

# The prompt atmospheric neutrino flux

Rikard Enberg

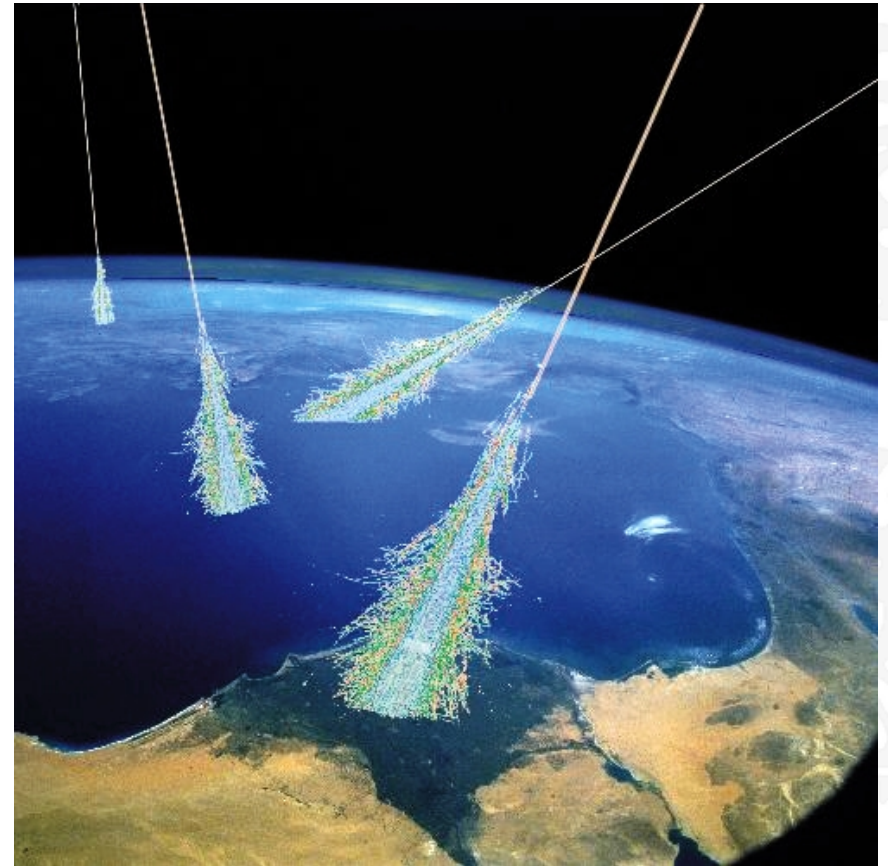
PAHEN, Naples, Sept 24, 2017



UPPSALA  
UNIVERSITET

# Atmospheric neutrinos

- Cosmic rays bombard upper atmosphere and collide with air nuclei
- Very large CMS energy  $\rightarrow$  Hadron production: pions, kaons, D-mesons ...
- Interaction & decay  $\Rightarrow$  cascade of particles
- Semileptonic decays  $\Rightarrow$  neutrino flux



*Credit: Astropic of the day, 060814*

# Conventional neutrino flux

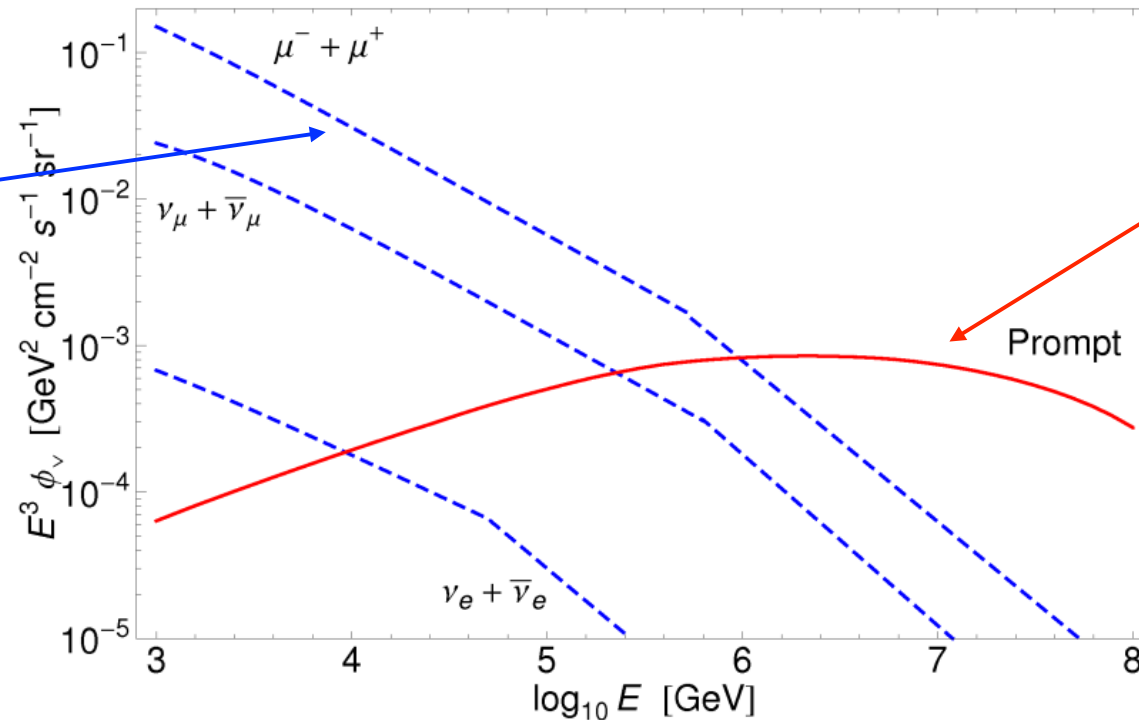
- Pions (and kaons) are produced in more or less every inelastic collision
- $\pi^+$  always decay to neutrinos:  $\text{BR}(\pi^+ \rightarrow \mu^+ \nu_\mu) = 99.98 \%$
- *But  $\pi^\pm, K^\pm$  are long-lived* ( $c\tau \sim 8$  meters for  $\pi^+$ )  
⇒ lose energy through collisions before decaying  
⇒ neutrino energies are degraded
- This is called the *conventional neutrino flux*

# Prompt neutrino flux

- Hadrons containing heavy quarks (*charm or bottom*) are **extremely short-lived**:
  - ⇒ decay before losing energy
  - ⇒ harder neutrino energy spectrum
- However, production cross-section is much smaller
- There is a cross-over energy above which prompt neutrinos dominate over the conventional flux
- This is called the *prompt neutrino flux*

# Prompt vs conventional fluxes of atmospheric neutrinos

Pions & kaons:  
long-lived  
⇒ lose energy before decay



Charmed mesons:  
short-lived  
⇒ don't lose energy  
⇒ harder spectrum

Prompt flux: Enberg, Reno, Sarcevic, arXiv:0806.0418 (**ERS**)

Conventional: Gaisser & Honda, Ann. Rev. Nucl. Part. Sci. **52**, 153 (2002)

# Why are we interested?

- Atmospheric neutrinos are a background to extragalactic neutrinos
- Test beam for neutrino experiments
- Learn about cascades and the underlying production mechanism
- Higher energy pp collisions than in LHC: can maybe even learn something about QCD?

# Calculations of the prompt flux

## Recent:

A. Bhattacharya, RE, M.H. Reno, I. Sarcevic, A. Stasto, [arXiv:1502.01076](#) (**BERSS**)

M.V. Garzelli, S. Moch, G. Sigl, [arXiv:1507.01570](#) (**GMS**)

R. Gauld, J. Rojo, L. Rottoli, S. Sarkar, J. Talbert, [arXiv:1511.06346](#) (**GRRST**)

A. Bhattacharya, RE, Y.S. Jeong, C.S. Kim, M.H. Reno, I. Sarcevic, A. Stasto, [arXiv:1607.00193](#) (**BEJKRSS**)

PROSA Collaboration (Garzelli et al), [arXiv:1611.03815](#)

M. Benzke, M. V. Garzelli, *et al.*, [arXiv:1705.10386](#)

## Older but widely used:

M. Thunman, G. Ingelman, P. Gondolo, [hep-ph/9505417](#)

L. Pasquali, M.H. Reno, I. Sarcevic, [hep-ph/9806428](#)

A.D. Martin, M.G. Ryskin, A. Stasto, [hep-ph/0302140](#) (**MRS**)

RE, M.H. Reno, I. Sarcevic, [arXiv:0806.0418](#) [hep-ph] (**ERS**)



# Calculations of the prompt flux

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Compare with

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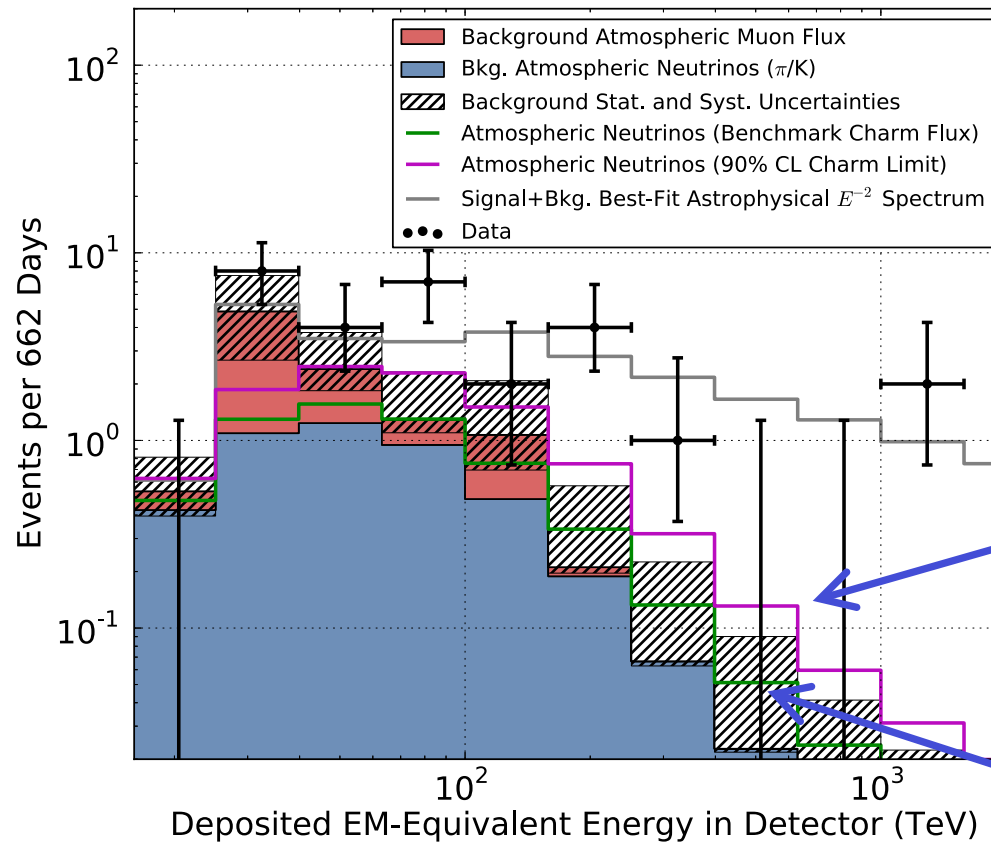
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# The IceCube events

The significance is sensitive to the prompt flux prediction

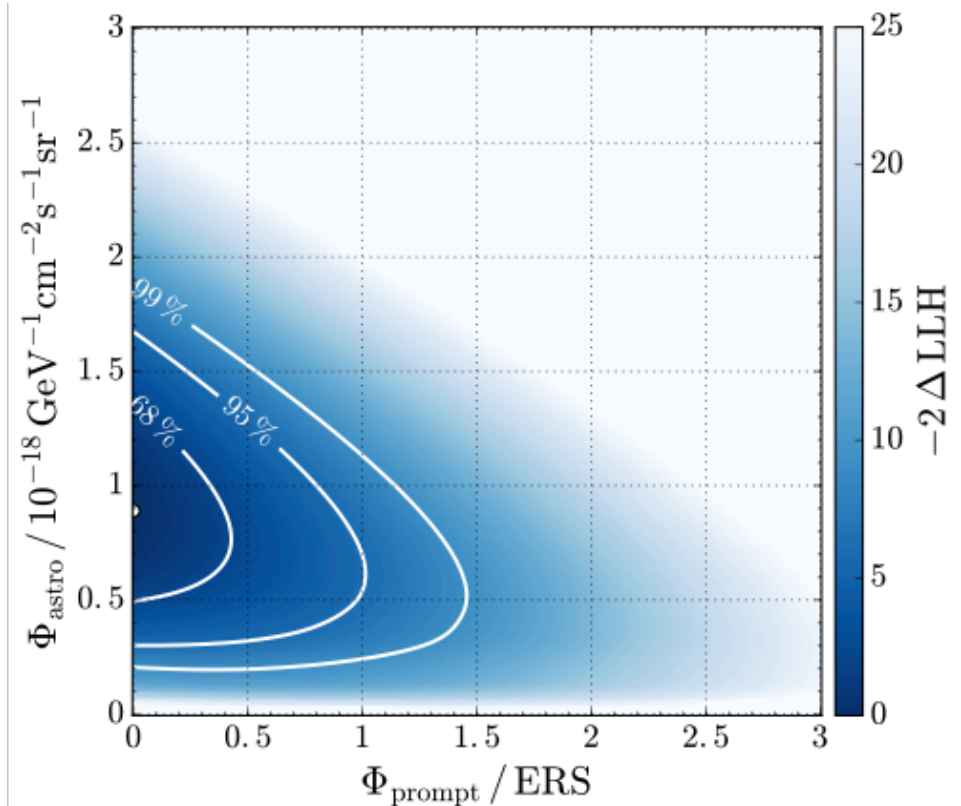
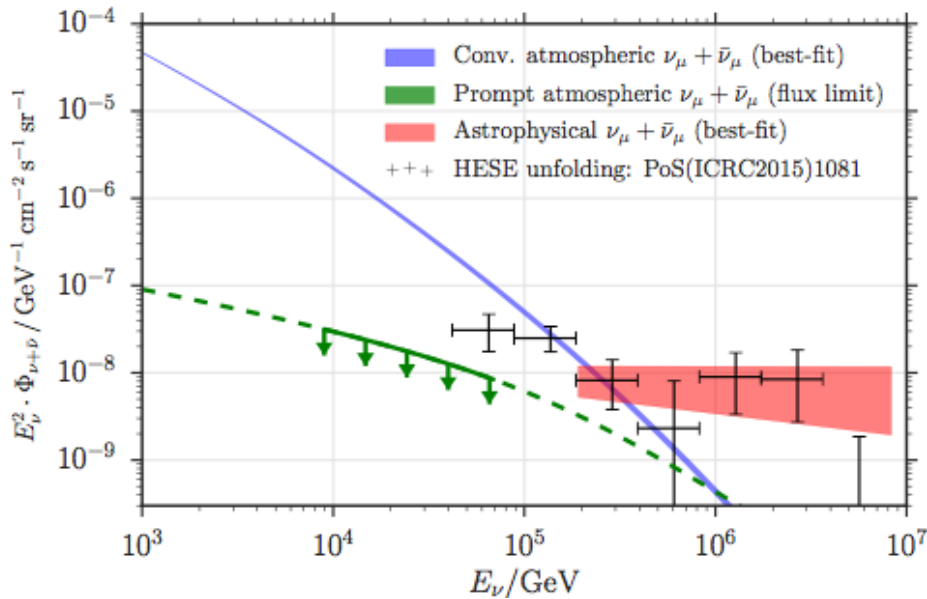


Prompt flux (limit)

Prompt flux (ERS calc)

IceCube, arXiv:1311.5238

# IceCube are using ERS



The shape of the ERS flux is used with overall normalization a free parameter

M.G. Aartsen et al., arXiv:1607.08006

# Important message

QCD is crucial for some astrophysical processes:

- Atmospheric neutrinos
- Neutrino-nucleon cross-section @ high energy
- (Interactions in astrophysical sources?)

For example:

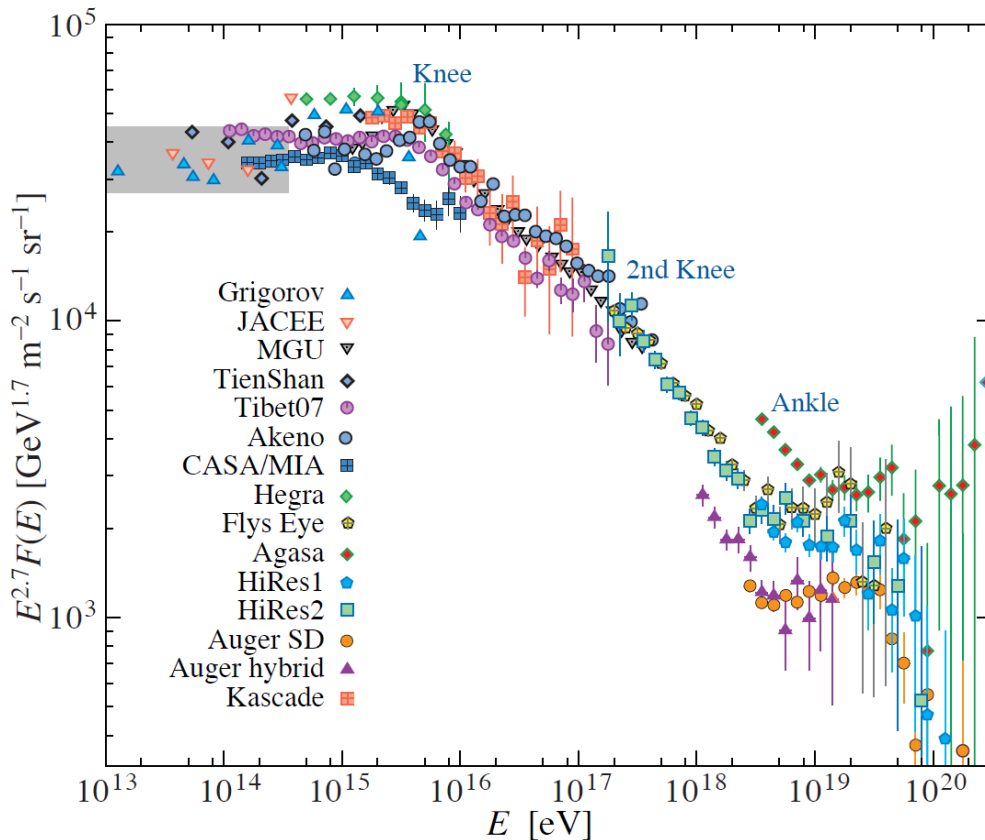
- What happens at small Bjorken- $x$ ? (Need very small  $x$ )
- Forward region (Hard to measure at colliders)
- Fragmentation of quarks  $\rightarrow$  hadrons
- Nuclear effects in pA hard interactions

# The calculation has many ingredients

- *Incident cosmic ray flux*
- Atmospheric density
- *Cross section for heavy quarks in pp/pA collisions at extremely high energy (perturbative QCD)*
- Rescattering of nucleons, hadrons (hadronic xsecs) (scattering lengths)
- Decay spectra of charmed mesons & baryons (decay lengths)
- Cascade equations and their solution (Semi-analytic: spectrum-weighted Z-moments)

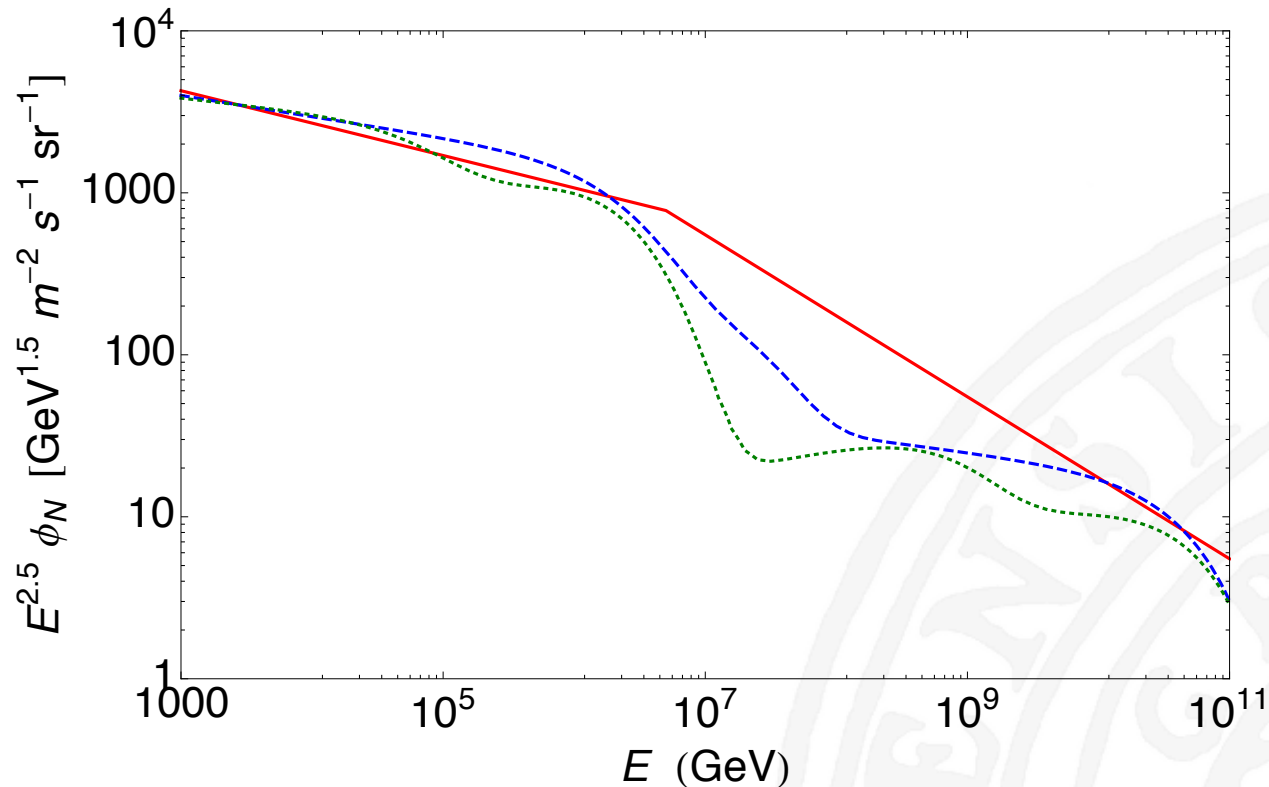
# Cosmic rays (CR)

Plot from Particle Data Group



- Knees and ankles → seems natural to associate different sources with different energy ranges of the CR flux
- Highest energies: Extragalactic origin? → GRBs, AGNs, or more exotic
- Lower energies: Galactic origin? → SNRs etc

# Incident cosmic ray flux: nucleons



Solid red = Broken power law (old standard)  
Dashed blue = Gaisser all proton (H3p)  
Dotted green = Gaisser, Stanev, Tilav (GST4)

# Calculating the neutrino flux

- To find the neutrino flux we must **either solve a set of cascade equations** given an incoming CR flux:

$$\frac{d\phi_N}{dX} = -\frac{\phi_N}{\lambda_N} + S(NA \rightarrow NY)$$

$$\frac{d\phi_M}{dX} = S(NA \rightarrow MY) - \frac{\phi_M}{\rho d_M(E)} - \frac{\phi_M}{\lambda_M} + S(MA \rightarrow MY)$$

$$\frac{d\phi_\ell}{dX} = \sum_M S(M \rightarrow \ell Y)$$

- $X$  is the slant depth: “amount of atmosphere”
  - $\rho d_M$  is the decay length, with  $\rho$  the density of air
  - $\lambda_M$  is the interaction length for hadronic energy loss
- Here: semi-analytic solution (e.g. **MCEq** does it numerically)
- ... or **Monte Carlo simulate** the cascade (e.g. **SIBYLL**)



# Particle production

Particle physics inputs: energy distributions

$$\frac{dn(k \rightarrow j; E_k, E_j)}{dE_j} = \frac{1}{\sigma_{kA}(E_k)} \frac{d\sigma(kA \rightarrow jY, E_k, E_j)}{dE_j}$$
$$\frac{dn(k \rightarrow j; E_k, E_j)}{dE_j} = \frac{1}{\Gamma_k} \frac{d\Gamma(k \rightarrow jY; E_j)}{dE_j}$$

along with interaction lengths, or cooling lengths

$$\lambda_N(E) = \frac{\rho(h)}{\sigma_{NA}(E) n_A(h)}$$

→ Need the charm production cross section  $d\sigma/dx_F$

# Problem with QCD in this process

Charm cross section in LO QCD:

$$\frac{d\sigma_{\text{LO}}}{dx_F} = \int \frac{dM_{c\bar{c}}^2}{(x_1 + x_2)s} \sigma_{gg \rightarrow c\bar{c}}(\hat{s}) G(x_1, \mu^2) G(x_2, \mu^2)$$

where

$$x_{1,2} = \frac{1}{2} \left( \sqrt{x_F^2 + \frac{4M_{c\bar{c}}^2}{s}} \pm x_F \right)$$

CMS energy is large:  $s = 2E_p m_p$  so  $x_1 \sim x_F$   $x_2 \ll 1$

$x_F=1:$	$E=10^5 \rightarrow x \sim 4 \cdot 10^{-5}$	$x_F=0:$	$E=10^5 \rightarrow x \sim 6 \cdot 10^{-3}$
	$E=10^6 \rightarrow x \sim 4 \cdot 10^{-6}$		$E=10^6 \rightarrow x \sim 2 \cdot 10^{-3}$
	$E=10^7 \rightarrow x \sim 4 \cdot 10^{-7}$		$E=10^7 \rightarrow x \sim 6 \cdot 10^{-4}$

Very small  $x$  is needed for forward processes (large  $x_F$ )!

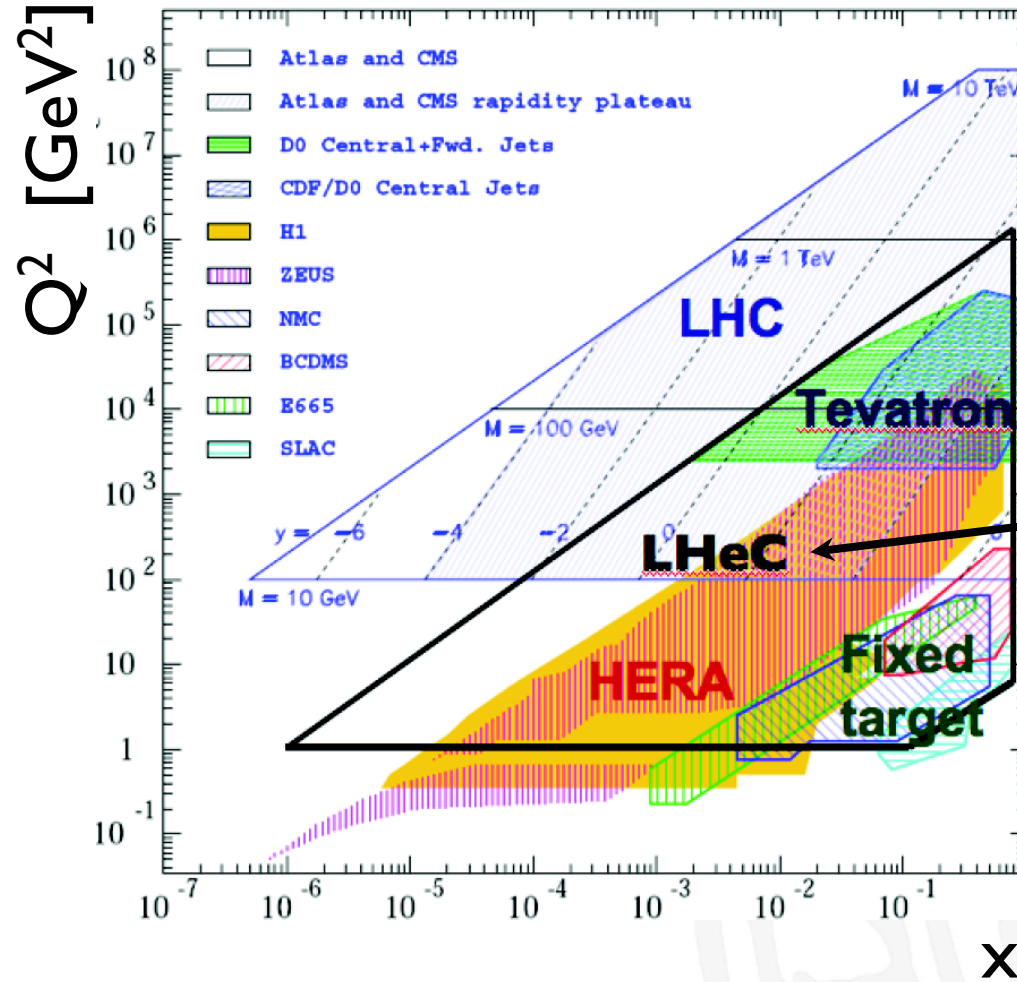
# Problem with QCD at small $x$

- Parton distribution functions poorly known at small  $x$
- At small  $x$ , must resum large logs:  $\alpha_s \ln(1/x)$
- If logs are resummed (**BFKL**):  
power growth  $\sim x^{-\lambda}$  of gluon distribution as  $x \rightarrow 0$
- Unitarity would be violated (T-matrix  $> 1$ )

# How small $x$ do we know?

- We haven't measured anything at such small  $x$
- E.g. the MSTW pdf has  $x_{\min} = 10^{-6}$
- **But that is an extrapolation!**
- HERA pdf fits:  $Q^2 > 3.5 \text{ GeV}^2$  and  $x > 10^{-4}$  !
- See Gao, Harland-Lang, Rojo, [arXiv:1709.04922](https://arxiv.org/abs/1709.04922) for more on pdfs

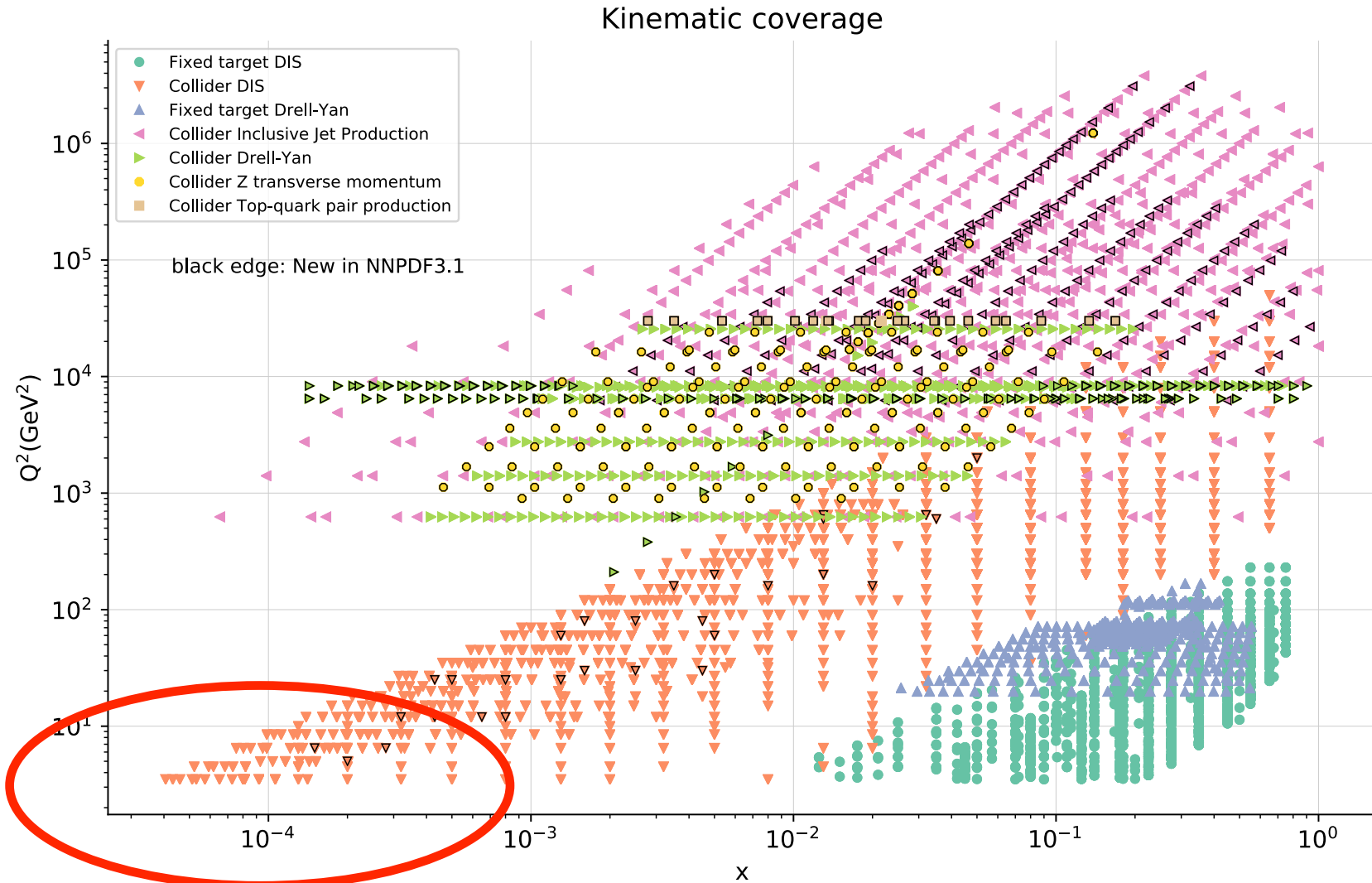
# Kinematic plane



Note LHeC!

HERA:  $x_{\min} \sim 10^{-4}$  used for PDF fits ( $Q^2 \sim 3.5 \text{ GeV}^2$ )

# Kinematic plane of NNPDF3.1



R.D. Ball et al, arXiv:1706.00428

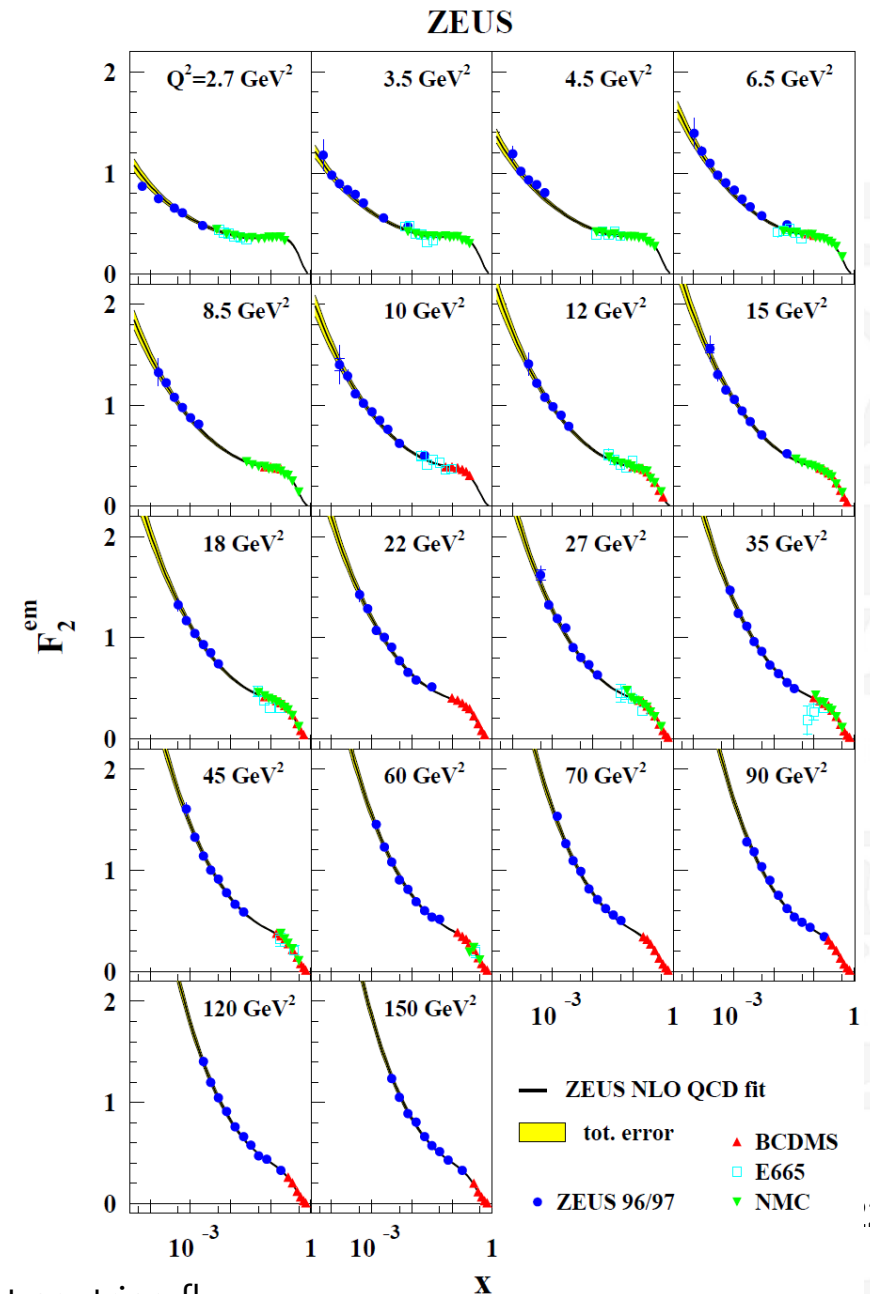
# Small x

$F_2$  measured at HERA (ZEUS)  
as a function of Bjorken- $x$ .

Note the steep power-law rise

Can this rise continue?

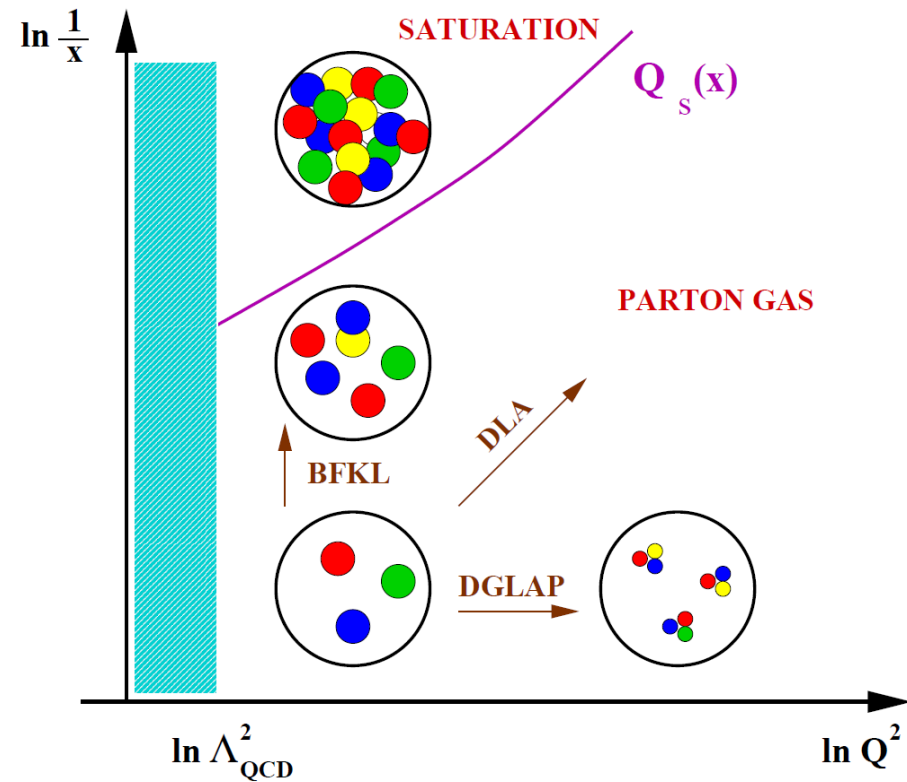
Theoretical answer: no





# Parton saturation

- **Saturation** to the rescue:
  - Number of gluons in the nucleon becomes so large that gluons recombine
  - Reduction in the growth



- This is sometimes called the **color glass condensate**
- Non-linear QCD evolution: **Balitsky-Kovchegov equation**

# Bhattacharya et al (BEJKRSS, 2016): Redo QCD calculations in 3 ways

- *Standard NLO QCD with newest PDFs*
  - BERSS updated with RHIC/LHCb input, uses Nason, Dawson, Ellis and Mangano, Nason, Ridolfi
- *Dipole picture with saturation*
  - Approximate solution of Balitsky-Kovchegov equation
  - Update of ERS calc with new HERA fits + other dipoles
- *kT factorization with and without saturation*
  - Resums large logs,  $\alpha_s \log(1/x)$  with BFKL
  - Off-shell gluons, unintegrated PDFs (+ subleading...)
  - Kutak, Kwiecinski, Martin, Sapeta, Stasto (permutations)

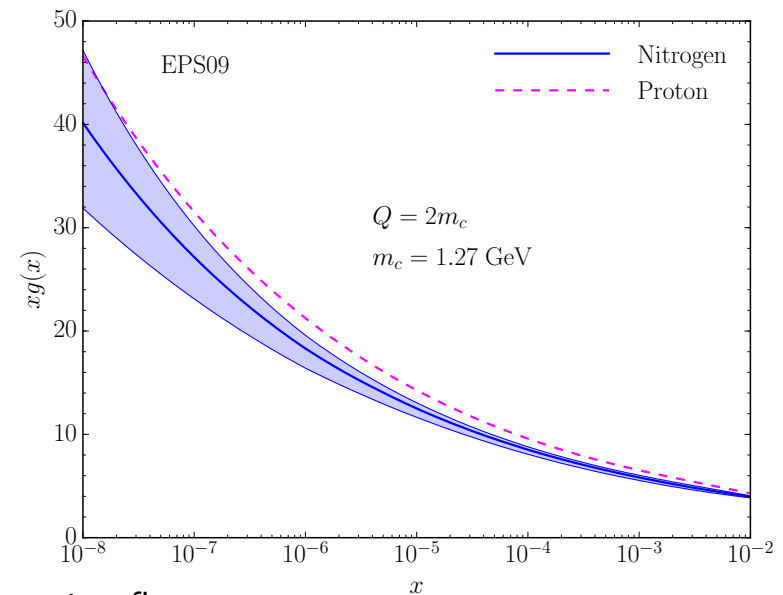
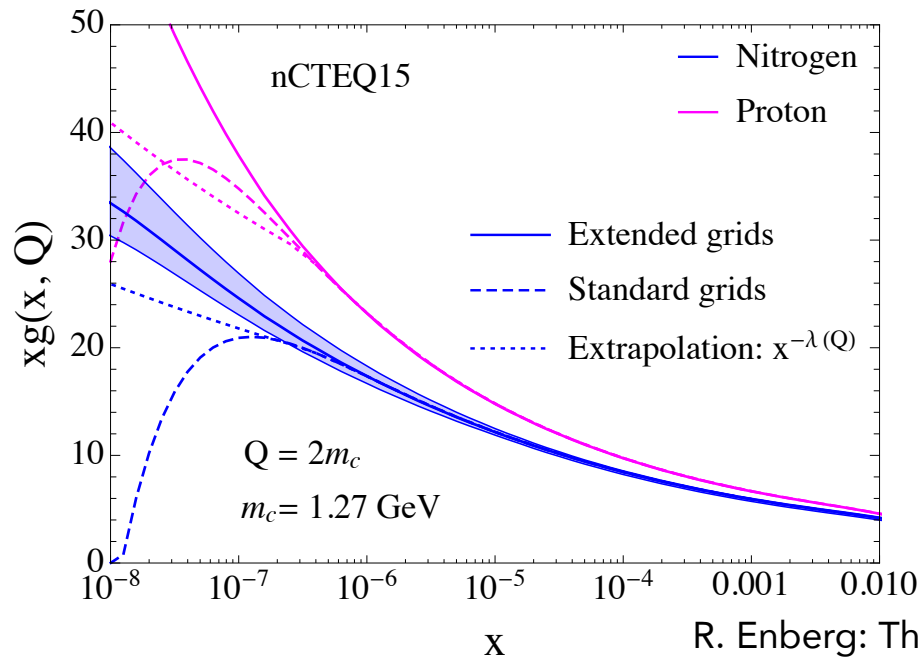
**Include scale variations, PDF errors, charm mass, etc**  
**→ Plausible upper and lower limits on xsec**

# Also include nuclear shadowing

Partons are not in a free nucleon, but in a nucleus!

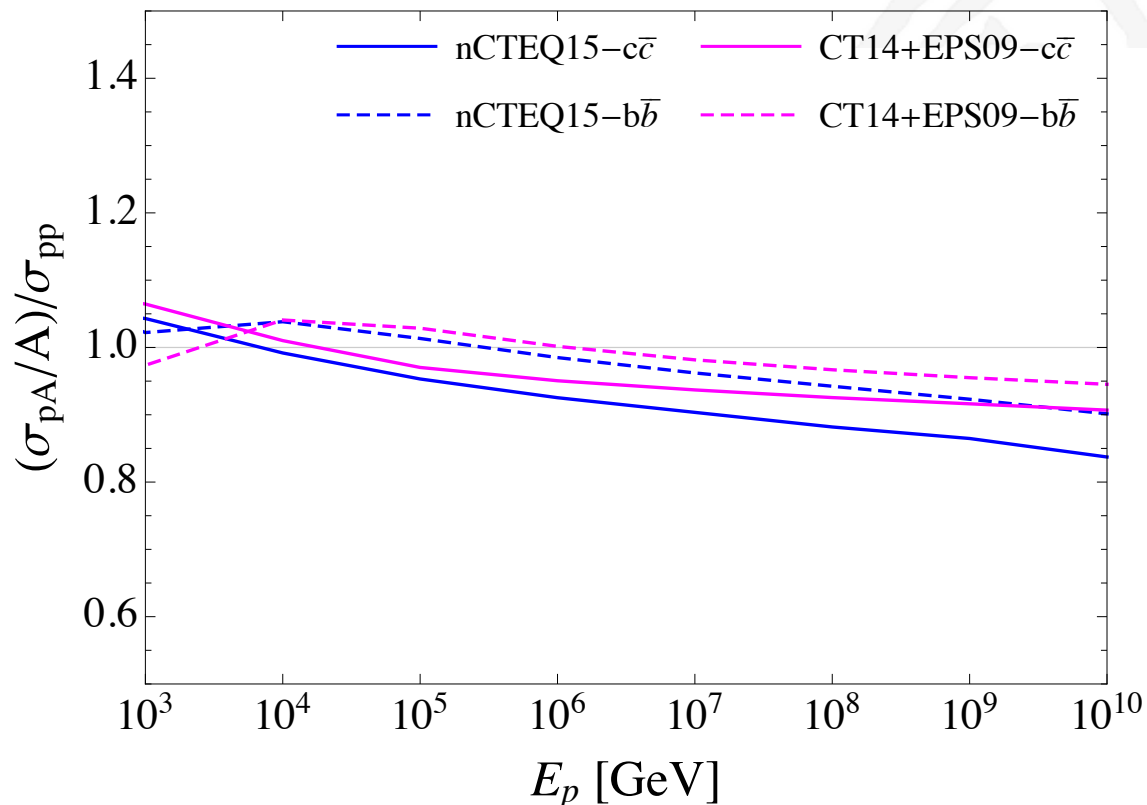
To estimate shadowing, we use PDFs:

- Eskola, Paukkunen, Salgado (EPS) for  $^{16}\text{O}$
- nCTEQ15 for  $^{14}\text{N}$
- CT14 for free protons

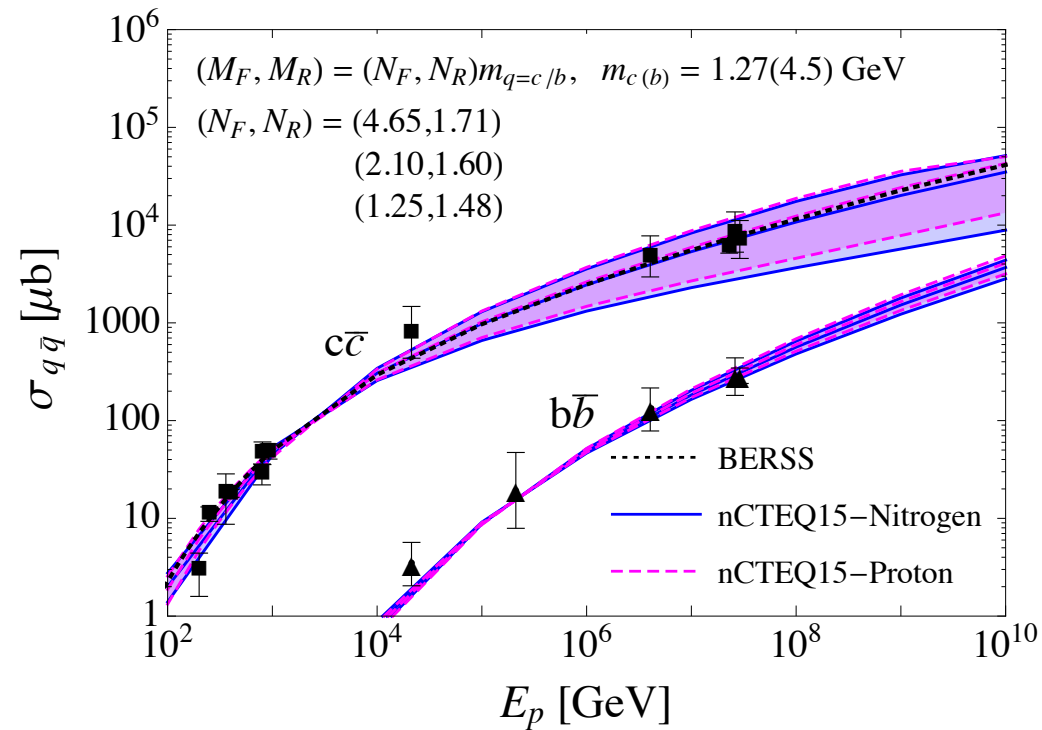
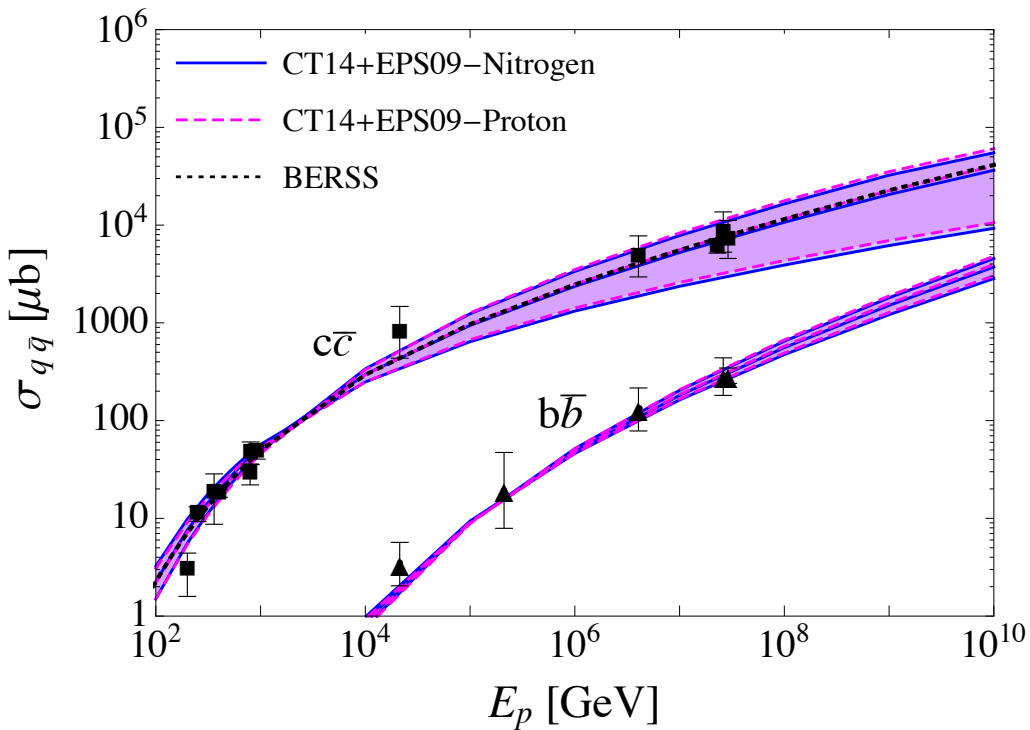


# Nuclear effects

- Nuclear shadowing reduces flux by 10–30% at the highest energies
- Effect is larger on the flux than on the total  $\sigma(cc)$  due to asymmetric  $x_{1,2}$



# $\sigma(cc)$ and $\sigma(bb)$



Data from RHIC, LHC and lower energies  
 Total cross sections well described by all calculations  
 (at high energies), nuclear shadowing small

(Error bands=scale variations and PDF uncertainties)

# Differential cross sections (LHCb)

LHCb measured D-meson production at 7 and 13 TeV

Kinematical range:  $p_T < 8 \text{ GeV}$ ,  $0 < y < 4.5$

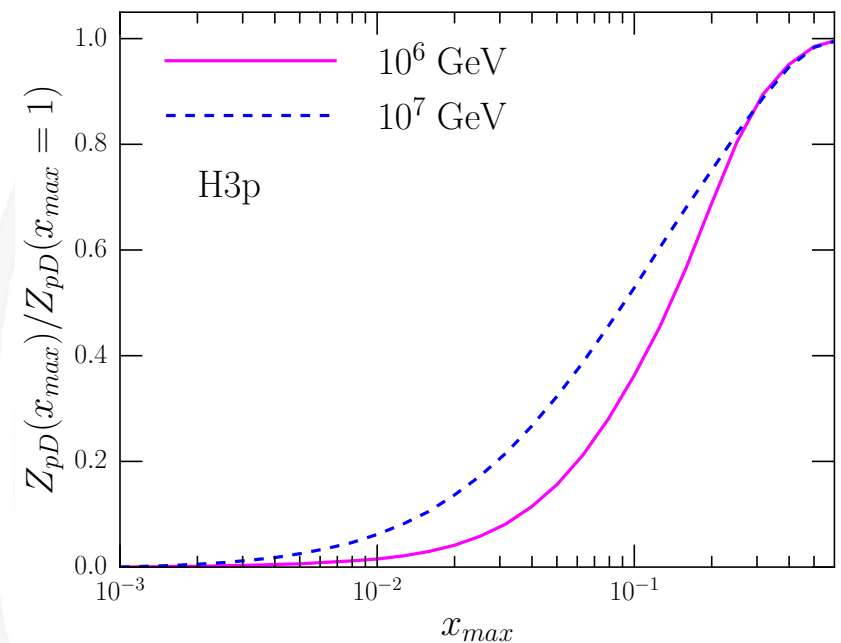
The flux is mostly sensitive to *large  $y$  and small  $p_T$* .

Cumulative fraction of Z-moment  
as function of  $x_F$ :

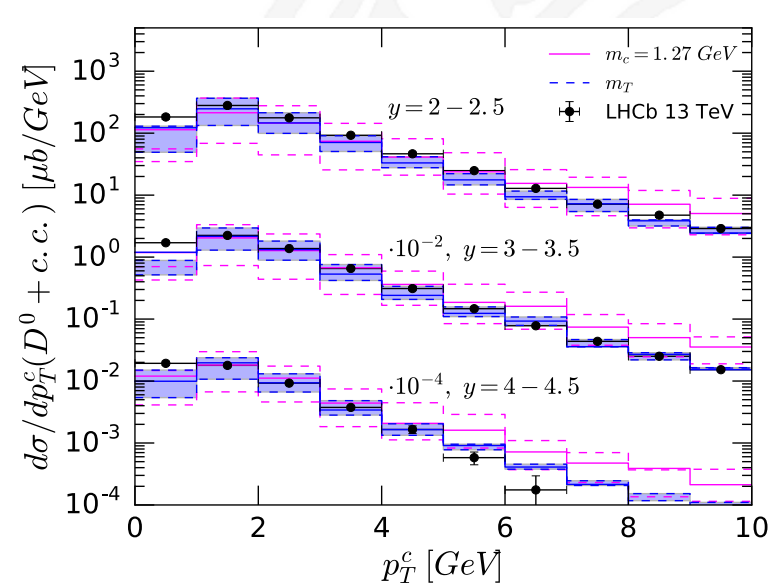
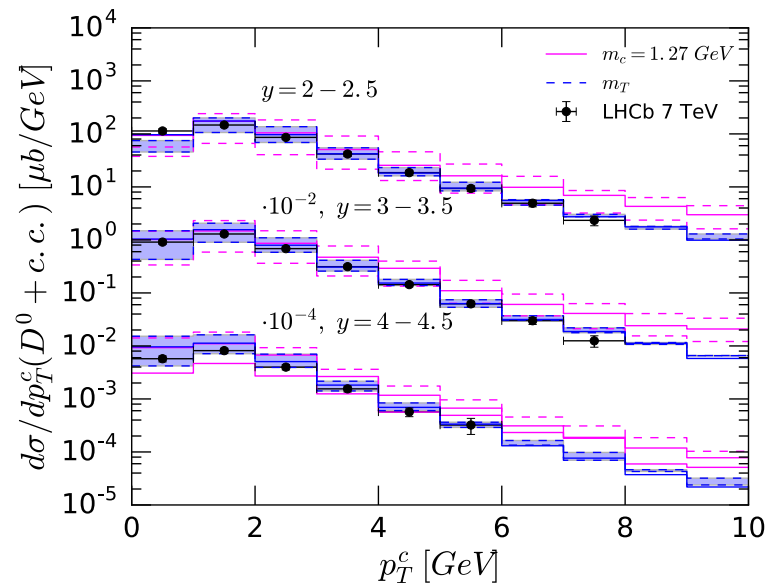
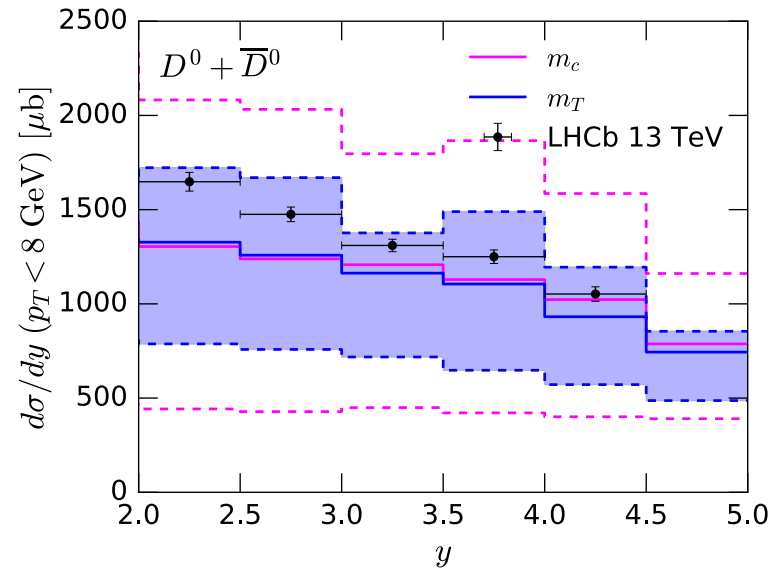
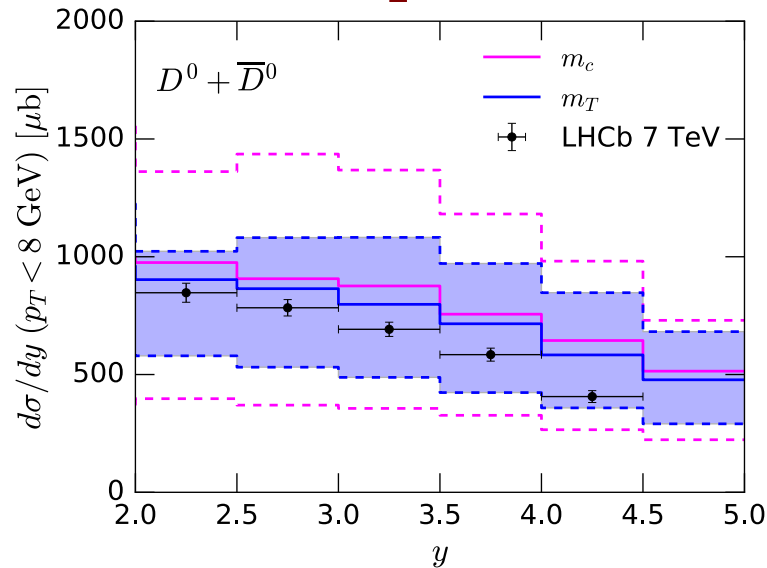
**Estimate:** 90% of  $Z_{pD}$  given by

$y > 4.9$  for  $E_p = 10^6 \text{ TeV}$

$y > 5.7$  for  $E_p = 10^7 \text{ TeV}$



# Comparison of NLO QCD



Data from LHCb: arXiv:1302.2864 and arXiv:1510.01707



# Prompt $\nu_\mu (= \nu_e = \mu)$ fluxes

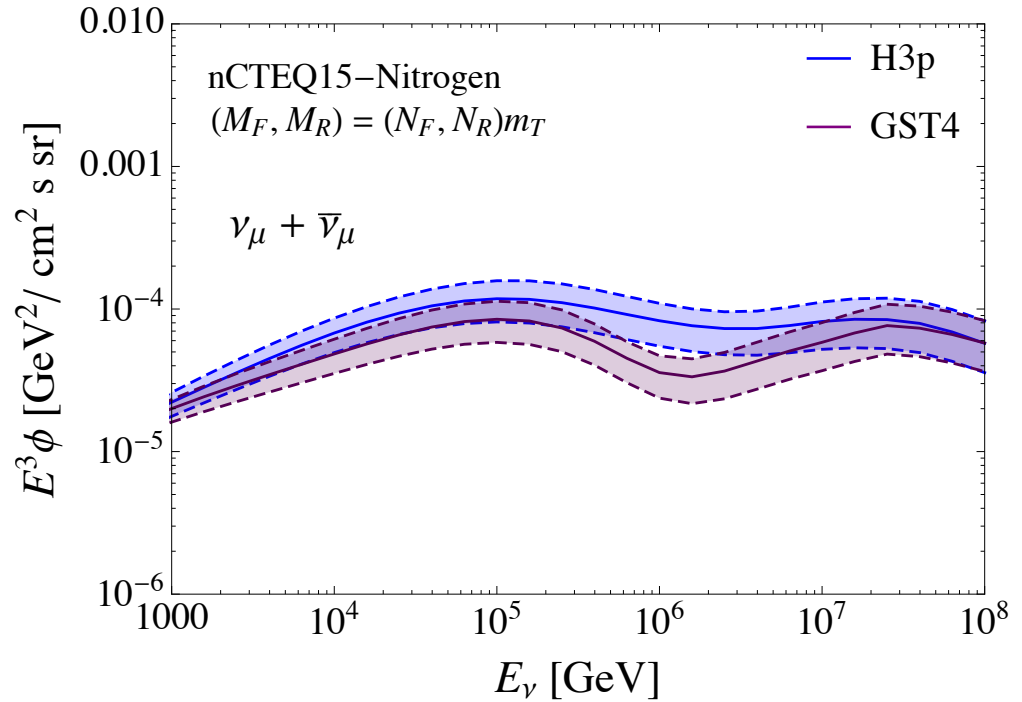
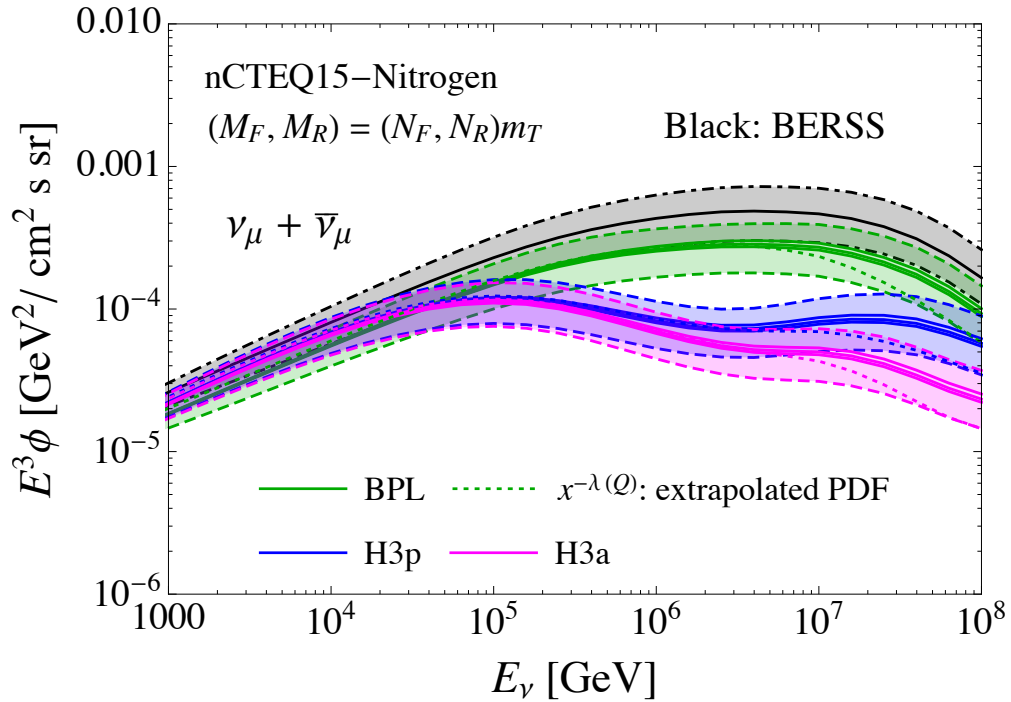
We have calculated prompt neutrino fluxes using all these variations in QCD, nuclear effects, cosmic ray fluxes.

Also compare to other calculations:

- RE, Reno, Sarcevic (ERS) [0806.0418](#)
- Bhattacharya et al (BERSS), [1502.01076](#)
- Garzelli, Moch, Sigl, [1506.08025](#)
- Gauld, Rojo, Rottoli, Sarkar, Talbert, [1511.06346](#)

→ estimate of theoretical uncertainties

# NLO QCD

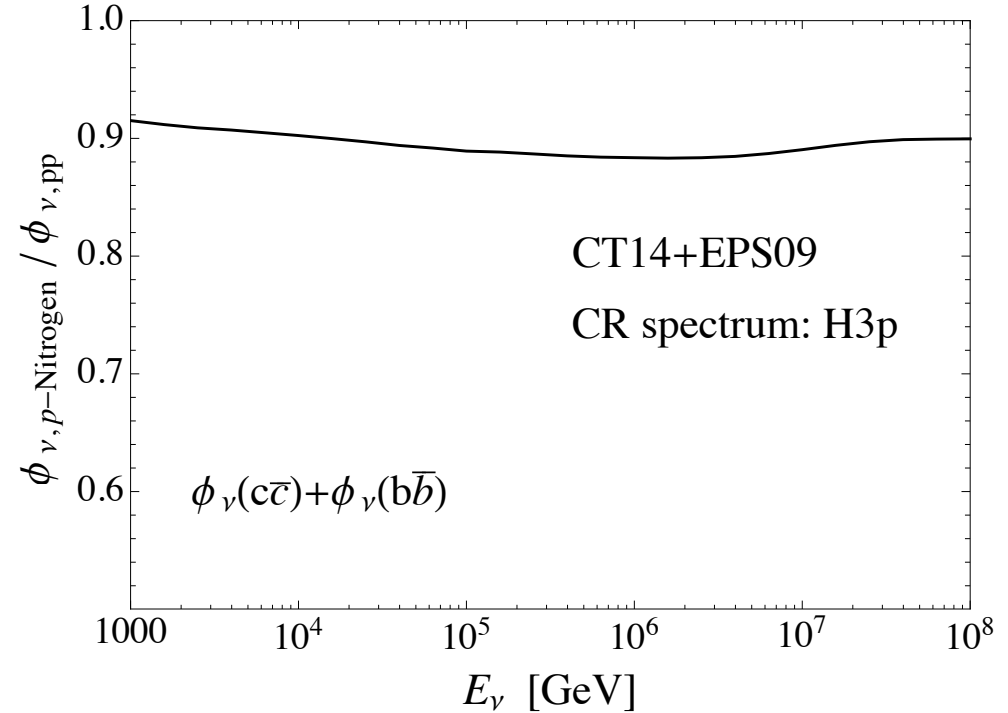
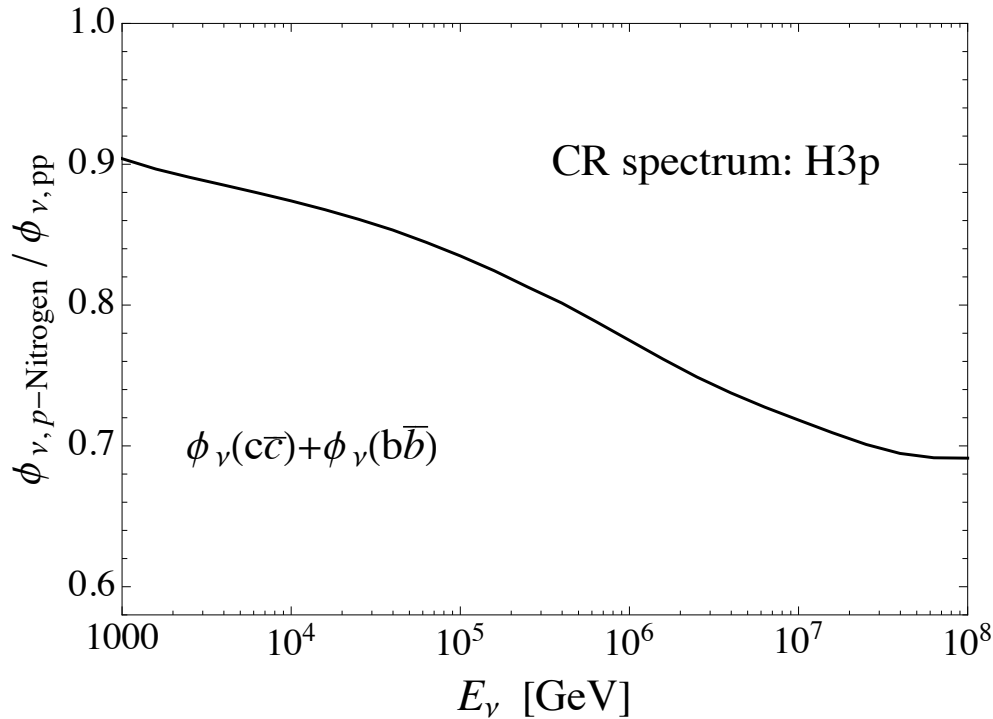


Compare with our BERSS NLO QCD and different cosmic ray fluxes

Difference to BERSS: bb now included, modified fragmentation fractions, nuclear effects (here: nCTEQ15)

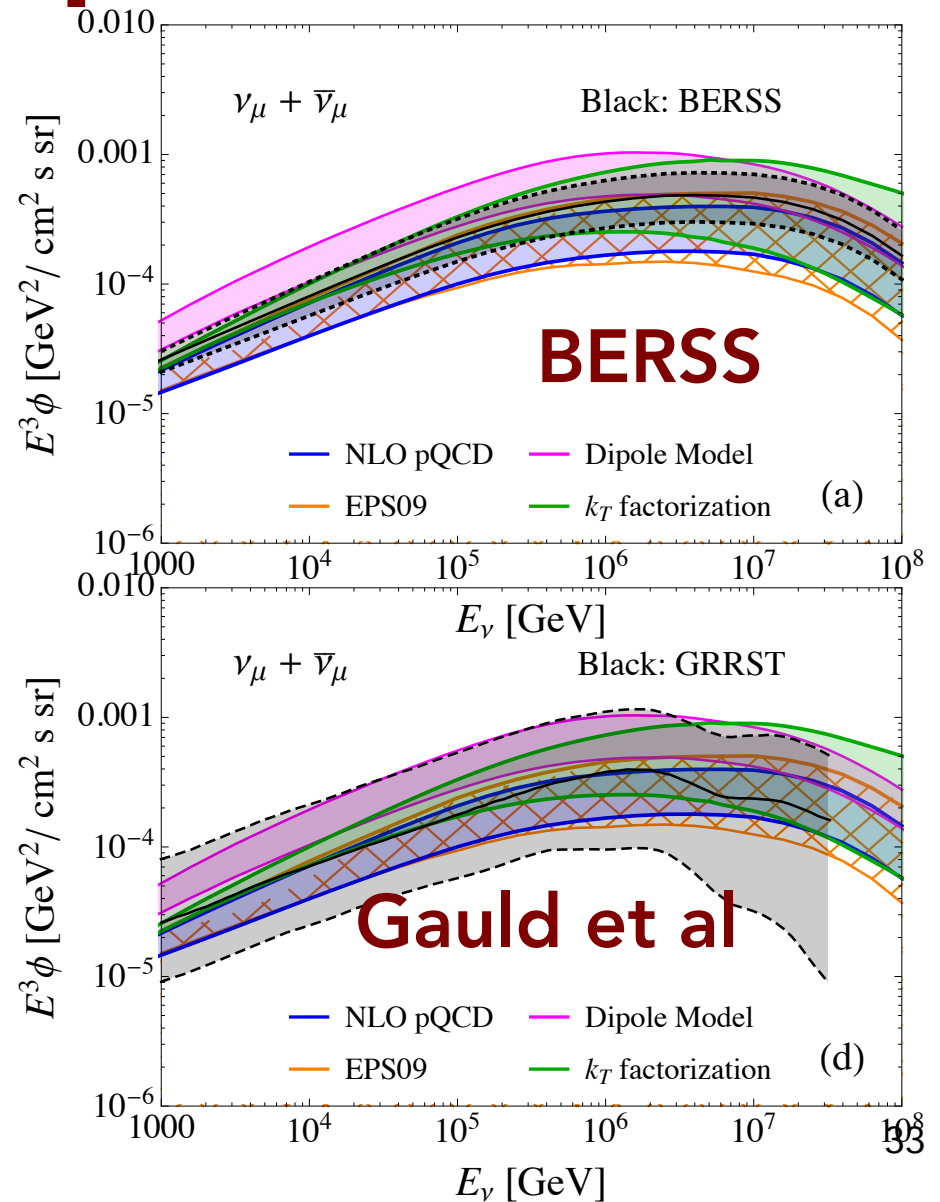
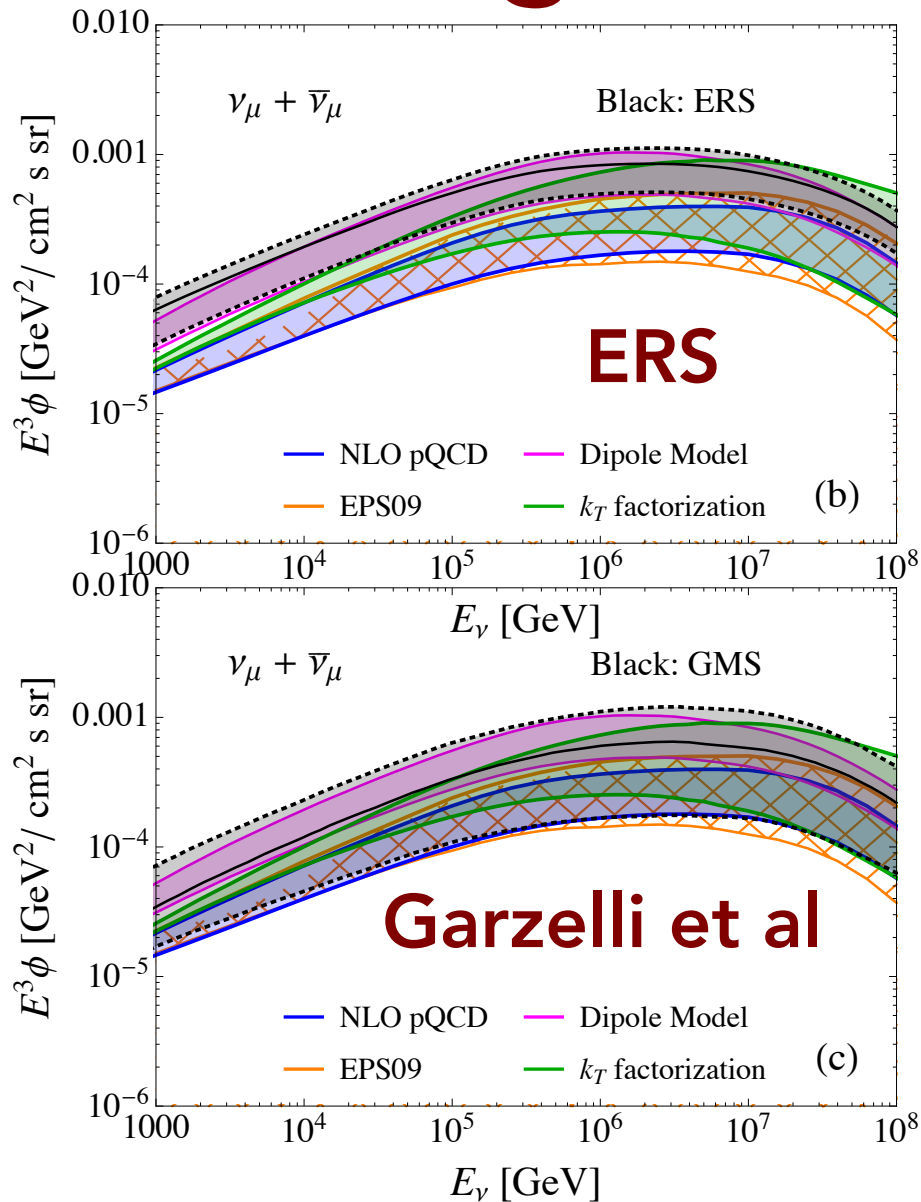
Overall: (30%, 40%, 45%) lower than BERSS at  $(10^3, 10^6, 10^8)$  GeV<sup>31</sup>

# Influence of nuclear shadowing



- Ratio of NLO QCD flux with and without nuclear effects
- 20–30% suppression from  $10^5$  to  $10^8$  GeV for nCTEQ  
(only 4–13% for total cross section)
  - But much less for EPS (frozen at  $x=10^{-6}$ )

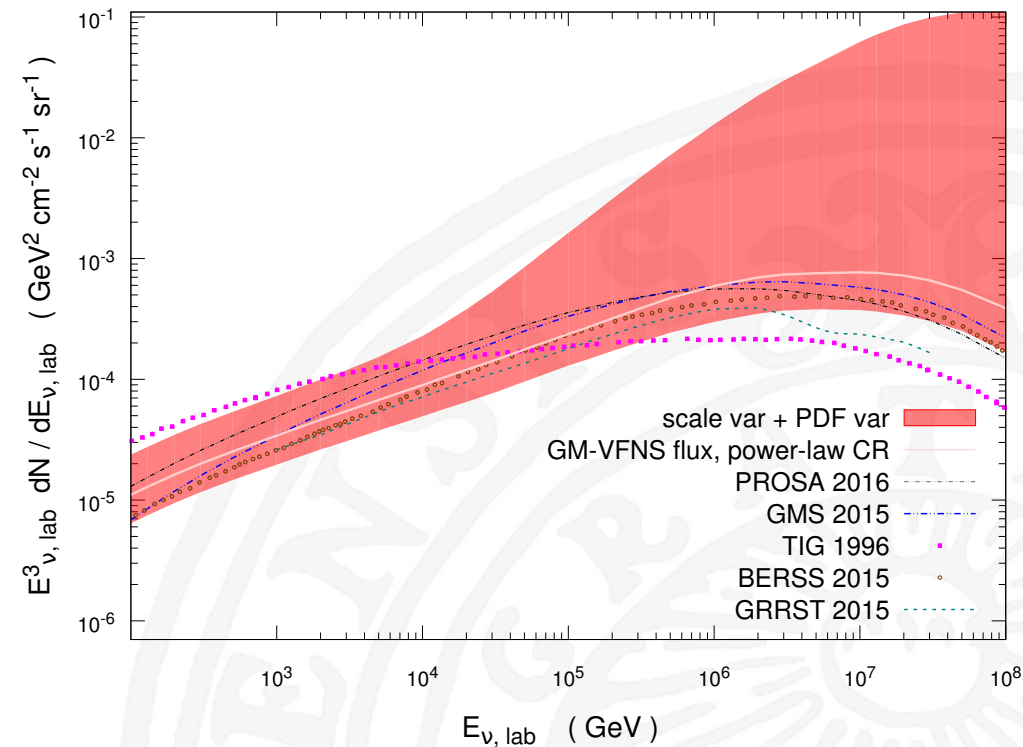
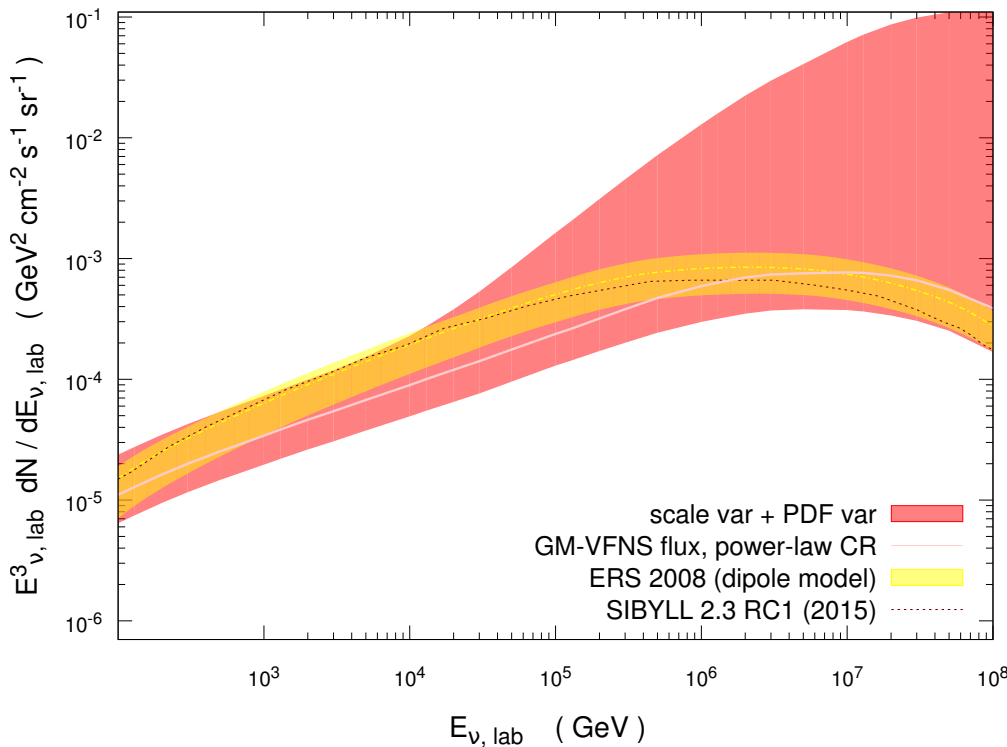
# And now everything, using broken power law



# Benzke et al GM-VFNS calculation

GM-VFNS ( $\nu_\mu + \text{anti-}\nu_\mu$ ) flux

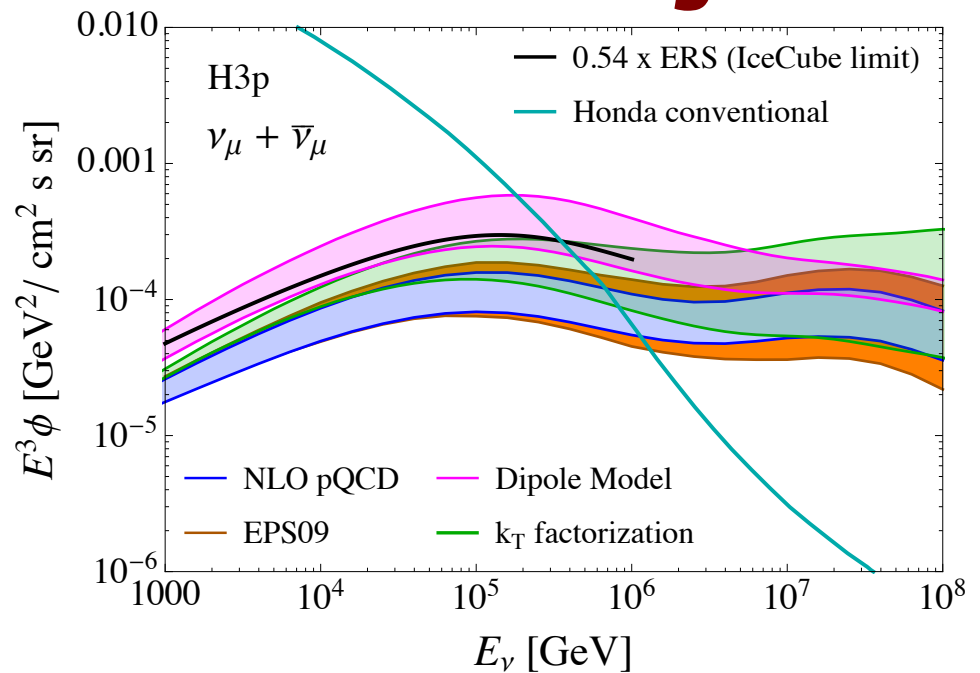
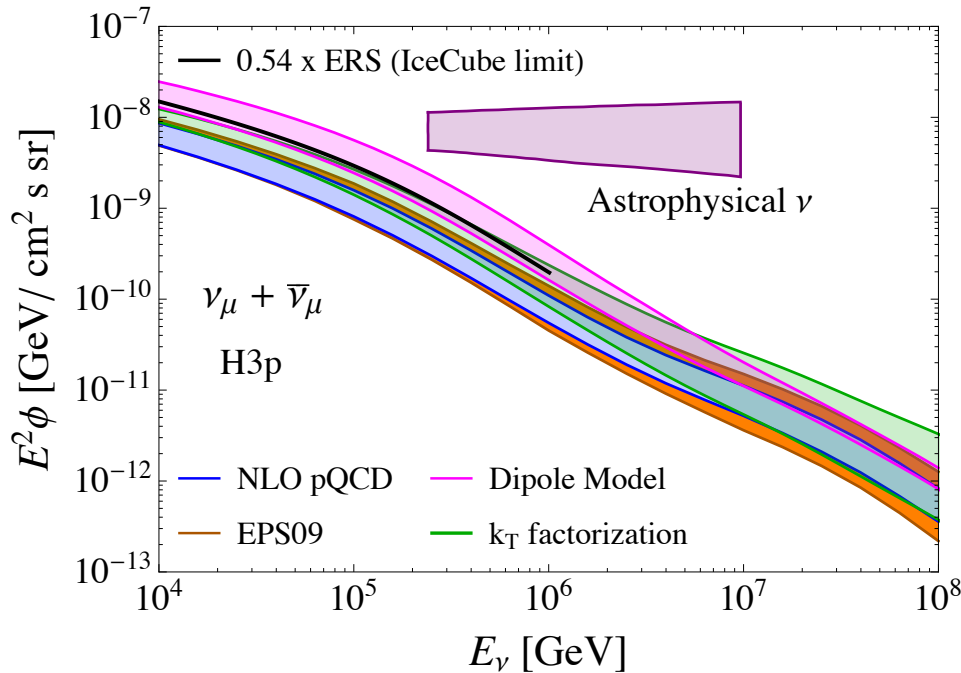
GM-VFNS ( $\nu_\mu + \text{anti-}\nu_\mu$ ) flux



pQCD calculation in “General Mass – Variable Flavor Number Scheme” (GM-VFNS)  
 M. Benzke, M. V. Garzelli, B. Kniehl, G. Kramer, S. Moch, G. Sigl, [arXiv:1705.10386](https://arxiv.org/abs/1705.10386)

The large pdf uncertainty at large energy arises from a particular set of CTEQ pdf fits (ct14nlo) – not constrained by data (but other sets do not show this – situation unclear)

# And what does IceCube say?



A recent IceCube limit (3 yrs) on the prompt flux sets a limit at 90% CL of

0.54 x (*ERS modified with H3p CR's*)

Best fit is still  $\phi_{\text{prompt}} = 0$

# Intrinsic charm

- “Normal” charm parton distribution is generated from gluon splittings
- There may be an “intrinsic” non-perturbative charm component in the nucleon  
[Brodsky, Hoyer, Peterson, Sakai, 1980]
- Would contribute charmed mesons at large  $x_F$   
[See e.g. Thunman et al; Bugaev et al.; Halzen and Wille...]

But there is hardly room in the data for that!  
Or is there?



# Conclusions

- The prompt neutrino flux poses one of the questions in neutrino astroparticle physics
  - How large is the flux?
  - Why hasn't it been discovered?
  - What is the proper way to calculate it?
- We think we know what we don't know – more accelerator and cosmic ray data needed!