

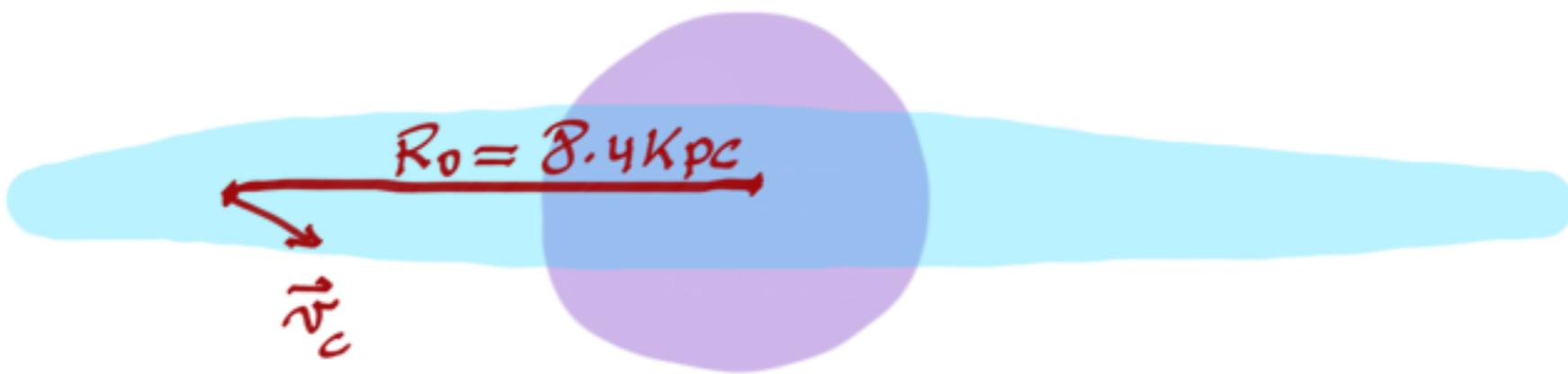
Light dark matter: new detection possibilities

AD Polosa
CERN, Sapienza University of Rome
and INFN Rome

OUTLINE

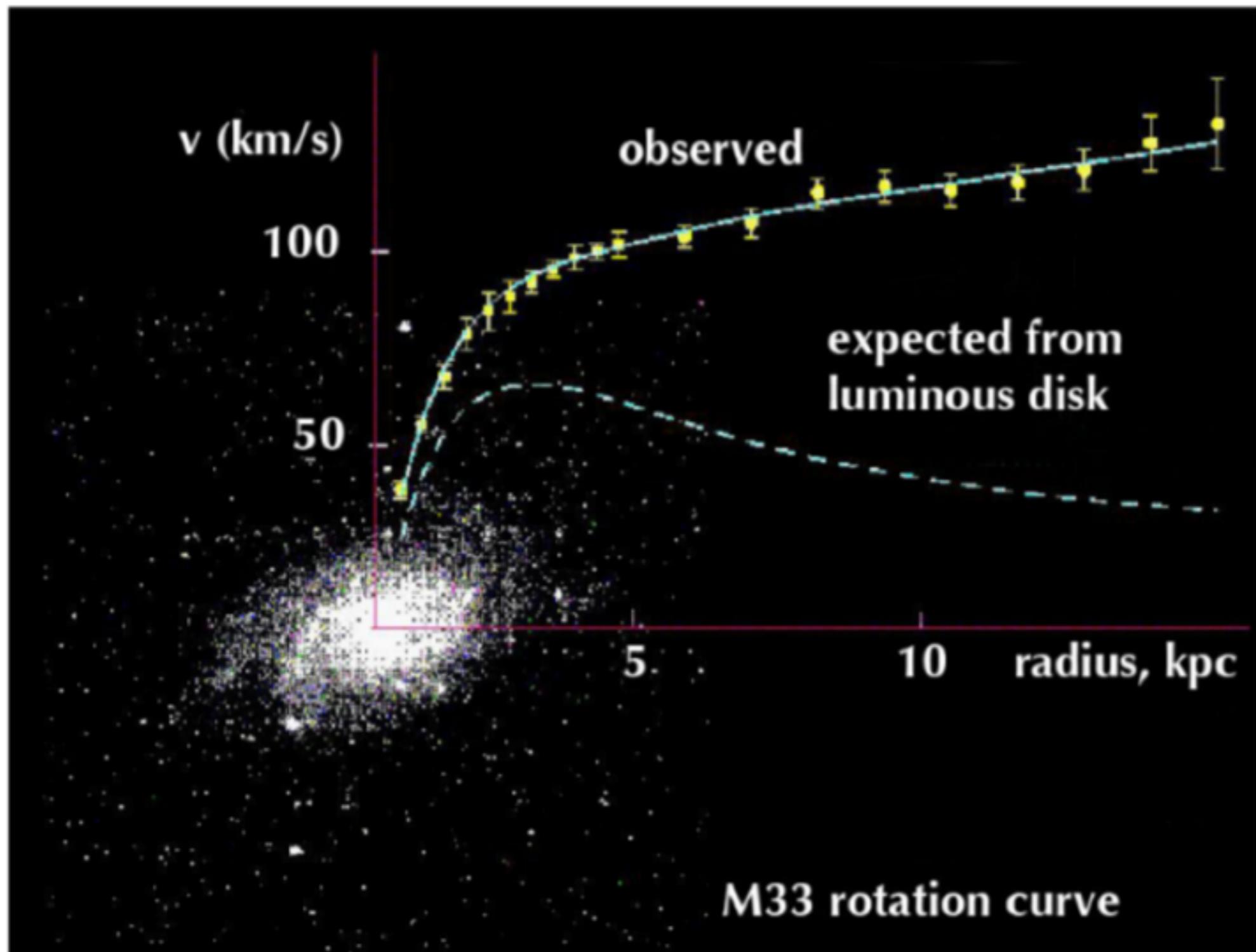
- I - DARK MATTER HALO AND WIMP WIND
- II - CARBON NANOTUBES AS DIRECTIONAL DETECTORS
- III - AXION-LIKE PARTICLES
- IV - LIGHT SHINING THROUGH WALL
WITH SUB-THz PHOTONS

DM halo



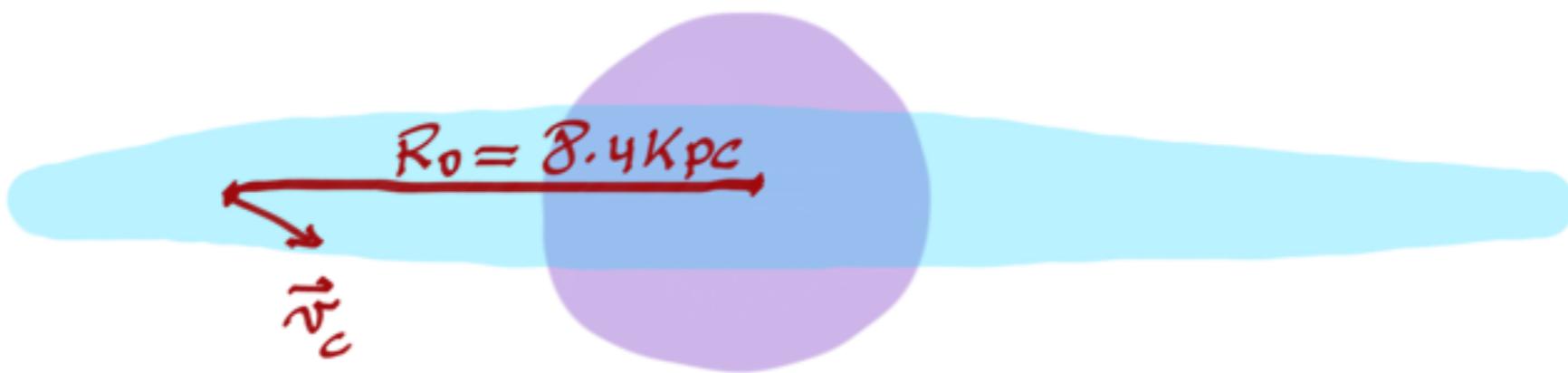
$$\frac{GM(r)}{r^2} = \frac{v_c^2(r)}{r}$$

(Velocity of the Local Standard of Rest)



FROM HI ABSORPTION LINES (neutral atomic
Hydrogen cloud in interstellar medium)

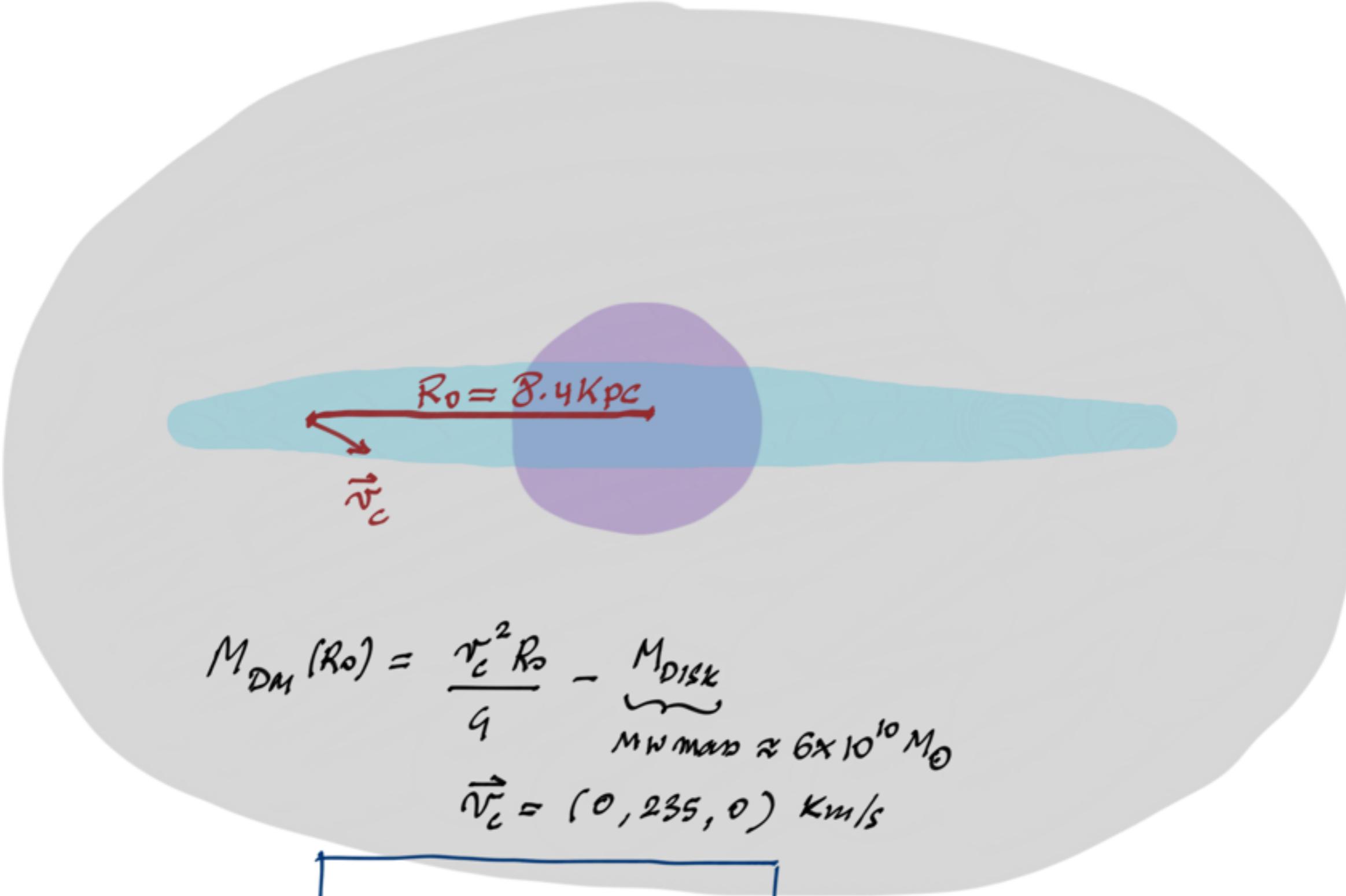
DM halo



$$\frac{GM(r)}{r^2} = \frac{v_c^2(r)}{r} \Rightarrow \rho_{DM} \sim \frac{1}{r^2}$$

out of the edge of the luminous disk

DM halo



$$M_{DM}(R_0) = \frac{\pi^2 R_0}{9} - \underbrace{M_{\text{DISK}}}_{MW \text{ mass} \approx 6 \times 10^{10} M_\odot}$$

$$\vec{v}_c = (0, 235, 0) \text{ km/s}$$

$$M_{DM}(R_0) \approx \frac{1}{2} M_{\text{DISK}}$$

DM halo

Any function f of the energy alone $f(E)$ is an equilibrium distribution ($\partial f / \partial t = 0$) of a collisionless Boltzmann eq. ($df/dt = 0$ or $C[f] = 0$).

$$f(\vec{v}) = \left(\frac{1}{\pi v_0^2} \right)^{3/2} e^{-\vec{v}^2/v_0^2} \quad (\text{Galaxy frame})$$

$$v_0 \approx v_{c,\infty} \approx 235 \text{ Km/s}$$

considering that particles with $v > v_{\text{esc}}(r)$ will not be gravitationally bound to the MW.

$$v_{\text{esc}} = \sqrt{2 |\Phi(r)|}$$

$$v_{\text{esc}}^2 = 2v_c^2 + \frac{8\pi G}{3} \int_{R_0}^{\infty} \rho(r) r dr$$

v_{esc} contains info. on the mass outside the solar circle.
The fact that $v_{\text{esc}} \gg \sqrt{2} v_c$ indicates significant amount of mass exterior to solar circle.

$$v_{\text{esc}} \approx 498 \div 608 \text{ km/s}$$

(From "high velocity stars")

DM halo

$$f(\vec{r}) = \begin{cases} \frac{1}{N} \left(\frac{1}{\pi v_0^2} \right)^{3/2} \left[e^{-\frac{v^2}{v_0^2}} - e^{-\frac{v_{esc}^2}{v_0^2}} \right] & (v < v_{esc}) \\ 0 & (\text{otherwise}) \end{cases}$$

- * The assumption of a smooth halo might not be so good - Halo substructure may affect directionality.
- * A co-rotational DM disk might exist, $\rho \sim 10 \div 50\%$ of ρ_{loc}^{DM} ($= 5 \cdot 10^{-25} \text{ gr/cm}^3$)

Left-over particles

In absence of annihilations

$$n(t) a^3(t) = n(t_0) a^3(t_0)$$

let σ be the xx exothermic annihilation cross-

$$n(t) a^3(t) = \frac{n(t_0) a^3(t_0)}{1 + n(t_0) a^3(t_0) \int_{t_0}^t \frac{\langle v \sigma \rangle}{a^3(t')} dt'}$$

$t \rightarrow +\infty$

where $[\rho r \sigma] = 1 \text{ e}^{-1}$

If the integral in the denominator is too large, there are no left-over particles.

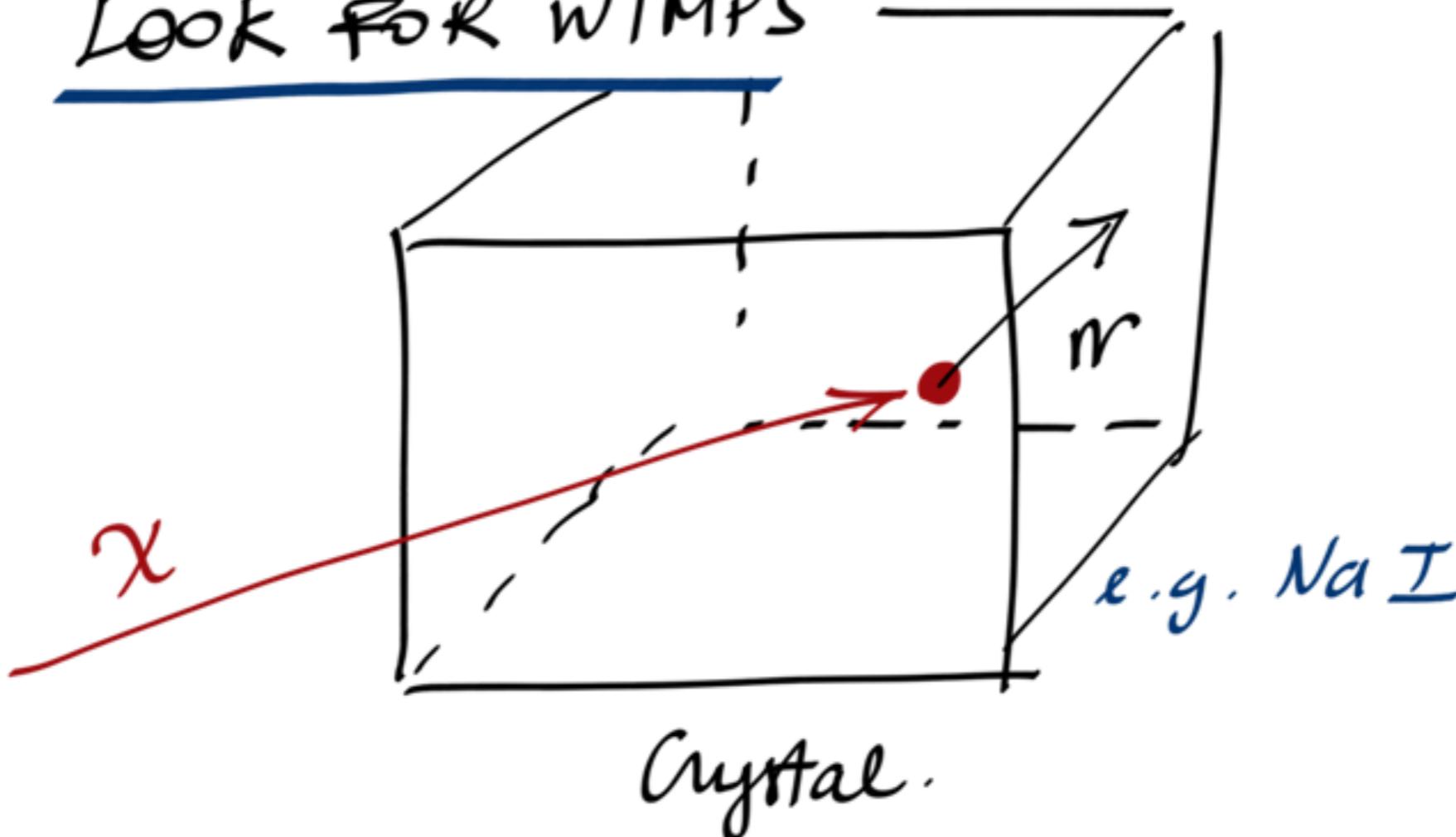
$$(v \sigma \sim k^{2\alpha+1} k'^{2\alpha+1} / k^2 \propto k \rightarrow 0, k' \rightarrow \text{const.}; T \sim a^{-1}; a \propto t^{2/3}; \langle \rangle_{\text{out}} \sim \int dE \bar{e}^{E/k} \dots)$$

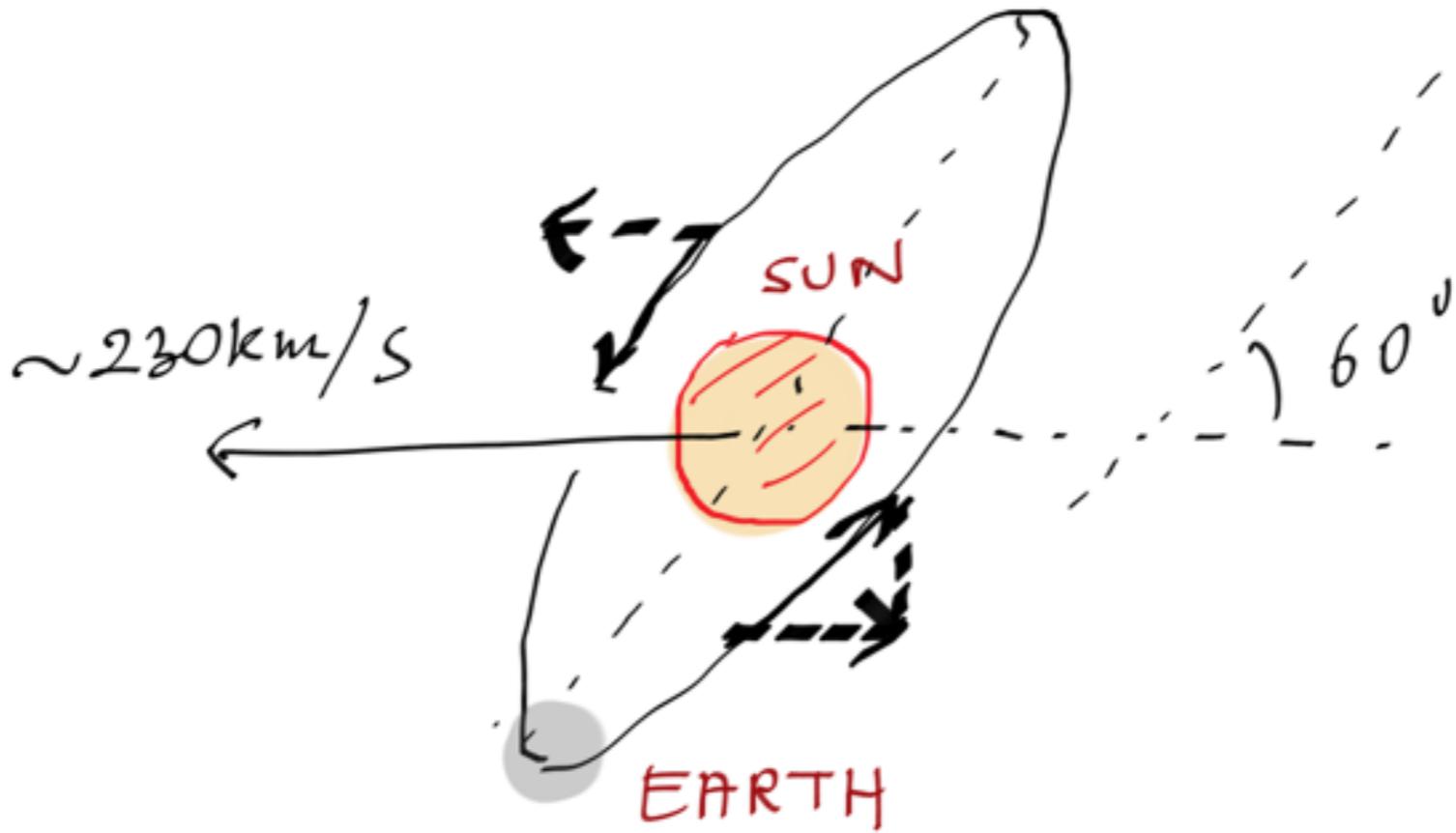
WIMPS

χ of $M_\chi \approx 100$ GeV weakly inter.
 with $\langle v \sigma \rangle \approx 10^{-26} \text{ cm}^3/\text{sec}$ give
 a left over \mathcal{S} which is

$$\mathcal{S} \approx \mathcal{S}_{\text{DM}}$$

Look for WIMPS





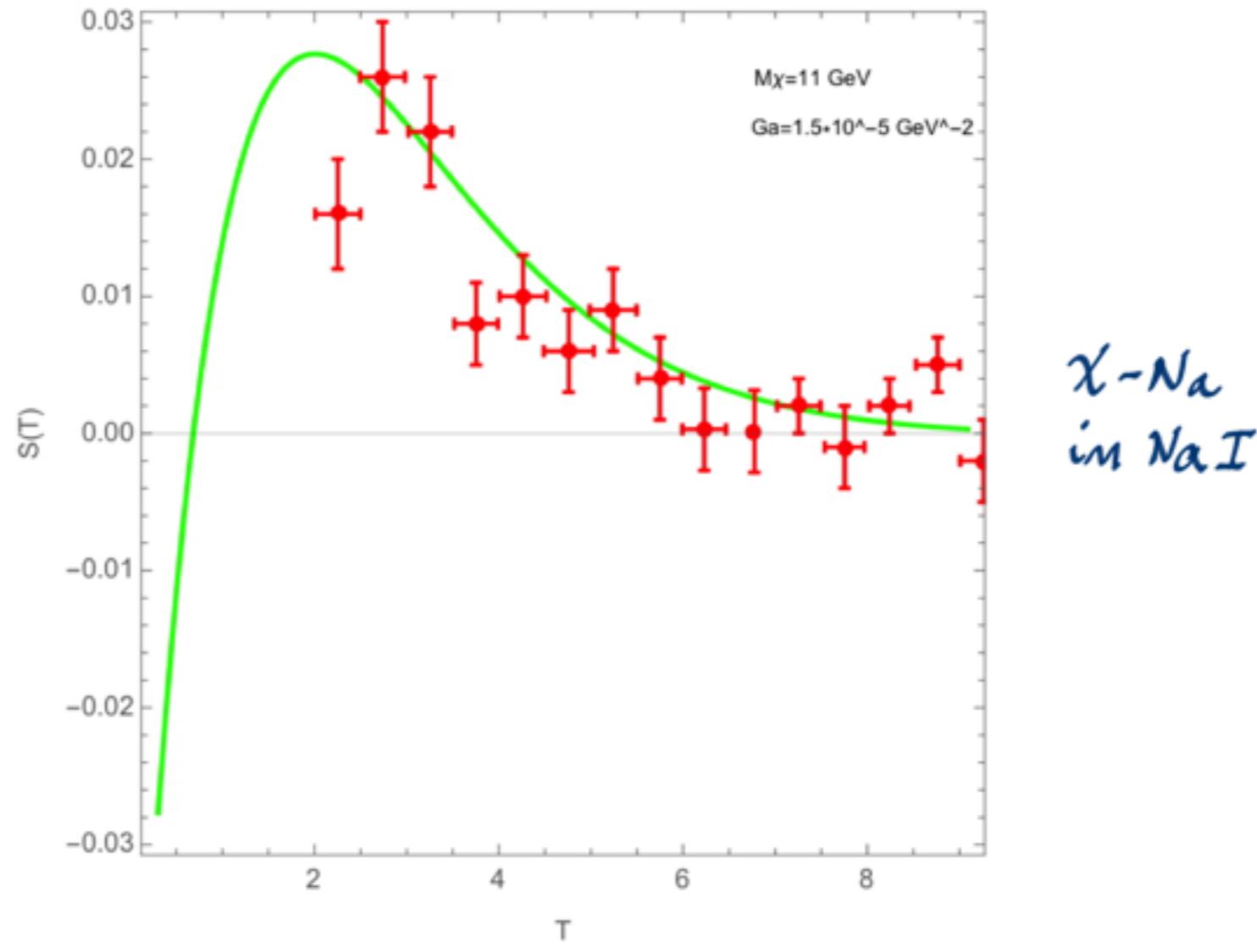
$$\vec{w}(t) = [232 + 15 \cos \psi(t)] \hat{k}$$

$$\psi(t) = \pi - \frac{t - 151.5}{365.25} = wt + \varphi_0$$

DAMA

$$\frac{d\Gamma}{dT} = A(T) + S(T) \cos(\omega T + \varphi_0)$$

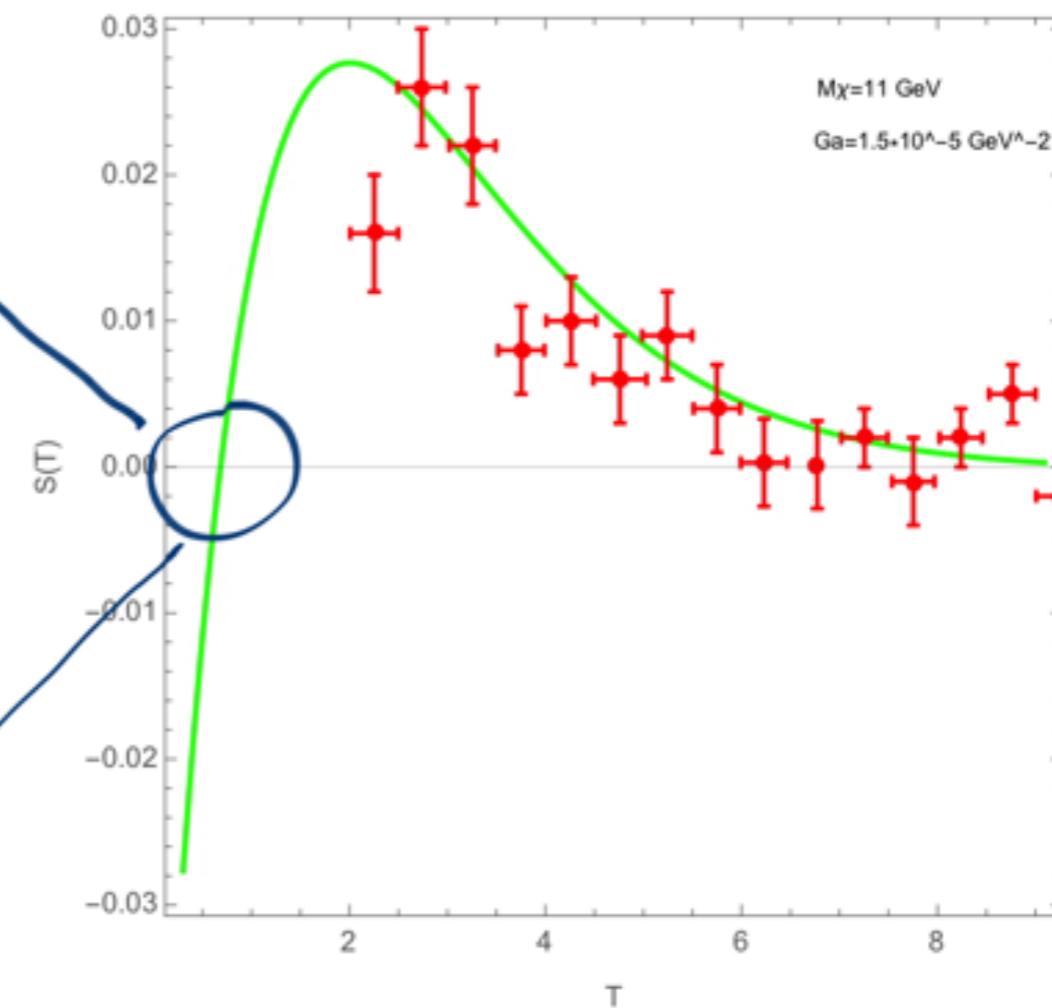
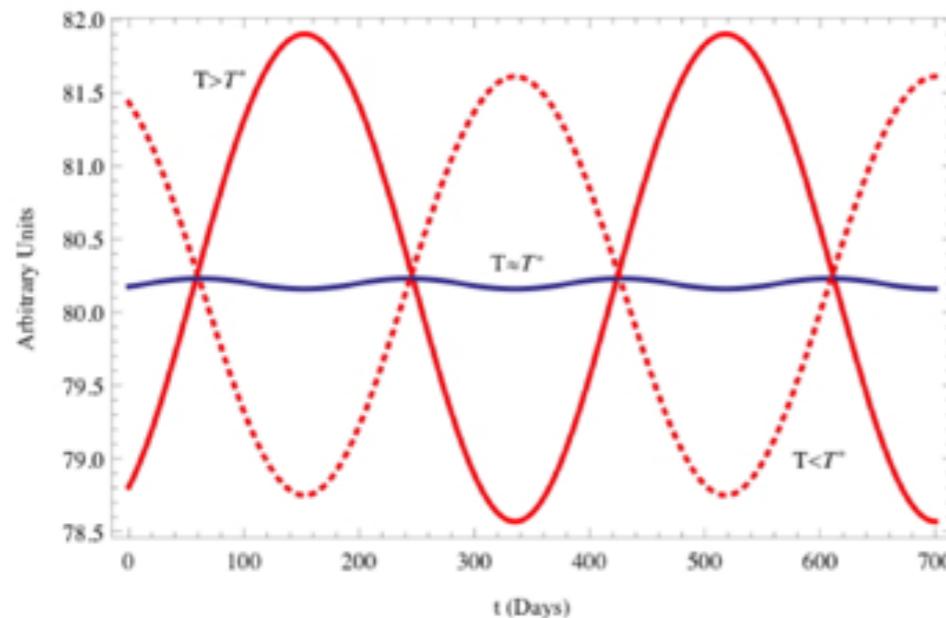
$$\left(\frac{cpd}{\text{kg keV}} \right)$$



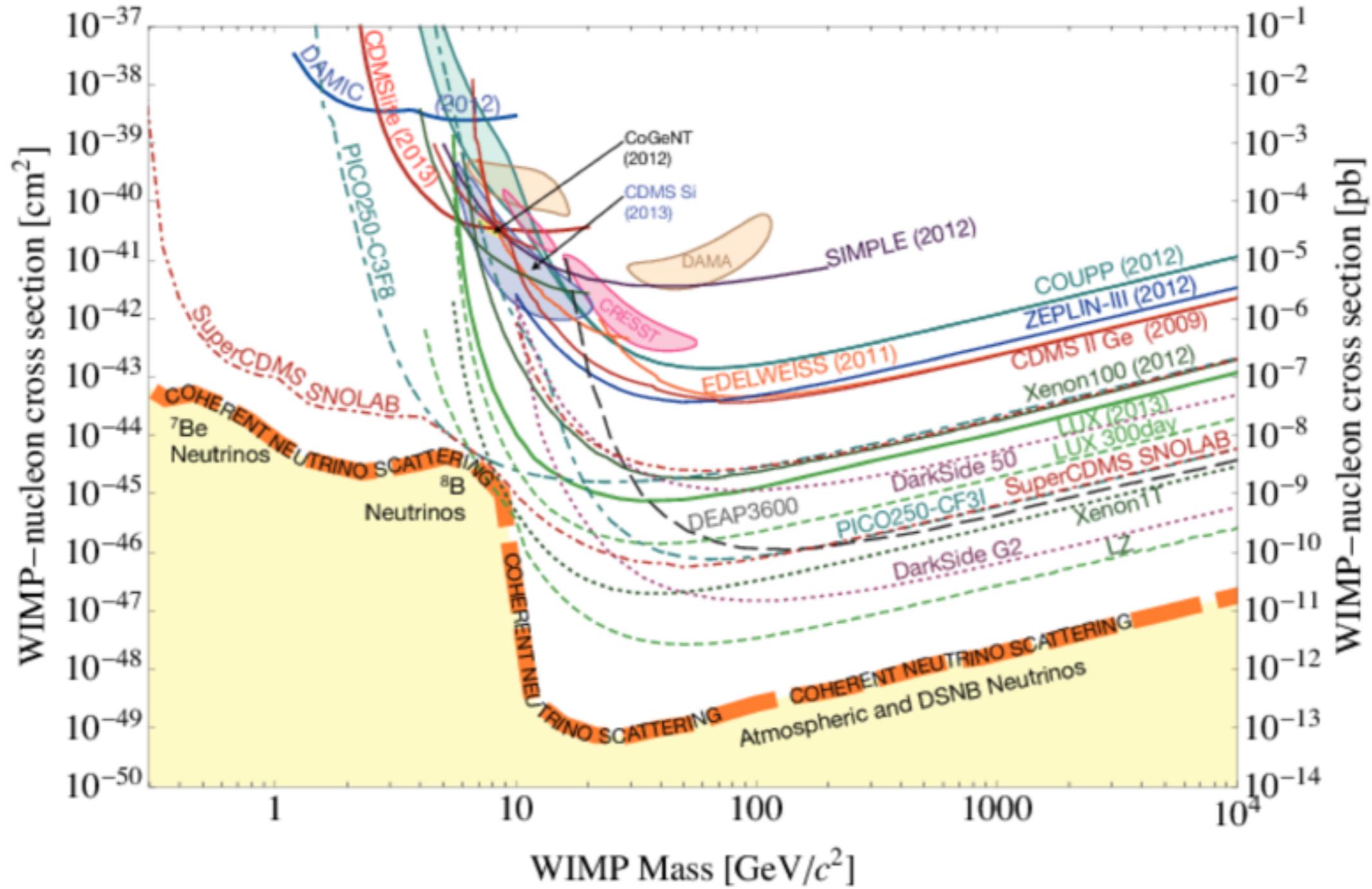
NUCLEAR RECOIL KINETIC ENERGY
(KeVee)

DAMA

$$\frac{d\Gamma}{dT} = A(T) + S(T) \cos(\omega t + \varphi_0)$$

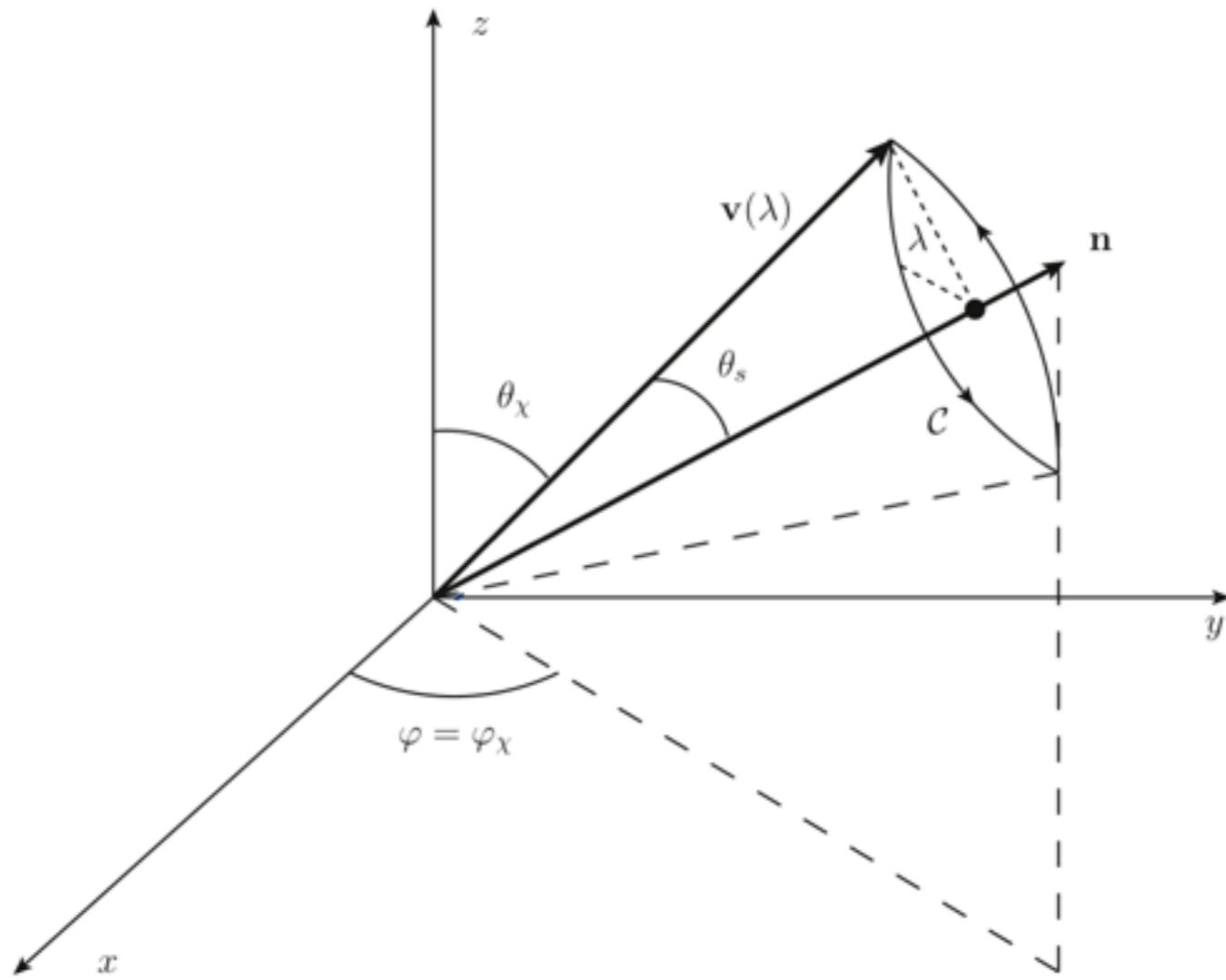


EXCLUSION PLOT



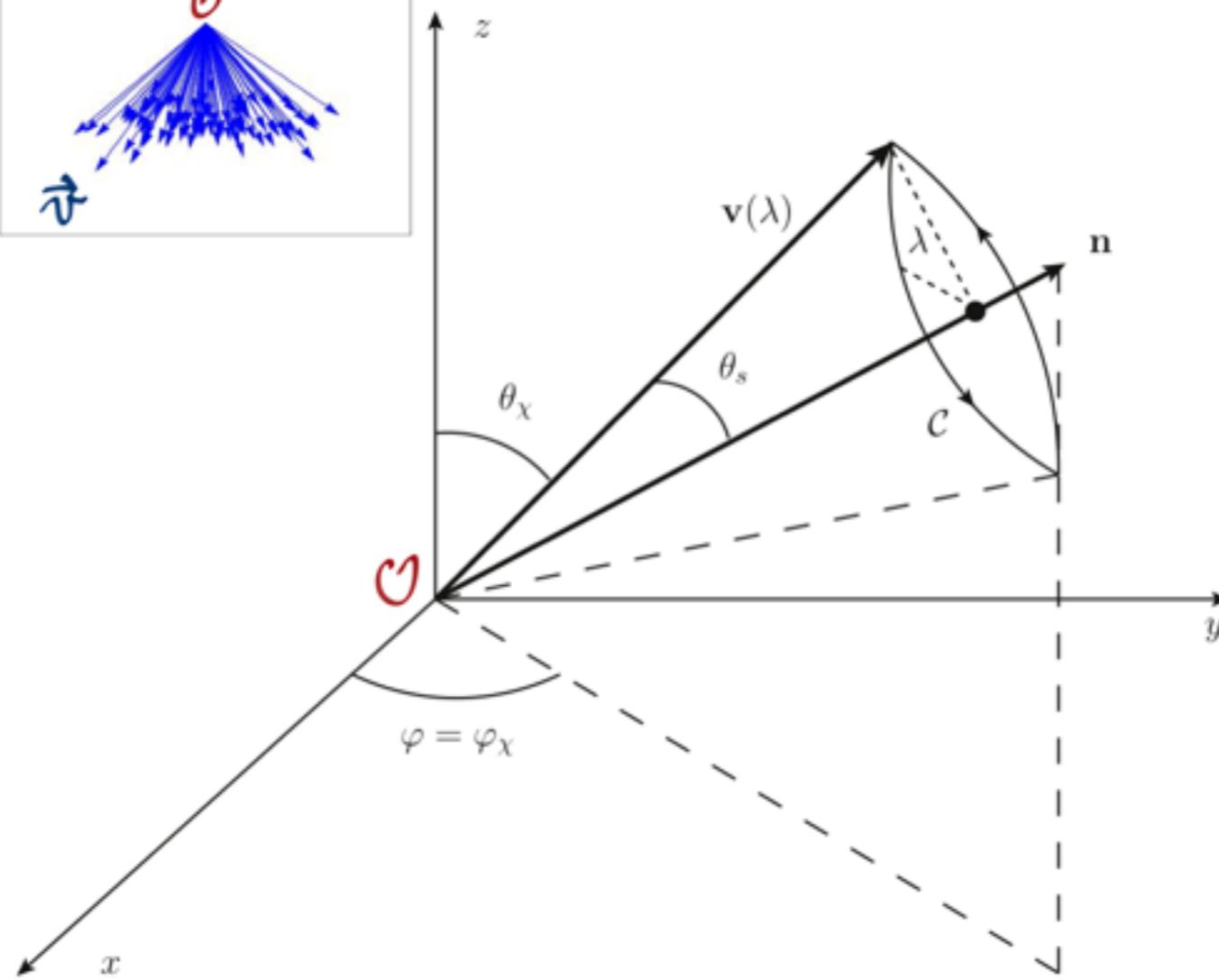
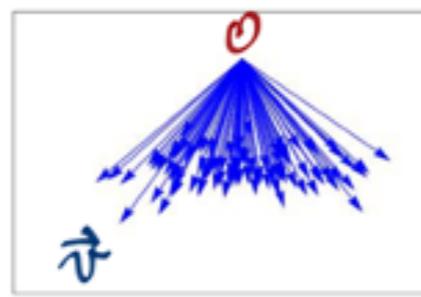
WIMP WIND

★ CYGNUS



WIMP WIND

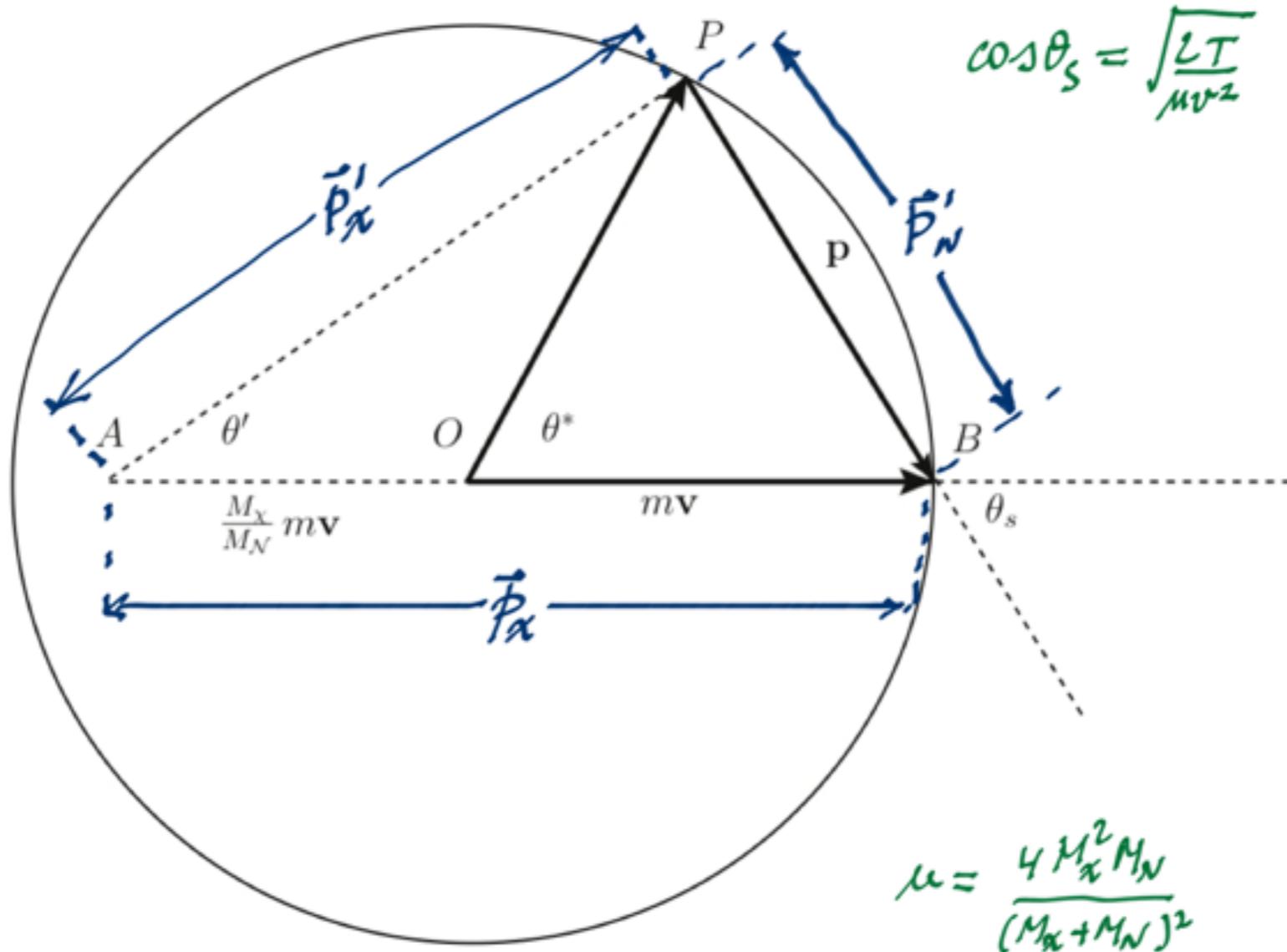
★ CYGNUS



$$f(\vec{r}) = \beta e^{-\alpha (\vec{r} + \vec{w}(t))^2}$$

$\theta (\equiv \theta_\chi + \theta_s \text{ if } \lambda=0) \approx \pi$ is the
wind orientation

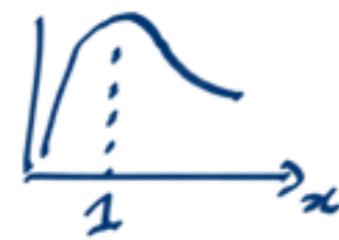
Kinematics



$$\cos \theta_s = \sqrt{\frac{LT}{mv^2}}$$

$$\mu = \frac{4 M_\alpha^2 M_N}{(M_\alpha + M_N)^2}$$

$$\frac{(T'_N)_{\max}}{T_\alpha} = \frac{4x}{(1+x)^2}, \quad x = \frac{M_\alpha}{M_N},$$



Nuclear Recoils

$$\frac{d\Gamma}{d\Omega_n} = n_\chi \langle v \frac{d\sigma}{d\Omega_n} \rangle_v$$

As a working point we take DAMA data on WIMP- Na collisions

$$\sigma_{\chi p} \simeq 2 \cdot 10^{-4} \text{ pb}$$

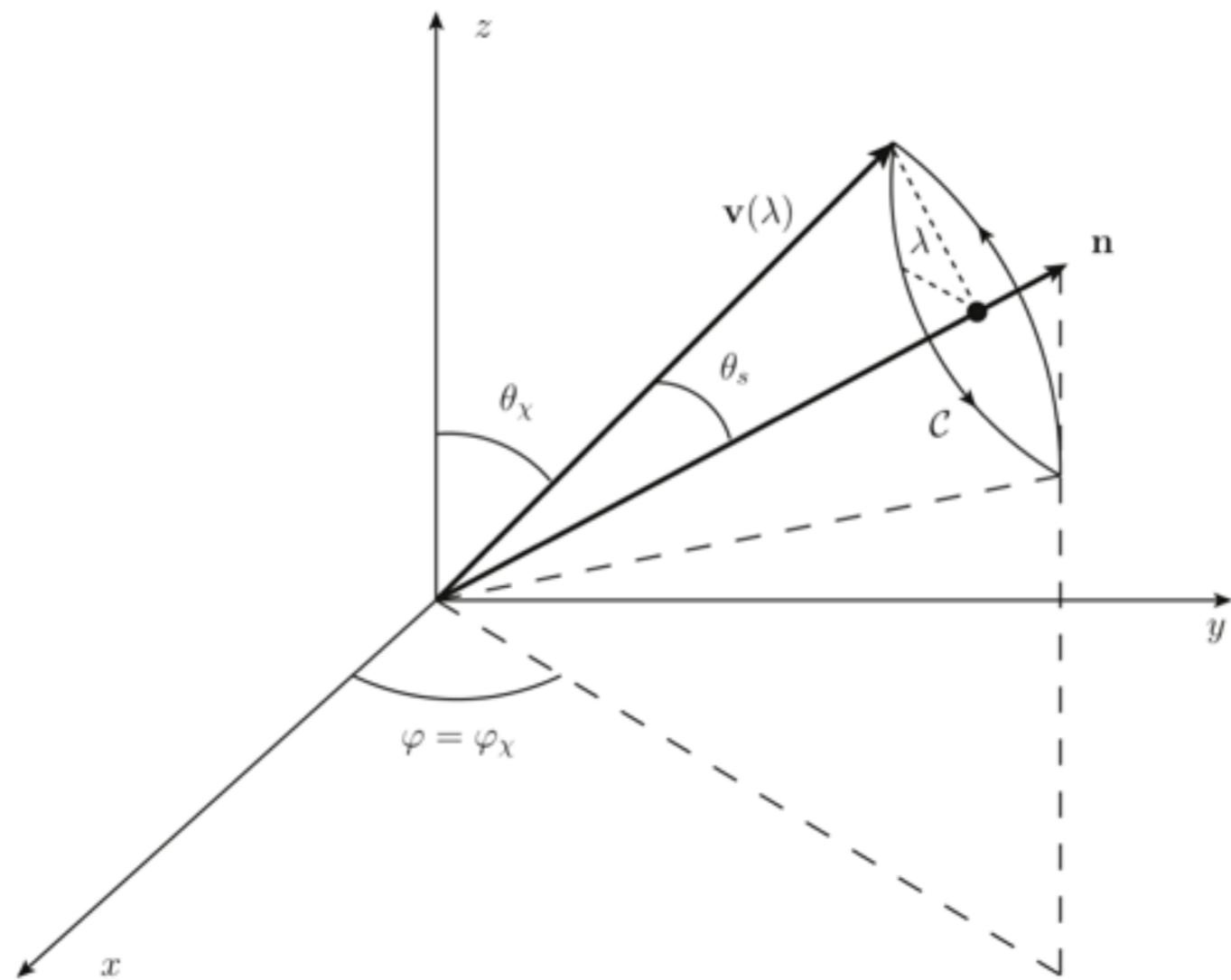
With this we find

$$G_A = \frac{A^2}{4} G \simeq 10^{-5} \text{ GeV}^{-2}$$

with $A=12$ and $M_\chi \simeq M_C$

WIMP WIND

★ CYGNUS



WIMP WIND

$$\vec{v}(\lambda, \theta_s) = \vec{v}_0 \cos \lambda + \underbrace{\hat{n}(\hat{n} \cdot \vec{v}_0)}_{\sim \cos \theta_s} (1 - \cos \lambda) + \underbrace{(\vec{v}_0 \times \hat{n})}_{\sim \sin \theta_s} \sin \lambda$$

Since $d\sigma/ds_{NN}$ is isotropic, $\langle v d\sigma/ds_{NN} \rangle_v \sim$

$$\int d^3r f(\vec{v}(\lambda, \theta_s)) = \int d^3v f(\vec{v}(\lambda, \theta_s)) \int dT \delta(T - \frac{1}{2} \mu v^2 \cos^2 \theta_s)$$

$$\mu = \frac{4 M_\chi^2 M_N}{(M_\chi + M_N)^2}$$

$$= \int dT \int dv v^2 \int d\lambda \int d \cos \theta_s f(\vec{v}(\lambda, \theta_s)) \delta(T - \frac{1}{2} \mu v^2 \cos^2 \theta_s)$$

$$= \int dT \int dv v^2 \int d\lambda f(\vec{v}(\lambda)) \frac{1}{v \sqrt{2\mu T}}$$

$$\frac{d\Gamma}{dT d \cos \theta} = C \int_{\sqrt{2T/\mu}}^{v_{esc}} dv \cdot v \int_0^{2\pi} d\varphi \int_0^{2\pi} d\lambda f(\vec{v}(\lambda))$$

$$\text{use } \int_0^{2\pi} d\lambda e^{-\alpha(A + B \cos \lambda)} = 2\pi e^{-\alpha A} I_0(\alpha B)$$

WIMP WIND

$$\frac{d\Gamma}{dT d\cos\theta} = C \int_{\sqrt{2T/\mu}}^{v_{esc}} dv v \beta e^{-\alpha A} I_0(\alpha B)$$

$$A = v^2 + w_z^2(t) + 2vw_z(t) \cos\theta_s \cos\theta$$

$$B = 2vw_z(t) \sin\theta_s \sin\theta$$

$$C = K \frac{m_\chi G_A^2 \Lambda^4 F_A^2(2M_N T)}{16 M_\chi^2 M_N}$$

$$\Lambda \sim \sqrt{s} \simeq M_\chi + M_N$$

$$K = 5 \cdot 10^7$$

to get $\frac{cpd}{kg \text{ KeV}}$ for CNTs

velocities on in units of c

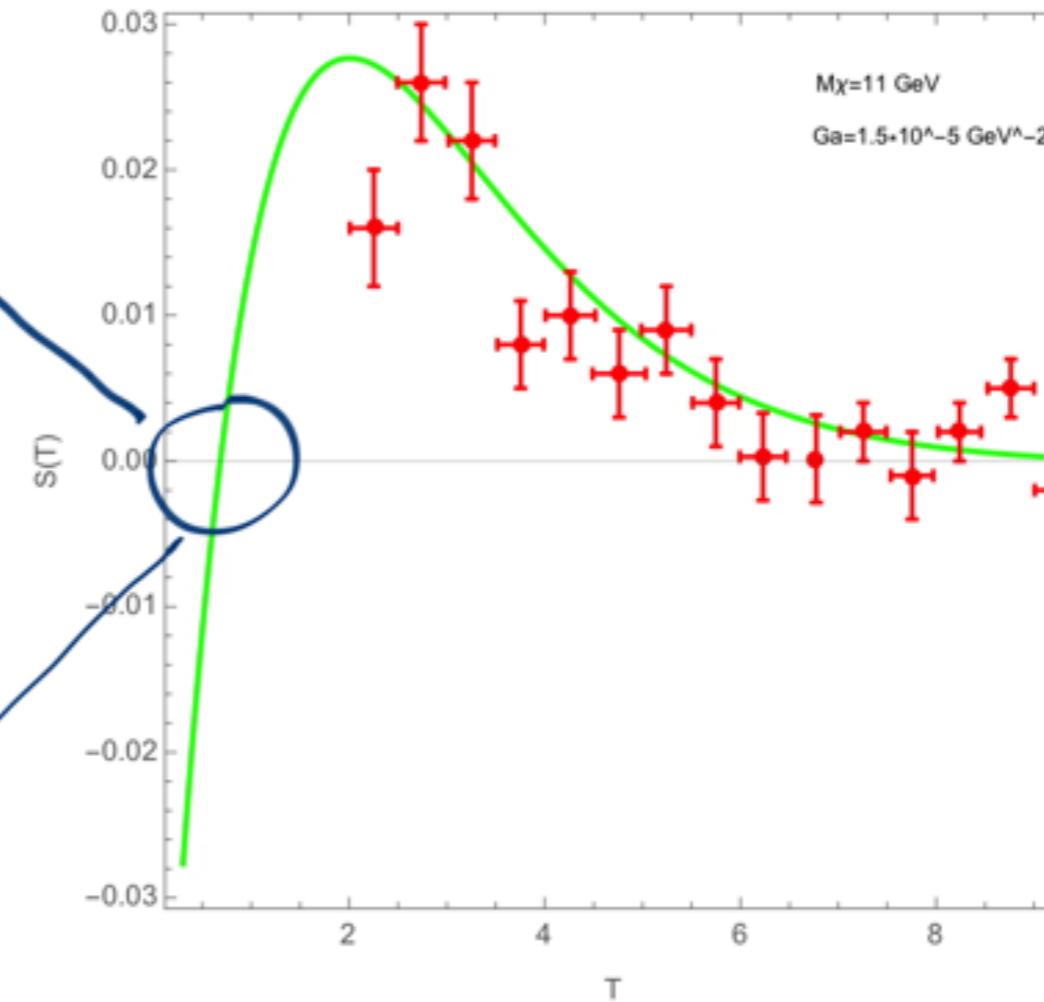
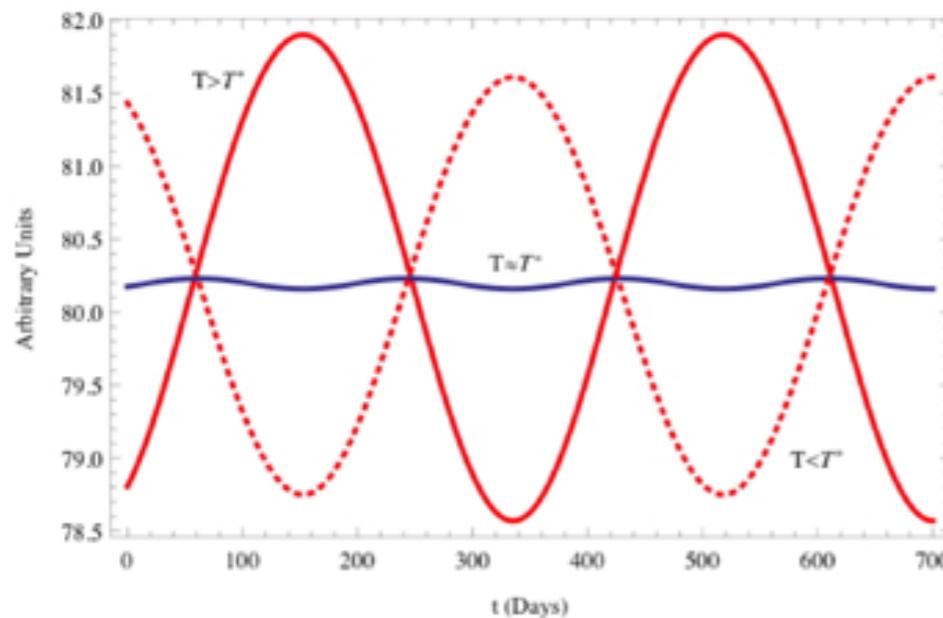
$$v_{esc} (\text{on } \oplus) \approx 780 \text{ km/s}$$

$$n_\chi = \rho_\chi / M_\chi = 0.4 \text{ GeV/cm}^3 / 11 \text{ GeV}$$

$$G_A \approx 10^{-5} \text{ GeV}^{-2}$$

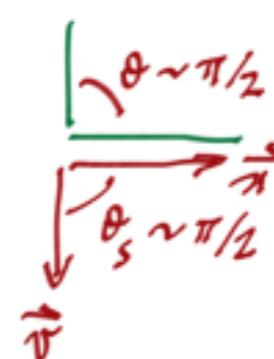
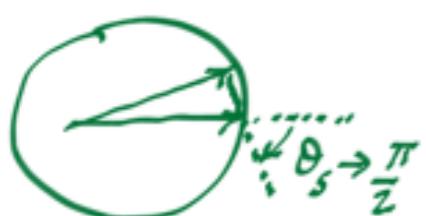
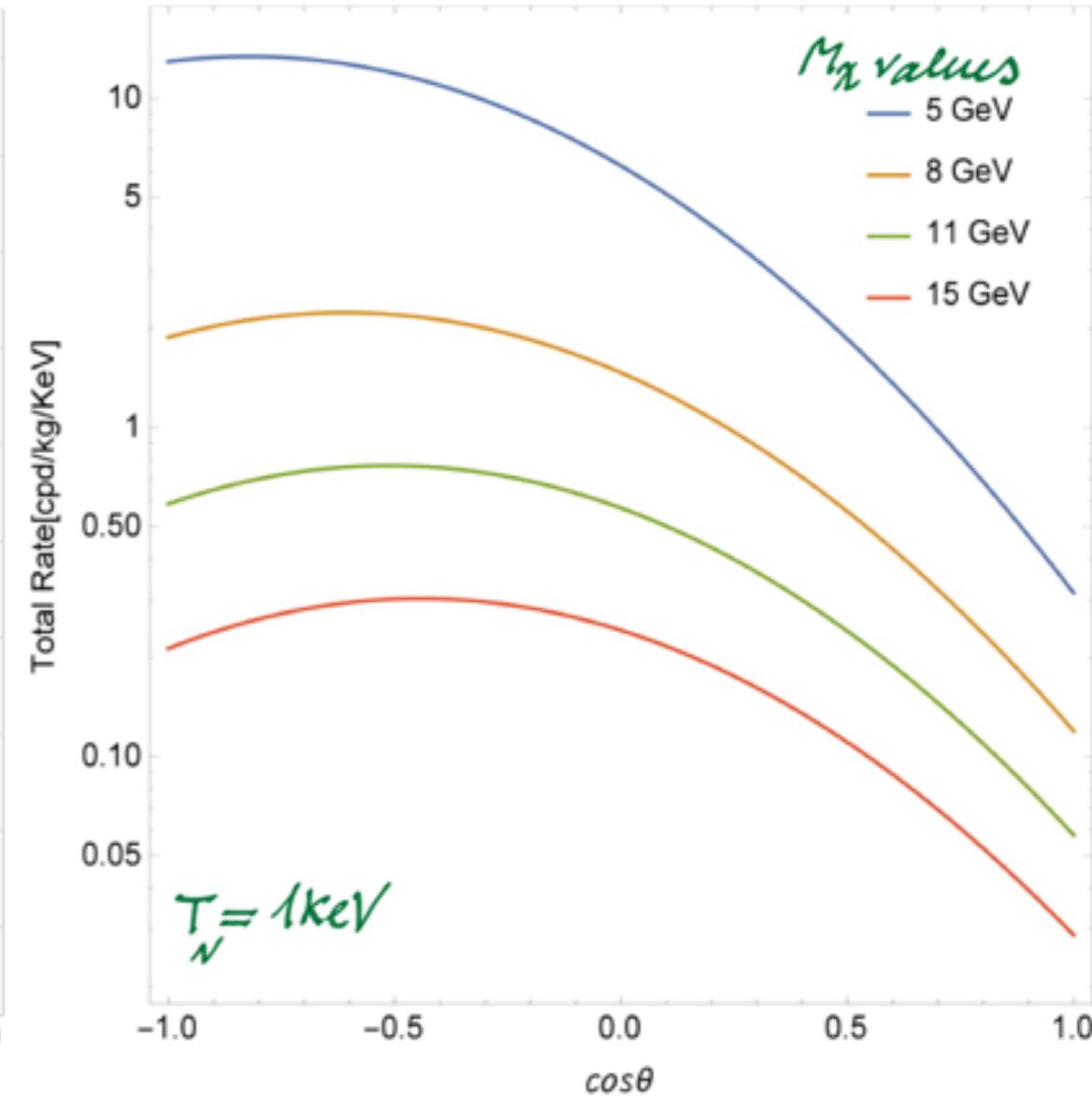
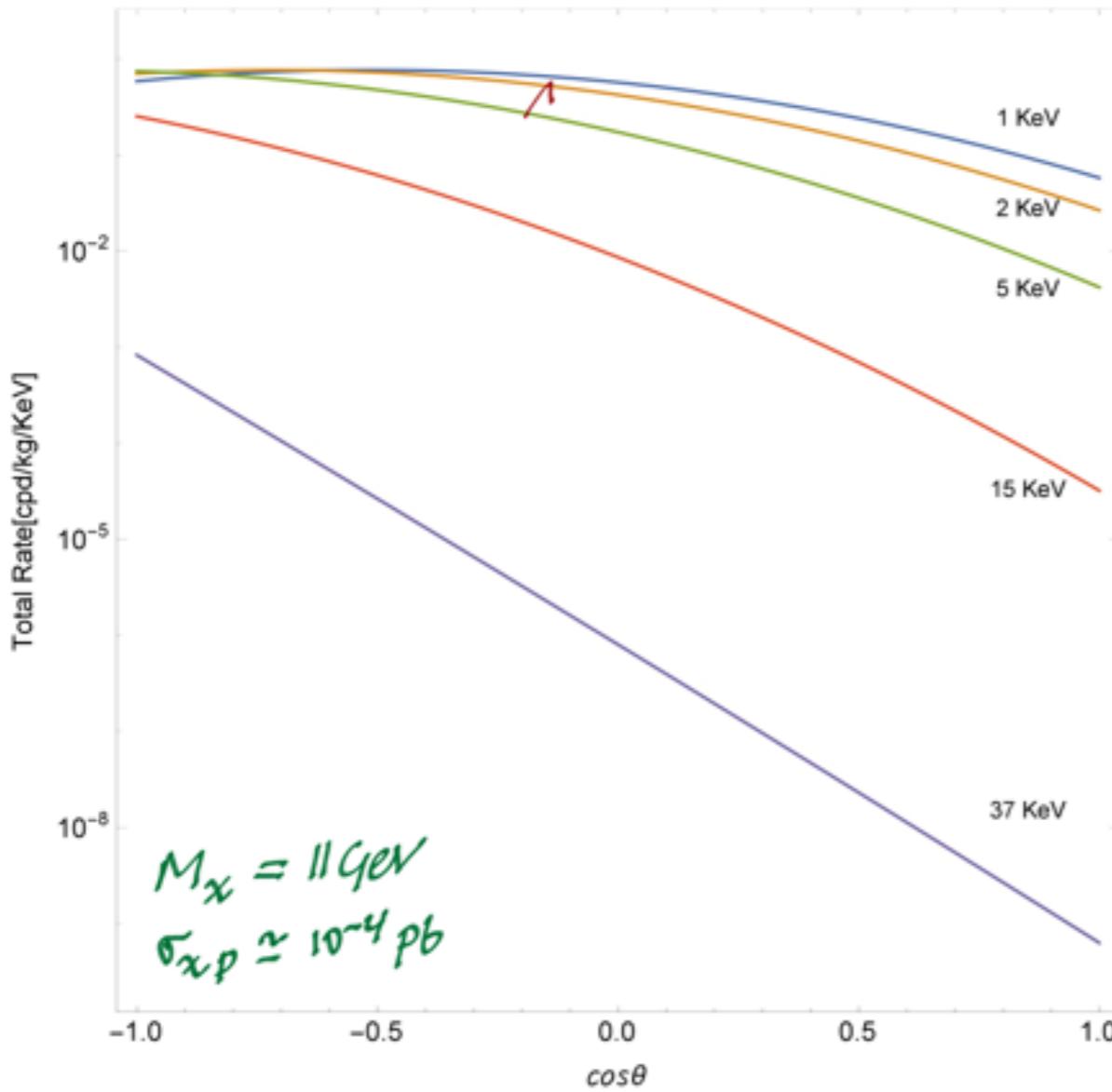
DAMA

$$\frac{d\Gamma}{dT} = A(T) + S(T) \cos(\omega t + \varphi_0)$$



$$\frac{d\Gamma}{dT} = \int d\cos\theta \frac{d\Gamma}{dT d\cos\theta} \rightarrow \text{Fano exp.}$$

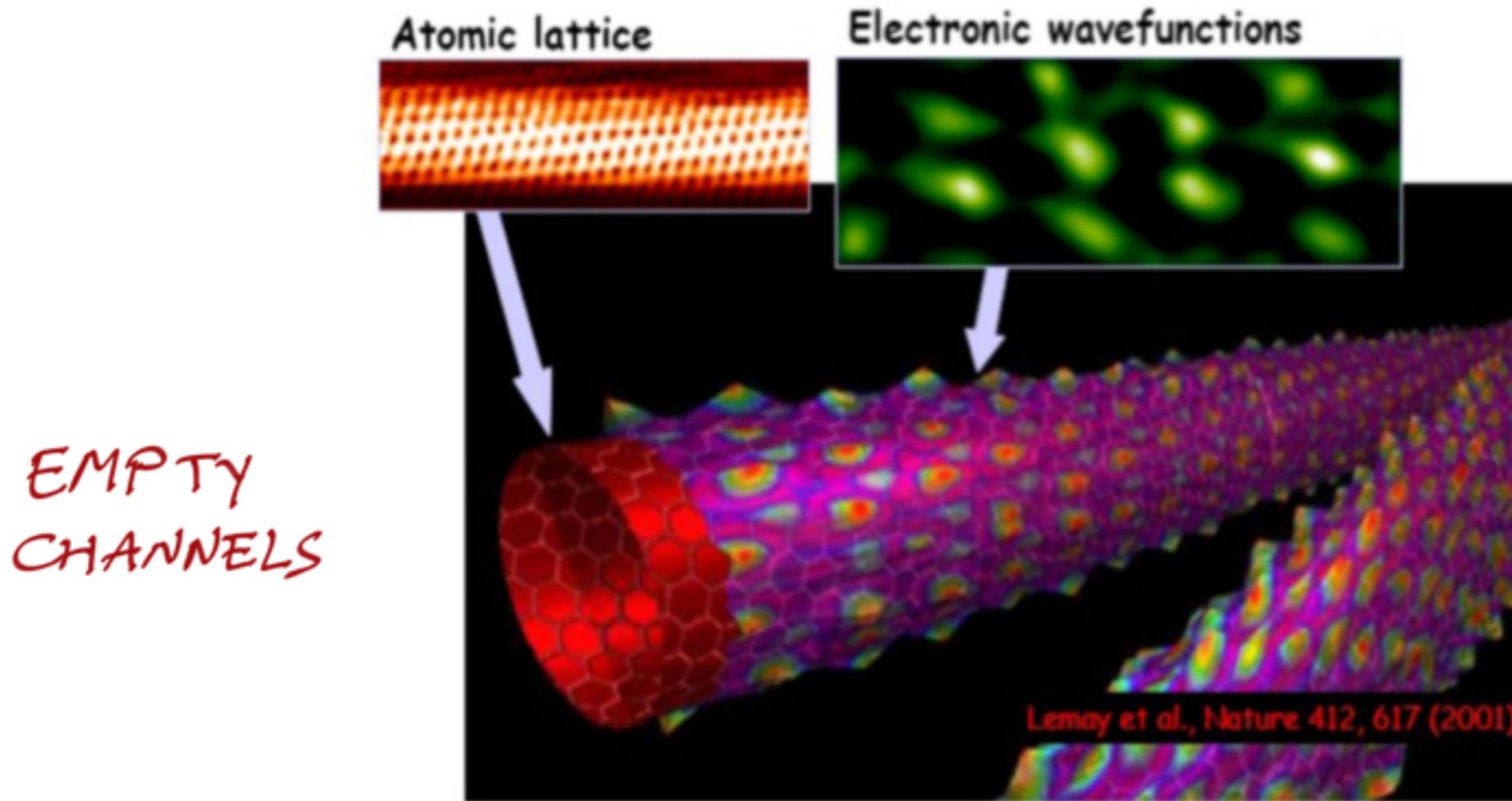
Nuclear Recoils



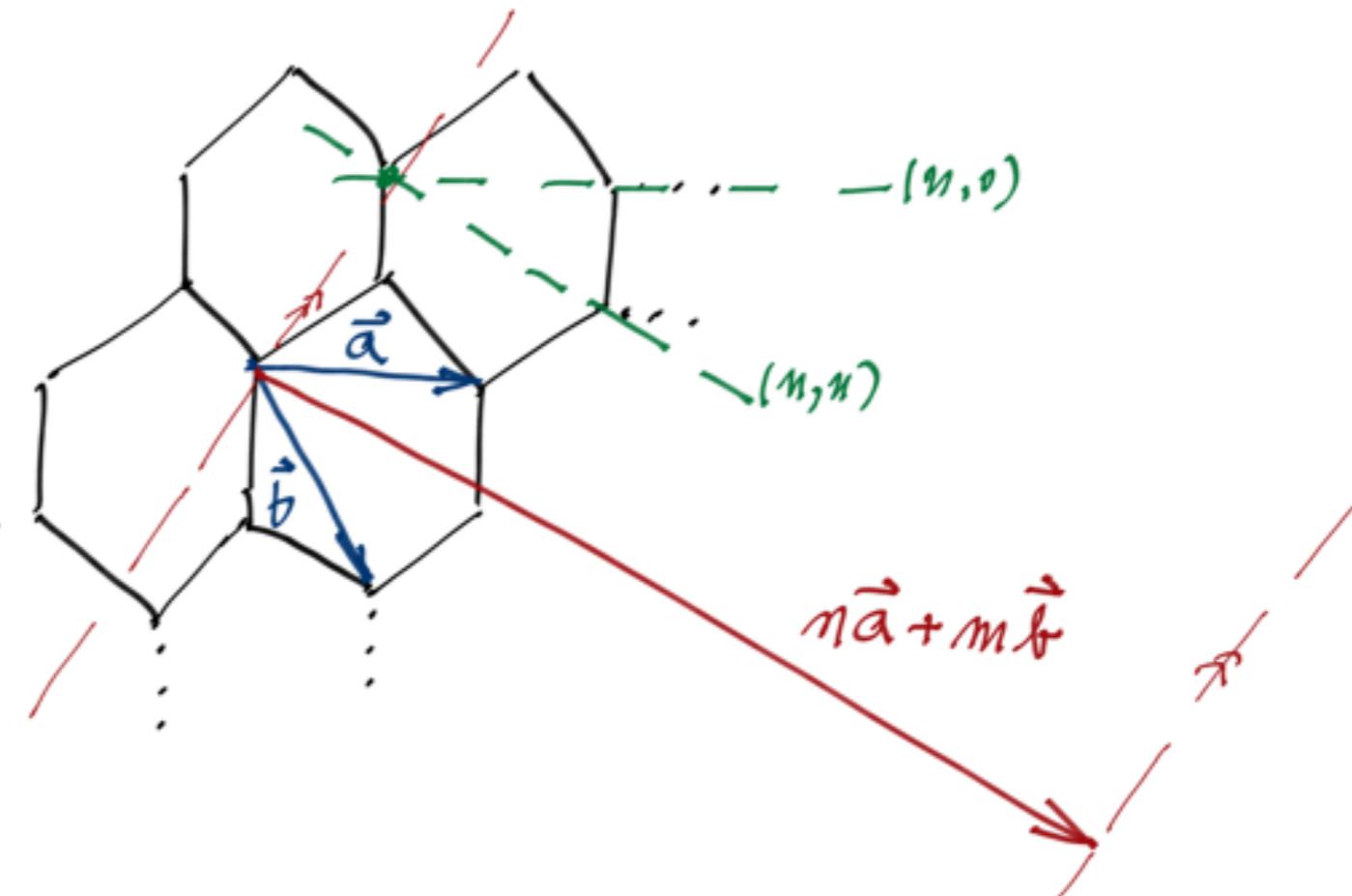
If T is increased, more countings with heavier wIMPs.

$$T_N^{\max} \underset{x \rightarrow 1}{\sim} T_\chi$$

CNT Target



CNT Target



$l \approx 0.14 \text{ nm}$ (bond length)

$$|\vec{a}| = |\vec{b}| = l\sqrt{3}$$

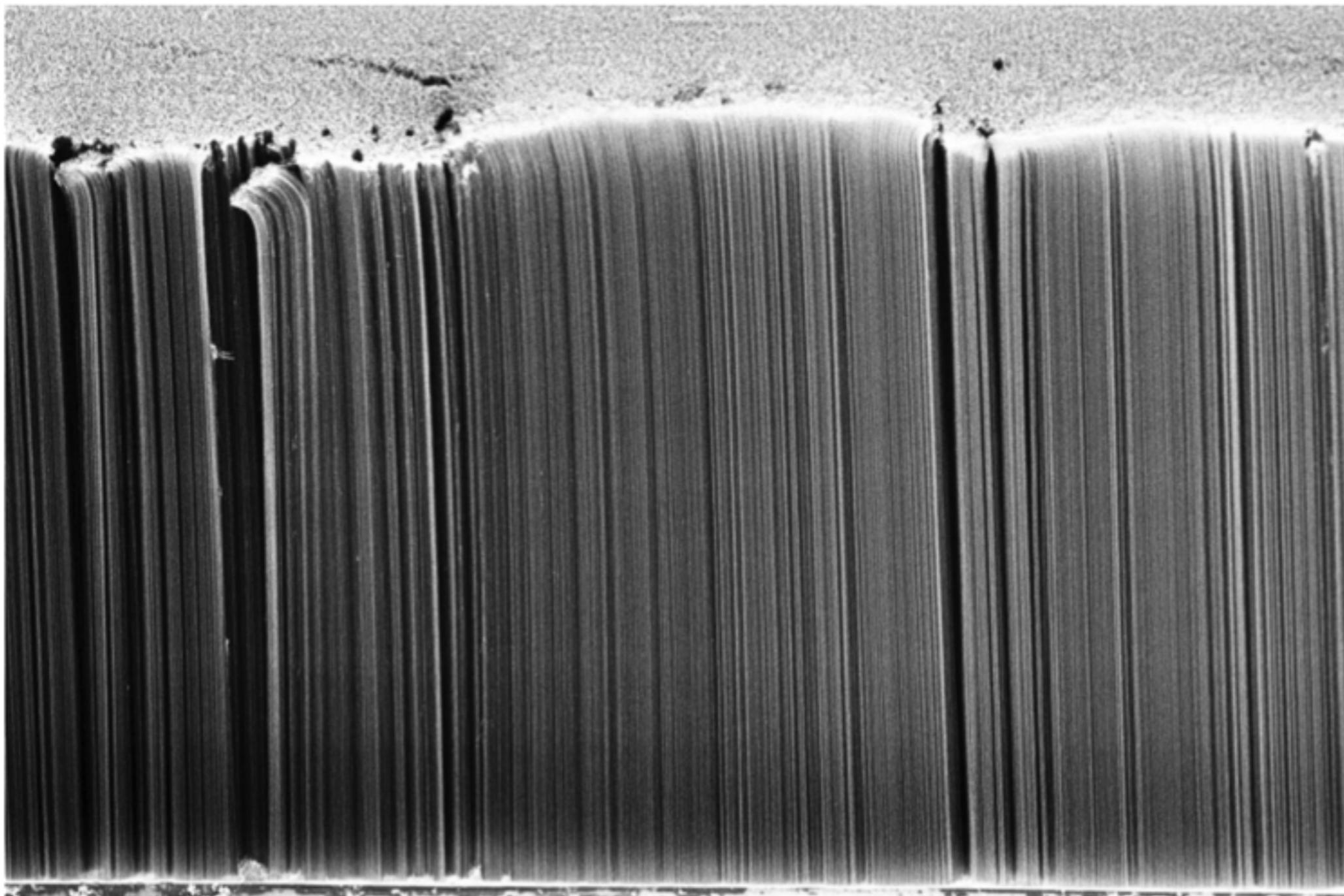
$$R_{CNT} = \frac{l\sqrt{3}}{2\pi} \sqrt{n^2 + nm + m^2}$$

(n, n) "HARMCHAIR" - METALLIC

(n, m) with $(n-m)$ multiple of 3 - SEMICONDUCT.

$(n, 0)$ "ZIG-ZAG"

CNTs



20 μm

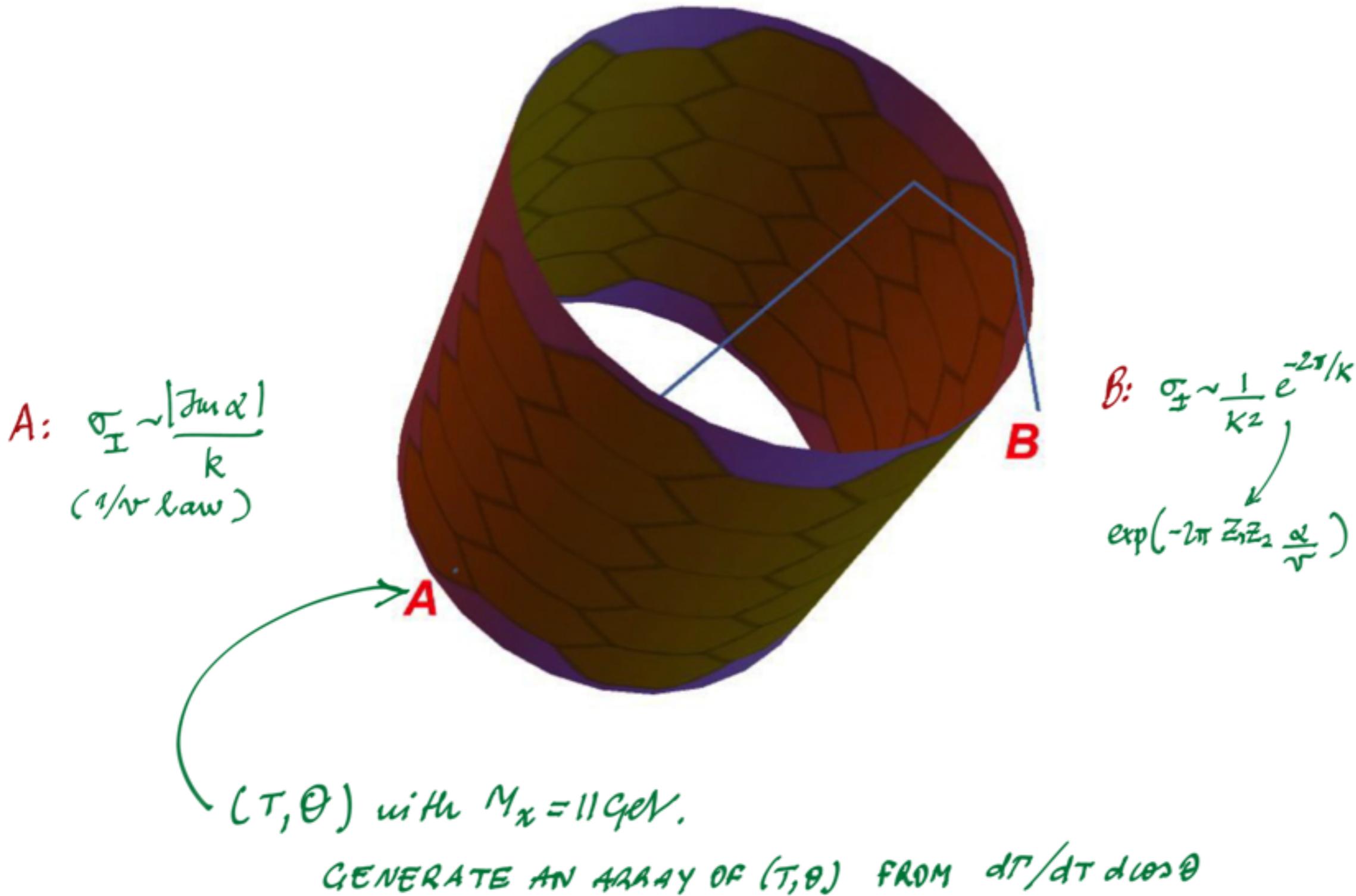
EHT = 8.00 kV
WD = 7.0 mm

Signal A = InLens
Mag = 800 X

Date :28 May 2015
Sample ID =

CNS

CNT Target



Extraction of a C ion

$$C = C \quad 145 \text{ Kcal/mol}$$

$$C - C \quad 85 \text{ Kcal/mol}$$

The extraction price of one C atom $\approx 20 \text{ eV}$

The ionization $C \rightarrow C^{4+}$ costs $\sim 147 \text{ eV}$

C^{5+} " $\sim 539 \text{ eV}$

C^{6+} " $\sim 1029 \text{ eV}$

$M_\chi (\text{GeV})$	$T (\text{keV})$	$T_n^{\max} (\text{keV})$
50	[25, 172]	[15, 109]
100	[50, 354]	[20, 135]
:		

CNT POTENTIALS

Effective potential in the transverse plane

$$U(r, \varphi) = U_0(r) + 2 \sum_{s=1}^{\infty} U_{SN}(r) \cos\left(\frac{\pi s(n+m)}{q}\right) \cos\left(sN\varphi + \frac{\pi s(n+m)}{q}\right)$$

$$= \sum_{\text{chains}} \bar{U}\left(\begin{array}{c} \text{---} \\ \text{---} \end{array}\right) - \text{each } \bar{U} \text{ as a Fourier series of azimuthal harmonics}$$

$$q = \gcd(2m+n, 2n+m)$$

$$N = \frac{2}{q} (n^2 + mn + m^2) \quad \#/\text{2 of rows parallel to the axis}$$

$$U_V(r) = 4\sqrt{\pi} \sigma \sum_j Z^2 e^2 \left(\frac{R}{r}\right)^{1/2} \sum_{j=1}^4 a_j b_j e^{-b_j^2 (r^2 + R^2)} \times$$

$$\times e^{2b_j^2 r R \left[\sqrt{1+g^2} - \xi \ln(\beta + \sqrt{1+\beta^2}) \right]}$$

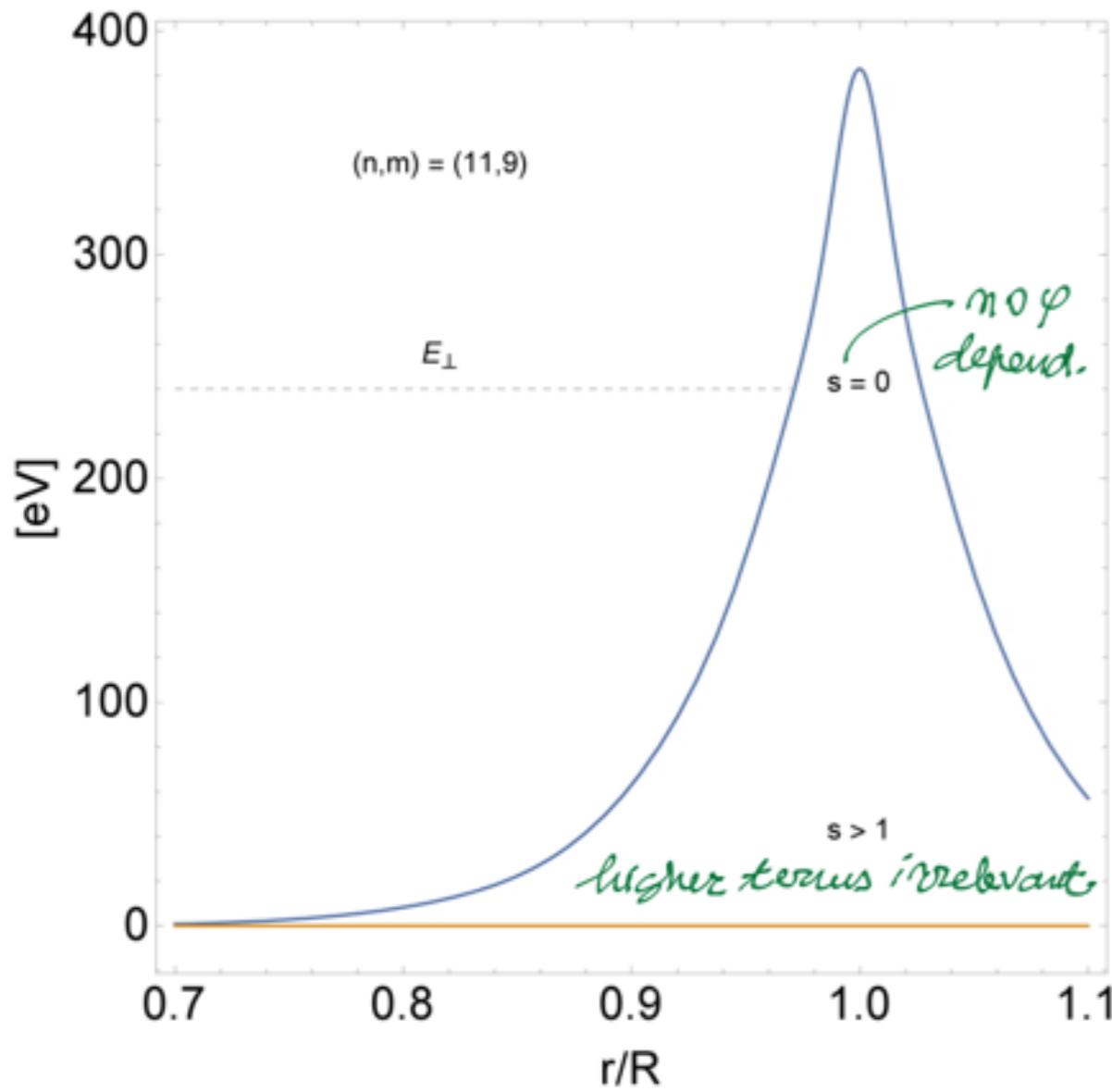
$$\xi = v / 2b_j^2 r R$$

$$\sigma = 4/e^2 s$$

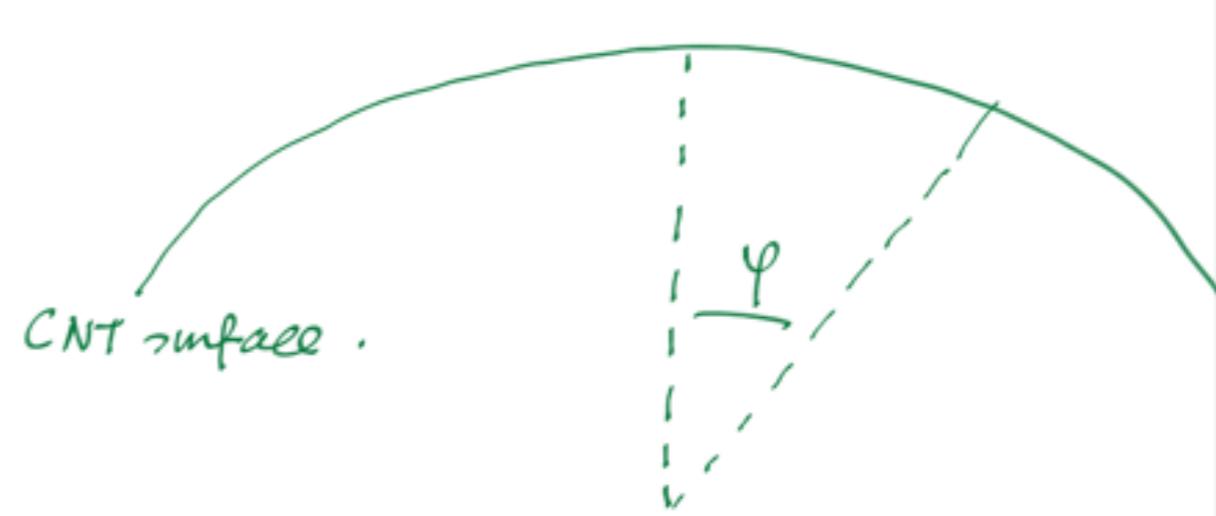
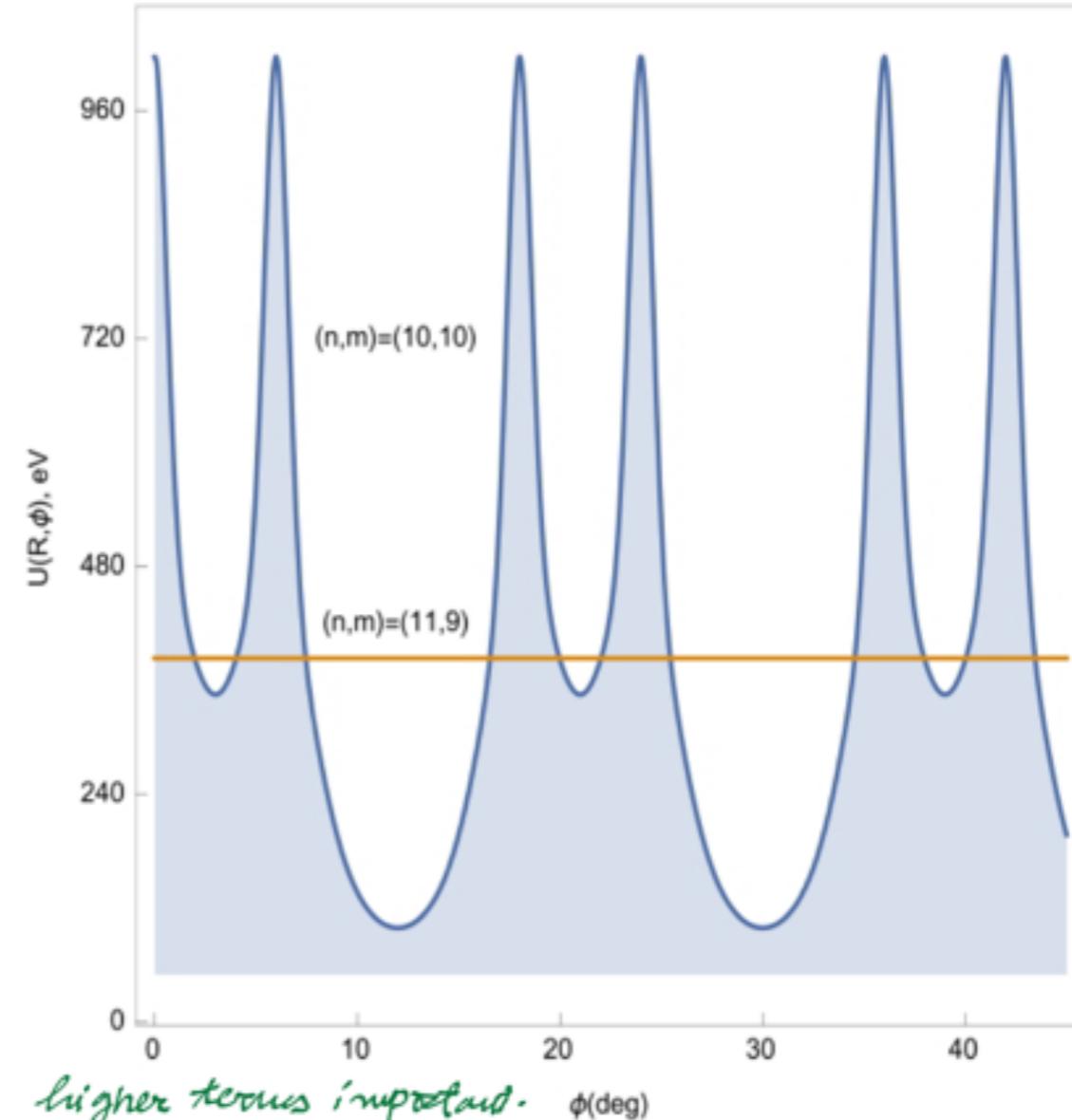
a_j [nm^2], b_j [nm^{-1}] reported in

ARTRU et al. Phys. Rept. 412, 59 (2005)

CNT POTENTIALS

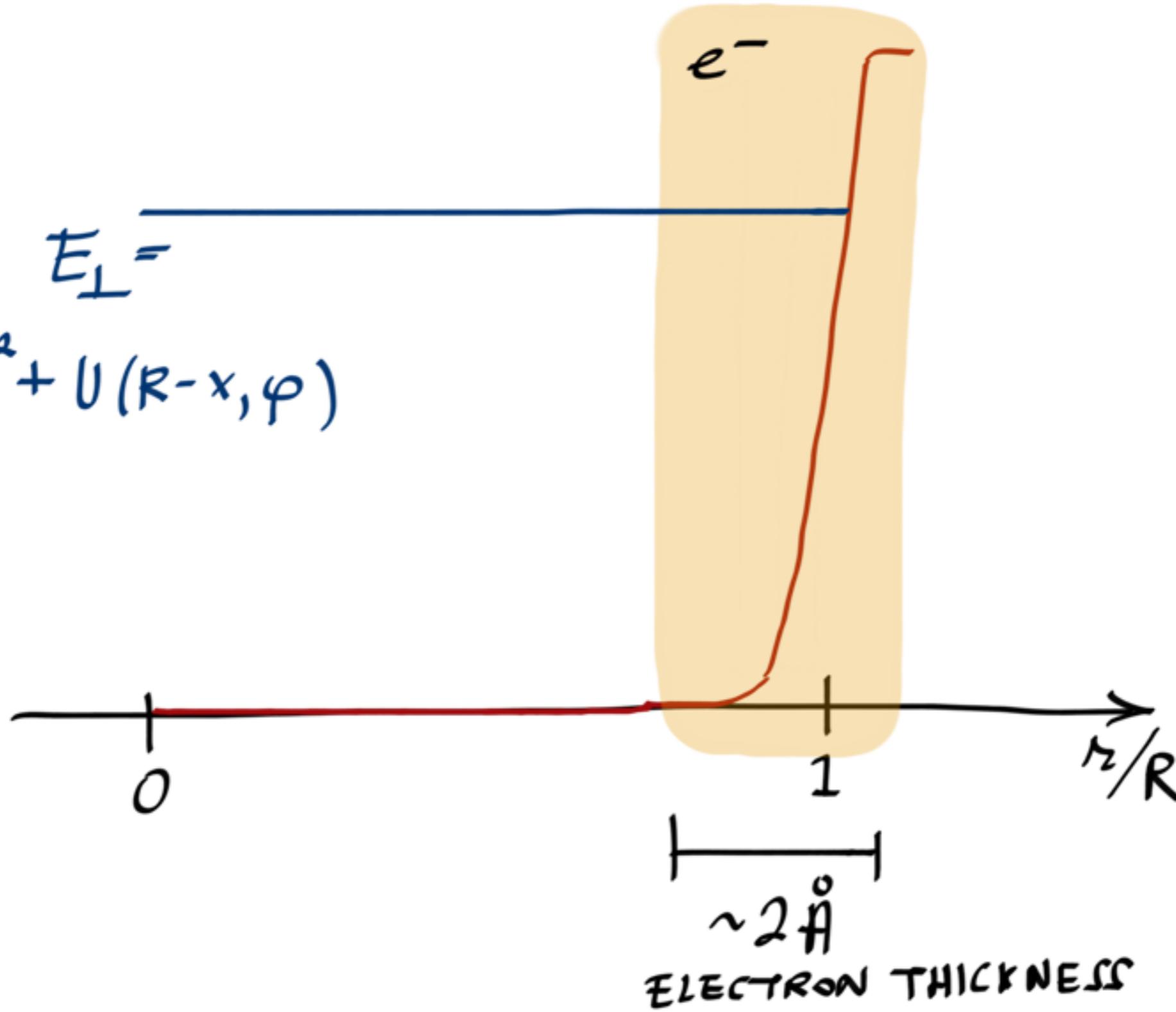


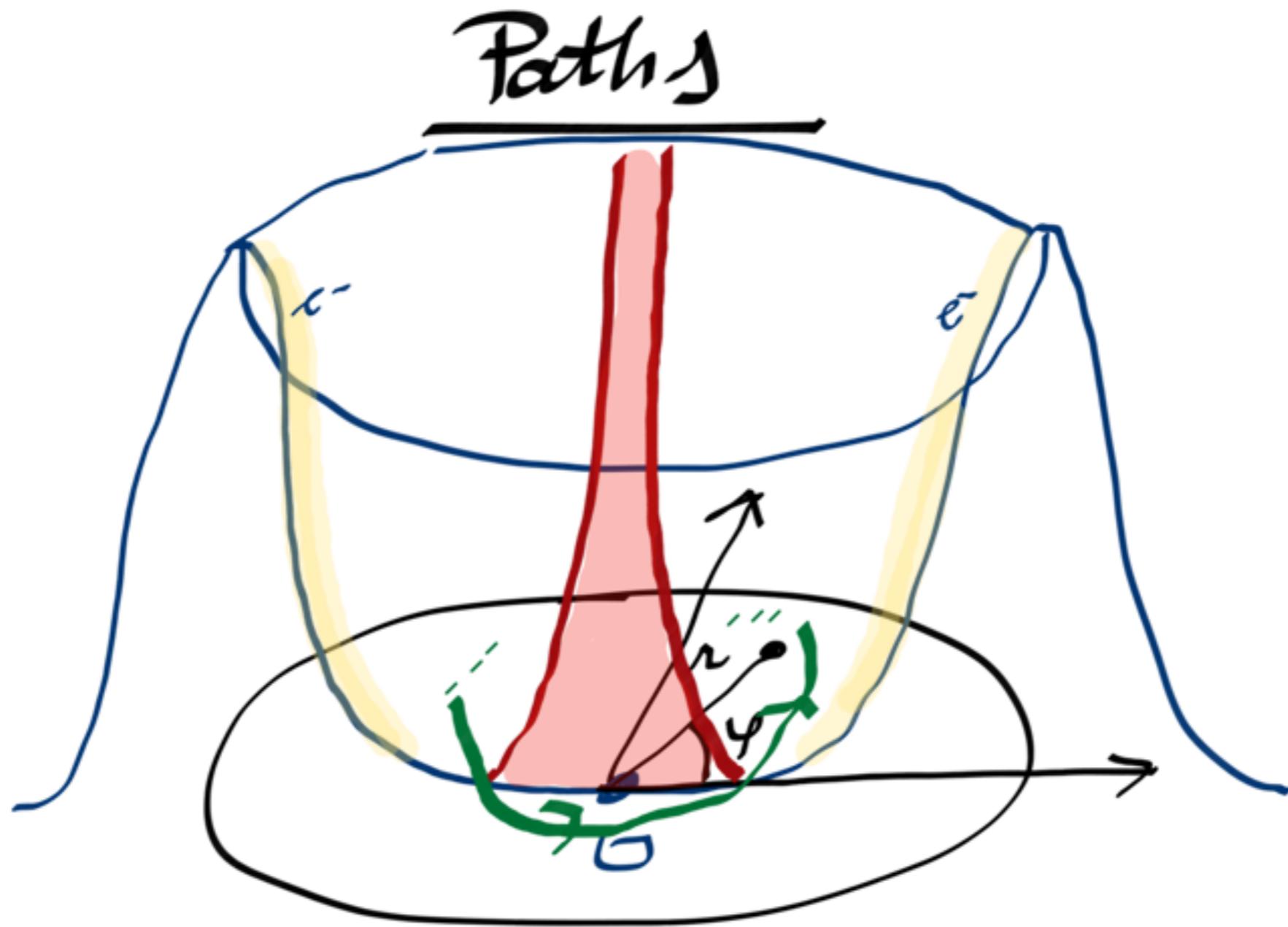
(For a C^{6+})



CHANNELS

$$E_T = \\ = T\theta^2 + U(R-x, \varphi)$$





If $L = mr^2\dot{\varphi}$ is conserved, φ changes monotonically along the path in $V \sim V(r) + L^2/2mr^2$.

Smaller values of L push closer to the boundaries (where ζ are)
 \rightarrow more frequent "dechannelings" or "dead events"

Channelling conditions

$$E_{\perp} = T \theta^2 + U(R-x, \phi) \lesssim \min_{\phi} U(R, \phi)$$

$\Rightarrow x_{\min}$

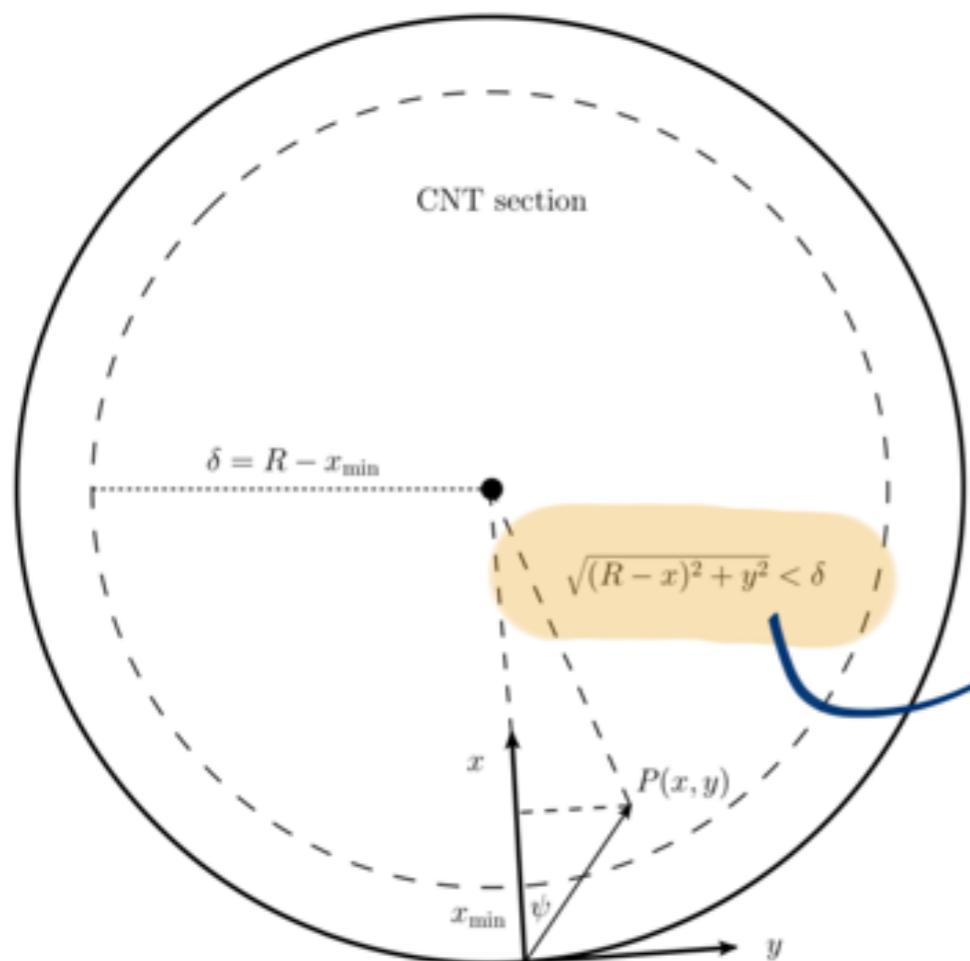
$$W(T, \theta) = \int \frac{e^{-x^2/2U_{\perp}(T^*)}}{\sqrt{2\pi} U_{\perp}(T^*)} \frac{e^{-y^2/2U_{\parallel}}} {\sqrt{2\pi} U_{\parallel}}$$

$x, y \in \mathbb{R}$

→ defines R

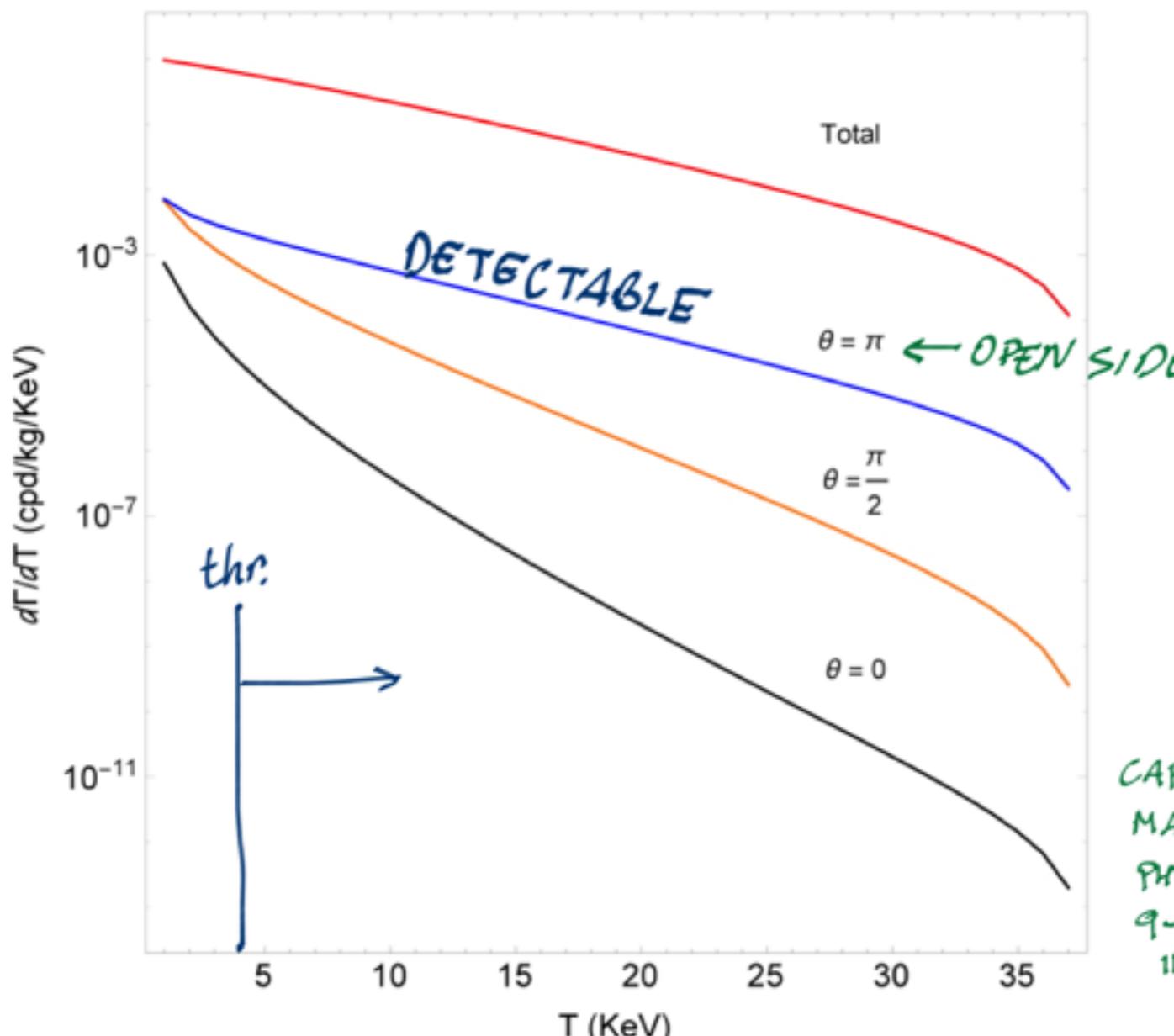
$$\left. \begin{array}{l} U_{\perp} = 0.0085 \text{ nm} \\ U_{\parallel} = 0.0035 \text{ nm} \end{array} \right\} @ \text{room } T^*$$

From Debye theory.



A. B. Gelmini
1201.4560

Channulings

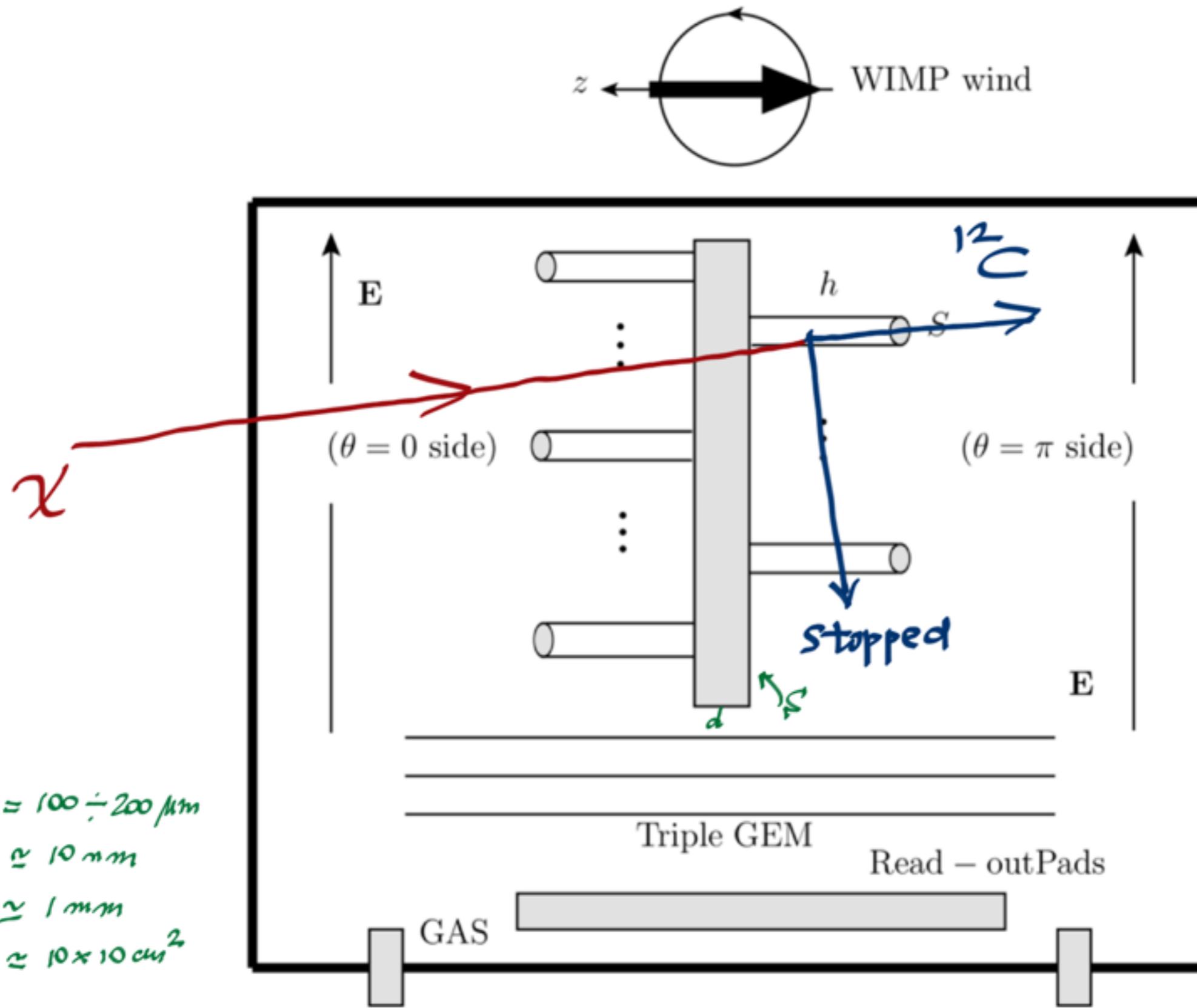


CAPPARELLI, CAVOTO
MAZZILLI, POMOSA
PHYS. DARK- UNIV.
9-10 (2015) 24
11 (2016) 79

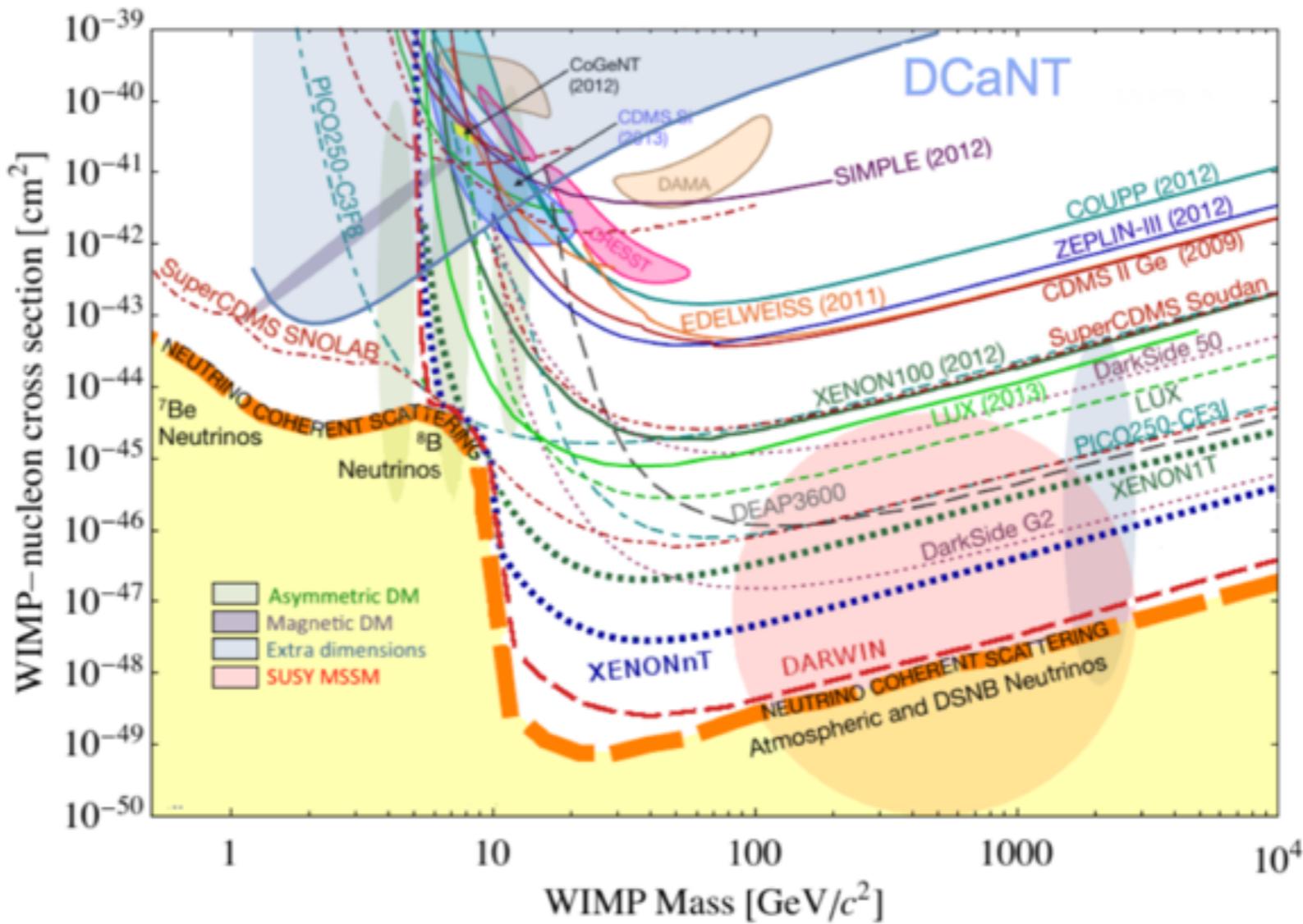
$$(n, m) = (73, 71)$$

HISTOGRAM OF THE CHANNELED EVENTS UNDER
THE VERY RESTRICTIVE CONDITIONS MENTIONED
BEFORE - RECHANNELINGS OR INTER-CNT
TRAPPING NOT INCLUDED HERE

DIRECTIONAL DETECTOR

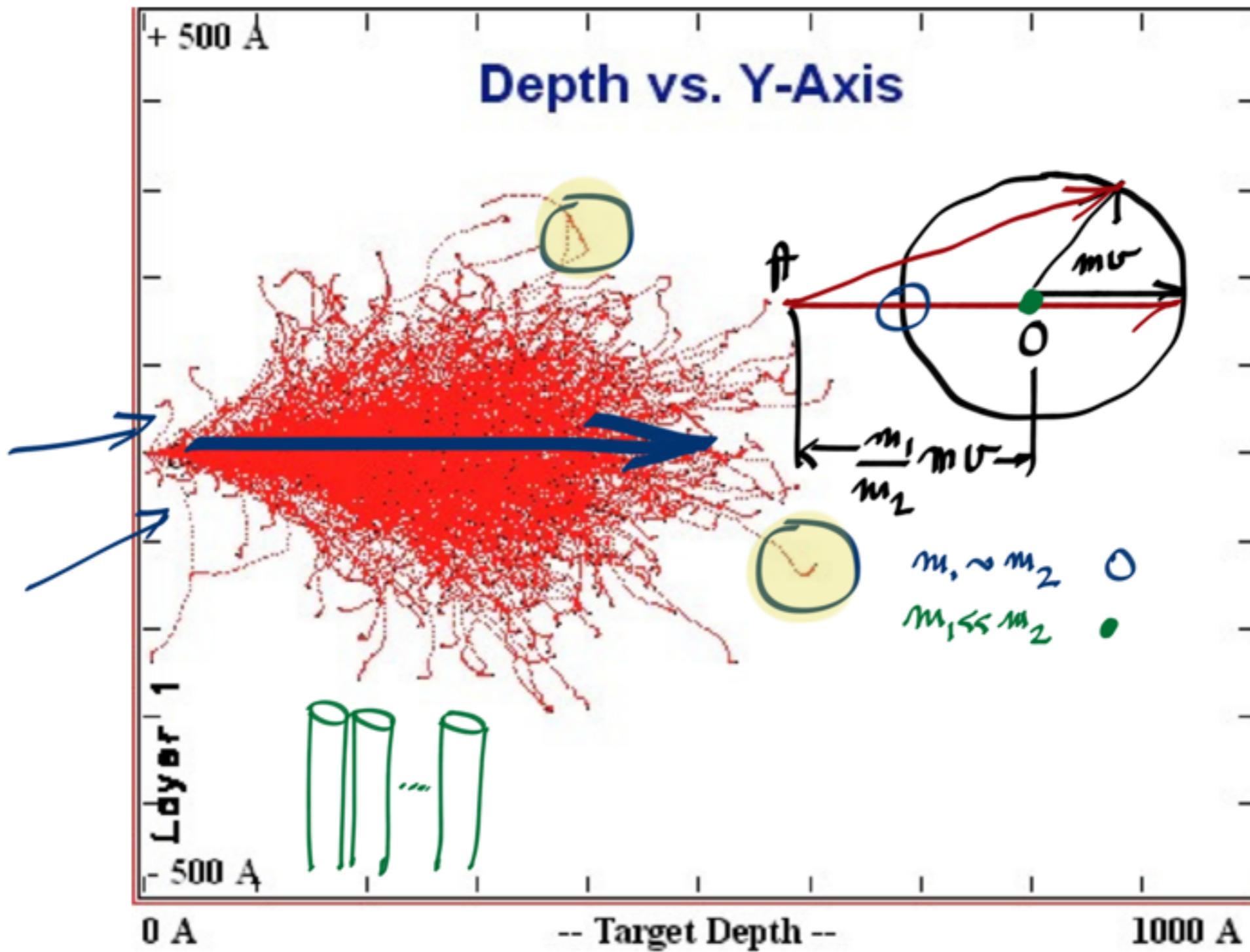


Sensitivity



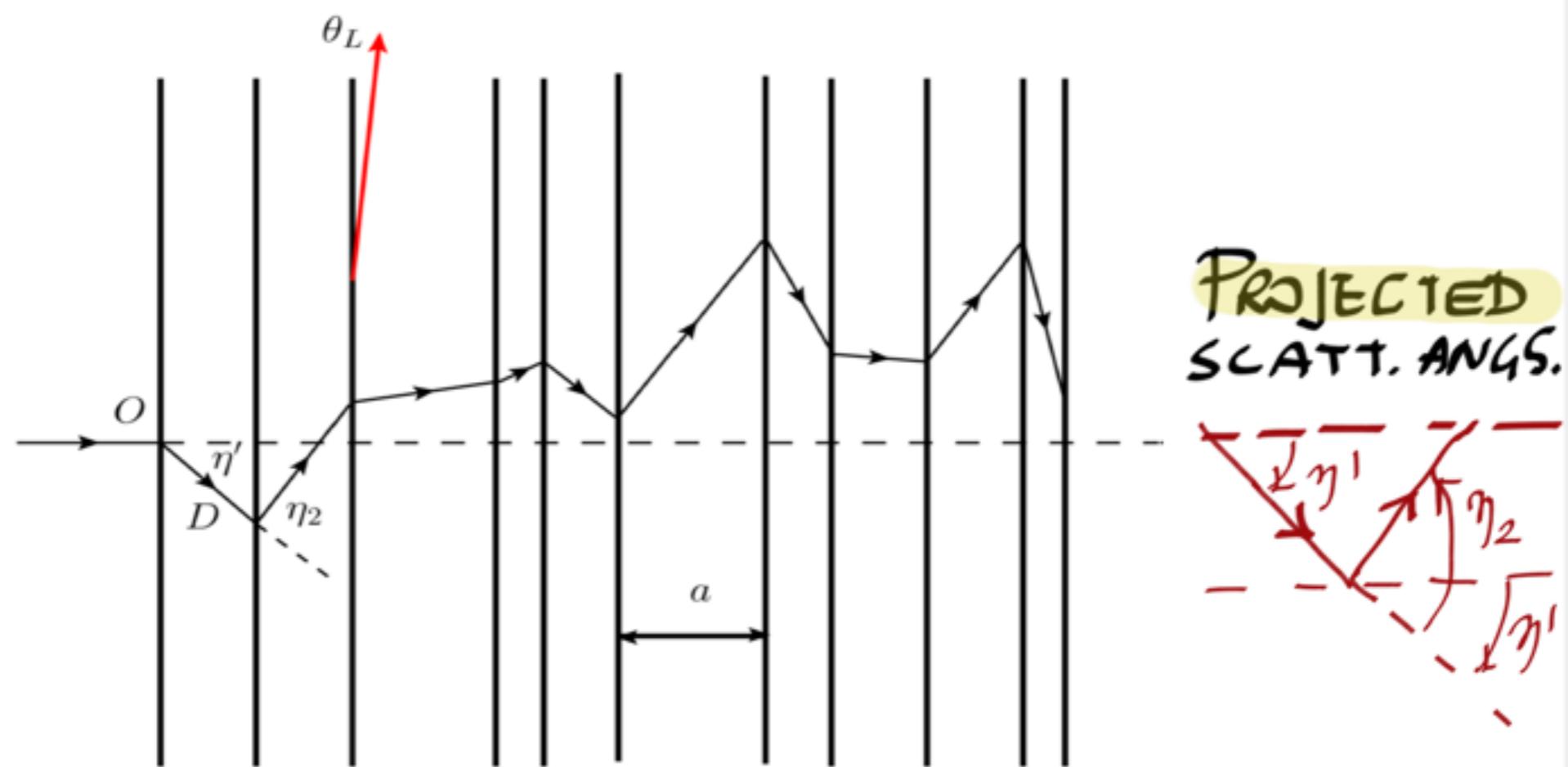
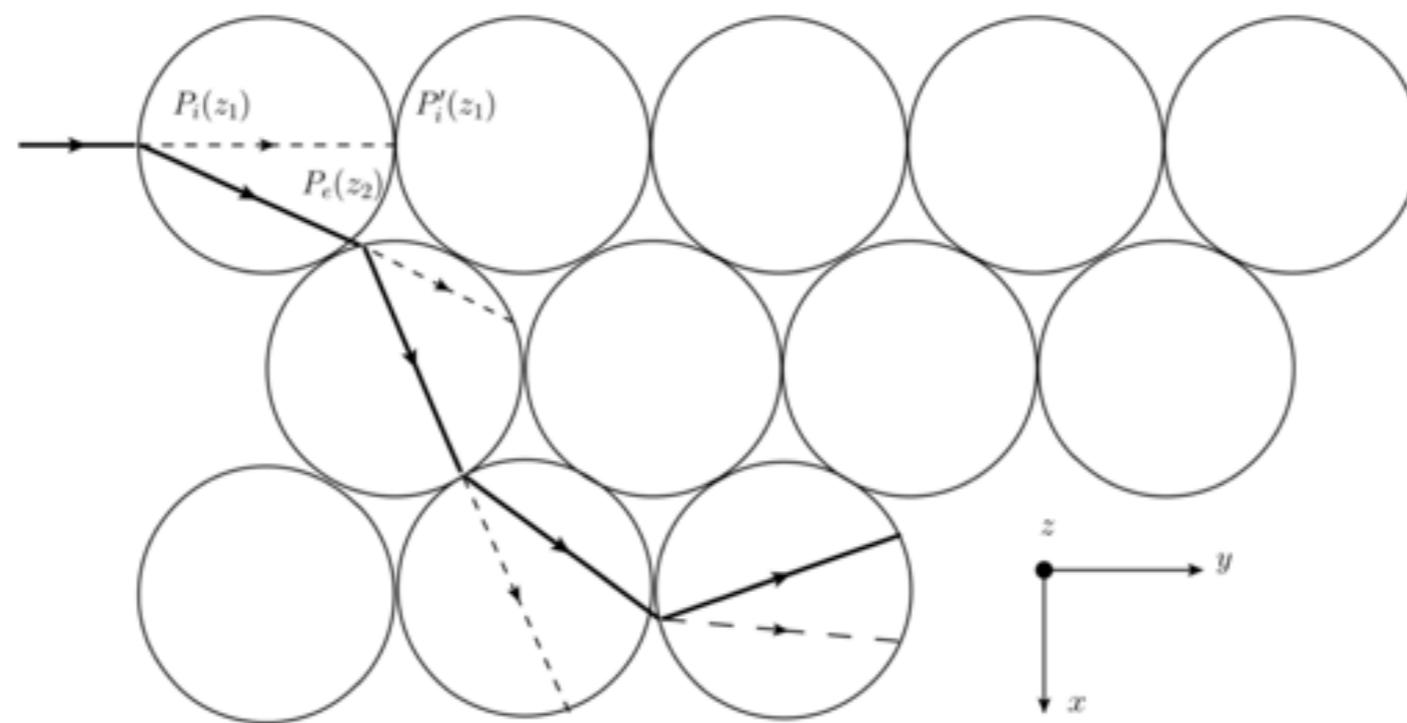
- 100 layers, 1m^2 each
- Compact readout \rightarrow few m^3 volume
- Rotated tracking CRYGNUS
- Sensitivity for 0.4 Kg y
(CNT trapping C ions detected down to 1 keV)

RE-CHANNELINGS

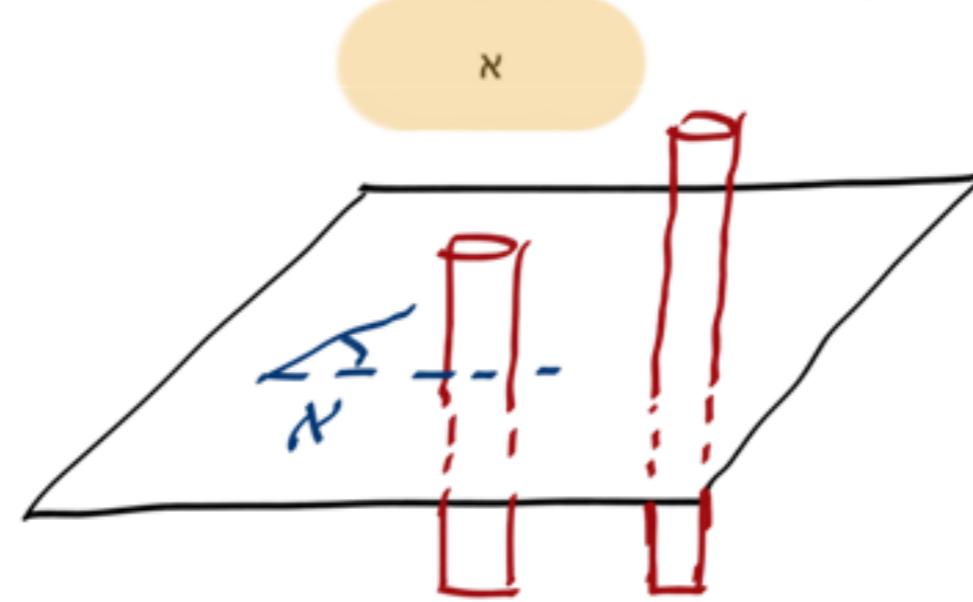
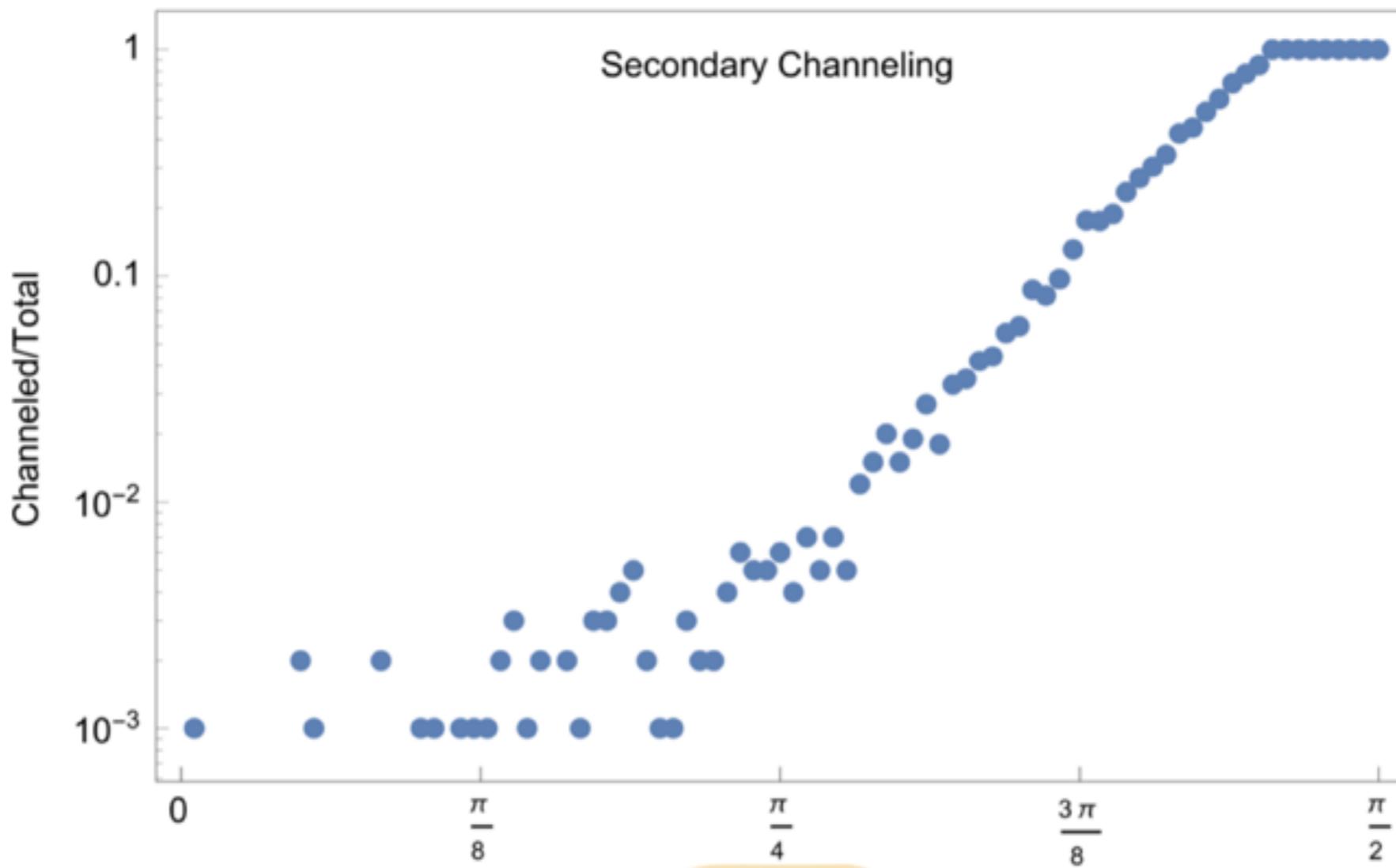


θ_s from dist. $\cos\theta_s/\sin^3\theta_s$ ($m_1 \sim m_2$)

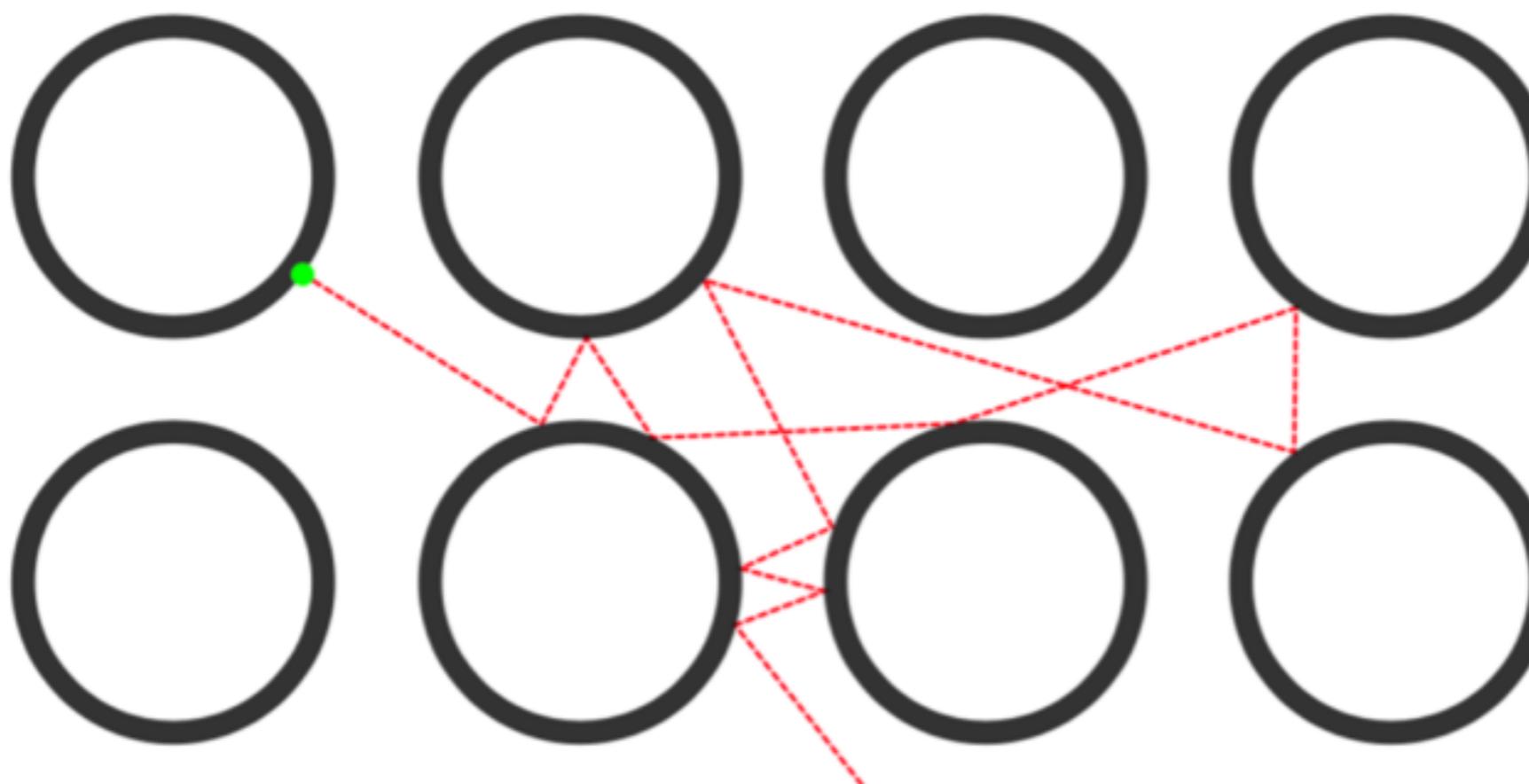
RE-CHANNELINGS



RE-CHANNELINGS

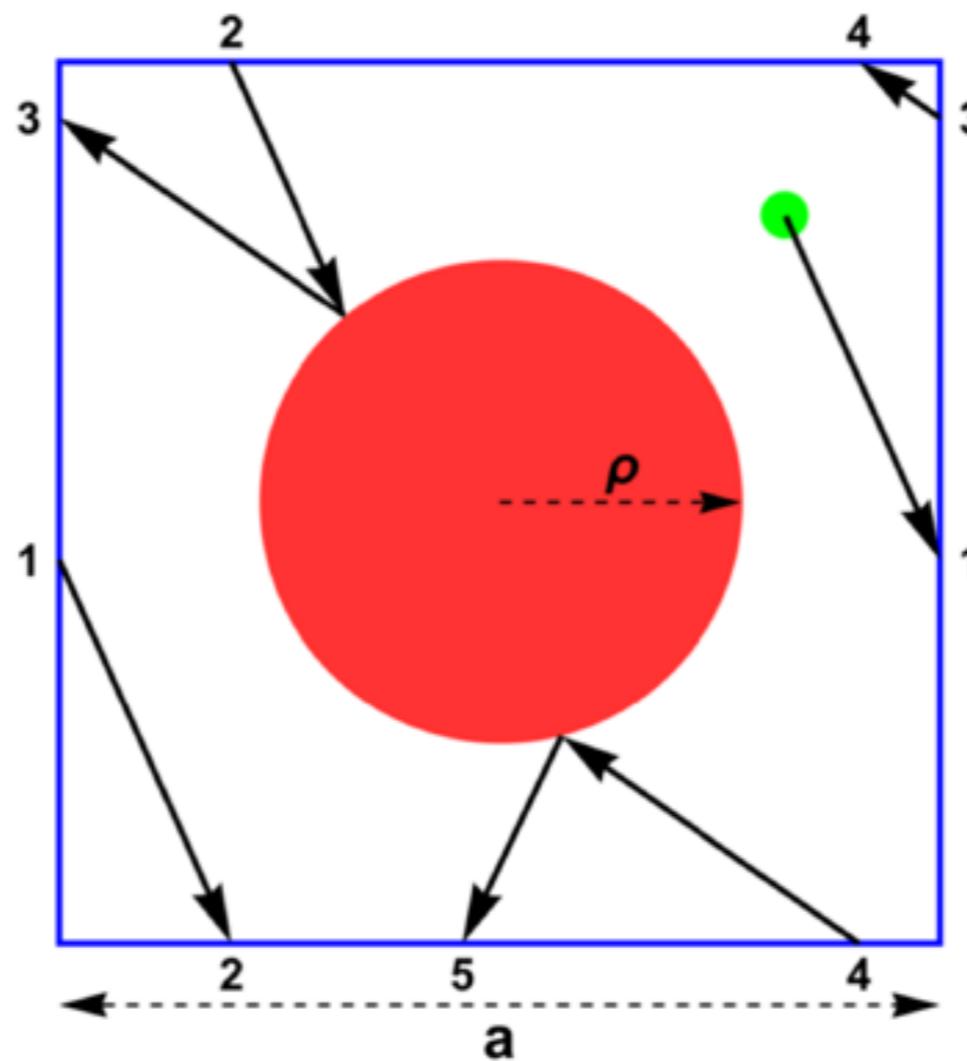


Billiards



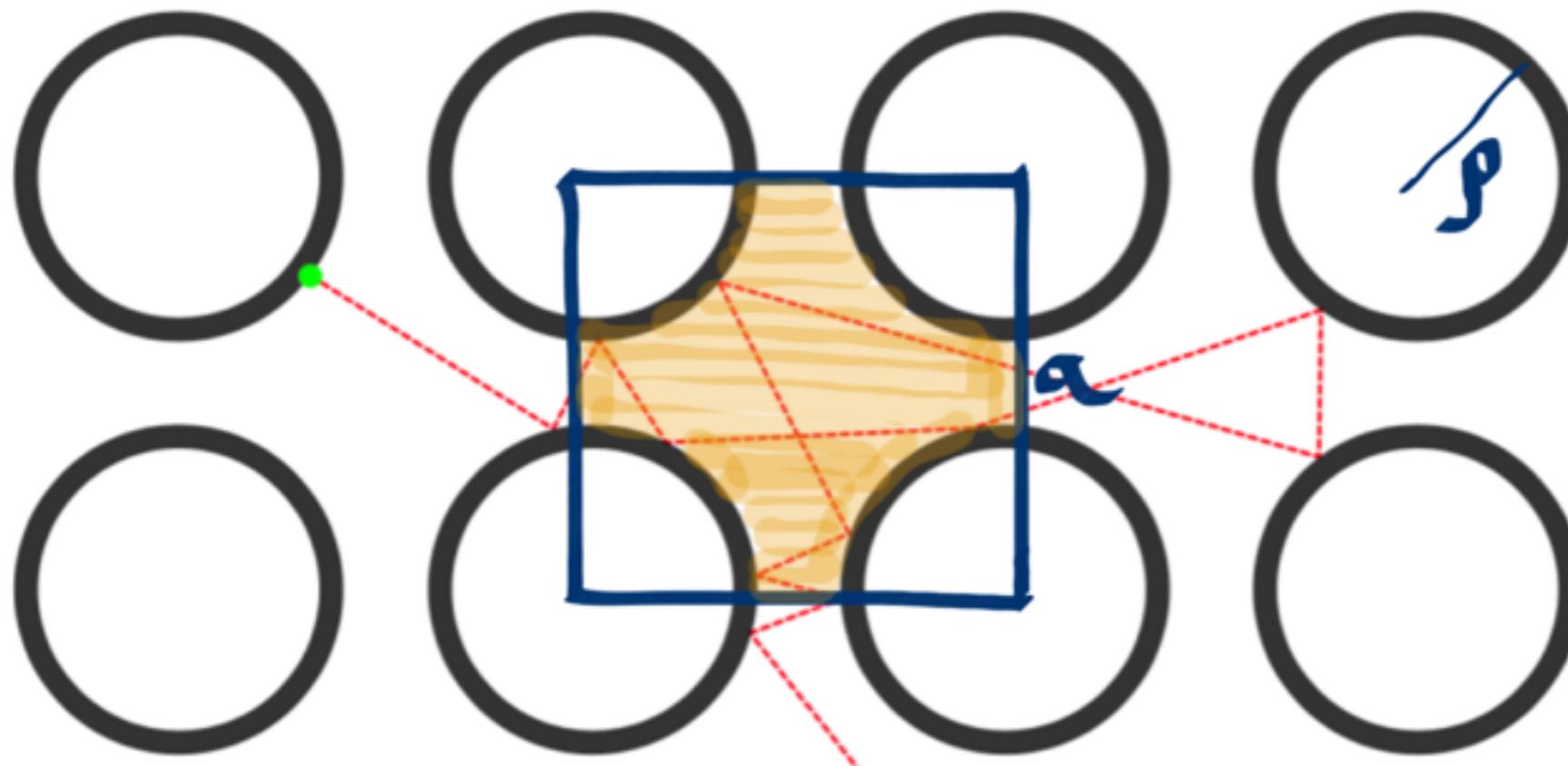
Billiards

Problem: a particle enters the CNT forest with $(v_{\parallel}, v_{\perp})$.
WILL IT REACH THE (OPEN) TOP OF THE FOREST BEFORE
EXITING FROM SIDES?



Billiards

$$\tau = n_{\text{hops}} \tau_R$$

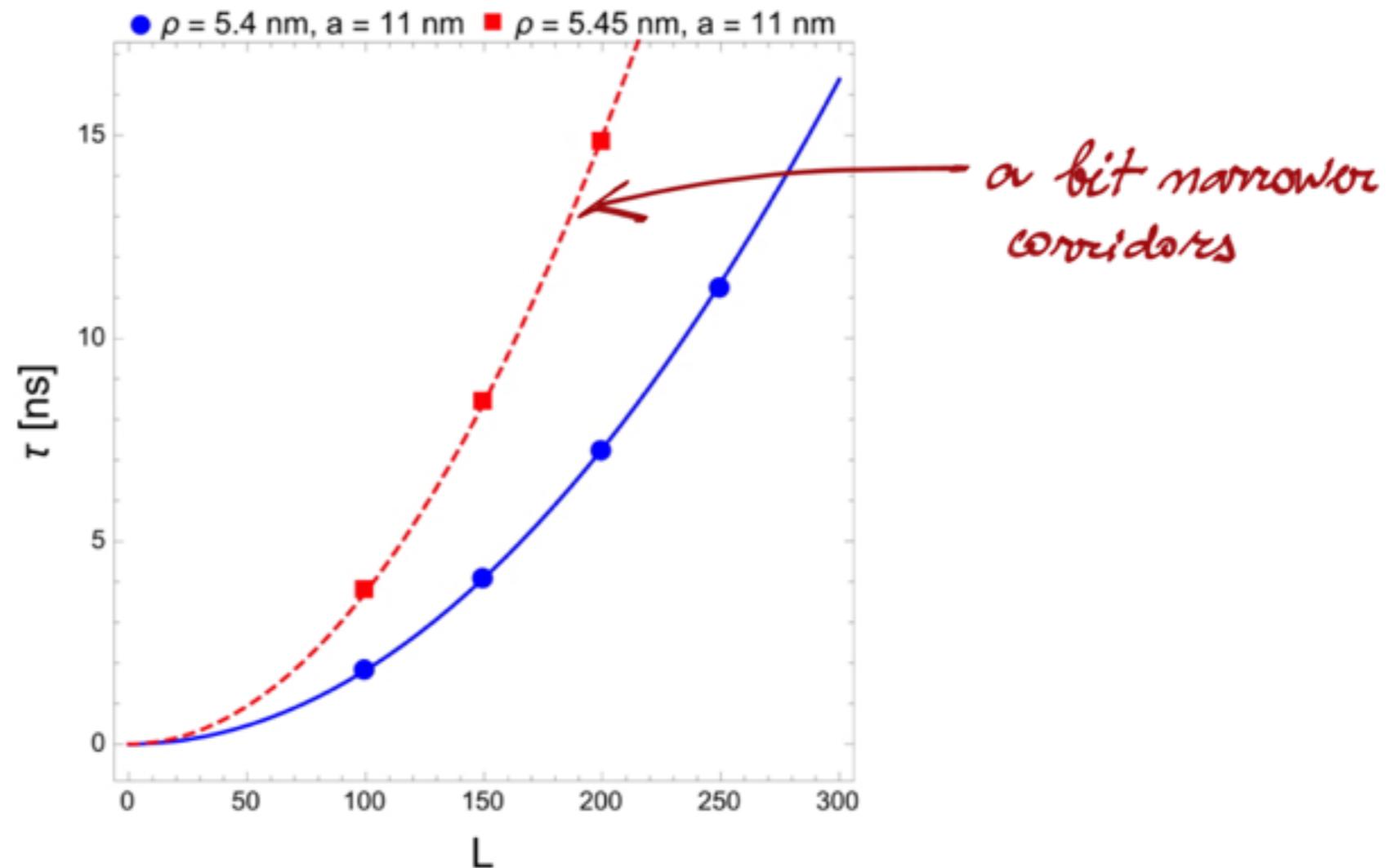


$$\delta = \alpha - 2\varphi$$

$\delta \ll \alpha = \text{NARROW CORRELATION REGIME}$

$$\tau_R = \frac{\pi(\alpha^2 - \pi p^2)}{4 v_L \delta}$$

Billiards



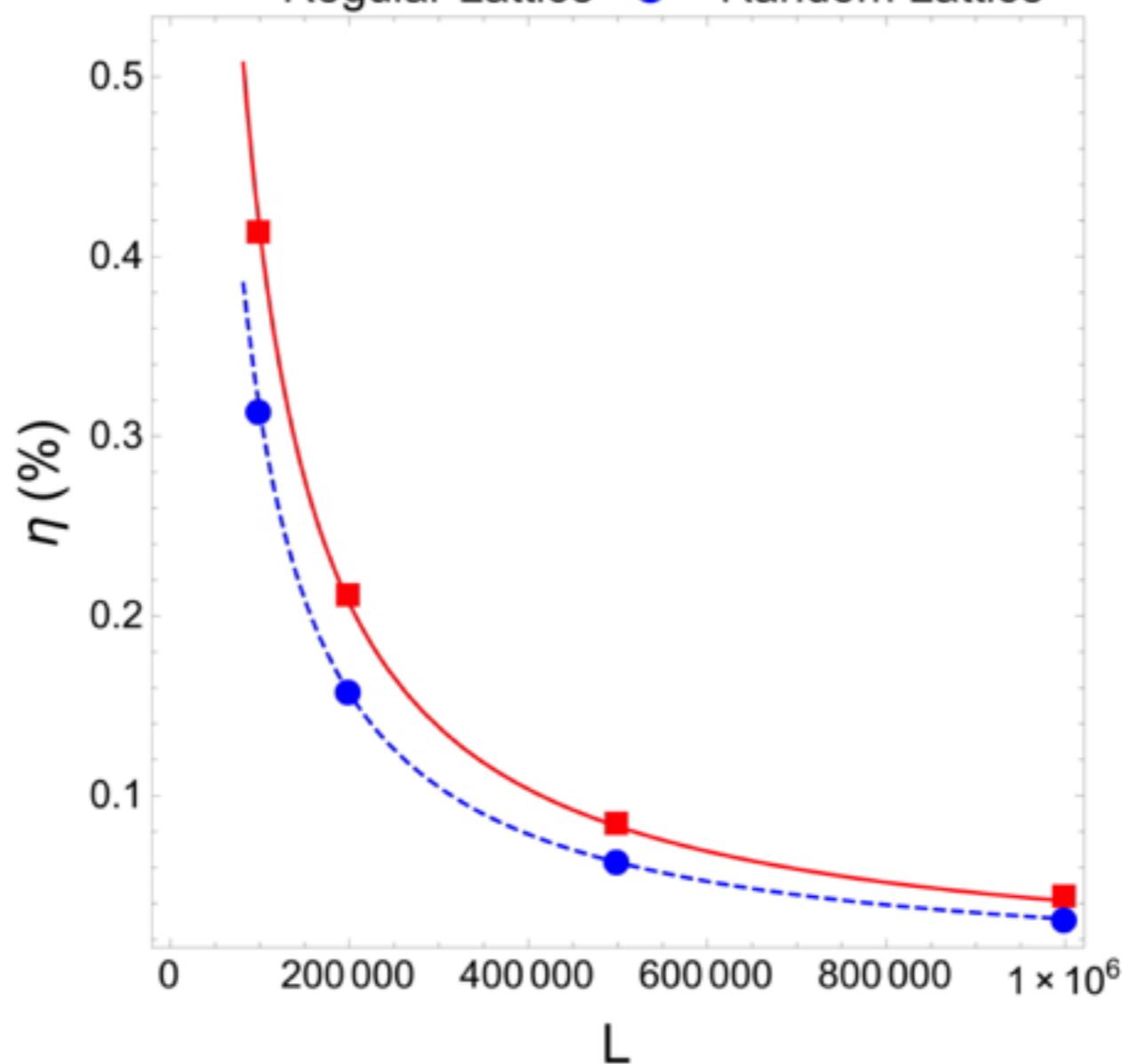
$$\text{find } n_h \approx \frac{L^2}{\pi} ; E_\perp \approx 300 \text{ eV}$$

τ = time needed to exit from the billiard.
MEAN EXIT TIME

Lateral losses

$E_{\parallel} = 1 \text{ keV}$, $E_{\perp} = 300 \text{ eV}$, $h = 300 \mu\text{m}$

■ = Regular Lattice ● = Random Lattice



γ = FRACTION OF PARTICLES LEAVING FROM SIDES
BEFORE REACHING THE TOP

$\gamma \sim L/L^2 \sim 1/L$ ($\approx 300 \div 400/L$)
TYPICAL $L > 10^5$

Energy losses

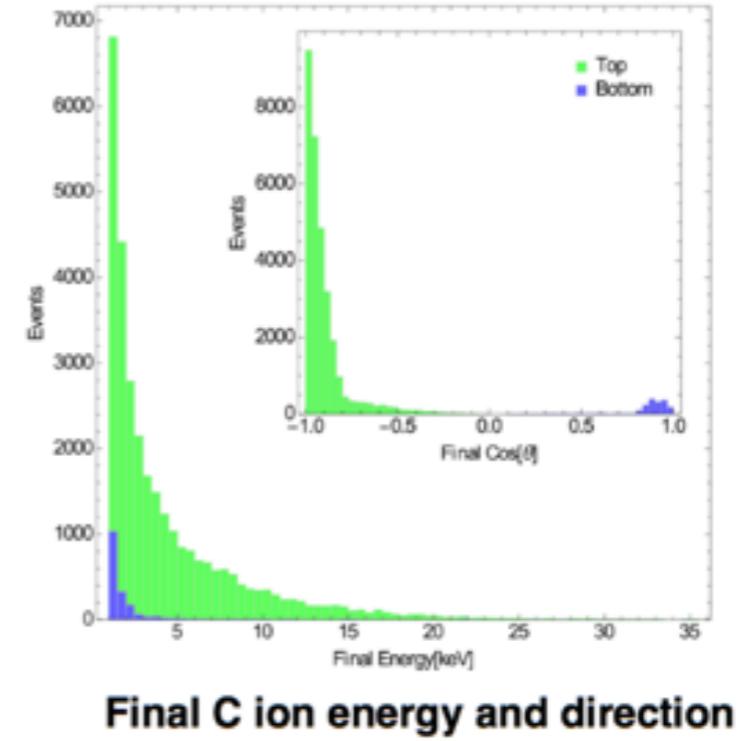
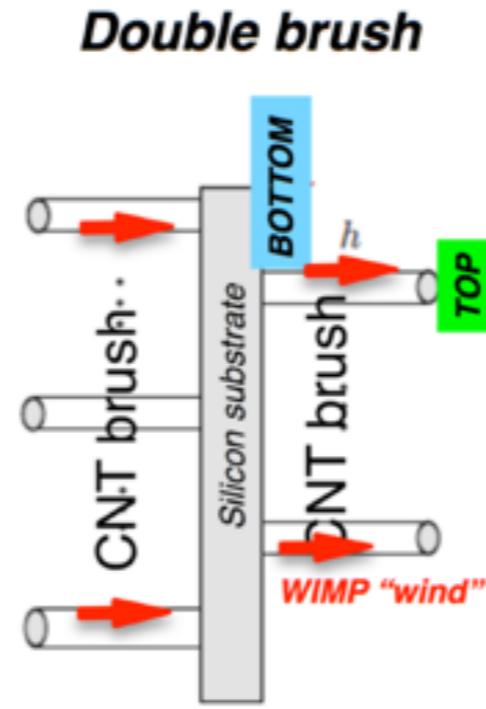
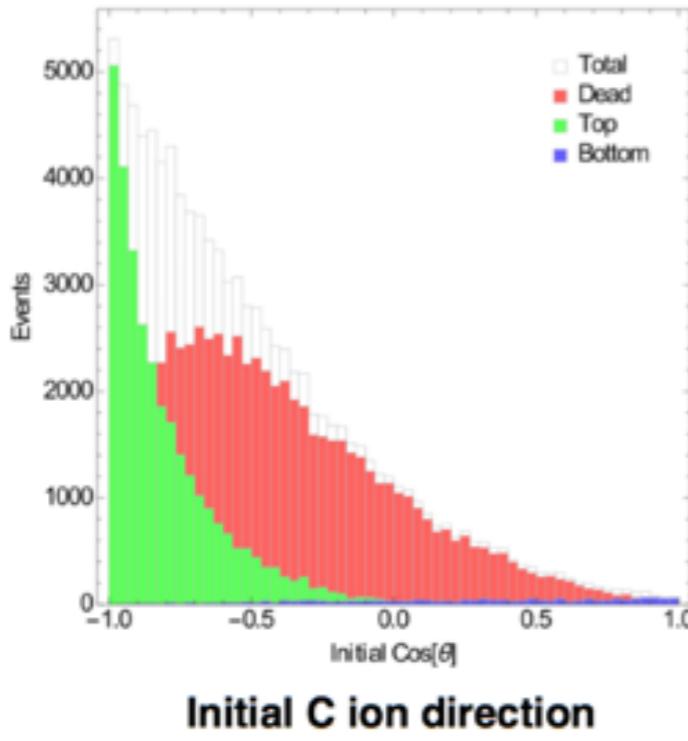
WE FIND HOWEVER THAT THE IONS MAY LOSE UP TO 4 keV ON THEIR WAY TOWARDS THE TOP OF THE ARRAY - in going from interstices to the interior of tubes and back

- 1) Top events: exit from the open end of the array with $E_{\parallel} > 1 \text{ keV}$
 - 2) Bottom events: opposite
 - 3) Dead events: ions reach energies below det. threshold while traveling in the array
 - 4) Side events: lateral losses
- With 10^5 ion trajectories we get

Top	Bottom	Side	Dead	Total
30802	1786	447	66965	100000

$\approx 1/20$

Energy losses



CAVOTO, COCINA, FERRETTI, Polosa arXiv: 1602.03216

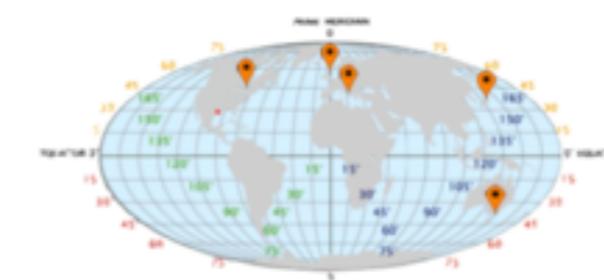
- After a WIMP scattering event, the fraction of ions channeled in a single CNT is $\approx 0.4\%$.
- Remaining ones are scattered outside of the CNT. However the CNT ARRAY might cooperate to recover part of the would-be-lost particles guiding them to the top.

$$\theta_A \sim 4^\circ \text{ CNT} \rightarrow \theta_A \sim 35^\circ \text{ CNT ARRAY}$$

CYGNUS-TPC proposal

- Galactic Nuclear Recoil Observatory: **measure WIMP and coherent neutrino scattering from the Sun with:**

- Recoil direction sensitivity
- keV-scale threshold (10 keV in the plots)
- Full 3D fiducialization
- TPCs distributed in 5 underground sites scattered around the globe



- Pathfinder approach (optimize readout and engineering)

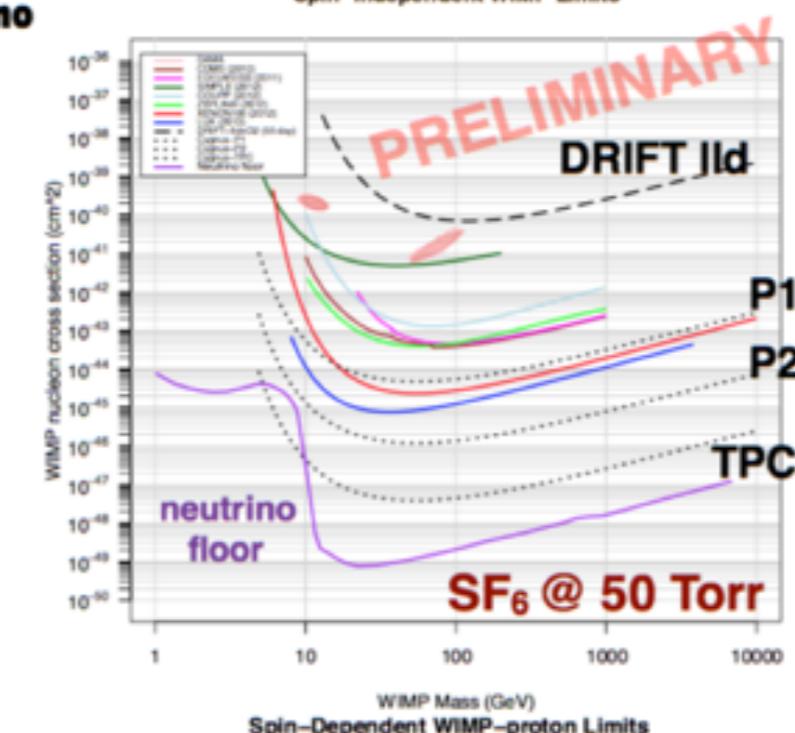
- CYGNUS-P1:** 24 m³ Large Volume (10Kg target mass) with already existing technology + 1 m³ High Definition pixelized readout (CNT ?)
- CYGNUS-P2:** down-selected technology for engineering optimization (400 kg)
- CYGNUS-TPC:** Galactic Observatory w/ multiple light target nuclei (1.2 ton)

Building an international collaboration
from various directional DM TPC groups to prepare LOI
DRIFT + NEWAGE + D³ + DMTPC + MIMAC + NITEC
UK + USA + Japan + Australia + Italy?

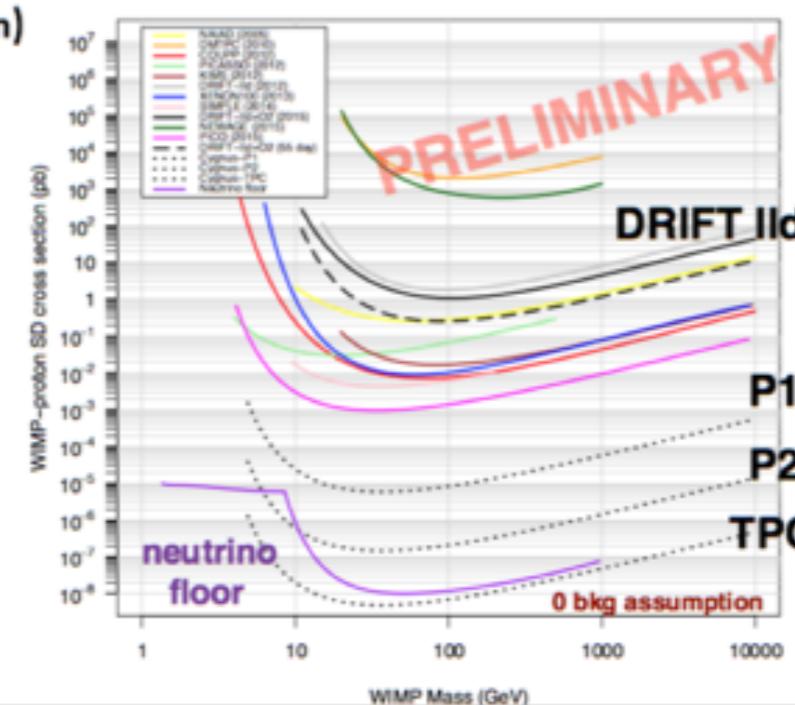
"CYGNUS-TPC kick-off meeting: a mini-workshop on directional DM search and coherent neutrino scattering"

7th-8th April 2016, Laboratori Nazionali di Frascati
<http://www.lnf.infn.it/~baracch/index.html>

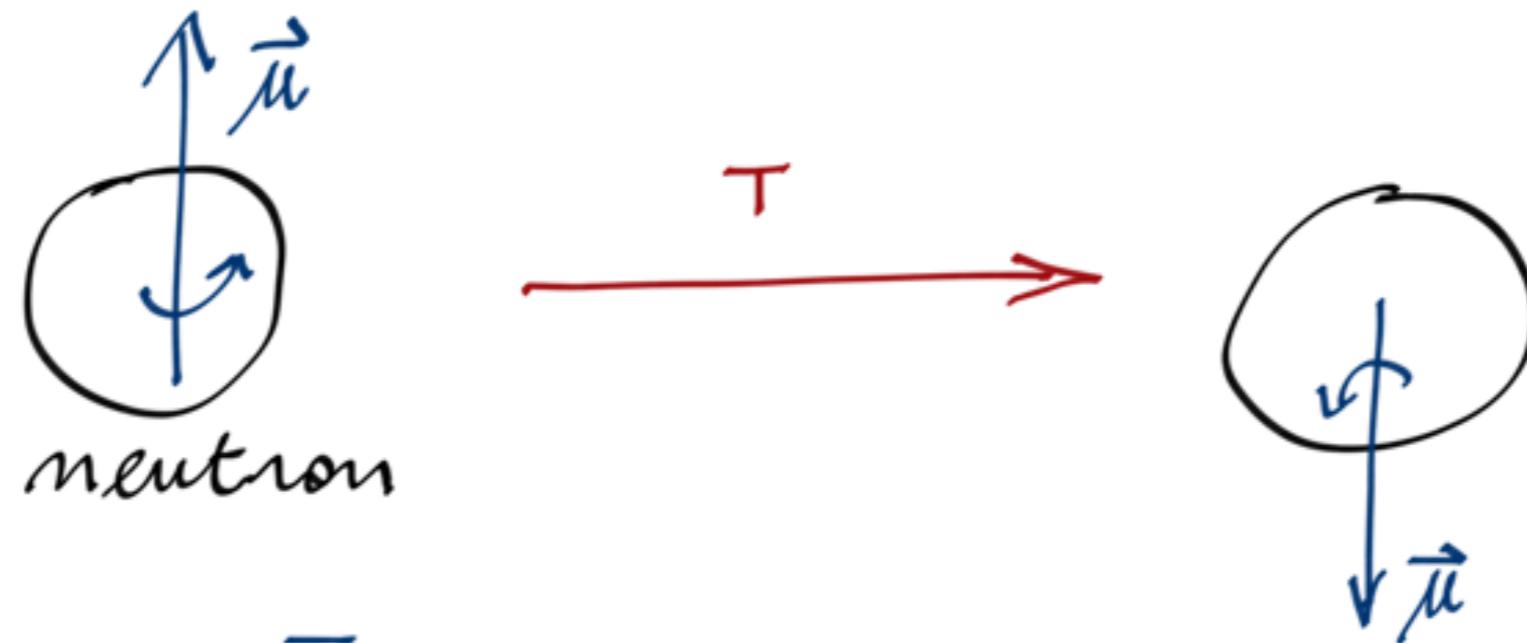
Spin-Independent WIMP Limits



Spin-Dependent WIMP-proton Limits



AXION-LIKE PARTICLES with m_b THE photons



$\bar{\psi} \sigma^{ij} \psi \cdot F_{ij}$ CP-even coupling.



$\bar{\psi} \sigma^{ij} \psi \cdot \tilde{F}_{ij}$ CP-odd
 $(\vec{\sigma} \cdot \vec{\Xi})$

QCD action contains a CP odd term (euclidean)

$$i \theta q[A]$$

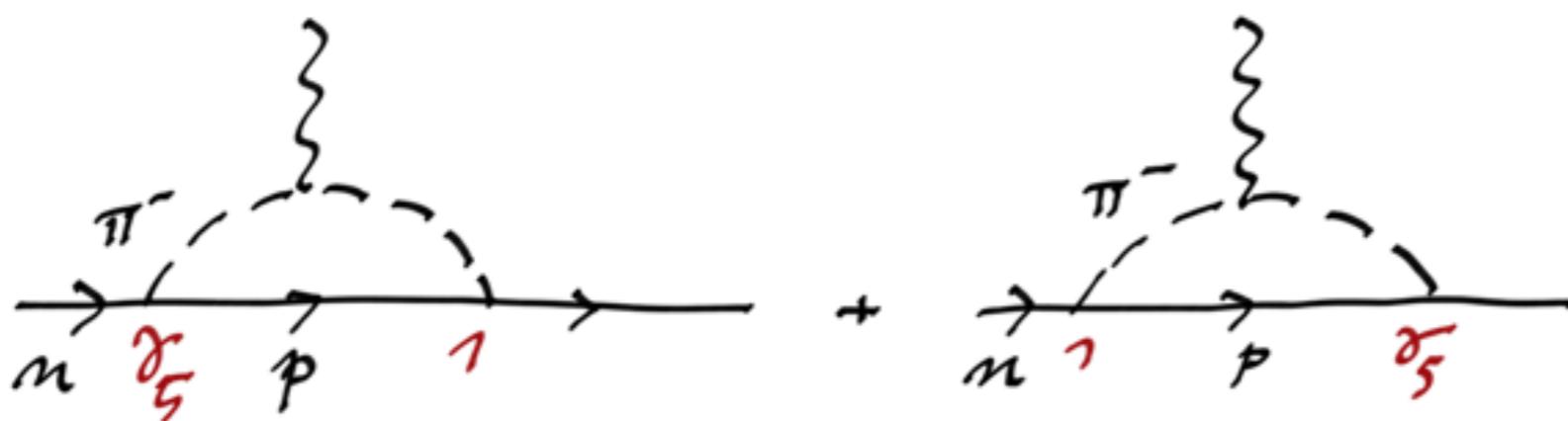
where

$$q[A] = \frac{g_0^2}{32\pi^2} \int F \cdot \tilde{F} d^4x$$

which induces a CP-odd term in the low energy theory

$$\begin{aligned} \mathcal{L}_{\pi NN} = & g_{\pi NN} \bar{\psi} \gamma_5 \vec{\sigma} \psi \cdot \vec{\pi} \\ & + g'_{\pi NN} \bar{\psi} \vec{\sigma} \psi \cdot \vec{\pi} \end{aligned}$$

Consider a gg' amplitude



\uparrow separation
of charge

$$\frac{l+q}{2} \leftarrow \sum_{\pi}^{\gamma} - \frac{l-q}{2}$$
$$P \rightarrow 0 \quad l + \frac{p+p'}{2} \quad P' \quad + (\gamma_5 \leftrightarrow 1)$$

$$\sim \left(\bar{u}(\vec{p}') i \sigma^{\mu\nu} q \gamma_5 u(\vec{p}') \right) \epsilon_\mu(q)$$

$$\sim \tilde{F}_{\mu\nu} \bar{\psi} \sigma^{\mu\nu} \psi$$

σ - π coupling ensures a $\ln \frac{\Lambda^2}{m_\pi^2}$ enhancement
where $\Lambda = 4\pi f_\pi$

$$g' \simeq \frac{\theta \zeta}{f_\pi} \quad \text{where } \zeta \simeq \frac{m_u m_d}{m_u + m_d}$$

$$g \simeq \frac{g_A m_N}{f_\pi} \quad \text{where } g_A = 1.27$$

Dependency on light quark masses

$$Z_\theta = N \int D\bar{A} e^{-\frac{1}{4}(F,F)} \sim i \theta q [4] \int D\Psi D\bar{\Psi} e^{-(\bar{\Psi}, (\bar{D}+M)\Psi) - (\bar{\eta}, \bar{\Psi}) - (\bar{\eta}, \Psi)}$$

One can set $\theta=0$ just chiral rotating sources.

If $q=1$, set $\alpha = \frac{\theta}{2N_f}$ to get $\theta=0$.

However

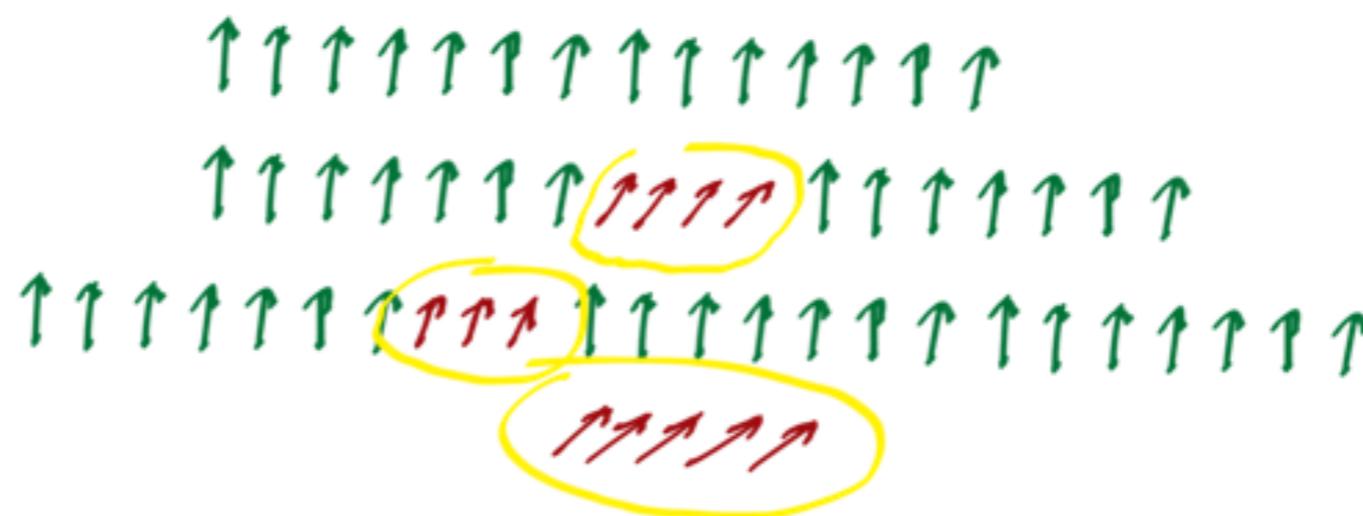
$$M \rightarrow M' = e^{-2i\alpha \delta_5} M$$

so M' depends on θ , and

$$M' = A' + i \delta_5 B' \quad (A', B' \text{ hermitian})$$

and require

$$\langle \pi | \bar{\Psi} i \delta_5 B' \Psi | 0 \rangle = 0$$



FROM THE MEASUREMENT OF d_n ($\lesssim 6 \times 10^{-26} e\cdot\text{cm}$)

$$|\theta| < 10^{-10}$$

Either $m_\nu = 0$ or there is a dynamical reason setting $\theta \rightarrow 0$.

$$\theta F\tilde{F} \longrightarrow (\theta + a/f) F\tilde{F}$$

where a is a new pseudoscalar field with a potential $V(a)$.

The minimum is at

$$a = -f\theta (+\tilde{a})$$

From the χ^2 term one gets

$$m_a^2 = \frac{m_\pi^2 f_\pi^2}{f^2} \frac{m_\nu m_d}{(m_\nu + m_d)^2}$$

All axion couplings are $1/f$ suppressed (Goldstone)

- AXIONS CAN BE COPIOUSLY PRODUCED IN THE EARLY UNIVERSE — if a certain upper bound is saturated ($f \lesssim 10^{10} \text{ GeV}$), they can constitute DM —

- A lower bound ($f \gtrsim 10^{10} \text{ GeV}$) from astrophysics.

$$\frac{\text{Rate}}{P} \sim \frac{\alpha}{f^2} \cdot n_\gamma \sim \frac{\alpha}{f^2} T^3$$

, , 'a

$$\text{Rate} \sim \frac{\alpha}{f^2} \cdot n_\gamma \sim \frac{\alpha}{f^2} T^3 \quad (T \sim 1 \text{ MeV})$$

son

$$R = \text{Rate}/V \sim n_p \frac{\alpha}{f^2} T^3 \quad \left(n_{e,p} = \frac{\#e}{R_{\text{ion}}^3} \simeq 3 \times 10^{17} \text{ GeV}^3 \right)$$

hydrogen

$$R = \frac{2.2 \times 10^{-28}}{f^2} \text{ GeV}^4$$

$$R_V = (G_F^2 E^2) n_e^2 = 1.2 \times 10^{-49} \text{ GeV}^4$$

Require $R_V \sim R \rightarrow f \sim 10^{10} \text{ GeV}, m_a \simeq 2 \text{ meV}$

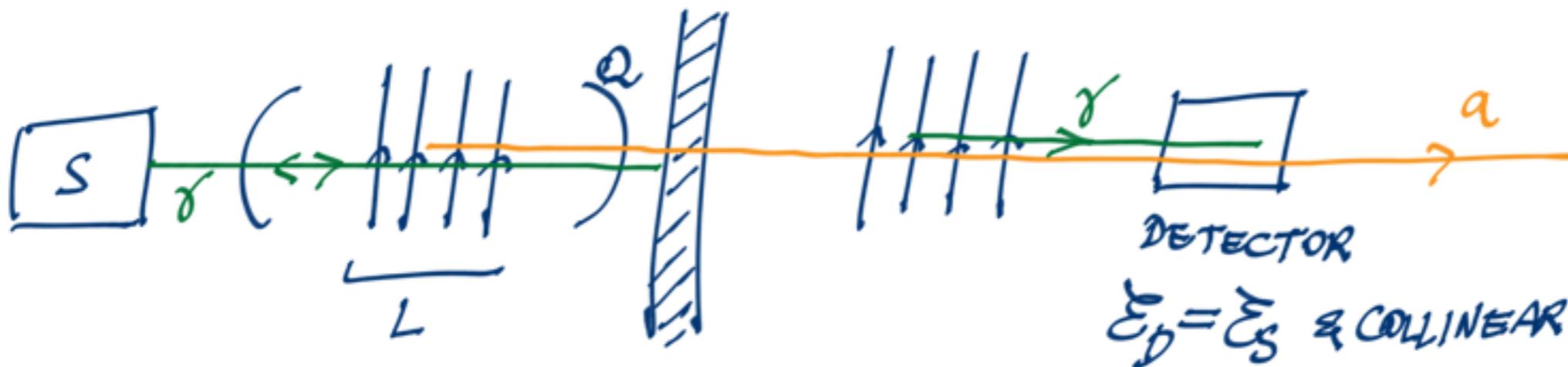
AXION- γ COUPLING

$$G_{a\gamma\gamma} \approx \frac{1}{f} \frac{\alpha}{4\pi} = \frac{m_a}{m_\pi f_\pi} \frac{\alpha}{2\pi}$$

$$T(\pi^0 \rightarrow 2\gamma) = -\frac{i}{f_\pi} \frac{\alpha}{2\pi} \langle k_1 e_1 | k_2 e_2 | F \cdot \tilde{F} | \pi^0 \rangle$$

f_π

LIGHT-SHINING-THROUGH-WALL



$$\dot{N}_e \propto \dot{N}_\gamma P_{\gamma \rightarrow a} P_{a \rightarrow \gamma}$$

$$\propto \dot{N}_\gamma (G \cdot H \cdot L)^4 \text{ where } G \sim 1/f$$

with $G \lesssim 10^{-10} \text{ GeV}^{-1}$

$$(GHL)^4 \lesssim 10^{-35}$$

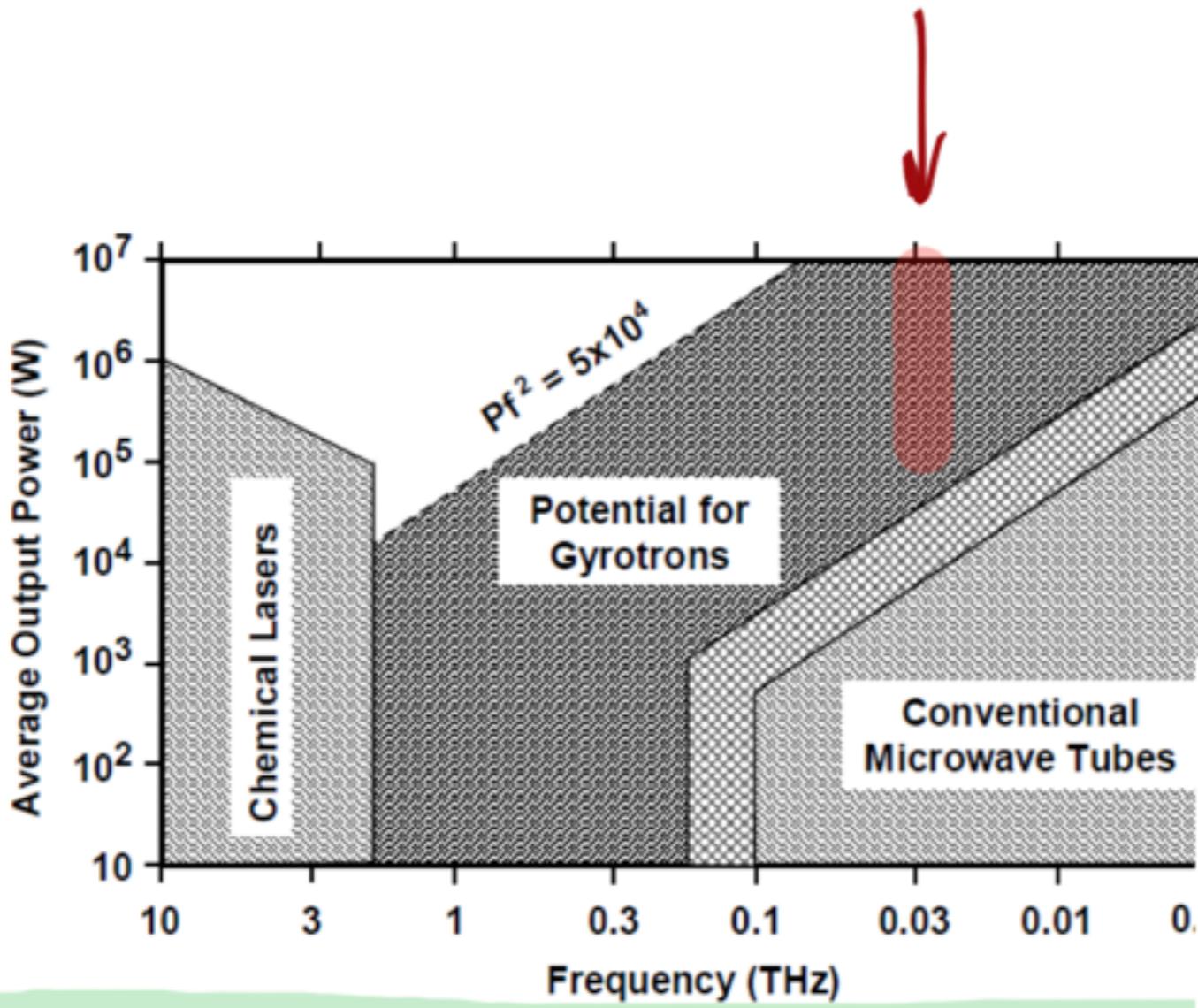
MEGAWATT GYROTRON SOURCES can produce (@30GHz)

$$\dot{N}_\gamma \approx 10^{28} / \text{kc}$$

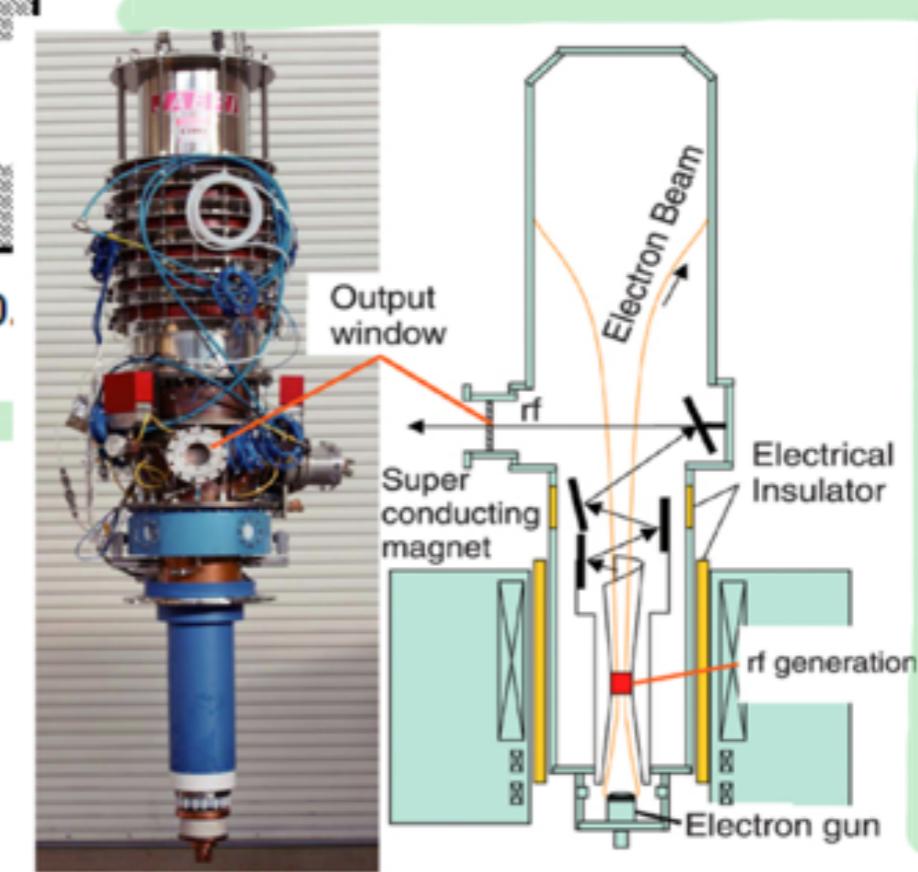
w/ continuous emission -

$$(10 \text{ LSW events/yr}) \times Q$$

Gyrotrons



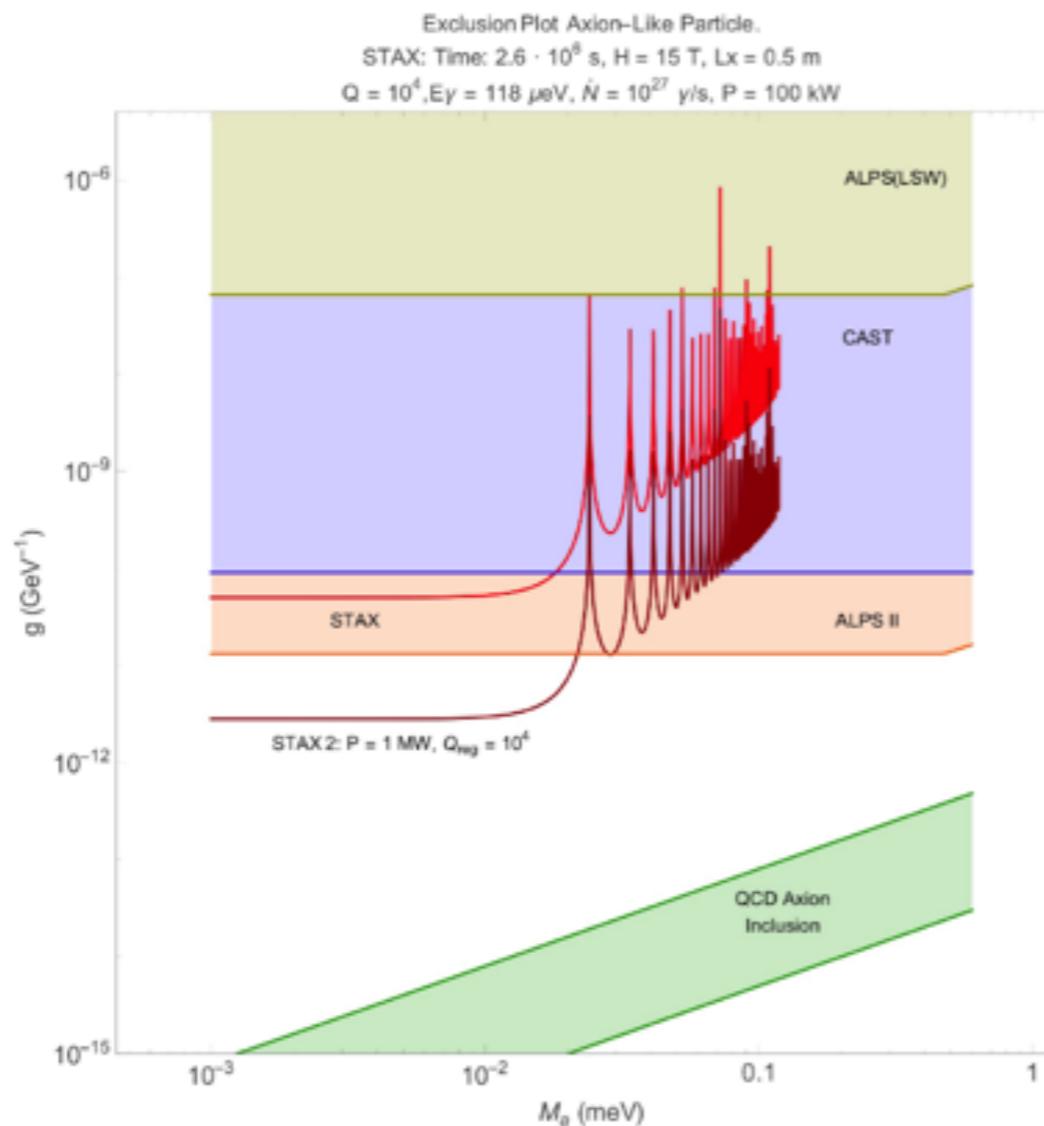
CW highly
derived.



POTENTIAL REACH

$$P = \frac{G^2 H^2}{q^2} \frac{\sin^2(qL/2)}{\frac{E_\gamma}{L + \sqrt{E_\gamma^2 - m_a^2}}}$$

$$q = E_\gamma - \sqrt{E_\gamma^2 - m_a^2} - \frac{1}{2}L$$



EXCLUSION @ 90% CL
 IN CASE OF A NULL RESULT
 FOR AXIONS
 $m_a \lesssim 0.02$ meV
 ONE MONTH EXPOSURE
 AND ZERO DARK COUNTS

STAX @ 100 kW
 STAX2 @ 1 MW
 + REG. Q.

L. CAPPARELLI et al.
 PHYS. DARK. UNIV. 12 (2016) 37

FABRY-PEROT CAVITIES

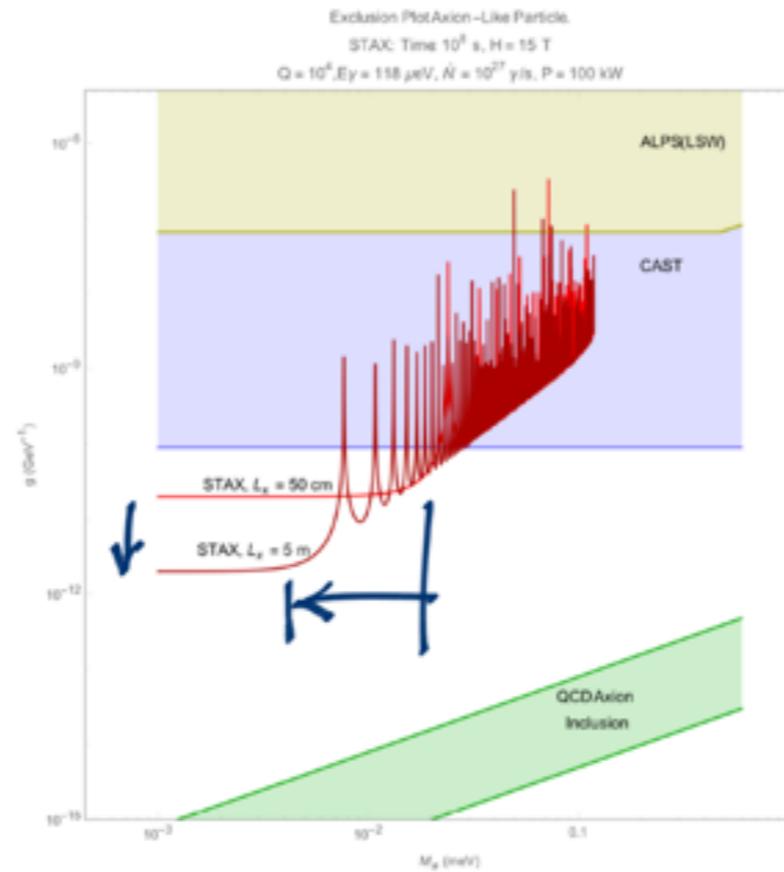
$$P \sim (GH)^4 \cdot L^2 \cdot L^2$$

↓

$$QL^2 \quad (Q \sim 10^5 \text{ in MW})$$

THIS ALLOWS TO EXPLORE G VALUES SMALLER BY $Q^{-\frac{1}{4}}$
 Someone suggests $Q^{-\frac{1}{2}}$ by setting a regeneration cavity.

MAKING L LONGER MEANS THAT THE ONSET OF OSCILLATIONS
 SHIFTS TO SMALLER VALUES BY $1/\sqrt{x}$ IF $L \rightarrow xL$



Some Numbers

Improvements are possible w/ FP cavities



Very high Q for mw. $\sim 10^4 \div 10^5$

Parameter	ALPS	STAX	$g_{\text{ALPS}} / g_{\text{STAX}}$	STAX II	$g_{\text{ALPS}} / g_{\text{STAXII}}$
Laser Power	0.8 W	100 kW	18.8	1 MW	188
Photon Energy	2.327 eV	124 μ eV	11.7	124 μ eV	11.7
Cavity Q-factor	55.0	10^4	3.7	10^8	37
$H \cdot L_x$	22 T m	7.5 T m	0.3	7.5 T m	0.3
Detection Efficiency	0.9	1.0	1.0	1.0	1.0
Detector Noise	$1.8 \cdot 10^{-3} \text{ sec}^{-1}$	10^{-9} sec^{-1}	34.0	10^{-9} sec^{-1}	34
Combined Improvement			$\sim 10^4$		$\sim 8 \times 10^5$

TES

TES work @ $T \underline{\text{slightly}} \underline{\text{below}} T_c$.

$$V_{\text{TES}} \approx 2 \times 10^{-11} \text{ m}^3 \text{ @ } 10 \text{ mK}$$

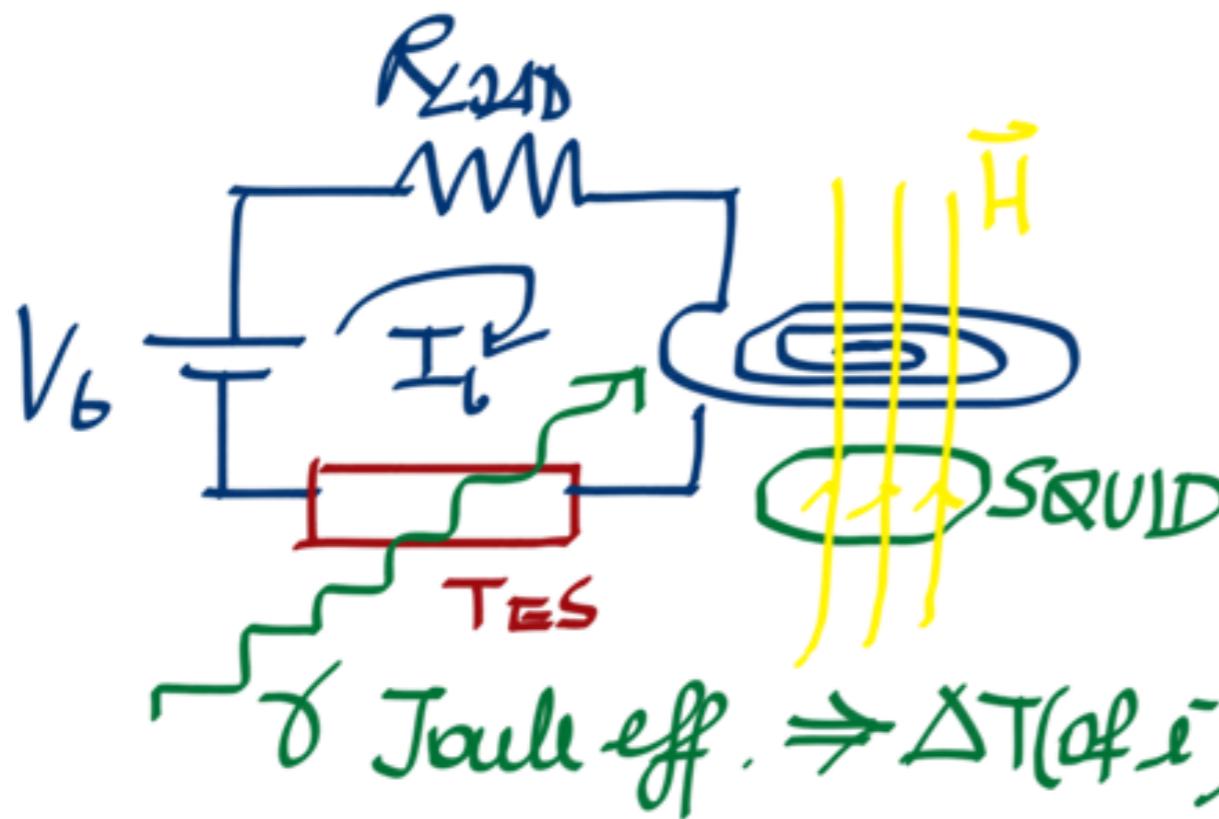
$$\gamma(30 \text{ GHz}) \rightarrow \Delta T_e \approx 40 \text{ mK}$$

Estimate & engineer ΔI -
— SQUID SPECTRAL NOISE DENSITY

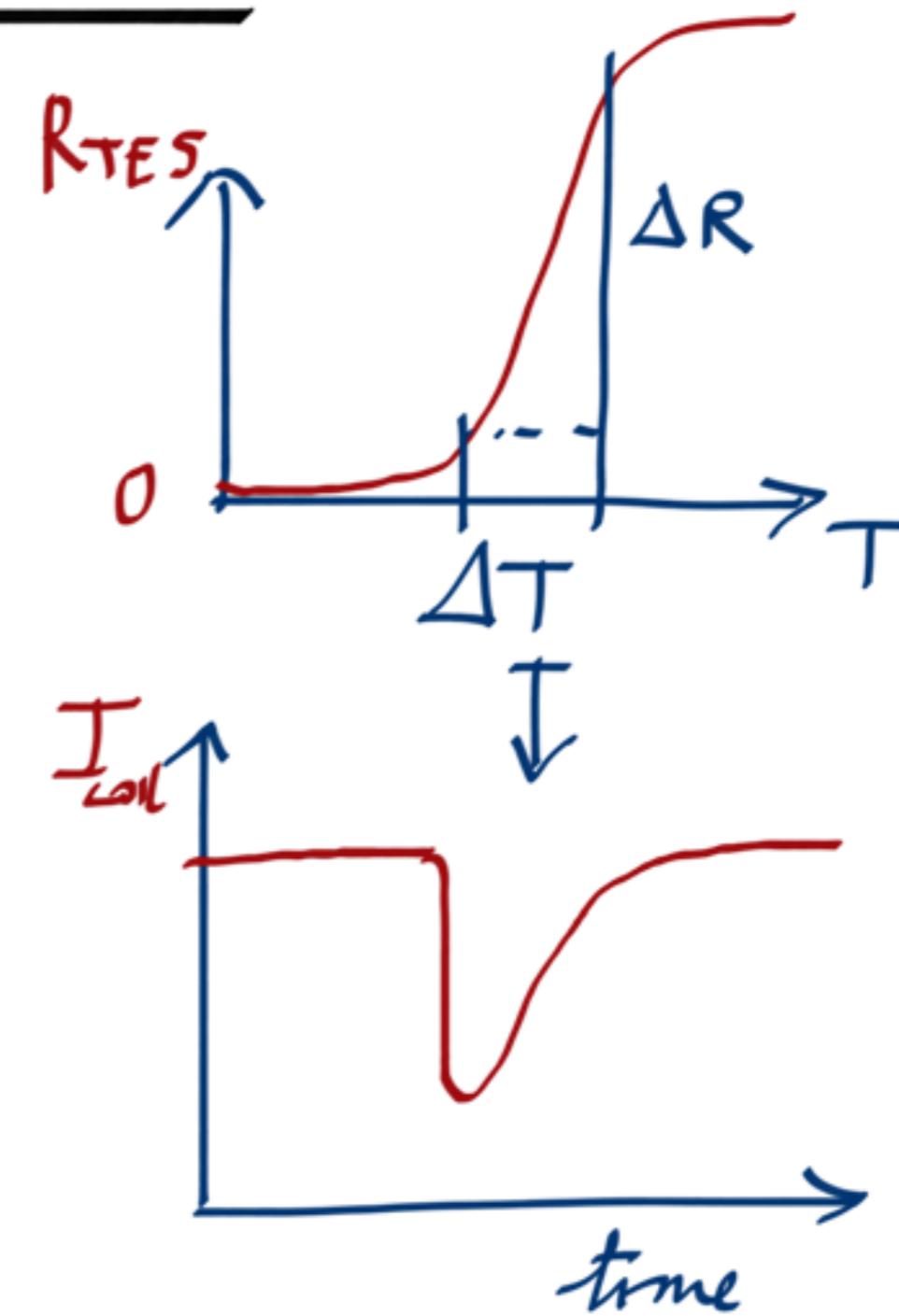
$$\frac{1 \text{ pA}}{\sqrt{\text{Hz}}}$$

— to be multiplied by the det. passband ν_2
 $\approx \sqrt{100 \text{ Hz}}$

EYE SCHEME



$$\tau(\ell - \phi @ 10 \text{ mK}) \gtrsim 0.18 \text{ sec}$$



Read a voltage on SQUID
 READ on $\Delta T, \Delta R, \Delta V_{SQUID}$ @ 30 GHz $\neq 10 \text{ mK}$.

Oscillations

Occur when $qL \ll 1$ fails -

$$q \approx \frac{m_a^2}{2\sum_\gamma} \rightarrow \frac{(m_a - m_\gamma^*)^2}{2\sum_\gamma}$$

Shifts the onset of oscillations to higher m_a values.

Example (CAST)

Introduce He gas in the cavity, γ will have an effective velocity $C/n(\omega) = |\vec{\epsilon}|/\epsilon_\gamma$
 $\Rightarrow m^* > 0$. N.B. CAST uses X-rays.

WIMPS & CNTs (DeCANT)

LM CAPPARELLI (UCLA)

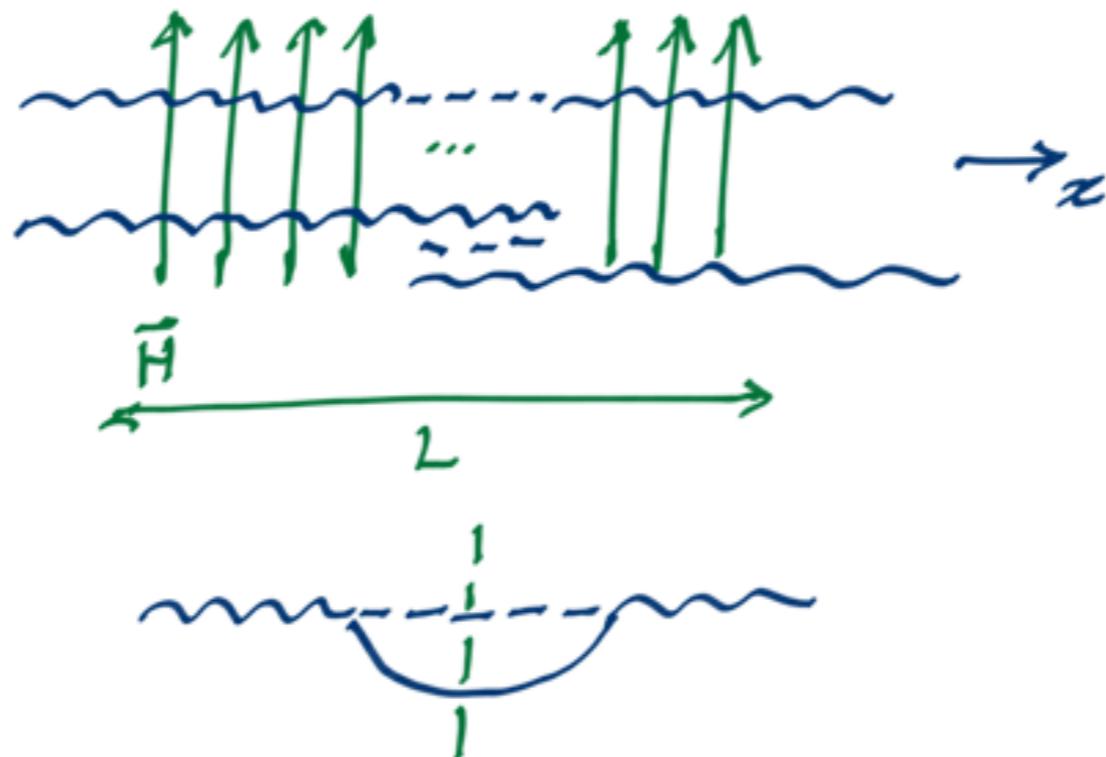
G CAVOTO (INFN ROMA)
F COCINA (SAPIENZA)
J FERRETTI (INFN ROMA)
D MAZZILLI (SAPIENZA)
ADP (SAPIENZA)

AXIONS & SUB-THz γ s (STAX)

LM CAPPARELLI (UCLA)

G CAVOTO (INFN ROMA)
J FERRETTI (INFN ROMA)
F GIAZOTTO (SNS & NEST)
ADP (SAPIENZA)
P SPAGNOLO (INFN PISA)

APPENDIX



$$\Sigma \sim G^2 H^2 \varepsilon_F^2 \int dq \quad \frac{\sin^2(qL/2)}{q^2(p^2 - m_q^2 + i\epsilon)}$$

$$(p^2 - m_q^2 + i\epsilon) = -(q - (q_1 + i\epsilon))(q - (q_2 - i\epsilon))$$

$$q_1 = \varepsilon_F + p^* \quad i\epsilon \leftarrow i\epsilon p^* - \epsilon^2$$

$$q_2 = \varepsilon_F - p^*$$

$$p^* = \sqrt{\varepsilon_F^2 - m_q^2} > 0$$

Do integral in the complex plane, take its 'Im' part
and get the standard formula

APPENDIX

$$P = G^2 H^2 \frac{\epsilon_g}{\sqrt{\epsilon_g^2 - m_a^2}} \left(\frac{n \pi^2 (q_2 L/2)}{q_2^2} + (2 \rightarrow 1) \right)$$

$$\lambda_a < \frac{L}{2} \Rightarrow |p| > \frac{1}{2L}$$

FWD a's $q < \epsilon_g - \frac{1}{2L}$ from $p = k - q$

Bkwd a's $q > \epsilon_g + \frac{1}{2L}$

Since $q_1 > q_2$

$$q_2 \approx m_a - \frac{1}{2L}$$

$$q_1 \approx m_a + \frac{1}{2L}$$

$\min(q_1 - q_2) = \frac{1}{L}$

Going back to the contour integral evaluation we find that this condition translates into an upper bound for the P

$$P_{\max} = G^2 H^2 \frac{\sin^2(qL/2)}{q^2} \frac{m_a}{1/L}$$