

# 3D structure: present and future

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Alessandro Bacchetta

Funded by



# Acknowledgements

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Even if I will present an overview, I acknowledge the contribution of my research group in shaping and developing many of the ideas that I will mention

- Filippo Delcarro, Luca Mantovani, Fulvio Piacenza (PhD students)
- Giuseppe Bozzi, Cristian Pisano (post-docs)
- Barbara Pasquini, Marco Radici (staff)

# Disclaimer

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My task was to talk about the present and the future, but

It is difficult to predict, especially the future

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# PDFs



Parton distribution functions ( $x$ )

Transverse-momentum distributions ( $x, \vec{k}_\perp$ )

Impact-parameter distributions ( $x, \vec{b}_\perp$ )

# TMDs

Wigner distributions ( $x, \vec{k}_\perp, \vec{b}_\perp$ )

  $\vec{b}_\perp$  dependence  
  $\vec{k}_\perp$  dependence



these two variables are NOT Fourier conjugate

*see, e.g., C. Lorcé, B. Pasquini, M. Vanderhaeghen, JHEP 1105 (11)*

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2D Fourier transform ( $\vec{b}_\perp$ )

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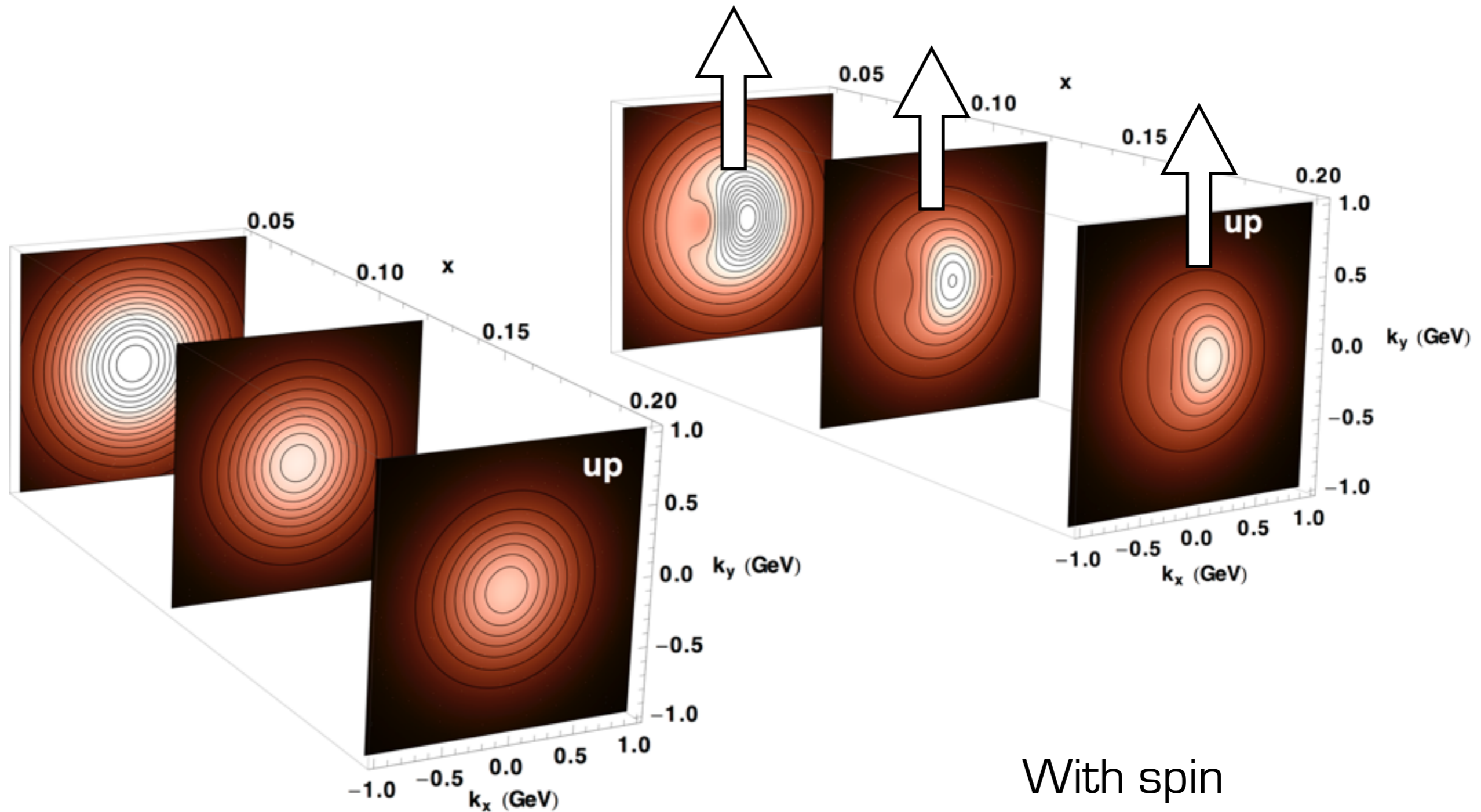


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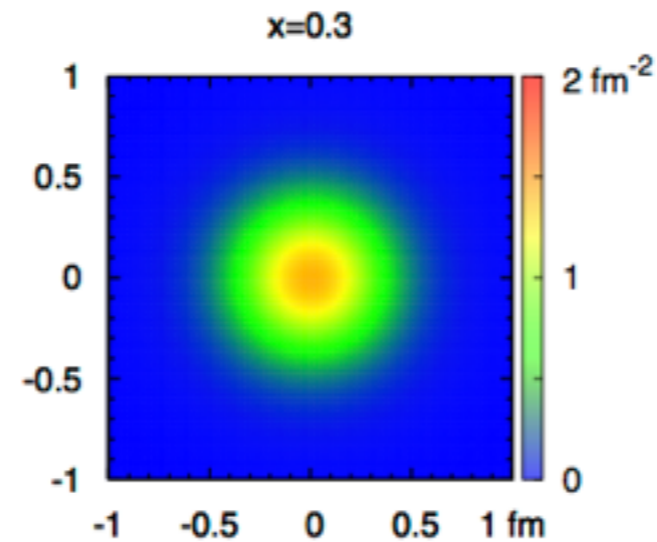
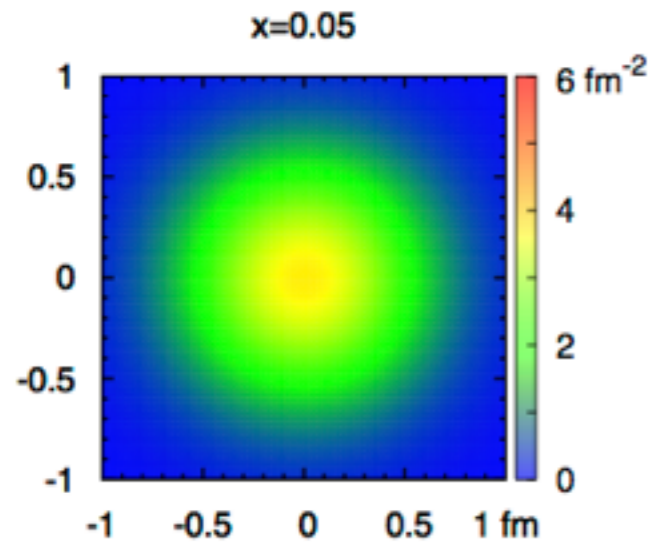
# 3D structure in momentum space



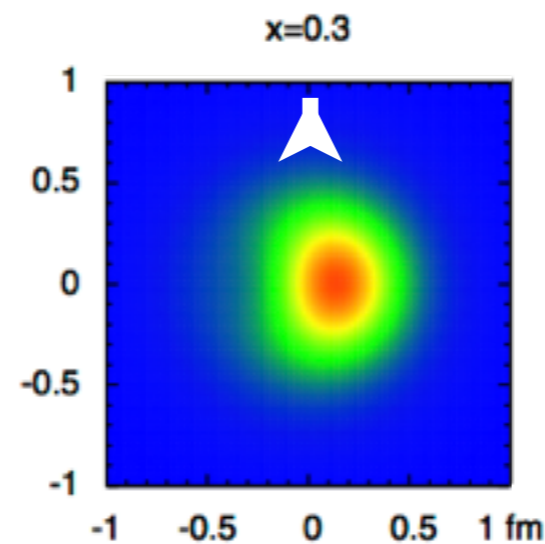
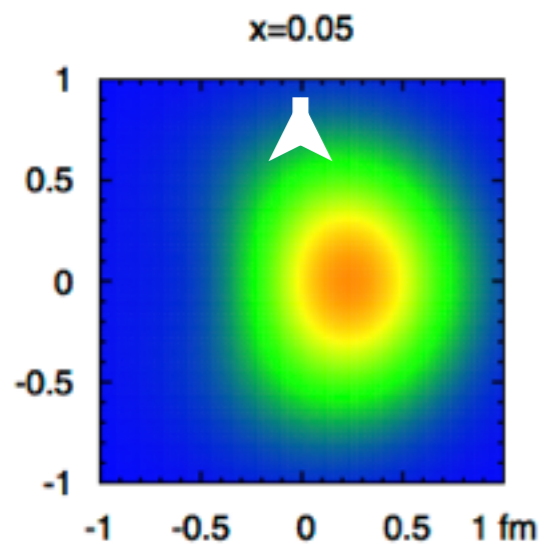
Unpolarized and Sivers TMDs

With spin

# 3D structure in impact parameter space



down valence



- Fourier t. of GPDs at  $(x,0,t)$
- Model assumptions are critical
- up: smaller distortion and opposite sign

# Recent review

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The European Physical Journal A  
All Volumes & Issues

## The 3-D Structure of the Nucleon

ISSN: 1434-6001 (Print) 1434-601X (Online)

In this topical collection (17 articles)



*EPJ A (2016) 52*

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- “Model assumptions” (intended in a broad way) are critical
- A good amount of data is already available (but still insufficient)

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- Find applications of this knowledge outside the field of “proton structure” studies (and react accordingly)
- Train young generations (and find jobs for them)

# Some of the present-day challenges

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# Change of sign of Sivers function

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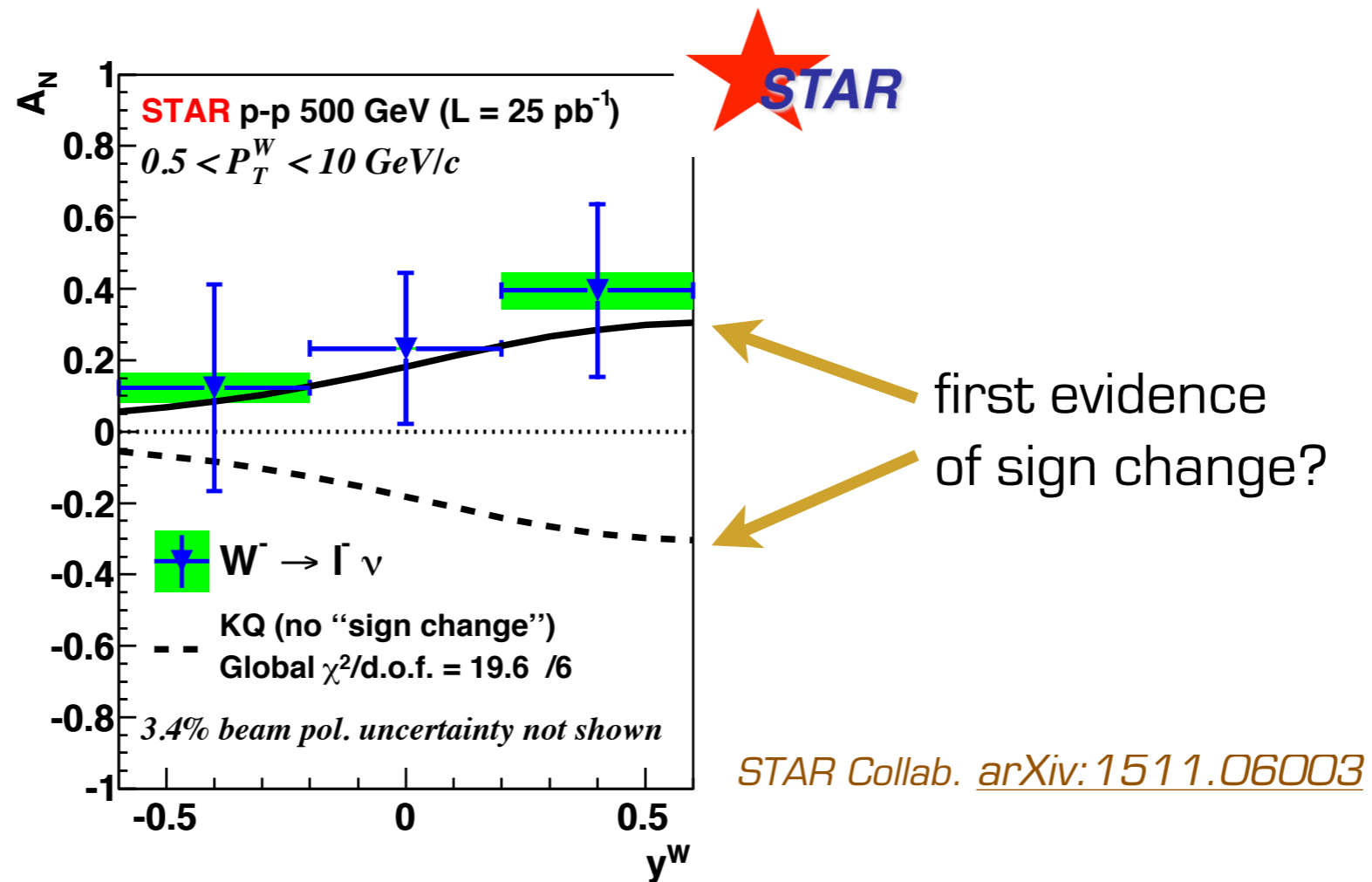
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Sivers function  $\text{SIDIS} = -$  Sivers function Drell-Yan  
*Collins, PLB 536 (02)*

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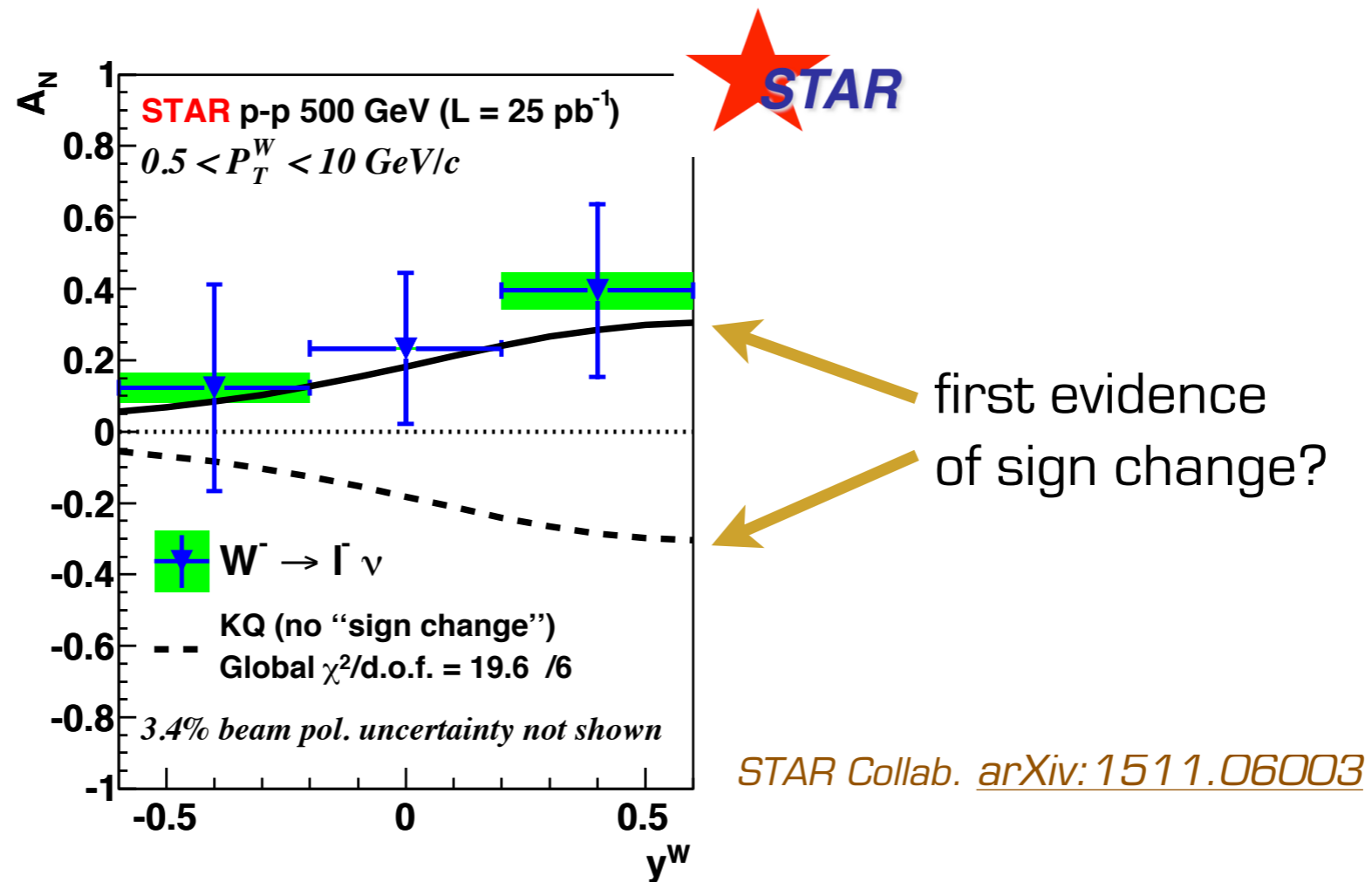
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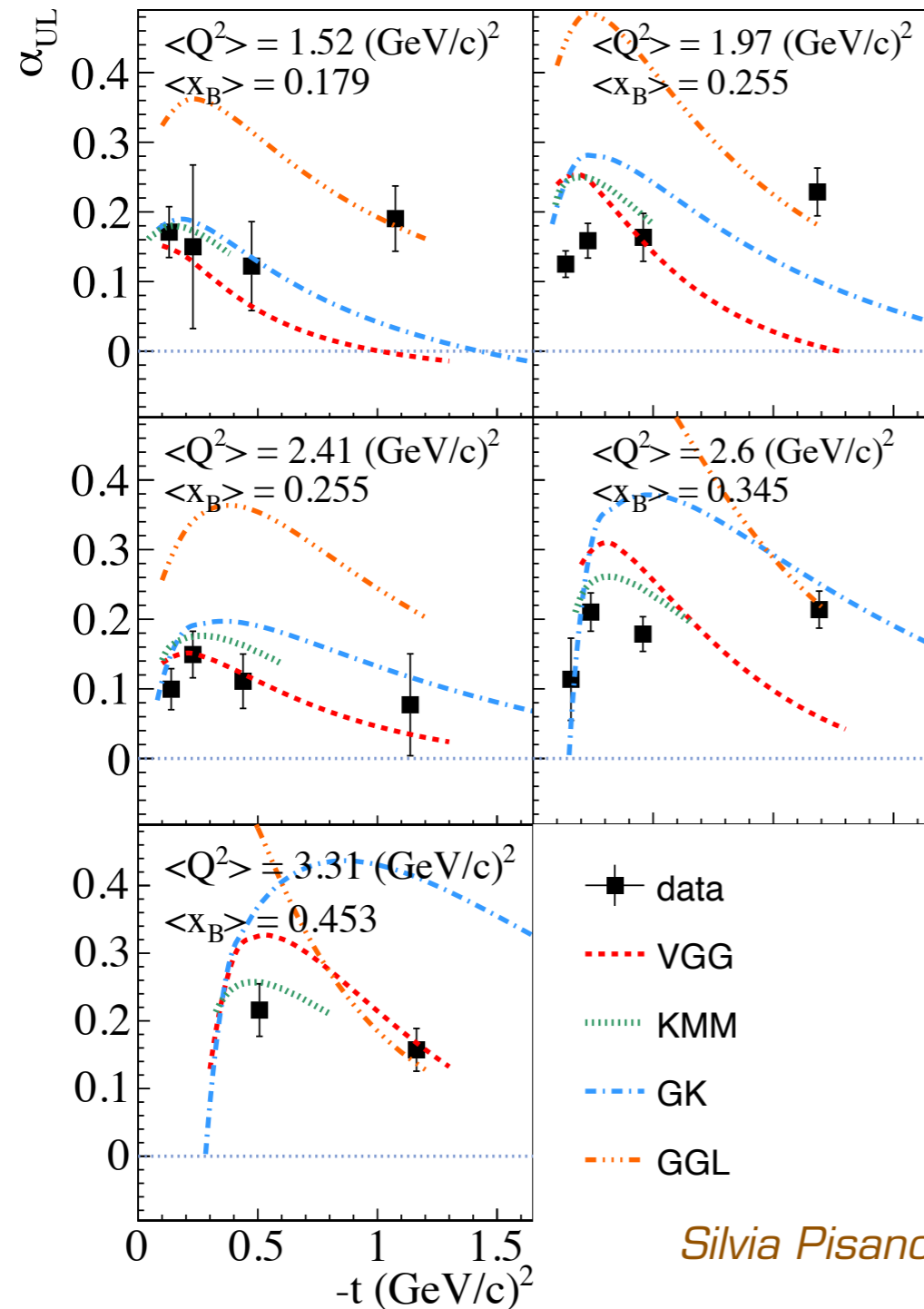
We hope to have a clear result from COMPASS

*see talks by Catarina Quintans*



# GPD parametrizations

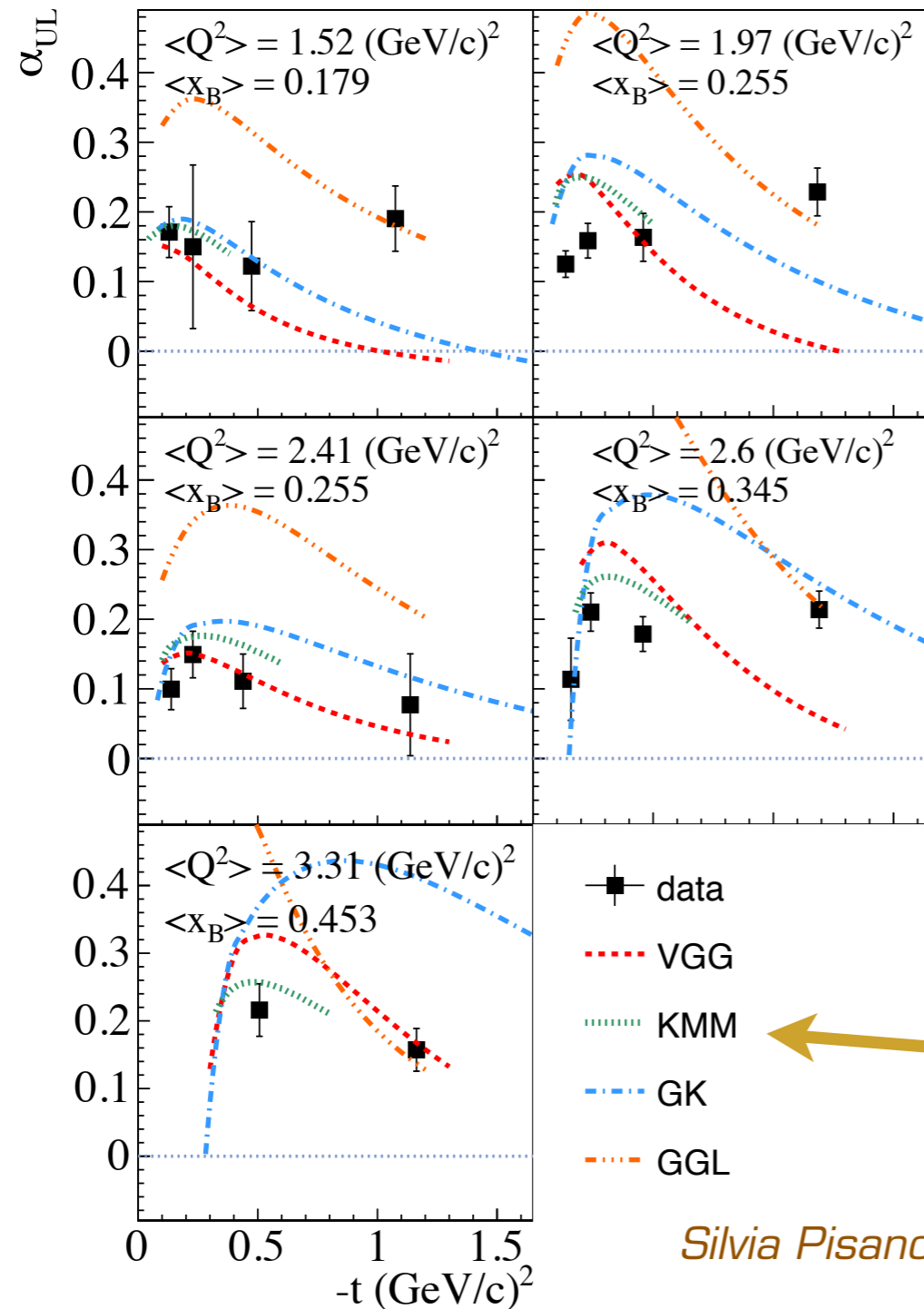
Example of data: target spin asymmetry at CLAS



Silvia Pisano et al., arXiv:1501.07052

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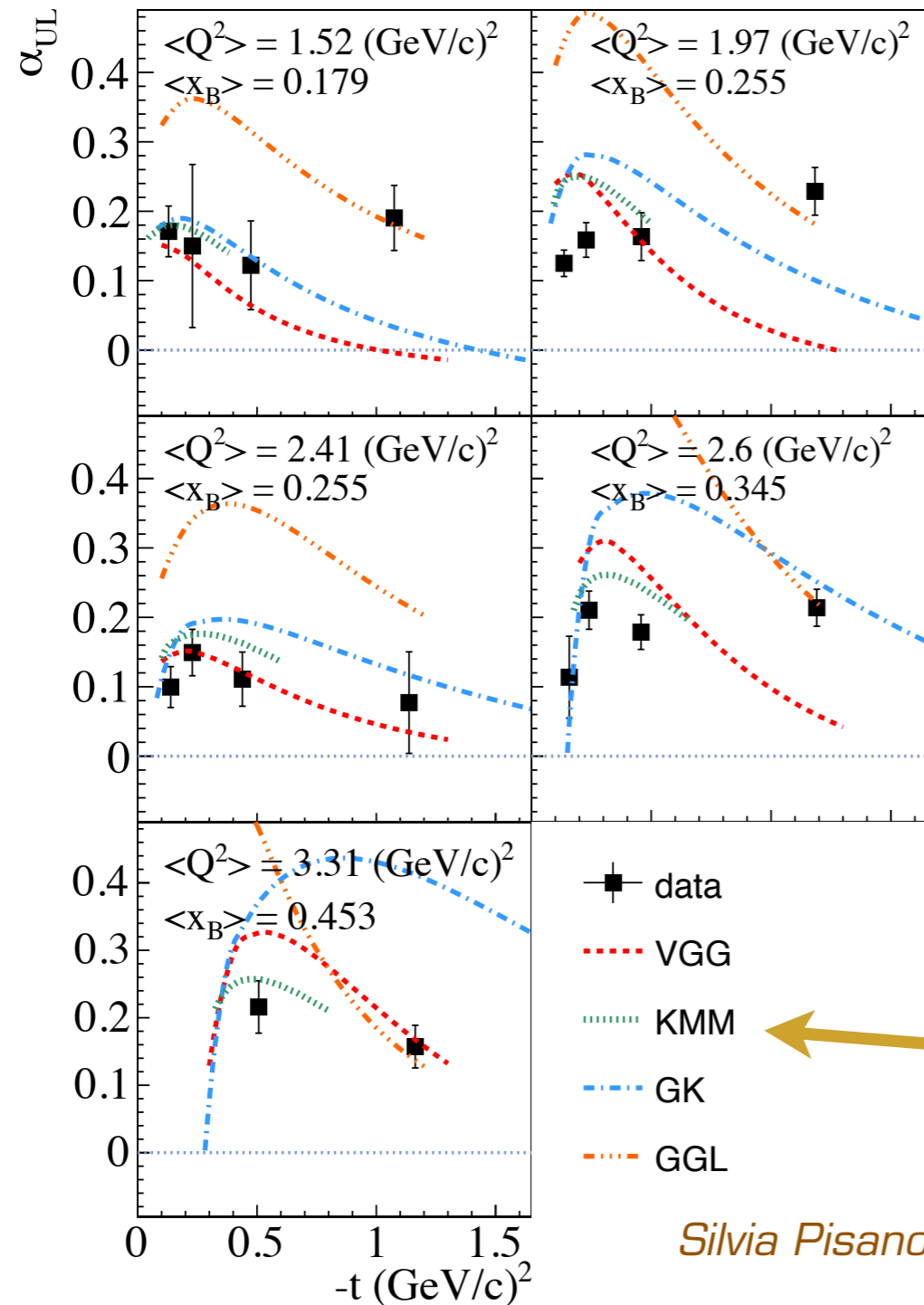


Parametrizations available on the market

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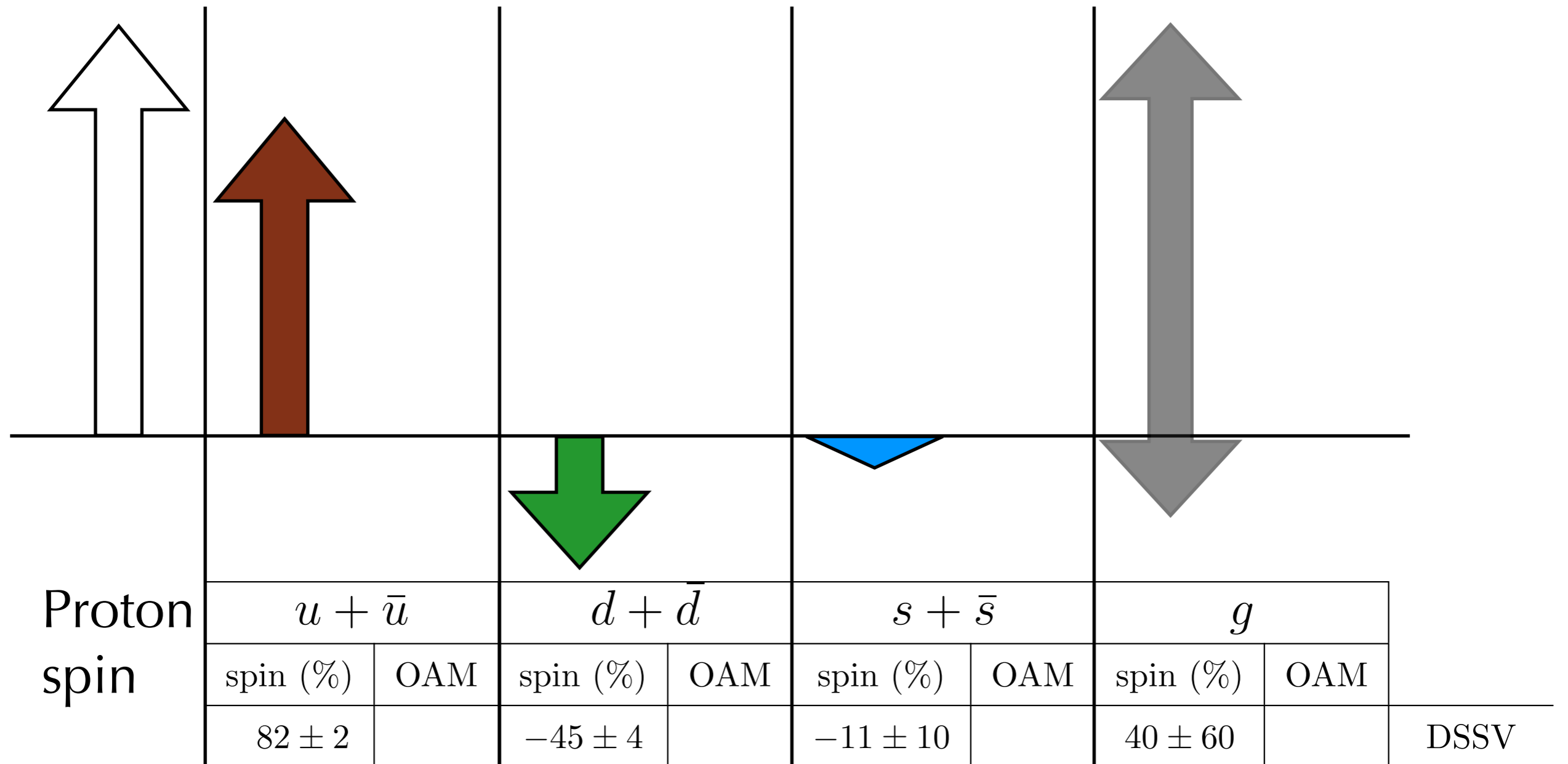


Most parametrizations are not describing ALL data in a satisfactory way.

Parametrizations available on the market

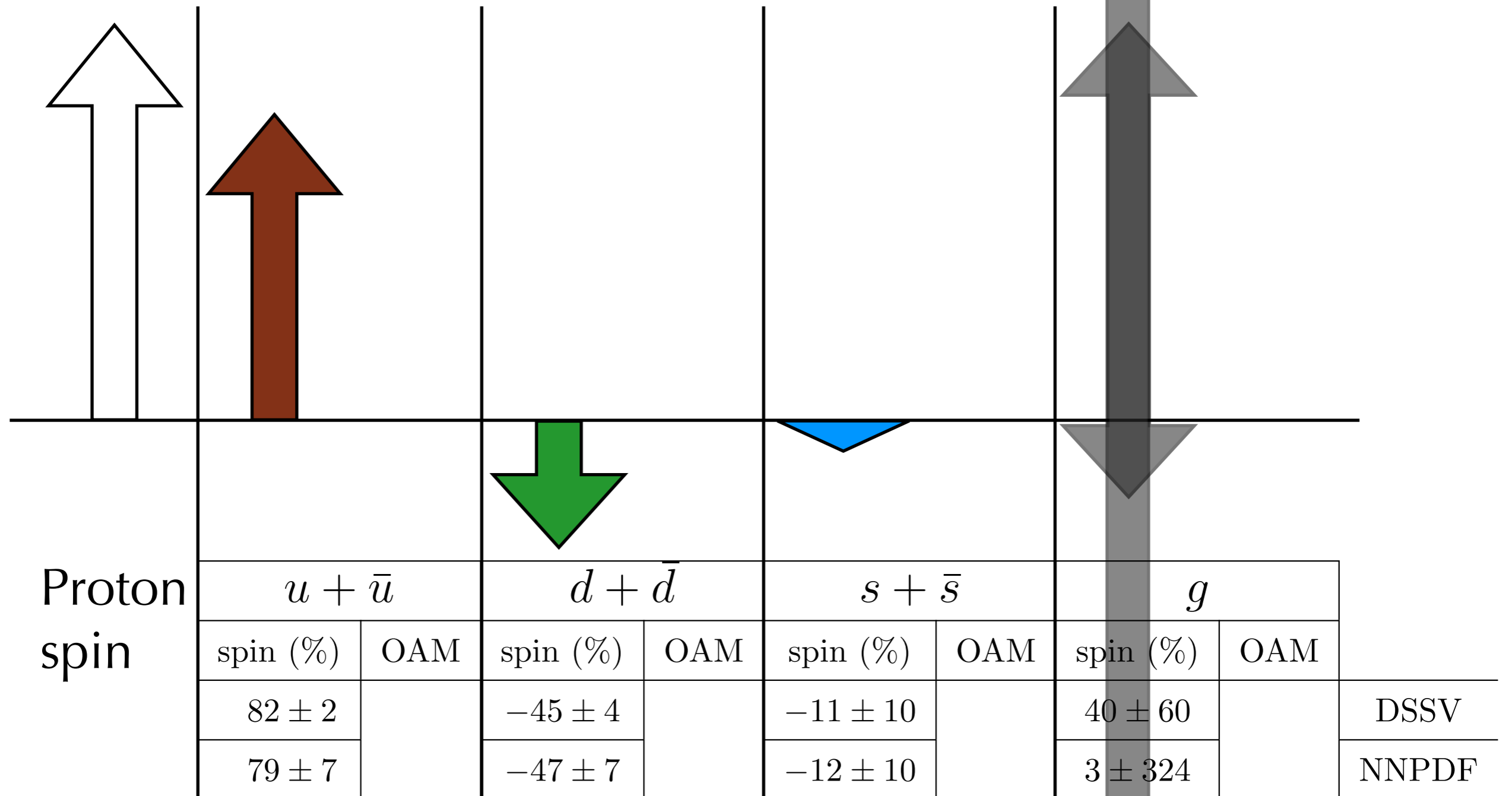
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# Status of spin sum rule



de Florian, Sassot, Stramann, Vogelsang, PRL 113 [14]  
 NNPDF, Ball et al. NPB 887 [14], Tab. 12, 13

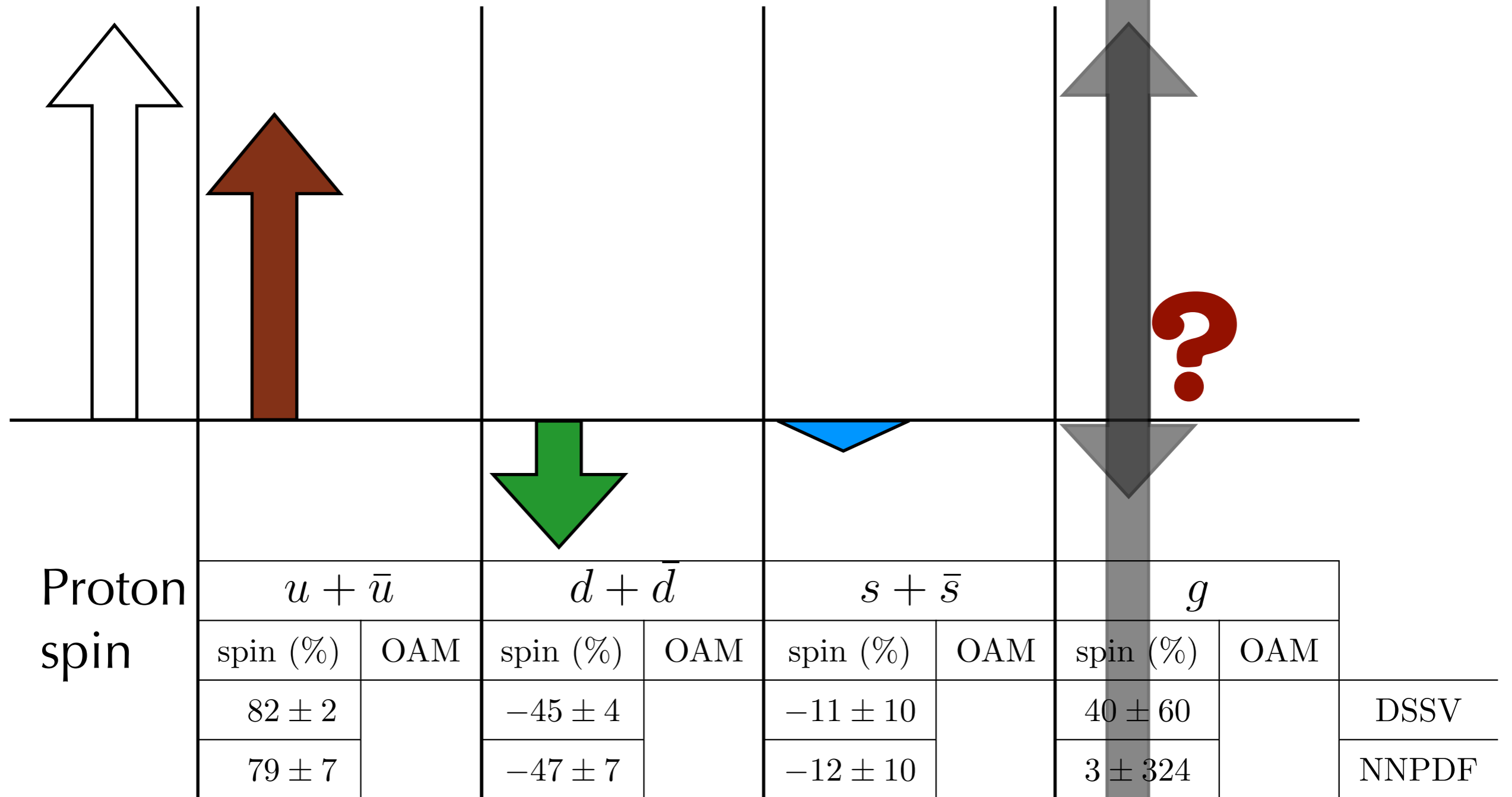
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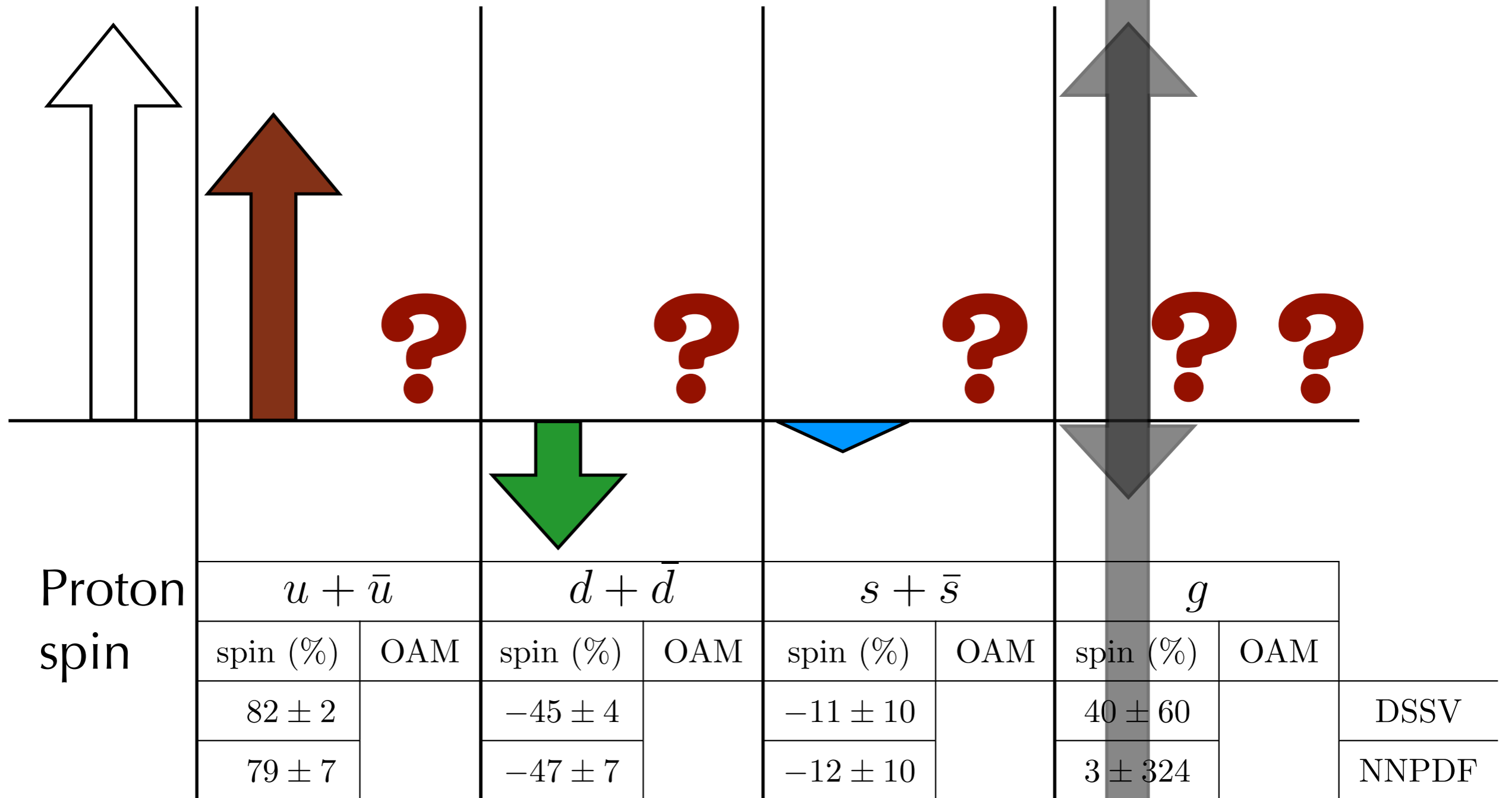
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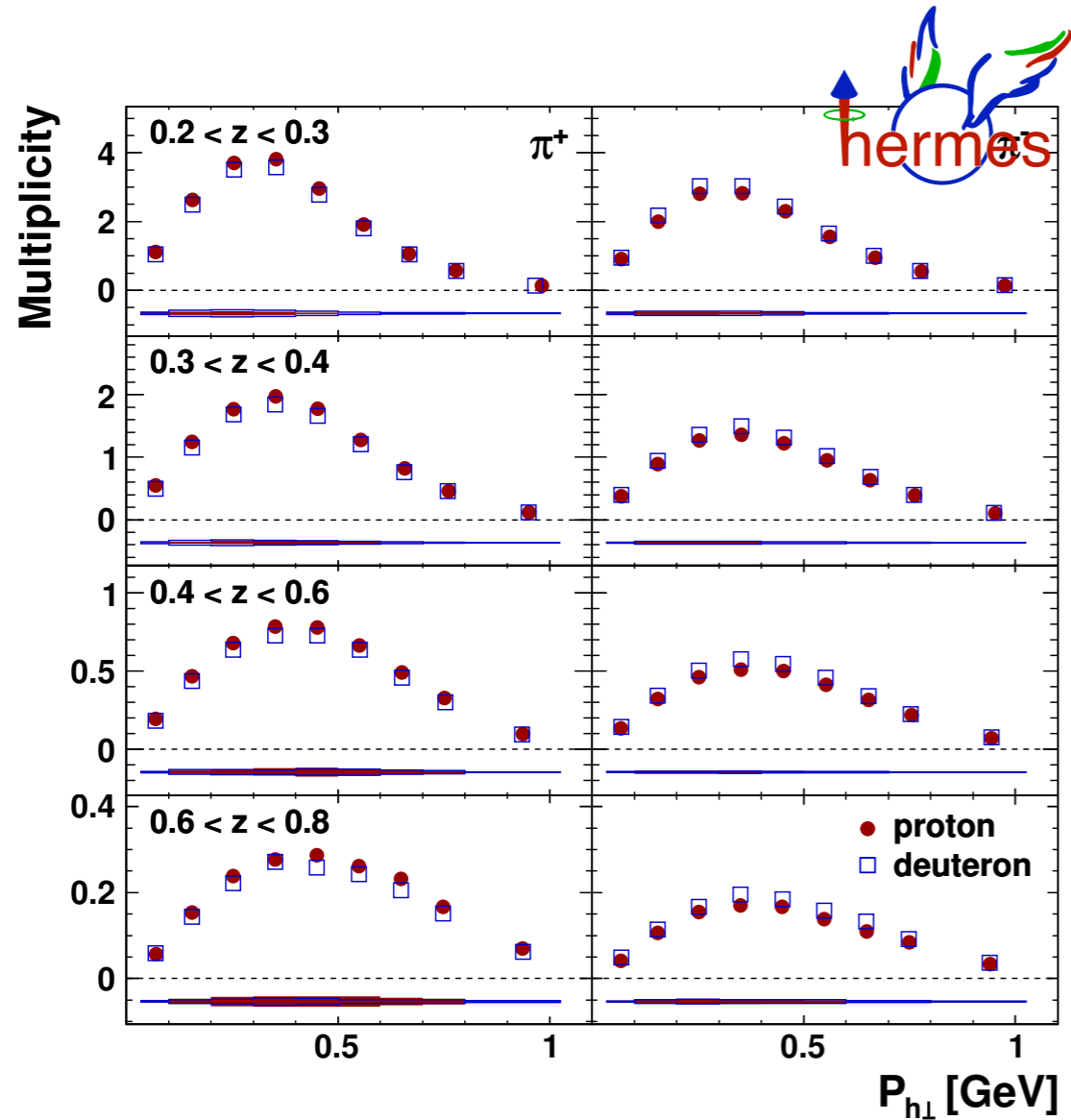


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# TMD evolution

HERMES,  $Q \approx 1.5$  GeV

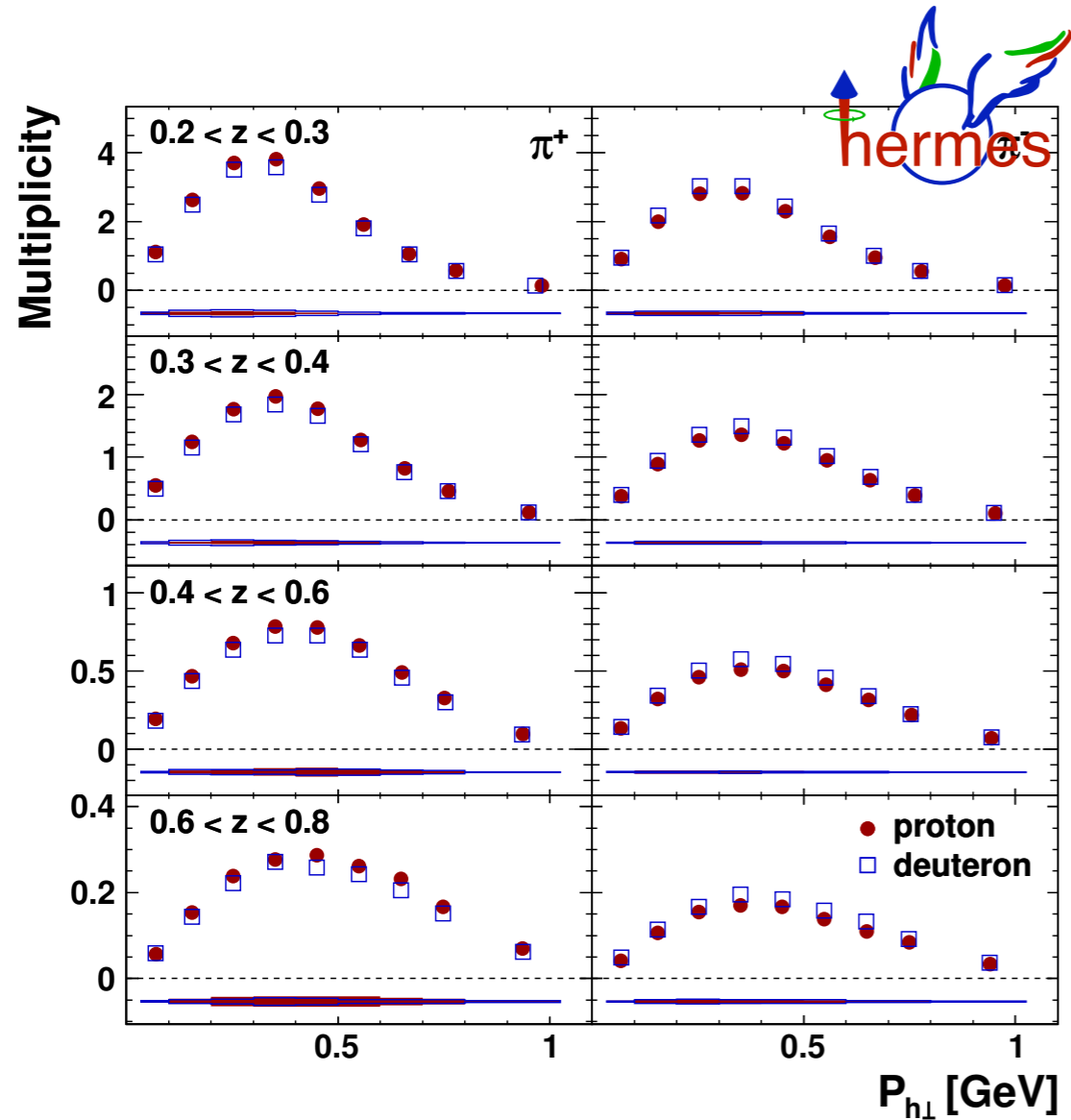


*Airapetian et al., PRD87 (2013)*



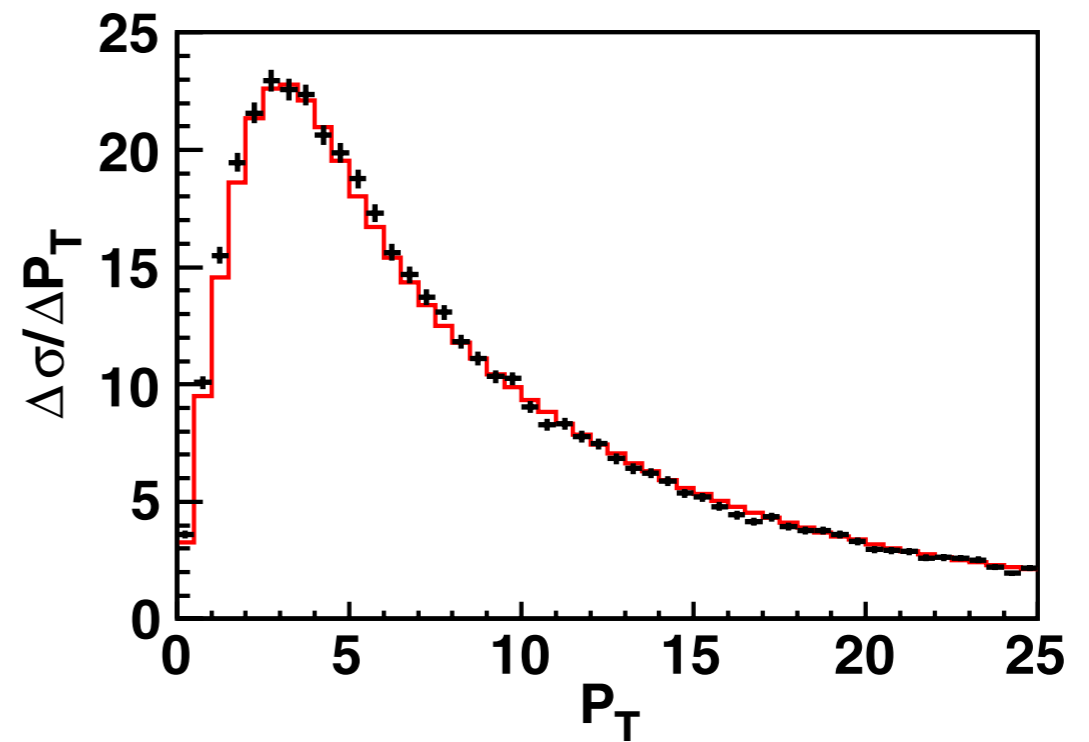
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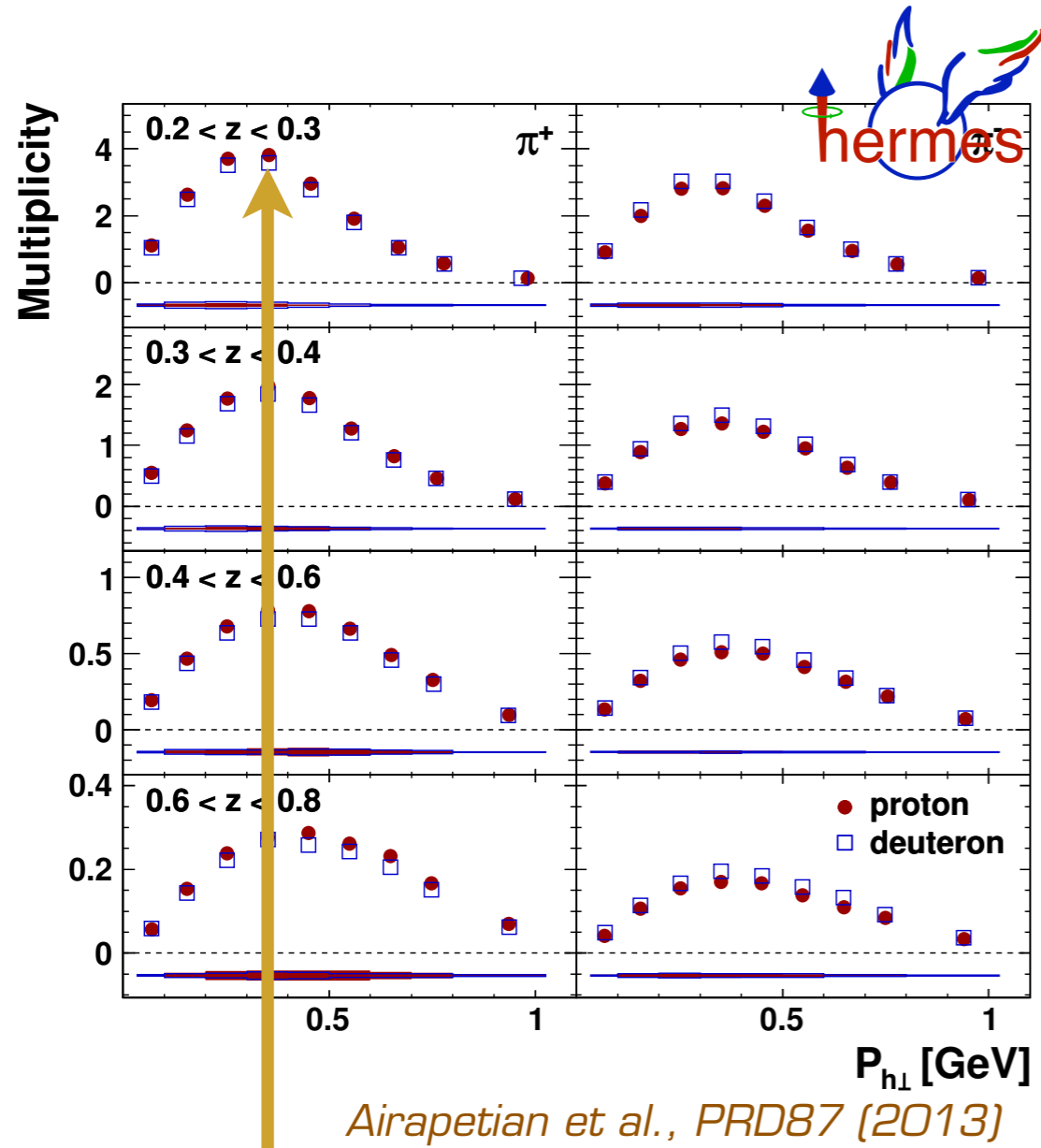
CDF,  $Q \approx 91$  GeV



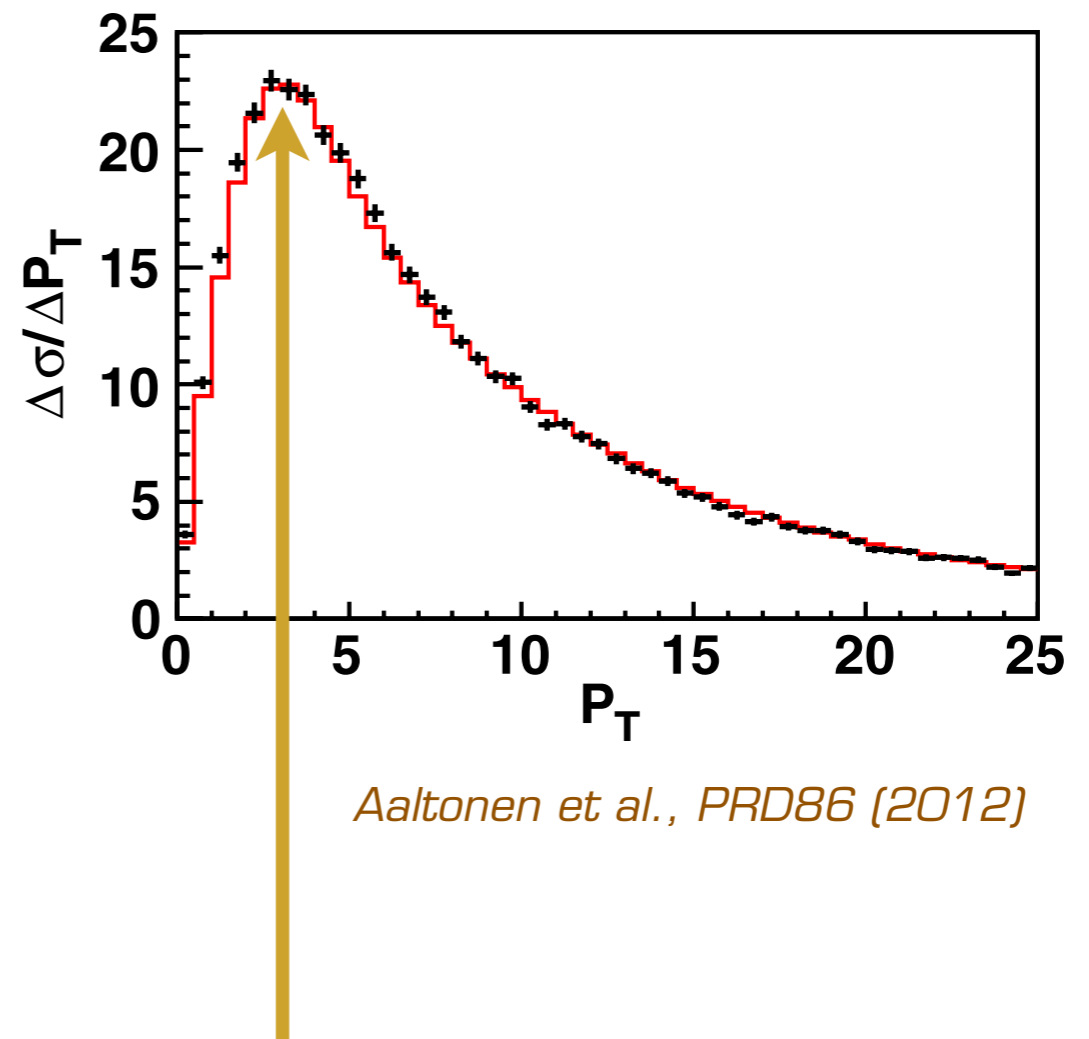
*Aaltonen et al., PRD86 (2012)*

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Width of TMDs changes of one order of magnitude: can we explain this in detail? (TMD evolution)

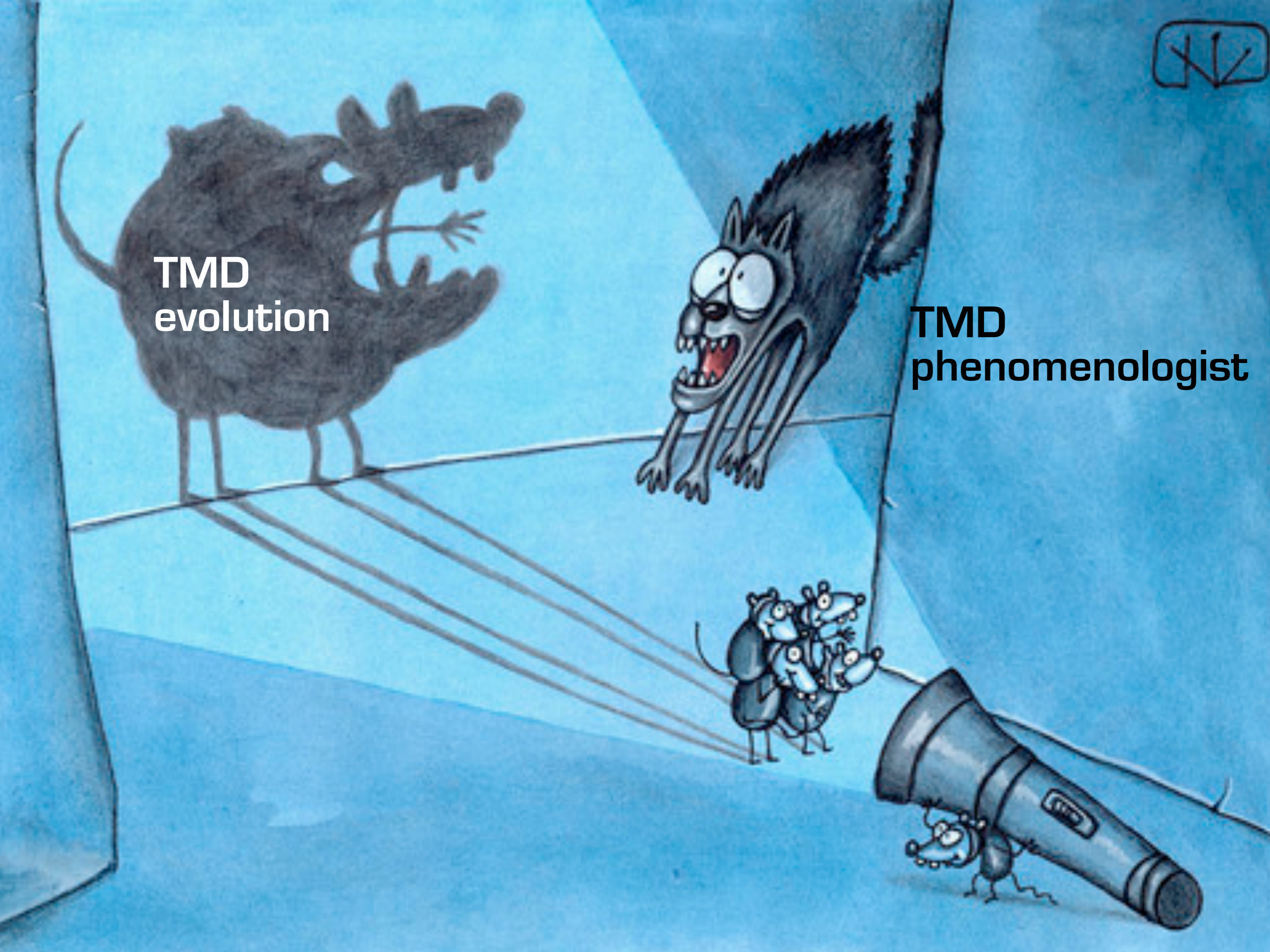


**TMD  
evolution**

**TMD  
phenomenologist**

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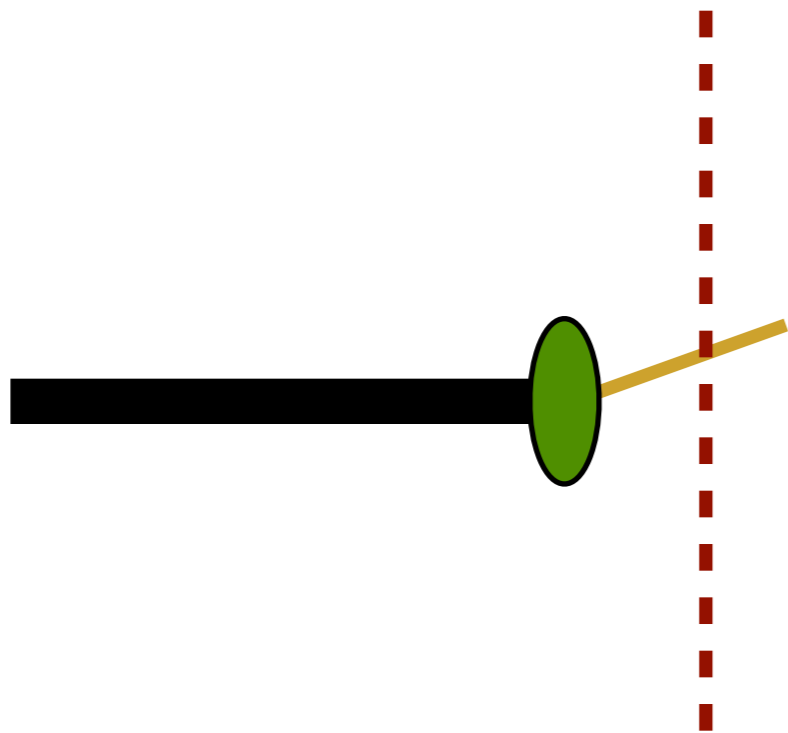
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# TMD and QCD corrections

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“intrinsic”  
transverse  
momentum



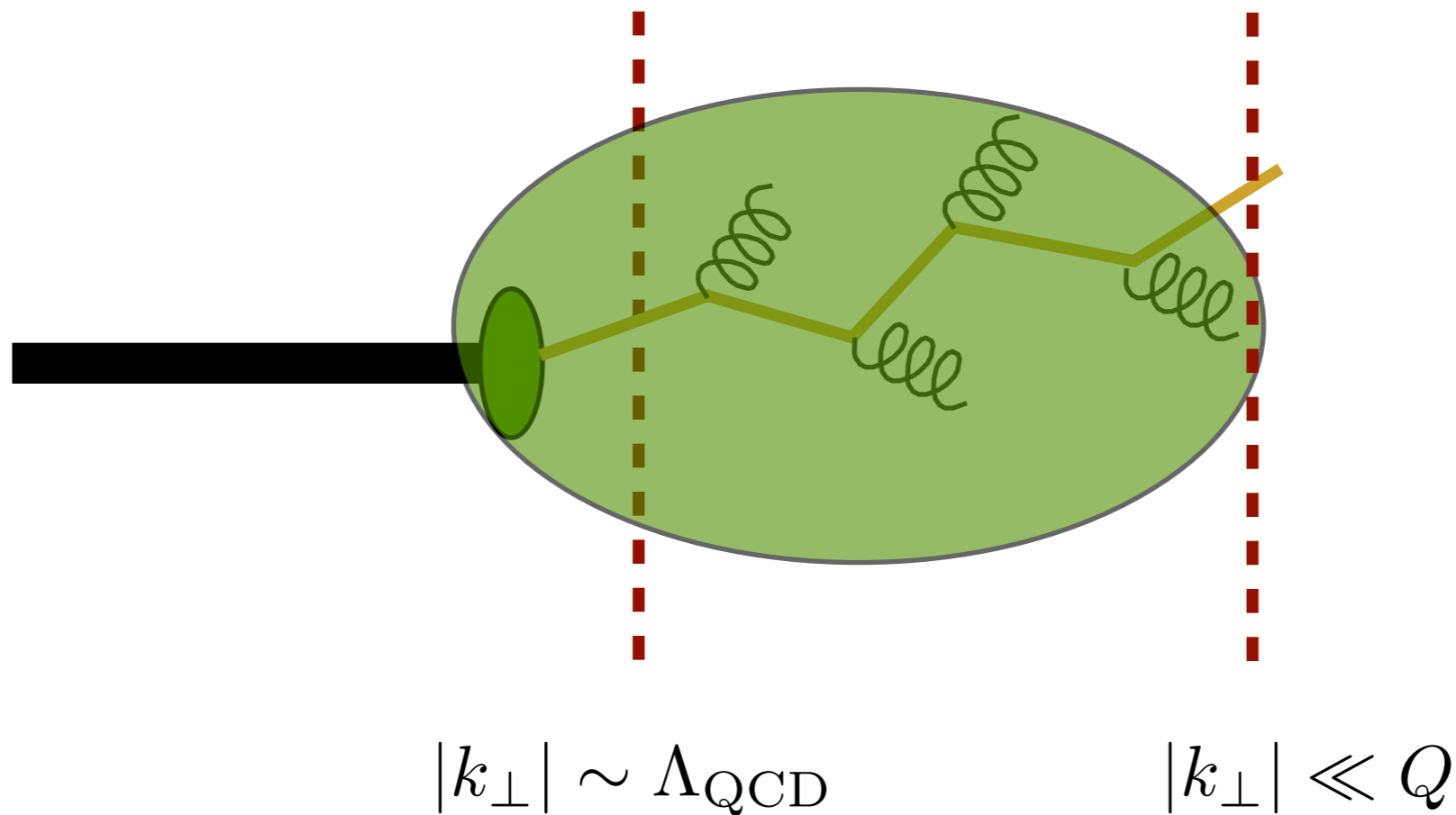
$$|k_{\perp}| \sim \Lambda_{\text{QCD}}$$

# TMD and QCD corrections

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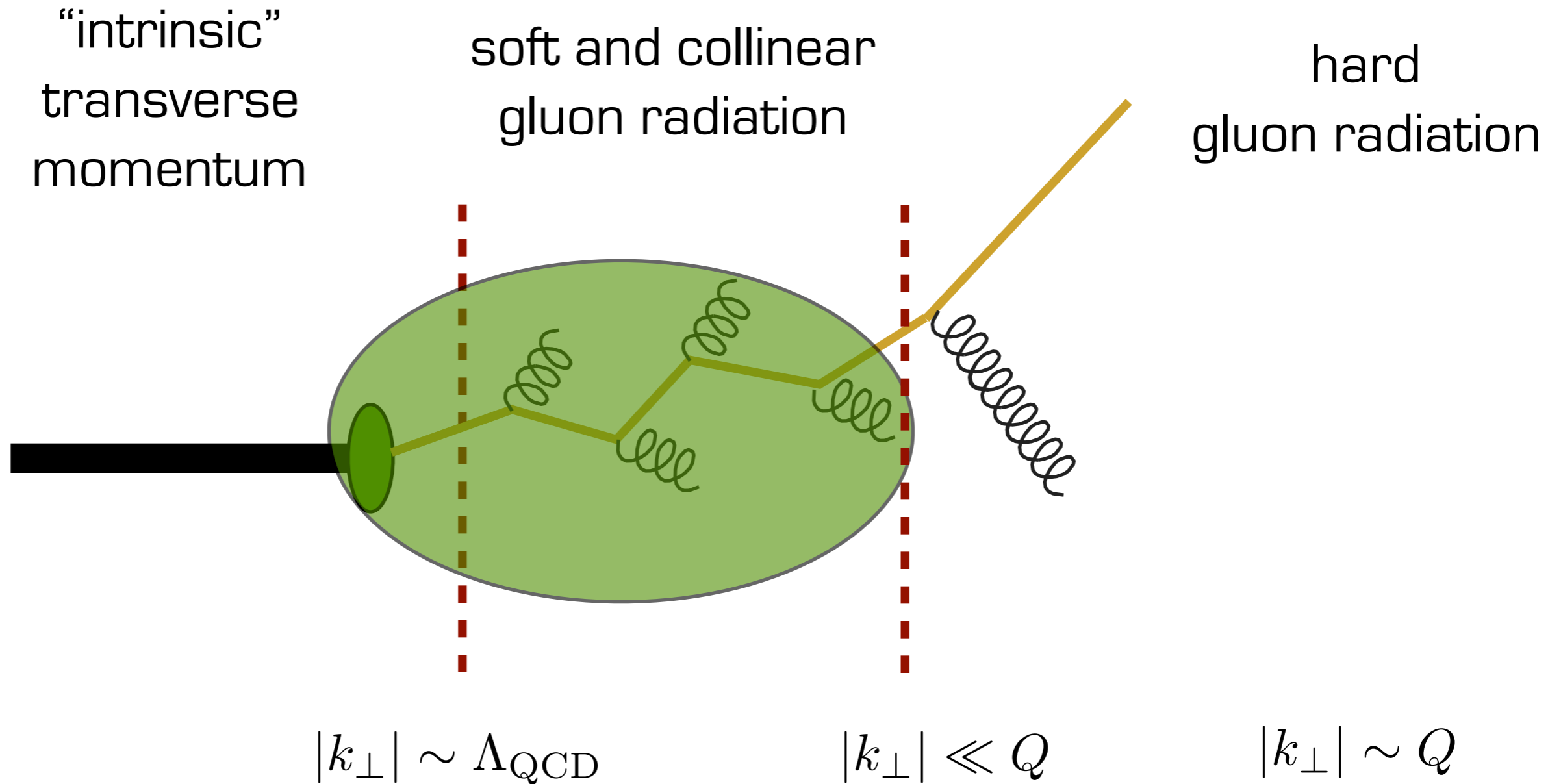
“intrinsic”  
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soft and collinear  
gluon radiation



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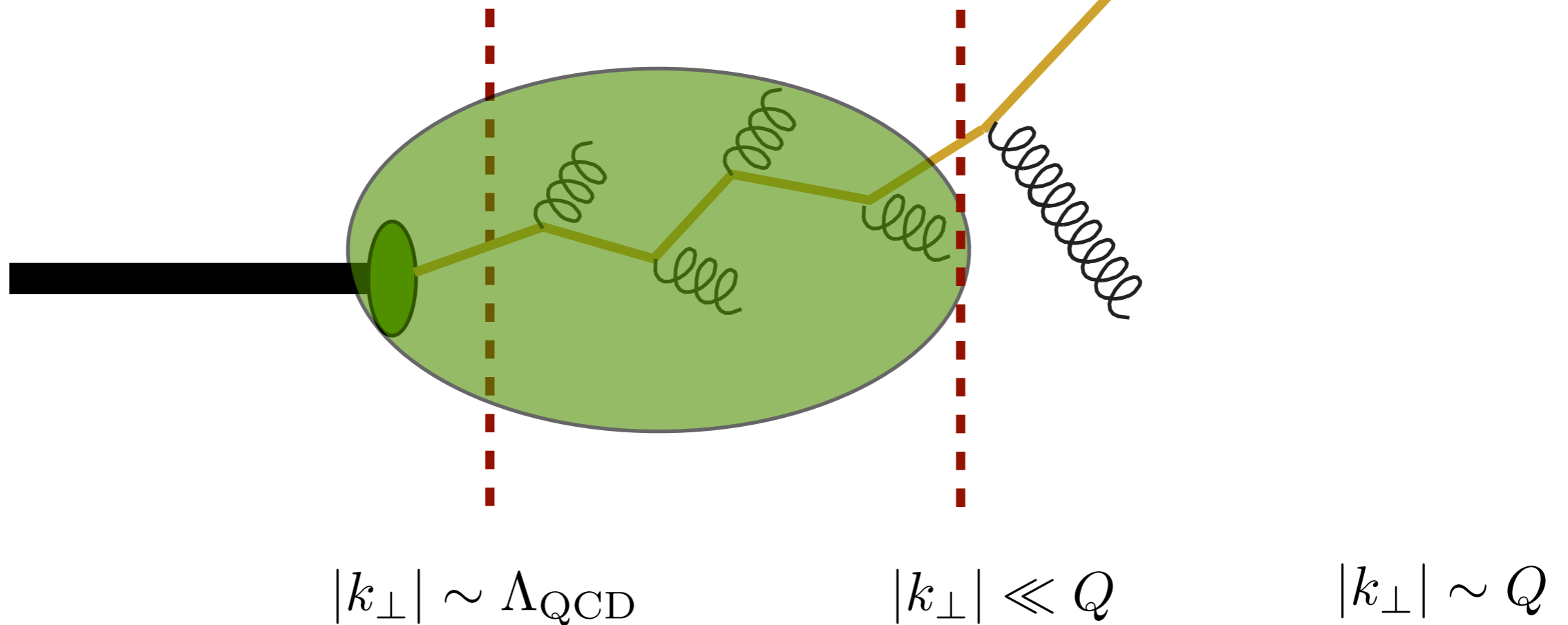
# TMD and QCD corrections

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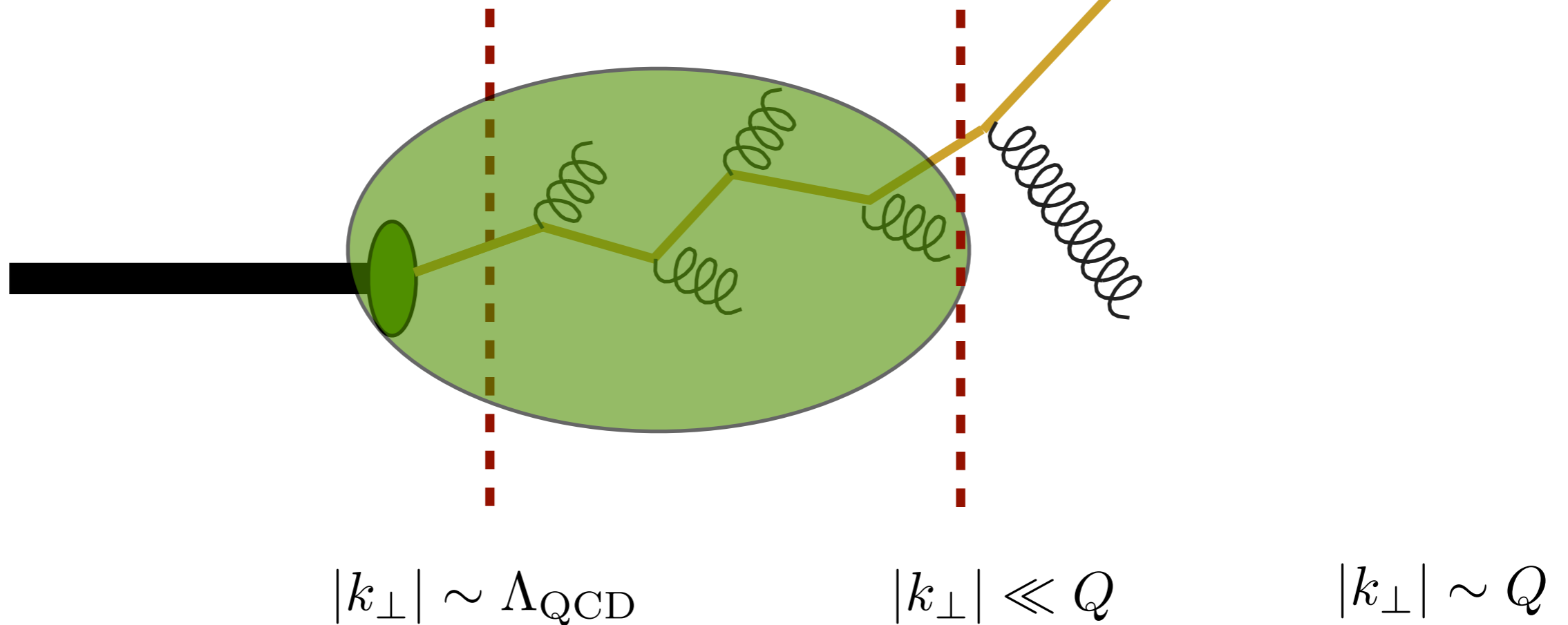
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(standard parton distribution functions - PDFs)



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Parton model

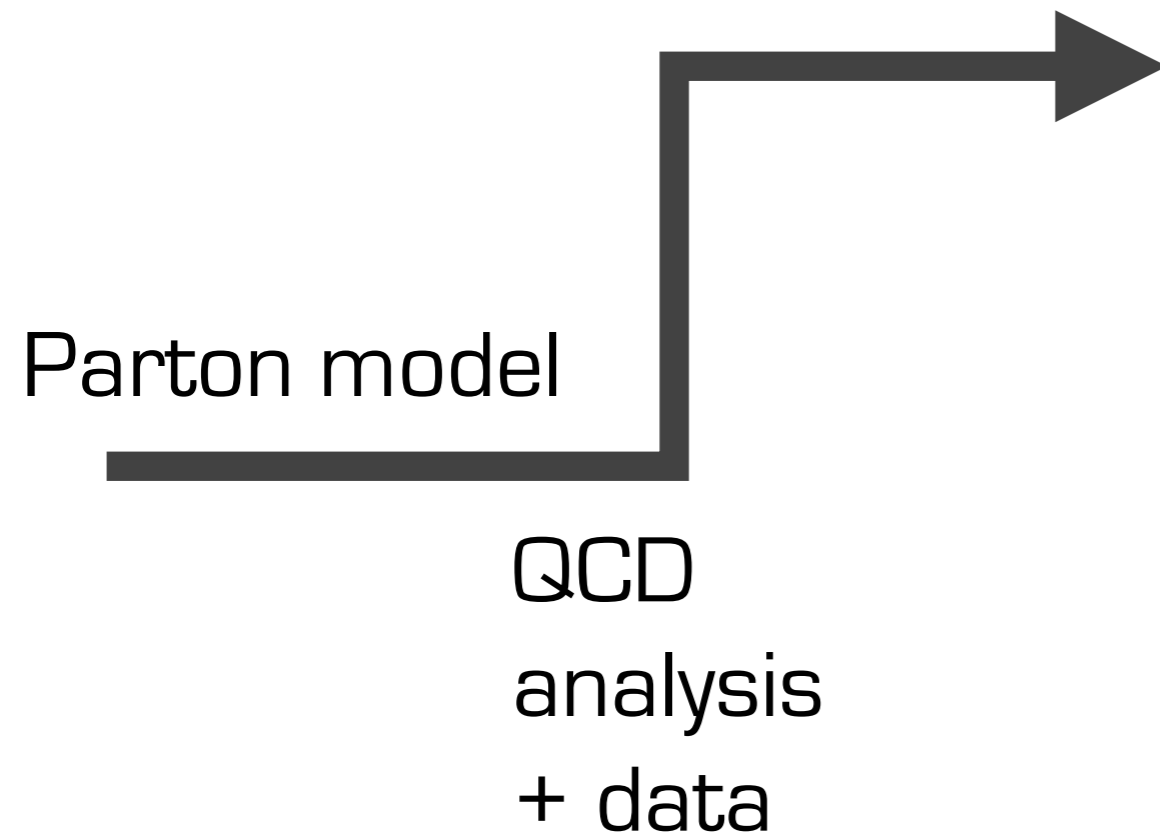


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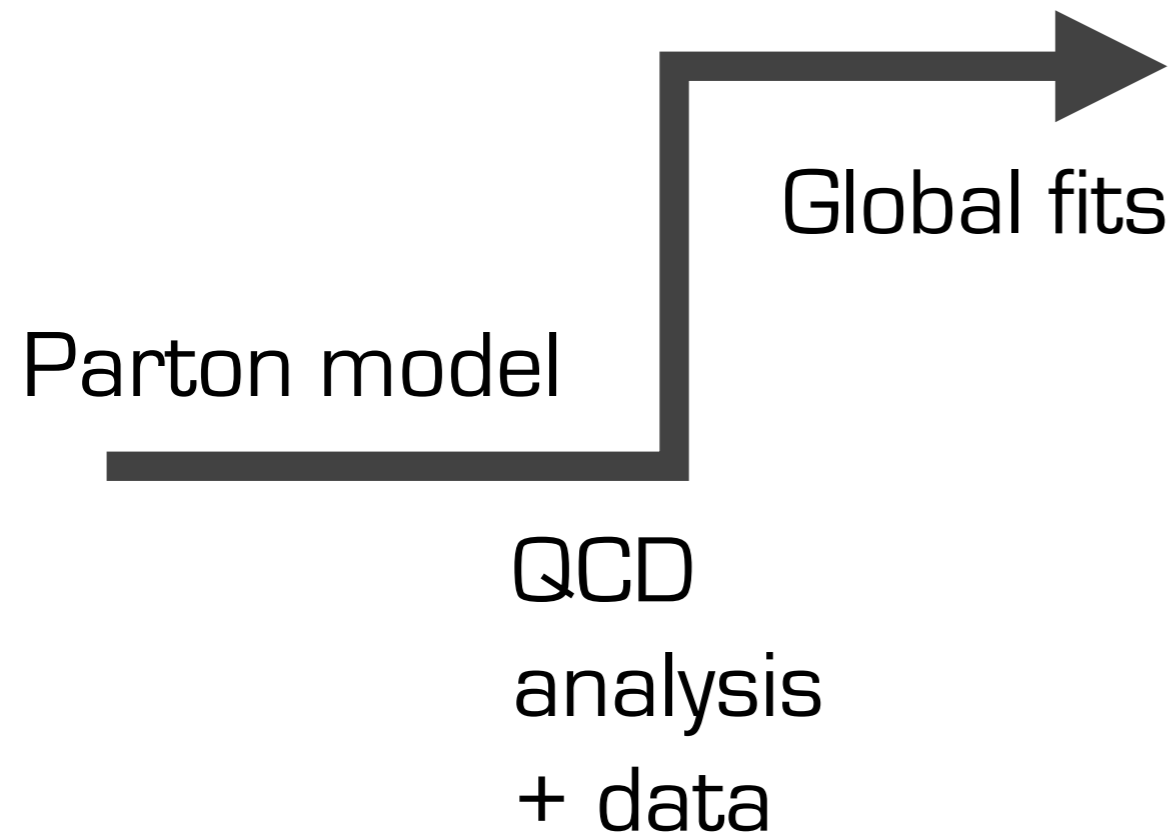


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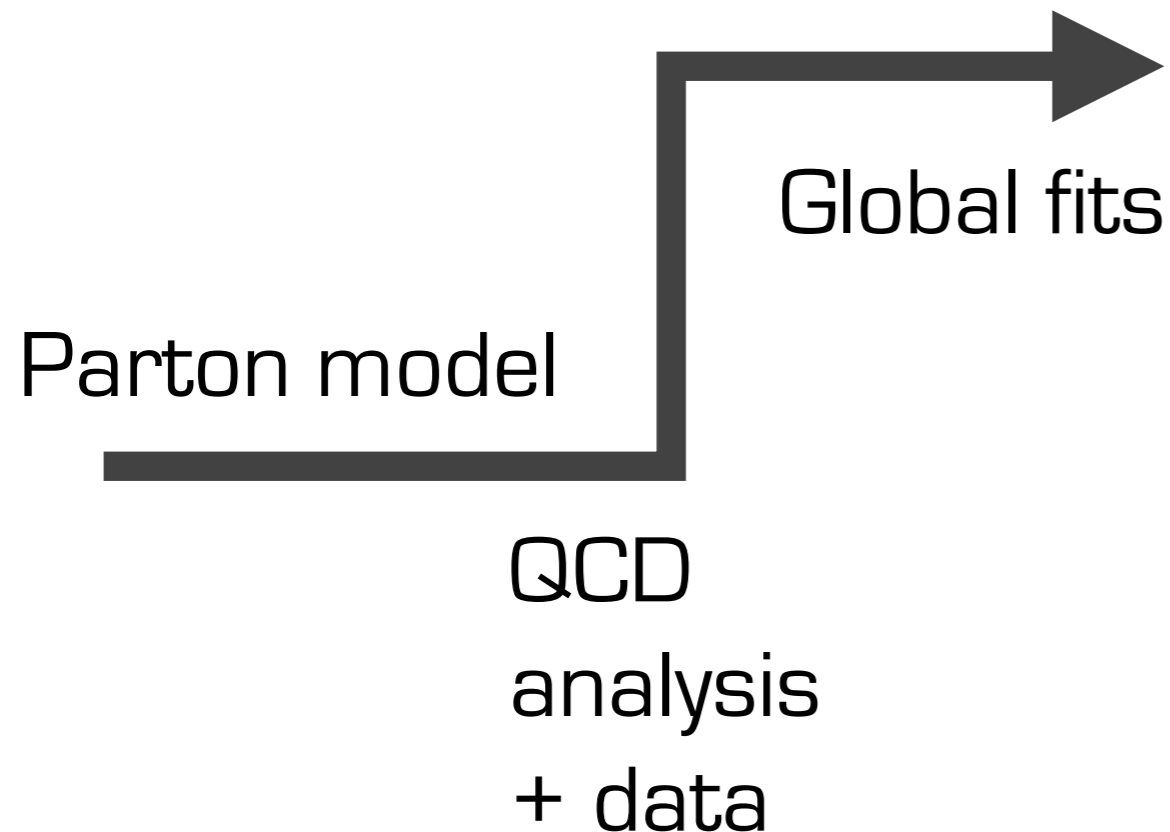


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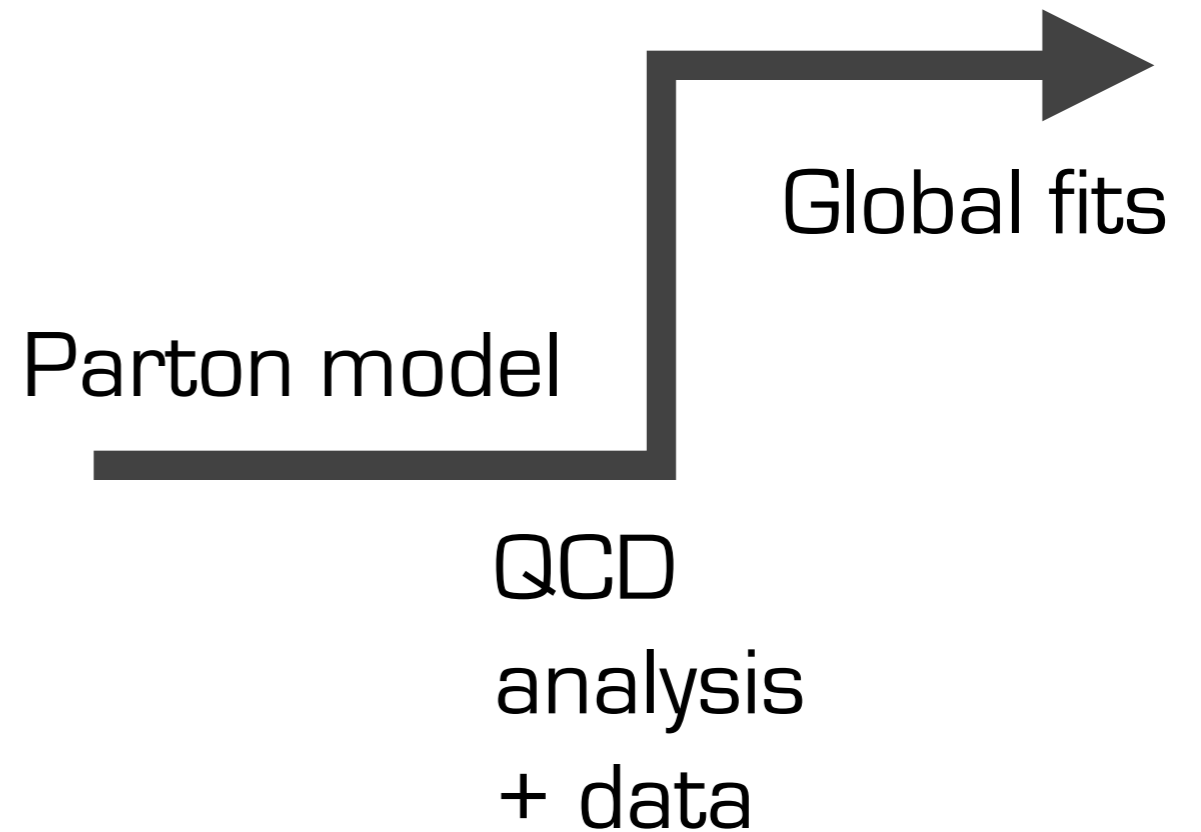
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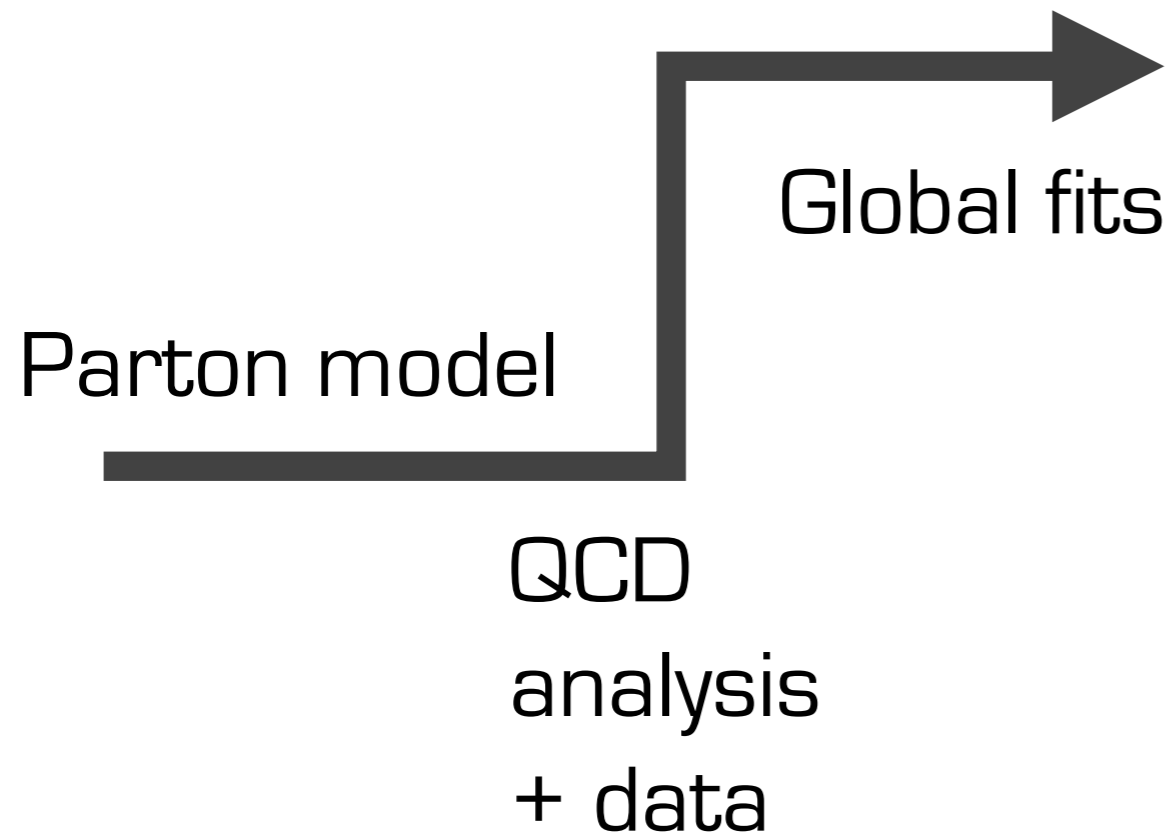


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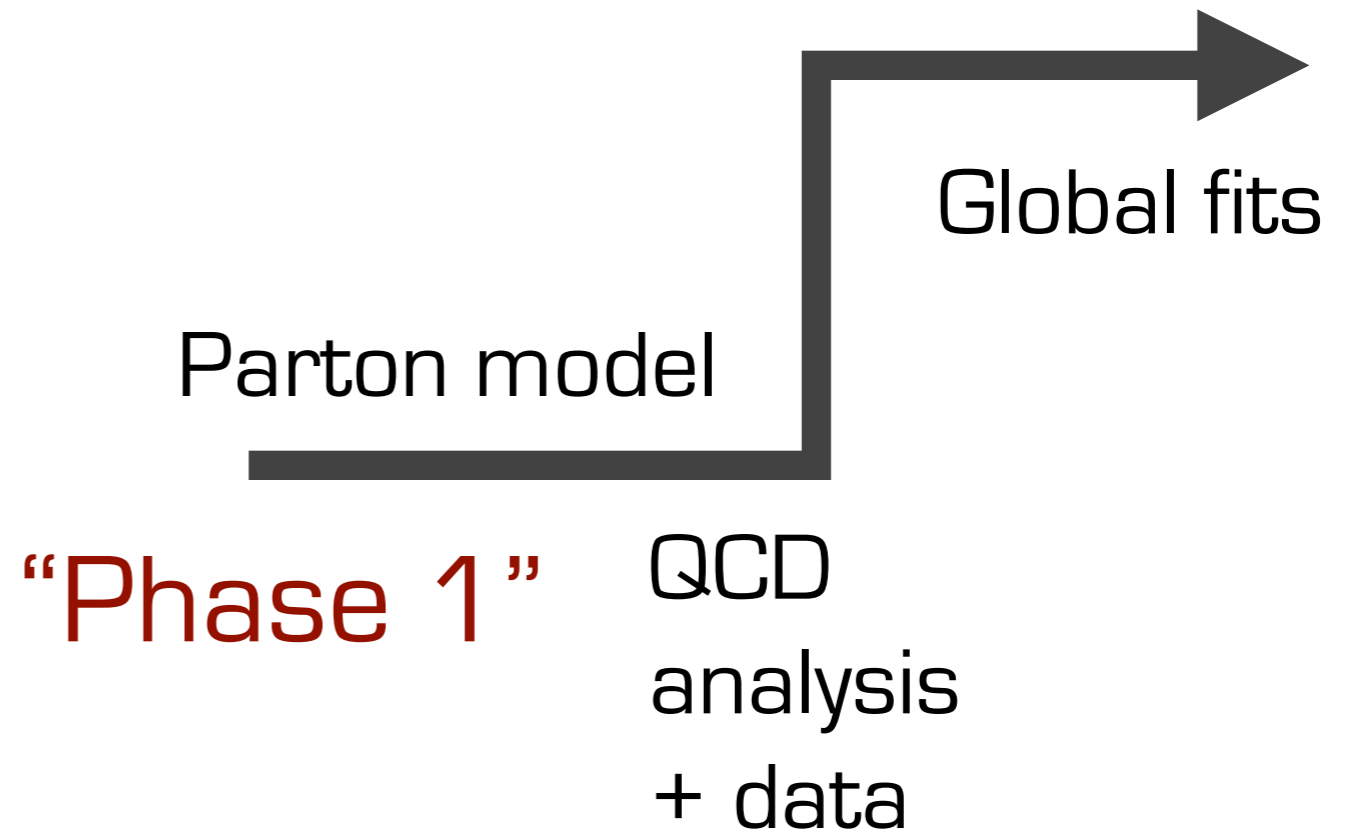
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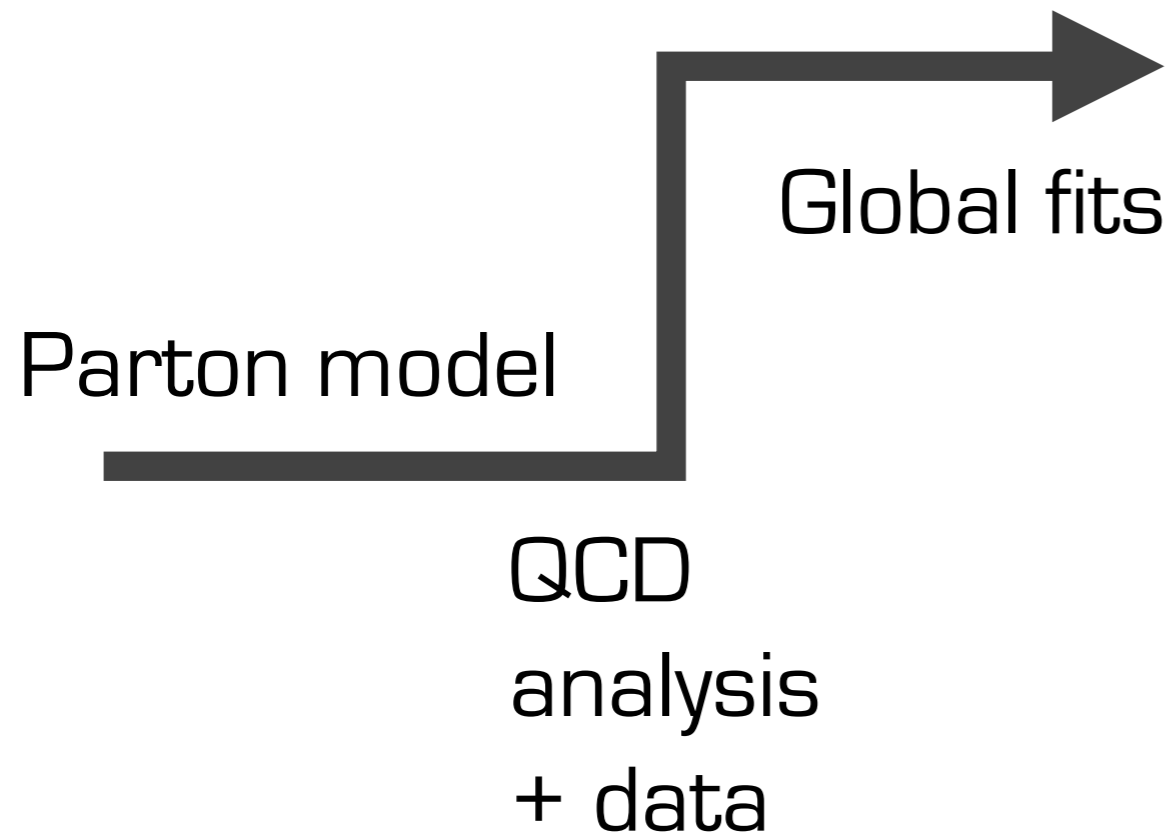


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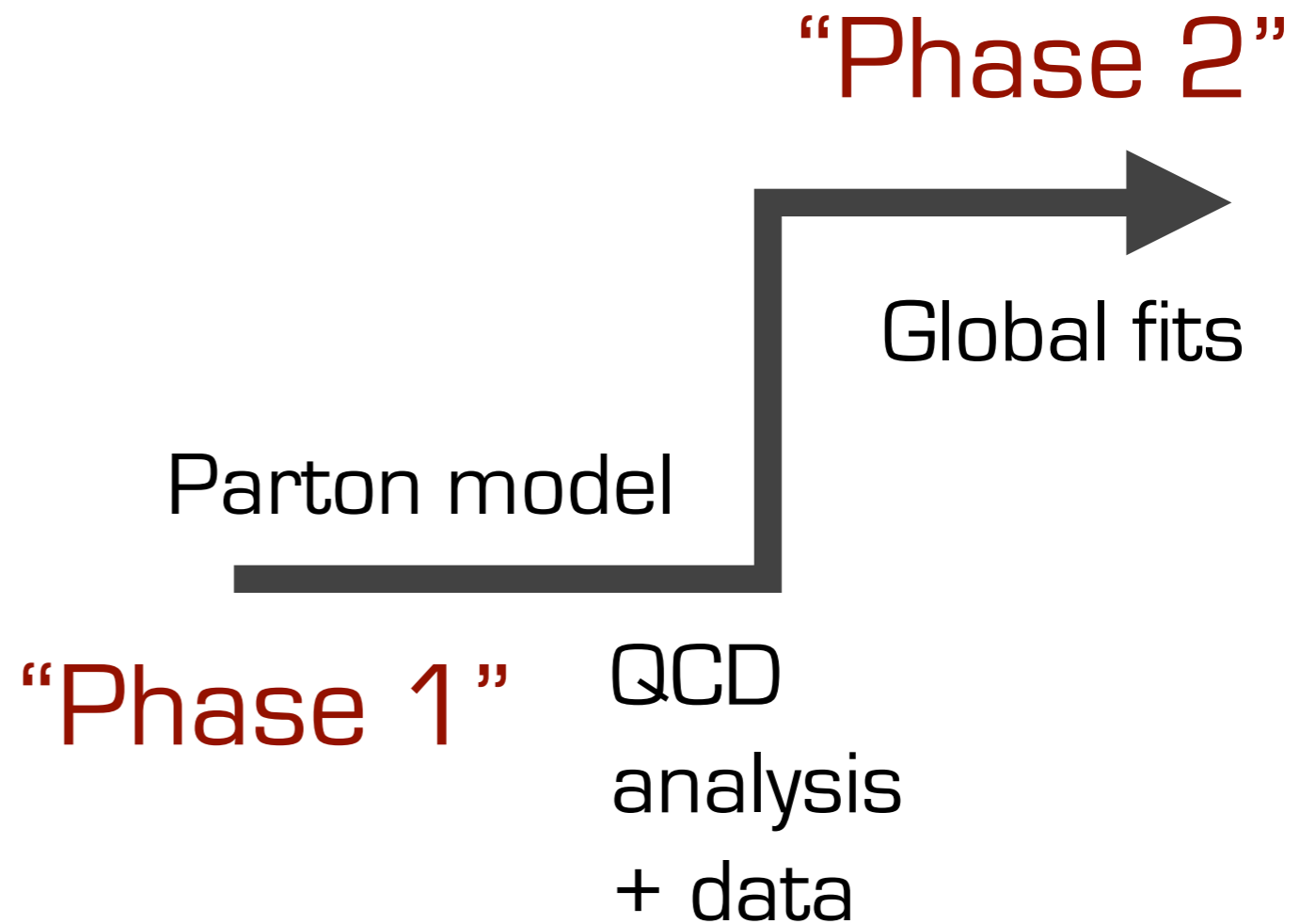
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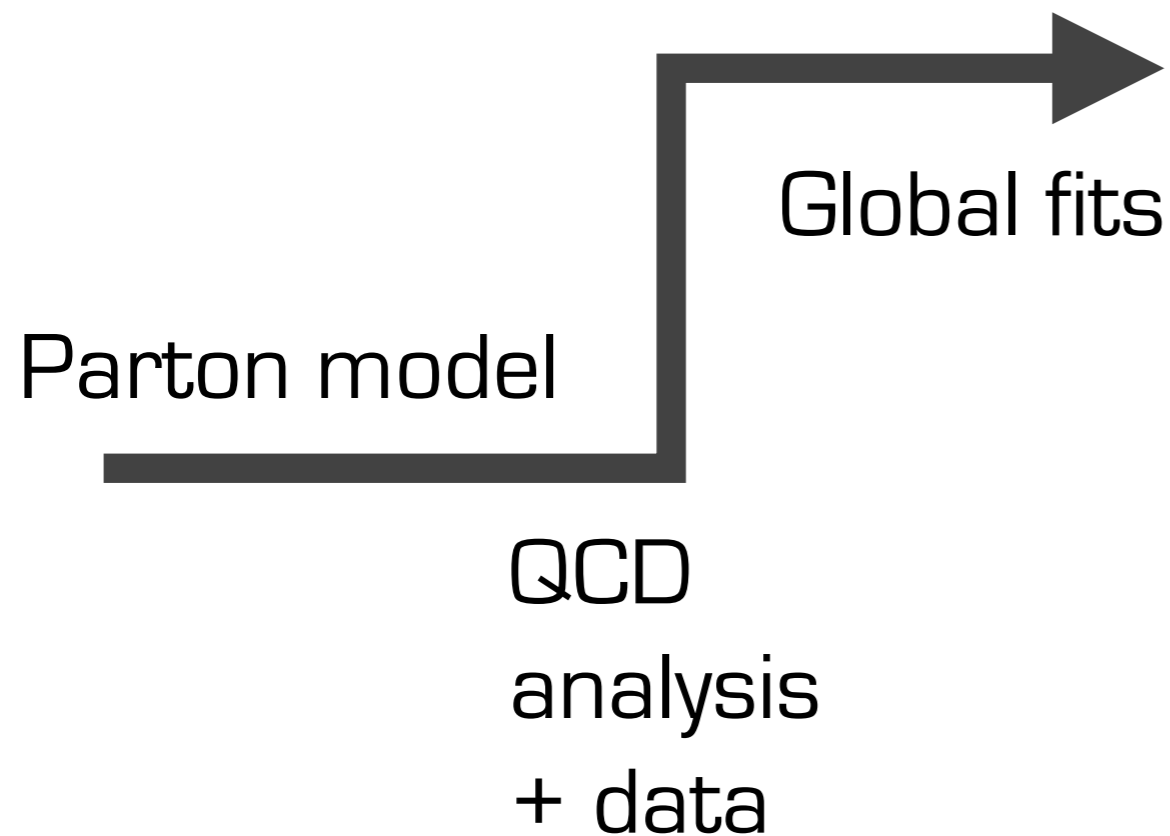


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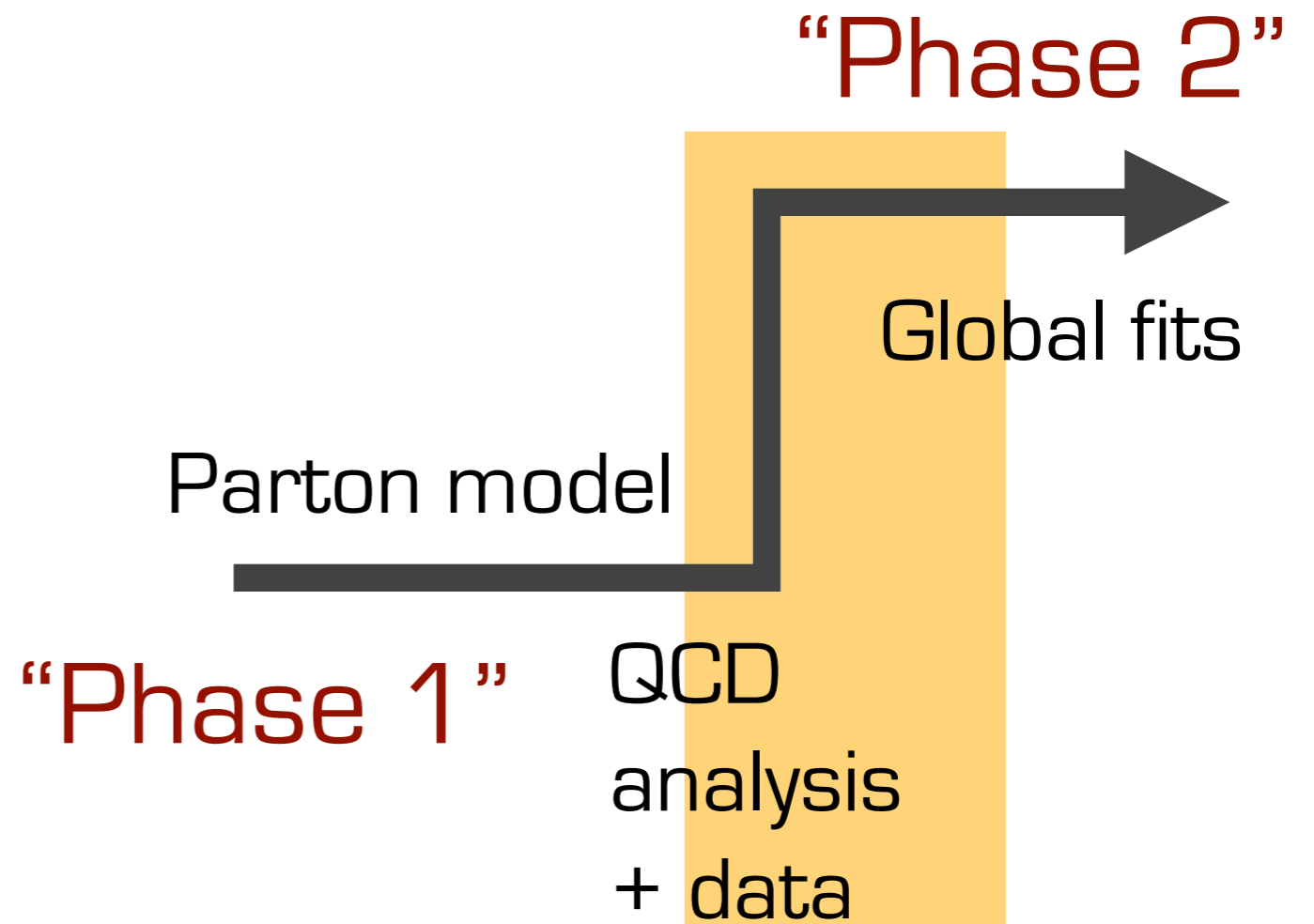
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**Phase  
1  
“parton  
model”**

**Phase  
2  
“global  
fits”**

# TMD evolution: Fourier transform

---

$$f_1^a(x, k_\perp; \mu^2) = \frac{1}{2\pi} \int d^2b_T e^{-ib_T \cdot k_\perp} \tilde{f}_1^a(x, b_T; \mu^2)$$

*Rogers, Aybat, PRD 83 (11)*

*Collins, "Foundations of Perturbative QCD" (11)*

*possible schemes, e.g.,*

*Collins, Soper, Sterman, NPB250 (85)*

*Laenen, Sterman, Vogelsang, PRL 84 (00)*

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collinear PDF

pQCD

nonperturbative part  
of evolution

nonperturbative part  
of TMD

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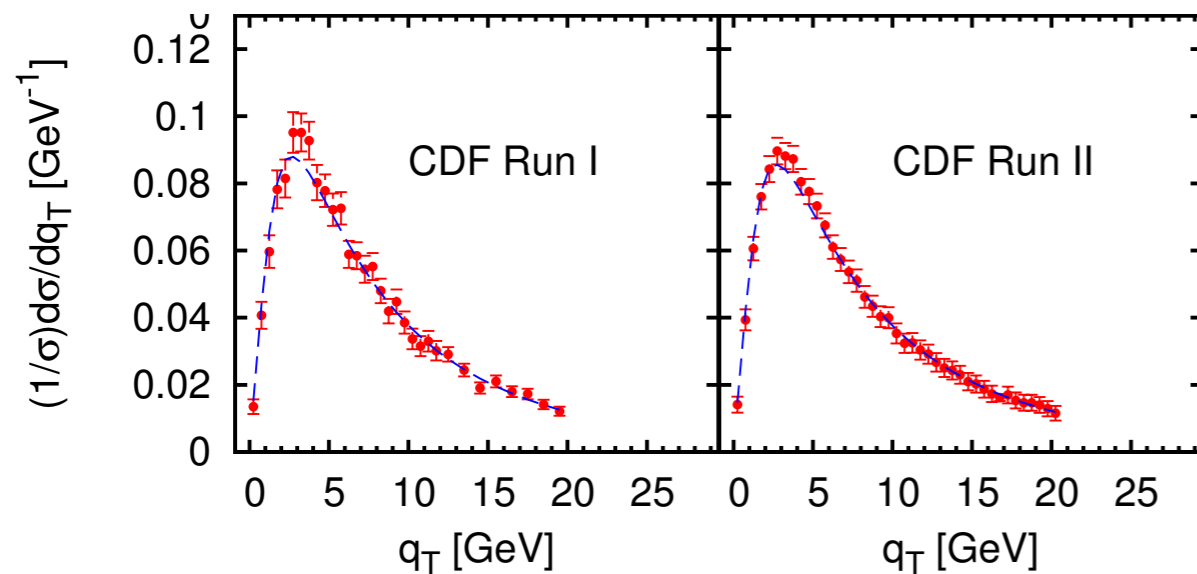
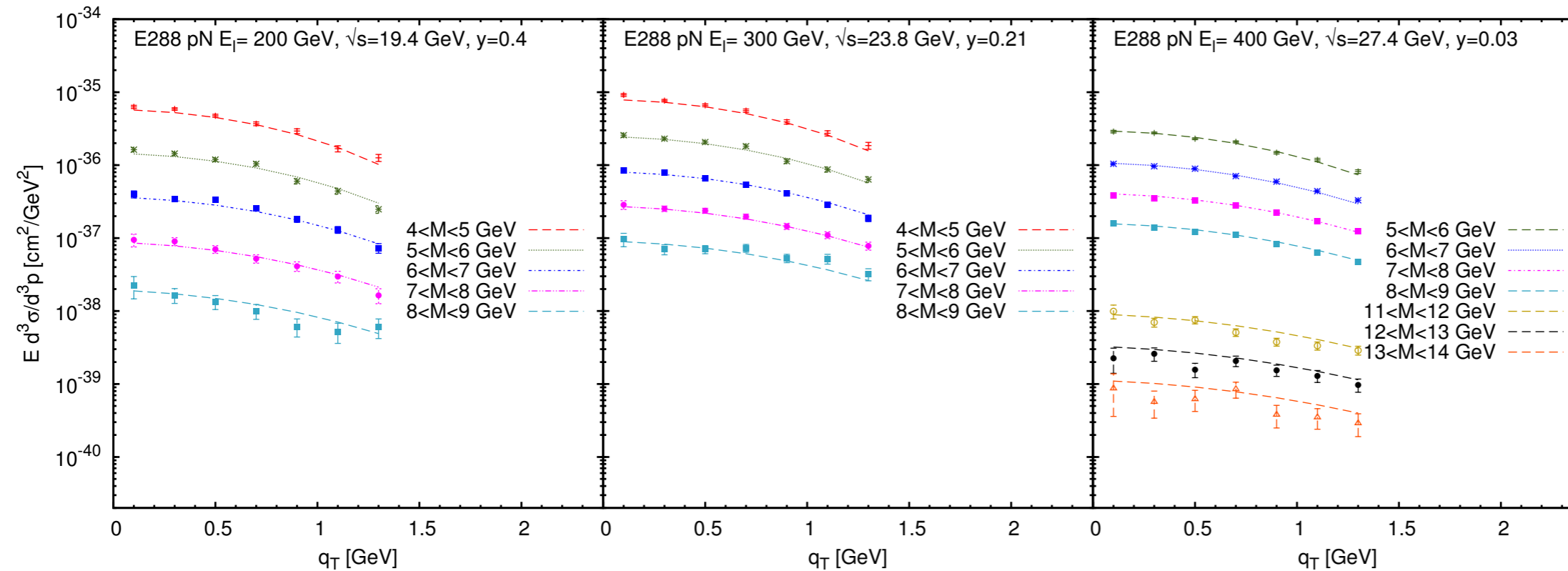
# Presently *or soon* available fits

	Framework	HERMES	COMPASS	DY	Z production	N of points
KN 2006 <a href="#"><i>hep-ph/0506225</i></a>	NLL	✗	✗	✓	✓	98
Pavia 2013 (+Amsterdam, Bilbao) <a href="#"><i>arXiv:1309.3507</i></a>	No evo	✓	✗	✗	✗	1538
Torino 2014 (+JLab) <a href="#"><i>arXiv:1312.6261</i></a>	No evo	✓ (separately)	✓ (separately)	✗	✗	576 (H) 6284 (C)
DEMS 2014 <a href="#"><i>arXiv:1407.3311</i></a>	NNLL	✗	✗	✓	✓	223
EIKV 2014 <a href="#"><i>arXiv:1401.5078</i></a>	NLL	1 (x, Q <sup>2</sup> ) bin	1 (x, Q <sup>2</sup> ) bin	✓	✓	500 (?)
Pavia 2016	NLL	✓	✓	✓	✓	8156

# DEMS 2014

*D'Alesio, Echevarria, Melis, Scimemi, JHEP 1411 (14)*

NNLL-NNLO



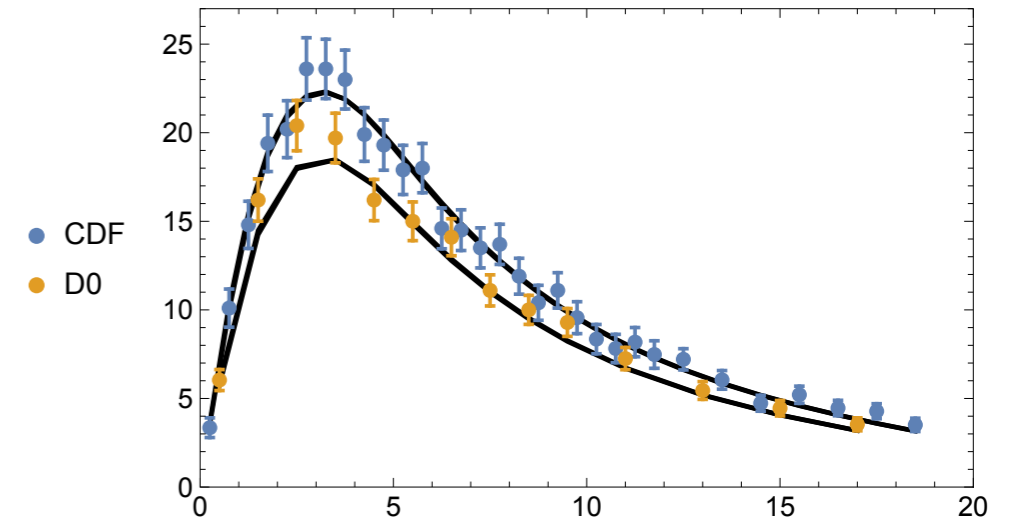
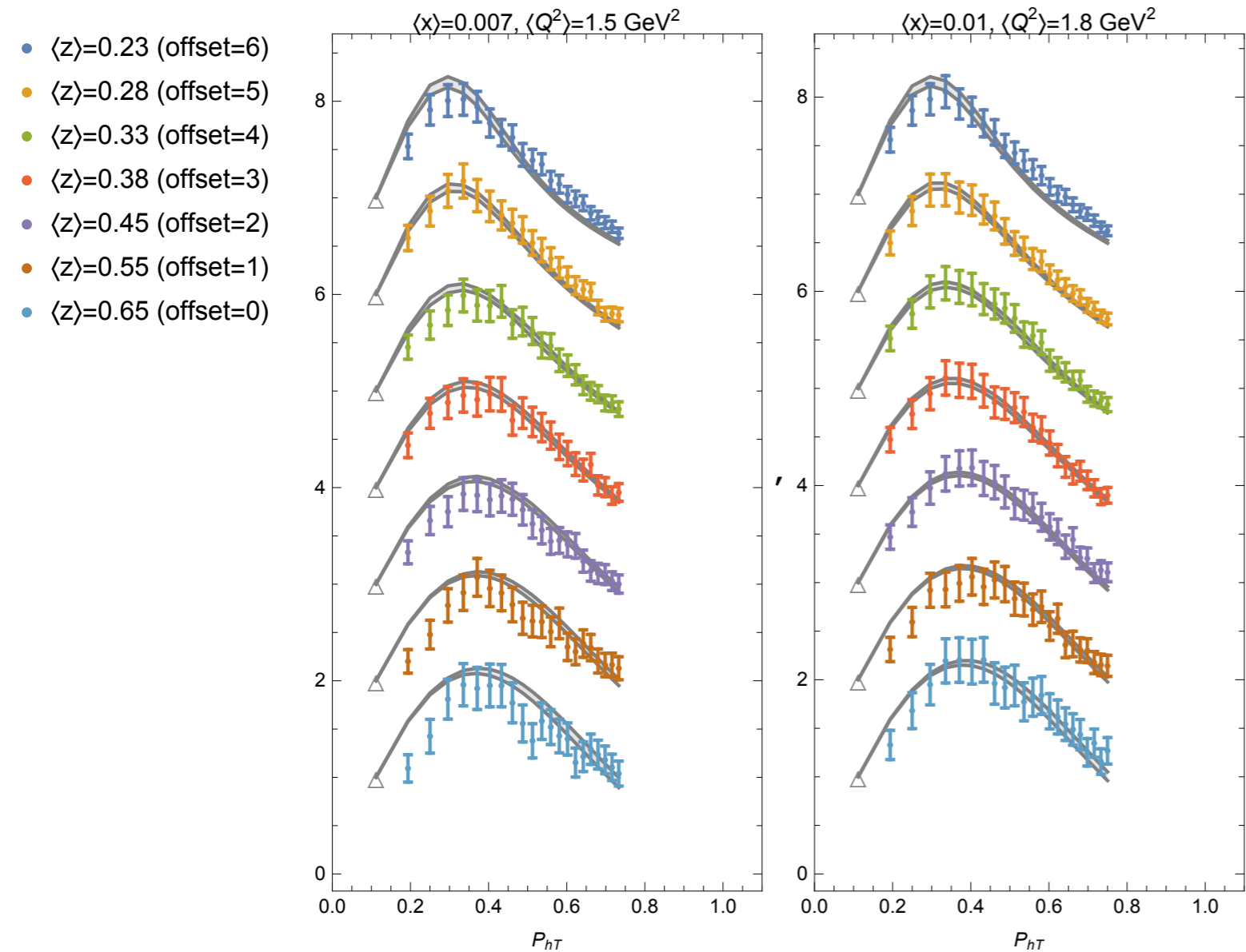
NNLL

$$\chi^2 / \text{dof} = 1.10$$

*see talk by U. D'Alesio*



# Glimpses of Pavia's results

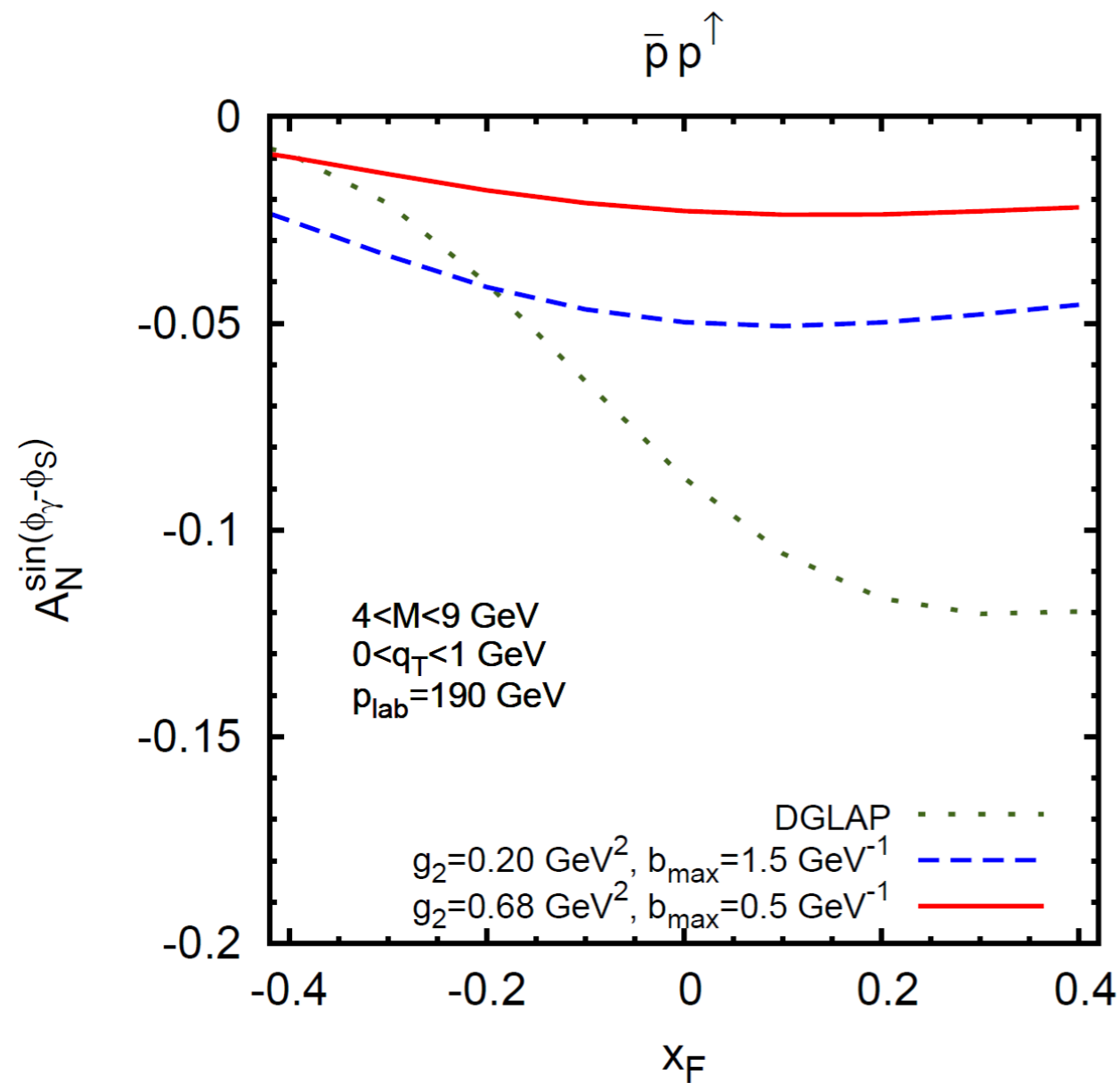


This is the first fit putting together data from SIDIS to Z production

$$\chi^2/\text{dof} = 1.55 \pm 0.05$$

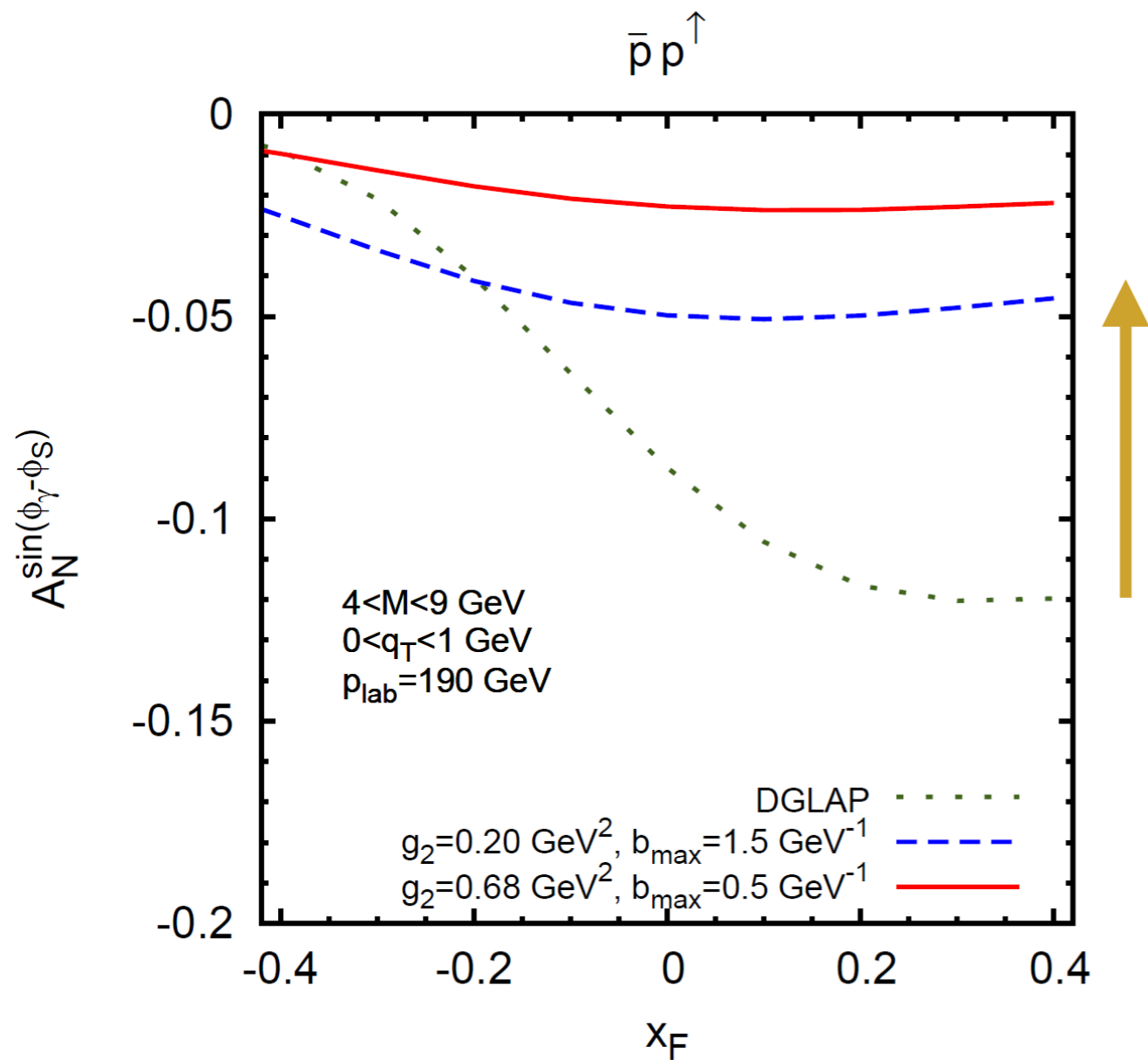
*Bacchetta, Delcarro, Pisano, Radici, Signori, in preparation*

# Evolution and Sivers sign change



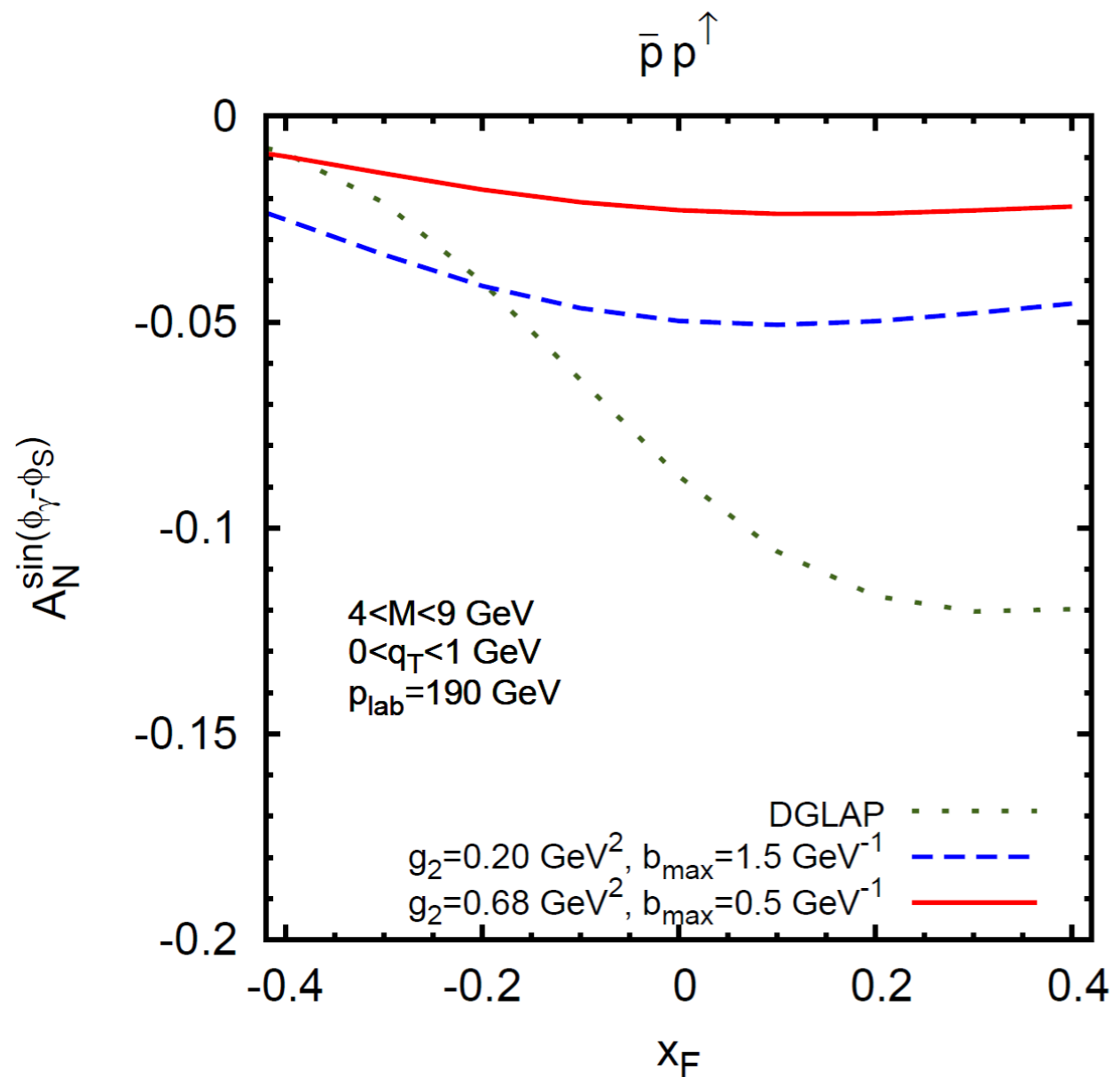
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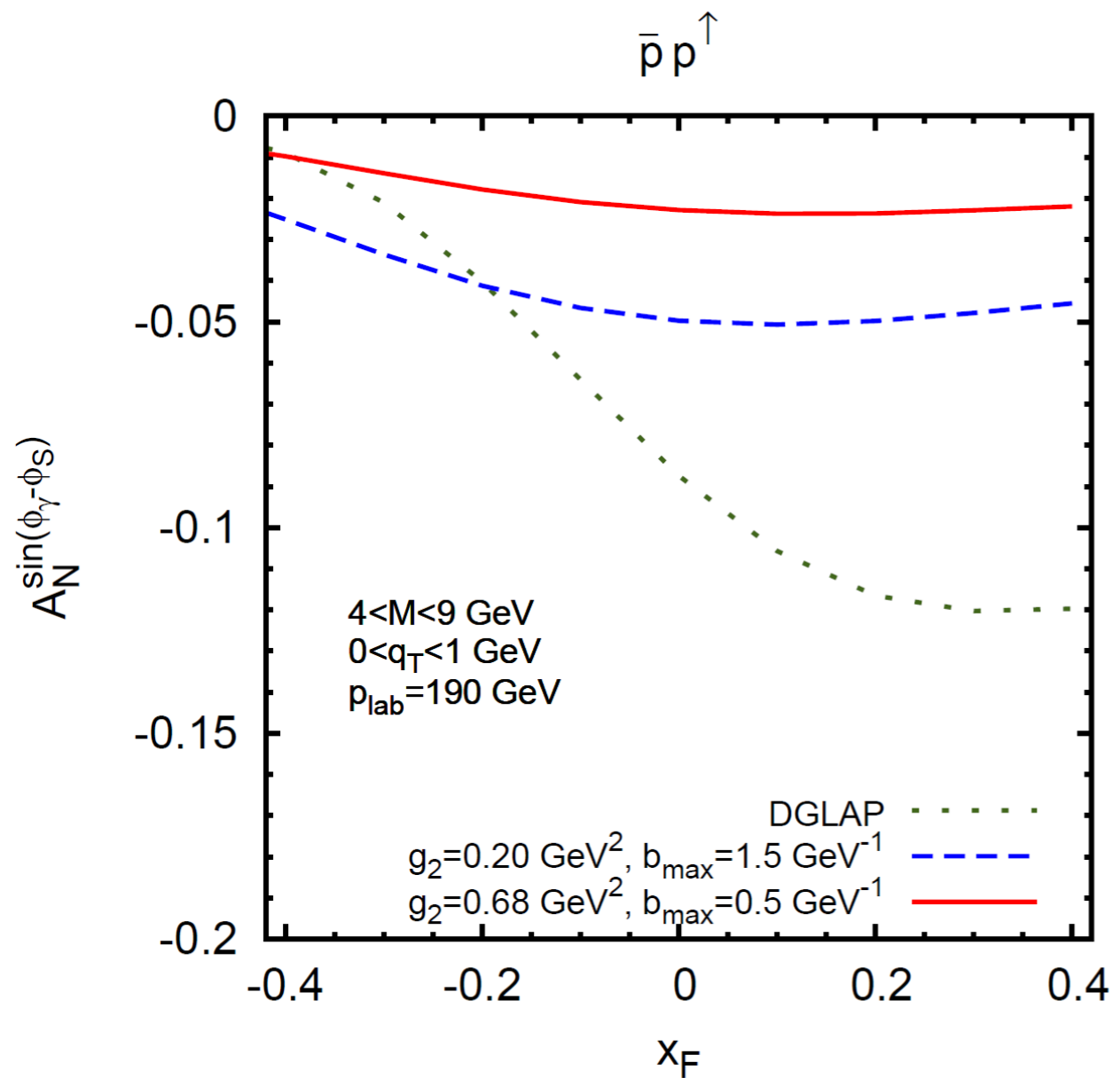
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Different implementations of TMD evolution affect the asymmetry in a different way (Pavia 2016:  $g_2 = 0.12$ )

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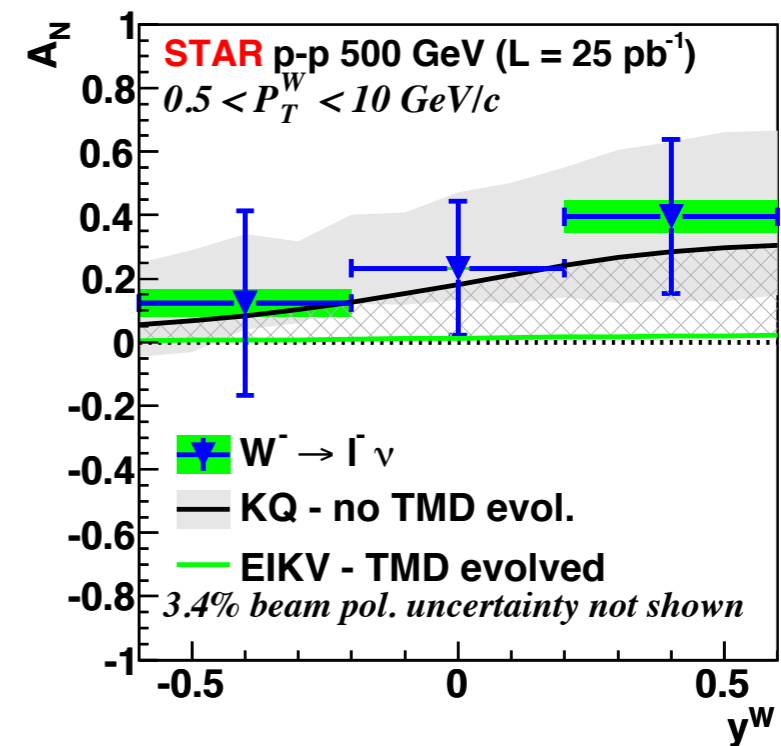
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Different implementations of TMD evolution affect the asymmetry in a different way (Pavia 2016:  $g_2 = 0.12$ )

*STAR Collab. arXiv:1511.06003*  
*EIKV, arXiv:1401.5078*



# The Y term

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*Collins et al., arXiv: 1605.00671  
and T. Rogers's talk at Trento 2016*

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*Collins et al., arXiv: 1605.00671  
and T. Rogers's talk at Trento 2016*

$$F_{UU,T}(x, z, \mathbf{P}_{hT}^2, Q^2) = x \sum_a \mathcal{H}_{UU,T}^a(Q^2; \mu^2) \int \frac{d\mathbf{b}_\perp^2}{4\pi} J_0(|\mathbf{b}_T| |\mathbf{P}_{h\perp}|) \tilde{f}_1^a(x, z^2 \mathbf{b}_\perp^2; \mu^2) \tilde{D}_1^{a \rightarrow h}(z, \mathbf{b}_\perp^2; \mu^2) \\ + Y_{UU,T}(Q^2, \mathbf{P}_{hT}^2) + \mathcal{O}(M^2/Q^2)$$

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## The W term

*Good approximation*

*If*

$$q_T \ll Q$$

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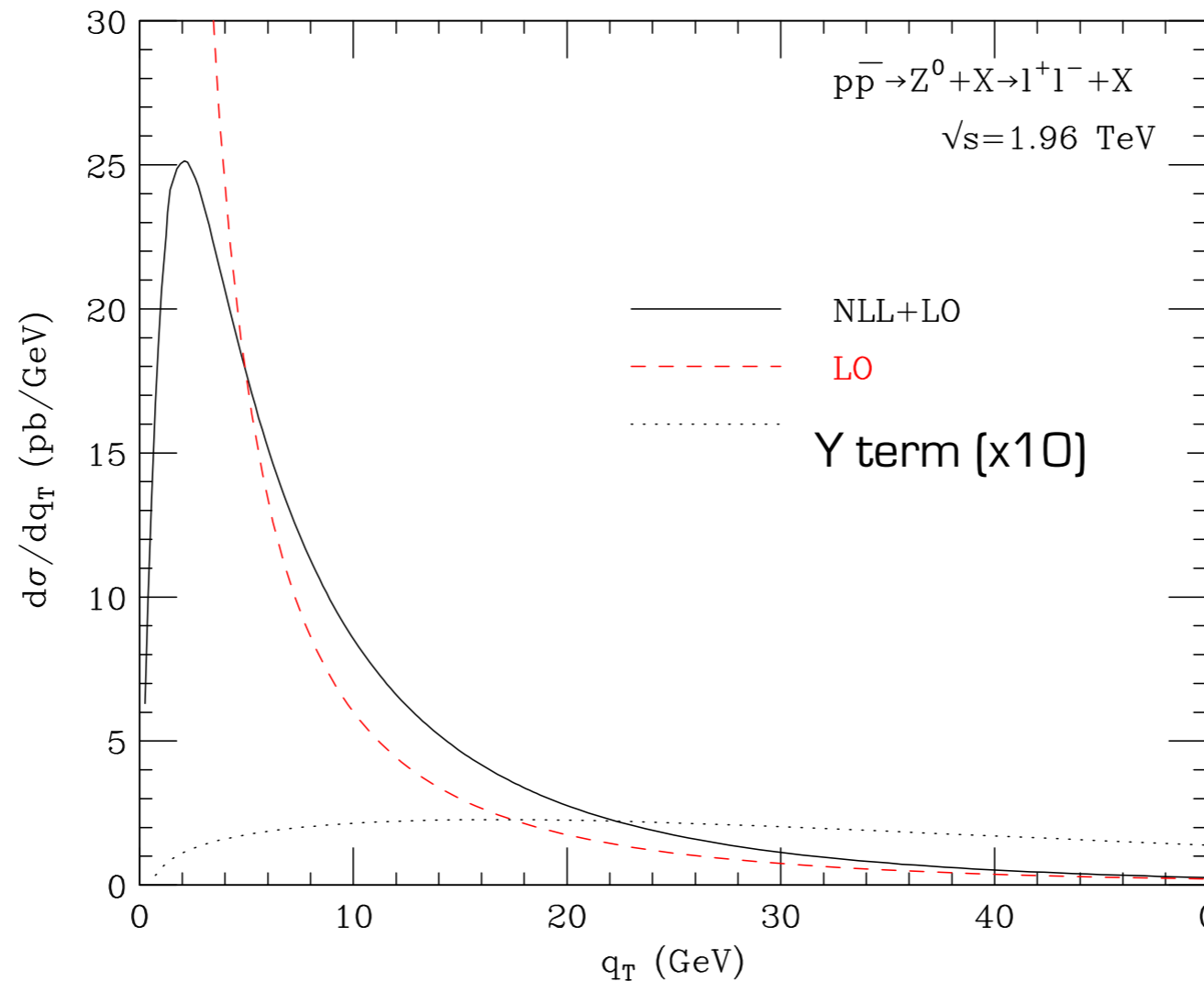
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*see talk by Gamberg*

# Y term in Z boson production

Bozzi et al. [arXiv:0812.2862](https://arxiv.org/abs/0812.2862)

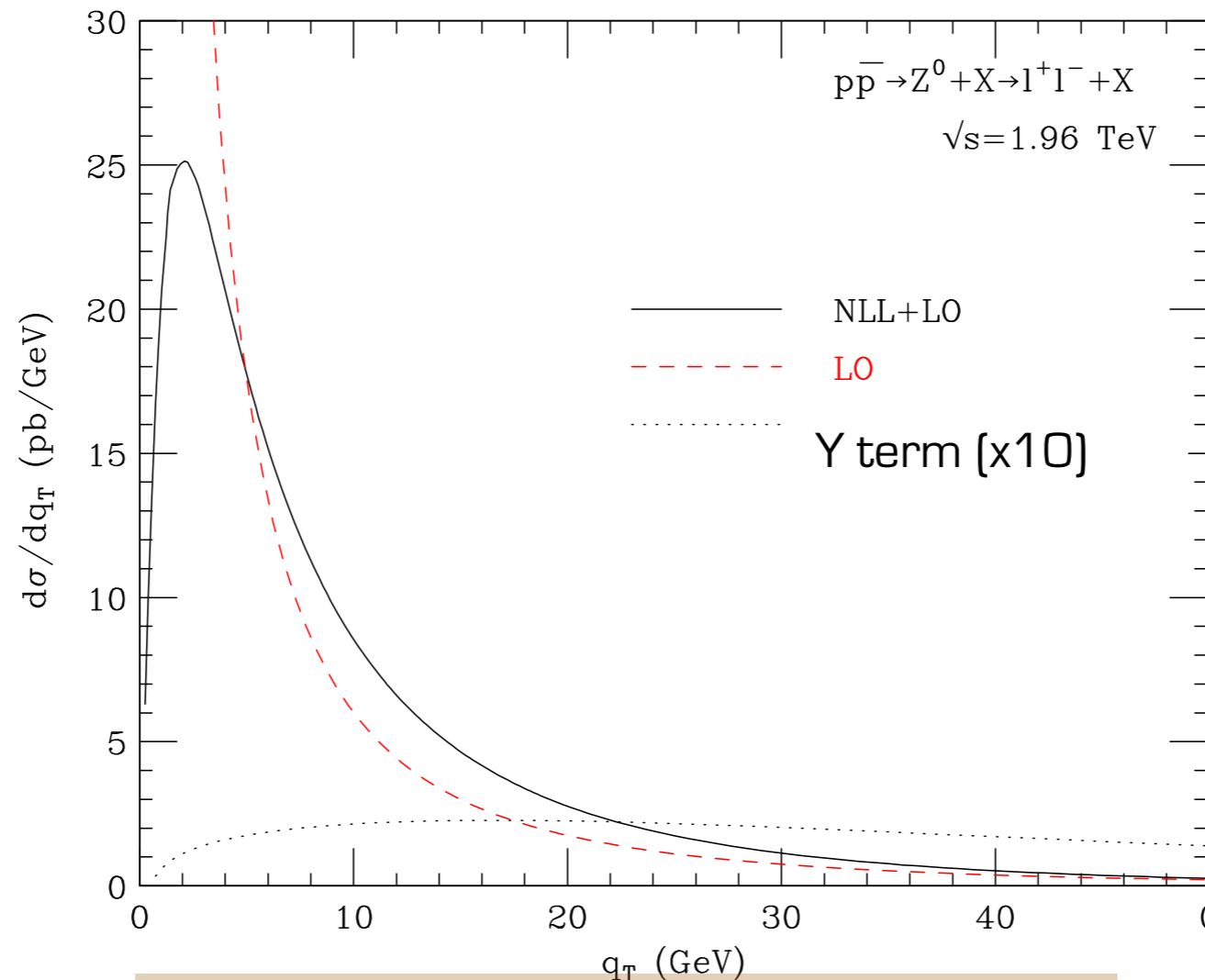


In these conditions, the matching works.

Almost the full range is dominated by resummation

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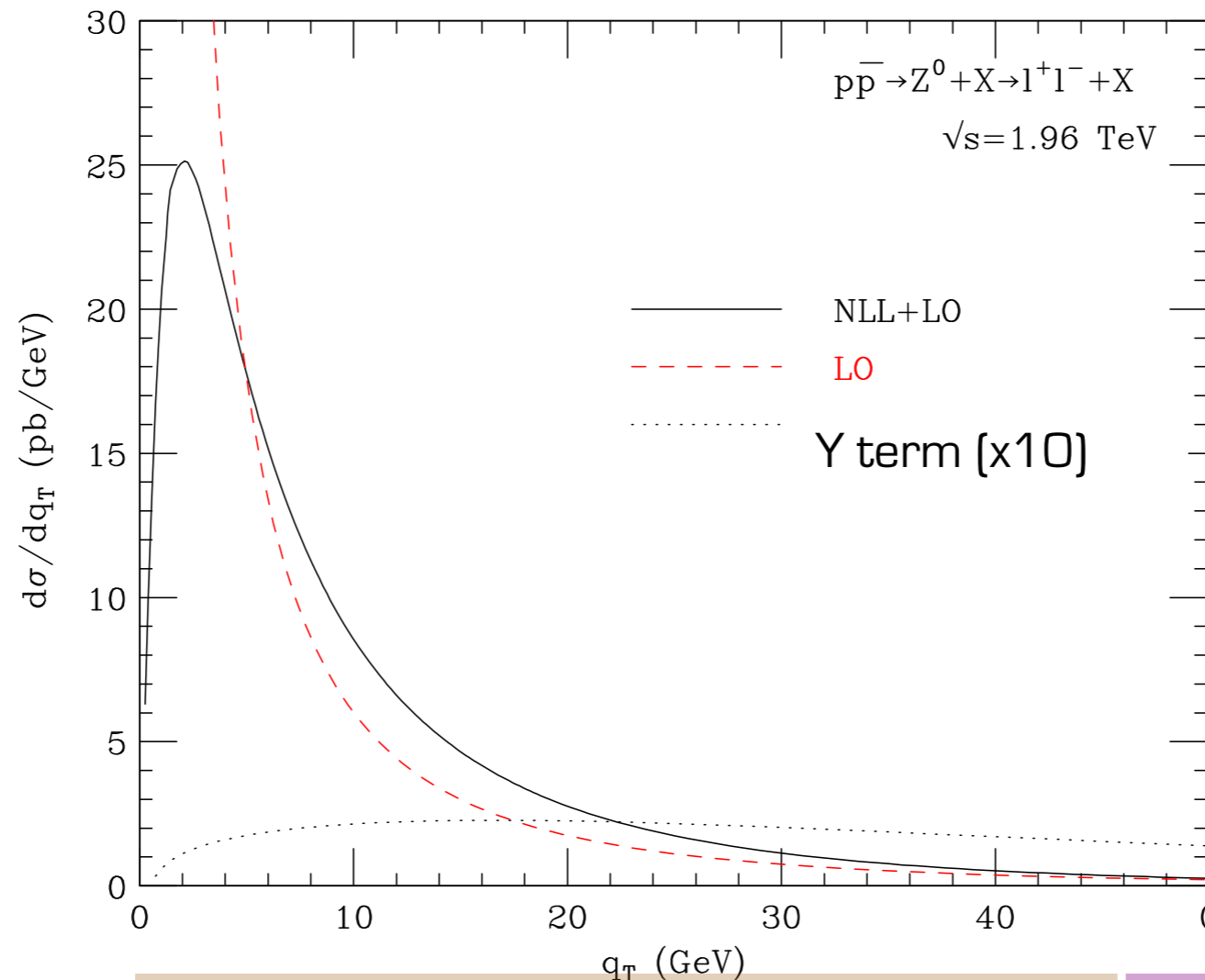
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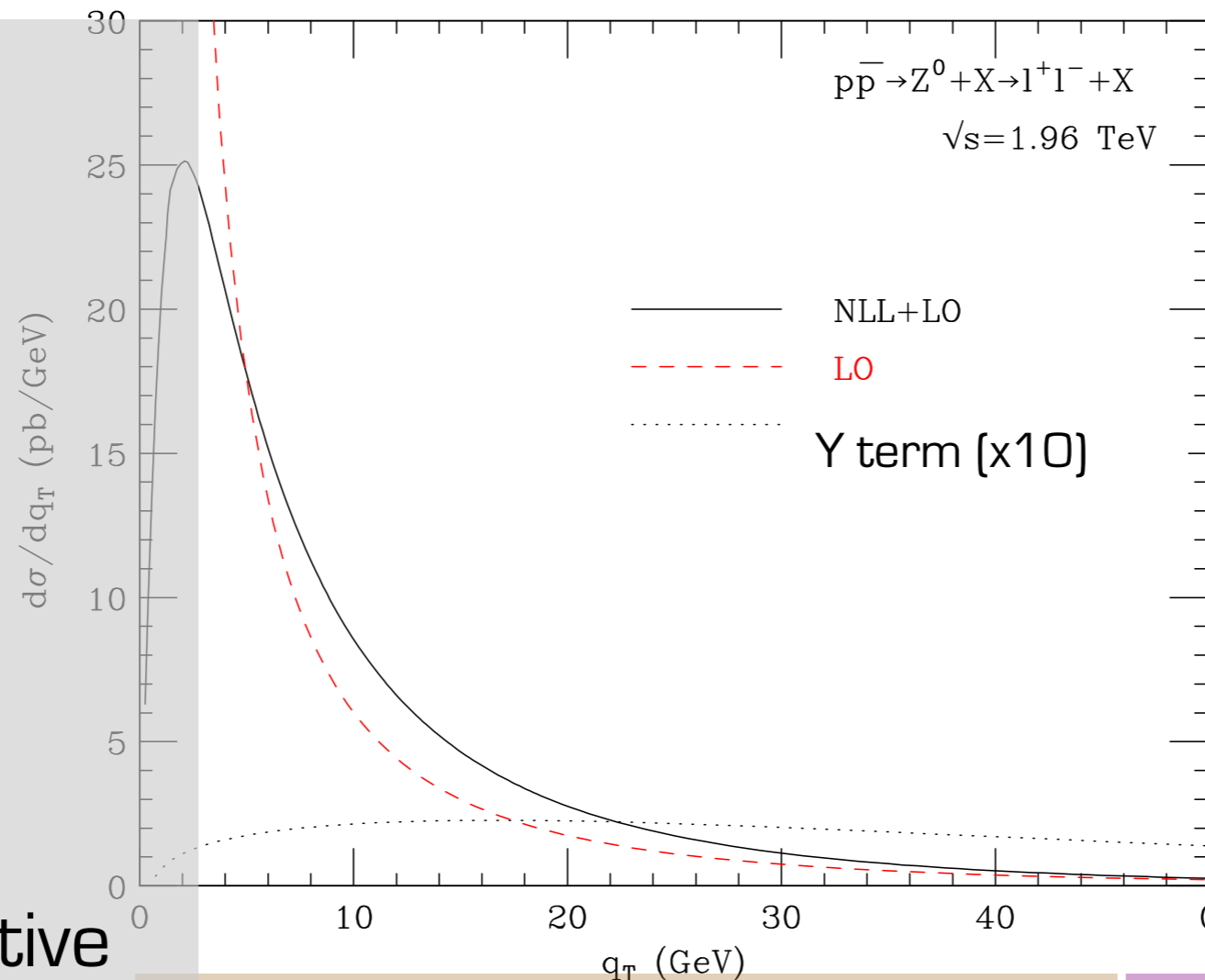
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Nonperturbative  
parts of TMDs

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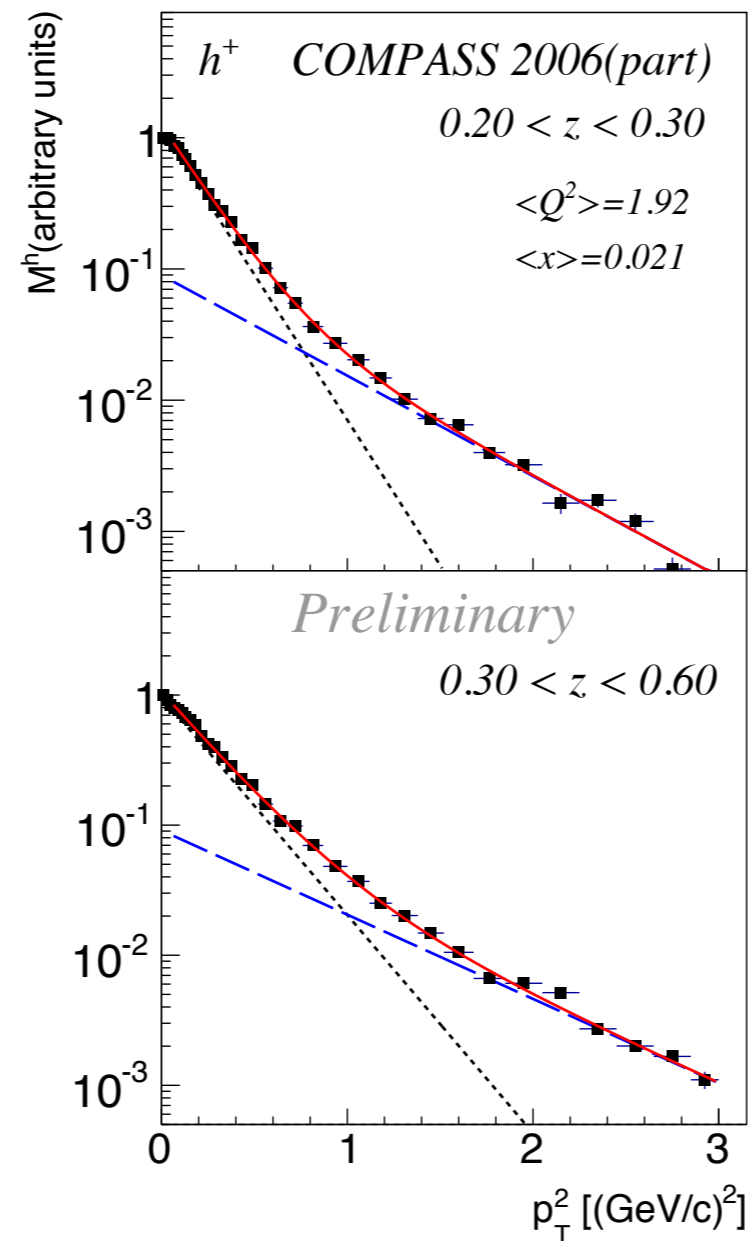
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# New COMPASS data and Y term

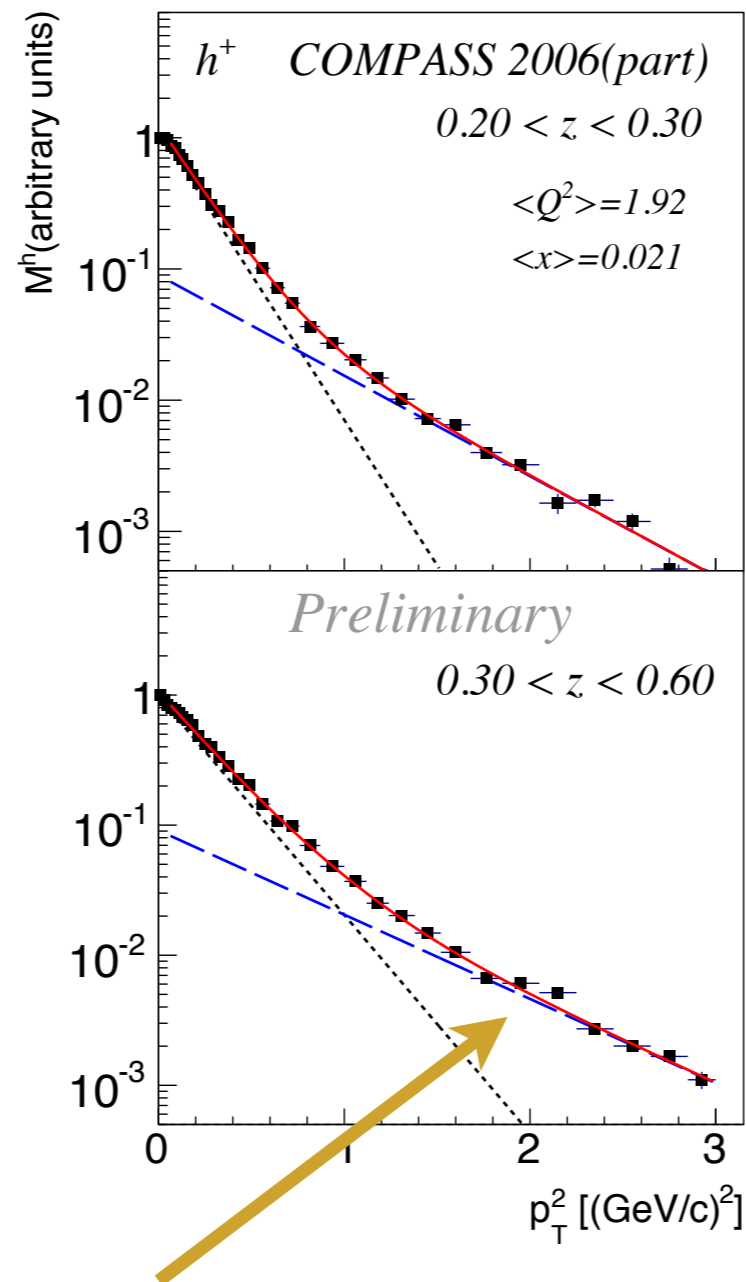
M. Stolarsky, SPIN 2014





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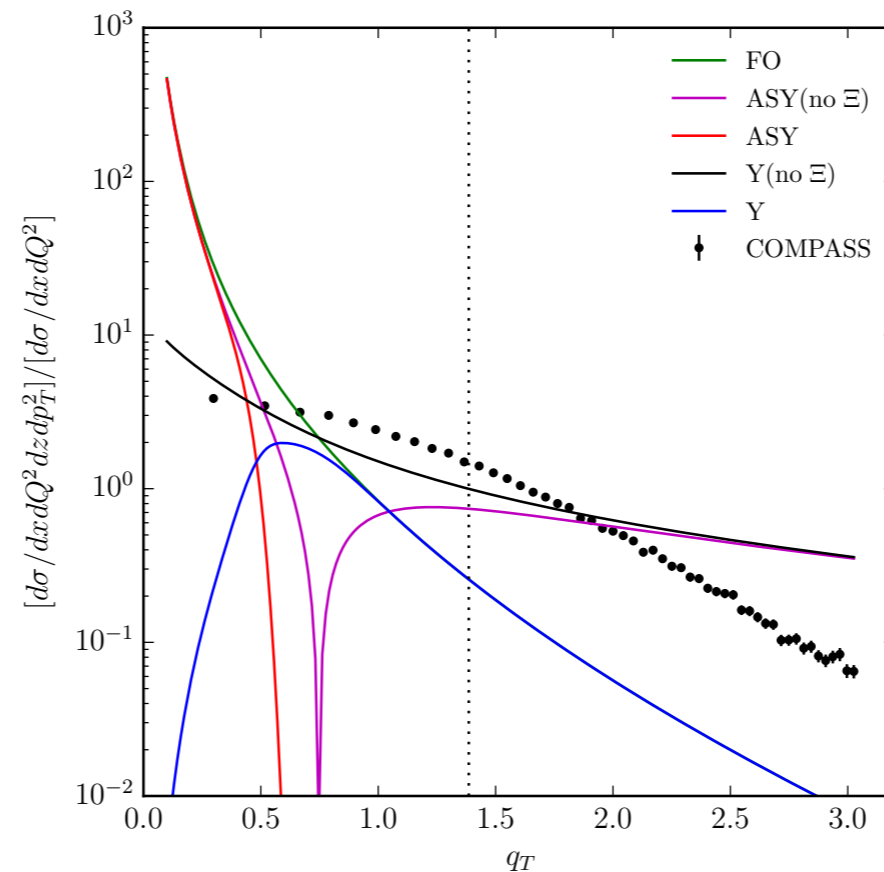
M. Stolarsky, SPIN 2014



Is this the onset of high-transverse-momentum perturbative contributions?

# Matching with fixed-order calculations

*Collins et al., arXiv: 1605.00671*

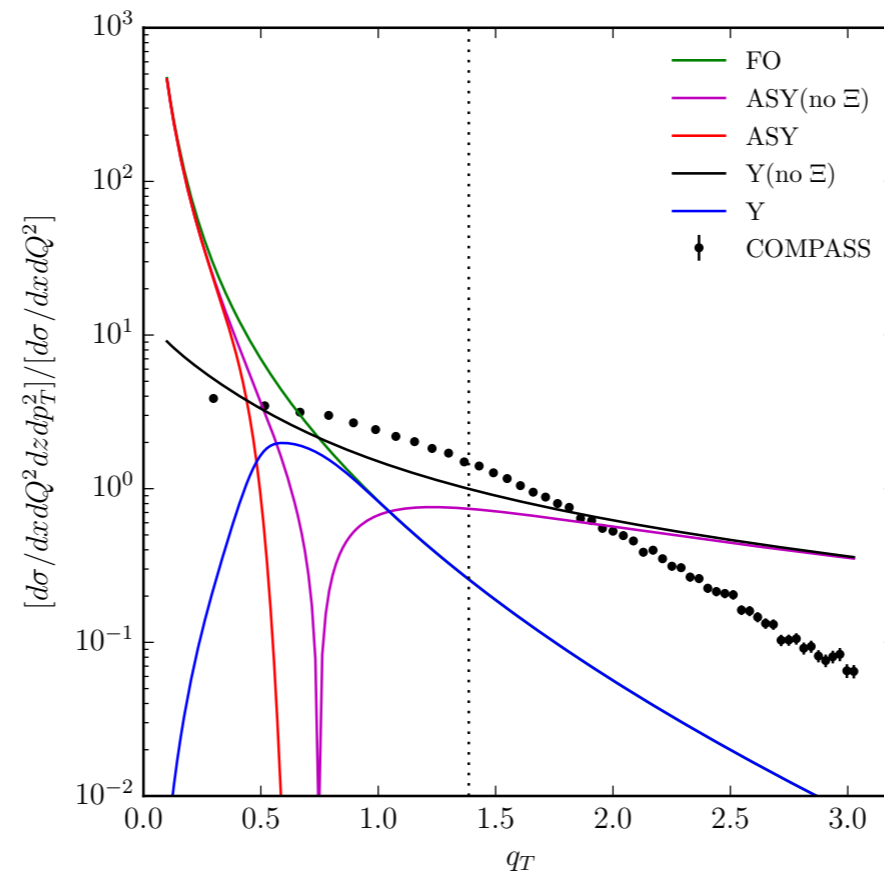


$$Q^2 = 1.92 \text{ GeV}^2, x = 0.0318, z = 0.375$$

The collinear calculation (green line) is much smaller than data  
Standard Y term is bigger than data (black line) → modifications  
needed (blue line)

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*Collins et al., arXiv: 1605.00671*

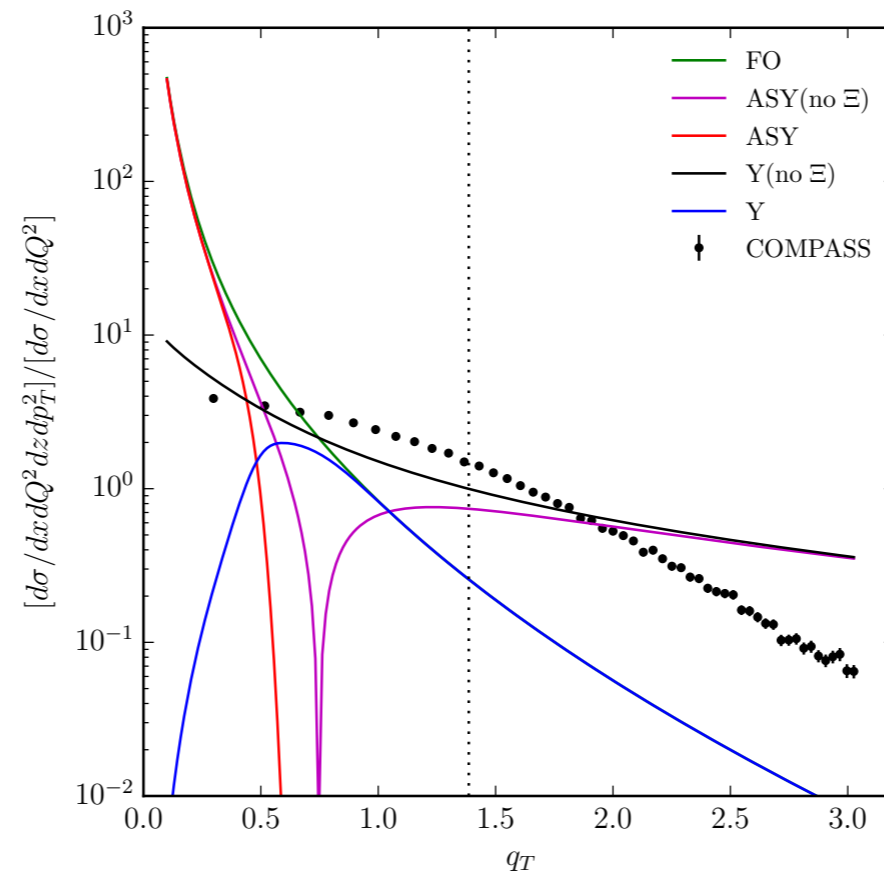


$Q^2 = 1.02 \text{ GeV}^2, x = 0.0318, z = 0.375$   
TMD formalism ?

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*Collins et al., arXiv: 1605.00671*

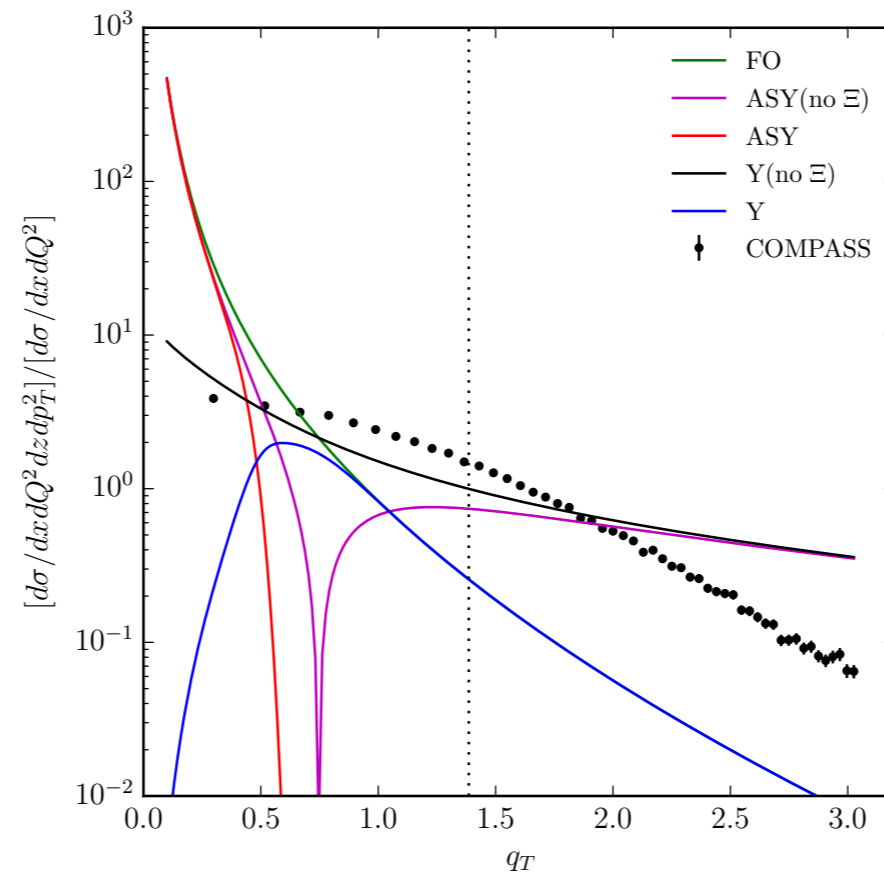


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*see talk by Gamberg*

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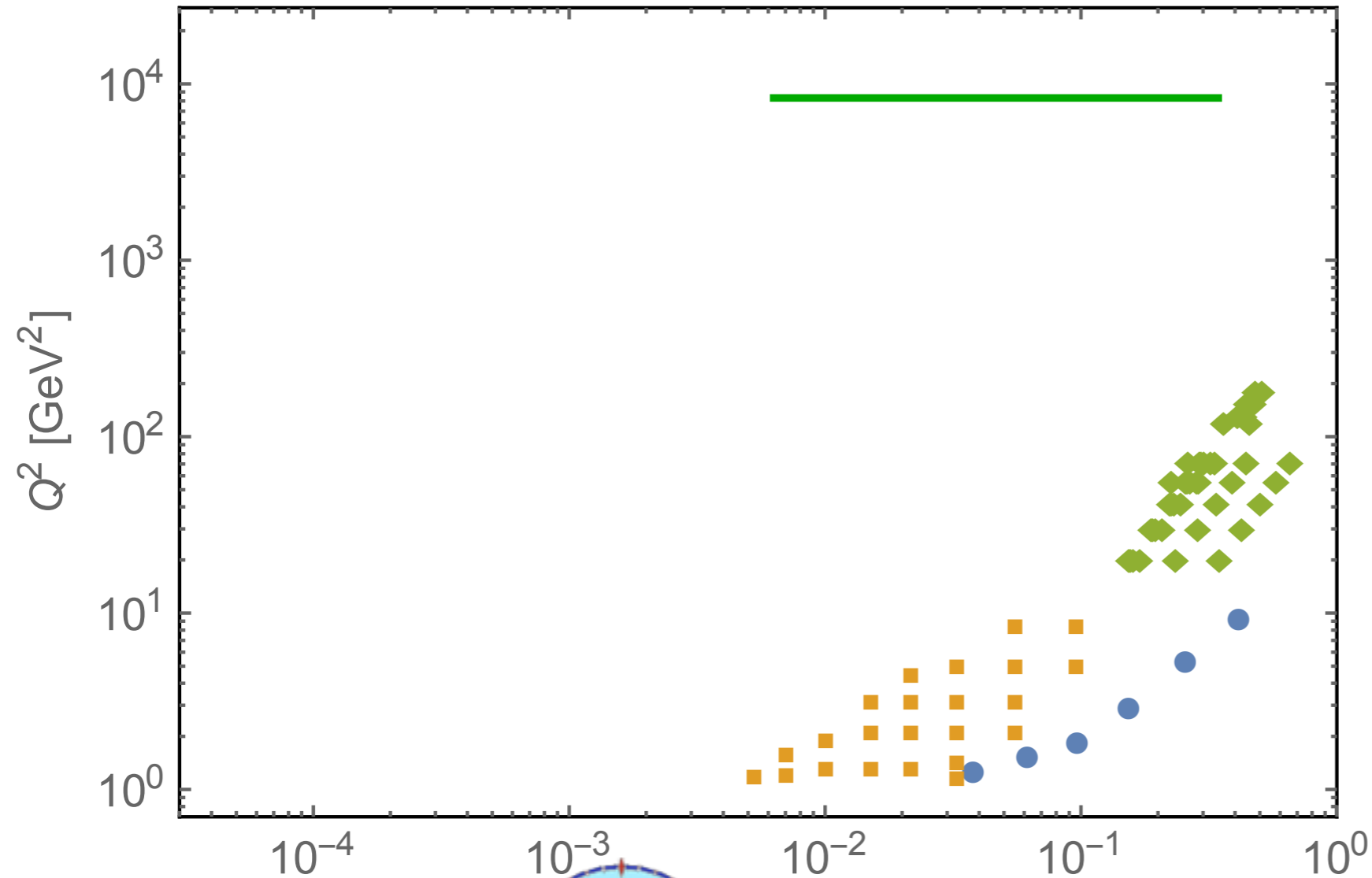
---

- Fit start working well with data from very different experiments
- There is still strong dependence on the assumptions made in the fits and on the implementation of TMD evolution
- The theory is still not completely under control in the low energy region

# Extensions of data sets

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# Available data

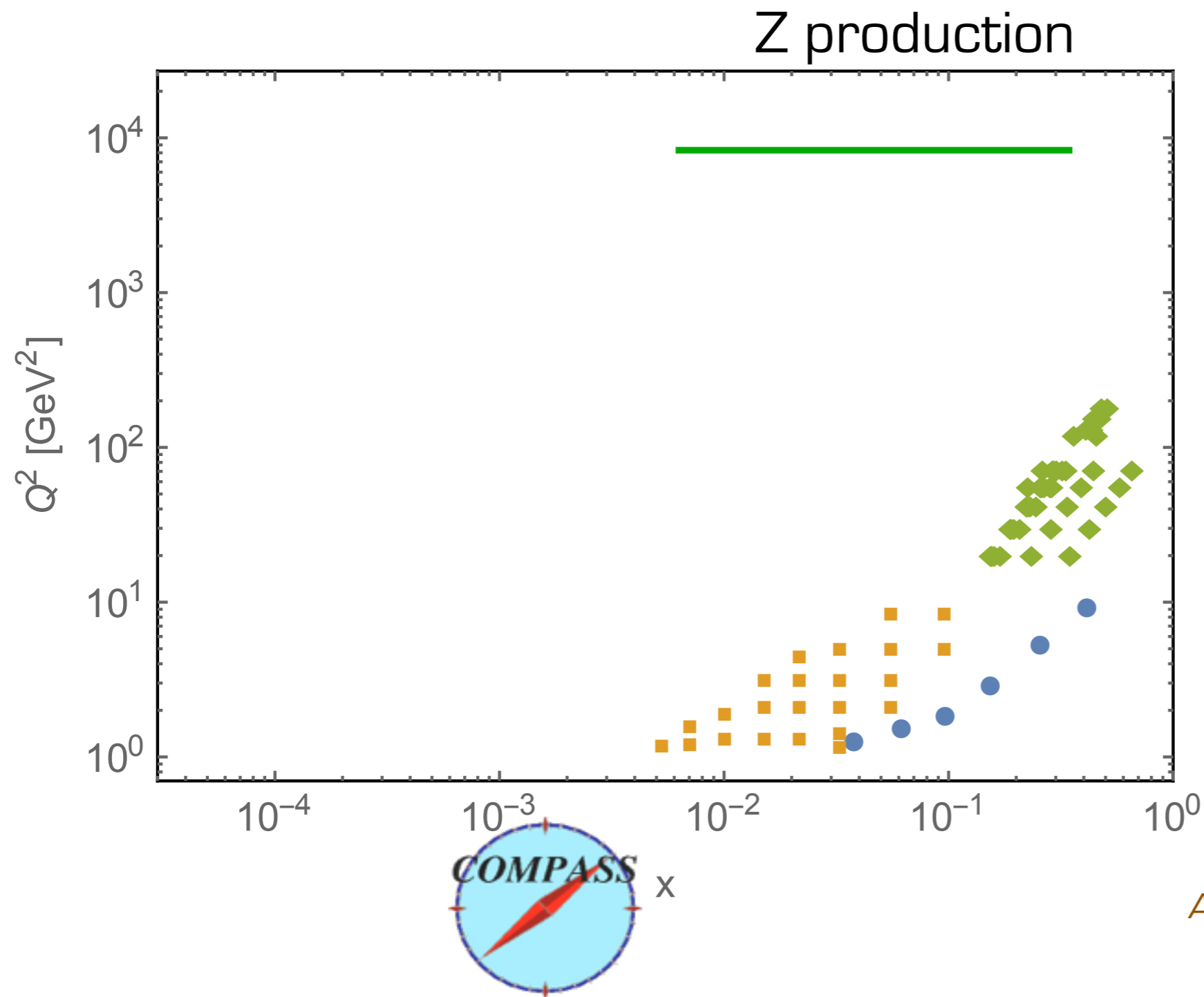


*Adolph et al., EPJ C73 (13)*



*Airapetian et al., PRD87 (2013)*

# Available data



*Adolph et al., EPJ C73 (13)*

*Abbot et al. hep-ex/9909020*  
*Affolder et al. hep-ex/0001021*  
*Abazov et al. arXiv:0712.0803*  
*Aaltonen et al. arXiv:1207.7138*

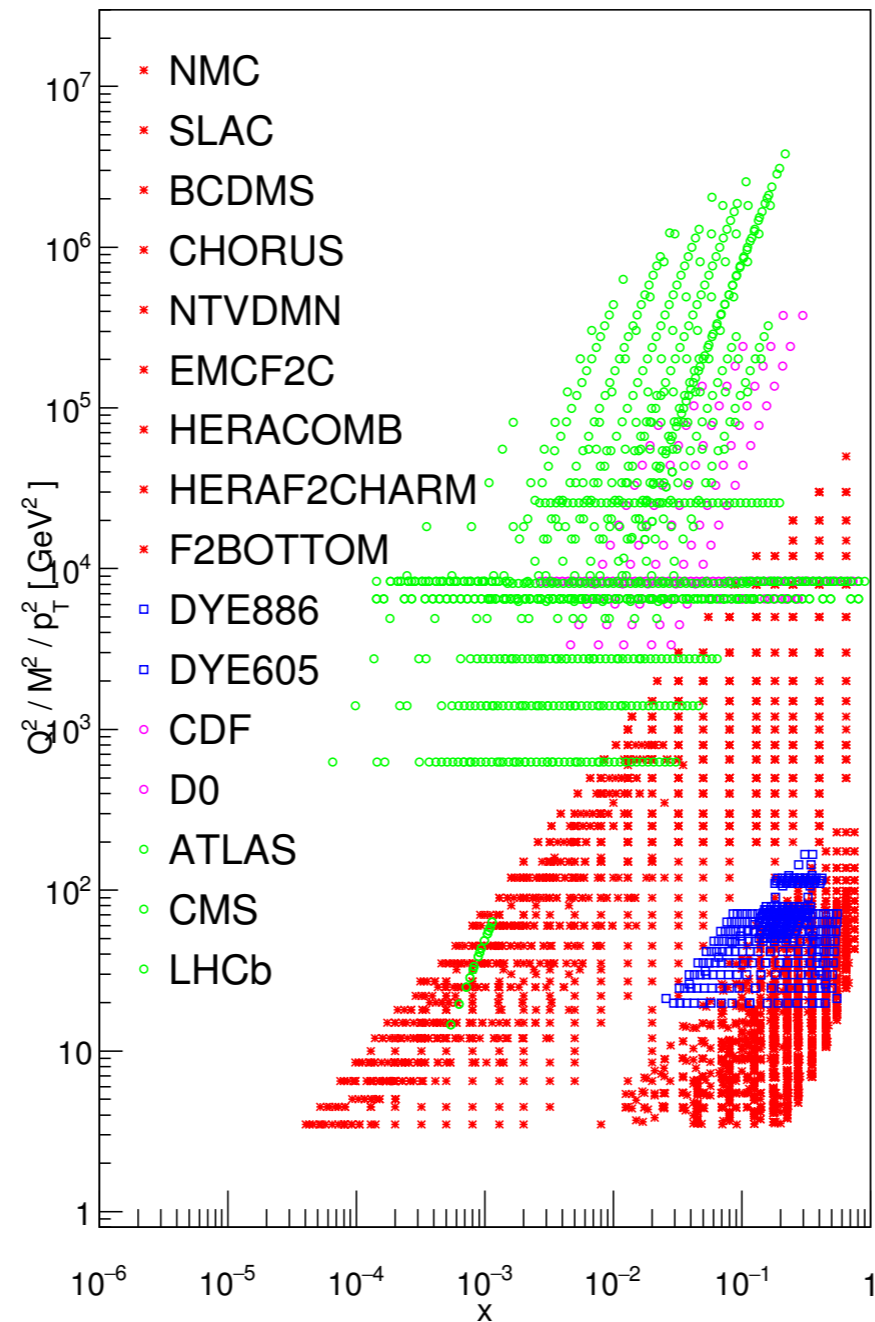
Drell-Yan@  
 Fermilab

*Ito et al., PRD93 (81)*  
*Moreno et al. PRD 43 (91)*  
*Antreyan et al. PRL47 (81)*



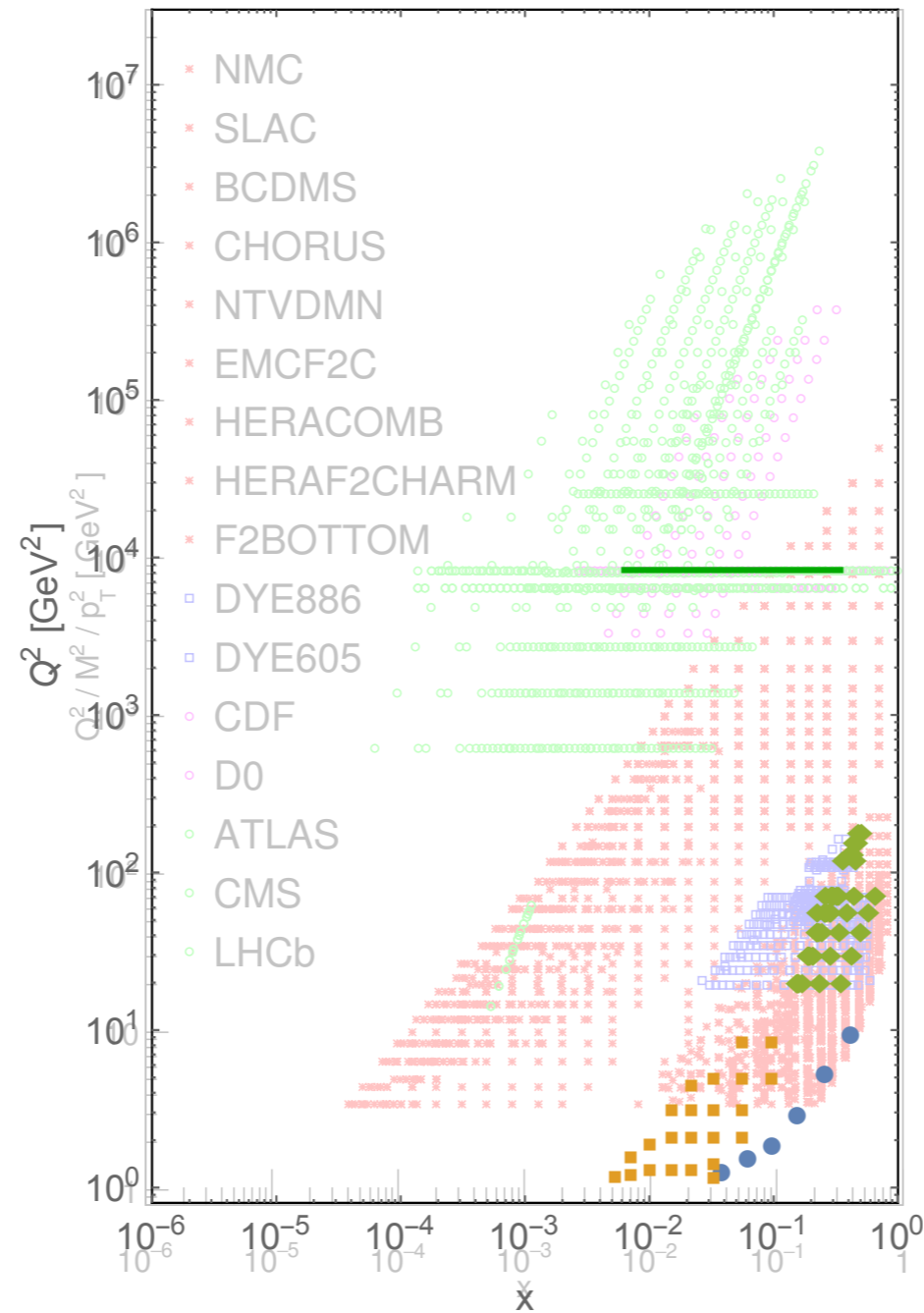
*Airapetian et al., PRD87 (2013)*

# Comparison with collinear PDFs



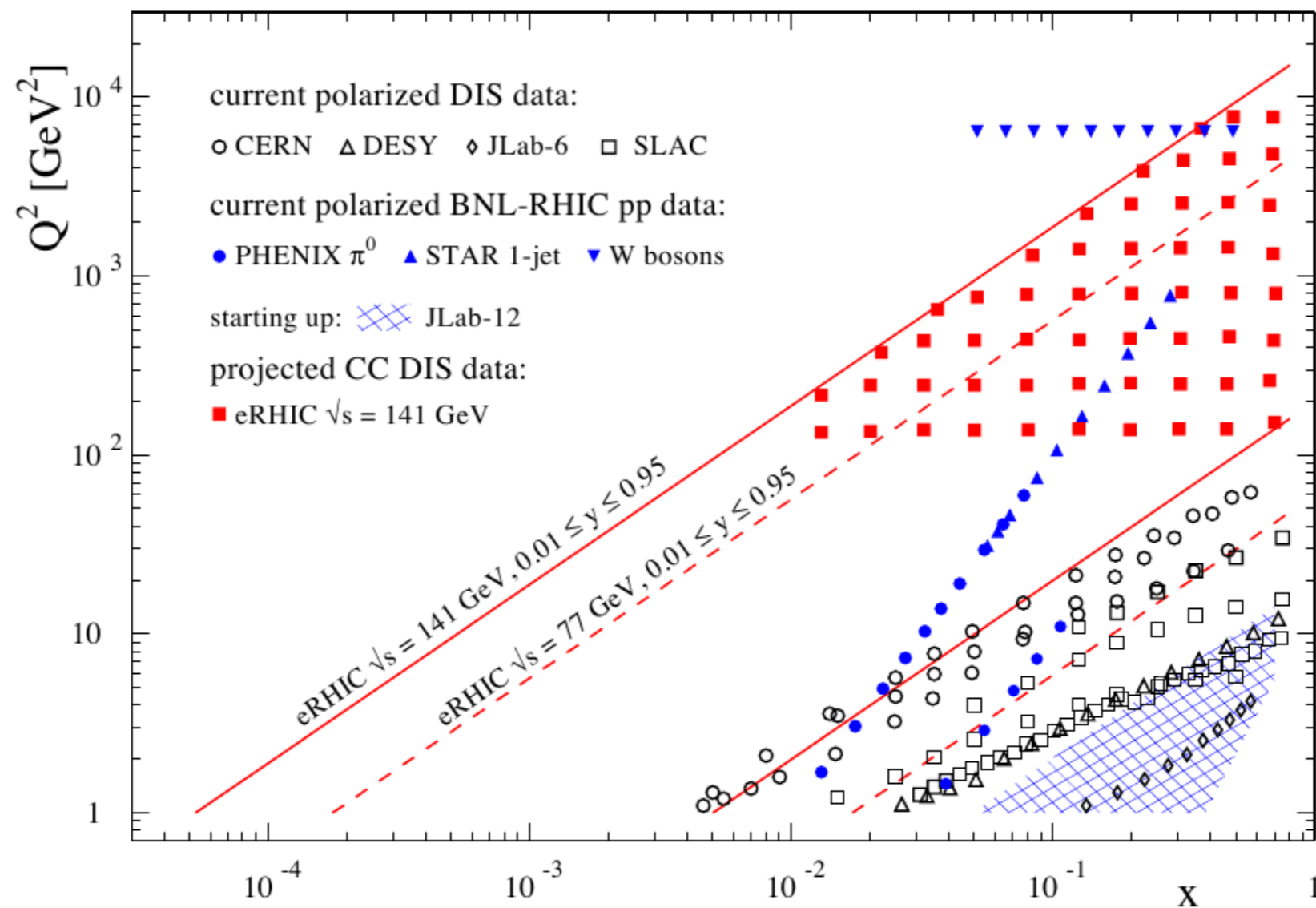
*talk by E. Nocera at POETIC2016*

# Comparison with collinear PDFs



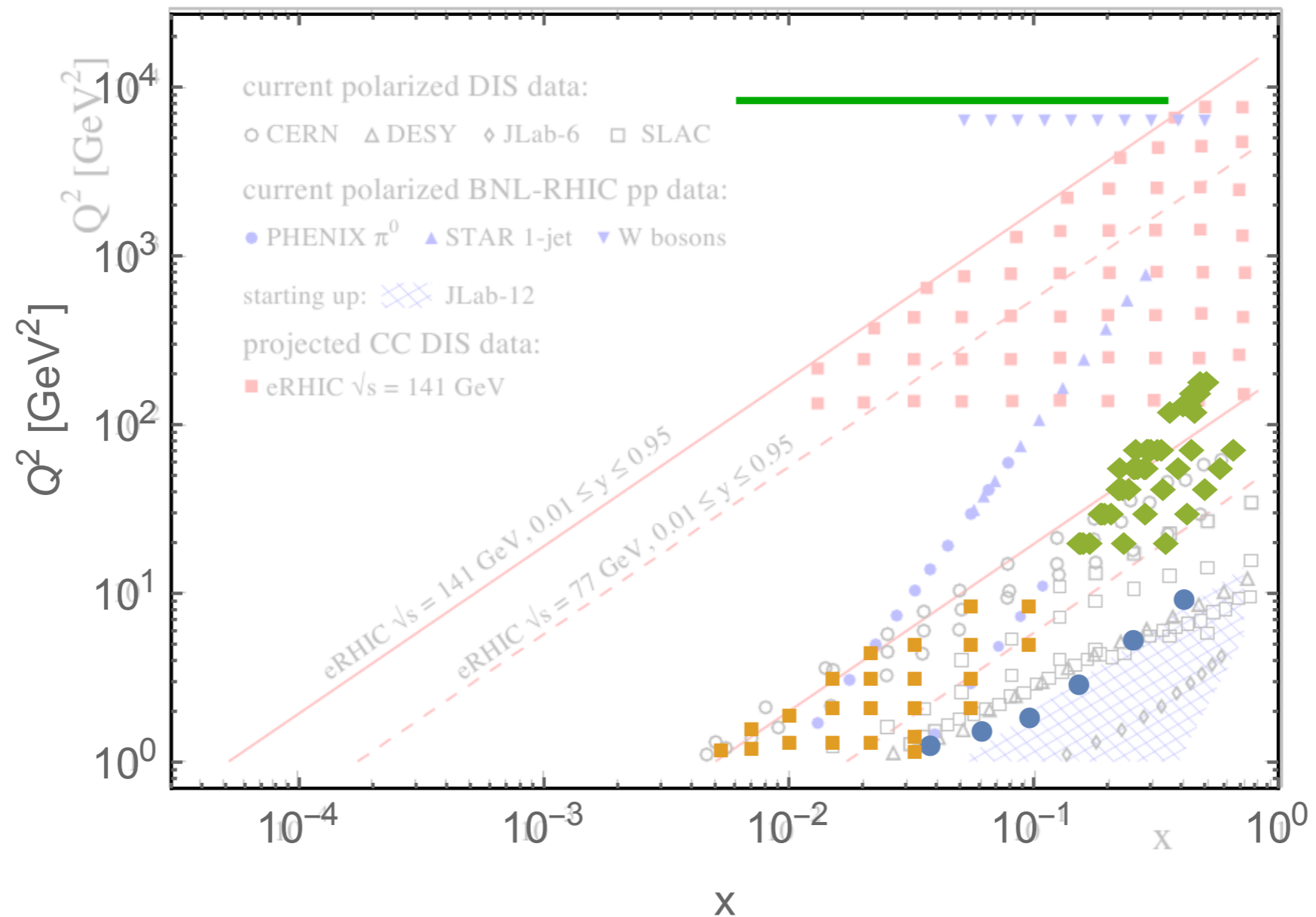
*talk by E. Nocera at POETIC2016*

# Comparison with future perspectives



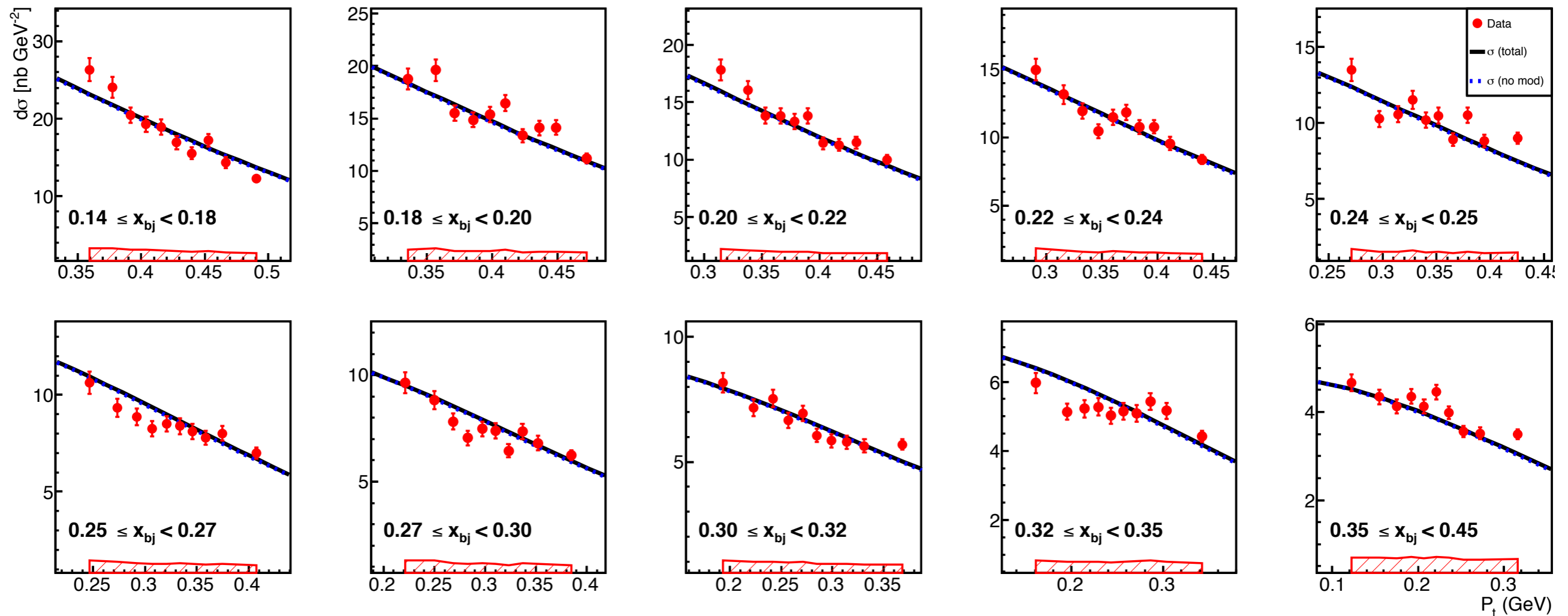
from EIC white paper EPJA 52 (2016), see talks by A. Deshpande, M. Contalbrigo

# Comparison with future perspectives

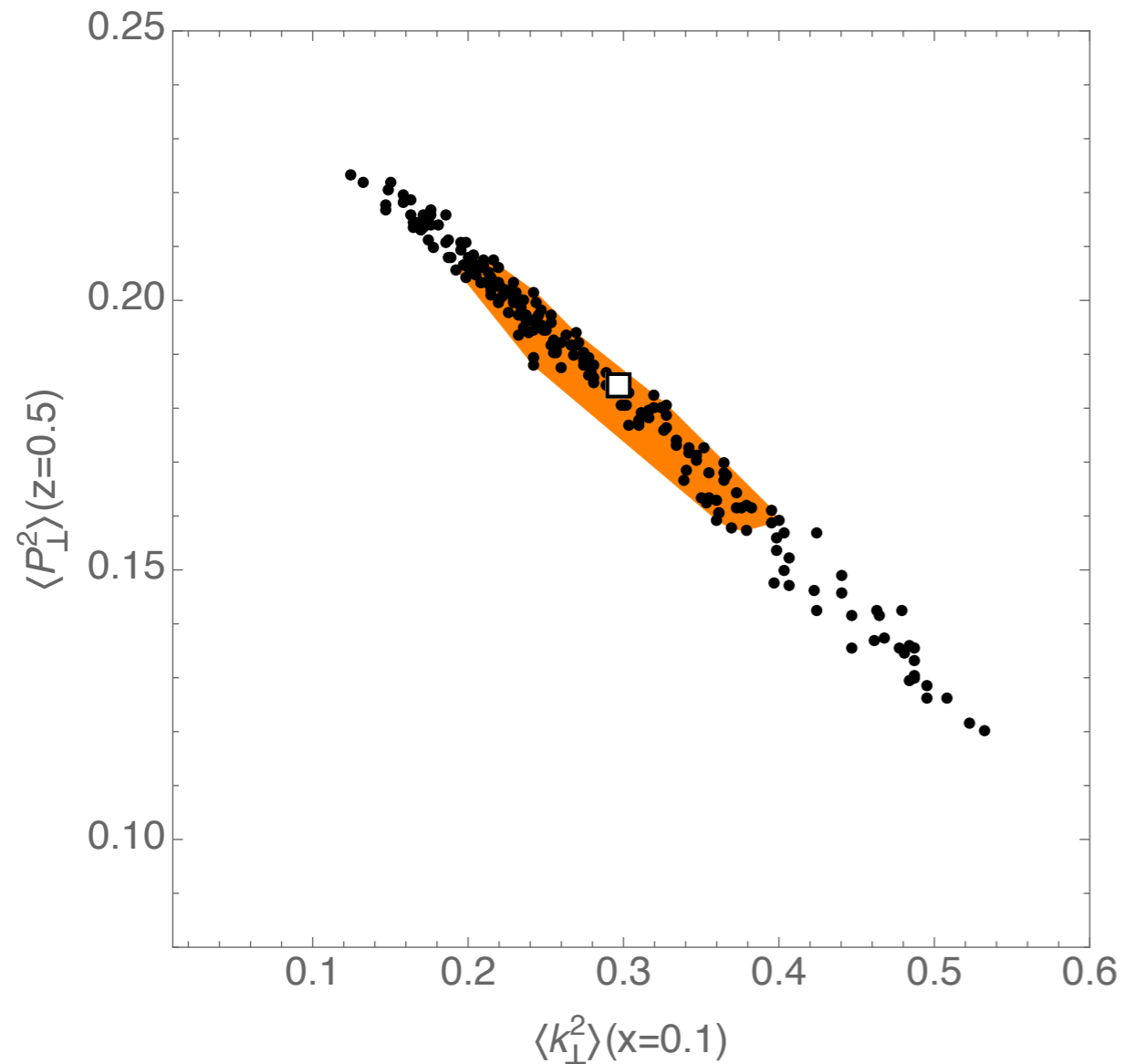




# Recent $^3\text{He}$ data from JLab Hall A

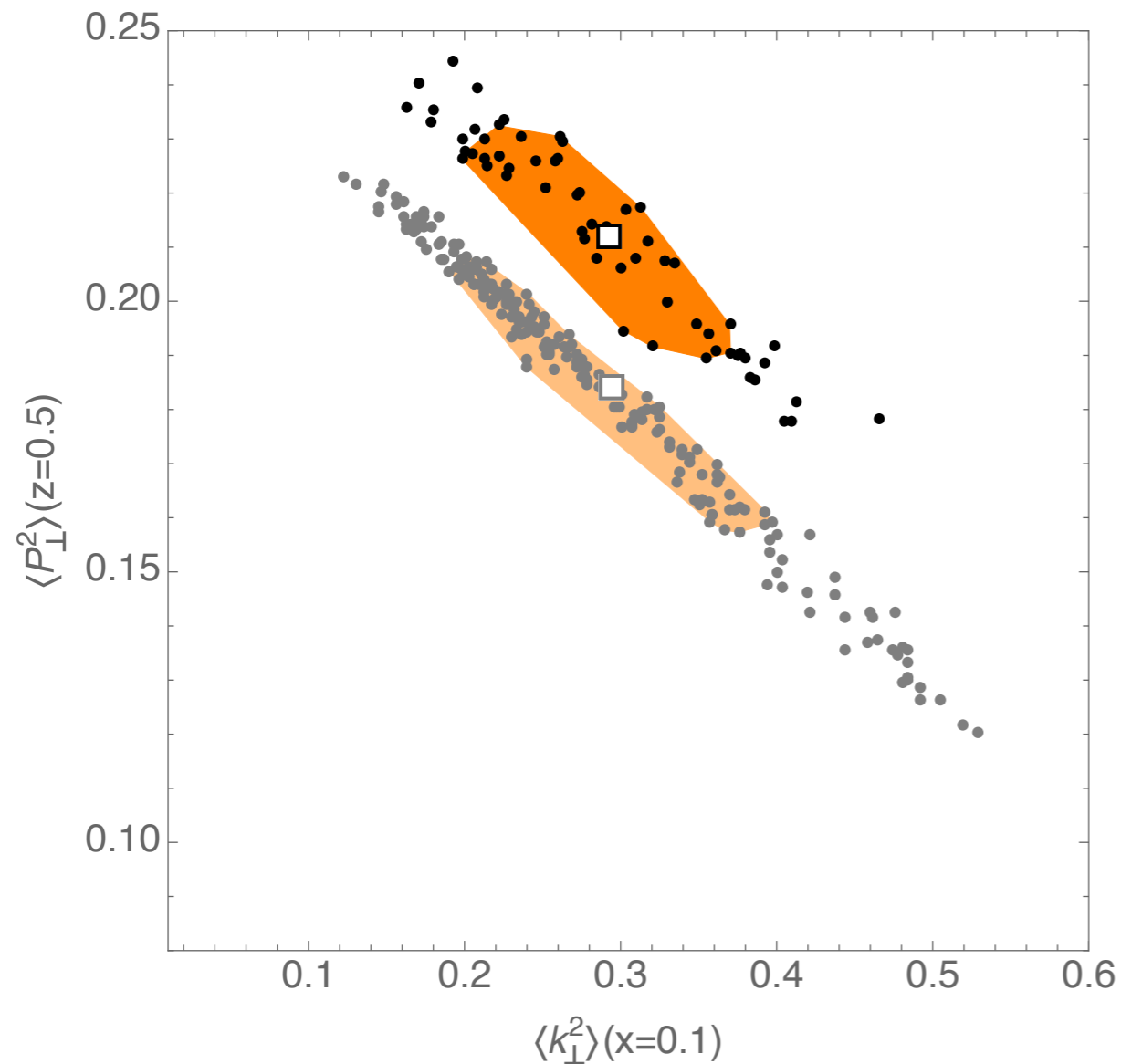


# Distribution-fragmentation $k_T$



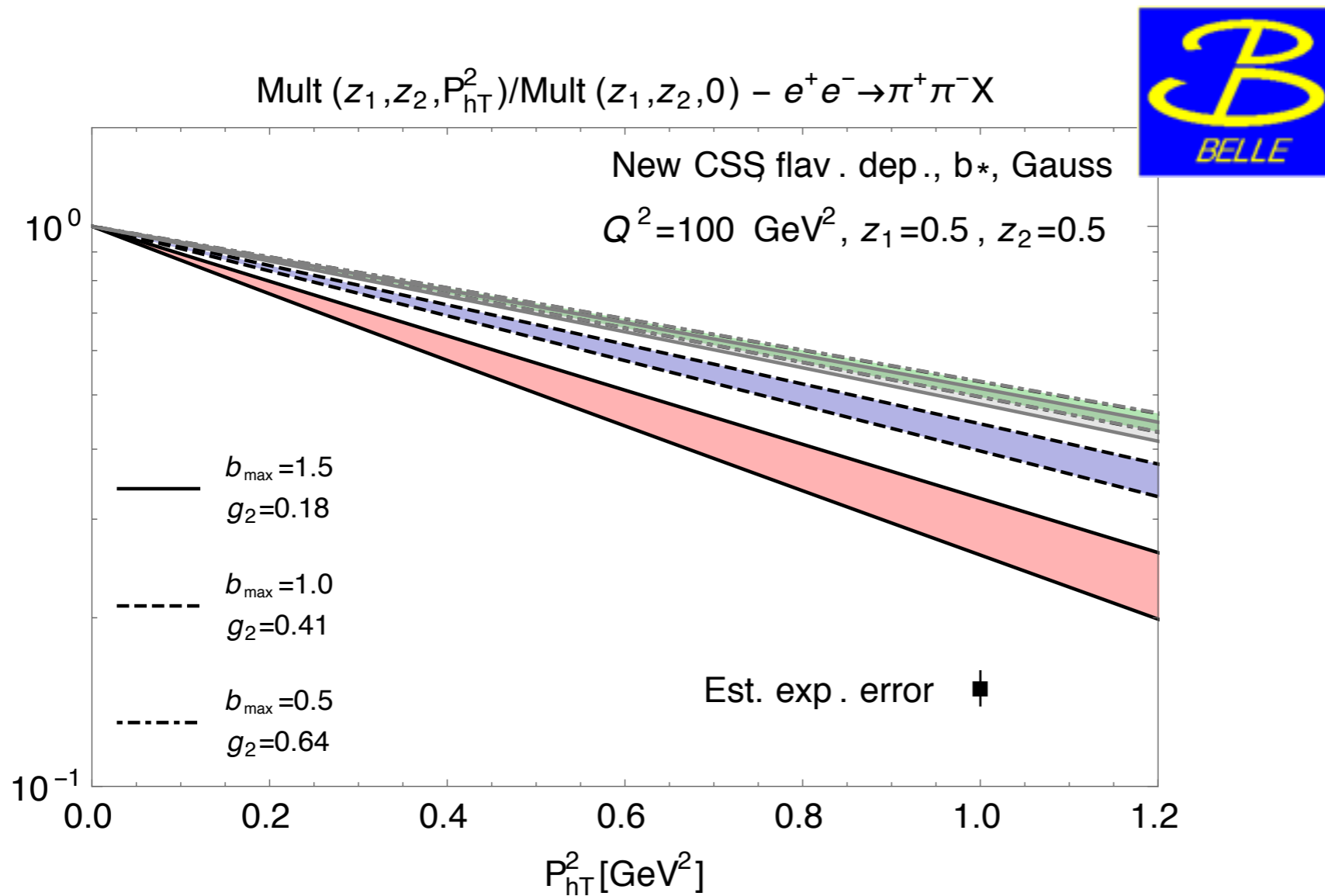
Pavia 2013 fit based only on SIDIS data showed a strong anticorrelation that could not be resolved without further data

# Distribution-fragmentation $k_T$

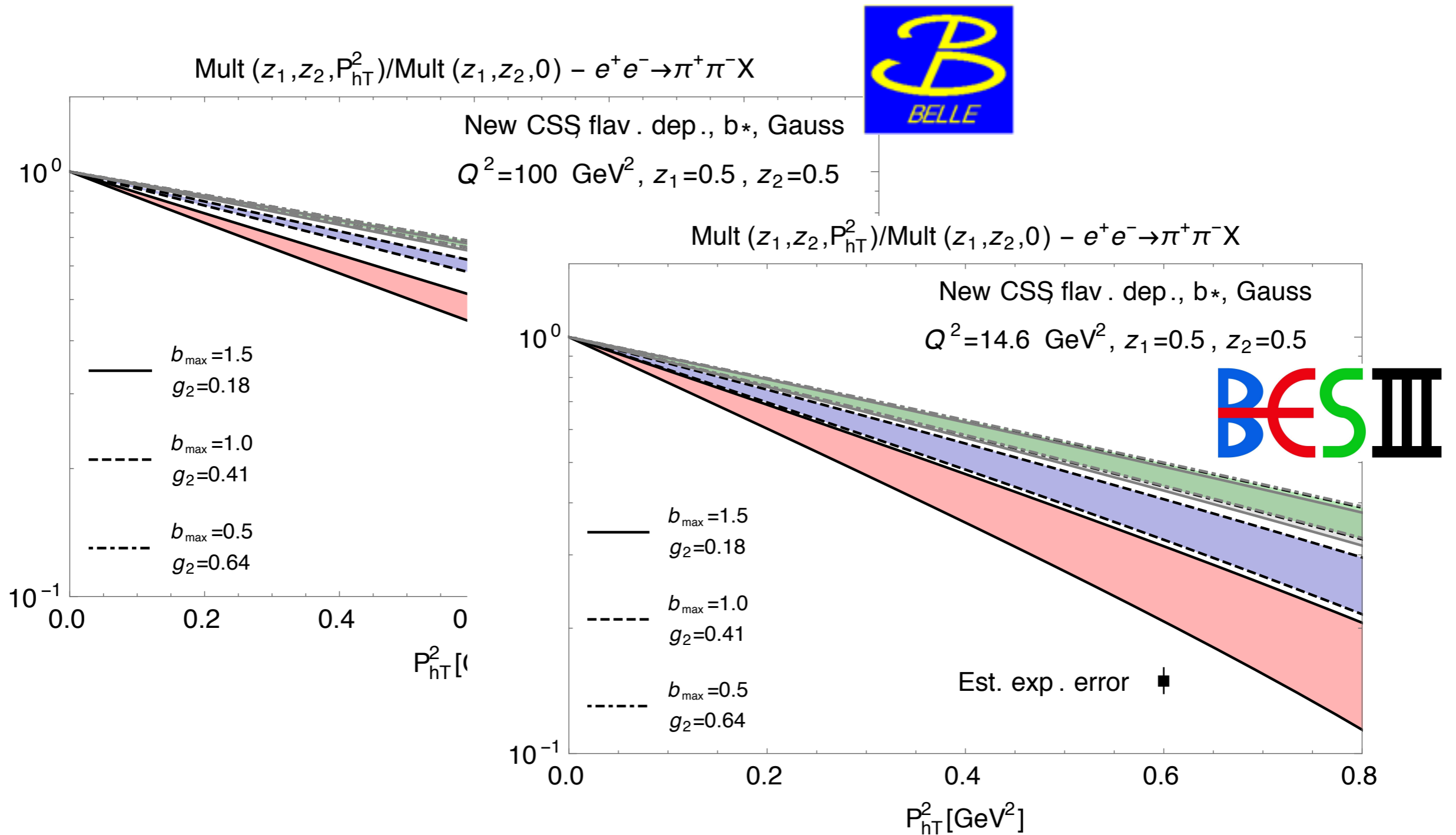


Pavia 2016 fit uses also DY data. The anticorrelation is weaker than before but still strong. Independent information about fragmentation  $k_T$  is necessary.

# TMD fragmentation functions

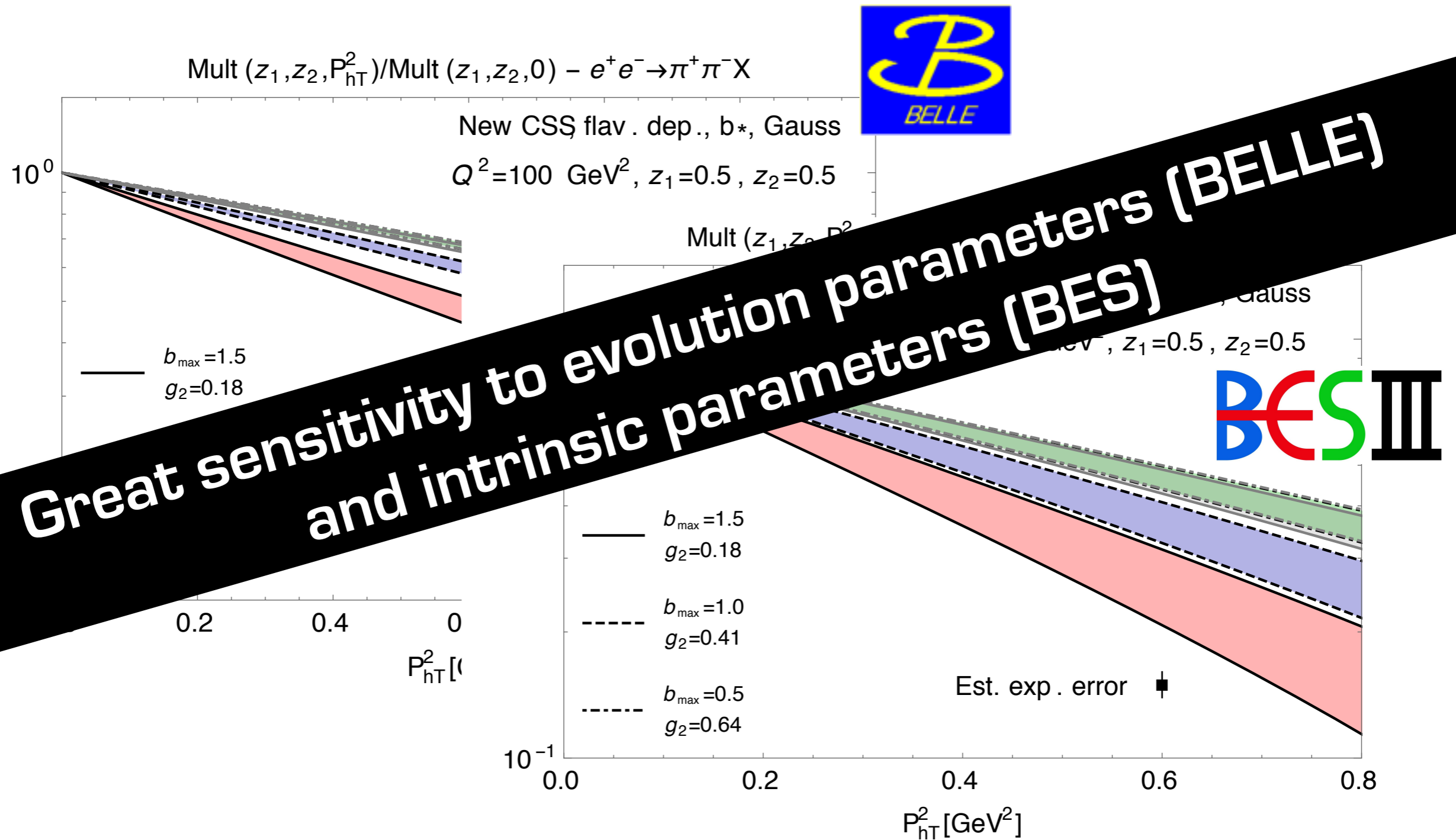


# TMD fragmentation functions



Bacchetta, Echevarria, Mulders, Radici, Signori, [arXiv:1508.00402](https://arxiv.org/abs/1508.00402)

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Bacchetta, Echevarria, Mulders, Radici, Signori, [arXiv:1508.00402](https://arxiv.org/abs/1508.00402)

# Bruno Touschek, pioneer of $e^+e^-$ colliders



You need also  $e^+e^-$  data  
to study  
TMD fragmentation functions

*see talks by Artru, Matevosyan, Radici, Liang*

# Status of other extractions

Data, theory, fits

quark pol.

	U	L	T
nucleon pol. U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

Only first attempts

Twist-2 TMDs

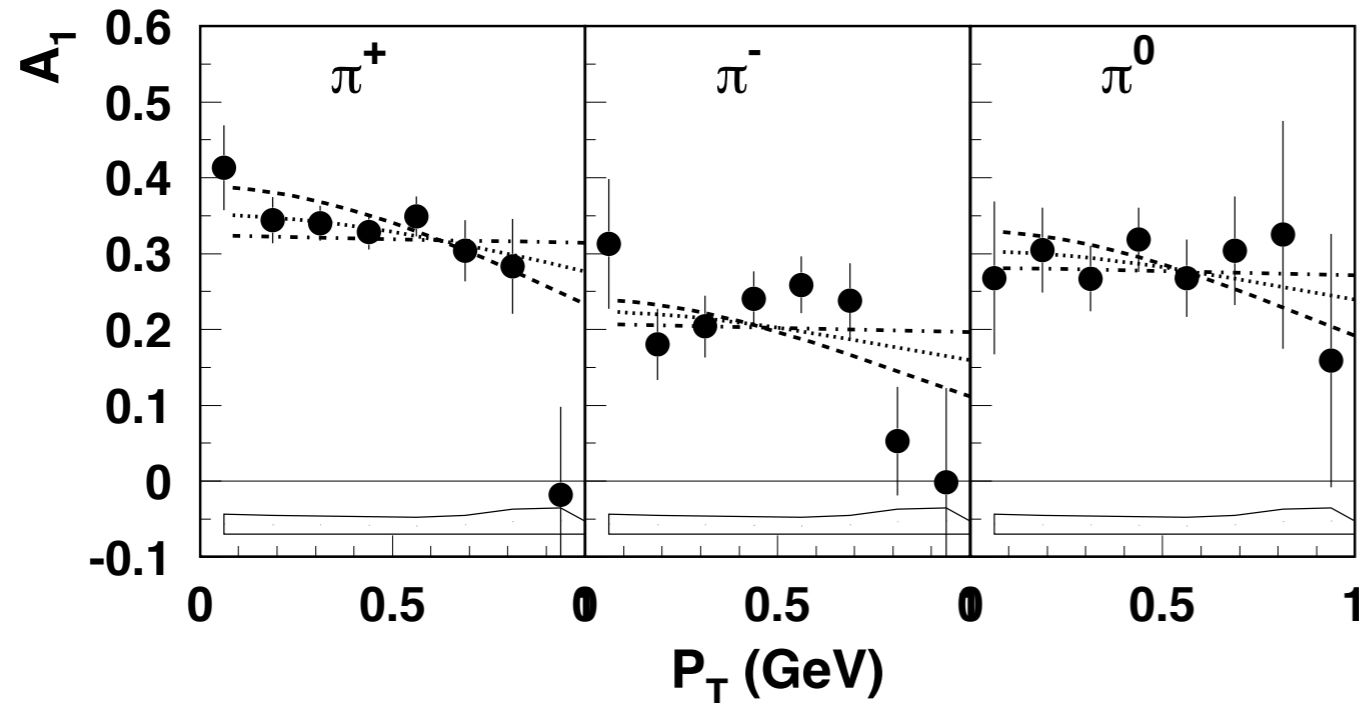
Limited data, theory, fits

*see talks by Courtoy, D'Alesio*

*Lu, Ma, Schmidt, [arXiv:0912.2031](https://arxiv.org/abs/0912.2031)  
Lefky, Prokudin [arXiv:1411.0580](https://arxiv.org/abs/1411.0580)  
Barone, Boglione, Gonzalez, Melis,  
[arXiv:1502.04214](https://arxiv.org/abs/1502.04214)*



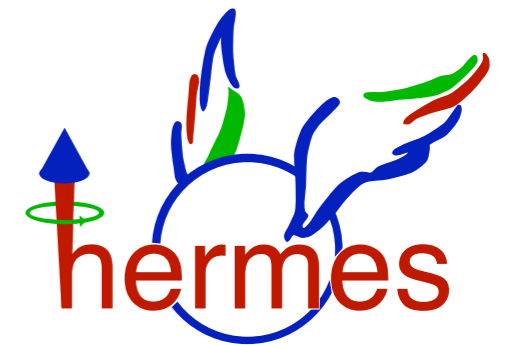
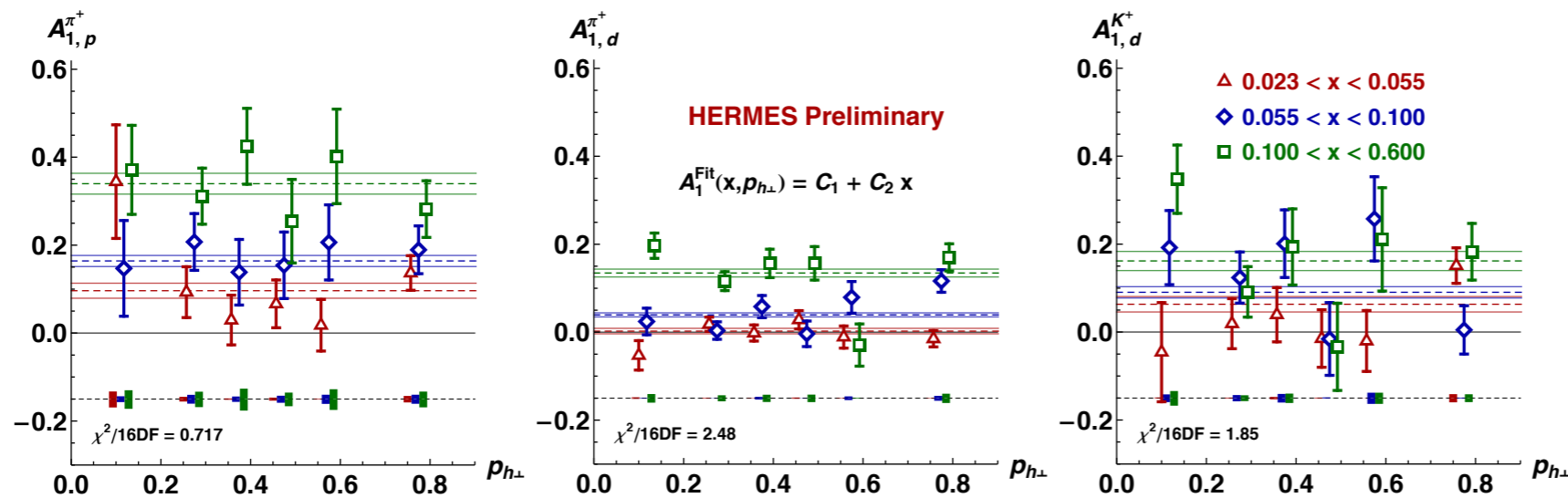
# Helicity TMD ( $F_{LL}$ structure function)



Jefferson Lab

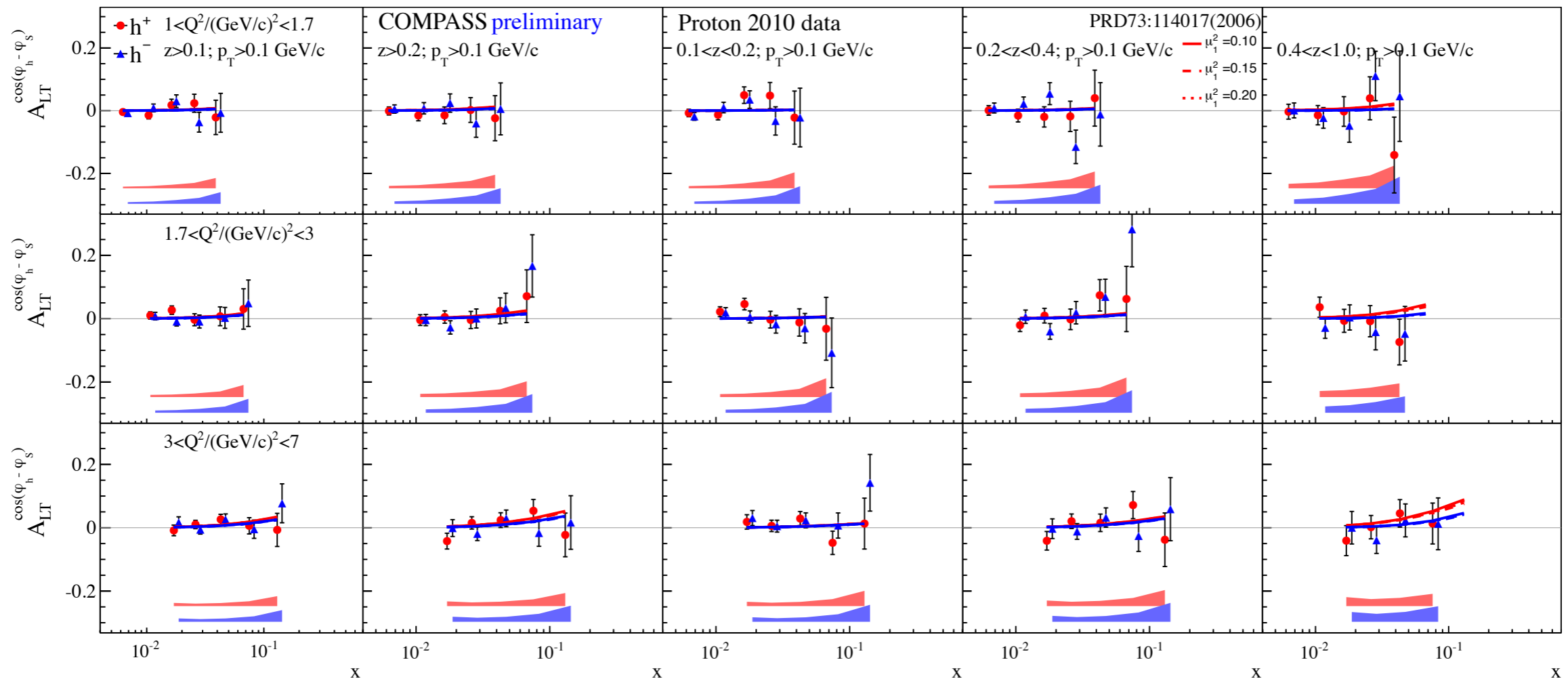


arXiv:1003.4549



<http://dx.doi.org/10.3204/DESY-THESIS-2010-043>

# Worm-gear TMDs

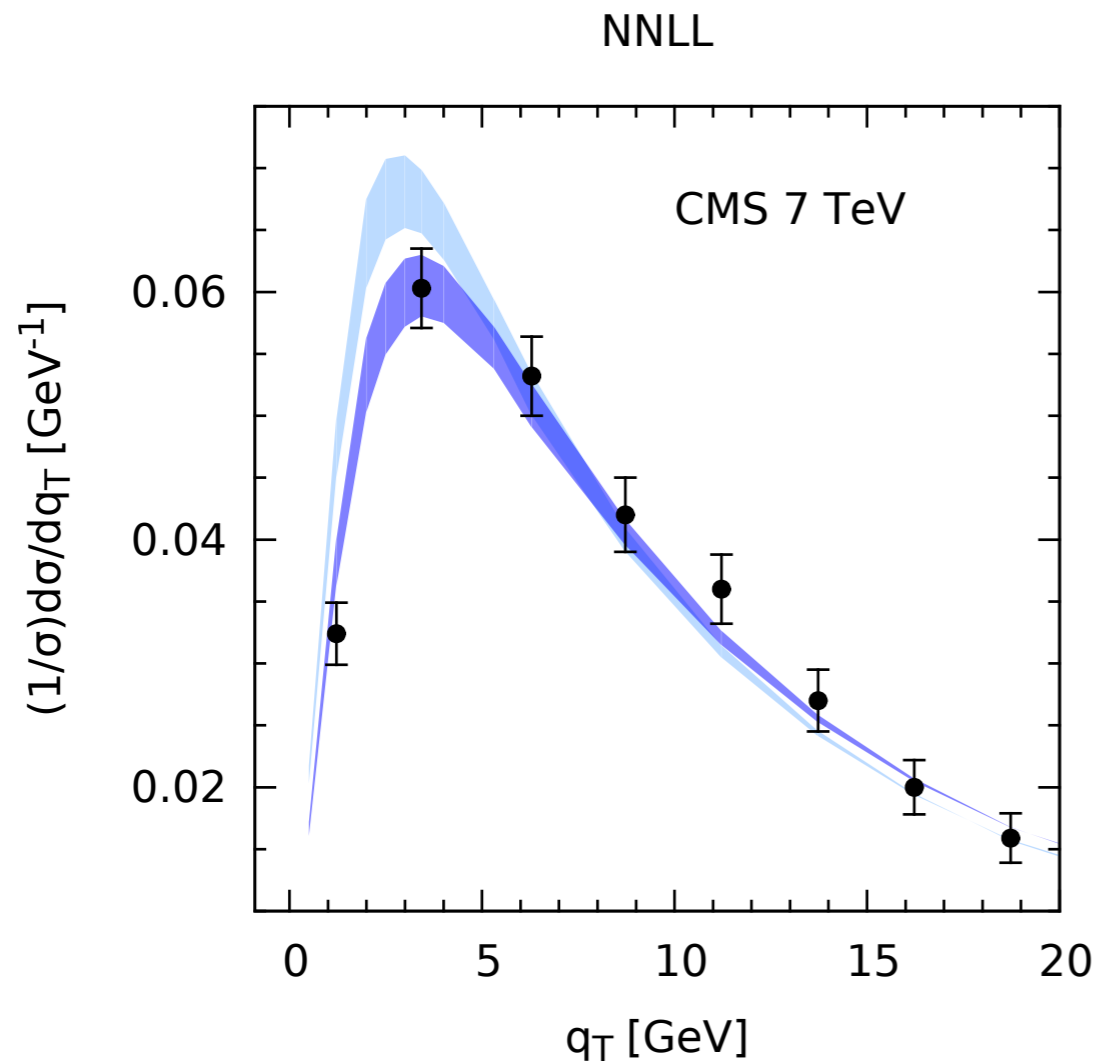


see talk by B. Parsamyan  
 see also HERMES, [arXiv:1107.4227](https://arxiv.org/abs/1107.4227)

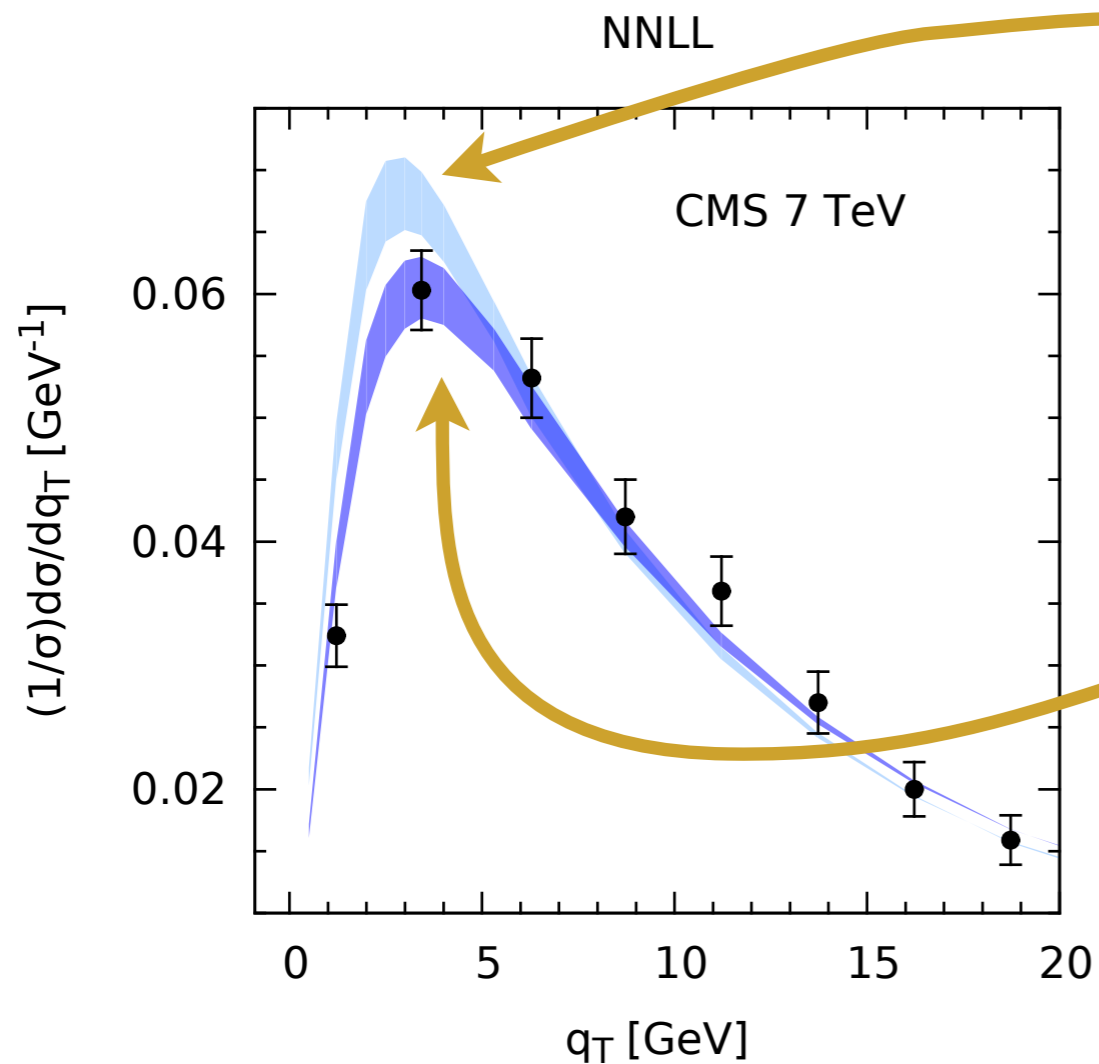
# TMDs at LHC

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# Z boson transverse momentum



# Z boson transverse momentum

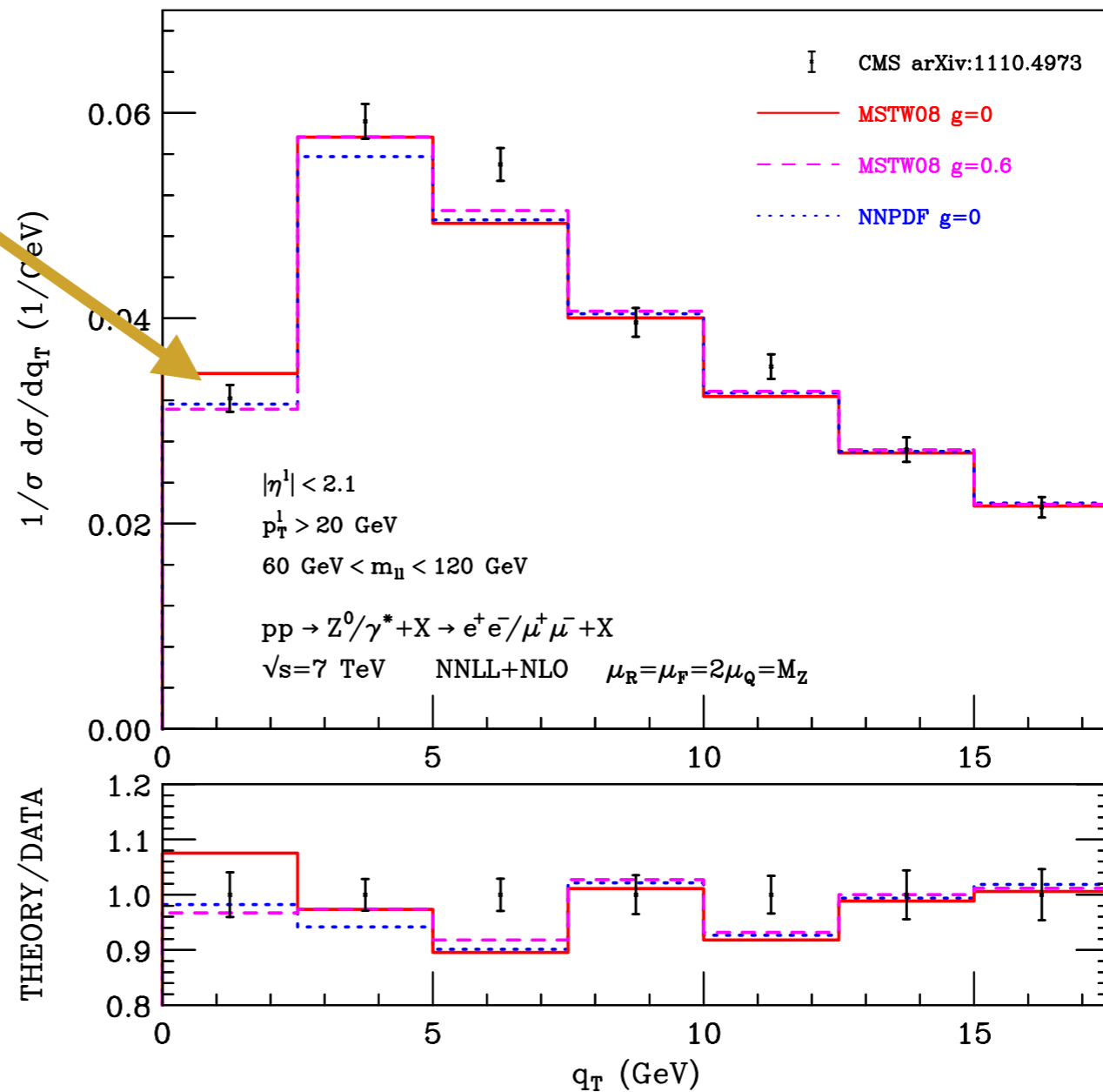


Perturbative  
transverse momentum  
only

With intrinsic  
transverse momentum

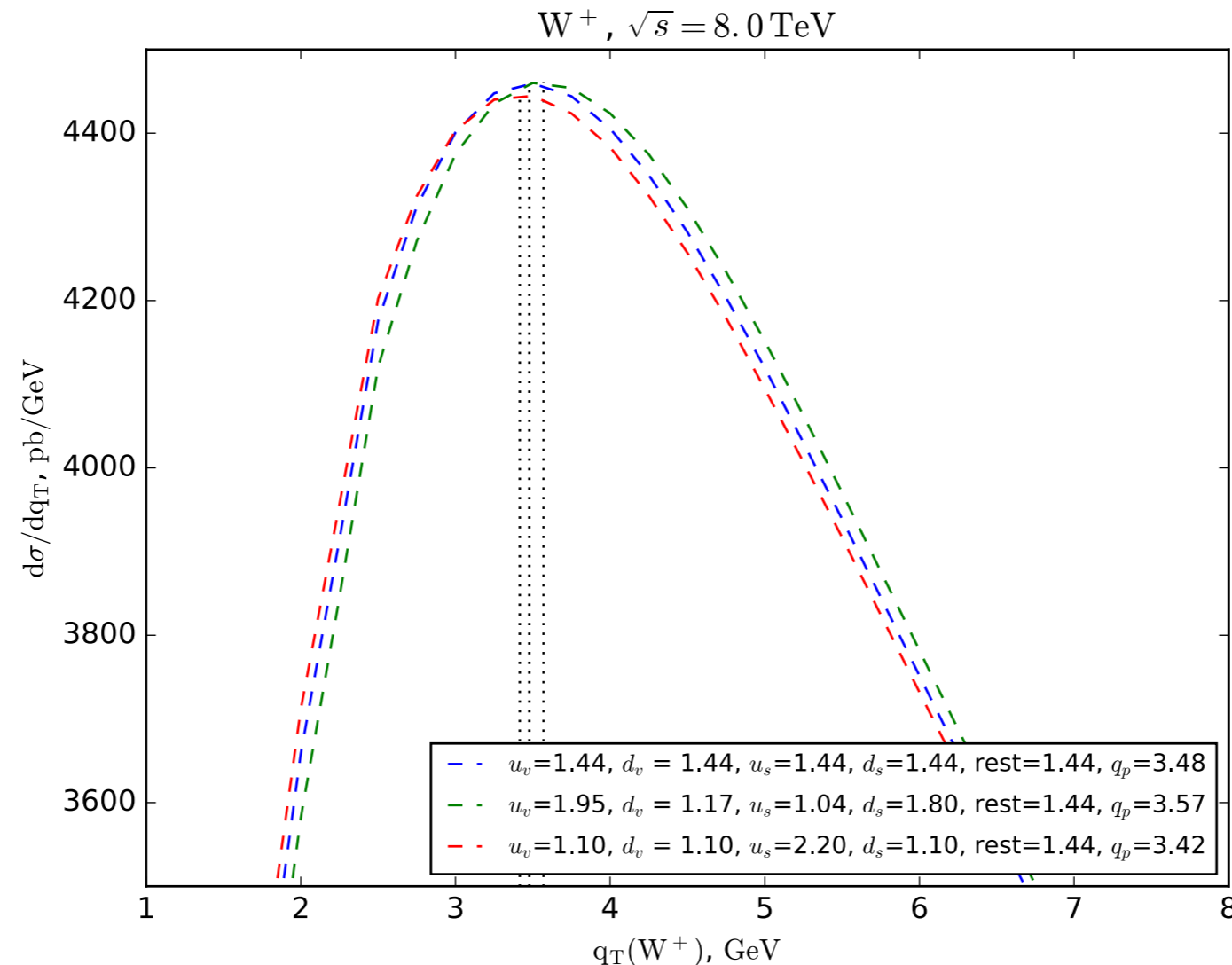
# Z boson transverse momentum

difference between  
red and magenta lines  
due to nonperturbative  
contributions



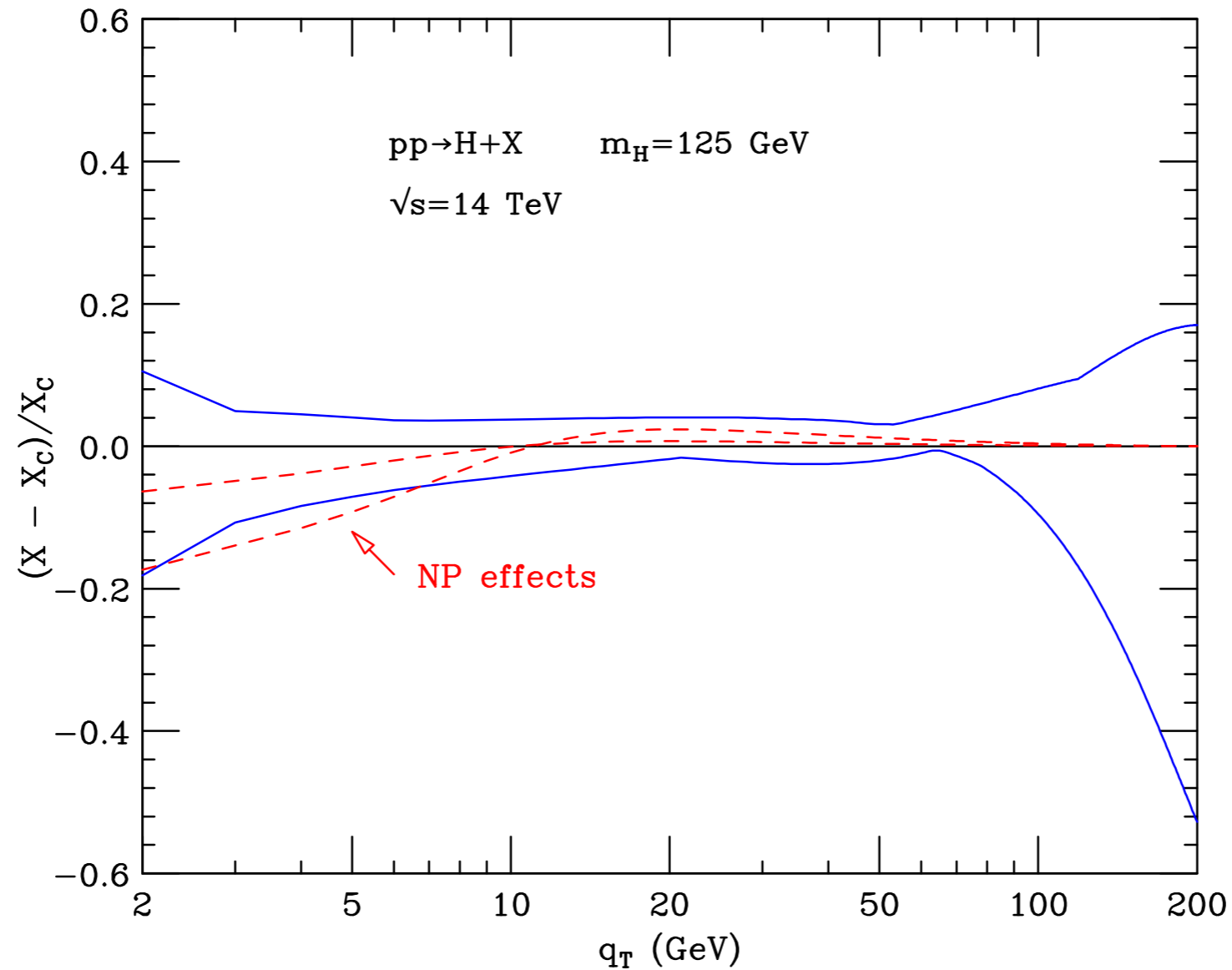
# W transverse momentum

PhD thesis Andrea Signori



Flavor dependence of TMDs can affect the shape of the transverse-momentum spectrum of W bosons. In turn, this might be relevant for precise determinations of  $M_W$

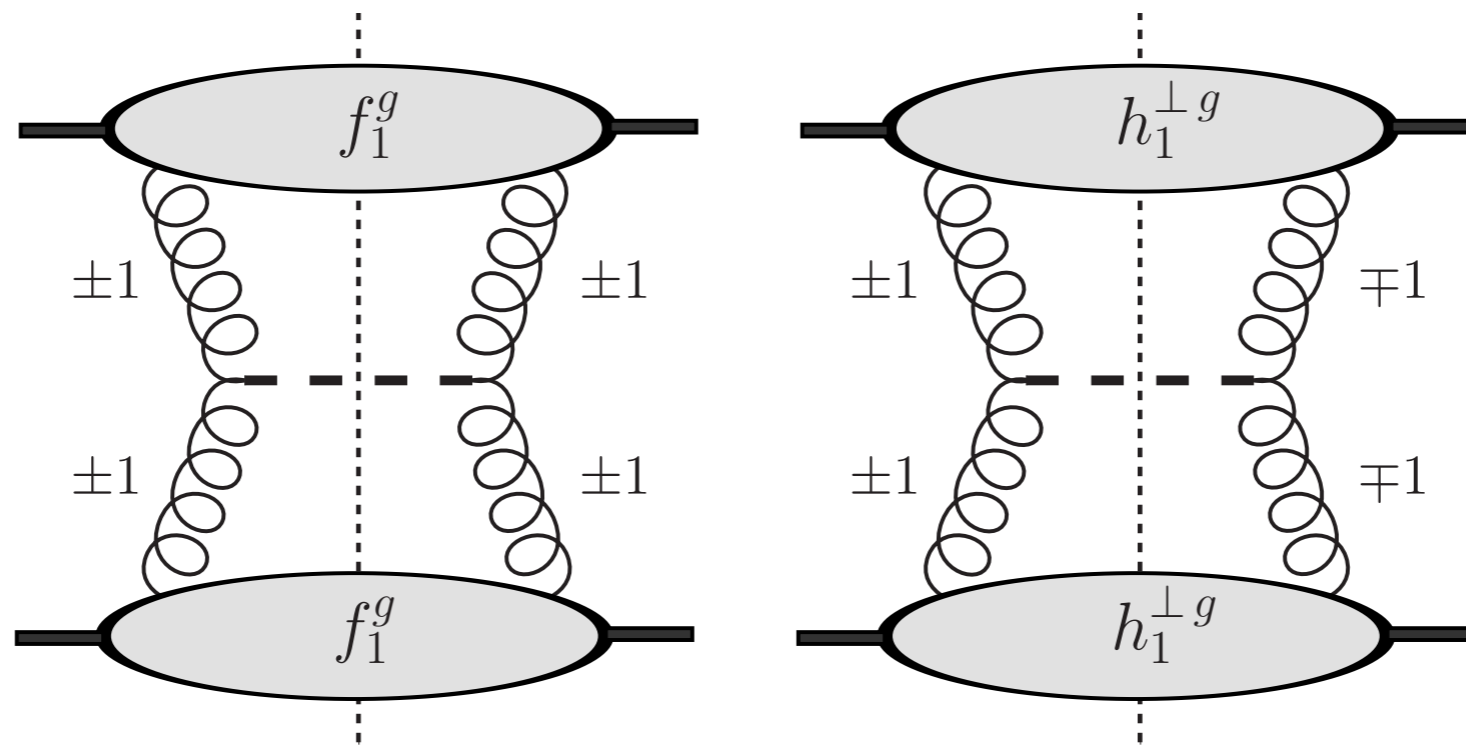
# Higgs transverse momentum





# Gluon TMDs (and linear polarisation)

*Boer, den Dunnen, Pisano, Schlegel, Vogelsang, PRL 108 (2012)*



Not only we could be potentially sensitive to unpolarized gluon TMDs, but also to linearly polarized gluon TMDs

*see talks by Boer, Schlegel, Pisano  
and also low-x talks by Kovchecov, Cherednikov*

# TMDs at LHC

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- Potential for gluon TMD studies

# Other important issues related to LHC

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- Role of parton distribution functions (including 3D ones) in searches for physics beyond the standard model

*see talks by Courtoy, Pitschmann*



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- Role of parton distribution functions (including 3D ones) in searches for physics beyond the standard model

*see talks by Courtoy, Pitschmann*

- 3D distributions are just single-parton density distributions. For LHC, multiparton distributions turn out to be extremely relevant. They are also related to twist-3 parton distribution functions.

*see talk by S. Scopetta*

# Conclusions

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- Steady progress in the field of 3D nucleon structure, both experimental and theoretical
- Accurate extractions of parton distributions (quark and gluons) require more data
- I did not manage to predict much about the future, but I can say for sure that it will be bright!