



Wir schaffen Wissen – heute für morgen

Paul Scherrer Institute

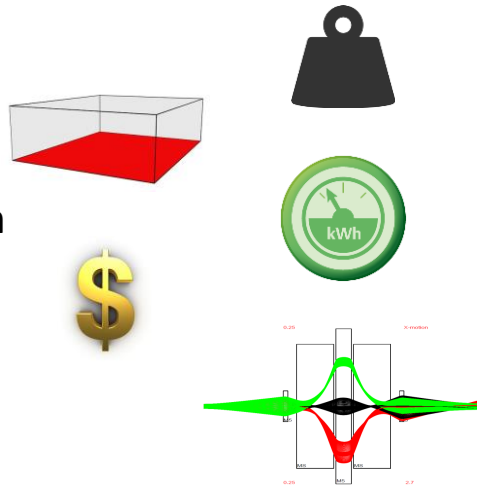
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Use of Complementary Simulation Codes in Complex Beam Optics

- Superconductivity in gantries
- Design proposed by PSI
- Beam optics code comparison
- Magnet design in OPERA
- Optics design including fringe fields

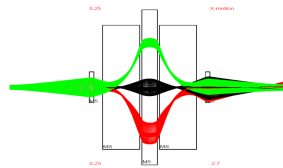
Advantages

- Lower:
 - Weight
 - Size
 - Power consumption
 - Overall facility cost



- Strong fields

=> new treatment techniques



Disadvantages

- Cost from cooling
- Risks of quenching
- Large stray fields
- Fast ramping required

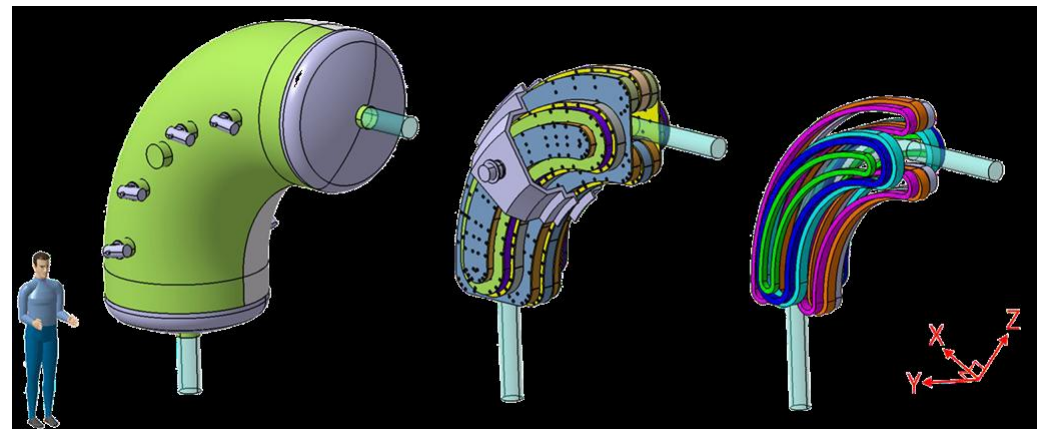
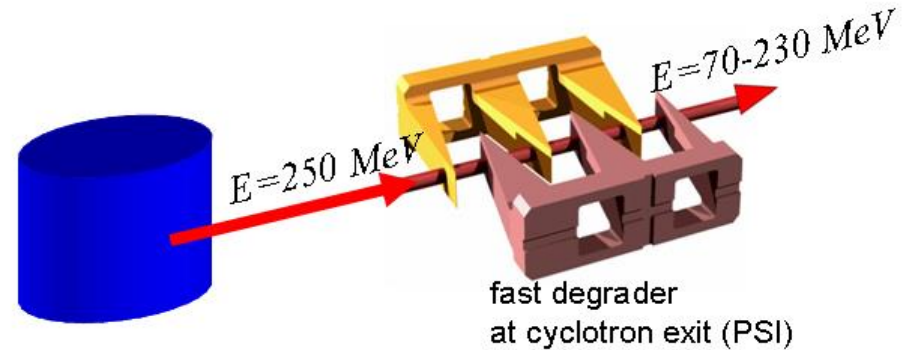
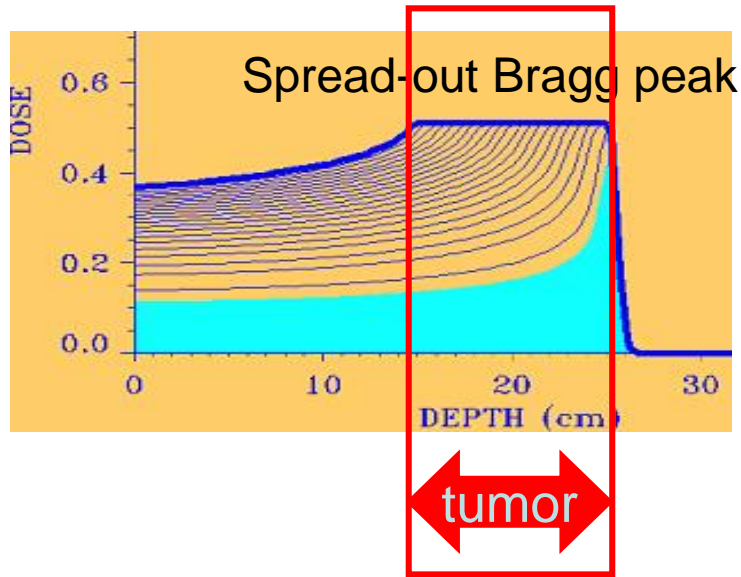


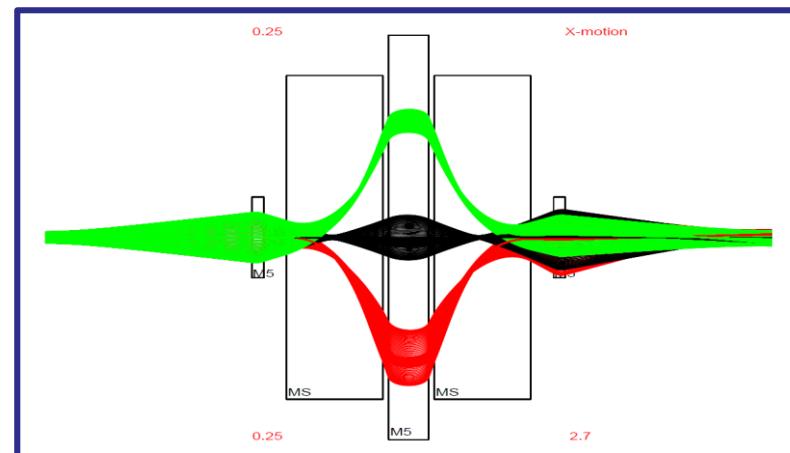
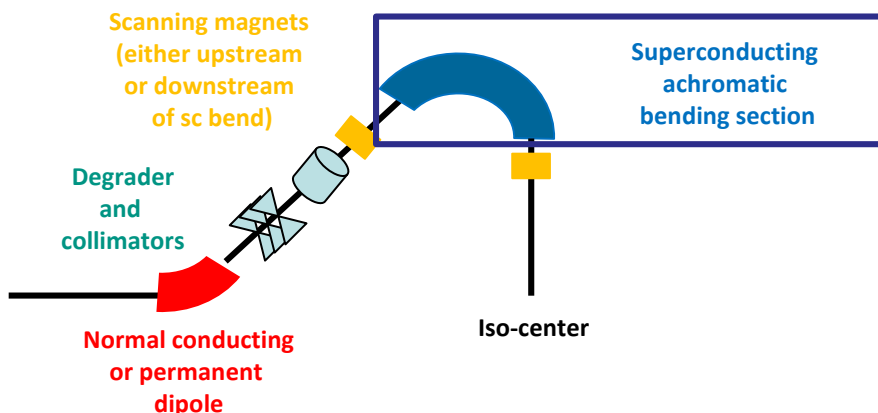
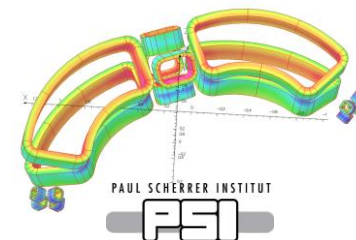
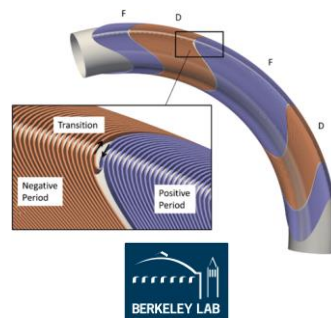
Figure courtesy: F. Kircher

Energy modulation - ramping

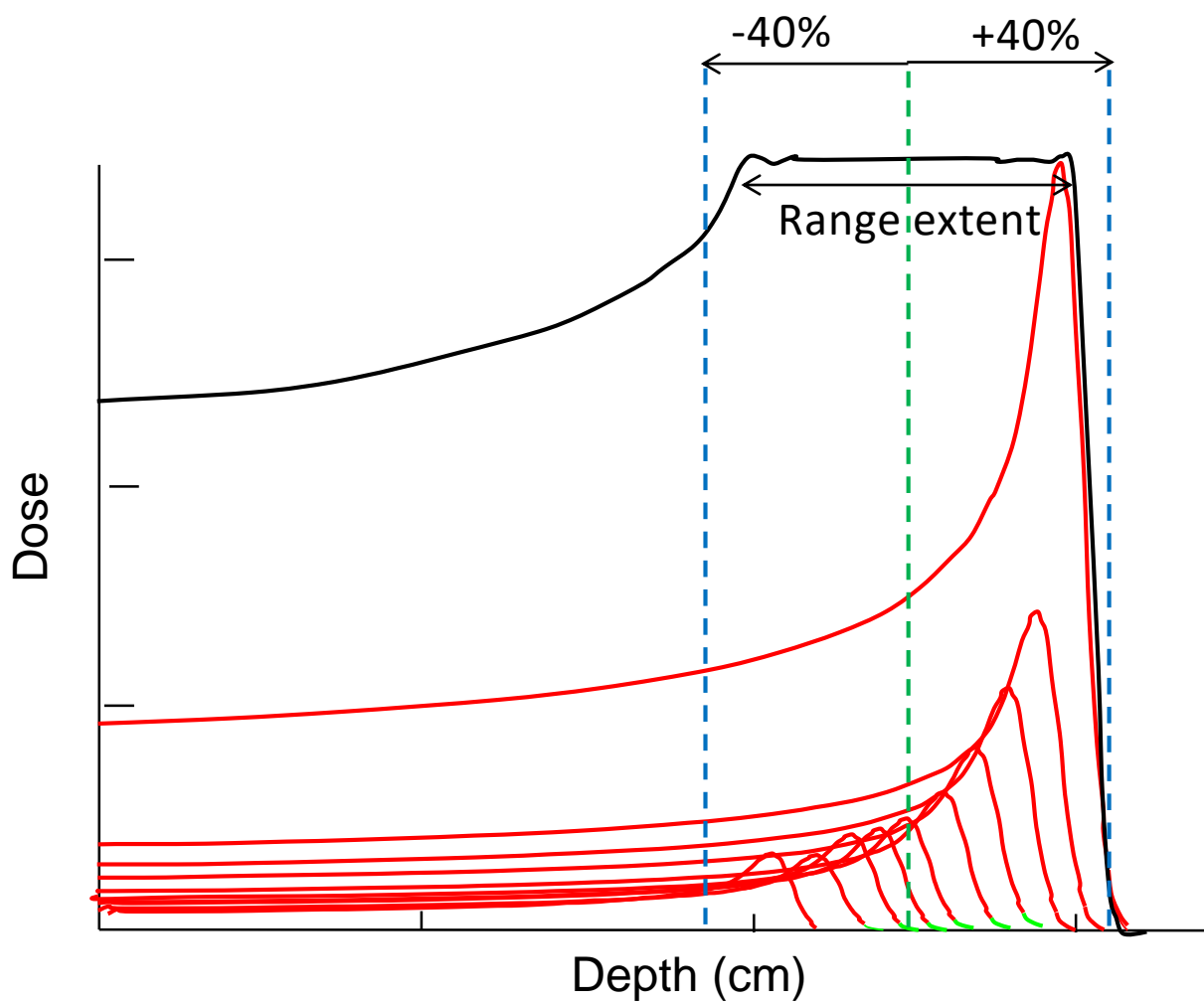


- Scanning is performed in layers
 - The momentum step between two layers is $\sim 1\%$
 - Energy change between two layers should be performed fast, e.g. in $\sim 100 \text{ ms}$
- => Two options:
- Magnet ramping speed of $\sim 1\% \text{ dB/B}$ in 100 ms
 - Gantry momentum acceptance very large ($\Delta p/p > 10-20\%$)

- Combined function magnets, e.g.
 - CCT magnets with alternating gradient
 - 3-5 racetrack magnets
- Momentum acceptance of over $\pm 10\%$
 - No energy selection needed
 - Degradar can be mounted on the gantry

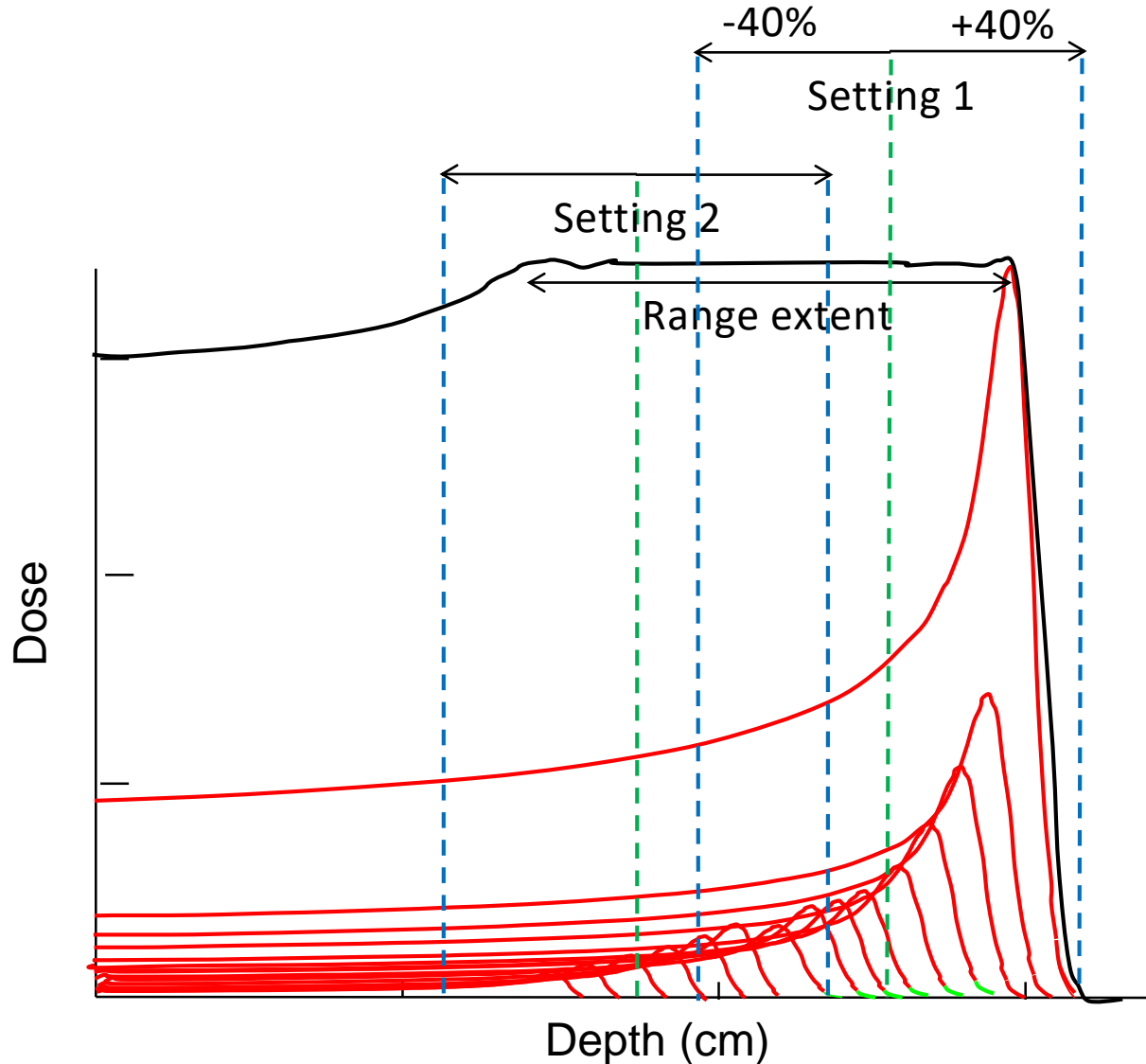


- Use of new treatment techniques



Large momentum acceptance allows:

- Treatment of the small tumors without change of the SC magnet field
- Can be used i.e. for volumetric rescanning on a very fast time scale



Large momentum acceptance allows:

- Treatment of the small tumors without change of the SC magnet field
- Can be used i.e. for volumetric rescanning on a very fast time scale
- Treatment of large tumors with only one or two of such changes (Magnet field change in 30-60 s)

Generation of SCOFF field maps

Sharp Cut Off Fringe Field (SCOFF) optics solution developed:

- 1st order in Transport and
- Higher orders in COSY

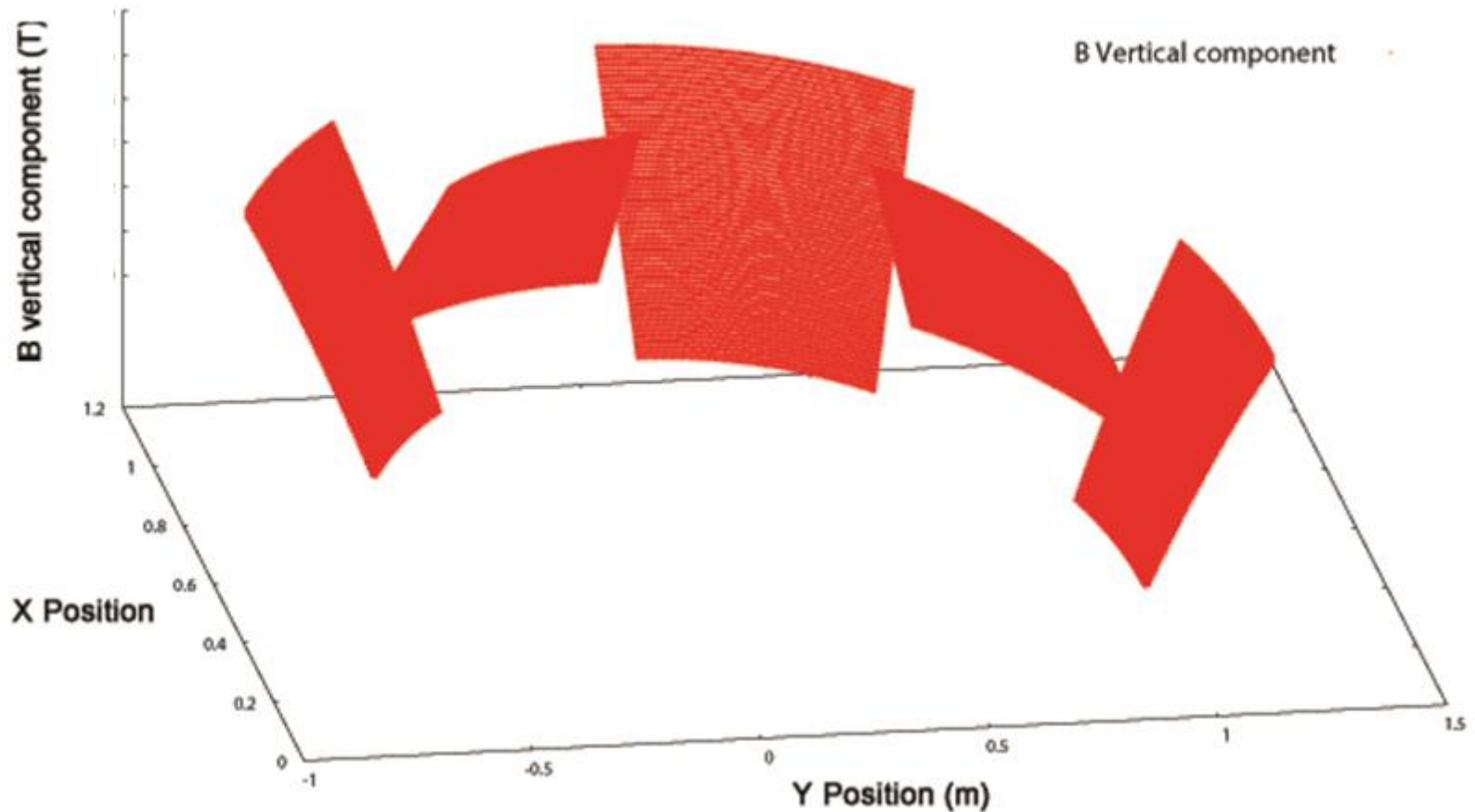
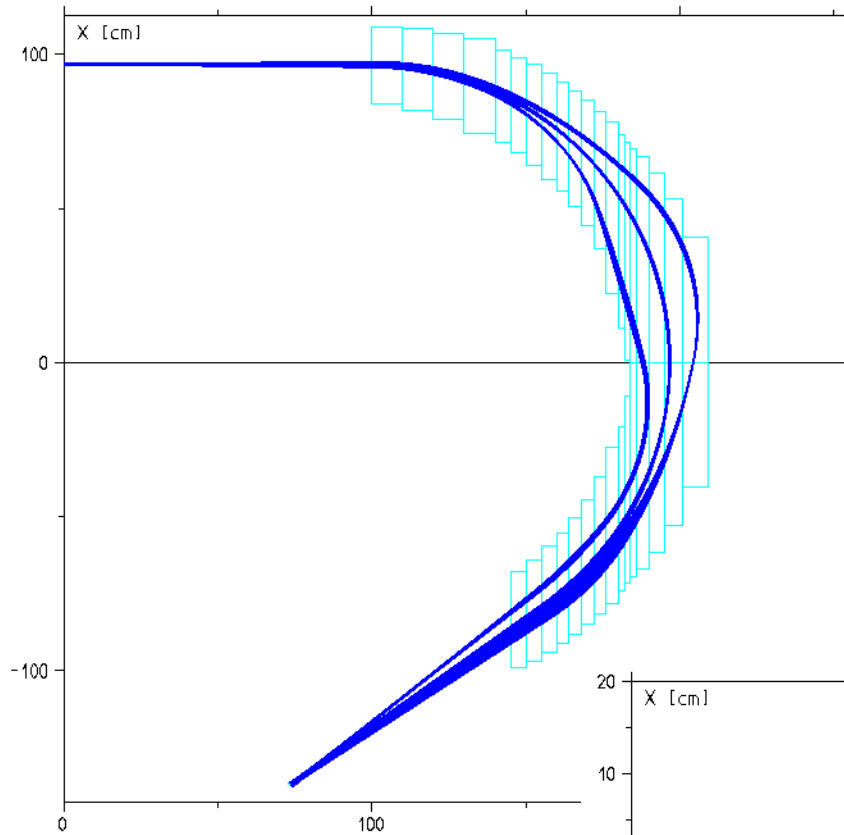


Figure courtesy: J. Bokor

Tracking through the 3D field map in Track



- Use 35 field maps
(because of field map size limit)
- Initial beam parameters:
 - 3 mm x 10 mrad at 2σ
 - The $\Delta p/p$ is
 - from -11.5 % (lower curve)
 - to +13.5 % (upper curve)

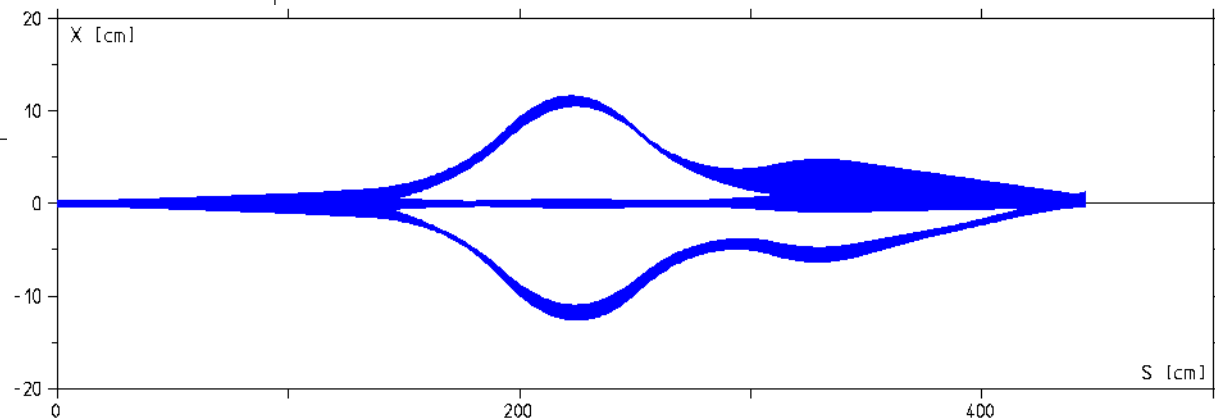
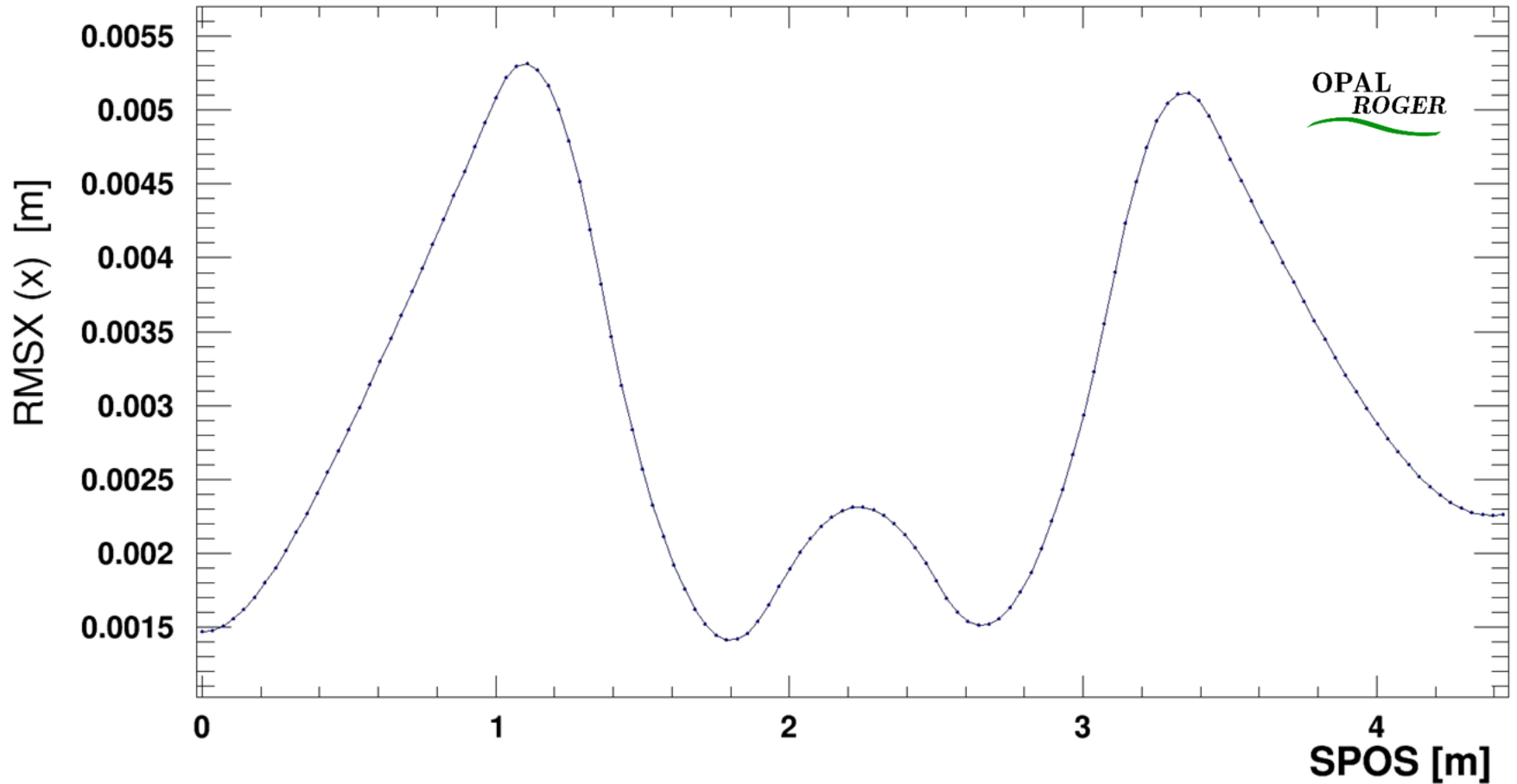


Figure courtesy: H. Zhang

Horizontal beam size (1σ)



OPAL and Track use MAD(X) convention

2.1 Magnetic Field and Vector Potential (Transverse Field, Curved Reference)

For all mid-plane symmetric elements MAD defines the magnetic field on the mid-plane of a sector dipole by its Taylor expansion:

$$B_x(x, 0, s) = 0, \quad B_y(x, 0, s) = B_0 + B_1 \frac{x}{1!} + B_2 \frac{x^2}{2!} + B_3 \frac{x^3}{3!} + \dots \quad B_s(x, 0, s) = 0. \quad (2.1)$$

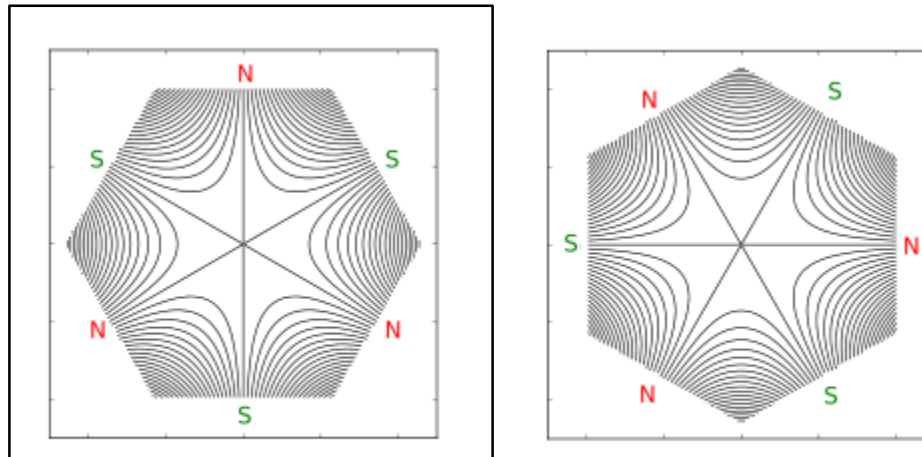
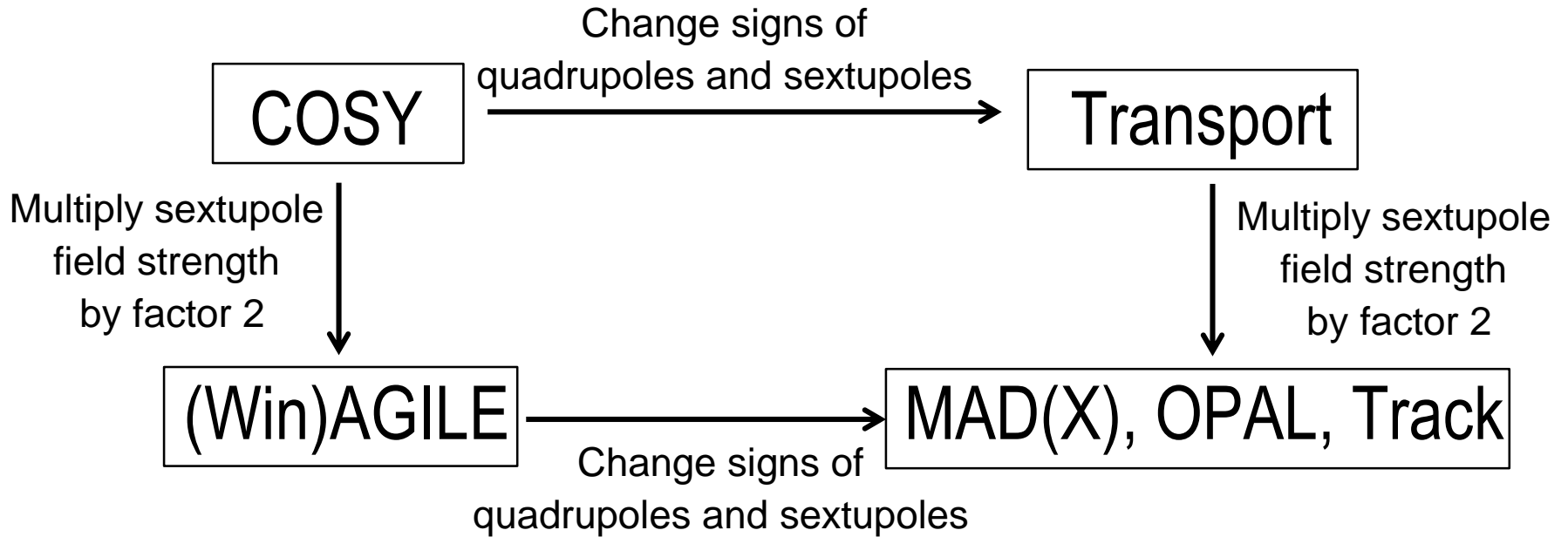
For positive x a positive field coefficient gives a contribution to the field in positive y -direction. The vector potential has a longitudinal component A_s depending on x, y only. Expanded to order four it takes the form

$$\begin{aligned} A_x(x, y, s) &= 0, \\ A_y(x, y, s) &= 0, \\ A_s(x, y, s) &= -B_0 \left(x - \frac{hx^2}{2(1+hx)} \right) - B_1 \left(\frac{1}{2}(x^2 - y^2) - \frac{h}{6}x^3 + \frac{h^2}{24}(4x^4 - y^4) + \dots \right) \\ &\quad - B_2 \left(\frac{1}{6}(x^3 - 3xy^2) - \frac{h}{24}(x^4 - y^4) + \dots \right) - B_3 \left(\frac{1}{24}(x^4 - 6x^2y^2 + y^4) + \dots \right) + \dots \end{aligned} \quad (2.2)$$

where h is the curvature of the reference orbit. Taking the curl of A_s in curvilinear coordinates the field components are to order three

$$\begin{aligned} B_x(x, y, s) &= \cancel{-} B_1 \left(y + \frac{h^2}{6}y^3 + \dots \right) \cancel{-} B_2 \left(2xy - \frac{h}{6}y^3 + \dots \right) \\ &\quad + B_3 \left(\frac{1}{6}(3x^2y - y^3) + \dots \right) + \dots \\ B_y(x, y, s) &= +B_0 \cancel{-} B_1 \left(x - \frac{h}{2}y^2 + \frac{h^2}{2}xy^2 + \dots \right) \cancel{-} B_2 \left(\cancel{-} \frac{1}{2}(x^2 - y^2) - \frac{h}{2}xy^2 + \dots \right) \\ &\quad + B_3 \left(\frac{1}{6}(x^3 - 3xy^2) + \dots \right) + \dots \\ B_s(x, y, s) &= 0. \end{aligned} \quad (2.3)$$

Converting between the codes



Rotation by 90° is not needed

Conversion rules developed for COSY, OPAL, Track, Transport and AGILE. However, not all codes are suitable for our purpose:

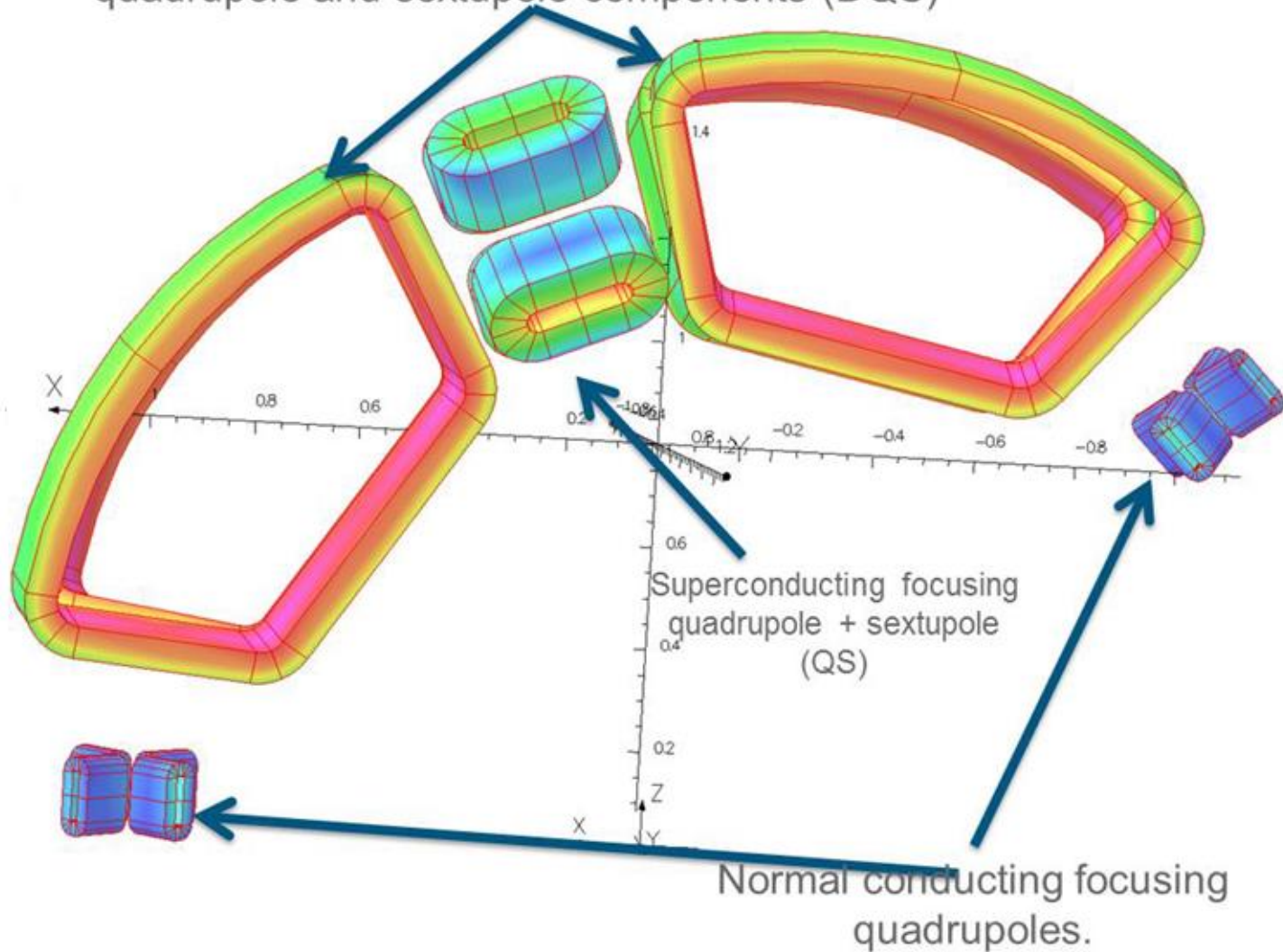
- Transport
 - Capable of calculating 2nd order effects
 - Optimization of sextupole fields does not function well
- WinAGILE
 - No 2nd order matrix calculation
- COSY
 - Capable of optimization with higher order effects and constraints
 - No matching of external 3D maps
- OPAL
 - OPAL-t
 - Can perform optimization (genetic algorithm optPilot)
 - 3D field maps only in straight geometries
 - OPAL-cycl
 - Tracking in a 3-D map
 - Can scale, but not modify the 3D field maps
- Track
 - Tracking in a 3-D map
 - Map size is limited
 - No optimization algorithms

Analytic

Tracking

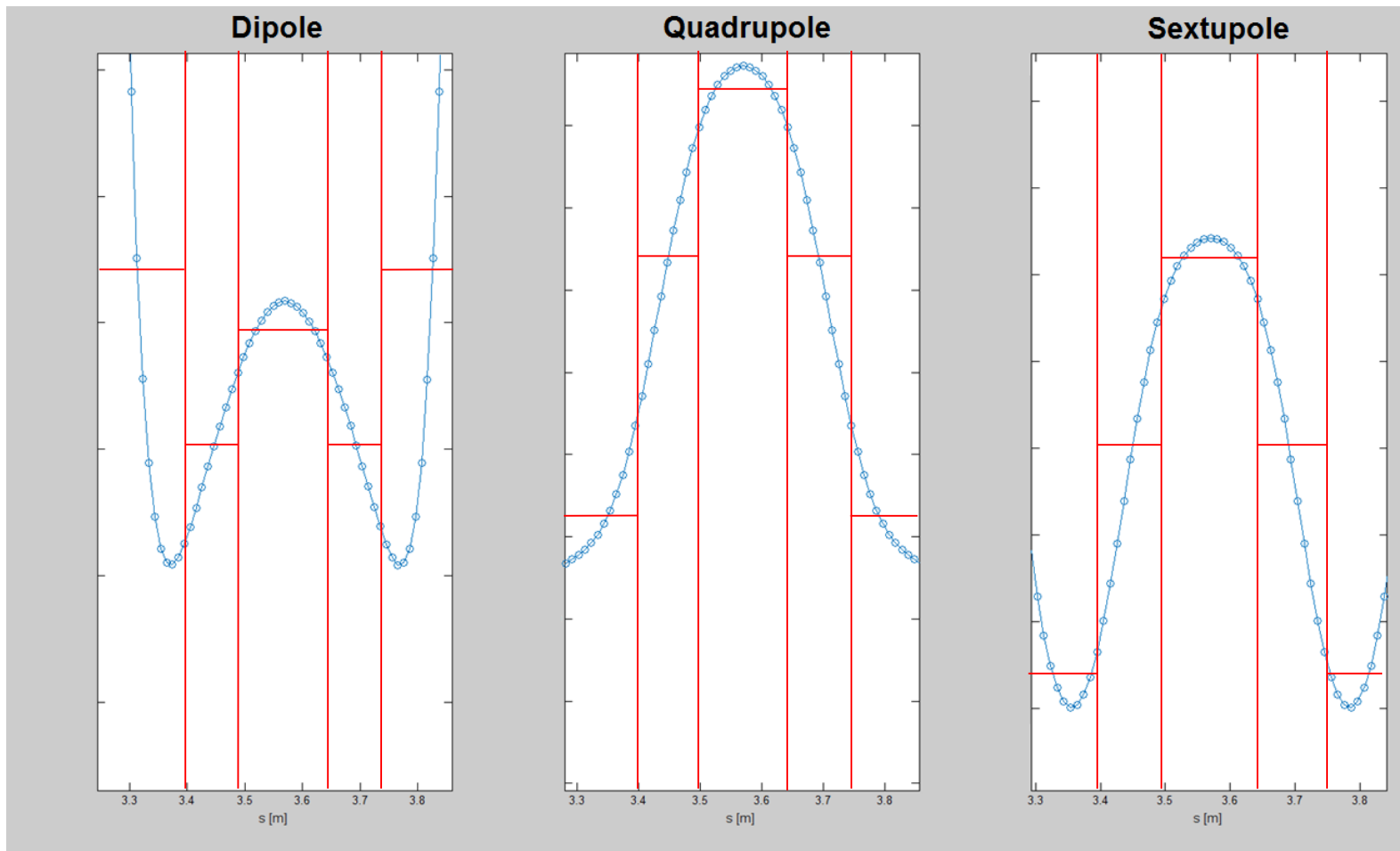
Magnet in OPERA

Superconducting dipoles with integrated quadrupole and sextupole components (DQS)



Steps for fringe field simulation

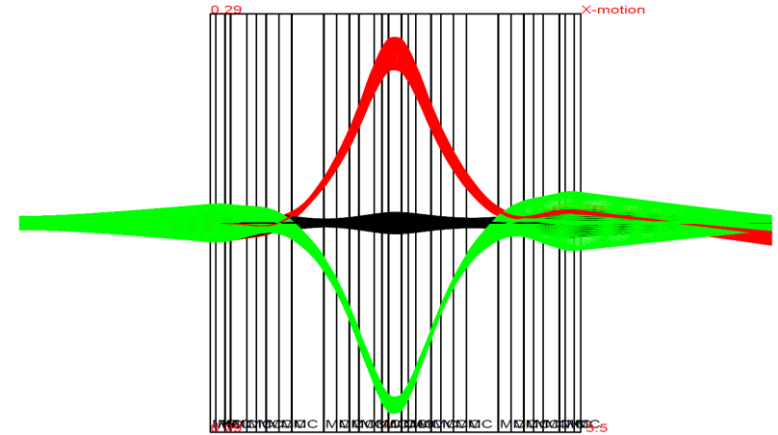
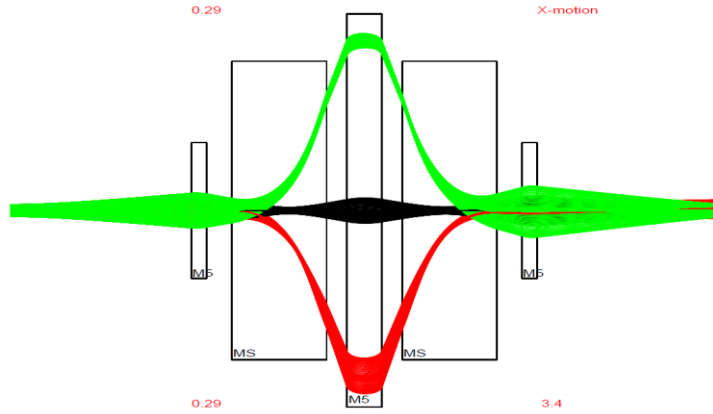
- Segment along the beam path
- Calculate averages for different segments



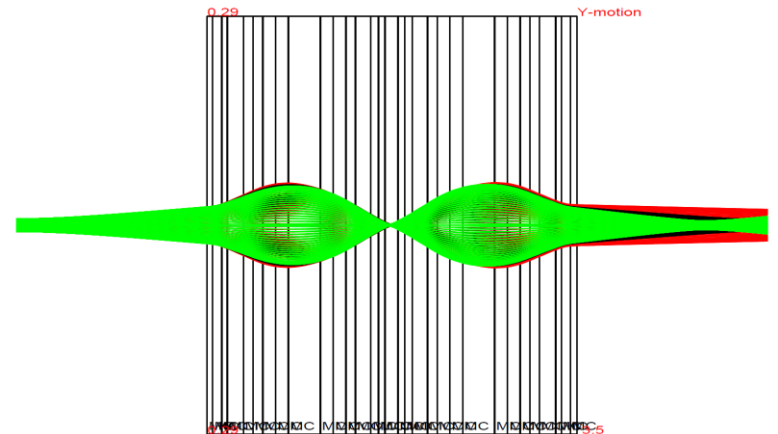
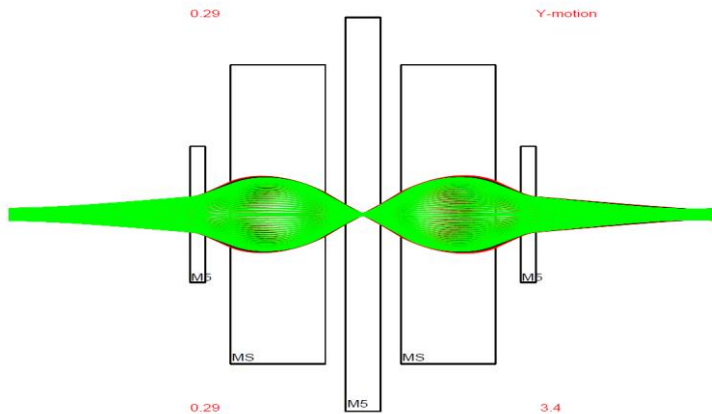
SCOFF simulation

Step function simulation

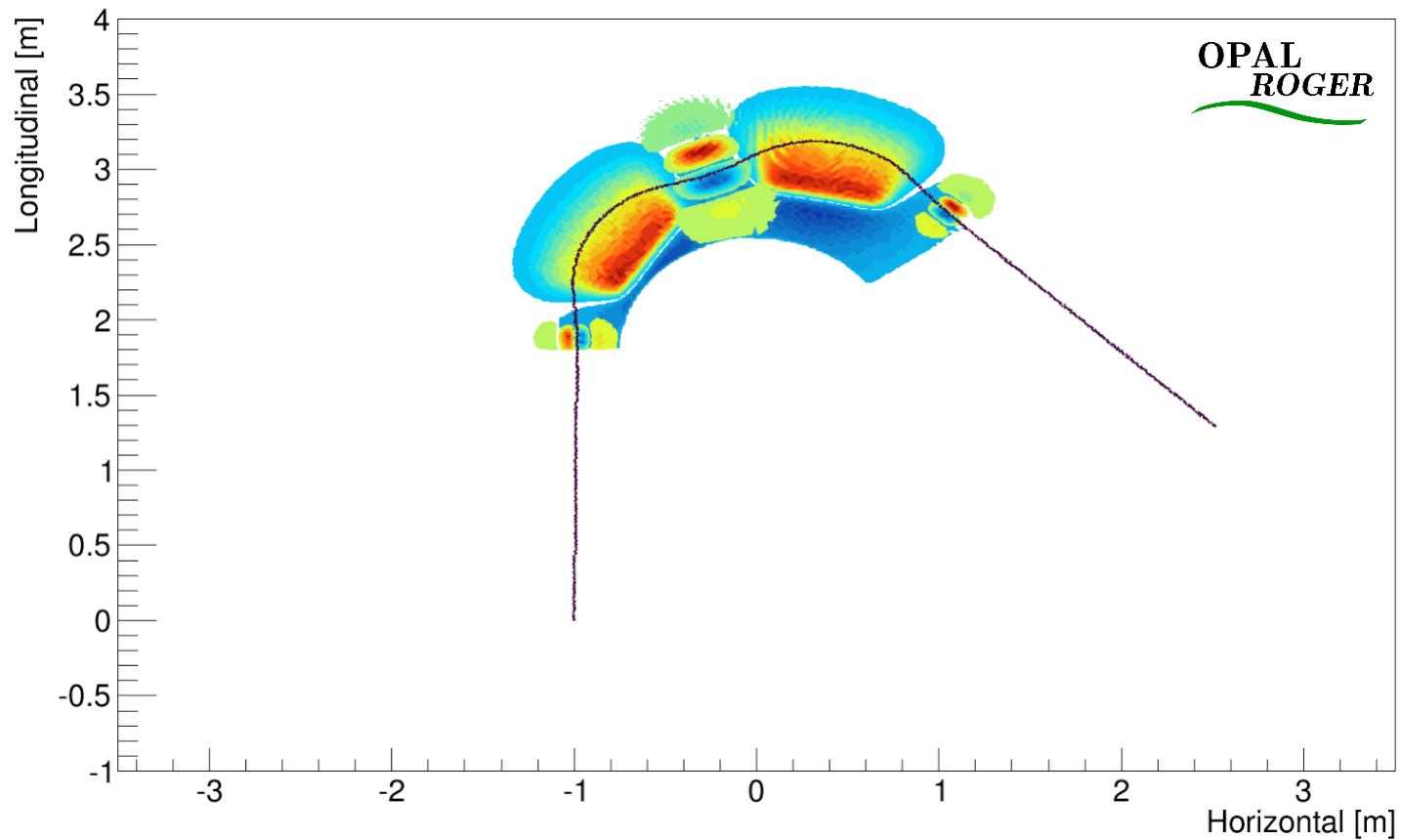
X-plane



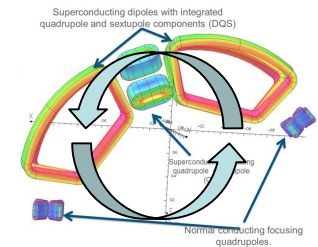
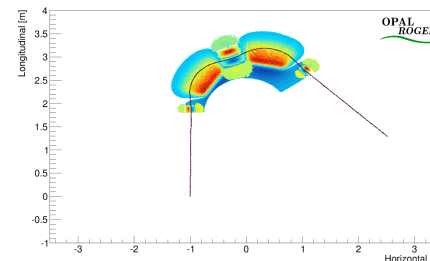
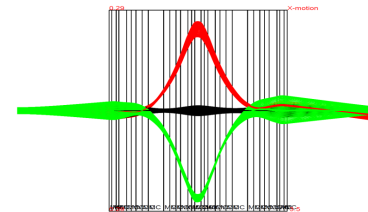
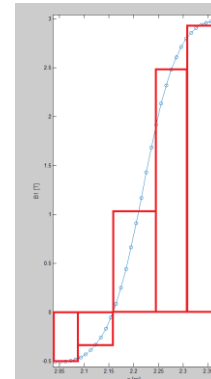
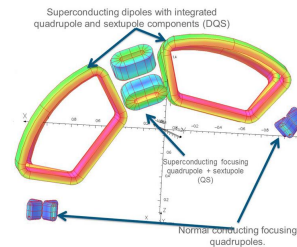
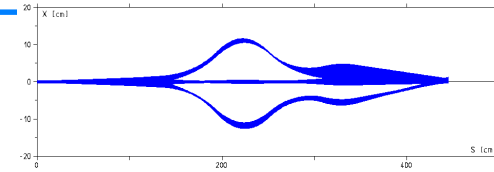
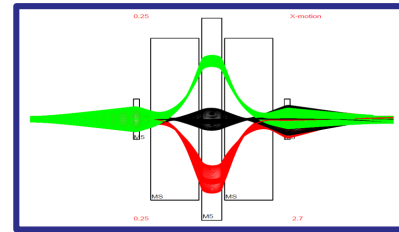
Y-plane



Realistic 3D field maps in OPAL



- Calculate SCOFF fields in COSY
- Verify SCOFF model with a tracking code
- Develop magnets in OPERA
- Approximate fringe fields with step functions
- More precise calculation of the required fields in COSY
- Modify magnets in OPERA
- Confirm with OPAL tracking through 3D field map



Thank you very much for your attention!

