

Claim of discoveris based on sigma's

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Preamble

(First slides from AT seminars at CERN)

Statistics lectures?

If I insist on **probability**, rather than speaking, very generally, about **statistics**, it is because I have good reasons.

Statistics lectures?

*As far as the laws of mathematics refer to reality,
they are not certain,
and as far as they are certain,
they do not refer to reality.*
(Einstein)

Statistics lectures?

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“If we were not ignorant there would be no probability, there could only be certainty. But our ignorance cannot be absolute, for then there would be no longer any probability at all. Thus the problems of probability may be classed according to the greater or less depth of our ignorance.”
(Poincaré)

Statistics lectures?

*“It is scientific only to say what is more likely
and what is less likely”*

(Feynman)

Statistics and truth (from lectures at CERN)

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- ▶ How to interpret the question?
 1. “Tell the Truth”?
 - ▶ What is the true value of a quantity?
 - ▶ What is the true theory that describes the world?
 2. “Tell the truth” \iff “to lie”?

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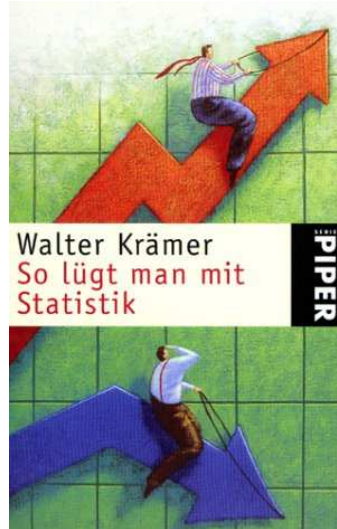
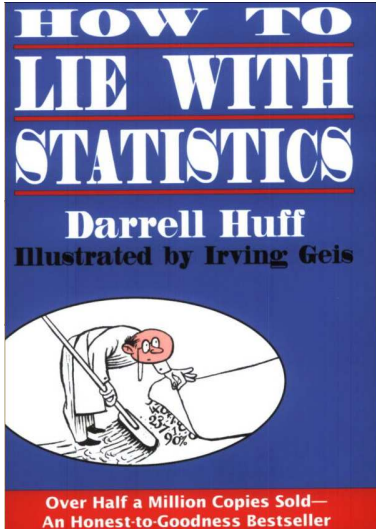
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*“There are three kinds of lies:
lies, damn lies, and statistics”
(Benjamin Disraeli/Mark Twain)*

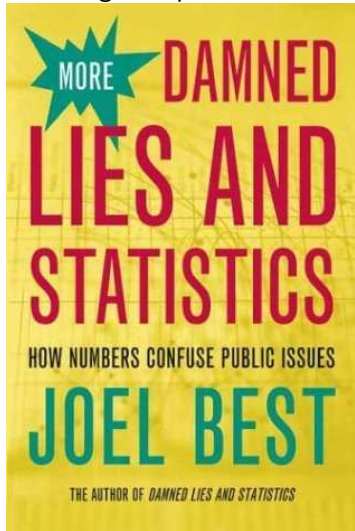
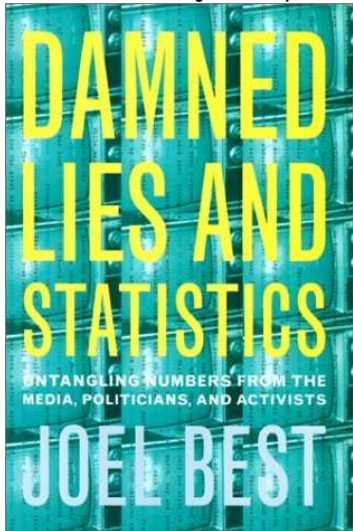
Damned lies and statistics

Well known subject



Damned lies and statistics

Well known subject, especially in marketing and politics





SCIENCE

Lies, Damned Lies and Physics

16 DEC 30, 2015 9:30 AM EST

By [Faye Flam](#)

To most of us, 93-to-1 odds would make for a clear-cut bet. To physicists? Not so much.

On Dec. 15, the New York Times [reported](#) that Santa may have brought physics a new subatomic particle, a hitherto unknown entity materializing in the giant collider at CERN, near Geneva. It wasn't a sure thing, but according to the Times, the odds are in the scientists' favor, with only a 1-in-93 chance that the data pointing to the particle represent a statistical fluke.

SCIENCE

Physicists in Europe Find Tantalizing Hints of a Mysterious New Particle

By DENNIS OVERBYE DEC. 15, 2015

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Does the [Higgs boson](#) have a cousin?

Two teams of physicists working independently at the [Large Hadron Collider](#) at CERN, the [European Organization for Nuclear Research](#), reported on [Tuesday](#) that they had seen traces of what could be a new fundamental particle of nature.

One possibility, out of a gaggle of



Researchers at the Large Hadron Collider at CERN are smashing together protons to search for new particles and forces.

Fabrice Coffrini/Agence France-Presse — Getty Images

“I don’t think there is anyone around who thinks this is conclusive,” said Kyle Cranmer, a physicist from New York University who works on one of the CERN teams, known as Atlas. “But it would be huge if true,” he said, noting that many theorists had put their other work aside to study the new result.

When all the statistical effects are taken into consideration, Dr. Cranmer said, the bump in the Atlas data had about a 1-in-93 chance of being a fluke — far stronger than the 1-in-3.5-million odds of mere chance, known as five-sigma, considered the gold standard for a discovery. That might not be enough to bother presenting in a talk except for the fact that the competing CERN team, named C.M.S., found a bump in the same place.

Le Scienze

EDIZIONE ITALIANA DI SCIENTIFIC AMERICAN

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Come risolvere il mi
dell'espansione acc
In edicola dal 4 ge

ABBONAMENTI E RINN



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optogenetica

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longevità

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19 dicembre 2015

Qualcosa di nuovo da LHC? Solo il tempo lo dirà



(Cortesia Maximilien Brice/CERN)

Nuovi dati degli esperimenti ATLAS e CMS del Large Hadron Collider del CERN di Ginevra hanno mostrato un eccesso nella produzione di coppie di fotoni, localizzato a una massa particolare. Ma è ancora troppo presto per dire se sia un primo segno di una nuova era per la fisica delle particelle oppure solo una fluttuazione del rumore di fondo *di Marco Delmastro*

Nel caso dell'eccesso sullo spettro delle coppie di fotoni, se uno prende il grafico di ATLAS in cui la montagna è più prominente, la probabilità che questa sia dovuta a una casualità è due su 10.000, dunque piuttosto piccola. Quando però consideriamo il fatto di aver cercato montagne un po' dappertutto, allora questa probabilità aumenta a due su 100. I numeri di CMS sono persino più grandi, indicando una probabilità ancora più grande che si tratti solo di una fluttuazione del rumore di fondo.

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“In the case of the excess in the two-photon spectrum, if one takes the ATLAS plot, where the bump is more prominent, the probability that this is due to randomness is 2 in 10,000, then rather small. When instead we consider the fact that we have been looking bumps everywhere, this probability increases to 2 in 100. CMS numbers are even larger, indicating an even larger probability that it is just a fluctuation of the background.”

Defining the issue

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Usually several things:

- ▶ **descriptive statistics** [e.g. Webster's (Kdict)]
 - ▶ “The science which has to do with the collection and classification of certain facts respecting the condition of the people in a **state**.”
 - ▶ “(pl.) Classified facts respecting the condition of the people in a state, their health, their longevity, . . . especially, those facts which can be stated in numbers, or in tables of numbers, or in any tabular and classified arrangement.”
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- ▶ **Probability theory**
- ▶ **Inference** ⇒ **primary interest to physicists**

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Inference: learning about **theoretical objects** from experimental **observations** (see later)

Where are the problems?

Descriptive statistics Little to comment, apart that the process of summarizing '*a State*' in a few numbers, in a diagram or in a table causes an enormous loss of detailed information, and this might lead to misunderstandings or even 'lies'.

⇒ the famous 'half chicken' joke.[†]

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Inference **Messy:**

▶ Traditionally, a collection of *ad hoc* prescriptions ... accepted more by authority than by full awareness of what they mean

⇒ The physicist is confused† between **good sense** and **statistics education**

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Inference Do better?

- ▶ Much improvement is gained if inference is grounded on probability theory
- ▶ Summaries of descriptive statistics can be used in those cases in which *statistical sufficiency* holds
(e.g. when we use the sample arithmetic average and standard deviation, instead of the n data points)

Statistics \leftrightarrow probability

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It is just because the ‘conventional’ statistical school misuses words and convey wrong messages (also among expert practitioners, as most [physicists](#)).

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2011: non only Opera...

- ▶ April, **CDF**: absolutely unexpected excess at about 150 GeV

$$\approx 3.2\sigma$$

- ▶ September, **Opera**: neutrinos faster than light

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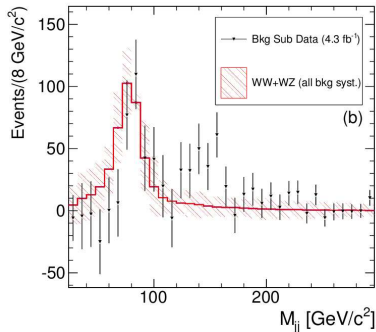
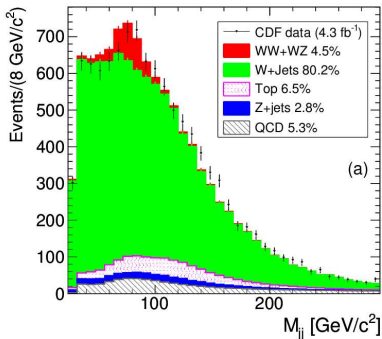
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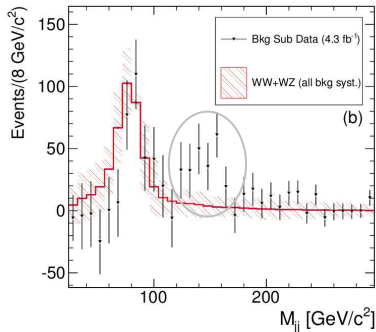
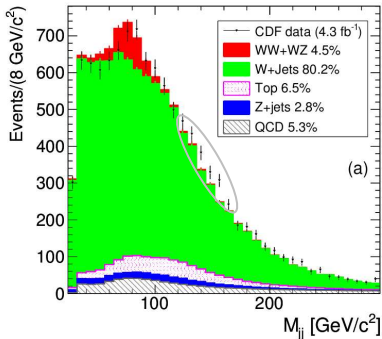
Why there was substantial **scepticism towards the first two announcements**, in contrast with a cautious/pronounced **optimism towards the third one**?

April 2011

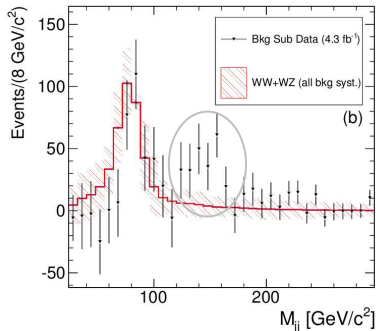
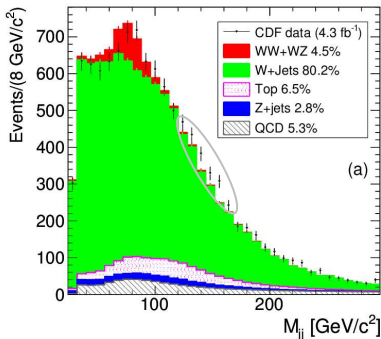
CDF Collaboration at the Tevatron



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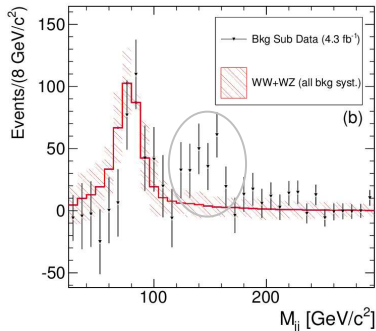
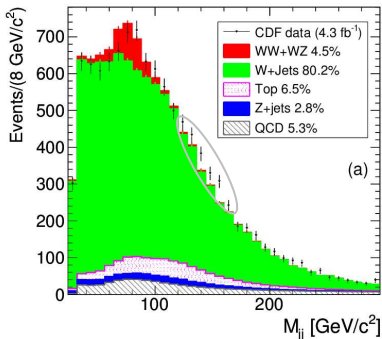
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April 2011

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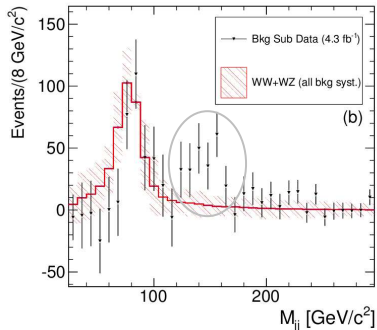
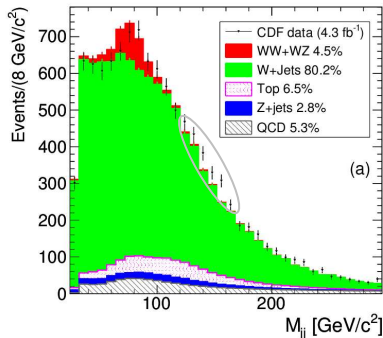


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3.2 σ !

April 2011

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What does it mean?

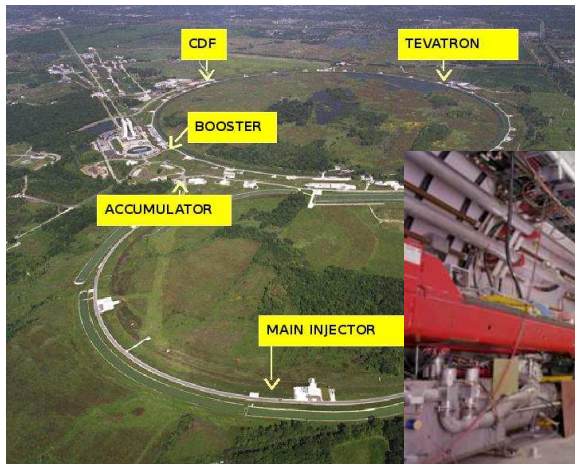
Tevatron and CDF

6.28 km, near Chicago



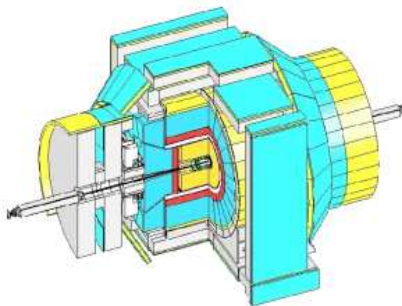
Tevatron and CDF

$$p \rightarrow \cdot \leftarrow \bar{p} \quad [\approx 1 \text{ TeV} + 1 \text{ TeV}]$$



Tevatron and CDF

CDF: a multipurpose ('hermetic') detector



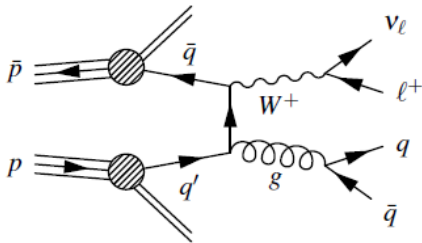
Tevatron and CDF

... a large, very sophisticated detector!



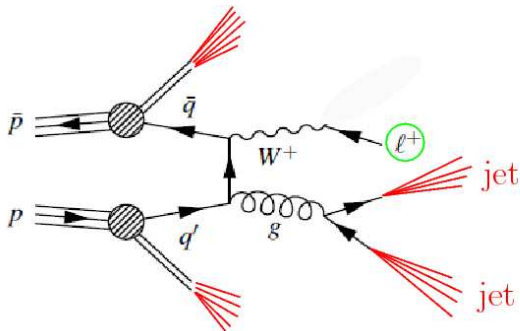
Jet-jet + W

$W + (q\bar{q})$ [+ 'remnants']



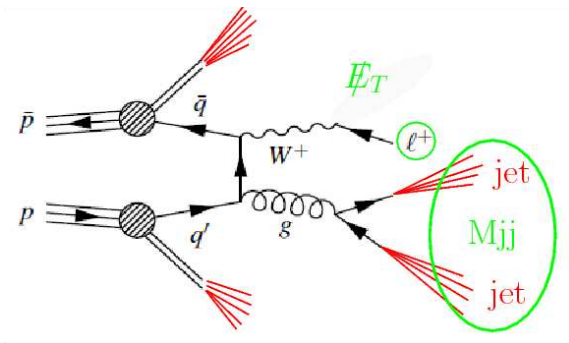
Jet-jet + W

$W + 2\text{jet}$ [+ much more]



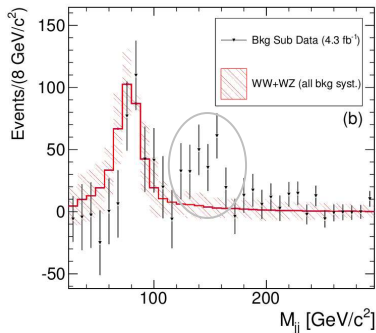
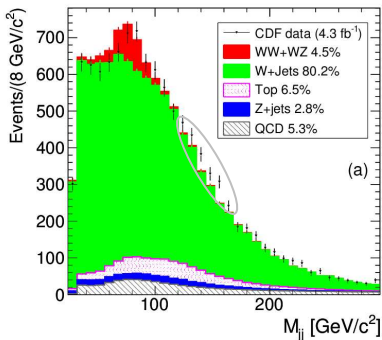
Jet-jet + W

$$\Rightarrow M_{jj} + W + \dots$$



The 'bump'!

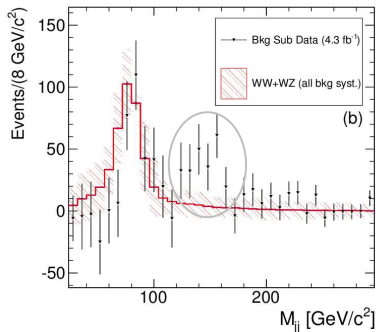
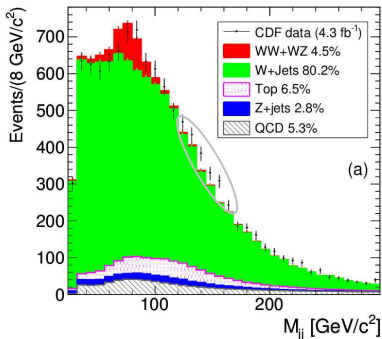
Invariant Mass Distribution of Jet Pairs Produced in Association with a W boson in $p\bar{p}$ Collisions at $\sqrt{s} = 1.96$ TeV", (CDF, 4 aprile 2011)



“we obtain a p-value of 7.6×10^{-4} , corresponding to a significance of 3.2 standard deviations” [“ 3.2σ ”]

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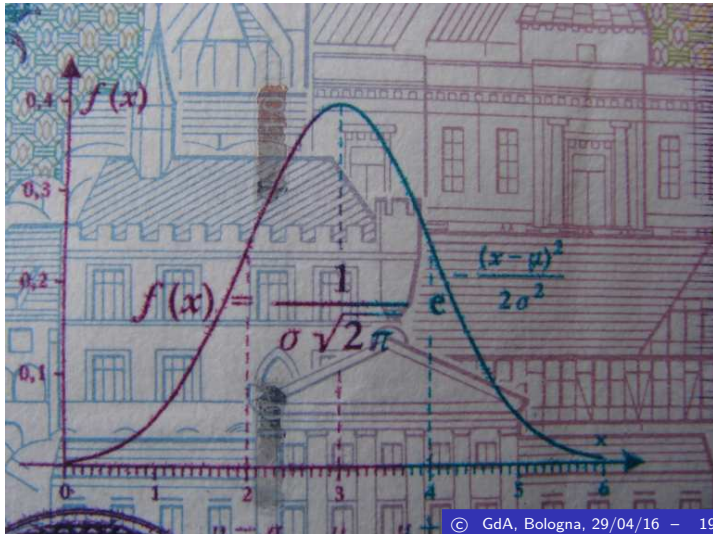
Sigma and gaussian distribution

Princeps mathematicorum



Sigma and gaussian distribution

“Functio nostra fiet...”



Sigma e probability [gaussian!]

If the random number X is described by a gaussian pdf

$$P(-\sigma \leq X \leq +\sigma) = 68.3\%$$

$$P(-2\sigma \leq X \leq +2\sigma) = 95.4\%$$

$$P(-3\sigma \leq X \leq +3\sigma) = 99.73\%$$

$$1 - P(-3\sigma \leq X \leq +3\sigma) = 0.27\%$$

$$1 - P(-4\sigma \leq X \leq +4\sigma) = 6.3 \times 10^{-5}$$

$$\dots = \dots$$

$$1 - P(-6\sigma \leq X \leq +6\sigma) = 2.0 \times 10^{-9}$$

$$1 - P(-3.2\sigma \leq X \leq +3.2\sigma) = 1.4 \times 10^{-3}$$

$$P(X \geq +3.17\sigma) = 7.6 \times 10^{-4} \quad \checkmark$$

p-value, significance and sigma

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Begin to fasten seat belts!



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- ▶ What is a p-value?
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- ▶ What is a **p-value**?
- ▶ In so far does it provides us a ‘**significance**’?

In short,

- ▶ Is 7.6×10^{-4} a **probability**?
- ▶ **of what?**

April 2011, the 'bump' explodes

The New York Times, Tuesday, April 5:

"Physicists at the Fermi National Accelerator Laboratory are planning to announce Wednesday that they have found a suspicious bump in their data that could be evidence of a new elementary particle or even, some say, a new force of nature.

...

*The experimenters estimate that **there is a less than a quarter of 1 percent chance their bump is a statistical fluctuation**"*

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Eureka!!

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[Do not ask me how 7.6×10^{-4} becomes $< 2.5 \times 10^{-3}$
(but this can be considered a minor detail...)]

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Who believed it was – at 99.75%! – a discover?

- ▶ the journalist who reported the news?
- ▶ the CDF contactperson and/or the Fermilab PR's who contacted him?

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Much more important the unusual fact that an ArXiv appeared one day was commented by NYT the day after!

Who believed it was – at 99.75%! – a discover?

- ▶ the journalist who reported the news?
- ▶ the CDF contactperson and/or the Fermilab PR's who contacted him?

From my experience, journalists might make imprecisions, bad they do not invent pieces of news [. . . at least scientific ones. . . :-)]

April 2011, the 'bump' explodes

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In other terms, *we do not organize an official seminar in the physics department everytime a student 'discovers' a new effect in the lab!*

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$$1/1375 = 7.3 \times 10^{-4} \Rightarrow P(\text{No stat. fluct.}) = 99.93\% !$$

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It seems we are understanding well, besides the fact of how 99.9% becomes 99.7%...

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"The last and greatest breakthrough from a fantastic machine, or a false alarm on the frontiers of physics?"

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But, at the end of the post:

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Assolutetly meaningful! (A part from the initial mismatch)

A masterpiece of good reasoning

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But how must our convictions rationally change on the light of new experimental data? Is there a **logical rule**?

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"de Rujula's paradox":

"If you disbelieve every result presented as having a 3 sigma – or "equivalently" a 99.7% chance – of being correct... You will turn out to be right 99.7% of the times."

(Alvaro de Rujula, private communication)

The cemetery of Physics

THE CEMETERY OF PHYSICS
IS FULL OF WONDERFUL
EFFECTS...



...THAT VERY OFTEN LEAD
TO THEORETICAL, EXPER. PROGRESS

Alvaro de Rujula

Testing one hypothesis

- ▶ Basic Idea:
 - ▶ let's start from a 'conventional' model
[Standard Modell, rather 'established theory', etc:]
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Let's review the practice and what is behind it ⇒

Falsificationism

Usually referred to Popper
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It seems OK – 'obvious'! – but it is indeed naïve for several aspects.

Proof by contradiction ... 'extended'...

Falsification rule: to what is 'inspired'?

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Proof by contradiction of classical, deductive logic:

- ▶ Assume that a hypothesis is true;
- ▶ Derive 'all' logical consequence;
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is this extension legitimate?

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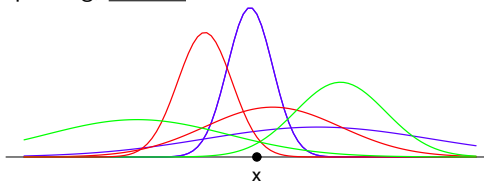
- ▶ What shall we do of all hypotheses not yet falsified? (Limbus? How should we progress?)
- ▶ What to do if **nothing** of what can be observed is incompatible with the hypothesis (or with many hypotheses)?
 - E.g. H_i being a Gaussian $f(x | \mu_i, \sigma_i)$
 - ⇒ Given any pair of parameters $\{\mu_i, \sigma_i\}$ (i.e. $\forall H_i$), all values of x from $-\infty$ to $+\infty$ are possible.

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- ⇒ Given any pair of parameters $\{\mu_i, \sigma_i\}$ (i.e. $\forall H_i$), all values of x from $-\infty$ to $+\infty$ are possible.
- ⇒ Having observed any value of x , none of H_i can be, strictly speaking, falsified.



Falsificationism in action...

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⇒ **Practically never in the experimental sciences!**

Falsificationism in action...

Obviously, this does not mean that falsificationism never works, **as long as no stochastic** processes are involved (randomness inherent to the physical processes, or due to 'errors' in measurement).

Certainly it works against itself:

- ▶ Science proceeds, in practice, rather differently:

The natural development of Science shows that researches are carried along the directions that seem more credible (and hopefully fruitful) at a given moment. A behaviour "179 degrees or so out of phase from Popper's idea that we make progress by falsifying theories" (Wilczek, <http://arxiv.org/abs/physics/0403115>)

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⇒ logically speaking, falsificationism
has to be considered ... falsified!

Falsificationism and statistics

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But from the **impossible** to the **improbable** there is not just a question of **quantity**, but a question of **quality**.

Falsificationism and statistics

... then, statisticians have invented the “hypothesis tests”, in which **the impossible is replaced by the improbable!**

But from the **impossible** to the **improbable** there is not just a question of **quantity**, but a question of **quality**.

This mechanism, logically flawed, is particularly dangerous because is deeply rooted in most scientists, due to education and custom, although not supported by logic.

⇒ **Basically responsible of all fake claims of discoveries in the past decades.**

[I am particularly worried about claims concerning our health, or the status of the planet, of which I have no control of the experimental data.]

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"most likely false"~~

But it is behind the rational behind
the statistical hypothesis tests!

Example

An Italian citizen is chosen at random and sent to take an AIDS test (test is not perfect, as it is the case in practice).

Simplified model:

$$P(\text{Pos} | \text{HIV}) = 100\%$$

$$P(\text{Pos} | \overline{\text{HIV}}) = 0.2\%$$

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$H_1 = \text{'HIV'}$ (Infected)

$E_1 = \text{Positive}$

$H_2 = \overline{\text{'HIV'}}$ (Not infected)

$E_2 = \text{Negative}$

Example

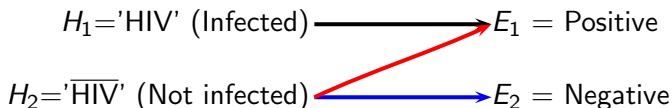
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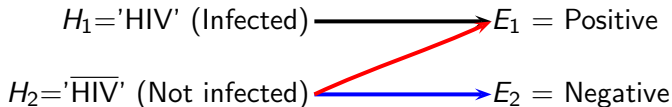
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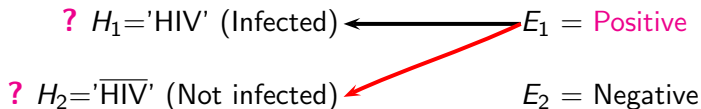
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HIV or not HIV?

What shall we conclude?

Being $P(\text{Pos} | \overline{\text{HIV}}) = 0.2\%$ and having observed 'Positive',
can we say

- ▶ "It is practically impossible that the person is healthy, since it was practically impossible that an healthy person would result positive"?

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Instead, $P(\text{HIV} | \text{Pos, randomly chosen Italian}) \approx 45\%$

Think about it (a crucial information is missing!)

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⇒ **Serious mistake!** (not just 99.8% instead of 98.3%)

$$P(A | B) \leftrightarrow P(B | A)$$

Pay attention no to arbitrary revert conditional probabilities:

$$\text{In general } P(A | B) \neq P(B | A)$$

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In particular

- ▶ A cause might produce a given effect with very low probability, and nevertheless could be the most probable cause of that effect, often the only one!

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→ What was the probability to give exactly that number?:

$$\begin{aligned}P(X = 3.1416 | H_0) &= \int_{3.14155}^{3.14165} f_G(x | \mu, \sigma) dx \\ &\approx f_G(3.1416 | \mu, \sigma) \times \Delta x \\ &\approx f_G(3.1416 | \mu, \sigma) \times 0.0001 \\ &\approx 39 \times 10^{-6}\end{aligned}$$

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→ What is the probability that X comes from H_0 ?

- ▶ Certainly **NOT** $\approx 39 \times 10^{-6}$;
- ▶ Indeed, it is **exactly 1**, since H_0 is the only cause which can produce that effect:

$$P(X = 3.1416 | H_0) \approx 39 \times 10^{-6}$$

$$P(H_0 | X = 3.1416) = 1.$$

Exercises with R

How to calculate the probability of the rounded value of an outcome (nd):

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- ▶ Repeat the last line to get a feeling.

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```

```
(x=round(rnorm(1,m,s),nd)); dnorm(x,m,s)*10-nd
```

- ▶ Repeat the last line to get a feeling.
- ▶ Maximum value: $\frac{10^{-nd}}{\sqrt{2\pi}\sigma}$ ($\rightarrow \approx 4^{-5}$ for $nd = 4, \sigma = 1$).

Exercises with R

How to calculate the probability of the rounded value of an outcome (nd):

```
nd=4; m=3; s=1;  
(x=round(rnorm(1,m,s),nd)); dnorm(x,m,s)*10^-nd
```

- ▶ Repeat the last line to get a feeling.
- ▶ Maximum value: $\frac{10^{-nd}}{\sqrt{2\pi\sigma}}$ ($\rightarrow \approx 4^{-5}$ for $nd = 4, \sigma = 1$).

Histogram of probabilities:

```
m=3; s=1; nd=4; n=100000  
x=round(rnorm(n,m,s),nd)  
log.p=log10(dnorm(x,m,s)*10^-nd)  
hist(log.p, nc=100, col='cyan',  
      xlim=c(min(log.p), max(log.p)*0.8) )
```

Probability of something else. . .

Besides the fact that the reasoning based only on the probability of the event given the cause is logically flawed, the **'technical issue' of low probability events which would lead to reject any hypothesis** forces the statistician to rethink the question. . .

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→ what matters is not the probability of the X , but rather the probability of X or of any other less probable number (or a number farther than X from the expected value – the story is a bit longer. . .):

$$P(X \geq 3.1416) = \int_{3.14155}^{+\infty} f_G(x | \mu, \sigma) dx \approx 44\%$$

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$$P(X \geq 3.1416) [= P(X \geq x_{obs})] \Rightarrow \text{'p-value'}$$

Probability of something else...

Besides the fact that the reasoning based only on the probability of the event given the cause is logically flawed, the **'technical issue' of low probability events which would lead to reject any hypothesis** forces the statistician to rethink the question...

- ⇒ Magically **the result 'becomes' rather probable!**
Why, we, silly, worried about it?
- ⇒ The statisticians are happy...

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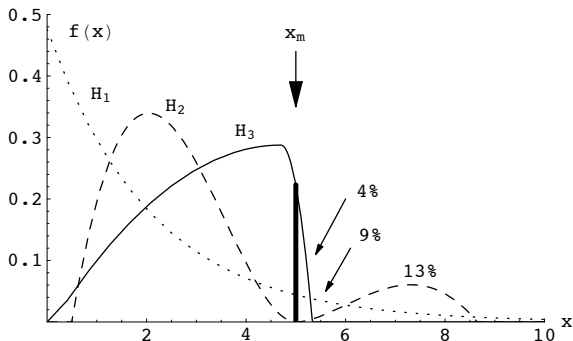
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Why, we, silly, worried about it?
- ⇒ The statisticians are happy. . . **scientists and general public cheated. . .**
- ⇒ **From the logical point** of view the situation has **worsened:**
→ our **conclusions** do not **depend** on what we have observed, but also **from rarer events not actually observed!**

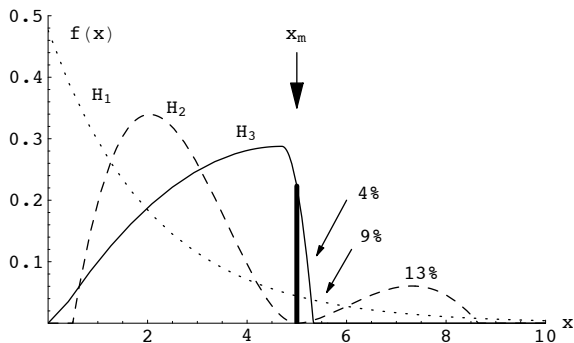
Comparing three hypotheses

Which hypothesis is favored by the experimental observation x_m ?



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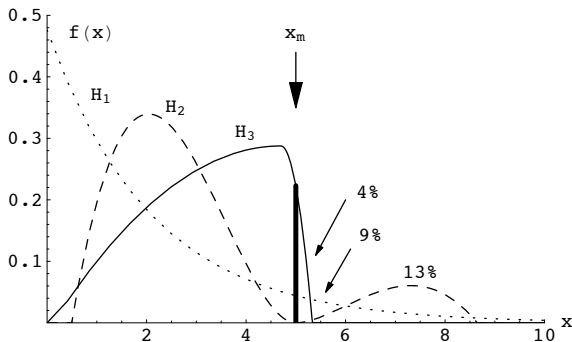


$$P(x_m | H_3) > P(x_m | H_1) > P(x_m | H_2) = 0 \quad (!)$$

Even if $P(x_m | H_i) \rightarrow 0$ (it depends on resolution)

Comparing three hypotheses

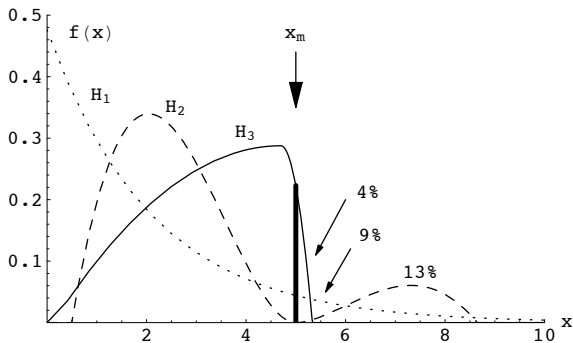
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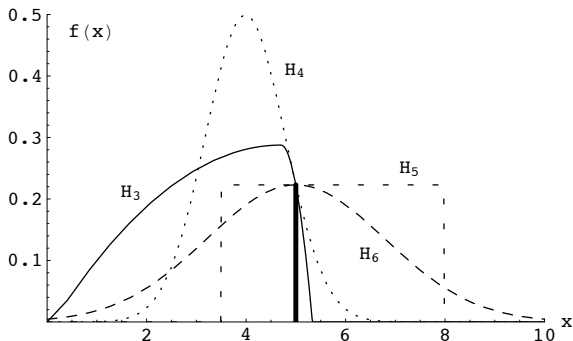
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In particular, the hypothesis H_2 is (truly) falsified (impossible!), although it yields the largest 'p-value', or 'probability of the tail(s)'

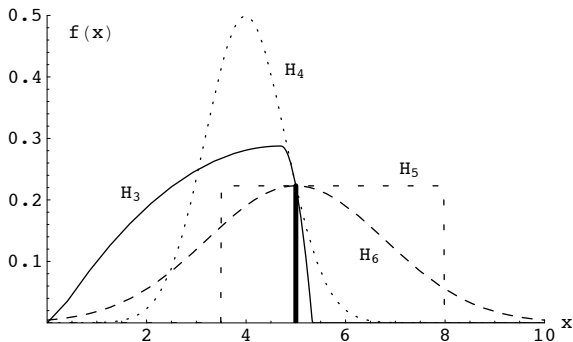
An irrelevant experiment

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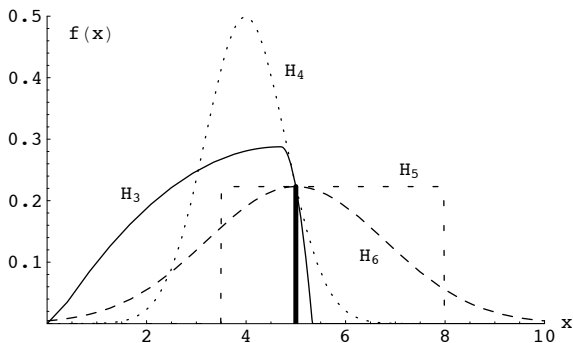


$$P(x_m | H_3) = P(x_m | H_4) = P(x_m | H_5) = P(x_m | H_6)$$

⇒ *The experimental result is irrelevant!*

An irrelevant experiment

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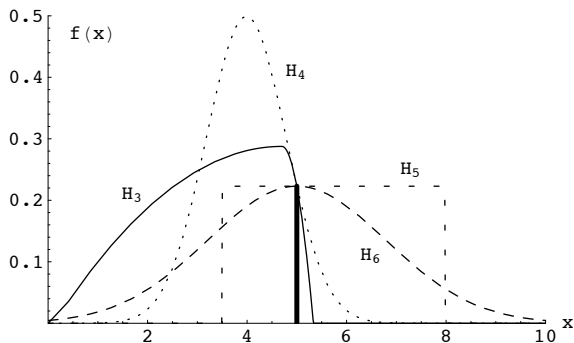


$$P(x_m | H_3) = P(x_m | H_4) = P(x_m | H_5) = P(x_m | H_6)$$

⇒ *The experimental result is irrelevant!*
→ we maintain our opinions about H_i

An irrelevant experiment

Which hypothesis is favored by the experimental observation x_m ?



$$P(x_m | H_3) = P(x_m | H_4) = P(x_m | H_5) = P(x_m | H_6)$$

⇒ *The experimental result is irrelevant!*

⇒ *... no matter what the different the p-values are!*

Which p-value?...

'p-value' = 'probability of the tail(s)'

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Of what?

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'p-value' = 'probability of the tail(s)'

Of what?

→ the test variable (' θ ') is absolutely arbitrary:

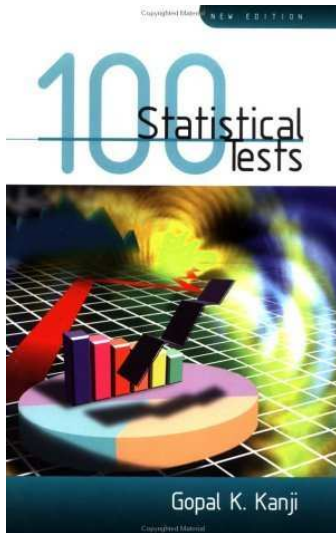
$$\theta = \theta(\mathbf{x})$$

$$\rightarrow f(\theta) \text{ [p.d.f]}$$

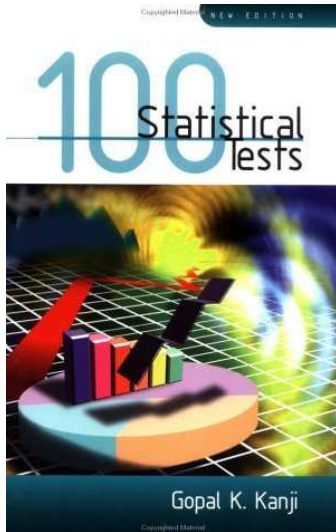
$$\text{Experiment: } \rightarrow \theta_{mis} = \theta(\mathbf{x}_{mis})$$

$$\text{p-value} = P(\theta \geq \theta_{mis}) \quad (\text{'one tail'})$$

Which p-value?...

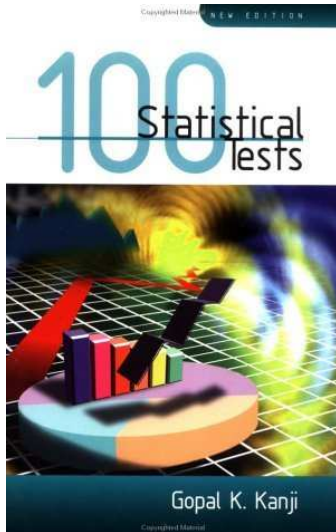


Which p-value?...



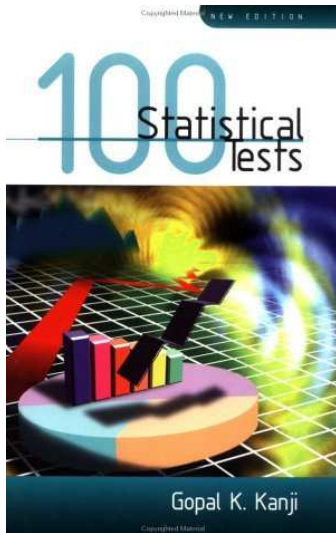
- ▶ far from exhaustive list,

Which p-value?...



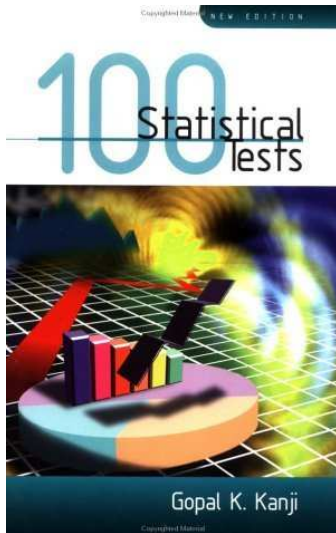
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Which p-value?...



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⇒ practitioners chose the one that provide the result they like better:
→ *like if you go around until "someone agrees with you"*

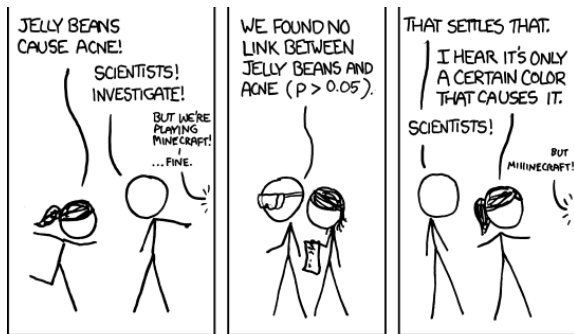
Which p-value?...



- ▶ far from exhaustive list,
- ▶ with **arbitrary** variants:
⇒ practitioners chose the one that provide the result they like better:
→ *like if you go around until "someone agrees with you"*
- ▶ personal **'golden rule'**:
"the more exotic is the name of the test, the less I believe the result", because I'm pretty shure that several 'normal' tests have been discarded in the meanwhile...

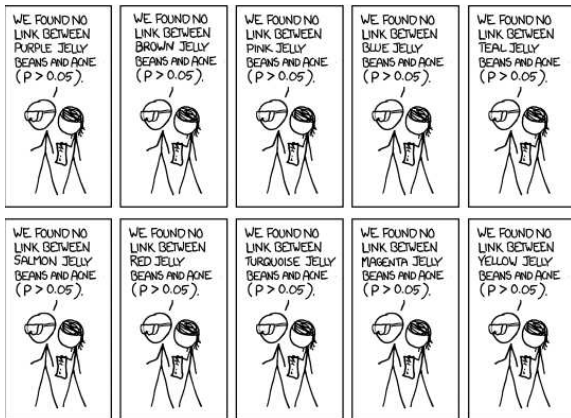
Or look around, searching for 'significance'

If changing the test does not help, change hypotheses...



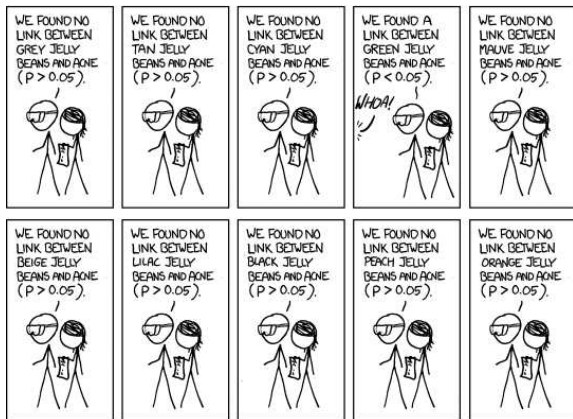
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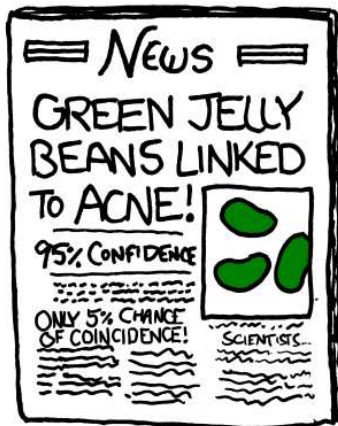
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P-hacking (“p-value hacking”)

The ‘science’ of inventing significant results. . .

p-hacking, or cheating on a p-value

June 11, 2015

By arthur charpentier

Share

(This article was first published on [Freakonometrics » R-english](#), and kindly contributed to [R-bloggers](#))

Yesterday evening, I discovered some interesting slides on False-Positives, p-Hacking, Statistical Power, and Evidential Value, via [@UCBITSS](#) 's post on Twitter. More precisely, there was this slide on how cheating (because that's basically what it is) to get a 'good' model (by targeting the p -value)

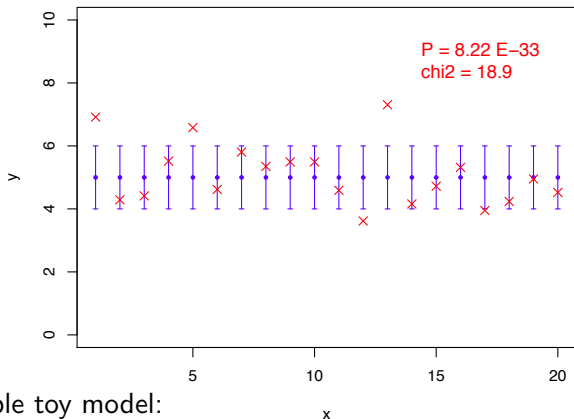
1. Stop collecting data once $p < .05$
2. Analyze many measures, but report only those with $p < .05$.
3. Collect and analyze many conditions, but only report those with $p < .05$.
4. Use covariates to get $p < .05$.
5. Exclude participants to get $p < .05$.
6. Transform the data to get $p < .05$.

<http://www.r-bloggers.com/p-hacking-or-cheating-on-a-p-value/>

► Google for “p-hacking”

χ^2 ... the mother of all p-values

Theory Vs experiment (*bars: expectation uncertainty*):



Very simple toy model:

- ▶ True value of y : 5, independently of x (a.u.);
- ▶ Gaussian instrumental error with $\sigma = 1$.

Probability of the data sample

$P = 8.22 \times 10^{-33}$ is the probability of the 'configuration' of experimental points:

- ▶ obtained multiplying the probability of each point (independent measurements):

$$P = \prod_i P_i$$

where

$$P_i = \int_{y_{m_i} - \Delta y/2}^{y_{m_i} + \Delta y/2} f(y) dy$$

- ▶ as seen, P_i depends on the 'resolution' Δy (instrumental 'discretization'):

$$\rightarrow \text{we use } \Delta y = \frac{1}{10} \sigma$$

'Distance' Experiment-theory: χ^2

The construction of the χ^2 is very popular
(usually in first lab. courses – 'Fisichetta'):

$$\begin{aligned}\chi^2 &= \sum_i \left(\frac{y_{m_i} - y_{th_i}}{\sigma_i} \right)^2 \\ &\rightarrow \sum_i \left(\frac{y_{m_i} - y_0}{\sigma} \right)^2\end{aligned}$$

$$\chi^2 \sim \Gamma(\nu/2, 1/2) \quad [\rightarrow \nu = 20]$$

$$E[\chi^2] = \nu \quad [\rightarrow 20]$$

$$\text{Var}[\chi^2] = 2\nu \quad [\rightarrow 40]$$

$$\text{Std}[\chi^2] = \sqrt{2\nu} \quad [\rightarrow 6.3]$$

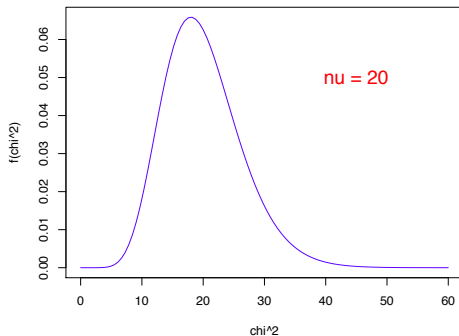
$$\text{Mode}[\chi^2] = \begin{cases} 0 & \text{if } \nu \leq 2 \\ \nu - 2 & \text{if } \nu > 2 \end{cases} \quad [\rightarrow 18]$$

\Rightarrow

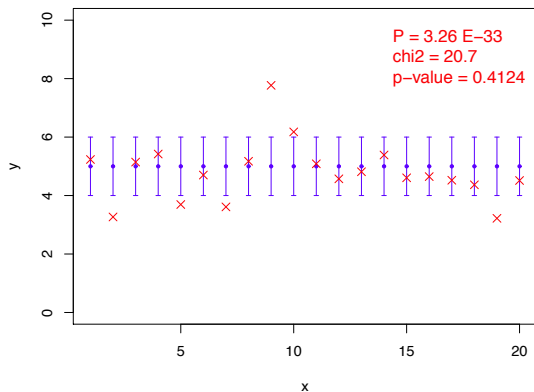
$$\boxed{\chi^2 = 20 \pm 6}$$

Our expectations about χ^2

$$\begin{aligned} E[\chi^2] &= \nu && [\rightarrow 20] \\ \text{Std}[\chi^2] &= \sqrt{2\nu} && [\rightarrow 6.3] \\ \Rightarrow & \boxed{\chi^2 = 20 \pm 6} \\ & [\text{mode: } 18] \end{aligned}$$



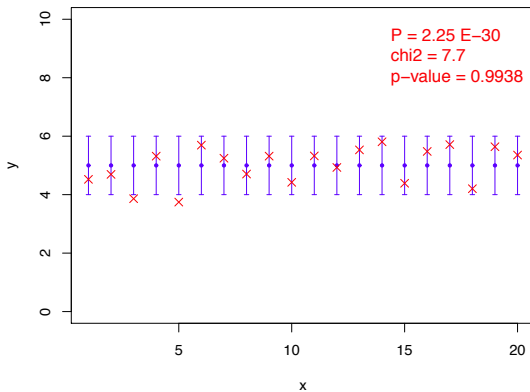
Some examples



In the average.

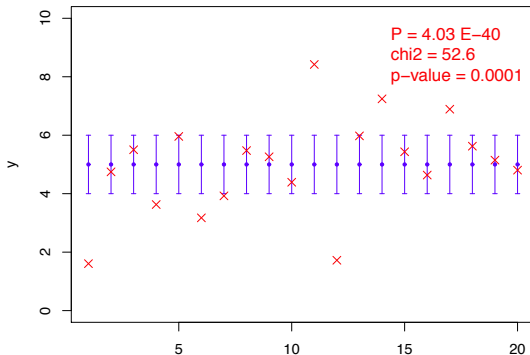
(but someone could see the points forming a 'constellation'...)

Some examples



Too good?

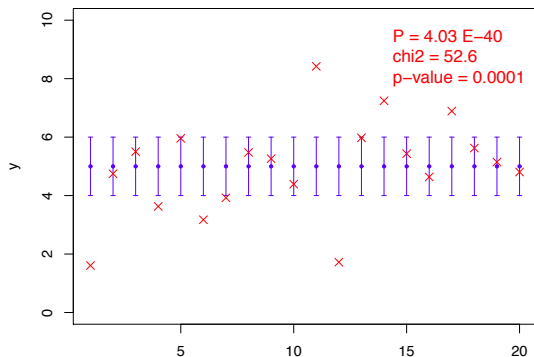
Some examples



$\chi^2 = 52.6$, with a p-value = 0.93×10^{-4}

At limit?

Some examples

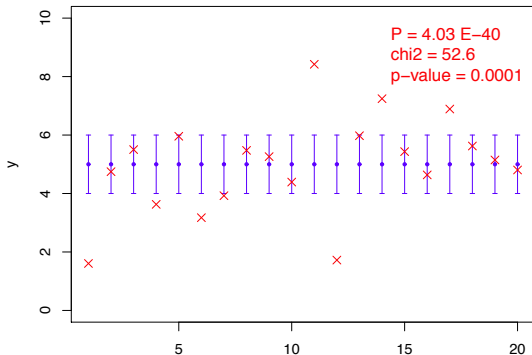


$\chi^2 = 52.6$, with a p-value = 0.93×10^{-4}

At limit? Just come out at the first time (9 Oct. 2012, 13:01)

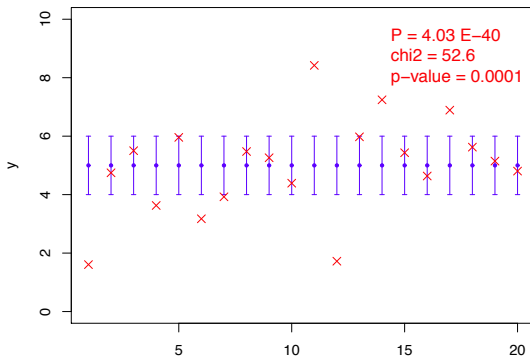
```
while(chi2.yr() < 38) source("chi2_1.R")
```


Some examples



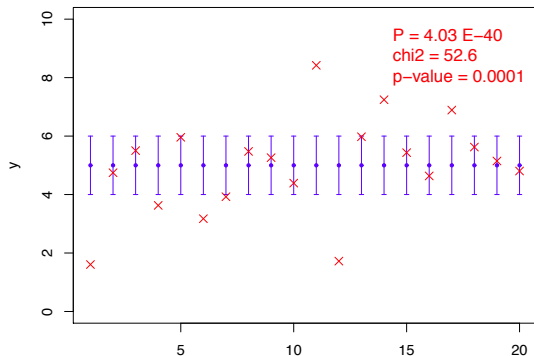
Note: χ_{mis}^2 52.6 is 5.1σ from its expectation $[\frac{52.6-20}{\sqrt{40}} = 5.1]$

Some examples



Note: χ_{mis}^2 52.6 is 5.1σ from its expectation $[\frac{52.6-20}{\sqrt{40}} = 5.1]$, but the p-value is **communicated as “3.7 σ ”**, referring to the probability of the tail above 3.7σ of an ‘**equivalent Gaussian**’.

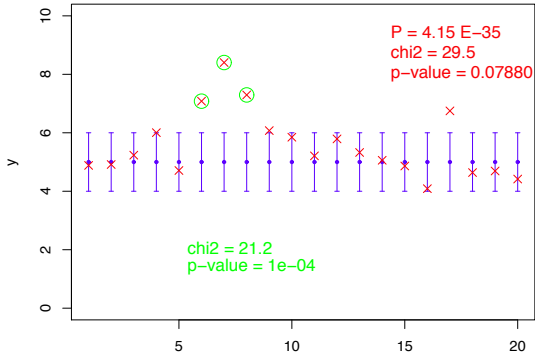
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(as if there were already not enough confusion...)

The art of χ^2

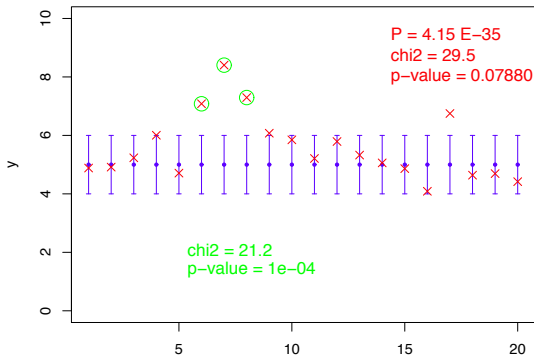
Sometimes the χ^2 test does not give “the wished result”



Then it is calculated in the ‘suspicious region’

The art of χ^2

Sometimes the χ^2 test does not give “the wished result”



Then it is calculated in the ‘suspicious region’

⇒ If we add the two side points, χ^2
becomes 22.2.

⇒ But with 5 points we had got a p-value of 5×10^{-4}

p-value: what they are

p-value:

- ▶ Probability of the tail(s) of a 'test variable' (a "statistic"):

$$P(\theta \geq \theta_{mis}) = \int_{\theta_{mis}}^{\infty} f(\theta | H_0) d\theta$$

$$P[(\theta \geq \theta_{mis}) \cap (\theta \leq (\theta^c)_{mis})] = 1 - \int_{(\theta^c)_{mis}}^{\theta_{mis}} f(\theta | H_0) d\theta$$

- ▶ θ is an arbitrary function of the data.
- ▶ ... and often of a subsample of the data.
- ▶ $f(\theta | H_0)$ is obtained 'somehow', analitically, numerically, or by Monte Carlo methods.

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What they are not \Rightarrow

Example: Has the student made a mistake?

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$$\begin{aligned} E[\bar{X}_{300}] &= \frac{1}{2} \\ \sigma[\bar{X}_{300}] &= \frac{1}{\sqrt{12}} \cdot \frac{1}{\sqrt{300}} = 0.017, \end{aligned}$$

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$$P(0.456 \leq \bar{X}_{300} \leq 0.544) = 99\%.$$

- ▶ Student gets a value outside the interval, e.g. $\bar{x} = 0.550$.
- ⇒ Has the student made a mistake?

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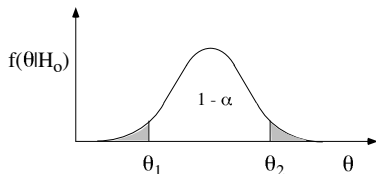
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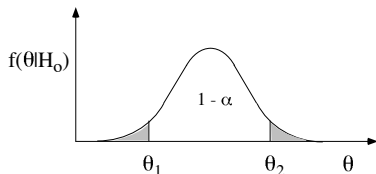


- ▶ Test variable θ is \bar{X}_{300} .
- ▶ Acceptance interval $[\theta_1, \theta_2]$ is $[0.456, 0.544]$.
We are 99% confident that \bar{X}_{300} will fall inside it:
→ $\alpha = 1\%$.

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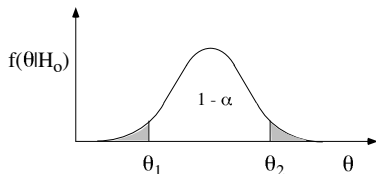


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- ⇒ **What does it mean?**

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Conclusion from test:

“the hypothesis $H_0 =$ ‘no mistakes’ is rejected at the 1% level of significance”.

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“there is only a 1% probability that the average falls outside the selected interval, if the calculations were done correctly”.

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So what?

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So what?

- ▶ It does not reply our natural question, i.e. that concerning the probability of mistake – quite impolite, by the way.
 - ▶ The statement sounds as if one would be 99% sure that the student has made a mistake! (Mostly interpreted in this way).
- ⇒ **Highly misleading!**

Something is missing in the reasoning

If you ask the students (before they take a standard course in hypothesis tests) you will realize of a crucial ingredient extraneous to the logic of hypothesis tests:

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“It all depends on whom has made the calculation!”

In fact, if the calculation was done by a well-tested program, the probability of mistake would be zero.

And students know rather well their tendency to do or not mistakes.

'Something is missing': another example

The value $x = 3.01$ is extracted from a Gaussian random number generator having $\mu = 0$ and $\sigma = 1$.

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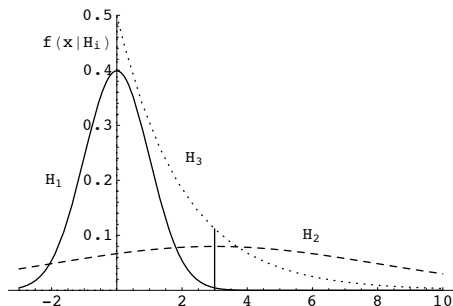
- ⇒ One cannot tell how much one is confident in generator A only if another generator B is not taken into account.
- ⇒ This is the original sin of conventional hypothesis test methods

Well posed problem

Choose among H_1 , H_2 and H_3 having observed $x = 3$:

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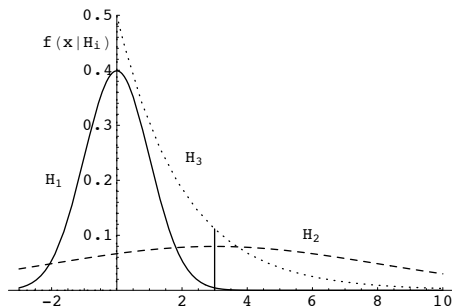


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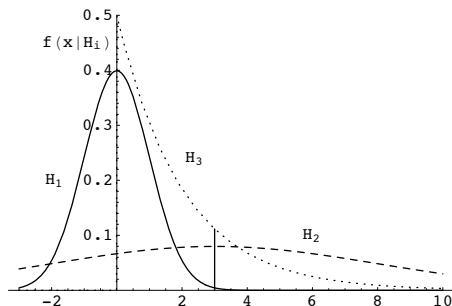


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⇒ Right!

Objections

“These are chosen academic examples.”

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How can we use a reasoning in frontier physics
if it fails in simple cases?

⇒ All fake claims of discoveries are due to
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“Hypotheses tests are well proved to work”

Yes and not. . .

⇒ They ‘often work’ due to reasons external to their logic, but which are not always satisfied, especially in the frontier cases that mostly concern us.

→ we shall come back to this point

Examples from particle physics

Many, too many, unfortunately...



In case I lived in first person was that of the (in)famous HERA events

⇒ see slides at

http://www.roma1.infn.it/~dagos/cernAT05_scanned/

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(And the logical error happens not only in the case of **fake discoveries**, but also when a **highly expected particle is finally found** – wait for a while. . .)

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⇒ BUT the p-value do not provide this:

$$P(\theta \geq \theta_{mis} | H_0) \not\leftrightarrow P(H_0 | \theta_{mis})$$

⇒ Although they are erroneously confused with this!

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Tight seat belts!



Misunderstandings p-values

<http://en.wikipedia.org/wiki/P-value#Misunderstandings>

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...
7. ...

The 5 sigma Higgs!

July 2012

- ▶ “The data confirm the 5 sigma threshold, **i.e.** a probability of discovery of 99.99994%” (one of the many claims you could read on the web).
- ▶ “I dati confermano la soglia dei 5 sigma, **vale a dire** una probabilità di scoperta pari al 99,99994 per cento” spiega Gian Francesco Giudice, teorico del CERN (corriere.it, 3 luglio)

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<http://www.roma1.infn.it/~dagos/badmath/#added>

Probabilistic reasoning

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- ▶ 'Mismatch' between our **natural way of thinking** and the **statistics theory**:
- ▶ $P(H_0 | \text{data}) \longleftrightarrow P(\theta \geq \theta_{mis} | H_0)$

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because explicitly forbidden! – **the fundamental thing we need in our game:**
- ▶ It is enough get rid of '900 statisticians (the 'frequentists')
and **reload 'serious guys'**,
→ restart from **Laplace**, together with **Gauss**, **Bayes**,
etc.,

Restarting from scratch (with some repetitions)

We need to restart from
scratch

(from a physicist's perspective)

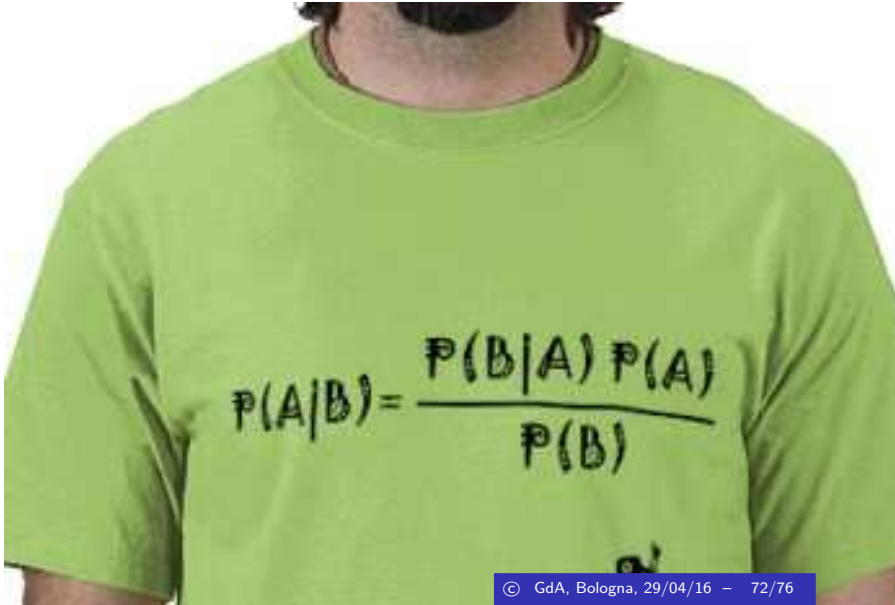
Probabilistic Inference

Basic rules of probability

1. $0 \leq P(A | I) \leq 1$
2. $P(\Omega | I) = 1$
3. $P(A \cup B | I) = P(A | I) + P(B | I)$ [if $P(A \cap B | I) = \emptyset$]
4. $P(A \cap B | I) = P(A | B, I) \cdot P(B | I) = P(B | A, I) \cdot P(A | I)$

Remember that probability is always conditional probability!

A simple, powerful formula

A person is shown from the chest up, wearing a bright green t-shirt. The t-shirt has a mathematical formula written on it in black ink. The formula is Bayes' theorem:
$$P(A|B) = \frac{P(B|A) P(A)}{P(B)}$$

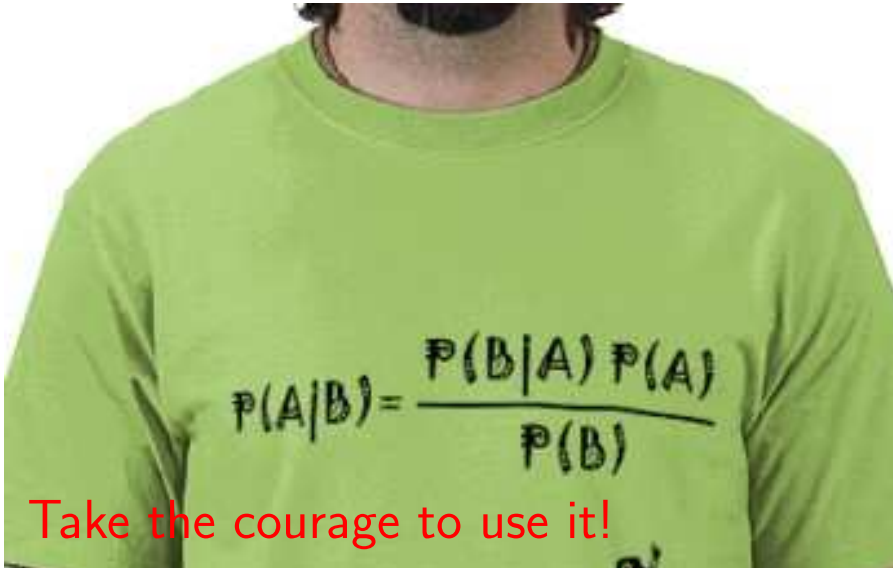
The formula is written in a hand-drawn style. The numerator consists of $P(B|A)$ and $P(A)$ separated by a vertical bar, with a horizontal line underneath. The denominator is $P(B)$.

A simple, powerful formula

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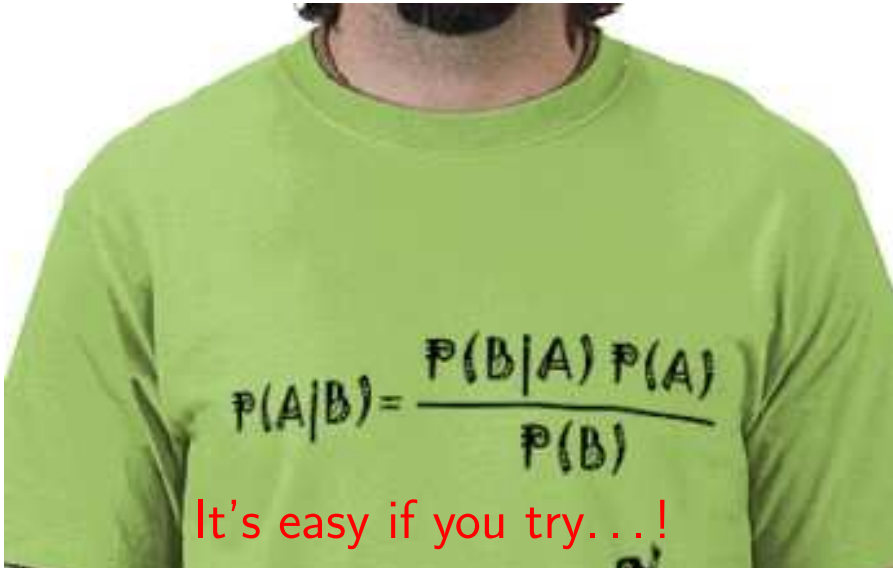
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Take the courage to use it!

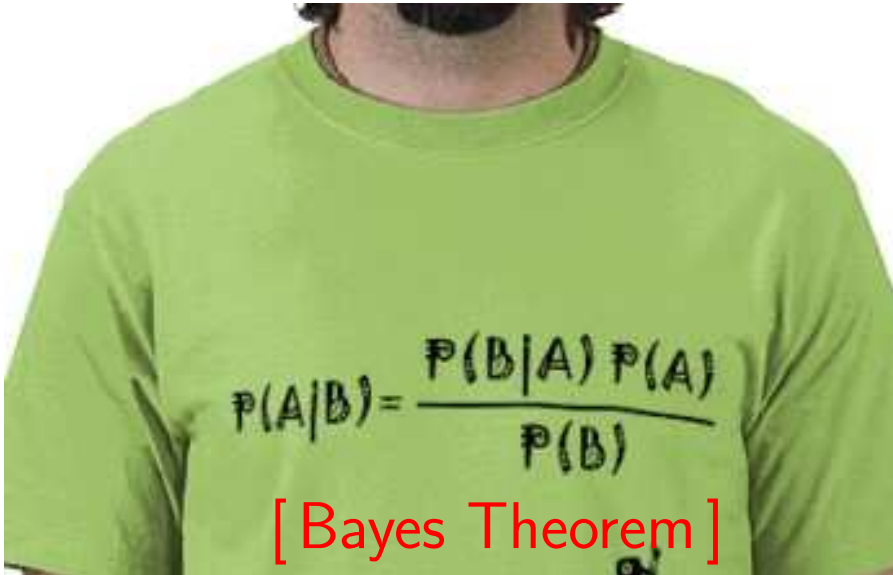
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It's easy if you try...!

A simple, powerful formula



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[Bayes Theorem]

Laplace's "Bayes Theorem"

"The greater the probability of an observed event given any one of a number of causes to which that event may be attributed, the greater the likelihood of that cause {given that event}.

$$P(C_i | E) \propto P(E | C_i)$$

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(Philosophical Essai on Probabilities)

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(*) In his “Philosophical essay” Laplace calls ‘principles’ the ‘fondamental rules’.

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Most convenient way to remember Bayes theorem

Conclusion?

What is the position of statisticians concerning p-values?

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- ▶ The 2016 p-value revolution
 - <http://www.roma1.infn.it/~dagos/dott-prob/>
 - Nr. 13 (10/3)

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What is the position of statisticians concerning p-values?

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(Many other links there concerning p-values)

The End

FINE