

# COMPASS studies of the transverse structure of the nucleon

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Trieste University and INFN

*on behalf of the COMPASS Collaboration*



**3D Parton Distributions: path to the LHC**

LNf 29/11 - 2/12/2016

# COMPASS



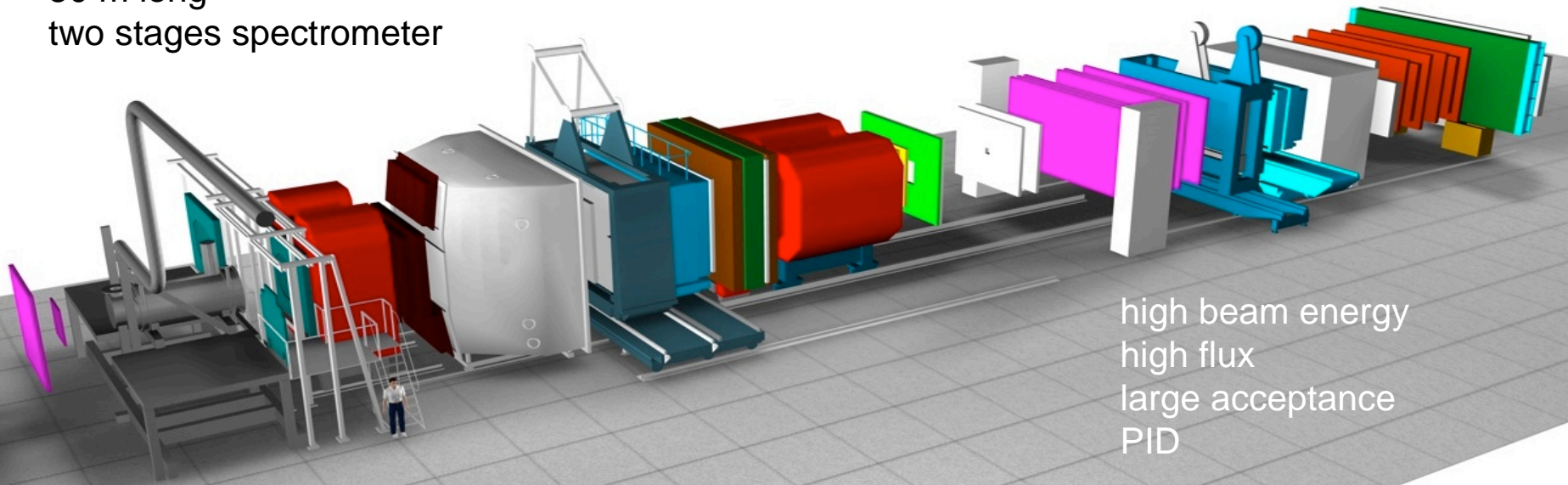
approved in 1997, data taking 2002 → 2018,  
plans for beyond 2020 being prepared

## fixed target experiment at CERN SPS

high energy (160-200 GeV) muon and hadron beams  
polarised and unpolarised targets

*Common  
Muon and  
Proton  
Apparatus for  
Structure and  
Spectroscopy*

50 m long  
two stages spectrometer



# COMPASS



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## **physics program**

- **pion, kaon and proton beams, LH<sub>2</sub> and nuclear targets** 2008, 2009, 2012
  - spectroscopy - looking for exotics
  - pion/kaon polarisability
- **muon beam - nucleon structure SIDIS, DVCS** 2002-2007, 2010 2011
  - quark and gluon helicities - **longitudinally polarised p and d targets**
  - transversity and TSA - **transversely polarised p and d targets**
  - GPDs - **liquid hydrogen target** [2012] 2016,2017
- **pion beam - nucleon structure**
  - Drell-Yan - **transversely polarised p target** [2014] 2015 (2018)

# COMPASS



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**used or being used  
to study TMDs**

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this talk:

## nucleon spin structure from SIDIS off transversely polarised and unpolarised targets

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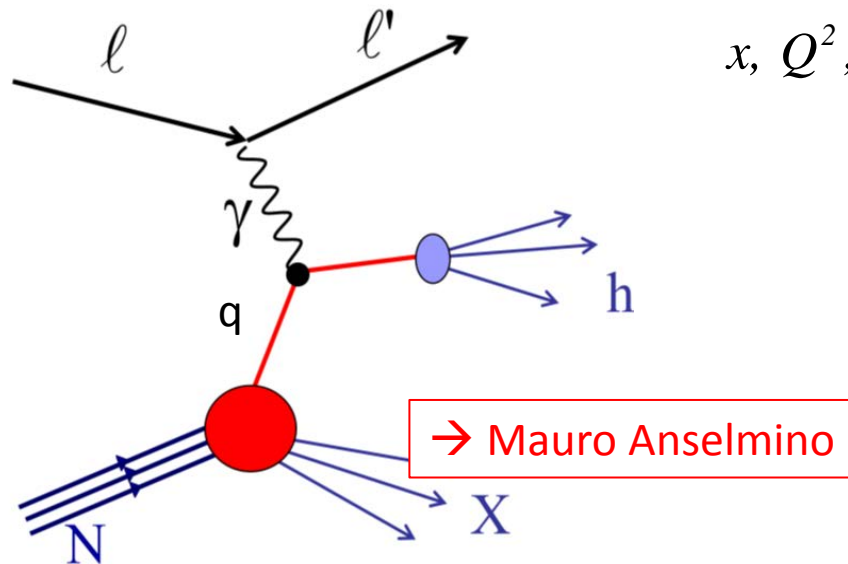
B. Parsamyan

A. Bressan

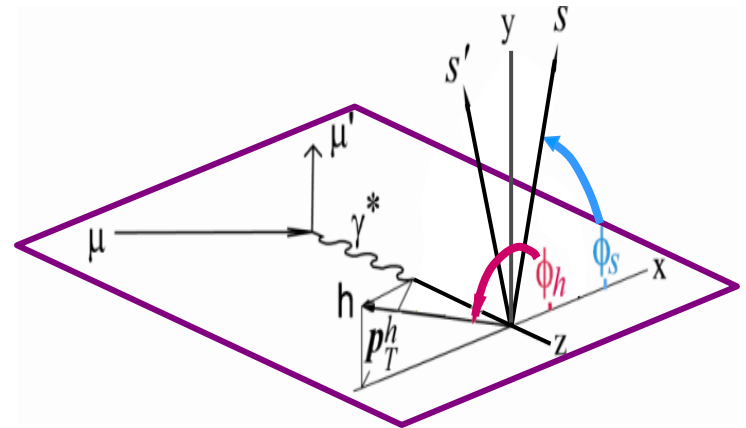
C. Quintans

# why SIDIS

a simple process, a special tool



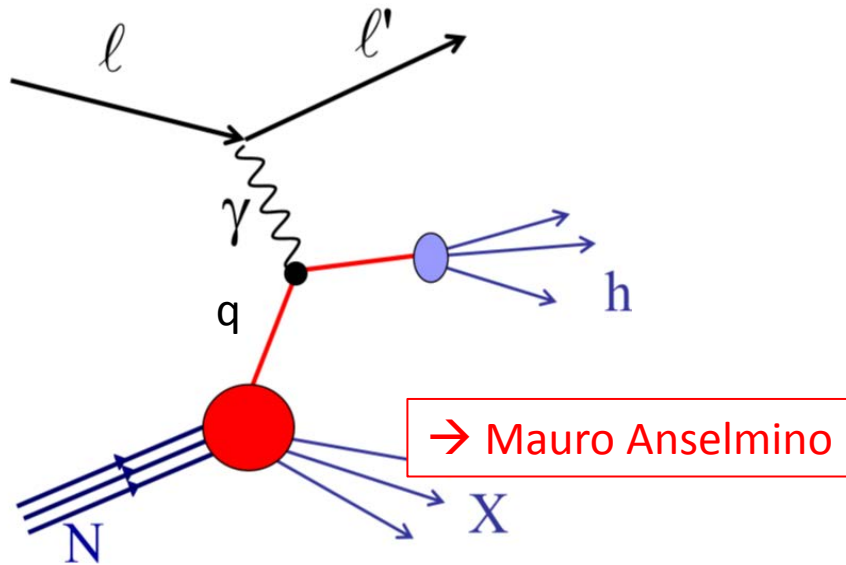
$x, Q^2; \quad z, P_T, \quad \phi_h, \phi_S$



$$d\sigma^{lp \rightarrow lhX} \sim \sum_q e_q^2 f_q(x, \mathbf{k}_\perp) \cdot d\sigma^{\ell q \rightarrow \ell q} \cdot D_q^h(z, \mathbf{p}_T)$$

# why SIDIS

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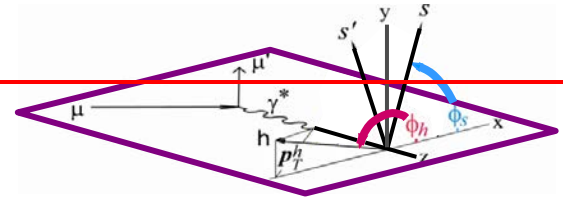
		nucleon		
		U	L	T
quark	U	$f_1$		$f_{1T}^\perp$
	L		$g_1$	$g_{1T}$
	T	$h_1^\perp$	$h_{1L}^\perp$	$h_1$ $h_{1T}^\perp$

$$d\sigma^{lp \rightarrow \ell h X} \sim \sum_q e_q^2 f_q(x, \mathbf{k}_\perp) \cdot d\sigma^{\ell q \rightarrow \ell q} \cdot D_q^h(z, \mathbf{p}_T)$$

all the TMD PDFs appear in the cross-section  
and the different effects can be disentangled

p, n, d targets, final state particle identification  
→ flavor separation

# why SIDIS



$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} =$$

$$\frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right.$$

$$+ \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h}$$

$$+ S_{\parallel} \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] + S_{\parallel} \lambda_e \left[ \sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_h F_{LL}^{\cos\phi_h} \right]$$

$$+ |S_{\perp}| \left[ f_{IT}^{\perp} D_1 \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \right.$$

$$+ \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)}$$

$$+ \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \left. \left. \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] \right.$$

$$+ |S_{\perp}| \lambda_e \left[ g_{IT}^{\perp} D_1 \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \right.$$

$$\left. \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \right\},$$

14 azimuthal modulations

measured  
at COMPASS, HERMES, JLab



# why SIDIS

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \right.$$

$$+ S_{\parallel} \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] + S_{\parallel} \lambda_e \left[ \sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_h F_{LL}^{\cos\phi_h} \right]$$

all of them have been measured at COMPASS on p and d with a 160 GeV muon beam

very clear signals for the azimuthal asymmetries on p related to **transversity** and **Sivers PDFs** only

$$+ |S_{\perp}| \left[ \underbrace{f_{1T}^{\perp} D_1}_{\text{blue oval}} \left[ \underbrace{\sin(\phi_h - \phi_S)}_{\text{yellow oval}} \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \right.$$

$$+ \varepsilon \underbrace{\sin(\phi_h + \phi_S)}_{\text{yellow oval}} F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \underbrace{\sin(3\phi_h - \phi_S)}_{\text{yellow oval}} F_{UT}^{\sin(3\phi_h - \phi_S)} \left. \right]$$

$$+ \underbrace{h_{1T}^{\perp} H_1^{\perp}}_{\text{red oval}} \left[ \underbrace{h_1 H_1^{\perp}}_{\text{blue oval}} + \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right]$$

$$+ |S_{\perp}| \lambda_e \left[ \underbrace{g_{1T} D_1}_{\text{red oval}} \left[ \sqrt{1-\varepsilon^2} \underbrace{\cos(\phi_h - \phi_S)}_{\text{yellow oval}} F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \right.$$

$$\left. \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \right\},$$

8 azimuthal modulations

# transversity PDF

$$\Delta_T q, h_1^q$$

# accessing transversity

(single hadron) **Collins asymmetry**

$$A_{Coll} \sim \frac{\sum_q e_q^2 h_1^q \otimes H_{1q}^\perp}{\sum_q e_q^2 f_1^q \cdot D_{1q}}$$



Collins FF  
independent information  
from  $e^+e^- \rightarrow hadrons$

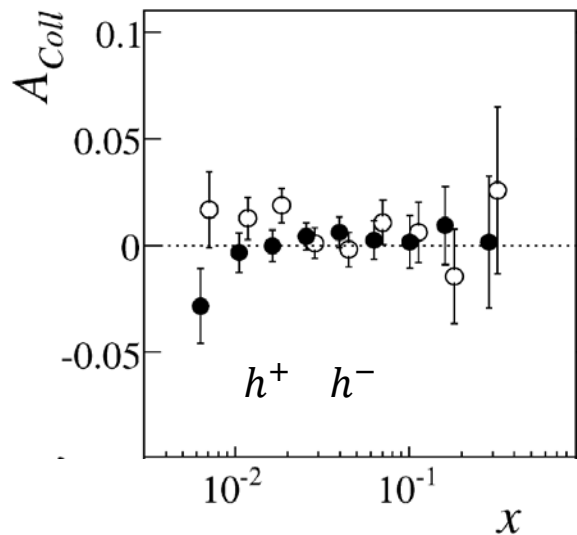
amplitude of the  
 $\sin(\phi_h + \phi_S + \pi)$  modulation

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**final results on deuteron**



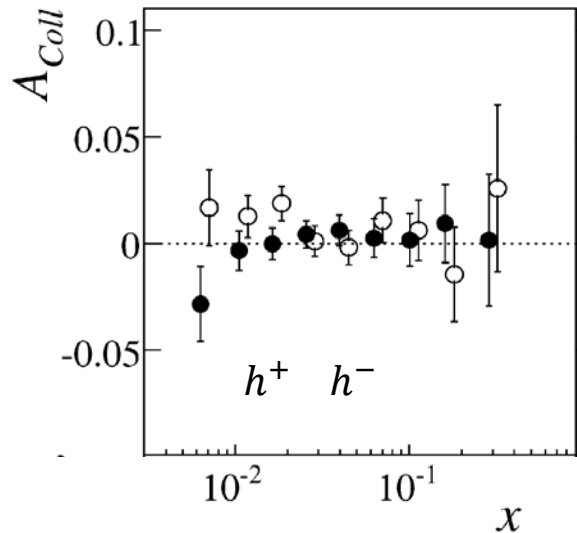
2002-2004 data  
NPB765 2007, PLB673 2009

# accessing transversity

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**final results on deuteron**

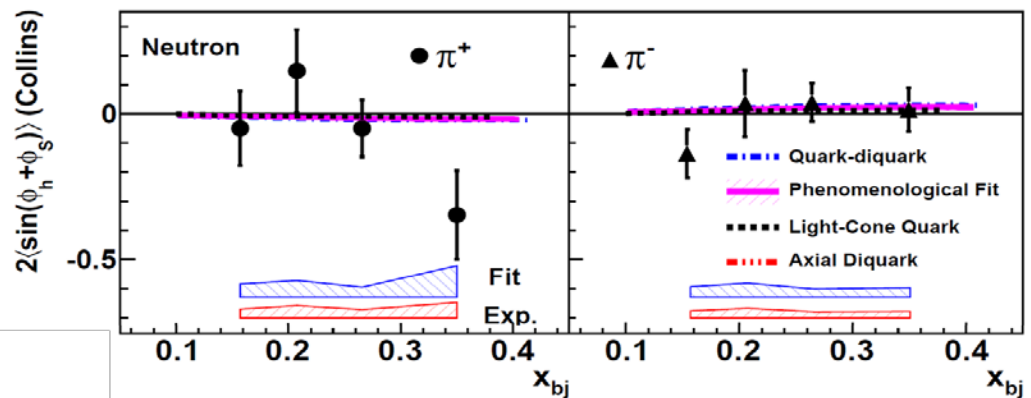


2002-2004 data  
NPB765 2007, PLB673 2009

and neutron



Hall A PRL107, 2011



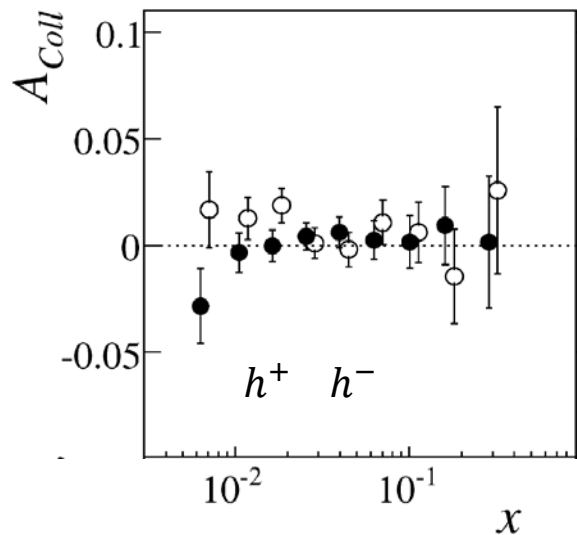


# accessing transversity

(single hadron) **Collins asymmetry**

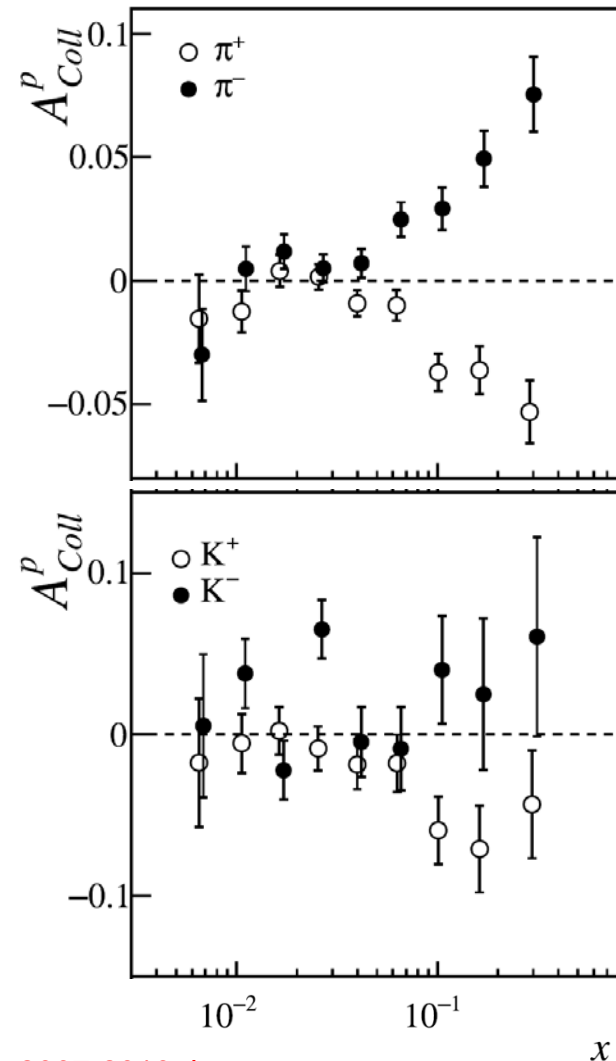
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## final results on deuteron



2002-2004 data  
NPB765 2007, PLB673 2009

## and on proton



2007-2010 data  
PLB744 2015



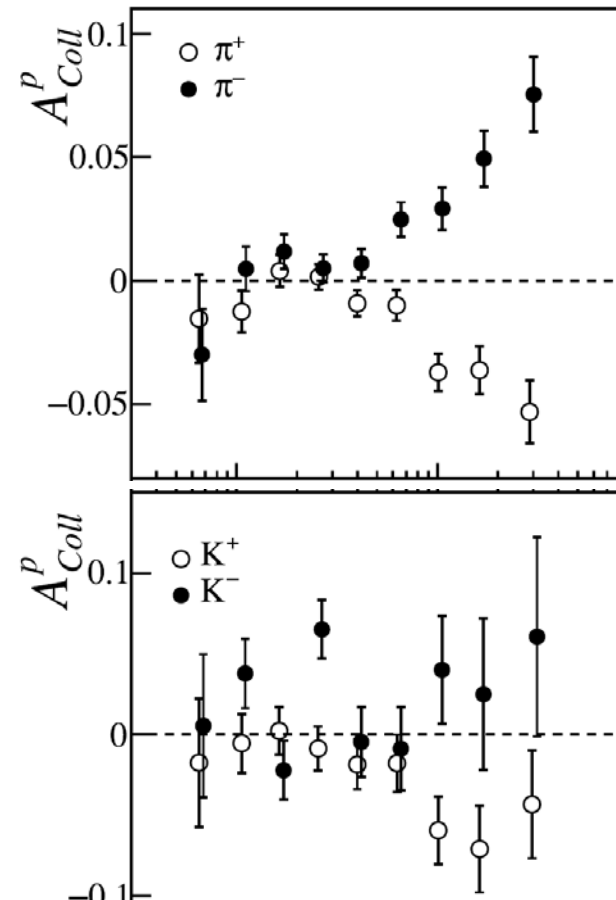
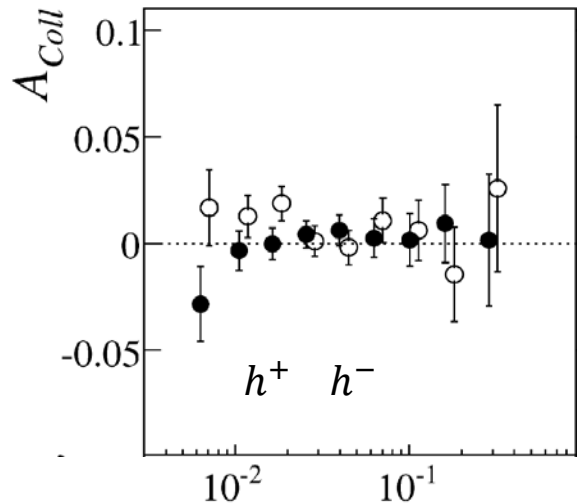
# accessing transversity

and on proton

(single hadron) **Collins asymmetry**

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final results on deuteron



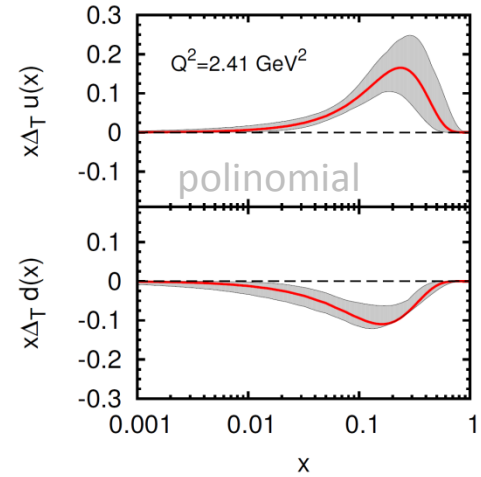
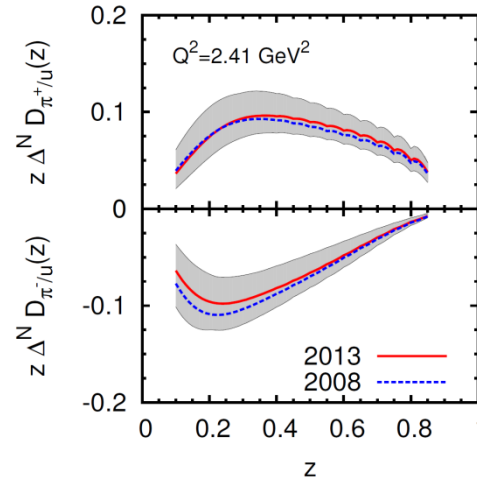
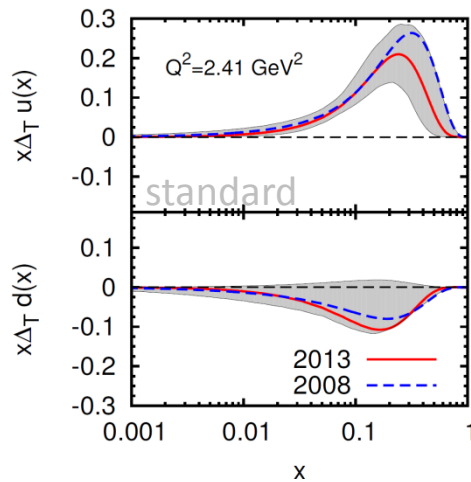
used with the HERMES p data and the corresponding  $e^+e^-$  results (Belle) to extract  $h_1^q$  and  $H_{1q}^\perp$  by several groups since 2005

# accessing transversity

simultaneous fit of SIDIS p & d, and  $e^+e^-$  data

very good  $\chi^2$

Anselmino  
et al.,  
PRD87 2013



●  $\delta u = 0.39^{+0.18}_{-0.12}$

●  $\delta d = -0.25^{+0.30}_{-0.10}$

▲  $\delta u = 0.31^{+0.16}_{-0.12}$

▲  $\delta d = -0.27^{+0.10}_{-0.10}$

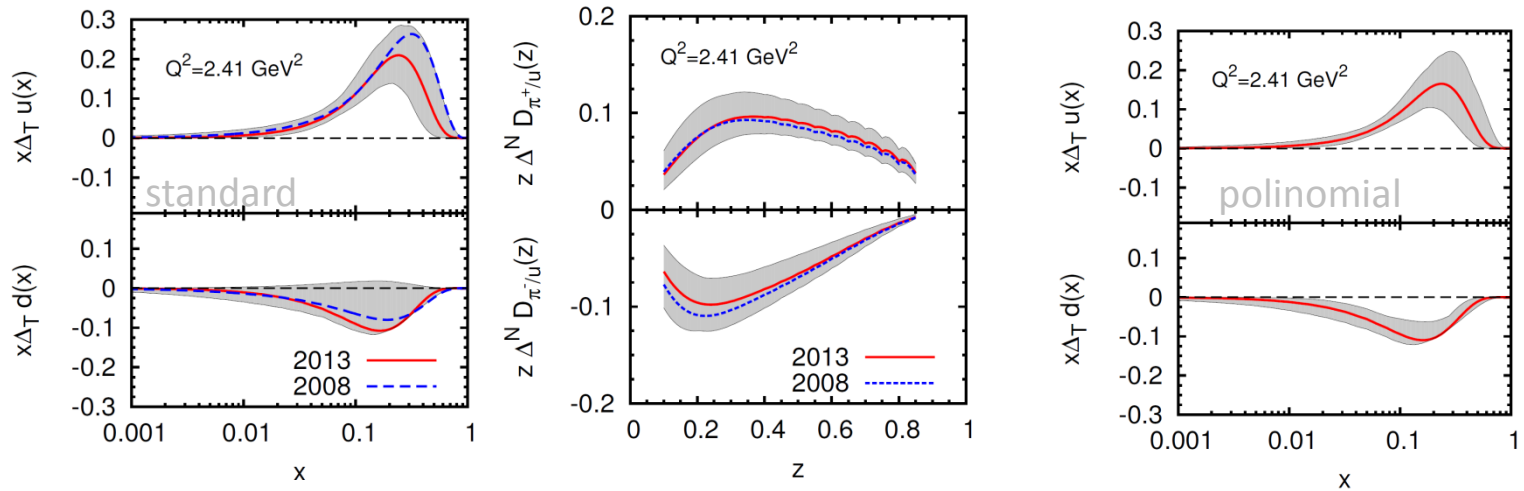


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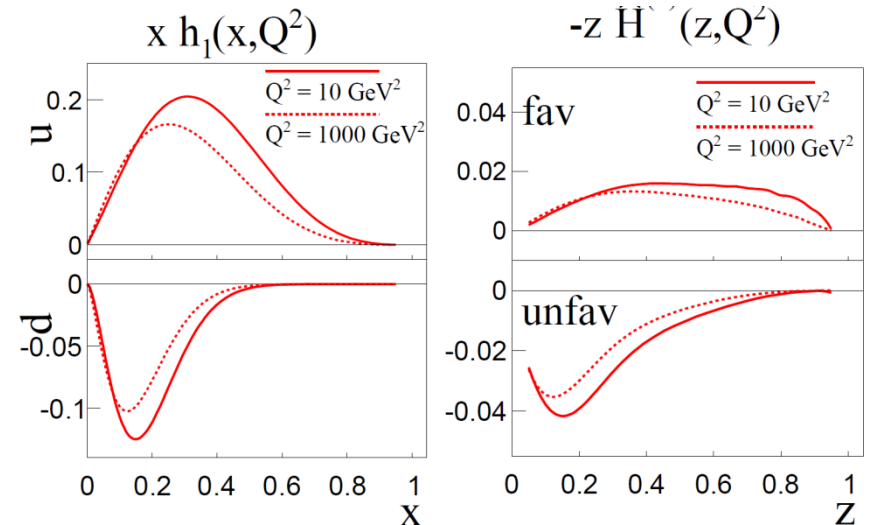
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- ▲  $\delta u = 0.31^{+0.16}_{-0.12}$
- ▲  $\delta d = -0.27^{+0.10}_{-0.10}$

Kang et al, PRD91 2015

$$\delta u^{[0.0065, 0.35]} = +0.30^{+0.12}_{-0.08}$$

$$\delta d^{[0.0065, 0.35]} = -0.20^{+0.28}_{-0.11}$$

higher order corrections,  $xz$



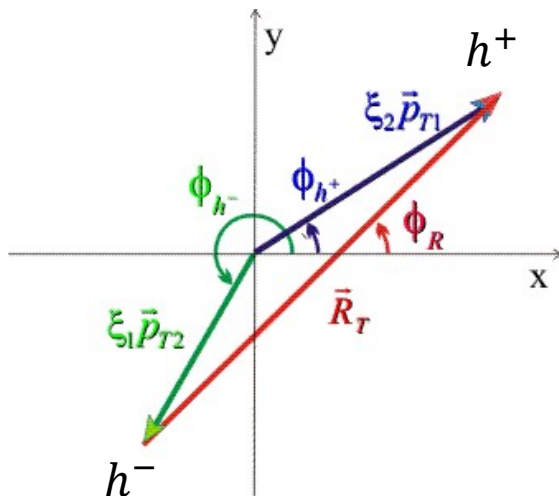
# accessing transversity - 2

measurement of the **dihadron asymmetry**

$$A_{2h} \sim \frac{\sum_q e_q^2 h_1^q \cdot H_q^\perp}{\sum_q e_q^2 f_1^q \cdot D_q^{2h}}$$

← DiFF in principle independent of  $H_{1q}^\perp$   
← quantitative information from  $e^+e^- \rightarrow \text{hadrons}$

amplitude of the  $\sin(\phi_R + \phi_S + \pi)$  modulation

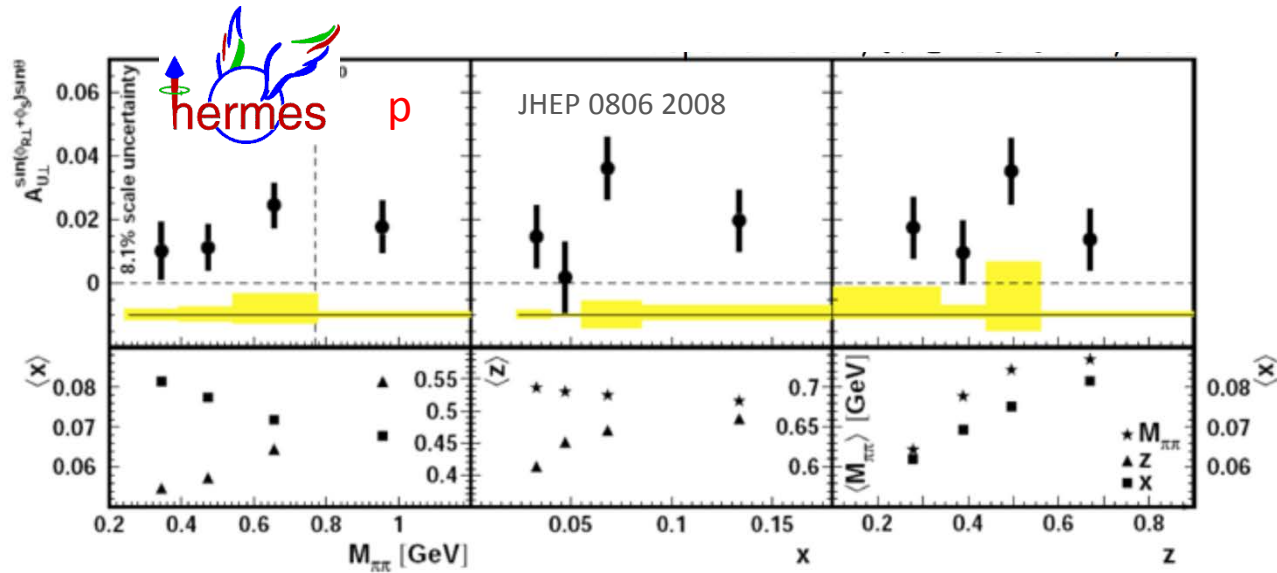


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# accessing transversity - 2

## dihadron asymmetry

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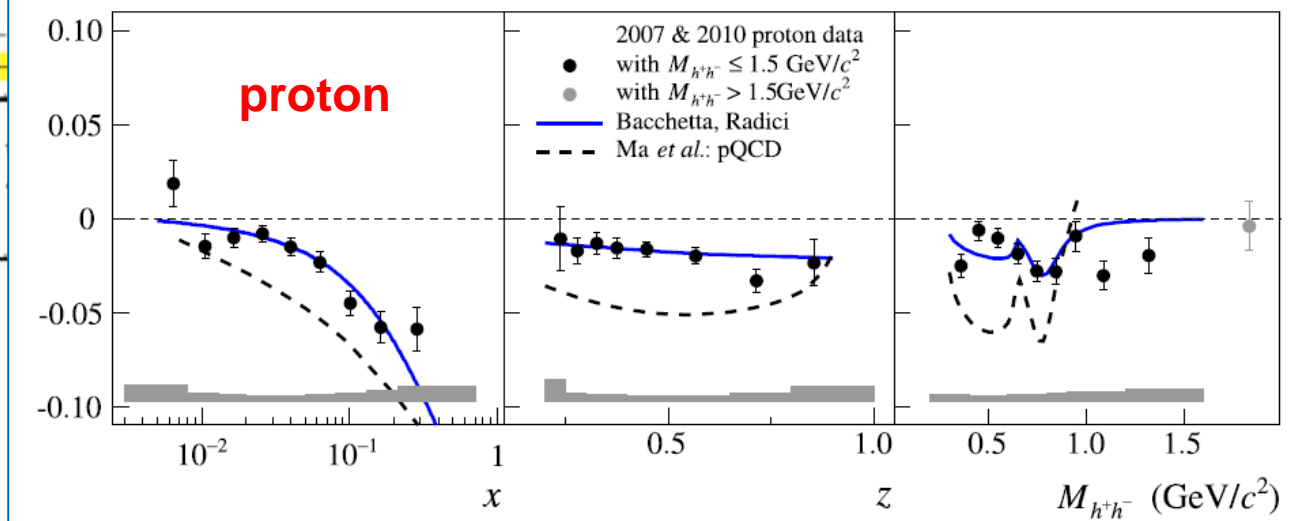
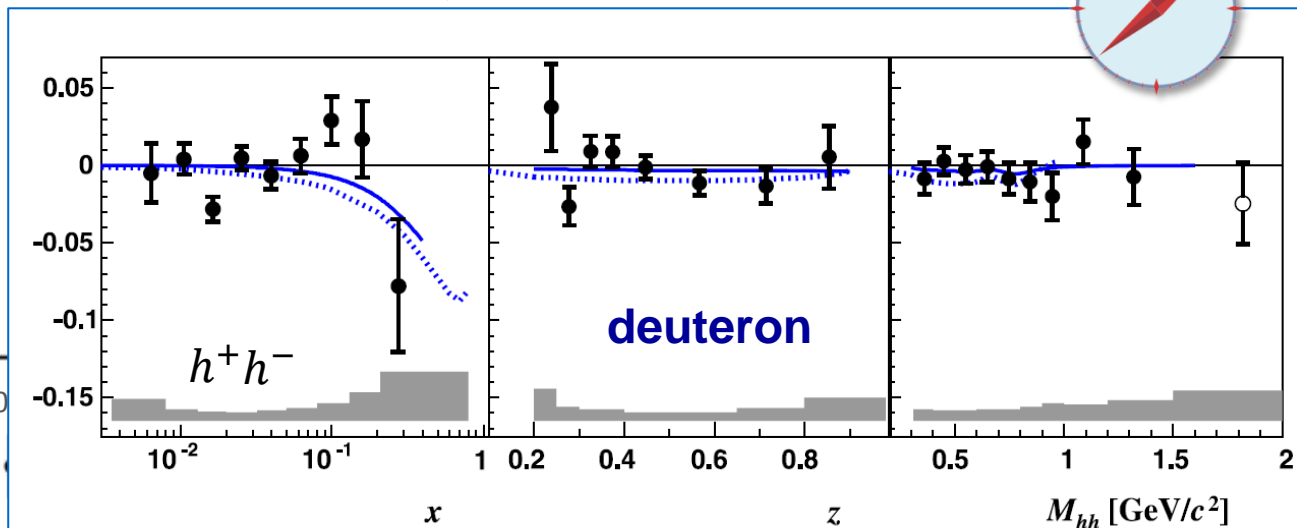
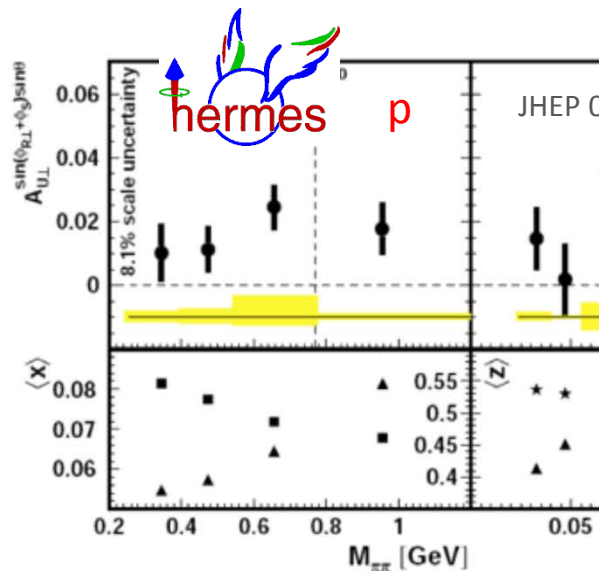
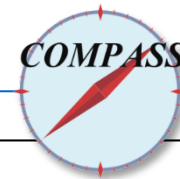


# accessing transversity - 2

## dihadron asymmetry

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PLB 713 2012, PLB736 2014



# accessing transversity - 2

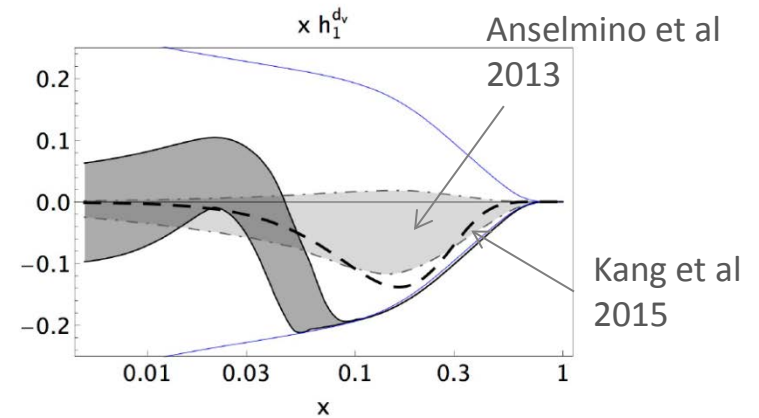
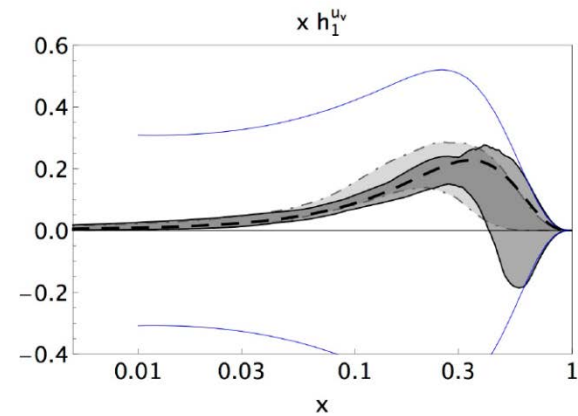
“collinear extraction” of  $h_1^{u_v}$  and  $h_1^{d_v}$

unpolarised DiFF from PYTHIA  
polarised DiFF from Belle  
dihadron asymmetries from  
HERMES (p) COMPASS (p, d)

linear combinations of  $h_1^{u_v}$  and  $h_1^{d_v}$   
fit with different parametrizations

M. Radici et al JHEP 1505 (2015)

*flexible*



# accessing transversity

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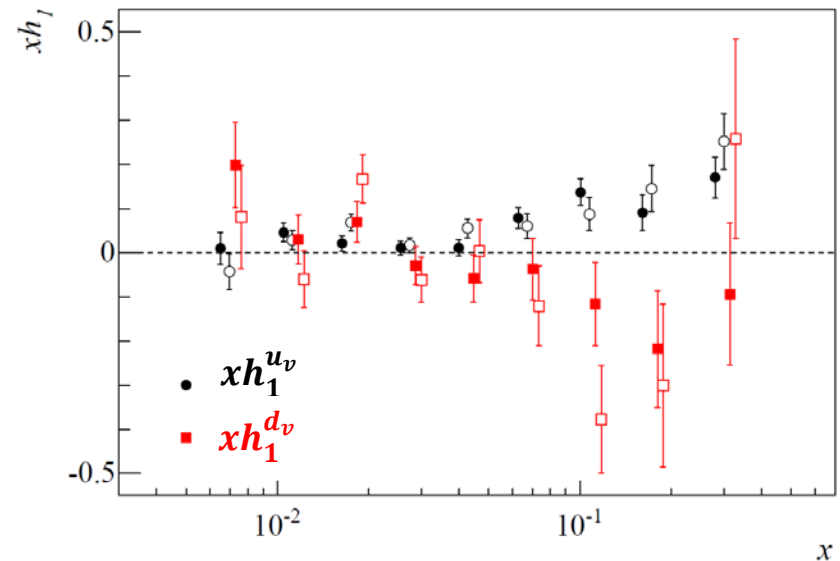
point-by-point extraction of transversity  
from SIDIS asymmetries measured  
on p and d at the same  $x, Q^2$  values  
and analysing power from  $e^+e^-$  asymmetries,  
with no parametrisation of PDFs and FFs

# accessing transversity

point-by-point extraction of transversity from SIDIS asymmetries measured on **p** and **d** at the same  $x, Q^2$  values and analysing power from  $e^+e^-$  asymmetries, with no parametrisation of PDFs and FFs

from COMPASS results for  
Collins asymmetry ● ■ and  
dihadron asymmetries ○ □  
and corresponding Belle data

- agreement between results from Collins and dihadron asymmetries  
*gaussian model with  $G=1$  vs collinear case*
- $h_1^{d_v}$  large errors: statistics with  $d$  marginal
- Collins
  - stable results vs different assumptions  
*in particular for evolution*

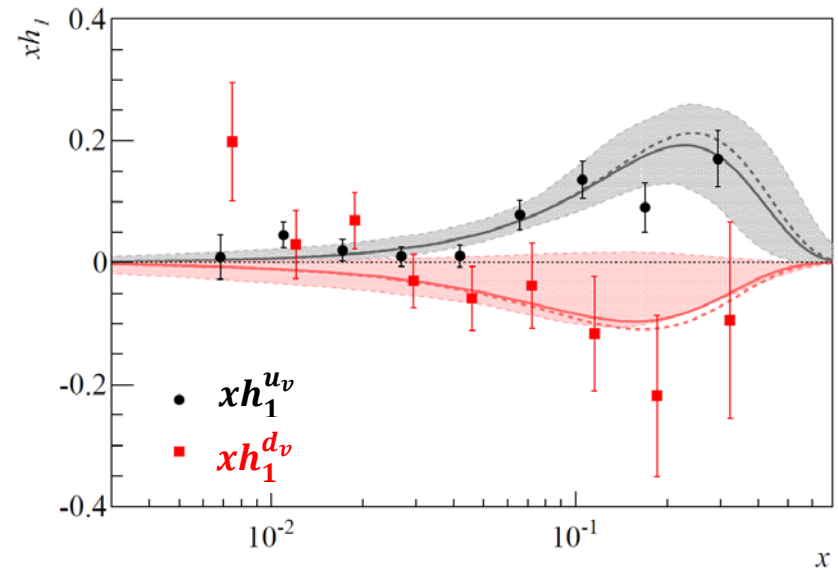


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  - agreement with previous extractions



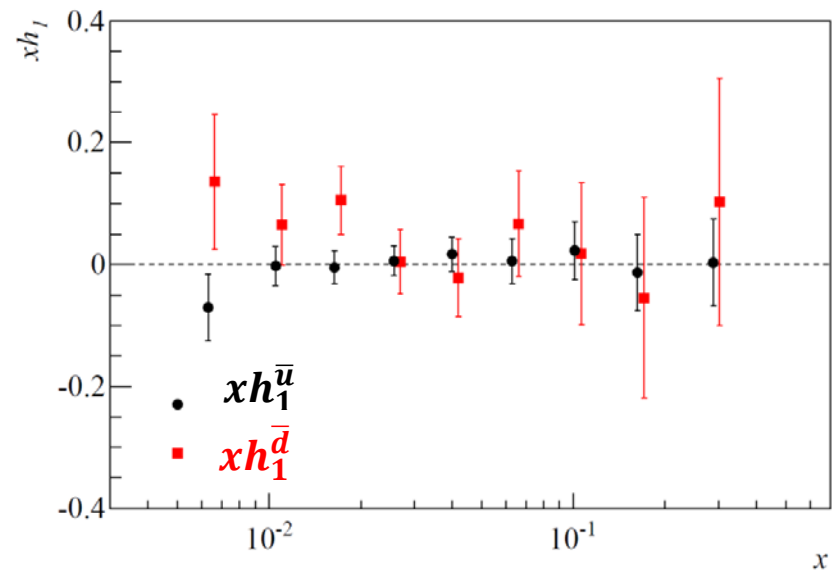
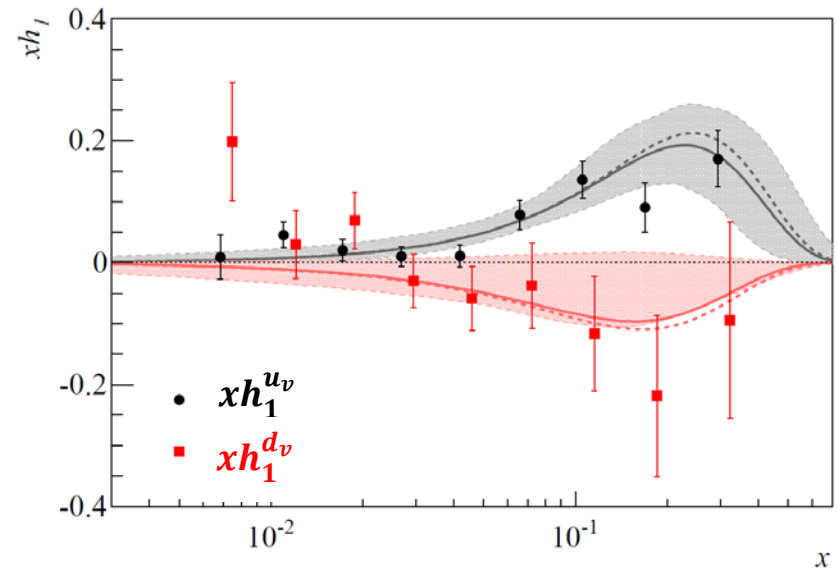


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point-by-point extraction of transversity from SIDIS asymmetries measured on **p** and **d** at the same  $x, Q^2$  values and analysing power from  $e^+e^-$  asymmetries, with no parametrisation of PDFs and FFs

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  - stable results vs different assumptions in particular for evolution
  - agreement with previous extractions
  - allows extraction of **sea quark transversity**



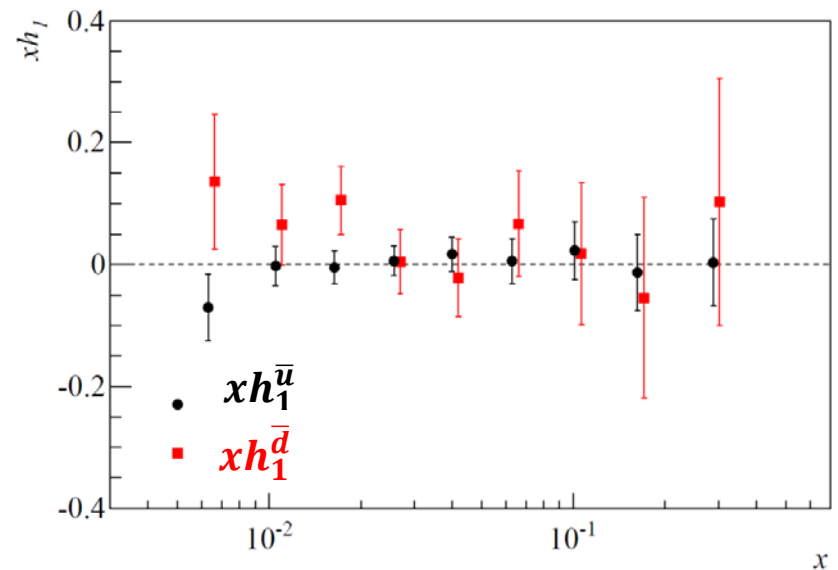
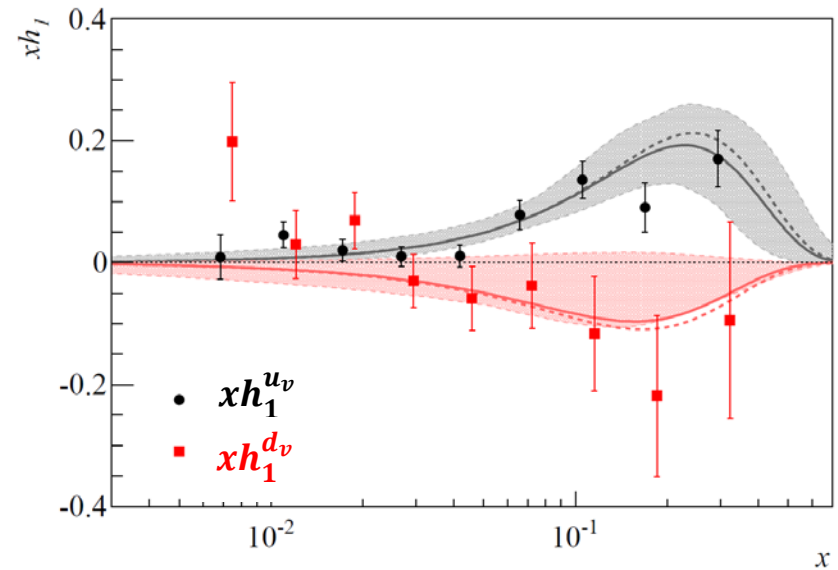
# accessing transversity

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  - stable results vs different assumptions in particular for evolution
  - agreement with previous extractions
  - allows extraction of **sea quark transversity**

a promising method, to be kept in mind by future experiments



# other recent COMPASS results - 1

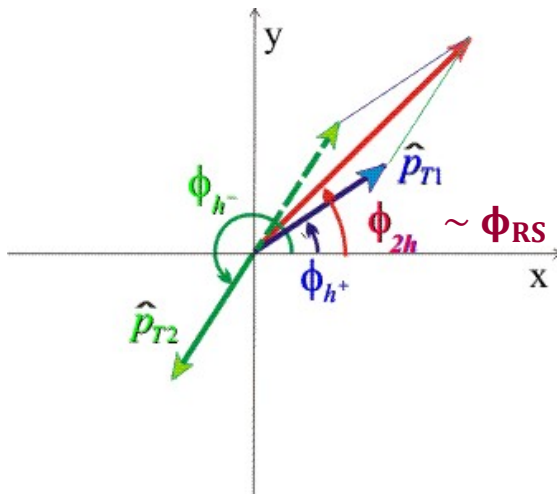
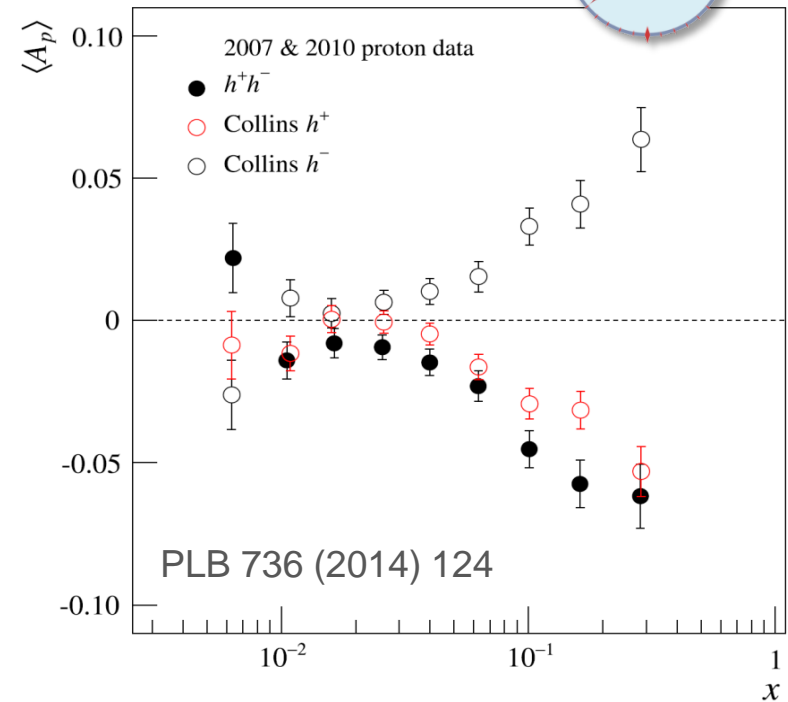
interplay among dihadron and single hadron asymmetries



- Collins asymmetry for  $h^+$  and for  $h^-$   
*“mirror symmetry”*
- dihadron asymmetry  
*only somewhat larger than  $h^+$  Collins*
- meaning of the relevant angles

hints for a common origin  
of the Collins FF and DiFF

Como 2013, DSpin2013, PLB736 (2014) 124



# other recent COMPASS results - 1

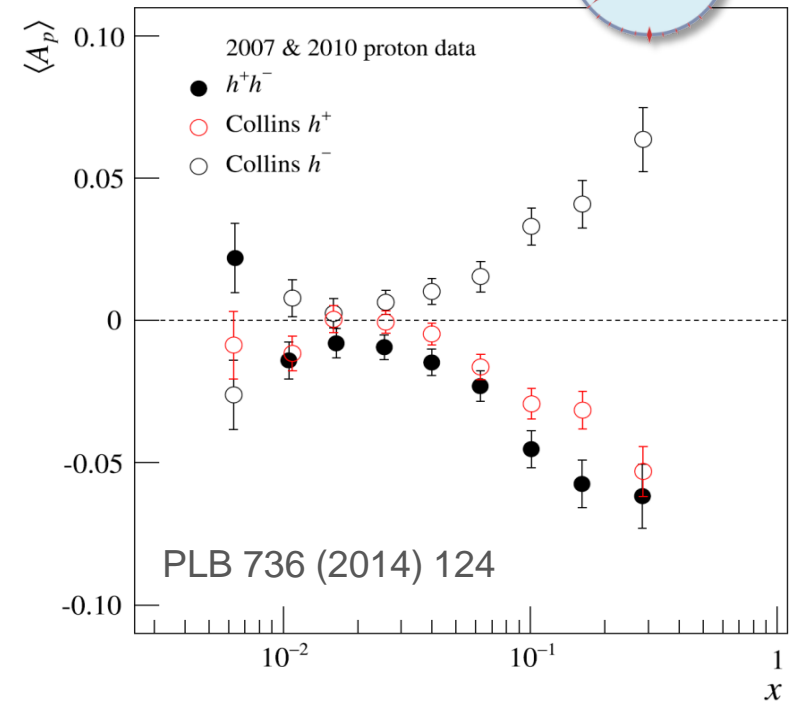
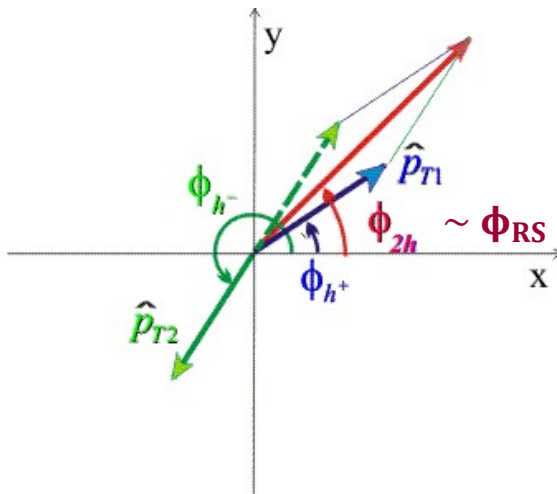
## interplay among dihadron and single hadron asymmetries



- Collins asymmetry for  $h^+$  and for  $h^-$   
“mirror symmetry”
- dihadron asymmetry  
*only somewhat larger than  $h^+$  Collins*
- meaning of the relevant angles

hints for a common origin  
of the Collins FF and DiFF

Como 2013, DSpin2013, PLB736 (2014) 124



further study: look at  
the  $\Delta\phi = \phi_1 - \phi_2$     1:  $h^+$     2:  $h^-$   
dependence of the asymmetries  
one of the COMPASS studies on  
final state hadron correlations

# interplay among dihadron and single hadron asymmetries



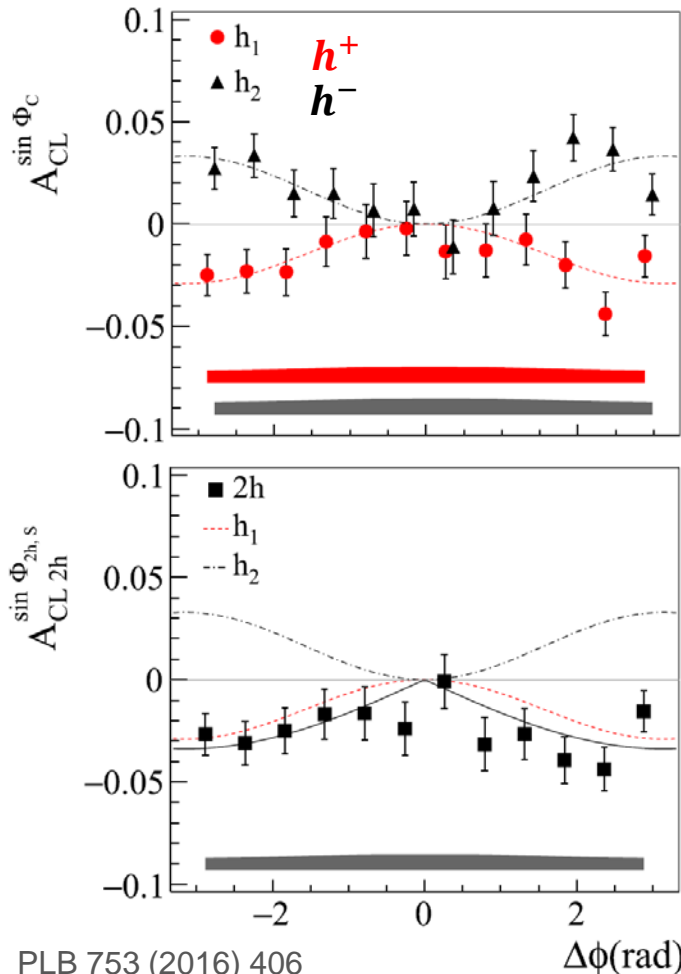
analytically

$$A_{CL1}^{\sin \Phi_C} = a_1 + a_2 \cos \Delta\phi$$

$$A_{CL2}^{\sin \Phi_C} = a_2 + a_1 \cos \Delta\phi$$

agreement with data if  $a_1 = -a_2 = a$

mirror symmetry



$$A_{CL 2h}^{\sin \Phi_{2h,s}} = a \sqrt{2(1 - \cos \Delta\phi)}$$

agreement with data

a very simple relationships among the asymmetries in the “2h sample” they are driven by the **same elementary mechanism**.

ratio of the  $\Delta\phi$  integrated 2h and 1h asymmetries:  $4/\pi$   
*slightly larger than  $h^+$*

can be studied in  $e^+e^-$  ?

# interplay among dihadron and single hadron asymmetries

**new:** preliminary results from a Monte Carlo code for transversely polarized quark jet based on the string fragmentation and including, for the first time, the  $^3P_0$  mechanism

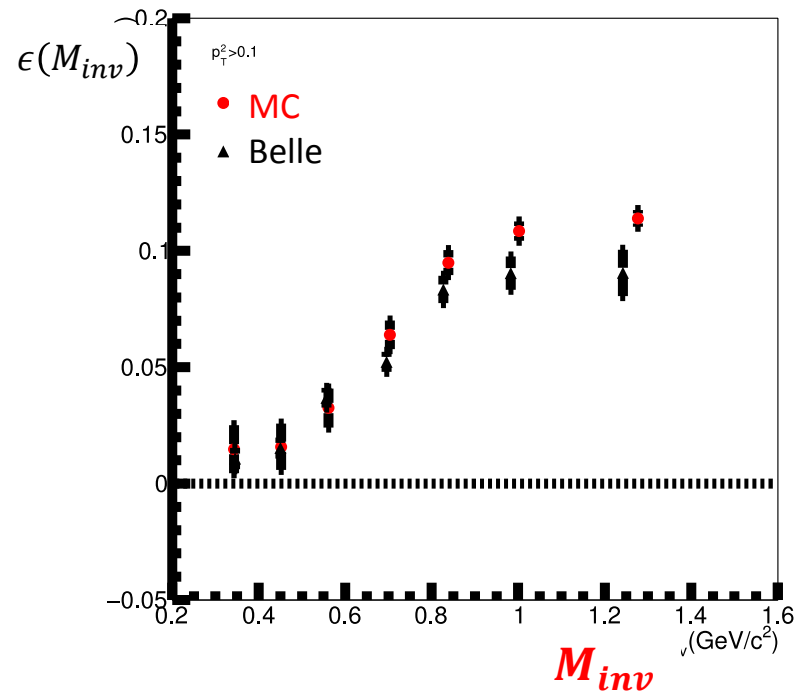
only one free parameter for spin effects

→ X. Artru

results in good qualitative agreement with 1h and 2h asymmetries at COMPASS and Belle:

- $h^+$  and  $h^-$ :
  - mirror symmetry as in COMPASS
  - $a_P$  in agreement with what obtained from Belle data
- $\pi^+\pi^-$  in good agreement with Belle

- $\epsilon(M_{inv}) = \langle a_P^{u \rightarrow \pi^+\pi^-} \rangle a_P^{u \rightarrow \pi^+\pi^-}(M_{inv})$
- $z_h > 0.1, p_T^2 > 0.1 (GeV/c)^2$  for each pion

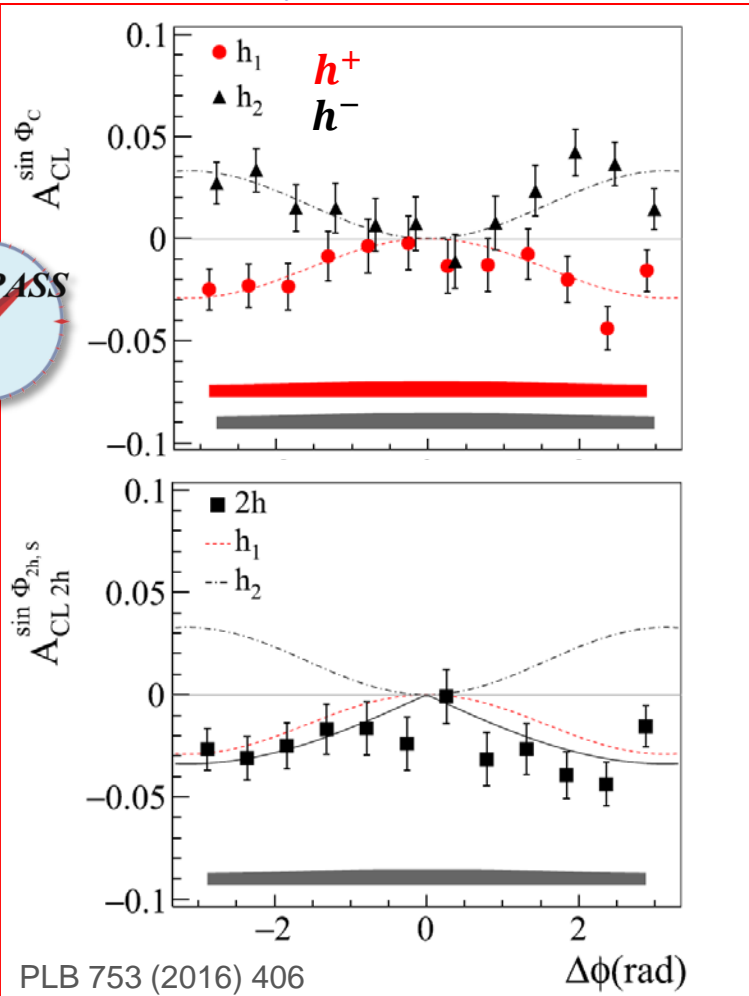


# interplay among dihadron and single hadron asymmetries

**new:** preliminary results from a Monte Carlo code for transversely polarized quark jet based on the string fragmentation and including, for the first time, the  $^3P_0$  mechanism

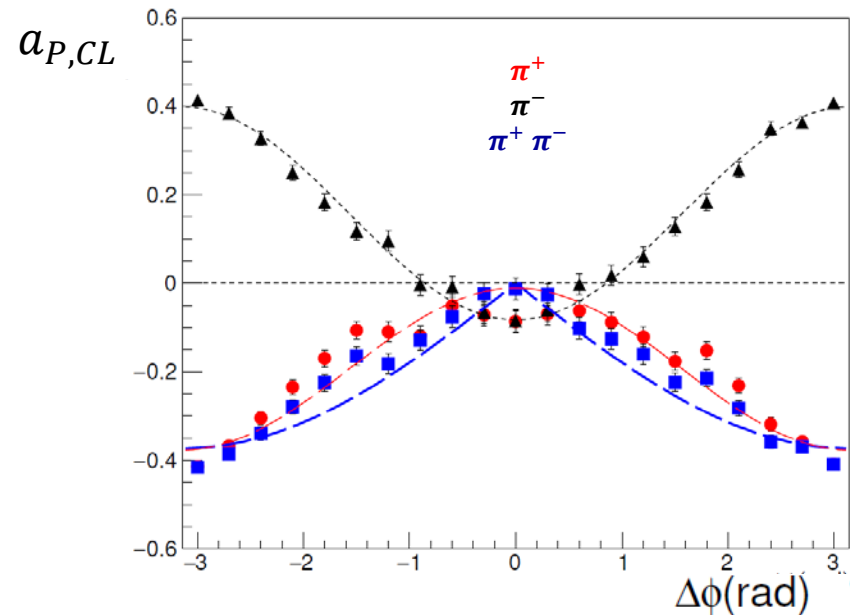
only one free parameter for spin effects

→ X. Artru



*1h and 2h  $a_p$  obtained as COMPASS asymmetries from the same sample of generated events*

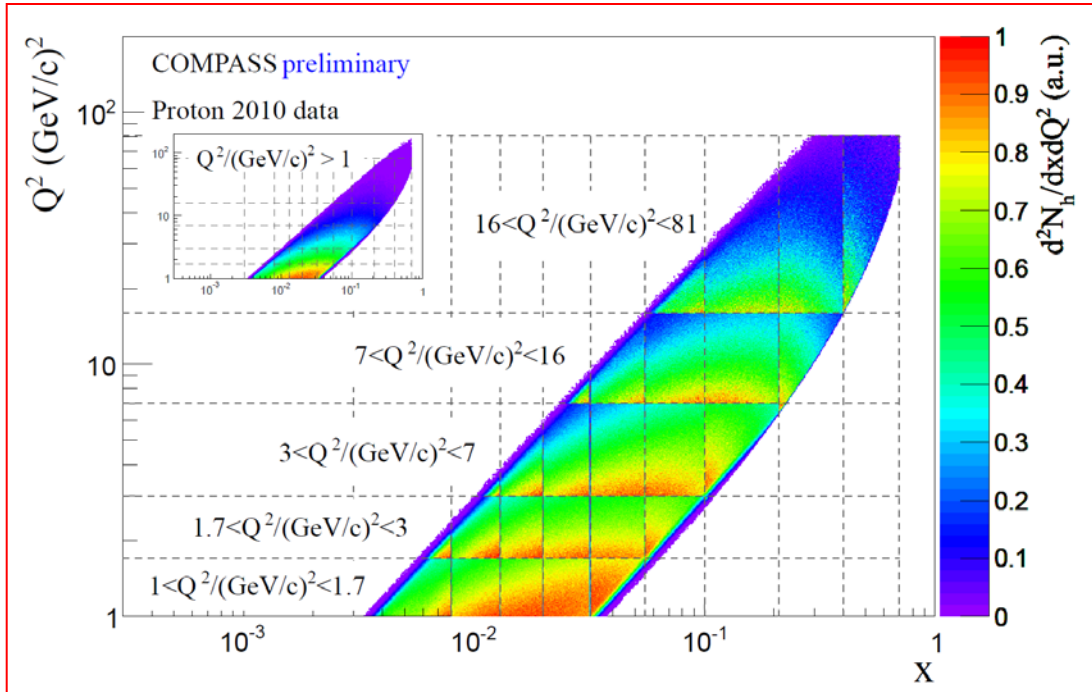
A. Kerbizi talk at SPIN2016



**very encouraging results**

# other recent COMPASS results - 2

multidimensional measurements of the Collins asymmetry



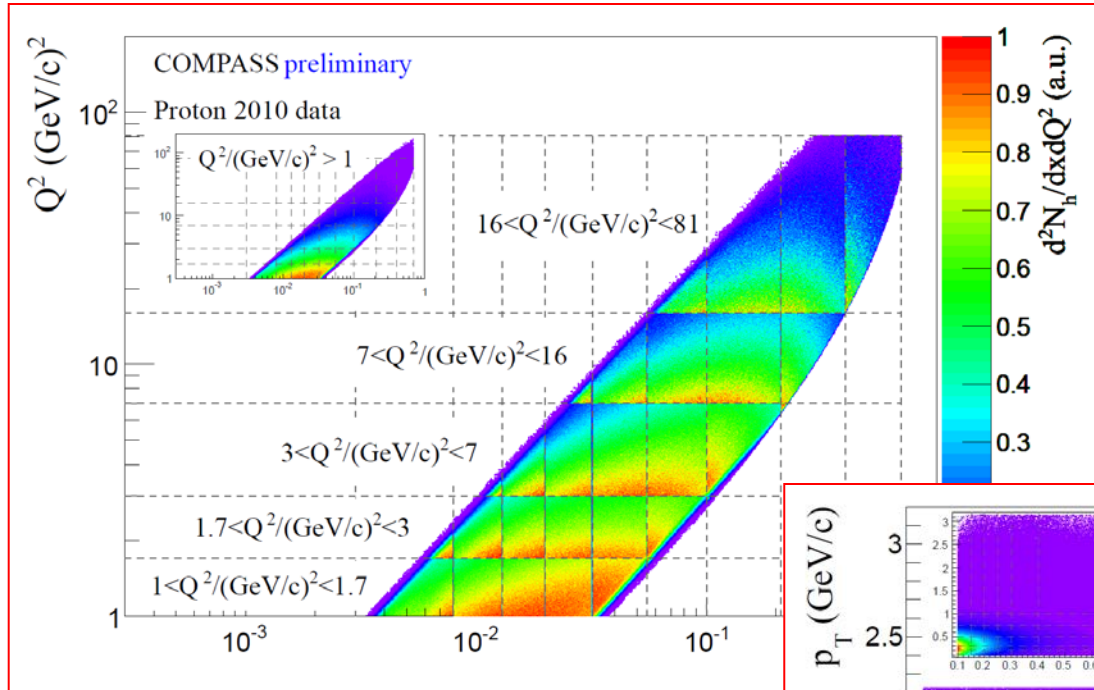
SPIN2014

x- $Q^2$  z- $p_T$  binning



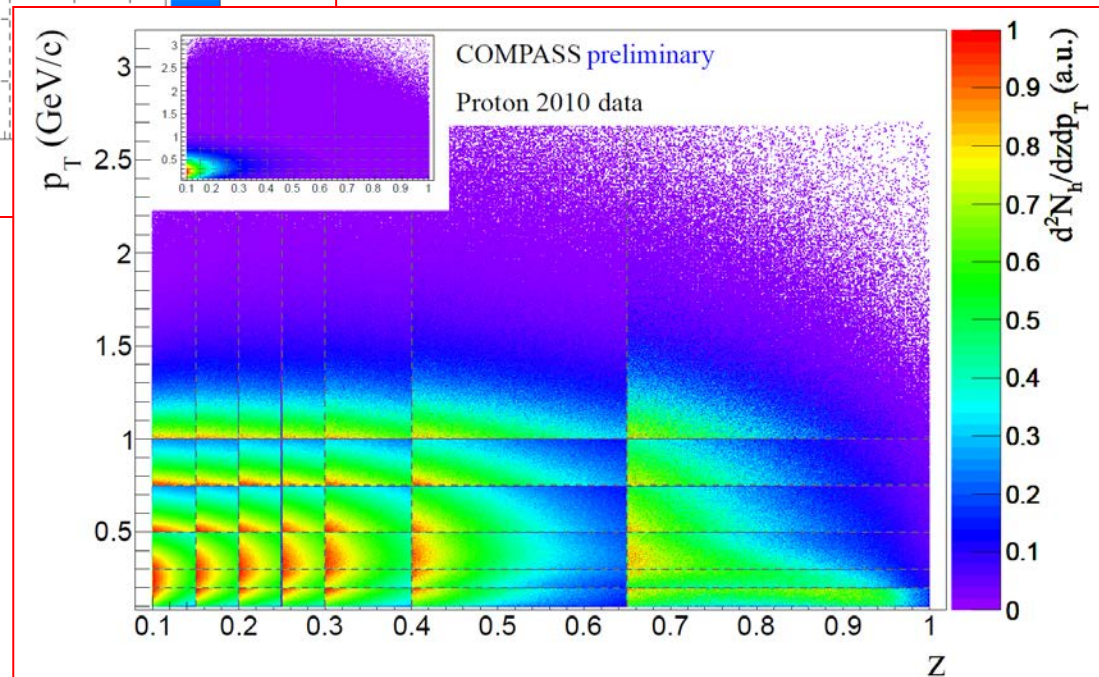
# other recent COMPASS results - 2

multidimensional measurements of the Collins asymmetry

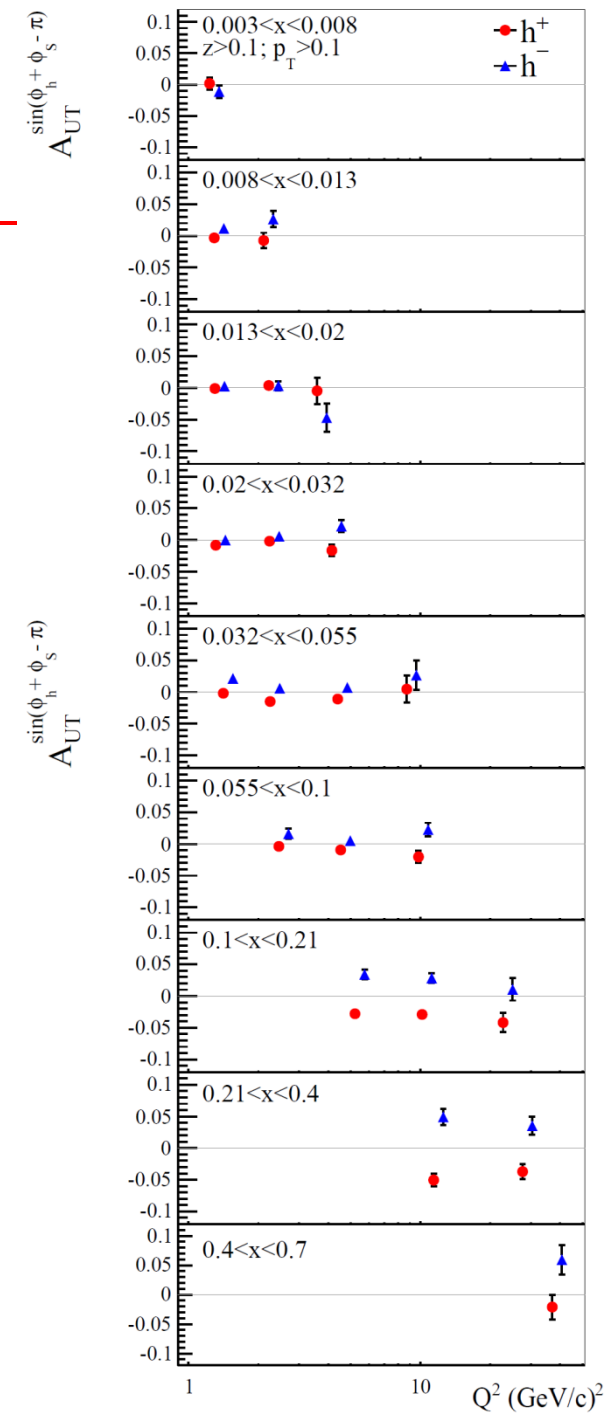


SPIN2014

$x$ - $Q^2$   $z$ - $p_T$  binning



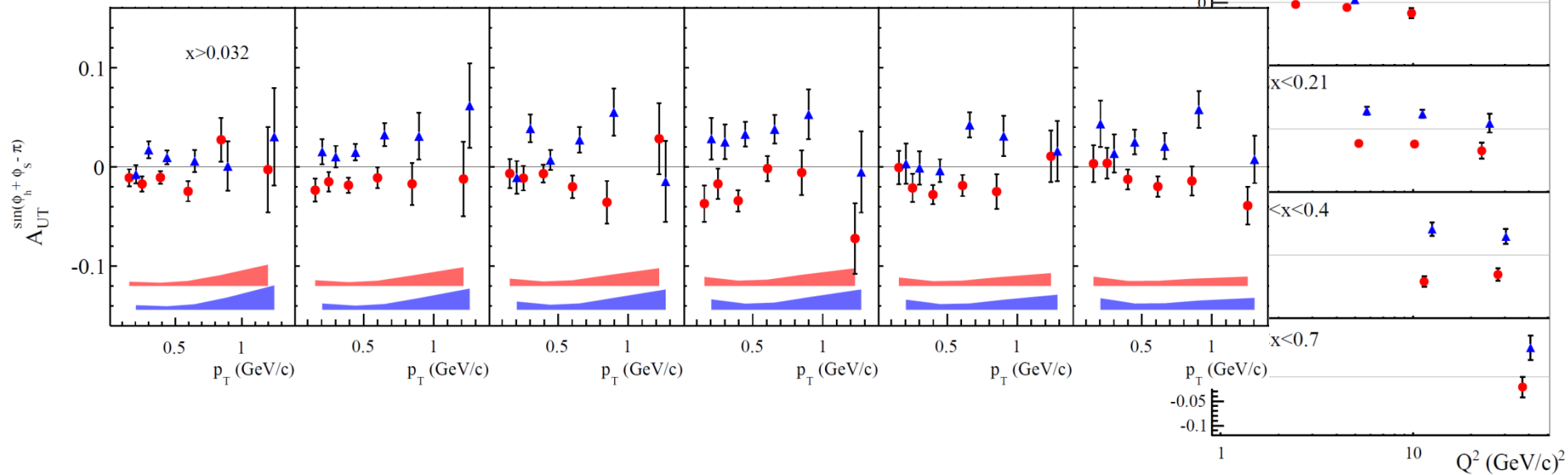
# multidimensional measurements of the Collins asymmetry



# multidimensional measurements of the Collins asymmetry



*relevant data to test the parametrisations of  $h_1^q$  and  $H_{1q}^\perp$  obtained from the fits of the integrated asymmetries*



## other recent COMPASS results - 3

### coming soon:

new results on  $\Lambda$  polarisation

an independent way to access transversity

one of the first proposed methods

$$\mathcal{P}_y^{h^\uparrow} = \hat{a}_T(t) \frac{h_1^q \quad H_1^{\Lambda/q}}{\sum_{q,\bar{q}} e_q^2 \Delta_T q(x, Q^2) \Delta_T D_{h/q}(z, Q^2)} \quad e^+e^- \rightarrow \Lambda^\uparrow \bar{\Lambda}^\uparrow X$$

# other recent COMPASS results - 3

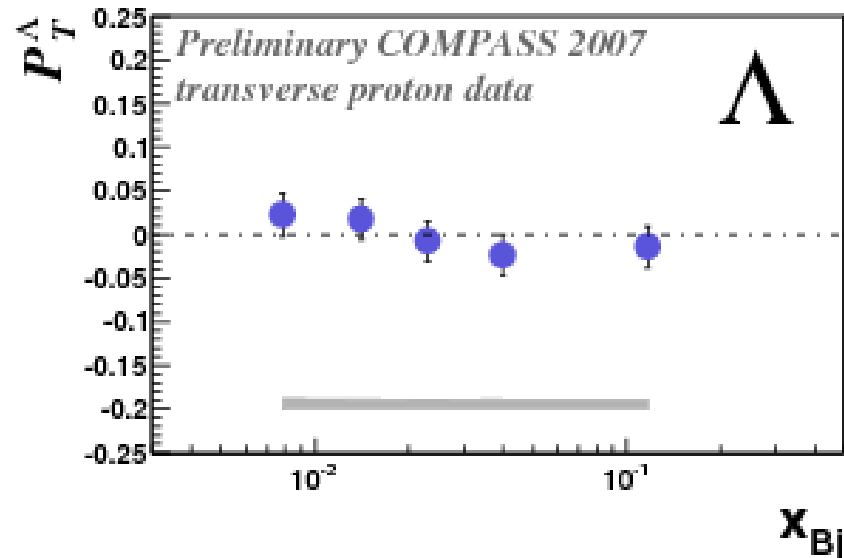
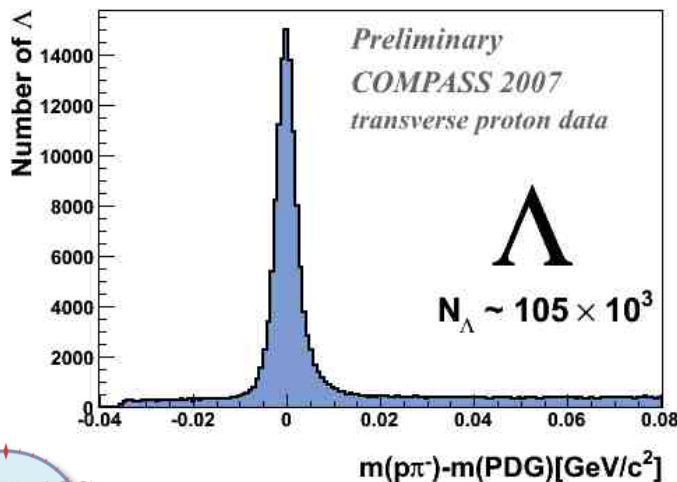
**coming soon:**

new results on  $\Lambda$  polarisation

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one of the first proposed methods

$$P_y^{h\uparrow} = \hat{a}_T(t) \frac{h_1^q H_1^{\Lambda/q}}{\sum_{q,\bar{q}} e_q^2 q(x, Q^2) D_{h/q}(z, Q^2)} \quad e^+e^- \rightarrow \Lambda^\uparrow \bar{\Lambda}^\uparrow X$$



**analysis of 2010 proton data started - expected statistics: x 2**

# accessing transversity

---

COMPASS has produced and is producing many interesting results and new “pioneering” analysis have been started

main limitation of existing data:

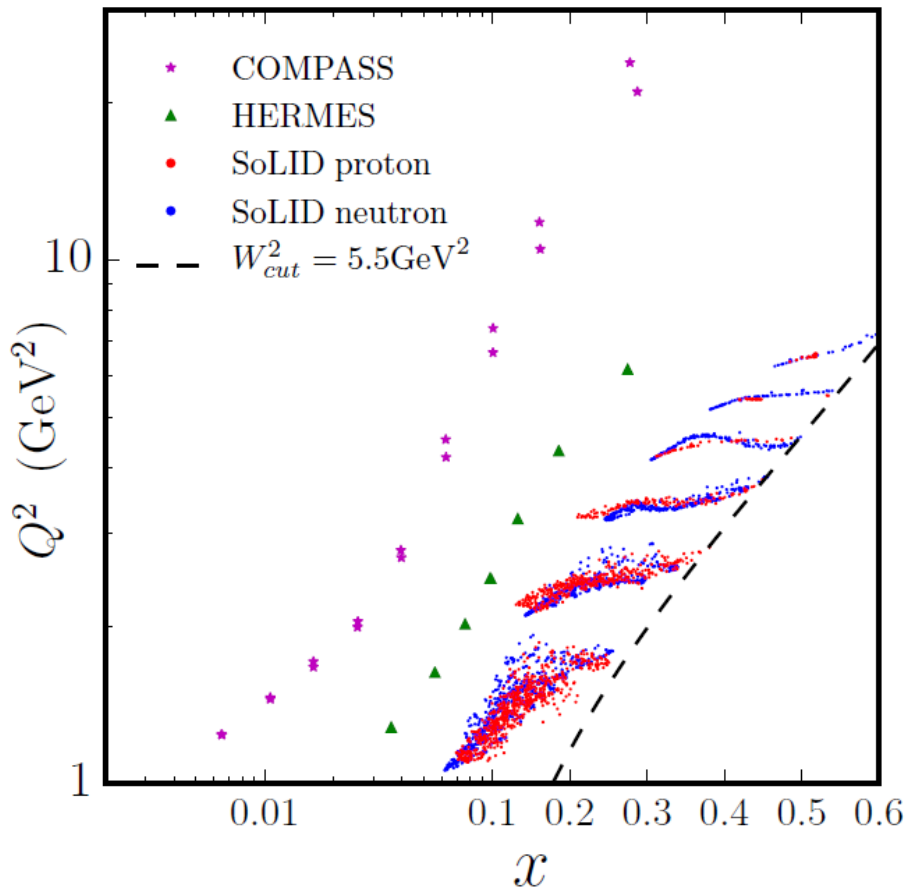
**statistics, in particular for transversely polarised d**

**new data needed soon!**

# one more year of data taking with transversely polarised d at *COMPASS*



an enormous amount of data will come from **JLab12** experiments  
and later on from **EIC**



COMPASS:

no competition on precision!

smaller  $x$ , factor  $> 5$  in  $Q^2$ , ...

the kinematical region is relevant  
and new d data coming soon are  
needed



A. Bressan,  
COMPASS beyond 2020 Workshop, CERN, March 2016

## New deuteron data

- Benchmark: extraction from Collins asymmetries

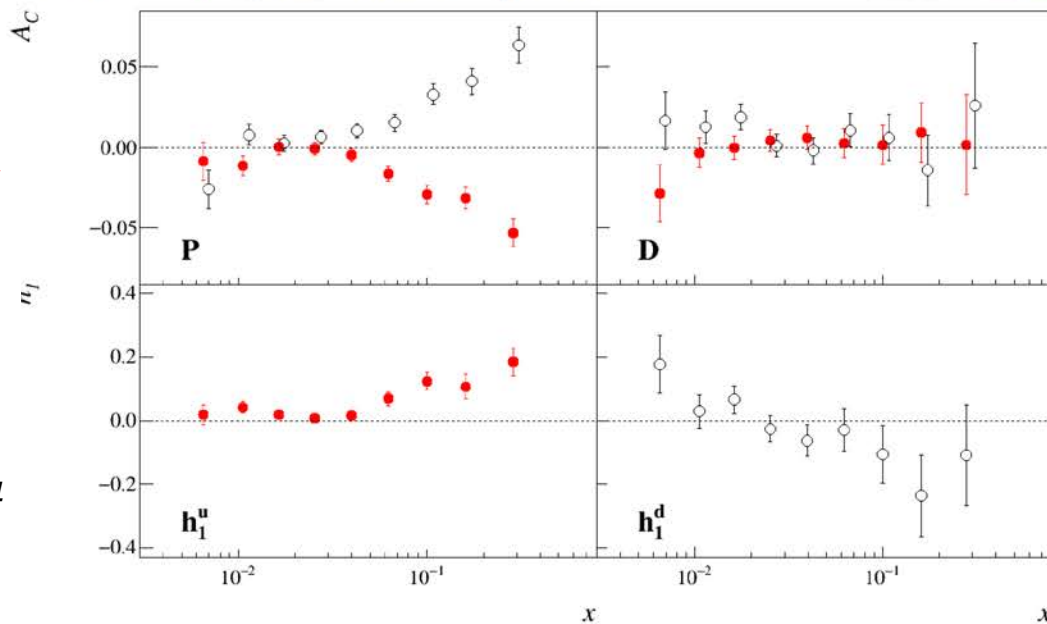
**present:**

**Collins asymmetry**

**transversity**

point-to-point  
extraction

PRD 91 (2015) 014034



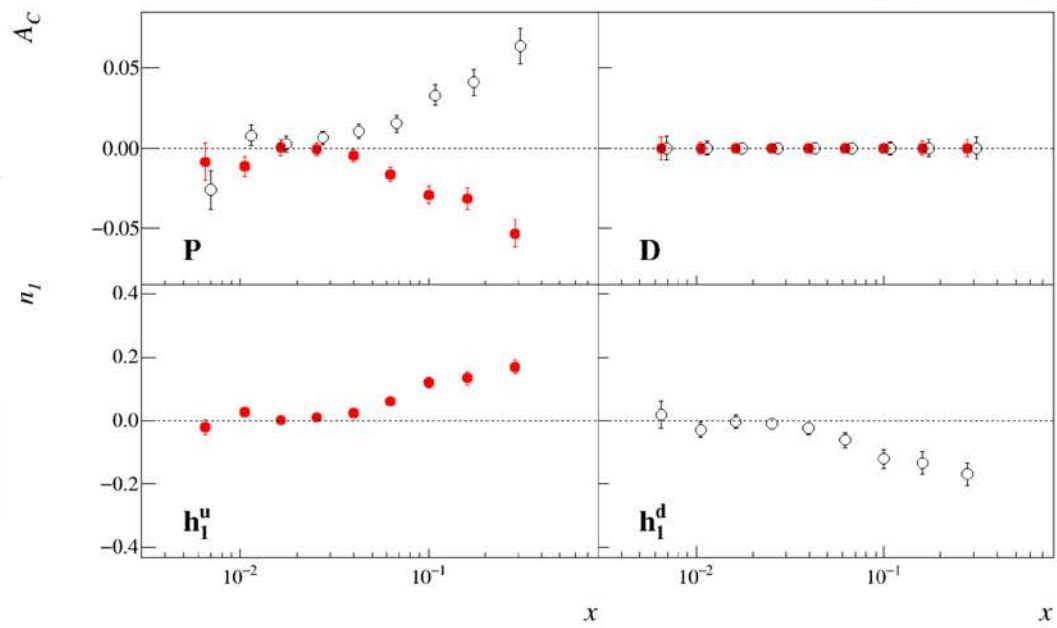




## New deuteron data

- 1 full year (same as 2010). We also gain from  $\frac{f_p^{P_{pT}}}{f_D^{P_{DT}}} = \frac{0.155 \times 0.8}{0.40 \times 0.5} = 0.6$

after 1 year of d  
*Collins asymmetry*  
*transversity*



THIS IS A MEASUREMENT THAT WILL IMPACT OUR KNOWLEDGE, KEY MEASUREMENT FOR THIS OR NEXT PHASE

# Sivers function

# accessing the Siverts function

---

**Siverts asymmetry**

$$A_{Siv} \sim \frac{\sum_q e_q^2 f_{1T}^{\perp q} \otimes D_{1q}}{\sum_q e_q^2 f_1^q \cdot D_{1q}}$$

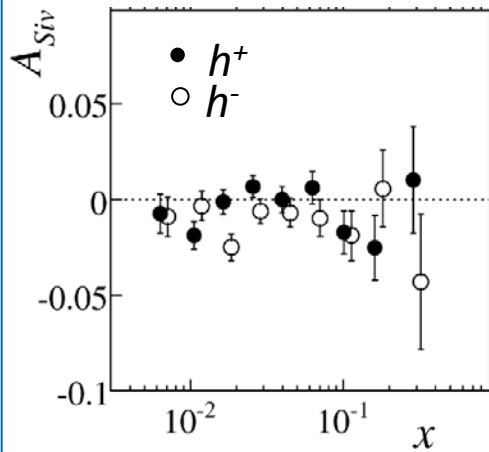
amplitude of the  
 $\sin(\phi_h - \phi_S)$  modulation

# accessing the Siverts function

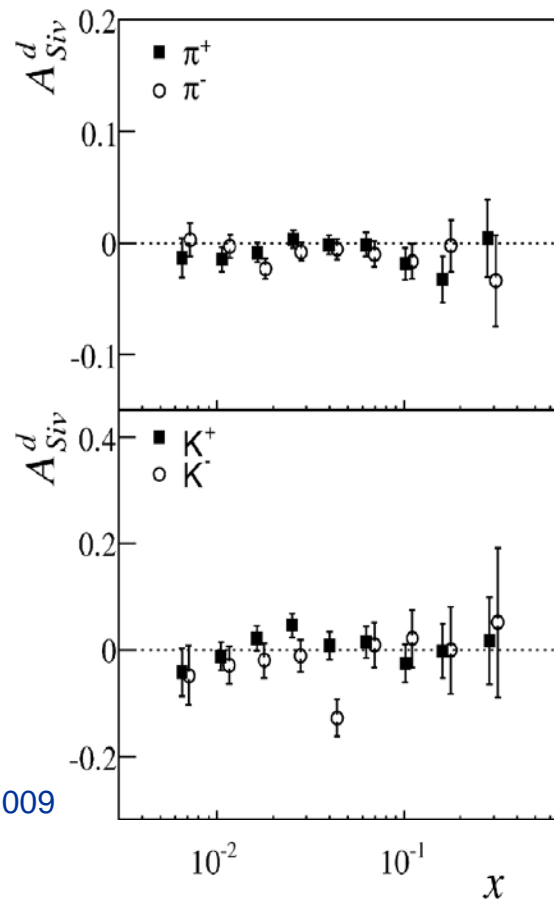
Siverts asymmetry

$$A_{Siv} \sim \frac{\sum_q e_q^2 f_{1T}^{\perp q} \otimes D_{1q}}{\sum_q e_q^2 f_1^q \cdot D_{1q}}$$

final results on  
deuteron



2002-2004 data  
NPB765 2007, PLB673 2009

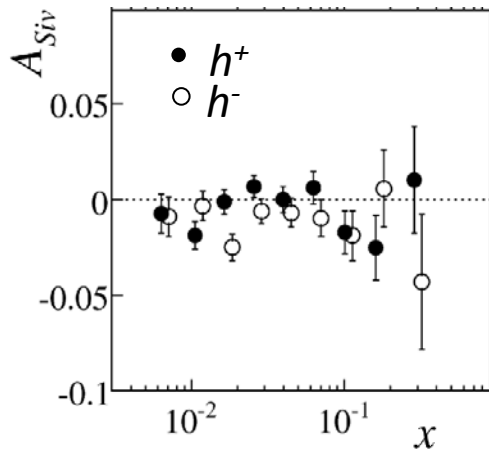


# accessing the Siverson function

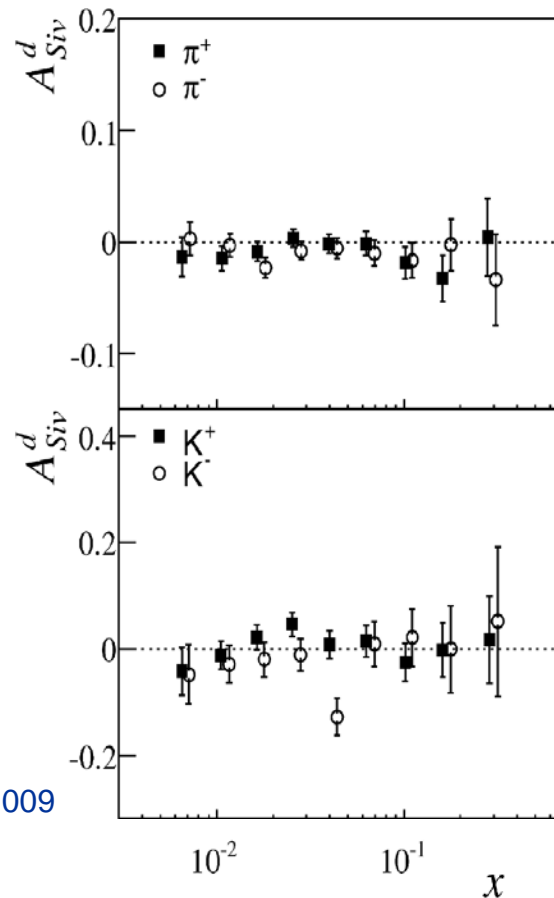
Sivers asymmetry

$$A_{Siv} \sim \frac{\sum_q e_q^2 f_{1T}^{\perp q} \otimes D_{1q}}{\sum_q e_q^2 f_1^q \cdot D_{1q}}$$

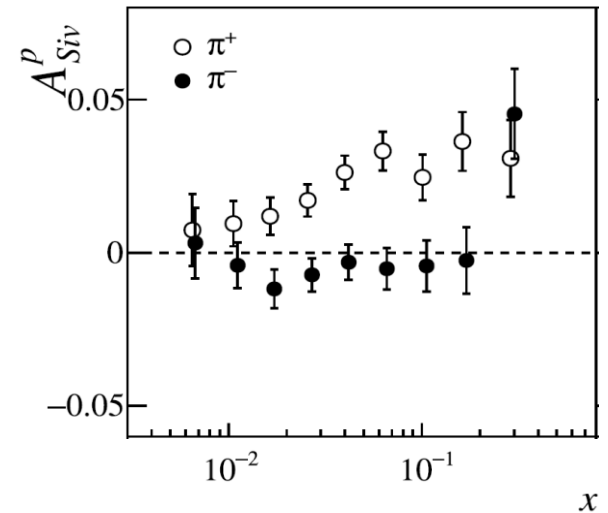
final results on  
deuteron



2002-2004 data  
NPB765 2007, PLB673 2009



final results on  
proton



clearly positive for  $\pi^+$   
down to  $x \sim 10^{-2}$

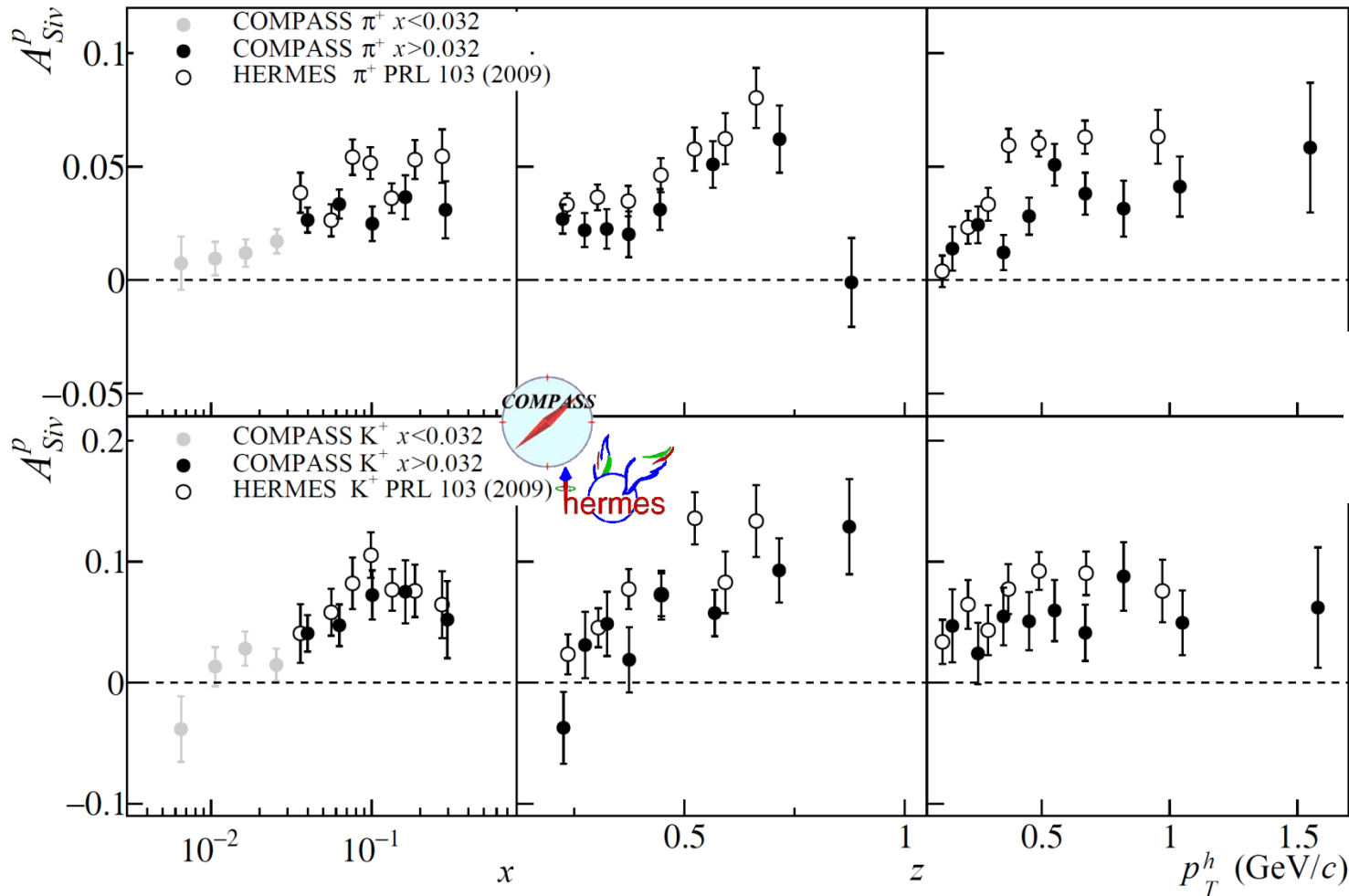
# accessing the Siverts function

## Siverts asymmetry

final results on proton for positive particles



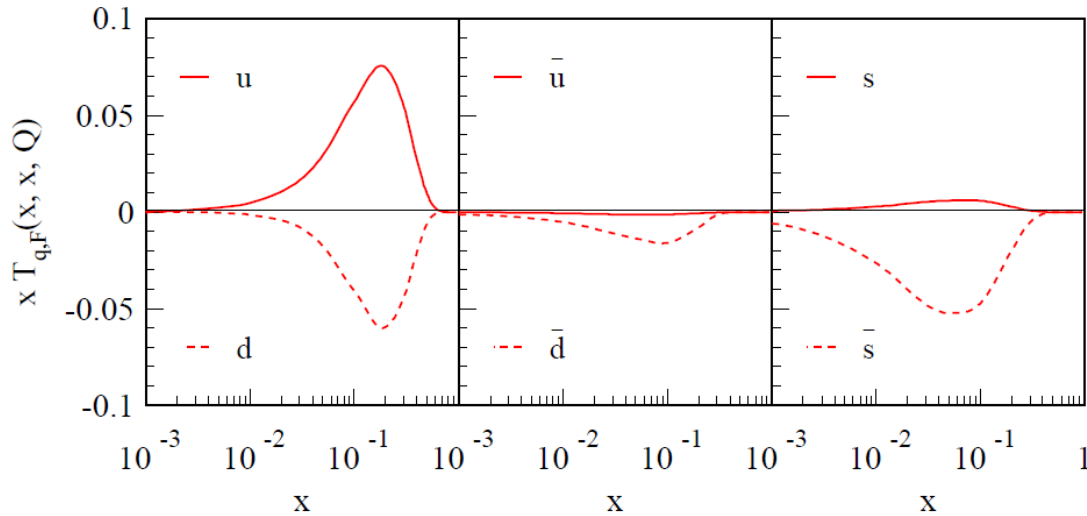
vs



$K^+$  asymmetries  
larger than  
 $\pi^+$  asymmetries

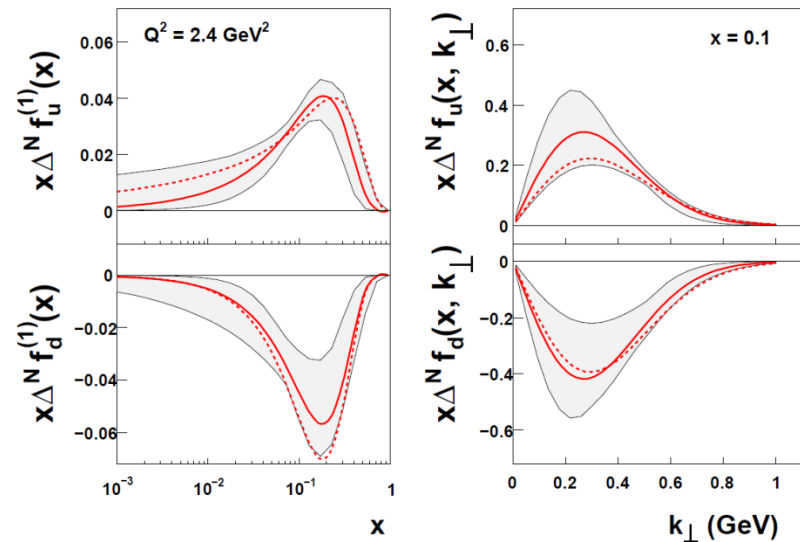
# accessing the Sivers function

fits to COMPASS and HERMES data since 2005



Echevarria et al  
Phys.Rev. D89 (2014)

Anselmino et al  
Eur.Phys.J. A39 (2009)



# accessing the Sivers function

## point-by-point extraction

~ transversity case

from p and d Sivers asymmetries measured at the same  $x, Q^2$  values

in the Gaussian model

**pions**

$$xf_{1T}^{\perp(1)u_v} = \frac{1}{5G\rho_\pi(1 - \beta_\pi^{(1)})} \left[ xf_p^{\pi^+} A_p^{\pi^+} - xf_p^{\pi^-} A_p^{\pi^-} + \frac{1}{3} \left( xf_d^{\pi^+} A_d^{\pi^+} - xf_d^{\pi^-} A_d^{\pi^-} \right) \right]$$

similar expressions for  $xf_{1T}^{\perp(1)d_v}$  and  $xf_{1T}^{\perp(1)\bar{u}} - xf_{1T}^{\perp(1)\bar{d}}$  from **pion**

and for  $xf_{1T}^{\perp(1)u_v}$  and  $xf_{1T}^{\perp(1)d_v}$  from **kaon** p and d asymmetries

independent extraction of  $xf_{1T}^{\perp(1)u_v}$  and  $xf_{1T}^{\perp(1)d_v}$   
from  $\pi$  and from  $K$  Sivers asymmetries

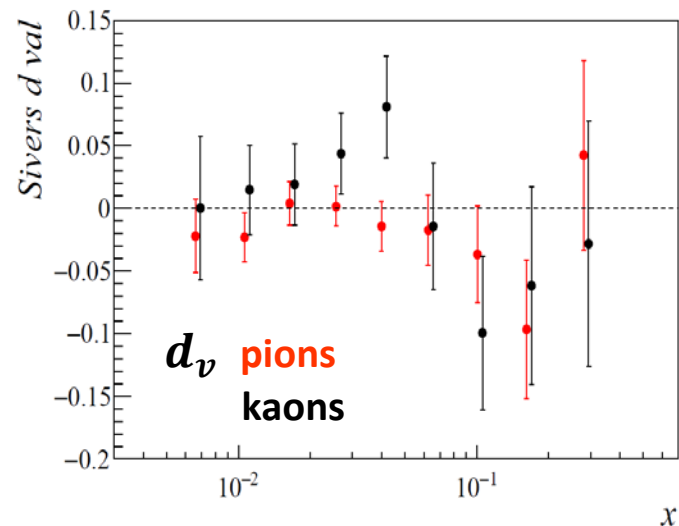
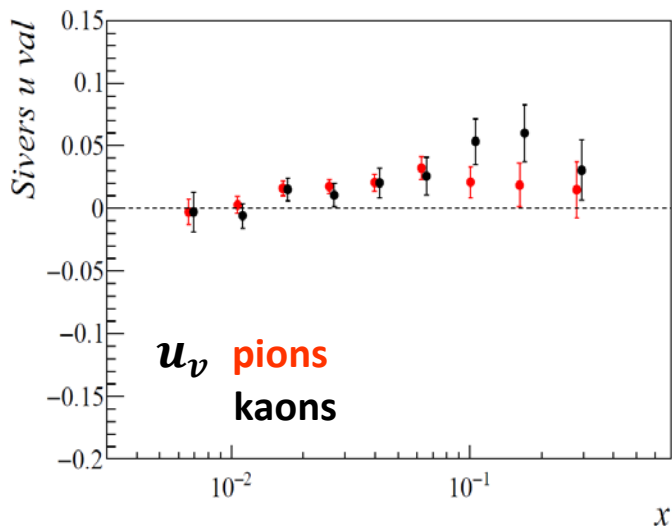


# accessing the Sivers function

## point-by-point extraction

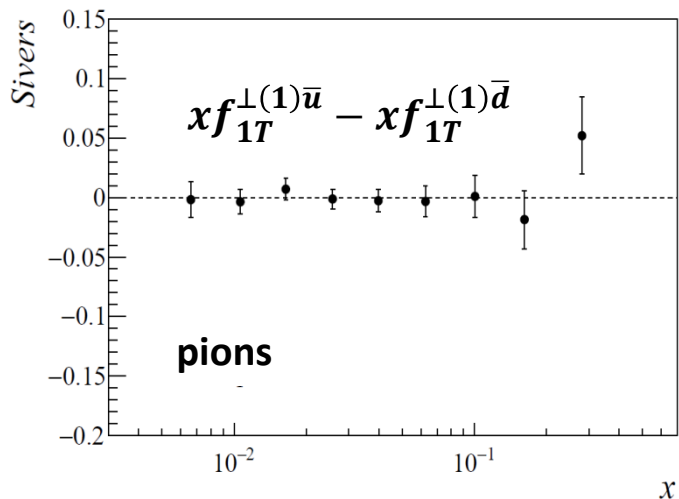
from p and d Sivers asymmetries measured at the same  $x, Q^2$  values

using  
COMPASS  
results

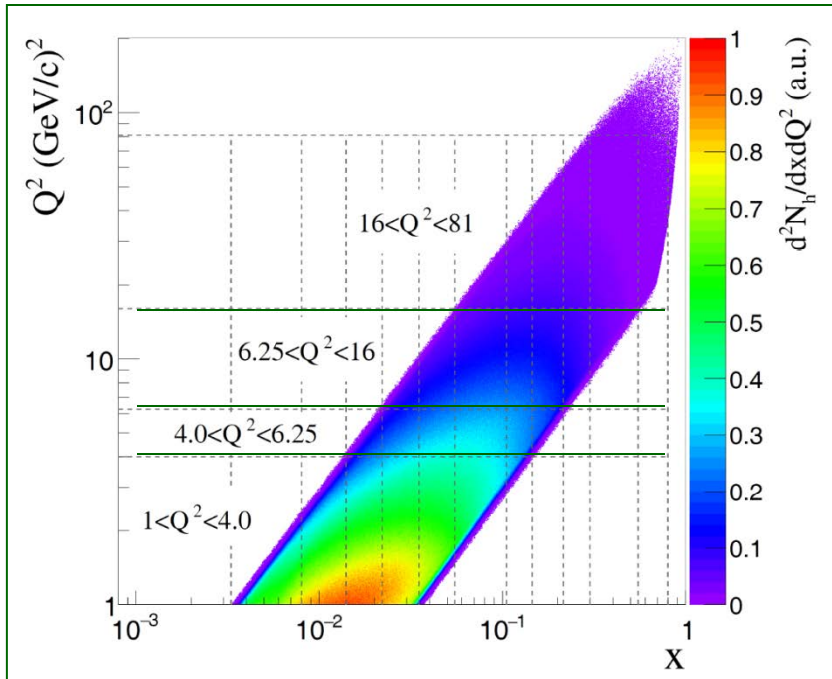


- similar values and uncertainties pions and kaons
- large statistical uncertainties for  $d_v$
- results compatible with recent parametrisations

result for  $f_{1T}^{\perp(1)\bar{u}} - f_{1T}^{\perp(1)\bar{d}}$  compatible with zero



# further results of the Sivers asymmetry



} Drell-Yan  $Q^2$  range at COMPASS  
no evolution SIDIS  $\rightarrow$  DY

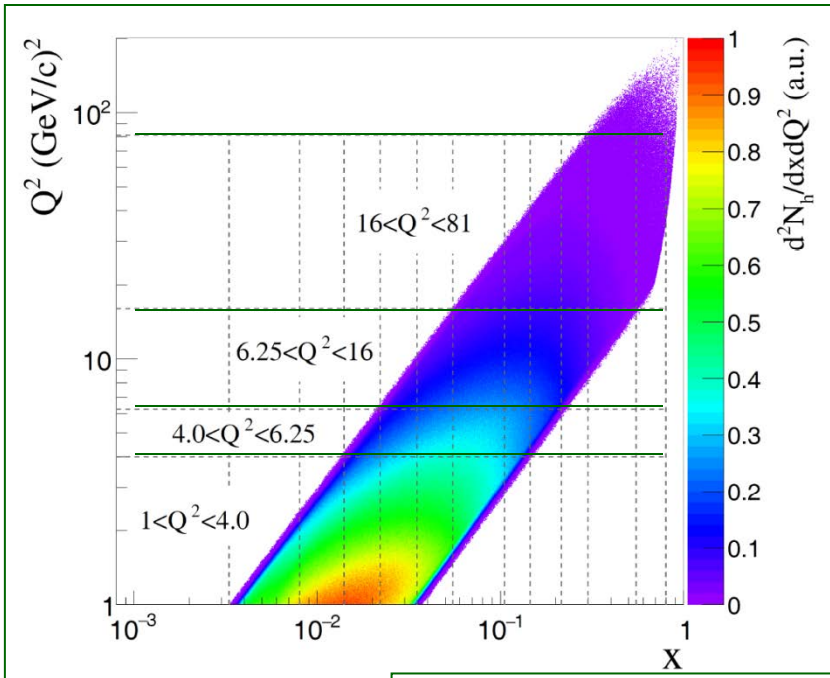


4  $Q^2$  bins

11  $x$  bins

$z, P_T^h$  binning

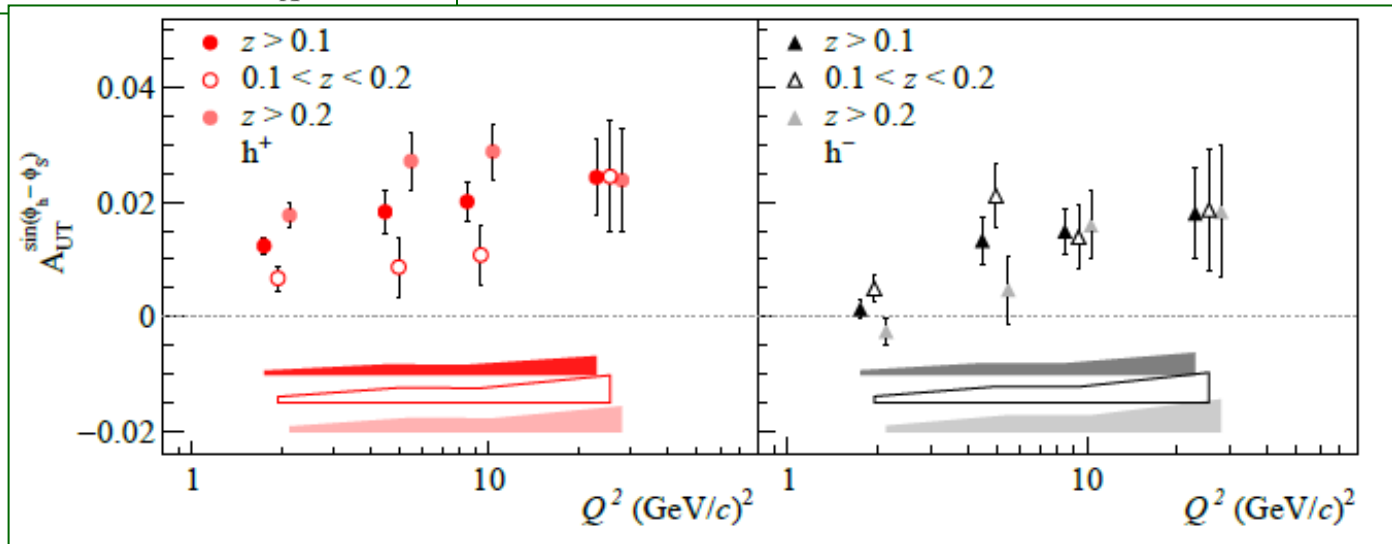
# further results of the Siverts asymmetry



Drell-Yan  $Q^2$  range at COMPASS  
no evolution SIDIS  $\rightarrow$  DY



more results in  
the paper  
arXiv:1609.07374  
[hep-ex]



# further results of the Sivers asymmetry

---

preliminary results have already been recently produced for

- multidimensional measurements of the Sivers asymmetry
- gluon Sivers asymmetries

J/ $\Psi$

high  $P_T^h$  hadron pairs

**new** preliminary results (QCD'N2016, SPIN2016)

- $P_T$  - **weighted asymmetries**

# $P_T$ weighted Sivers asymmetry

$$A_{Siv} \propto \frac{\sum_q e_q^2 \cdot f_{1T}^{\perp q} \otimes D_{1q}^h}{\sum_q e_q^2 \cdot f_1^q \cdot D_{1q}^h}$$

convolution

→ non negligible uncertainties in extractions  
 $\vec{k}_T$  !

a possible way out: use of the  $P_T$  weighted asymmetries

obtained by weighting the spin dependent part of the cross-section

$$w = P_T/zM \quad A_{Siv}^w = 2 \frac{\sum_q e_q^2 \cdot f_{1T}^{\perp(1)q} \cdot D_{1q}^h}{\sum_q e_q^2 \cdot f_1^q \cdot D_{1q}^h}$$

proposed a long time ago ...

A. Kotzinian and P. J. Mulders, PLB 406 (1997) 373

D. Boer and P. J. Mulders, PRD 57 (1998) 5780

J. C. Collins et al. PRD 73 (2006) 014021

reconsidered recently

Zhong-Bo Kang et al., Phys.Rev. D87 (2013)

....

# $P_T$ weighted Siverts asymmetry

only existing data:

preliminary results by HERMES

Acta Phys.Polon. B36 (2005) 209

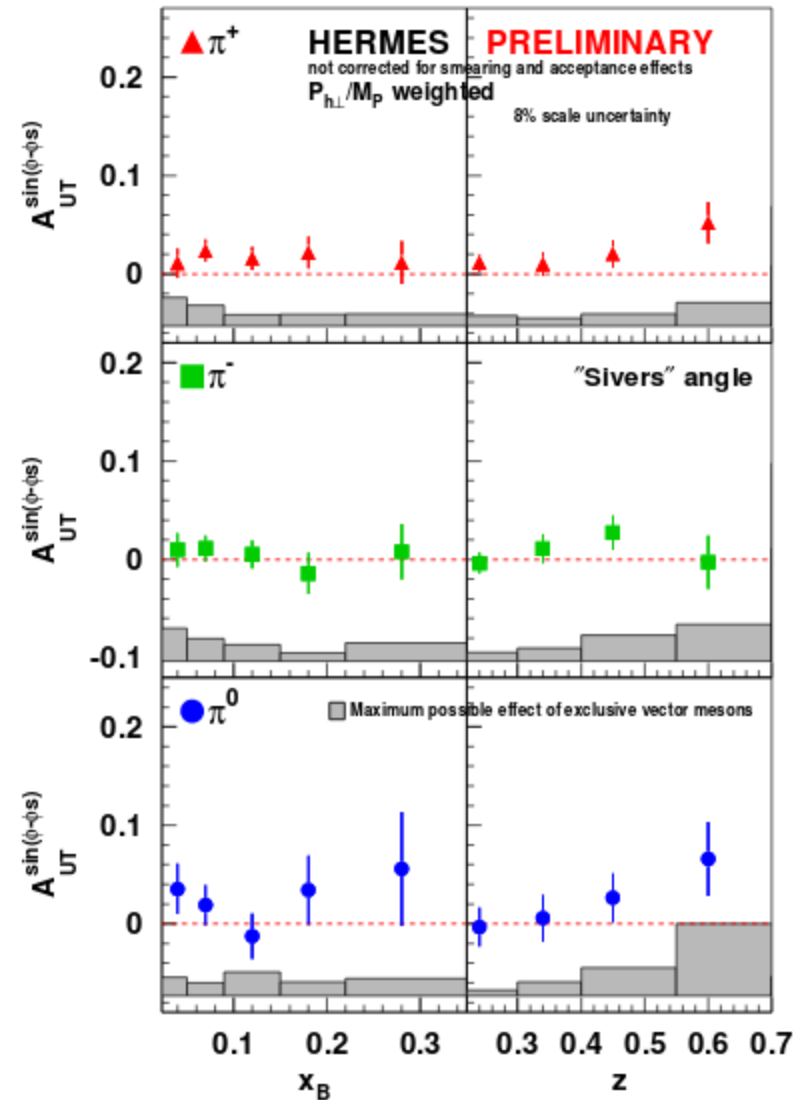
used to extract the Siverts function

A.V. Efremov et al., Phys.Lett. B612 (2005) 233

A. Bacchetta et al., Eur.Phys.J. A45 (2010) 373

...

$$w = P_T/M$$

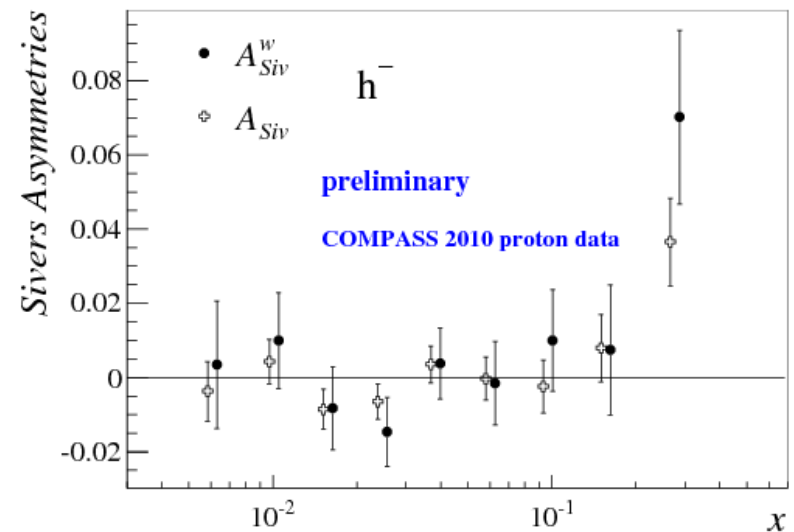
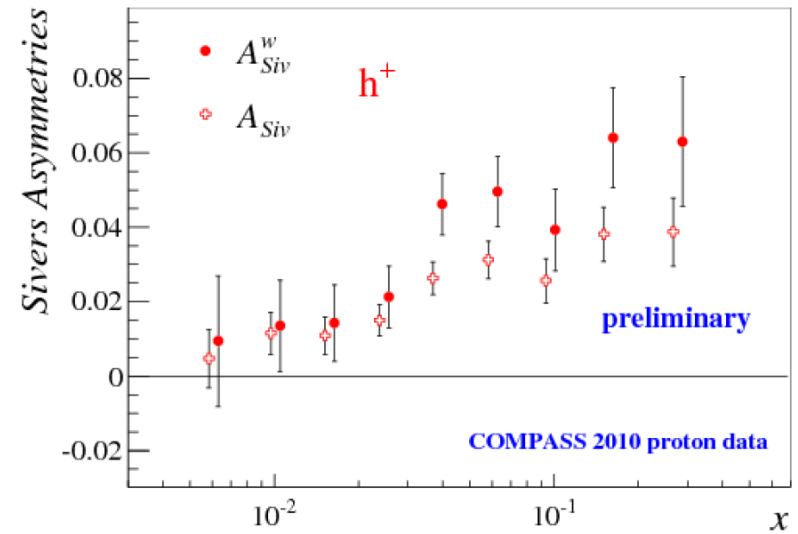


# $P_T$ weighted Siverts asymmetry

**NEW:** COMPASS results  
*proton only!*



$$w = P_T/zM$$

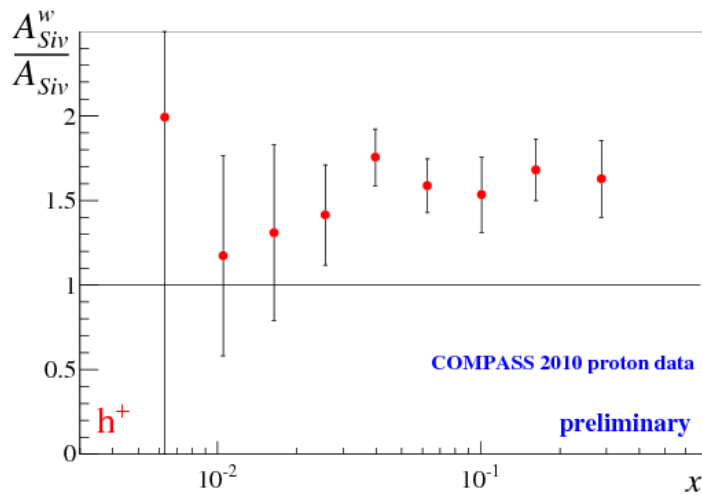


# $P_T$ weighted Siverts asymmetry

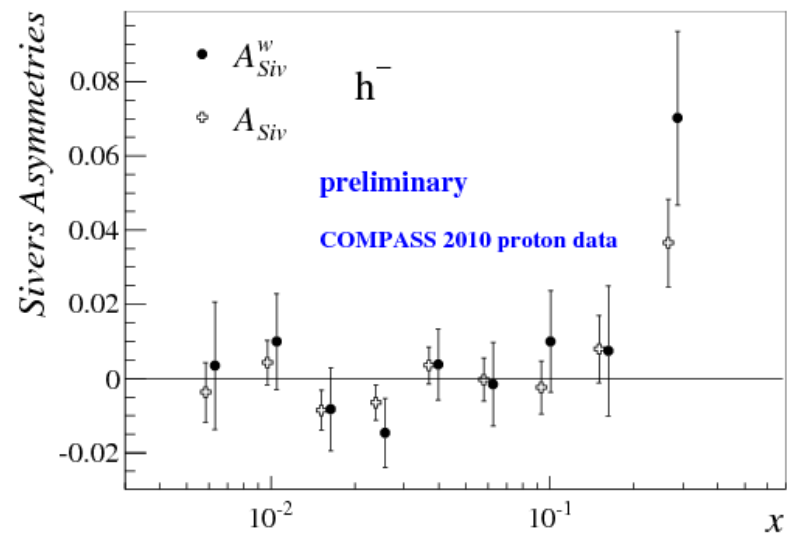
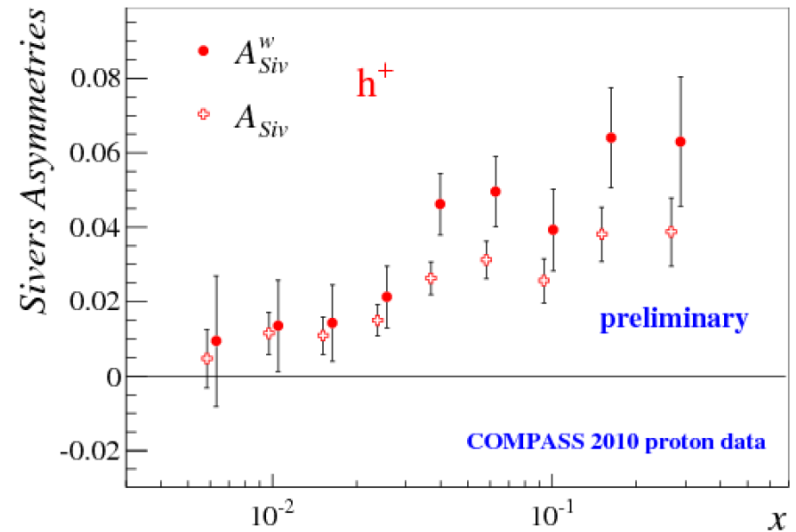
**NEW: COMPASS results**  
*proton only!*



$$w = P_T/zM$$



*look promising!*  
*plans to publish soon*





# unpolarised SIDIS

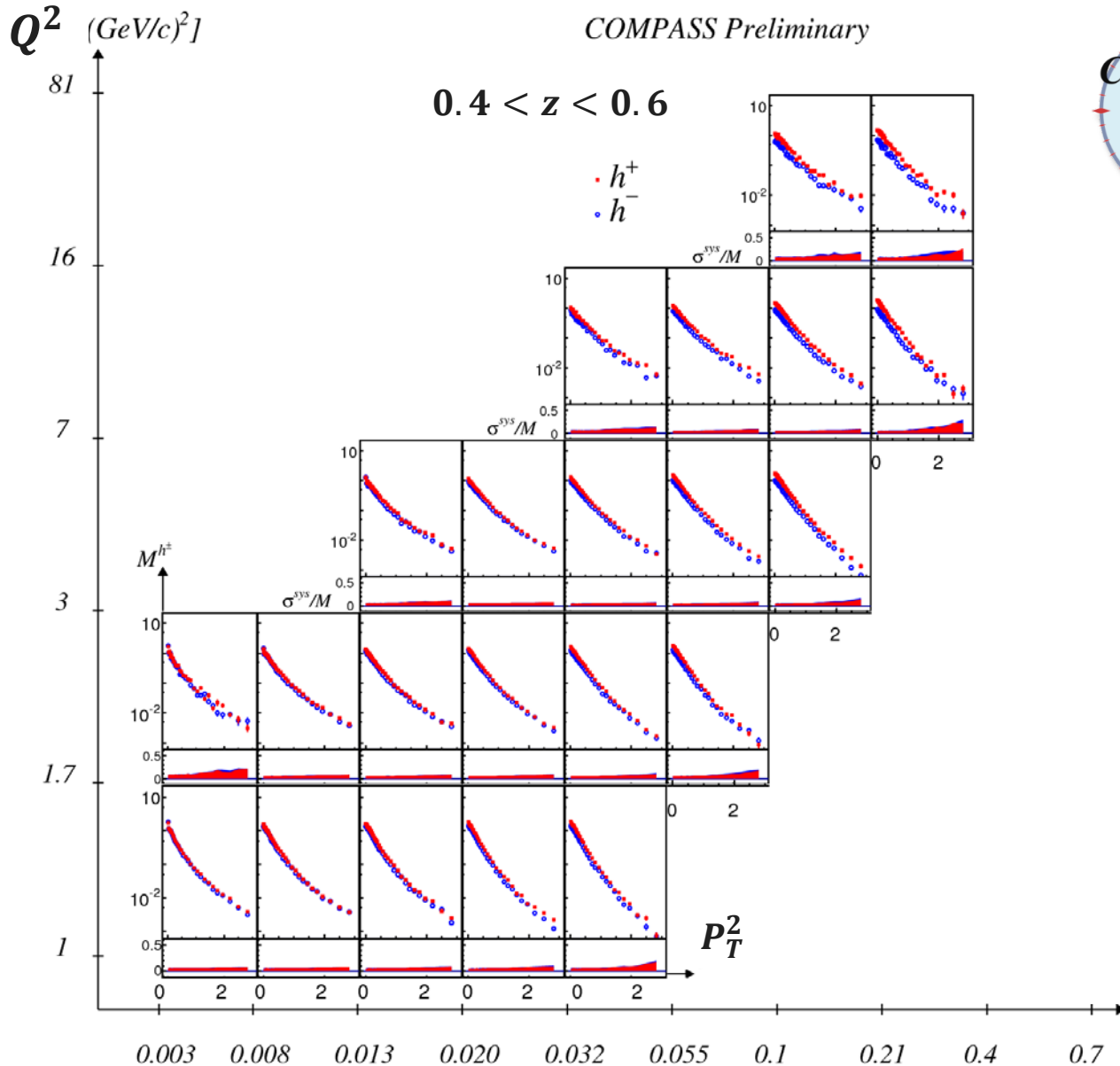
allows to

- access  $k_T$  multiplicities vs  $P_T$   
 $\cos \phi$  asymmetries
- study the Boer-Mulders function  $\cos 2\phi$  asymmetries

a lot of data from COMPASS, on d ( $^6\text{LiD}$ ) only

and from HERMES (p and d) and JLab

# unpolarised SIDIS – $P_T^2$ distributions



2006 d data  
SPIN2014

$0.2 < z < 0.3$

$0.3 < z < 0.4$

$0.6 < z < 0.8$

total:

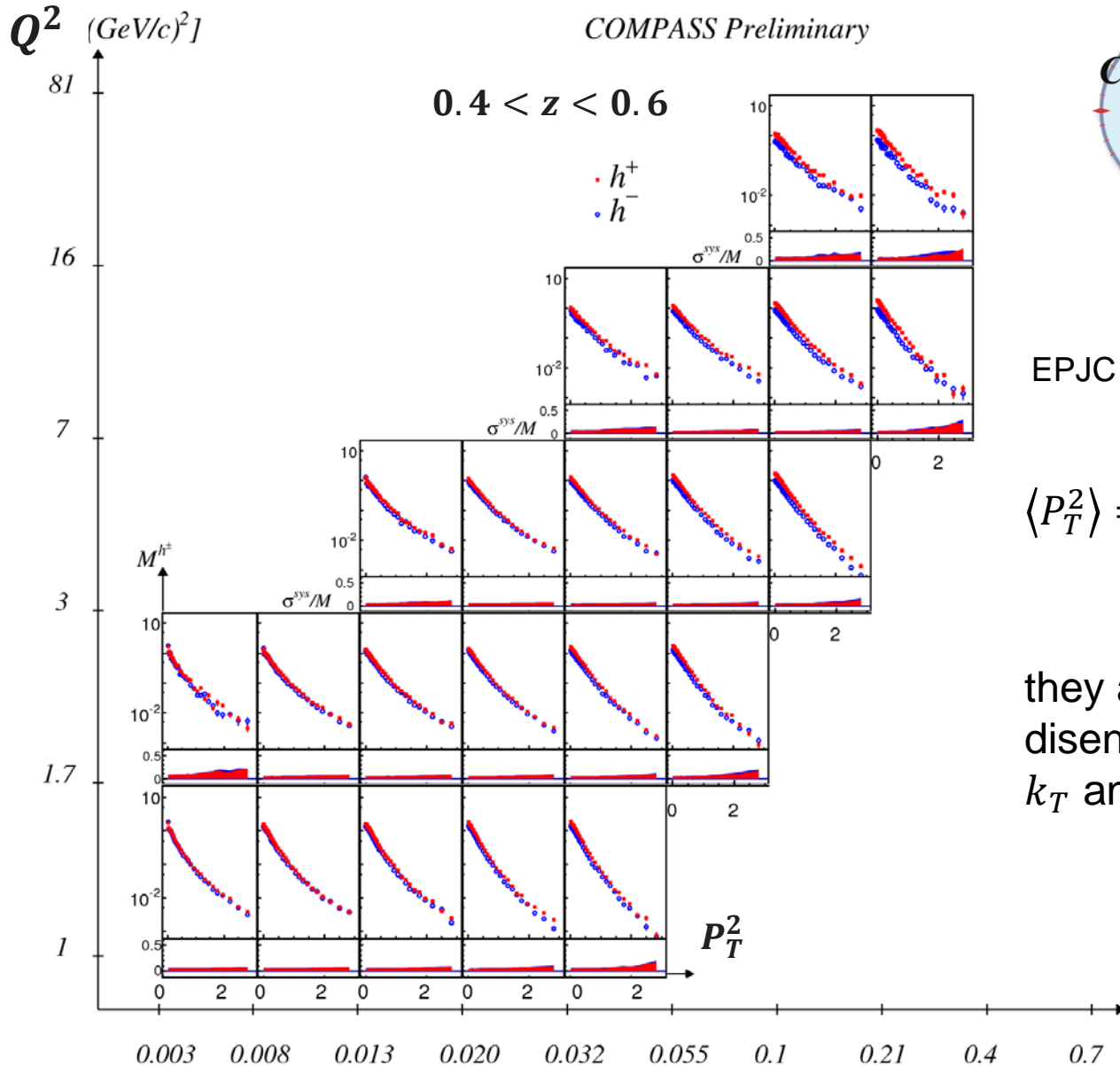
**4918 data points**

wider kinematic range,  
higher precision than  
published results

EPJC 73 (2013) 2531

**plus HERMES, JLab**

# unpolarised SIDIS – $P_T^2$ distributions



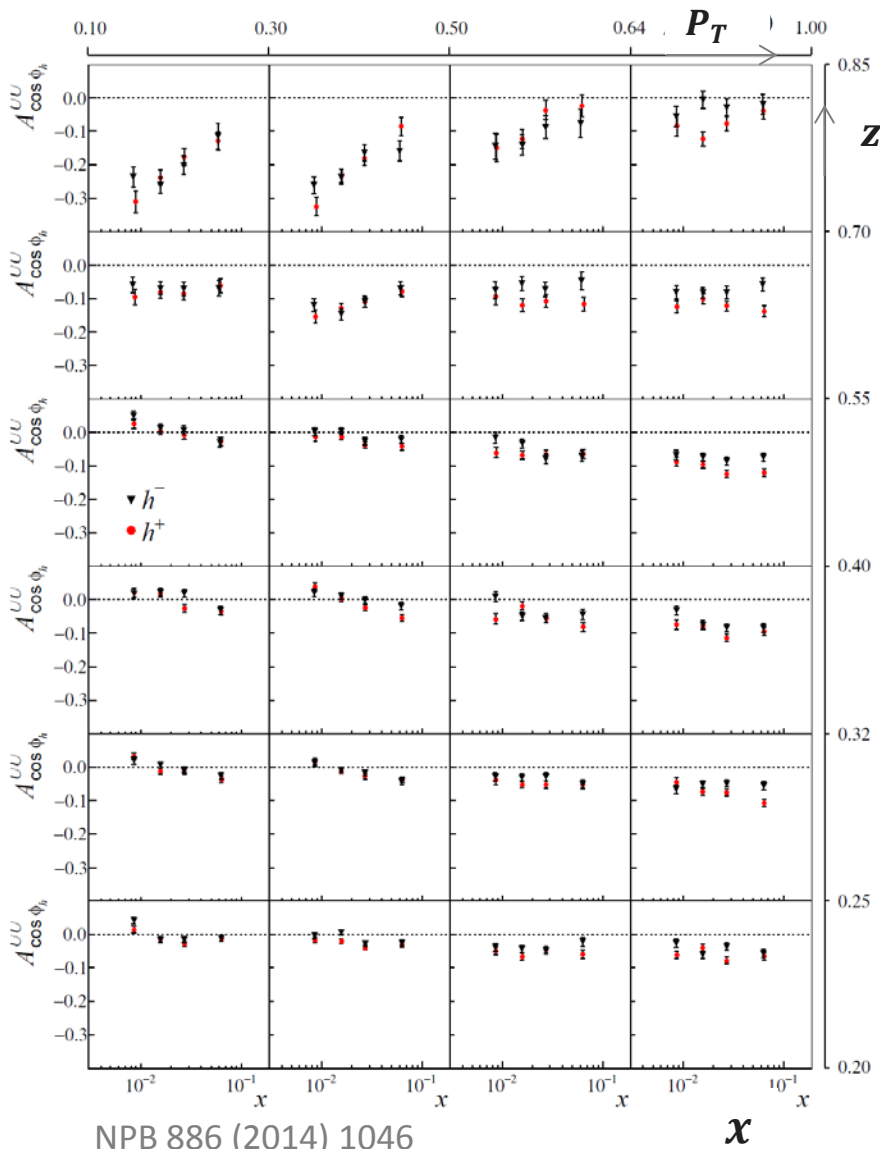
EPJC 73 (2013) 2531

$$\langle P_T^2 \rangle \neq z^2 \langle k_T^2 \rangle + \langle p_T^2 \rangle$$

if  $\langle p_T^2 \rangle$  const

they alone do not allow to disentangle the  $k_T$  and the  $p_T$  contributions

# unpolarised SIDIS – azimuthal asymmetries



$A_{\cos\phi}$ , “Cahn asymmetry”  $\rightarrow k_T$

- strong  $x, z, P_T$  dependence
- difficult to explain it
- small value of  $k_T$
- presence of further twist-3 terms ?
- non-zero Boer-Mulders effect ? \*



(\*) with HERMES data  
V. Barone et al.  
Phys.Rev. D91 (2015)

# unpolarised SIDIS – azimuthal asymmetries

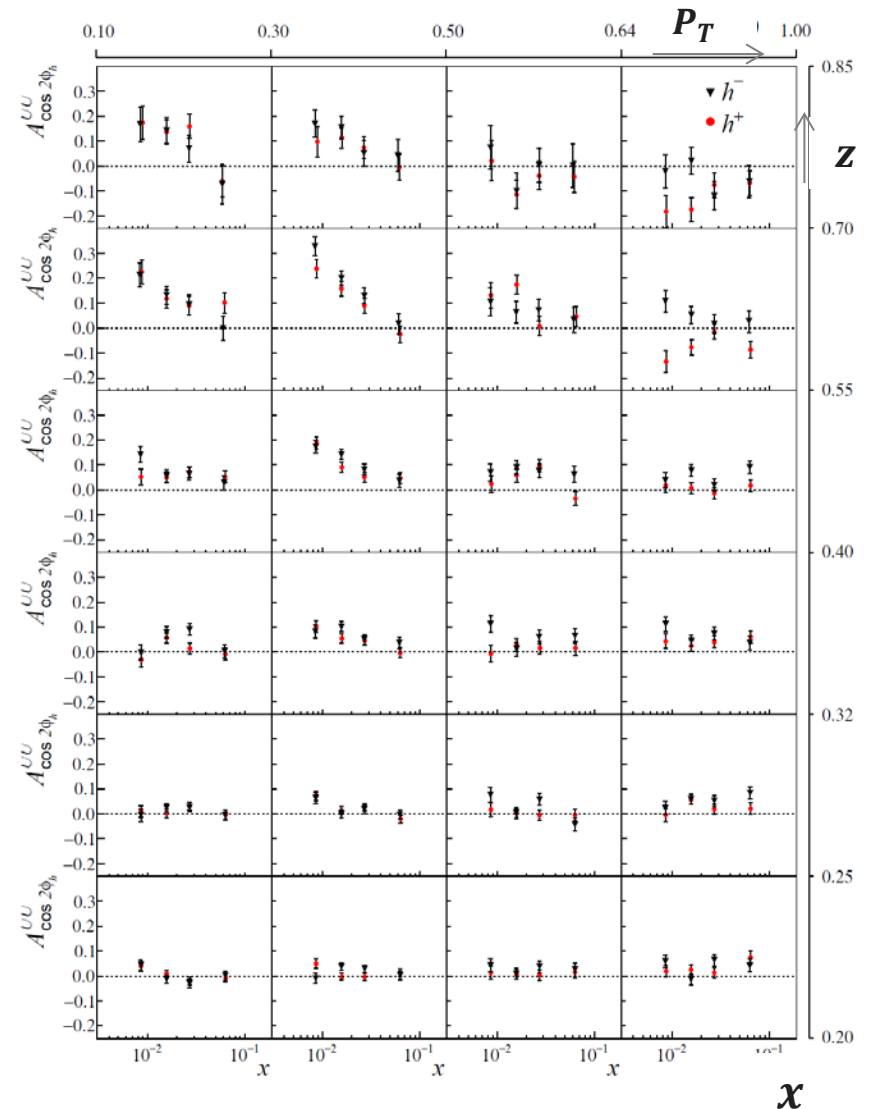
$A_{\cos 2\phi}$  → Boer-Mulders function

- strong  $x, z, P_T$  dependence

other higher-twist effects ? \*



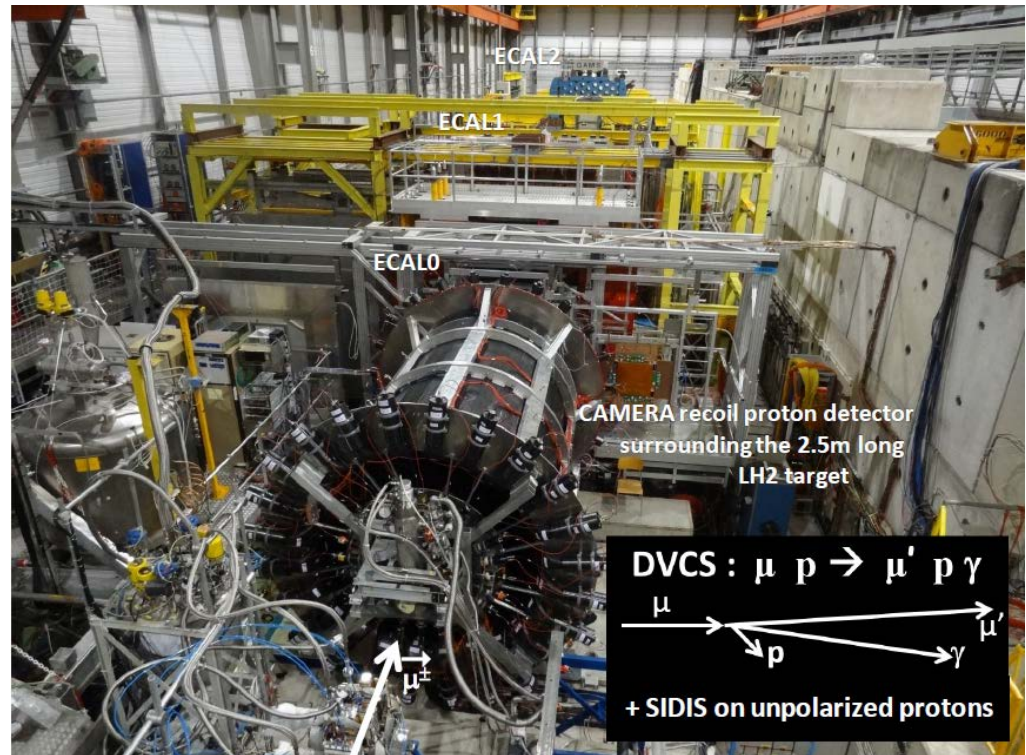
still a lot to be done



# unpolarised SIDIS – near future

data from 2016-17 runs, collected in parallel with DVCS

- LH<sub>2</sub> target
  - about the same phase space as in 2004
- and
- smaller systematic uncertainties



# summary

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SIDIS experiments, and COMPASS, have given fundamental contributions to the study of the transverse spin and transverse momentum structure of the nucleon

much more will be learned measuring SIDIS at the new facilities  
with extremely high precision measurements

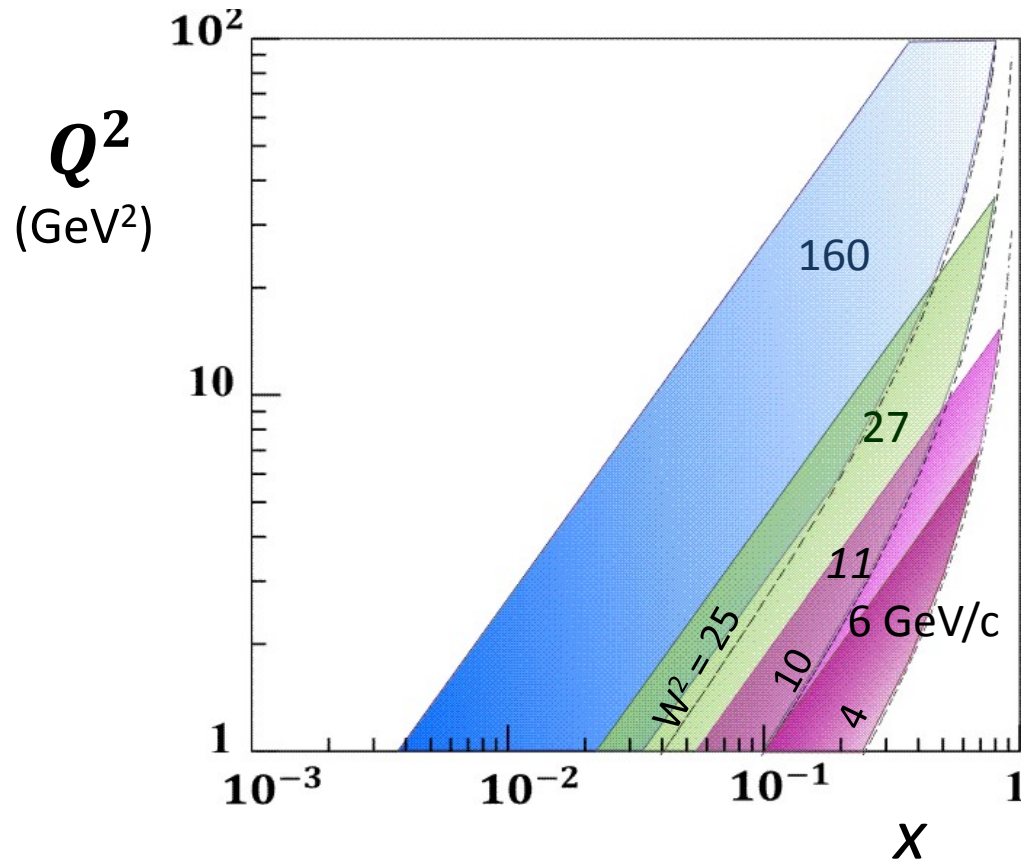
in the mean time more can be learned at COMPASS,  
performing relevant measurements using

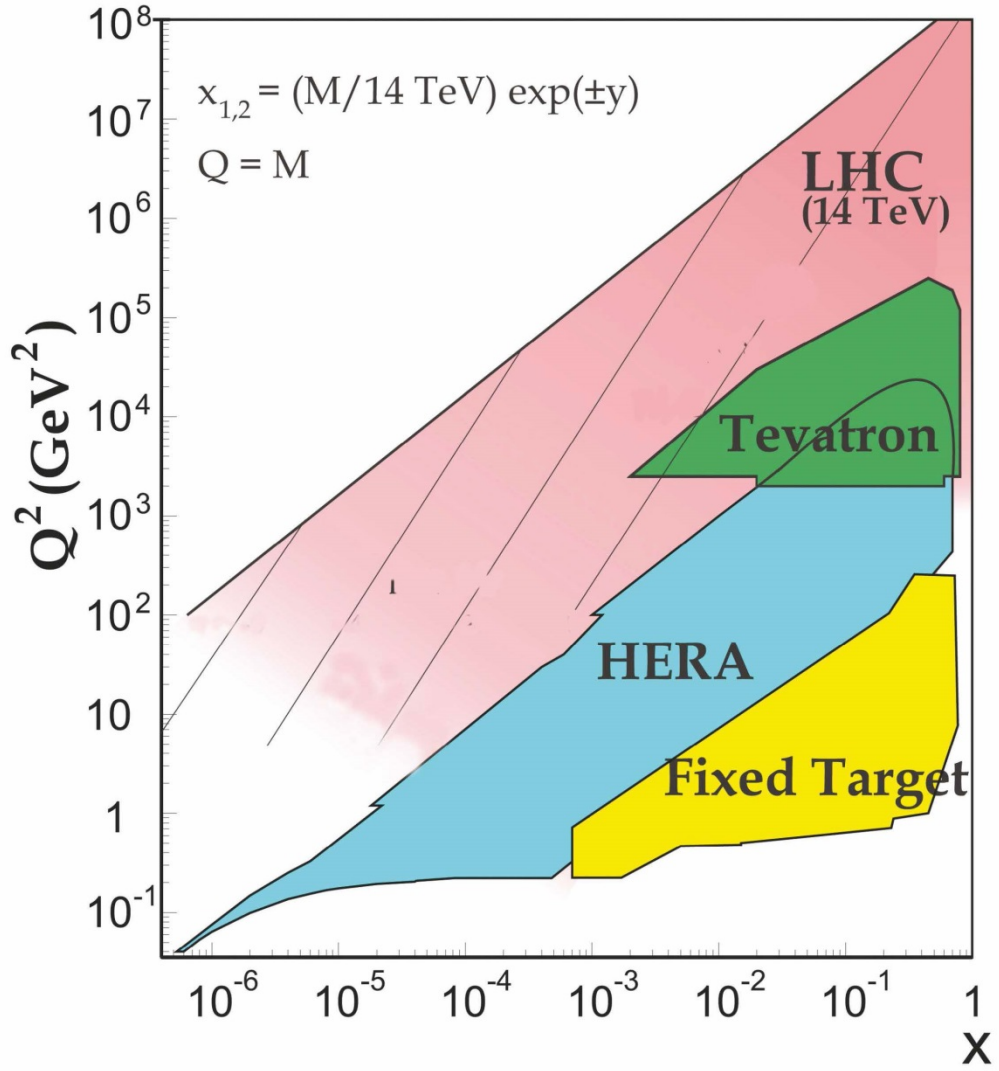
existing data  $\Delta$  polarisation, weighted asymmetries, fragmentation ...  
and new data  $\text{LH}_2$ , and hopefully  $d\uparrow$

**new ideas are coming out !**









# accessing the Siverts function

direct point-by-point extraction of the Siverts PDFs

from p and d Siverts asymmetries measured at the same  $x, Q^2$

in the Gaussian model

$$A_{Siv}^h(x, z, Q^2) = G z \frac{\sum_q e_q^2 \cdot x f_{1T}^{\perp(1)q}(x, Q^2) \cdot D_{1q}^h(z, Q^2)}{\sum_q e_q^2 \cdot x f_1^q(x, Q^2) \cdot D_{1q}^h(z, Q^2)}$$

$$f_{1T}^{\perp(1)q} = \int d^2\vec{k}_T \frac{k_T^2}{2M^2} f_{1T}^{\perp q}(k_T^2)$$

$$G = \frac{\sqrt{\pi}M}{\sqrt{z^2\langle k_T^2 \rangle_S + \langle p_T^2 \rangle}} \simeq \frac{\pi M}{2\langle P_T \rangle} \quad \text{from data, assumed to be constant}$$

and with the usual assumptions on fav/unfav FFs

**pions**

$$x f_{1T}^{\perp(1)u_v} = \frac{1}{5G\rho_\pi(1 - \beta_\pi^{(1)})} \left[ x f_p^{\pi^+} A_p^{\pi^+} - x f_p^{\pi^-} A_p^{\pi^-} + \frac{1}{3} \left( x f_d^{\pi^+} A_d^{\pi^+} - x f_d^{\pi^-} A_d^{\pi^-} \right) \right]$$

similar expressions for  $x f_{1T}^{\perp(1)d_v}$  and  $x f_{1T}^{\perp(1)\bar{u}} - x f_{1T}^{\perp(1)\bar{d}}$  from **pion**

and for  $x f_{1T}^{\perp(1)u_v}$  and  $x f_{1T}^{\perp(1)d_v}$  from **kaon** p and d asymmetries

A. M., F. Bradamante, V. Barone, SPIN2016

# further results on the Sivers asymmetry

already published:

TSA vs  $z$  and  $p_T$  in different  $x$  ranges

vs  $x$  and  $p_T$  in different  $z$  ranges

vs  $x$  and  $z$  in different  $p_T$  ranges

or in extended kinematical ranges

low  $z$  / low  $y$

