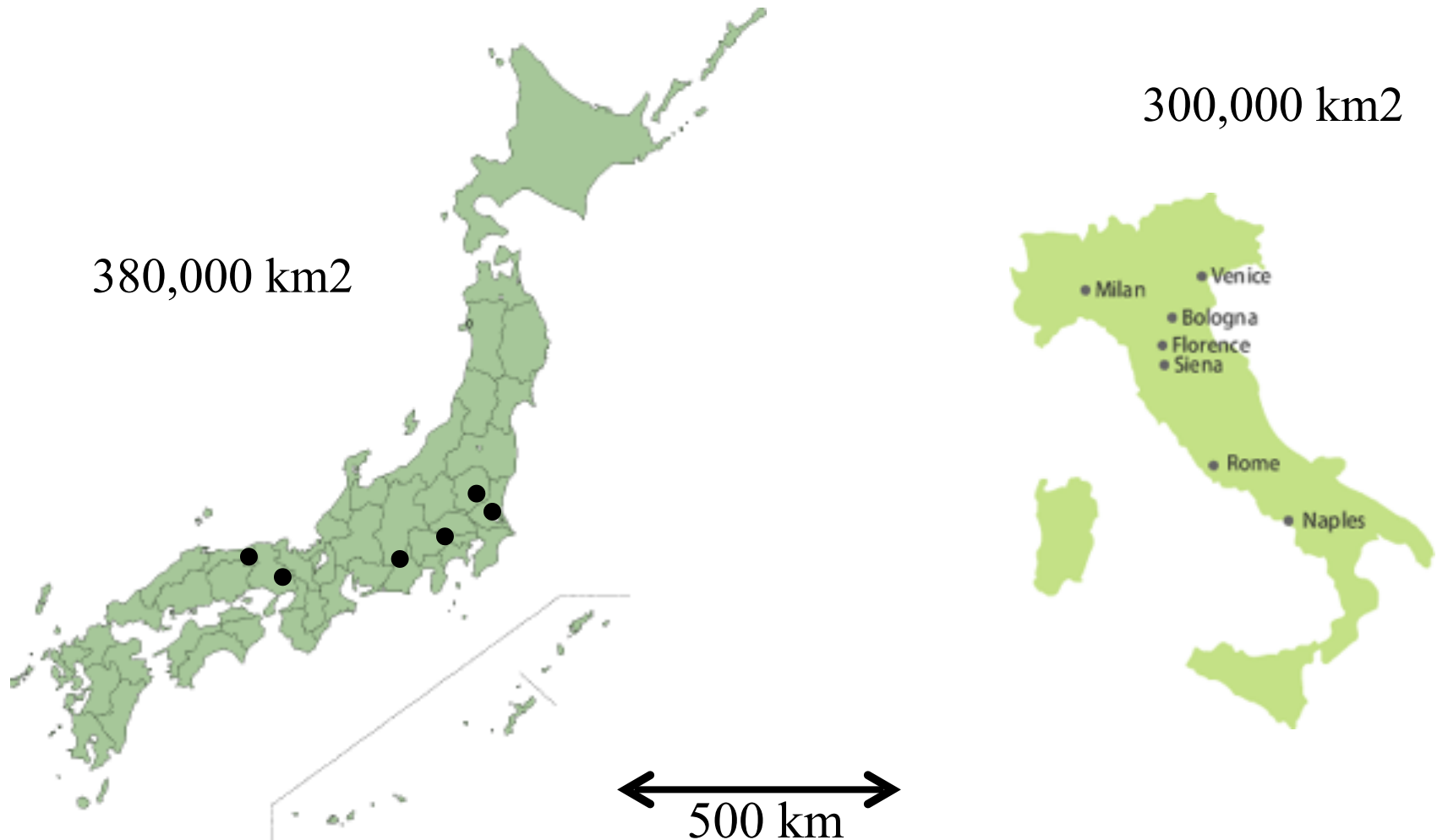
RCNP, Osaka University

Seminar at INFN, Genova, Italy

October 5th (Wed), 2016

1. Introduction of RCNP/Osaka University
2. Introduction — Why charmed baryons? —
Separation of λ and ρ modes
3. Pion emission decays
4. Production
5. Summary

Japan → Osaka → OU → RCNP





500 km



Around three campuses

Mino
Suita
Toyonaka



Expo park '70



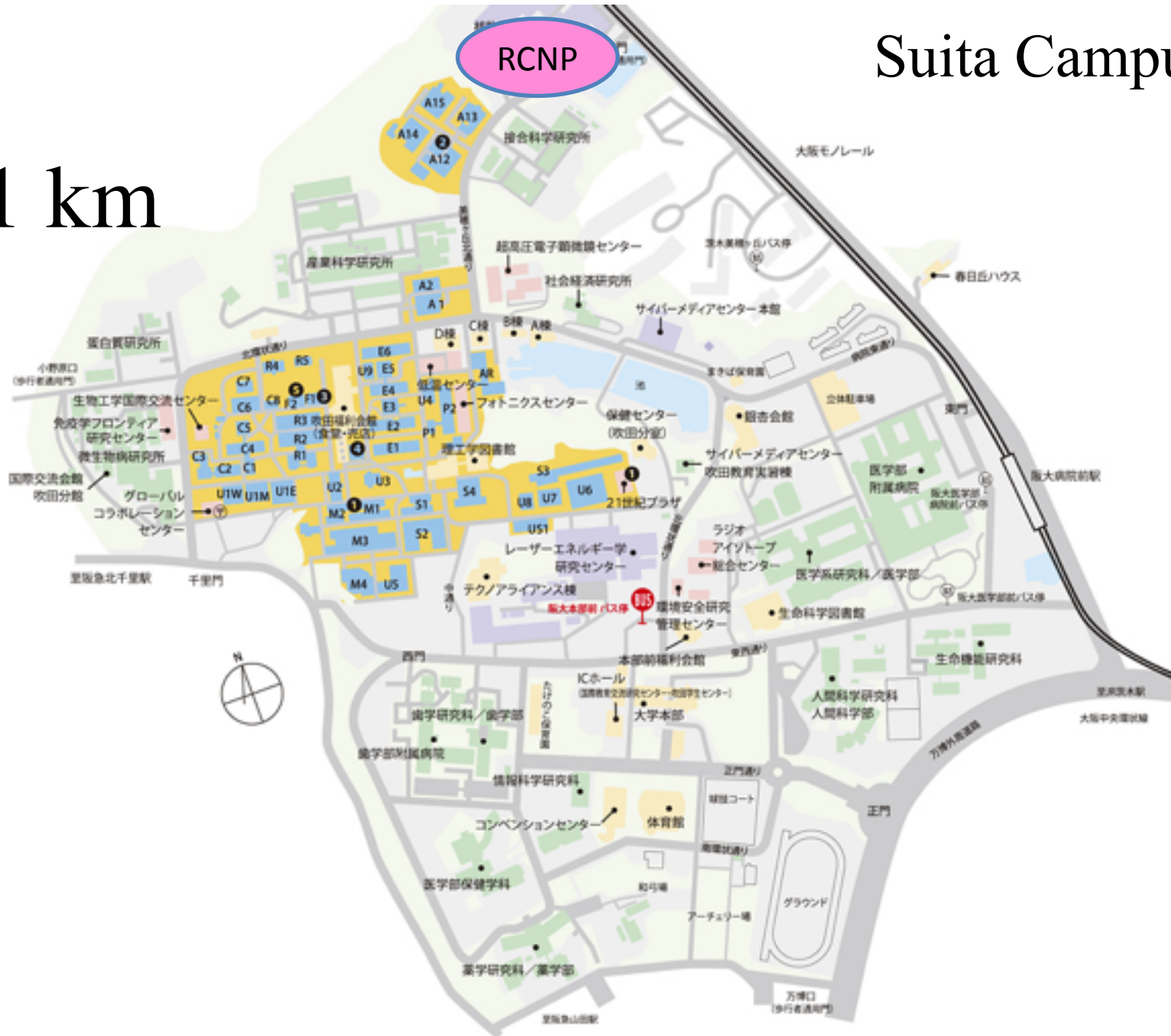
Downtown



Osaka Castle

RCNP

1 km



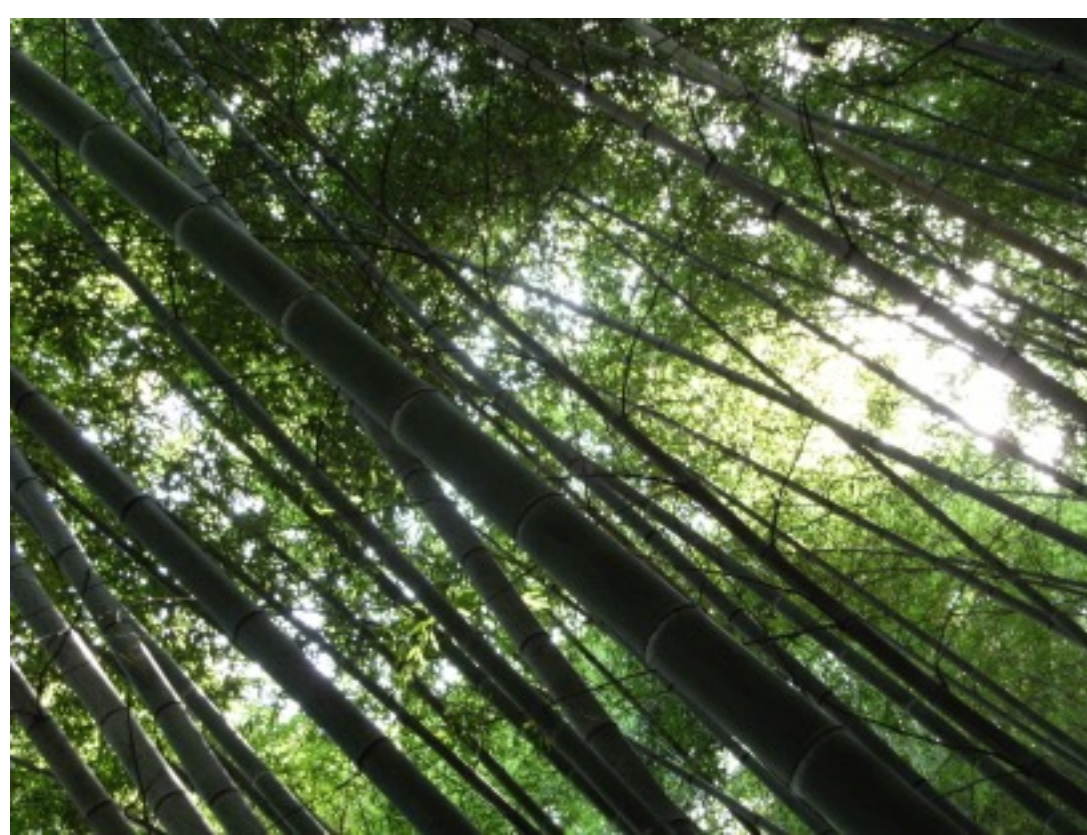


Cherry trees



Hospital

Bamboo woods and bamboo shoots



大阪大学

12大学院

文学研究科
人間科学研究科
法学研究科
経済学研究科
理学研究科
医学系研究科
薬学研究科
工学研究科
基礎工学研究科
言語文化研究科
国際公共政策研究科
情報科学研究科

www.osaka-u.ac.jp

10学部

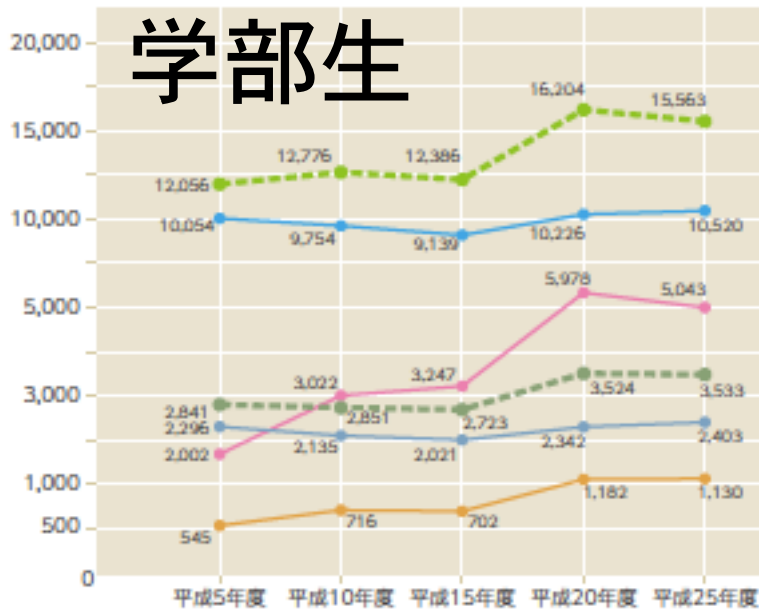
文学部
人間科学部
法学部
経済学部
理学部
医学部
歯学部
薬学部
工学部
基礎工学部

23研究所・センター

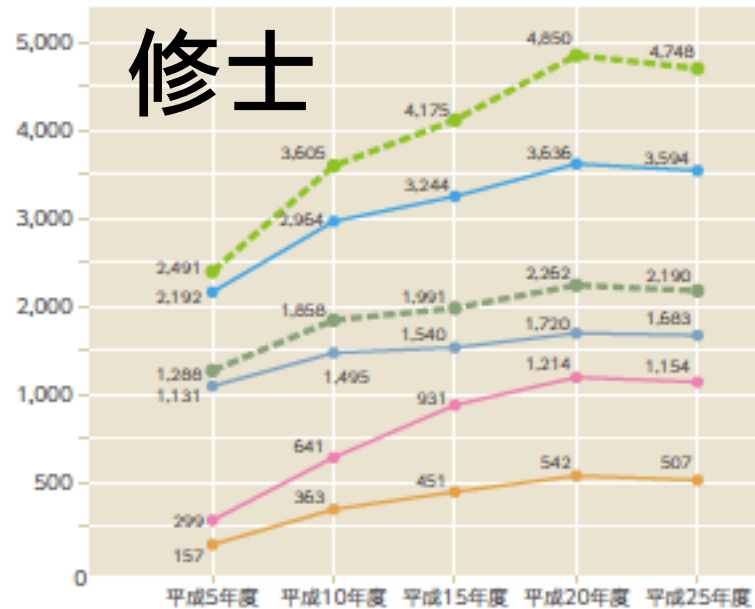
微生物病研究所
産業科学研究所
蛋白質研究所
社会経済研究所
接合科学研究所
レーザーエネルギー学研究センター
工作センター
低温センター
超高圧電子顕微鏡センター
ラジオアイソトープ総合センター
太陽エネルギー化学研究センター
環境安全研究管理センター
留学生センター
生物工学国際交流センター
極限科学研究センター
総合学術博物館
大学教育実践センター
先端科学イノベーションセンター
保健センター
臨床医工学融合研究教育センター
コミュニケーションデザイン・センター
サイバーメディアセンター

核物理研究センター

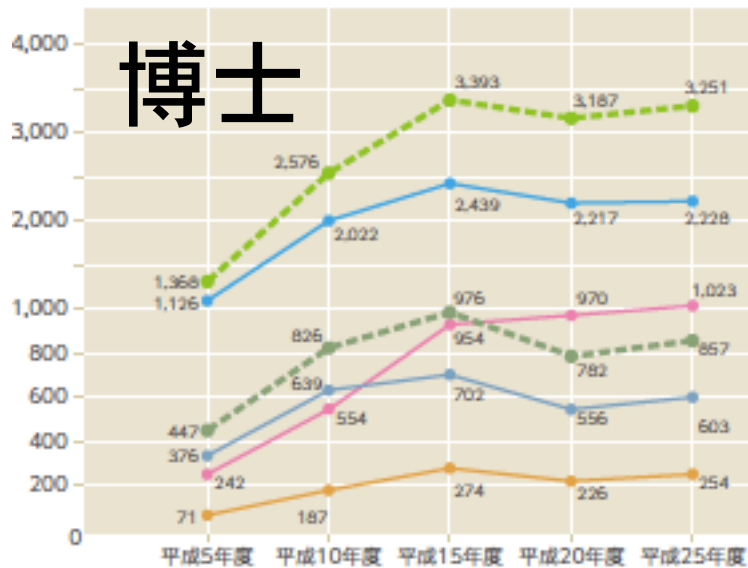
学部生



修士



博士



学部生： 15,563

大学院生： 3,251

教員： 3,111

職員： 1,483

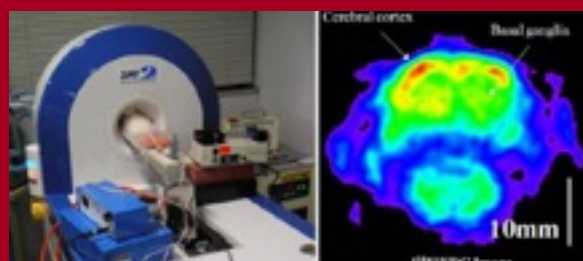


RCNP Cyclotron Facility



Osaka University Undertaking by cooperation among RCNP and Graduate School of Medicine and Science

Graduate School of Medicine

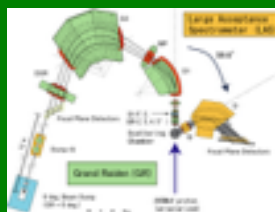


Training of medical physicists by higher education using accelerators

Medical and clinical applications of accelerator science, nuclear physics, radiation physics

- Heavy-particle gantry
- Next generation BNCT
- High intensity compact accelerator

RCNP



- Diagnostics
- Nuclear data

RI production

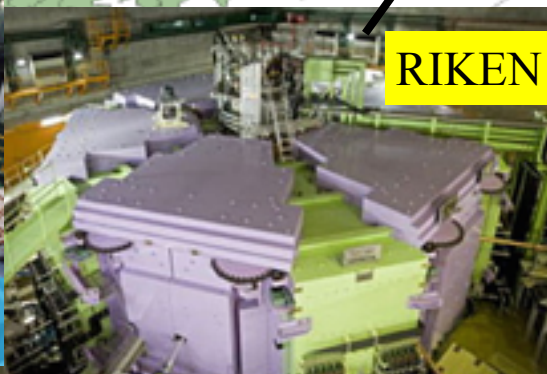
RI separation and synthesis

Graduate School of Science



Accelerators in Japan

← 500 km →



RIBF RIビームファクトリー

> 29, 2016

Supercomputer

- Cooperating **SX-ACE (NEC)** vector processor ~ **393 TF**
- Spend about 20 million yen (~ 0.2 million dollar)/year
- ~ 100 users (about 10 foreign uses), ~ 30 active users
- Lattice QCD, Nuclear structure, Few-body, Supernova
- About 10-20 publications/year

Role in the community

High **P**erformance **C**omputer **I**nfra
with the Japan largest supercomputer. **KEI**



Physics now

1. Introduction

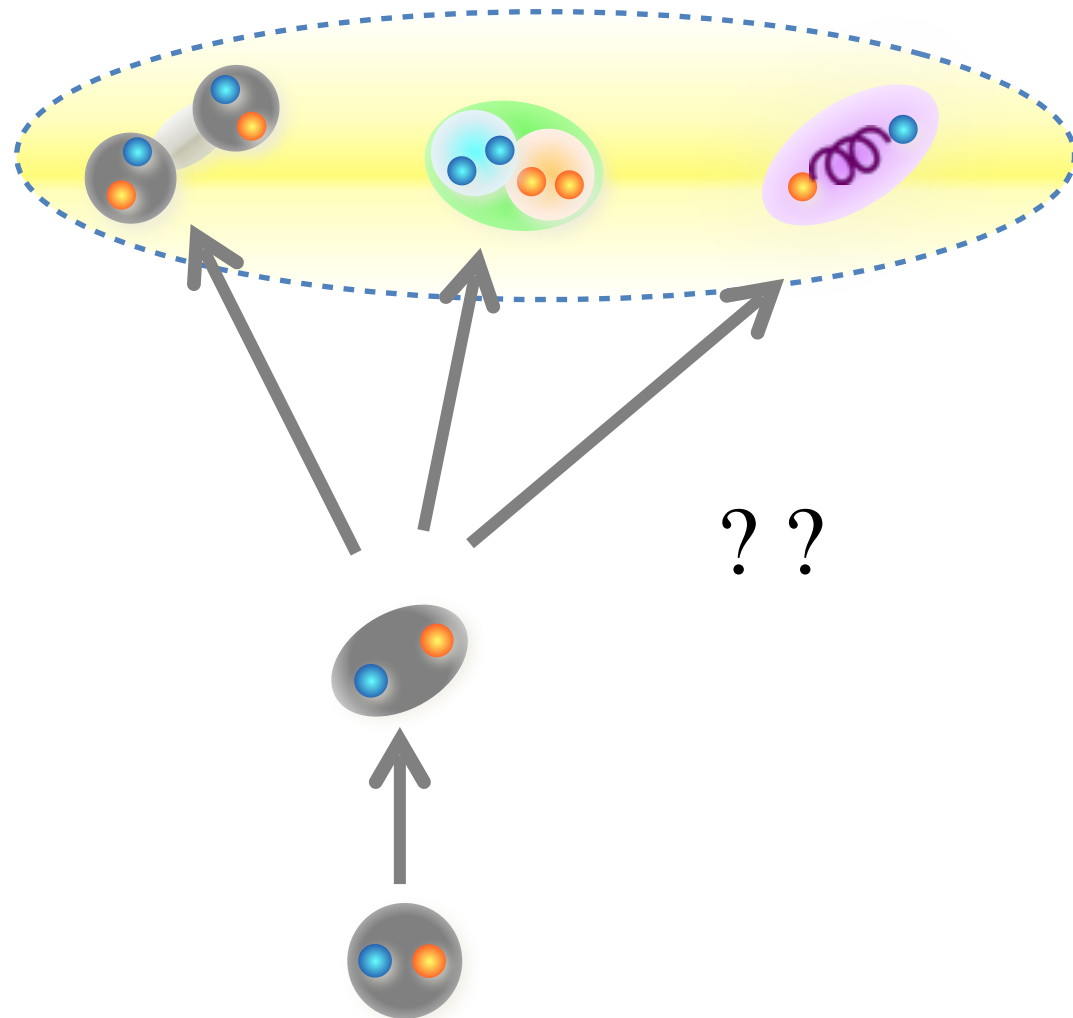
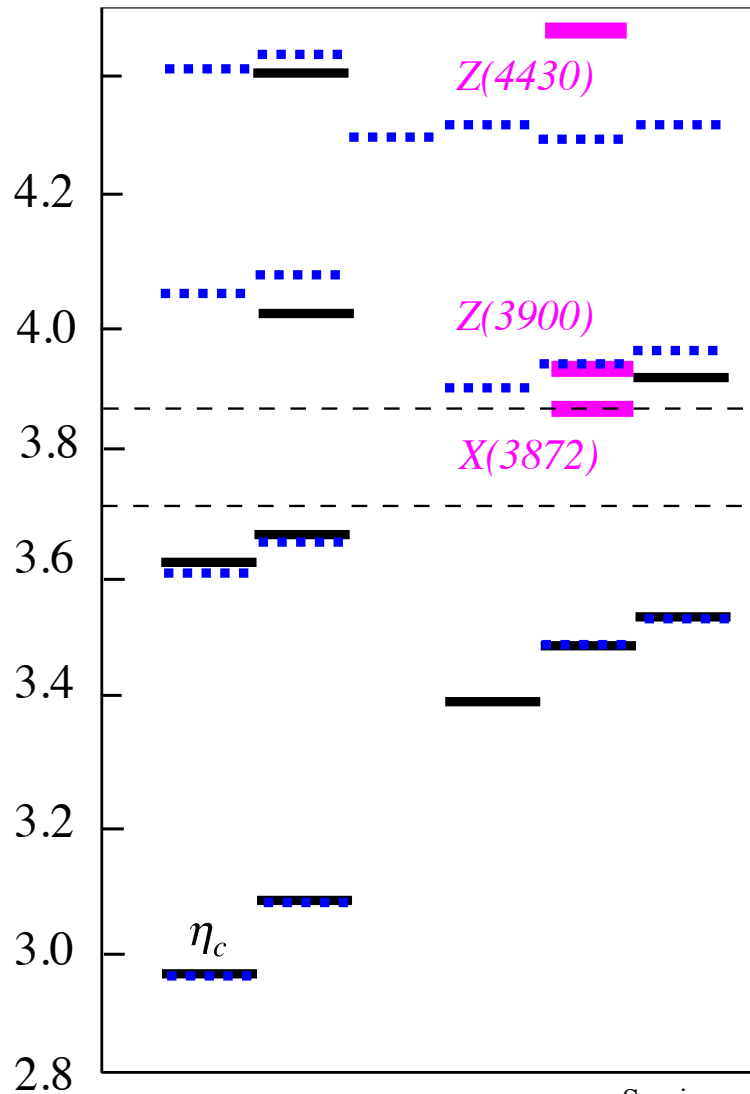
— Why charmed baryons —

- There are only **a few number** of heavy baryons known
- Simplest system of a **heavy and light quarks**
- Helpful to understand **exotic hadrons**

Next page

Better understanding is needed for exotic hadrons of heavy and light quarks

Charmonium-like states



Physics now

1. Introduction

— Why charmed baryons —

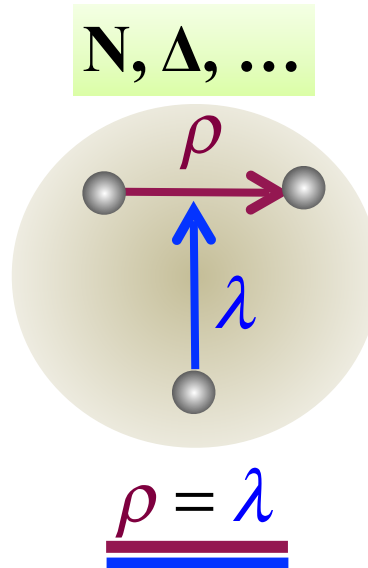
- There are only **a few number** of heavy baryons known
- Simplest system of a **heavy and light quarks**
- Helpful to understand **exotic hadrons**

Next page

- As a unique feature, separation of two orbital motions
 λ and ρ motions

Heavy quarks distinguish the internal modes λ and ρ

Isotope-shift: Copley-Isgur-Karl, PRD20, 768 (1979)

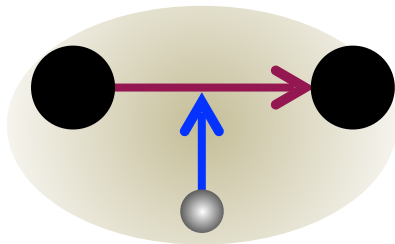


$$m_Q = m_{u,d}$$

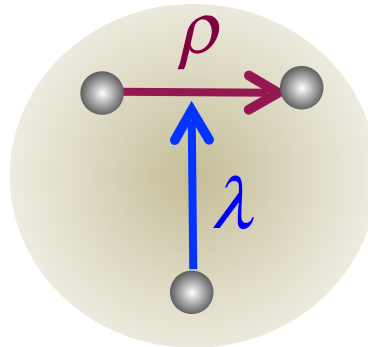
Heavy quarks distinguish the internal modes λ and ρ

Isotope-shift: Copley-Isgur-Karl, PRD20, 768 (1979)

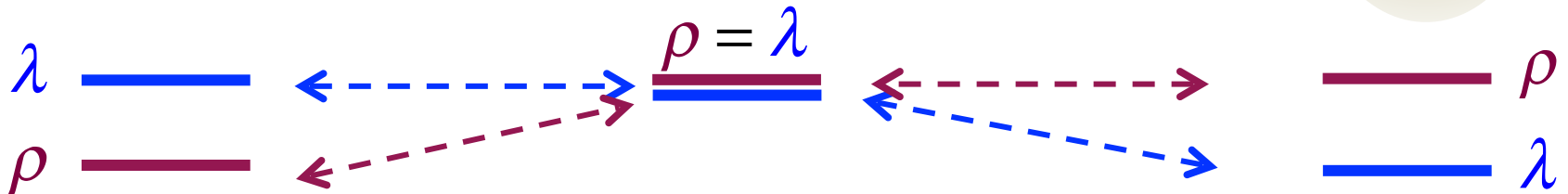
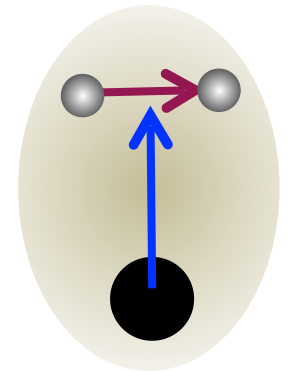
Ξ, Ξ^*, \dots



N, Δ, \dots



$\Lambda_c, \Sigma_c, \dots$



$$m_Q, m_Q \rightarrow \infty$$

$$m_Q = m_{u,d}$$

$$m_Q \rightarrow \infty$$

These structures should be sensitive to reactions

Wave functions \sim Harmonic oscillator

$$H = \frac{p_1^2}{2m_q} + \frac{p_2^2}{2m_q} + \frac{p_3^2}{2M_Q} - \frac{P^2}{2M_{tot}}$$

$$+ V_{conf}(HO) + V_{spin-spin}(Color - magnetic) + \dots$$

$$m = 0.35 \pm 0.05 \text{ GeV}$$

$$M = 1.5 \pm 0.1 \text{ GeV}$$

$$k = 0.02 - 0.04 \text{ GeV}^3$$



$$\hbar\omega_\lambda \sim 0.3 - 0.4 \text{ GeV}$$

$$\sqrt{\langle R^2 \rangle} \sim 0.45 - 0.55 \text{ fm}$$

$\Lambda_c^*, \Sigma_c, \dots$

$$\Lambda_c(J^-; \lambda) = \left[[\psi_1(\vec{\lambda}) \psi_0(\vec{\rho}), d^0]^1, \chi_c \right]^{J=\frac{1}{2}, \frac{3}{2}} D^0_c$$

$$\Sigma_c(1/2^+) = \left[[\psi_0(\vec{\lambda}) \psi_0(\vec{\rho}), d^1]^1, \chi_c \right]^{\frac{1}{2}} D^1_c$$

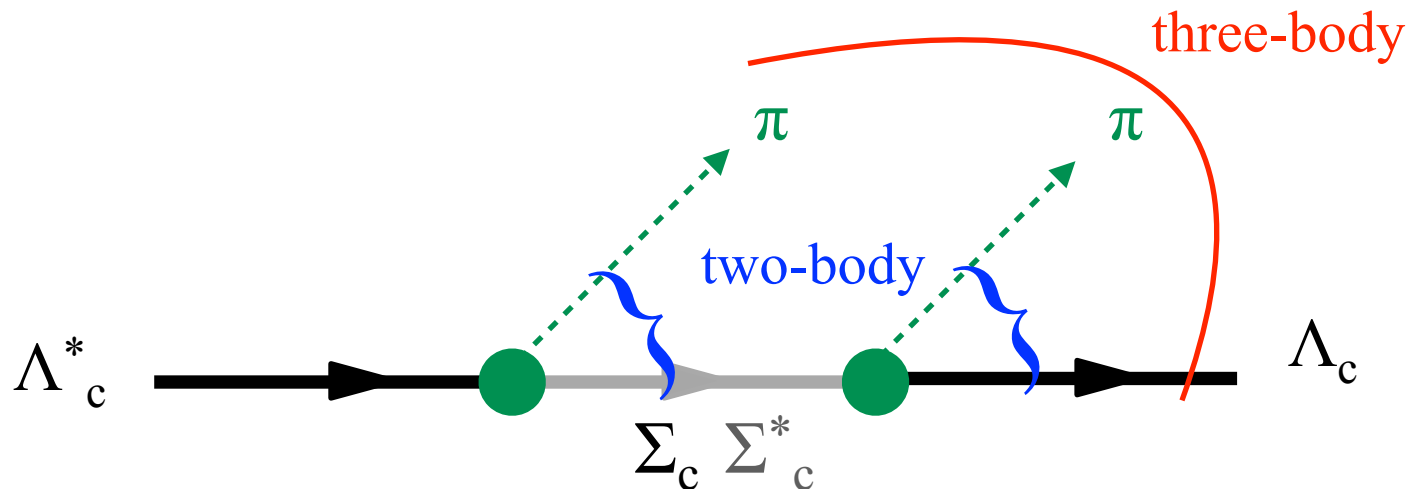
etc.

di-quark spin

2. Decays —Pion emission—

On going, Nagahiro, Yasui, ..., Arifi

Nagahiro et al, arXiv:1609.01085



Two-body decays

and

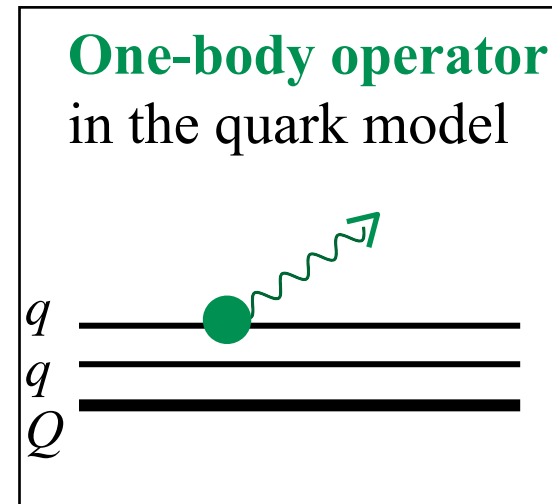
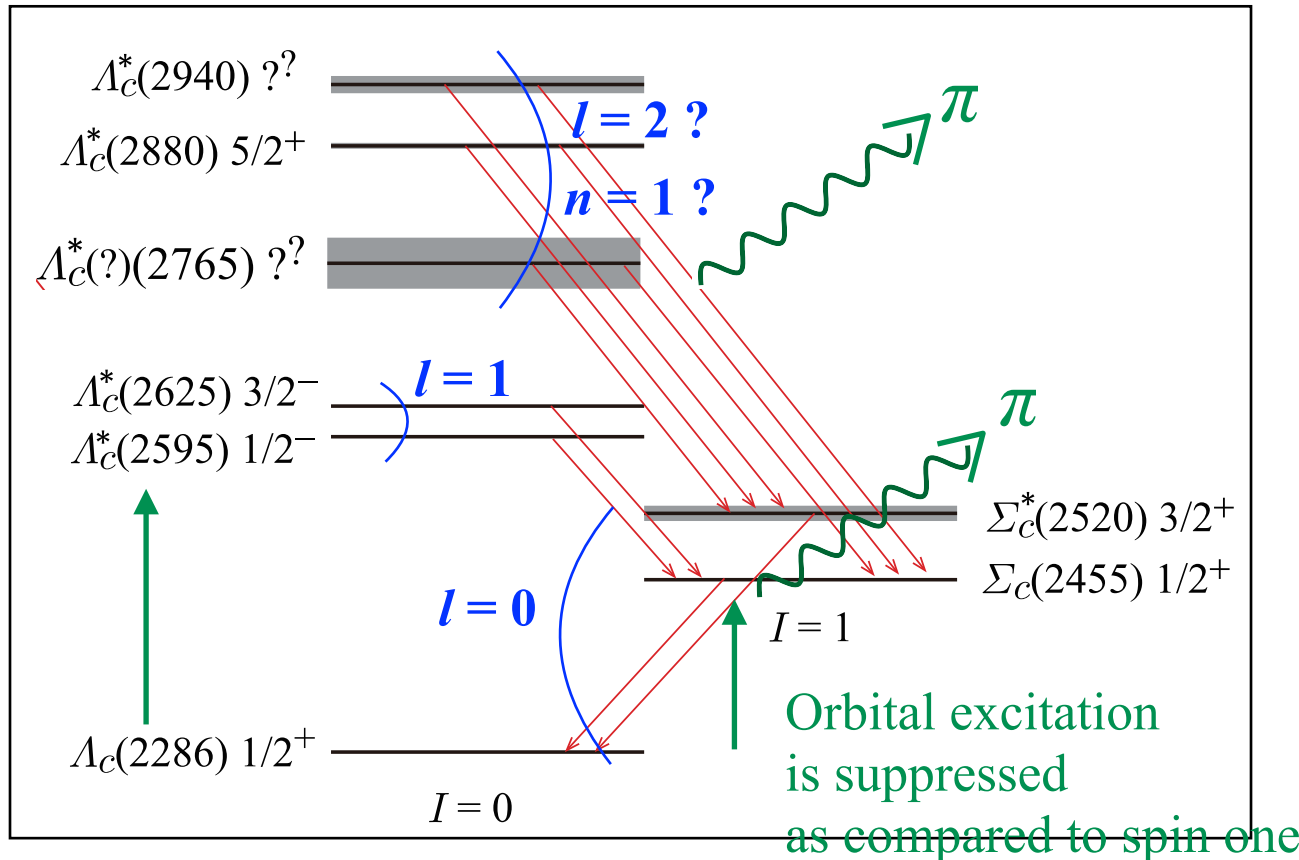
Three-body decays

2. Decays —Pion emission—

On going, Nagahiro, Yasui, ..., Arifi

Nagahiro et al, arXiv:1609.01085

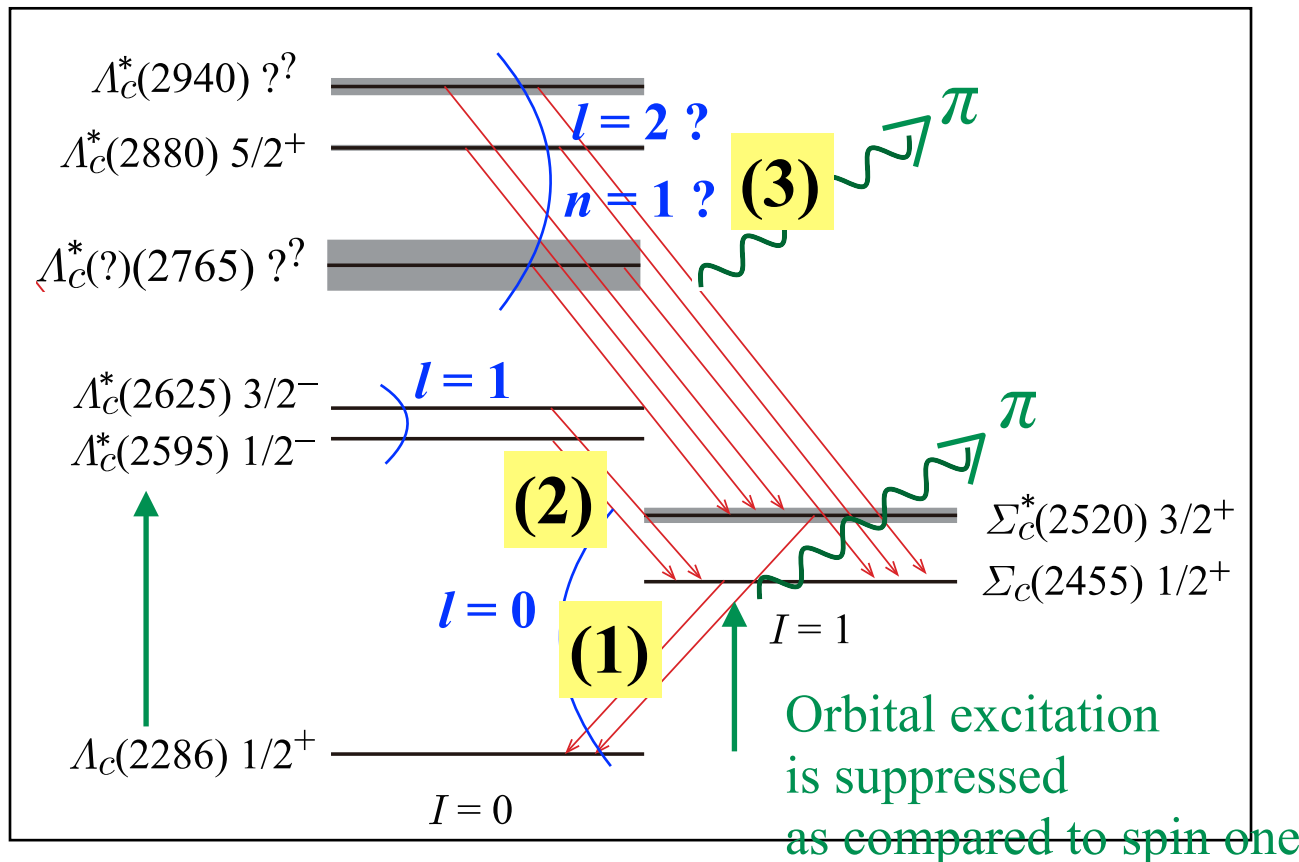
Two-body decays



2. Decays —Pion emission—

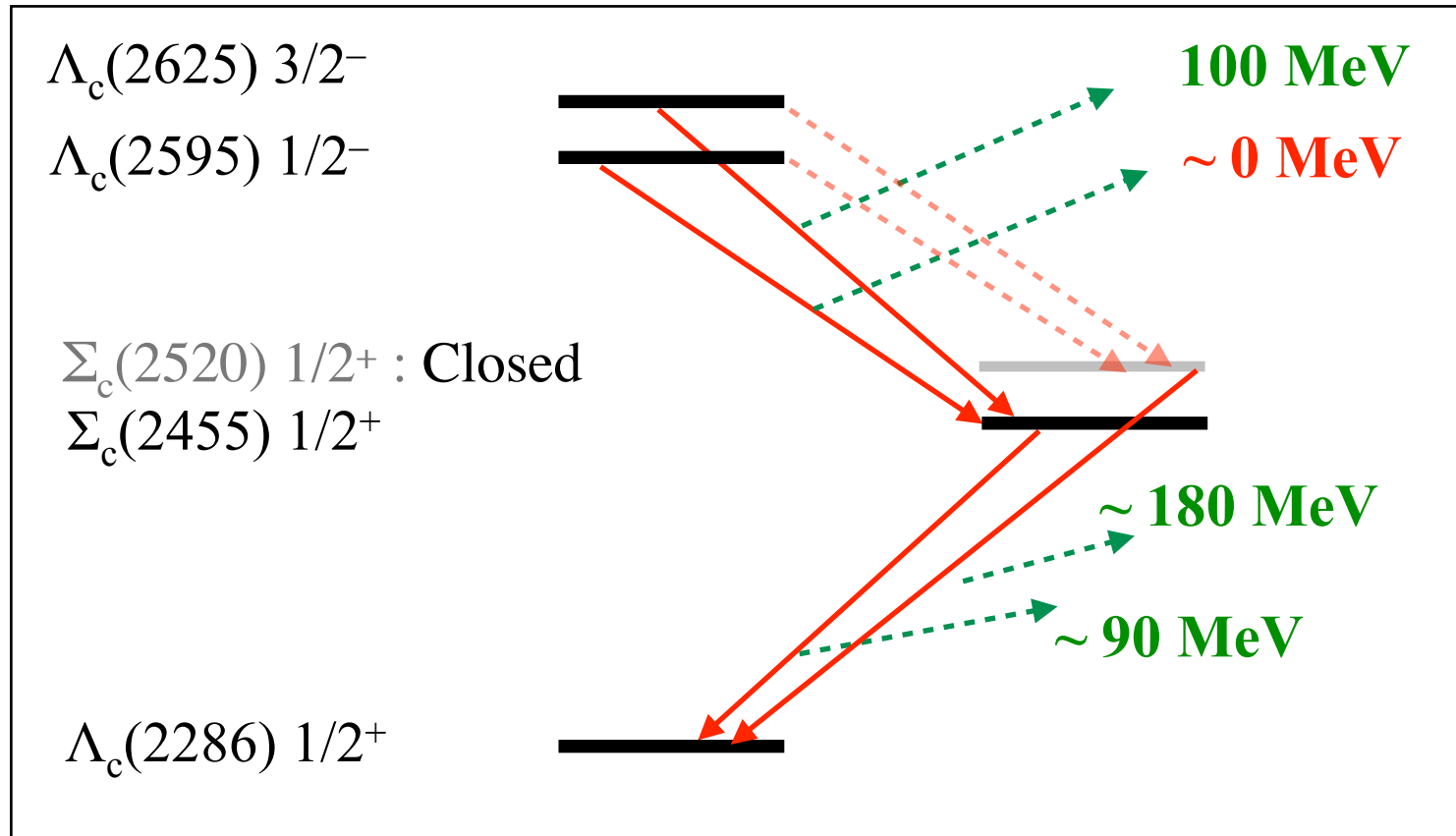
On going, Nagahiro, Yasui, ..., Arifi

Two-body decays



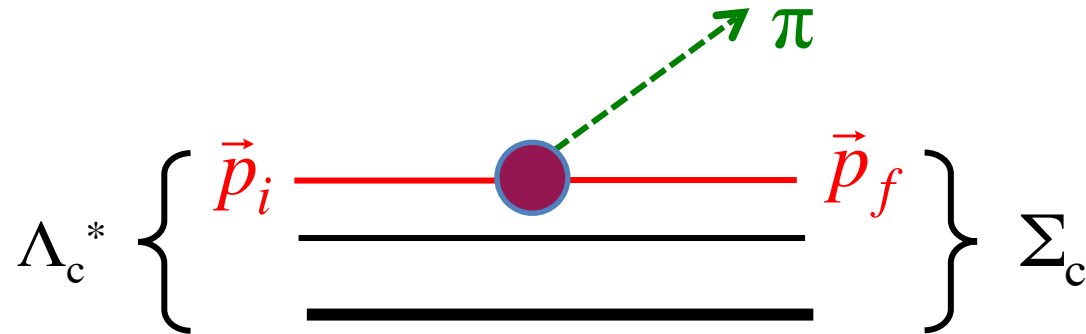
- (1) $0h\omega \rightarrow 0h\omega$
- (2) $1h\omega \rightarrow 0h\omega$
- (3) $2h\omega \rightarrow 0h\omega$

Low lying decays, $0h\omega \rightarrow 0h\omega$, $1h\omega \rightarrow 0h\omega$
with small p_π (MeV)



To compare with $\Delta \rightarrow \pi N$ at $p_\pi \sim 230 \text{ MeV}$
Low energy pion dynamics works well

Low energy πqq interaction



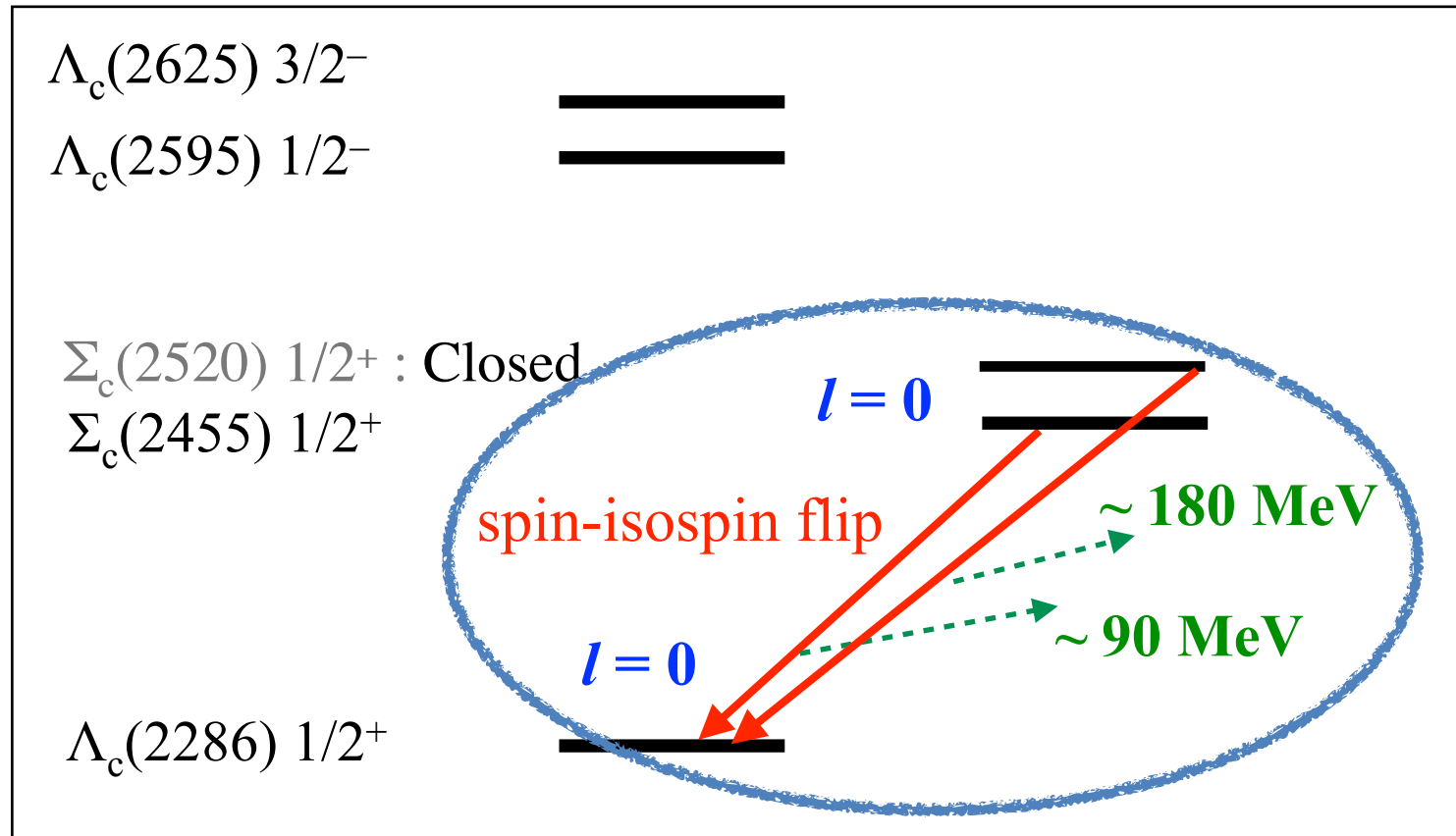
Non-relativistic $\vec{\sigma} \cdot \vec{p}_i, \vec{\sigma} \cdot \vec{p}_f$

Relativistic $\bar{q}\gamma_5 q \phi_\pi, \bar{q}\gamma^\mu \gamma_5 q \partial_\mu \phi_\pi$
PS *PV: preferable*

$$\mathcal{L}_{\pi qq}(x) = \frac{g_A^q}{2f_\pi} \bar{q}(x) \gamma_\mu \gamma_5 \vec{\tau} q(x) \cdot \partial^\mu \vec{\pi}(x)$$

$g_A^q \sim 1$: Quark axial coupling

(1) Ground to ground transitions, $0h\omega \rightarrow 0h\omega$



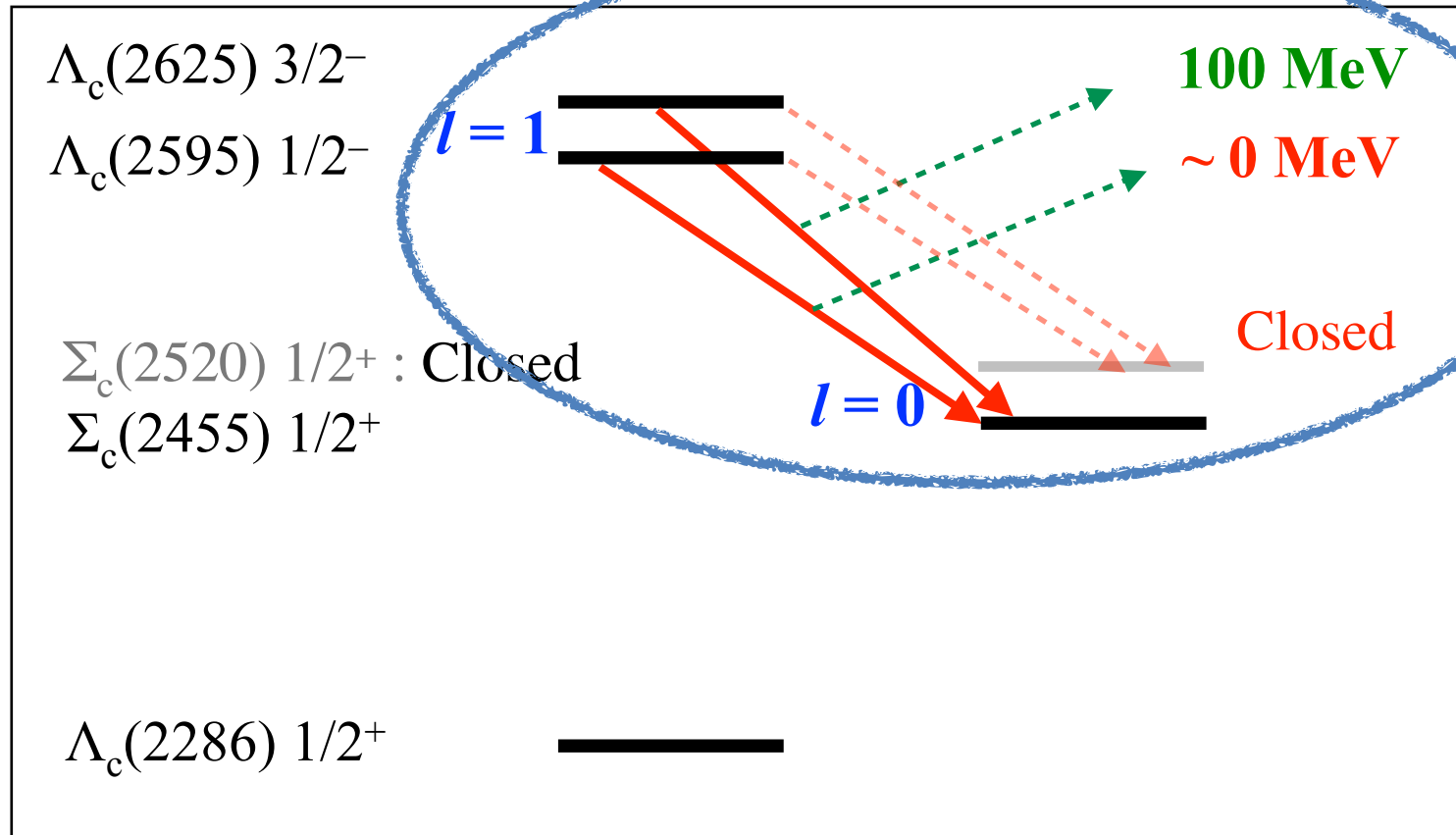
Ground $(1/2, 3/2^+) \rightarrow$ Ground $(1/2^+)$ [Nagahiro et al, arXiv:1609.01085](#)

$B_i J^P$ (MeV)	$\Gamma_{\text{exp}}^{\text{full}}(\Gamma_i)$ (MeV)	q (MeV)	$\Gamma_{\text{th}}(\Sigma_c(J^+)^{++} \rightarrow \Lambda_c^{gs}(1/2^+; 2286)^+ \pi^+)$ (MeV)
$\Sigma_c(2455) 1/2^+$ (2453.98) ($\omega_\pi = 0$ limit)	2.26 (2.26) (2.26)	89	4.27–4.33
$\Sigma_c(2520) 3/2^+$ (2517.9) ($\omega_\pi = 0$ limit)	14.9 (14.9)	176	30.0–31.2

Factor 2 difference, which is due to ...

$$g_A^q = 1 \rightarrow g_A^N = 5/3 < 1.25_{\text{exp}}$$

(2) P-wave to ground transitions, $1h\omega \rightarrow 0h\omega$



P-wave $(1/2^-, 3/2^-)$ to ground state $(1/2^+)$

Nagahiro et al, arXiv:1609.01085

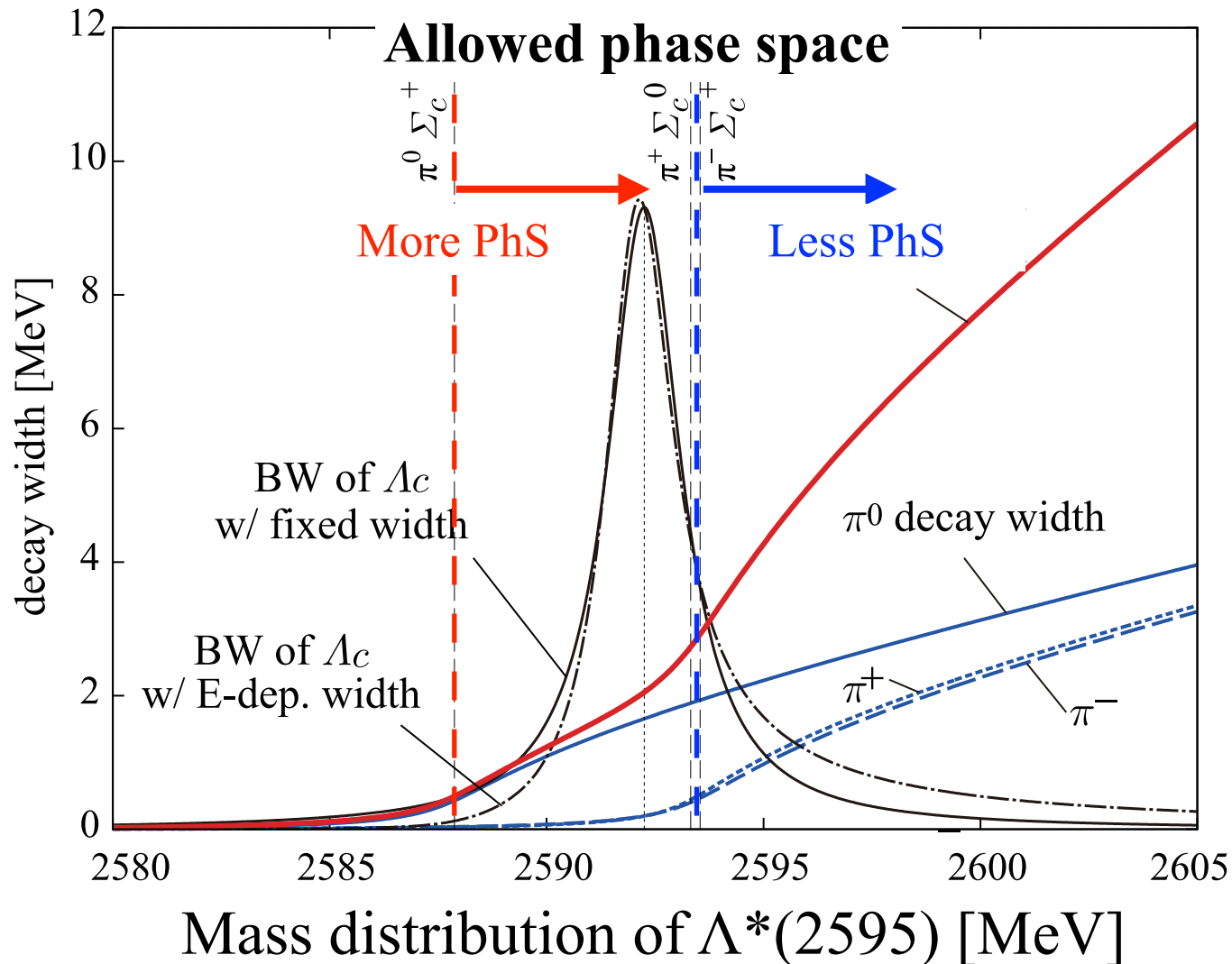
$\Lambda_c(2595) 1/2^-$

	decay channel	full	$[\Sigma_c \pi]^+$	$\Sigma_c^{++} \pi^-$	$\Sigma_c^0 \pi^+$	$\Sigma_c^+ \pi^0$
Experiments	(MeV) [5]	2.6 ± 0.6	-	<u>0.624 (24%)</u>	<u>0.624 (24%)</u>	-
Momentum	q (MeV/c)	-	-	\dagger	\dagger	29
$(n_\lambda, \ell_\lambda), (n_\rho, \ell_\rho)$	$J_\Lambda(j)^P$					
$(0, 1), (0, 0)$	$1/2(1)^-$		$1.5\text{--}2.9$	<u>$0.13\text{--}0.25$</u>	<u>$0.15\text{--}0.28$</u>	<u>$1.2\text{--}2.4$</u>
$(0, 0), (0, 1)$	$1/2(0)^-$		0	0	isospin violated	
	$1/2(1)^-$		$6.5\text{--}11.9$	$0.57\text{--}1.04$	$0.63\text{--}1.15$	$5.3\text{--}9.7$

- 80 % of the decay of is explained with strong isospin breaking
- λ -mode results consistent, ρ -mode results overestimate

Isospin breaking between $\pi^0 \Sigma_c^+$ and $\pi^+ \Sigma_c^0, \pi^- \Sigma_c^{++}$

Mass distribution of $\Lambda^*(2595)$ and different phase space



P-wave $(1/2^-, 3/2^-)$ to ground state $(1/2^+)$

Nagahiro et al, arXiv:1609.01085

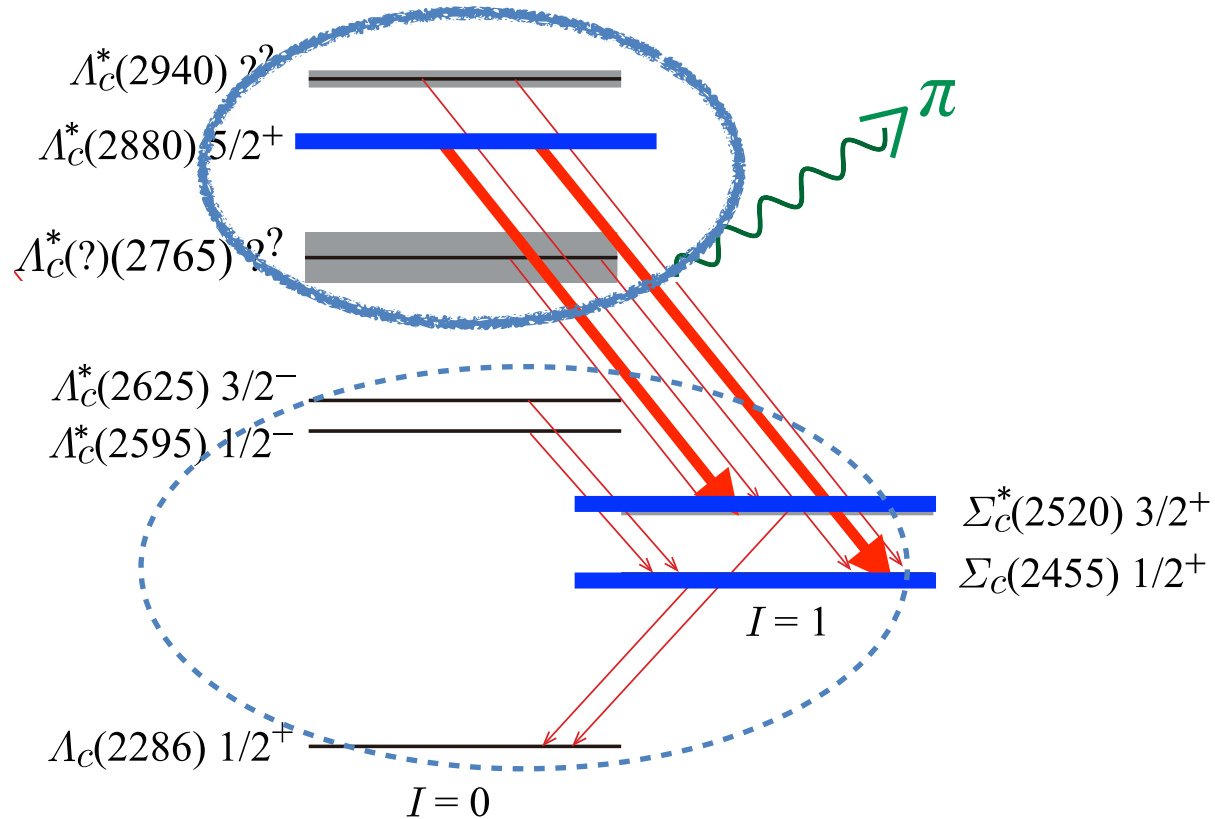
$\Lambda_c(2625) 31/2^-$

	decay channel	full	$\Sigma_c^{++} \pi^-$
Experimental value Γ (MeV) [5]		< 0.97	$< 0.05 (< 5\%)$
momentum of final particle q (MeV/c)		-	101
this work	$(n_\lambda, \ell_\lambda), (n_\rho, \ell_\rho)$	$J_\Lambda(j)^P$	
Γ	$(0, 1), (0, 0)$	$1/2(1)^-$	5.4–10.7
(MeV)		$3/2(1)^-$	0.024–0.039
	$(0, 0), (0, 1)$	$1/2(0)^-$	0

D-wave decay

- Only a small part of the decay width is from the two-body
- The remaining is considered later

(3) Transitions from higher states, $2h\omega \rightarrow 0h\omega$



$$R = \frac{\Gamma(\Sigma_c^*(3/2^+)\pi)}{\Gamma(\Sigma_c(1/2^+)\pi)}$$

sensitive to J^P and the structure of the decaying particle

$\Lambda_c(2880) 5/2^+$

decay channel	full	$[\Sigma_c^{(*)}\pi]_{\text{total}}$	$[\Sigma_c\pi]^+$	$[\Sigma_c^*\pi]^+$	R
Experimental value Γ (MeV)	<u>5.8 ± 1.1</u> [5]				<u>0.225</u> [14]
m of final particle q (MeV/c)			375	315	
$(n_\lambda, \ell_\lambda), (n_\rho, \ell_\rho)$	$J_\Lambda(j)^P$				
	<u>$5/2(1)^+$</u>	<u>$11.2\text{--}26.1$</u>	$1.2\text{--}2.8$	$9.9\text{--}23.3$	<u>$8.1\text{--}8.4$</u>
$(0, 0), (1, 0)$	$1/2(0)^+$	$16.5\text{--}40.2$	$7.0\text{--}18.2$	$9.5\text{--}22.1$	$1.2\text{--}1.4$
$(0, 0), (0, 2)$	$3/2(\textcolor{red}{2})^+$	$44.8\text{--}85.4$	$39.5\text{--}76.0$	$5.3\text{--}9.4$	$0.12\text{--}0.13$
	<u>$5/2(\textcolor{red}{2})^+$</u>	<u>$27.8\text{--}52.2$</u>	$1.4\text{--}2.6$	$26.4\text{--}49.5$	<u>$18.7\text{--}18.9$</u>
$(n_\lambda, \ell_\lambda), (n_\rho, \ell_\rho)$	$J_\Lambda(j)_\ell^P$				
$(0, 1), (0, 1)$	<u>$5/2(2)_2^+$</u>	<u>$51.7\text{--}109.6$</u>	$1.8\text{--}3.5$	$49.9\text{--}106.1$	<u>$27.5\text{--}30.1$</u>
	<u>$5/2(2)_1^+$</u>	<u>$0.63\text{--}1.68$</u>	0	$0.63\text{--}1.68$	<u>(∞)</u>
	<u>$5/2(3)_2^+$</u>	<u>$2.9\text{--}5.8$</u>	$2.1\text{--}4.0$	$0.85\text{--}1.73$	<u>$0.41\text{--}0.43$</u>

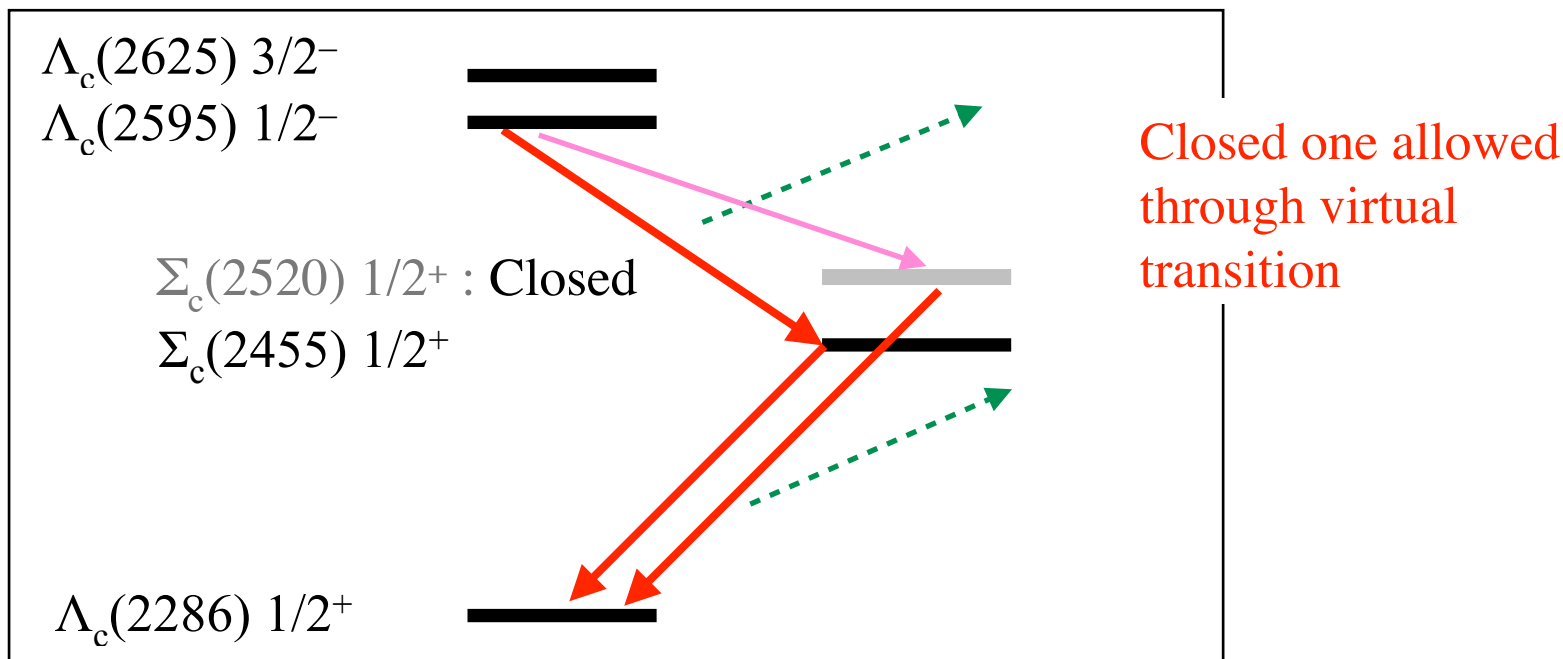
- Both absolute values and R ratio are sensitive to configurations
- Brown muck of $j = 3$ seems preferred.
- This implies that $\Lambda_c(2940)$ could be $7/2^+$

$$R = \frac{\Gamma(\Sigma_c^*(3/2^+)\pi)}{\Gamma(\Sigma_c(1/2^+)\pi)}$$

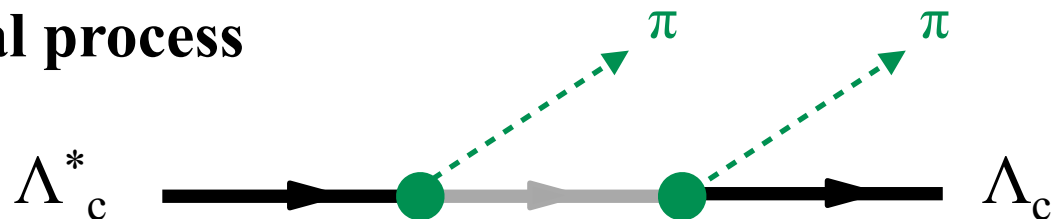
Three-body decay

Three-body decay

Experimentally, $\Lambda_c(2625) \ 3/2^-, \Lambda_c(2595) \ 1/2^- \rightarrow \pi\pi\Lambda_c(2286) \ 1/2^+$

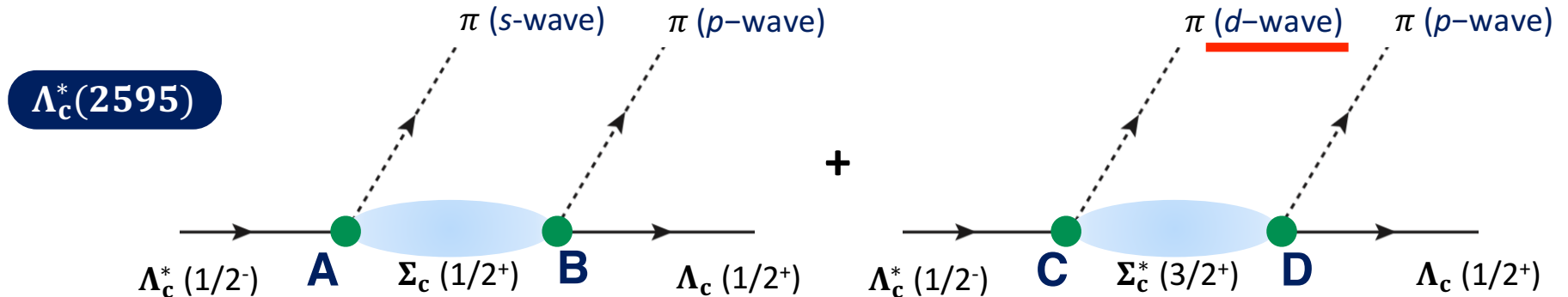


Sequential process



Effective Lagrangian

Three-Body Decay of $\Lambda_c^*(2595)$



Non-Relativistic

Coupling constants are determined by the quark model

$$\mathbf{A} \quad \mathcal{L}_A = g_a \chi_{\Sigma_c}^\dagger \chi_{\Lambda_c^*}$$

$$\mathbf{C} \quad \mathcal{L}_C = g_c \chi_{\Sigma_c^*}^\dagger \left(\vec{S}^\dagger \cdot \vec{p}_\pi \vec{\sigma} \cdot \vec{p}_\pi - \frac{1}{3} \vec{S}^\dagger \cdot \vec{\sigma} |\vec{p}_\pi|^2 \right) \chi_{\Lambda_c^*}$$

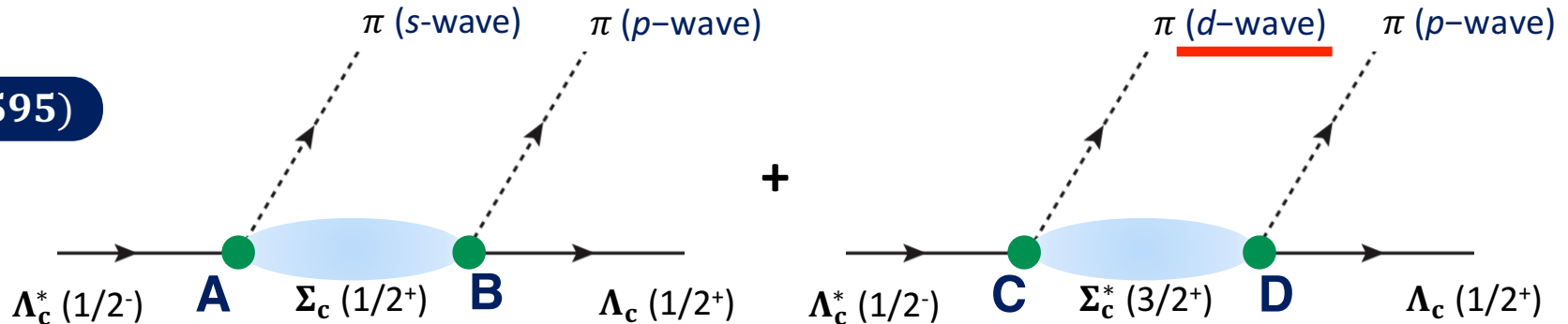
$$\mathbf{B} \quad \mathcal{L}_B = i g_b \chi_{\Lambda_c}^\dagger (\vec{\sigma} \cdot \vec{p}_\pi) \chi_{\Sigma_c}$$

$$\mathbf{D} \quad \mathcal{L}_D = i g_d \chi_{\Lambda_c}^\dagger (\vec{S} \cdot \vec{p}_\pi) \chi_{\Sigma_c^*}$$

Effective Lagrangian

Three-Body Decay of $\Lambda_c^*(2595)$

$\Lambda_c^*(2595)$



Non-Relativistic

Coupling constants are determined by the quark model

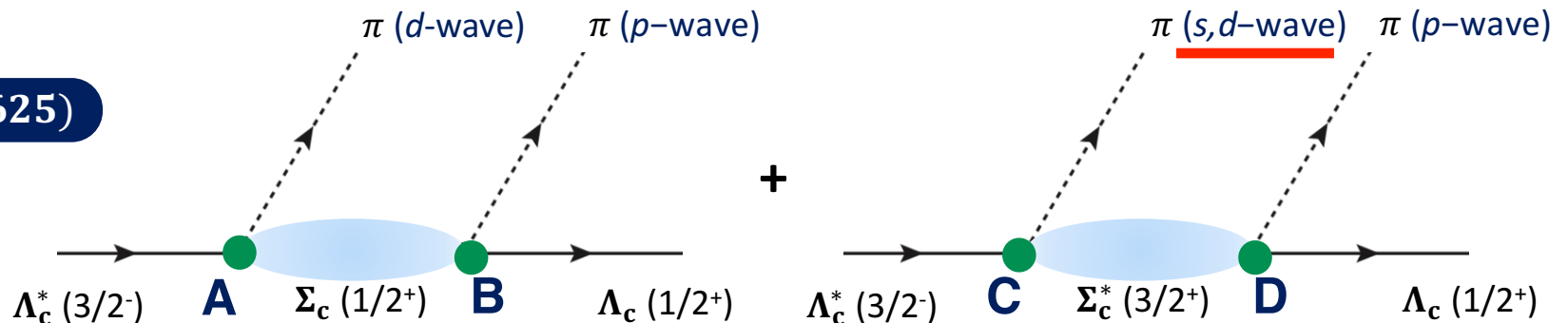
A $\mathcal{L}_A = g_a \chi_{\Sigma_c}^\dagger \chi_{\Lambda_c^*}$

C $\mathcal{L}_C = g_c \chi_{\Sigma_c^*}^\dagger \left(\vec{S}^\dagger \cdot \vec{p}_\pi \vec{\sigma} \cdot \vec{p}_\pi - \frac{1}{3} \vec{S}^\dagger \cdot \vec{\sigma} |\vec{p}_\pi|^2 \right) \chi_{\Lambda_c^*}$

B $\mathcal{L}_B = i g_b \chi_{\Lambda_c}^\dagger (\vec{\sigma} \cdot \vec{p}_\pi) \chi_{\Sigma_c}$

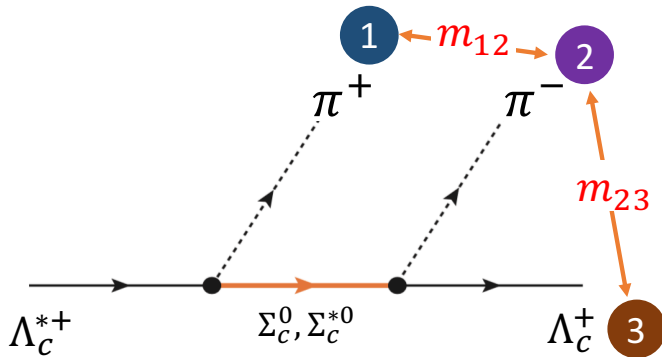
D $\mathcal{L}_D = g_d \chi_{\Lambda_c}^\dagger (\vec{S} \cdot \vec{p}_\pi) \chi_{\Sigma_c^*}$

$\Lambda_c^*(2625)$



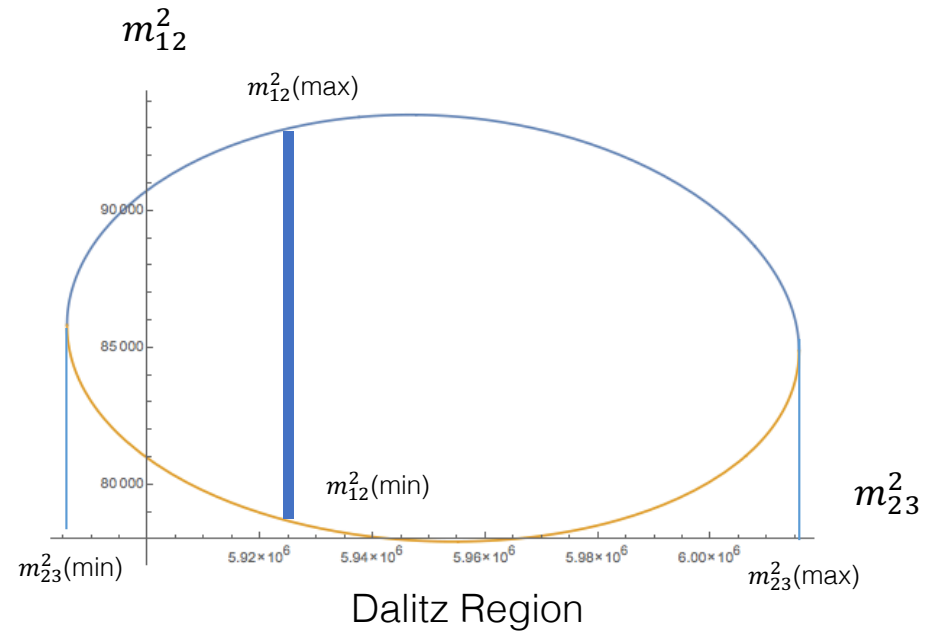
Decay Kinematics

Decay Width and Dalitz Region



Decay Width

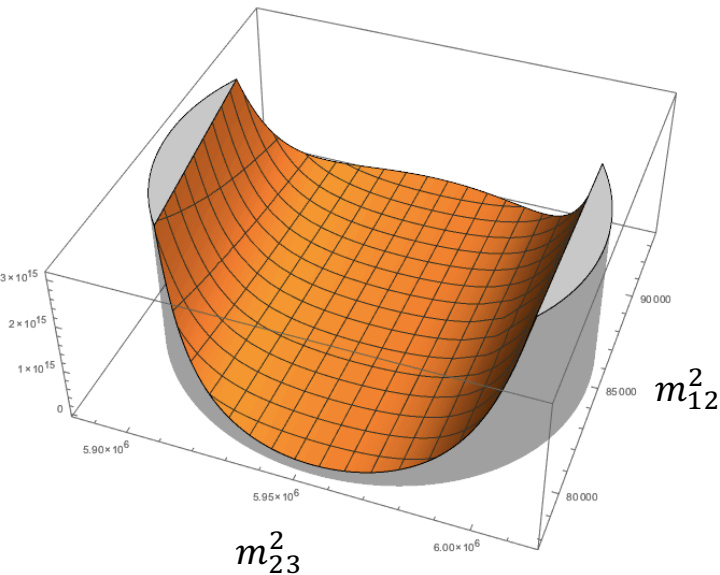
$$d\Gamma = \frac{1}{(2\pi)^3} \frac{1}{32M^3} |\overline{\mathcal{M}}|^2 dm_{12}^2 dm_{23}^2$$



$\Lambda_c^*(2595)$ Assuming the λ -mode excitations

Three-body Decay

The Results (MeV)



Dalitz Plot

Contribution	2-Body	3-Body	Exp. Data
$\Sigma_c^{++}\pi^-$	0.13 – 0.25	0.16	0.624 (24%)
$\Sigma_c^0\pi^+$	0.15 – 0.28	0.25	0.624 (24%)
$\Sigma_c^+\pi^0$	1.2 – 2.4	1.63	-
3-body	-	10^{-6} (tail Σ_c^*)	0.468 (18%)
Interference	-	0.05	-
Total	1.5 – 2.9	2.09	2.6 ± 0.6

Parameters

$$f_\pi = 94 \text{ MeV}$$

$$a_\lambda = 400 \text{ MeV}$$

$$m = 350 \text{ MeV}$$

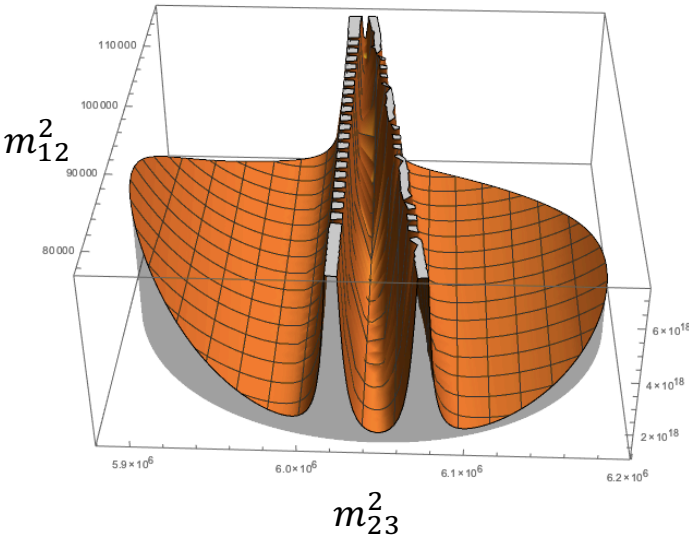
$$a_\rho = 290 \text{ MeV}$$

$$M = 1500 \text{ MeV}$$

- 80 % of the decay of $\Lambda_c(2595)$ is due to the two body decay: confirmed
- The virtual process of $\Sigma_c(2520)$ has only minor role due to the D-wave nature
- The remaining ~ 20 % is from other $\pi\pi$ couplings (σ , ...?)

$\Lambda_c^*(2625)$

Three-body Decay



The Results (MeV)

Contribution	2-Body	3-Body	Exp. Data
$\Sigma_c^{++}\pi^-$	0.024 – 0.039	0.036	< 0.05 ($< 5\%$)
$\Sigma_c^0\pi^+$	-	0.032	< 0.05 ($< 5\%$)
$\Sigma_c^+\pi^0$	-	0.053	-
3-body	-	0.180 (tail Σ_c^*)	(large)
Interference	-	0.033	-
Total	-	0.334	< 0.970

- The two body decay of $\Lambda_c(2625)$ is only minor
- The virtual process of $\Sigma_c(2520)$ is large due to S-wave nature
- With the ρ mode excitation, the width is overestimated

➡ $\Lambda_c(2595)$ and $\Lambda_c(2625)$ are most likely
the λ mode HQ doublet of $l_\lambda (=1) + 1/2_Q = 1/2^-, 3/2^-$

Summary

- Heavy (strange, charm, bottom) quarks disentangle different modes of baryons, ρ and λ modes
- Productions are useful for the study of structure
A similar feature with hyper nuclei
- Production rates of excited states may depend on flavor
Excitations are abundantly produced for charm
- Decay rates are sensitive to the structure
- Also a good laboratory to test low energy chiral dynamics
- The nature of states are well studied,
 $\Lambda_c(2595, 1/2^-)$ and $\Lambda_c(2625, 3/2^-)$ are most likely the λ mode

Charm $k_{\pi}^{CM} = 2.71$ [GeV] , $k_{\pi}^{Lab} = 16$ [GeV]

$l = 0$	$\Lambda_c(\frac{1}{2}^+)$ 1.00	$\Sigma_c(\frac{1}{2}^+)$ 0.02	$\Sigma_c(\frac{3}{2}^+)$ 0.16					
<u>$l = 1$</u>	$\Lambda_c(\frac{1}{2}^-)$ 0.90	$\Lambda_c(\frac{3}{2}^-)$ 1.70	$\Sigma_c(\frac{1}{2}^-)$ 0.02	$\Sigma_c(\frac{3}{2}^-)$ 0.03	$\Sigma'_c(\frac{1}{2}^-)$ 0.04	$\Sigma'_c(\frac{3}{2}^-)$ 0.19	$\Sigma'_c(\frac{5}{2}^-)$ 0.18	
<u>$l = 2$</u>	$\Lambda_c(\frac{3}{2}^+)$ 0.50	$\Lambda_c(\frac{5}{2}^+ -)$ 0.88	$\Sigma_c(\frac{3}{2}^+)$ 0.02	$\Sigma_c(\frac{5}{2}^+)$ 0.02	$\Sigma'_c(\frac{1}{2}^+)$ 0.01	$\Sigma'_c(\frac{3}{2}^+)$ 0.03	$\Sigma'_c(\frac{5}{2}^+)$ 0.07	$\Sigma'_c(\frac{5}{2}^+)$ 0.07

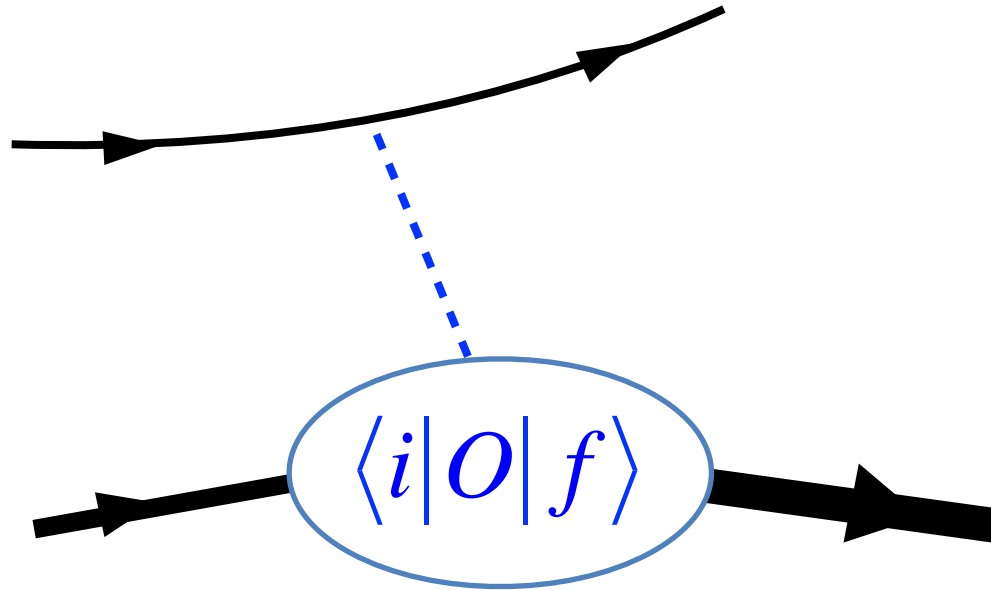
Strange $k_{\pi}^{CM} = 1.59$ [GeV], $k_{\pi}^{Lab} = 5.8$ [GeV]

$l = 0$	$\Lambda_{-}(\frac{1}{2}^{+})$ 1.00	$\Sigma_{-}(\frac{1}{2}^{+})$ 0.067	$\Sigma_{-}(\frac{3}{2}^{+})$ 0.44					
$l = 1$	$\Lambda_{-}(\frac{1}{2}^{-})$ 0.11	$\Lambda_{-}(\frac{3}{2}^{-})$ 0.23	$\Sigma_{-}(\frac{1}{2}^{-})$ 0.007	$\Sigma_{-}(\frac{3}{2}^{-})$ 0.01	$\Sigma'_{-}(\frac{1}{2}^{-})$ 0.01	$\Sigma'_{-}(\frac{3}{2}^{-})$ 0.07	$\Sigma'_{-}(\frac{5}{2}^{-})$ 0.067	
$l = 2$	$\Lambda_{-}(\frac{3}{2}^{+})$ 0.13	$\Lambda_{c}(\frac{5}{2}^{+}-)$ 0.20	$\Sigma_{-}(\frac{3}{2}^{+})$ 0.007	$\Sigma_{-}(\frac{5}{2}^{+})$ 0.01	$\Sigma'_{-}(\frac{1}{2}^{+})$ 0.004	$\Sigma'_{-}(\frac{3}{2}^{+})$ 0.02	$\Sigma'_{-}(\frac{5}{2}^{+})$ 0.038	$\Sigma'_{-}(\frac{5}{2}^{+})$ 0.04

Productions

Productions

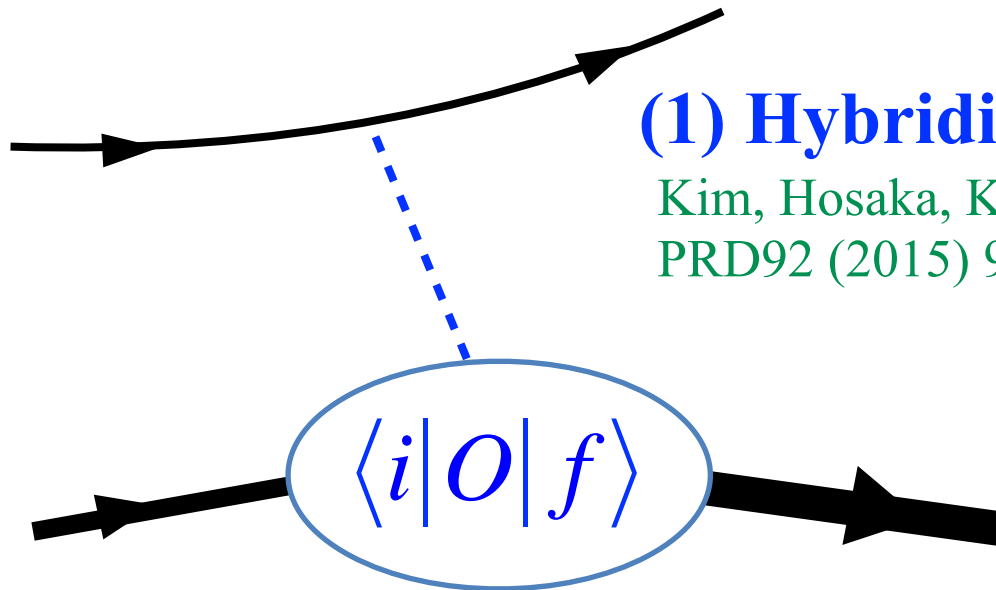
$$\pi + N \rightarrow D^* + \Lambda_c, \quad K^* + \Lambda$$



- (1) How much is charm produced?
- (2) How are they related to internal structure of Λ_c^* ?

Productions

$$\pi + N \rightarrow D^* + \Lambda_c, \quad K^* + \Lambda$$



(1) Hybridized Regge model

Kim, Hosaka, Kim, Noumi
PRD92 (2015) 9, 094021

(2) Quark model

Kim, Kim, Noumi, Shirotori, Hosaka
PTEP 2014 (2014) 10, 103D01,

(1) How much is charm produced?

(2) How are they related to internal structure of Λ_c^* ?

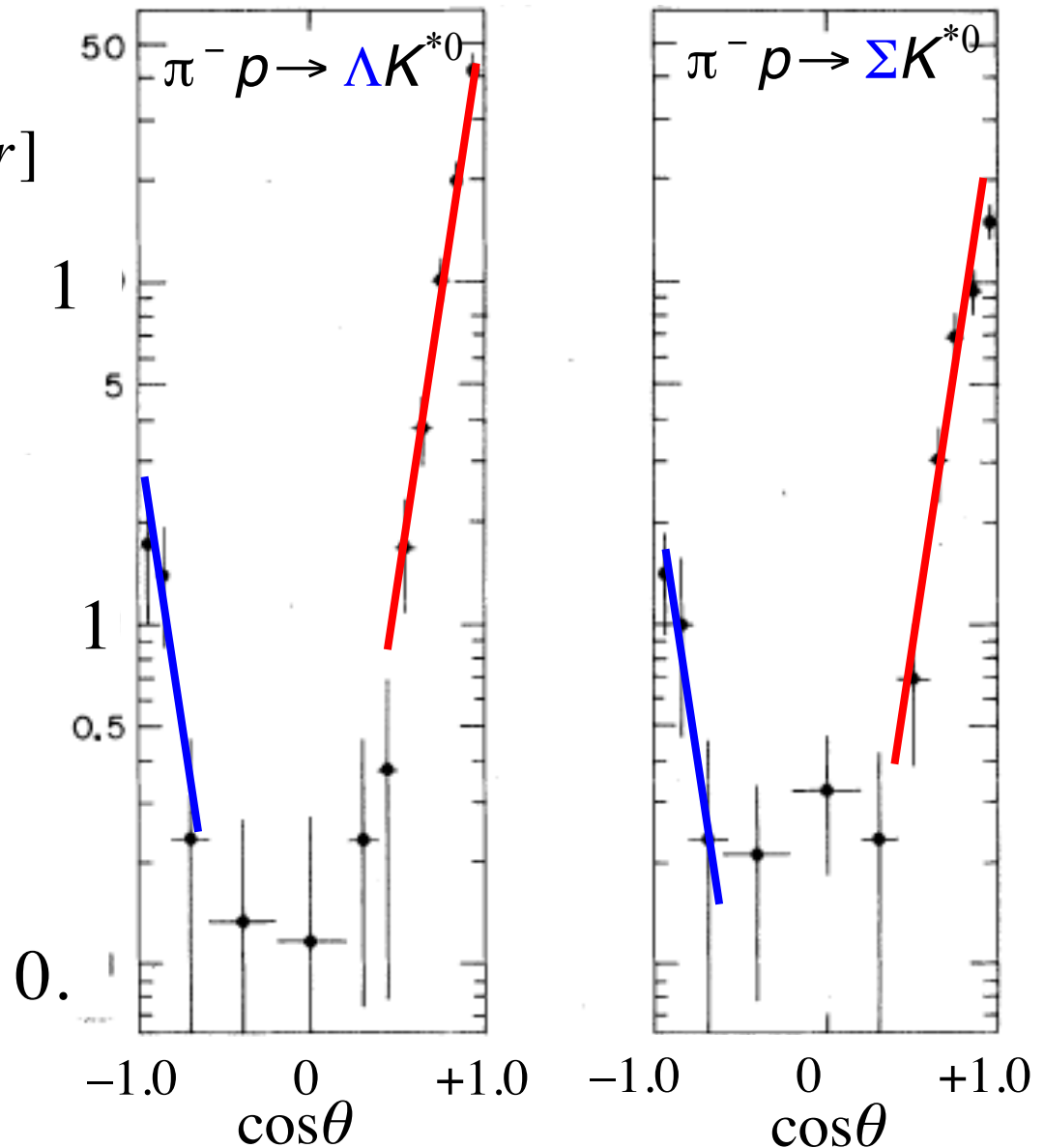
Evidence of the diffractive pattern (t-channel dynamics)

Evidence of the diffractive pattern (t-channel dynamics)

$$\frac{d\sigma}{d\Omega} [\mu b / sr]$$

$$p_{\pi, \text{Lab}} = 4.5 \text{ GeV}$$

D.J. Krennel et al
PRD6, 1220 (1972)

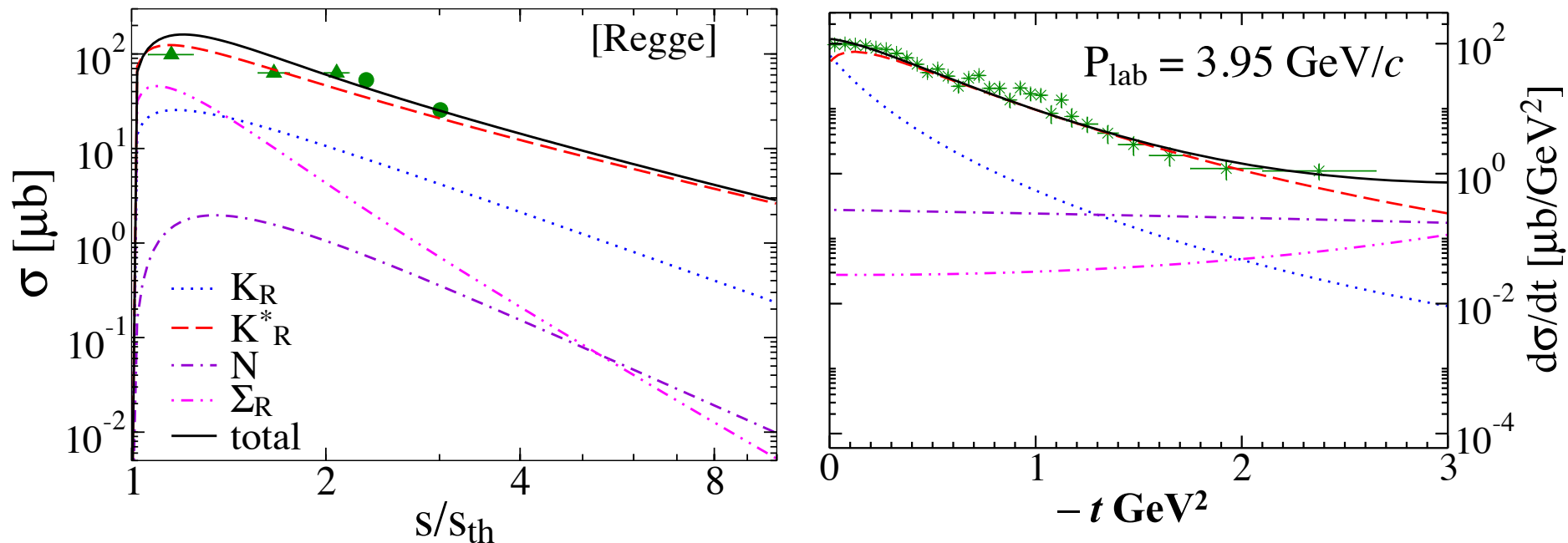


(1) How much is charm produced?

Kim, Hosaka, Kim, Noumi, PRD92 (2015) 9, 094021

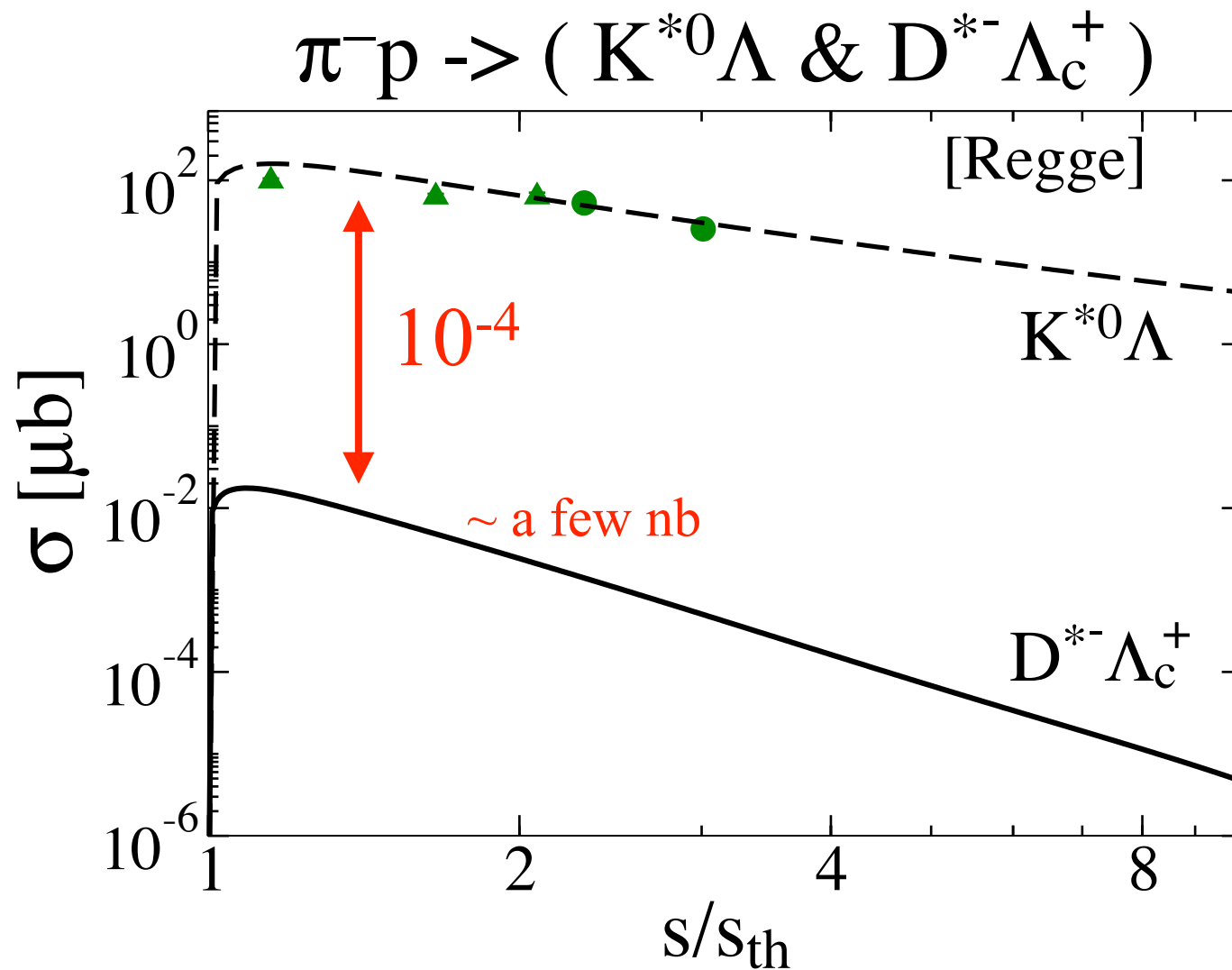
Hybridized Regge model: with effective Lagrangian for low energy

$$\pi^- + N \rightarrow K^{*0} + \Lambda$$



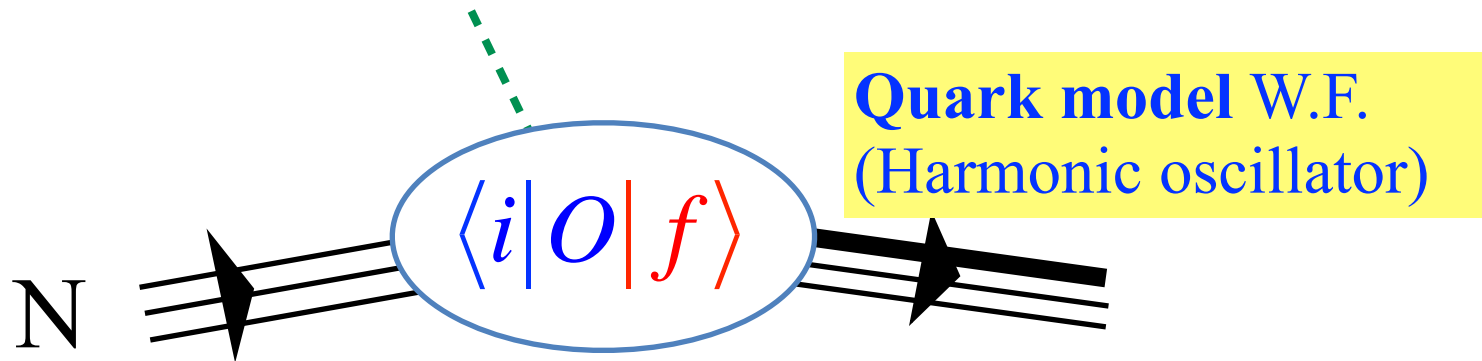
- Vector-Reggeon dominance with some pseudoscalar-Reggeon
- Both angular and energy dependences are well explained

Prediction to the charm production



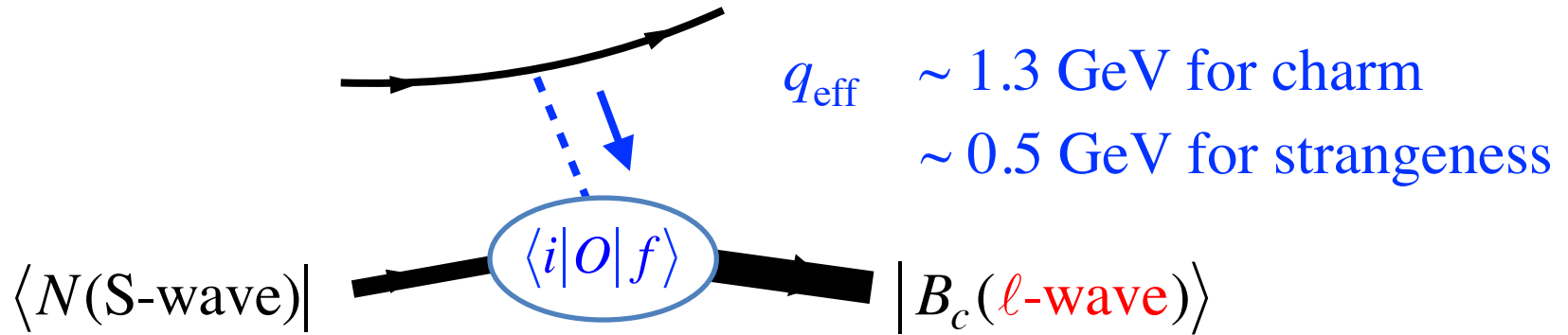
(2) How are they related to internal structure?

PTEP 2014 (2014) 10, 103D01



Various Y_s, Y_C

Λ			Λ_c^+
$\Lambda(1405)$	$\Sigma(1385)$	$\Xi(1530)$	$\Lambda_c(2595)^+$
$\Lambda(1520)$	$\Sigma(1480)$	$\Xi(1620)$	$\Lambda_c(2625)^+$
$\Lambda(1600)$	$\Sigma(1560)$	$\Xi(1690)$	$\Lambda_c(2765)^+$
$\Lambda(1670)$	$\Sigma(1580)$	$\Xi(1820)$	$\Lambda_c(2880)^+$
$\Lambda(1690)$	$\Sigma(1620)$	$\Xi(1950)$	$\Lambda_c(2940)^+$
$\Lambda(1710)$	$\Sigma(1620)$	$\Xi(2030)$	$\Sigma_c(2455)$
• • • • •			$\Sigma_c(2520)$
			$\Sigma_c(2800)$



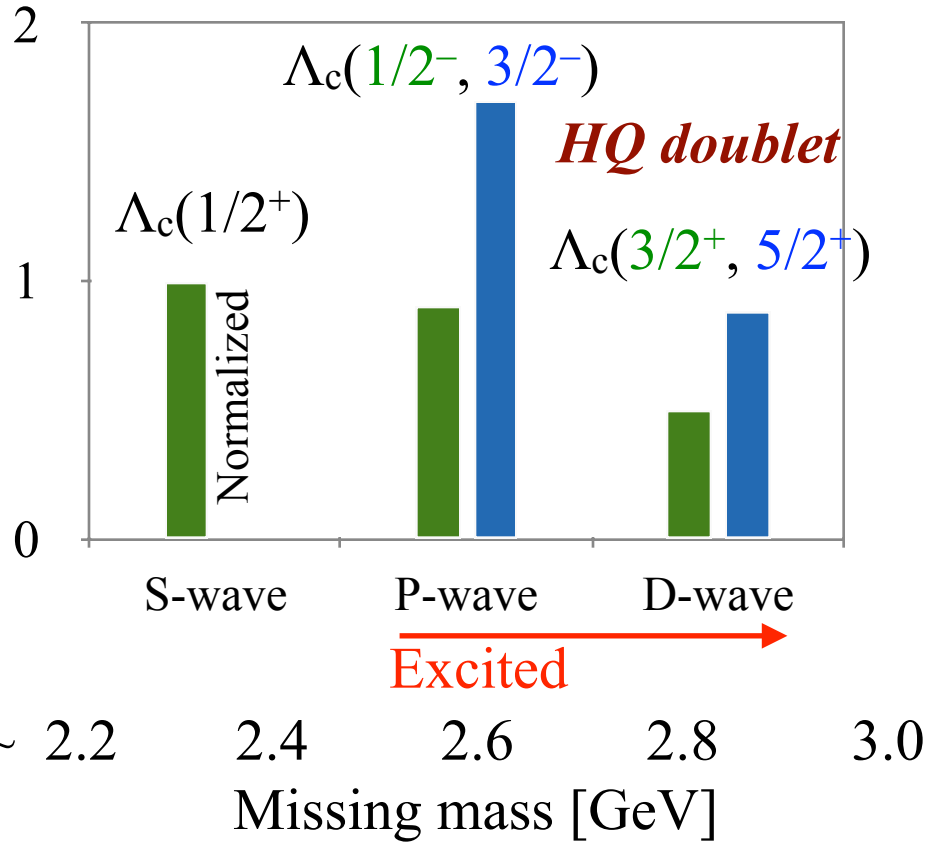
$$\langle B_c(\ell\text{-wave}) | \vec{e}_\perp \cdot \vec{\sigma} e^{i\vec{q}_{\text{eff}} \cdot \vec{x}} | N(\text{S-wave}) \rangle_{\text{radial}} \sim \left(\frac{q_{\text{eff}}}{A} \right)^\ell \times \exp \left(-\frac{q_{\text{eff}}^2}{4A^2} \right)$$

$$\ell_{\text{max}} \sim \frac{q_{\text{eff}}}{\sqrt{2}A} \sim \begin{cases} \sim 2 & \text{for charm} \\ \sim 0 & \text{for strangeness} \end{cases}$$

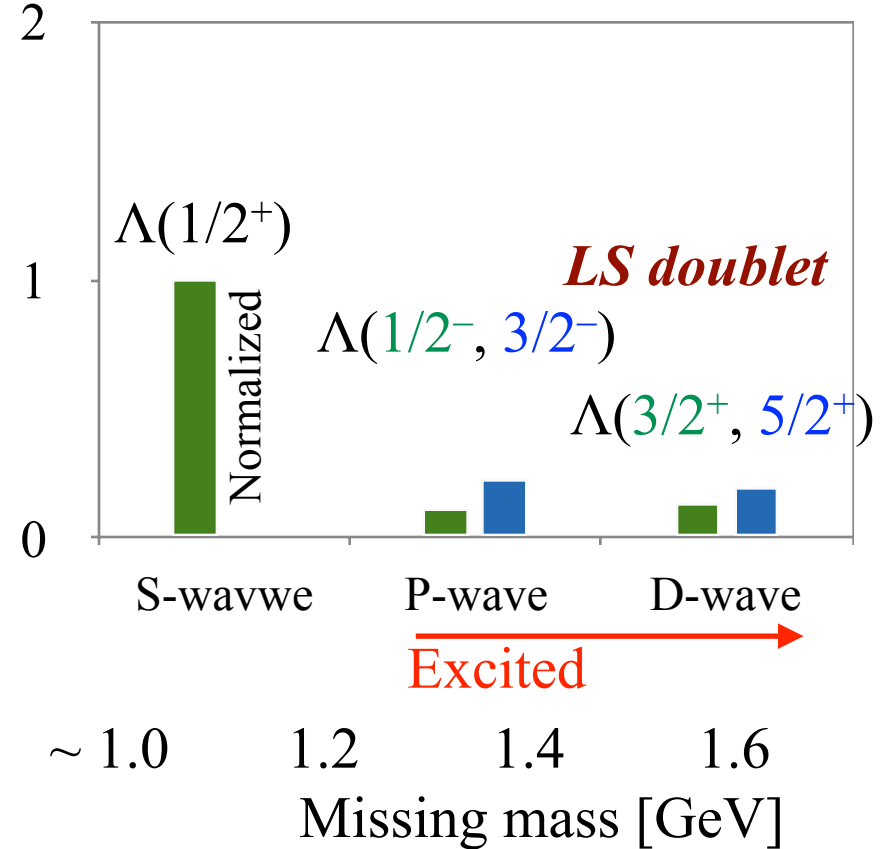
For charm: excited states are produced abundantly

Production rates (relative)

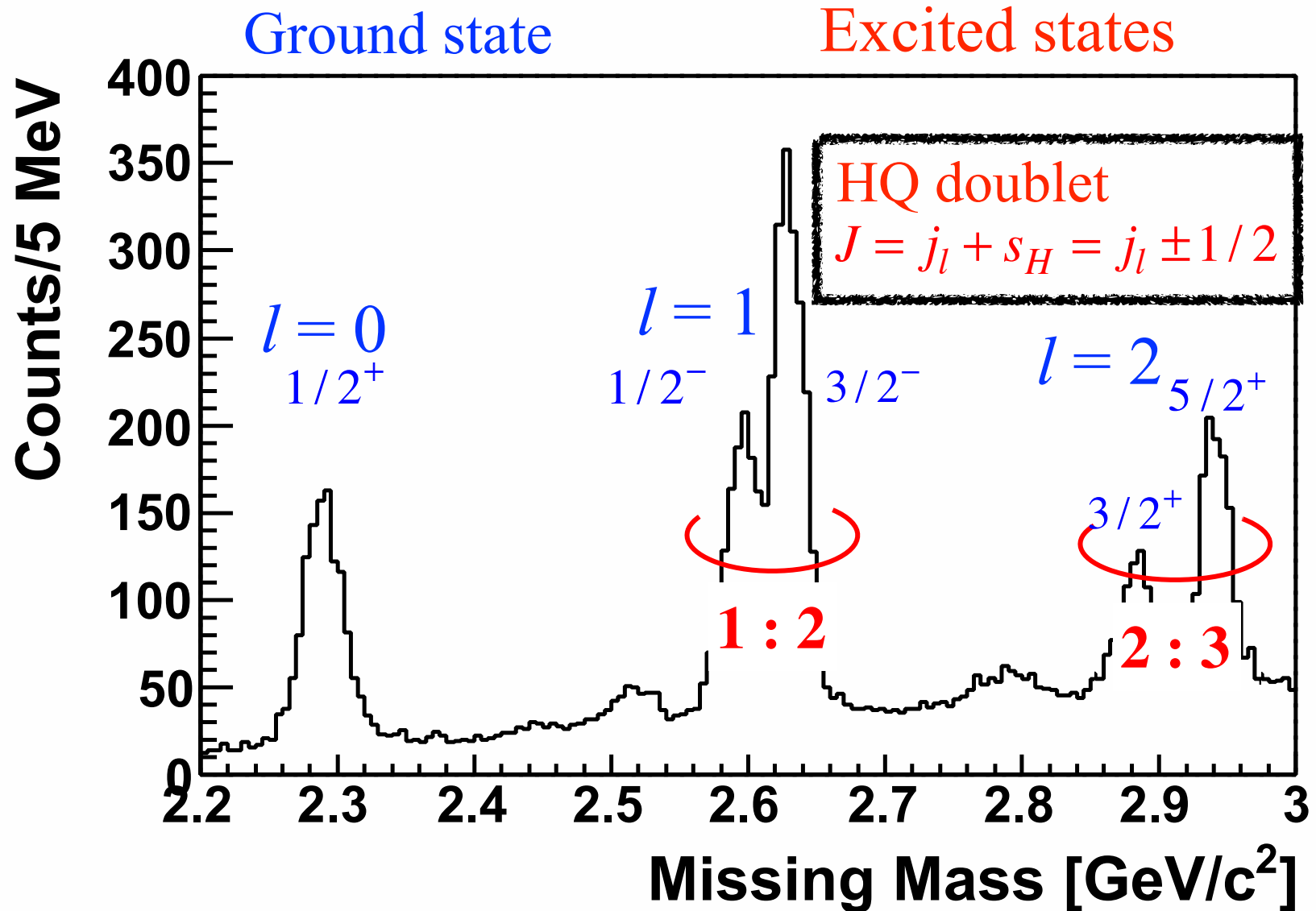
Charm



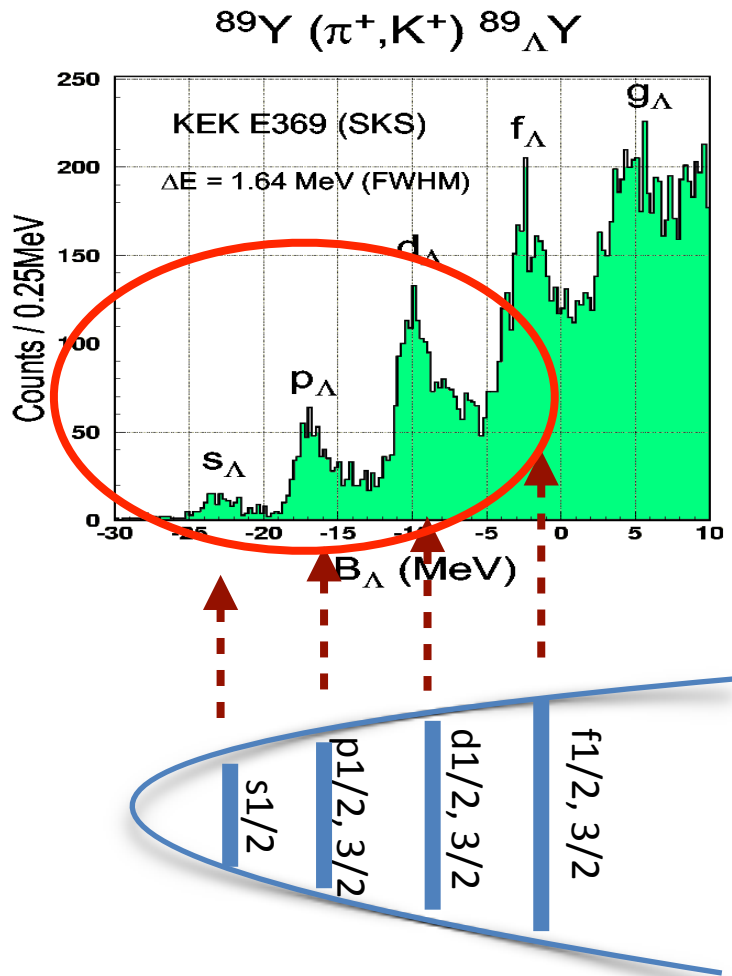
Strangeness

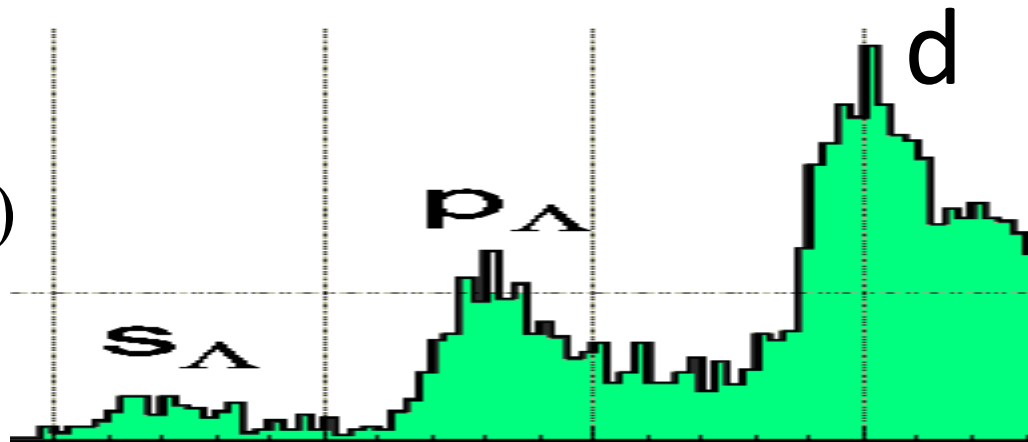
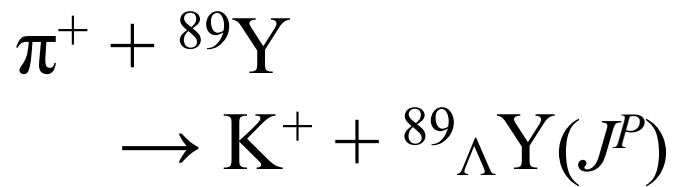
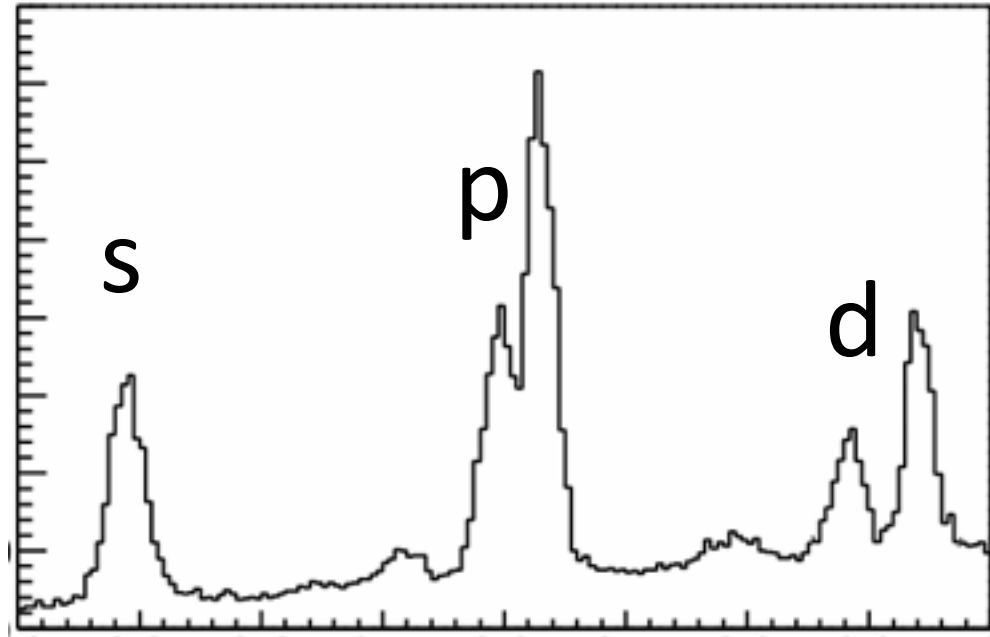
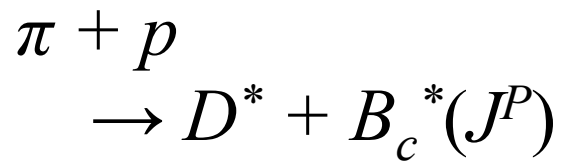


Charm production spectrum

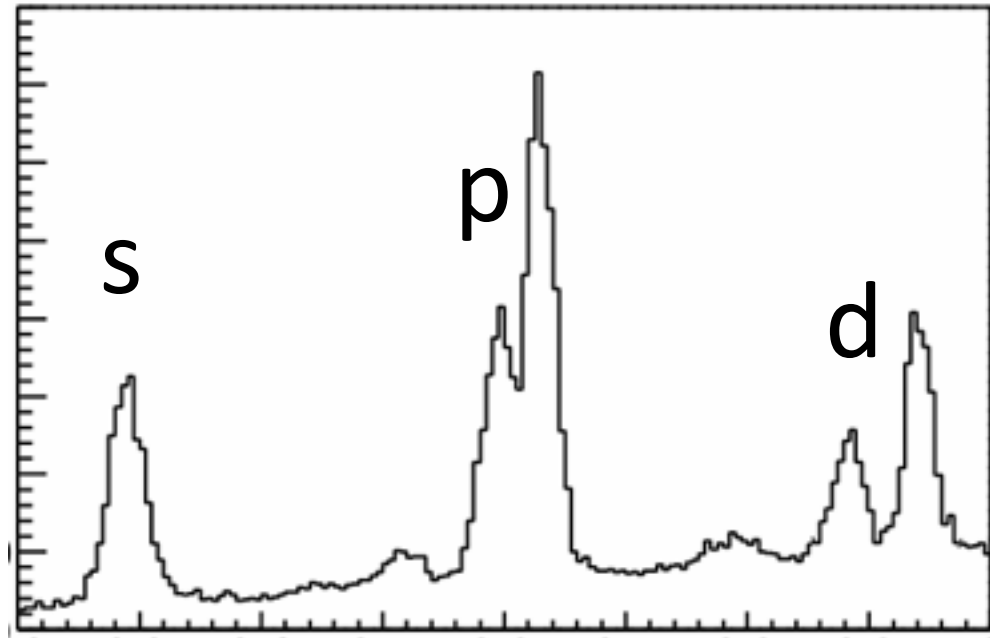


Coming back to this again

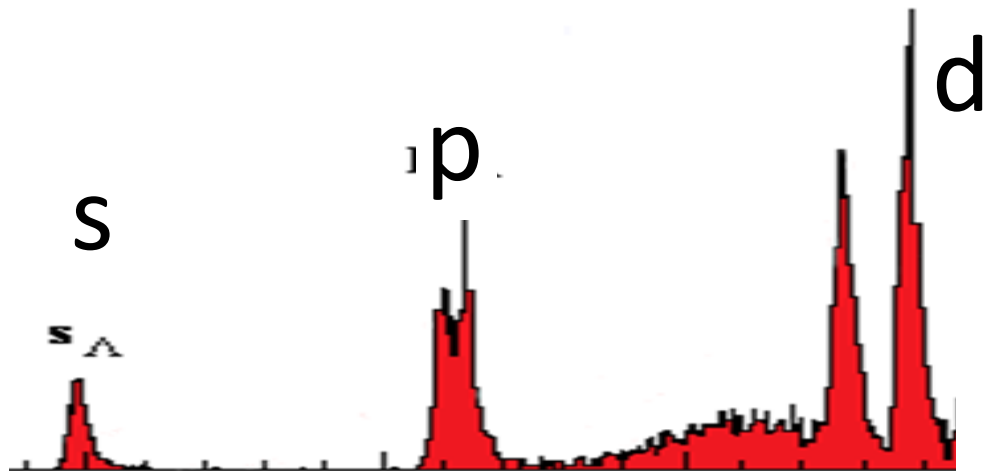




$$\pi^+ + p \rightarrow D^* + B_c^*(J^P)$$



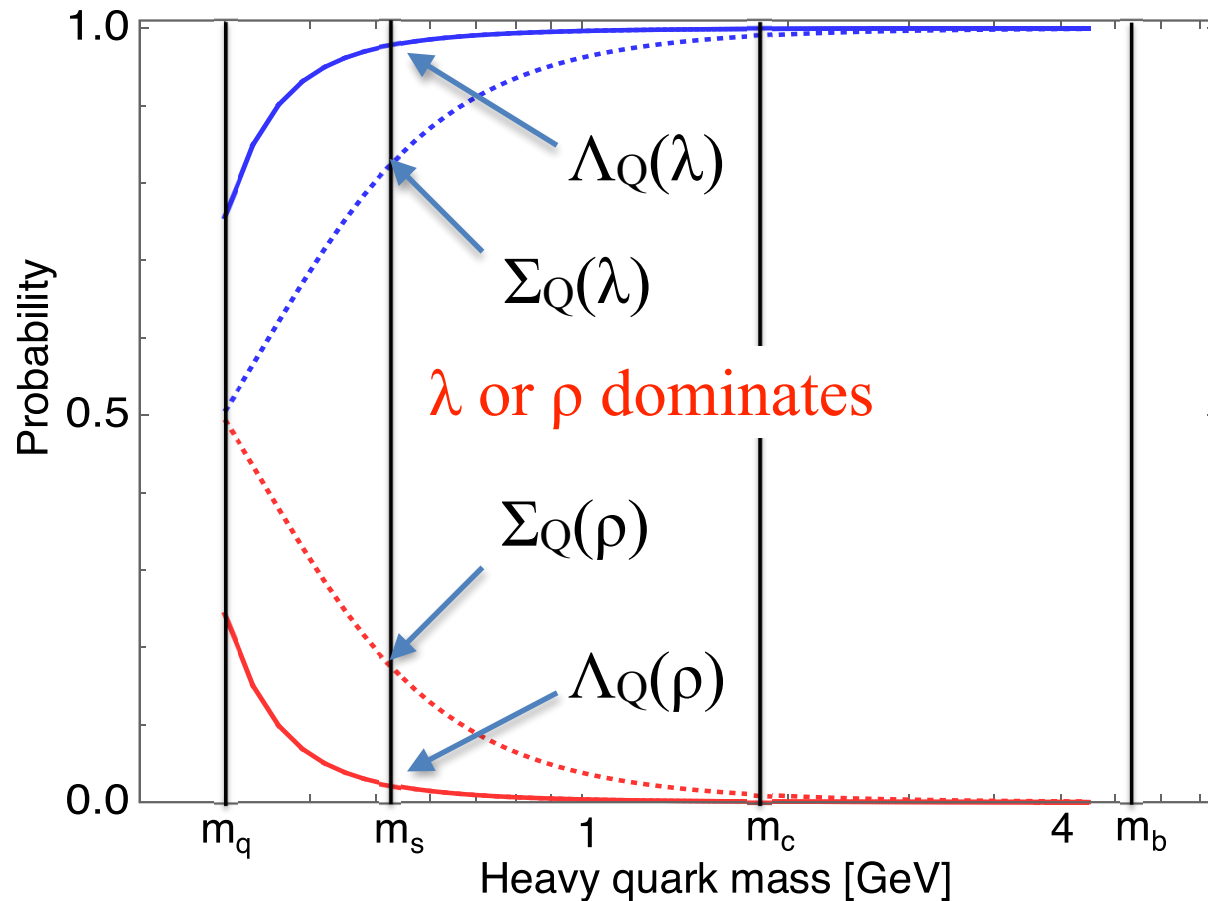
$$\pi^+ + {}^{89}\text{Y} \rightarrow \text{K}^+ + {}^{89}_{\Lambda}\text{Y}(J^P)$$



Charm quark is heavy; is strange quark so?

T. Yoshida et al, PRD 92, 114029 (2015)

Wave function mixing for the lowest $1/2^-$ Λ_c and Σ_c



Regard **s** and **c** as **heavy**