Drell-Yan lepton angular distributions in perturbative QCD

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Outline:

- Angular coefficients in pQCD
- Extraction of coefficients at NLO
- Numerical results
- New ATLAS results

in collaboration with Martin Lambertsen

Introduction / Motivation

Lepton angular distribution in Drell-Yan (photon ex.):

$$\frac{d\sigma}{d^4q \, d\Omega} = \frac{\alpha^2}{2\pi N_c Q^2 s^2} \Big(W_T \left(1 + \cos^2 \theta\right) + W_L \left(1 - \cos^2 \theta\right) + W_\Delta \sin^2 \theta \cos^2 \theta \Big)$$
$$+ W_\Delta \sin 2\theta \cos \phi + W_{\Delta\Delta} \sin^2 \theta \cos 2\phi \Big)$$



$$\frac{d\sigma}{d^4q \, d\Omega} = \frac{\alpha^2}{2\pi N_c Q^2 s^2} \Big(W_T \left(1 + \cos^2 \theta\right) + W_L \left(1 - \cos^2 \theta\right) + W_\Delta \sin^2 \theta \cos^2 \theta \Big)$$
$$+ W_\Delta \sin 2\theta \cos \phi + W_{\Delta\Delta} \sin^2 \theta \cos 2\phi \Big)$$

$$\frac{dN}{d\Omega} \equiv \left(\frac{d\sigma}{d^4q}\right)^{-1} \frac{d\sigma}{d\Omega d^4q}$$
$$= \frac{3}{4\pi} \frac{1}{\lambda+3} \left[1 + \lambda \cos^2\theta + \mu \sin 2\theta \cos \phi + \frac{\nu}{2} \sin^2\theta \cos 2\phi\right]$$

where:

$$\lambda = \frac{W_T - W_L}{W_T + W_L} , \quad \mu = \frac{W_\Delta}{W_T + W_L} , \quad \nu = \frac{2W_{\Delta\Delta}}{W_T + W_L}$$

Brandenburg, Mirkes, Nachtmann '93



• clearly a relevant issue for extraction of Boer-Mulders fct.



Peng, Chang, McClellan, Teryaev 2015; (CMS 2015)

ATLAS 2016



Angular coefficients in pQCD



$$W_P = \sum_{a,b} \int dx_a dx_b f_a(x_a,\mu) f_b(x_b,\mu) \widehat{W}_{P,ab}(x_a P_a, x_b P_b, q, \alpha_s(\mu),\mu)$$
$$(P = T, L, \Delta, \Delta\Delta)$$

• \widehat{W}_P partonic structure fcts.: perturbative

$$\widehat{W}_P = \frac{\alpha_s}{\pi} \,\widehat{W}_P^{(1)} + \left(\frac{\alpha_s}{\pi}\right)^2 \,\widehat{W}_P^{(2)} + \dots$$

• zeroth order $q\bar{q} \to V \to \ell^+ \ell^-$:



$$\lambda = 1, \ \mu = \nu = 0$$

- however, has $q_T = 0$
- first non-trivial order (= LO)





 $\lambda \neq 1, \ \mu \neq 0, \ \nu \neq 0$

• but: $1 - \lambda - 2\nu = 0$ (Lam-Tung relation)

• NLO:



first computed by Mirkes '92; Mirkes, Ohnemus '95

New NLO results Lambertsen, WV

• region $q_T \ll Q$:



- all-order resummation very well understood for $W_{\rm T}$ Collins-Soper-Sterman formalism
- and, of course, TMDs...

Boer, Mulders; Boer, Brodsky, Hwang; Lu, Ma; Pasquini, Schweitzer; ...

Bacchetta, Boer, Diehl, Mulders

Extraction of λ , ν at NLO

"How far do we get w/ fixed-order pQCD?"

 a lot of work in recent decade on perturbative corrections for Drell-Yan process

Hamberg, van Neerven, Matsuura; Harlander, Kilgore; Anastasiou, Dixon, Melnikov, Petriello; Melnikov, Petriello; Li, Petriello, Quackenbusch; Catani, Cieri, Ferrera, de Florian, Grazzini; Li, von Manteuffel, Schabinger, Zhu; Anastasiou et al.;

• especially useful: NNLO $\mathcal{O}(\alpha_s^2)$ Monte-Carlo codes

. . .

FEWZ: Melnikov, Petriello; Melnikov, Petriello; Li, Petriello, Quackenbusch DYNNLO: Catani, Cieri, Ferrera, de Florian, Grazzini

• full control over 4-momenta of produced particles, including leptonic decay

$$\lambda = \frac{W_T - W_L}{W_T + W_L} , \quad \nu = \frac{2W_{\Delta\Delta}}{W_T + W_L}$$

Lam, Tung '78:

$$2W_T + W_L = \mathcal{N} \, \frac{d\sigma}{d^4 q}$$

$$W_T - W_L = \frac{8}{3} \mathcal{N} \left[\frac{d\sigma}{d^4 q} \left(|\cos \theta| > \frac{1}{2} \right) - \frac{d\sigma}{d^4 q} \left(|\cos \theta| < \frac{1}{2} \right) \right]$$

$$W_{\Delta\Delta} = \frac{\pi}{2} \mathcal{N} \left[\frac{d\sigma}{d^4 q} \left(\cos 2\phi > 0 \right) - \frac{d\sigma}{d^4 q} \left(\cos 2\phi < 0 \right) \right]$$

• lepton momentum:

$$\ell_{\rm CS}^{\mu} = \frac{Q}{2} \begin{pmatrix} 1 \\ \sin\theta\cos\phi \\ \sin\theta\sin\phi \\ \cos\theta \end{pmatrix} \xrightarrow{\text{Lorentz Tr.}} \ell_{\rm cm}^{\mu} = \frac{1}{2} \begin{pmatrix} q_0 \left(1 + \sin\alpha\sin\theta\cos\phi\right) + q_L\cos\alpha\cos\phi \\ q_T + Q\frac{\sin\theta\cos\phi}{\cos\alpha} \\ Q\sin\theta\sin\phi \\ q_L \left(1 + \sin\alpha\sin\theta\cos\phi\right) + q_0\cos\alpha\cos\theta \end{pmatrix}$$

$$\sin \alpha \equiv \frac{q_T/Q}{\sqrt{1 + (q_T/Q)^2}}, \qquad \cos \alpha \equiv \frac{1}{\sqrt{1 + (q_T/Q)^2}}$$

• from this:

$$\cos \theta = -\frac{2\,\ell_{\rm cm}\cdot\mathcal{P}_1}{(Q^2+q_T^2)\cos\alpha} \qquad \cos 2\phi = 1 - \frac{2\,(\ell_{\rm cm}\cdot\mathcal{P}_2)^2}{q_T^2\left[\frac{Q^2}{4} - \frac{(\ell_{\rm cm}\cdot\mathcal{P}_1)^2}{Q^2+q_T^2}\right]}$$

where
$$\mathcal{P}_1^{\mu} \equiv \begin{pmatrix} q_L\\ 0\\ 0\\ q_0 \end{pmatrix} \qquad \mathcal{P}_2^{\mu} \equiv q_T \begin{pmatrix} 0\\ 0\\ -1\\ 0 \end{pmatrix}$$

Numerical results

- use FEWZ and DYNNLO codes
- excellent agreement. NLO results below are for FEWZ
- benchmark against our own LO code
- MSTW proton PDFs GRV pion PDFs no genuine nuclear effects (other than isospin)
- choose scale $\,\mu=Q$; scale dependence weak
- NLO computationally very demanding









pp, E = 800 GeV

E866



NA10





 $\pi W, E_{\pi} = 194 \,\mathrm{GeV}$

NA10

$$\pi W, \ E_{\pi} = 252 \,\mathrm{GeV}$$
 E615



• note: $\lambda = \frac{W_T - W_L}{W_T + W_L}$

ightarrow positivity constraint $\lambda \leq 1$ Lam, Tung '78



New ATLAS results



- dependence on scales and PDFs is small
- do not expect TMD effects to be relevant beyond $q_T = 10 \text{ GeV}$
- a regime where $log(q_T/Q)$ is not particularly large
- region $q_T \ll Q$:





• low-q_T structure functions at $O(\alpha_s)$ (CS frame):

$$\begin{split} \widehat{W}_{T}^{(1)} &= -C_{F} \frac{\alpha_{s}}{2\pi} \frac{2\log(q_{T}^{2}/Q^{2}) + 3}{q_{T}^{2}} + \dots \\ \widehat{W}_{L}^{(k)} &= 2 \widehat{W}_{\Delta\Delta}^{(k)} = -C_{F} \frac{\alpha_{s}}{2\pi} \left(2\log(q_{T}^{2}/Q^{2}) + 3 \right) + \dots \\ \\ \text{Boer, WV} \end{split}$$

• leading logs same to all orders in $\widehat{W}_T, \, \widehat{W}_L, \, \widehat{W}_{\Delta\Delta}$

Berger, Qiu, Rodriguez

• to leading log:

$$\begin{split} W_T^{\text{Resum}} &= \left(1 - \frac{1}{2} \frac{Q_{\perp}^2/Q^2}{1 + Q_{\perp}^2/Q^2} \right) \frac{W^{\text{Resum}}}{2} \\ W_L^{\text{Resum}} &= \frac{Q_{\perp}^2/Q^2}{1 + Q_{\perp}^2/Q^2} \frac{W^{\text{Resum}}}{2} \\ W_{\Delta\Delta}^{\text{Resum}} &= \frac{1}{2} \frac{Q_{\perp}^2/Q^2}{1 + Q_{\perp}^2/Q^2} \frac{W^{\text{Resum}}}{2} \end{split}$$

(up to matching)

- differences at next-to-leading log Boer, WV
- still, expect small resummation effects for $~\lambda,~
 u$

$$\nu = \frac{2W_{\Delta\Delta}}{W_T + W_L}$$
 K factors
denominator / numerator



LO/NLO partonic channels for ν :



NNLO effect? We'll know soon...



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The NNLO QCD corrections to Z boson production at large transverse momentum

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Conclusions and outlook:

- have extracted coefficients λ, ν at NLO from FEWZ and DYNNLO codes
- "dispel myth" that pQCD cannot describe data: overall reasonable description
- not meant to argue that there are no effects beyond fixed-order pQCD
- serious studies of Boer-Mulders should include pQCD radiative effects (including resummation)
- clear call for better data in fixed-target regime