

# Numerically inverting the fundamental stellar parameters of A/F stars

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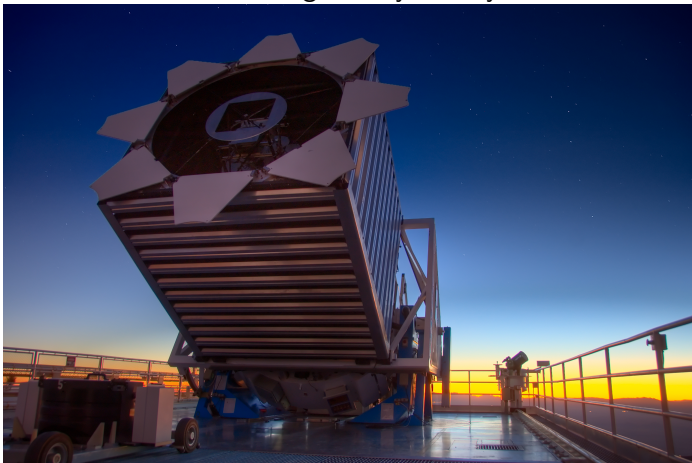
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The Fourth Azarquiel School of Astronomy

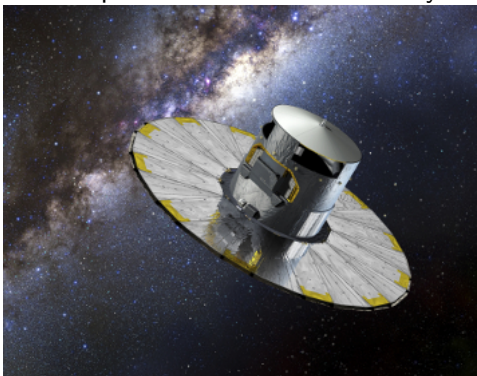


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## SDSS Sloan Digital Sky Survey



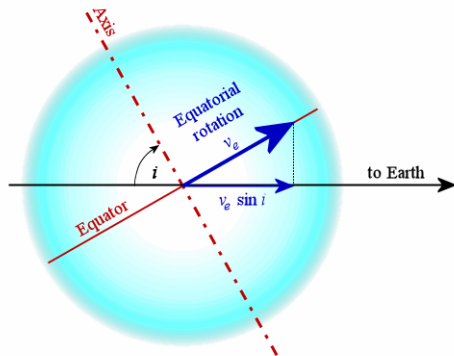
## Gaia space telescope Complemented Gaia-ESO survey



# Star Parameters

Fundamental stellar parameters:

- $T_{eff}$
- $\log(g)$
- $[\frac{Fe}{H}]$
- $\xi_t$



In addition to these parameters we can find the  $v_e \sin(i)$  which is the projected equatorial velocity

# The benefit of the parameters

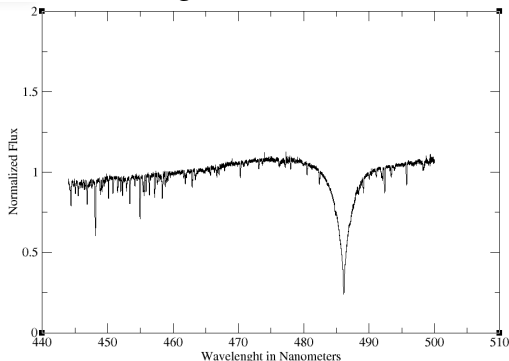
They form constrains for:

- Cosmology
- Galactic chemical evolution and dynamics
- Extra-solar habitability
- .... And many more....

# Spectra from surveys

- Spectroscopic data from many stars
- We need to find **its** fundamental parameters

HD98377  
 $RA : 11^h 19^{min} 06^{sec}$   
 $DEC : +09^\circ 45^{arcmin} 03^{arcsec}$   
 $mag_B : 8.17 \pm 0.02$   
 $mag_V : 8.05 \pm 0.01$



# Finding the parameters numerically

## LUT: Look up table

Radiative transfer model of stellar atmospheres → database(synthetic spectra)

- Check Gebran et al.(2016): A new method for the inversion of atmospheric parameters of A/Am stars
- Dr. Mounib Eid's (AUB) Lecture

## Inversion

- Observed spectra are compared to synthetic spectra
- The parameters of synthetic spectra with the best fit with the observed are used.

# The big data era

- Large quantity of data from surveys
- High resolution spectra  $\Rightarrow$  many flux values (up to 20000)
- Many parameter permutations
- Reaching up to Petabytes =  $10^6$  Gigabytes

YOU WILL NOT LIVE TO SEE YOUR RESULTS!!!!



# Dimension Reduction

I will share with you my secret numerical recipes!

- PCA: Principle Component Analysis
- SIR: Sliced Inverse Regression

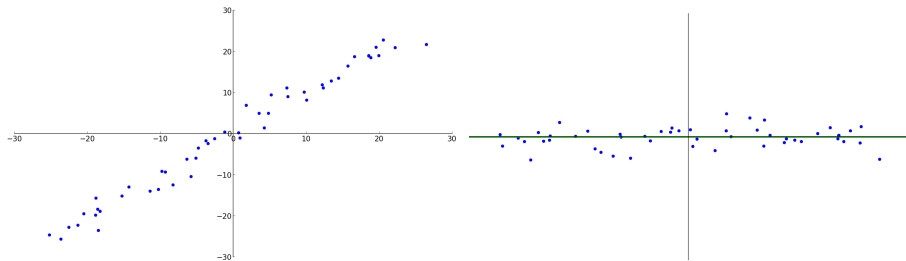
These 2 techniques are used to reduce the dimension of the spectra

- PCA was invented in 1901 by Karl Pearson
- Finds a lower dimensional space and projects all the data on this new subspace using the covariance matrix.

$$C = (S - \bar{S})^T (S - \bar{S}) \quad (1)$$

- $S$  is the row matrix of spectra
- $\bar{S}$  is the matrix of average of spectra (**identical rows**)
- $N$  eigenvectors with largest eigenvalues of  $C$  form the new eigenbasis
- In Gebran et al.(2016)  $N=12$  (Dimension lowered from 20000 to 12)

# 2D to 1D example



- SIR was elaborated by Ker-Chau Li(1991)
- We adopted reducing the dimension of spectra into 1



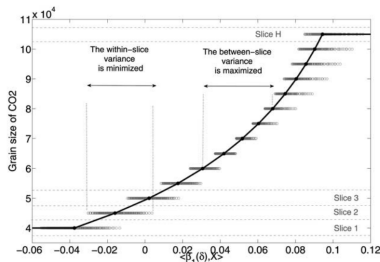
**Estimation of Mars surface physical properties from  
hyperspectral images using Sliced Inverse Regression**  
Caroline Bernard-Michel, Sylvain Douté, Laurent Gardes, Stephane Girard

- Doing regression vs parameters
- Calculate a **sorted** covariance matrix of all spectra:  $\Sigma$
- Find covariance matrix of averages of slices:  $\Gamma$
- Finally the eigenvector of the largest eigenvector

$$\Sigma^{-1}\Gamma \quad (2)$$

Serves as an eigenbasis

BERNARD-MICHEL ET AL.: RETRIEVAL OF MARS SURFACE PROPERTIES



## Latest work on the topic

- $\Sigma^{-1}\Gamma$  is ill-posed(ill-conditioned)
- At **NDU Louaize - Lebanon** in collaboration with **Paul Sabatier University-Toulouse-France** as a part of my masters thesis , we are working to regularize this covariance matrix and make it well-conditioned ( well-posed)

# Latest work on the topic

PCA has been applied on stars with high accuracy of parameter value in the works of:

- Gebran et al.(2016) → For A and F stars
- Paletou, Gebran et al.(2015) → For M dwarfs
- New tests of SIR will be done on A and F stars aiming to achieve higher accuracy of parameters.

**Grazie per il tuo tempo!!**



**Thank you for your time!!**