

# Neutral $\eta'$ Decays with the Crystal Ball

Physics:

- Photoproduction Cross Section
- $\Gamma(\eta' \rightarrow 2\gamma)/\Gamma(\eta \rightarrow 2\gamma)$
- $\eta' \rightarrow \eta\pi^0\pi^0/\eta' \rightarrow 3\pi^0$
- C and CP violating decays



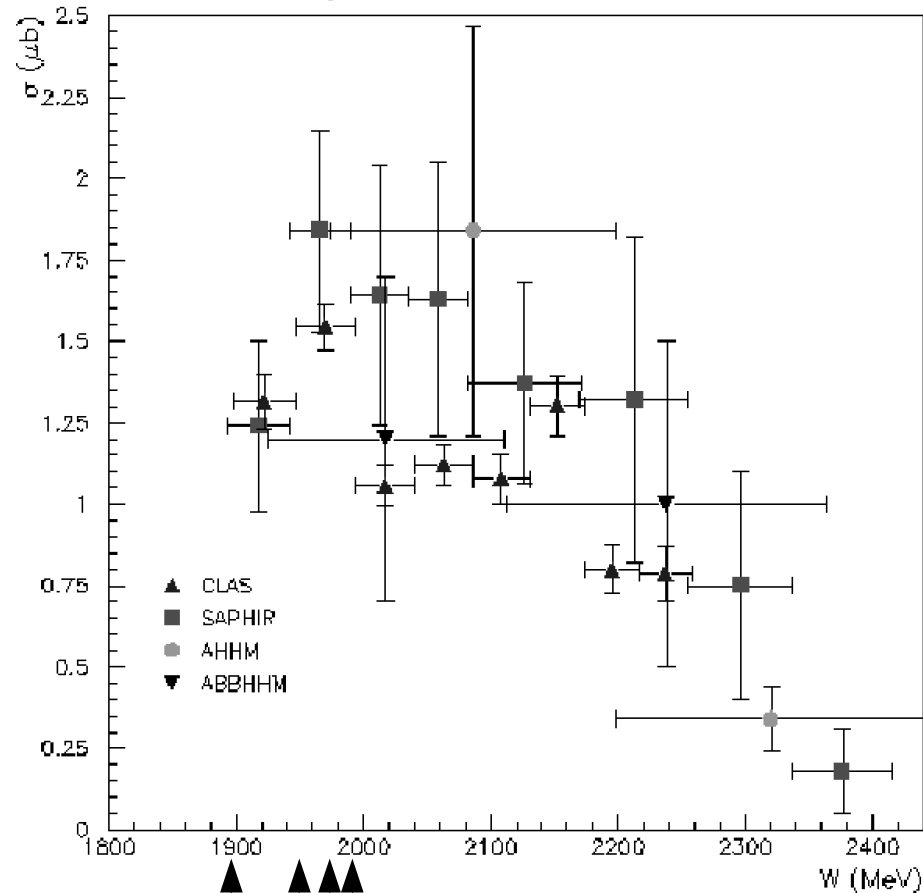
Marc Unverzagt  
Institut für Kernphysik  
University Mainz

Frascati, 08.04.2009



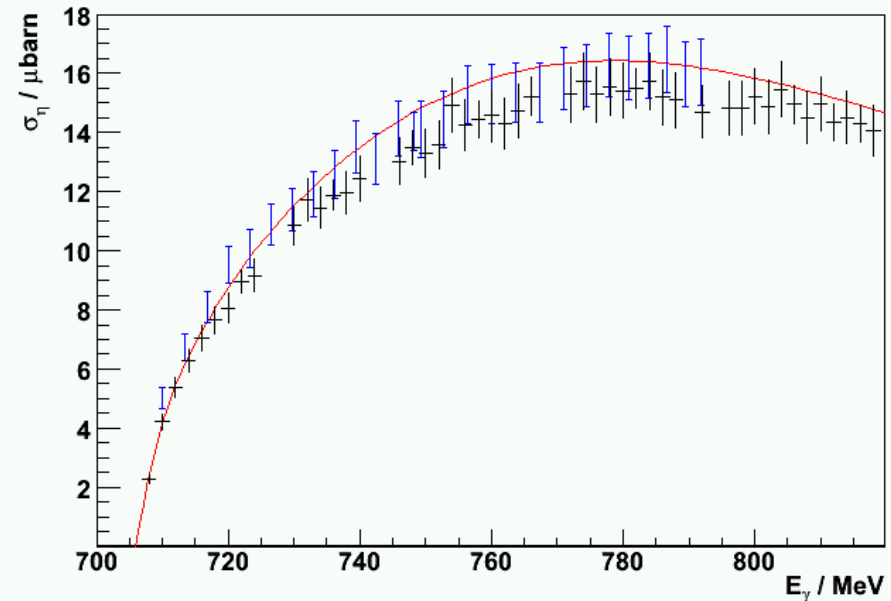
# $\eta'$ Photoproduction

$\eta'$  Cross Section



$E_\gamma = 1650$  MeV  
 $E_\gamma = 1600$  MeV  
 $E_\gamma = 1558$  MeV  
 $E_\gamma = 1447$  MeV (threshold)

$\eta$  Cross Section



- First goal: determine  $\eta'$  photoproduction cross section with high precision as for  $\eta$
- Get normalisations under control
- Examine not well known threshold region

# $\eta/\eta'$

- Dominant decays:

$$\eta' \rightarrow \eta \pi^+ \pi^- \quad \text{BR}=44.6 \%$$

$$\eta' \rightarrow \rho^0 \gamma \quad \text{BR}=29.4 \% \quad (\text{including nonresonant } \pi^+ \pi^- \gamma)$$

$$\eta' \rightarrow \eta \pi^0 \pi^0 \quad \text{BR}=20.7 \%$$

$$\eta' \rightarrow \omega \gamma \quad \text{BR}=3.0 \%$$

$$\eta' \rightarrow 2\gamma \quad \text{BR}=2.1 \%$$

$$\eta' \rightarrow 3\pi^0 \quad \text{BR}=0.156\%$$

- $\eta$  and  $\eta'$  are perfectly suited to study **symmetries** and **symmetry violations in QCD**

- $\eta' \rightarrow \eta \pi \pi$  and  $\eta' \rightarrow \pi \pi \pi$  sensitive to  $\pi \eta$  and  $\pi \pi$  scattering lengths (FSI)

- $\eta/\eta' \rightarrow \pi \pi \pi$  is sensitive to **isospin symmetry breaking** due to light quark mass difference  $m_u - m_d$

- Anomalous decays  $\eta/\eta' \rightarrow 2\gamma$  probe **chiral anomalies** of QCD

- PDG lists 7 **C or CP violating** decays of the  $\eta'$  meson, 9 for the  $\eta$

- $\eta$  and  $\eta'$  closely related to each other, they have the same **quantum numbers**:

$$I^G(J^P C) = 0^+(0^- +)$$

# $\Gamma(\eta' \rightarrow 2\gamma)/\Gamma(\eta \rightarrow 2\gamma)$

- From chiral symmetry breaking 8 pseudoscalar Goldstone-bosons are expected:

$$(\pi^+, \pi^-, \pi^0, K^+, K^-, K^0, \bar{K}^0, \eta_8) \quad \text{SU(3)-octet}$$

- Have the same quantum numbers as respective  $q\bar{q}$  pairs:

$$(u\bar{d}, d\bar{u}, (u\bar{u}-d\bar{d}), u\bar{s}, s\bar{u}, d\bar{s}, s\bar{d}, (u\bar{u}+d\bar{d}-2s\bar{s}))$$

- 9th state possible, lightest candidate  $\eta'(958)$ :

$$\eta_0 \sim (u\bar{u}+d\bar{d}+s\bar{s}) \quad \text{SU(3)-singlet}$$

- Neither  $\eta$  nor  $\eta'$  are pure singlet or octet states ( $\theta=-(20\pm 2)^\circ$ ):

$$\eta = \eta_0 \sin\theta - \eta_8 \cos\theta$$

$$\eta = \eta_0 \cos\theta + \eta_8 \sin\theta$$

- Also scheme with two mixing angles possible and additional gluonic content
- For extraction of mixing angle both decay widths have to be known with high precision  
 $\eta: \Gamma(\eta \rightarrow \text{all}) = (1.30 \pm 0.07) \text{ keV} \quad \Gamma(\eta \rightarrow 2\gamma) = (39.31 \pm 0.20)\%$   
 $\eta': \Gamma(\eta' \rightarrow \text{all}) = (0.30 \pm 0.09) \text{ keV} \quad \Gamma(\eta' \rightarrow 2\gamma) = (2.10 \pm 0.12)\%$

- Theoretically mixing not fully understood. Connection to QCD is missing ( $N_c, m_q$ )

# Determination of $(m_d - m_u)/m_s$

- Gross, Treiman, Wilczek, Phys. Rev. D **19**, 2188 (1979):

$$\frac{\Gamma(\eta' \rightarrow 3\pi^0)}{\Gamma(\eta' \rightarrow \eta \pi^0 \pi^0)} = \Phi \cdot \left( \frac{m_d - m_u}{m_s - \hat{m}} \right)^2 \quad \hat{m} = \frac{1}{2}(m_u + m_d)$$

- Two assumptions:

- a) Decay  $\eta' \rightarrow 3\pi^0$  proceeds entirely via  $\eta' \rightarrow \eta \pi^0 \pi^0$  followed by  $\pi^0$ - $\eta$  mixing
- b) Amplitudes for both decays are constant over phase space

- Borasoy, Meißner, Nißler, Phys. Lett. B **643**, 41 (2006):

„Our results clearly indicate that the two underlying assumptions ... are not justified.“

- Large coupling of the  $\eta' \rightarrow 3\pi$  process to  $\rho(770)$  resonance

- Borasoy, Meißner, Nißler, Phys. Lett. B **643**, 41 (2006):

„More precise data on  $\eta$  and  $\eta'$  decays needed in order to eventually clarify this issue.“

# Slope Parameters

- Energy release small ( $\sim 141$  MeV) in  $\eta' \rightarrow \eta \pi^0 \pi^0$

$$|M|^2 = |1 + \alpha y|^2 + c x + d x^2$$

x, y = Dalitz plot variables

- Dalitz plot variations due to  $\eta\pi$  and  $\pi\pi$  scattering described by  $\alpha$  (linear parametrisation):

GAMS-2000	$\alpha = -0.058 \pm 0.013$	5400 Events
CLEO	$\alpha = -0.021 \pm 0.025$	6700 Events
VES	$\alpha = -0.072 \pm 0.012 \pm 0.006$	7000 Events

- $\text{Im}(\alpha)$  so far consistent with 0
- C-violating decay parameter  $c = 0.015 \pm 0.011 \pm 0.014$  (VES with 20k events)
- d assumed to be 0
- $\eta' \rightarrow 3\pi^0$  has only one parameter as in  $\eta \rightarrow 3\pi^0$ :

$$|M|^2 = (1 + 2\beta z)$$

$$z = x^2 + y^2$$

- Only value so far from GAMS-2000:  $\alpha = -0.1 \pm 0.3$  with 40 events

# $\pi\pi$ and $\pi\eta$ Scattering Lengths

- $\eta' \rightarrow \eta \pi^+ \pi^-$  contributes to  $\eta' \rightarrow \eta \pi^0 \pi^0$  via  $\pi^+ \pi^- \rightarrow \pi^0 \pi^0$ , also for  $\eta' \rightarrow 3\pi^0$
- Cusp arises at  $\pi^+ \pi^-$  threshold in  $\pi^0 \pi^0$  invariant mass spectrum
- Cabibbo and Isidori as well as Bissegger *et al.* have developed framework to extract  $a_0 - a_2$  from  $K \rightarrow 3\pi$  and  $\eta \rightarrow 3\pi$   $\pi^0 \pi^0$  invariant mass spectrum, but cusp effect in  $\eta$  decay only at 1% level
- Rough estimate from Kubis (HISKP) for cusp strength:
  - $K^+ \rightarrow 3\pi$ : 2
  - $K_L \rightarrow 3\pi$ : 1/3
  - $\eta \rightarrow 3\pi$ : 1/3
  - $\eta' \rightarrow \eta 2\pi$ : 1.3 – 1.5
- As cusps were measured with high statistics in Kaon decays this it is not to be seen as a highlight to see it in  $\eta'$  sector
- Schneider, Kubis, Meißner (soon on arXiv) state an 8% cusp effect in  $\eta' \rightarrow \eta \pi^0 \pi^0 \rightarrow$  extraction of  $\pi\eta$  scattering length is possible, which can not easily be measured in other experiments

# C and CP Violating Decays

- In QED and QCD **C** and **CP** symmetry should be conserved
- $\eta'$  well suited to investigate symmetry breaking
- Only weak upper limits for **C** and **CP** violating  $\eta'$  decays exist

- **C** violating:

$$\eta' \rightarrow \eta e^+ e^- \quad \text{BR} < 2.4 \cdot 10^{-3}$$

$$\eta' \rightarrow \pi^0 e^+ e^- \quad \text{BR} < 1.4 \cdot 10^{-3}$$

$$\eta' \rightarrow 3\gamma \quad \text{BR} < 1.0 \cdot 10^{-4}$$

- **CP** violating:

$$\eta' \rightarrow 4\pi^0 \quad \text{BR} < 5.0 \cdot 10^{-4}$$

- **CPT** violating:

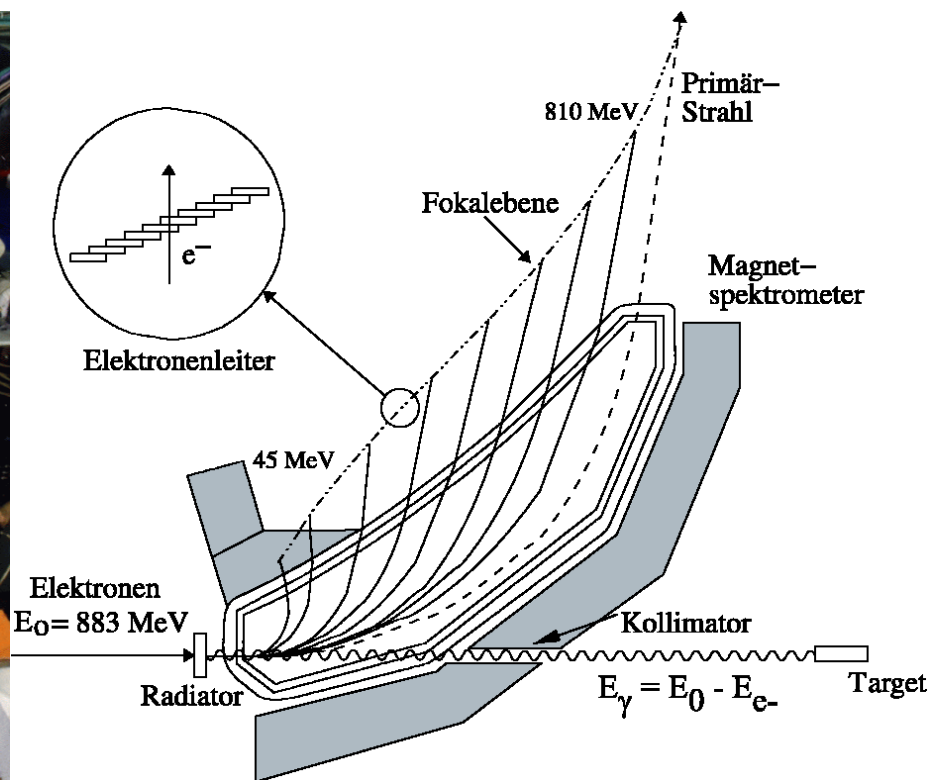
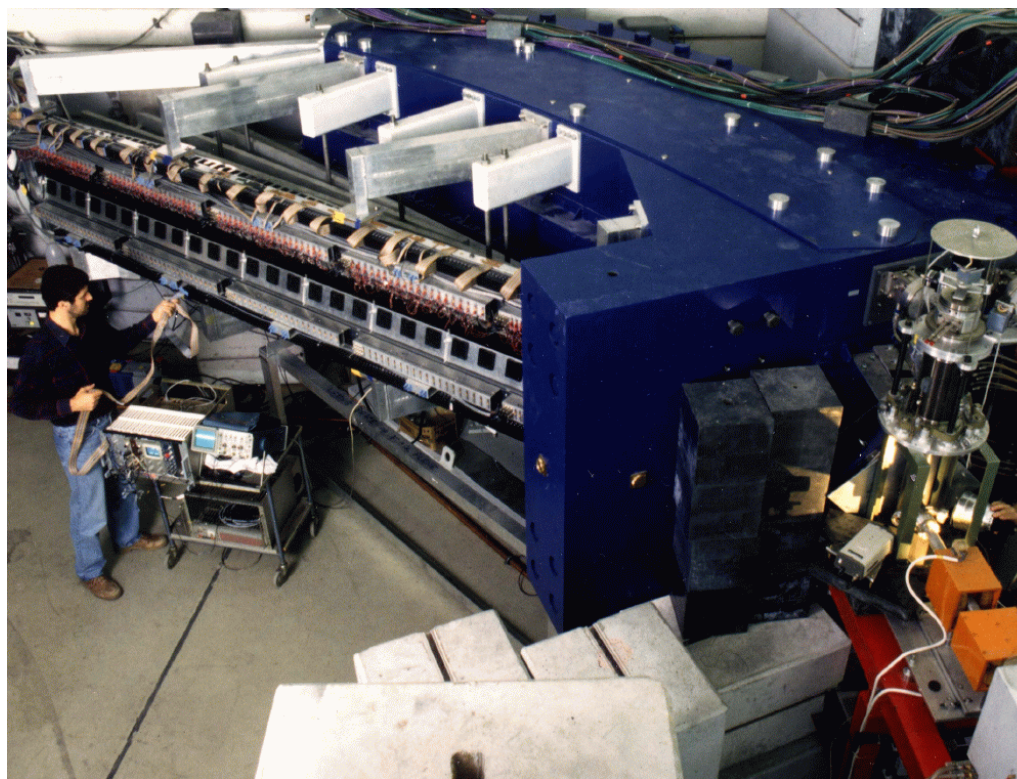
$$\eta' \rightarrow \pi^0 \mu^+ \mu^- \quad \text{BR} < 6.0 \cdot 10^{-5}$$

$$\eta' \rightarrow \eta \mu^+ \mu^- \quad \text{BR} < 1.5 \cdot 10^{-5}$$

Not possible with current rates

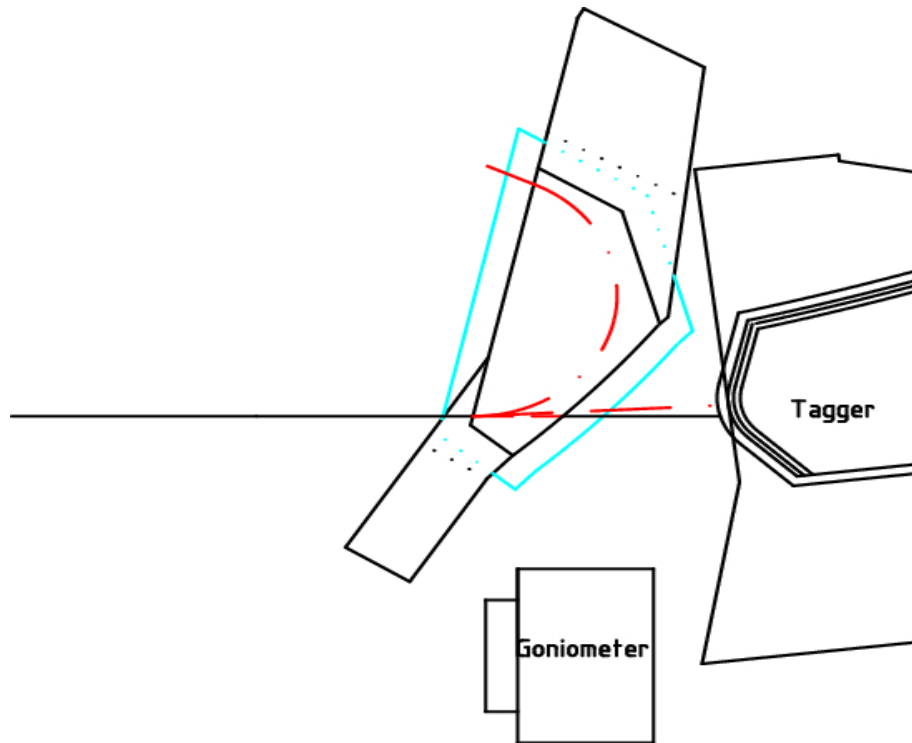


# Glasgow-Mainz-Tagger



- Photon beam produced by Bremsstrahlung at radiator:  $e^- + A \rightarrow e^- + A + \gamma$
- 353 overlapping scintillators  $\rightarrow$  352 channels
- Electrons momentum analysed in magnetic spectrometer
- Energy tagging through  $E_\gamma = E_0 - E_{e^-}$
- $\Delta E_\gamma \approx 2 \text{ MeV}$  at 883 MeV electron energy,  $\Delta E_\gamma \approx 4 \text{ MeV}$  at 1558 MeV electron energy
- Tagging range: 5 to 92% of the electron beam energy

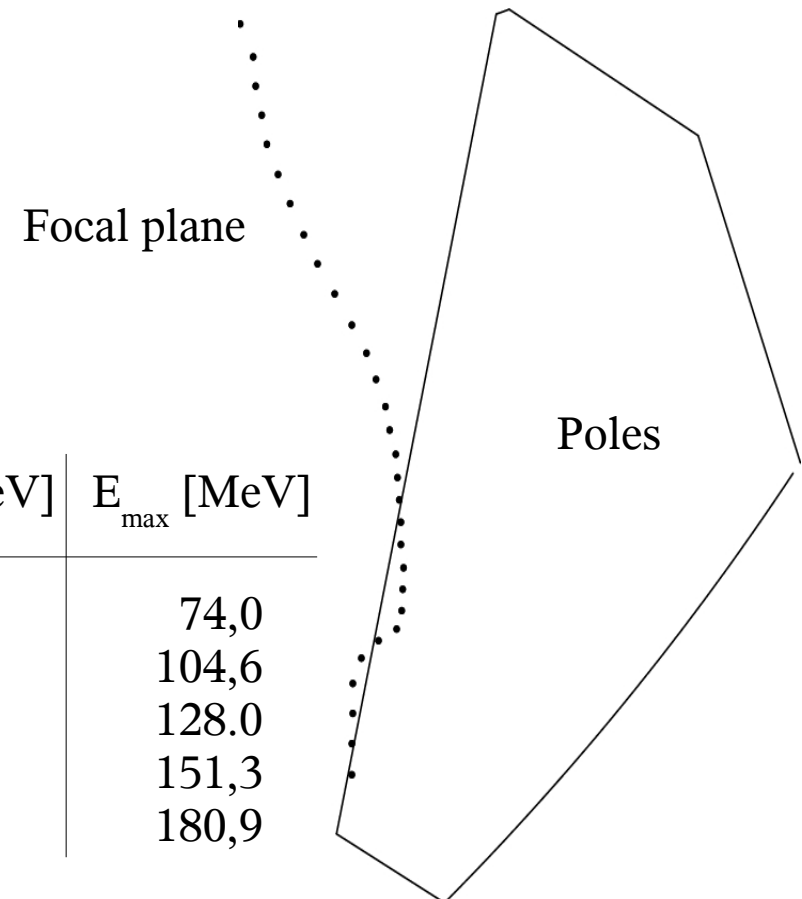
# End-Point Tagger



- Suitable magnet from MAMI-A
- Plan: use 1.5 T field → **150 MeV** range
- Use cards and PMTs from Lund tagger
- 64 channels →  **$\Delta E = 2.3$  MeV**
- Possibly include end-point tagger in trigger

	$E_\gamma$ [MeV]	$E_e$ [MeV]
$K\pi\Sigma$	1299.9	208.1
$\omega\pi$	1366.3	141.7
last tagger channel	1445	113
$\eta'$	1446.6	61.4
$K\Lambda(1405)$	1454.0	54
$f_0$	1491.8	16.2
$a_0$	1501.4	6.6

B [T]	$E_{\min}$ [MeV]	$E_{\max}$ [MeV]
0,7	2,9	74,0
1,0	4,0	104,6
1,2	4,8	128.0
1,5	5,3	151,3
1,8	6,0	180,9



# Event Rate Estimate

- Incoming electron beam energy:  $E_0 = 1558 \text{ MeV}$
- Photon energy range tagged:  $E_\gamma = 1450 - 1550 \text{ MeV} \rightarrow \Delta E_\gamma = 100 \text{ MeV}$
- Photon flux:  $N_\gamma = 10^5 \text{ s}^{-1} \text{ MeV}^{-1}$
- Number of protons in a 10 cm  $\text{IH}_2$  target:  $N_t = 4.3 \cdot 10^{23} \text{ cm}^{-2}$
- $\eta'$  photoproduction cross section (average):  $\sigma(\gamma p \rightarrow \eta' p) = 1 \text{ } \mu\text{b}$

$$N_{\eta'} = \Delta E_\gamma \cdot N_\gamma \cdot N_t \cdot \sigma(\gamma p \rightarrow \eta' p) \cdot 3600 \text{ s} \approx 1.5 \cdot 10^4 / h$$

- Detection efficiency of  $\eta' \rightarrow \eta \pi^0 \pi^0 \sim 30\%$ , livetime  $\sim 80\%$  and  $\text{BR}(\eta' \rightarrow \eta \pi^0 \pi^0) = 20\%$   
 $\rightarrow 700 \text{ good } \eta' \rightarrow \eta \pi^0 \pi^0 \text{ events per hour}$
- Current highest statistics  $\sim 7000$  events. To increase by one order of magnitude at least 100 hours of beam time.

# Summary

- Although, or maybe because, the  $\eta'$  meson is not a Goldstone boson and too heavy to be treated in  $\chi$ PT in the standard way, it is interesting and important to measure  $\eta'$  decays
- Proposed channels:  $\eta' \rightarrow 2\gamma$  in combination with  $\eta \rightarrow 2\gamma$ ,  $\eta' \rightarrow \eta\pi^0\pi^0$ ,  $\eta' \rightarrow 3\pi^0$
- Physic goals:  $\eta$ - $\eta'$  mixing, slope parameters from Dalitz plots, cusps,  $\pi\pi$  and  $\pi\eta$  scattering lengths
- (Improve upper limits for branching ratios of C and CP violating  $\eta'$  decays like  $\eta' \rightarrow \eta e^+e^-$ ,  $\eta' \rightarrow \pi^0 e^+e^-$ ,  $\eta' \rightarrow 3\gamma$ ,  $\eta' \rightarrow 4\pi^0$ ) if possible!!
- New equipment as  $\text{PbWO}_4$  crystals in TAPS and end-point tagger and increased  $e^-$  energy could improve event rate.
- Proposed  $\eta'$  production rate:  $1.5 \cdot 10^4/\text{h}$ , main neutral decay  $\eta' \rightarrow \eta\pi^0\pi^0$  700/h