



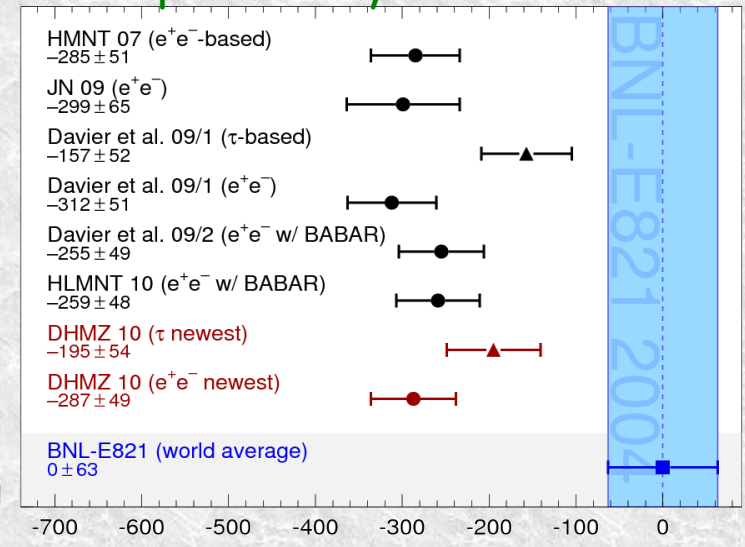
Status  
on pion form factor  
at CMD-3

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# SM prediction for muon g-2

ArXiv:1010.4180, arXiv:1105.3149

$\Delta \text{Exp} - \text{Theory} \sim 3.3 - 3.6\sigma$



The anomalous magnetic moment of the muon

$$a_{\mu}^{\text{experimental}} = (g-2)_{\mu} / 2$$

Experimental world average  $a_{\mu} = 11\,659\,208.9 \pm 6.3 \times 10^{-10}$

Theoretical prediction  $\delta a_{\mu} = \pm 4.9 \times 10^{-10}$

HLMNT 11

Hadronic content of  $a_{\mu}$  calculated

From measured cross-section by dispersion integral

LO hadronic  $694.1 \pm 4.3 \times 10^{-10}$  HLMNT 11

main channels contribution to precision at  $\sqrt{s} < 1.8 \text{ GeV}$

From direct integration  
Without model constraints

$\pi^+\pi^-$	$505.65 \pm 3.09$	
$\pi^+\pi^-\pi^0$	$\pm 1.15$	
$\pi^+\pi^-\pi^0$	$\pm 0.99$	(mostly from omega region)
.....		

Light-by-light  $10.5 \pm 2.6$  Prades, de Rafael & Vainshtein

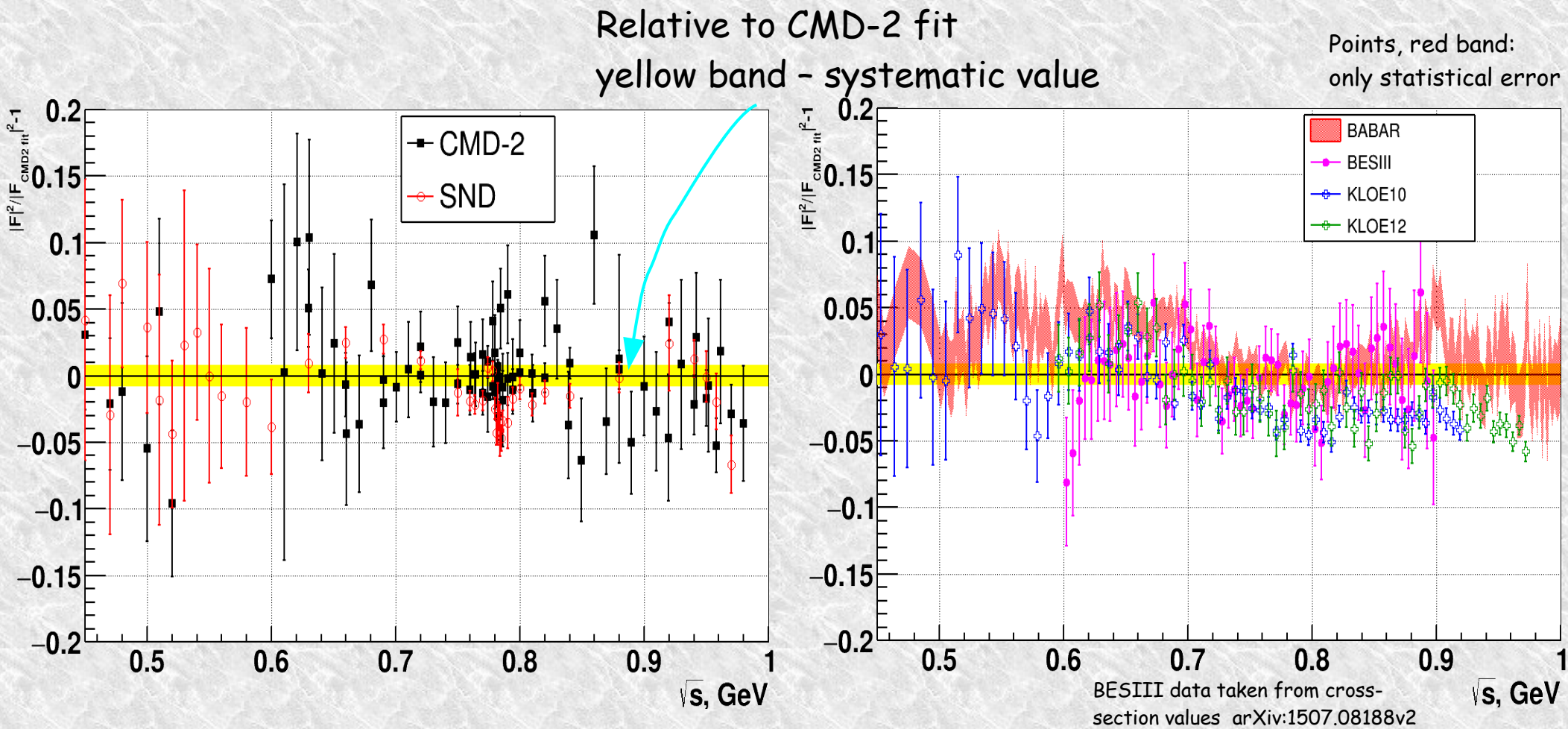
need more theory input,

with help of experimental transition form factors

$a_{\mu} - a_{\mu}^{\text{exp}}$   
New g-2 experiments at FNAL and J-PARC have plans to reduce error to  $1.5 \times 10^{-10}$

$\pi^+\pi^-$  gives the main contribution to hadronic value and overall theoretical precision of  $a_{\mu}$

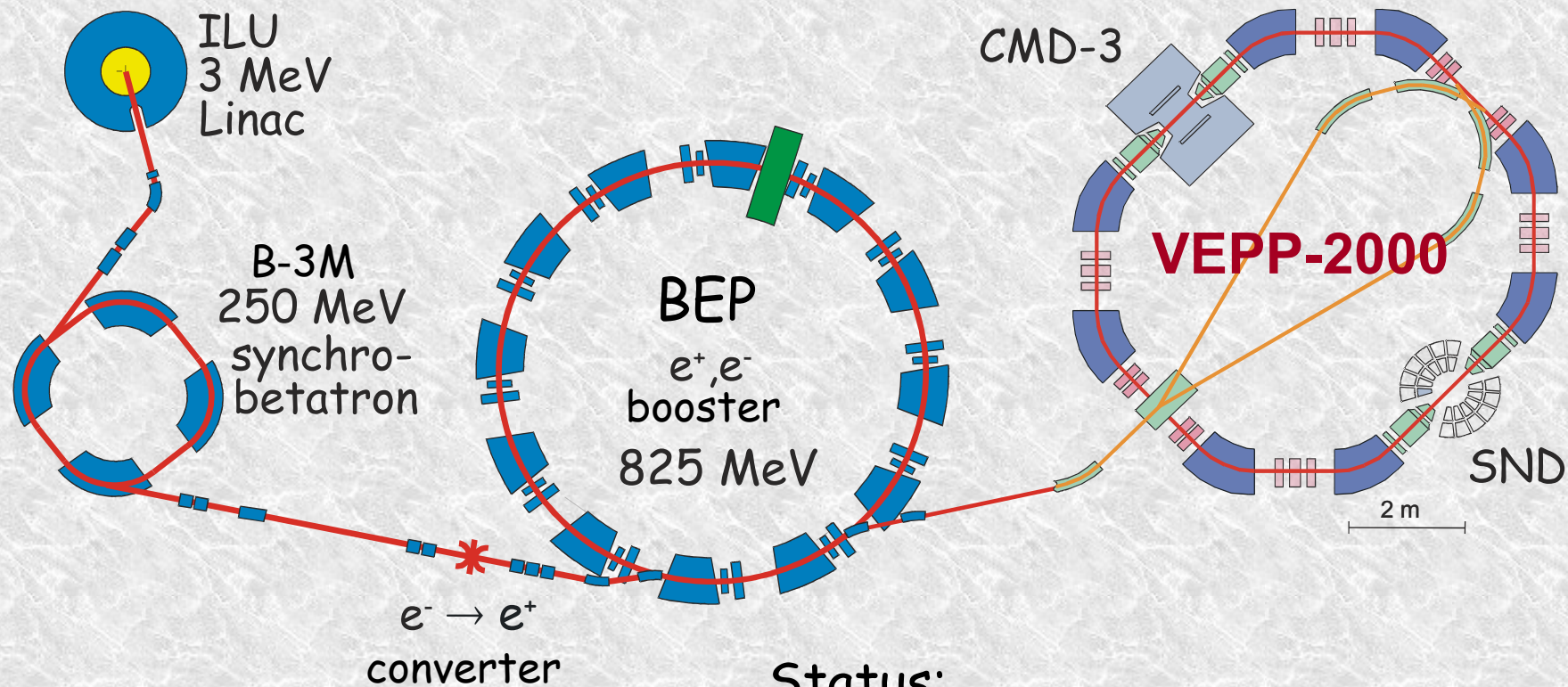
# Published cross section $e^+ e^- \rightarrow \pi^+ \pi^-$



Local inconsistencies larger than claimed systematic errors seen



# VEPP-2000 collider



Status:

2010 - start of experiments

2013-2015 - upgrade of positron  
injection facility

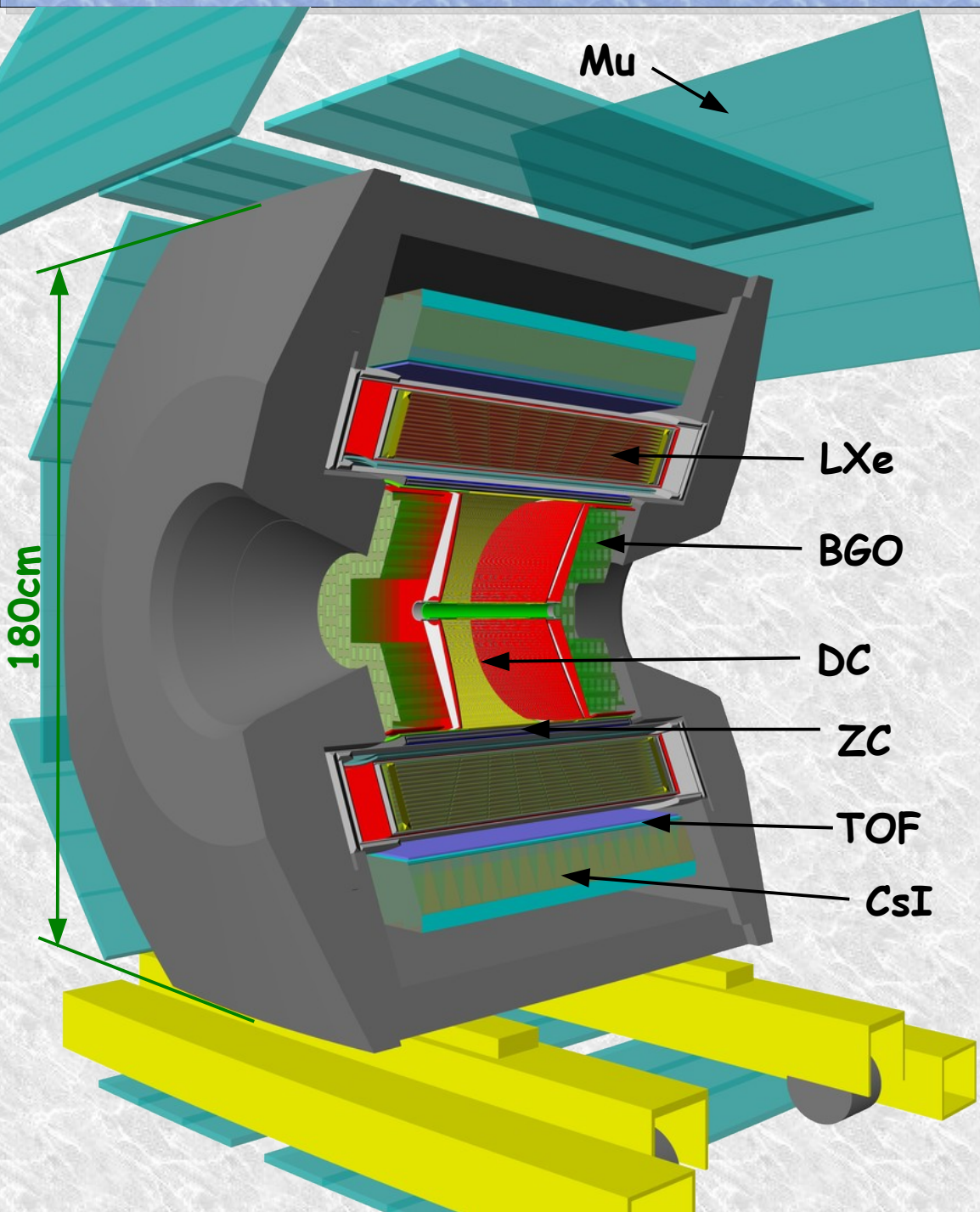
Plans:

$\approx 100 \text{ pb}^{-1}$  per detector per year

- Up to 2 GeV c.m. Energy
- VEPP-2000 uses unique "round beams" optic, which gives additional gain in luminosity and will provide:

$$L=10^{32} \text{ cm}^{-2}\text{s}^{-1}, \sqrt{s}=2.0 \text{ GeV}$$

# CMD-3 Detector



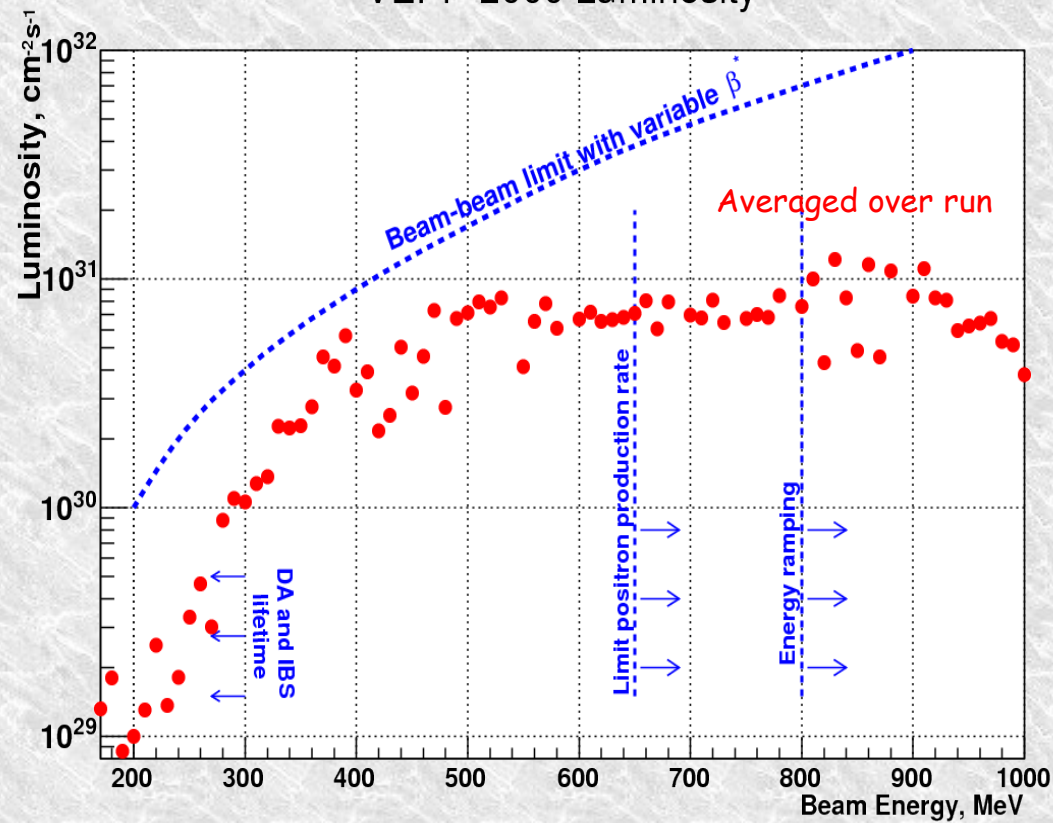
Advantages for this analysis compared to previous CMD-2:

- x new drift chamber with x2 better spatial resolution, higher B field  
better efficiency  
better momentum resolution

- x Unique LXe calorimeter with 7 ionization layers with strip readout  
~2mm measurement of conversion point,  
tracking capability,  
shower profile (from 7 layers + CsI)

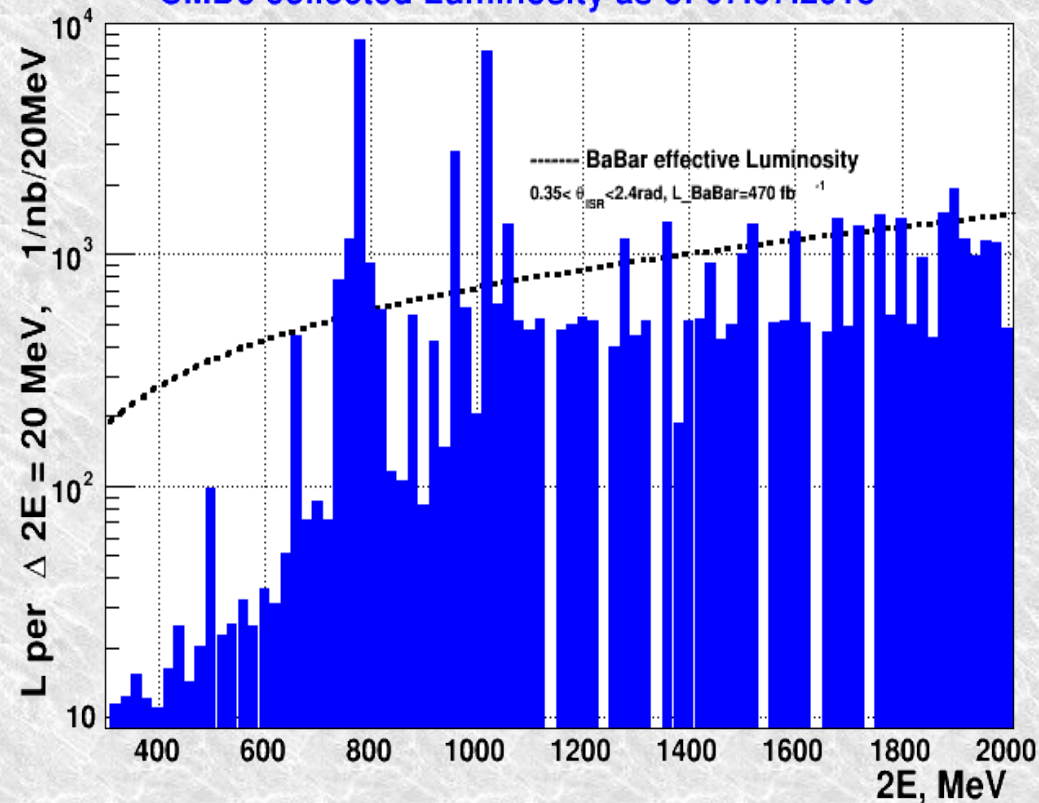
# Collected Luminosity

VEPP-2000 Luminosity



The  $10^{31} \text{ cm}^{-2} \text{ s}^{-1}$  luminosity at  $\sqrt{s}=2.0 \text{ GeV}$  was reached  
 Currently the luminosity at high energy is limited by a deficit of positrons and maximum energy of the booster (now 825 MeV), after upgrade it will gain a factor of 10

CMD3 collected Luminosity as of 07.07.2013



Collected L  $\sim 60 \text{ pb}^{-1}$  per detector

- 8.3  $\text{pb}^{-1}$   $\omega$  - region
- 9.4  $\text{pb}^{-1}$   $< 1 \text{ GeV}$  (except  $\omega$ )
- 8.4  $\text{pb}^{-1}$   $\phi$  - region
- 34.5  $\text{pb}^{-1}$   $> 1.04 \text{ GeV}$



# Event selection

- Two charged collinear tracks:

$$|\Delta \phi| < 0.15, \quad |\Delta \theta| < 0.25$$

$$Q_1 + Q_2 = 0$$

- Vertex position close to interaction point:

$$\rho_{\text{average}} < 0.3 \text{ cm}, \quad |Z_{\text{average}}| < 5 \text{ cm}$$

$$|\Delta \rho| < 0.3 \text{ cm}, \quad |\Delta Z| < 5 \text{ cm}$$

- Fiducial volume inside good region of DCh:

$$1. < (\pi + \theta^+ - \theta^-) / 2 < \pi - 1.$$

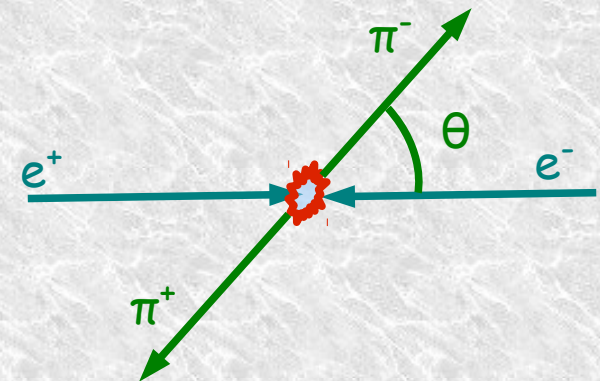
- Quality of selected tracks:

$$\chi^2 / \text{ndf} < 10, \quad N_{\text{hits}} \geq 10$$

- Filtration of low momentum and cosmic background:

$$0.45 E_{\text{beam}} < p^+, p^- < E_{\text{beam}} + 100 \text{ MeV}/c$$

Simple event signature with  
2 back to back charged particles



Data sample includes events with:  $e^+e^-$ ,  $\mu^+\mu^-$ ,  $\pi^+\pi^-$ , cosmic muons  
Mostly doesn't have any other background at  $\sqrt{s} < 1 \text{ GeV}$

# Event separation

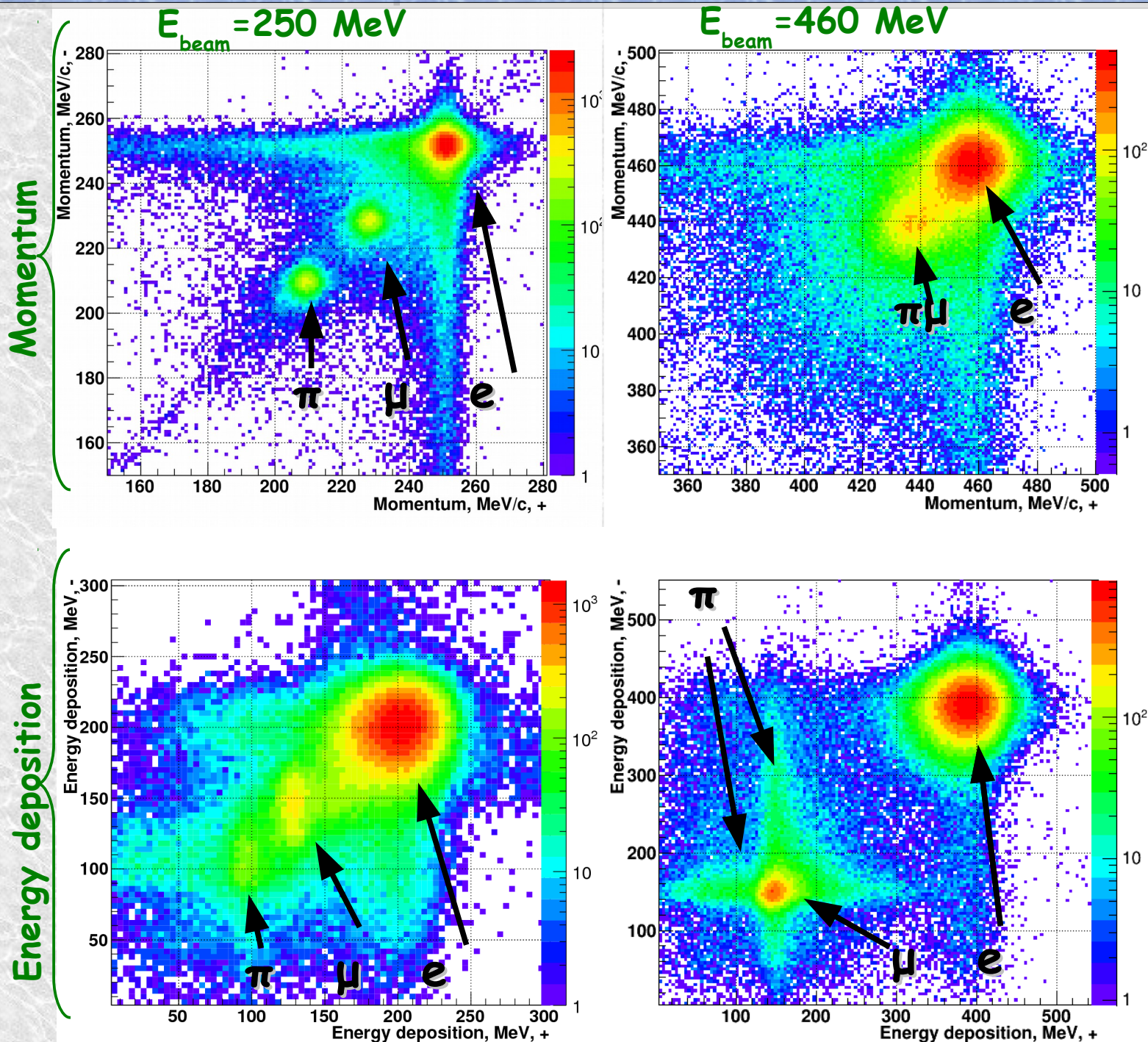
Particle ID can be done by momentum or energy deposition

At low energies momentum resolution of DCh enough to separate different types

At higher energies Electron shower in calorimeter far away from MIPs

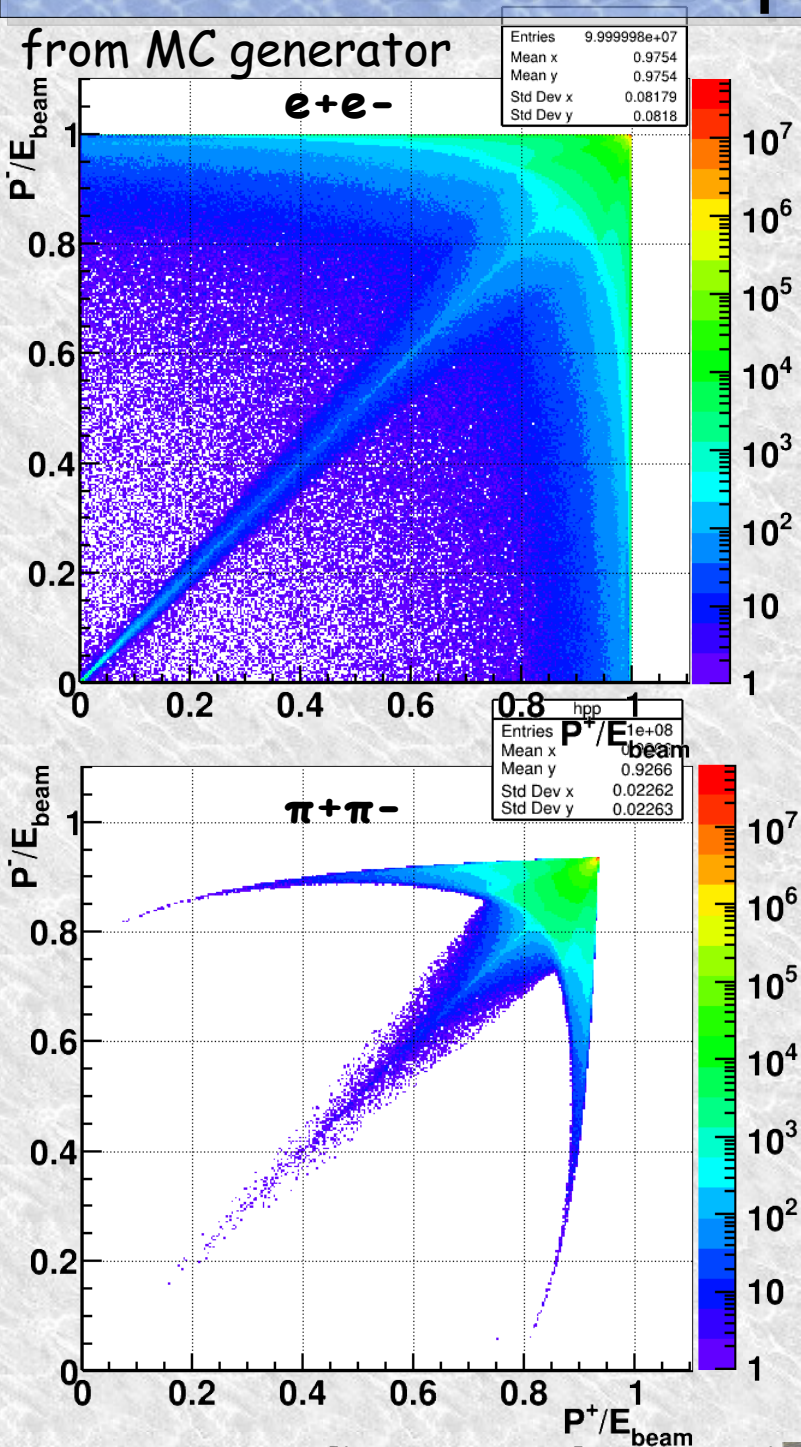
Both methods can be used separately for cross-check

$N_{\mu\mu}$  can be fixed (or not) from QED





# Event separation by momentum



For particle separation:

As input: momentum spectra for  $ee, \pi\pi, \mu\mu$  events from MC generator (in applied selection criteria) + cosmic,  $3\pi$  background from data(MC)

Generated distributions are convoluted with detector response function which include (with mostly all free parameters in it):

- x momentum resolution,
- x bremsstrahlung of electron on vacuum tube,
- x pion decay in flight

$N_{\pi\pi}/N_{ee}$  obtained as result of binned likelihood minimization

# Event separation by energy deposition

At this moment: Full energy deposition in LXe+CsI calorimeter is used for particle separation

As input: PDF distributions are taken from MC or data itself (fitted by analytical function, and used with some free parameters)

x Electron - described by mostly free function

x Muons - from simulation + additional smearing (plan to be taken from data)

x Pions - from  $\phi \rightarrow 3\pi$ ,  $\omega \rightarrow 3\pi$  events

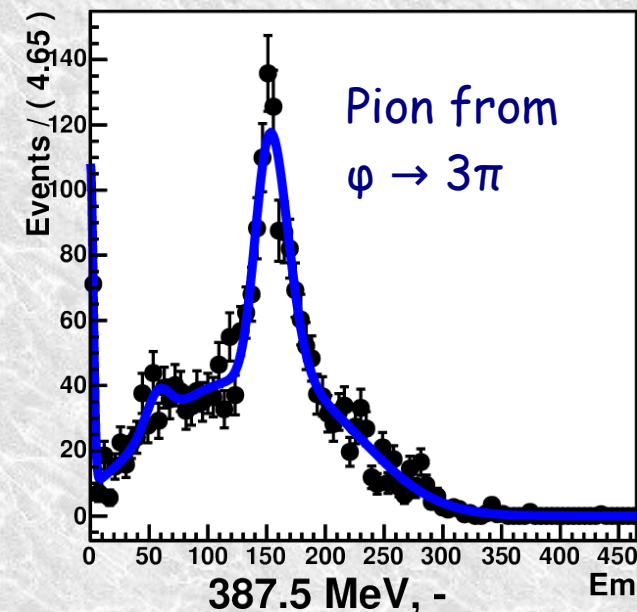
x Cosmic - from data itself (events are selected by vertex position)

$N_{\pi\pi}/N_{ee}$  obtained as result of binned likelihood minimization

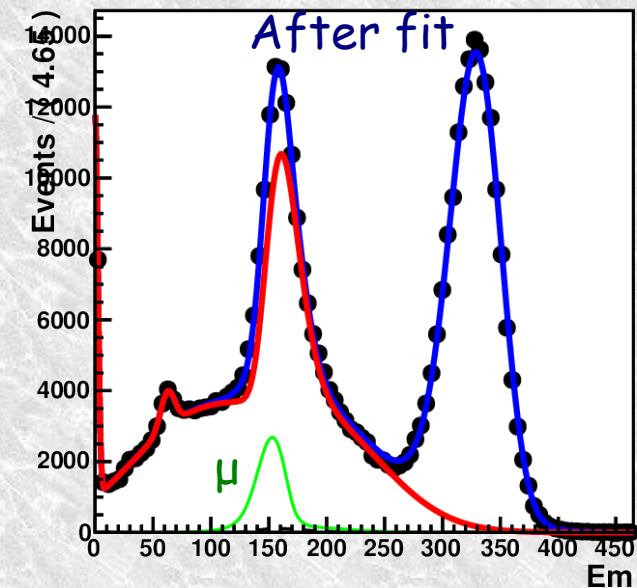
As plans: to exploit information about shower profile (energy deposition in 7 layers of LXe, + CsI)

Neural net can be used for event classification

387.5 MeV, pi-

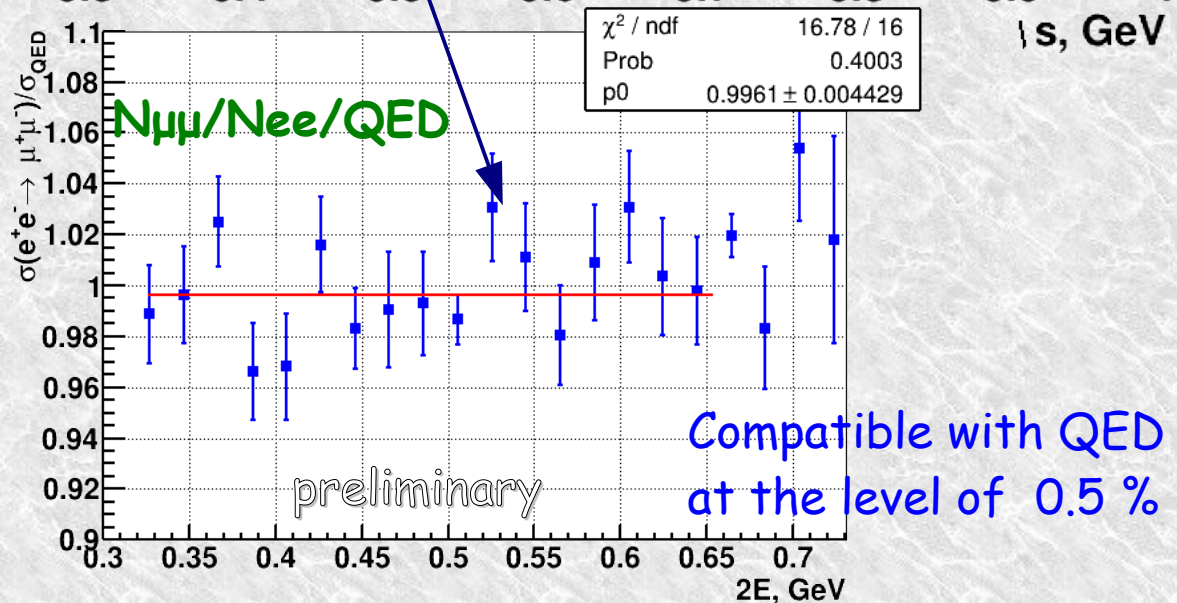
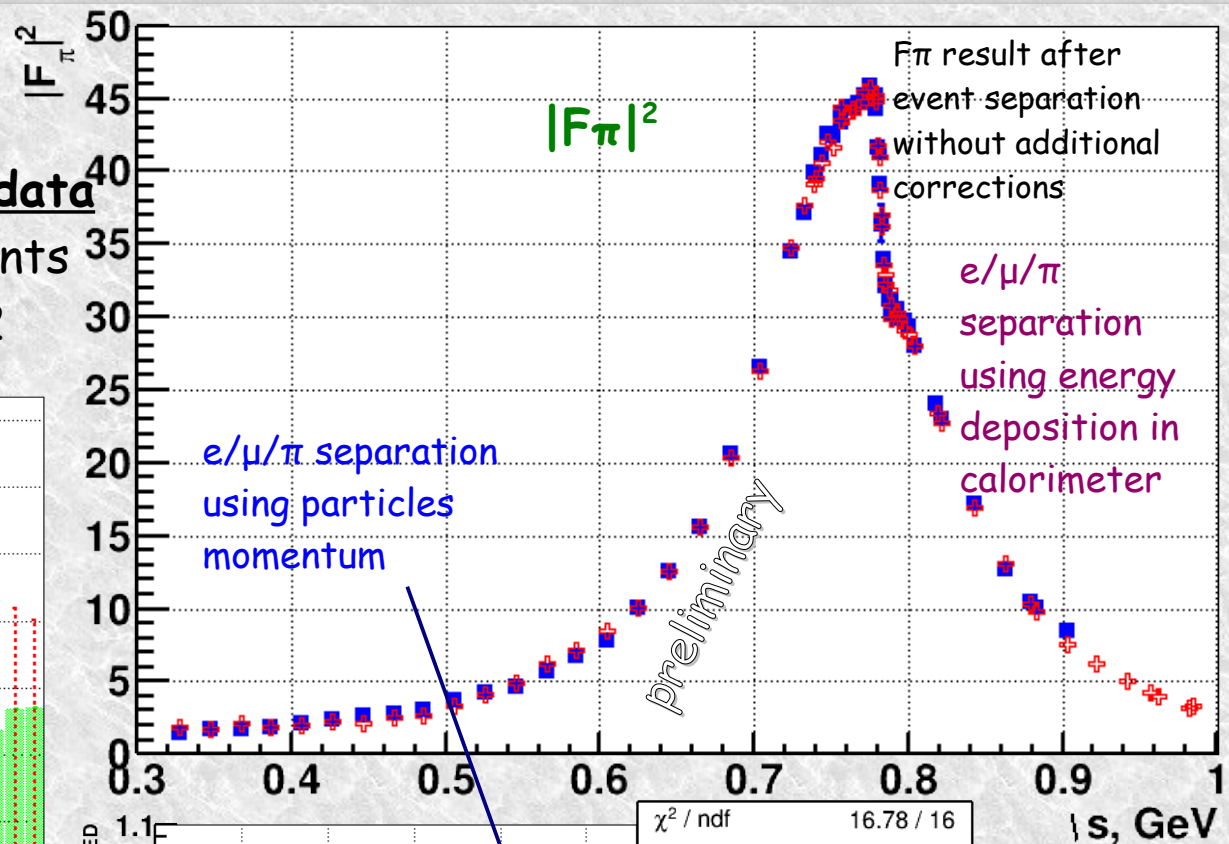
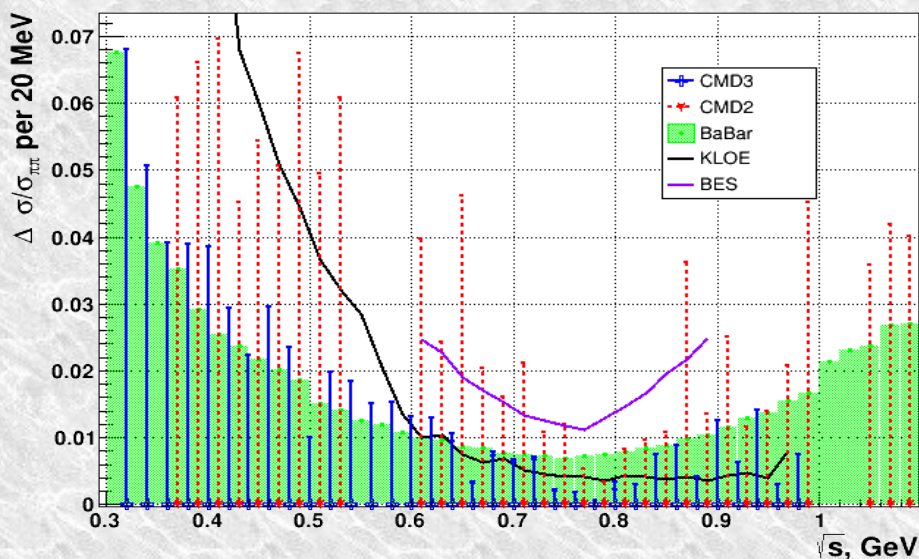


387.5 MeV, -



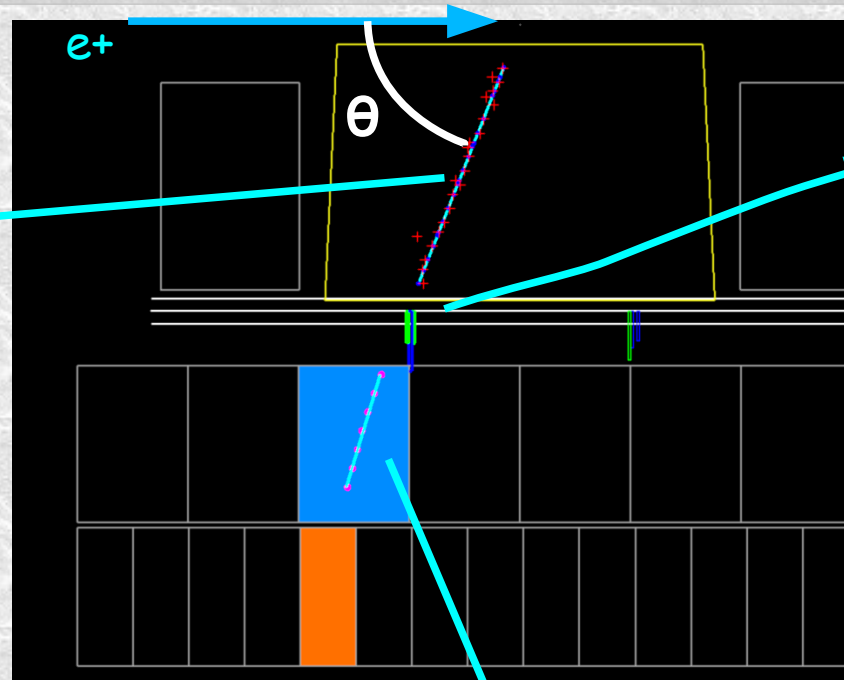
# $e^+e^- \rightarrow \pi^+\pi^-$ by CMD-3

Statistical precision of cross section measurement for **2013 data** is at the same level as other experiments and a few times better than at CMD-2



# Precision of fiducial volume

DC chamber  
Polar angle measured by  
with help of charge  
division method  
(Z resolution  $\sim 2\text{mm}$ ),  
Unstable, depends on  
calibration and thermal  
stability of electronic  
Calibration done  
relative to ZC (LXe)



## ZC chamber

multiwire chamber  
with 2 layers and with strip  
readout along Z coordinate

strip size: 6mm

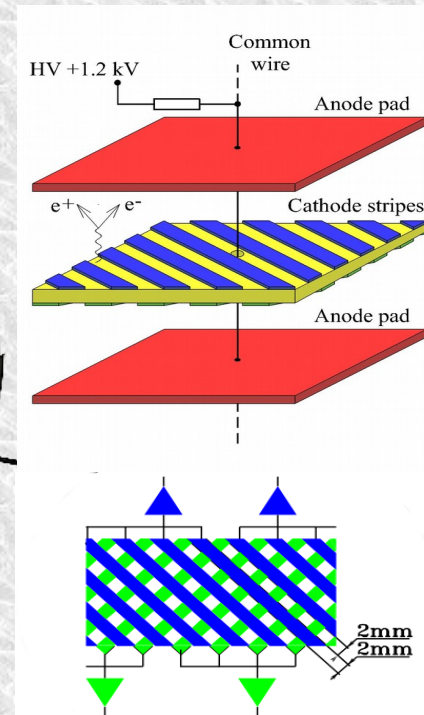
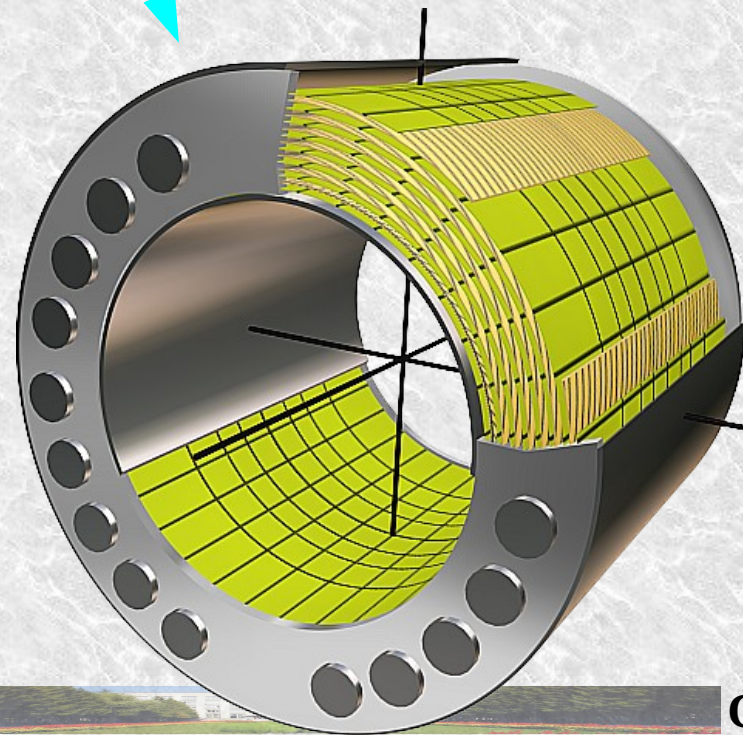
Z coordinate resolution  $\sim$   
0.7 mm (for  $\theta_{\text{track}} \sim 1 \text{ rad}$ )

## LXe calorimeter

ionization collected in 7 layers with  
cathode strip readout,

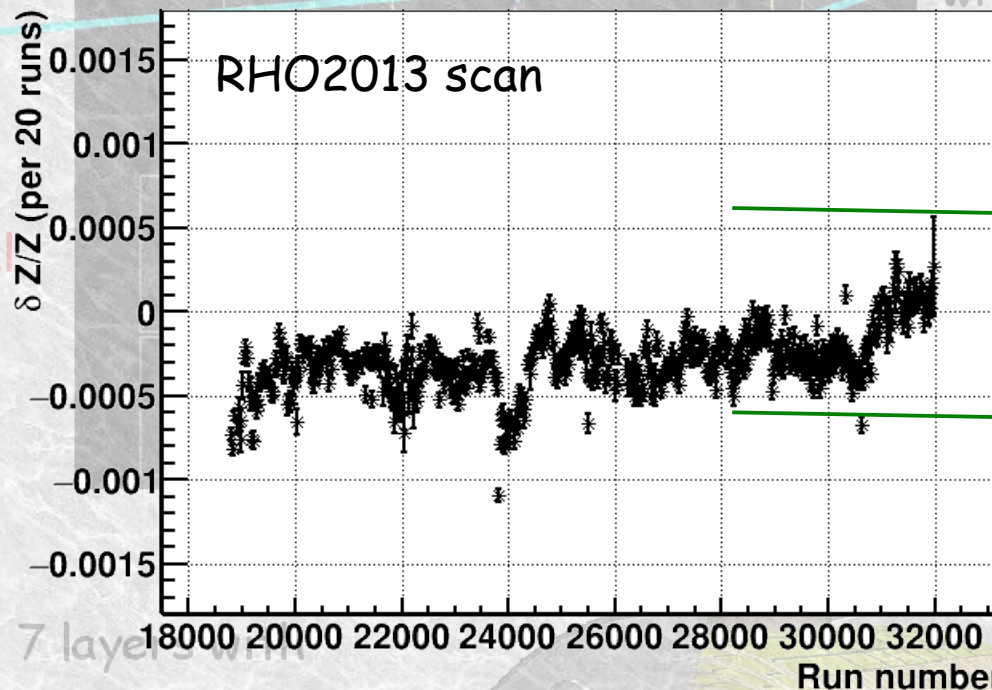
combined strip size: 10-15 mm  
Coordinate resolution  $\sim 2\text{mm}$

Both subsystem  
with strip precision  $< 100 \mu\text{m}$   
give  $< 0.1\%$  in Luminosity determination



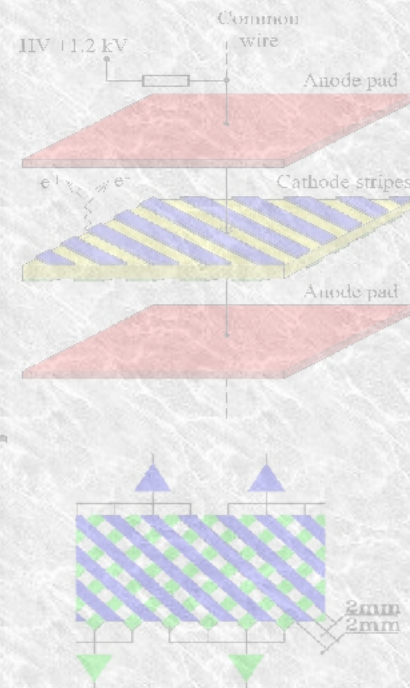
# Precision of fiducial volume

## Monitoring of z-measurement between ZC vs LXe



Variation because of  
DCh instability,  
different B field,  
ZC noise level

strips size: 6mm  
coordinate resolution ~ 1mm  
 $\pm 0.1\%$  Luminosity determination at  $\theta > 1\text{rad}$



Polar angle measured by  
DC chamber  
with help of charge  
division method  
(Z resolution ~ 2mm),  
Unstable, depend on  
calibration and thermal  
stability of electronic  
Calibration done  
relative to ZC (LXe)

### LXe calorimeter

ionization collected in 7 layers  
cathode strip readout,

combined strip size: 10-15 mm  
Coordinate resolution ~ 2mm

Both subsystem  
with strip precision < 100  $\mu\text{m}$   
give < 0.1% in Luminosity determination

# MC generators

High experimental precision relies on theoretical precision of MC tools:

Most recent  $e+e^- \rightarrow e+e^-$  (gamma) generators

include exact  $O(\alpha)$  + some parts from High Order terms:

MCGPJ (VEPP-2000) - accuracy 0.2% for  $e+e^-$ ,  $\pi+\pi^-$  etc

1 real photon (from any particle)

+ photon jets along all particles (collinear Structure function)

BabaYaga@NLO (KLOE, BaBar) - 0.1% for  $e+e^-$ ,  $\mu+\mu^-$

Parton shower approach: n photons with angle distribution

interference for 1 photon radiation

BHWIDE (LEP) - 0.5% ( $\sim 0.1\%$ ?),  $e+e^-$

n real photons by Yennie-Frautschi-Suura (YFS) exponentiation method

interference on  $O(\alpha)$  level

And there are other generators for different channels:

PHOKHARA (KLOE)  $\mu+\mu^-$ ,  $\pi+\pi^-$  etc

KKMC ( $\mu+\mu^-$ ),

etc



# BabaYaga@NLO vs MCGPJ generators

BabaYaga@NLO used by KLOE, BaBar

MCGPJ used by Novosibirsk group

Selection cuts:

$$|\Delta\varphi| < 0.15, |\Delta\theta| < 0.25$$

$$1 < \theta_{\text{average}} < \pi - 1$$

$$P^{+-} > 0.45 E_{\text{beam}}$$

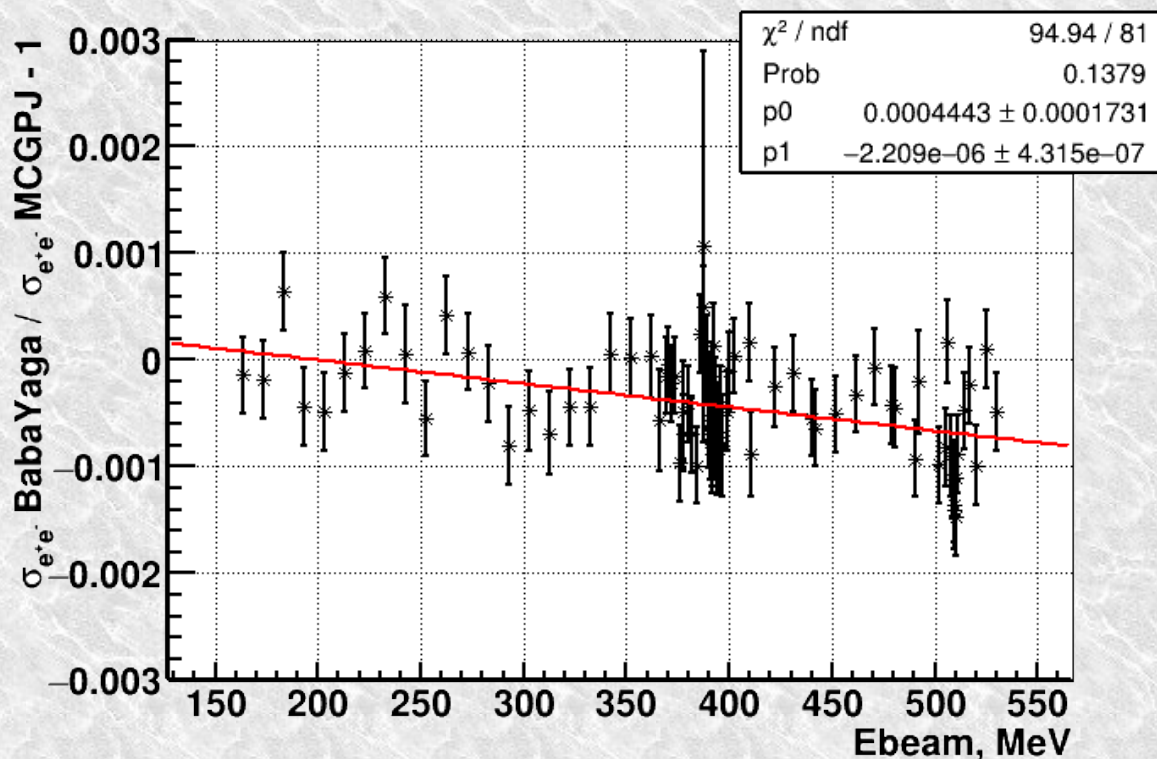
Calculated cross-section

at  $E_{\text{beam}} = 391.48 \text{ MeV}$

MCGPJ :  $751.671 \pm 0.034 \text{ nb}$

BabaYaga@NLO :  $751.218 \pm 0.059 \text{ nb}$

$$\Delta \sim 0.06\%$$



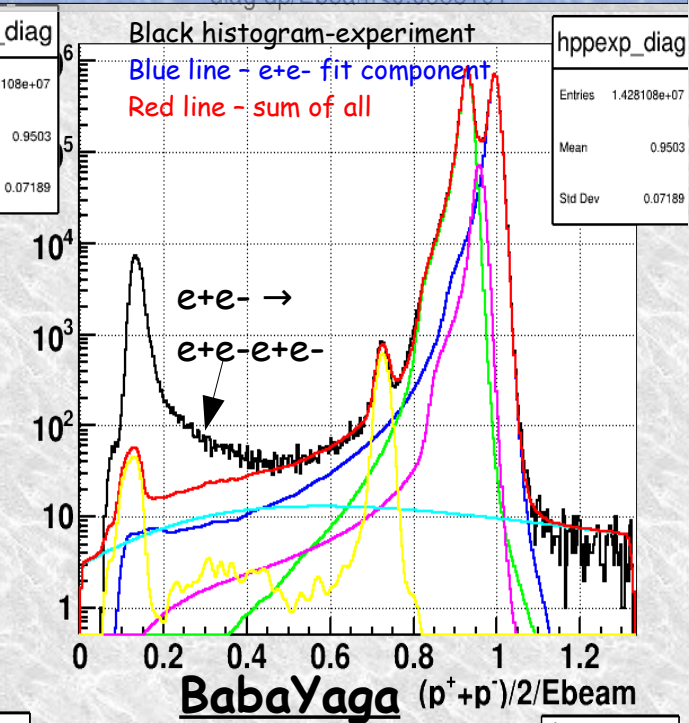
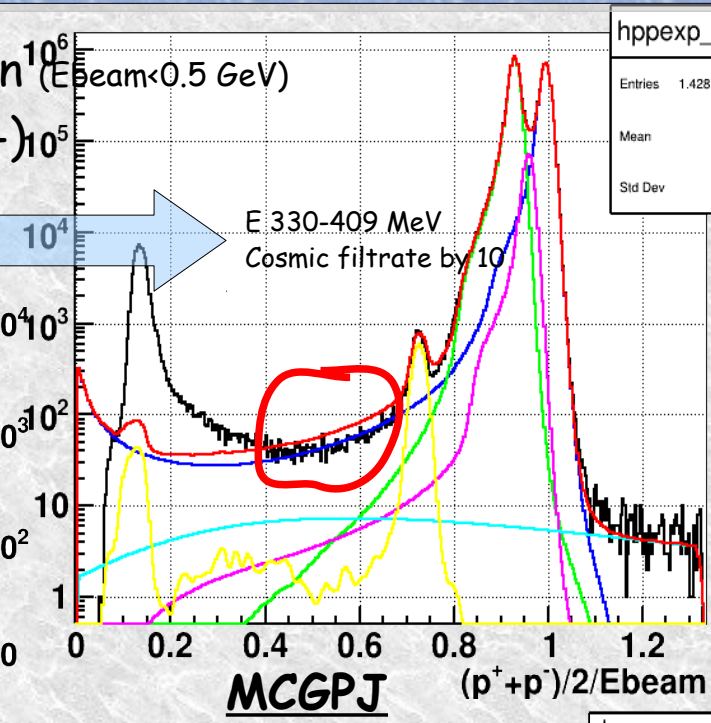
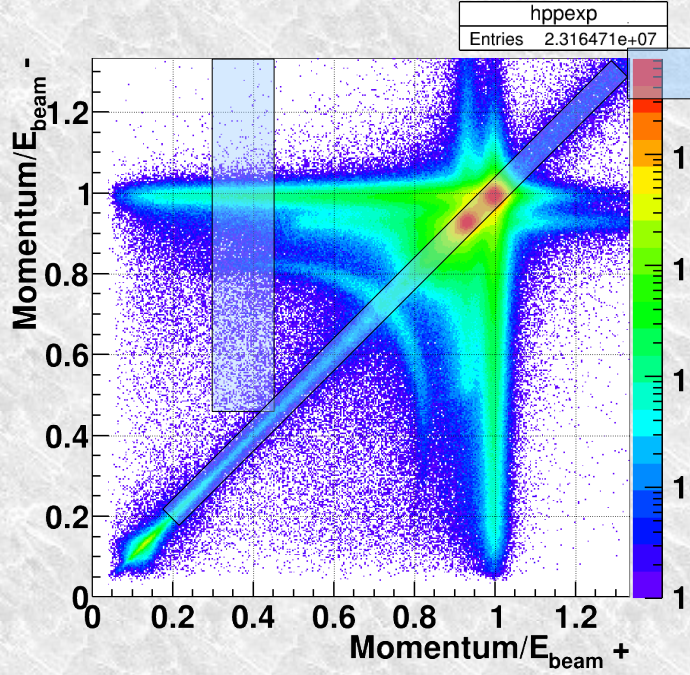
Integrated cross-section  
**consistent at the level <0.1%**

BabaYaga@NLO ~ x1000 slower than MCGPJ

A discrepancy was observed in momentum distribution of experimental data vs fitted functions with input from MCGPJ

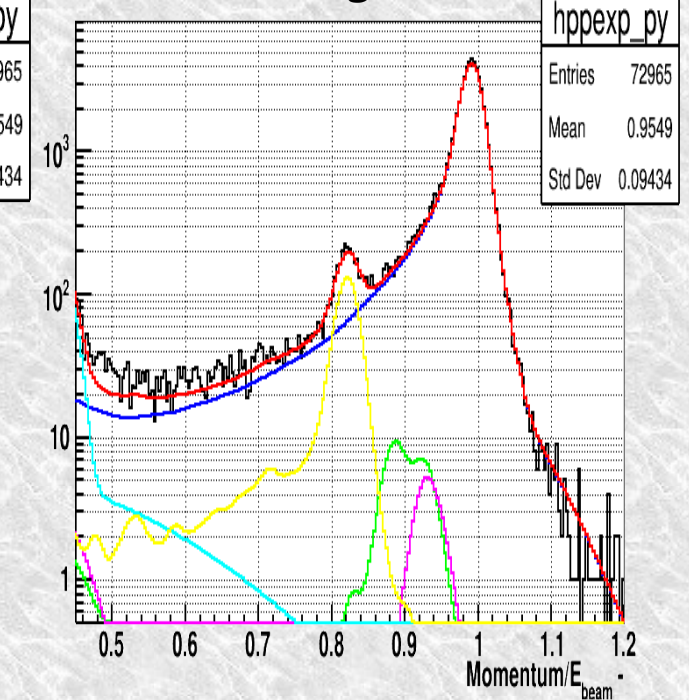
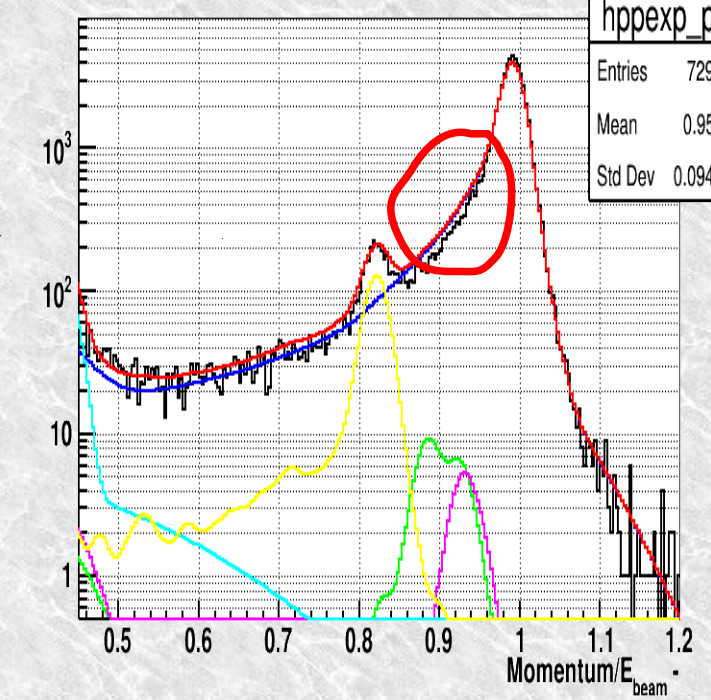
# BabaYaga @ NLO vs MCGPJ vs experiment

All events from RHO2013 scan ( $E_{beam} < 0.5 \text{ GeV}$ )  
 (~ 10 millions of  $e^+e^-$  and  $\pi^+\pi^-$ )



BabaYaga better describe experimental data

MCGPJ should be improved by adding angular distribution to photon jets



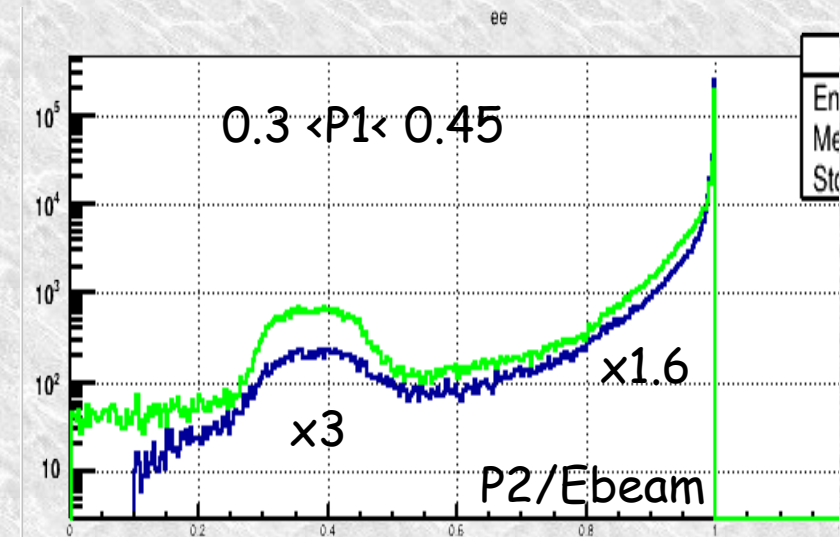
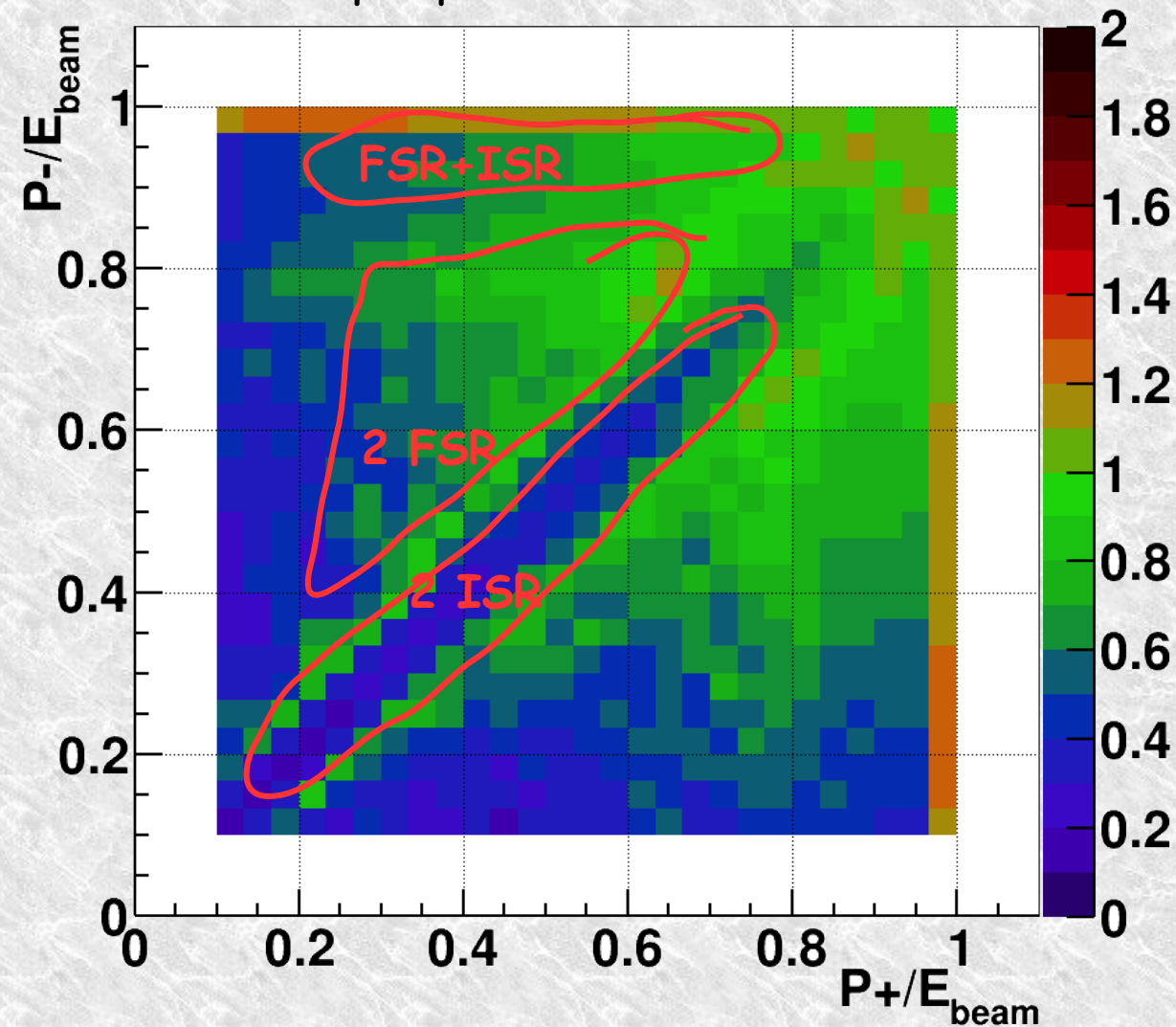


# BabaYaga @ NLO vs MCGPJ

Ebeam = 391.48 MeV

Comparison of momentum spectrum from generators  
BabaYaga divided by MCGPJ

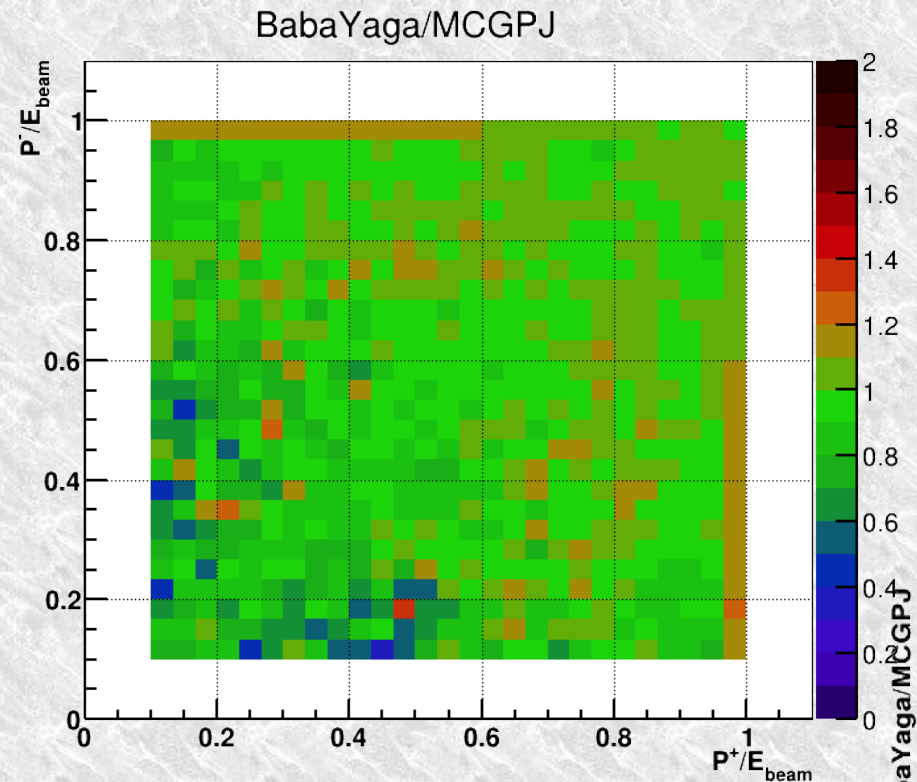
$$\frac{\partial^2 \sigma}{\partial p^+ \partial p^-} \text{BabaYaga/MCGPJ}$$



# MCGPJ vs BabaYaga

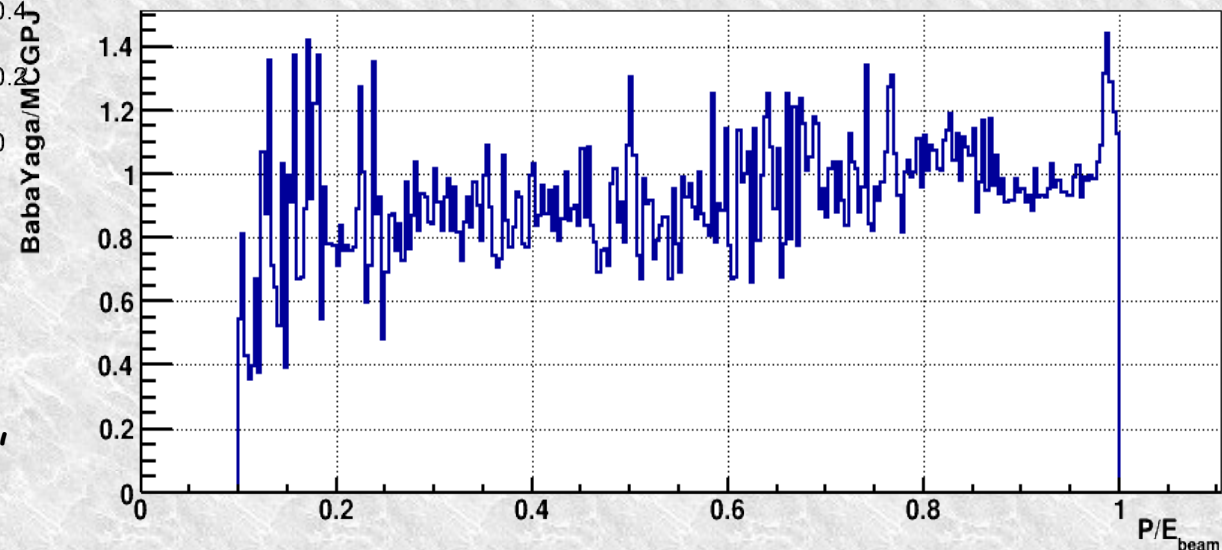
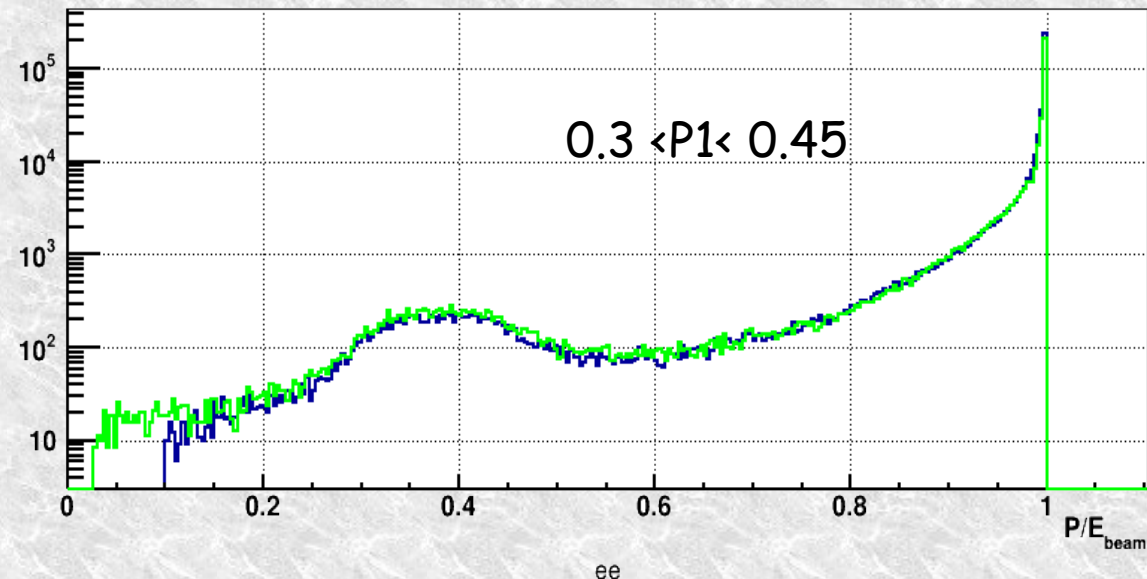
After adding angle distribution for jets

$E_{\text{beam}} = 391.48 \text{ MeV}$



$$|\Delta\varphi| < 0.15, |\Delta\theta| < 0.25,$$
$$1 < \theta_{\text{average}} < \pi - 1$$

Also we want to redo "compensator"



For precision  $\sim < 0.1\%$  necessary to have exact  $e^+e^- \rightarrow e^+e^- \gamma\gamma$  contribution



# Theta distribution for separation

$E = 391.48 \text{ MeV}$

First attempt:

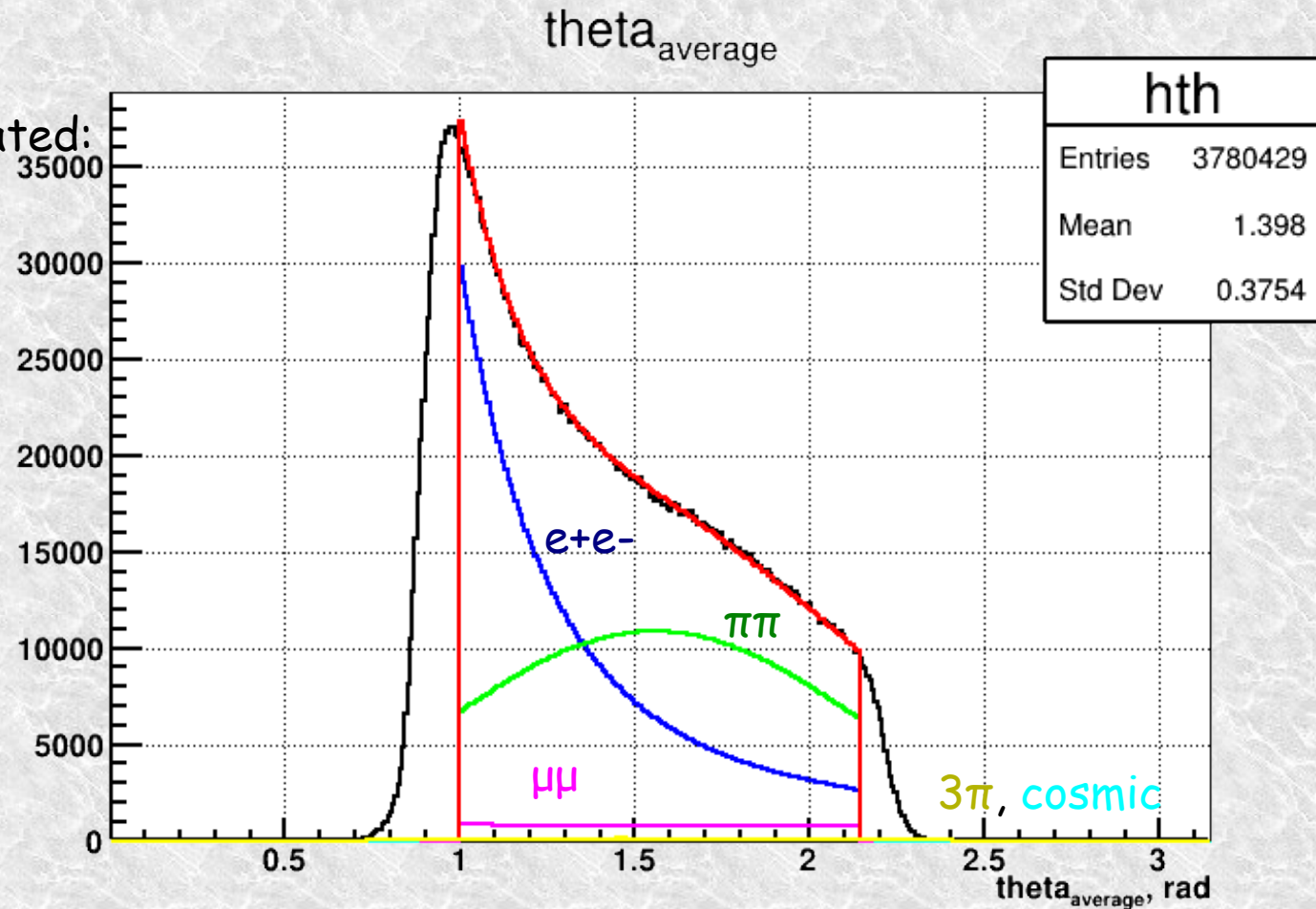
In approximation of not correlated:  
 $f(\theta)$  and  $f(p^+, p^-)$

$f(\theta)$

$e^+e^-$ ,  $\mu\mu$ ,  $\pi\pi$  - from generator

$3\pi$  - from simulation

Cosmic - from events not in  
VEPP time phase



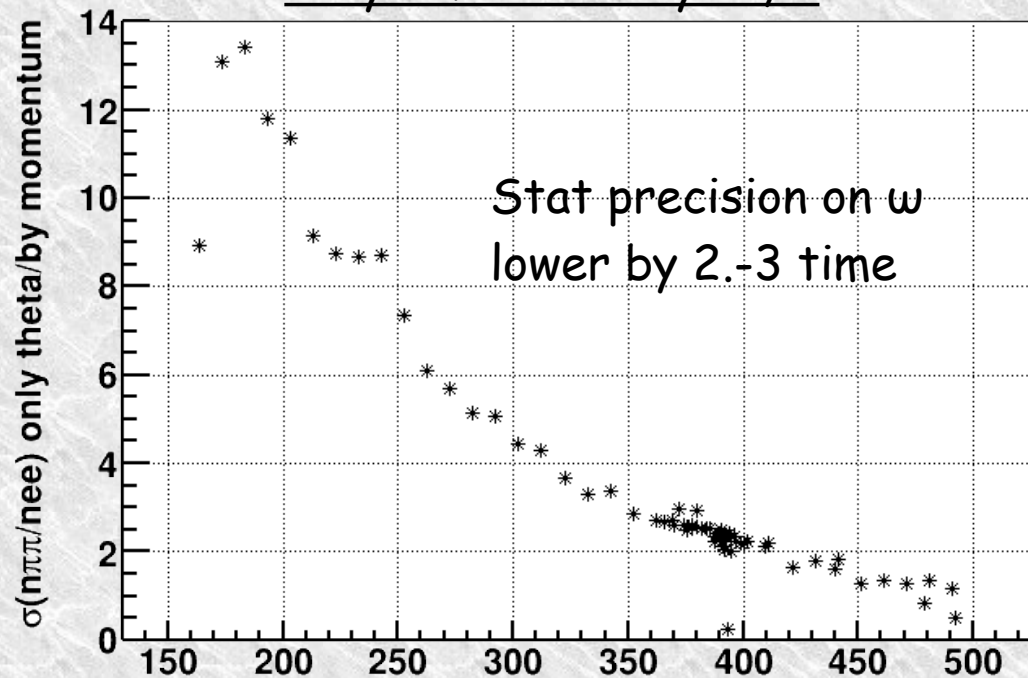
For real usage should be included (as additional parameters):

- 1) z-scale
- 2) spread from angle resolution
- 3) efficiency versus theta



# Theta distributions vs momentum separation

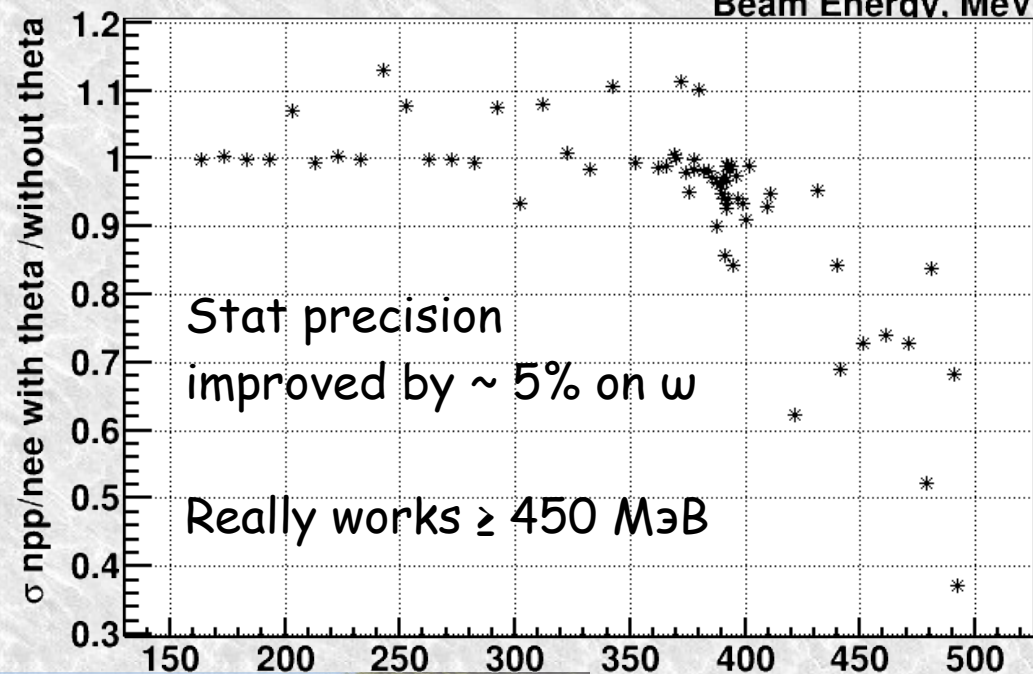
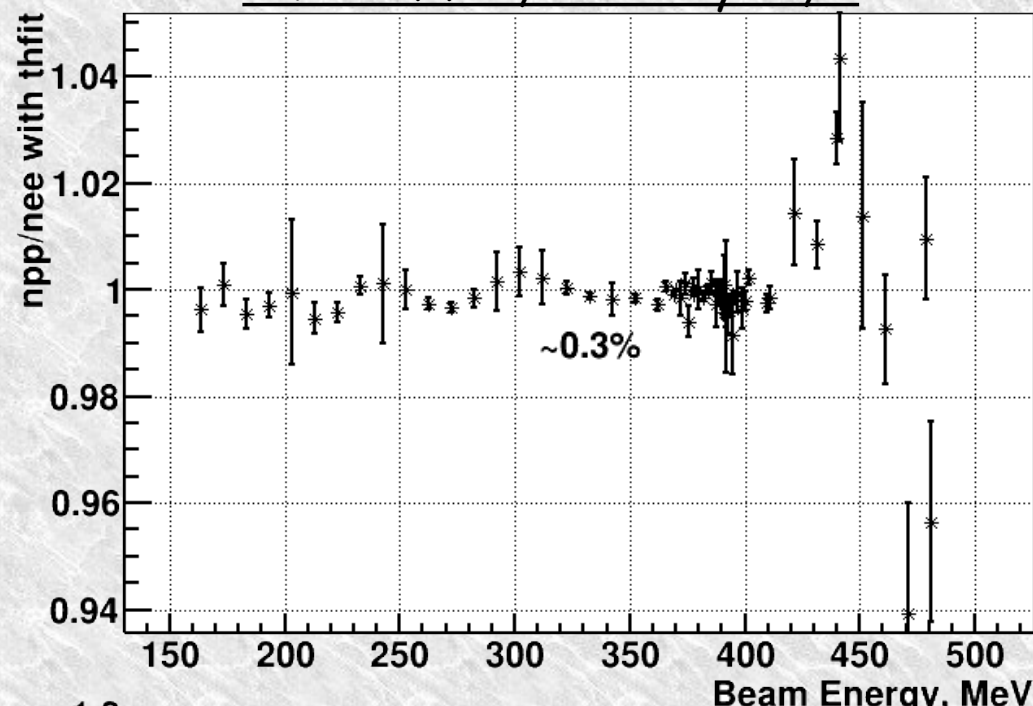
Only Theta vs only P+,P-



For precision ~ 0.1%

can be additional cross check of fidiucal volume determination

Theta && P+,P- vs only P+,P-



# $\pi^+\pi^-\pi^0$ background

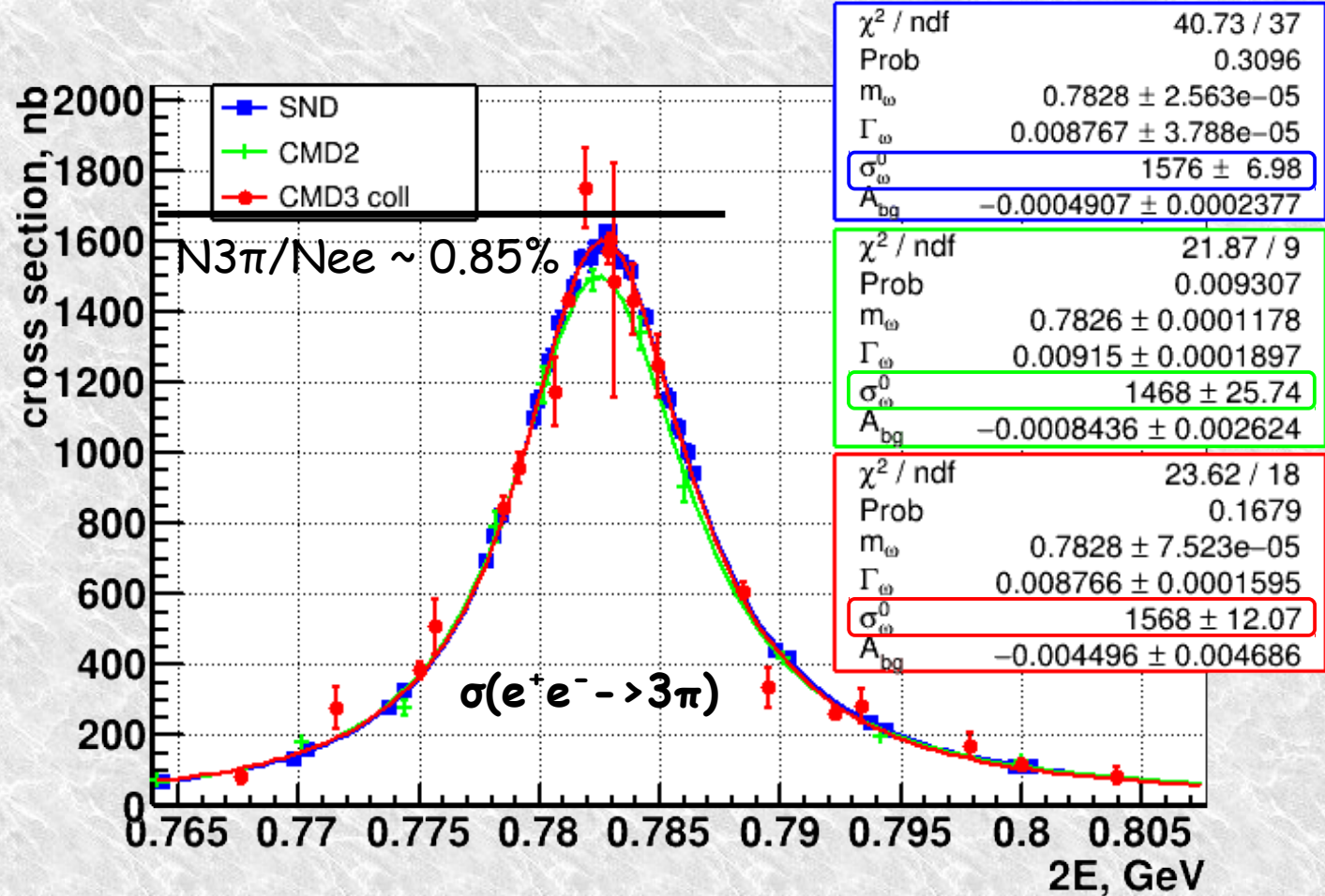
Only significant physical background in selected data sample:

$\pi^+\pi^-\pi^0$  on  $\omega$ -resonance

Contribution < 1%

This events well seen during particle separation by momentum distributions

Extracted  $\sigma(e^+e^- \rightarrow 3\pi)$  from collinear events (in phase space model) compatible with published results



$\epsilon(3\pi) = 0.4833\%$  acceptance efficiency from simulation by phase space model

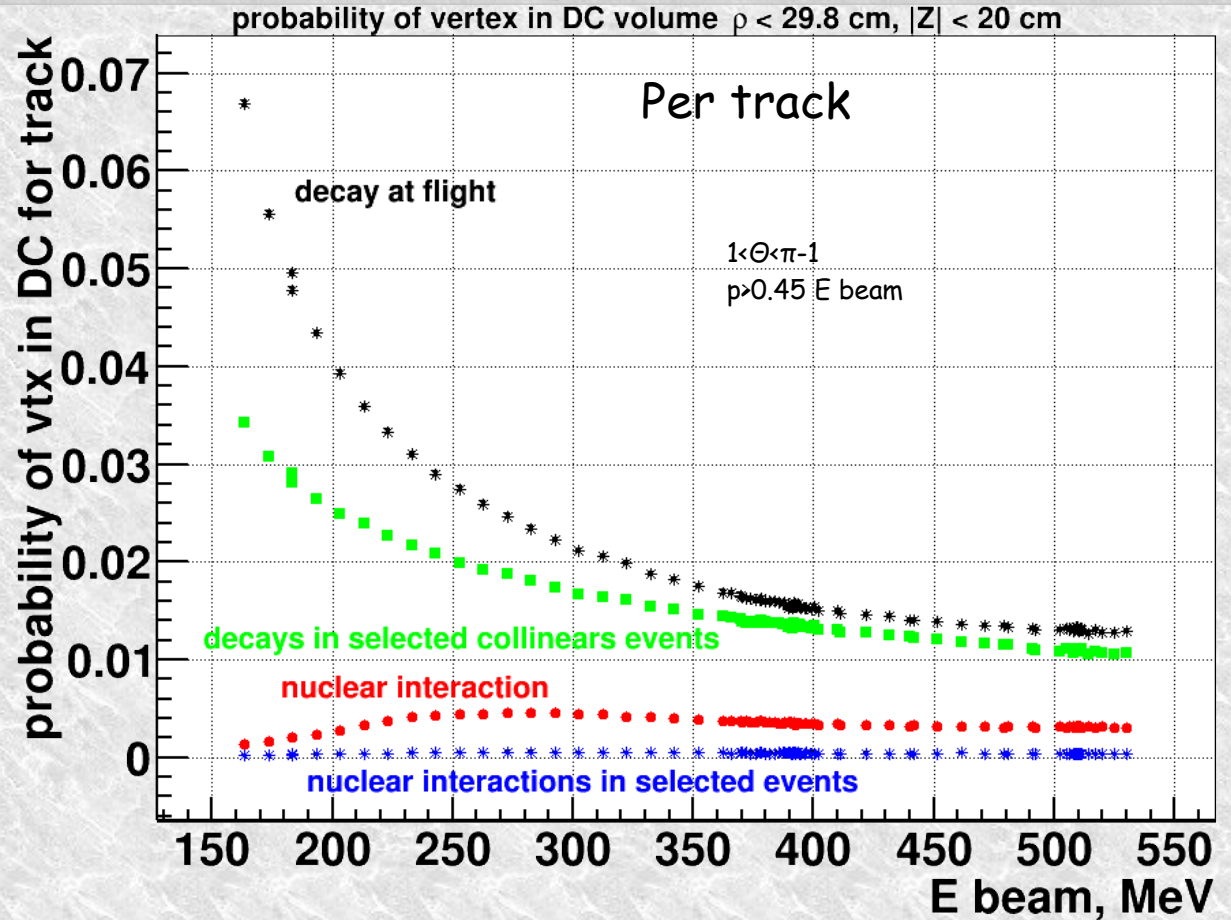
# Pion inefficiency

1.5 - 7 % of pions decay in volume of Drift chamber  
More than half pass selections

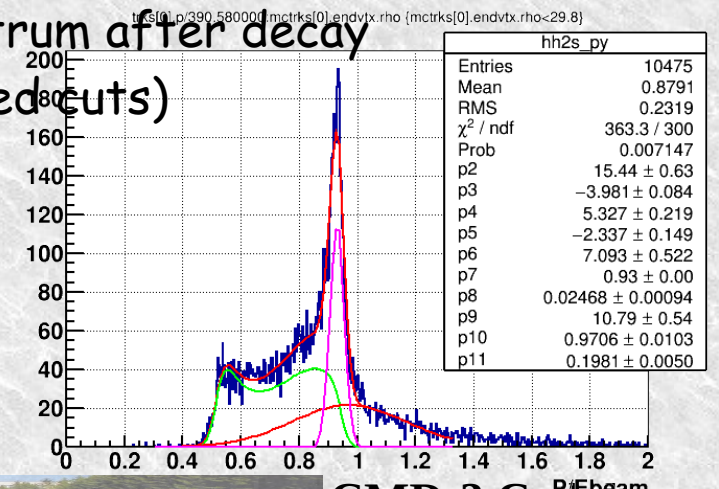
## Cuts inefficiencies

$E < 350$  MeV 6.5 - 0.5 %  
above  $\sim 0.5 - 0.4$  %

$< 0.5$  % of pions have nuclear interaction in Drift chamber (mostly on vacuum tube),  
All events are lost after cuts (survived  $< 0.06$  %)



## Pion spectrum after decay (in selected cuts)

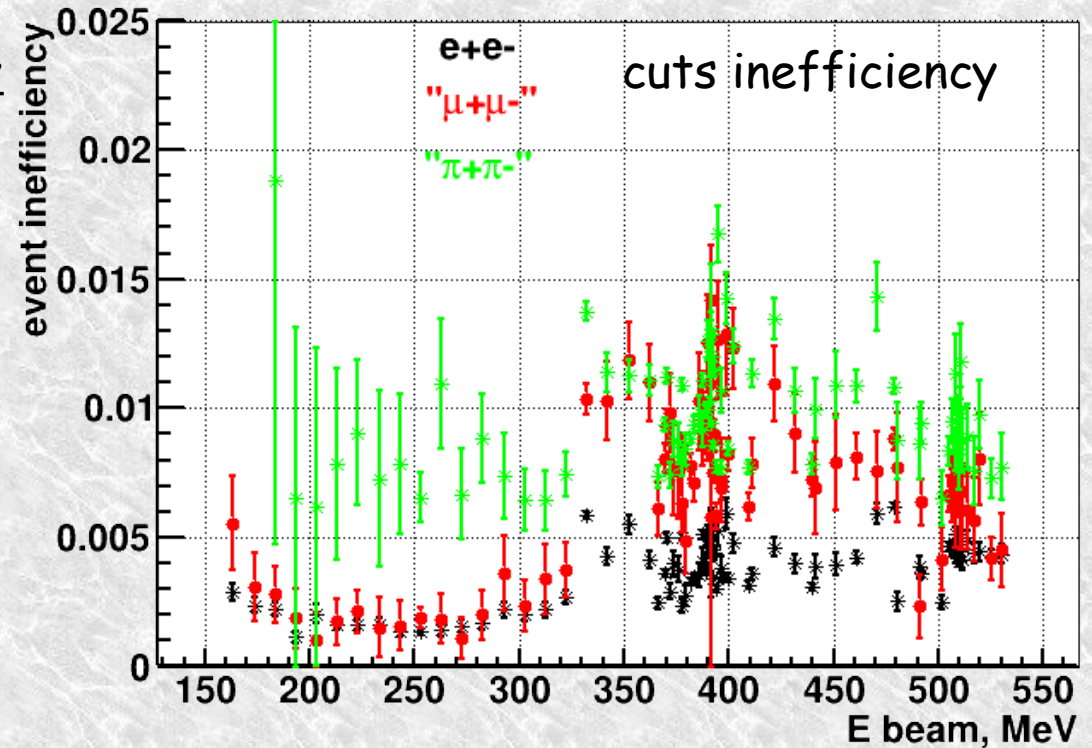


Nuclear interaction coorection (not depend on detector performance):  
from simulation or can be studied from  $\omega \rightarrow 3\pi$   
**Decay at flight (depend on detector efficiency):**  
behavior of momentum spectrum with variation of cuts

# efficiencies

Part of track reconstruction inefficiency  
from test events  
selected only by 2 collinear clusters in  
calorimeter  
-> check if a track was reconstructed  
or not

Inefficiency  $\sim 0.2-1\%$   
3-10 times less than was at CMD-2



Pion specific loss of events:

x decay in flight ( $\sim 6\%$  at 160 MeV) (dominated at low energies )

x nuclear interaction on vacuum tube ( $< 1\%$ )

Can be checked from  $\varphi \rightarrow 3\pi$  ,  $\omega \rightarrow 3\pi$  events

# Systematic $e^+e^- \rightarrow \pi^+\pi^-$ by CMD3

As our grand total(not reached yet)

Our goals are to reach systematic level up to 0.35%:

x Radiative corrections - 0.1%

x  $e/\mu/\pi$  separation - 0.2%

can be checked and combined from different methods

x Fiducial volume - 0.1%

controlled independently by LXe and ZC subsystems

x Beam Energy - 0.1 %

measured by method of Compton back scattering  
of the laser photons( $\sigma_E < 50$  keV)

x Pion specific correction - 0.1%

decay, nuclear interaction taken from data

0.3% - with current MCGPJ  
need precision < 0.07%

Many systematic studies rely on high statistics



# Conclusion

- x VEPP-2000 collider successfully operates with a goal to get  $\sim 1\text{fb}^{-1}$  in 5-10 years which should provide new precise results on the hadron production
- x We have upgraded the CMD-3 detector, with much better performance and monitoring of different detector subsystems
- x First scan  $< 1\text{ GeV}$  for  $\pi^+\pi^-$  measurement was done
- x High statistics allow us to study and to control better different systematic contributions, with final goal up to 0.35%
- x More data expected after VEPP-2000 upgrade with new positron injection facility



# $e^+e^- \rightarrow e^+e^-e^+e^-$

diag dp/Ebeam < 0.1

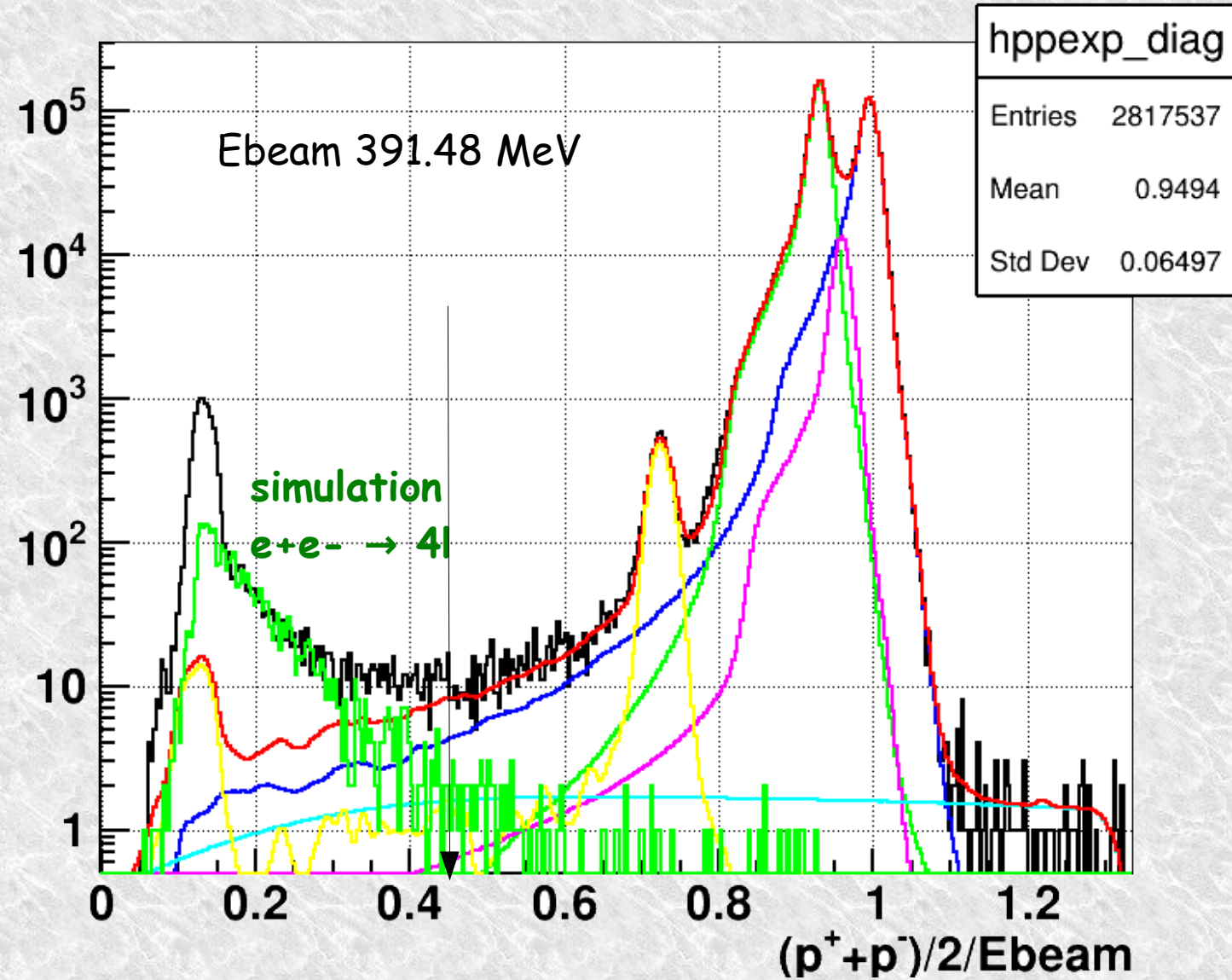
Diag36 generator (1986)

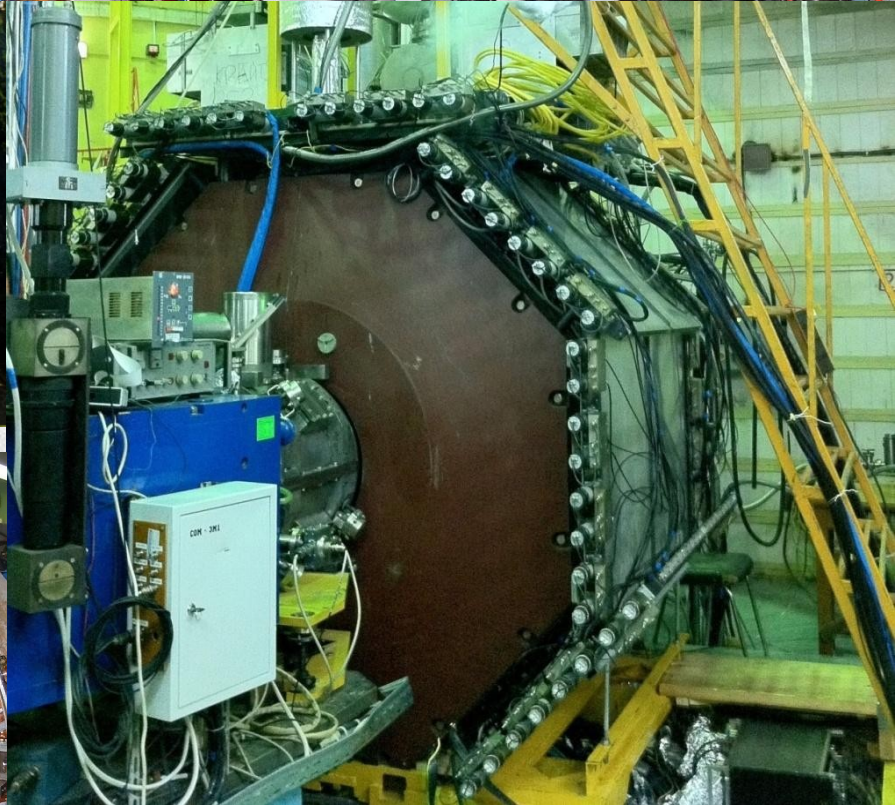
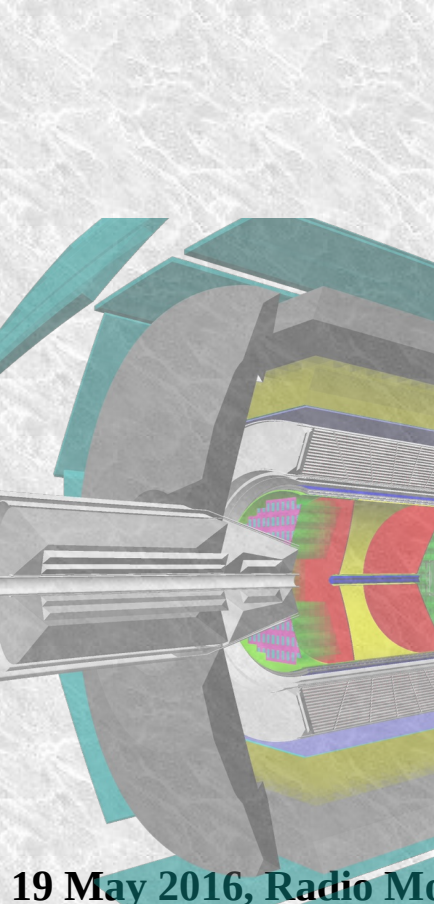
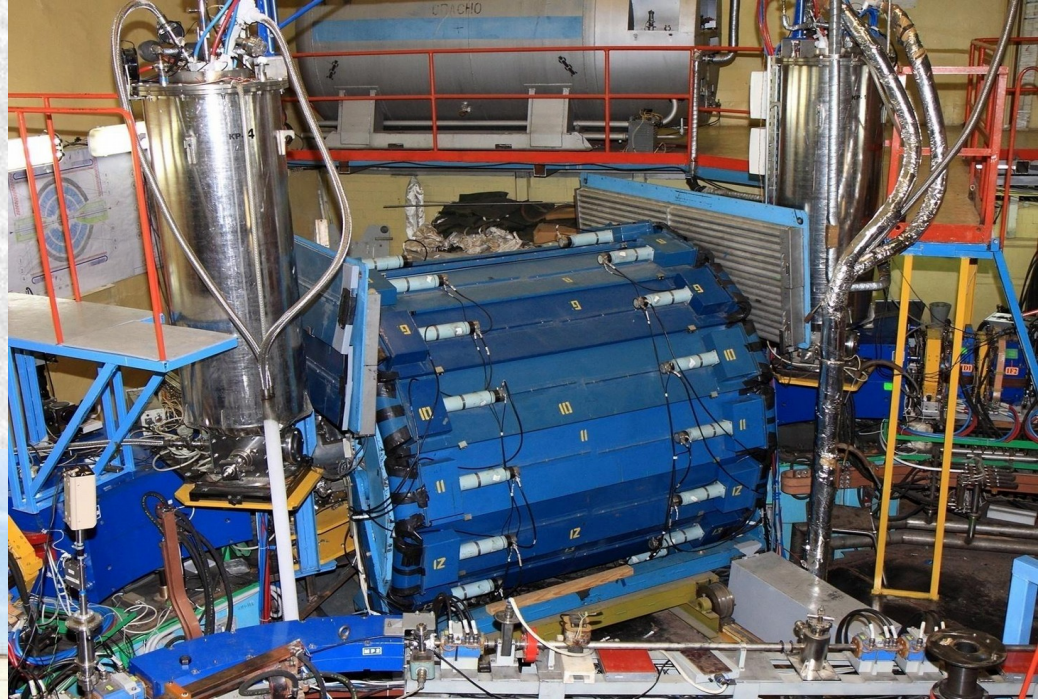
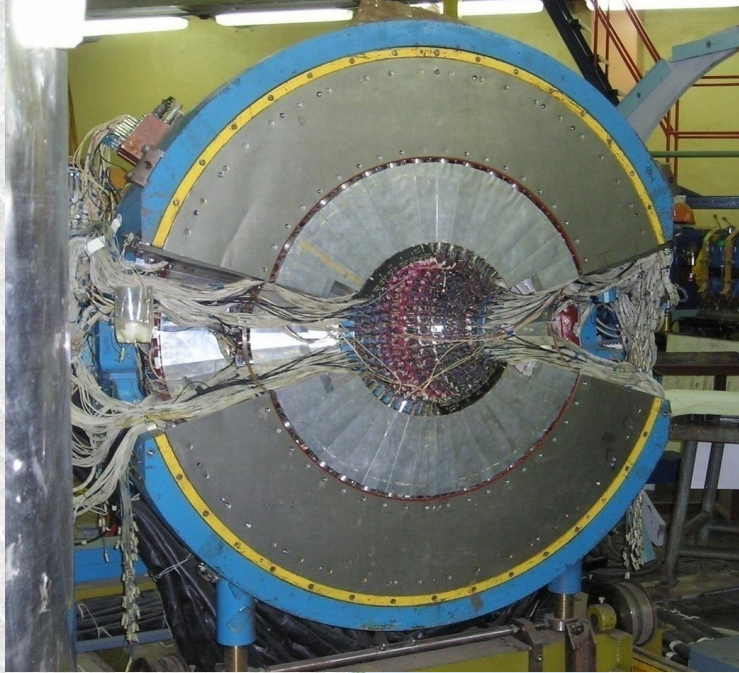
F.A.Berends et al.

<http://inspirehep.net/record/238520>

All diagrams for 4 lepton in final state

Main contribution from 2 photon annihilation

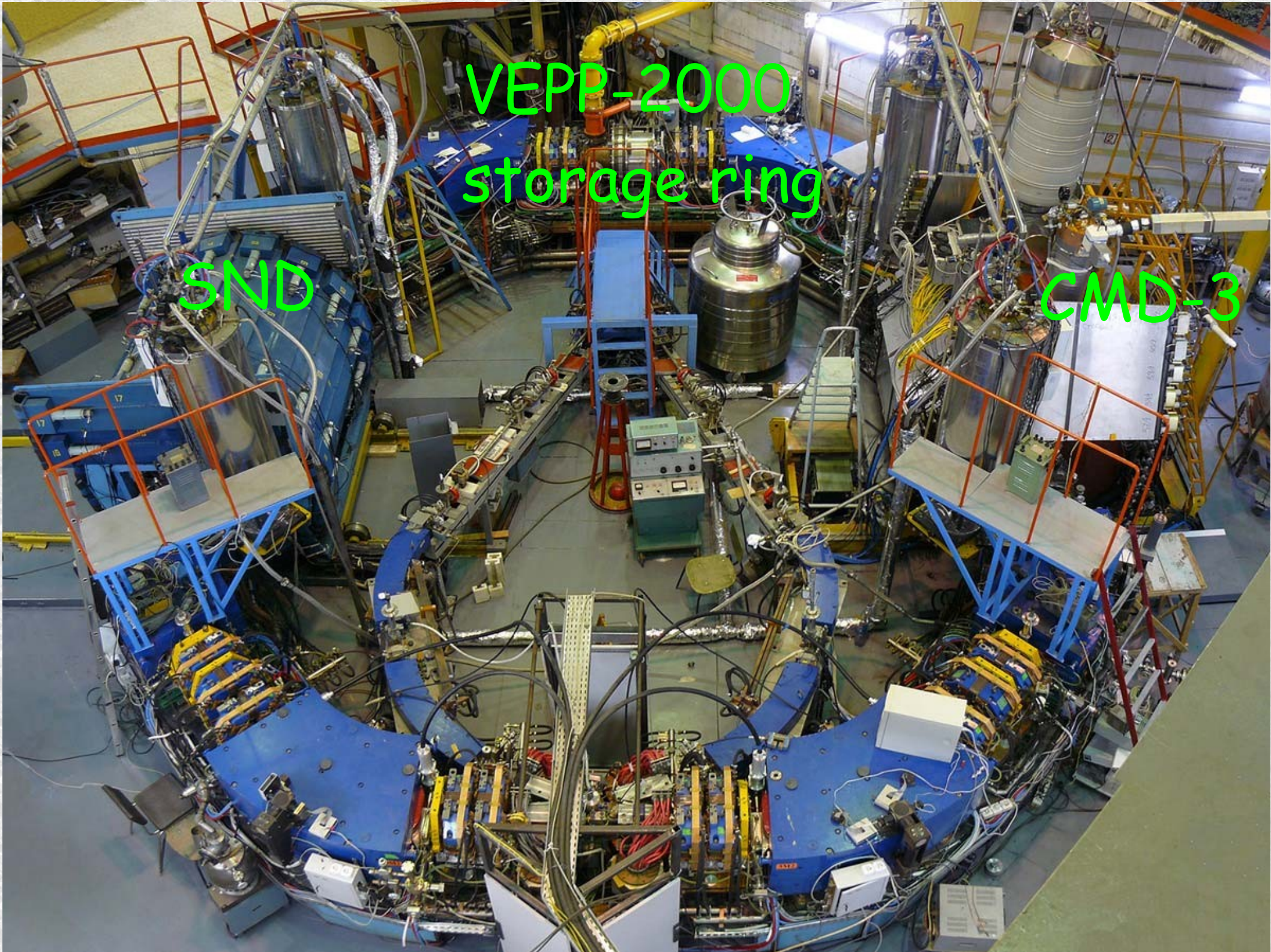




VEPP-2000  
storage ring

SND

CMD-3



# SM prediction for muon g-2

ArXiv:1010.4180, arXiv:1105.3149

$$a_{\mu}^{\text{experimental}} = (g-2)_{\mu} / 2$$

$$11\,659\,208.9 \pm 6.3 \times 10^{-10} \text{ world average}$$

$$a_{\mu}^{\text{theory}} = a_{\mu}^{\text{QED}} + a_{\mu}^{\text{EW}} + a_{\mu}^{\text{hadron}}$$

QED contribution	11 658 471.808 ± 0.015	Kinoshita & Nio, Aoyama et al
EW contribution	15.4 ± 0.2	Czarnecki et al
NLO hadronic	-9.8 ± 0.1	HLMNT11

## Hadronic contributions

From measured cross-section by dispersion integral

$$\text{LO hadronic} \quad 694.1 \pm 4.3 \times 10^{-10} \text{ HLMNT 11}$$

main channels contribution to precision at  $\sqrt{s} < 1.8 \text{ GeV}$

$\pi^+\pi^-$	$505.65 \pm 3.09$	
$\pi^+\pi^-2\pi^0$	$18.62 \pm 1.15$	
$\pi^+\pi^-\pi^0$	$47.38 \pm 0.99$	(mostly from omega region)
$2\pi^+2\pi^-$	$13.64 \pm 0.36$	(BaBar)
$K^+K^-$	$22.95 \pm 0.26$	(BaBar)

from Isospin relations  $5.98 \pm 0.42$  for not measured  $KK\pi, KK2\pi, 2\pi4\pi^0, 2\pi3\pi^0$

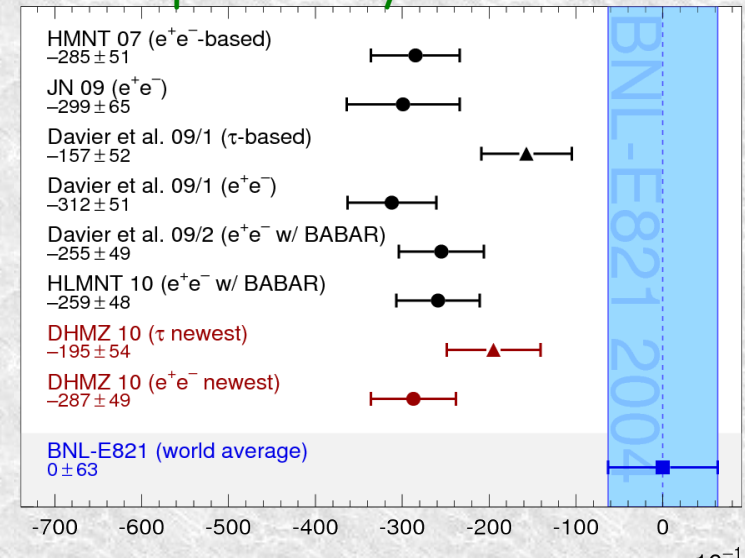
(or  $12.46 \pm 0.76$  for  $\sqrt{s} < 2 \text{ GeV}$ ) (contribution at 1.5-3σ of total error - crucial if something is wrong with used isospin relations)

$$R_{\text{qcd}}[2-11.09\text{GeV}] \quad 41.19 \pm 0.82$$

$$\text{Light-by-light} \quad 10.5 \pm 2.6 \text{ Prades, de Rafael & Vainshtein}$$

$$\text{Theory TOTAL} \quad \pm 4.9$$

$\Delta \text{Exp} - \text{Theory} \sim 3.3-3.6\sigma$



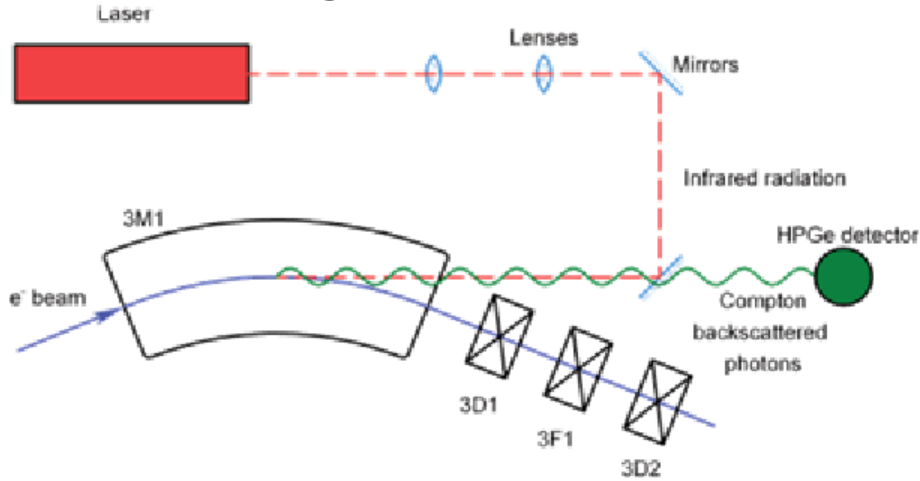
$a_{\mu} - a_{\mu}^{\text{exp}}$   
New g-2 experiments at FNAL and J-PARC have plans to reduce error to  $1.5 \times 10^{-10}$

need more theory input, probably with help of experimental transition form factors

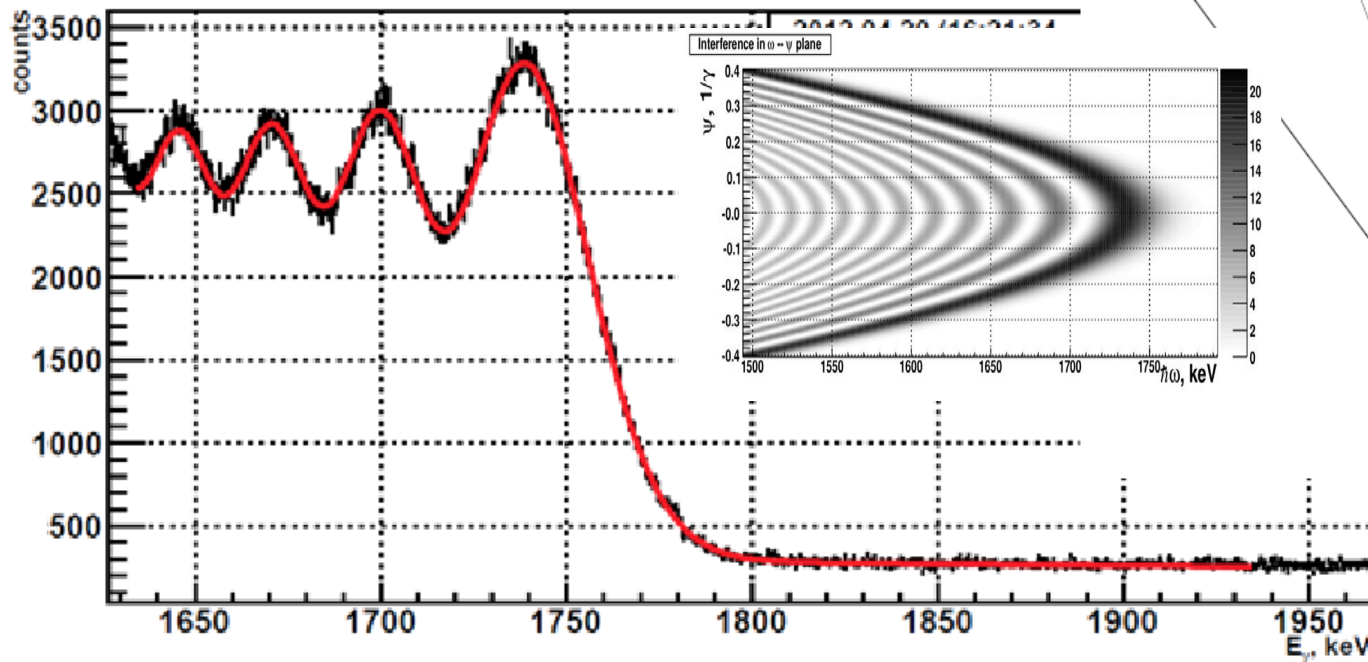
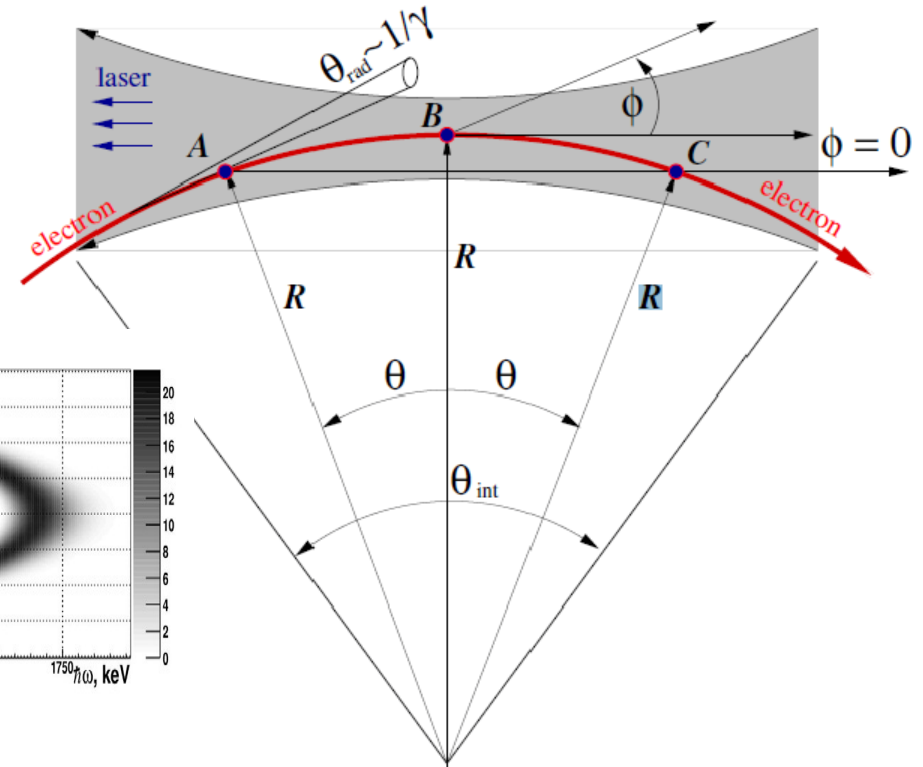
From direct integration Without model constraints  $\delta a_{\mu}$

# Energy measurement by Compton back scattering

Starting from 2012, energy is monitored continuously using compton backscattering



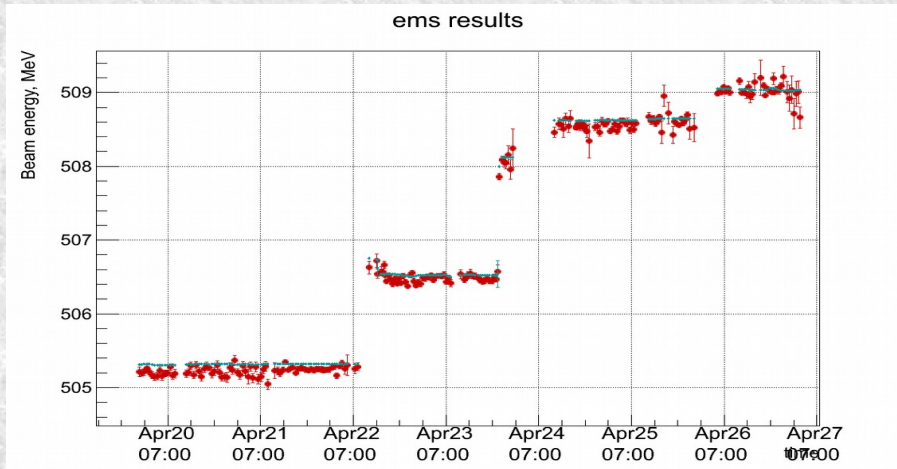
Излучение из точек А и С под углом  $\phi = 0$  интерферирует



$$E = 993.662 \pm 0.016 \text{ MeV}$$

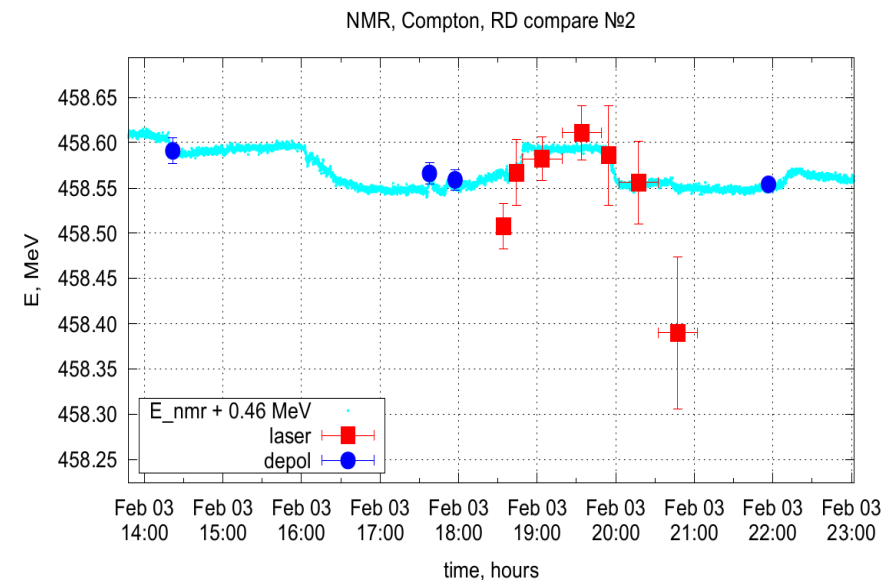
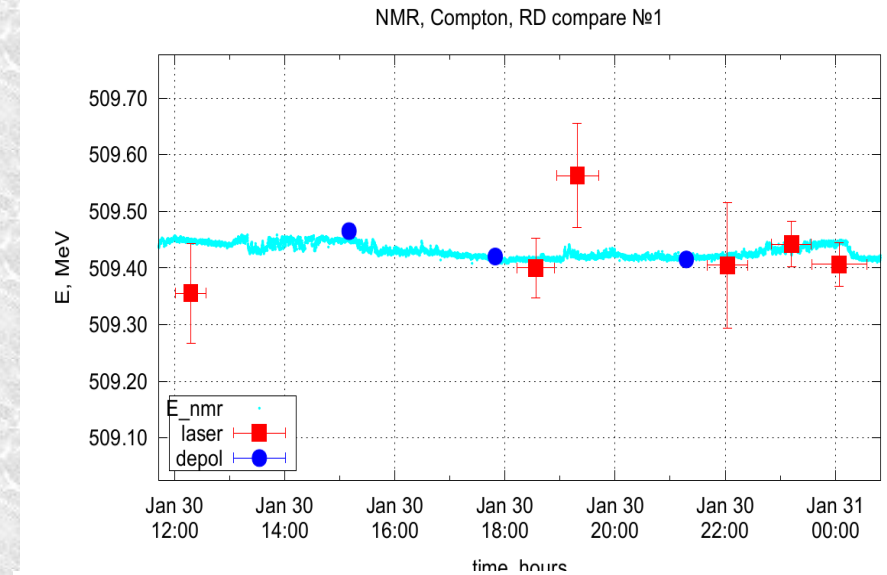
# Beam energy measurement at VEPP-2000

- **Magnetic field control in bending magnets**
  - 8x2 NMR probes, continuous control
  - Absolute calibration using:
    - $\phi$ -meson ( $1019.455 \pm 0.020$  MeV),
    - $\omega$ -meson ( $782.65 \pm 0.12$  MeV).
- **Measurement of photon energy from back scattering laser light**
  - Installed in 2012.
  - Needs beam current (20  $\mu$ A),  $\sim 20$ -50 keV accuracy in 10 min
  - Energy control during data taking.



- **Resonance depolarization method**
  - Very high accuracy ( $\delta E/E < 10^{-5}$ ).
  - Special configuration of VEPP-2000: "warm"

Methods comparison:



# Pion formfactor

