

Update on comparison of various PID performance predictions

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Content

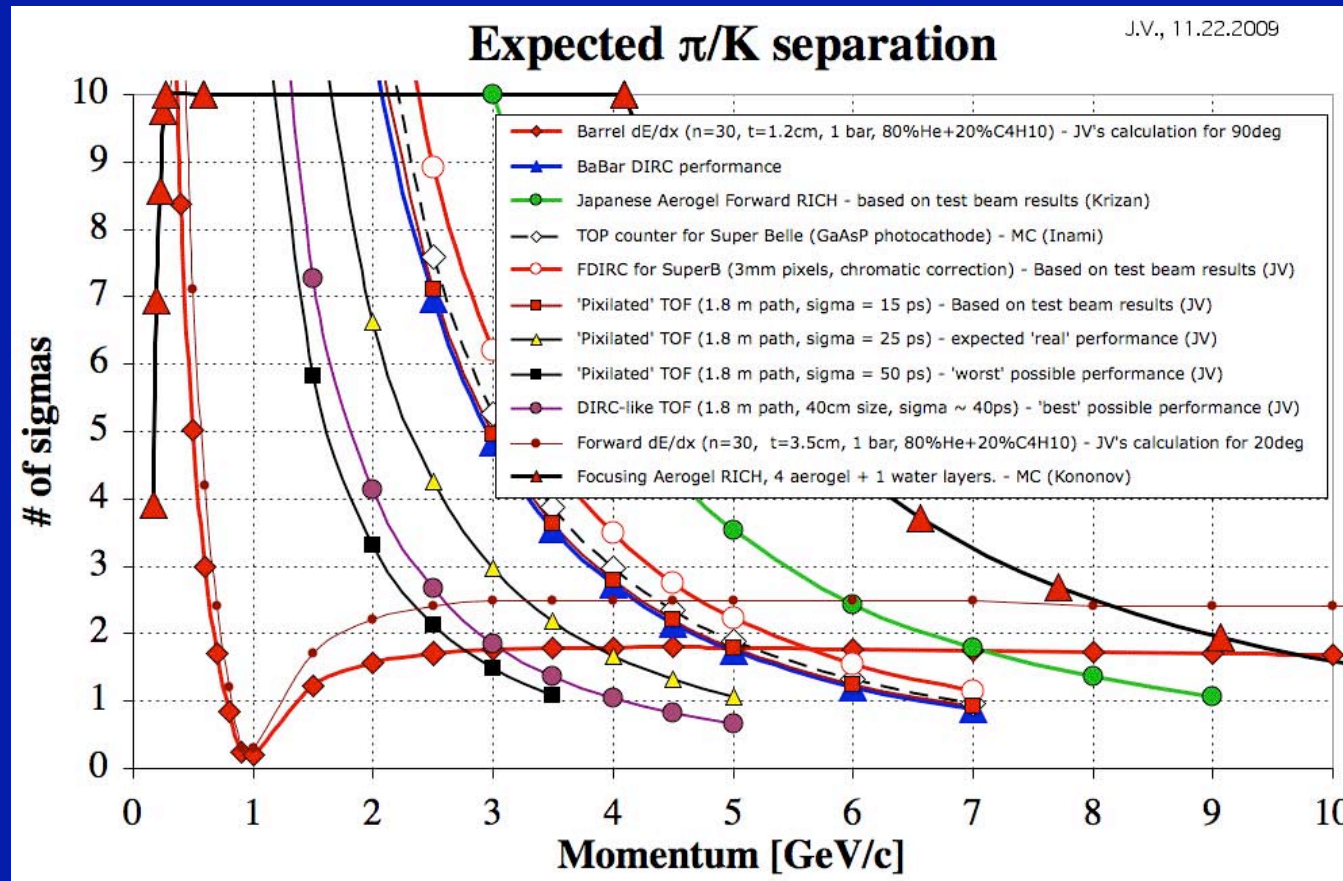
- Forward Aerogel RICH - MC simulation
- Forward dE/dx performance
- How is it all calculated ?

PID performance under “ideal” conditions

J. Va'vra, $dE/dx = f(\beta_{\gamma})$ study.xls spreadsheet

Example of various Super-B PID designs:

Calculation done for flight path length = 1.8m

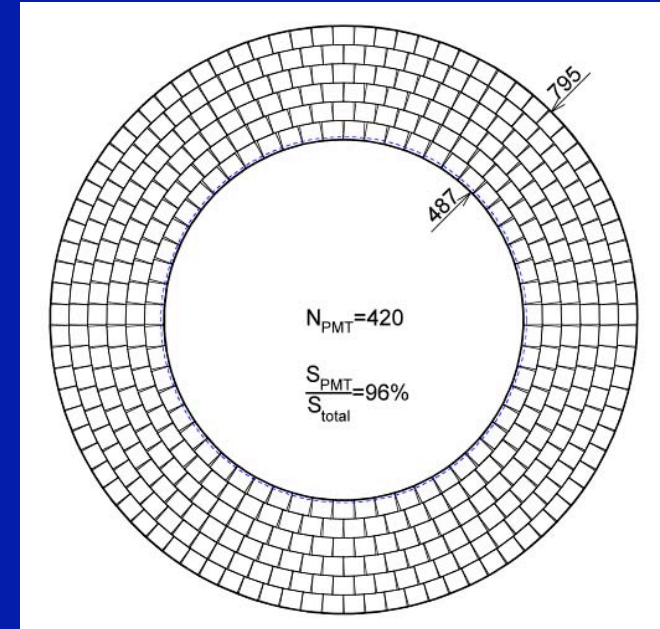
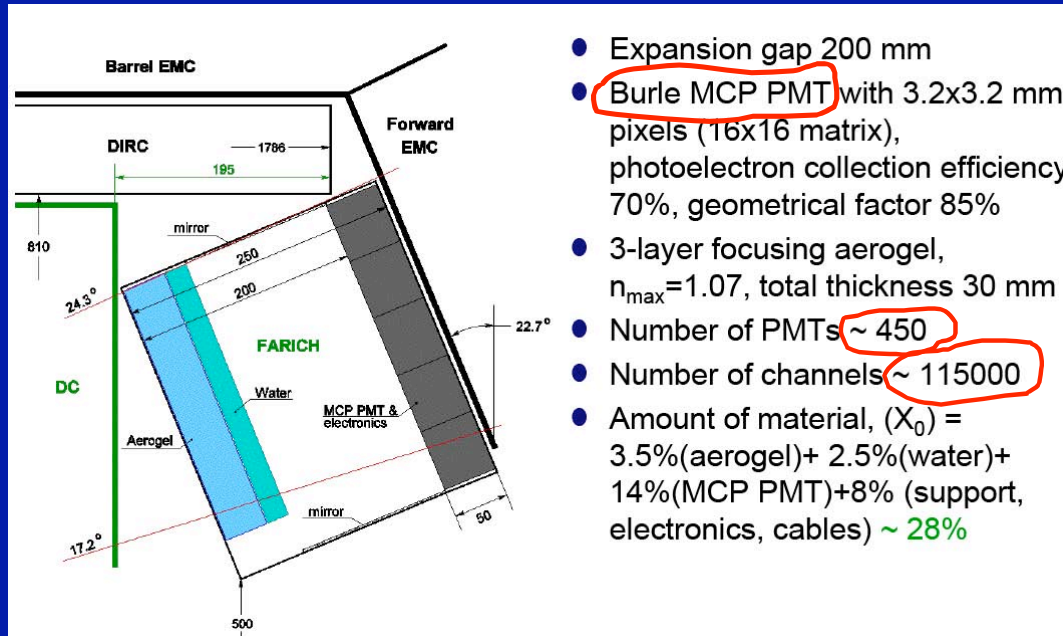


- If a DIRC-like TOF would achieve $\sigma \sim 50\text{ps}$, it will be still useful up to ~ 2.5 GeV/c.
- Forward Aerogel RICH has superior PID performance compared to the TOF proposal, or any other scheme.
- Use my calculation of the dE/dx in the forward direction (a bit more pessimistic compared to Fastsim).

Novosibirsk forward Aerogel RICH

S. Kononov, E. Kravchenko and A. Onuchin, Novosibirsk

Kravchenko, SuperB workshop, SLAC:

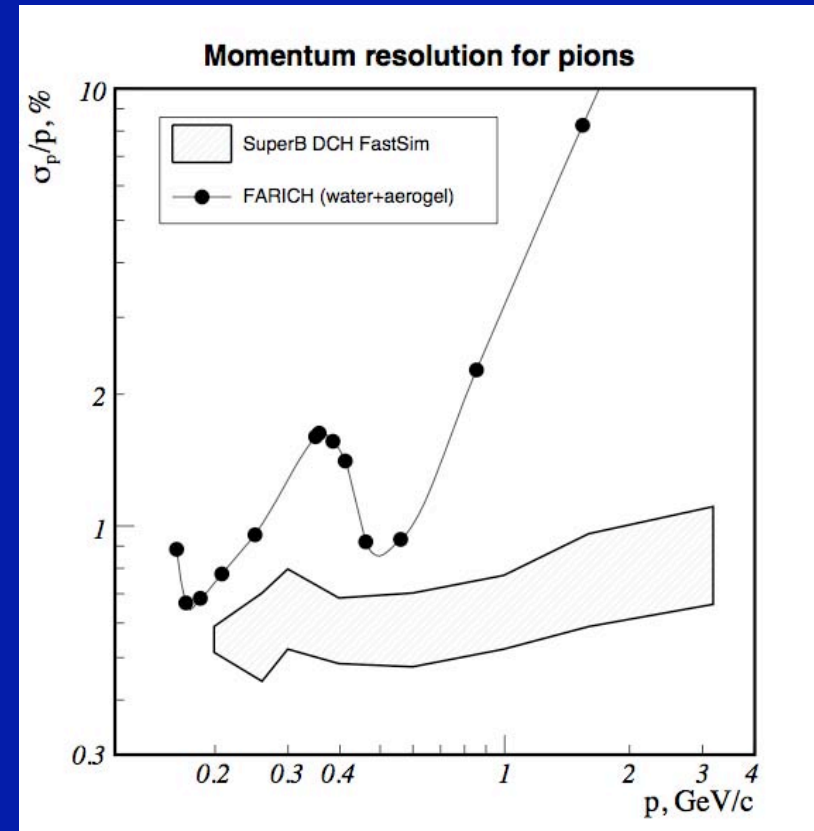
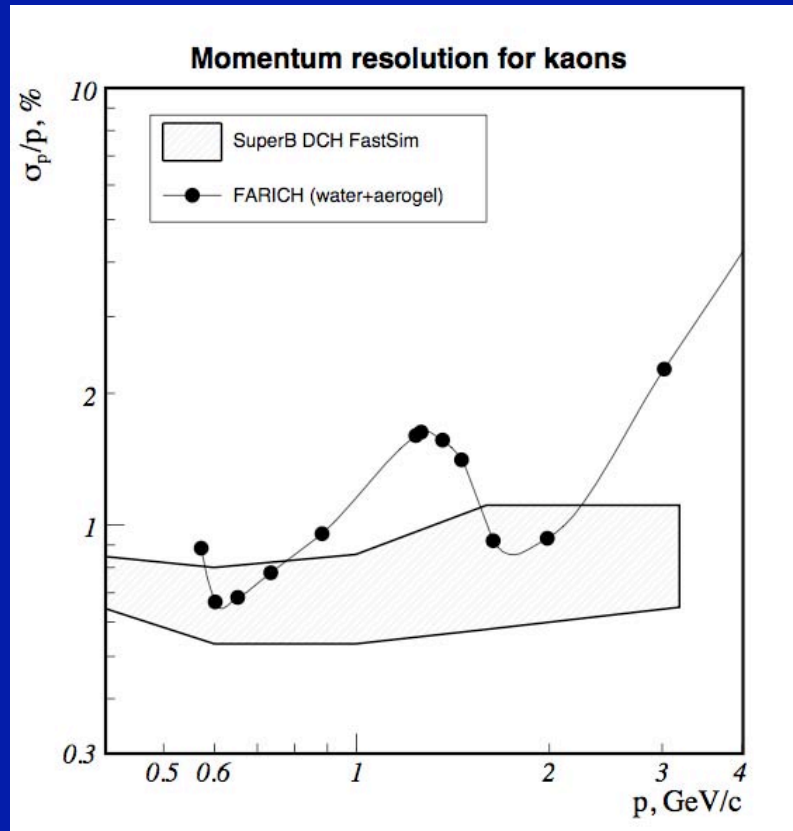


The latest plot assumes:

- **5-layer radiator: four aerogel layers and one layer of water.**
- **Add water, with higher n, to improve the low momentum PID capability.**
- **The system would use 450 Photonis MCP-PMTs with 10 micron holes.**

Aerogel RICH MC

S. Kononov, E. Kravchenko and A. Onuchin, Novosibirsk

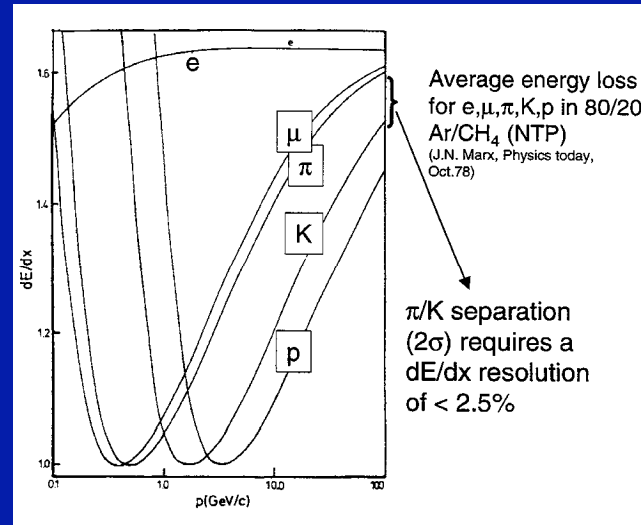


- **Forward Aerogel RICH is capable of measuring a momentum**
- **Momentum is measured by DCH**

dE/dx PID technique

$$N_{\sigma} = [dE/dx(m_1) - dE/dx(m_2)] / \sigma(dE/dx)$$

Bethe-Bloch were first to calculate it in 1930's



- To predict dE/dx, one can use:
 - Bethe - Bloch - Sternheimer calculation, or
 - Landau - Sternheimer calculation, or
 - Allison - Cobb Monte Carlo simulation, or
 - Empirical curves based on fitting the data, such as in the book of Ronaldi-Bloom.

- To predict $\sigma(dE/dx)$, one can use:
 - Allison - Cobb Monte Carlo simulation, or
 - Empirical curves based on fitting the data.

Which model works best and is most useful ?

Prediction of dE/dx

J. Va'vra, Nucl. Instr. & Meth., A453(2000)262, and SLAC-PUB-8356, Jan. 2000, and dE_dx = f(beta_gamma) study.xls

Bethe-Bloch formula for dE/dx with Sternheimer parameterization of the density function:

$$\frac{dE}{dx} = -0.3071 \frac{Z}{A} \rho t \frac{1}{\beta^2} \left[\frac{1}{2} \ln \frac{2 m_e c^2 \beta^2 \gamma^2 E_{cut}}{I^2} - \frac{\beta^2}{2} - \frac{\delta}{2} \right]$$

where

Z is atomic number of medium,
 A is atomic mass of the medium,
 ρ is density of the medium,
 t is sample thickness,
 m_e is mass of electron,
 I is mean excitation energy of the medium,
 E_{cut} is maximum kinetic energy which can be given to a free electron in a single collision,
 δ is density correction due to polarization of the medium.

Sternheimer parametrization of density function δ:

$$\begin{aligned} \delta &= 0 && \text{for } X = \ln \beta\gamma < X_0 \\ \delta &= 4.606(X - X_0) + \frac{4.606(X_1 - X_0)}{(X_1 - X_0)^3} (X_1 - X)^3 && \text{for } X_0 \leq X < X_1 \\ \delta &= 4.606(X - X_1) && \text{for } X > X_1 \end{aligned}$$

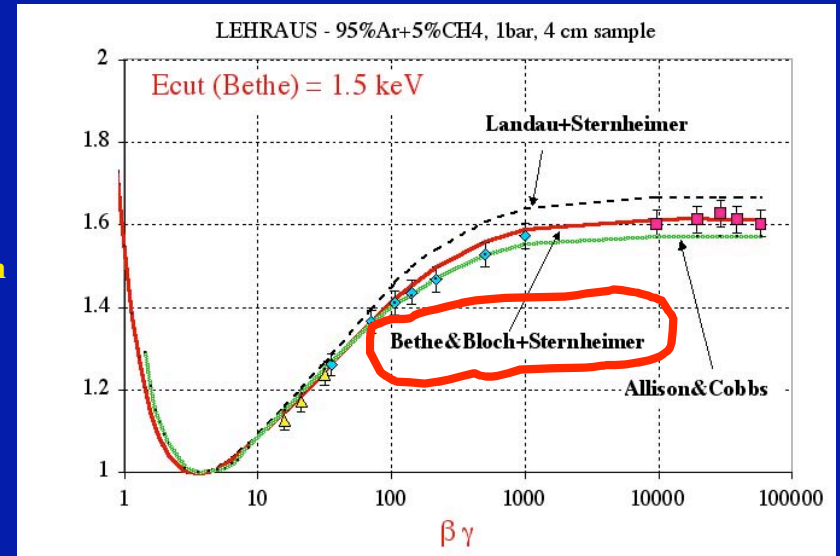
Electron density:

$$n_{el} = N_A * Z * \rho / A$$

Bloch found that the mean ionization potential can be approximated by:

$$I \sim (10\text{eV}) * Z$$

One of many examples in the paper:

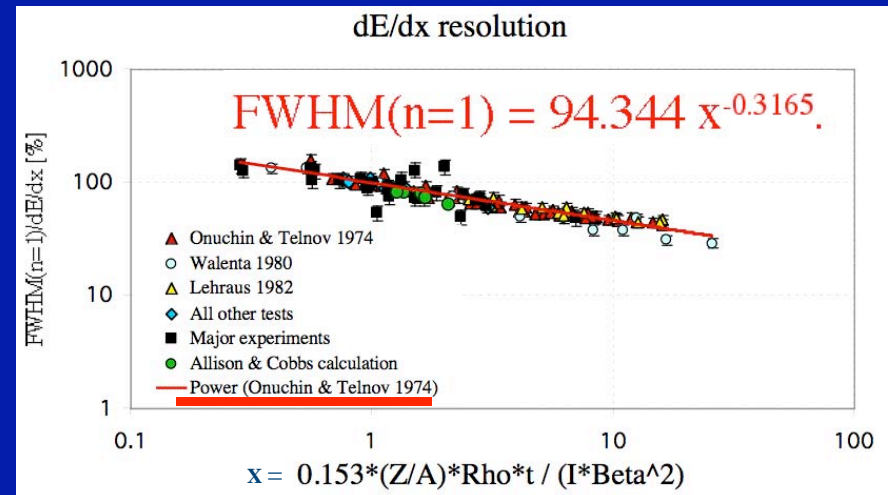
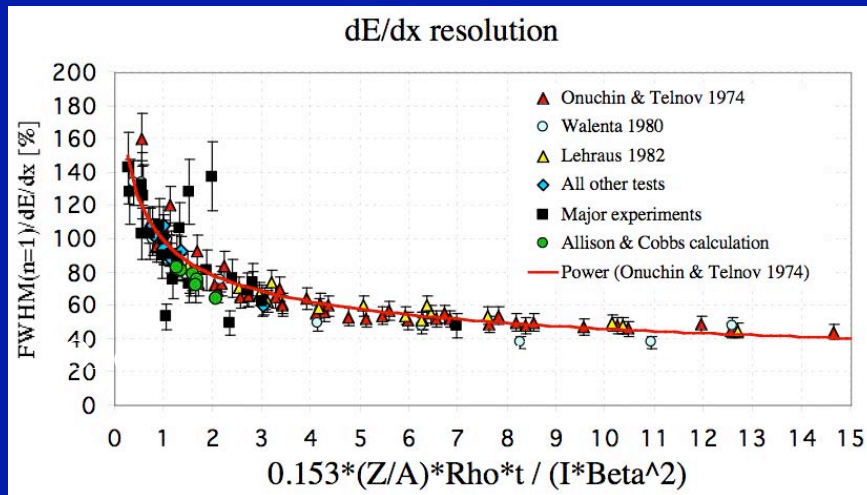


- The density function parameterization is important to get an agreement in the relativistic part of the curve.
- Landau formula does not have E_{cut} variable, and therefore does not do that well.
- Although Allison-Cobb MC method is a correct way to do it, I find that the Bethe-Bloch-Sternheimer parameterization is simple, practical and it works.

Prediction of dE/dx resolution

J. Va'vra, Nucl. Instr. & Meth., A453(2000)262, and SLAC-PUB-8356, Jan. 2000, and dE_dx = f(beta_gamma) study.xls

**Empirical formula for dE/dx resolution, i.e.,
 $\sigma(dE/dx) = f(\text{electron density in the medium})$:**



n - number of samples

Electron density:
 $n_{el} = N_A * Z * \rho / A$

• **Conclusion of the paper:**

dE/dx: a) **Bethe-Bloch-Sternheimer formula works best.**

b) **Allison - Cobb Monte Carlo agrees with data within ~3%.**

$\sigma(dE/dx)$: Allison - Cobb prediction works well. However, I have found that the empirical fit is a fast and equally correct way to do it.

TOF PID technique

Principle is simple:

$$\Delta t = (L_{\text{path}}/c) * (1/\beta_1 - 1/\beta_2) = (L_{\text{path}}/c) * [\sqrt{1+(m_1c/p)^2} - \sqrt{1+(m_2c/p)^2}] = \\ \sim (L_{\text{path}}c/2p^2) * (m_1^2 - m_2^2)$$

Therefore expected particle separation:

$$N_{\sigma} = [(L_{\text{path}}c/2p^2) * (m_1^2 - m_2^2)] / \sigma_{\text{Total}}$$

where

$$\sigma_{\text{Total}} \sim \sqrt{[(\sigma_{\text{TTS}}/\sqrt{N_{\text{pe}}})^2 + (\sigma_{\text{Chromatic}}/\sqrt{N_{\text{pe}}})^2 + \sigma_{\text{Electronics}}^2 + \sigma_{\text{Track}}^2 + \sigma_{\text{T0}}^2]}$$

$\sigma_{\text{Electronics}}$ - electronics contribution ~ 10 ps

$\sigma_{\text{Chromatic}}$ - chromatic term = f (photon path length) ~ 5 -45 ps for path lengths 10-50 cm long

σ_{TTS} - transit time spread ~ 35 ps for the best MCP-PMT detectors

σ_{Track} - timing error due to track length L_{path} (poor tracking in the forward direction) ~ 5 -10 ps

σ_{T0} - start time dominated by the SuperB crossing bunch length ~ 20 -25 ps (?)

- **In the plot I consider:**

a) **“Pixilated” TOF resolutions:** $\sigma_{\text{Total}} \sim 15, 25$ and 50 ps

where **15 ps** was obtained in the test beam and bench tests, **25 ps** is probably the best one can do at SuperB, and **50 ps**, if we screw up (?)

b) **“DIRC-like” TOF resolution:** $\sigma_{\text{Total}} \sim 40$ ps.

“DIRC-like” TOF detector - simple

$$\sigma_{\text{Total}} \sim \sqrt{[\sigma_{\text{Electronics}}^2 + (\sigma_{\text{Chromatic}} / \sqrt{(\epsilon_{\text{Geometrical_loss}} * N_{\text{pe}})^2} + (\sigma_{\text{TTS}} / \sqrt{\epsilon * N_{\text{pe}}})^2 + \sigma_{\text{Track}}^2 + \sigma_{\text{bar thickness}}^2 + \sigma_{\text{detector coupling to bar}}^2 + \sigma_{\text{to}}^2]}$$

$\sigma_{\text{Electronics}}$ - electronics contribution ~ 10 ps

$\sigma_{\text{Chromatic}}$ - chromatic term = f (photon path length) ~ 40 ps for path lengths ~ 25 cm (Bialkali)

σ_{TTS} - transit time spread ~ 35 ps

σ_{Track} - timing error due to track length L_{path} (poor tracking in the forward direction) ~ 5 - 10 ps

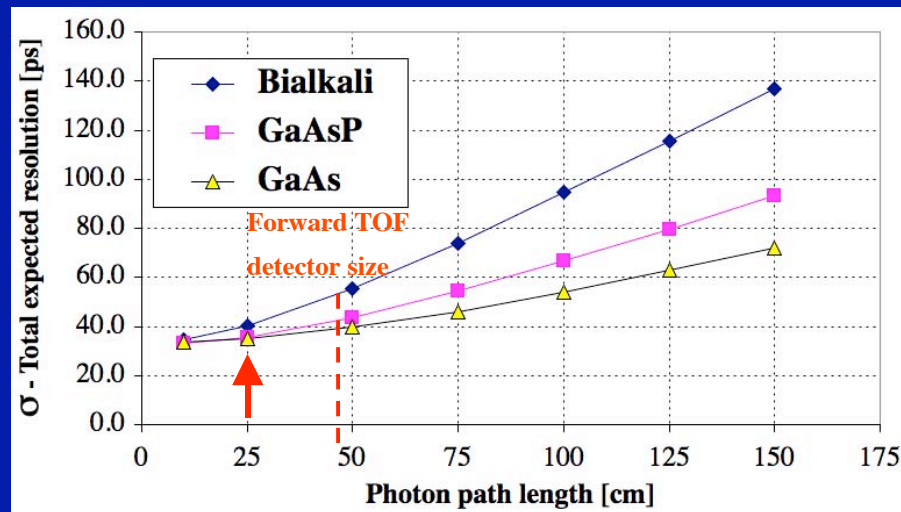
$\sigma_{\text{detector coupling to bar}}$ - timing error due to detector coupling to the bar ~ 10 ps

$\sigma_{\text{bar thickness}}$ - timing error due to bar thickness ~ 12 ps

σ_{to} - start time dominated by the SuperB crossing bunch length ~ 25 ps

$\epsilon_{\text{Geometrical_loss}}$ - loss due to a geometrical acceptance (“reject” bad photons) $\sim 20\%$

Total expected final resolution:



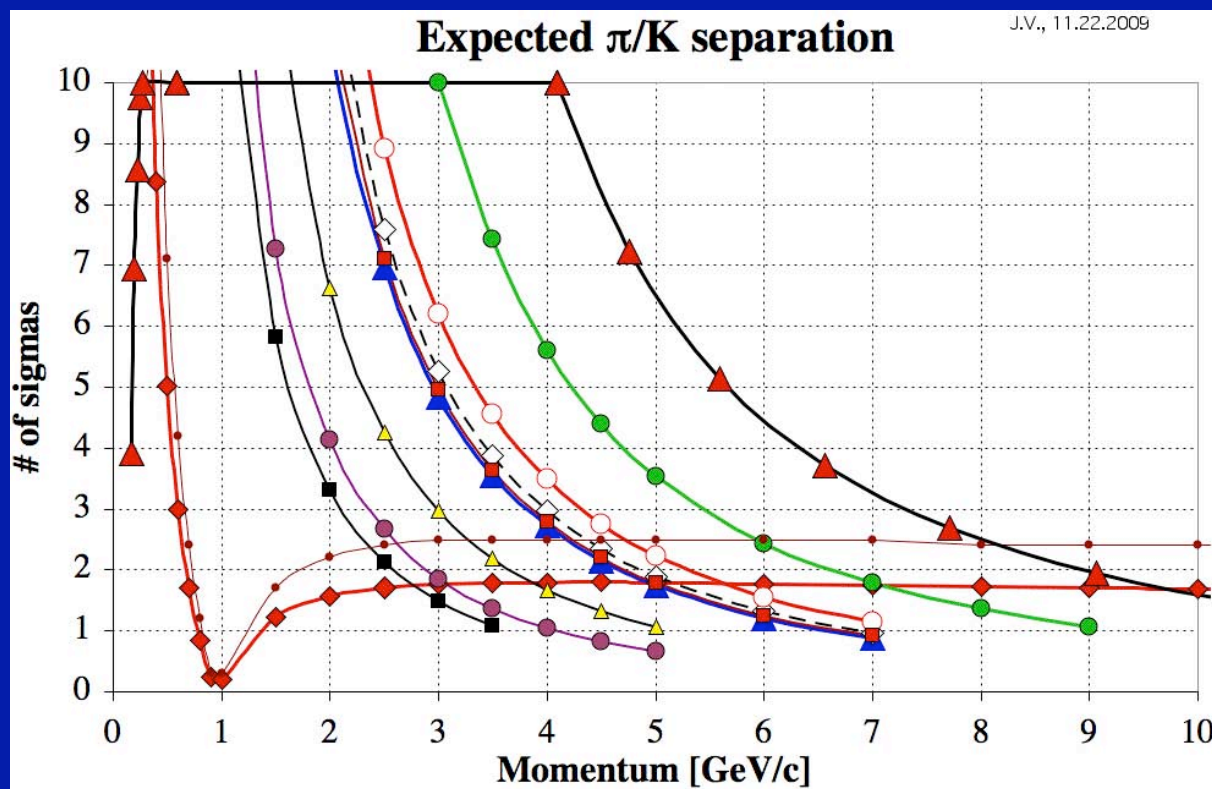
- **Bialkali photocathode will give $\sigma_{\text{ave}} \sim 40$ ps at best.**

RICH PID separation under “ideal” condition

$$N_{\sigma} = [\theta_c (m_1) - \theta_c (m_2)] / \sigma_{\theta_c}(\text{tot}) - \text{separation in number of sigmas}$$

- **In the plot I consider:**
 - a) Calculate $\theta_c (m_1) - \theta_c (m_2)$
 - b) **BaBar DIRC resolution:** $\sigma_{\text{Total}} \sim 2.4$ mrad/track
 - c) **FDIRC resolution:** Scale the performance by a ratio:
 $\sigma_{\text{DIRC}} / \sigma_{\text{FDIRC}} \sim 9.6 \text{ mrad} / 7.5 \text{ mrad} \sim 1.28$, i.e., assuming the FDIRC prototype test beam results with a chromatic corrections applied.
 - d) **TOP counter:** This is a problem, as they update results every 2-3 months. In the plot I assume PID separation of 3 sigmas at 4 GeV/c and scale it from there. However, this is for the GaAsP photocathode, which is probably “unobtainium” because of the cost and difficulty to make it. For a multi-alkali photocathode the prediction will be worse, but do not know how much worse at the moment.

Plot again - caption separated



- ◆— Barrel dE/dx (n=30, t=1.2cm, 1 bar, 80%He+20%C4H10) - JV's calculation for 90deg
- ▲— BaBar DIRC performance
- Japanese Aerogel Forward RICH - based on test beam results (Krizan)
- ◇— TOP counter for Super Belle (GaAsP photocathode) - MC (Inami)
- FDIRC for SuperB (3mm pixels, chromatic correction) - Based on test beam results (JV)
- 'Pixilated' TOF (1.8 m path, sigma = 15 ps) - Based on test beam results (JV)
- ▲— 'Pixilated' TOF (1.8 m path, sigma = 25 ps) - expected 'real' performance (JV)
- 'Pixilated' TOF (1.8 m path, sigma = 50 ps) - 'worst' possible performance (JV)
- DIRC-like TOF (1.8 m path, 40cm size, sigma ~ 40ps) - 'best' possible performance (JV)
- Forward dE/dx (n=30, t=3.5cm, 1 bar, 80%He+20%C4H10) - JV's calculation for 20deg
- ▲— Focusing Aerogel RICH, 4 aerogel + 1 water layers. - MC (Kononov)