

Progress on PHOKHARA

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Outline

- 1 χ_c production through radiative corrections
- 2 Radiative corrections to pion pair production
- 3 Conclusions

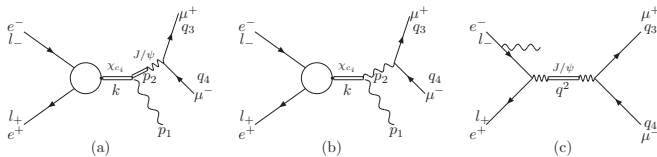
Production of charmonium resonances with J^{++}

- Electromagnetic production only through higher order electromagnetic process.
- Strongly suppressed by ordinary annihilation through one photon to J^{--}
- High luminosity colliders (eg. BESIII) are needed.
- Signal can be observed in reactions:

$$e^+e^- \rightarrow \chi_c \rightarrow \textit{hadrons}$$

$$e^+e^- \rightarrow \chi_c \rightarrow \gamma J/\psi (\rightarrow \mu^+\mu^-)$$

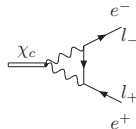
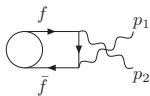
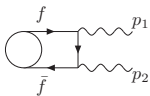
Cross section for the process $e^+e^- \rightarrow \chi_c \rightarrow \gamma J/\psi (\rightarrow \mu^+\mu^-)$



- Background (Fig.(c)) has to be taken into account
- $\sqrt{s} = M_{\chi_c}$
- ω_γ has to be chosen in the proper kinematic region
- possible contribution from a diagram from Fig.(b) is negligible for our event selections:

$$9.58916 < Q^2 < 9.59262$$

Short distance approximation



- $A(\chi_c \rightarrow \gamma\gamma) \propto \phi'(0)$
- Terms $\propto b$ in the $A(\chi_c \rightarrow \gamma\gamma)$ break gauge invariance

$$c_\gamma = \frac{4e^2 a}{\sqrt{m}} \frac{1}{(M_\chi^2/2 + b^2/4 + bM_\chi/2)^2}$$

- $b = 2m - M_{\chi_c}$
- $a = \sqrt{\frac{1}{4\pi}} 3Q^2 \phi'(0)$

$$\Gamma_{1ee} = \frac{1}{3} \frac{|g_1|^2}{4\pi} M_{\chi_{c1}}$$

$$\Gamma_{2ee} = \frac{1}{5} \frac{|g_2|^2}{8\pi} M_{\chi_{c2}}$$

J. H. Kuhn, J. Kaplan and E. G. O. Safiani, Nucl. Phys. B **157** (1979) 125.

$$x = \frac{4m^2}{M_{\chi_{c_i}}^2} \rightarrow 1$$

$$g_{1\gamma\gamma} \rightarrow \frac{16\sqrt{2}\alpha^2 a}{M_{\chi_{c_1}}^{5/2}} 2(\log(-2z_i) - i\pi)$$

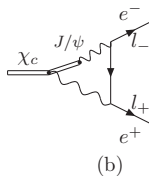
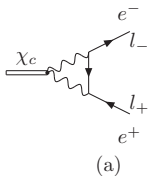
$$g_{2\gamma\gamma} \rightarrow \frac{64\alpha^2 a}{M_{\chi_{c_2}}^{5/2}} [(\log(-2z_i) - i\pi) + \frac{1}{3}(i\pi + \log 2 - 1)]$$

$$z_i = \frac{b_i}{M_{\chi_{c_i}}},$$

$$|\phi'(0)|^2 = 0.1 \text{ GeV}^5$$

	Γ_{1ee}	Γ_{2ee}
	$b = 0.5 \text{ GeV}$	
Leading term	0.0226 eV	0.0243 eV
exact result	0.0317 eV	0.0159 eV
	$b = -0.5 \text{ GeV}$	
Leading term	0.164 eV	0.0512 eV
exact result	0.141 eV	0.0731 eV

Binding energy corrections



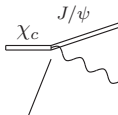
$$\Gamma_{1ee} = \frac{1}{3} \frac{|g_1|^2}{4\pi} M_{\chi_{c1}}$$

$$\Gamma_{2ee} = \frac{1}{5} \frac{|g_2|^2}{8\pi} M_{\chi_{c2}}$$

$$g_i = g_{i\gamma\gamma} + g_{iJ/\psi\gamma}$$

$\chi_c - \gamma\gamma$ FF

$$c_\gamma = \frac{4e^2}{\sqrt{m}} \left(a + \frac{fa_J}{M_{J/\psi}^2} \right) \frac{1}{(M_\chi^2/2 + b^2/4 + bM_\chi/2)^2}$$

 $\chi_c - \gamma J/\psi$ FF

$$c_{J/\psi} = \frac{4ea_J}{\sqrt{m}} \frac{1}{(M_\chi^2/2 + b^2/4 + bM_\chi/2 - M_{J/\psi}^2/2)^2}$$

- $b = 2m - M_{\chi_c}$
- $a = \sqrt{\frac{1}{4\pi}} 3Q^2 \phi'(0)$
- $f = \sqrt{\frac{3\Gamma_{J/\psi \rightarrow e^+e^-} M_{J/\psi}^3}{4\pi\alpha^2}}$
- a_J - free parameter

H. Czyż, J. H. Kühn and S. Tracz (in preparation)

$$\begin{aligned}
 a &= 0.073 \text{ GeV}^{5/2} \\
 |\phi'(0)|^2 &= 0.04 \text{ GeV}^5 \\
 a_J &= 0.11
 \end{aligned}$$

$$\begin{aligned}
 m &= 1.7 \text{ GeV} \\
 b_1 &= -0.204 \text{ GeV} \\
 b_2 &= -0.249 \text{ GeV}
 \end{aligned}$$

$$\begin{aligned}
 \Gamma(\chi_{c1} \rightarrow e^+e^-) &= \frac{M_{\chi_{c1}}}{3\pi} \left[\frac{|g_1|^2}{4} + \frac{aG_F}{\sqrt{2}mQ^2} \text{Re}(g_1) \right. \\
 &\quad \left. + \frac{a^2 G_F^2}{mQ^4} \left(1 - 4 \sin^2 \theta_W + 8 \sin^4 \theta_W \right) \right],
 \end{aligned}$$

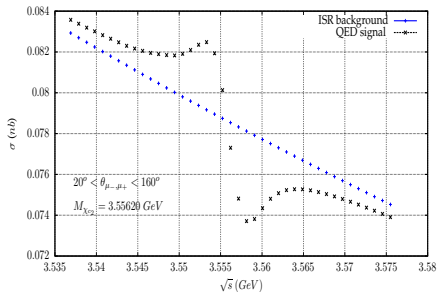
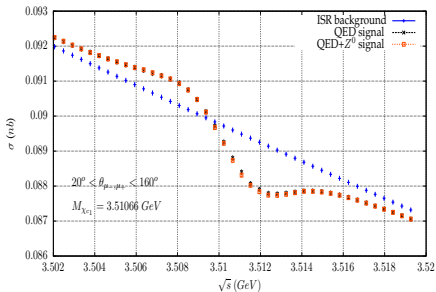
Electronic widths

	$\gamma\gamma + J/\psi\gamma$	$\gamma\gamma$	$J/\psi\gamma$	QED+ Z^0
Γ_{1ee} [eV]	0.078	0.073	0.003	0.071
Γ_{2ee} [eV]	1.35	0.032	0.975	-

$$e^+e^- \rightarrow \chi_c \rightarrow \gamma J/\psi (\rightarrow \mu^+\mu^-)$$

$$\Gamma_{1ee} = 0.071 \text{ eV}$$

$$\Gamma_{2ee} = 1.35 \text{ eV}$$



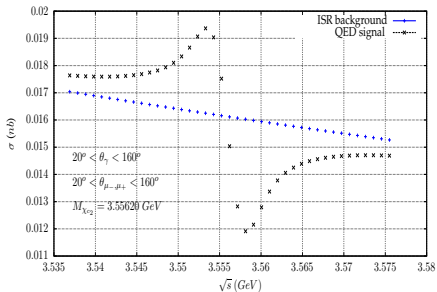
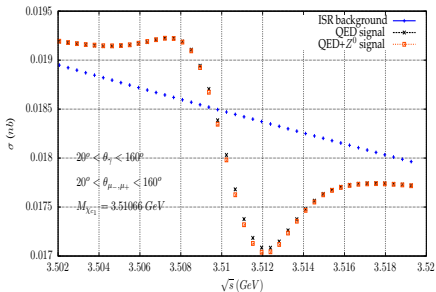
$\Delta E = 1 \text{ MeV}$ beam resolution per beam was assumed.

H. Czyż, J. H. Kühn and S. Tracz (in preparation)

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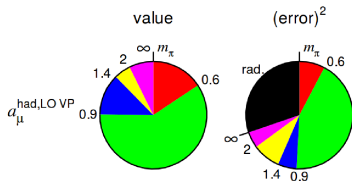


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H. Czyż, J. H. Kühn and S. Tracz (in preparation)

Corrections to the reaction $e^+e^- \rightarrow \pi^+\pi^-\gamma$

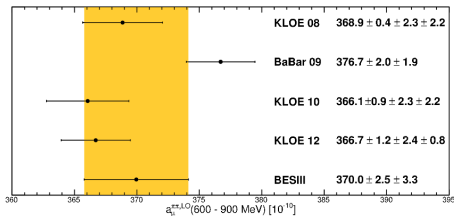
F. Campanario, H.Czyż, Sz. Tracz, D. Zhuridov, J. Gluza, T. Jeliński, T. Riemann



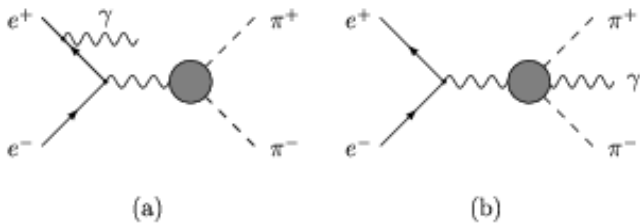
D. Nomura's talk

Matter to the Deepest, Ustroń
2015.

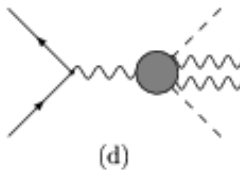
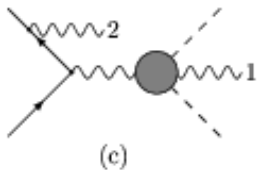
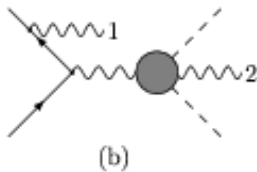
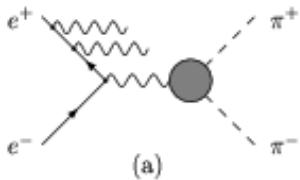
M. Ripka [BESIII Collaboration],
Acta Phys. Polon. B **46** (2015)
no.11, 2261.



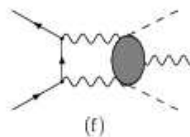
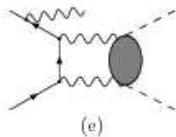
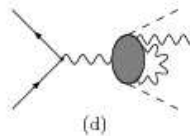
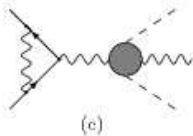
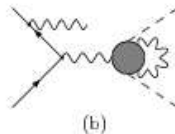
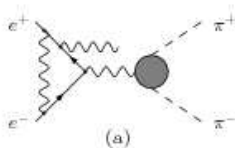
Born amplitudes



Two photons emission

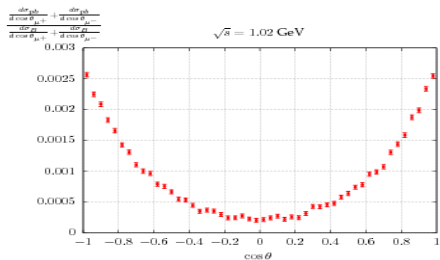
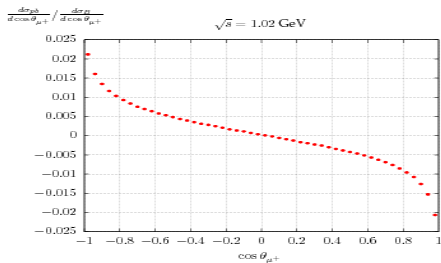


Virtual corrections



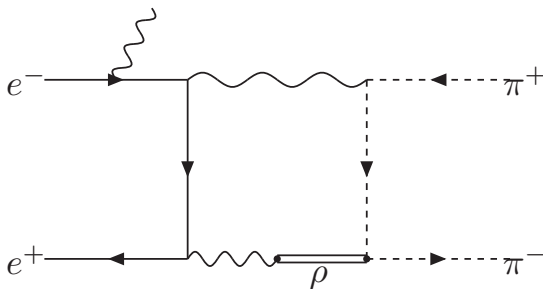
- Diagrams describing virtual corrections contribute through their interference with the Born amplitude.
- sQED
 - including form Factor
 - 2 independent codes

sQED - we do not expect large contributions



F. Campanario, H. Czyż, J. Gluza, M. Gunia, T. Riemann, G. Rodrigo and V. Yundin, JHEP 1402 (2014) 114, [arXiv:1312.3610 [hep-ph]].

FF -possible resonant enhancement for Q near to the mass of the ρ



Final remarks

- Direct resonant production of $\chi_{c1,2}$ lead to measurable resonant enhancement in cross section.
- The prediction exhibits a sizeable model dependence.
- Resonant signal both in the hadronic cross section and in the $\gamma\mu^+\mu^-$ channel could be seen at the BESIII
- We keep working on radiative corrections to pions pair production and expect the first results soon.